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Towards optimizing two-qubit operations in three-electron double quantum dots



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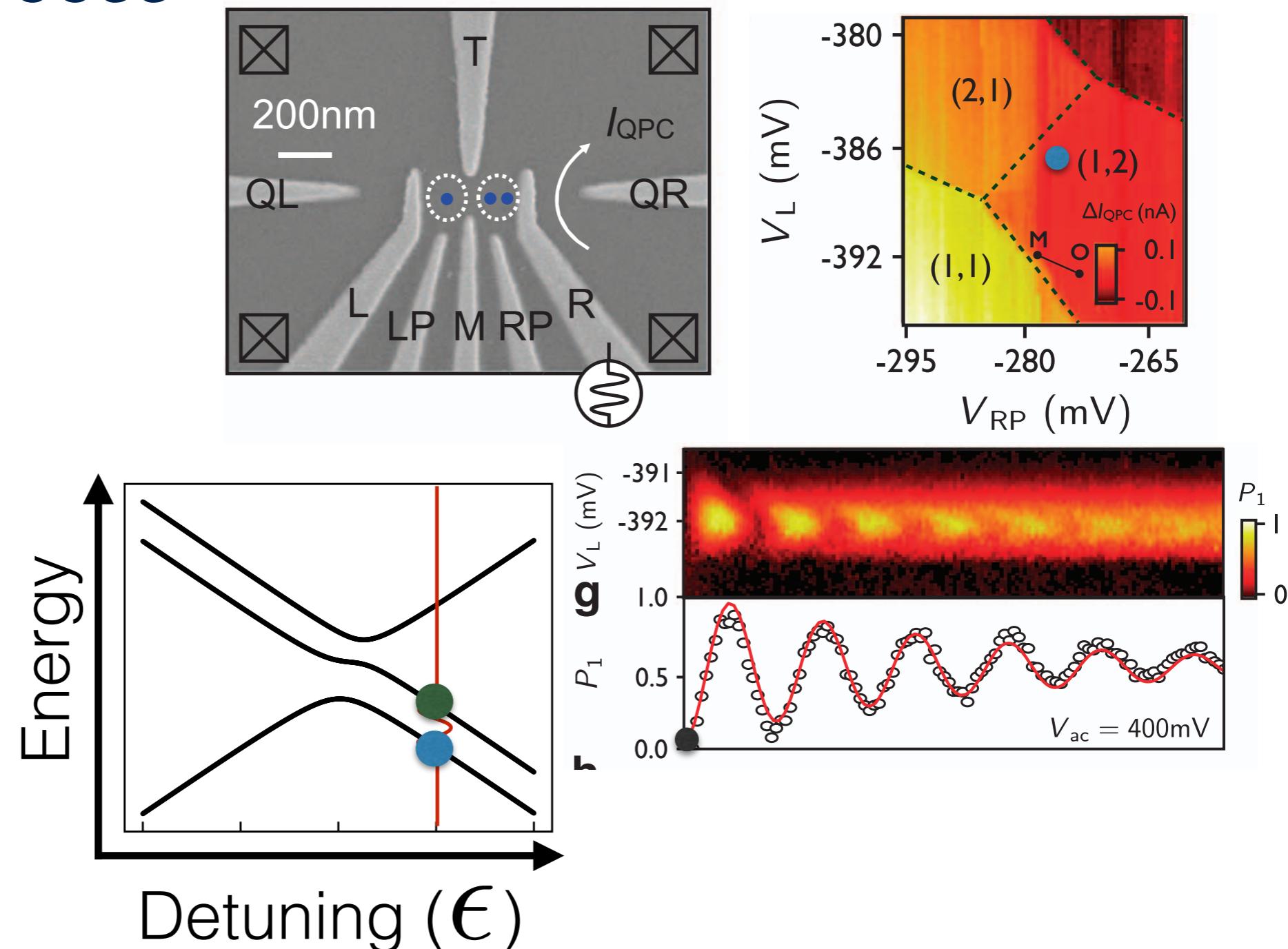
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Quantum dot “hybrid” qubit has had experimental success



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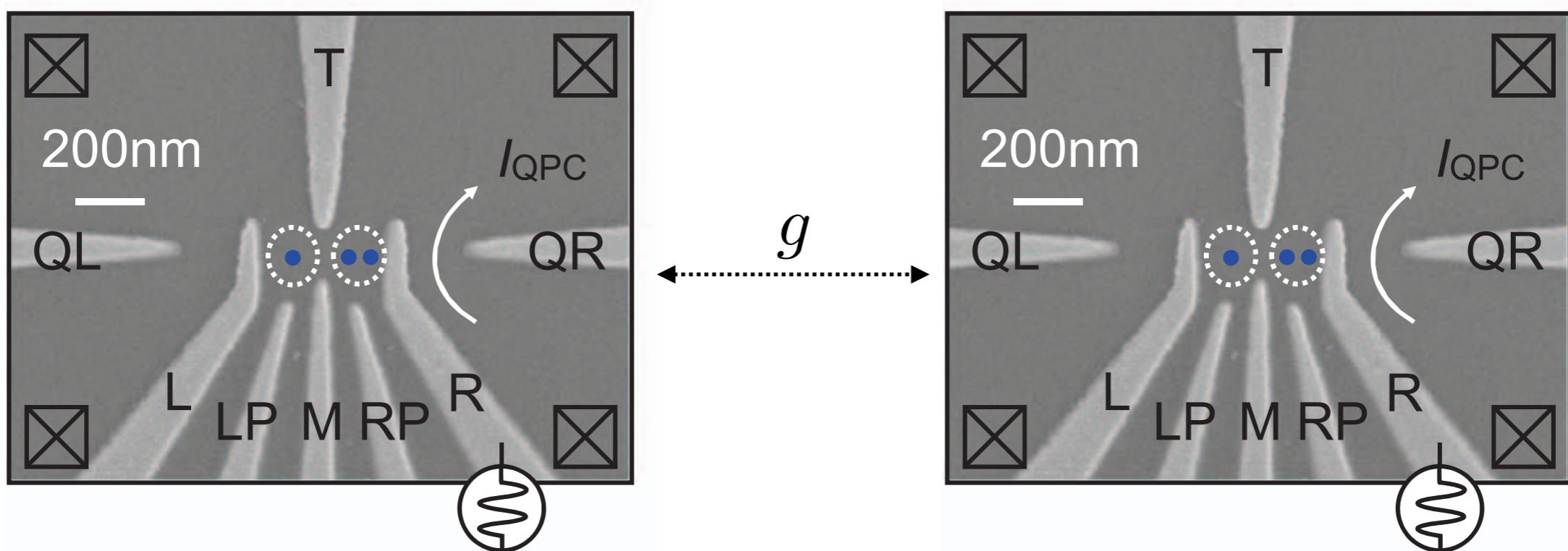
- The hybrid qubit consists of three electrons and two dots
- The sweet spot is very broad, which makes it fairly resistant to charge noise



Dohun Kim, D. R. Ward, C. B. Simmons, D. E. Savage, M. G. Lagally, Mark Friesen, S. N. Coppersmith, and M. A. Eriksson, npj Quant. Inf. 1, 15004 (2015).

Proposed approach: AC-driven capacitively coupled hybrid qubits

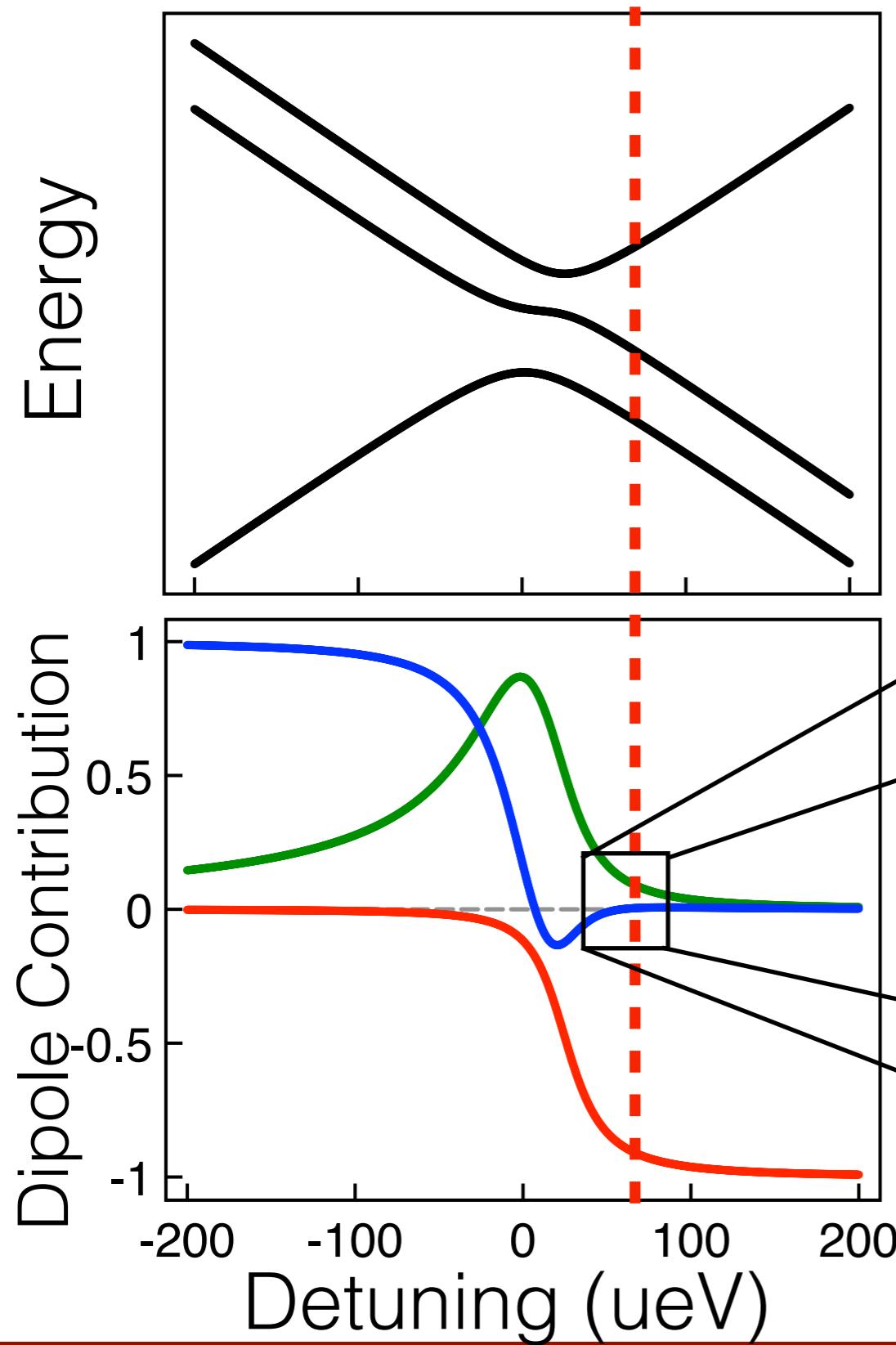
- Capacitively coupled hybrid qubits show promise as high-fidelity two-qubit system.
- It may be possible to tune the system parameters to extend the beneficial properties of the single-qubit operations to two-qubit operations.
- Here we focus on the weakly coupled limit, putting a lower bound on the resulting entangling gates.



Two-level systems have dipoles with longitudinal and transverse components



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$$\mathcal{H}(t) = \frac{\omega}{2} \sigma_z + \mathcal{P} \sin(\omega_d t + \phi)$$

Transverse field

$$\mathcal{P} = \alpha I + \beta \sigma_x + \gamma \sigma_z$$

Longitudinal field

Capacitively coupled hybrid qubits in the weakly coupled limit

$$\mathcal{H} = \frac{\omega_1}{2} \sigma_z \otimes I + \frac{\omega_2}{2} I \otimes \sigma_z + g \mathcal{P}^{(1)} \otimes \mathcal{P}^{(2)}$$



Take coupling to first order

$$\mathcal{H} = \left(\frac{\omega_1}{2} + g \alpha^{(2)} \gamma^{(1)} \right) \sigma_z \otimes I + \left(\frac{\omega_2}{2} + g \alpha^{(1)} \gamma^{(2)} \right) I \otimes \sigma_z + \\ + g \left(\beta^{(1)} \sigma_x + \gamma^{(1)} \sigma_z \right) \otimes \left(\beta^{(2)} \sigma_x + \gamma^{(2)} \sigma_z \right)$$



Remove single-qubit longitudinal field

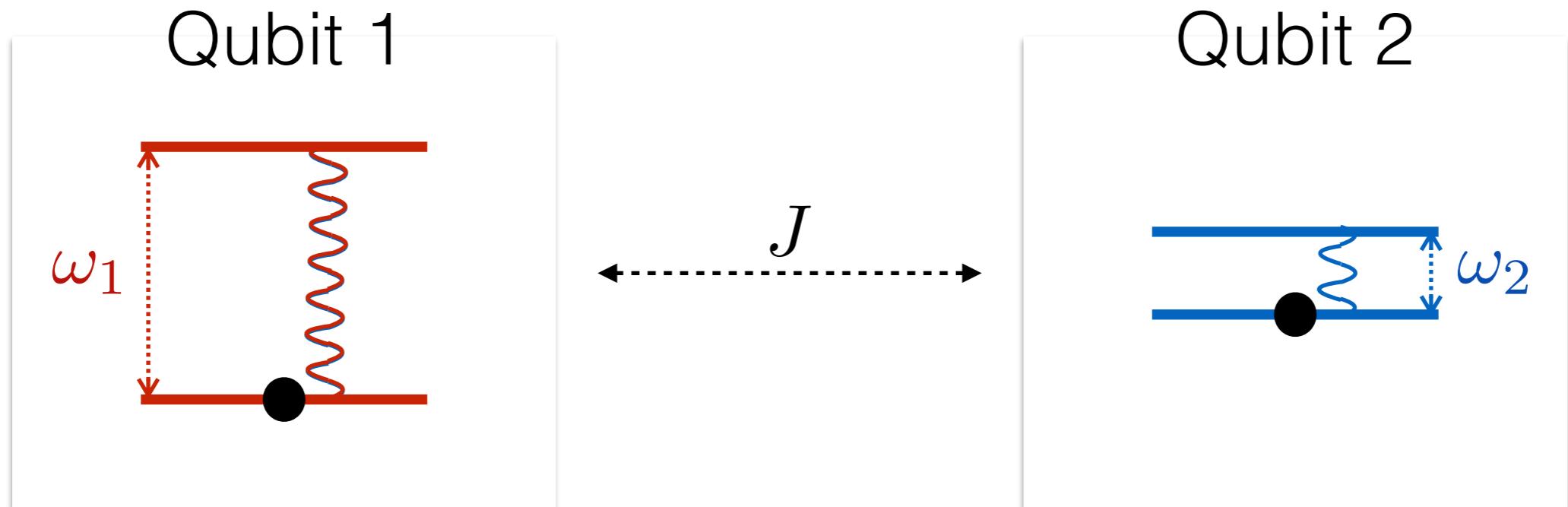
$$\mathcal{H} = \frac{\omega_1}{2} \sigma_z \otimes I + \frac{\omega_2}{2} I \otimes \sigma_z + g \beta^{(1)} \beta^{(2)} \sigma_x \otimes \sigma_x$$

The “cross-resonant” Hamiltonian is an ideal coupled system



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$$\mathcal{H} = \frac{\omega_1}{2} \sigma_z \otimes I + \frac{\omega_2}{2} I \otimes \sigma_z + J \sigma_x \otimes \sigma_x$$



C. Rigetti, A. Blais, and M. Devoret, PRL **94**, 240502 (2005)

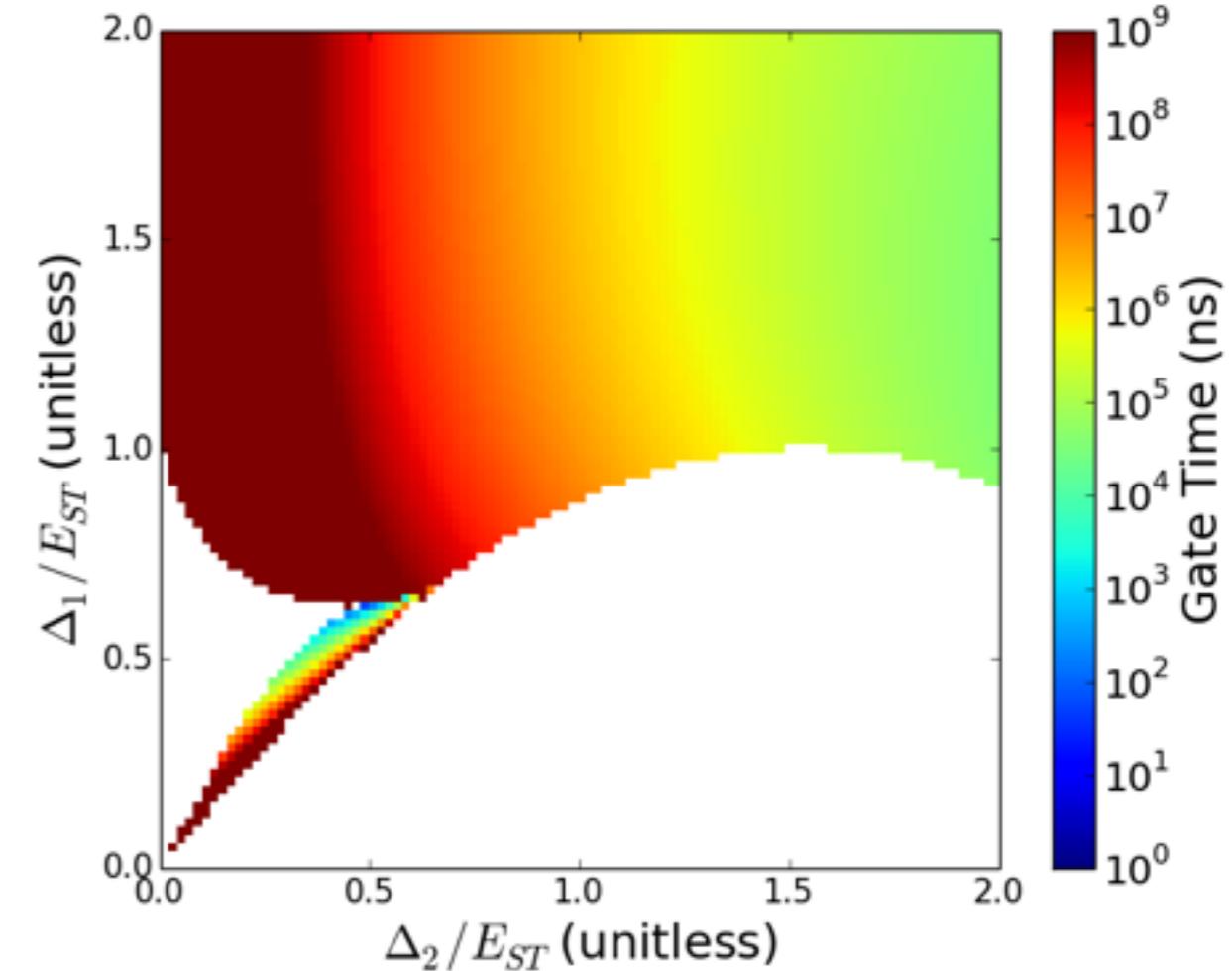
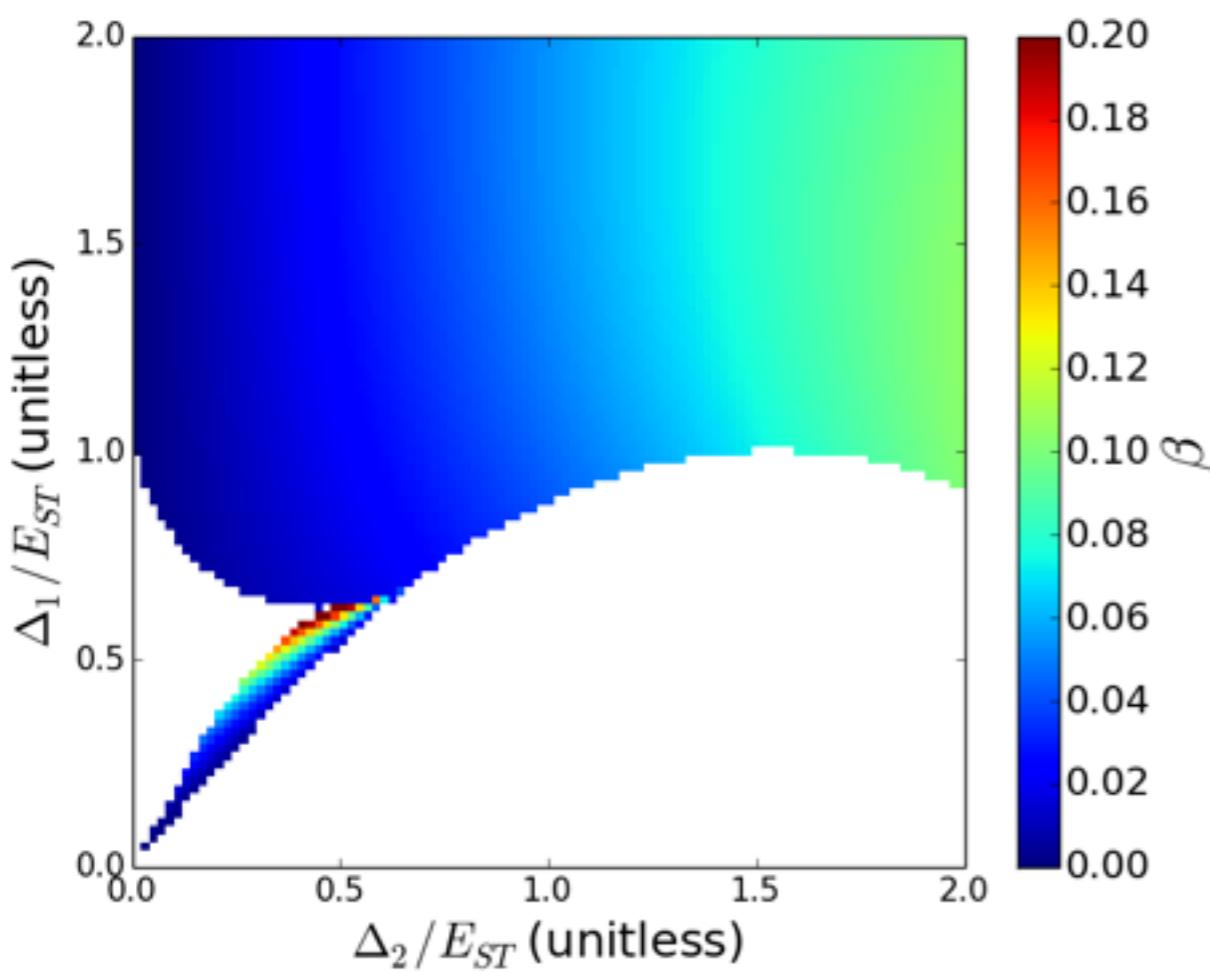
J.M. Chow, A.D. Córcoles, J.M. Gambetta, C. Rigetti, B.R. Johnson, J.A. Smolin, J.R. Rozen, G.A. Keefe, M.B. Rothwell, M.B. Ketchen, and M. Steffen, PRL **107**, 080502 (2011)

Small cross-resonant matrix element means slow entangling gate



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- Cross-resonant matrix element is $\sim \frac{g}{(\omega_1 - \omega_2)} \beta^3$
- For weak coupling approximation to hold, $\beta^3 \gg \frac{g}{(\omega_1 - \omega_2)}$



Strong coupling regime has faster gate times, is more complicated



- We can expand in the inverse of the energy separation between the logical and leakage states
- Single qubit operations are second order interactions, entangling operations are fourth order
- β^3 is sixth order, therefore it does not dominate other two-qubit interactions



Thank You!



Additional Slides

Dipole operators are useful diagnostic tools

Dipole operators

$$\mathcal{H} = \mathcal{H}_0 + \frac{\epsilon^{(1)}}{2} \mathcal{P}^{(1)} + \frac{\epsilon^{(2)}}{2} \mathcal{P}^{(2)}$$

depends on e.g.

$\Delta_1^{(1)}, \Delta_2^{(1)}, \Delta_1^{(2)}, \Delta_2^{(2)}, E_{ST}^{(1)}, E_{ST}^{(2)}, g$

Properties of Dipole:

- $\langle \Psi_i | \mathcal{P}^{(j)} | \Psi_i \rangle = \frac{\partial E_i}{\partial \epsilon^{(j)}}$ is a measure of dephasing due to charge noise
- $\langle \Psi_i | \mathcal{P}^{(j)} | \Psi_l \rangle$ is inversely proportional to the Rabi frequency

The “cross-resonant” Hamiltonian is an ideal coupled system

- In the coupled eigenbasis, the cross-resonant Hamiltonian takes the form:

$$\mathcal{H} = \frac{\omega_1}{2} \sigma_z \otimes I + \frac{\omega_2}{2} I \otimes \sigma_z + J \sigma_x \otimes \sigma_x$$

- With the dipoles:

$$\mathcal{P}_1 = \sigma_x \otimes I \quad \mathcal{P}_2 = I \otimes \sigma_x$$

- Which means that in the eigenbasis,

$$\mathcal{P}_1 = \cos(\theta_+) \sigma_x \otimes I + \sin(\theta_+) \sigma_z \otimes \sigma_x$$

- with: $\mathcal{P}_2 = \cos(\theta_-) I \otimes \sigma_x + \sin(\theta_-) \sigma_x \otimes \sigma_z$

$$\theta_+ = \frac{\theta_1 + \theta_2}{2} \quad \theta_- = \frac{\theta_2 - \theta_1}{2} \quad \tan \theta_1 = \frac{2J}{\omega_1 + \omega_2} \quad \tan \theta_2 = \frac{2J}{\omega_1 - \omega_2}$$



Small cross-resonant matrix element means slow entangling gate

$$\mathcal{H} = \frac{\omega_1}{2} \sigma_z \otimes I + \frac{\omega_2}{2} I \otimes \sigma_z + g \beta^{(1)} \beta^{(2)} \sigma_x \otimes \sigma_x$$



Diagonalize, take coupling to first order

$$\mathcal{P}^{(1)} = \alpha^{(1)} I + \beta^{(1)} \sigma_x \otimes I + g \frac{2\omega_1 (\beta^{(1)})^2 \beta^{(2)}}{(\omega_1^2 - \omega_2^2)} \sigma_z \otimes \sigma_x$$

$$\mathcal{P}^{(2)} = \alpha^{(2)} I + \beta^{(2)} I \otimes \sigma_x + g \frac{2\omega_2 \beta^{(1)} (\beta^{(2)})^2}{(\omega_1^2 - \omega_2^2)} \sigma_x \otimes \sigma_z$$

Entangling gate far too slow! (~ 0.1 s)