

Nonlinear dynamics of aqueous dissolution of silicate glasses and its implications to glass waste form durability

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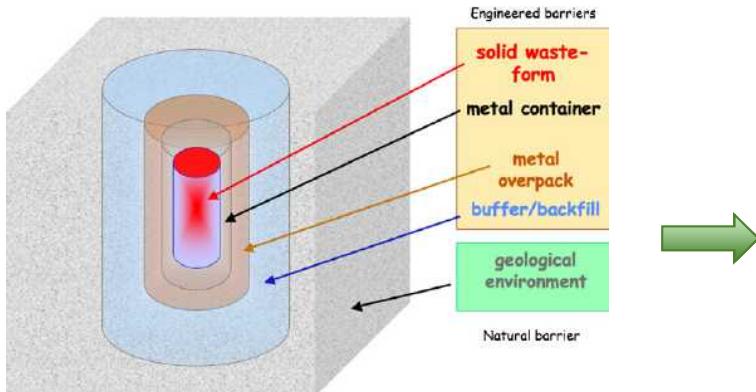
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May 23, 2017

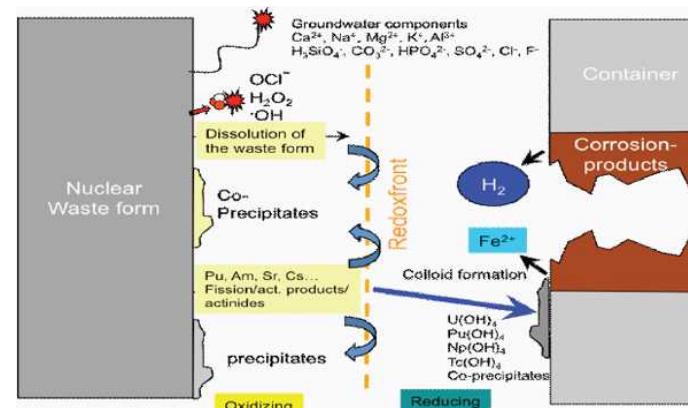
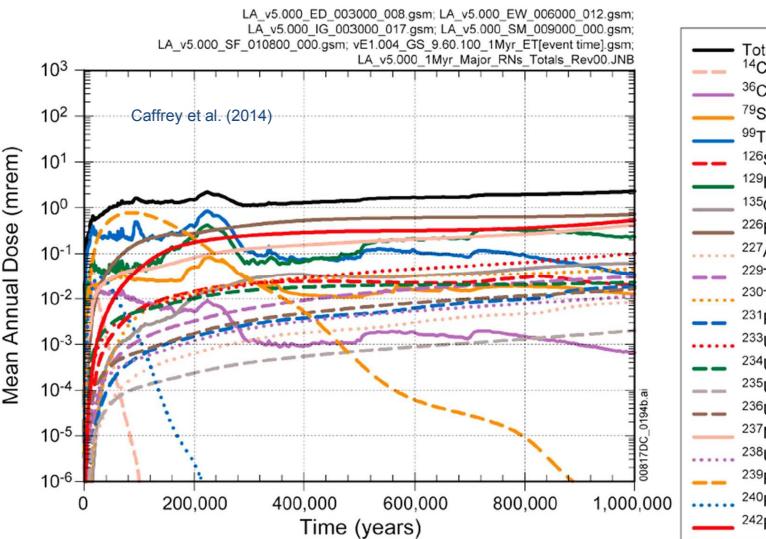
Multiple barrier system



<http://www.bbc.com/news/uk-england-cumbria-21161367>

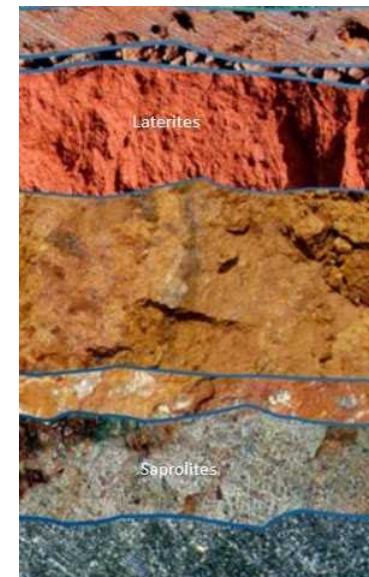
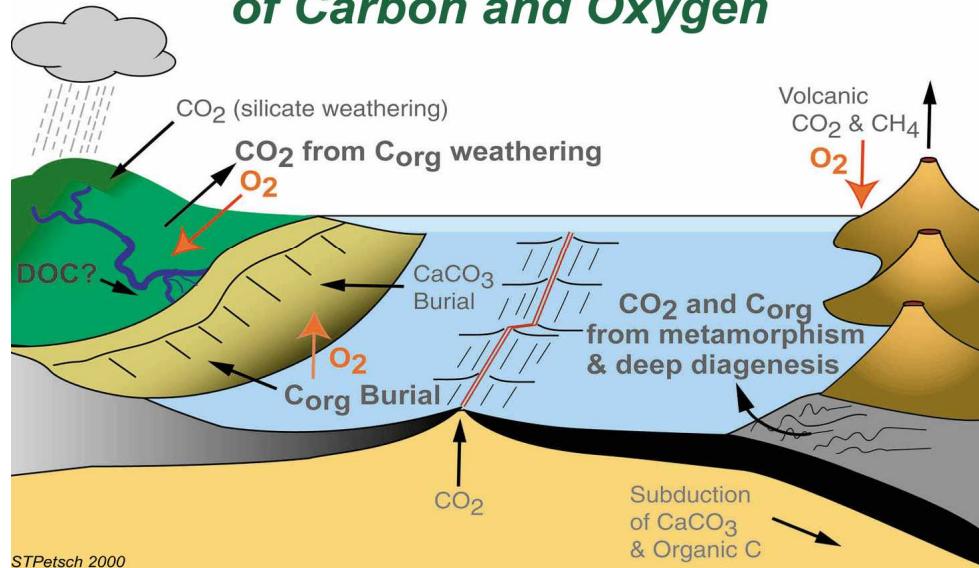


Chapman & Hooper (2012)

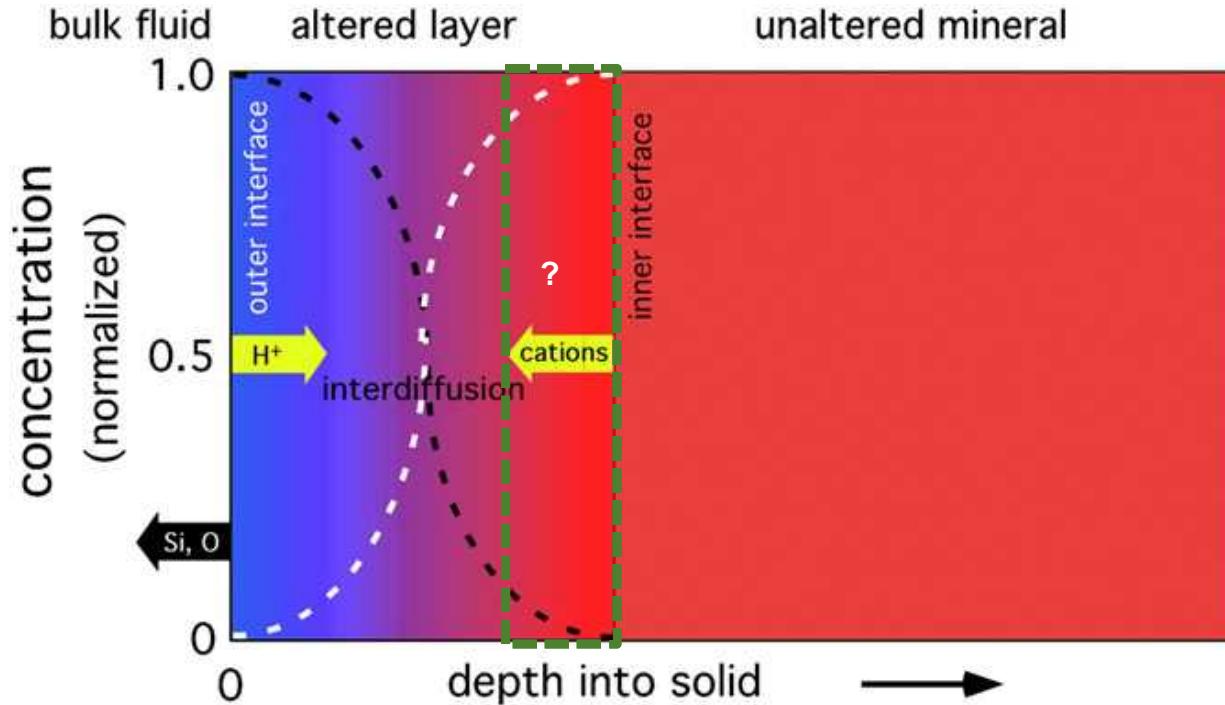


Silicate weathering & biogeochemical cycle

Long-Time-Scale Biogeochemical Cycle of Carbon and Oxygen

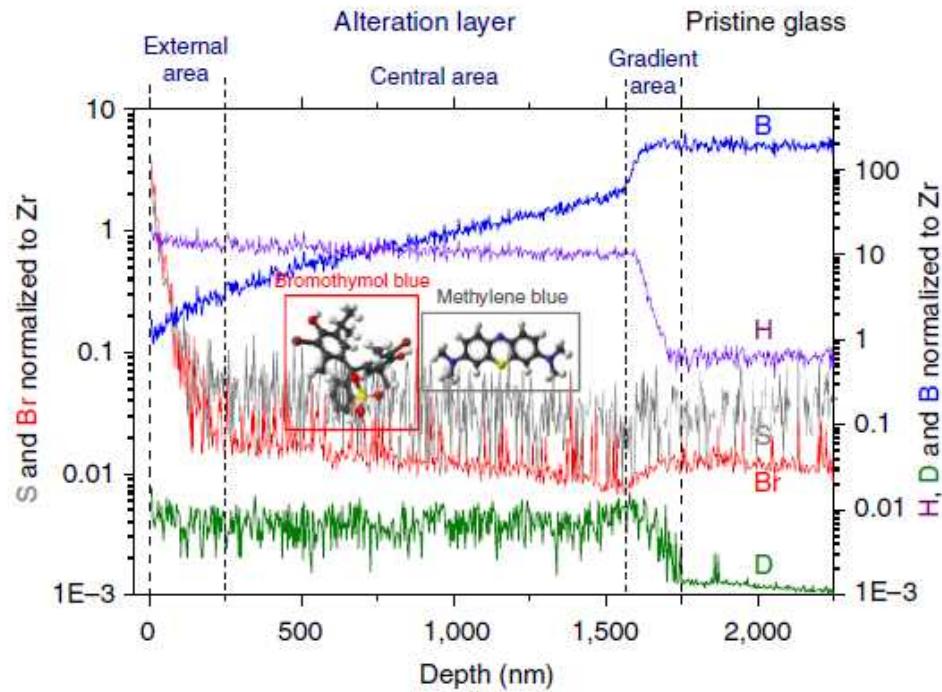


Silicate glass dissolution: knowns & unknowns

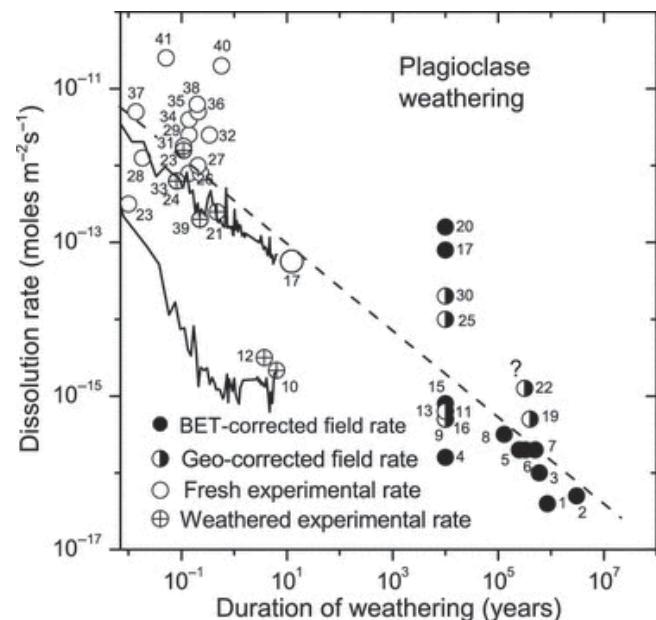


Hellmann et al. (2012)

Borosilicate dissolution: Surface layer formation in silica saturated solution

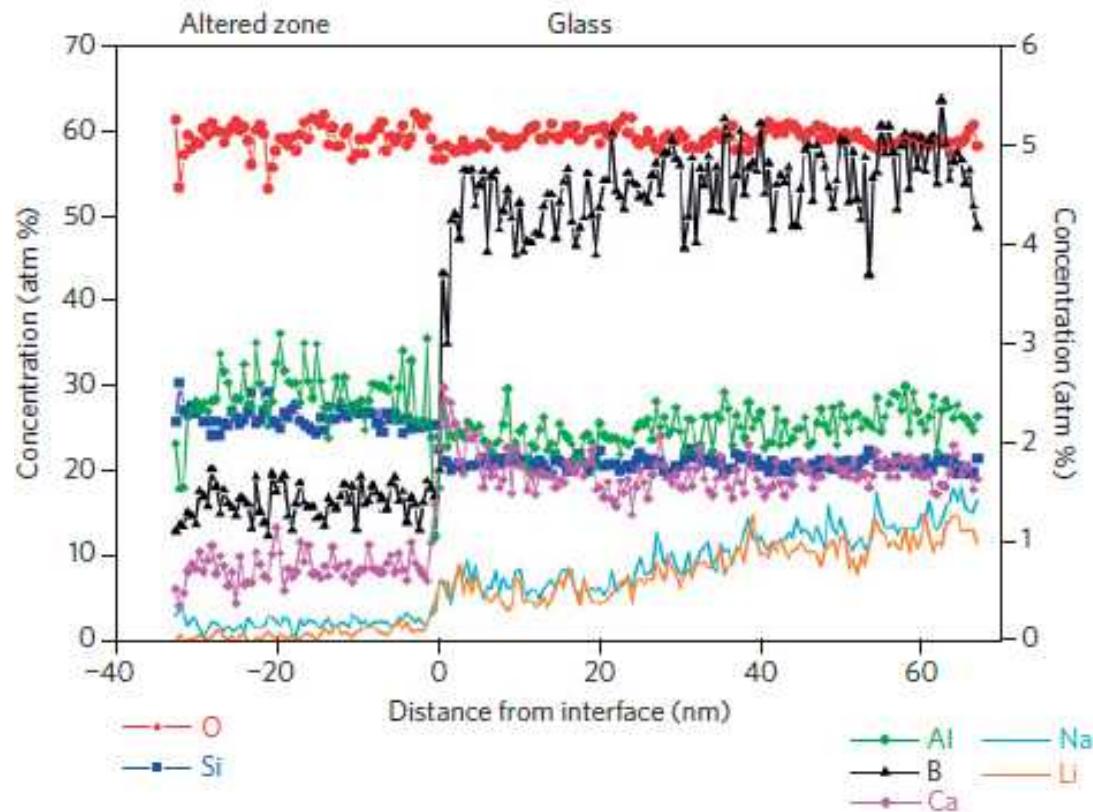


Gin et al. (2015)



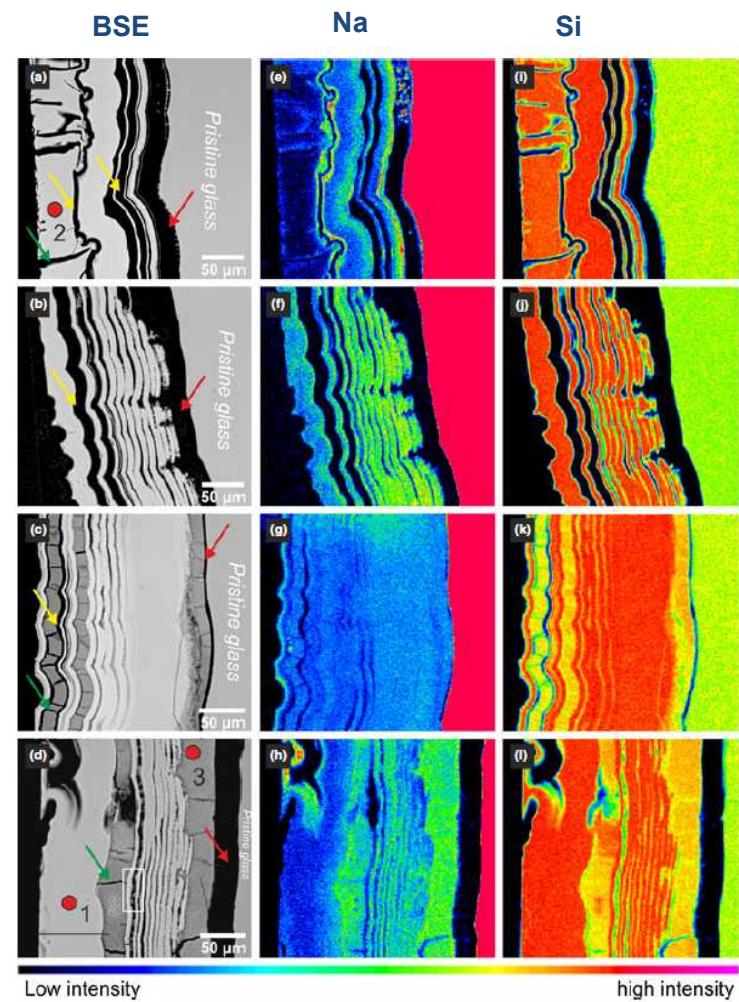
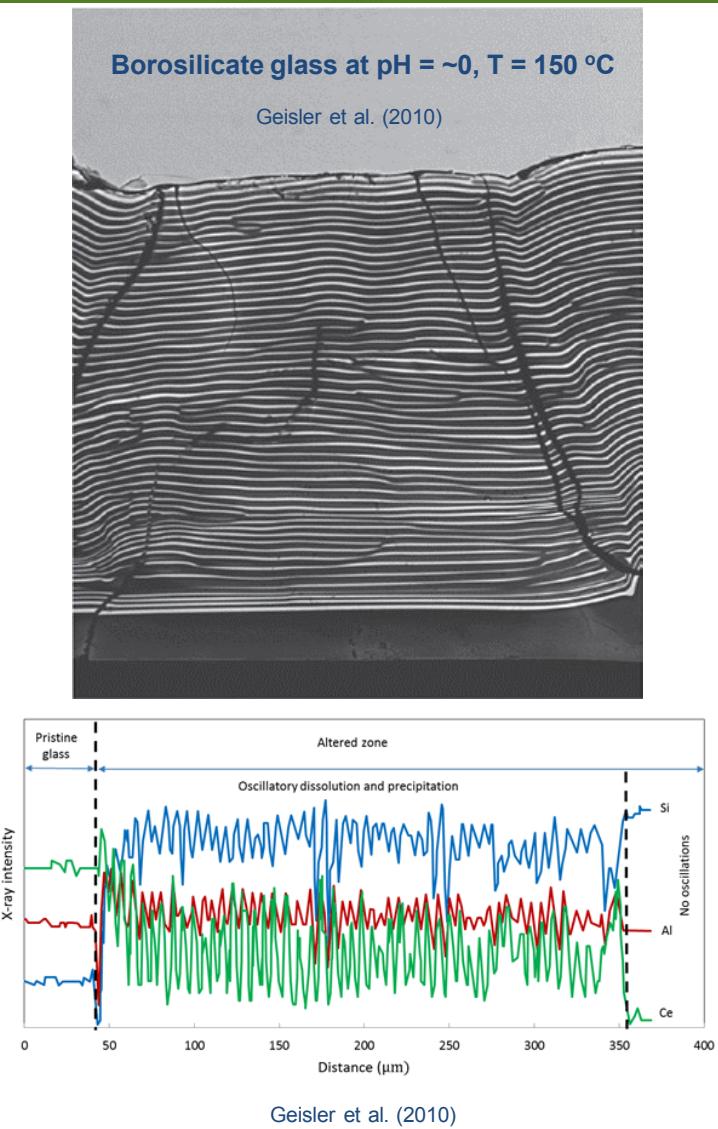
Brantley et al. (2011)

Borosilicate glass dissolution in deionized water at 50 °C



Hellmann et al. (2015)

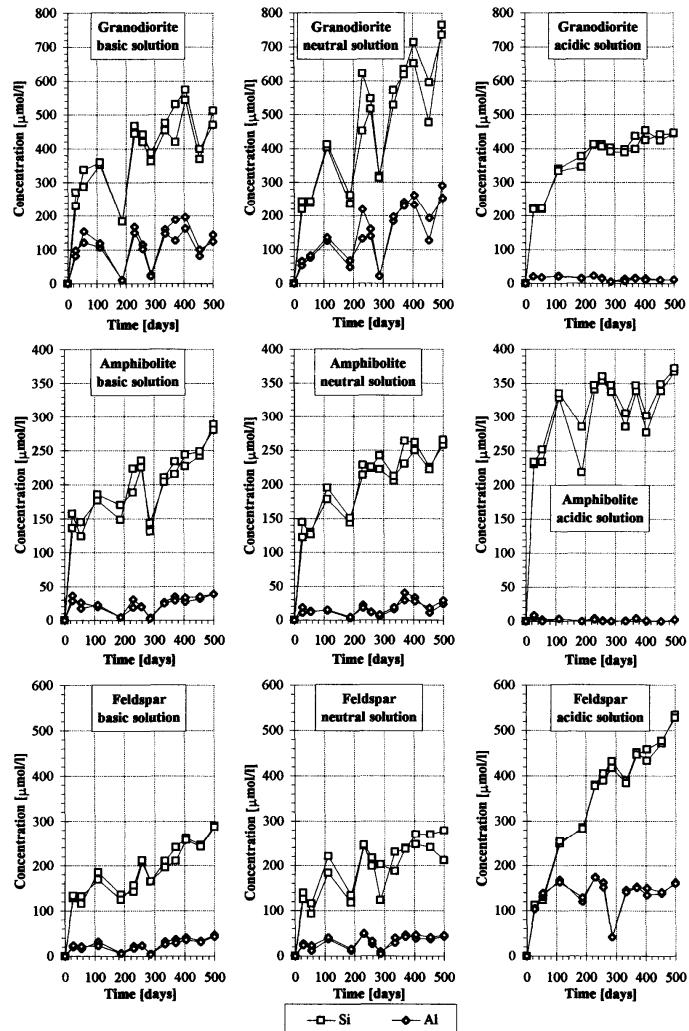
Oscillatory dissolution/precipitation



Borosilicate glass at initial pH = 2-12, T = 90 °C

Dohmen et al. (2013)

Oscillatory silicate mineral dissolution



Faimon. (1996)

Self-organization: Pattern arising from internal dynamics

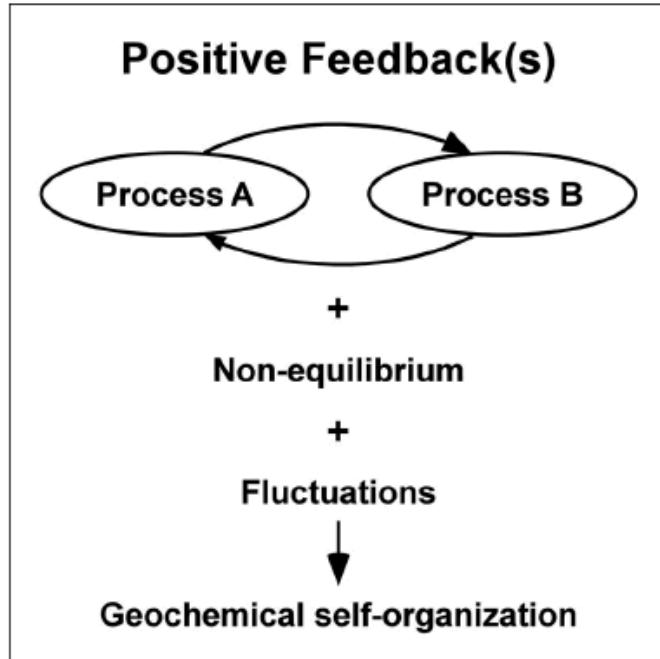
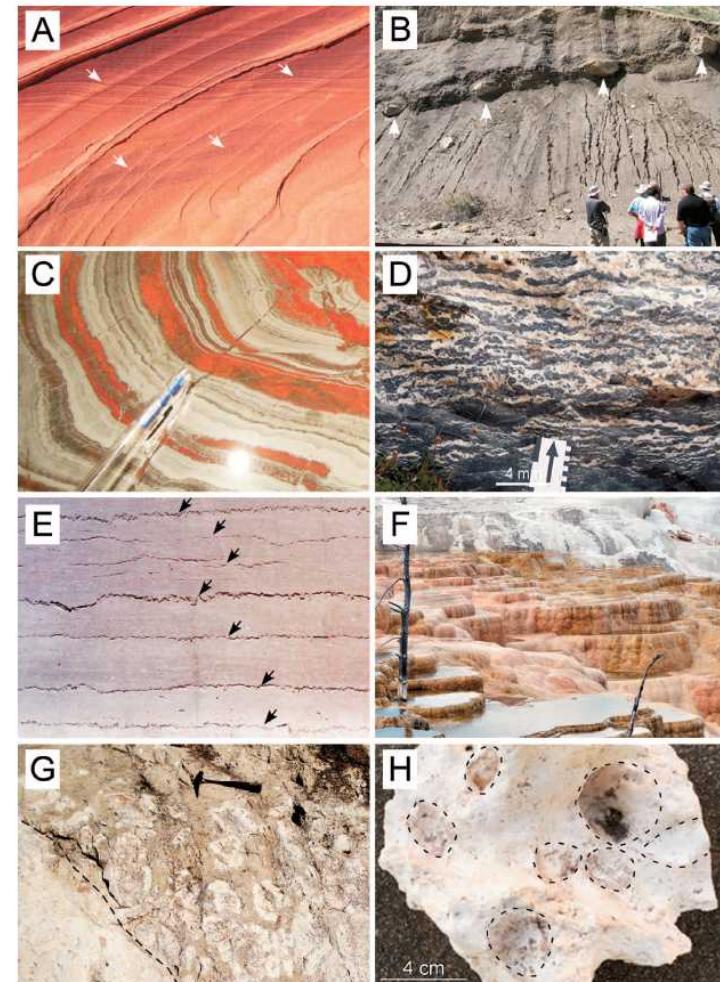
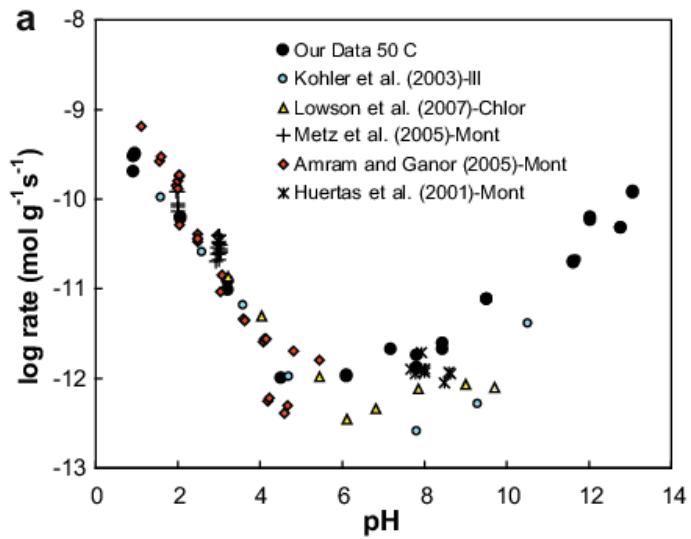


FIG. 1.—Necessary conditions for geochemical self-organization.

Wang & Budd. (2016)

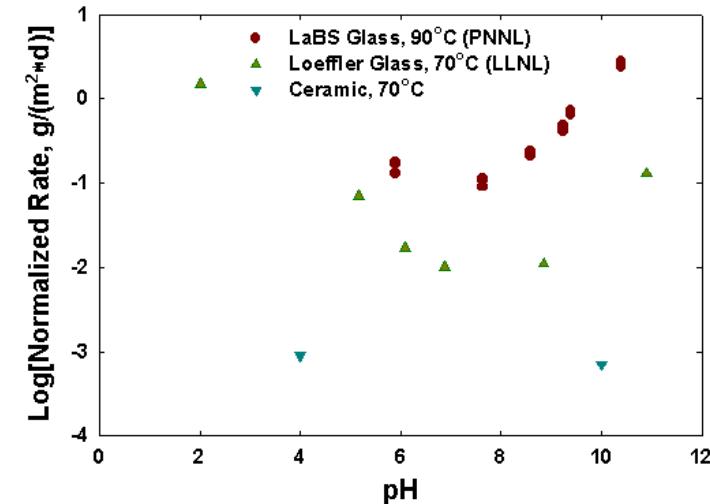
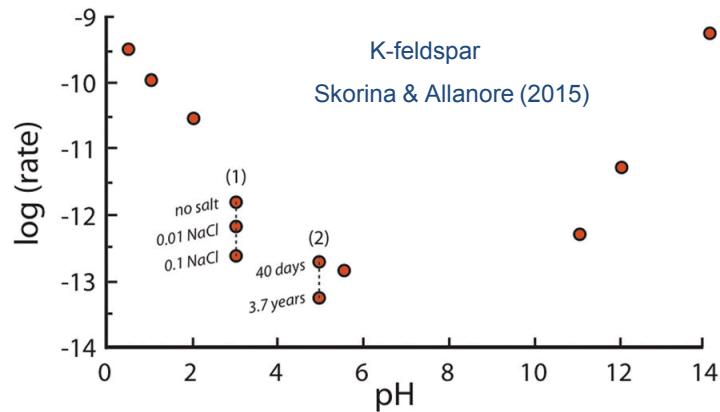


pH-dependent dissolution rate



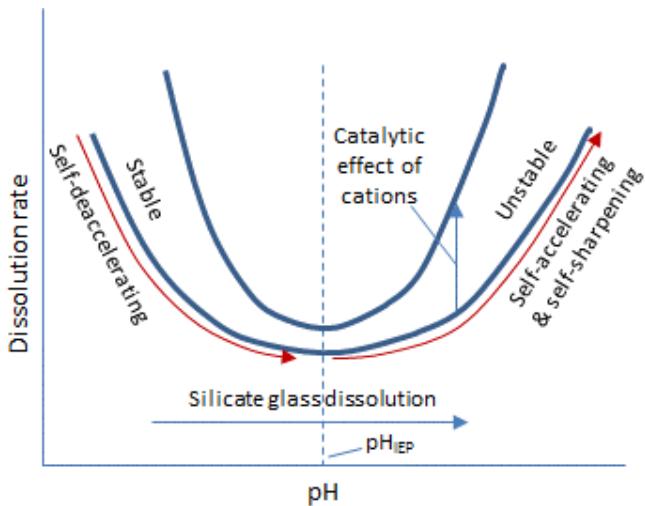
Rozan et al. (2009)

Dissolution catalyzed by H^+ and OH^-

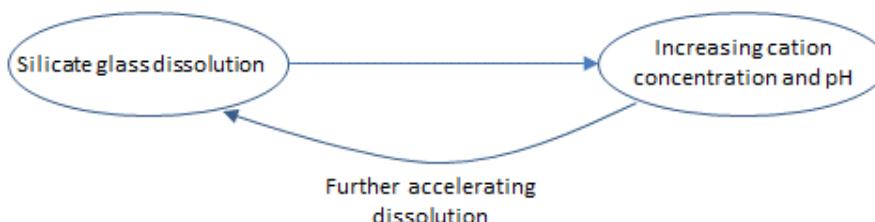


Strachan et al. . (2008)

Positive feedback in silicate dissolution



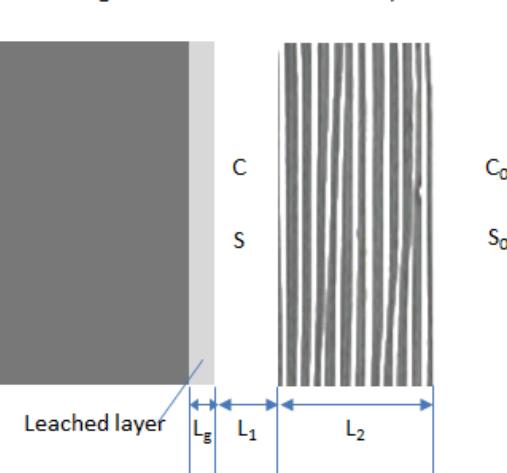
A



B

Wang et al. (2016)

Mathematical model



$$L_1 \frac{dC'}{dt} = \alpha k_d C_{\text{IEP}} \left[1 + \beta \left(\frac{C'}{C_{\text{IEP}}} \right)^n \right] (S_d^e - S') - \frac{D_c}{L_2} (C' - C_0)$$

$$L_1 \frac{dS'}{dt} = \alpha k_d C_{\text{IEP}} \left[1 + \beta \left(\frac{C'}{C_{\text{IEP}}} \right)^n \right] (S_d^e - S') - \frac{D_s}{L_2} (S' - S_0) - k_p (S' - S_p^e)$$

where

C' – Cation concentration within the boundary layer

C_0 – Cation concentration in the bulk solution (outside the altered zone)

D_c – Diffusion coefficient of cations in the altered zone

D_s – Diffusion coefficient of dissolved silica in the altered zone

L_1 – Thickness of the boundary layer at the dissolution interface

L_2 – Thickness of the altered zone

k_d – Reaction rate constant for silicate material dissolution

k_p – Reaction rate constant for silica mineral precipitation

n – Order of silicate dissolution reaction with respect to cation

S' – Silica concentration within the boundary layer

S_0 – Silica concentration in the bulk solution

S_d^e – Equilibrium silica concentration for material dissolution

S_p^e – Equilibrium silica concentration for silica precipitation

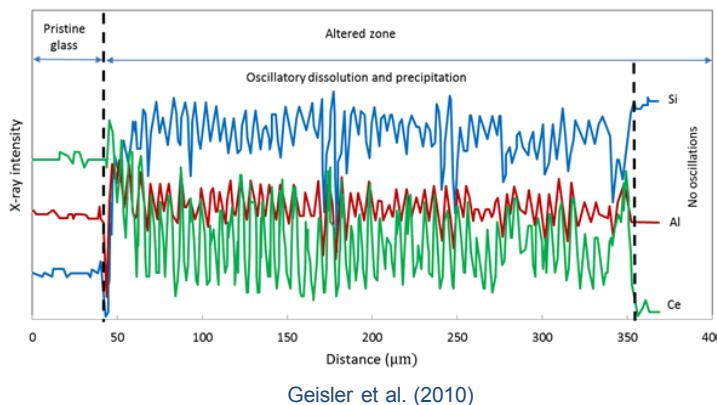
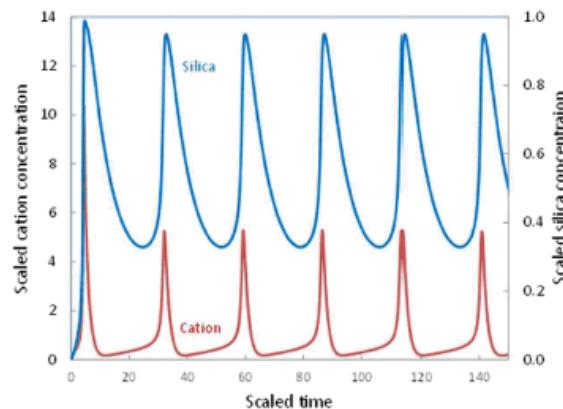
t – Time

α – Molar ratio of cations (mainly Na^+) to Si^{4+} in the pristine silicate material

β – Positive constant characterizing the catalytic effect of cations on silicate material dissolution

Wang et al., 2016, Scientific Reports

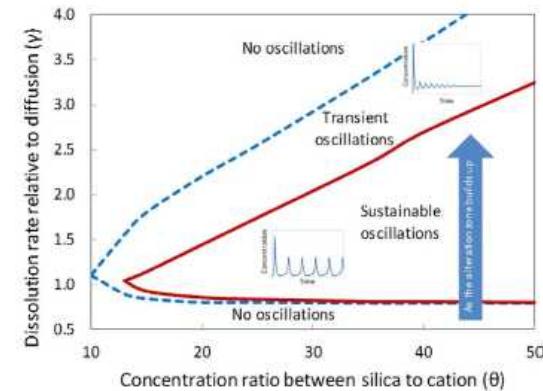
Nonlinear dynamics of silicate dissolution



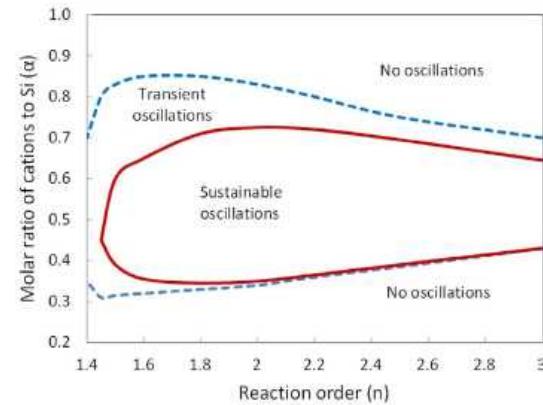
Predicted time scale: hours to years

Predicted spatial scale: sub-micron to tens of microns

Archeologic study of ancient Roman glass shows that each band might have formed over a year.



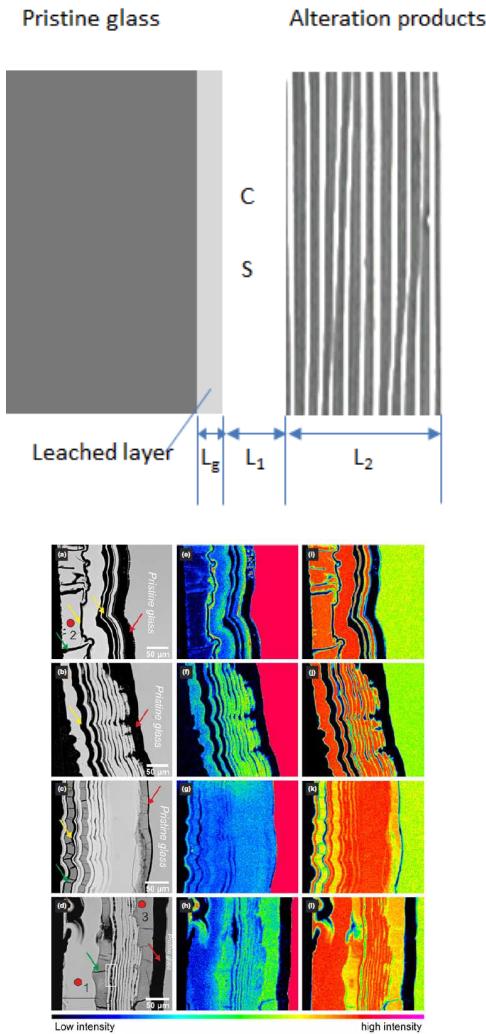
A



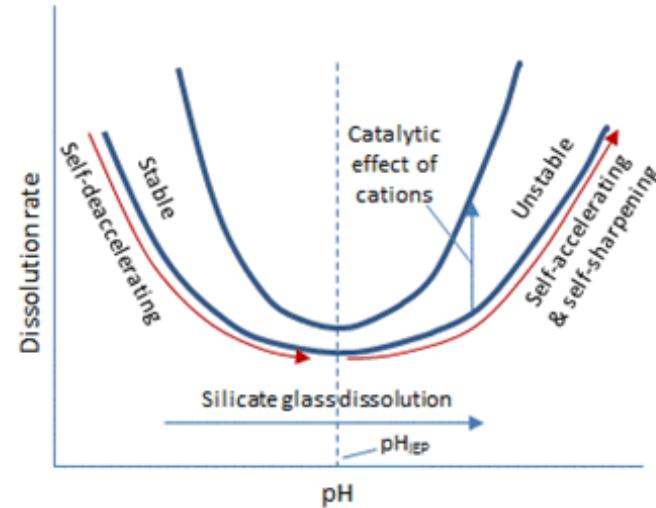
B

Wang et al., 2016, Scientific Reports

Self-sharpening & morphologic instability of a reaction front



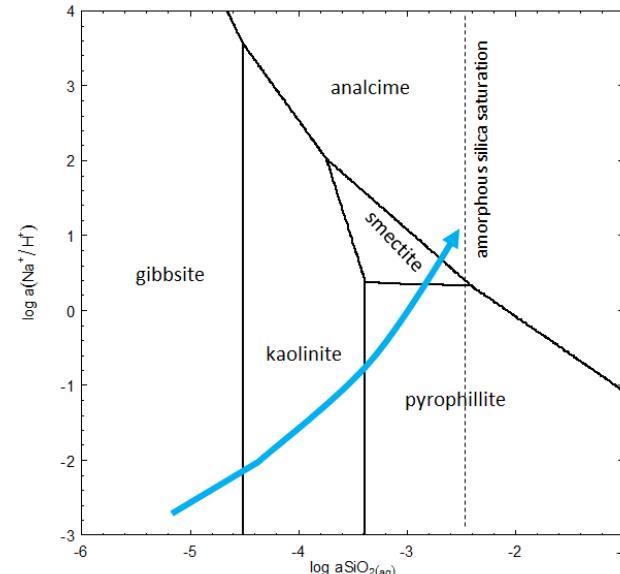
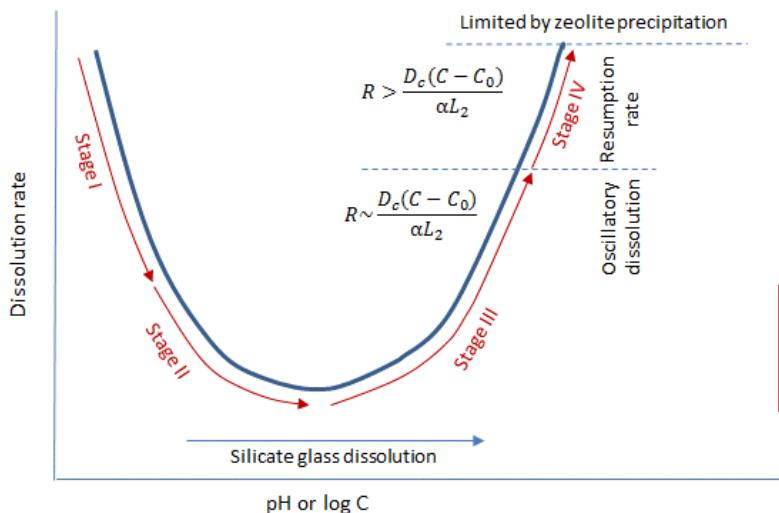
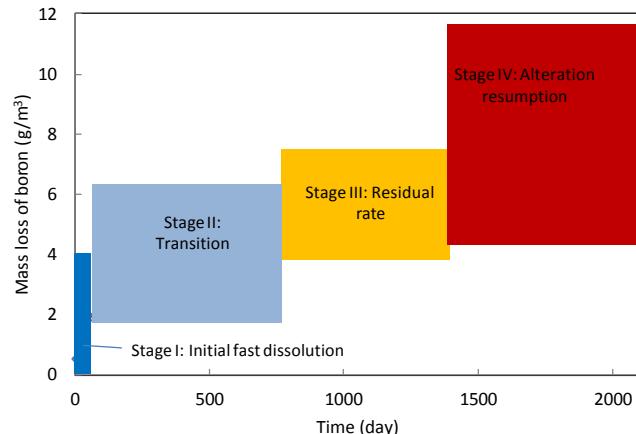
Dohmen et al. (2013)



$$\frac{dL_g}{dt} \approx \frac{D_g}{L_g} - Rv_m = \frac{D_g}{L_g} - v_m k_d C_{IEP} (S_d^e - S) \left[1 + \beta \left(\frac{D_g L_2}{C_{IEP} L_g} \right)^n \right]$$

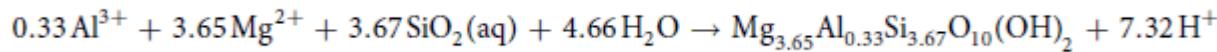
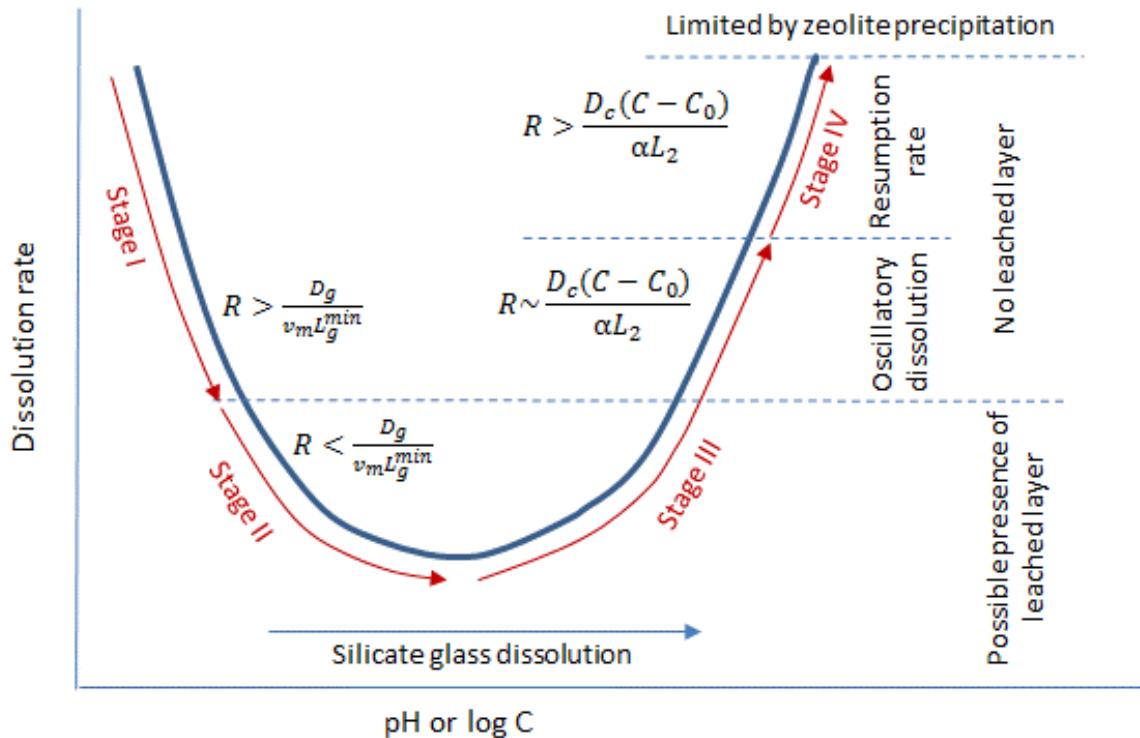
Morphologic instability arises from the same positive feedback.

Alteration resumption and zeolite formation

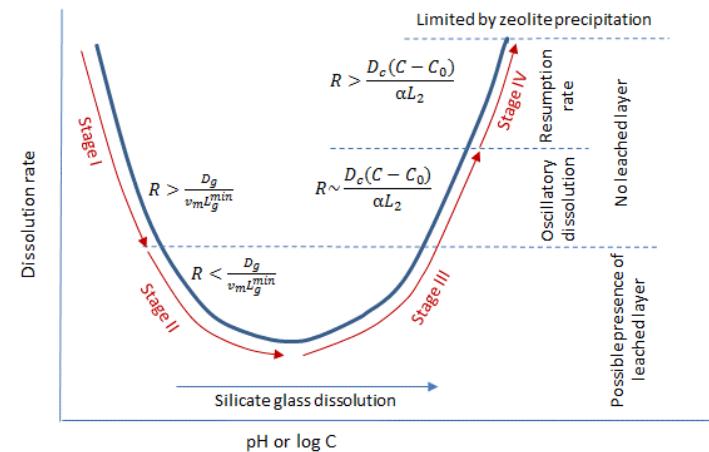
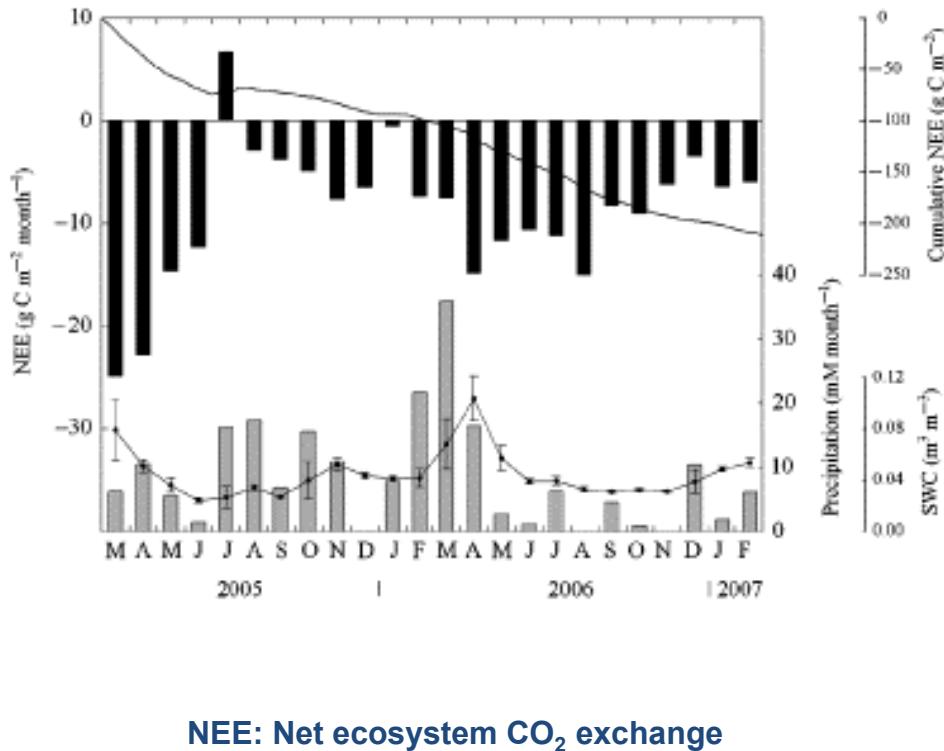


Eventually, the dissolution rate overtakes the mass exchange rate, leading to a “runaway” situation with a sharp increase in the cation concentration at the interface and therefore the dissolution rate.

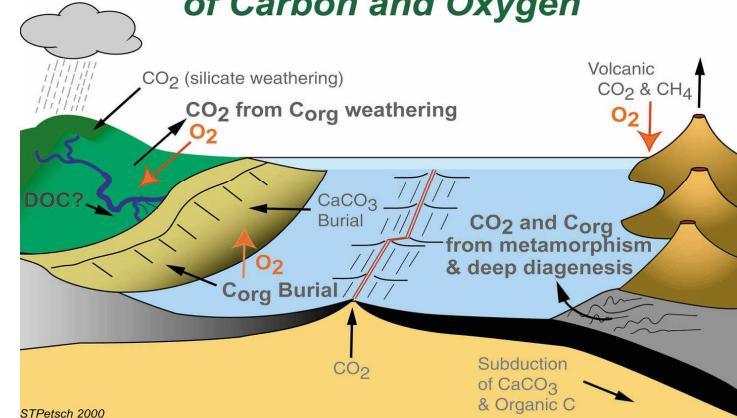
Waste durability: Chemical composition and water chemistry



Implication to weathering



Long-Time-Scale Biogeochemical Cycle of Carbon and Oxygen



Concluding remarks

- Complex silicate material dissolution behaviors can emerge from a simple positive feedback between dissolution-induced cation release and cation-enhanced dissolution kinetics.
- This mechanism enables a systematic prediction of the occurrence of sharp dissolution fronts, oscillatory dissolution behaviors and multiple stages of glass dissolution.
- It provides a new perspective for predicting long-term silicate weathering rates in actual geochemical systems and developing durable silicate materials for various engineering applications.

Acknowledgements



- DOE-Spent Fuel Waste Science & Technology (SFWST)
- DOE-Energy Frontier Research Center (EFRC)