

A Comprehensive View of Gaseous Hydrogen-Assisted Cracking

Brian Somerday

Sandia National Laboratories, Livermore CA, USA
International Institute for Carbon-Neutral Energy
Research (I²CNER), Fukuoka, Japan

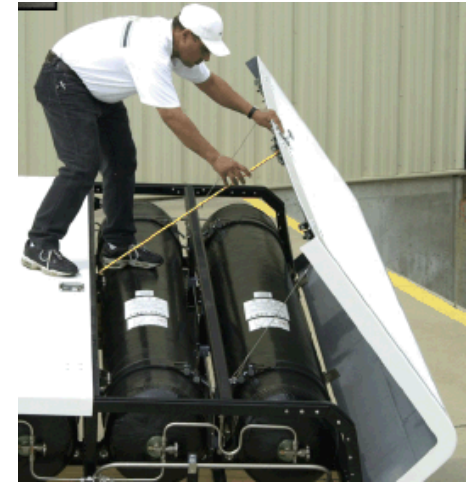
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GE Global Research, Niskayuna, NY
May 19, 2015

Design and materials selection for hydrogen fuel components must consider H₂-assisted cracking

stationary and transport vessels
(martensitic steels)



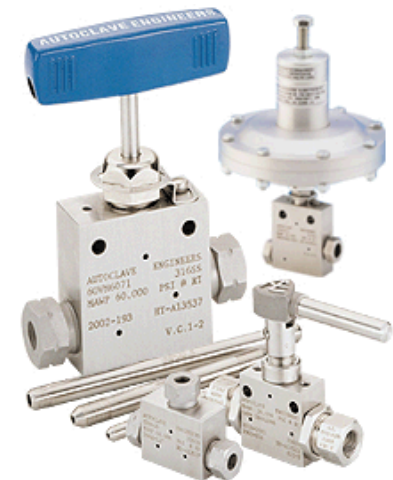
on-board tanks
(aluminum liners, stainless steel boss)



pipelines
(ferritic steels)

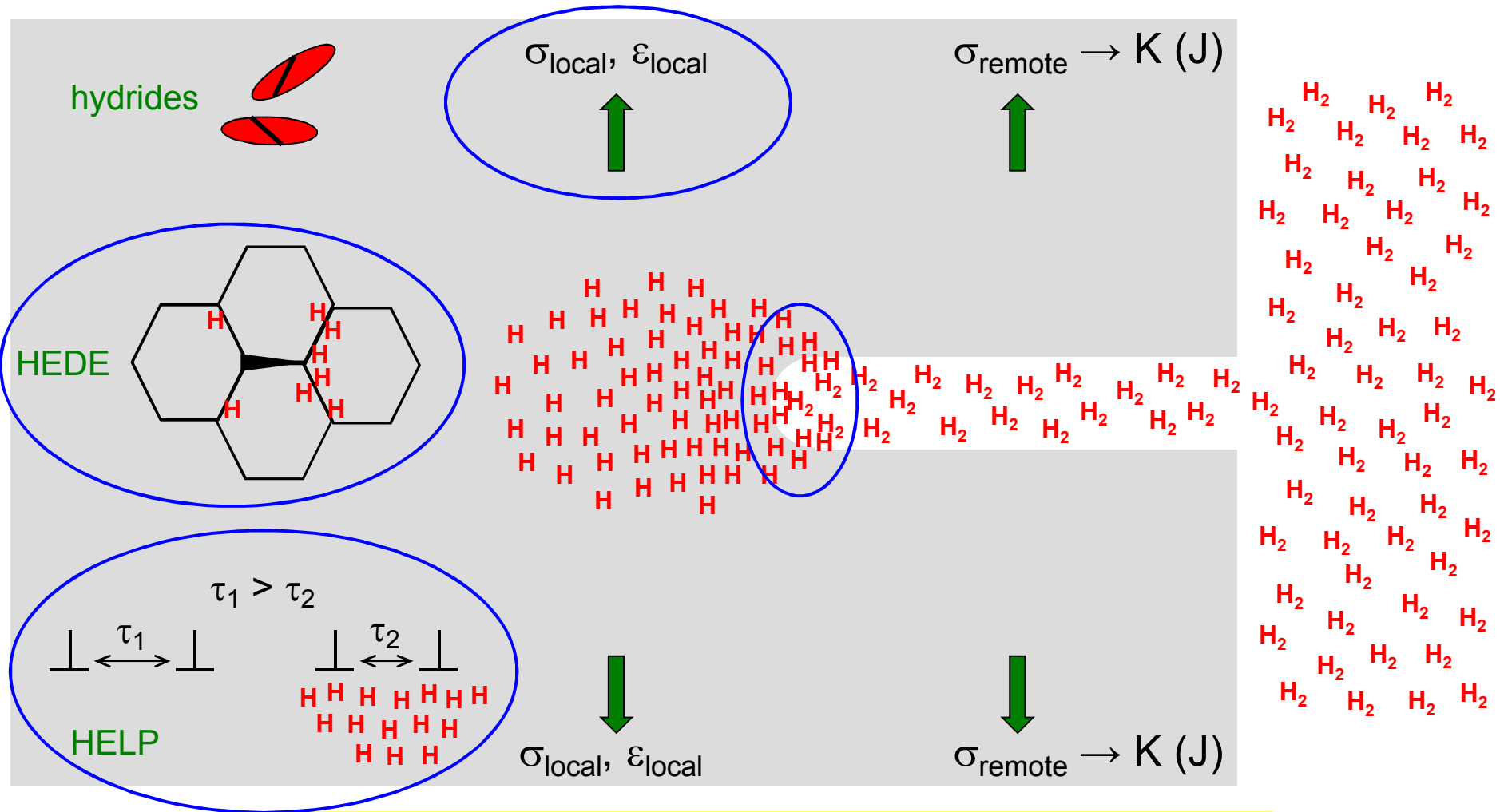


manifold components
(stainless steels)



H₂-assisted cracking is multi-element phenomenon

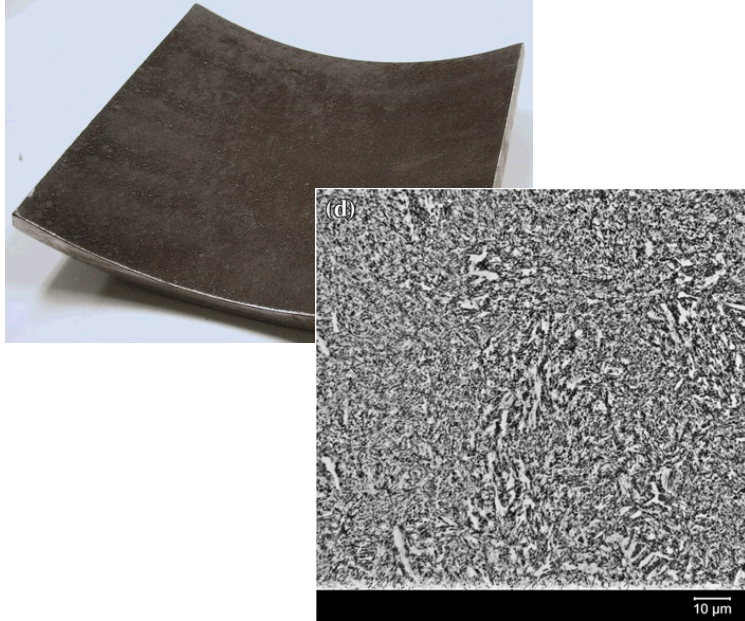
Trends may be dominated by one element



Hydrogen-assisted cracking governed by crack-tip strain field

Issue-driven research goal: measure H₂-assisted cracking thresholds for martensitic steels

K.A. Nibur et al., *Metall Mater Trans A*, 2013



• Material

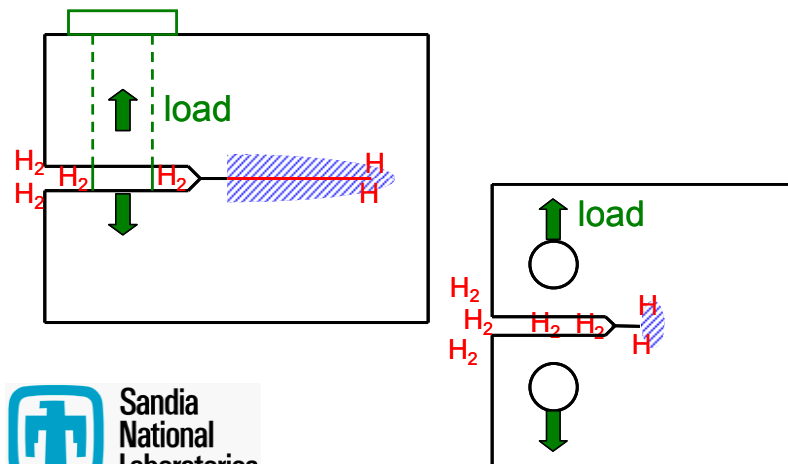
- Cr-Mo(-Ni) pressure vessel steels
- Yield strengths = 600 to 1050 MPa

• Mechanical loading

- Constant displacement
- Rising displacement = 0.05 mm/min (~3 MPa m^{1/2}/min)

• Environment

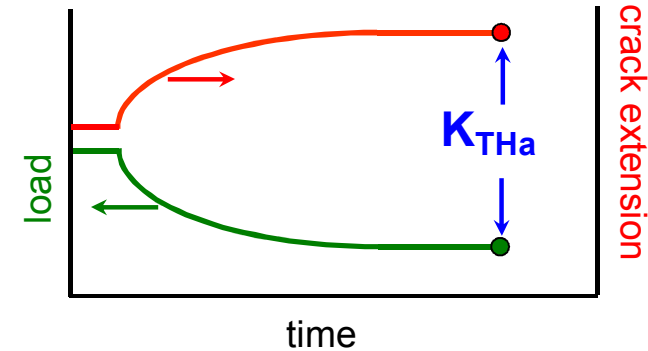
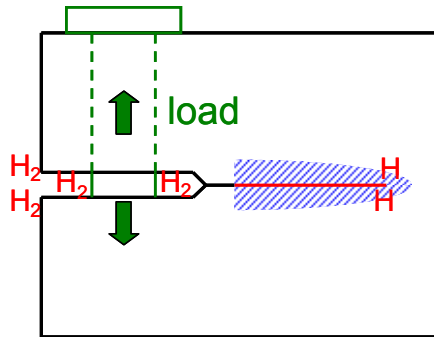
- Supply gases: 99.9999% H₂
- Pressure = 103 MPa (15,000 psi)
- Room temperature



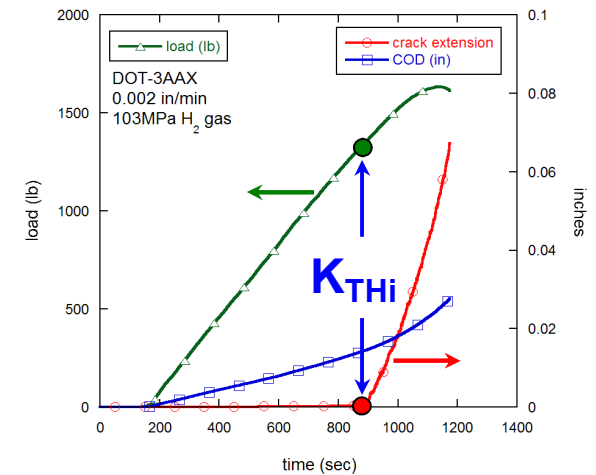
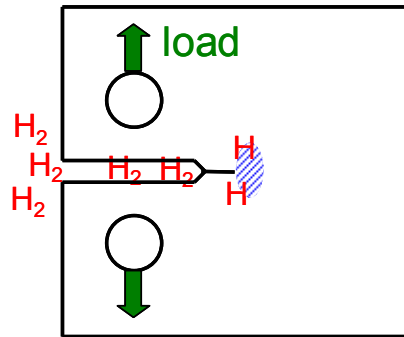
H₂-assisted cracking thresholds measured using two conventional methods

K.A. Nibur et al., *Metal Mater Trans A*, 2013

constant displacement method:
“arrest” threshold, K_{THa}



rising displacement method:
“initiation” threshold, K_{THi}

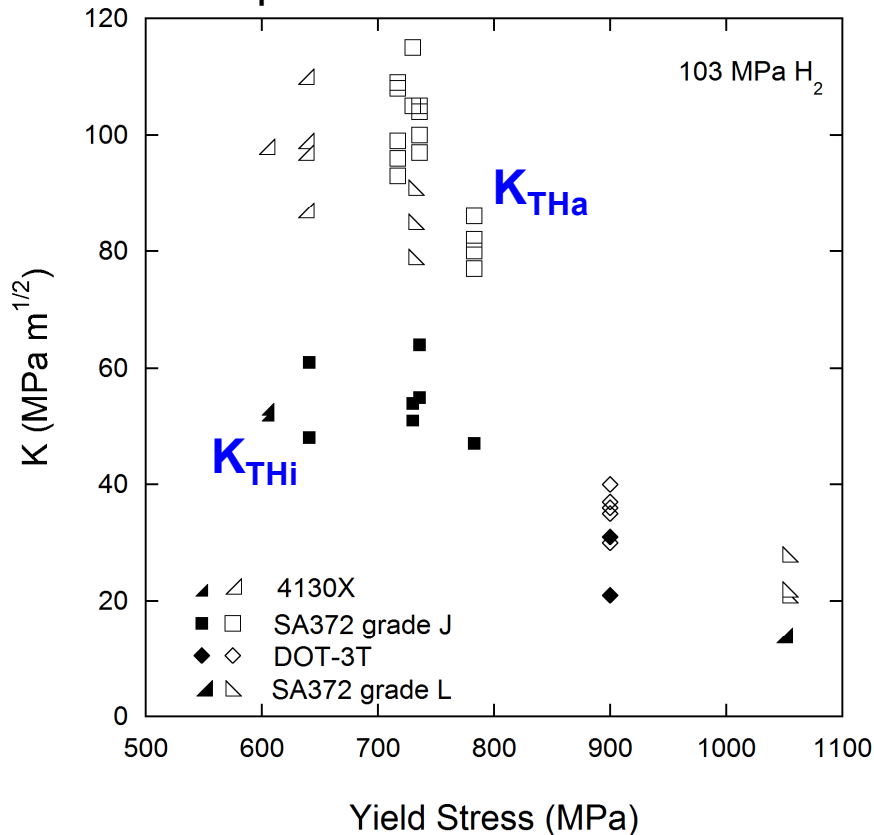


Key difference in test methods: propagating crack vs. stationary crack

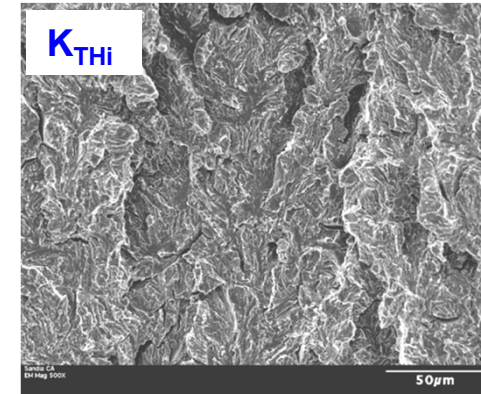
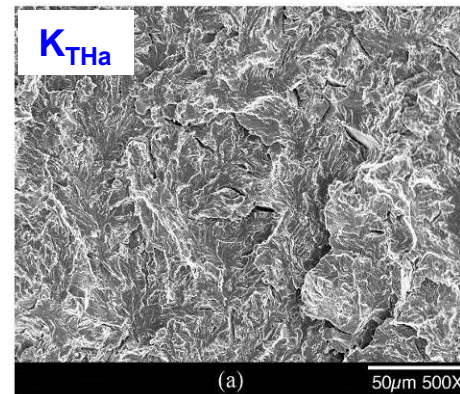
Crack arrest thresholds (K_{THa}) higher than crack initiation thresholds (K_{THi}) at lower σ_{YS}

K.A. Nibur et al., *Metall Mater Trans A*, 2013

pressure vessel steels



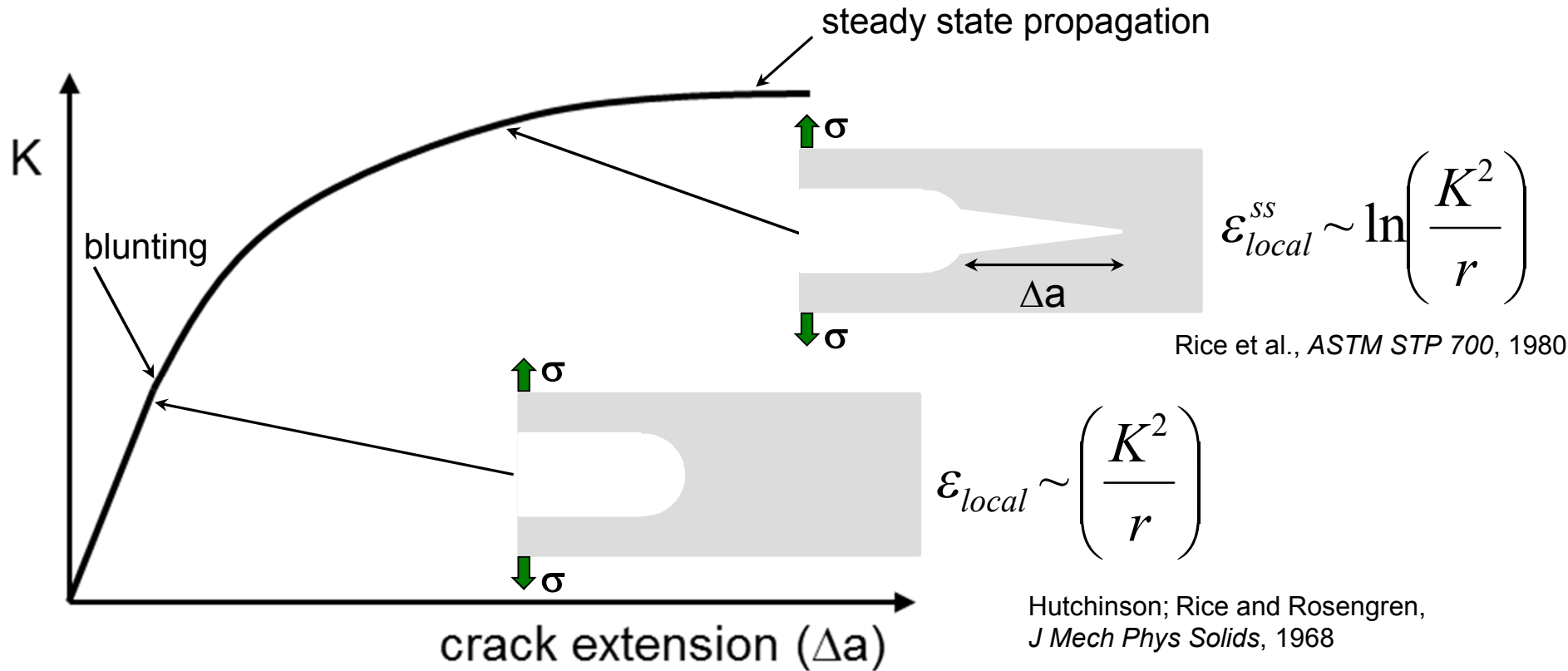
4130X pressure vessel steel



- **Divergent thresholds not attributed to difference in fracture mechanism**
 - **Assume fracture mechanism is strain-controlled, i.e., governed by ϵ_{local}**
 - **Consistent with plasticity-related hydrogen-induced cracking (PRHIC)**
- Takeda and McMahon, *Metall Trans A*, 1981

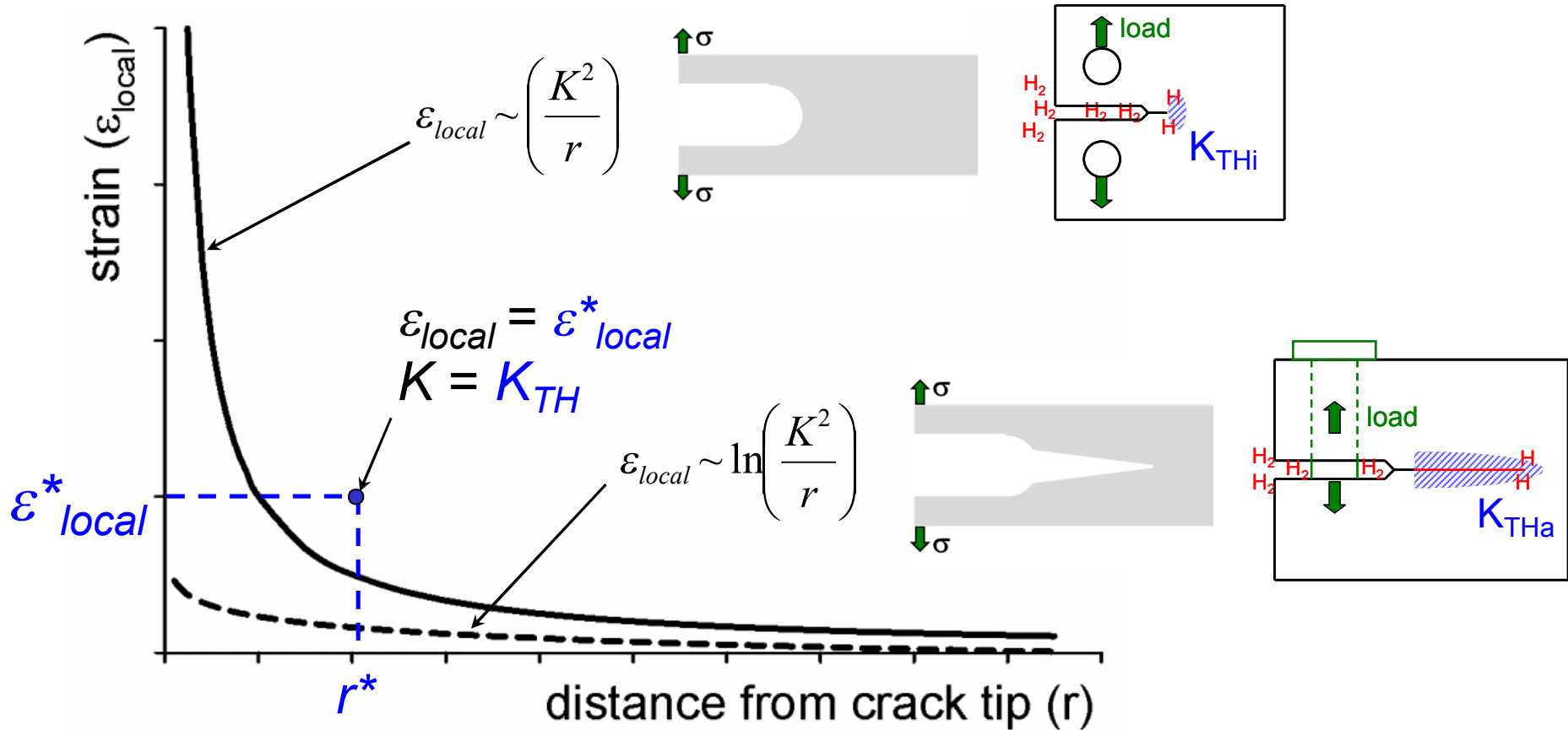
Can observed trends be rationalized based on crack-tip mechanics?

Mechanics of propagating vs. stationary cracks illuminated by crack growth resistance curves



Crack-tip strain field weaker for propagating crack vs. stationary crack

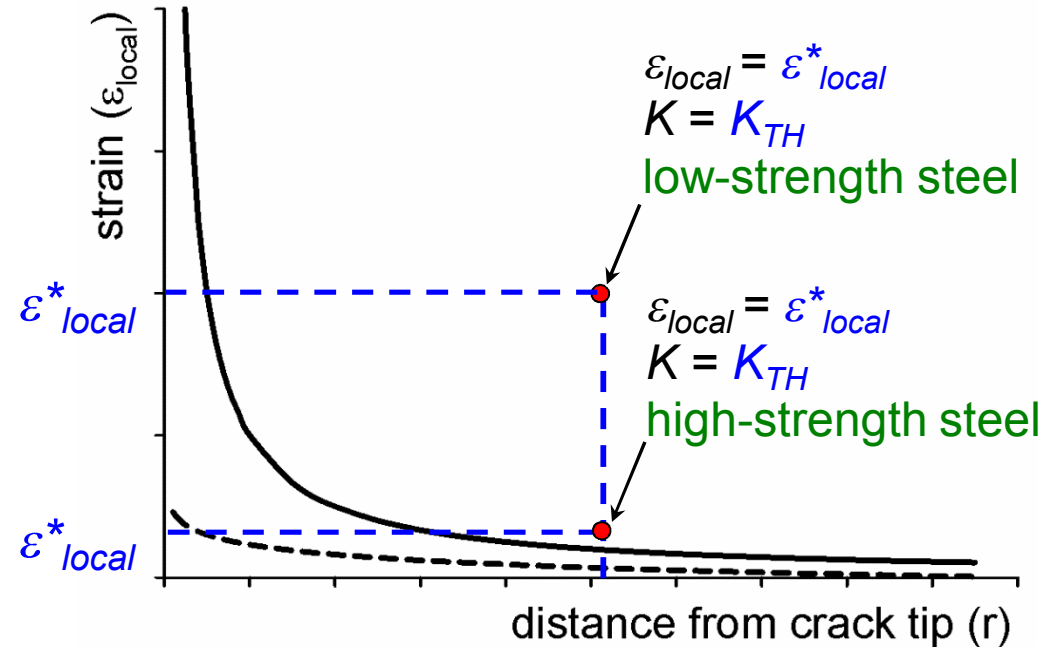
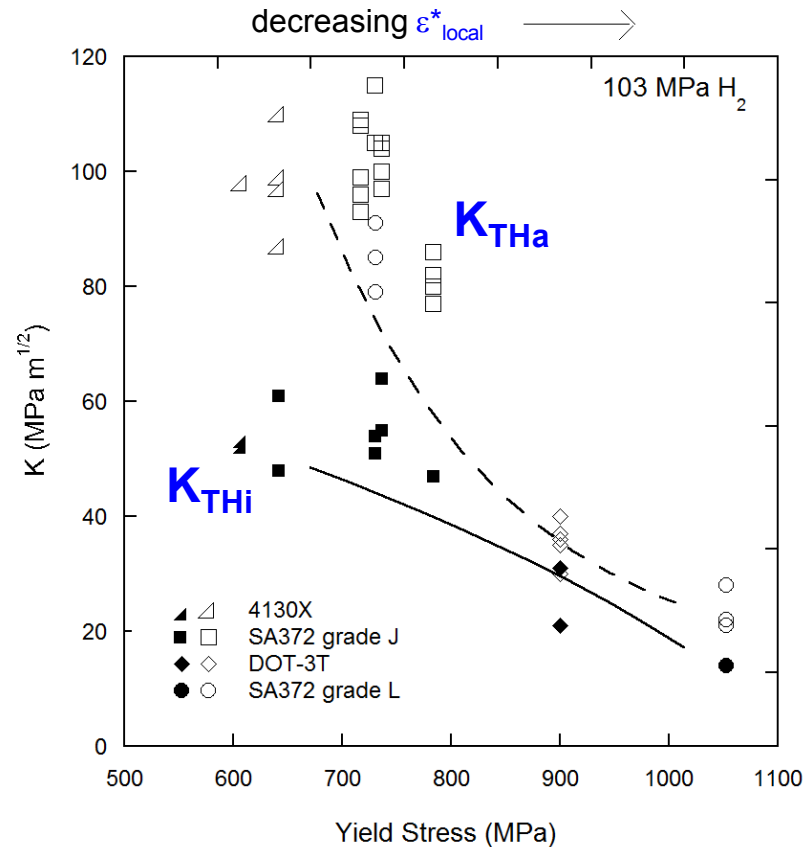
Weaker crack-tip strain field for propagating crack can account for higher crack-arrest thresholds



Strain-controlled fracture criterion (ϵ^*_{local}) coupled with strain field amplitudes leads to $K_{THa} > K_{THi}$

K_{TH} vs. yield strength trends can be rationalized based on crack-tip mechanics framework

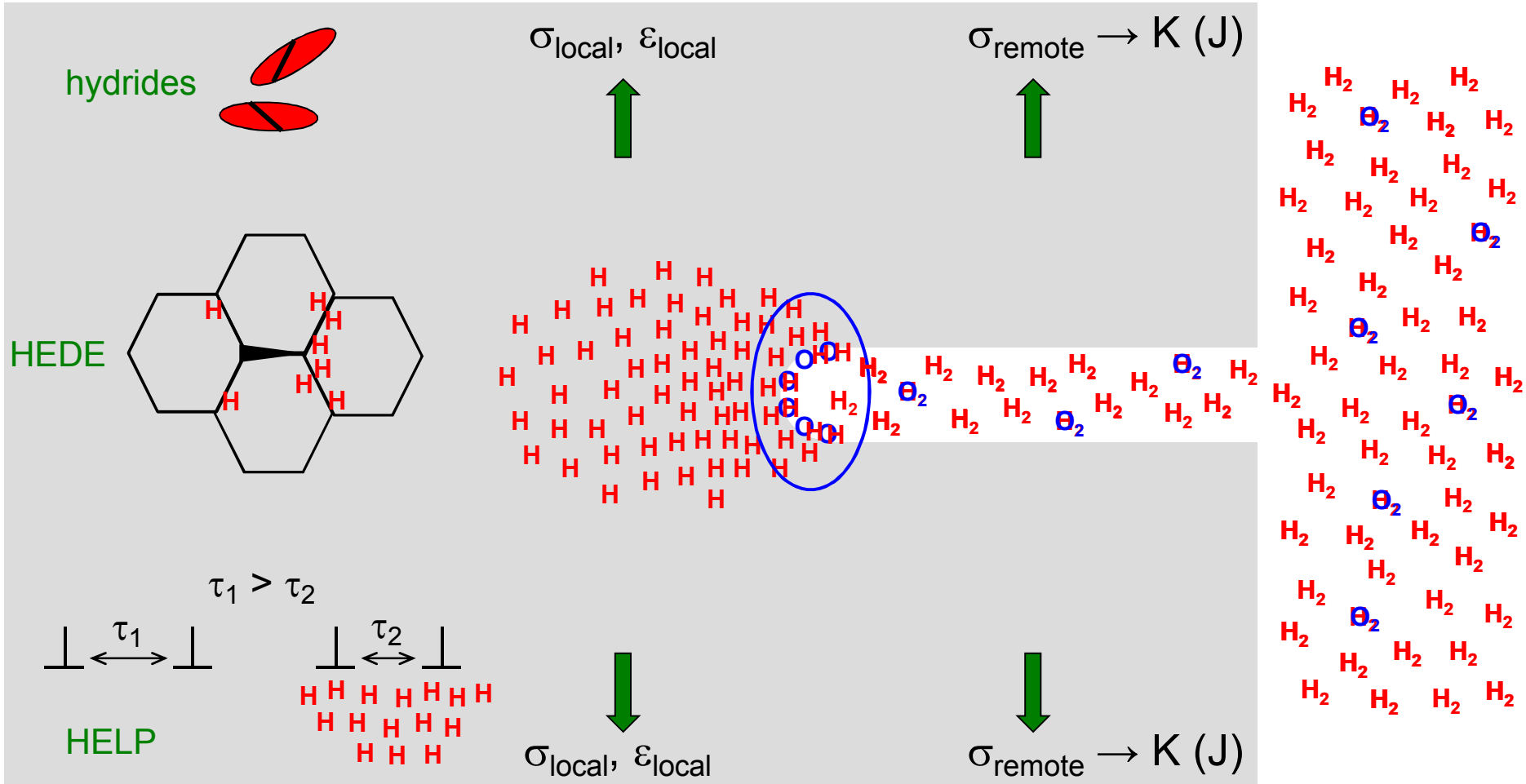
K.A. Nibur et al., *Metal Mater Trans A*, 2013



Assumption that ϵ^*_{local} decreases as yield strength increases can explain converging K_{THa} and K_{THi}

H₂-assisted cracking is multi-element phenomenon

Trends may be dominated by one element



Hydrogen uptake retarded by oxygen adsorption on crack-tip surface

Issue-driven research goal: quantify O₂-modified, H₂-accelerated fatigue crack growth for pipe steel

B.P. Somerday et al., *Acta Mater*, 2013

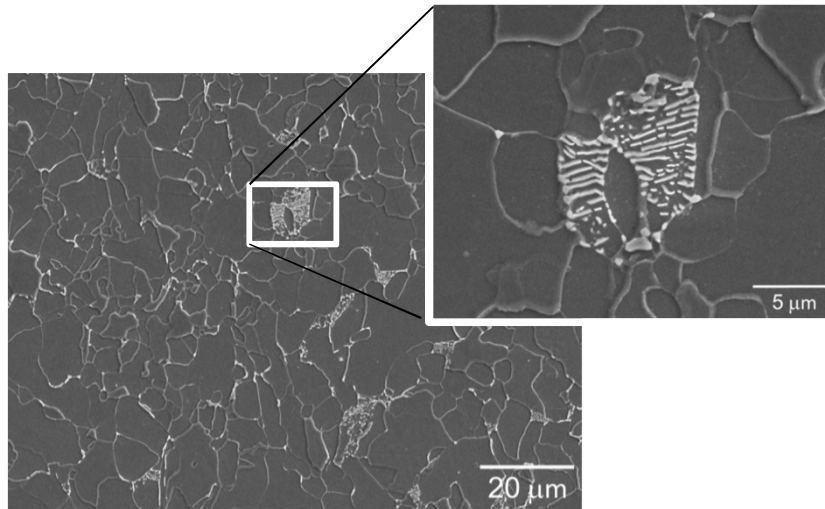
- API 5L X52 steel composition

C	Mn	P	S	Si	Cu	Ni	Cr	V	Nb	Al	CE
0.06	0.87	0.011	0.006	0.12	0.03	0.02	0.03	0.002	0.03	0.034	0.11

- Tensile properties

- Yield strength: 428 MPa
- Ultimate tensile strength: 483 MPa

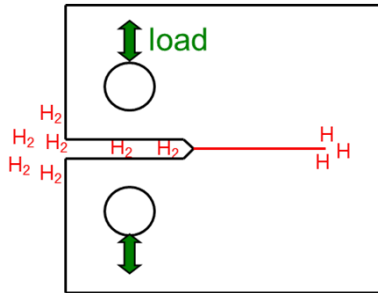
ferrite + 8 vol%
pearlite



324 mm OD x 12.7 mm WT

Measured fatigue crack growth relationships for X52 steel in high-pressure H₂ with controlled O₂ levels

B.P. Somerday et al., *Acta Mater*, 2013



- **Material**

- X52 ERW pipeline steel

- **Instrumentation**

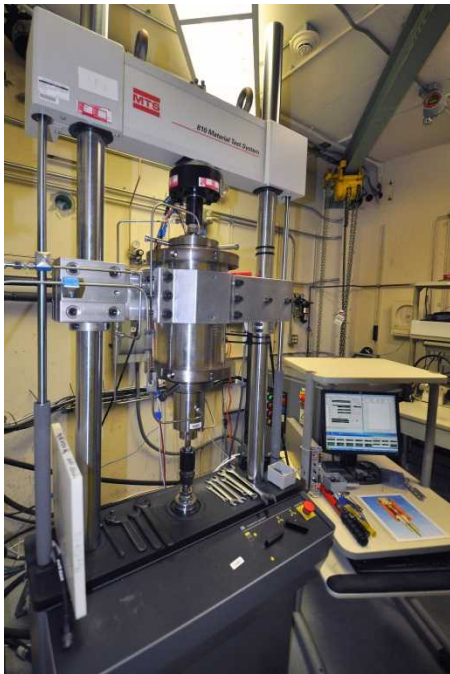
- Internal load cell in feedback loop
- Crack-opening displacement measured internally using LVDT
- Crack length calculated from compliance

- **Mechanical loading**

- Triangular load-cycle waveform
- Constant load amplitude or constant ΔK

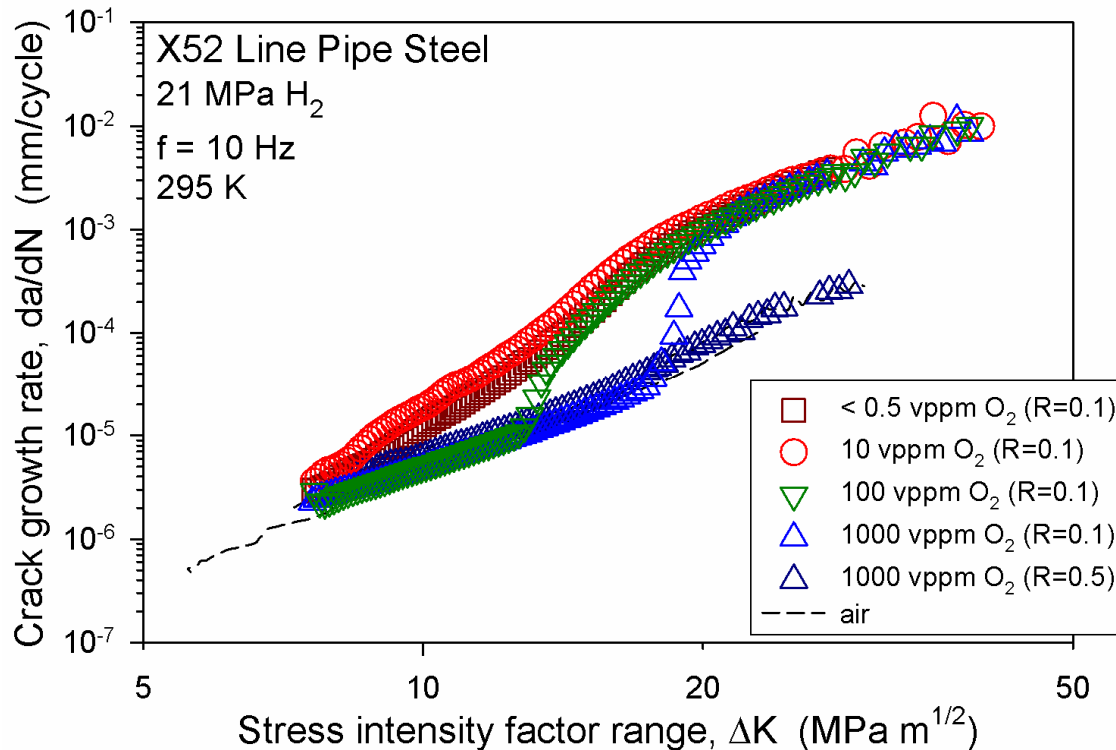
- **Environment**

- Supply gases: 99.9999% H₂
H₂ with 10-1000 vppm O₂
- Pressure = 21 MPa (3,000 psi)
- Room temperature



H₂-accelerated fatigue crack growth not absolutely inhibited by O₂: depends on da/dN and R ratio

B.P. Somerday et al., *Acta Mater*, 2013



- At lower ΔK , crack growth rates in H₂ environments same as rates in air
- At R=0.1, hydrogen-accelerated crack growth observed at higher ΔK
 - da/dN at onset of hydrogen-accelerated crack growth depends on O₂ concentration
- At R=0.5, hydrogen-accelerated crack growth not observed

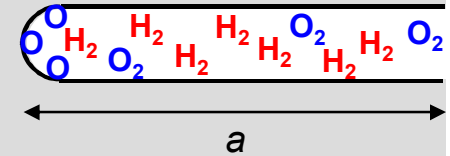
- *Why is da/dN at onset of H₂-accelerated cracking a function of O₂ concentration?*
- *Why does higher R promote inhibition?*

Central physical premise: oxygen adsorption at crack tip can inhibit H uptake

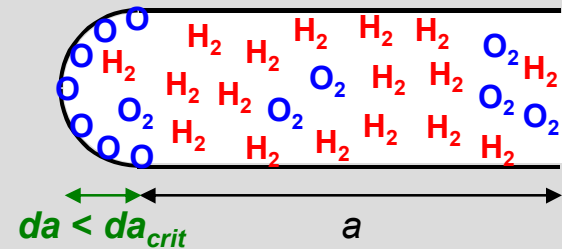
B.P. Somerday et al., *Acta Mater*, 2013

- Initial inert-environment crack growth modeled by blunting-resharpening
- Oxygen out-competes hydrogen for adsorption sites on freshly exposed crack-tip surface
- Extent of oxygen adsorption depends on crack-tip area, proportional to crack-growth increment (da)
 - when $da < da_{crit}$, crack tip *fully passivated* by oxygen
 - when $da > da_{crit}$, crack tip *not fully passivated* → **H uptake**
- Develop model that quantitatively relates adsorbed oxygen (H uptake) to mechanical and environmental variables

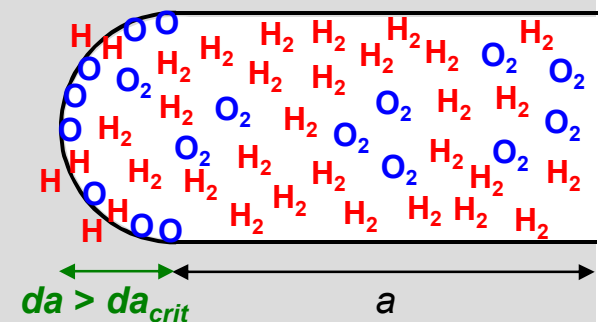
$$K = K_{min}$$



$$K = K_{max1}$$



$$K = K_{max2} > K_{max1}$$



Model developed based on idealized crack geometry and diffusion-limited oxygen adsorption

B.P. Somerday et al., *Acta Mater*, 2013

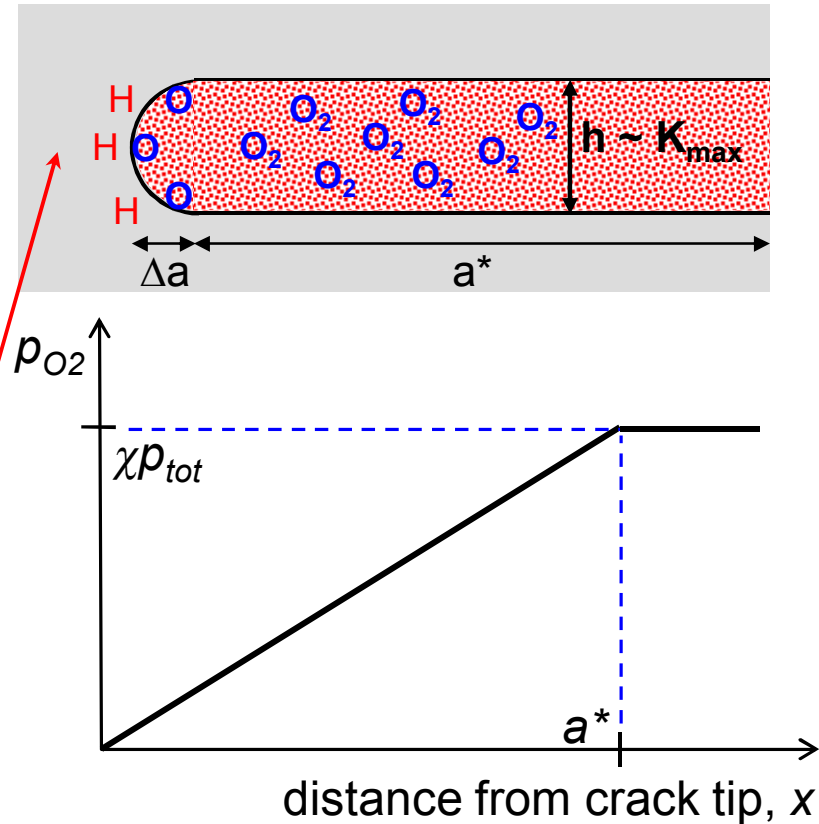
- *Goal*: quantify amount of adsorbed oxygen (n) during load-cycle time (Δt)
- *Key assumption*: **adsorption rate-limited by O_2 diffusion in crack channel**
 - constant crack-channel height (h) during diffusion
 - steady state p_{O_2} profile
- *Model foundation*: oxygen delivered to crack tip ($Jh\Delta t$) = oxygen adsorbed on crack tip ($S\theta\pi\Delta a$)

$$J = \text{flux} = D \frac{\chi p_{tot}}{R_g T a^*}$$

$$h = \text{channel height} = 0.6(1 - \nu^2) \frac{\sigma_0}{E} \left(\frac{\Delta K}{\sigma_0(1 - R)} \right)^2$$

$$\Delta t = 1/f$$

$$\theta = \text{oxygen coverage} \quad S = \text{surface site density}$$



H uptake and accelerated crack growth when $\theta = \theta_{crit}$

$$(\Delta a) f|_{crit} = \frac{0.3 \chi D p_{tot} (1 - \nu^2)}{\pi S \theta_{crit} R_g T E \sigma_0} \left(\frac{\Delta K}{\sqrt{a^*} (1 - R)} \right)^2$$

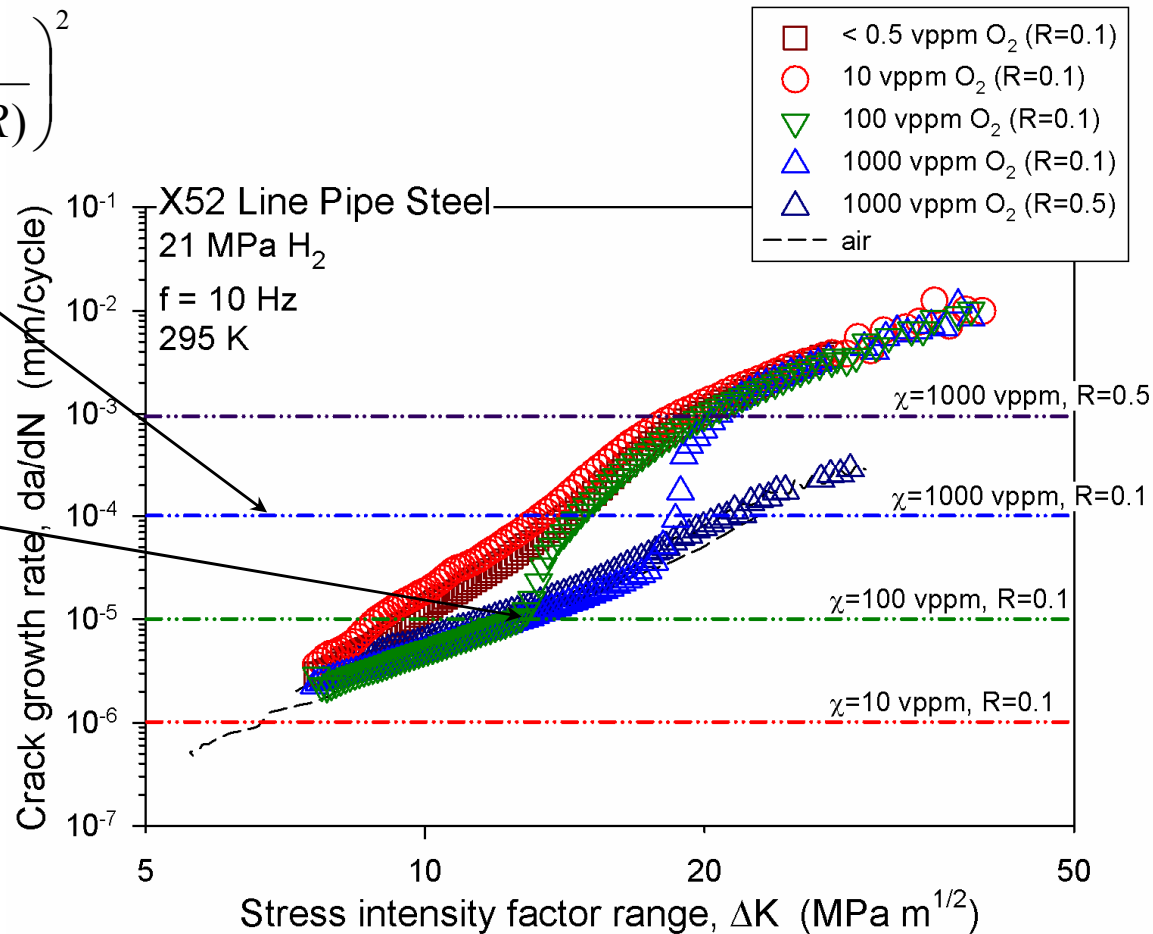
Model predictions consistent with da/dN vs. ΔK data measured in H₂+O₂ gas at R = 0.1 and 0.5

B.P. Somerday et al., *Acta Mater*, 2013

$$\Delta a_{crit} = \frac{0.3 \chi D p_{tot} (1 - \nu^2)}{f \pi S \theta_{crit} R_g T E \sigma_0} \left(\frac{\Delta K}{\sqrt{a^* (1 - R)}} \right)^2$$

assume $\Delta a \sim da/dN$

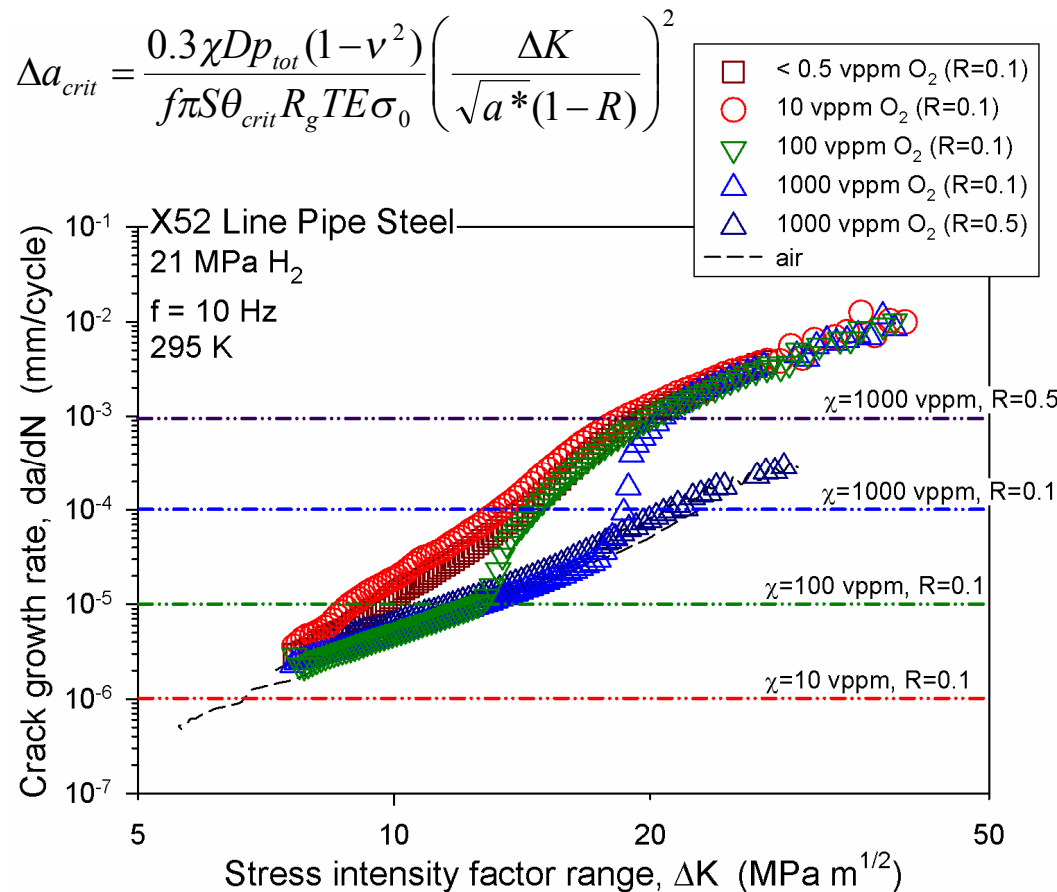
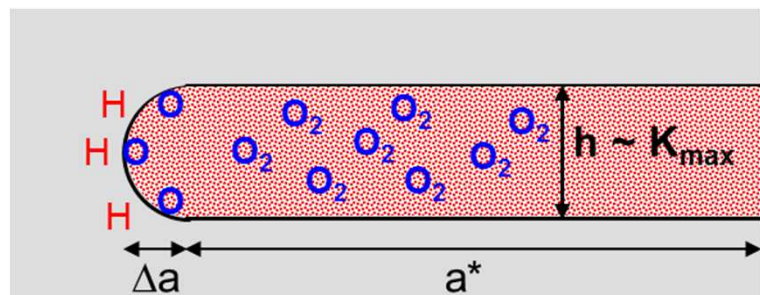
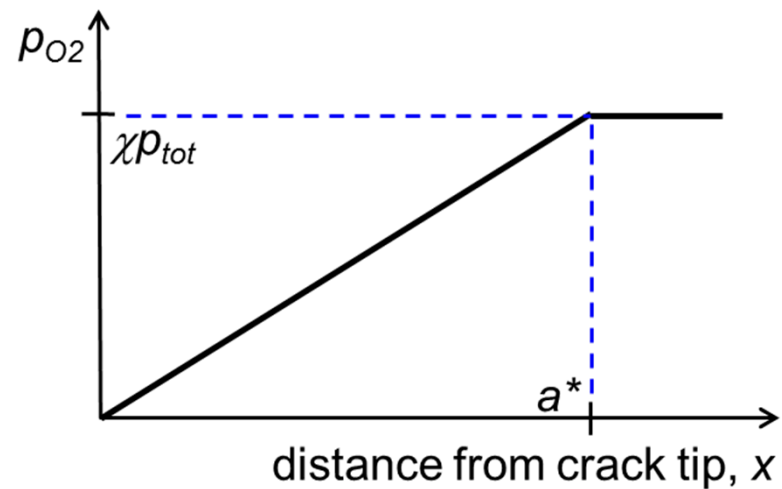
$S \theta_{crit}$ calculated from measured da/dN at onset of accelerated crack growth for H₂+100 vppm O₂



Favorable correlation between measurements and model gives credence to physical assumptions

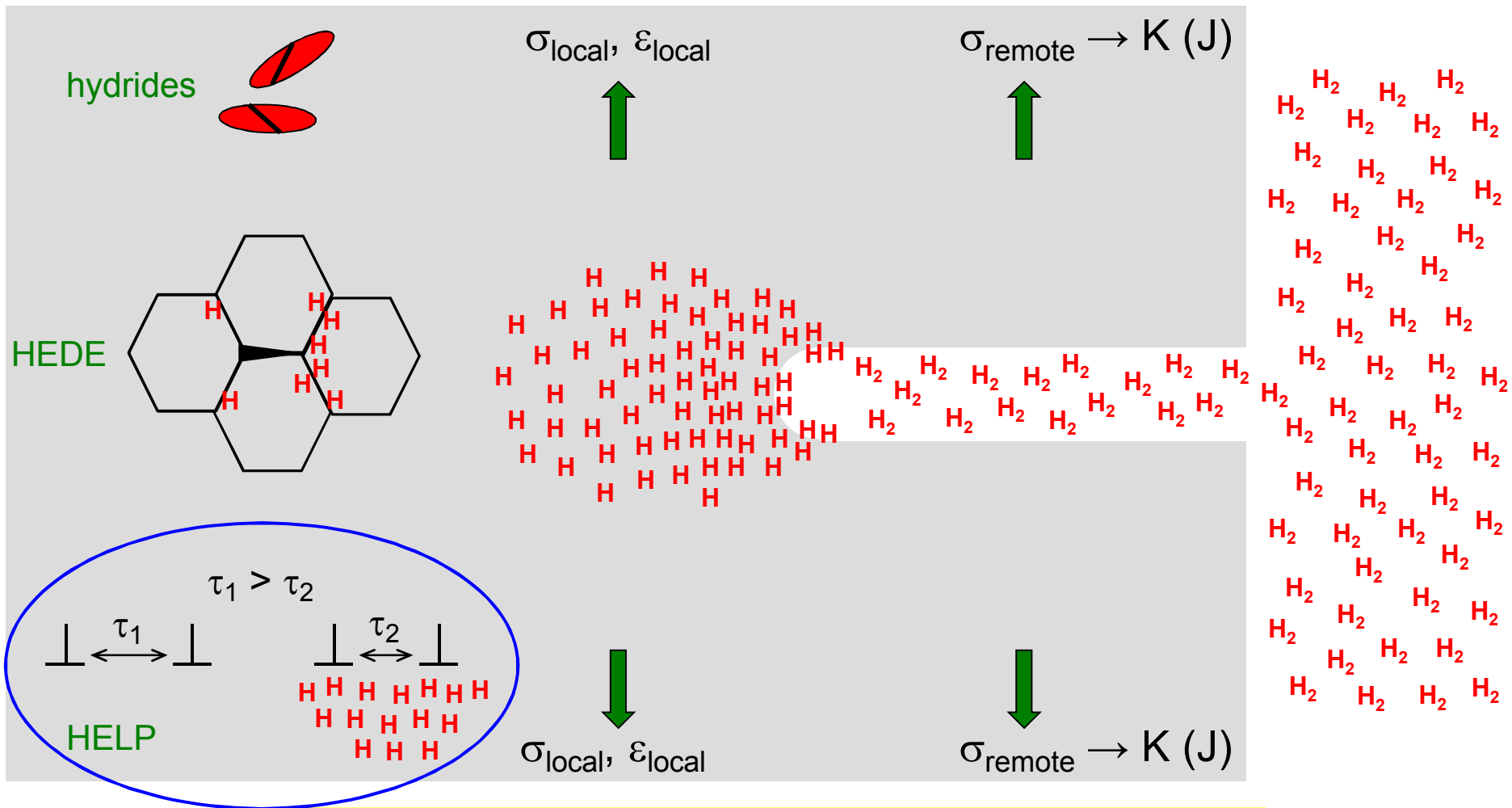
Establishing physical description allows rationalization of O₂ concentration and R ratio effects

- O₂ concentration (χ) → affects gradient in crack channel
- R ratio → affects height of crack channel



H₂-assisted cracking is multi-component phenomenon

Trends may be dominated by one component



Hydrogen-assisted cracking dictated by H-deformation interactions

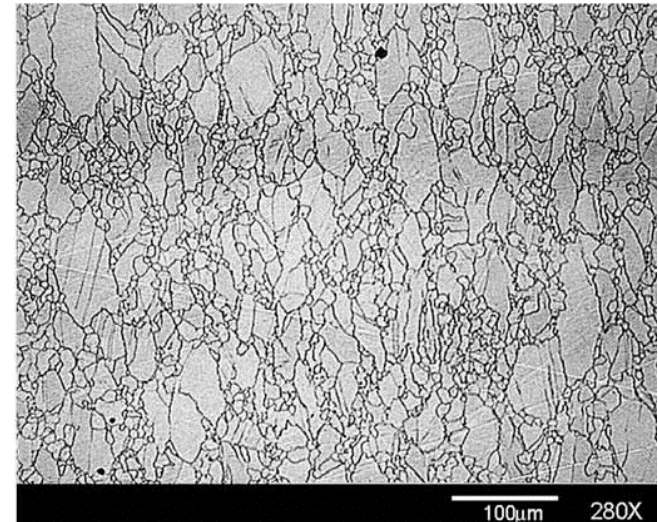
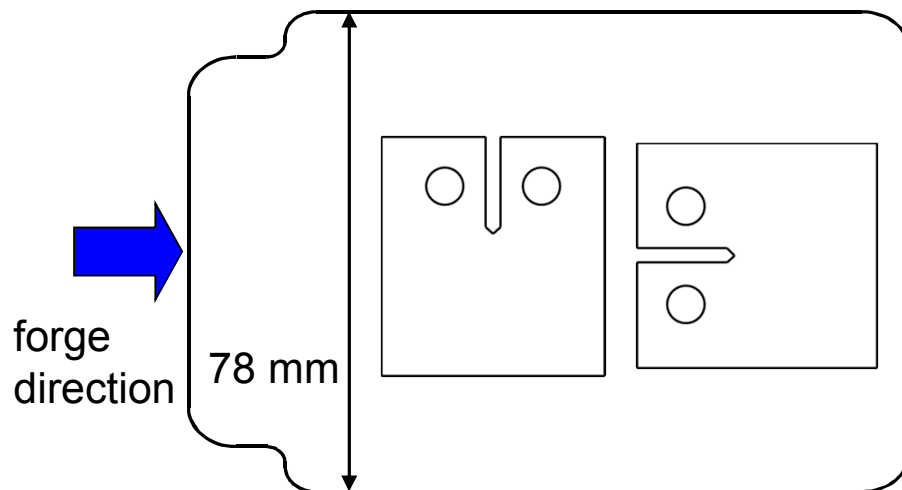
Issue-driven research goal: characterize H-assisted crack extension in stainless steel forgings

K.A. Nibur et al., *Acta Mater*, 2009

- 21Cr-6Ni-9Mn (21-6-9) alloy composition

Cr	Ni	Mn	N	C	Si	P	S	FN
21.0	6.7	8.9	0.23	0.030	0.35	0.020	0.00004	<0.2

- Forged 927 °C + water quenched
 - Yield strength = 656 MPa
 - Ultimate tensile strength = 891 MPa



Measured crack growth resistance curves for H-charged 21-6-9 stainless steel

K.A. Nibur et al., *Acta Mater*, 2009



- **Material**

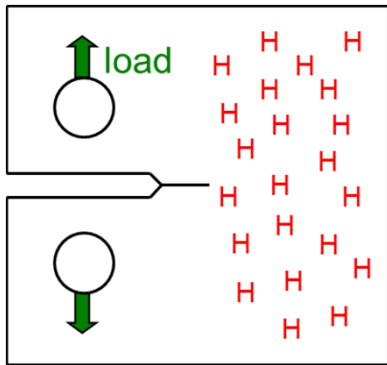
- 21-6-9 austenitic stainless steel

- **Environment**

- Thermal precharging in high-pressure H₂ (99.9999% H₂)
- Pressure = 138 MPa H₂ (20,000 psi)
- Temperature = 300 °C
- Resulting **H concentration** ~ 1.3 at%

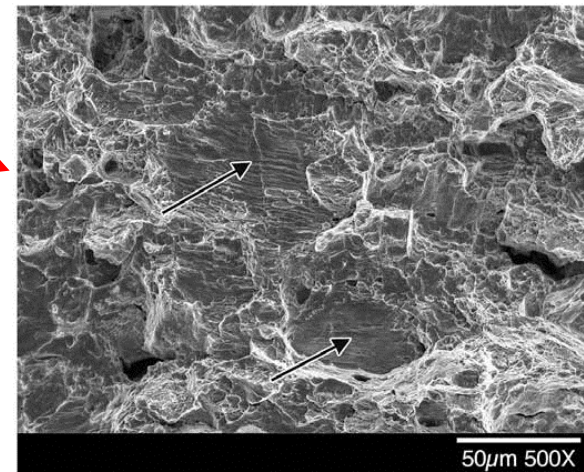
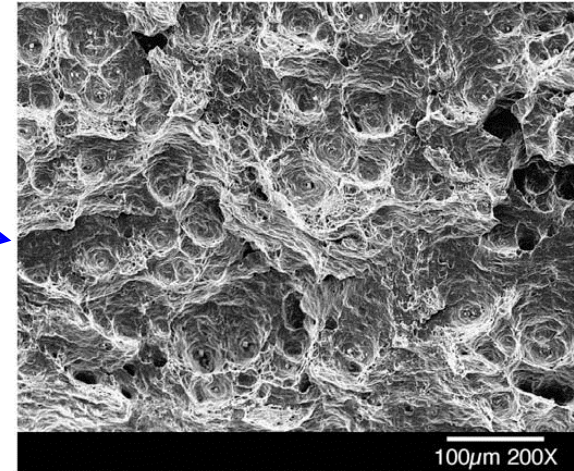
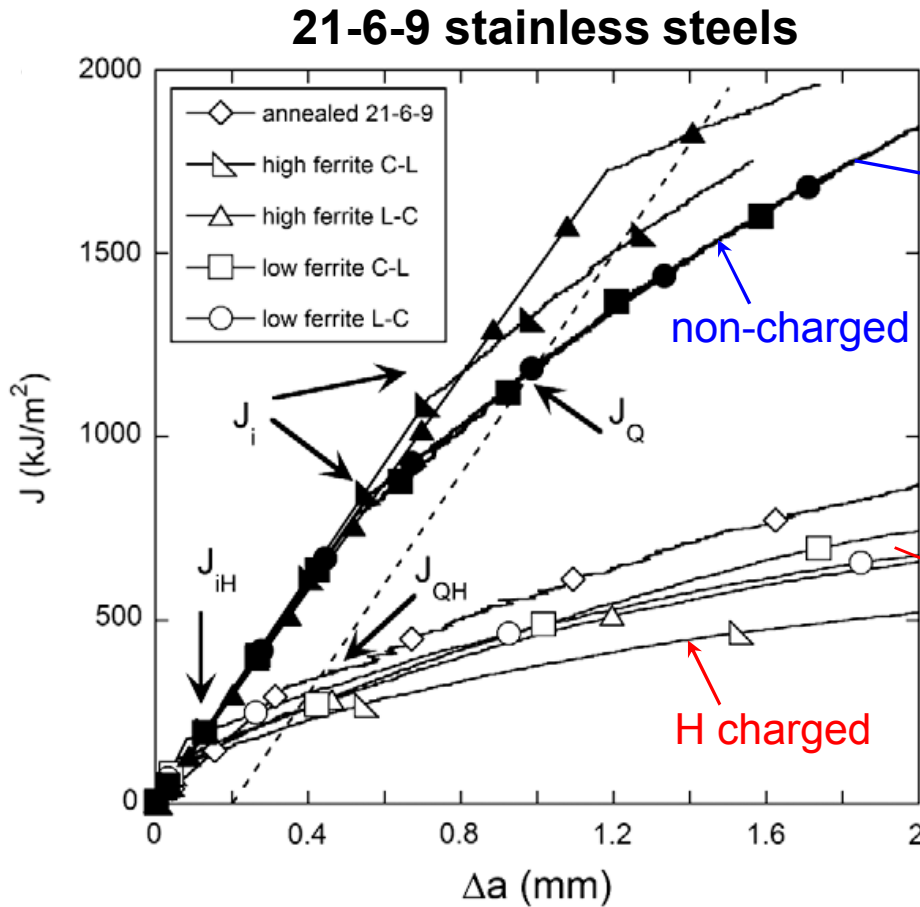
- **Mechanical loading**

- J vs. Δa curves measured under rising displacement in air at 25 °C
- Displacement rate = 0.4 mm/min



Hydrogen degrades crack growth resistance and alters fracture surface features

K.A. Nibur et al., *Acta Mater*, 2009

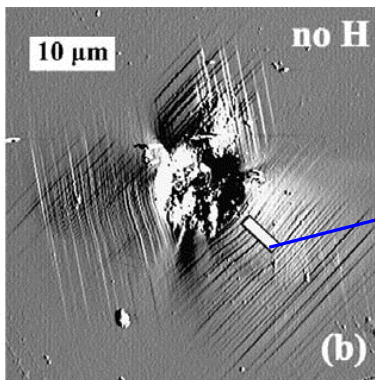
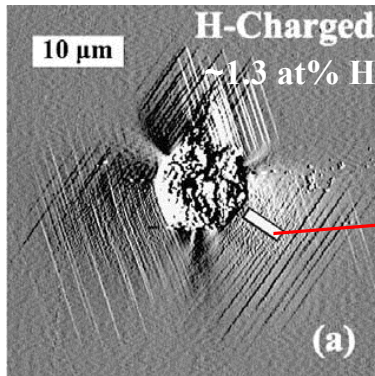


What are H-material interactions and associated damage mechanisms that dictate observed trends?

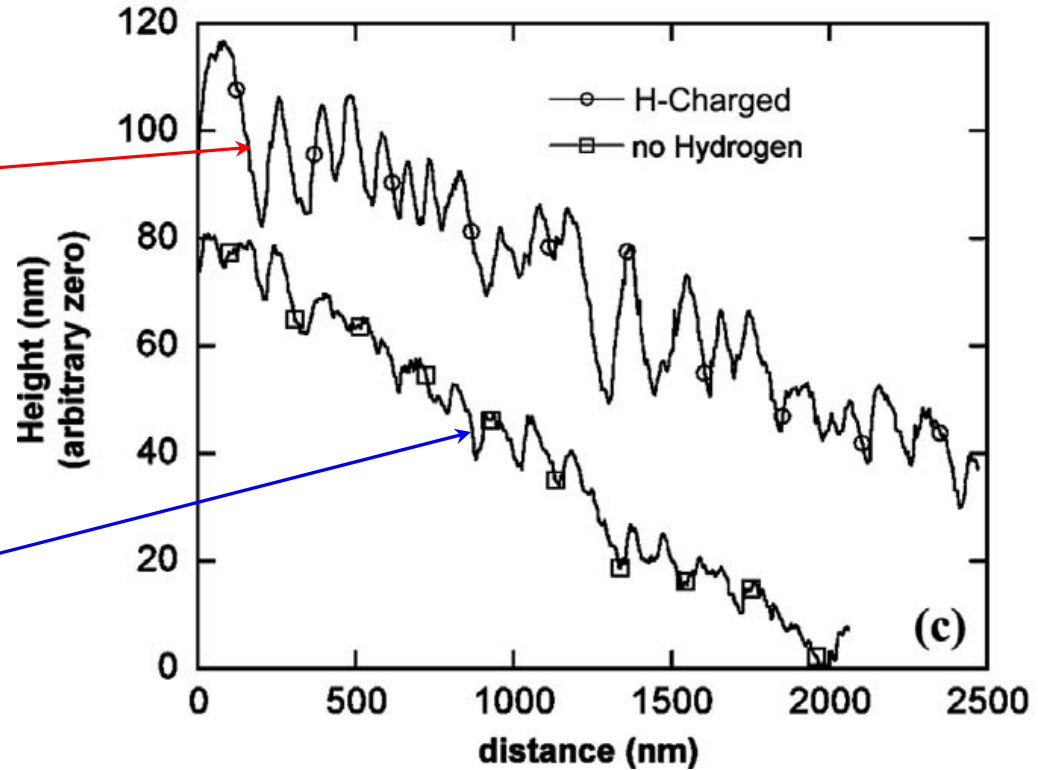
Indentation + AFM show that hydrogen amplifies height of deformation band intersections with surface

K.A. Nibur et al., *Acta Mater*, 2006

21-6-9



Atomic Force Microscopy (AFM) measurements

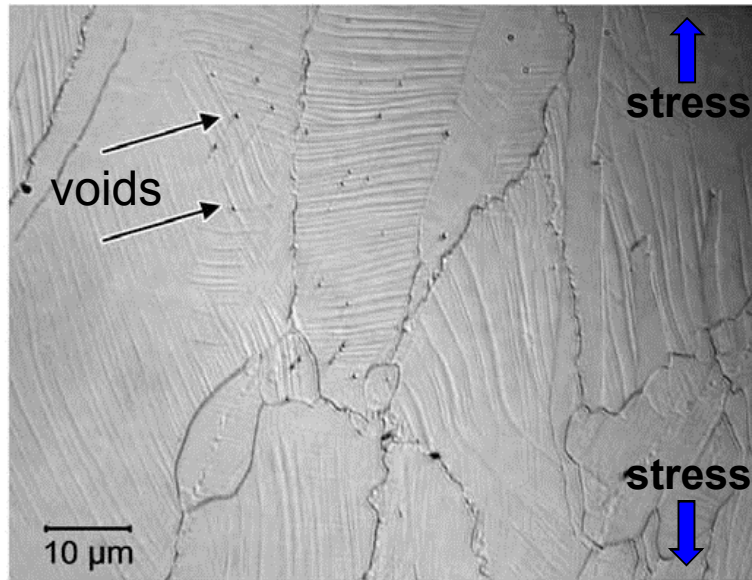


Hydrogen promotes localized deformation in 21-6-9 stainless steel

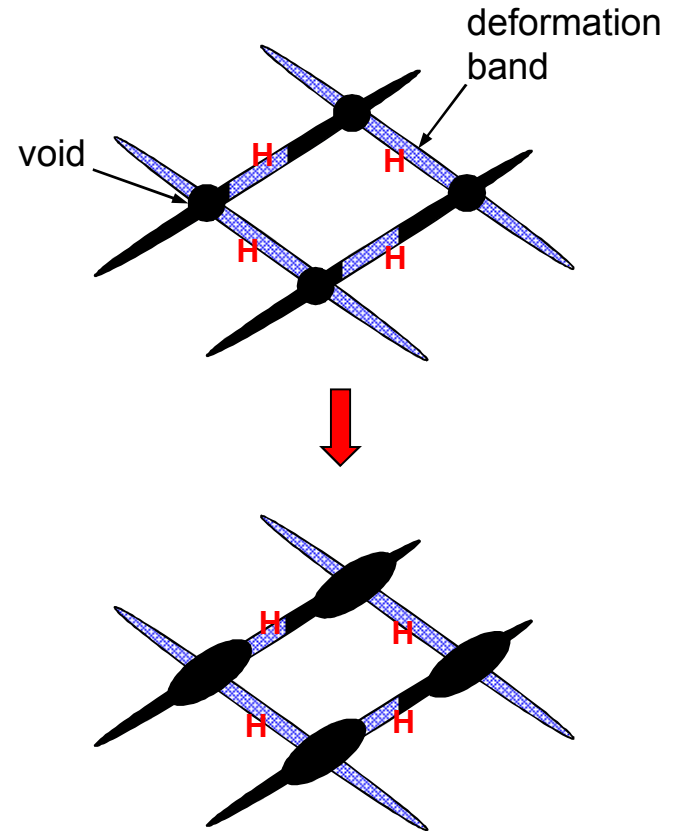
H-induced localized deformation leads to void damage at band intersections

K.A. Nibur et al., *Acta Mater*, 2009

Fracture profile from H-charged 21-6-9



optical image

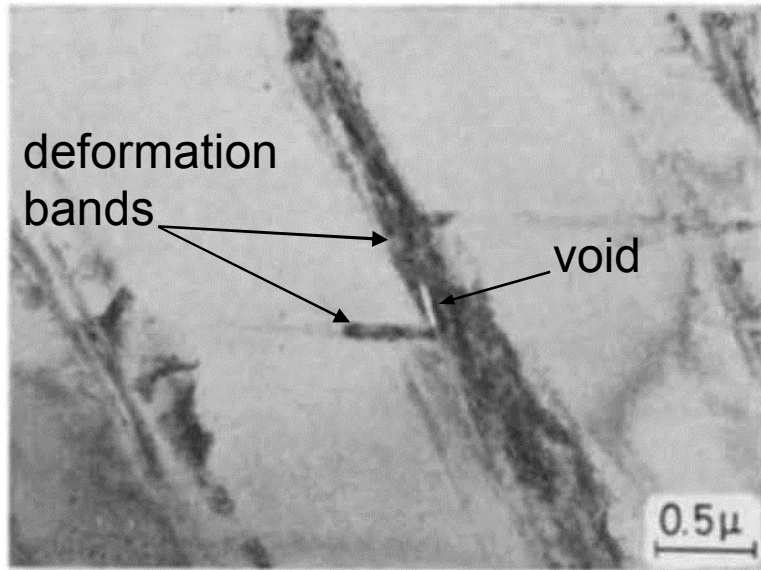


Observations provide concrete link between H-affected deformation and material damage in bulk specimens



Results from other systems demonstrate that localized deformation alone can govern damage

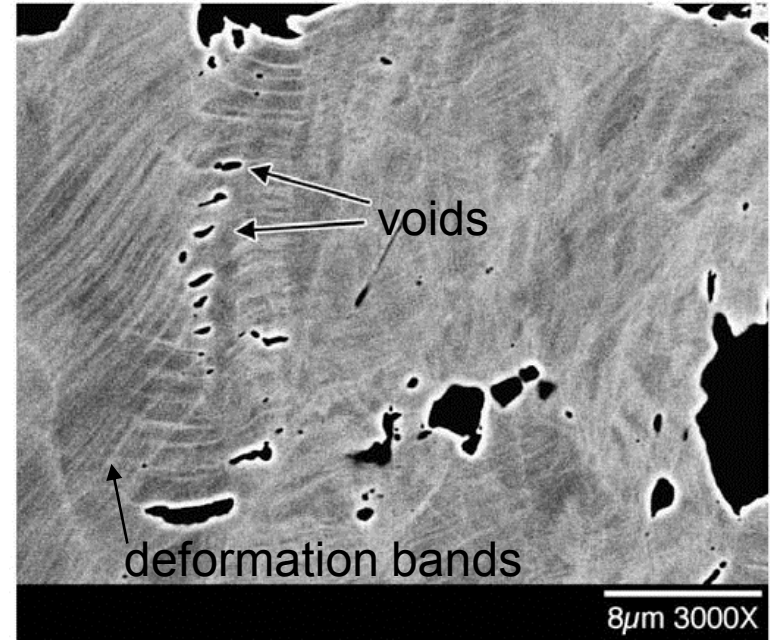
Ti-11 at% Mo (no H)



TEM image

A. Gysler et al., *Acta Metall*, 1974

21-6-9 (H-charged)



BEI image

K.A. Nibur et al., *Acta Mater*, 2009

- *Can H-assisted damage in 21-6-9 be attributed solely to H-induced localized deformation?*
- *Does hydrogen directly lower fracture resistance?*

Gaseous Hydrogen-Assisted Cracking: A Comprehensive View

- H₂-assisted cracking most effectively analyzed by recognizing its multiple components → *inherently multi-disciplinary*
 - Crack-tip strain fields driving hydrogen-induced damage (*solid mechanics*)
 - Gas-surface interactions governing crack-tip hydrogen uptake (*surface science*)
 - Hydrogen-material interactions leading to damage (*materials science*)
- Conclusions from three research stories:
 - Strain-controlled fracture criterion coupled with strain field amplitude explains difference between H₂-assisted cracking thresholds
 - Model based on diffusion-limited oxygen adsorption quantifies effect of mechanical and environmental variables on H₂-accelerated cracking
 - H-affected deformation may have direct link to material damage in bulk specimens

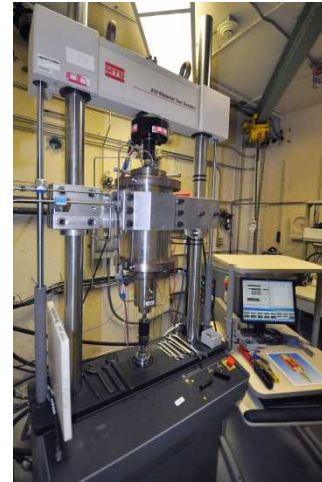
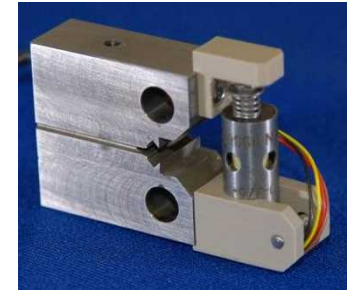
Acknowledgments

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 - Prof. Alex Staykov (Kyushu University)
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Back-up Slides

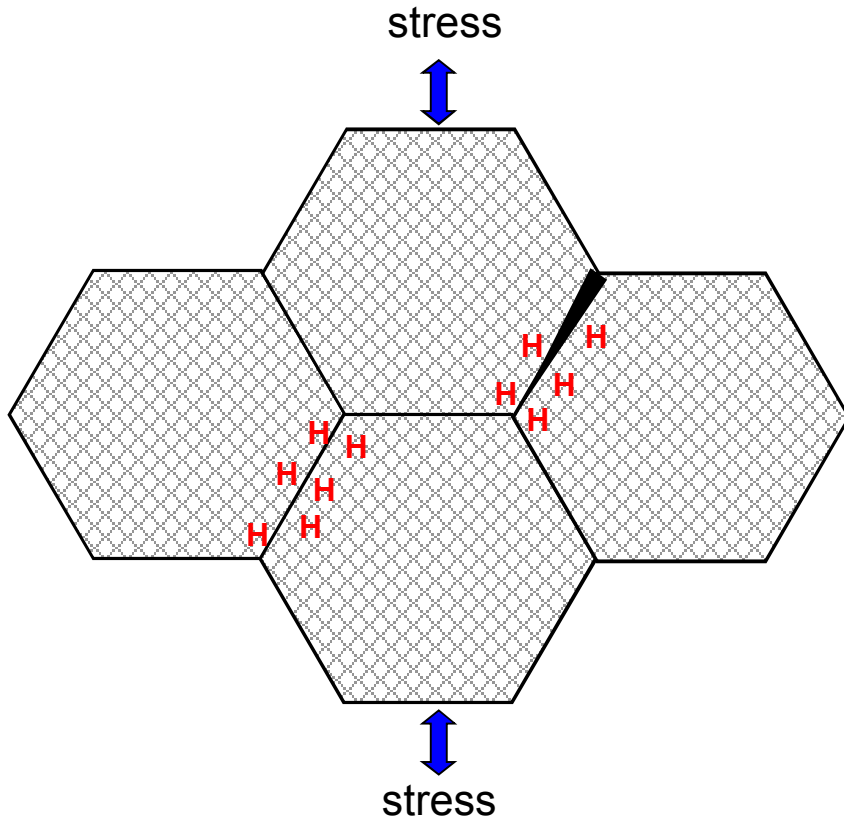
SNL core capability in hydrogen embrittlement features Hydrogen Effects on Materials Lab

- Static-loading crack-growth system
 - Wedge opening load (WOL) and double cantilever beam (DCB) specimens
 - H₂ pressure up to 200 MPa
 - Temperature -70 to 170 °C
- Dynamic-loading crack-growth system
 - Compact tension (CT) and single edge notch (SEN) specimens
 - H₂ pressure up to 138 MPa
 - New pressure vessel design with target temperatures -100 to 200 °C

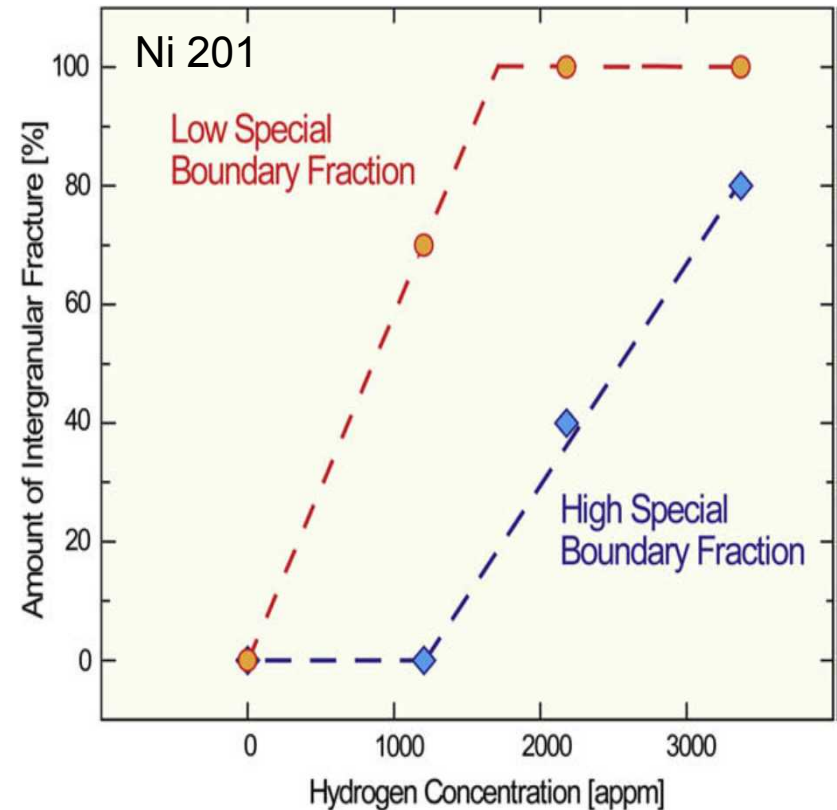


Materials testing in H₂ supports technology development in several mission areas

Grain-boundary structure affects susceptibility to H-induced intergranular cracking

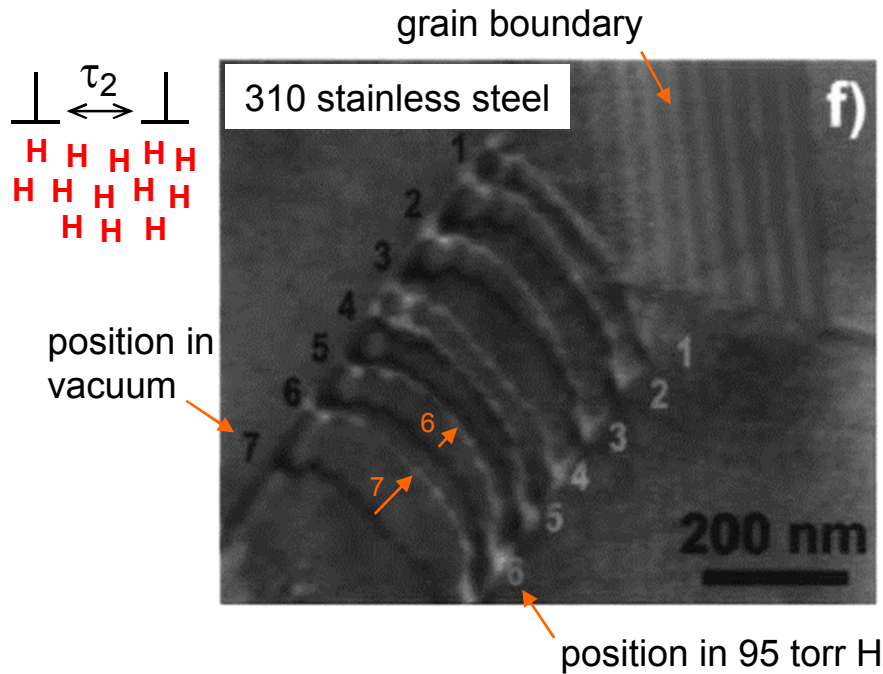


S. Bechtle, et al., *Acta Mater*, 2009



- Special (i.e., CSL) boundaries less susceptible to H-induced cracking than random boundaries

Hydrogen-enhanced localized plasticity (HELP) conclusively demonstrated for numerous metals



I. Robertson, *Eng Fract Mech*, 2001

- Enhanced dislocation mobility (softening) and stress shielding concept demonstrated through *in situ* TEM experiments
- Other observations:
 - H stabilizes edge component of mixed dislocations
 - H promotes localized deformation

Unresolved issue: “What is the detailed mechanism by which the enhanced dislocation mobility causes fracture in *bulk* specimens?” H. Birnbaum, *CDI 96*, 1997

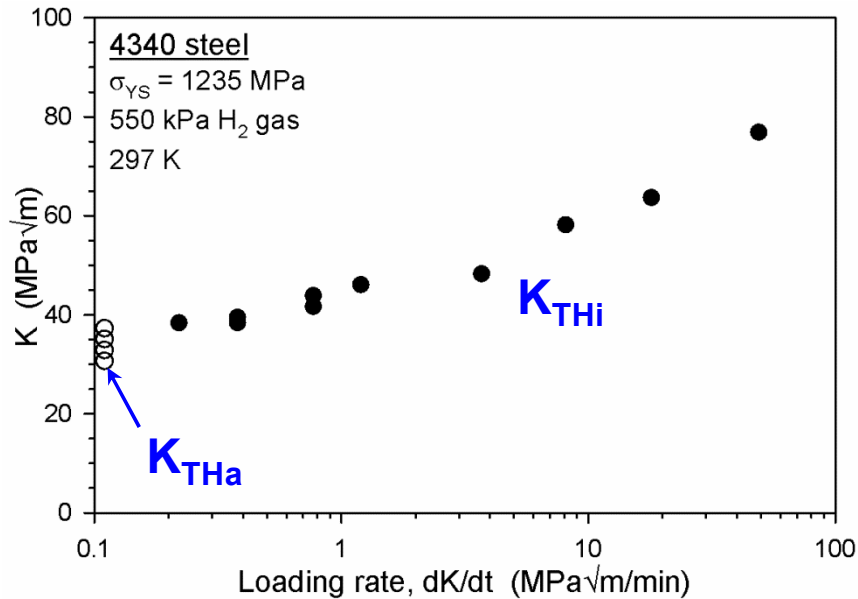
Yield strength and alloy composition of martensitic pressure vessel steels

Table I. Yield Strength and Composition of the Pressure Vessel Steels

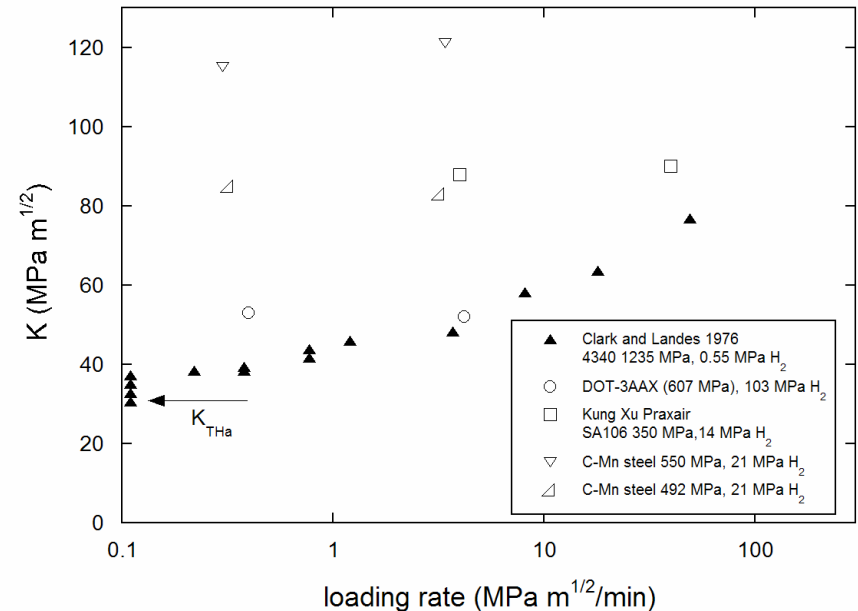
Alloy	Yield Strength (MPa)	C	Cr	Cu	Mo	Ni	Al	Mn	Si	P	S	Fe
4130X	607	0.29	0.92	nr	0.19	nr	0.035	0.62	0.28	0.008	0.004	bal
4130X	641	0.30	0.95	nr	0.18	nr	0.030	0.63	0.28	0.008	0.005	bal
SA372 grade <i>J</i>	641	0.46	0.94	nr	0.18	nr	nr	0.92	0.25	0.011	0.006	bal
SA372 grade <i>J</i>	717	0.48	0.96	nr	0.18	nr	0.026	0.92	0.30	0.010	0.002	bal
SA372 grade <i>J</i>	730	0.48	1.01	nr	0.19	nr	nr	0.98	0.27	0.013	0.005	bal
SA372 grade <i>J</i>	736	0.47	0.96	nr	0.19	nr	0.032	0.92	0.30	0.012	0.003	bal
SA372 grade <i>J</i>	783	0.49	0.99	nr	0.18	nr	nr	0.93	0.28	0.008	0.004	bal
SA372 grade <i>L</i>	731	0.4	0.82	0.1	0.26	1.93	0.022	0.75	0.28	0.006	0.007	bal
SA372 grade <i>L</i>	1053	0.4	0.82	0.1	0.26	1.93	0.022	0.75	0.28	0.006	0.007	bal
DOT-3T	900 <i>A</i>	0.45	0.97	nr	0.18	nr	0.034	0.86	0.25	0.013	0.006	bal
DOT-3T	900 <i>B</i>	0.44	0.99	nr	0.18	nr	0.031	0.85	0.26	0.007	0.003	bal

nr = not reported.

K_{THi} reaches lower bound as loading rate decreases



Clark and Landes, ASTM STP 610, 1976



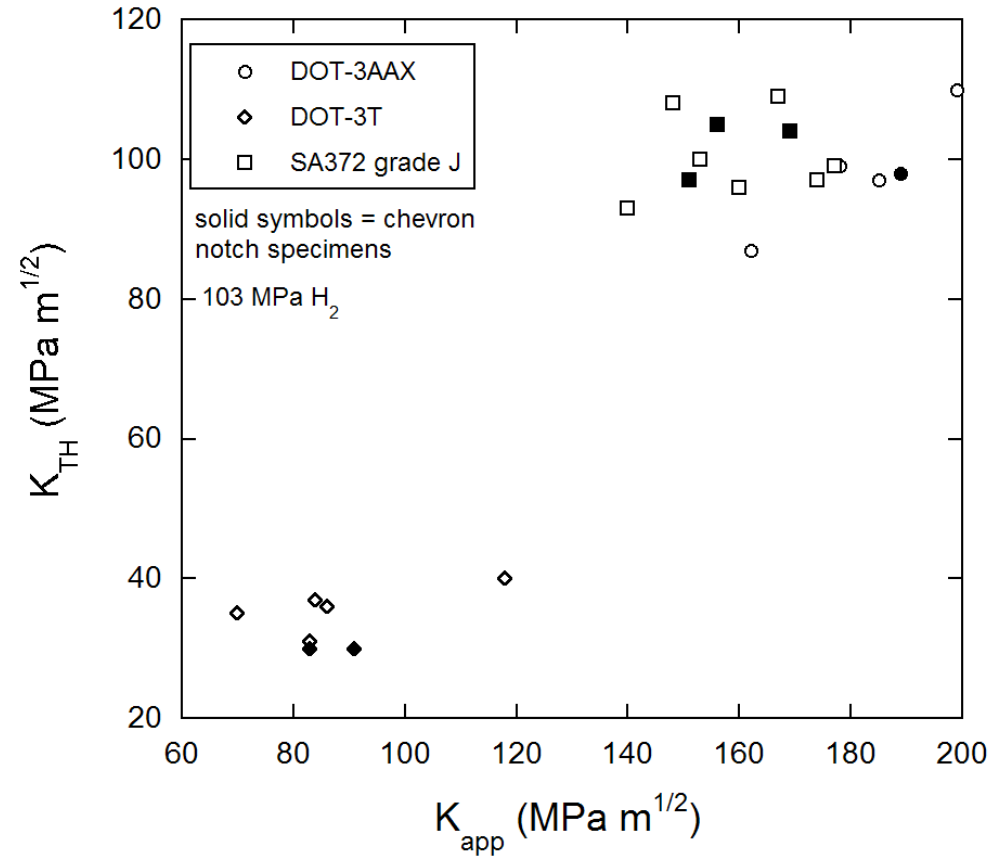
K.A. Nibur et al., SAND2010-4633, 2010

Higher K_{THa} compared to K_{THi} not attributed to crack arrest near back face in conventional WOL

Conventional WOL specimen



Chevron-notched WOL specimen

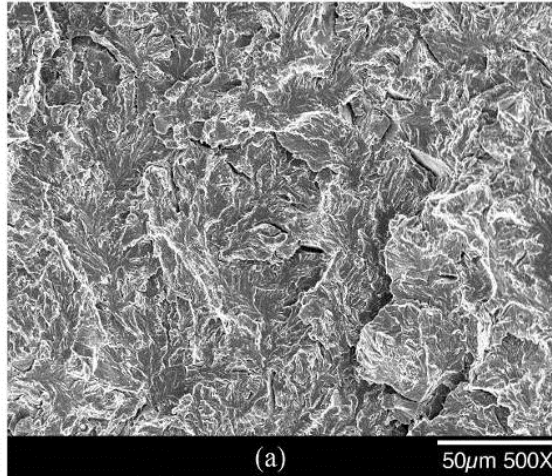


• Chevron-notched WOL specimen

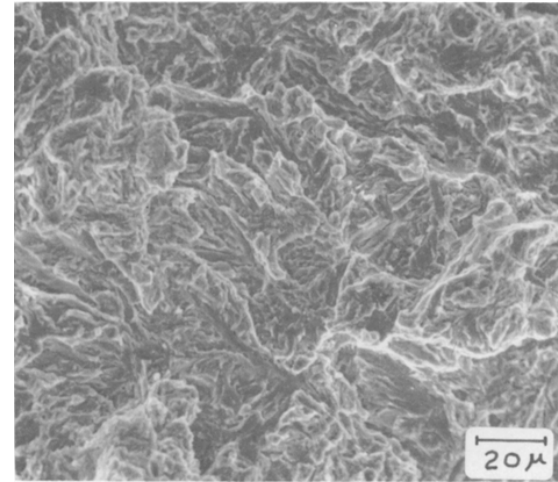
- Reduced compliance leads to lower initial loads
- Lower initial loads allow shorter precracks, which limit final crack length at K_{THa}

Plasticity-related hydrogen-induced cracking assumed for martensitic pressure vessel steels

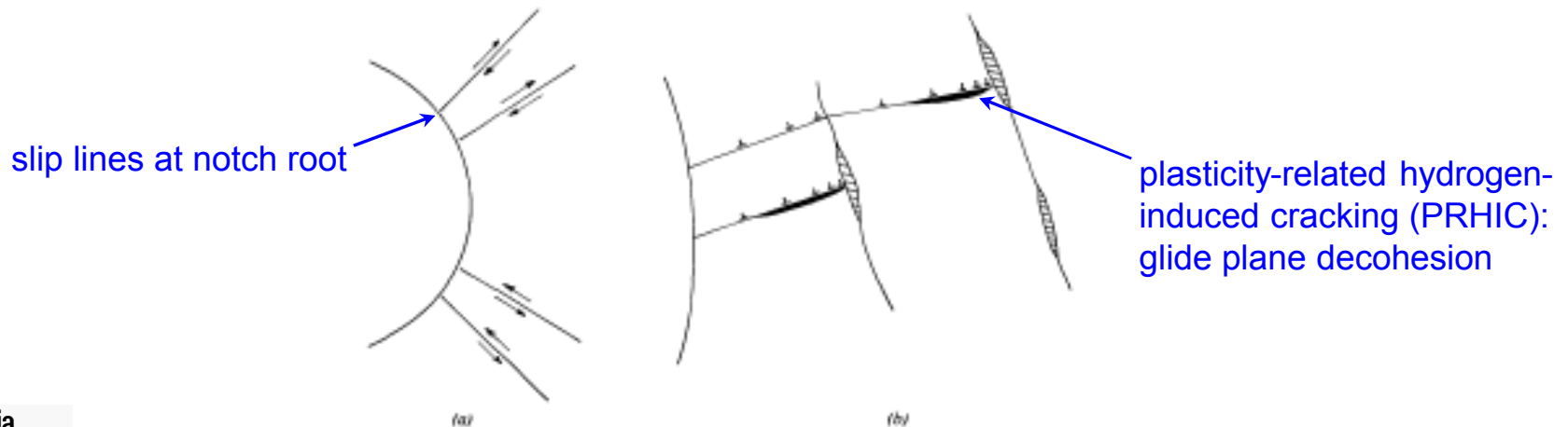
4130X
100 MPa H₂ gas



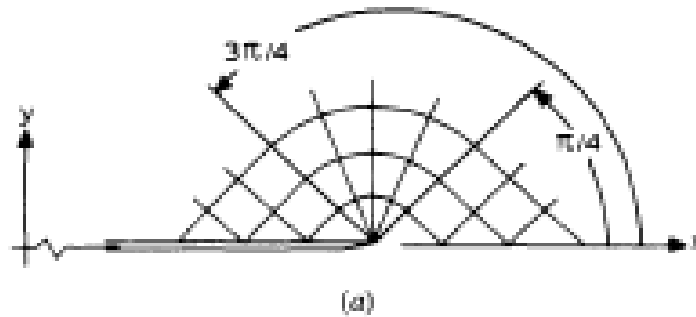
HY 130-type
0.2 MPa H₂ gas



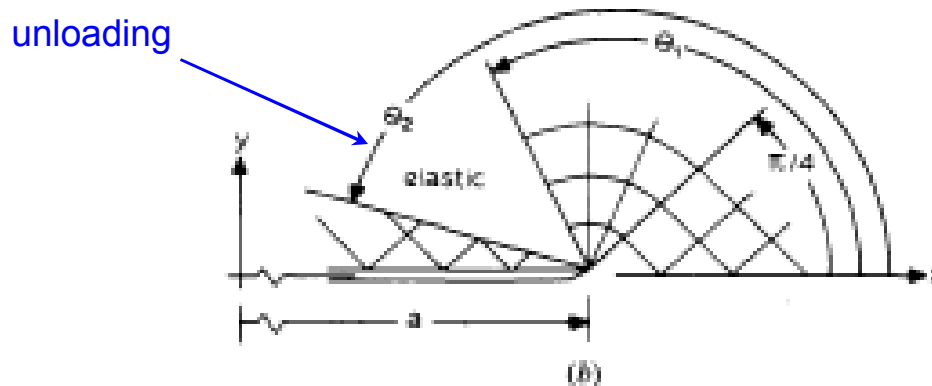
Takeda and McMahon, *Metall Trans A*, 1981



Elastic unloading behind crack tip leads to distinct strain field for propagating crack vs. stationary crack



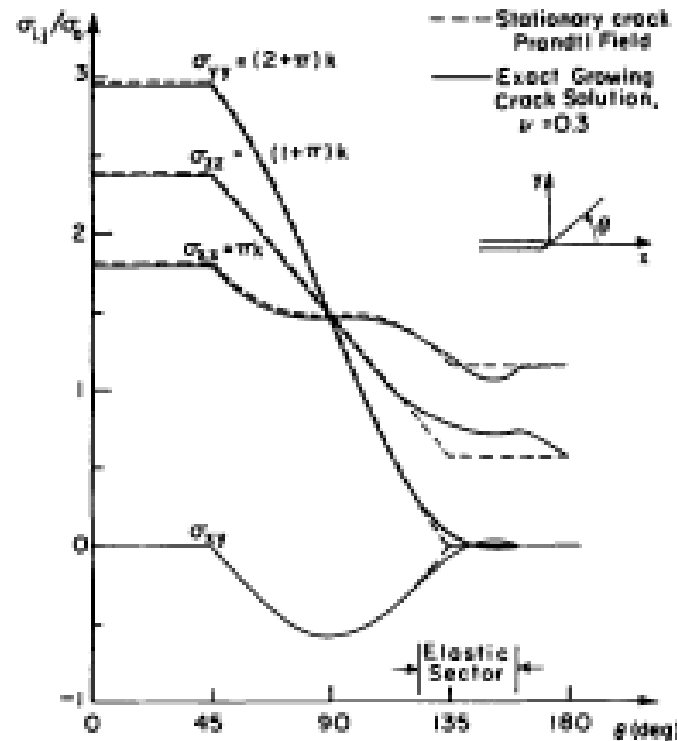
stationary crack



propagating crack

Plane strain slip-line representation of crack tip stress states of Prandtl field for stationary crack and propagating crack

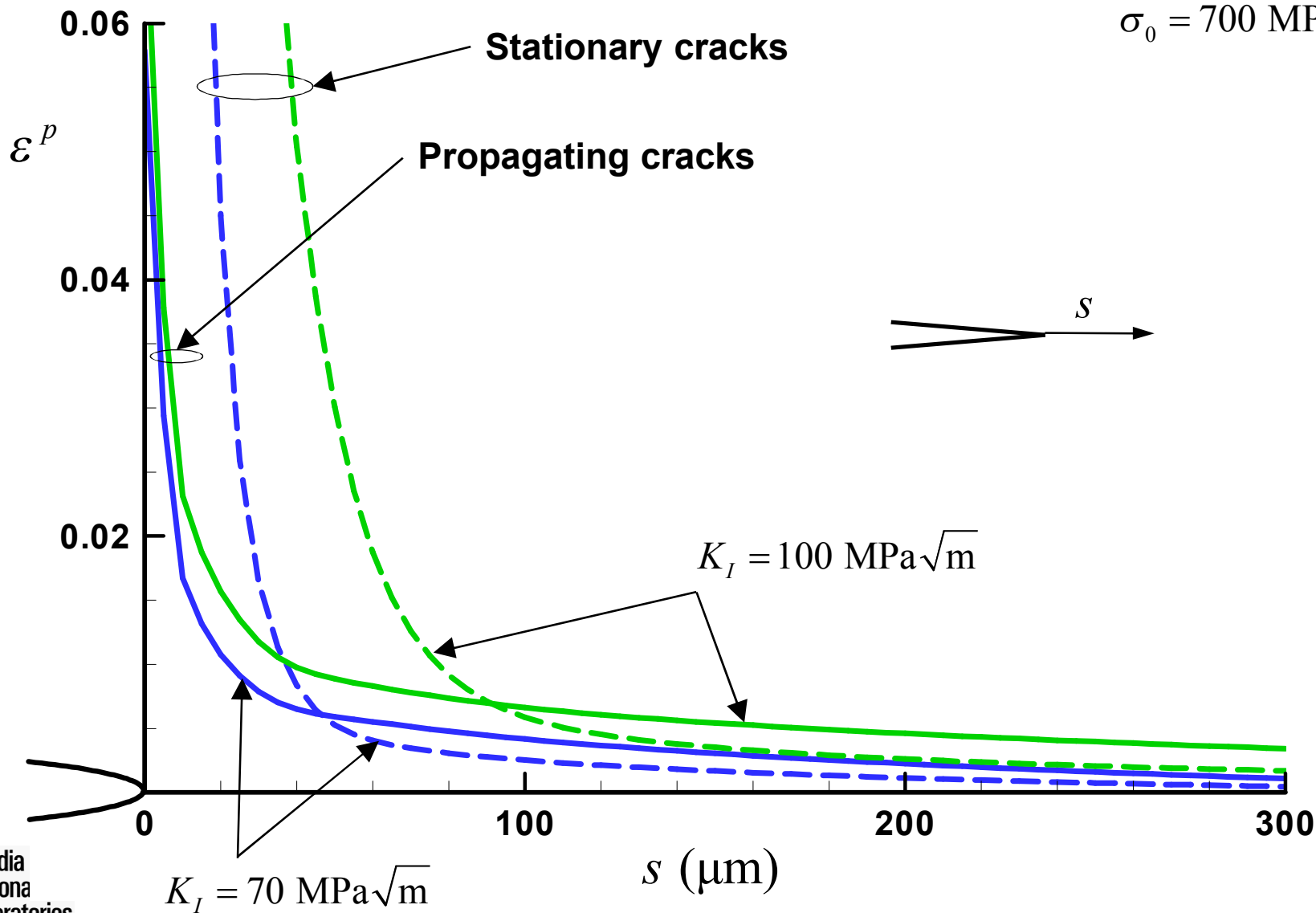
Stress fields near crack tip similar for stationary and propagating cracks



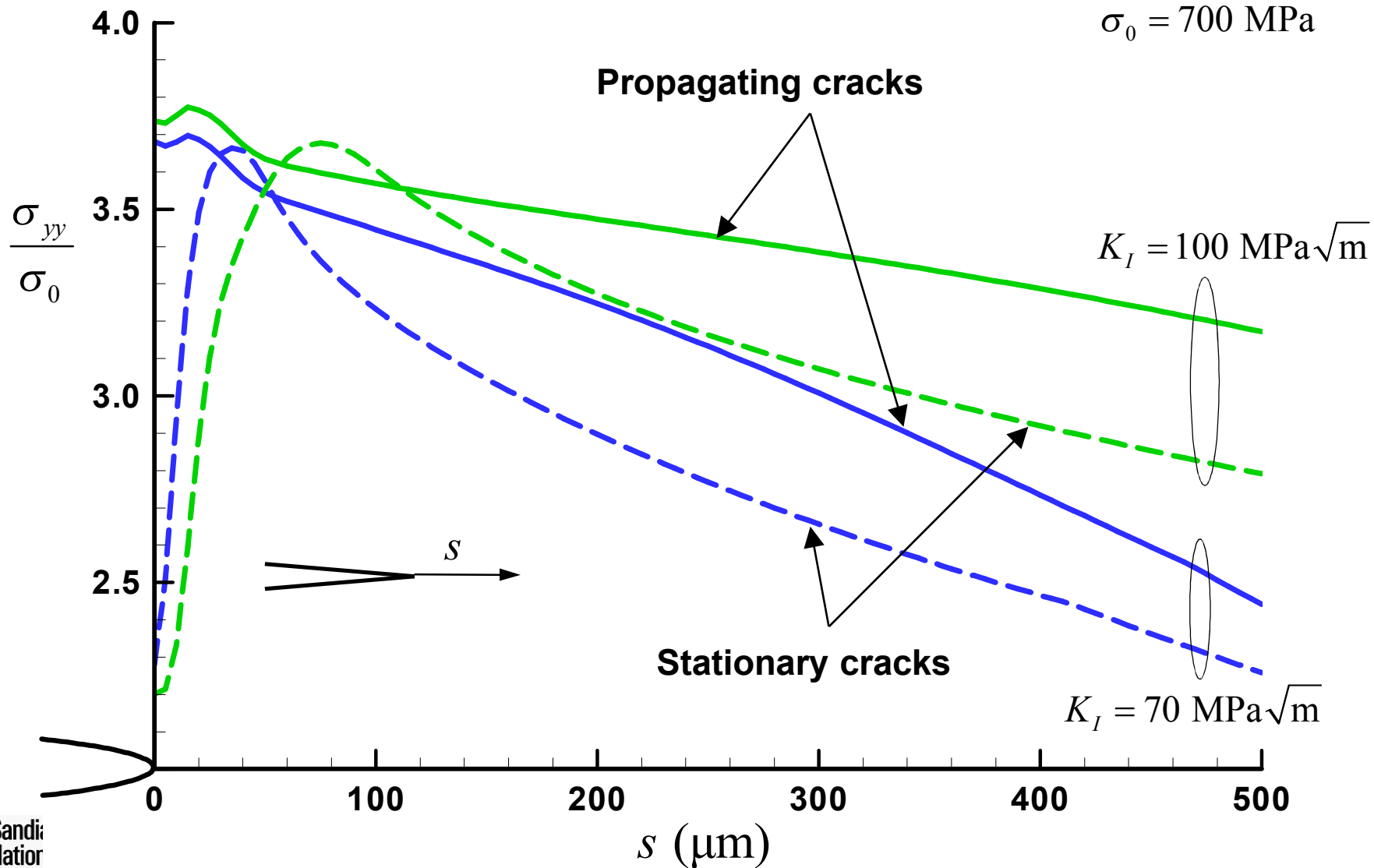
Local stresses ahead of crack tip as a function of angle θ for stationary crack and propagating crack

FEM simulations of plastic strain ahead of propagating and stationary cracks

$\sigma_0 = 700 \text{ MPa}$

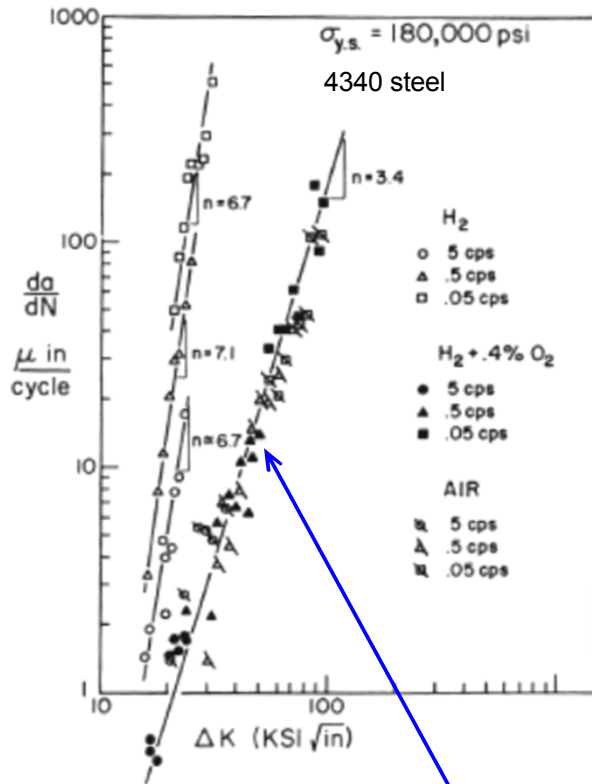


FEM simulations of opening stress ahead of propagating and stationary cracks

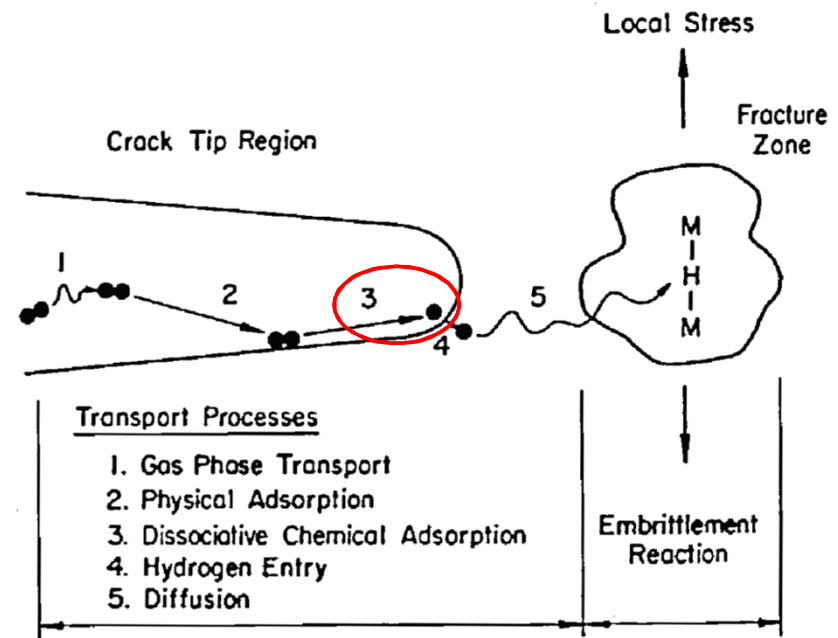


Gas constituents such as O₂ can inhibit H₂-accelerated fatigue cracking in steels

H. Johnson, *Stress Corrosion Cracking and Hydrogen Embrittlement of Iron Based Alloys*, 1977



R. Wei and R. Gangloff, *ASTM STP 1020*, 1989

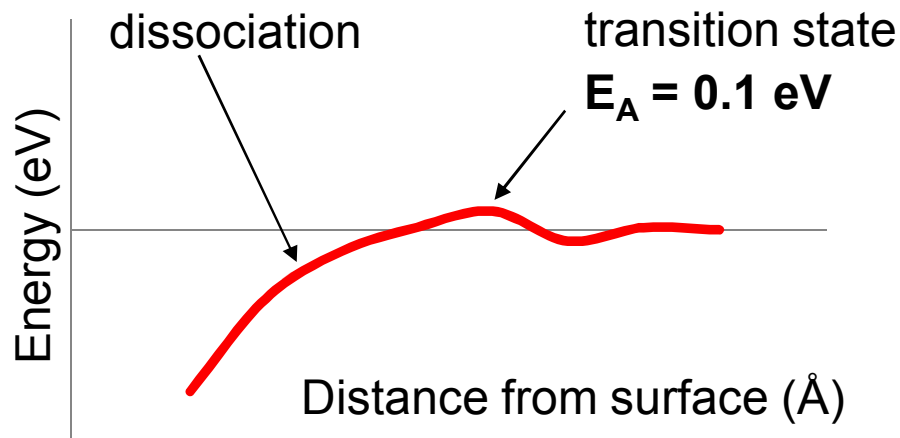
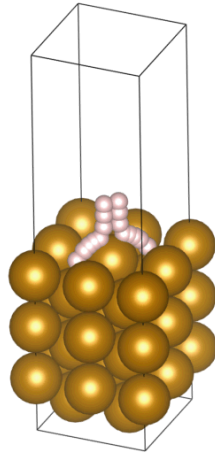


How is O₂ inhibition affected by variables such as ΔK , frequency, R ratio, and O₂ content?

Density functional theory (DFT) simulations suggest mechanism for O₂ inhibition of H uptake

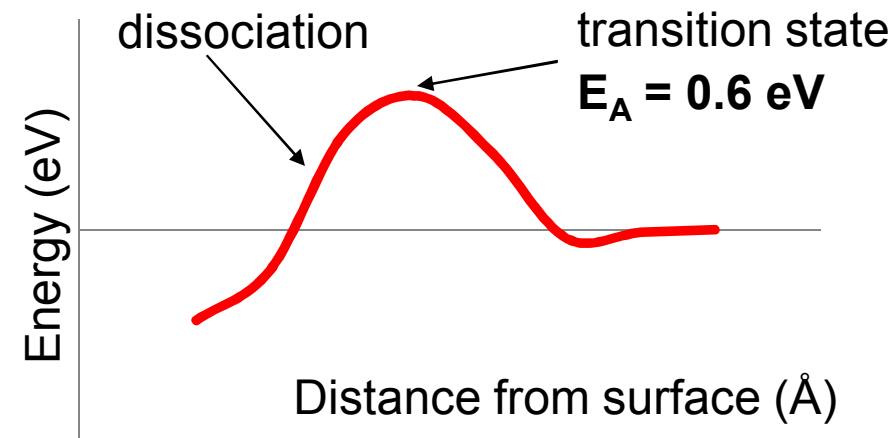
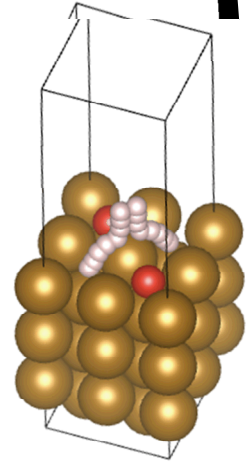
Potential energy surface scan for H₂ approaching Fe(100) surface

H₂ molecule approaches directly on top Fe atom



Potential energy surface scan for H₂ approaching Fe(100) surface with preadsorbed O atoms

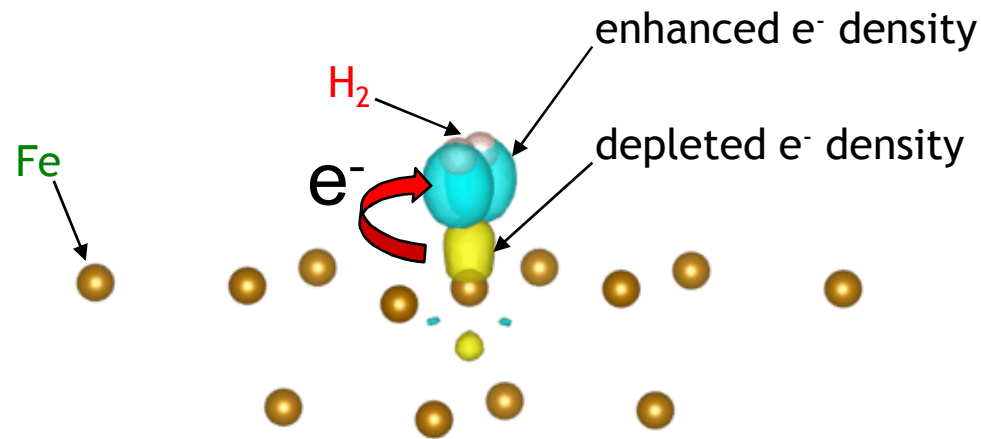
H₂ molecule approaches directly on top Fe atom



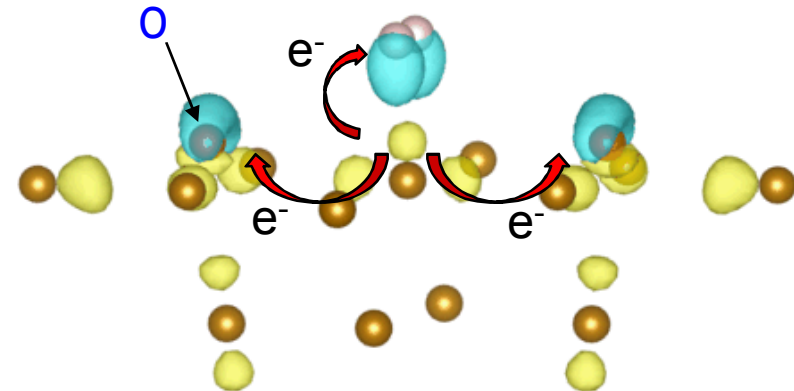
Preadsorbed oxygen on iron surface raises activation energy for H₂ dissociation

Electron density difference method provides insight into dissociation inhibition mechanism

H_2 approaching Fe(100) surface



H_2 approaching Fe(100) surface with preadsorbed O atoms

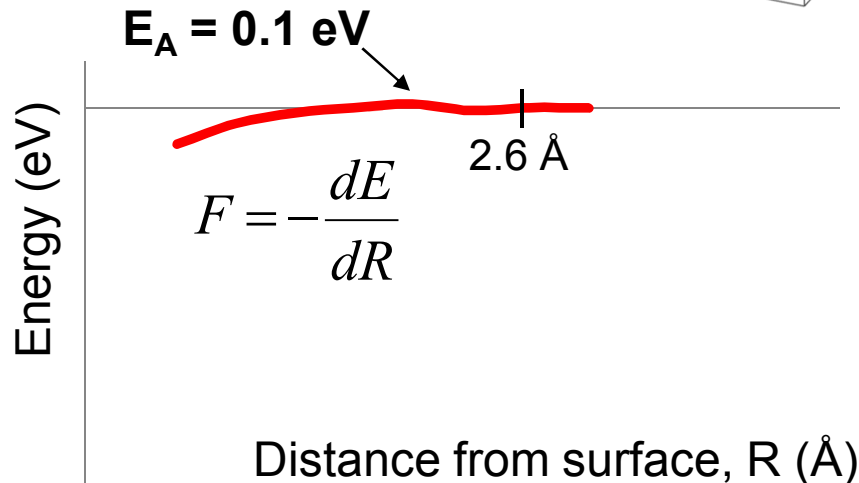
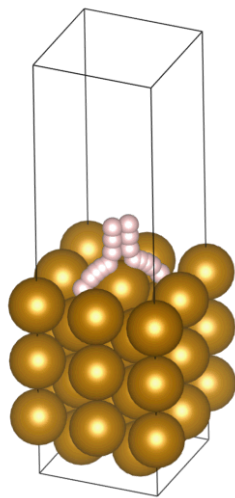


- *Oxygen atoms on surface localize e^- density, reducing ability of neighboring Fe atoms to donate e^- to H_2*
- *Less e^- density available for H_2 activation: dissociation hindered*

DFT simulations provide rationale for preferential adsorption of O_2 in mixed H_2+O_2 gas

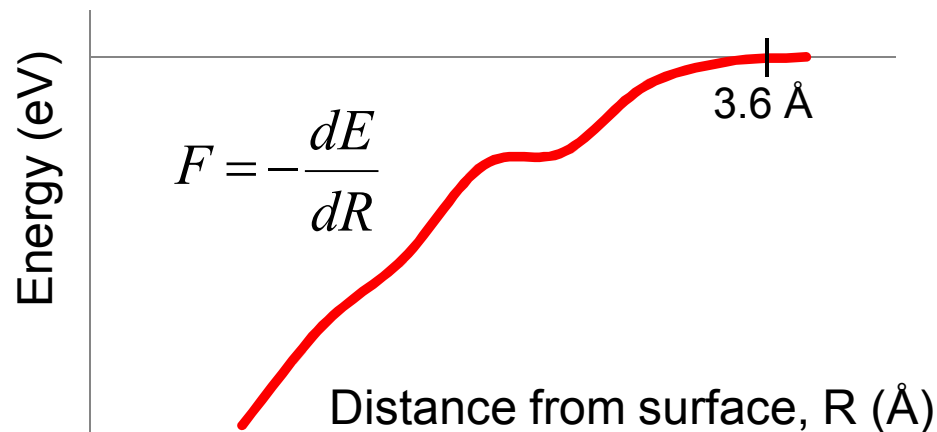
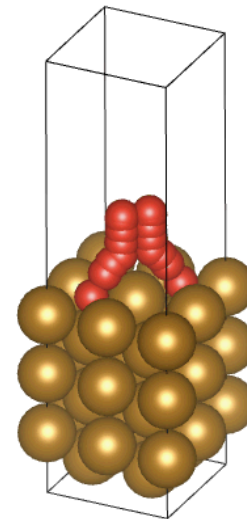
Potential energy surface scan for H_2 approaching Fe(100) surface

- H_2 is detected at 2.6 Å
- Weak attractive force
- Activation barrier: not all H_2 molecules dissociate



Potential energy surface scan for O_2 approaching Fe(100) surface

- O_2 is detected at 3.6 Å
- Strong attractive force
- No activation barrier: all O_2 molecules dissociate

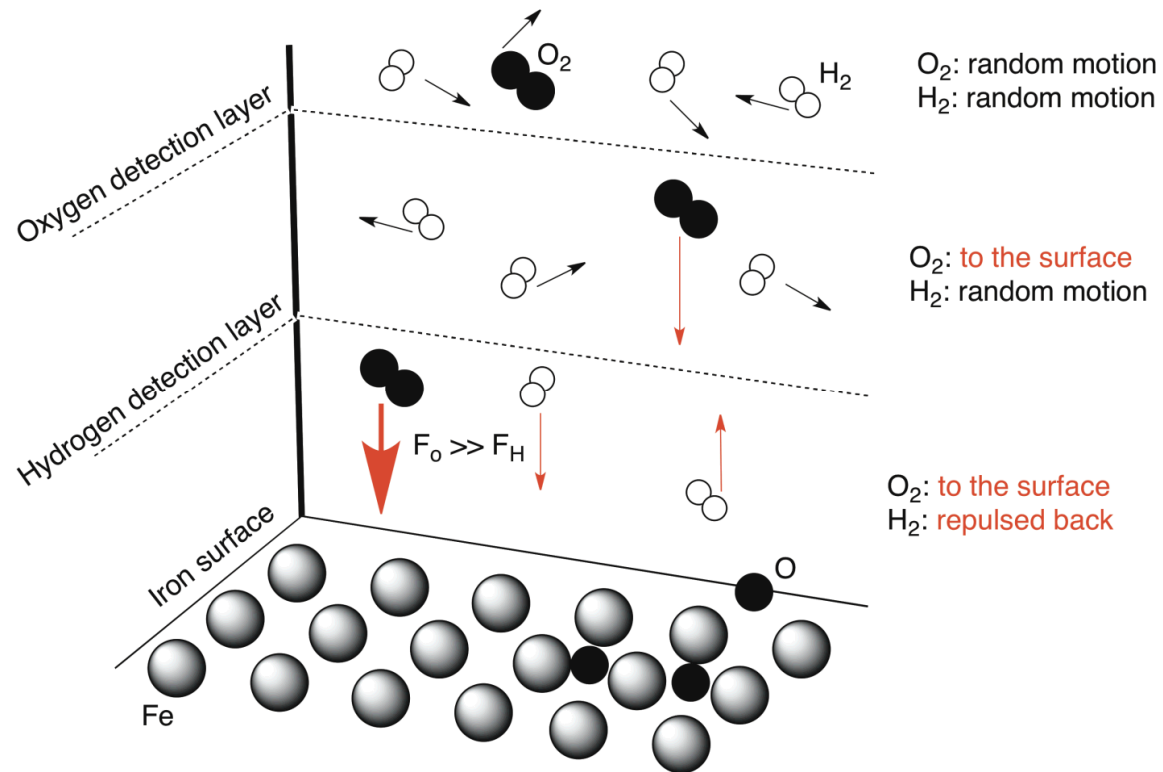


Strong attractive force and absence of activation barrier allow O_2 to out-compete H_2

DFT simulations define potential scenario for O_2 inhibition of H uptake

Key elements in O_2 inhibition scenario:

- O_2 detected deeper in gas volume compared to H_2
- Force on $O_2 \gg$ force on H_2
 - O_2 can out-compete H_2 for adsorption sites
- Adsorbed O leads to repulsive force on H_2



Density Functional Theory (DFT): Methods of Calculation

Theory: plane wave DFT

Program: VASP

Functional: optB86b-vdW
(includes long-range interactions)

Results verified with GGA-PBE

Spin polarized calculations
(accurate spin guess applied)

Energy cut-off: 400 eV

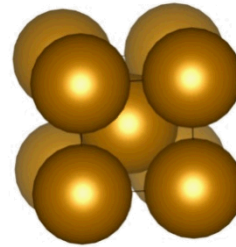
K-points: 8x8x8 bulk; 3x3x1 surface

Transition state search:
climbing nudged elastic band method
8 images per band

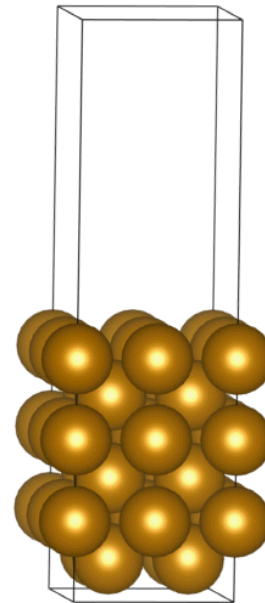
Analysis:

Bader population analysis

Electron density difference method



BCC Fe lattice
Ferromagnetic coupling

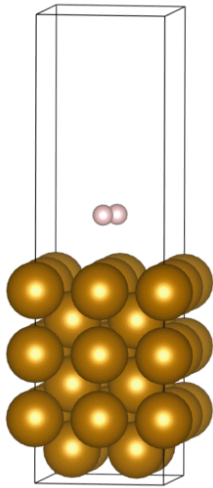


2x2 surface supercell
6 layers Fe atoms
12 Å Vacuum slab

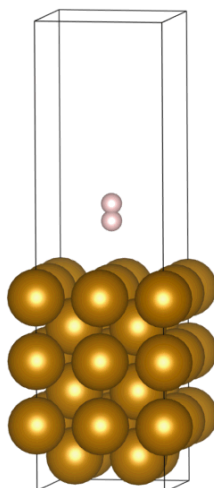
Top 3 layers are relaxed
Bottom 3 layers are fixed

H₂ starting geometries on Fe surface

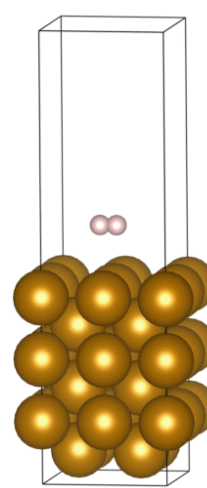
On top
side-on



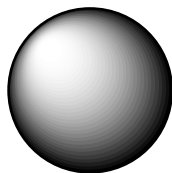
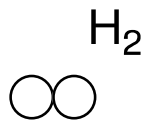
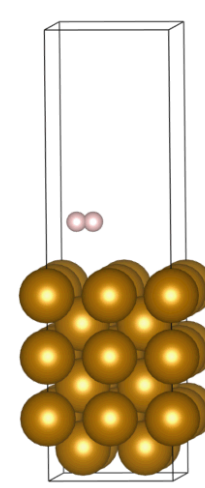
On top
end-on



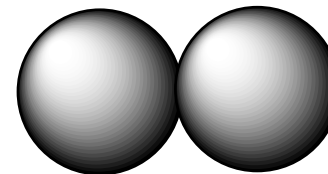
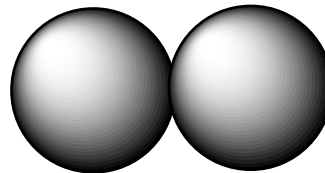
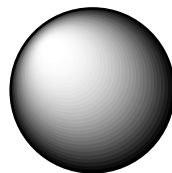
Bridge



Bridge
cross



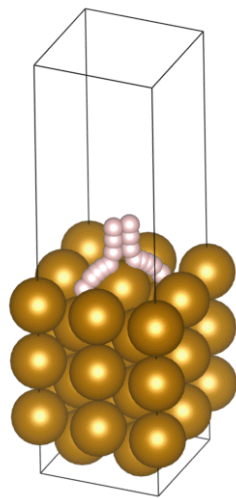
Fe



H₂ dissociation on Fe surface

**On top
side-on**

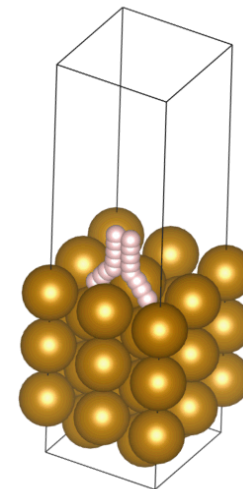
trajectory



Single H₂ molecule approaches the surface in parallel orientation

Bridge cross

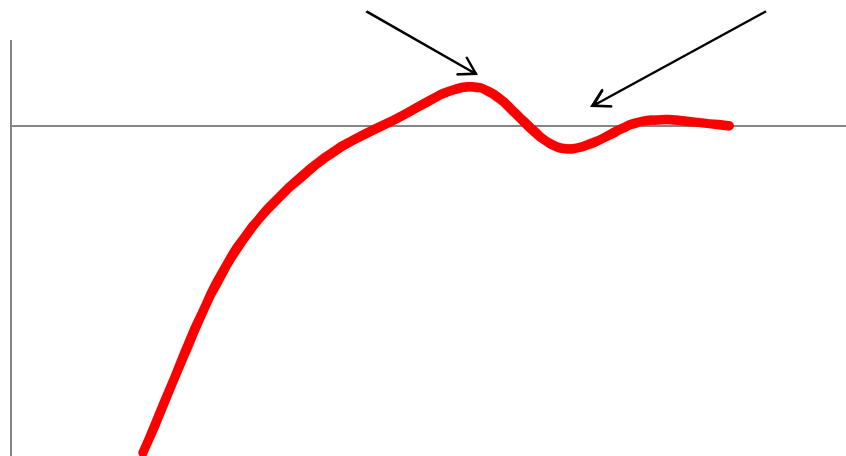
trajectory



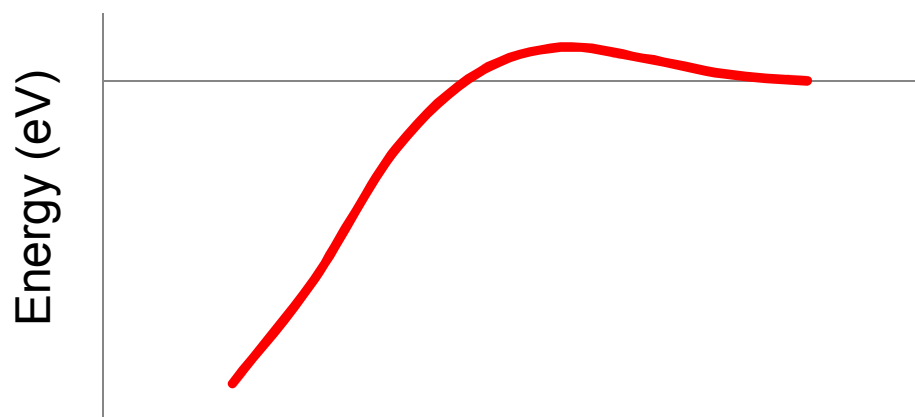
Single H₂ molecule approaches the surface in parallel orientation across a bridge site

transition state

chemisorption state

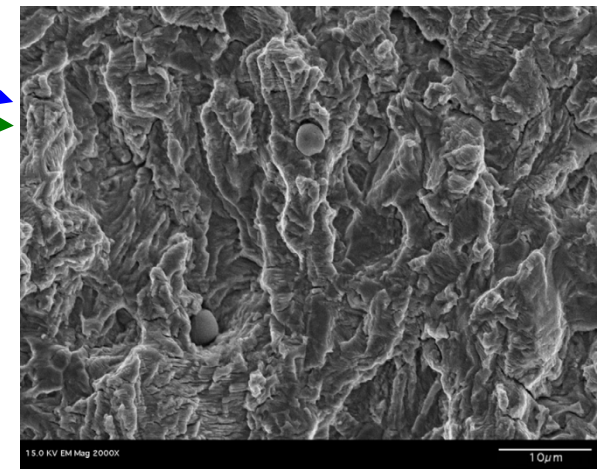
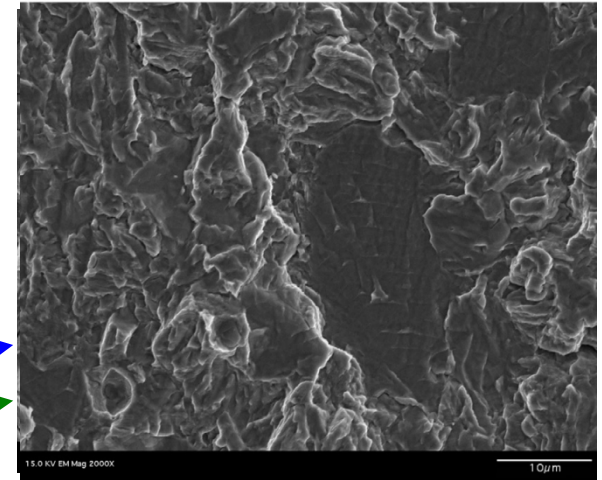
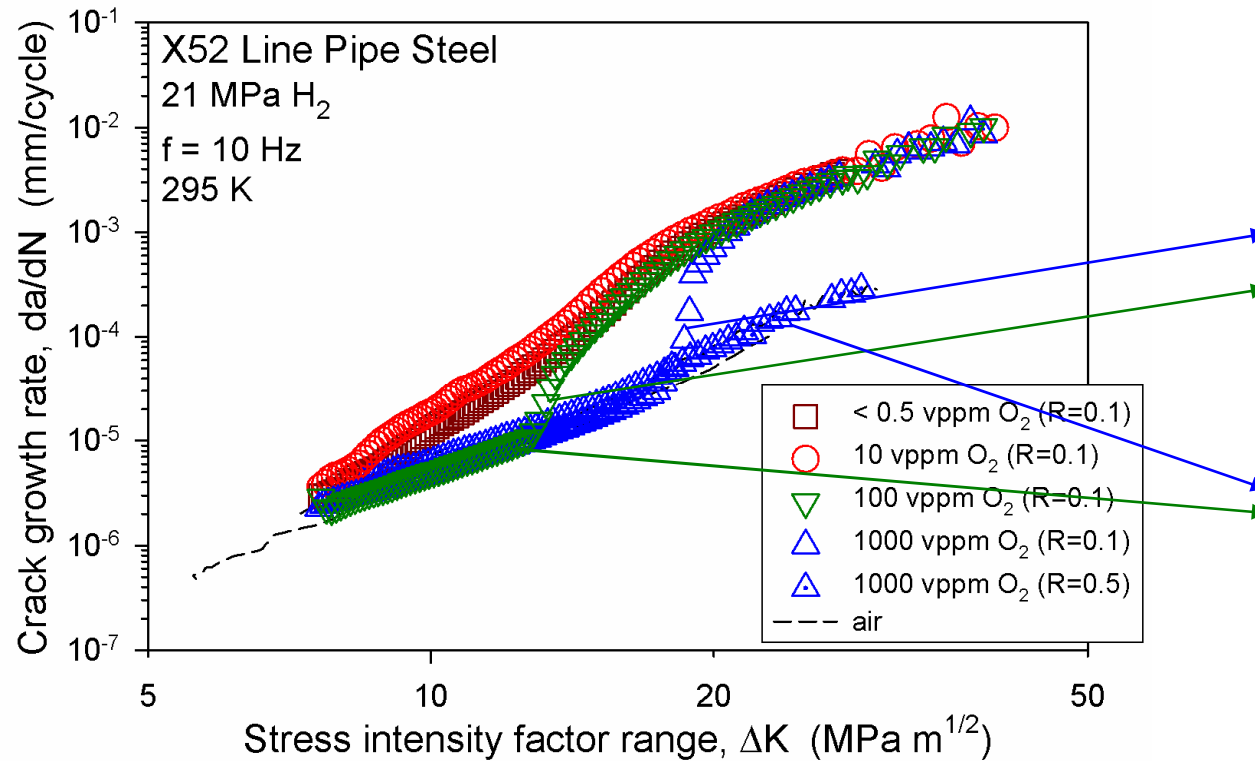


Distance from surface (Å)



H₂-accelerated fatigue crack growth not absolutely inhibited by O₂: depends on da/dN and R ratio

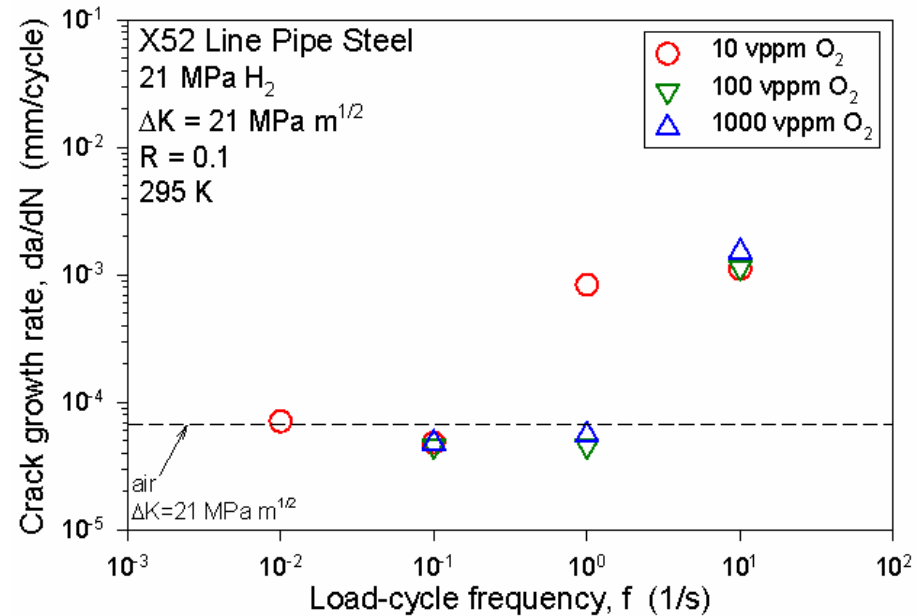
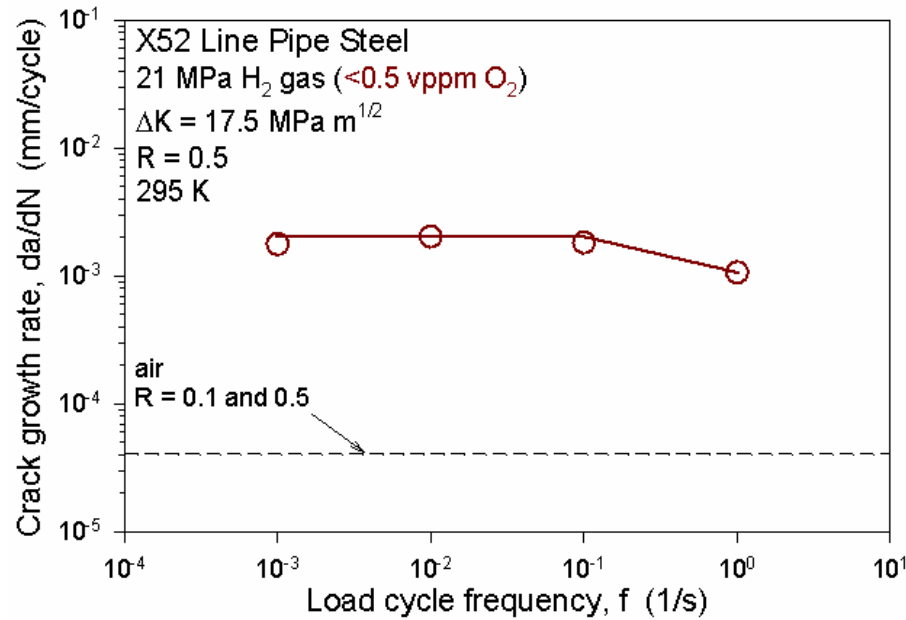
B.P. Somerday et al., *Acta Mater*, 2013



H-assisted crack path evolves from intergranular to transgranular

da/dN measured as function of frequency in H₂ gas over range of O₂ concentrations

B.P. Somerday et al., *Acta Mater*, 2013



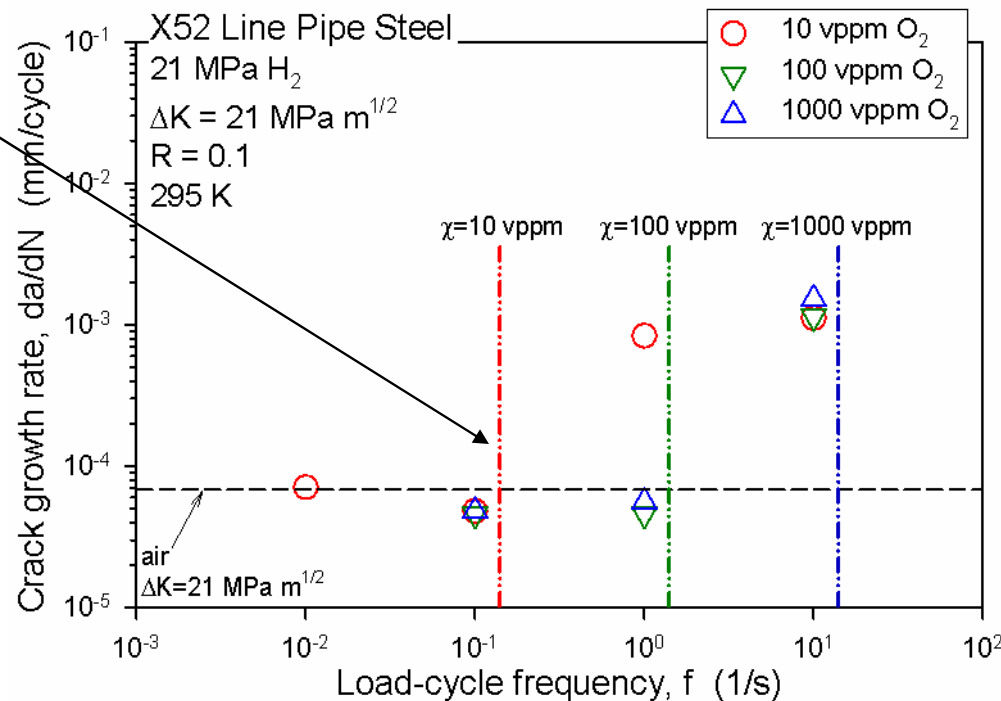
- In H₂ gas with O₂ impurities, da/dN decreases to rates in air as frequency decreases
- Frequency at transition from accelerated da/dN to rates in air depends on O₂ concentration

Model predictions consistent with da/dN vs. frequency data measured in H_2+O_2 gas

B.P. Somerday et al., *Acta Mater*, 2013

$$f|_{crit} = \frac{0.3 \chi D p_{tot} (1 - \nu^2)}{(da/dN) \pi (z\theta)_{crit} R_g T E \sigma_0} \left(\frac{\Delta K}{\sqrt{a^*} (1 - R)} \right)^2$$

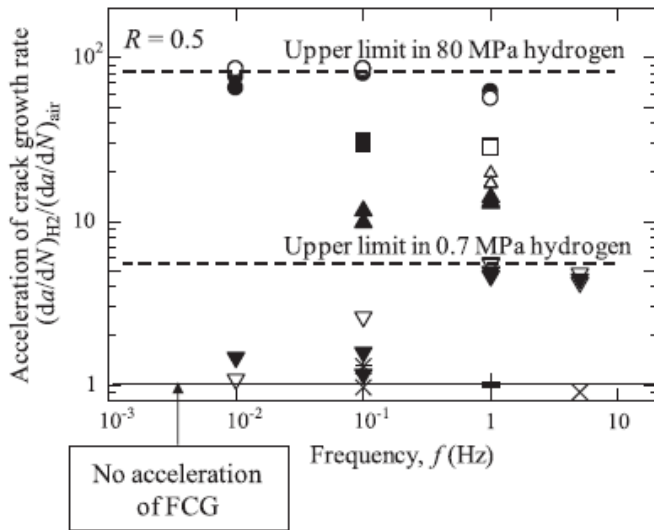
$(z\theta)_{crit}$ from measured da/dN vs. ΔK data in H_2+100 vppm O_2



Predicted frequency for transition to accelerated da/dN consistent with measurements at 10 and 100 vppm O_2

Model can guide interpretation of H₂-assisted fatigue crack growth data

Macadre et al., *Engineering Fracture Mechanics*, 2011



Hydrogen atmosphere

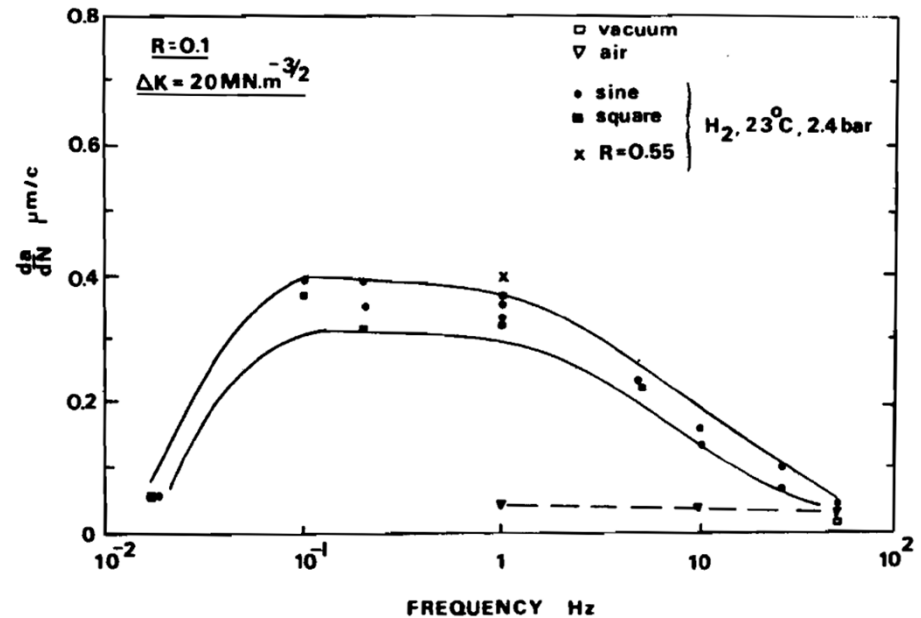
Specimens	0.7 MPa	10 MPa	40–45 MPa	90 MPa
Circumferential (SCI, SCO)	▼	▲	■	●
Longitudinal (SLI, SLO)	▽	△	□	○

Nitrogen atmosphere

Specimens	0.7 MPa N ₂	90 MPa N ₂
Longitudinal (SLI, SLO)	×	+

$$f|_{crit} = \frac{0.3\chi D p_{tot} (1-\nu^2)}{(da/dN)\pi(z\theta)_{crit} R_g T E \sigma_0} \left(\frac{\Delta K}{\sqrt{a^*(1-R)}} \right)^2$$

Stewart, *Mechanisms of Environment Sensitive Cracking of Materials*, 1977

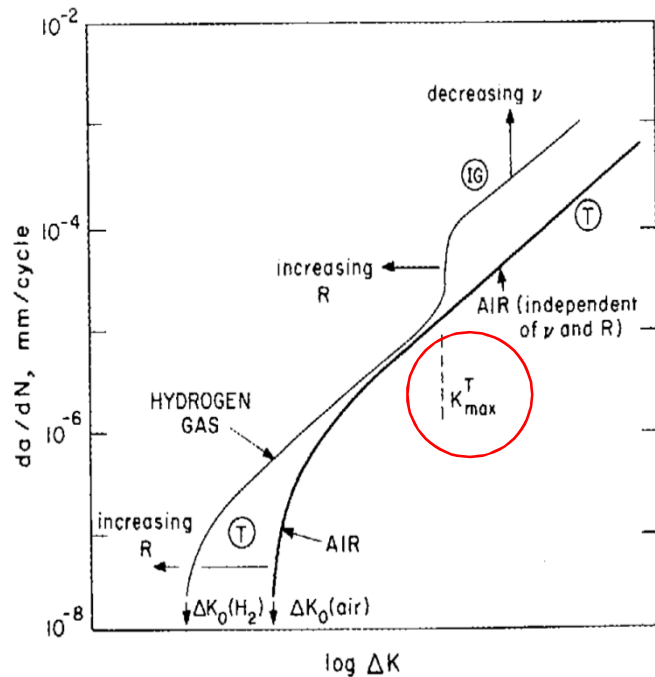


Model indicates that decreasing da/dN at lower frequency could be attributed to O₂ impurities

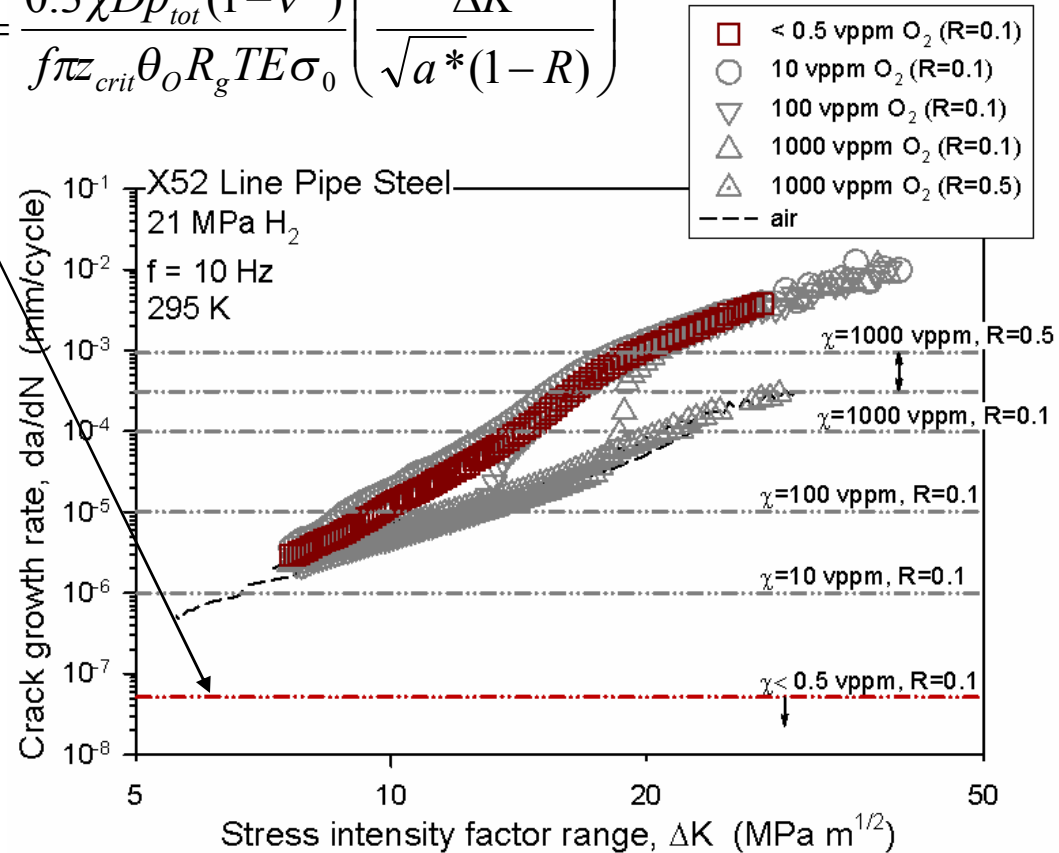
Model does not predict onset of accelerated crack growth for high-purity H₂ case

Z_{crit} from measured da/dN vs. ΔK data in H₂+100 vppm O₂

$$\left. \frac{da}{dN} \right|_{crit} = \frac{0.3 \chi D p_{tot} (1 - \nu^2)}{f \pi z_{crit} \theta_O R_g T E \sigma_0} \left(\frac{\Delta K}{\sqrt{a^* (1 - R)}} \right)^2$$



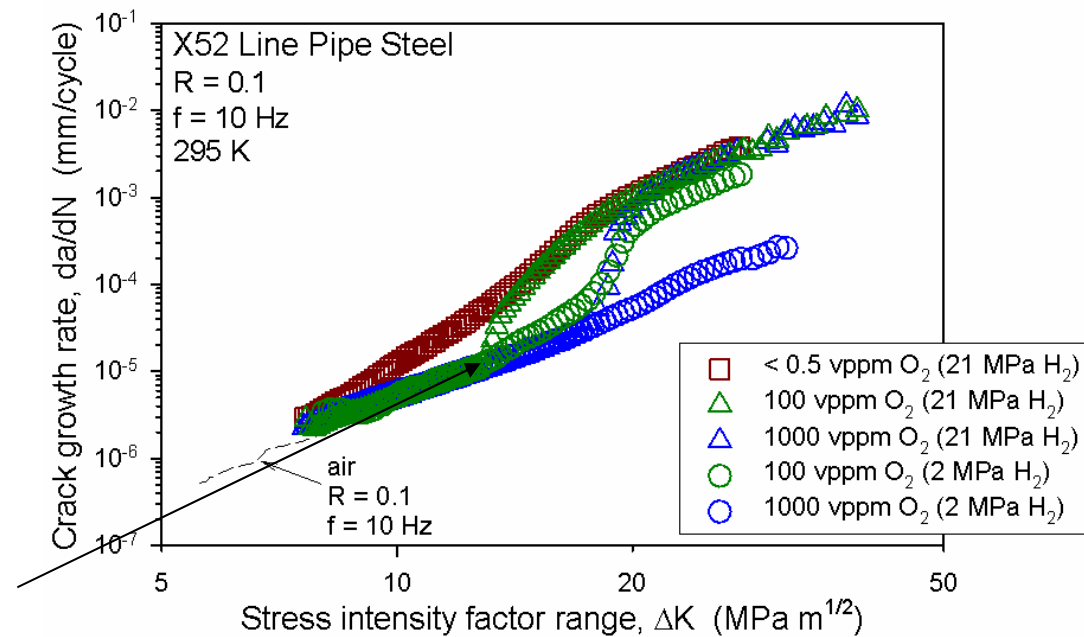
Suresh and Ritchie, *Metal Science*, 1982



Rationale: onset of accelerated crack growth dictated by threshold values of both da/dN and K_{max}

Model critically tested by performing fatigue crack growth experiments at lower pressure

- Question: inhibition governed by O_2 concentration or absolute O_2 partial pressure?
- Results at constant system pressure inconclusive \rightarrow both concentration and absolute partial pressure vary
- Can isolate partial pressure by varying system pressure at constant O_2 concentration
 - Results show no effect on critical da/dN for accelerated crack growth
 - Conclusion: inhibition dictated by O_2 concentration
- Model predicts governing role of O_2 concentration
 - Dp_{tot} term is constant

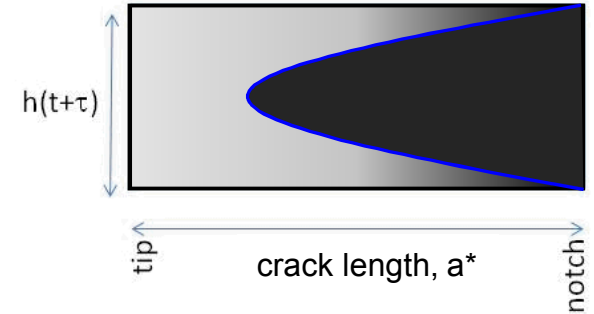
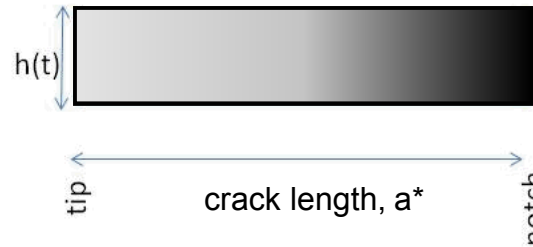
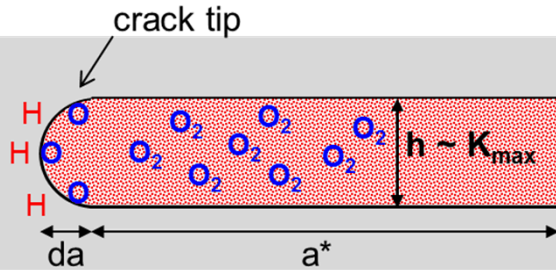


$$\left. \frac{da}{dN} \right|_{crit} = \frac{0.3 \chi Dp_{tot} (1-\nu^2)}{f \pi z_{crit} \theta_O R_g T E \sigma_0} \left(\frac{\Delta K}{\sqrt{a^* (1-R)}} \right)^2$$

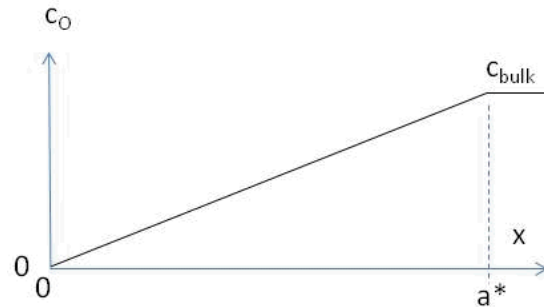
More advanced model accounts for varying O_2 profile in “breathing” crack

B.P. Somerday et al., *Acta Mater*, 2013

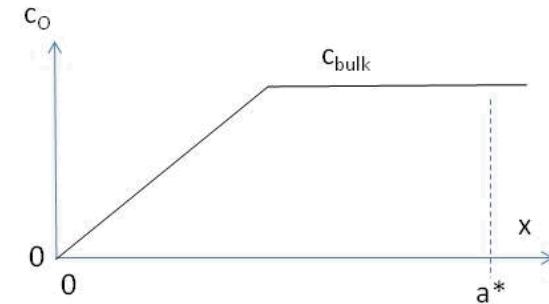
gray-scale shading →
oxygen concentration, c_o



minimum tension



maximum tension



$$S\theta = \frac{0.3\chi D p_{tot} (1-\nu^2)}{(da/dN) f \pi R_g T E \sigma_0 a^*} \bar{h}$$

Model based on “breathing” crack retains dependence on O_2 concentration (χ) and frequency (f)