

# Highly Accurate Calculations of the Phase Diagram of Cold Lithium

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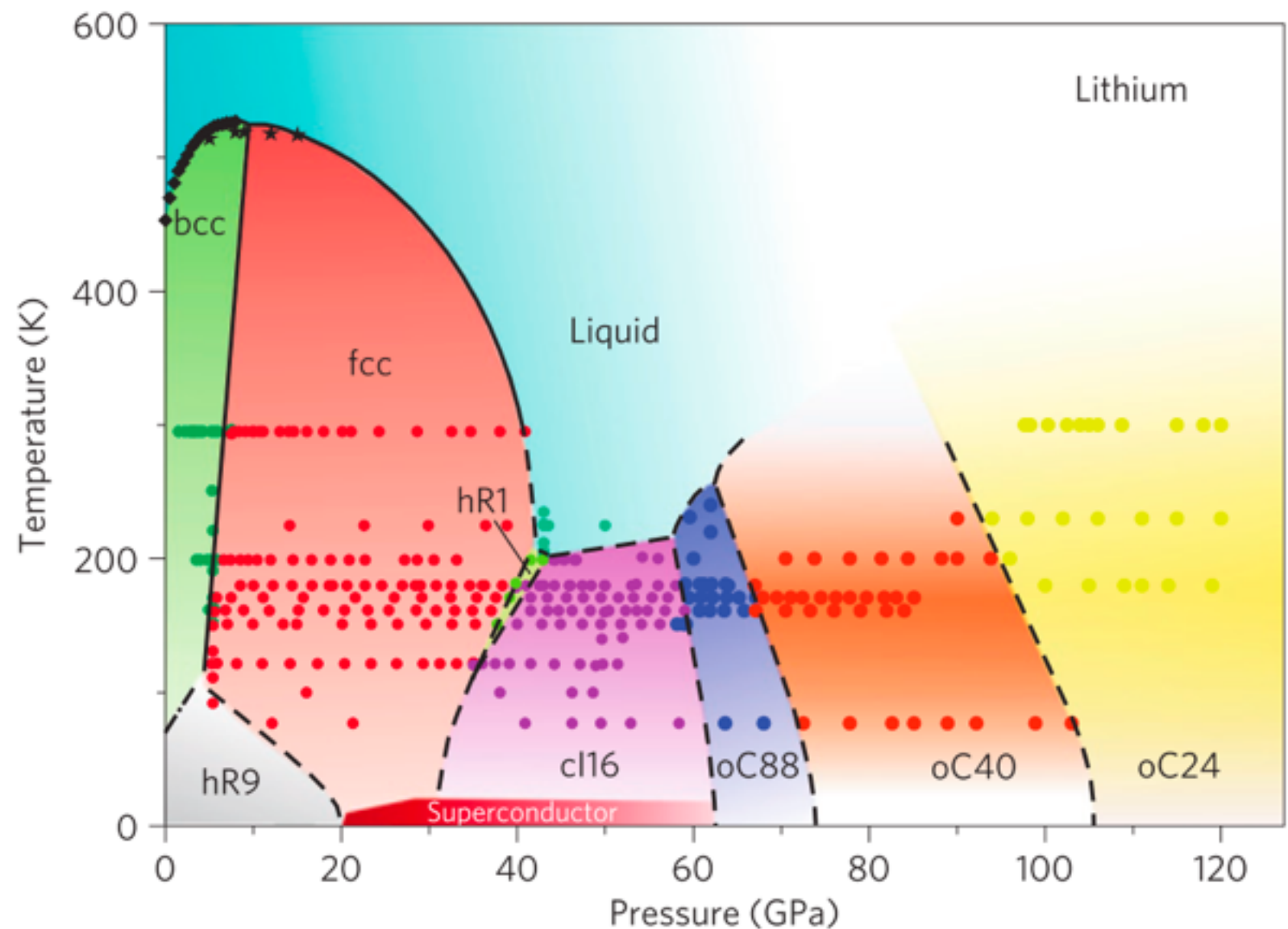
Many thanks to my **collaborators**

**Andrew D. Baczewski**  
**Michael P. Desjarlais**  
**Christopher T. Seagle**

Who are at **Sandia National Laboratories**

**Elemental Li** has a surprisingly rich phase diagram

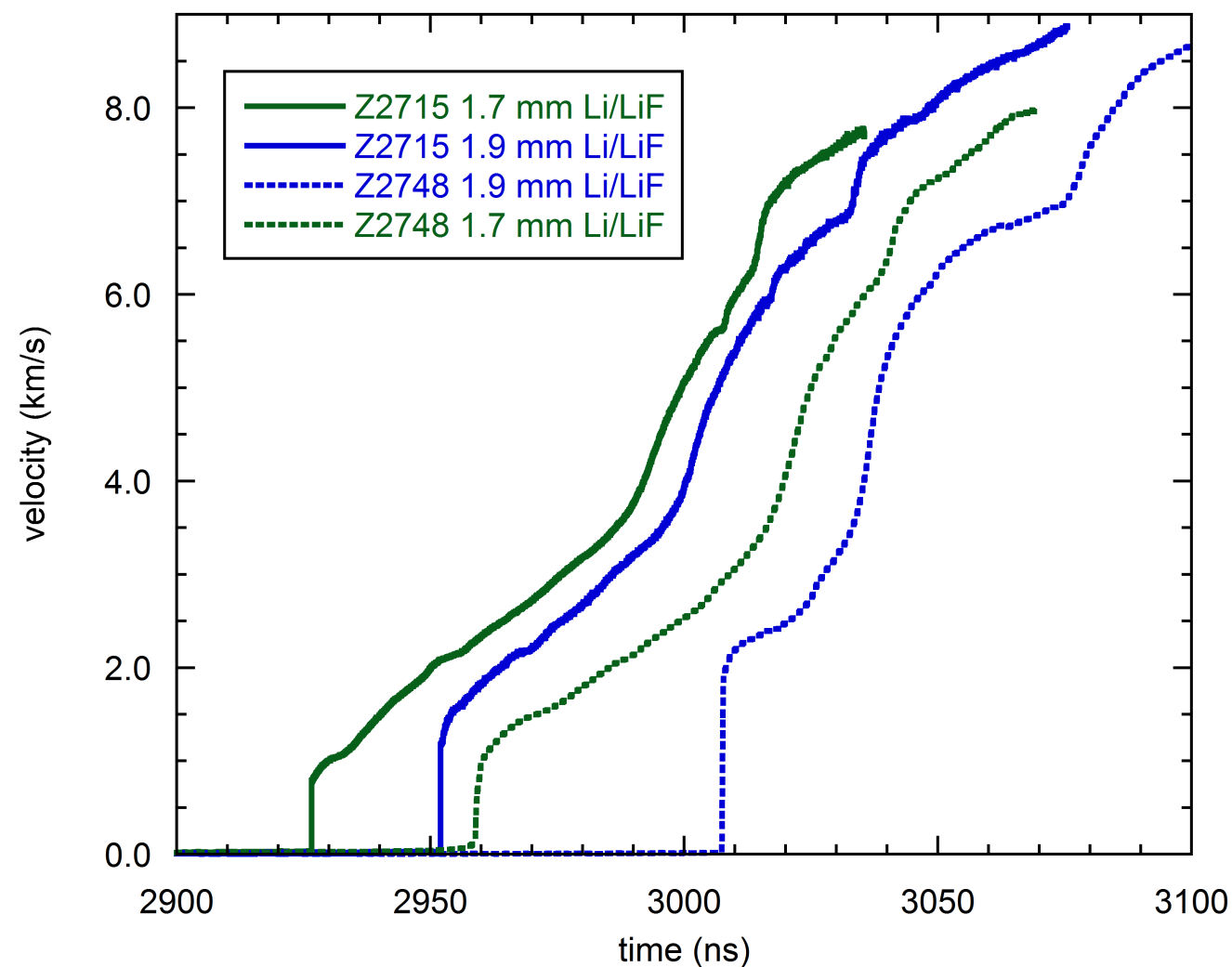
- 8 observed solid phases
- Electride phase (oC40)
- Metal-semiconductor-metal transition
- Smallest difference between  $T_c$  and melting



Guillaume, et. al., Nat. Phys., **7** (2011)

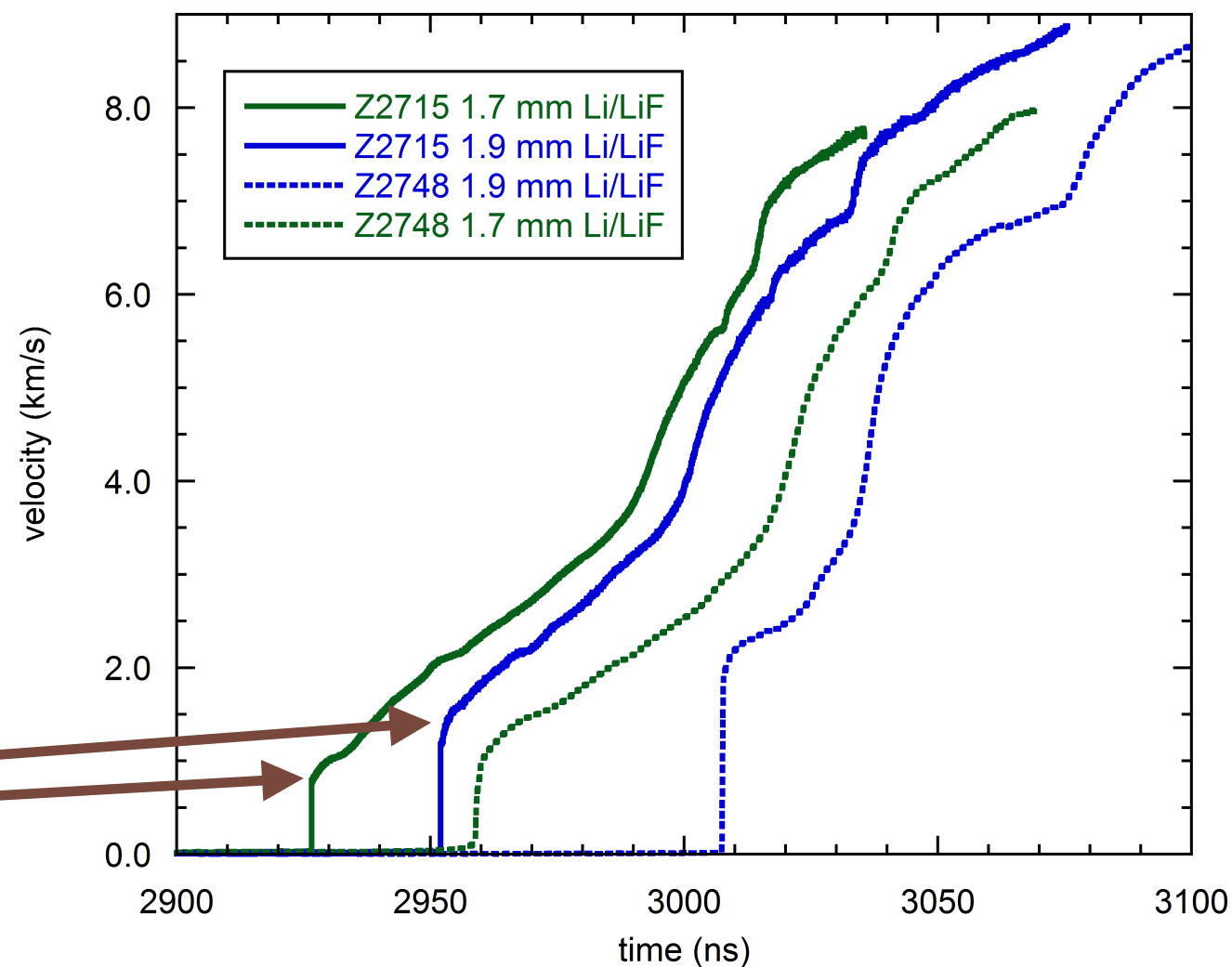
Recent dynamic compression experiments suggest passage through several phase transitions

- Two experiments performed with similar results
- VISAR measures Li/LiF interface velocity
- Traces show several interesting features



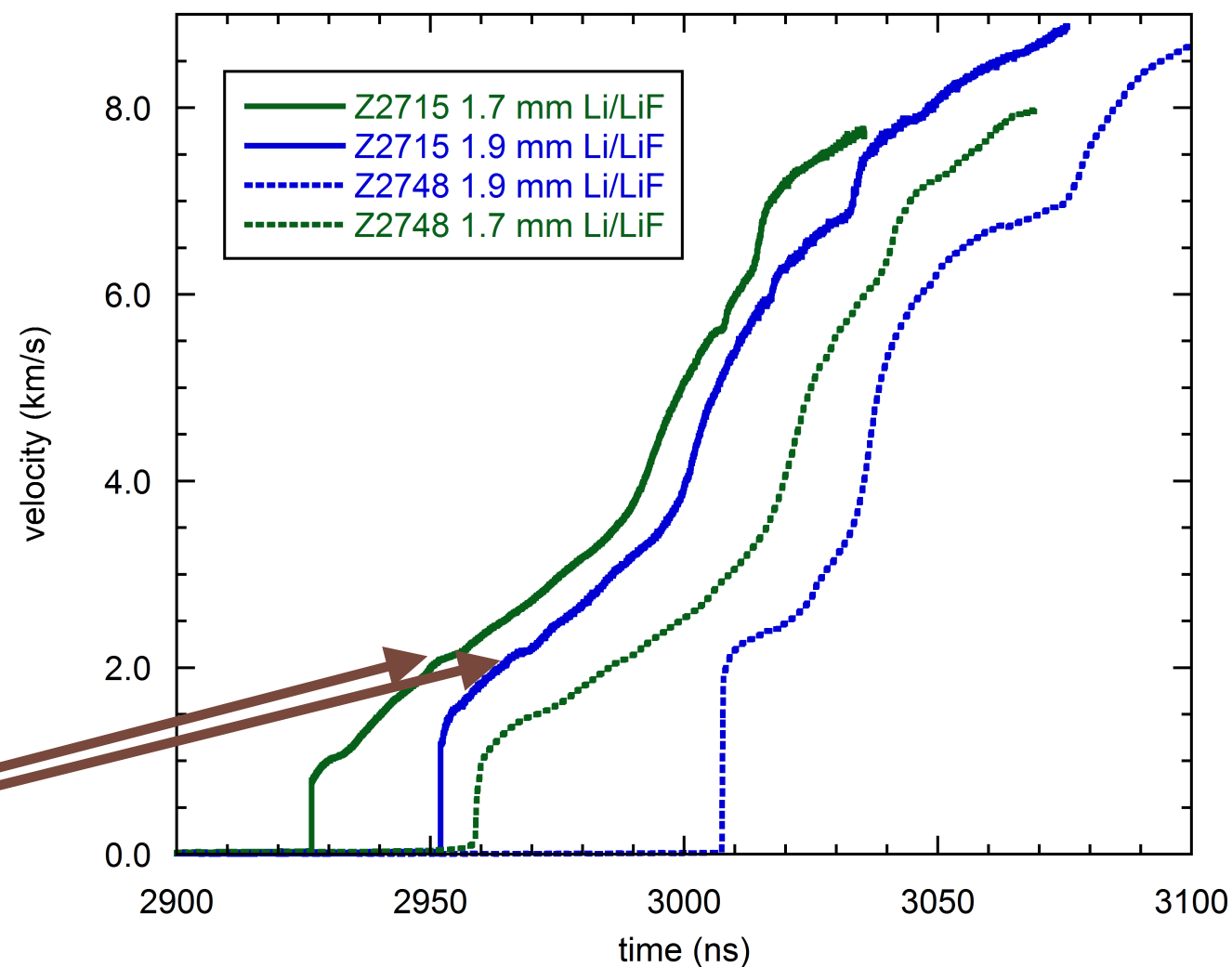
Recent shock experiments suggest passage through several phase transitions

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  - **Initial shock**
  - First softening
  - Late time softening
  - Reverberation



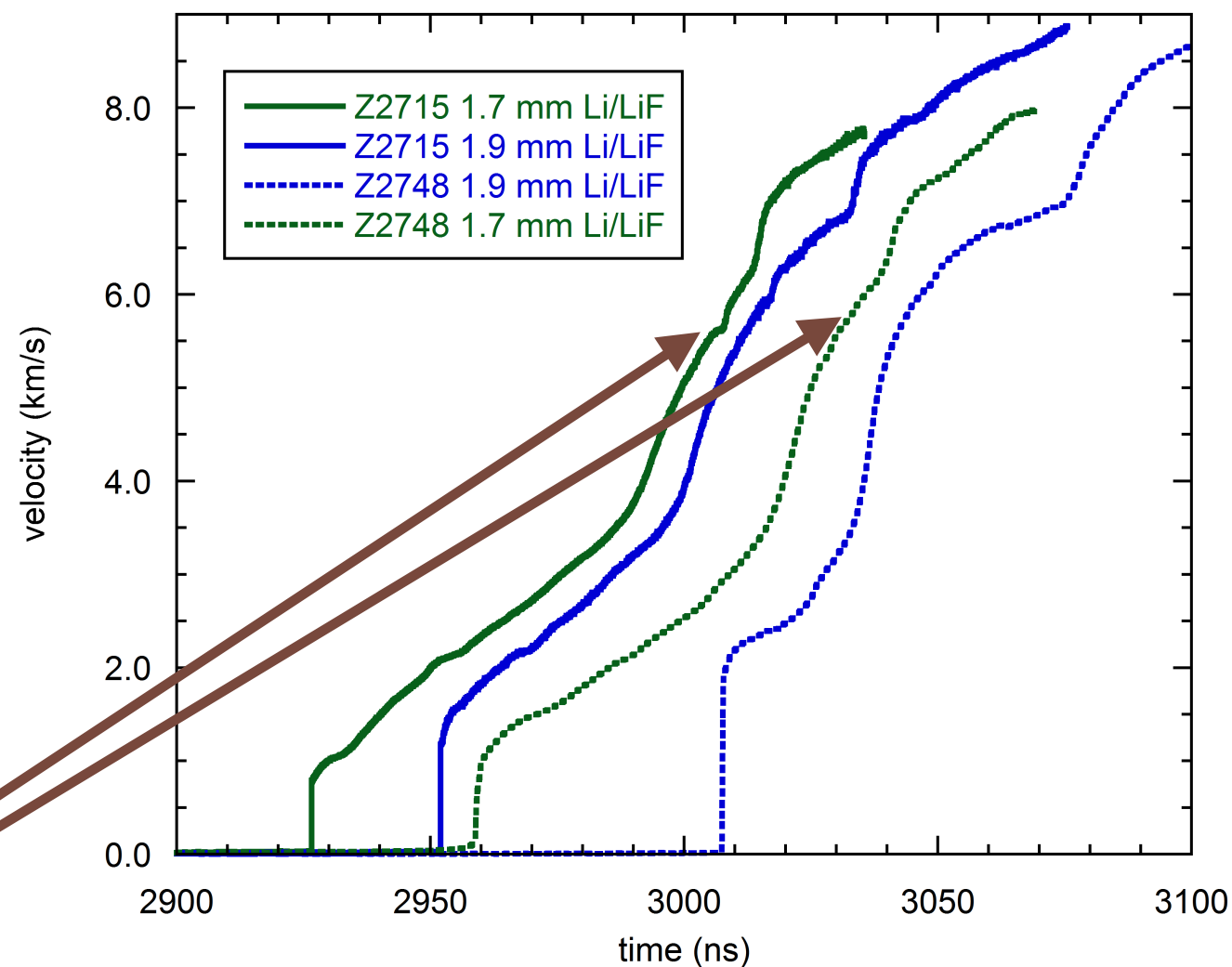
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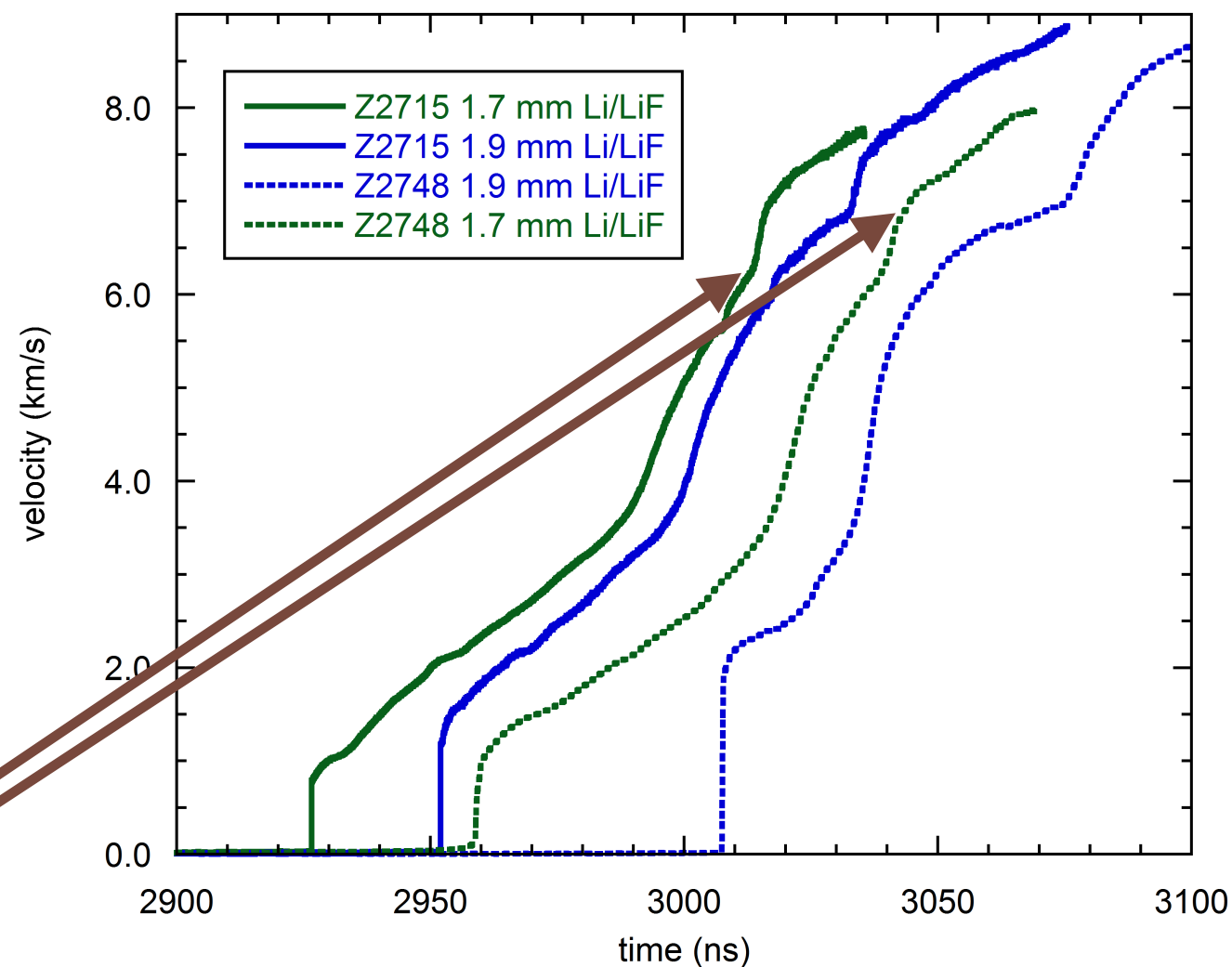
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We would like an **equation of state** for Li to help rationalize these experiments

Today we will only consider **structural phase transitions** but the melt line is of deep interest

DFT is a popular approach, but it relies upon a choice of exchange-correlation functional

LDA/GGA do remarkably well for low pressure Li...

...but at high pressure we know of 2 issues:

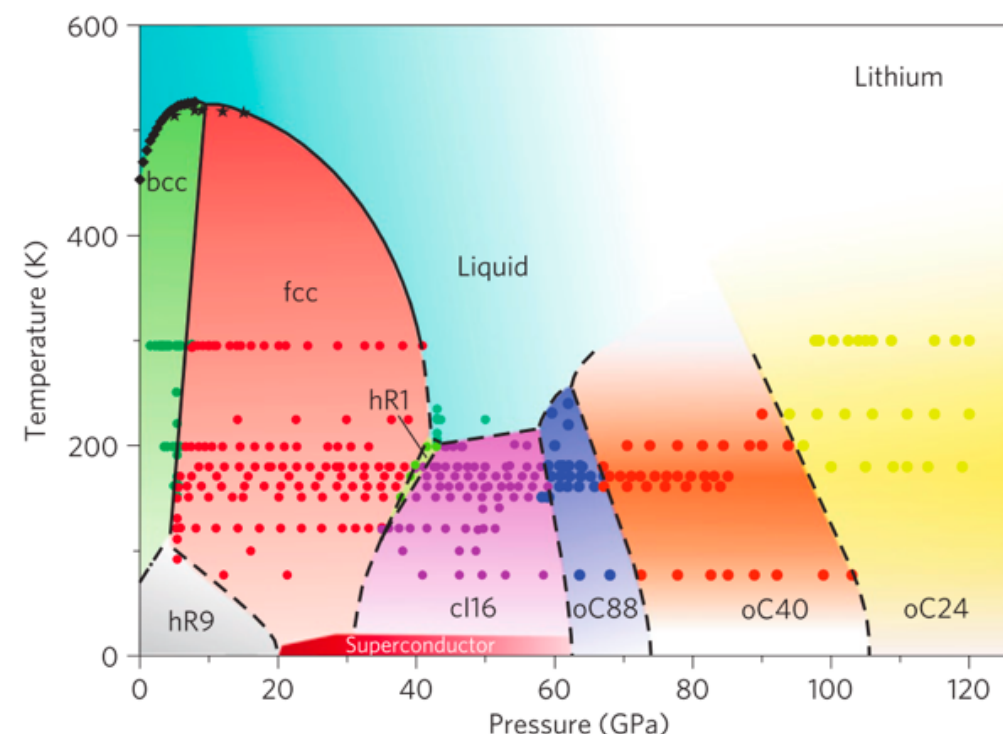
1. **Electride phase** - semi-local DFT should not describe this well
2. **Re-entrant behavior** - gap opens and closes in pressure

Using methodology in Shulenburger and Mattsson, PRB **88** (2013)  
We are developing an equation of state for Li using quantum Monte Carlo (QMC)

- Shulenburger, Mattsson, and Desjarlais, arXiv:1501.03850
  - **Pseudopotential error** largest in Be transition pressures
  - We can afford to study Li with **all 3 electrons**
- Rasch and Mitas, PRB, **92** (2015)
  - Fixed-node DMC gets **96-99% of correlation energy in Li**
  - Only solid phase considered was bcc (STP stable)

## Phases studied:

- bcc, fcc - volume uniquely determined
- hR9 - fixed  $c/a = 7.31$  (expt.)
- cl16, oC40, Pbca, Aba2-24
  - “relaxed” with DFT - GGA
  - DFT energies sensitive at level of microHa/atom (inside DMC error bar)

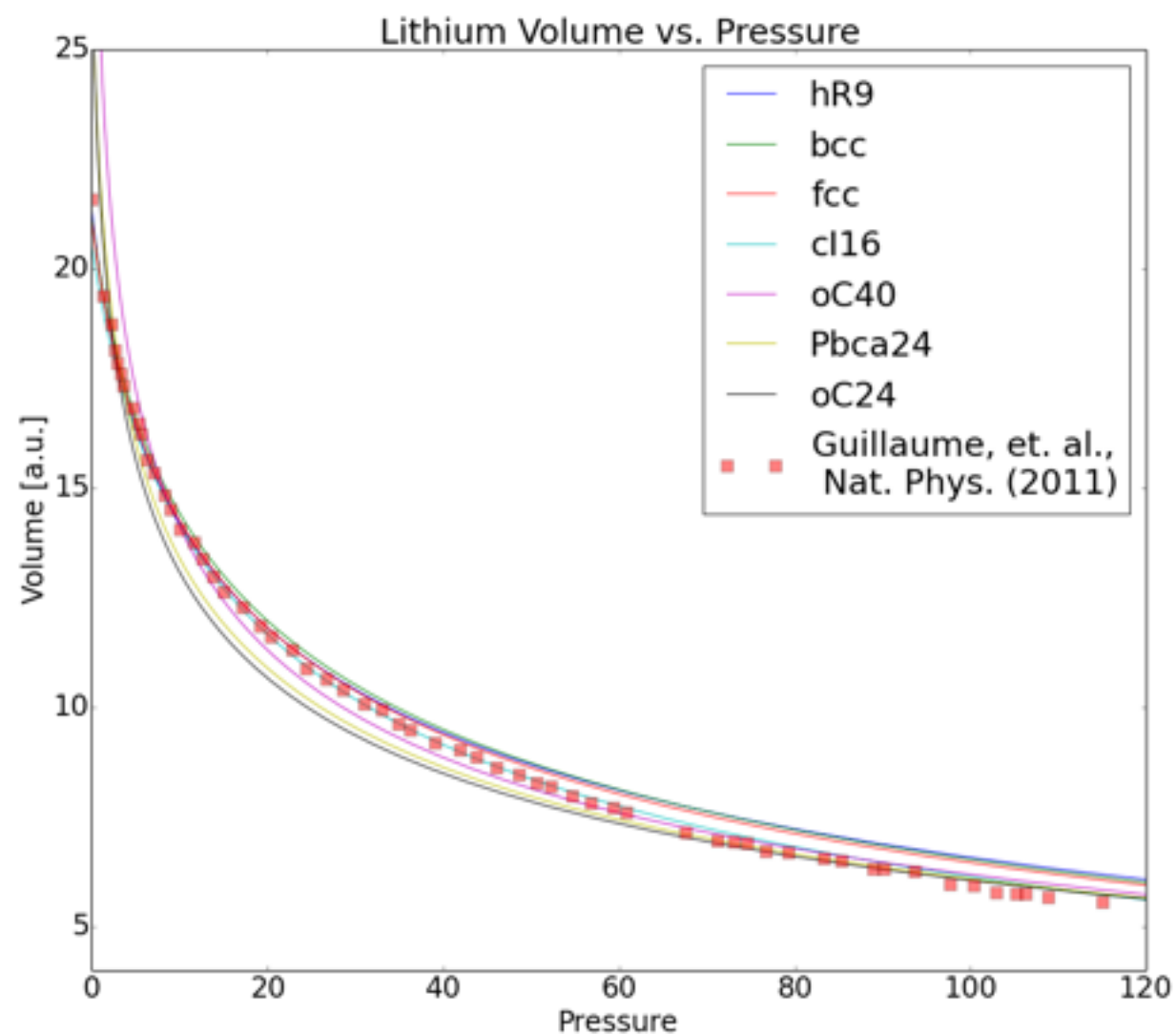


Guillaume, et. al., Nat. Phys., **7** (2011)

- Quasi-harmonic treatment of thermal degrees of freedom
- Nuclear quantum effects effect melt weakly (Feng et al. J. Chem Phys **142**, 064506 (2015))
- All QMC calculations done with O(200) Li atoms
- Finite size extrapolation appears to be largest approximation

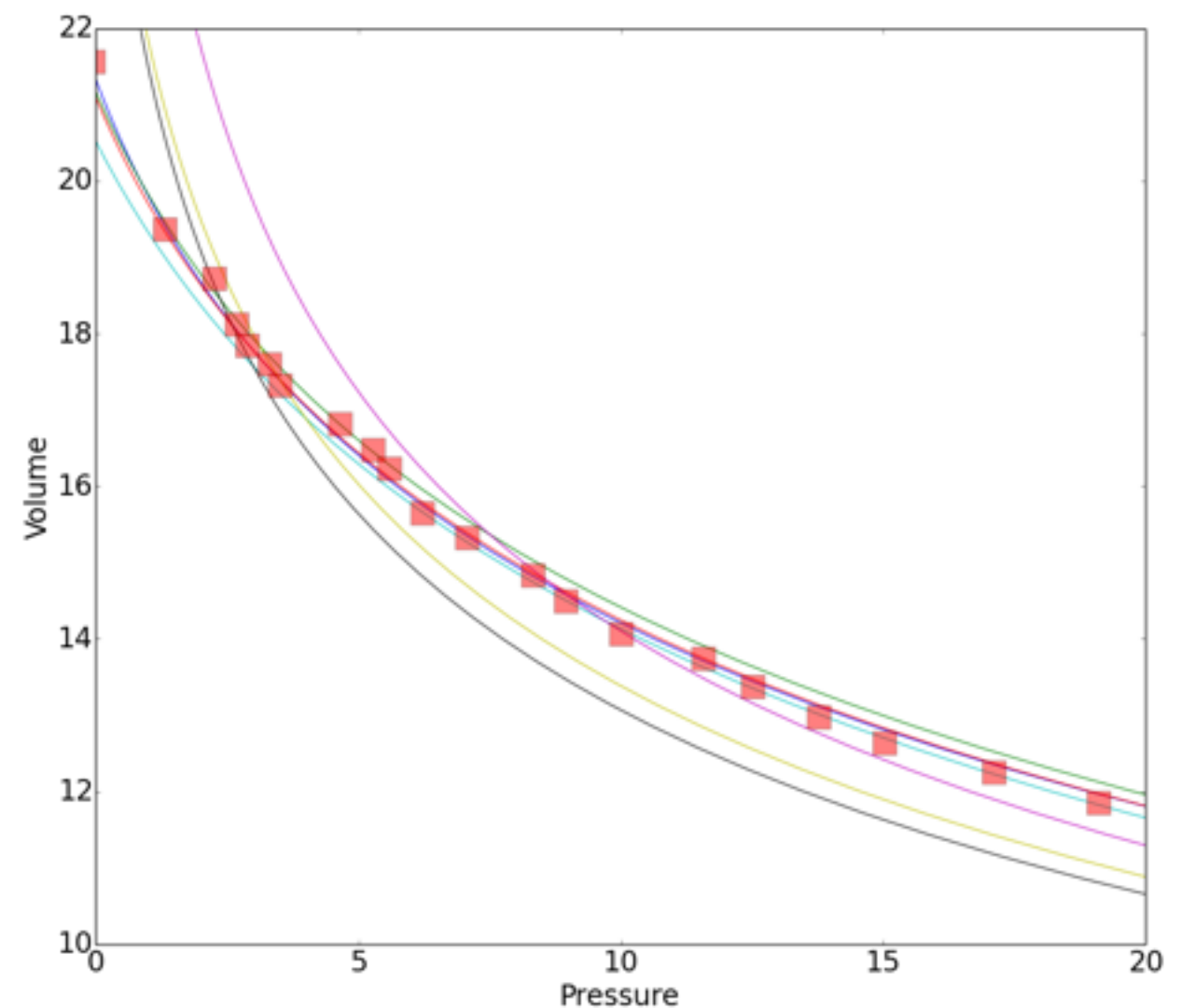
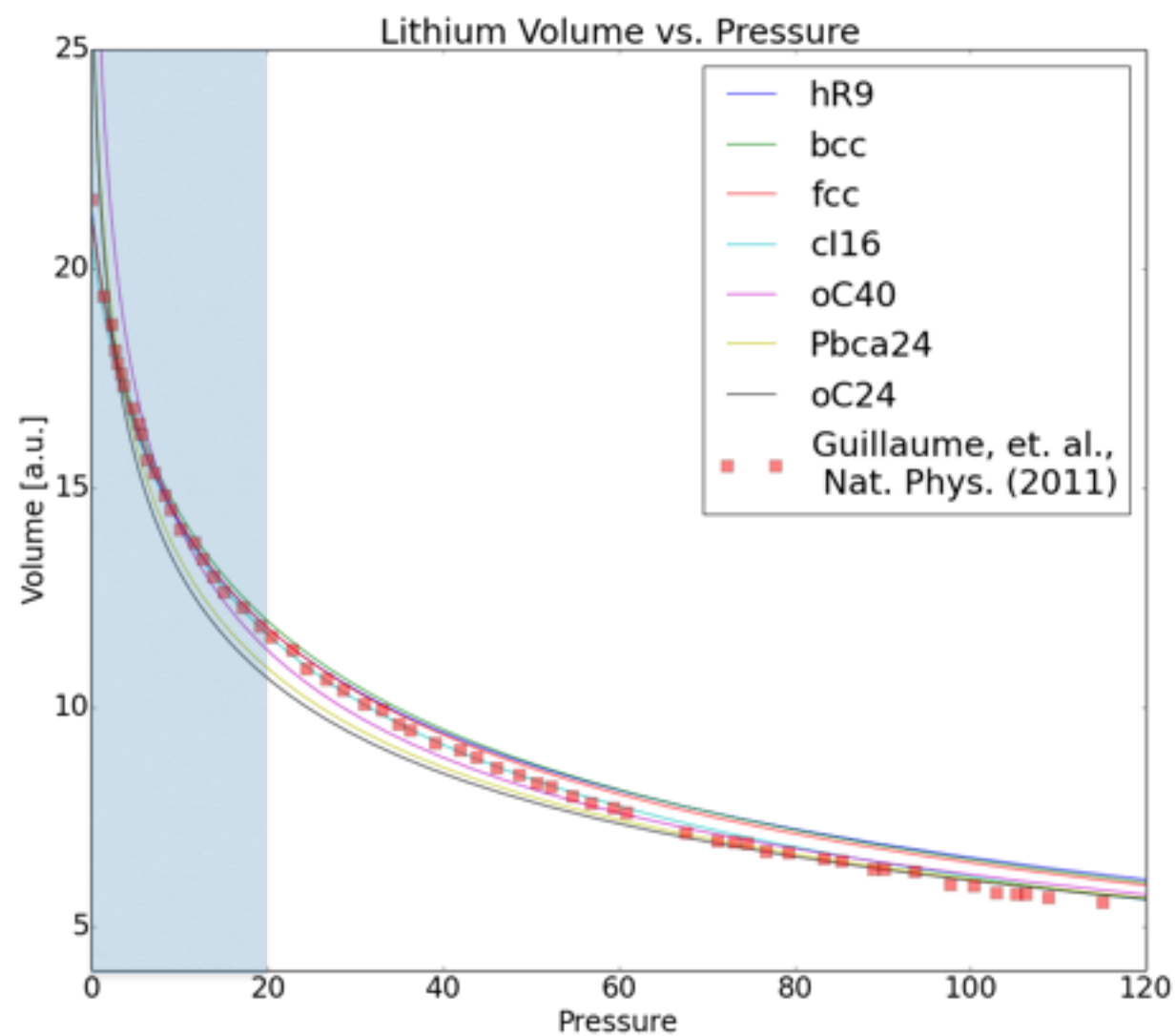
- Phase transition pressures are calculated from total energies with statistical error
- Forces fit of auxiliary equation of state to provide pressure (vinet)
- Requires calculations far from transition to constrain equation of state

Vinet fit of energy vs. volume curve gives pressure



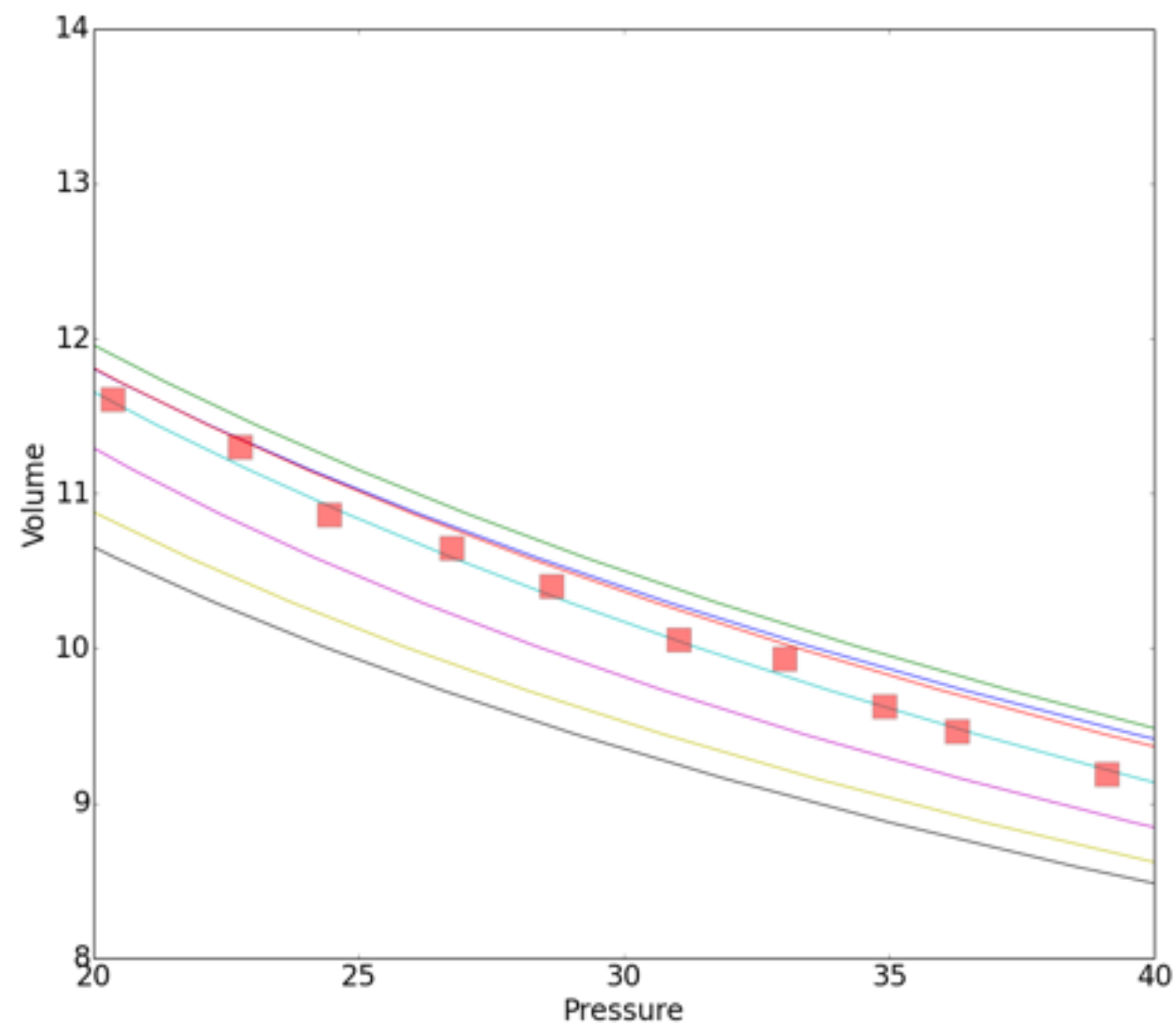
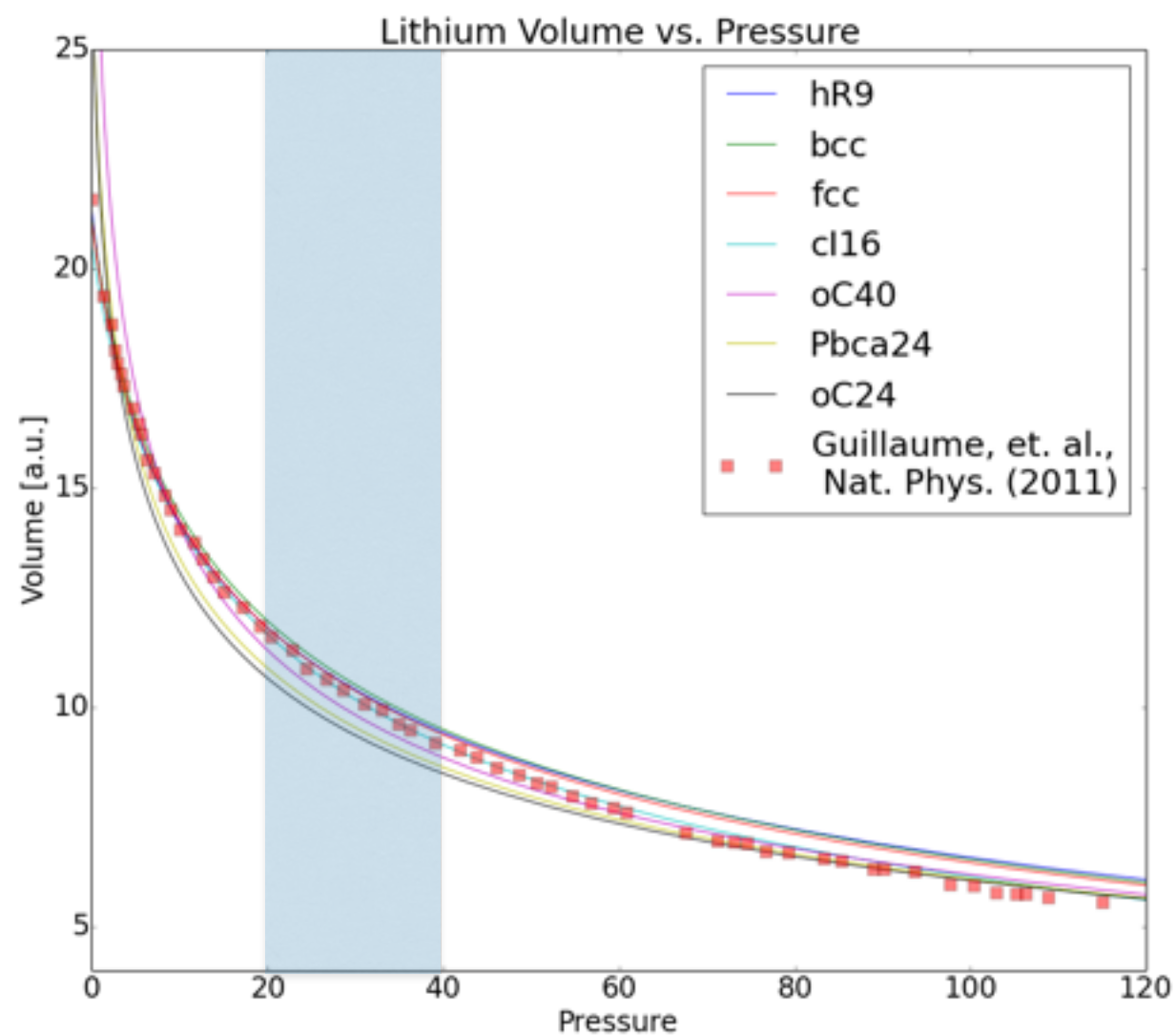
Comparison made against DAC experiment

Vinet fit of energy vs. volume curve gives pressure



Low pressures - consistent with hR9, bcc, and fcc curves

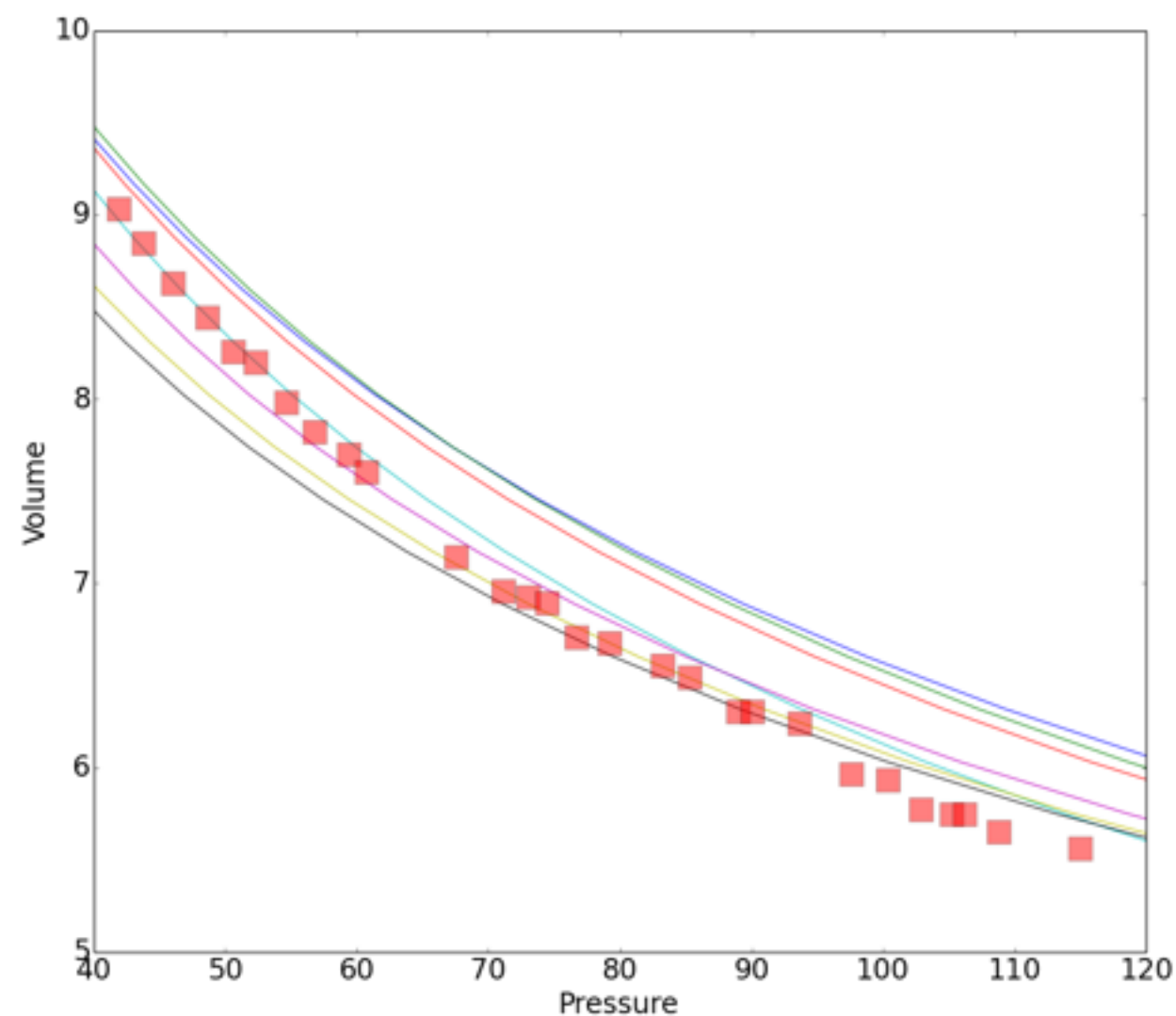
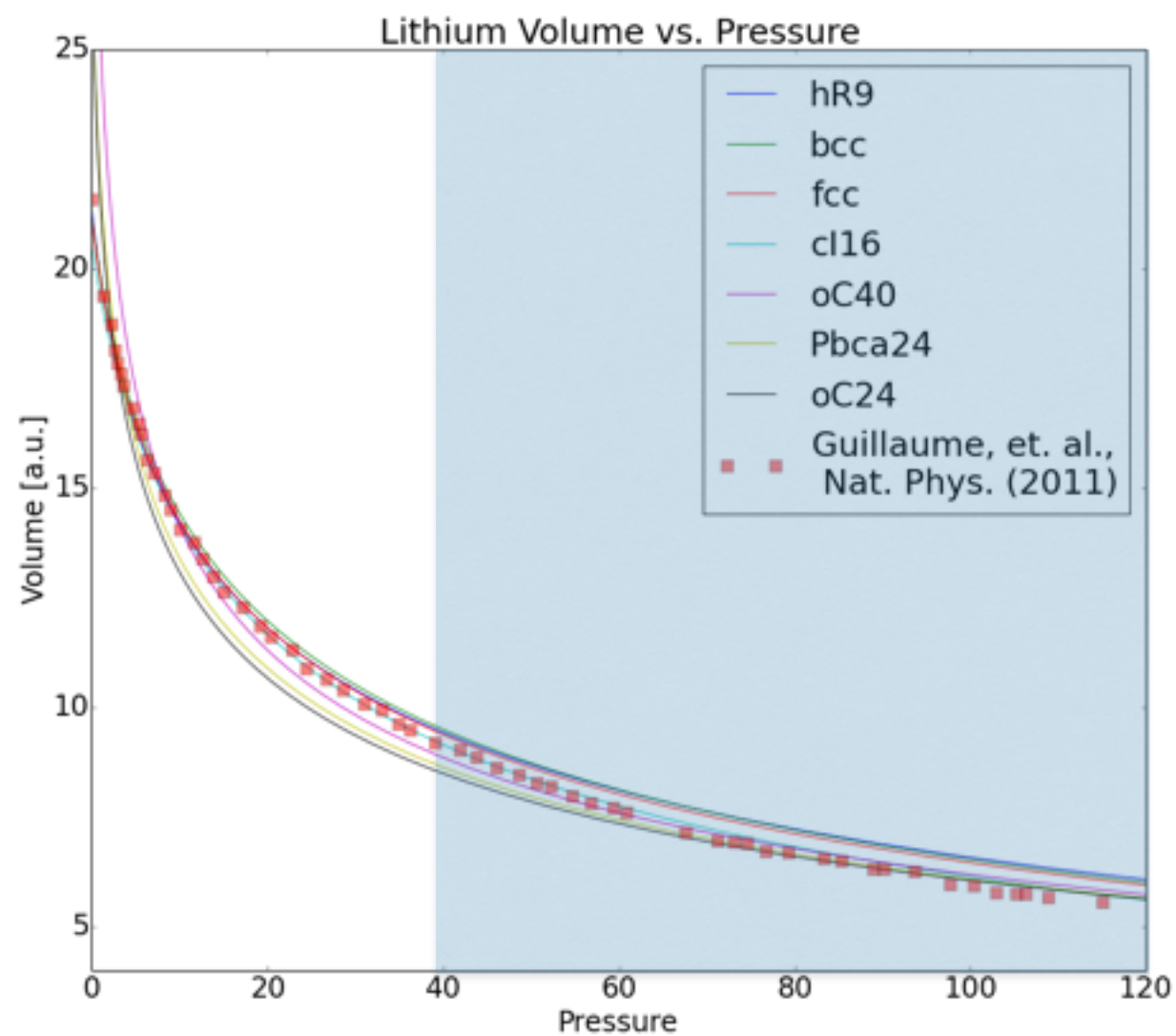
Vinet fit of energy vs. volume curve gives pressure



Intermediate pressures - crossover to cl16



Vinet fit of energy vs. volume curve gives pressure

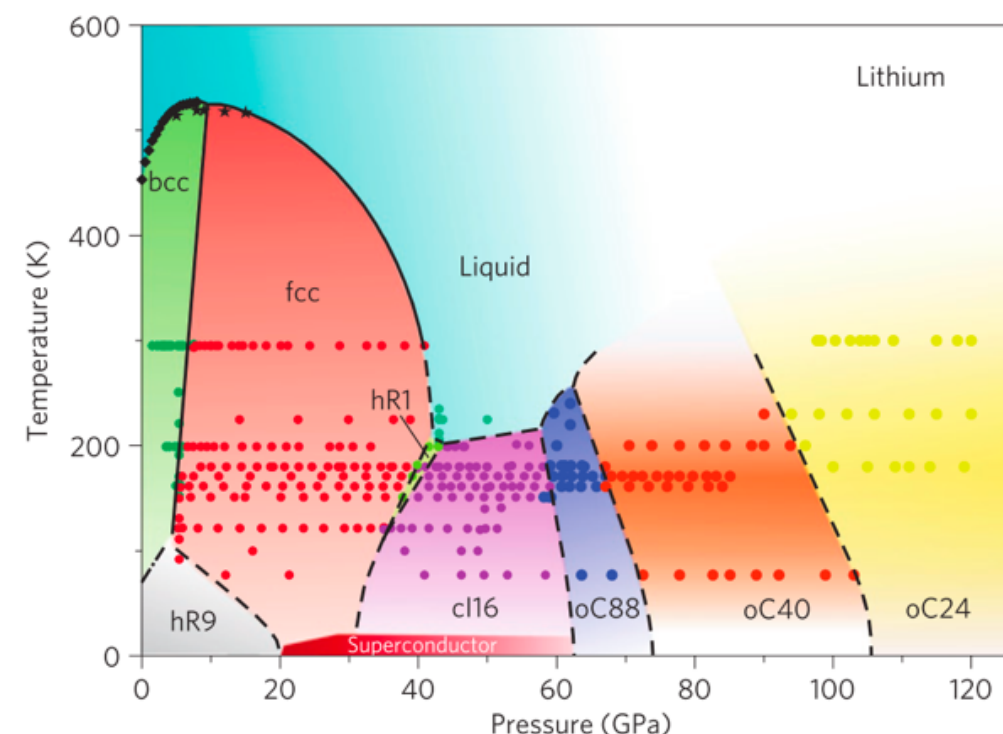


High pressures - crossover to low symmetry phases



Preliminary results for phase transition pressures:

- bcc to fcc - **8.6 GPa**
- fcc to cl16 - **30.2 GPa**
- cl16 to oC40 - **66.5 GPa**
- Understand the role of temperature
- Incorporate more phases
- Examine sensitivities to finite size correction schemes
- Impact of implicit reliance on DFT:
  - Generation of geometries
  - Quasi-harmonic contributions



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