



# A Numerical Round Robin for the Prediction of the Dynamics of Jointed Structures

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# Outline

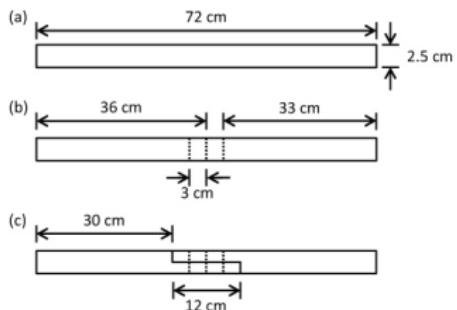
- 1 Benchmark description and objectives
- 2 FE model and non-linear static analysis
- 3 Three non-linear dynamic modelling approaches
- 4 Brake-Reuss beam non-linear dynamic analysis
- 5 Conclusion

## Objectives of the study

**Assess the ability for different numerical approaches to model accurately a structure with a mechanical joint**

- Create a well-defined benchmark system that facilitates meaningful comparison between the different approaches.
- Develop a metric to compare the numerical approaches with each other, and with experimentally-derived data.
- Determine the best practices for performing a numerical analysis on systems with localized nonlinearities.

# Benchmark system



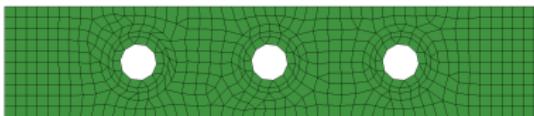
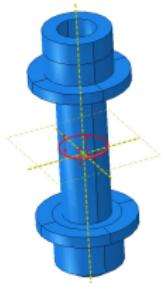
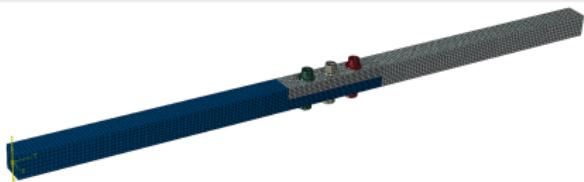
**Figure:** Brake-Reuss beam geometry



**Figure:** Brake-Reuss beam

**72cm long beam with a lap joint**

# Non-linear static analysis: modelling



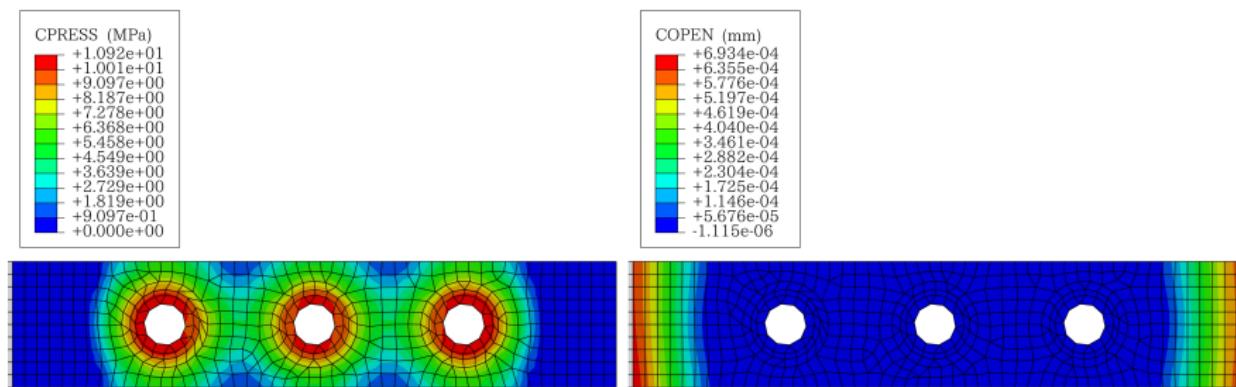
- FE model:

- 2 beams + 3 monolithic bolt assemblies
- Fixed-free boundary condition
- Same isotropic material for all parts
- Fixed coupling between the washers and the top/bottom surfaces of the beam
- Each bolt virtually cut into two pieces to apply a 4kN pretension load

- Interface modelling:

- matching mesh of 592 nodes per face
- Surface-to-surface approach
- Pressure-overclosure: 'hard contact'
- Contact enforcement: Lagrange multipliers
- Friction formulation: penalty method,  
 $\mu = 0.6$

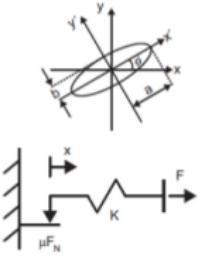
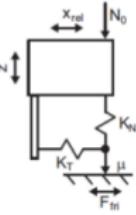
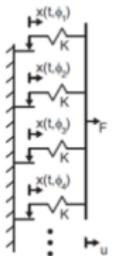
# Non-linear static analysis: results



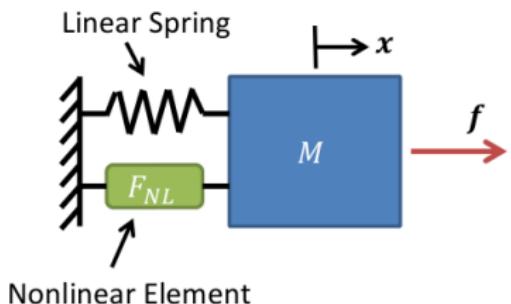
**Figure:** Contact pressure (left) and contact opening (right)

**Static solution used to set the non-linear dynamic simulations**

# Non-linear dynamic modelling approaches

	Stuttgart Approach	Imperial Approach	Sandia Approach
FE Tool	CalculiX	NASTRAN	SIERRA/SD
Model Fidelity	Craig-Bampton ROM	Rubin ROM	Craig-Bampton ROM
Nonlinear Element	2D Jenkins Element 	3D Contact Element 	Iwan Element 
Nonlinear Solver	ROCMAN	FORSE	ROMULIS
Solver Type	Harmonic Balance	Multi-Harmonic Balance	Transient Integration

# Comparison on a SDOF system

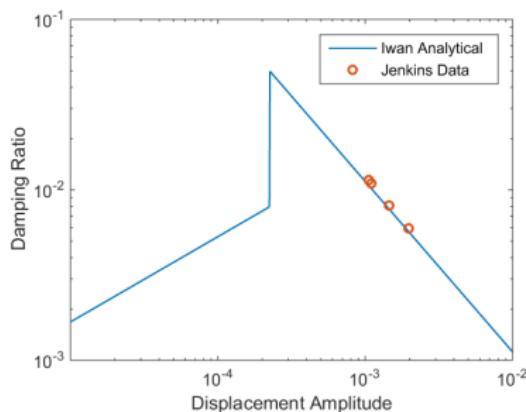


Equivalent damping ratio:

$$\zeta_r = \frac{D_r}{2\pi M |V_r|^2}$$

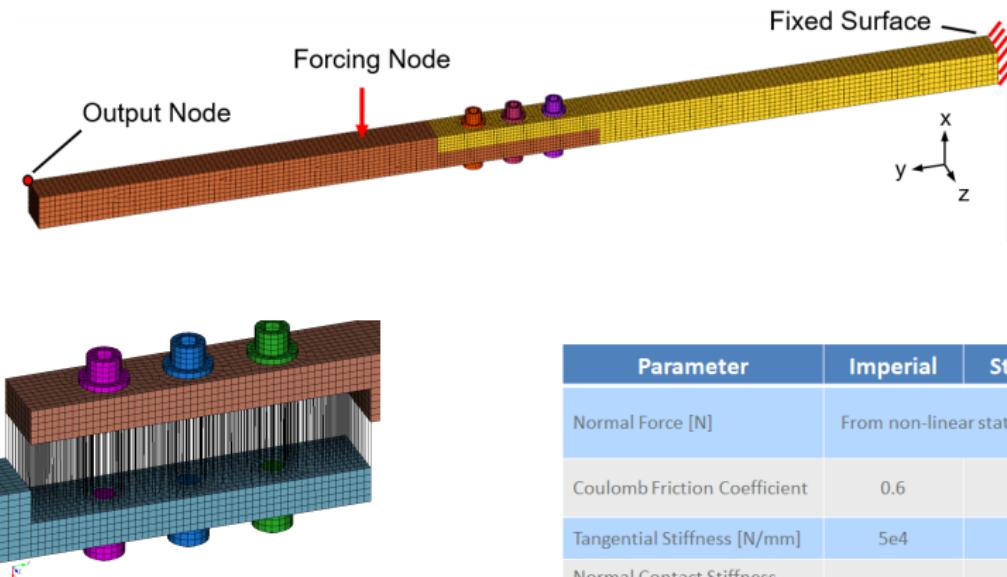
$D_r$ : energy dissipated per cycle

$V_r$ : velocity of the mass at resonance



**Match obtained but only in the macro-slip regime of the Iwan element**

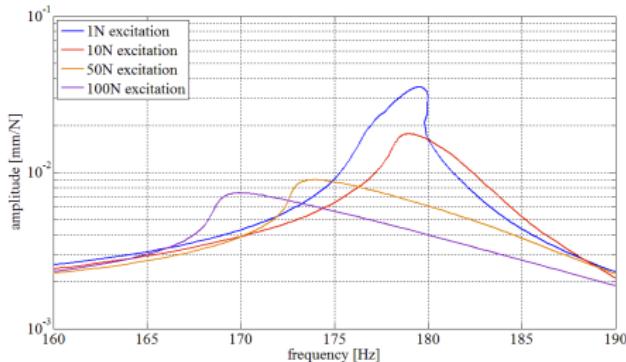
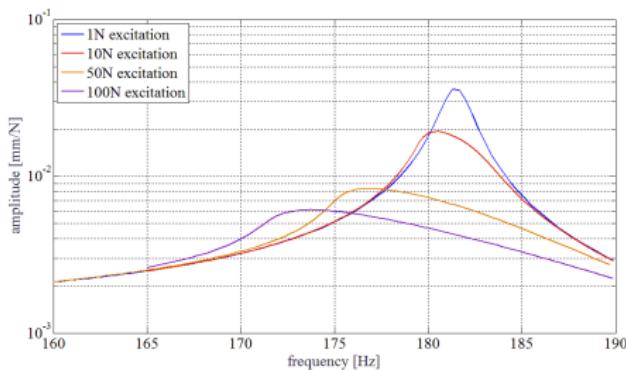
## Brake-Reuss beam NL dynamic analysis



**Figure:** Tie coincident nodes on the friction interface with Jenkins/3D contact elements

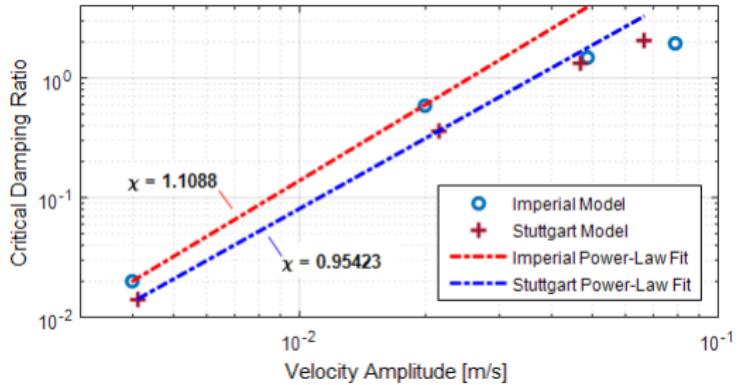
Parameter	Imperial	Stuttgart
Normal Force [N]	From non-linear static analysis	
Coulomb Friction Coefficient	0.6	0.6
Tangential Stiffness [N/mm]	5e4	5e4
Normal Contact Stiffness [N/mm]	1e6	MPCs
Number of Harmonics	1	1
Number of Nonlinear Elements	592	460

# Harmonic balance results



**Figure: Stuttgart (top) vs. Imperial non-linear FRFs (bottom)**

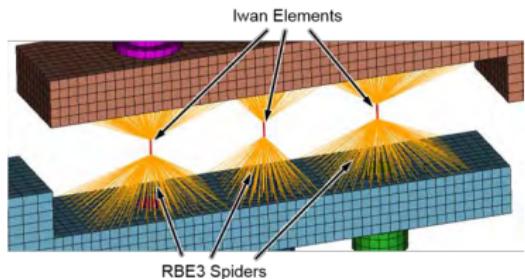
## Iwan element calibration (1/2)



- Power-law fit only valid for low amplitude (micro-slip)
- In previous works,  $\chi \approx -0.3$
- Large  $C_r$  leads to physically unreasonable value of  $K_t$

$$\zeta_r = C_r |V_r|^{\chi+1}$$

# Iwan element calibration (2/2)

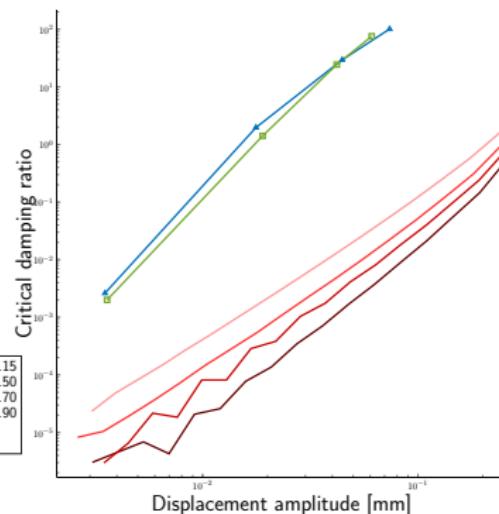
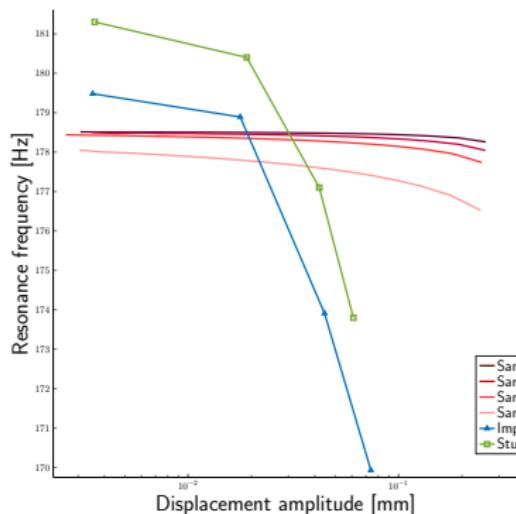


**Figure:** Iwan joint model

Parameter	Sandia
Slip Force [N]	2400
Tangential Stiffness [N/mm]	1e8
Power-law slope ( $\chi$ )	-0.15 to -0.9
Power-law intercept ( $\beta$ )	0.05
Number of Nonlinear Elements	6

**Figure:** Iwan element parameters

# Brake-Reuss beam results



**Figure:** Brake-Reuss beam: 2nd bending mode behaviour

## Conclusions and perspectives

- Particular care must be taken to model the bolt pretension to obtain accurate initial conditions at the contact interface prior to the non-linear dynamic simulations
- A comparison between transient and harmonic simulations was achieved by using amplitude-dependant variables
- A good agreement was obtained between the two harmonic approaches.
- Qualitative good agreement between the three methods in describing general joint behaviour
- Quantitatively, the Iwan model needs more parameters to reproduce the harmonic balance results

Further work:

- Use of non-linear normal modes as an alternative comparison metric
- Comparison with experimental results

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