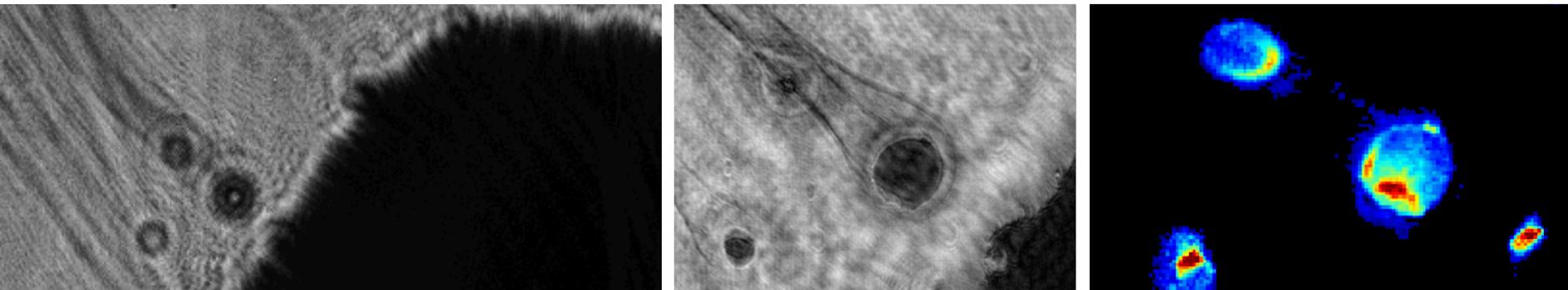


Exceptional service in the national interest



Digital Imaging Holography and Pyrometry of Aluminum Drop Combustion in Solid Propellant Plumes

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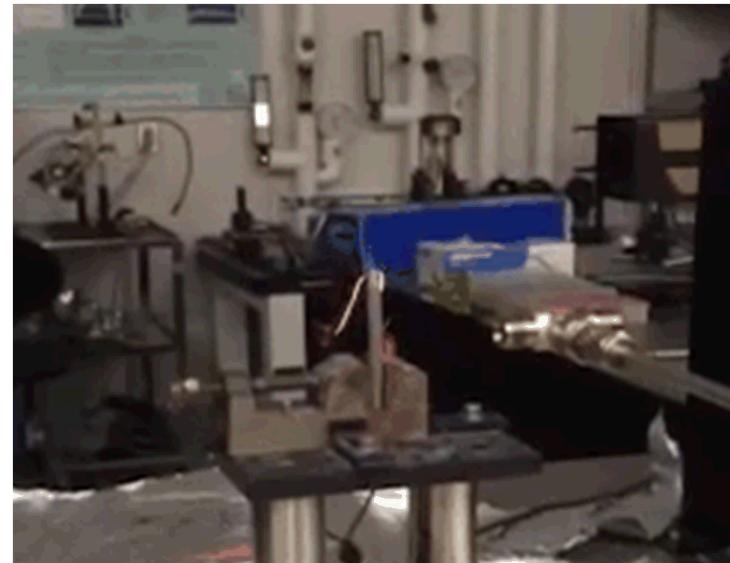
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Motivation

<http://www.cbsnews.com/news/rocket-crash-no-immediate-threat-to-station-but-cause-is-unknown/>



Color video of burning propellant



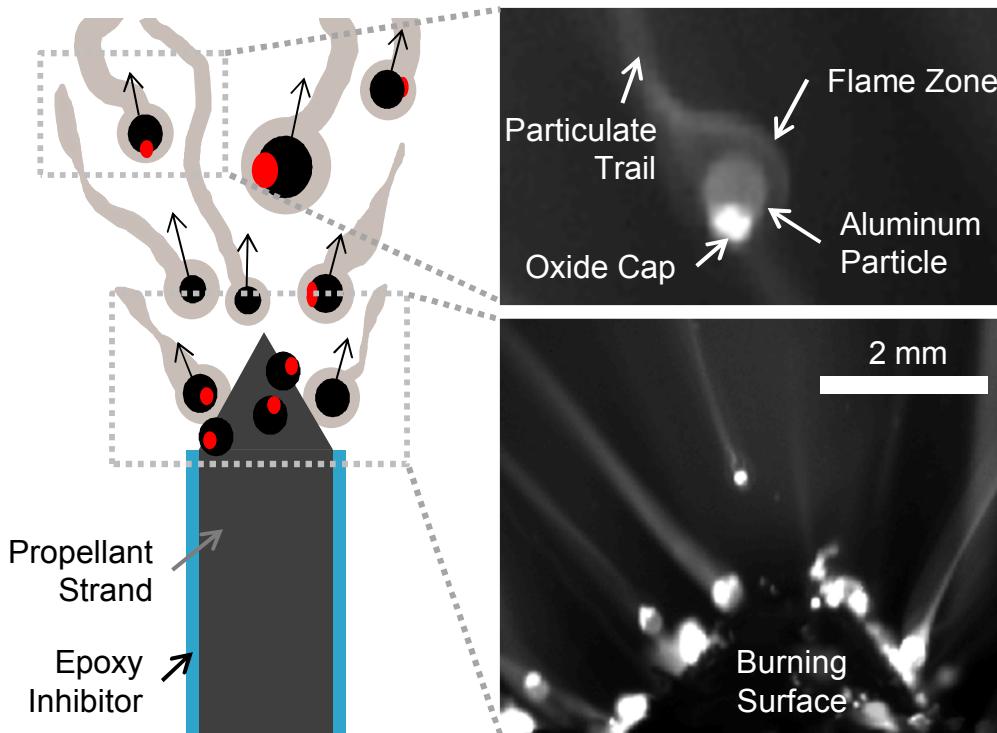
Problem:

- Rocket failures can lead to propellant fires
- Aluminum agglomeration at the surface yields large reacting drops with high damage potential
- Prediction requires knowledge of particle ***size, position, and temperature***

Goals:

- Making measurements in real propellant sticks
- Measuring the size of small particles that are out-of-focus

Approach



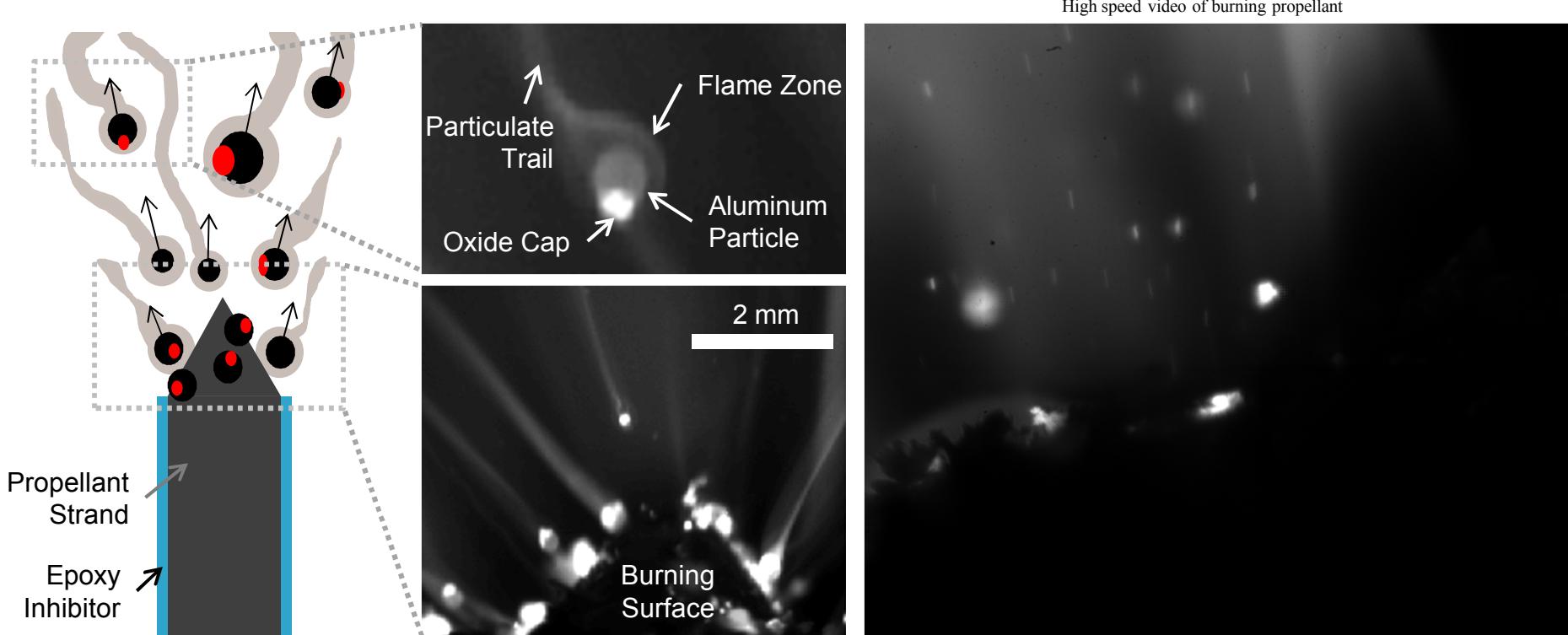
Propellant

- 6 mm diameter, 50 mm long
- 70 wt.% ammonium perchlorate oxidizer (AP)
- 20 wt.% aluminum particulate
- 10 wt.% inert hydroxyl terminated polybutadiene binder (HTPB)
- Epoxy inhibitor outer coating
- Burn rate \sim 1.4 to 1.6 mm/s

Combustion Process

- Propellant ignited with hot nichrome wire
- AP melts at 830 K, adiabatic flame temp 1205 K
- Al_2O_3 creates a flame holding effect, raising the flame temperature by \sim 1000 K
- Some Al particles (\sim 30 μm) and Al_2O_3 shells melt at 2345 K
- These agglomerate into balls (\sim 100 to 500 μm) and oxidizes to Al_2O_3 (caps and smoke) producing a flame zone (Al_2O_3 vaporizes at 3240 K)

Approach



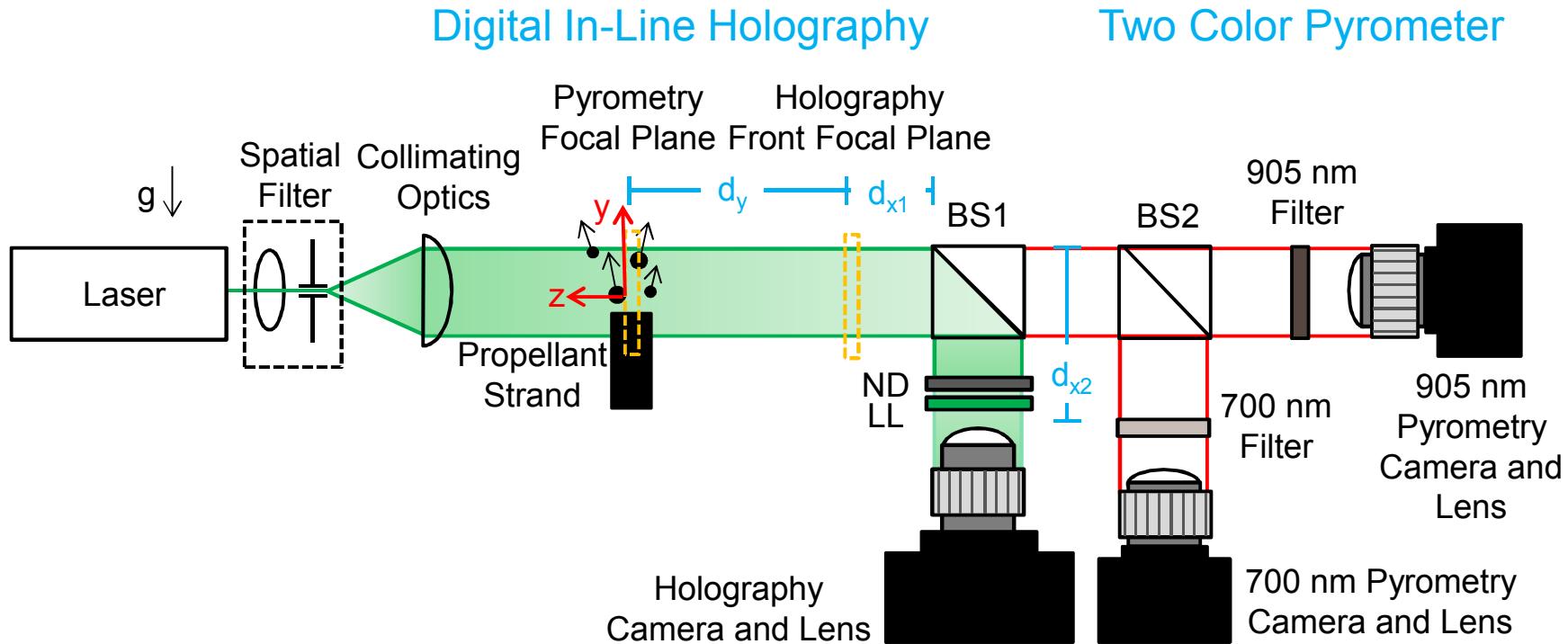
- Particle Size and Position?
- Particle Velocity?
- Particle Temperature?
- Gas Temperature and Composition?

Digital In-Line Holography (DIH)
Double Frame DIH
Two-Color Imaging Pyrometer
Coherent Anti-Stokes Raman
Scattering (CARS)

DTh2E.3 (Thurs @ 12:15 PM)
D. Guildenbecher and P. Sojka
Digital in-line holography (DIH) to quantify the impact
of a viscous drop on a thin film

LW5G.3 (Wed @ 5:45 PM)
S. Kearney and D. Guildenbecher
Temperature and oxygen measurements in a
metallized propellant flame by hybrid fs/ps rotational
coherent anti-Stokes Raman scattering

Experimental Setup



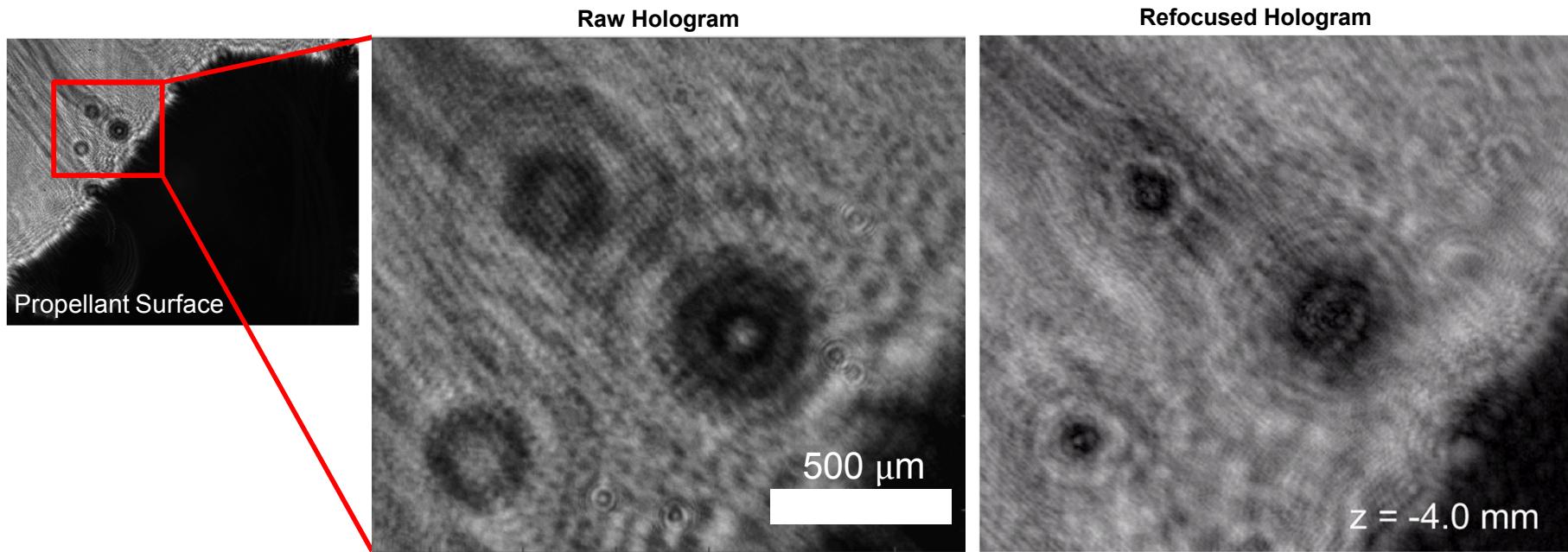
- $d_x = d_{x1} + d_{x2} = \sim 170$ mm, $d_y = 50$ mm
- Double-pulsed ND:YAG laser (Continuum MiniLite PIV, 532 nm, 5 ns pulse duration, 40 μ s pulse separation)
- Holography camera LaVision sCMOS (2560x2160 pixels, 6.5 μ m pixel pitch, 16 bit depth, global shutter mode) and lens (Infinity K2 Distamax with CF2 objective)
- Pyrometer cameras LaVision ProX 4M (2048x2048 pixels, 7.4 μ m pixel pitch, 14 bit depth, global shutter mode) and lens (Navitar Zoom 7000 lenses, aperture full open)
- ND – Neutral Density Filter (OD2)
- LL – Laserline filter at 532 nm with bandwidth of 1 nm (Andover 532FS02-50)
- BS1 – Beam splitter, reflection @ 532 nm and transmission @ 650 to 900 nm
- BS2 – Beam splitter, reflection @ 650 to 750 nm and transmission @ 850 to 950 nm
- 700 and 905 nm filters with bandwidth of 10 nm

Digital In-Line Holography

Light propagation is described by the diffraction integral equation:

$$E(x,y,z) = \frac{1}{\lambda} \iint E(\xi, \eta, z=0) \frac{e^{-jkr}}{r} d\xi d\eta \quad \text{where: } r = \sqrt{(\xi - x)^2 + (\eta - y)^2 + z^2}$$

$E(x,h,0) \equiv$ complex amplitude at hologram plane = $h(x,h) \cdot E_r^*$
 $E(x,y,z) \equiv$ refocused complex amplitude at optical depth z



Digital In-Line Holography

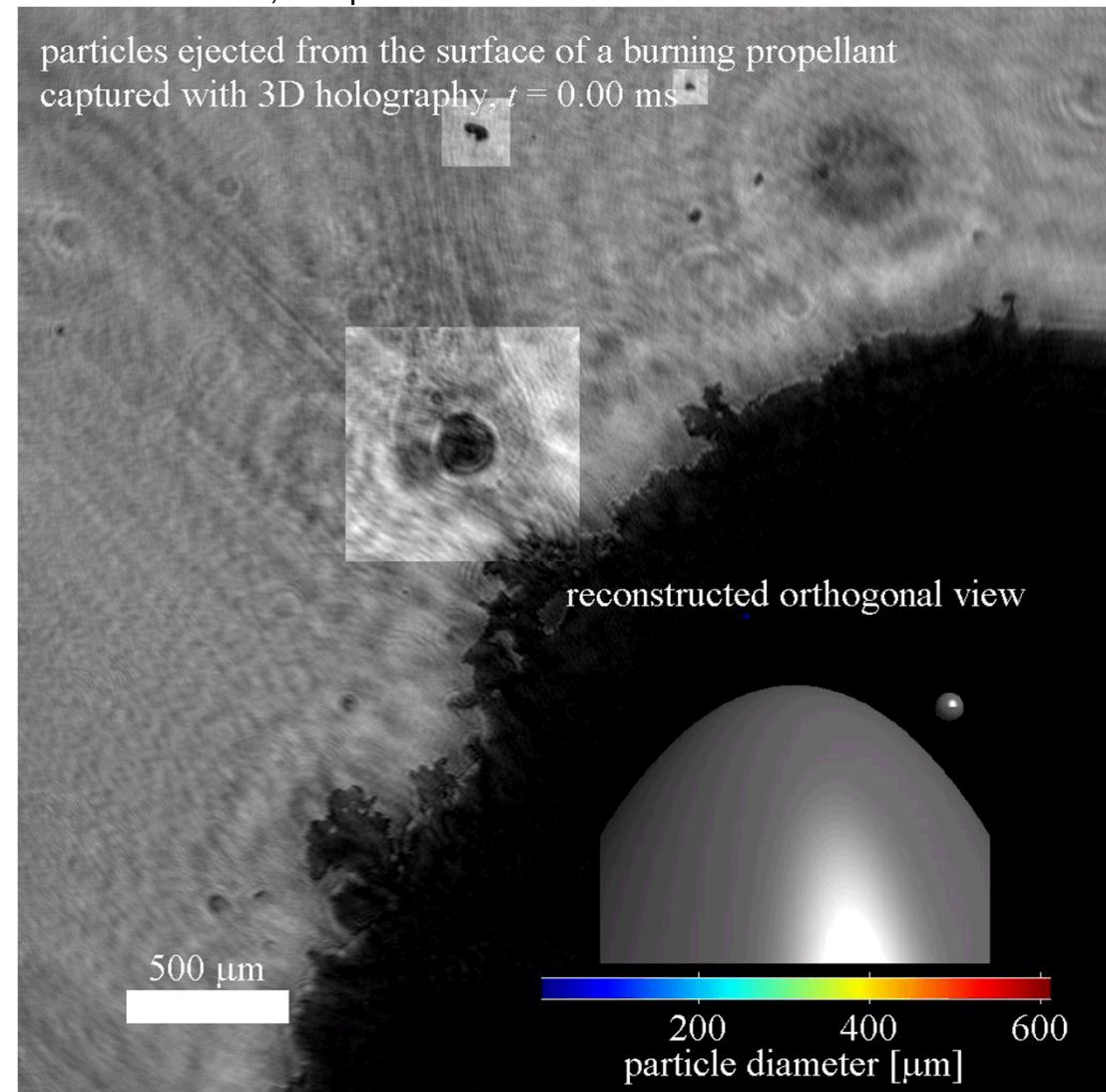
Recorded at 20,000 fps on Photron SA-Z with Coherent Verdi V6 Laser

Calibration

- Use a 1mm spacing dot grid
- Dewarp the images on 3 cameras to the same field of view

Detection Methods

- Find particle z-position by minimizing intensity and maximizing edge sharpness across a series of z-slices
- Find particle diameter by counting the number of dark pixels (minimum $d = 11 \mu\text{m}$)



D. Guildenbecher et. al., Applied Optics Vol. 55 (11), 2016.

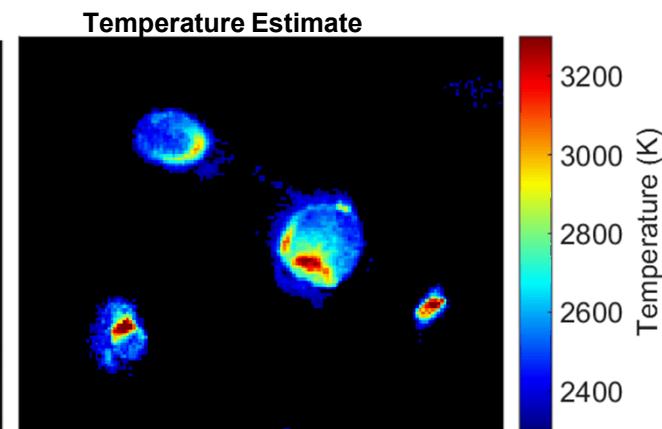
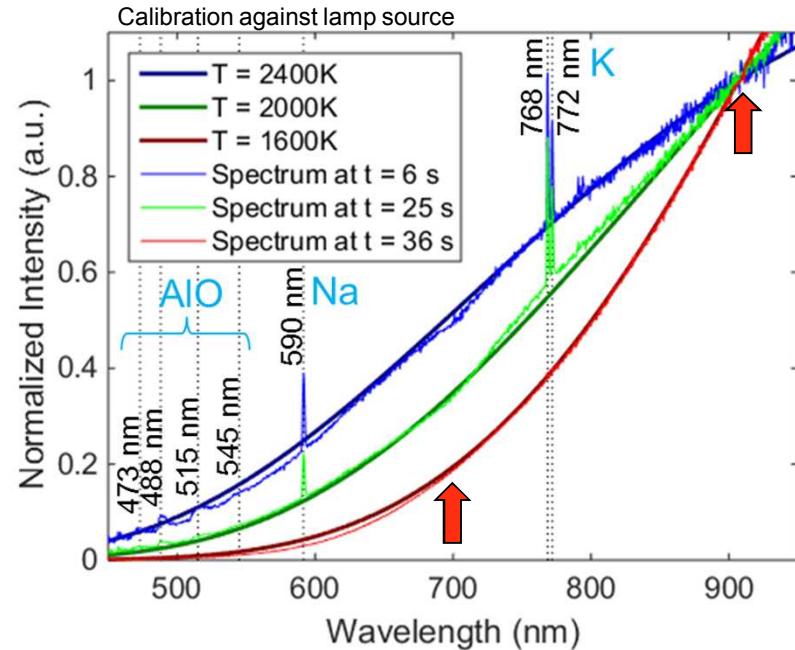
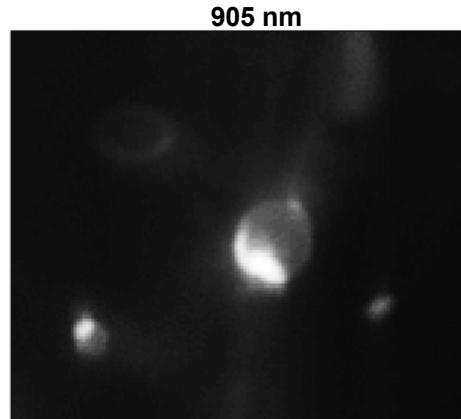
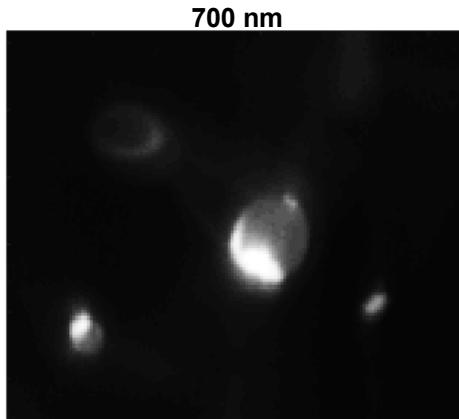
Two-Color Pyrometer

- Can use Plank's Law, assuming grey body emission
- Choose wavelengths to avoid combustion peaks
- If $hc/\lambda \gg kT$, use Wein's approximation for each pixel:

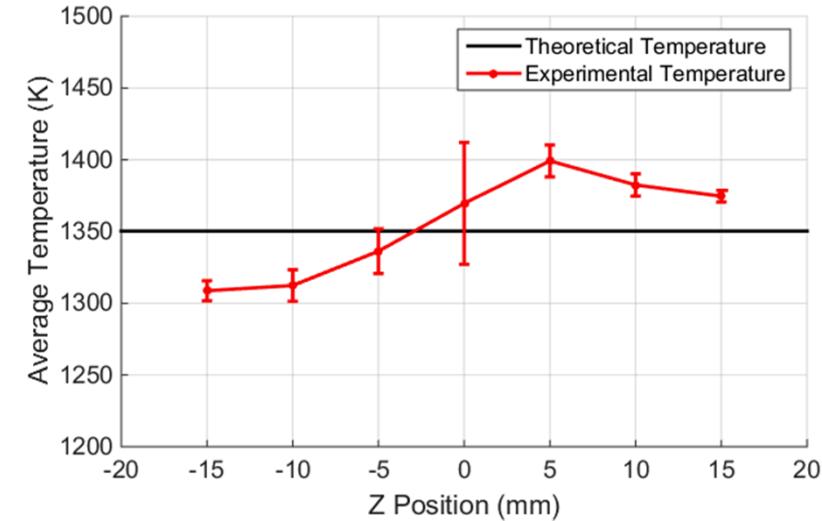
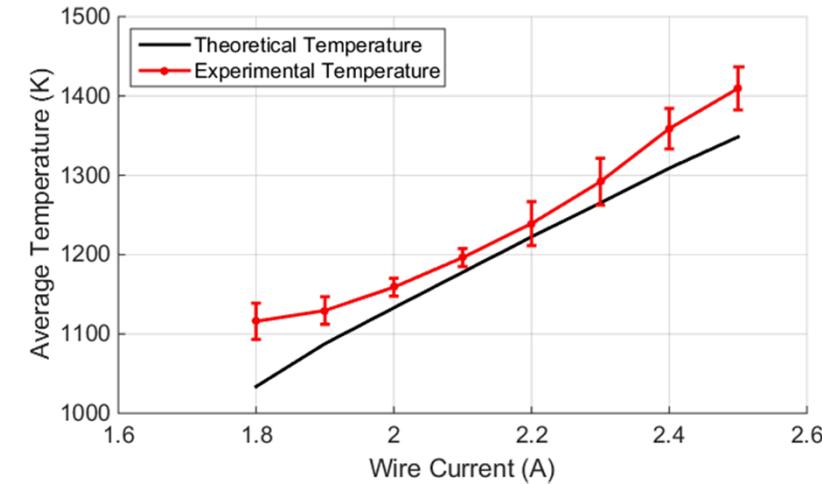
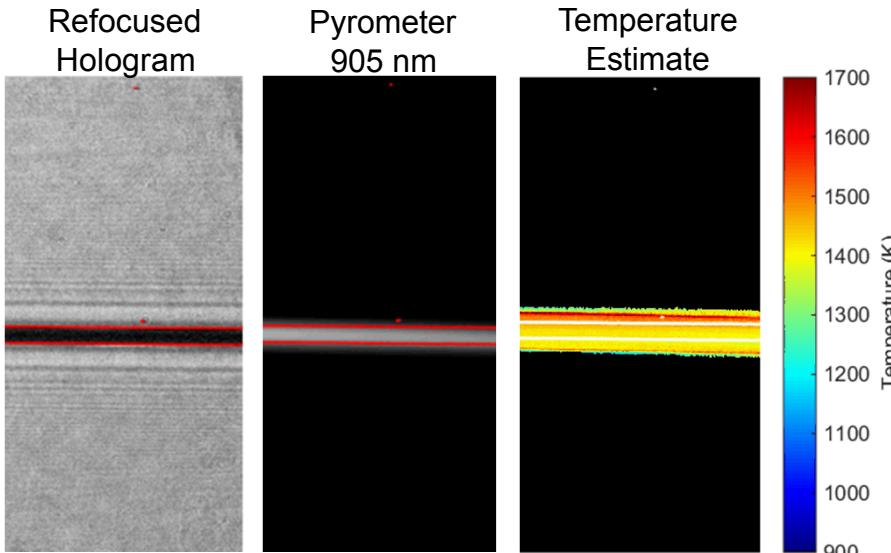
$$T = \left[\frac{k}{hc} \frac{\lambda_1 \lambda_2}{\lambda_2 - \lambda_1} \left(\ln(R) - 5 \ln\left(\frac{\lambda_1}{\lambda_2}\right) \right) \right]^{-1}$$

$$\text{where } R = \frac{I_2}{I_1} \frac{E_1 \eta_1}{E_2 \eta_2}$$

- Determine the matching pixels from DIH camera to pyrometer cameras (low intensity pixels removed)

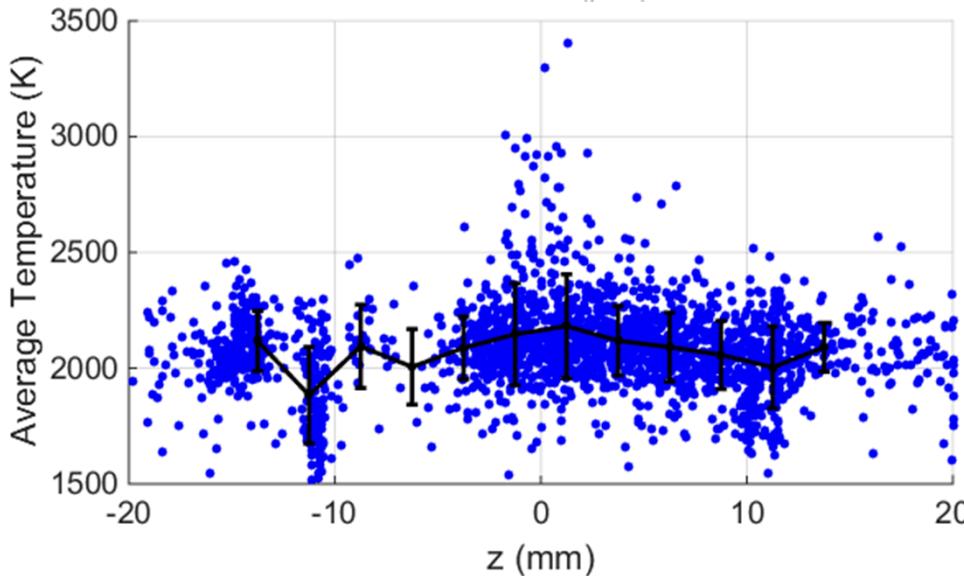
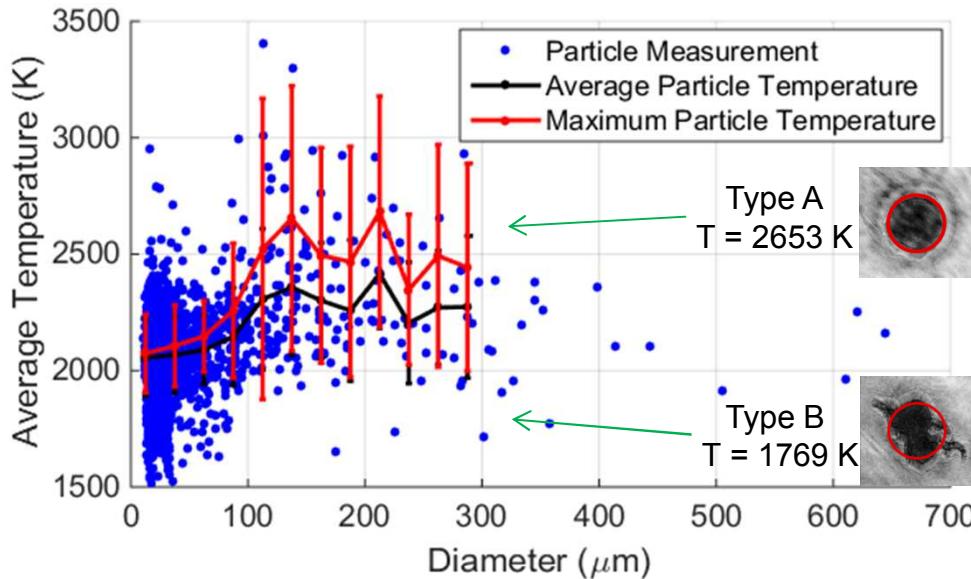


Pyrometer Calibration



- Checked temperature calibration against a 240 μm hot nichrome wire
- Determined the effect of focus on temperature estimate
 - In-focus features have more temperature variation
 - Out-of-focus features have less variation
 - Overall temperature variation ± 50 K

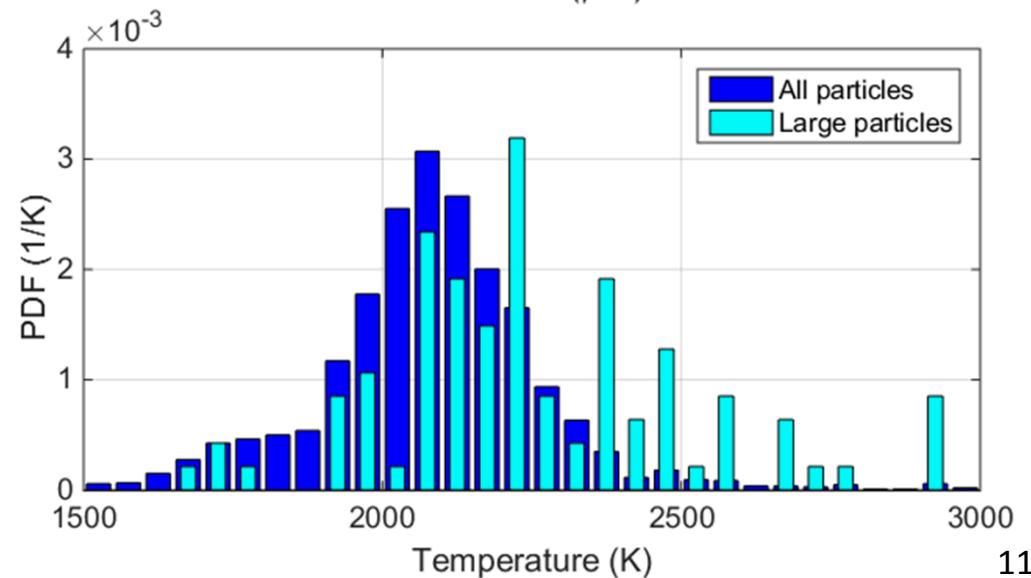
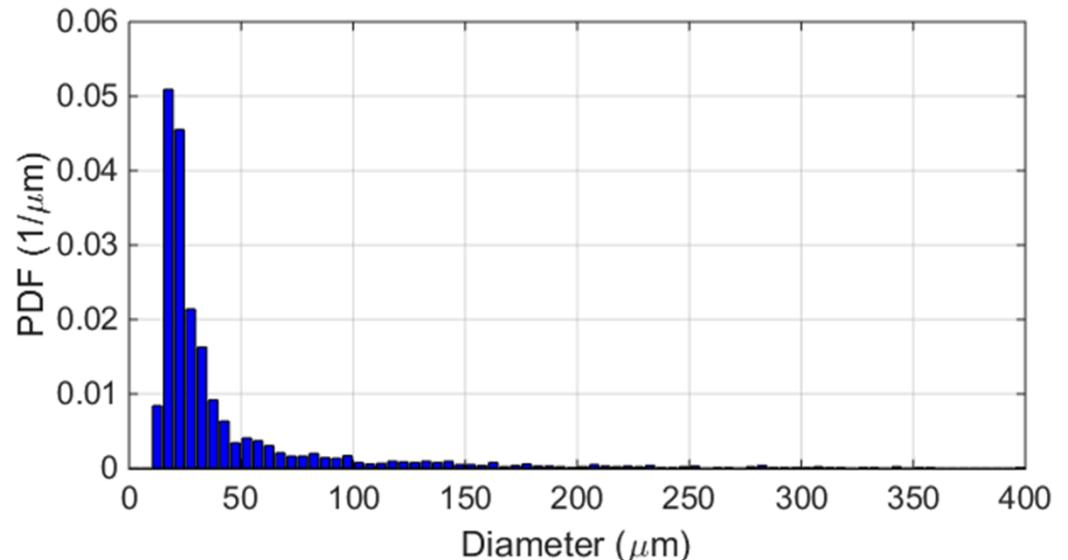
Measured Statistics



- One propellant stick burn with 2120 particles across 143 frames
- Sampled at 14 fps, each frame is uncorrelated
- Temperature of small particles approaches the temperature of the gas quickly
- Average particle temperatures are less than boiling point for Al (2792 K)
- Maximum particle temperatures less than boiling point for Al_2O_3 caps (3240 K)
- Temperature variation near the focal point is the greatest,
 - Similar to the calibration
 - May be evidence of hotter particles in the center of the flame

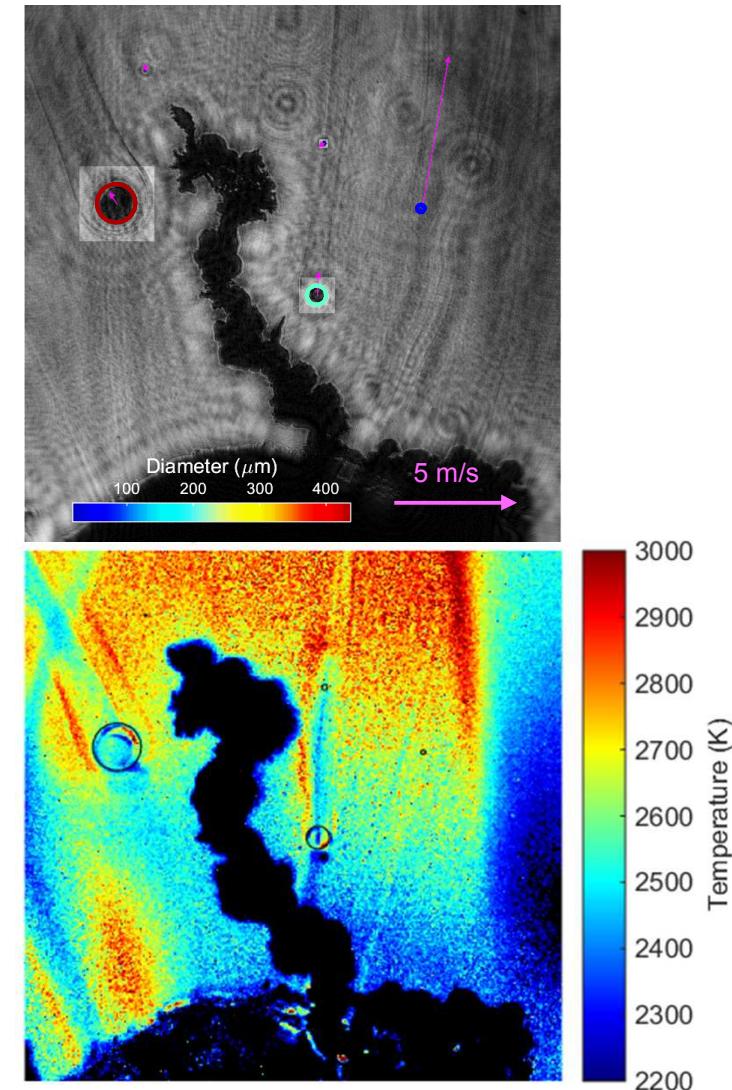
Measured Statistics

- The majority of the particles are small
- $D_{10} = 43.0 \mu\text{m}$
(mean diameter)
- $D_{32} = 249 \mu\text{m}$
(Sauter or surface area weighted)
- $D_{43} = 377 \mu\text{m}$
(volume weighted)
- Particle temperatures are a complex mixture of particles in different stages of combustion
- Since most of the particles measured are small, we expect average temperatures to be similar to gas temperatures
- For all particles
 $T_{\text{ave}} = 2084 \pm 189 \text{ K}$
- For large particles ($>150 \mu\text{m}$)
 $T_{\text{ave}} = 2131 \pm 256 \text{ K}$
- Similar to average gas temperatures measured with CARS



Conclusions and Future Work

- Demonstrated simultaneous DIH and Two-Color Pyrometer measurements of aluminized ammonium perchlorate propellant sticks
 - Position
 - Size
 - Temperature
- Sources of error and bias
 - Temperature calibration accuracy
 - Camera readout smear for short exposures
 - Gray body assumption
 - Overlap of particles and soot at different temperatures
- Future work
 - Additional propellant stick burns for better statistics
 - Velocity statistics to correct probability distributions



Acknowledgements



- The Weapons Systems Engineering Assessment Technology program
- The Laboratory Directed Research and Development program
- Howard Lee Stauffacher for his work with the propellant igniter system
- Thomas W. Grasser for his work with the optical system construction



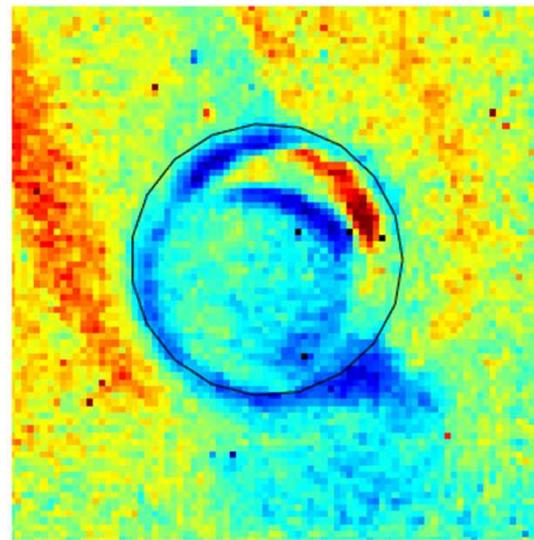
Sandia National Laboratories



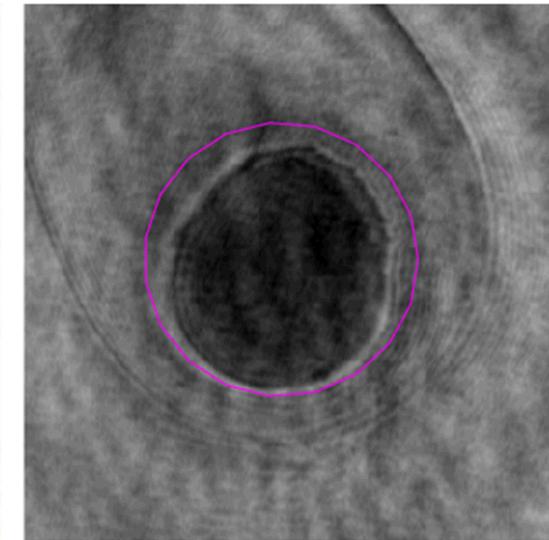
**U.S. DEPARTMENT OF
ENERGY**



Temperature Estimate



Refocused Hologram



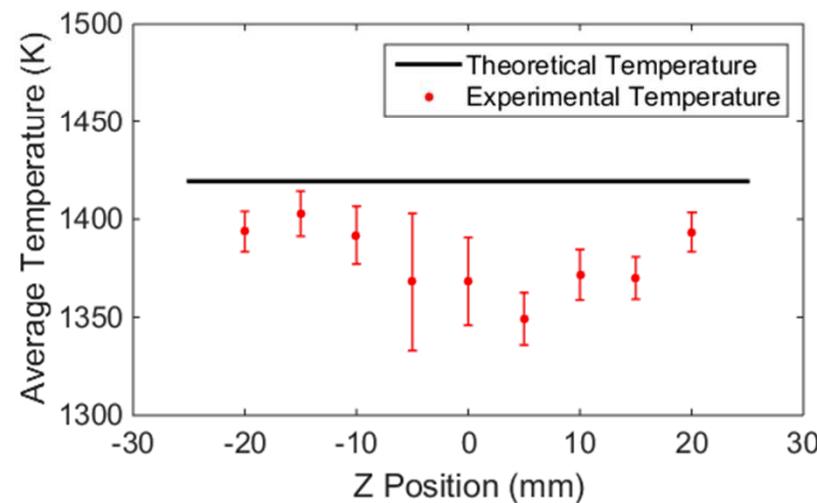
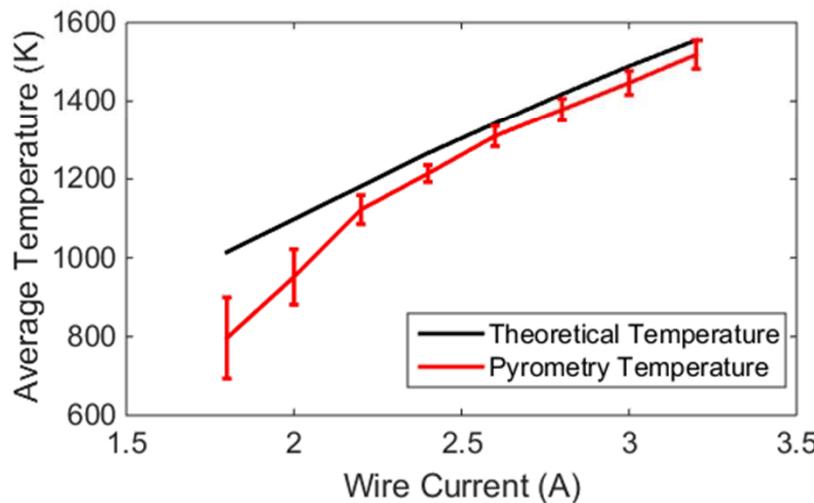
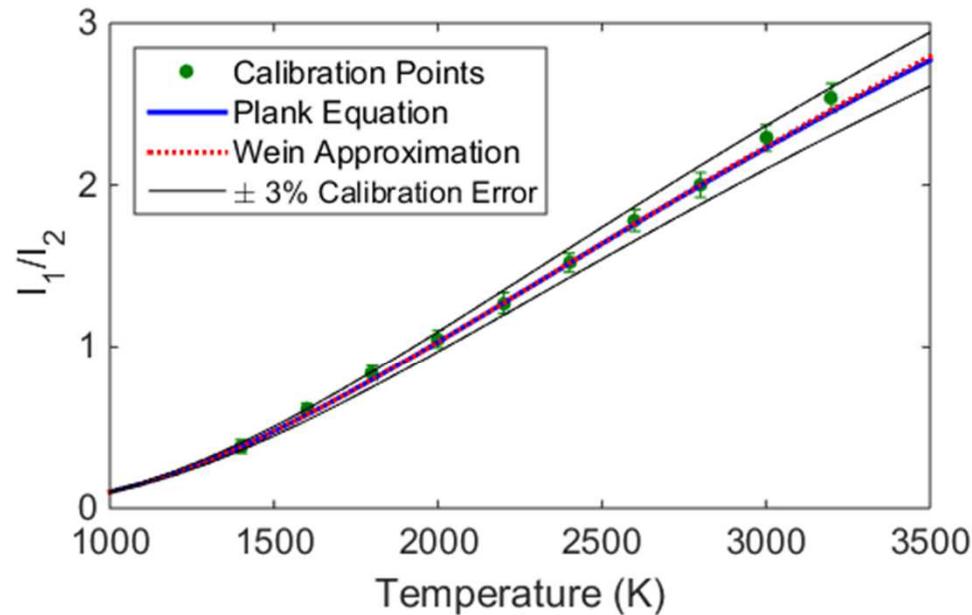
QUESTIONS?

References

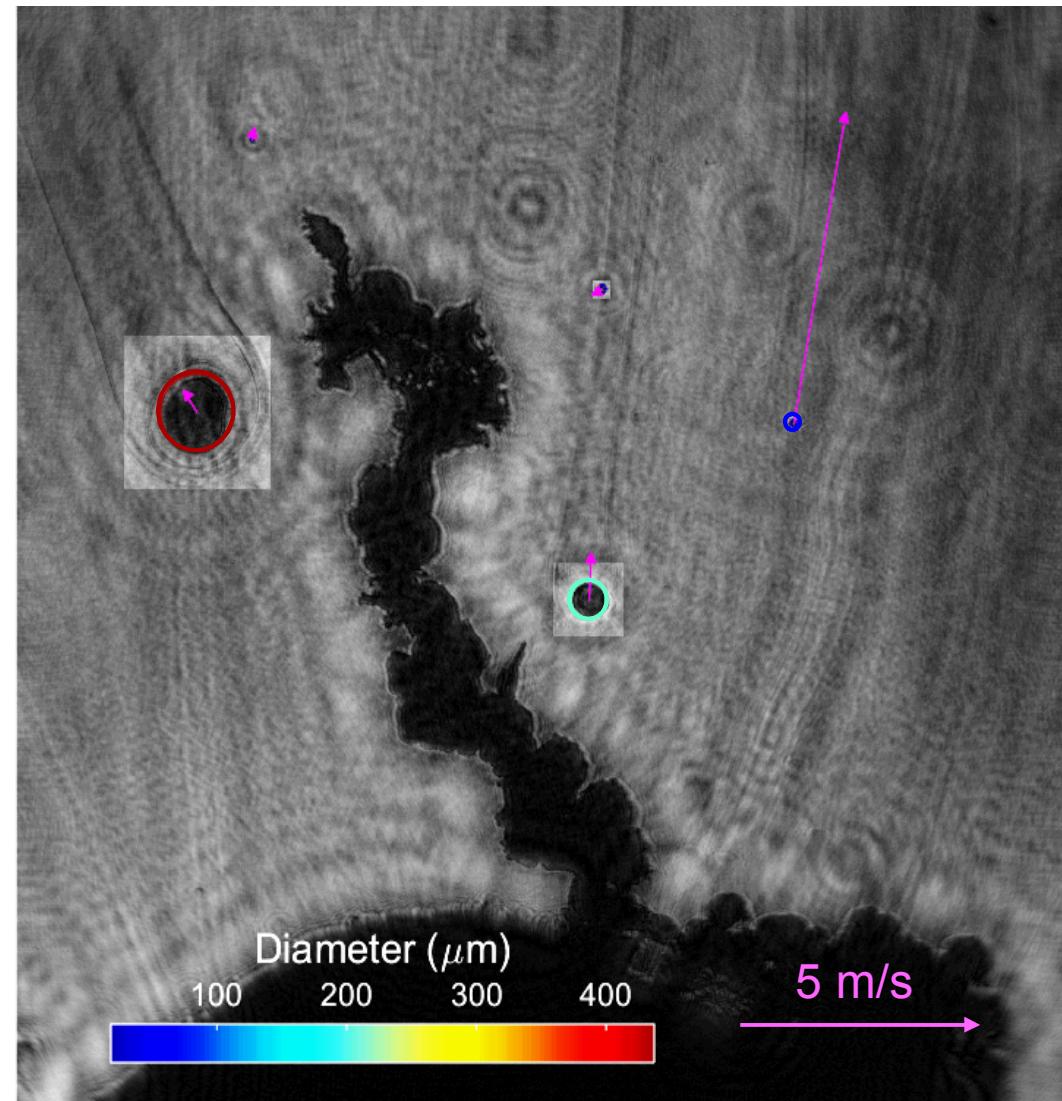
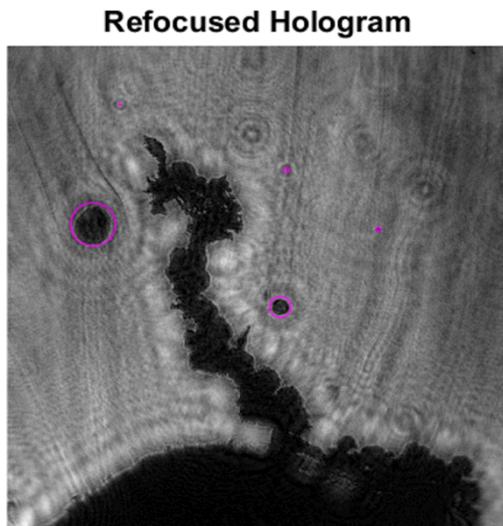
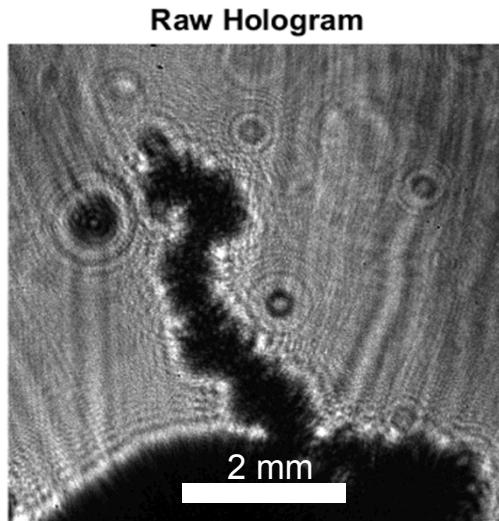
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BACKUP SLIDES

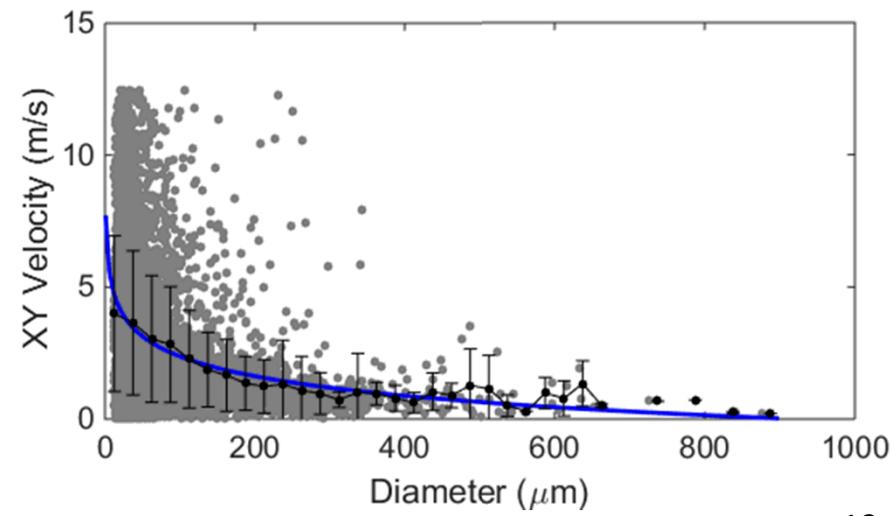
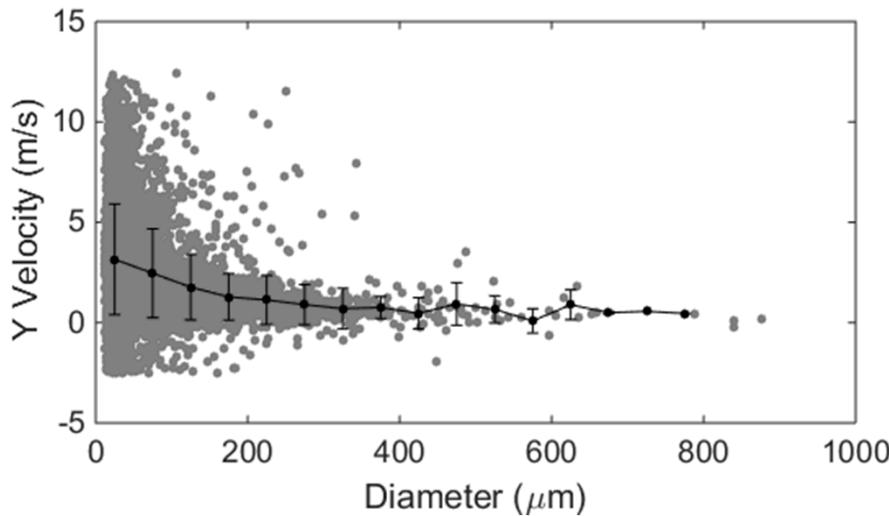
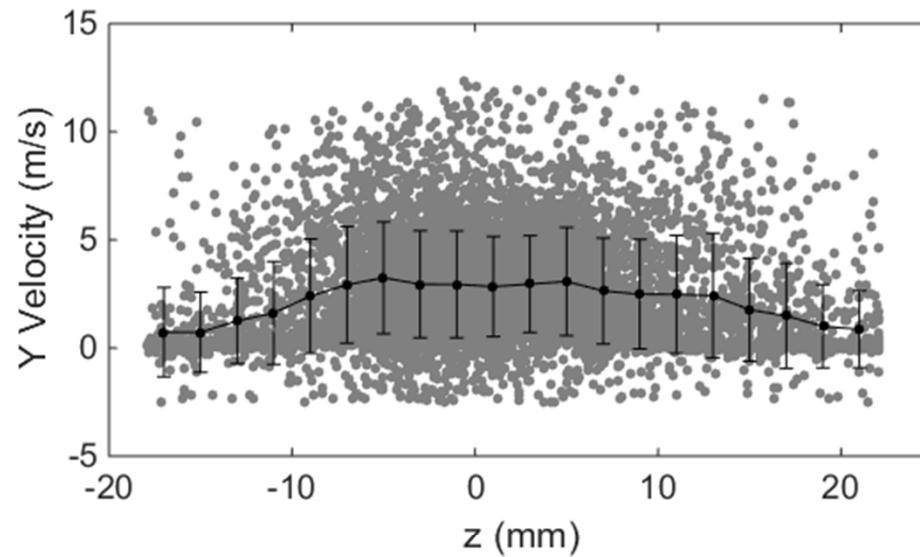
Black Body Calibration



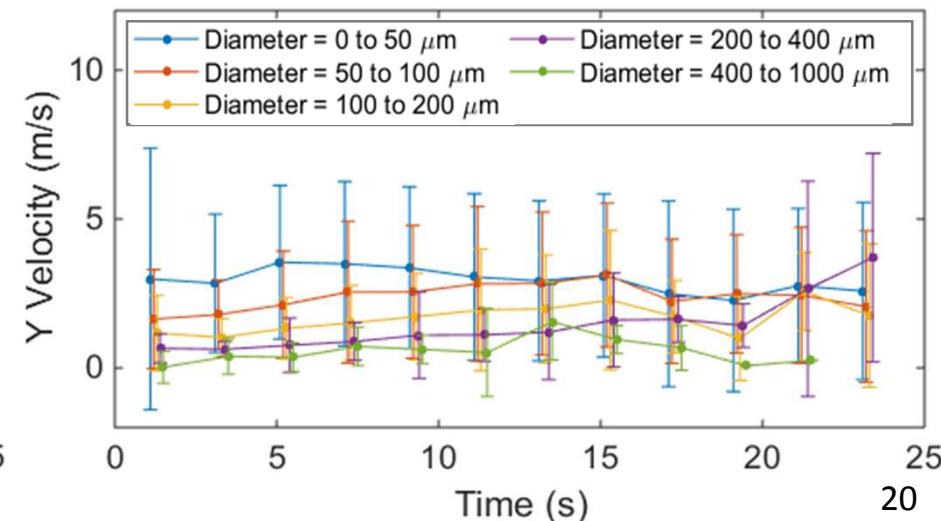
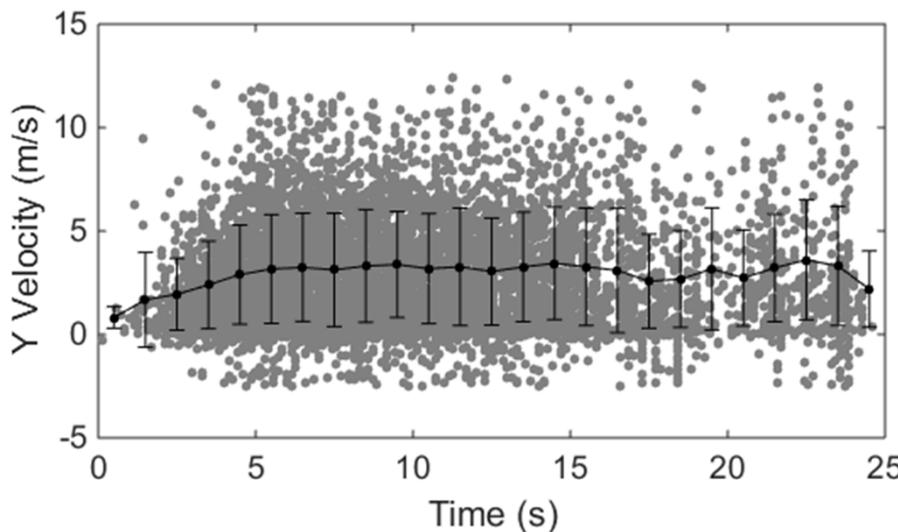
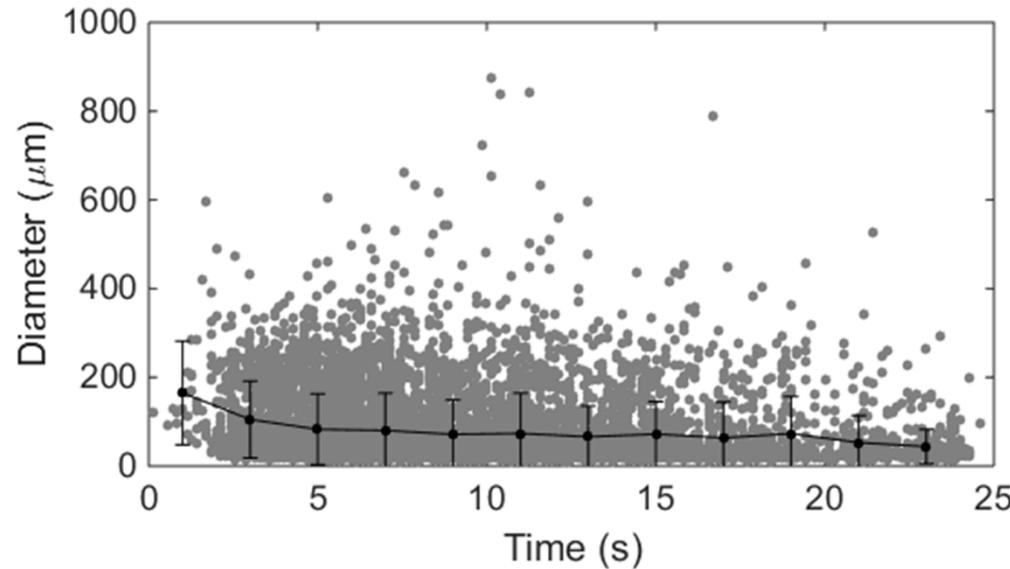
Velocity Measurement



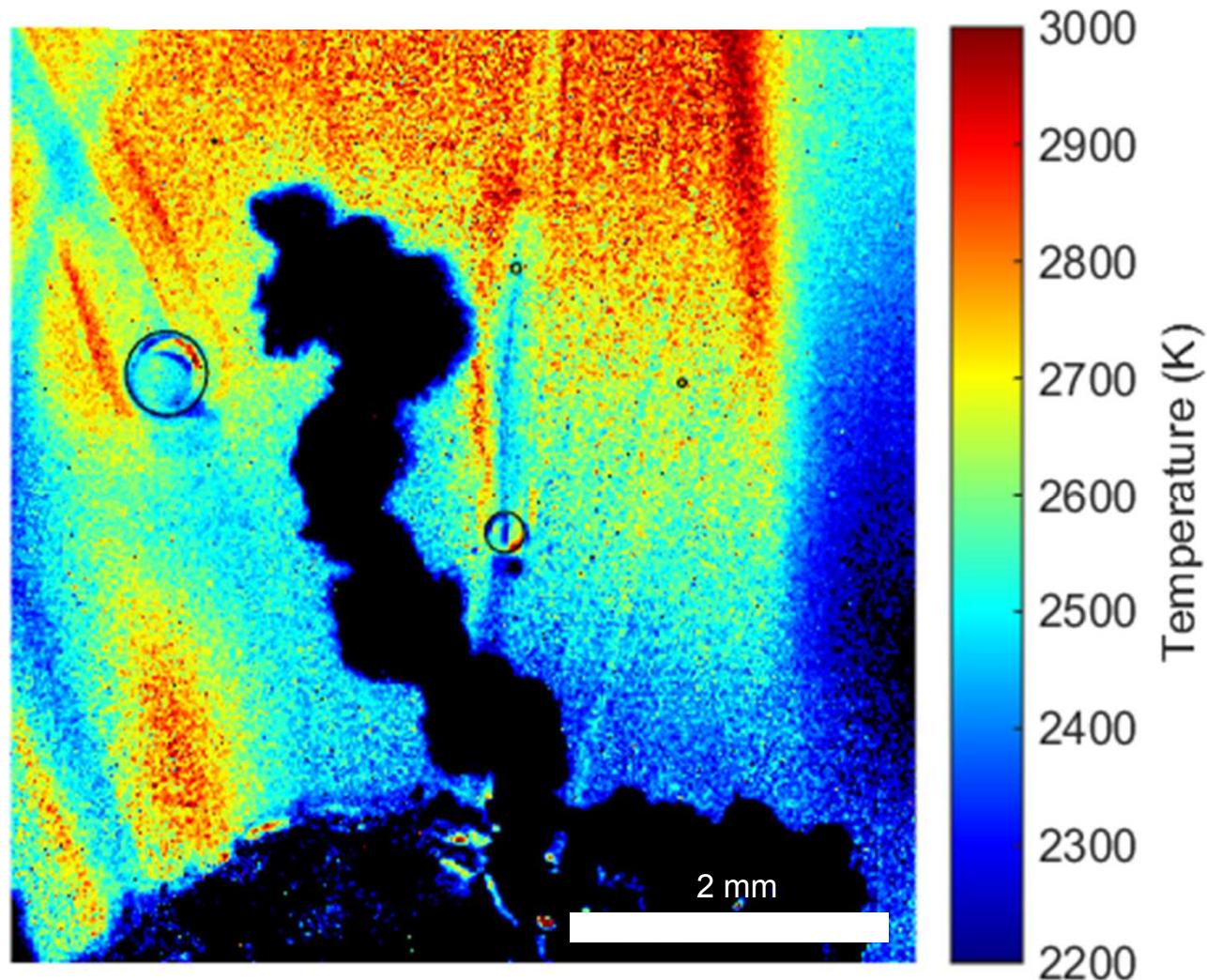
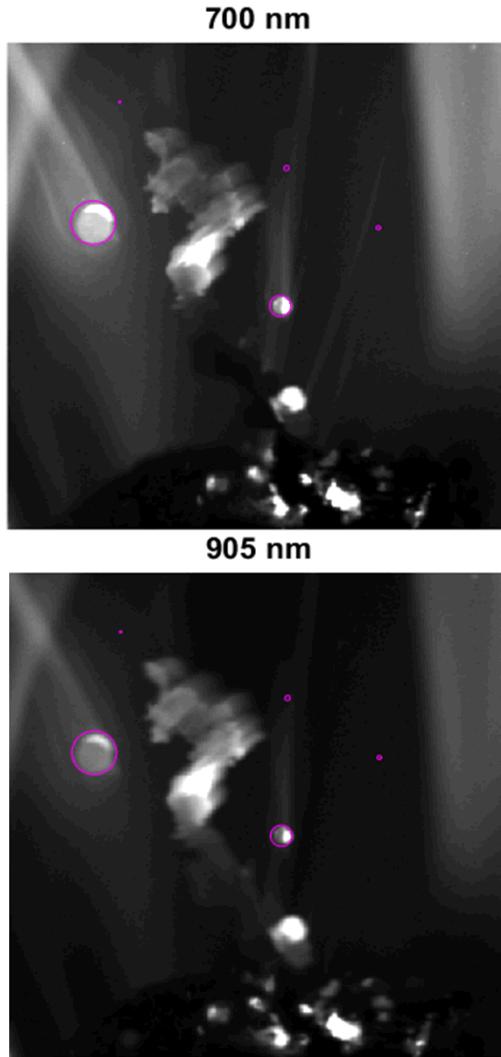
Velocity Measurement



Time Evolution

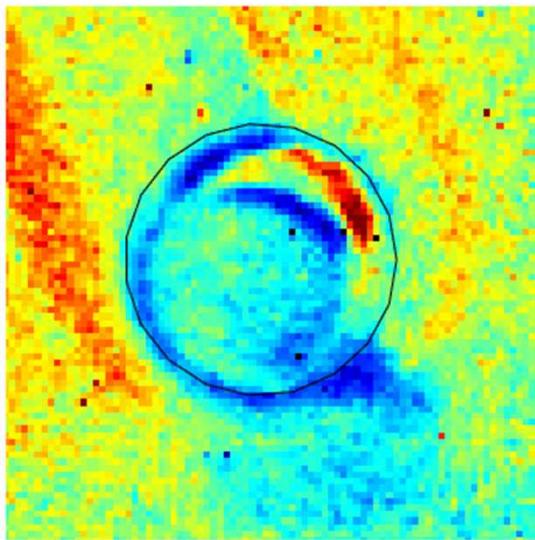


Temperature Measurement

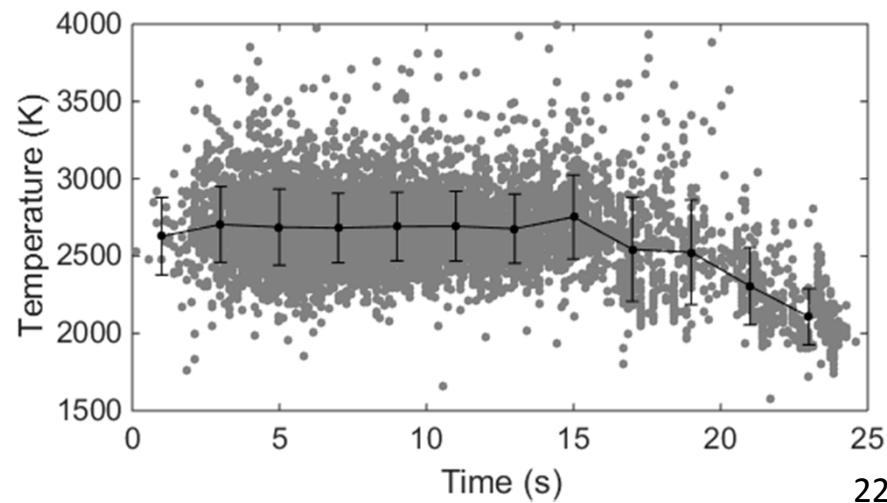
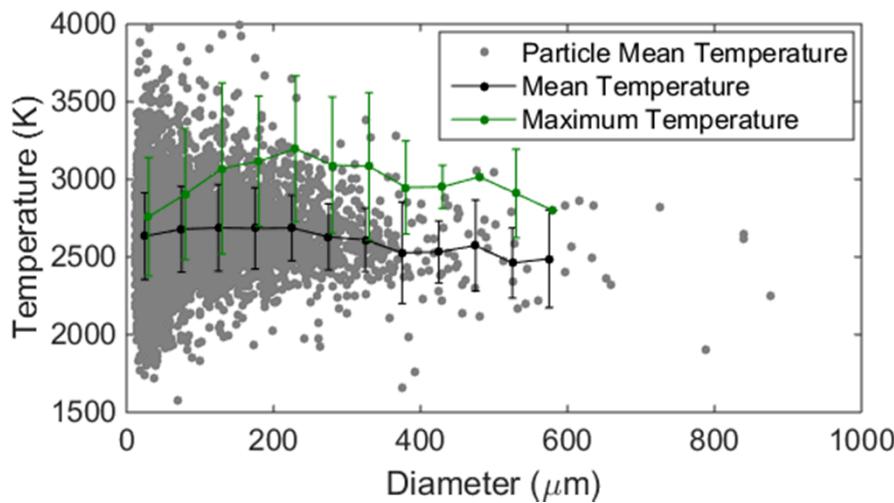
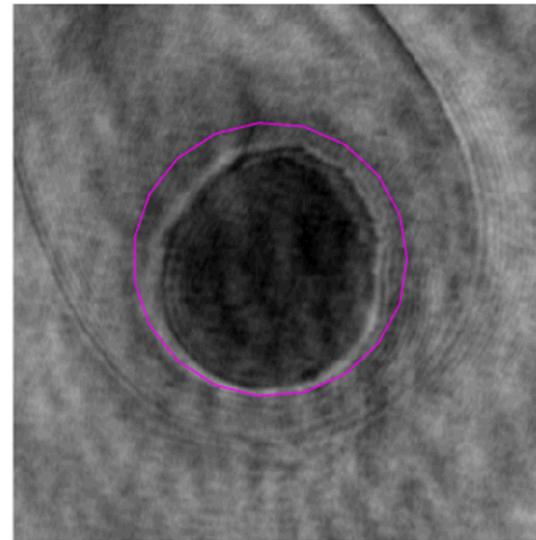


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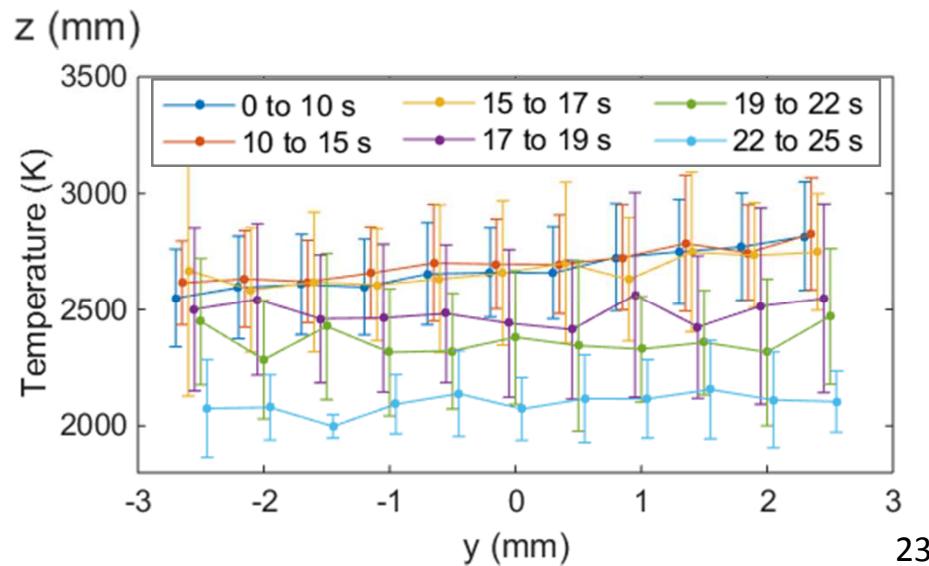
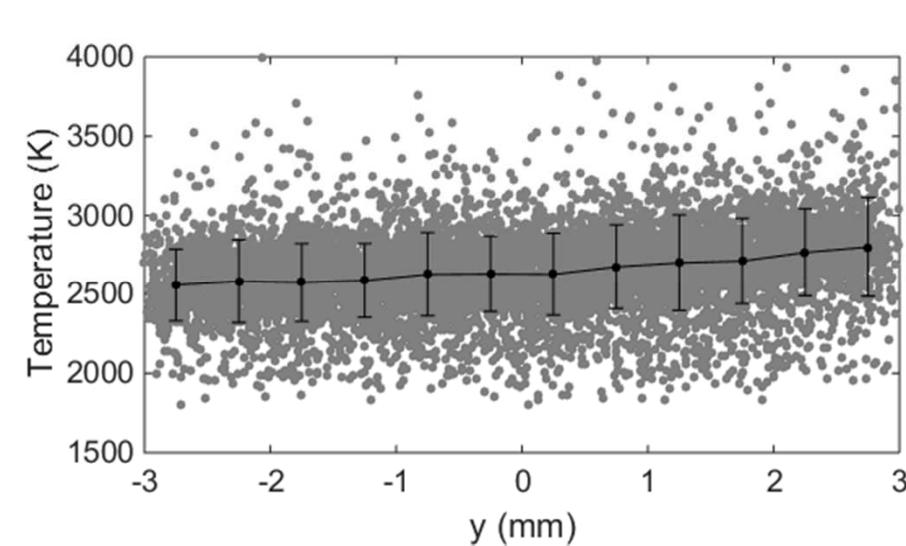
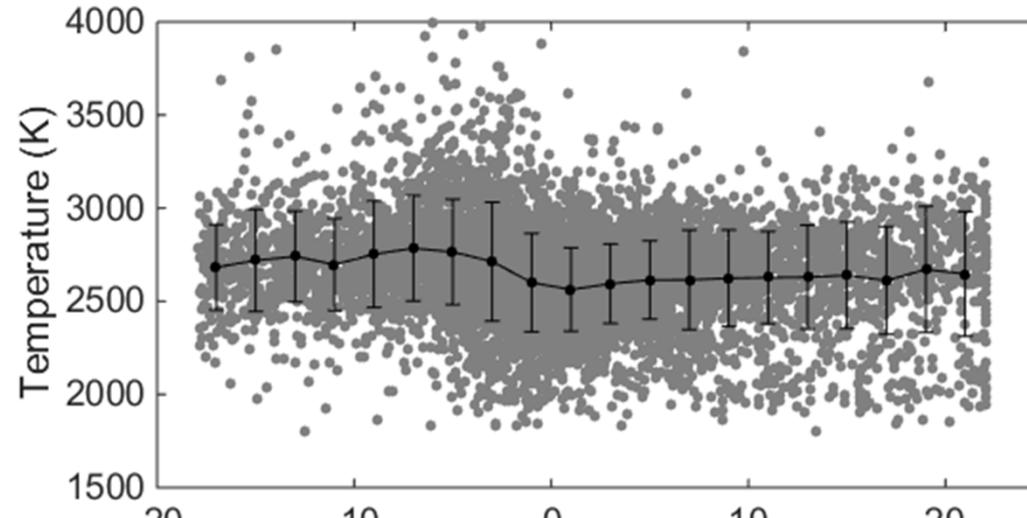
Temperature Estimate



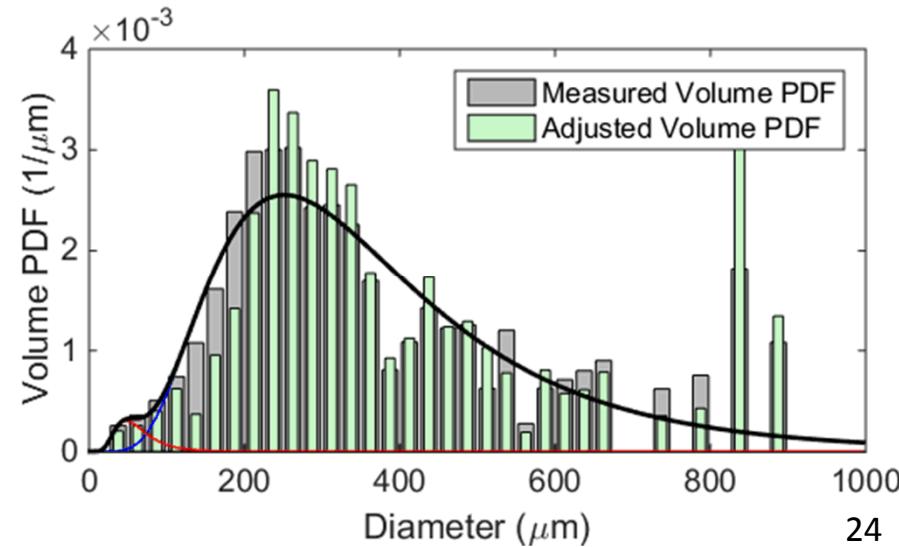
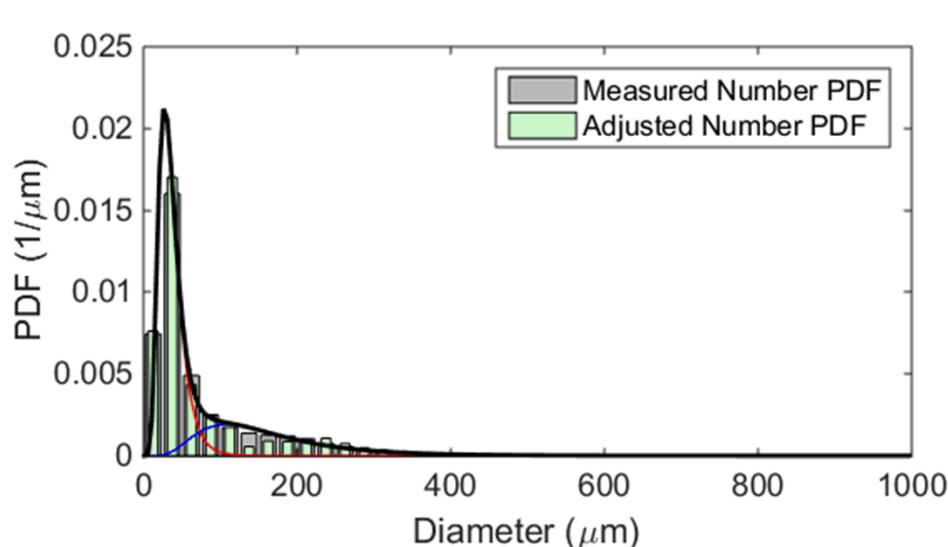
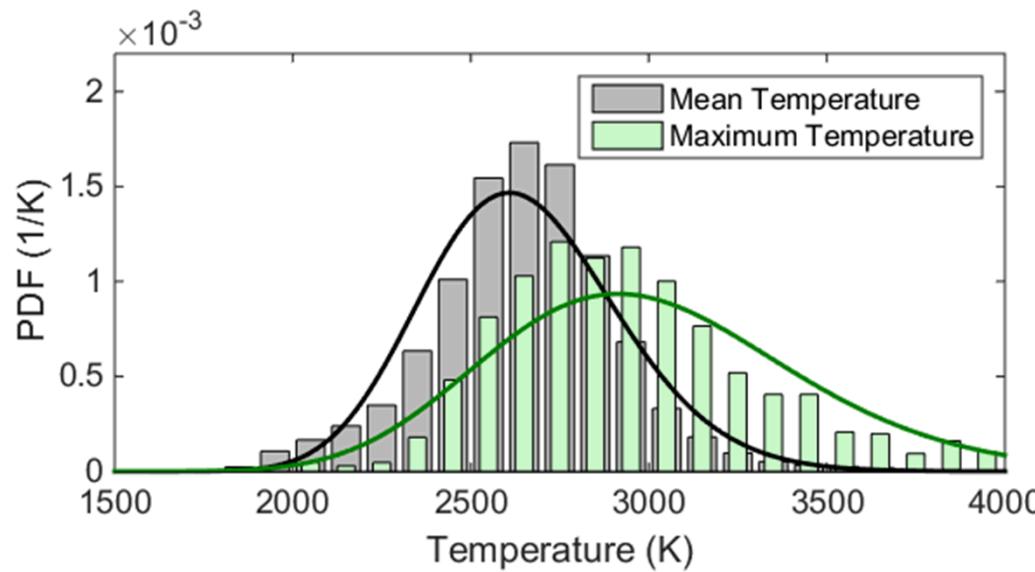
Refocused Hologram



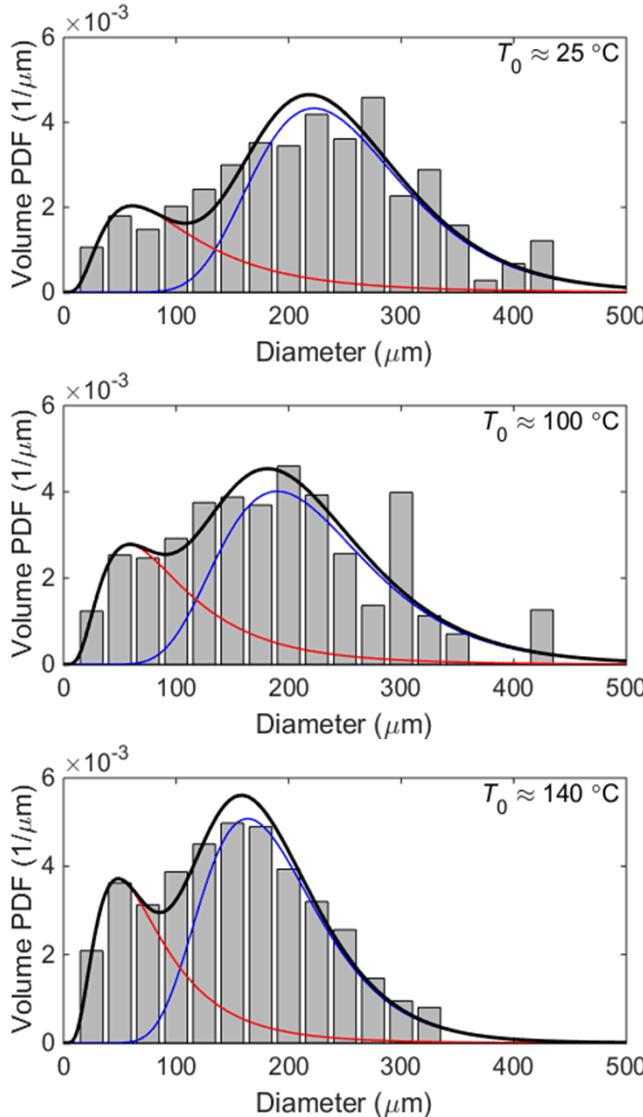
Temperature Measurement



Particle Statistics



Initial Propellant Temperature



| T_0 ($^\circ\text{C}$) | N | D_{10} (μm) | D_{32} (μm) | D_{43} (μm) | MMD (μm) |
|-------------------------------|-------|-------------------------------|-------------------------------|-------------------------------|--------------------------|
| 25 | 17496 | 37.9 | 150.7 | 217.6 | 220.5 |
| 100 | 6890 | 39.0 | 127.4 | 187.6 | 185.7 |
| 140 | 15346 | 35.2 | 104.5 | 153.8 | 151.6 |

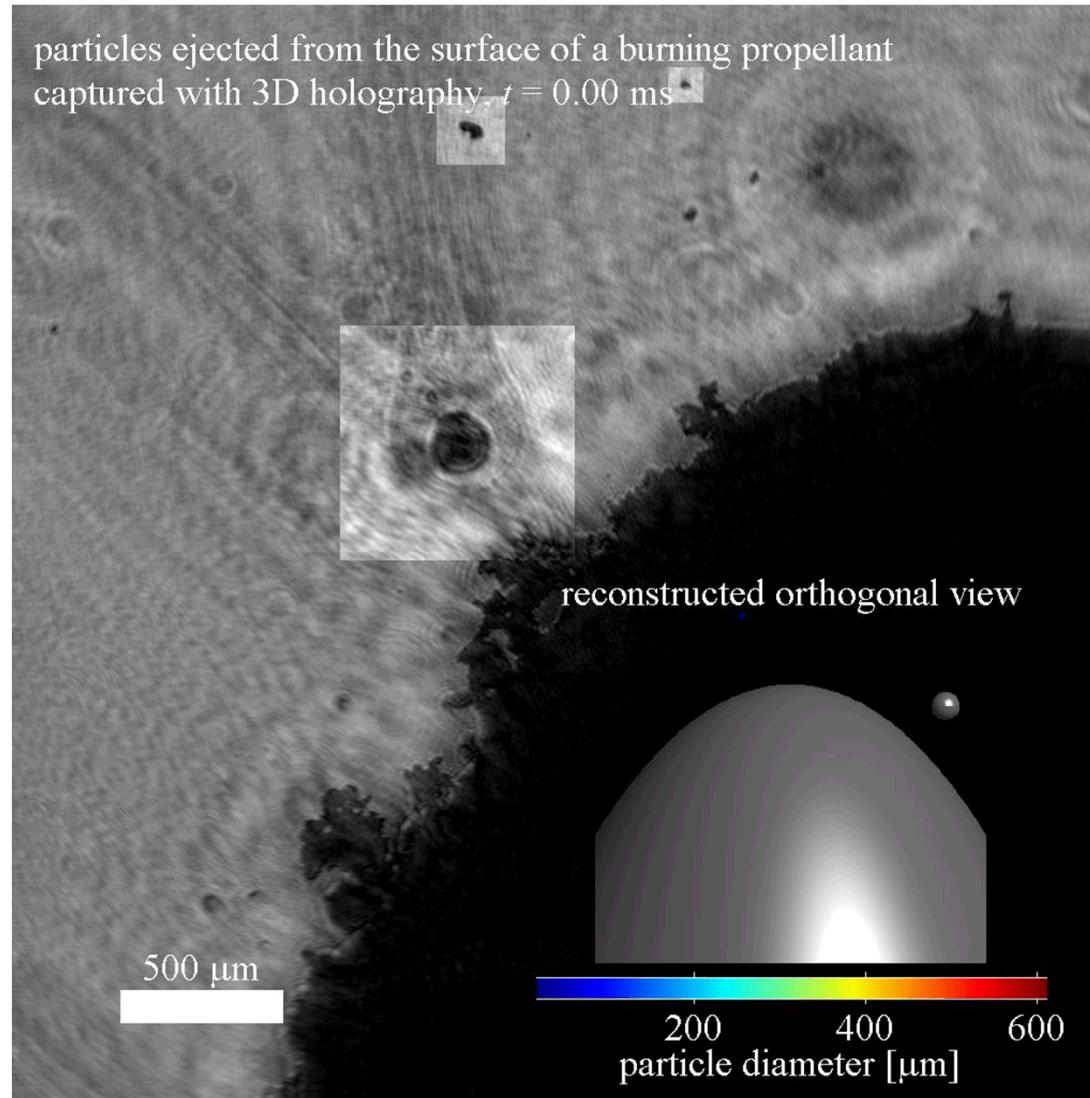
Bi-modal log-normal fits

$$f(d) = \frac{1-w}{d\sigma_a\sqrt{2\pi}}e^{-\frac{(ln d - \mu_a)^2}{2\sigma_a^2}} + \frac{w}{d\sigma_b\sqrt{2\pi}}e^{-\frac{(ln d - \mu_b)^2}{2\sigma_b^2}}$$

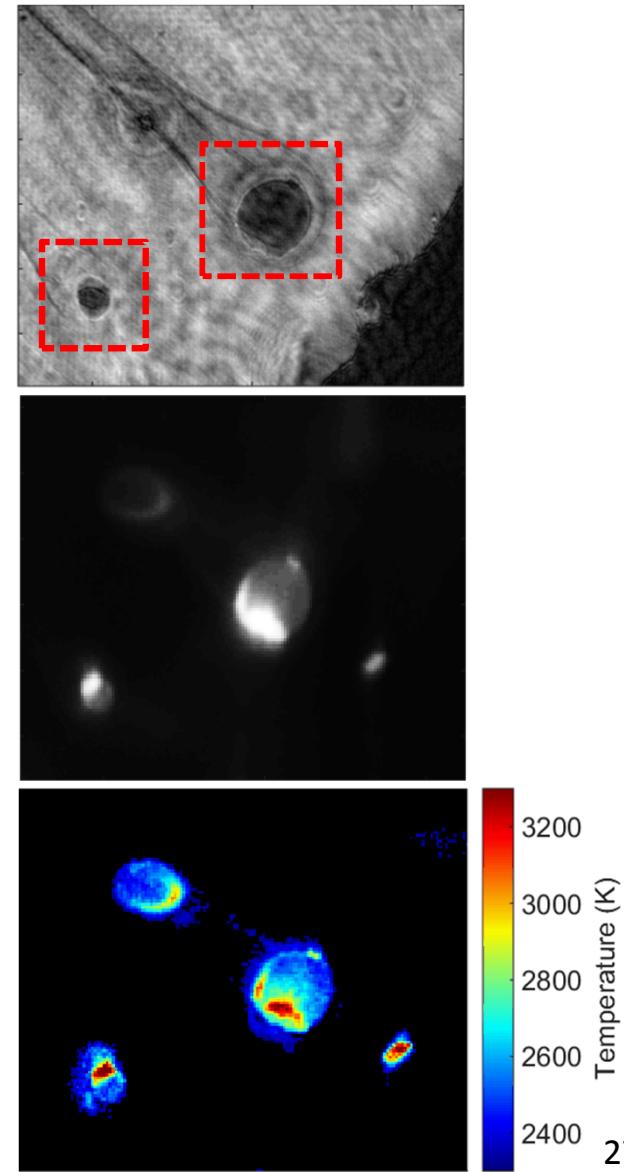
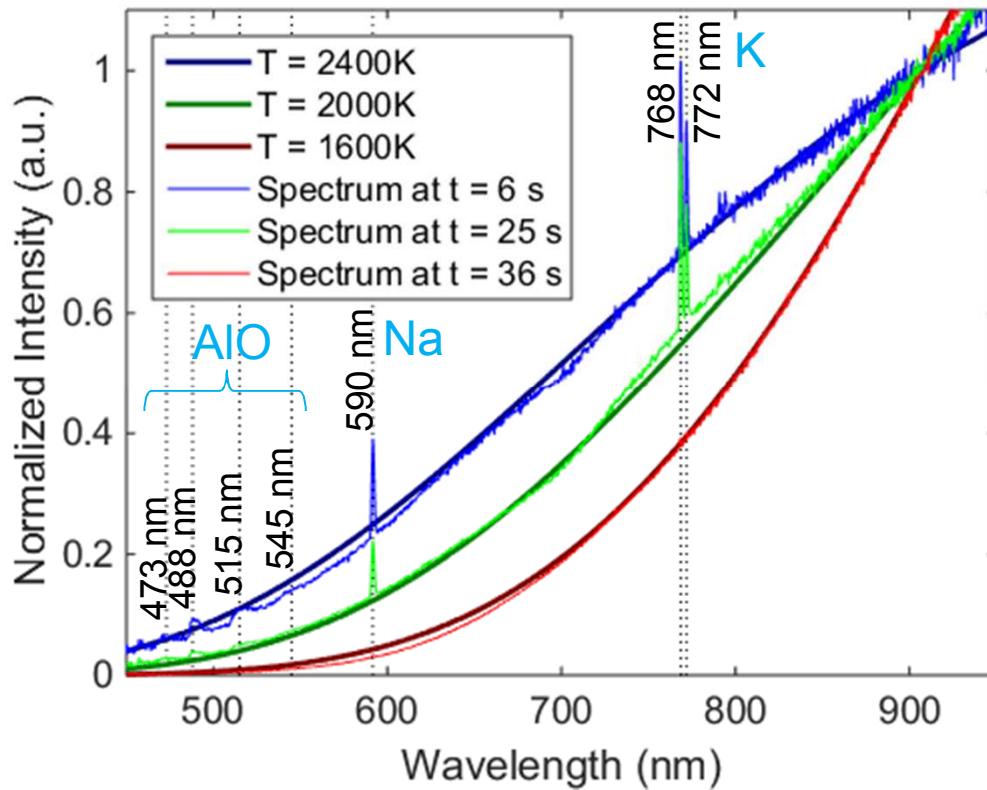
| T_0 ($^\circ\text{C}$) | w | μ_a ($\ln[\mu\text{m}]$) | σ_a ($\ln[\mu\text{m}]$) | μ_b ($\ln[\mu\text{m}]$) | σ_b ($\ln[\mu\text{m}]$) |
|-------------------------------|------|-----------------------------------|--------------------------------------|-----------------------------------|--------------------------------------|
| 25 | 0.74 | 4.56 | 0.67 | 5.49 | 0.29 |
| 100 | 0.69 | 4.47 | 0.64 | 5.36 | 0.34 |
| 140 | 0.67 | 4.25 | 0.61 | 5.19 | 0.31 |

As the initial propellant stick temperature increases, the minimum size of agglomerated particle decreases and the weight fraction of larger particles decreases

High Speed Video



Two-Color Pyrometry



Equations

Diffraction Integral Equation

$$E(x, y, z) = \frac{1}{\lambda} \iint E(\xi, \eta, z=0) \frac{e^{-jkr}}{r} d\xi d\eta \quad \text{where: } r = \sqrt{(\xi - x)^2 + (\eta - y)^2 + z^2}$$

Two-Color Pyrometer Equation using Wein's Approximation

$$T = \left[\frac{k}{hc} \frac{\lambda_1 \lambda_2}{\lambda_2 - \lambda_1} \left(\ln(R) - 5 \ln\left(\frac{\lambda_1}{\lambda_2}\right) \right) \right]^{-1}$$

where $R = \frac{I_2}{I_1} \frac{E_1 \eta_1}{E_2 \eta_2}$