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Effects of internal acoustic coupling on the response of a base-excited hollow structure

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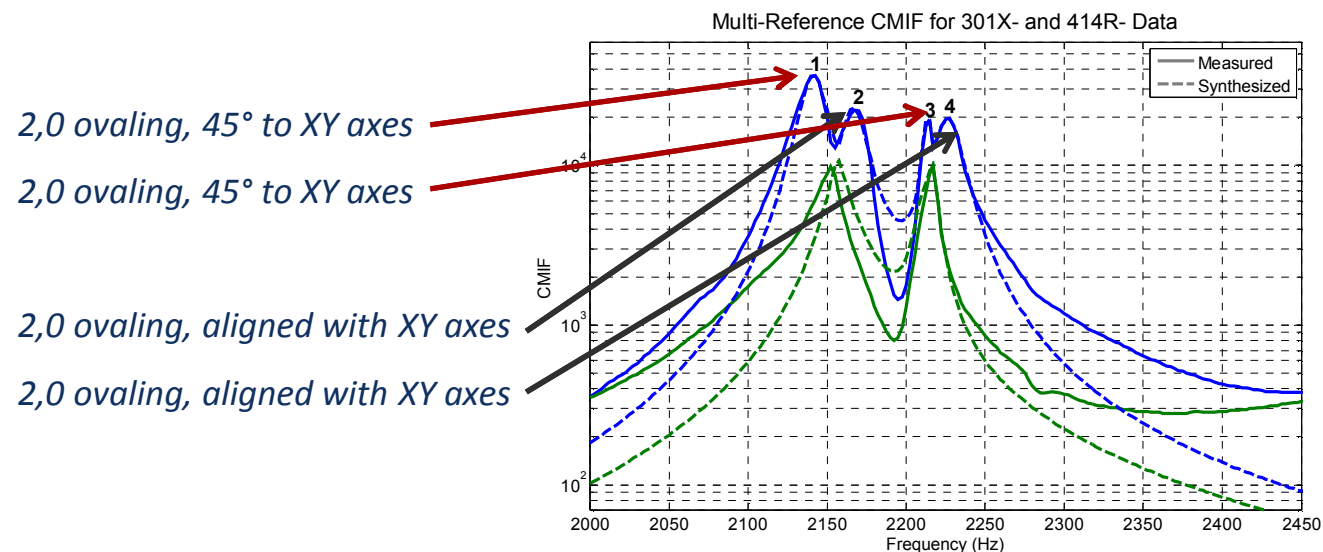
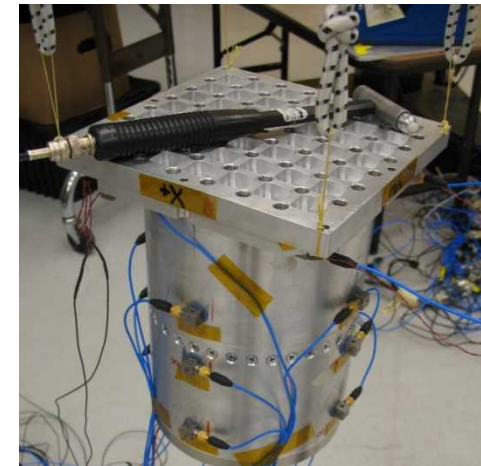
Motivation

- Sandia does a lot of structural dynamics modeling and testing
 - Make predictions of system/component response in dynamic (vibration/aero-acoustic) environments
 - Large effort toward validated structural dynamics FE models
- We usually assume our structures are not affected by air in hollow cavities because...
 - *The cavities are small!*
 - *It's just air!*
 - *How would we know!*
- But – what if these assumptions are not valid?
 - Acoustic modes of the cavity could couple with the structure
 - We would get strange modal test results (repeated shapes)
 - Our model wouldn't correlate well to the modal test results
 - Our model response predictions would be wrong

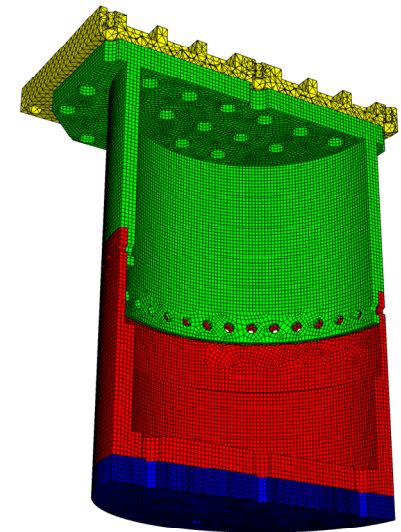
Recent examples of coupling in modal tests at Sandia: Closed Can on a Baseplate*

- Modal test of a hollow cylindrical article revealed repeated shapes at different frequencies
- Calculation of the (2,1,0) acoustic mode:

$$f_{lmn} = \frac{c}{2} \sqrt{\left(\frac{\alpha_{mn}}{\pi a}\right)^2 + \left(\frac{l}{h}\right)^2} = \frac{343}{2} \sqrt{\left(\frac{3.05}{\pi 0.080}\right)^2} = 2081 \text{ Hz}$$



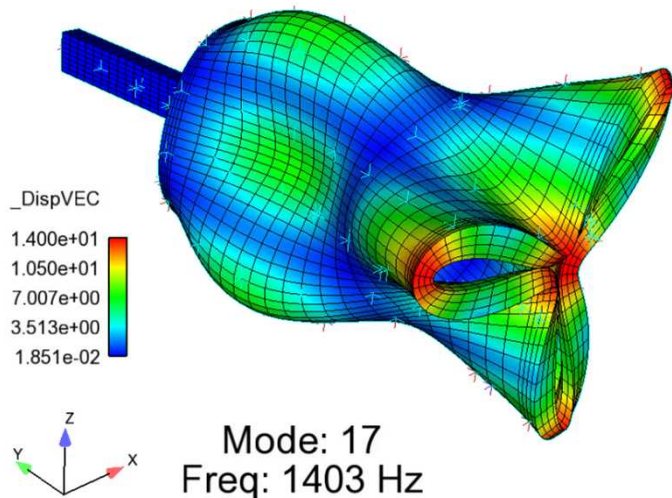
Complex Mode Indicator Function (CMIF)



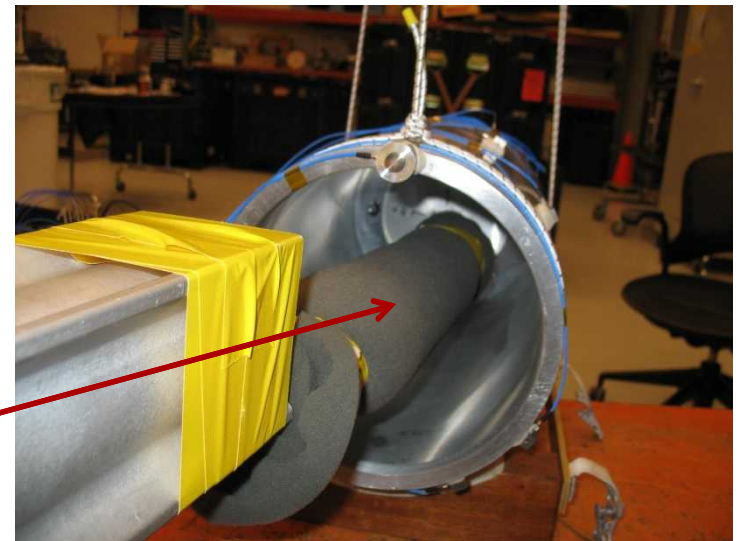
*Example & figures taken from: B. Pacini, D.G. Tipton, "Structural-acoustic mode coupling in a bolted aluminum cylinder," Proceedings of IMAC XXXIV, 2016.

Recent examples of coupling in modal tests at Sandia: Open-ended Cylinder

- Modal test indicated repeated (3,1) shapes around 1408 & 1416 Hz
 - Get a double peak in the structural FRF where a single peak is expected
- Calculation of the acoustic modes:
 - *assuming closed cylinder*
 - (2,1,1) acoustic mode right around 1420 Hz
- Mitigated the coupling issue by adding absorbing material to the cavity

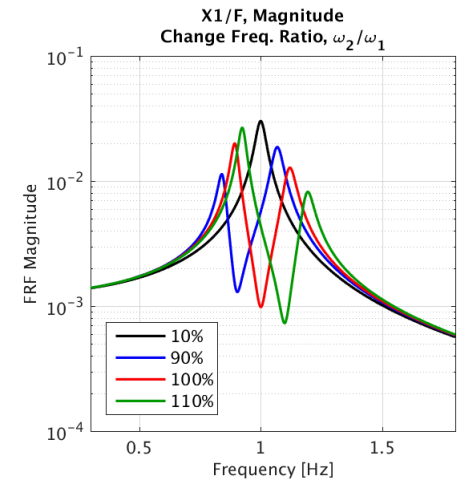
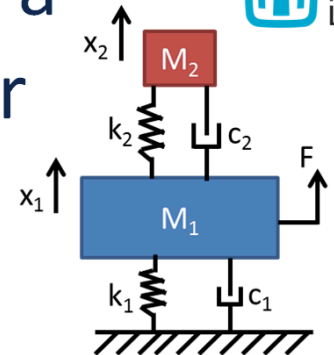


*Foam added
into cavity*



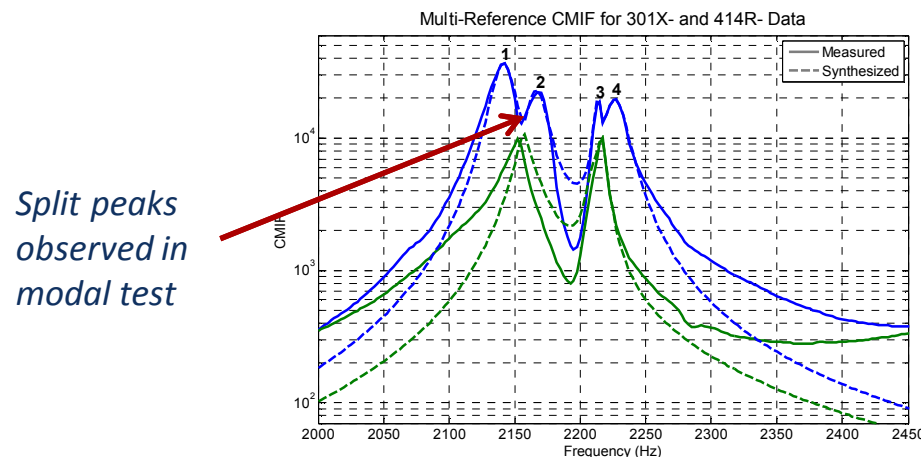
Effect of air on the structure looks like a simple 2-DOF tuned vibration absorber

- Addition of 2nd mass causes a split in the FRF peak of the 1st mass
- Effect on the FRF depends on:
 - Natural frequencies of the two masses
 - Relative mass
 - Damping



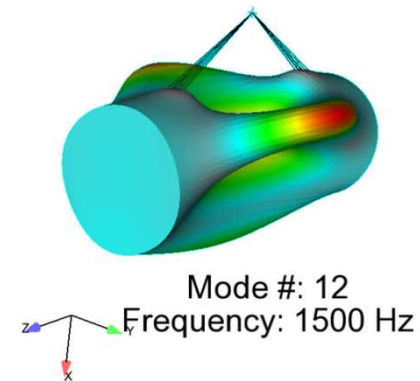
Effect of Proximity of ω_{n1} and ω_{n2} :

- FRF affected if ω_{n2} near ω_{n1}
- Single resonance peak split into two peaks
- Max response is reduced



Investigate how coupling could affect response prediction with a simulation study

- Simple cylinder with force input to 2 points on side
 - Like a store on a wing subject to a base excitation
- Dimensions: 32" long, 12" diameter
- Shell elements allow for varying the wall thickness to align structure and acoustic modes
 - Determine wall thickness to match the (3,1,0) acoustic mode



Analytically-calculated Acoustic Modes

Shape	Freq. [Hz]
Axial 1	211.0
Slosh 1	659.1
Ovaling 2 lobe	1092.5
Ovaling 3 lobe	1504.5
Ovaling 2 + Axial 1	1112.7
Radial 1 (bullseye)	1371.9

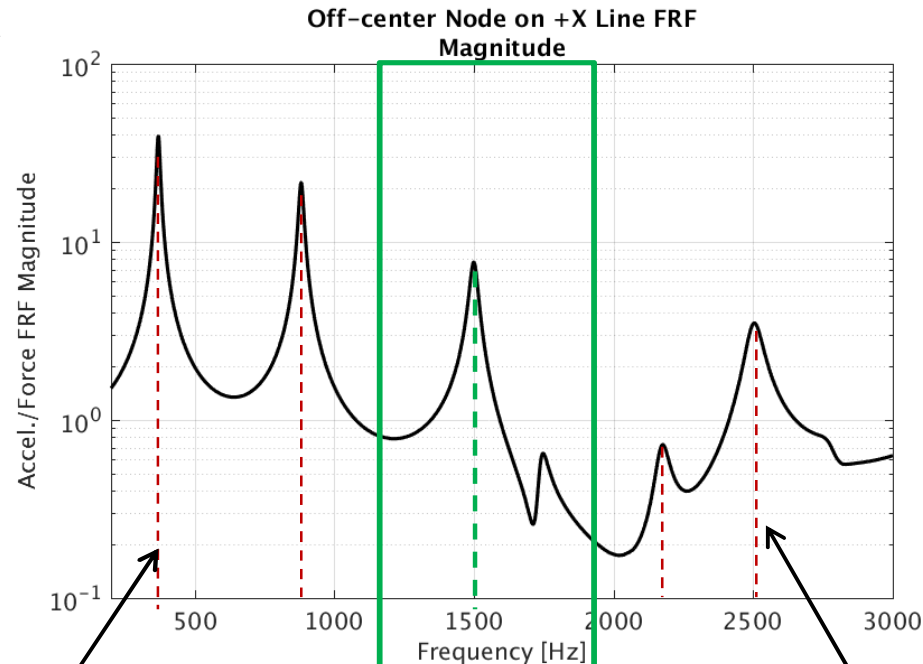
Structural Modes:

0.65" Thick – Aligns with (3,1,0) Acs. Mode

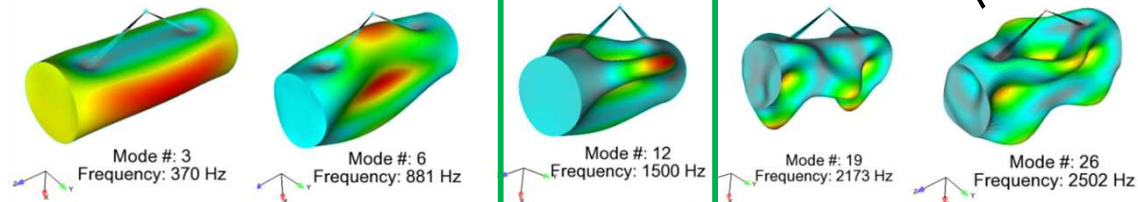
Shape	Freq. [Hz]
2,0 (2nd)	881
3,0	1500
1st bending	1740
3,2	2173

Structural FRFs & Acoustic Modes

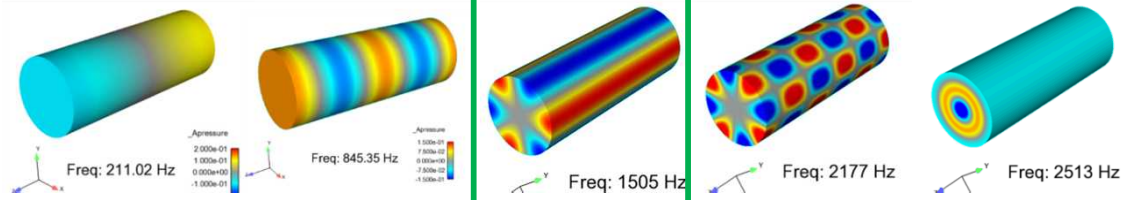
- Direct frequency response
Analysis using
Sandia's Sierra
Mechanics finite
element suite



Structural
Mode

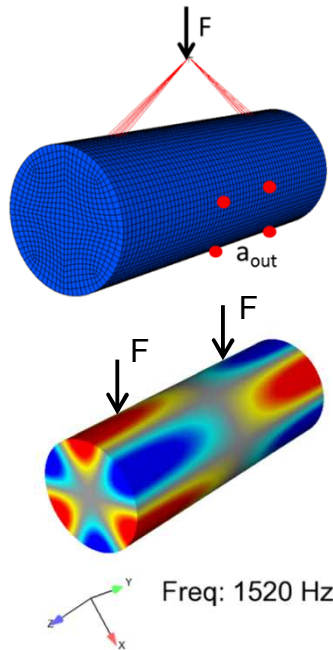


Acoustic
Mode

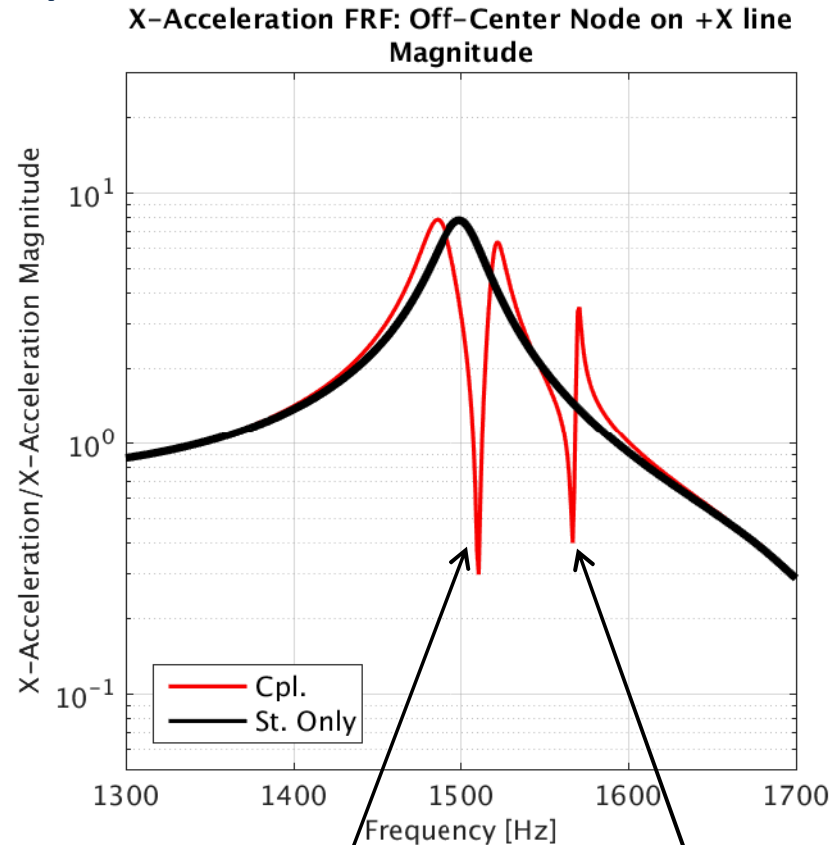


Hollow Cylinder: Effect of Coupling on FRF Peak for the (3,1) Structure Mode

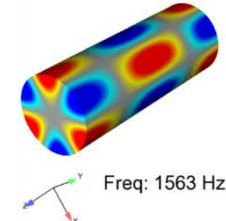
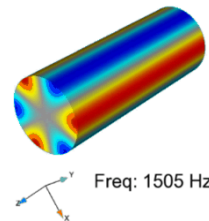
- (3,1,0) and (3,1,2) interact with the structure, but not the (3,1,1) because it is incompatible with the input



Freq: 1520 Hz



*Acs. (3,1,0)
coupling at
structural
mode*

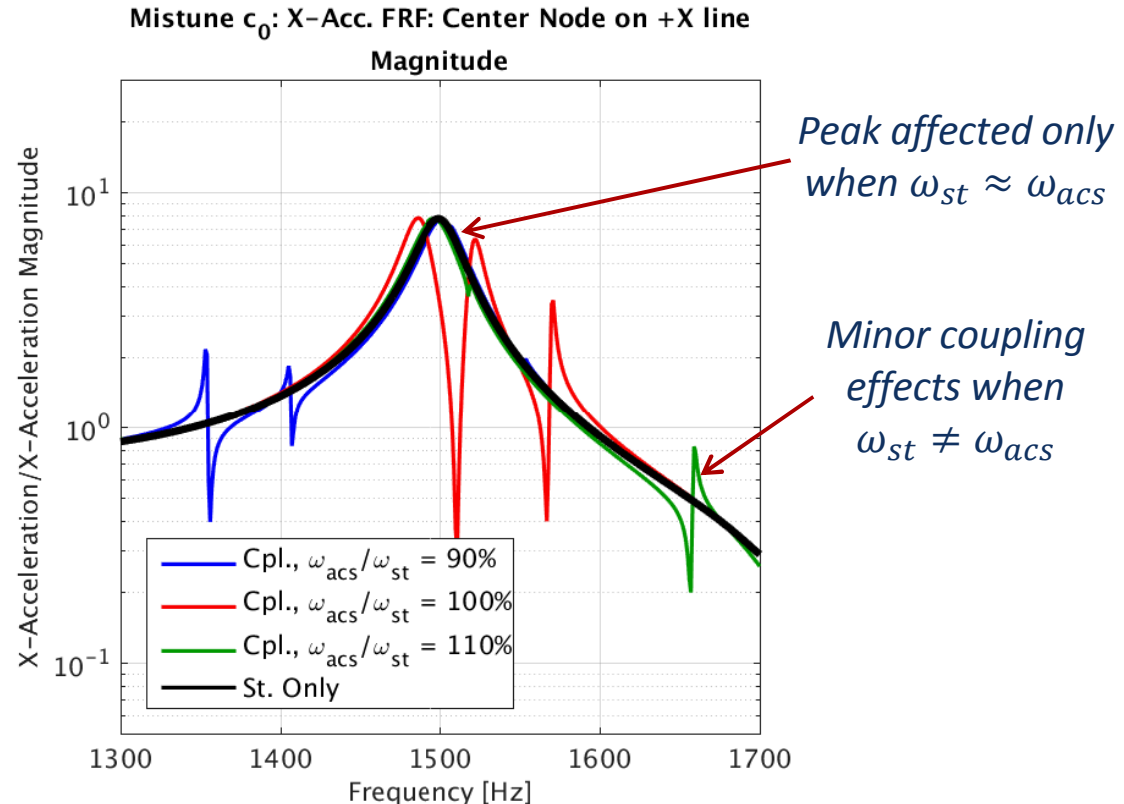
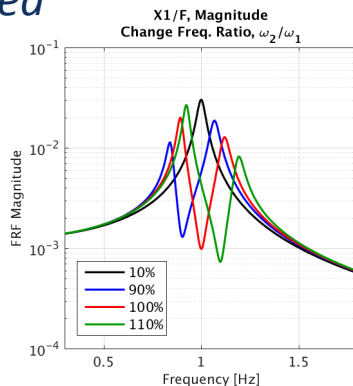
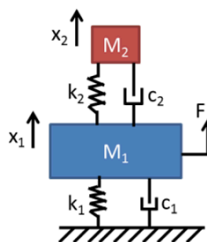


*Acs. (3,1,2)
mode also
couples with
same mode*

Hollow Cylinder: Effect of Mistuning (ω_{n2}/ω_{n1}) on (3,0) Structural Response

- Mistune the system by adjusting the sound speed of the air
 - 90, 100, 110% of structural mode frequency
- Get strong coupling, peak splitting when $\omega_{st} \approx \omega_{acs}$
 - Peak is not affected when $\omega_{st} \neq \omega_{acs}$

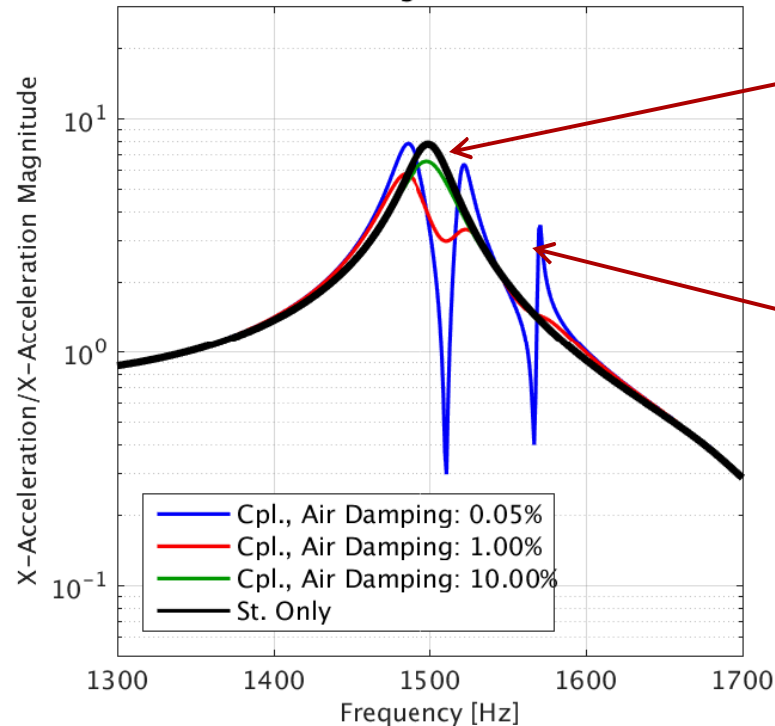
2-DOF Tuned Absorber



Hollow Cylinder: Effect of Increased Air Damping (c_2) on (3,0) Structural Response

- Add damping to the tuned mass (air) by changing the proportional damping terms
 - 0.05%, 1%, 10% damping
- Added Air Damping could be from:
 - Venting (holes in case)
 - Absorbing material (foam)

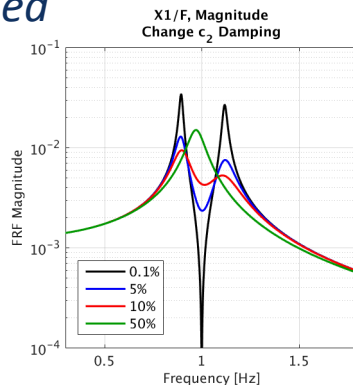
Change Air Damping: X-Acc. FRF: Center Node on +X line
Magnitude



High damping locks together the air & structure, acts like added mass

Low damping causes high resonant coupling

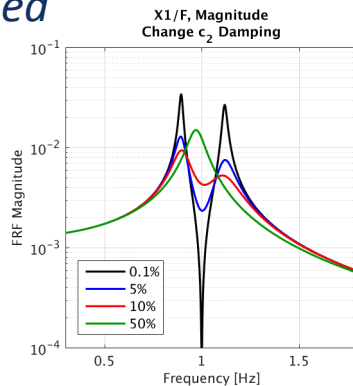
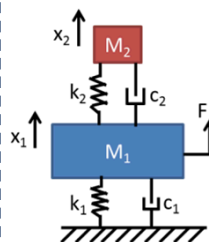
2-DOF Tuned Absorber



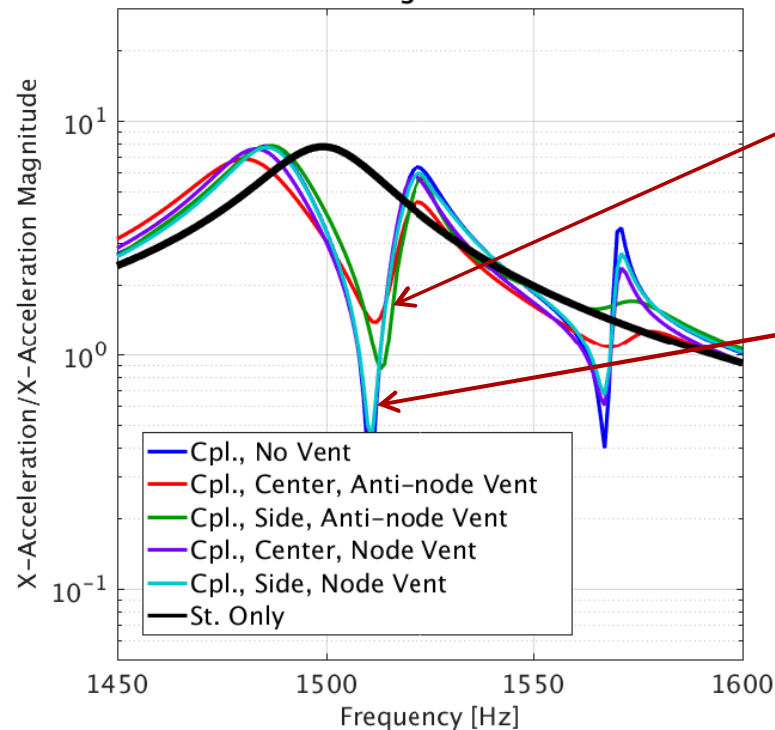
Hollow Cylinder: Effect of Holes on the Coupled Cylinder Response

- Place holes in the casing and add an absorbing (impedance matched) boundary condition on the air at these holes
- Located at pressure nodes, anti-nodes and centered or near the end

2-DOF Tuned Absorber



Change Venting: X-Acc. FRF: Off-Center Node on +X line
Magnitude



Holes at anti-nodes add damping

Holes at nodes have little effect

How Does This Coupling Affect Quantities of Interest?

- Doing a Modal Test:
 - Coupling can add additional modes to the FRF, with repeated shapes which can give parameter estimation algorithms trouble
 - Additional peaks in the FRF would make it seem like more gages are needed on the structure – which isn't necessary
- Making Model Predictions:
 - In-vacuo structural model won't have peak response at same frequency as coupled, physical system
 - Rather than single, narrow peak in response, response may be spread in frequency due to the double peak in the coupled system

Conclusions

- Structural-acoustic coupling can be important for structures we care about
 - Causes a change in the structural response, similar to adding a tuned absorber to the system
 - Observe repeated shapes in the FRF, which can cause problems with parameter estimation algorithms & affect FE model correlation
 - Structure doesn't have to be sealed to exhibit coupling
- **What can you do?**
 - Simple calculations can be used to determine if there are compatible acoustic modes in the vicinity of structural modes
 - In testing, adding absorbing material to the cavity may be enough to reduce the acoustic mode and avoid noticeable coupling
 - For making predictions, add air cavities to finite element models