

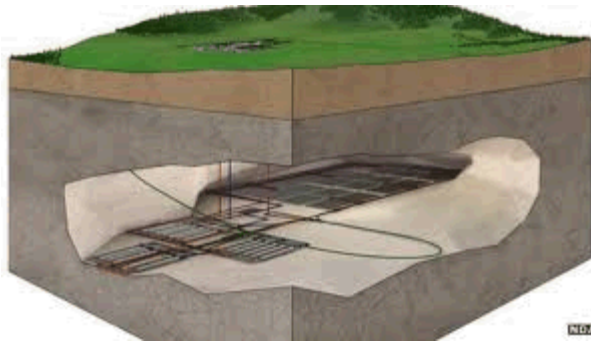
Nonlinear dynamics of aqueous dissolution of silicate glasses and its implications to glass waste form durability

Yifeng Wang, Carlos F. Jove-Colon and Kristopher L. Kuhlman

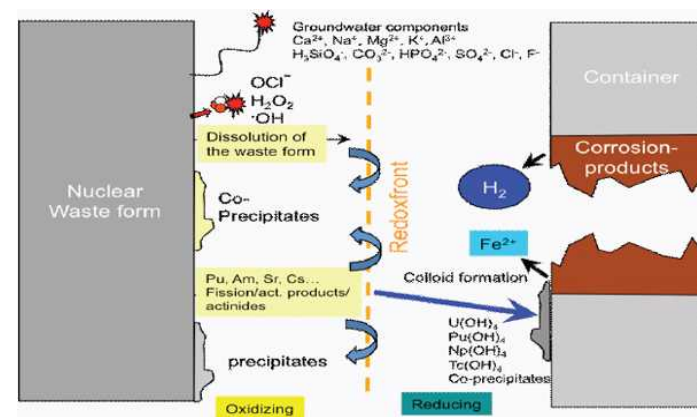
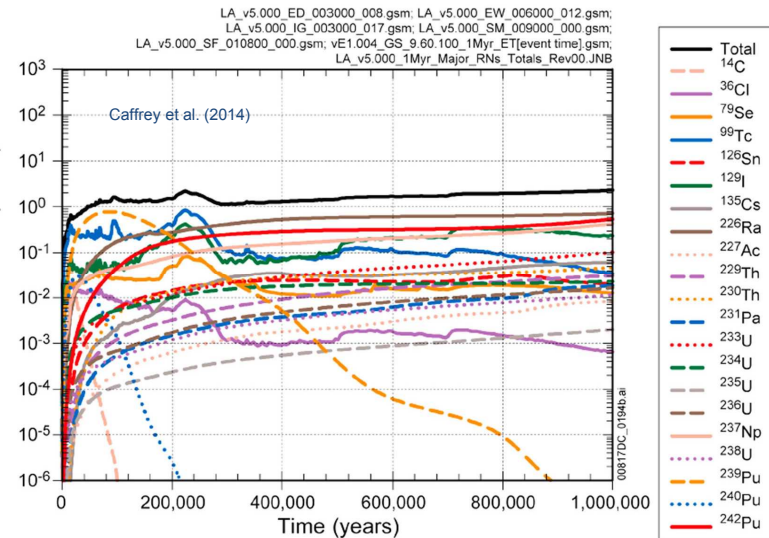
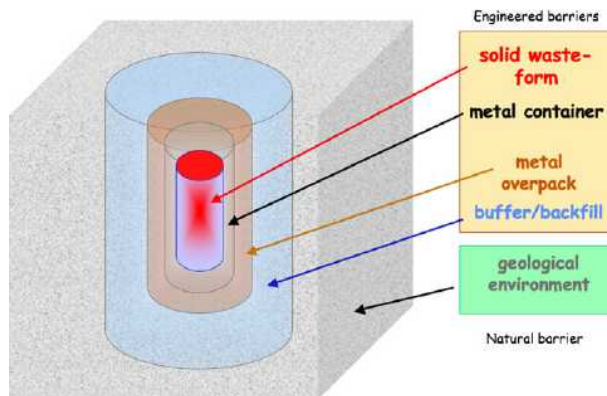
Sandia National Laboratories, P. O. Box 5800, Albuquerque, New Mexico 87185-0779, USA

May 23, 2017

Multiple barrier system



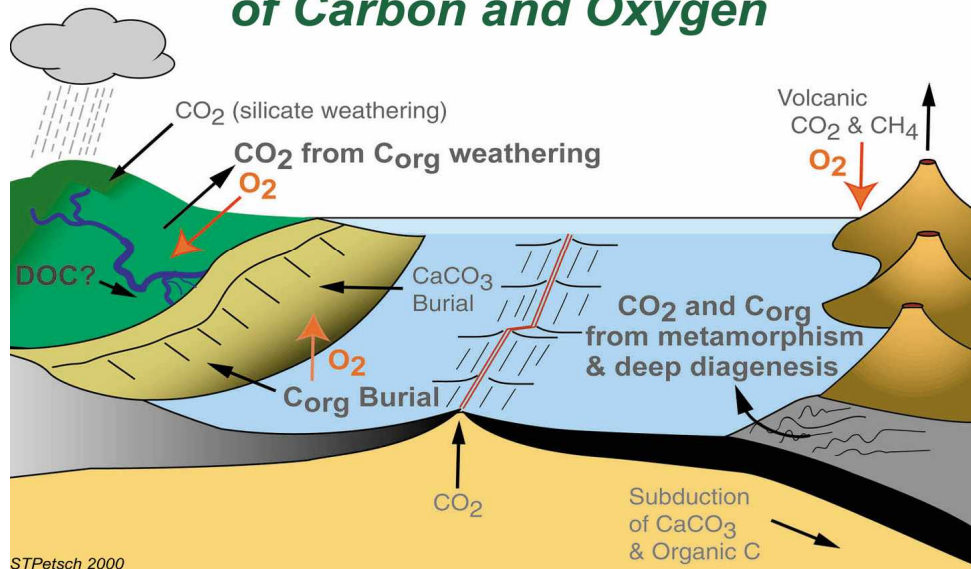
<http://www.bbc.com/news/uk-england-cumbria-21161367>



Chapman & Hooper (2012)

Silicate weathering & biogeochemical cycle

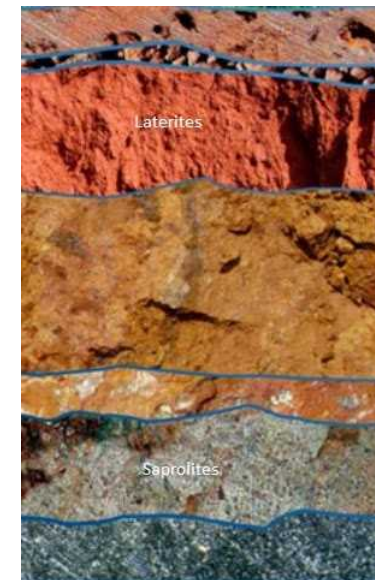
Long-Time-Scale Biogeochemical Cycle of Carbon and Oxygen



<http://www.indiana.edu/~geol105b/1425chap8.htm>

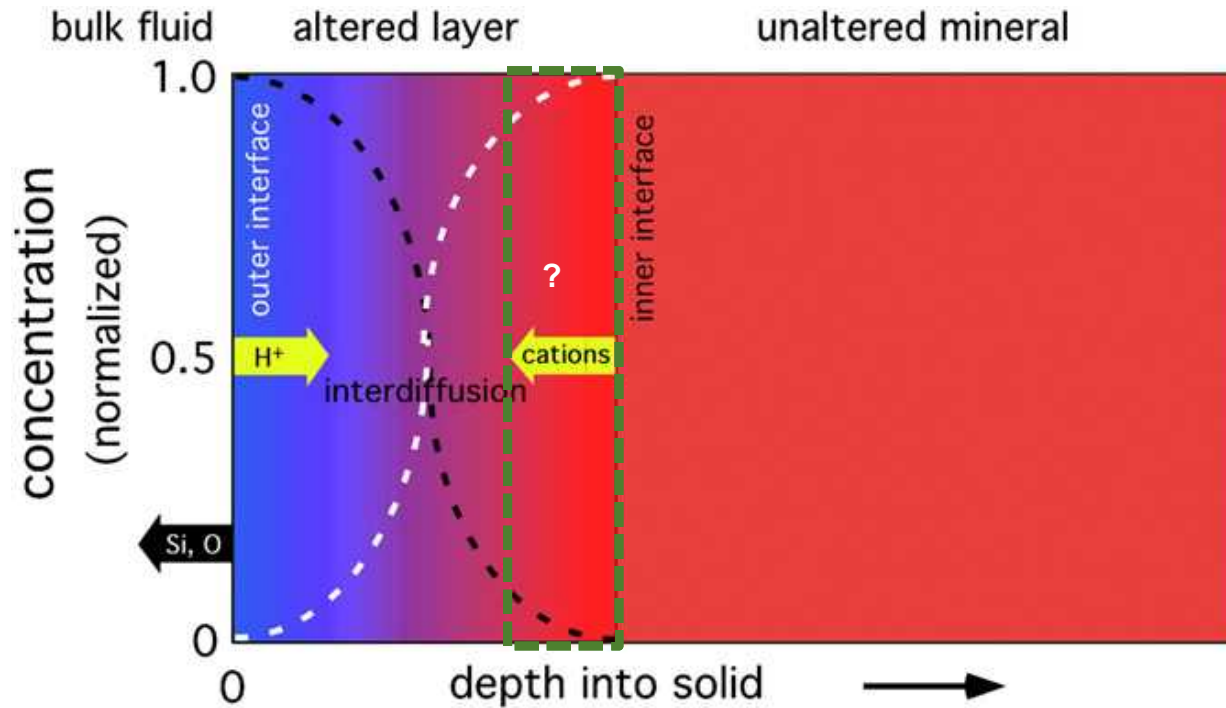


<https://www.pinterest.com/pin/291397038360020104/>



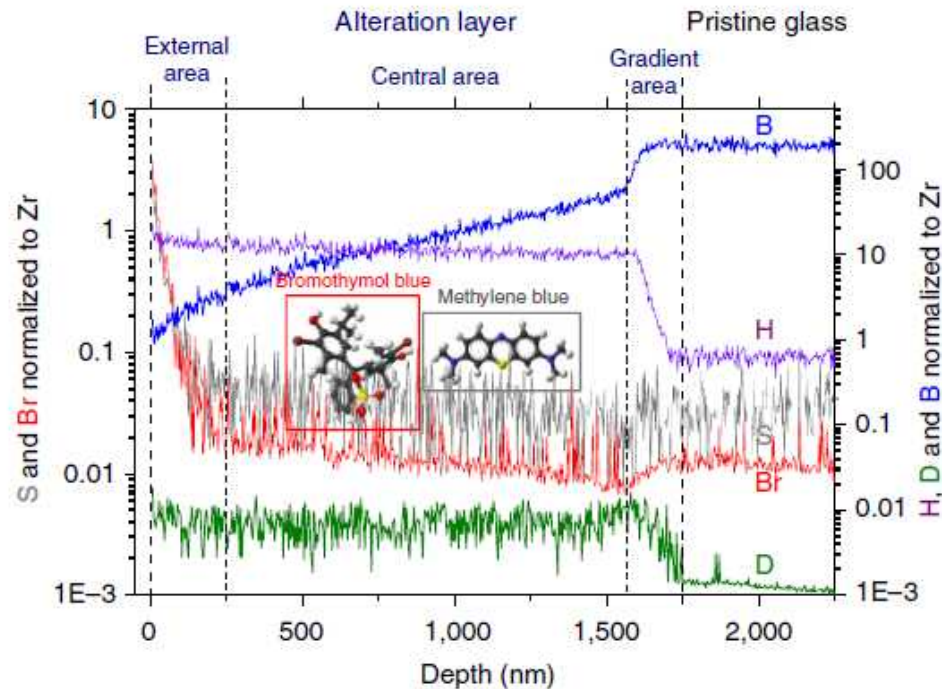
<https://civil-engg-world.blogspot.com/2014/04/Residual-Soil-Laterites-Saprolites.html>

Silicate glass dissolution: knowns & unknowns

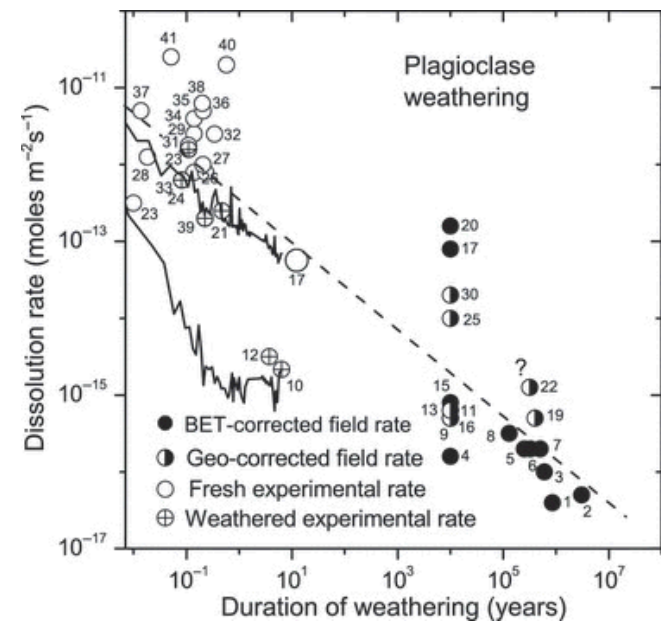


Hellmann et al. (2012)

Borosilicate dissolution: Surface layer formation in silica saturated solution

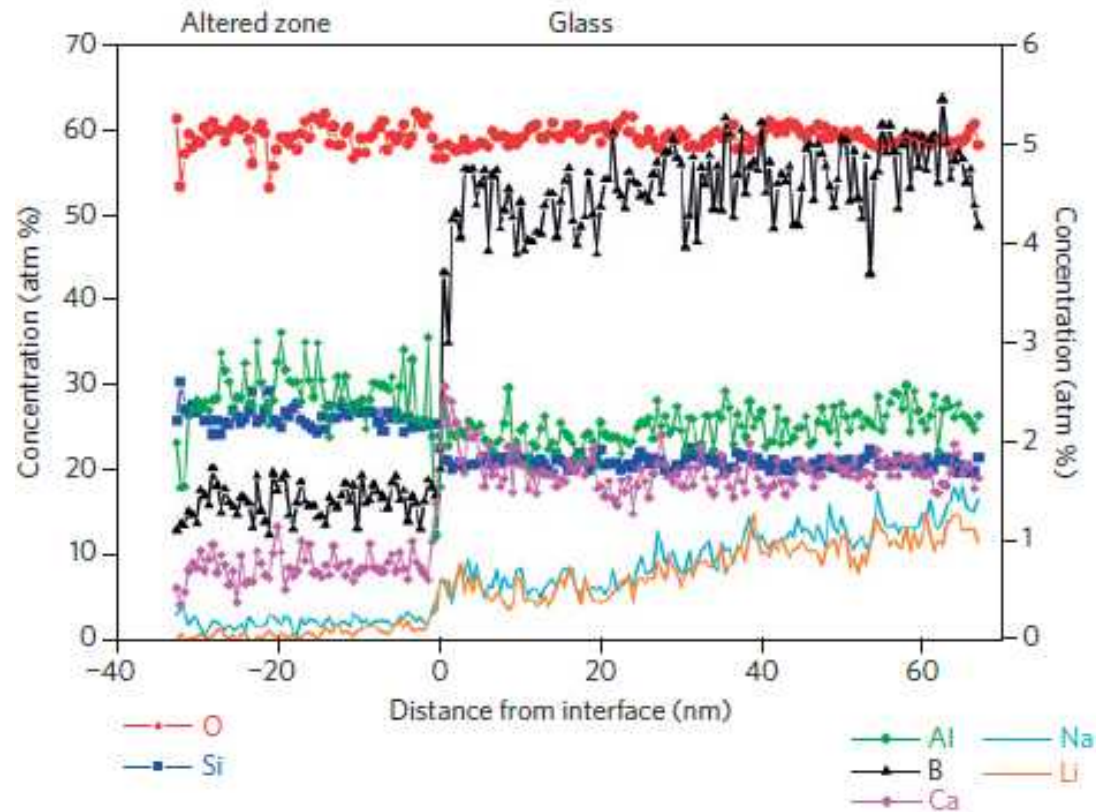


Gin et al. (2015)



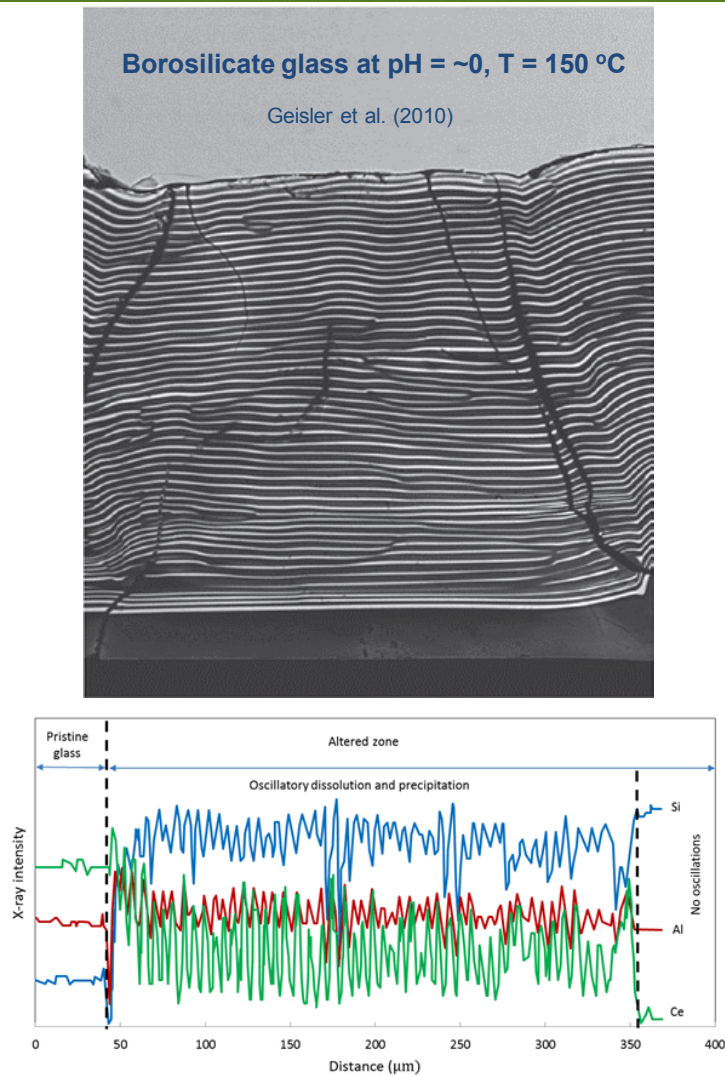
Brantley et al. (2011)

Borosilicate glass dissolution in deionized water at 50 °C

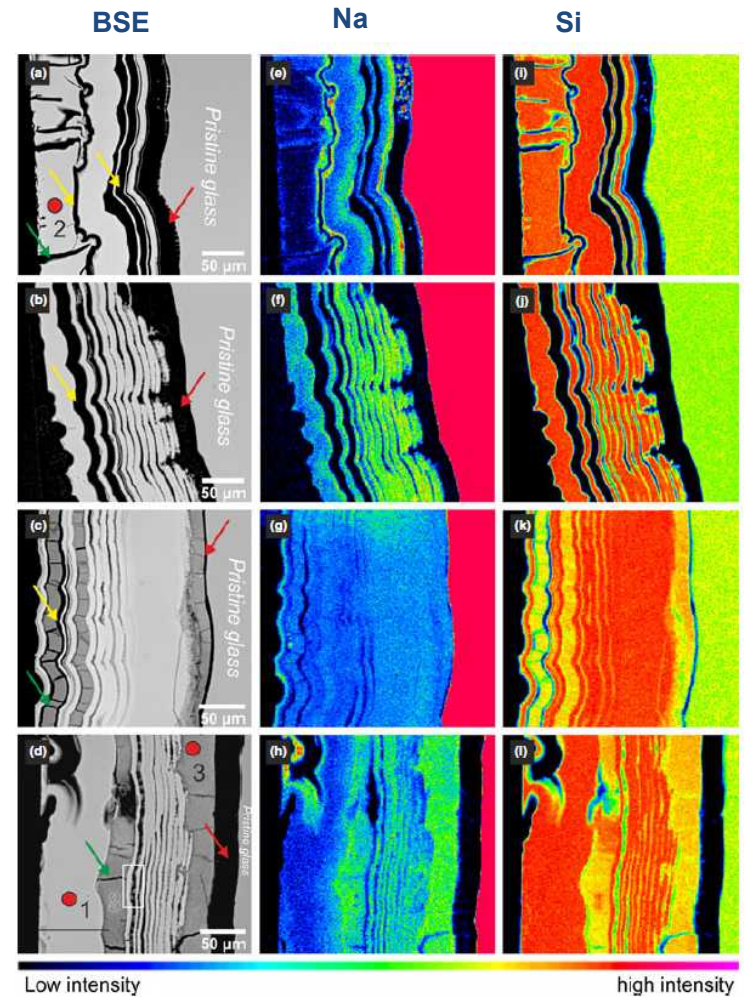


Hellmann et al. (2015)

Oscillatory dissolution/precipitation



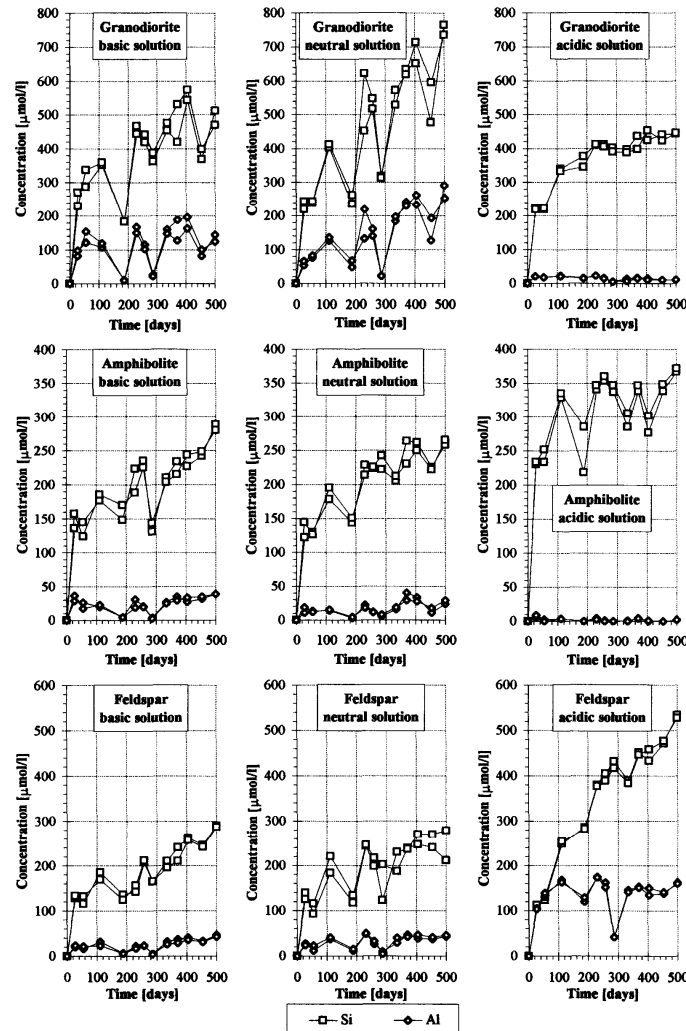
Geisler et al. (2010)



Borosilicate glass at initial pH = 2-12, T = 90 °C

Dohmen et al. (2013)

Oscillatory silicate mineral dissolution



Faimon. (1996)

Self-organization: Pattern arising from internal dynamics

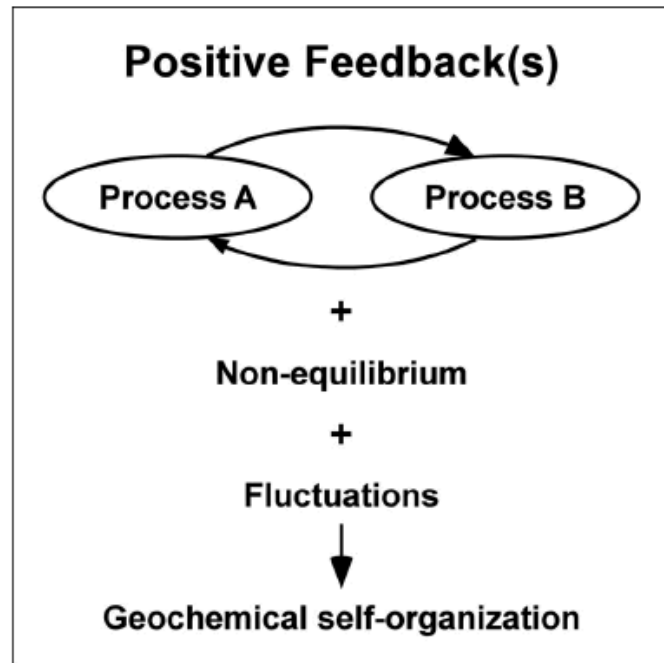
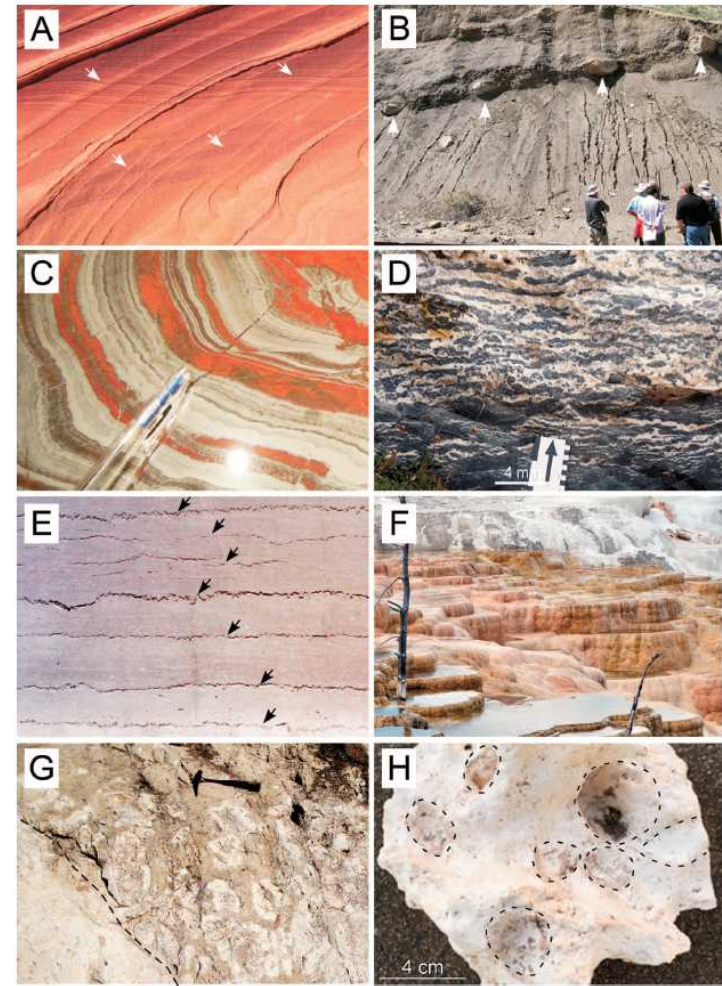
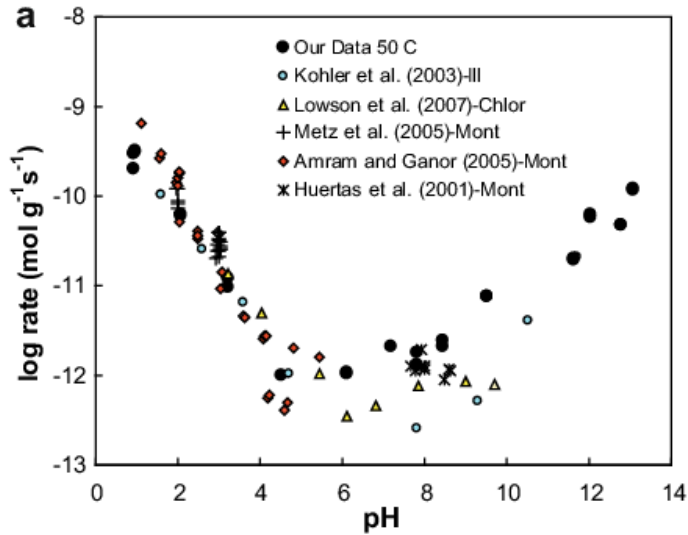


FIG. 1.—Necessary conditions for geochemical self-organization.

Wang & Budd. (2016)

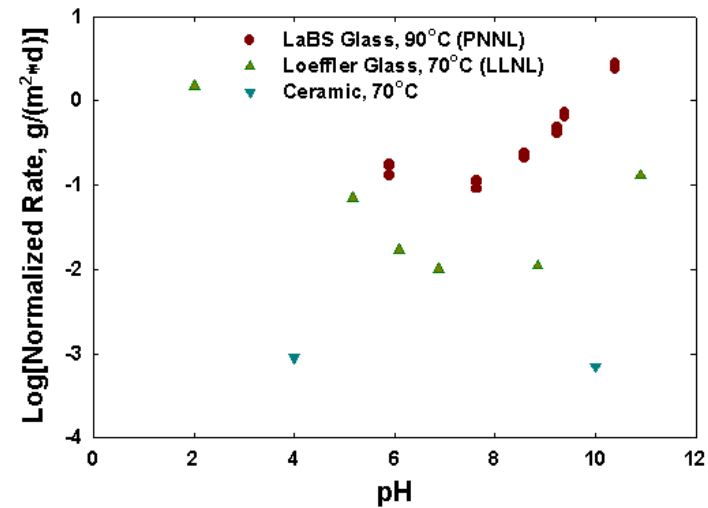
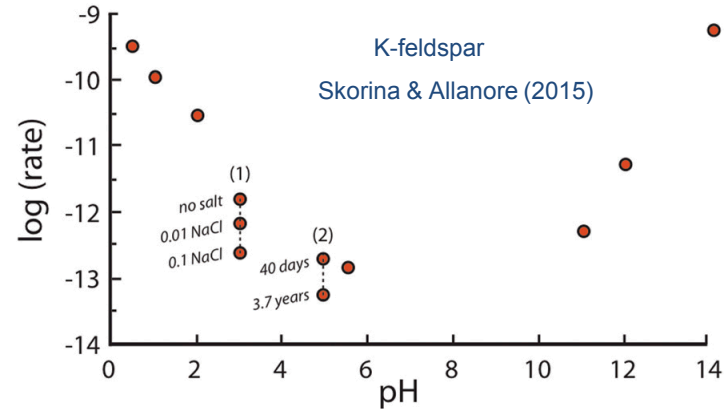


pH-dependent dissolution rate



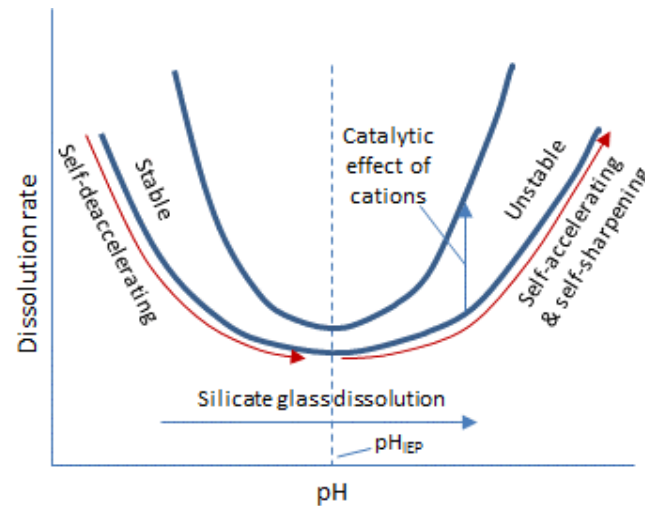
Rozan et al. (2009)

Dissolution catalyzed by H^+ and OH^-

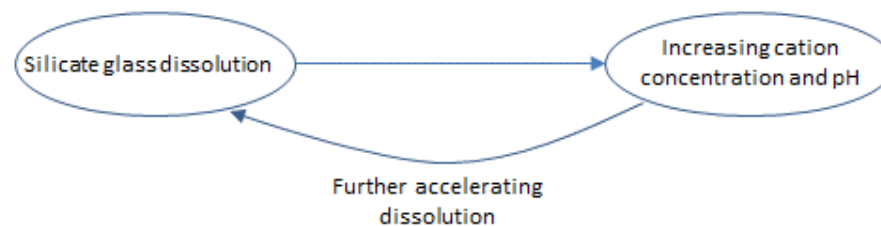


Strachan et al. . (2008)

Positive feedback in silicate dissolution



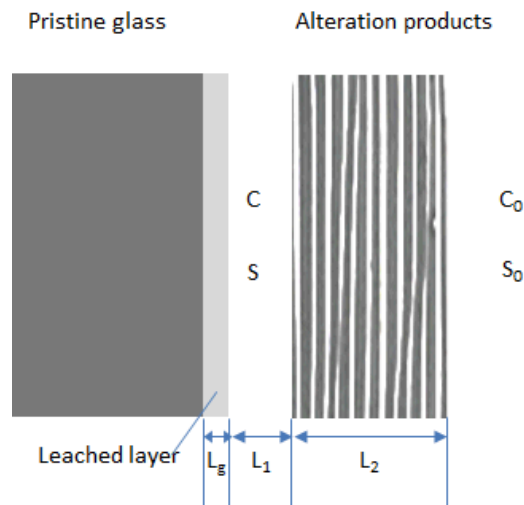
A



B

Wang et al. (2016)

Mathematical model



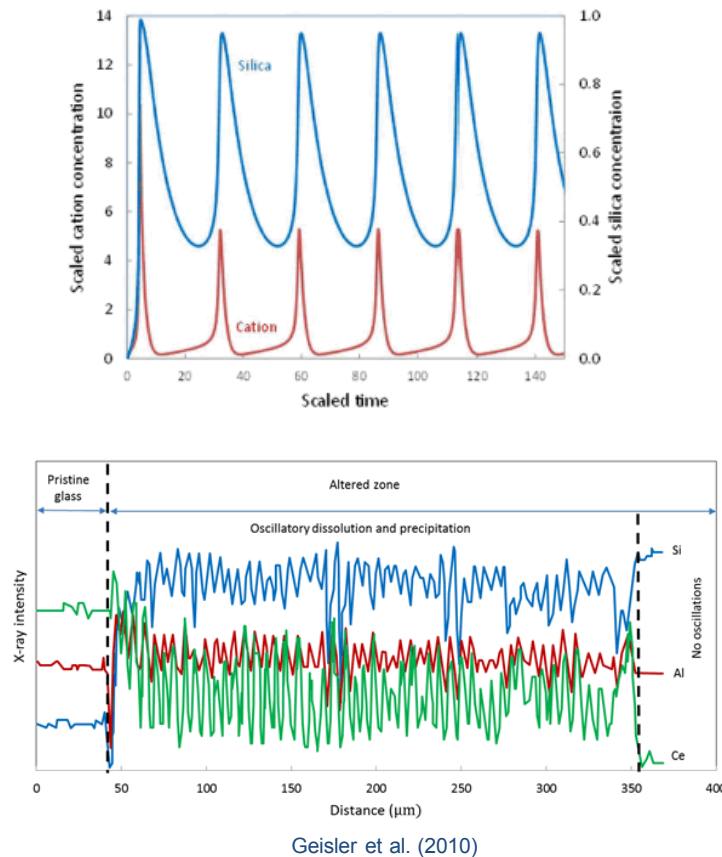
$$L_1 \frac{dC'}{dt} = \alpha k_d C_{IEP} \left[1 + \beta \left(\frac{C'}{C_{IEP}} \right)^n \right] (S_d^e - S') - \frac{D_c}{L_2} (C' - C_0)$$

$$L_1 \frac{dS'}{dt} = \alpha k_d C_{IEP} \left[1 + \beta \left(\frac{C'}{C_{IEP}} \right)^n \right] (S_d^e - S') - \frac{D_s}{L_2} (S' - S_0) - k_p (S' - S_p^e)$$

where

- C' – Cation concentration within the boundary layer
- C_0 – Cation concentration in the bulk solution (outside the altered zone)
- D_c – Diffusion coefficient of cations in the altered zone
- D_s – Diffusion coefficient of dissolved silica in the altered zone
- L_1 – Thickness of the boundary layer at the dissolution interface
- L_2 – Thickness of the altered zone
- k_d – Reaction rate constant for silicate material dissolution
- k_p – Reaction rate constant for silica mineral precipitation
- n – Order of silicate dissolution reaction with respect to cation
- S' – Silica concentration within the boundary layer
- S_0 – Silica concentration in the bulk solution
- S_d^e – Equilibrium silica concentration for material dissolution
- S_p^e – Equilibrium silica concentration for silica precipitation
- t – Time
- α – Molar ratio of cations (mainly Na^+) to Si^{4+} in the pristine silicate material
- β – Positive constant characterizing the catalytic effect of cations on silicate material dissolution

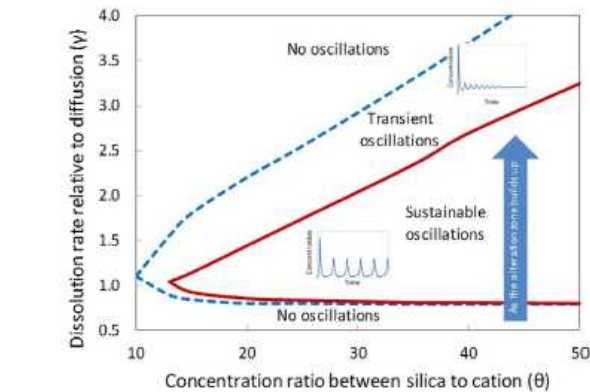
Nonlinear dynamics of silicate dissolution



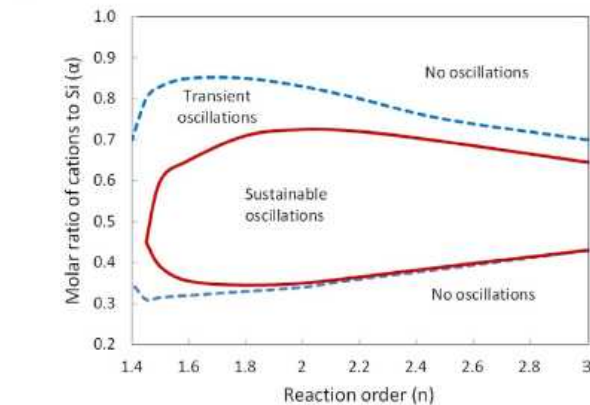
Predicted time scale: hours to years

Predicted spatial scale: sub-micron to tens of microns

Archeologic study of ancient Roman glass shows that each band might have formed over a year.



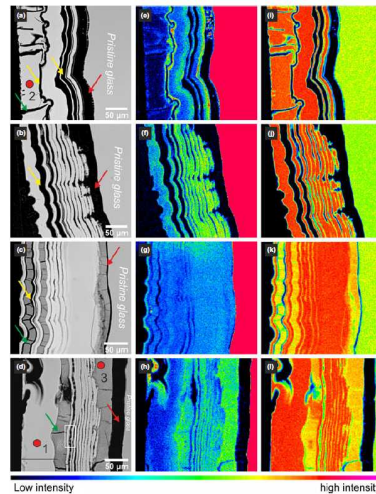
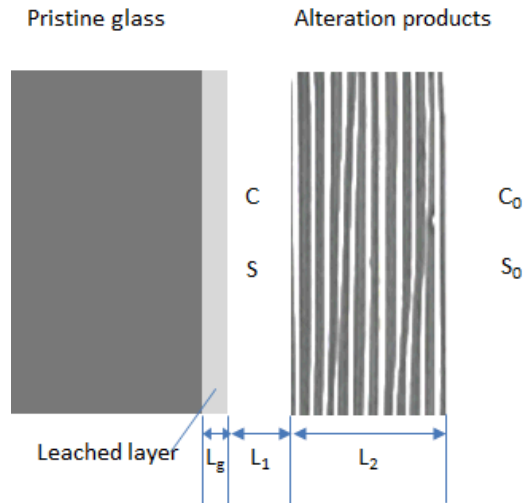
A



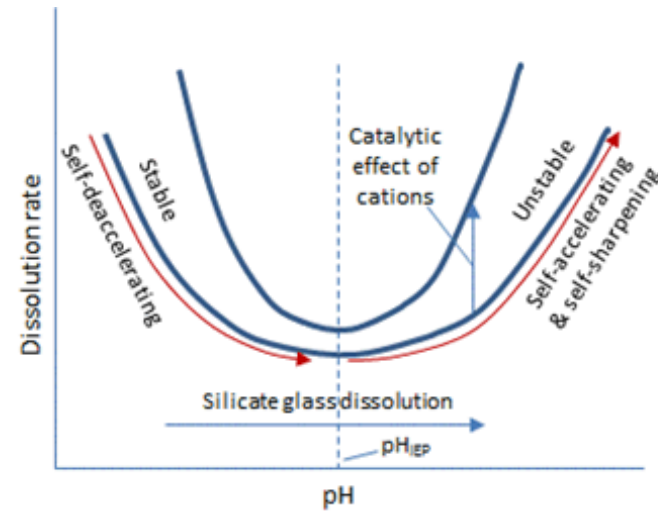
B

Wang et al., 2016, Scientific Reports

Self-sharpening & morphologic instability of a reaction front



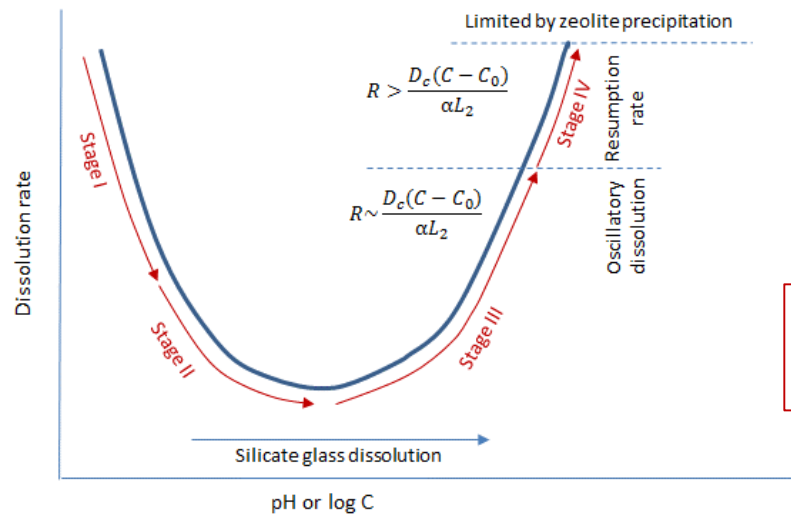
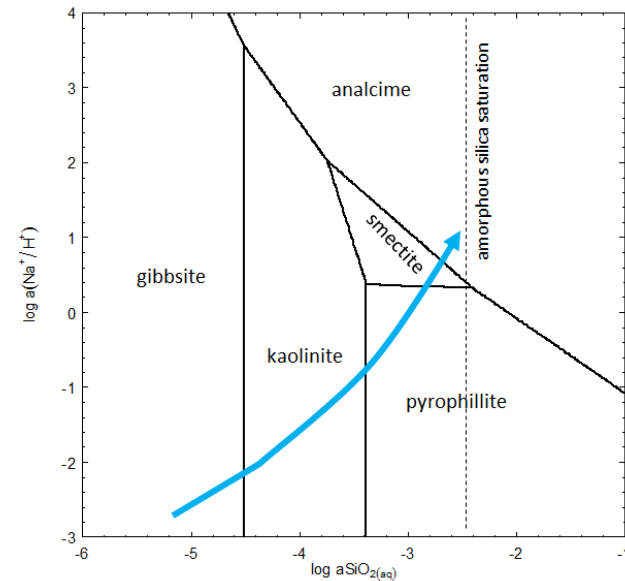
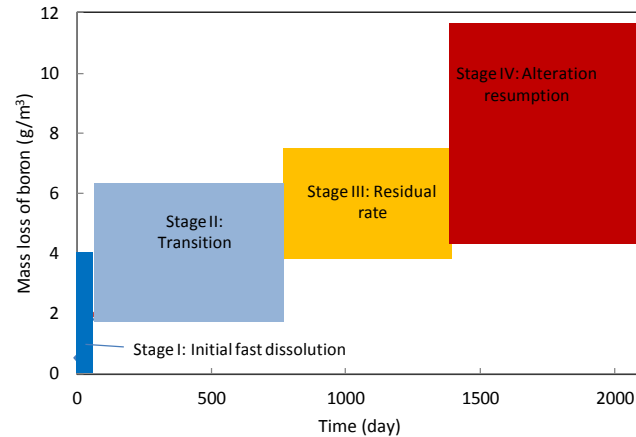
Dohmen et al. (2013)



$$\frac{dL_g}{dt} \approx \frac{D_g}{L_g} - Rv_m = \frac{D_g}{L_g} - v_m k_d C_{IEP} (S_d^e - S) \left[1 + \beta \left(\frac{D_g L_2}{C_{IEP} L_g} \right)^n \right]$$

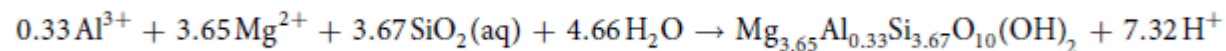
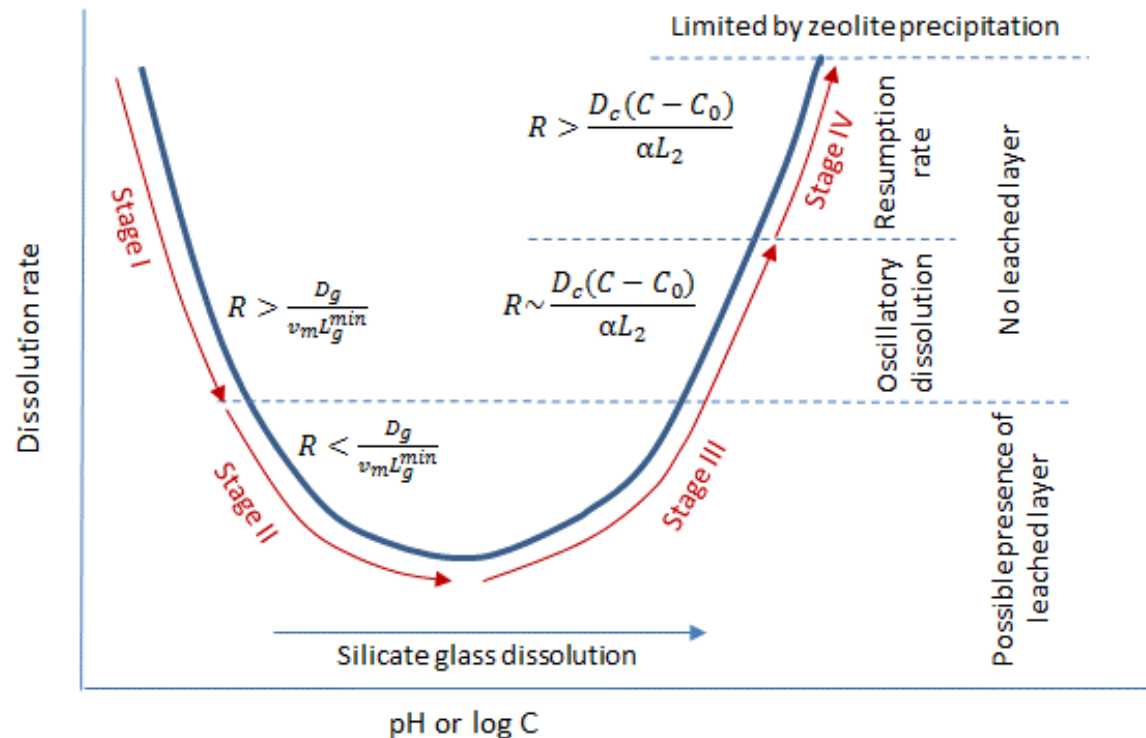
Morphologic instability arises from the same positive feedback.

Alteration resumption and zeolite formation

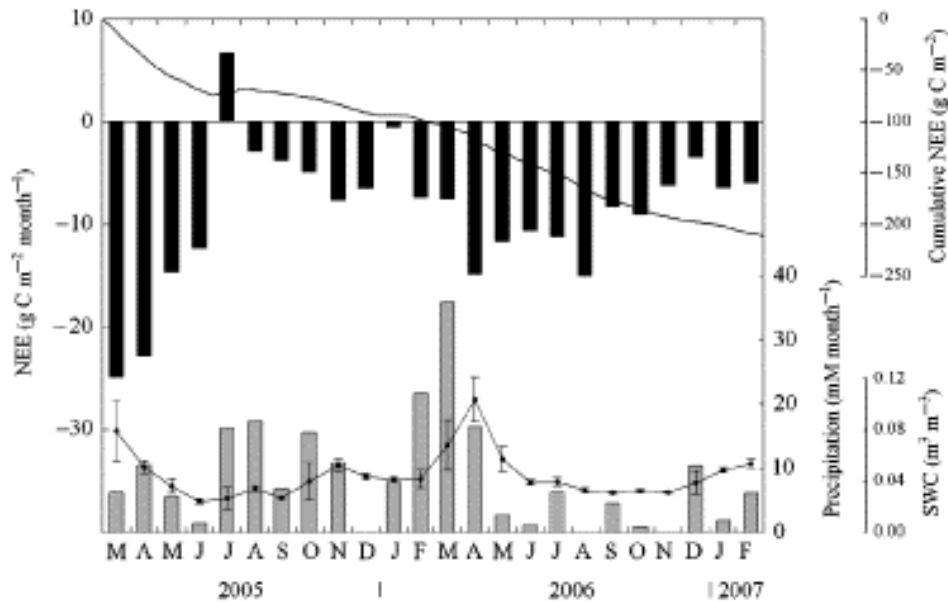


Eventually, the dissolution rate overtakes the mass exchange rate, leading to a “runaway” situation with a sharp increase in the cation concentration at the interface and therefore the dissolution rate.

Waste durability: Chemical composition and water chemistry

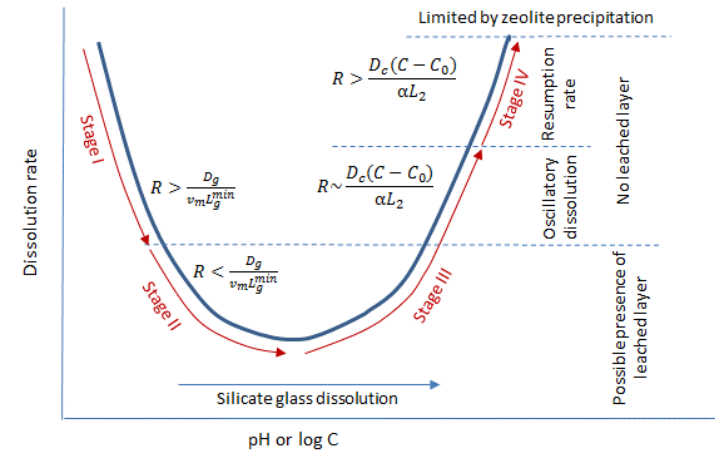


Implication to weathering

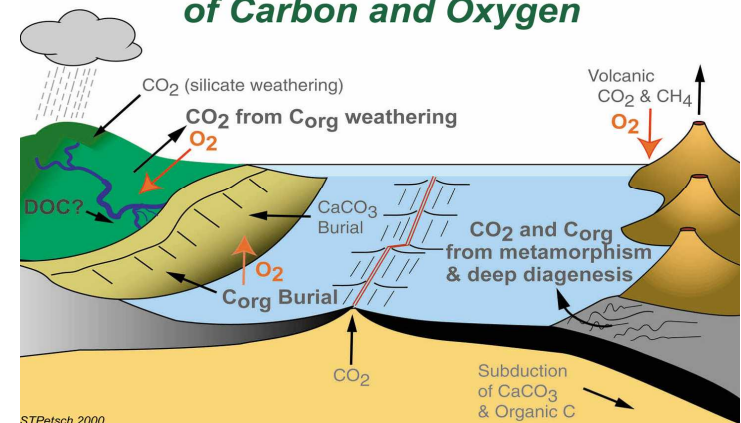


NEE: Net ecosystem CO₂ exchange

Wohlfahrt et al. (2002)



Long-Time-Scale Biogeochemical Cycle of Carbon and Oxygen



Concluding remarks

- Complex silicate material dissolution behaviors can emerge from a simple positive feedback between dissolution-induced cation release and cation-enhanced dissolution kinetics.
- This mechanism enables a systematic prediction of the occurrence of sharp dissolution fronts, oscillatory dissolution behaviors and multiple stages of glass dissolution.
- It provides a new perspective for predicting long-term silicate weathering rates in actual geochemical systems and developing durable silicate materials for various engineering applications.

Acknowledgements

- DOE-Spent Fuel Waste Science & Technology (SFWST)
- DOE-Energy Frontier Research Center (EFRC)