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10 A joint experimental and theoretical study is presented for the electronic structures of copper oxides including
 11 Cu₂O, CuO, and the metastable mixed-valence oxide Cu₄O₃. The optical band gap is determined by experimental
 12 optical absorption coefficient, and the electronic structure in valence and conduction bands is probed by
 13 photoemission and electron energy loss spectroscopies, respectively. The experimental results are compared
 14 with many-body *GW* calculations utilizing an additional onsite potential for *d*-orbital energies that facilitates
 15 tractable and predictive computations. The side-by-side comparison between the three oxides, including a band
 16 insulator (Cu₂O) and two Mott/charge-transfer insulators (CuO, Cu₄O₃) leads to a consistent picture for the
 17 optical and band-structure properties of the Cu oxides, strongly supporting indirect band gaps of about 1.2 and
 18 0.8 eV in CuO and Cu₄O₃, respectively. This comparison also points towards surface oxidation and reduction
 19 effects that can complicate the interpretation of the photoemission spectra.

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I. INTRODUCTION

22 Cuprous oxide Cu₂O (cuprite) and cupric oxide CuO
 23 (tenorite) are important prototypical materials for the elec-
 24 tronic structure of oxides. As one of the first known semi-
 25 conductors, Cu₂O is a band insulator and still of active
 26 interest for studying exciton physics [1] and for solar energy
 27 conversion, due to the abundance of the elements, nontoxicity,
 28 and versatile fabrication routes [2–8]. CuO is described as a
 29 strongly correlated charge transfer insulator [9] and serves as
 30 a prototype system for high *T_C* superconductors [10]. Cu₂O
 31 and CuO have been widely studied for the past three decades,
 32 both experimentally [4,9,11–15] and theoretically [4,16–22].
 33 The third oxide phase, Cu₄O₃, is a metastable mixed-valence
 34 intermediate compound between Cu₂O and CuO [14,16,23–
 35 25] that occurs as the exceedingly rare mineral paramelaconite,
 36 giving rise to a mysterious veil.

37 The band structure of Cu₂O is experimentally well estab-
 38 lished, with a dipole forbidden direct gap at 2.17 eV and
 39 a difference of 0.45 eV between the first (forbidden) and
 40 second (allowed) conduction band at the zone center [4,26,27].
 41 Computationally, however, the accurate description of Cu₂O
 42 is still challenging. For example, even when different cal-
 43 culations agree in the direct band gap of about 2 eV, there
 44 can be discrepancies in the conduction band ordering [15,16].
 45 Although CuO has received wide attention since the discovery
 46 of high temperature cuprate superconductors, its electronic
 47 structure has not been fully settled. The onset of direct-
 48 allowed absorption has been determined at 1.57 eV at low
 49 temperature [15], but the type of band gap (direct [28–30] or
 50 indirect [12,16,21,31]) remains controversial. The correlated
 51 nature of CuO presents a greater challenge for electronic
 52 structure calculations. The local density approximation (LDA)
 53 fails to predict both band gap and magnetism in CuO. The

54 opening of a band gap and the correct antiferromagnetic 54
 55 ground state is obtained in LDA + *U* [31] and with hybrid 55
 56 functionals [16]. However, a band gap prediction is not pos- 56
 57 sible with these functionals, since LDA + *U* underestimates 57
 58 the Cu₂O gap (0.99 vs 2.17 eV), and hybrid functionals 58
 59 overestimate the CuO gap (2.74 vs 1.57 eV direct) [16]. A 59
 60 recent *GW* study demonstrated that the band gap energy and 60
 61 density of states (DOS) in CuO strongly depend on rather 61
 62 subtle details of the calculations [21]. The current knowledge 62
 63 about the electronic structure of Cu₄O₃ is even more limited. 63
 64 From optical absorption in thin films, the band gap was 64
 65 estimated between 1.3 and 2.5 eV, depending on whether 65
 66 a direct or indirect gap was assumed for the analysis [14]. 66
 67 Calculations using LDA + *U* and Heyd-Scuseria-Ernzerhof 67
 68 (HSE) hybrid functionals have been employed to calculate the 68
 69 electronic structure of Cu₄O₃ [16,24], but these results are 69
 70 subject to the same ambiguities as mentioned above for CuO. 70

71 In view of the interest in Cu oxides as solar energy 71
 72 conversion materials [4,8], it is highly desirable to fill the 72
 73 knowledge gaps that still exist in particular for the Cu²⁺ 73
 74 containing oxides. Hence, the aim of this joint experimental 74
 75 and theoretical study is to develop a comprehensive electronic 75
 76 structure picture across all three Cu oxides. Experimentally, 76
 77 we characterize thin film samples of Cu₂O, CuO, and 77
 78 Cu₄O₃. Photoemission spectroscopy with different photon 78
 79 energies is used to determine the valence band electronic 79
 80 structure. The optical properties are determined from optical 80
 81 absorption coefficient measurements by a spectrophotometry, 81
 82 which allows more direct access to the band gap energies 82
 83 than other optical methods, e.g., ellipsometry, especially 83
 84 in the presence of subgap absorption. For the conduction 84
 85 band structure, we employ electron energy loss spectroscopy 85
 86 (EELS), which has rapidly grown as a useful technique to study 86
 87 the unoccupied electronic states, with great advantages due to 87
 88 large penetration depth and high spatial resolution. In EELS 88
 89 measurements, electrons are excited from core states into unoc- 89
 90 cupied states [32], allowing the comparison with the calculated 90

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91 conduction band DOS under consideration of dipole selection
92 rules.

93 Computationally, many-body perturbation theory in the
94 GW approximation has emerged as a standard computational
95 tool to predict the electronic structures of semiconductors and
96 insulators, yielding systematic improvements with respect to
97 other methods [17,18,33–35]. Although various GW schemes
98 have been introduced and tested for transition metal (TM)
99 oxides, a single universal scheme that can describe the band
100 structures reliably for a wide range of TM oxides is not yet
101 available. Recently, a GW scheme with local-field effects and
102 an empirical onsite potential (V_d) for TM d orbitals has been
103 proposed, which allows for reasonably predictive band gaps
104 for different oxide stoichiometries and TM oxidation states at
105 an acceptable computational expense [17,36]. However, the
106 band gap is just one characteristic of electronic structure of
107 semiconductors or insulators and does not contain detailed
108 information on the electronic structure as a whole. Thus, we
109 here present a side-by-side comparison of the full optical
110 absorption spectrum and of the quasiparticle DOS in both
111 the valence and conduction band.

112 II. EXPERIMENTAL AND COMPUTATIONAL DETAILS

113 A. Experiments

114 Cu_2O , Cu_4O_3 , and CuO thin films were deposited on
115 glass and (100) silicon substrates at room temperature by
116 reactive pulsed-dc magnetron sputtering in an argon and
117 oxygen atmosphere. The Ar flow rate was fixed at 25 sccm,
118 while the O_2 flow rate was 13, 19, and 24 sccm for single
119 phase Cu_2O , Cu_4O_3 , and CuO , respectively. X-ray diffraction
120 and micro-Raman spectrometry were used to check the phase
121 structures. More details concerning the thin film growth and
122 the characterization can be found in Refs. [23] and [37].

123 The p -type conductivity of Cu_2O thin film has been iden-
124 tified by Hall effect measurements in a previous paper [38].
125 Here, positive Seebeck coefficients of Cu_4O_3 ($+102 \mu V/K$)
126 and CuO ($+180 \mu V/K$) thin films have been attained, indi-
127 cating p -type conductivity. The optical absorption coefficient
128 at room temperature was determined from transmission (T)
129 and reflectance (R) spectra measured by an ultraviolet-visible-
130 near-infrared (UV-Vis-NIR) spectrophotometry (Varian Cary
131 5000).

132 The photoemission spectra were measured in an ultrahigh
133 vacuum (UHV) experimental setup equipped with a photo-
134 emission analyzer (Scienta SES-200). Al $K\alpha$ (1486.7 eV) and
135 He I (21.2 eV) photon sources were employed for x-ray pho-
136 toemission spectroscopy (XPS) and ultraviolet photoemission
137 spectroscopy (UPS) measurements, respectively. The Ar^+ ion
138 etching was performed to clean the surface until there is no
139 evolution in the C-1s XPS core level spectra. Silver paste
140 was put in the corner of samples, contacting with the metallic
141 holder. The purpose of this is to relieve the charge effect during
142 the measurement and to identify the Fermi level by using silver
143 as a reference.

144 The EELS experiments were carried out in a transmission
145 electron microscopy (JEOL ARM 200-Cold FEG fitted with a
146 GIF Quantum ER) equipped with an EELS spectrometer. For
147 the acquisition of energy loss near edge structure (ELNES)

148 spectra, an accelerating voltage of 200 kV, an emission current
149 of $5 \mu A$ and an energy dispersion of 0.05 eV/ch were
150 employed. All the spectra were recorded in the image mode,
151 with the energy resolution of $0.45 \sim 0.5$ eV defined by the full
152 width at half maximum (FWHM) of the zero loss peak (ZLP).
153 The convergence semiangle α and the collection semiangle
154 β were 7 and 18 mrad, respectively. Before the EELS spectra
155 measurements, the cross-sectional thin foils were prepared by a
156 focused ion beam (FIB) scanning electron microscope (SEM)
157 dual beam system (FEI Helios 600) using the *in situ* liftout
158 technique. The FIB thinning was performed at high energy
159 (30 keV) followed by a cleaning step at low energy (5 keV) to
160 minimize surface amorphization effects and ion implantation.

161 B. Calculations

162 The electronic structures of Cu_2O , Cu_4O_3 , and CuO
163 were calculated within the GW method [39], employing
164 the projector augmented wave (PAW) implementation for
165 density functional theory (DFT) and GW calculations in the
166 Vienna *Ab initio* Simulation Package (VASP) code [40,41]. For
167 monoclinic CuO , the experimentally known low temperature
168 antiferromagnetic configuration [42] with a 16 atom unit cell
169 was used. In paramelaconite Cu_4O_3 , the 14 atom primitive
170 cell has four nonmagnetic Cu^{1+} and four magnetic Cu^{2+} ions,
171 and we used the lowest energy antiferromagnetic configuration
172 within this cell, as given in the generalized gradient approxima-
173 tion (GGA) [43] with a Coulomb parameter of $U = 5$ eV [44]
174 for Cu- d orbitals. As described in detail in Refs. [17] and [36],
175 the present GW scheme was defined as such to allow fairly
176 efficient calculations over a wide range of materials using
177 a uniform approach. Specifically, after an initial GGA + U
178 calculation, the wave functions are kept constant, and the GW
179 quasiparticle energies are iterated to self-consistency, using the
180 random phase approximation (RPA) for W . Density functional
181 theory derived local field (LF) effects are included via time-
182 dependent DFT (TD-DFT) [45], which increases somewhat
183 the dielectric response and consequently yields smaller band
184 gaps compared to the random phase approximation. Using an
185 energy cutoff of 330 eV and a total number of bands of 64^*n_{at} ,
186 where n_{at} is the number of atoms in the unit cell, this approach
187 yields fairly accurate band gaps for main group compounds,
188 typically with less than 10% deviation from experiment.

189 However, following this approach, the d -orbitals are sys-
190 tematically located at too high energies in the case of $3d$
191 oxides [17], which is likely the combined result due to several
192 limitations, i.e., the slow convergence behavior of d -orbital
193 energies with respect to the number of bands [46], omission
194 of vertex corrections [47,48], and spurious hybridization
195 effects in the DFT + U wave functions [49]. Rather than
196 resorting to computationally more demanding approaches,
197 this issue was addressed in the $GW^{LF} + V_d$ approach [17]
198 by an additional onsite potential V_d , which acts to lower
199 the d -orbitals energies, thereby placing them at the correct
200 energy relative to the spectrum of sp states. The potential
201 strength parameter was determined in Ref. [17] empirically
202 by comparison with experimental data for the $3d$ oxides. For
203 example, $V_d = -2.4$ eV was found for Cu- d based on data for
204 Cu_2O and CuO . Even though the V_d parameter is of empirical
205 nature, we found that it is fairly system independent, thereby

allowing real predictions for materials whose band gaps and optical properties are unknown. We further emphasize that V_d is simply a constant potential offset for the average d -orbital energy and does not directly affect electron correlation. All electron-electron correlation effects are handled by the GW method. Note that these present GW calculations are part of a larger dataset of electronic structure calculations for semiconductors and insulators, including TM compounds [36], which is accessible at <http://materials.nrel.gov>.

For the purpose of this paper, we use GW quasiparticle energy spectrum, which omits lifetime broadening effects and satellite structures. A more detailed analysis of these effects is in principle possible within the GW approach, but lies beyond the scope of this paper which focuses on the comparison between the different Cu oxides. Considering the different photoionization cross-sections for O- p and Cu- d states in UPS and XPS (see below), we determined the angular-momentum resolved partial DOS (PDOS), using an integration radius of 1.0 Å, so to facilitate the comparison with experiment. A Gaussian broadening with a width of 0.4 eV was used for comparison with the experimental spectra. Similarly, the PDOS is also used for the comparison with EELS spectra, where the transition matrix elements for the photoionization are rudimentarily accounted for by selecting the angular momentum for the PDOS according to the dipole selection rules. We also note that the electron-core hole interaction is not explicitly taken into account, i.e., the alignment of the computational and experimental spectra implies a rigid shift of the DOS due to the core hole effect. Explicit core-hole calculations can be done in supercell calculations in all-electron approaches, or by using the so-called $Z + 1$ approximation or core-hole pseudopotentials [50]. However, such supercell calculations usually require a more approximate DFT functional. Thus, an alignment is generally still needed, and the underestimated band gaps and band widths in DFT need to be corrected for [50]. By taking the results of GW calculations for the experiment-theory comparison, this paper aims to provide a better description of the conduction band quasiparticle energies but, on the other hand, relies on a rather basic model for simulating the spectra.

The optical absorption spectra are calculated in two different approximations, i.e., the independent particle approximation (IPA), and including excitonic effects within TD-DFT using a hybrid-functional kernel [45]. Here, we used a distance-independent fraction of $1/\varepsilon$ of the Hartree-Fock (HF) exchange, where ε is the static electronic dielectric constant obtained from the preceding GW calculation. These results are labeled “TD-HF” in the following. For better comparability, the k -derivatives of the wave functions were calculated using a finite differences approach [51] for either of the two approximations. The calculated TD-HF spectra are subject to a Lorentzian broadening of 50 meV width.

III. RESULTS AND DISCUSSIONS

A. Thermodynamic properties

Due to the intermediate stoichiometry of Cu_4O_3 between Cu_2O and CuO , it is interesting to investigate their thermodynamic properties. Several attempts have been made for this

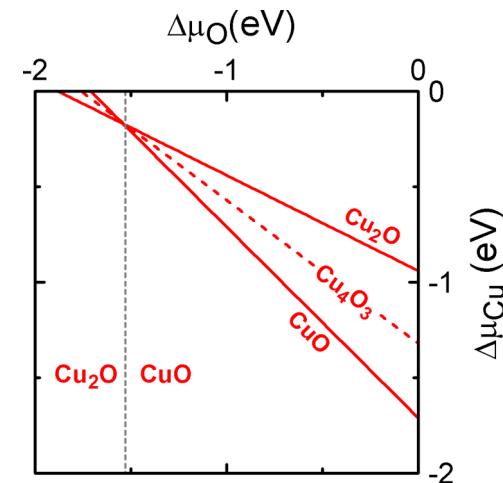


FIG. 1. Phase stability as a function of oxygen chemical potential ($\Delta\mu_O$).

purpose [16,52]. The experimental thermodynamic analysis performed by Bloibaum *et al.* [52] shows that Cu_4O_3 is a metastable phase with an upper stability limit that ranges between 670 and 800 K, above which it will decompose into Cu_2O and CuO according to the reaction



Using the total energies calculated in GGA + U and the elemental reference energies of Ref. [53], we show in Fig. 1, the phase stability as a function of the oxygen chemical potential. The transition between CuO and Cu_2O lies at $\Delta\mu_O = -1.53$ eV, close to the transition point at -1.51 eV obtained from tabulated experimental formation enthalpies of CuO and Cu_2O . In the vicinity of this phase transition, Cu_4O_3 is very close in free energy to Cu_2O and CuO . The decomposition energy of Cu_4O_3 according to Eq. (1) is found to be only 17 meV per formula unit (2 meV/atom). Such a small energy indicates a weak thermodynamic driving force for the decomposition of Cu_4O_3 . These results are qualitatively similar to the HSE calculations of Heinemann *et al.* [16], although the decomposition energy seems to be significantly larger in HSE. Experimentally, we observe that the thermal stability of Cu_4O_3 in air is close to that of Cu_2O , indicating similar kinetic barriers for the oxidation towards CuO which is the thermodynamic ground state in air ($p\text{O}_2 = 0.2$ atm) up to about 1000 °C.

B. Band gap

The band gap and optical properties of Cu_2O have already been widely studied in theoretical calculations and experiments [3,14,15,21,22,32,35,47]. Experimentally, it is well established that Cu_2O has a direct forbidden gap of about 2.17 eV and a direct optically allowed band gap of 2.62 eV (low temperature values). The results of the present GW calculations and thin film room temperature measurements for Cu_2O , Cu_4O_3 , and CuO are summarized in Table I, showing good overall consistency for all three oxides. For Cu_2O , it should be noted that this GW approach yields the correct conduction band ordering with a difference of

TABLE I. The band gap energies (in eV) of Cu_2O , Cu_4O_3 , and CuO obtained from the GW calculations and experiments. The direct (d) or indirect (i) nature of the gap (E_g) has been noted. (E_{abs}) is the absorption threshold energy for direct and allowed optical transitions (in the IPA), determined somewhat arbitrarily from $\alpha > 10^3 \text{ cm}^{-1}$. (E_{abs}^*) is the experimental optical absorption threshold energy, which is identified from the inflection point.

	GW calculation		Experiment
	(E_g)	(E_{abs})	(E_{abs}^*)
Cu_2O	2.04 (d)	2.53	2.5 ^a
Cu_4O_3	0.84 (i)	1.61	1.37
CuO	1.24 (i)	1.48	1.44

^aReference [38].

$\Delta E_C = +0.66 \text{ eV}$ between the allowed and the forbidden transition at Γ [17], slightly larger than the experimental value of $+0.45 \text{ eV}$ [4,26,27]. Without the onsite potential, the band ordering is inverted, even when a HSE hybrid functional is used as the starting point [17].

Figure 2(a) shows the experimental and calculated absorption coefficients α of Cu_4O_3 . The GW calculation predicts an indirect band gap of 0.84 eV and a direct band gap of 1.59 eV with an absorption onset of 1.61 eV in the IPA (see Fig. 2(a) and Table I), just above the direct gap. It should be pointed out that the calculations do not include phonon-assisted indirect transitions and are performed for the low temperature antiferromagnetic configuration, whereas magnetic fluctuations above the Neel temperature could affect the optical absorption in the experimental measurement. As seen in Fig. 2(a), the experimental optical absorption spectrum shows two regions, as indicated by the green dash lines. At photon energies larger than 1.37 eV , the absorption coefficient increases sharply with increasing photon energy. The tail below 1.37 eV is subject to the subgap absorption, and the oscillation is ascribed to the interference effect.

The origin of two absorption regions in experimental spectrum of Cu_4O_3 thin films could come from a variety of

factors. One possible source is the phonon assisted transitions with low intensity. As the indirect band gap of 0.84 eV predicted by the GW calculation is much lower than the direct band transition of 1.59 eV , the phonon assisted transitions at room temperature may cause absorption below the direct gap. Excitonic effects corresponding to the excitation of delocalized electron-hole pairs also contribute to the subgap absorption. As shown in Fig. 2(a), the excitonic effects in the TD-HF calculation cause a redshift of about 150 meV compared to the IPA. Other intraatomic $d-d$ and/or $s-d$ excitations could also produce subgap absorption in TM oxides, although they have not been reported in binary copper oxides. Yet another source of subgap absorption could be defect states. In Cu_2O , a defect band tail has been clearly identified by the analysis of subgap absorption [38], which is also detected in the present UPS spectrum with the nonzero states close to Fermi level (see the supporting information). However, such nonzero states are not noticeable in Cu_4O_3 and CuO thin films, indicating that valence band tails are less prevalent in these materials. On the other hand, the large estimated Urbach energy of 0.77 eV (equal to 56% of the optical absorption threshold energy) seems to be inconsistent with the high degree of crystallinity of the Cu_4O_3 thin films (see Ref. [23]), thus speaking against subgap absorption due to defect band tails. While the different mechanisms may jointly contribute to the absorption below the direct gap, the spectra are consistent with the picture given by the present GW calculations. Thus, the observation of an absorption tail corroborates the prediction of an indirect band gap.

Previous HSE calculations gave a much larger band gap of Cu_4O_3 at 2.5 eV and also showed a significant overestimation for CuO [16]. These discrepancies for the Cu^{2+} containing oxides are surprising, since the HSE functional gives a very accurate description of the Cu^{1+} oxide Cu_2O [16,17]. Even when considering that the appropriate fraction of Fock exchange (fixed at $\alpha = 0.25$ in HSE) should decrease with increasing dielectric screening, the observed trends of HSE band gaps are hard to reconcile, as the dielectric constants vary only little between the three oxides. From our present GW calculations, we obtain electronic static dielectric constants

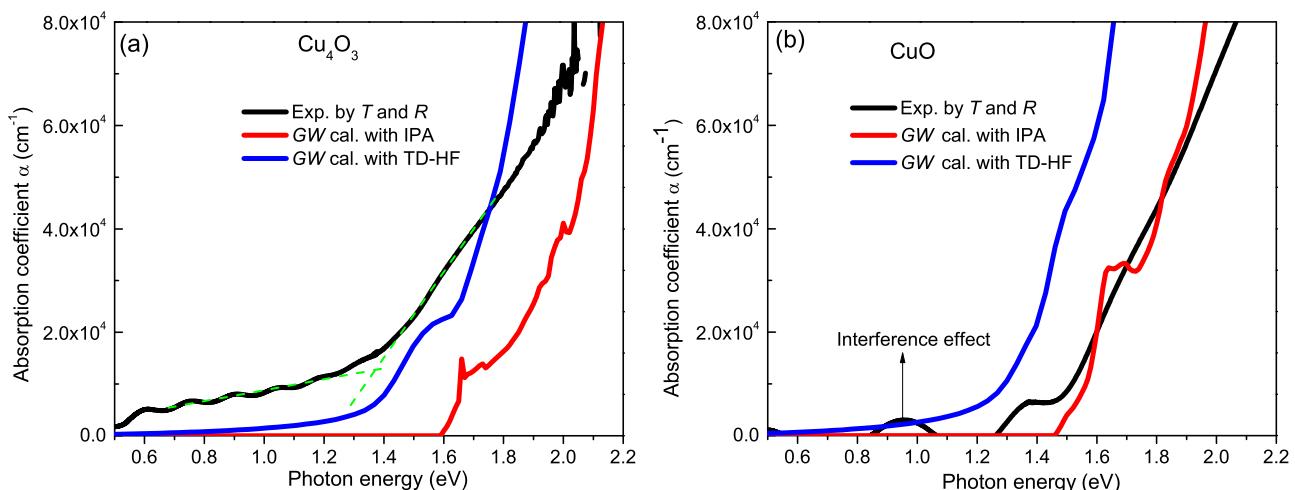


FIG. 2. (a) Experimental and calculated absorption coefficients of Cu_4O_3 . The green dashed lines show two regions with different slopes of the absorption coefficient as a function of the photon energy. (b) Experimental and calculated absorption coefficients of CuO .

of $\varepsilon = 5.7$, 6.2 , and 7.1 for Cu_2O , Cu_4O_3 , and CuO . Thus, as a signature of electron correlation in Cu^{2+} oxides, the magnitude of the band gap seems to be affected by dynamic (energy dependent) or nonlocal screening effects within the $\text{Cu}-d^9$ manifold, which are included in GW , but not in the HSE Hamiltonian.

Moving on to CuO , the experimental and calculated absorption coefficient spectra are shown in Fig. 2(b). An indirect band gap of 1.24 eV and a direct band gap of 1.46 eV are predicted by the GW calculation (see Table I). As seen in Fig. 2(b), the experimental absorption of the CuO thin film also shows two different regions: the absorption rises fast when the photon energy is over 1.44 eV; the absorption at photon energy between 1.3 and 1.44 eV is weak, but quite clear, even when considering the interference effect. Such absorption below the direct gap has also been observed in single crystal CuO between 10 and 300 K [15]. The experimental absorption onset energy of about 1.44 eV at room temperature here agrees well with the theoretical value of 1.46 eV, as well as the onset at 1.34 eV in the single crystals at 300 K [15]. The same mechanisms for a slow absorption onset as discussed above for Cu_4O_3 apply here as well. For instance, the excitonic effects calculated by TD-HF theory cause a similar redshift, as shown in Fig. 2(b). The difference between the calculated indirect and direct band gaps is much smaller in CuO than in Cu_4O_3 , which could explain the fact that the low energy tail in the absorption spectrum of Cu_4O_3 is more pronounced than in CuO . This observation again supports the presence of an indirect gap.

Similar to the case of Cu_4O_3 , previous HSE calculations for CuO also showed a large overestimation of the band

gap [16]. A recent paper comparing different GW schemes noted the extreme sensitivity of the band gap depending on the starting point and degree of self-consistency [21]. While details of electronic screening and subtle differences in the electronic wave functions evidently play an important role, the physical origin of these variations is not well understood. From a practical perspective, the current GW results provide a consistent description between Cu_2O , Cu_4O_3 , and CuO , but it is also clear that these materials will remain crucial test cases for future developments in electronic structure theory.

C. Valence band electronic structure

The valence band electronic structure has been investigated by XPS and UPS and is compared with the calculated DOS. Before discussing the results in detail, we briefly comment on the relative sensitivities of the two photoemission sources on the $\text{O}-2p$ and $\text{Cu}-3d$ spectral weights. $\text{Al K}\alpha$ (1486.7 eV) and He I (21.2 eV) sources have been employed to record the valence band spectra for XPS and UPS, respectively. The cross-section ratios of $\sigma(\text{O} - 2p)/\sigma(\text{Cu} - 3d) \approx 0.02$ and 1.41 for $\text{Al K}\alpha$ and He I , respectively, are determined utilizing the known energy dependence of the photoionization cross-section [55]. This means that XPS primarily probes the d states, whereas $\text{O}-p$ states are excited with higher, albeit comparable, probability than the $\text{Cu}-d$ states in UPS. It is also important to note that UPS is more surface sensitive than XPS and thus very sensitive to surface contamination and surface oxidation or reduction processes.

The photoemission valence band spectra and the theoretical DOS of Cu_2O are shown in Fig. 3(a), where the valence

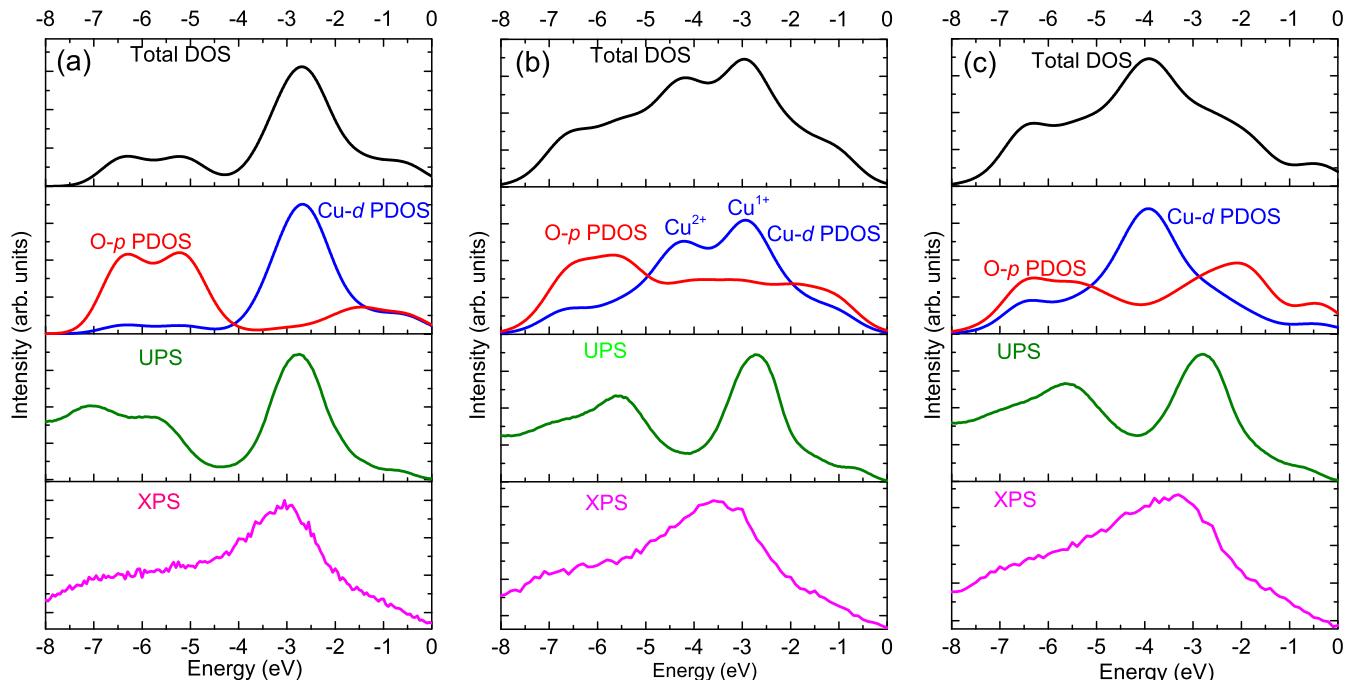


FIG. 3. Experimental valence band spectra and theoretical DOS for (a) Cu_2O , (b) Cu_4O_3 , and (c) CuO . The VBM is set to zero. The theoretical total DOS (in black), $\text{O}-p$ (in red) and $\text{Cu}-d$ (in blue) PDOS are convoluted with a Gaussian broadening of 0.4 eV to mimic temperature and instrumental broadening effects. All theoretical DOS have been normalized to integrate to unity over the valence band. The UPS and XPS spectra are plotted in green and magenta, respectively.

band maximum (VBM) is set to zero. One can distinguish three energy regions in the theoretical DOS. Between -8 and -4 eV, it is dominated by O- $2p$ character. Pronounced Cu- $3d$ states are concentrated in the energy range of -4 to -1.5 eV with a peak at -2.7 eV. Due to hybridization, the states close to the VBM (-1.5 to 0 eV) have both Cu- $3d$ and O- $2p$ character with similar intensities. As shown in Fig. 3(a), the UPS spectrum is consistent with the calculated DOS when considering the contributions from both O- $2p$ and Cu- $3d$. As expected, the XPS spectrum shows mainly the Cu- $3d$ contributions, and the features due to the O- $2p$ states are less pronounced. Looking at the dominant O- $2p$ character in the energy range of -8 to -4 eV, the theoretical DOS exhibit similar shape with respect to UPS spectrum, but the theoretical peak positions are shifted approximately 0.6 eV to higher energies. This discrepancy indicates that the present GW calculations underestimate somewhat the valence band width. Notably, HSE calculations [16,17] reproduce the energies of the O- $2p$ related peaks between -8 and -5 eV almost perfectly, notwithstanding the above discussed issues related to the band gaps of the Cu $^{2+}$ containing oxides.

Figure 3(b) compares the photoemission spectra and theoretical DOS for the metastable mixed-valence phase Cu $_4$ O $_3$. The O- $2p$ PDOS stretches over the entire valence band energy range but has an increased intensity between -7 and -5 eV, which is also reflected in the UPS spectrum. The Cu- $3d$ PDOS has a double-peak structure with maxima at -2.9 and -4.3 eV, corresponding to Cu $^{1+}$ and Cu $^{2+}$ sites, respectively. The larger binding energy of the Cu $^{2+}$ sites can be understood by the reduction of the Coulomb repulsion in the d^9 configuration as compared to the d^{10} configuration of Cu $^{1+}$, thereby indicating correlation effects. The UPS spectrum shows a peak at -2.7 eV, in good agreement with the calculated peak position due to Cu $^{1+}$, but the expected lower energy signal for Cu $^{2+}$ is not observed. Indeed, the UPS spectrum shows a valley in the energy range around -4 eV. Note that the calculated PDOS due to O- $2p$ is practically constant in this energy range and should not affect the peak position measured by UPS. In the XPS spectrum, however, we observe peak shift to lower energies at about -3.5 eV, which agrees reasonably well with the average of the calculated Cu $^{1+}$ and Cu $^{2+}$ peaks. The absence of the Cu $^{2+}$ peak expected from theory and the pronounced shift of the peak position between UPS and XPS (which is hard to explain by the O- p contribution in UPS) could indicate that the surface near the region probed by UPS is a more reduced Cu oxide phase compared to the Cu $_4$ O $_3$ bulk. The deeper probing depth of XPS picks up the contributions from both oxidation states of Cu, leading to a broadening and shift of the apparent peak energy. Such surface reduction effects seem also to be present in CuO and are likely related to the vacuum instabilities observed in previous photoemission papers [56], as discussed below.

Moving on to monoclinic CuO, we first compare our experimental valence band spectra for CuO thin-films with previously reported experimental results (see the supporting information), demonstrating the consistency with literature data. In Fig. 3(c), the experimental CuO valence band spectra are shown in comparison to the calculated DOS. The O- $2p$ DOS shows up in the low energy range between -7 and -5 eV, similar to the case of Cu $_2$ O and Cu $_4$ O $_3$, but now also dominates

the energies close to the VBM. This behavior can be expected because increasing the Cu oxidation state from $+1$ (d^{10}) to $+2$ (d^9) lowers the d -orbital energy due to reduced Coulomb repulsion, so that the O- $2p$ intensities dominate at the higher energies. The Cu- $3d$ DOS exhibits a single peak structure with a maximum at about 4 eV below the VBM. Since the Cu- $3d$ peak is straddled by O- $2p$ contributions at both higher and lower energies, CuO cannot unambiguously be labeled as Mott or charge transfer insulator.

It is notable that the Cu- $3d$ peak positions occur rather consistently around -3 and -4 eV for Cu $^{1+}$ and Cu $^{2+}$, respectively, across all three oxides. At first glance, however, the UPS spectrum for CuO seems to be inconsistent with the calculated DOS. The peaks at -2.8 and -5.5 eV roughly resemble the structure of the O- $2p$ DOS, but the UPS shows a valley at -4 eV, i.e., at the energy where the calculations place the Cu- $3d$ peak. Even when considering the slightly larger UPS cross-section for O- $2p$ than for Cu- $3d$, this discrepancy is difficult to reconcile. However, in the XPS spectrum with more Cu $3d$ sensitivity and larger penetration depth than UPS, the peak shifts to about -3.5 eV closer to the predicted Cu- $3d$ maximum. The peak at about -3 eV in the UPS spectrum of CuO has also been observed by Thuler *et al.* [57] and Shen *et al.* [56]. However, Shen *et al.* also observed a sideband feature at -4 eV, which disappeared after exposure to vacuum and which was speculated to be due to nonbonding oxygen states. However, in light of the present UPS and XPS measurements for both Cu $_4$ O $_3$ and CuO and the respective GW calculations, it seems likely that the UPS spectra largely correspond to a reduced Cu $_2$ O-like surface phase and that the XPS spectra represent a superposition of intensities from near-surface Cu $^{1+}$ ions and from Cu $^{2+}$ ions located in the actual Cu $_4$ O $_3$ and CuO phases. This interpretation would also explain the strong similarities of both UPS and XPS between Cu $_4$ O $_3$ and CuO [cf. Figs. 3(b) and 3(c)], despite the clearly different characteristics in the conduction band DOS as observed by EELS (see below), which has a much larger probing depth.

D. XPS core level and EELS spectra

The Cu $2p_{3/2}$ XPS core level spectra of copper oxides are shown in Fig. 4. Satellite peaks in CuO due to the intraatomic multiplet coupling and hybridization have been clearly observed, but they are absent in Cu $_2$ O, which agrees with the well-known characteristics of Cu $_2$ O and CuO [9]. Similar satellite peaks in Cu $_4$ O $_3$ demonstrate the configuration of Cu $^{2+}$ in the ground state. The FWHMs of the main peaks at about 933 eV are 1.7 , 1.9 , and 2.3 eV in Cu $_2$ O, Cu $_4$ O $_3$, and CuO, respectively. Due to the similar peak shapes and peak positions, the Cu $2p_{3/2}$ XPS core level spectra do not allow us to further resolve differences between the Cu oxides.

In order to further study the electronic structure of the Cu oxides, we therefore employed EELS. The ELNES spectra of Cu $L_{2,3}$ and O K edges are shown in Figs. 5(a) and 5(b), respectively. The spectral shape and the relative position of the Cu $L_{2,3}$ edges in CuO and Cu $_2$ O are in excellent agreement with previous reports of x-ray absorption spectroscopy (XAS) [13,22,58], including the substructures indicated by asterisks in Fig. 5 in Cu $_2$ O. As seen in Fig. 5(a), strong and

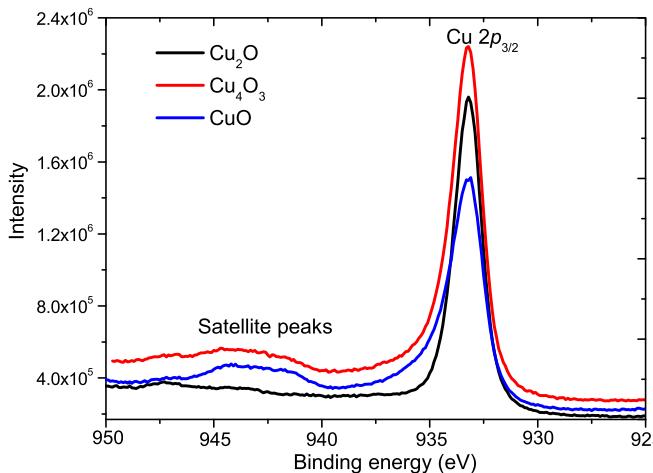


FIG. 4. Cu $2p_{3/2}$ core-level XPS spectra of Cu_2O , Cu_4O_3 , and CuO thin films.

sharp $L_{2,3}$ white lines have been clearly observed in Cu_2O , which is in contrast to the traditional simple ionic model. The dipole selection rules allow transitions from the $2p$ level into final states of s ($\Delta l = -1$) or d ($\Delta l = +1$) character, but the $\Delta l = -1$ channel is extremely low, and it can be safely ignored in a first approximation [11]. Hence, the presence of L edges white lines in EELS or XAS requires empty d orbitals, which should be absent in the ionic model for Cu^{1+} with a closed $3d^{10}$ shell. However, there is quite a strong consensus that the sharp $\text{Cu } L_{2,3}$ white lines in Cu_2O can always be measured by EELS or XAS [11,13,22,58]. The origin of this kind of unfilled $3d$ shell in Cu_2O remains controversial. One hypothesis assumes that the $3d$ shell of metallic Cu just contains 9.6 electrons, and there are only 9.5 electrons in the $3d$ orbital of Cu_2O [59,60]. Since this assumption employs the questionable white lines in metallic Cu, we believe that this hypothesis may require careful reconsideration. Another explanation could be the pronounced onsite Cu $3d$ - $4s$ hybridization, which is allowed by symmetry in Cu_2O , will produce a significant intensity of unoccupied d_z^2 states in the conduction band [17], thereby providing a channel for excitation of Cu- $2p$ core level electrons.

Checking the peak positions of Cu $L_{2,3}$ white lines in Cu_2O and CuO [see Fig. 5(a)], it is revealed that the positions of Cu $L_{2,3}$ edges are shifted to lower energy loss for the higher oxidation state. This contradicts the trends in Mn, V, and Fe oxides, in which the energy loss moves to higher energy for the higher oxidation state [61]. Employing the Cu L_3 edges of Cu_2O and CuO as references, the white lines of Cu_4O_3 can be identified easily, where the strongest peak with the energy loss of 931.1 eV corresponds to Cu^{2+} , and the peak at 933.7 eV corresponds to Cu^{1+} , as shown in Fig. 5(a). A similar structure exists at the L_2 edge. Concerning the O K edges, these three phases also exhibit significant differences, as shown in Fig. 5(b). Cu_2O shows a prominent peak at 532.5 eV and minor features at higher energy loss. In Cu_4O_3 , four energy loss peaks are found at energies of 530.5, 533.4, 536, and 541 eV, whereas in CuO , there are features at 528.4, 532.9, 537.4, and 541 eV. These ELNES features distinguish the different Cu oxide phases more clearly than the XPS and UPS spectra discussed above.

E. Conduction band electronic structure

The L_3 edge in ELNES corresponds to $2p_{3/2}$ electrons being excited into unoccupied d states above Fermi level, while O K edge represents $1s$ electrons being excited into empty p states, within the consideration of the parities of the initial and final states. Thus, it is interesting to compare the experimental Cu L_3 ELNES spectrum with the calculated Cu- d PDOS in the conduction band and, similarly, the O K edge spectra with the O- p PDOS. Figures 6(a) and 6(b) show that the GW calculated unoccupied Cu- d and O- p PDOS match well the basic shape of the respective experimental Cu L_3 and O K ELNES spectra in Cu_2O . The ELNES spectra in Cu_4O_3 exhibit a much richer structure and more features both in the Cu L_3 and O K spectra, which is related to the coexistence of Cu^{1+} and Cu^{2+} states. Given the simplicity of the approach to compare the experimental spectra with the PDOS (see discussion above), the computational results describe the measured features remarkably well. For example, the two peaks in the Cu L_3 spectrum [Fig. 6(c)] around 1 and 4 eV can be clearly ascribed due to Cu^{2+} and Cu^{1+} sites in

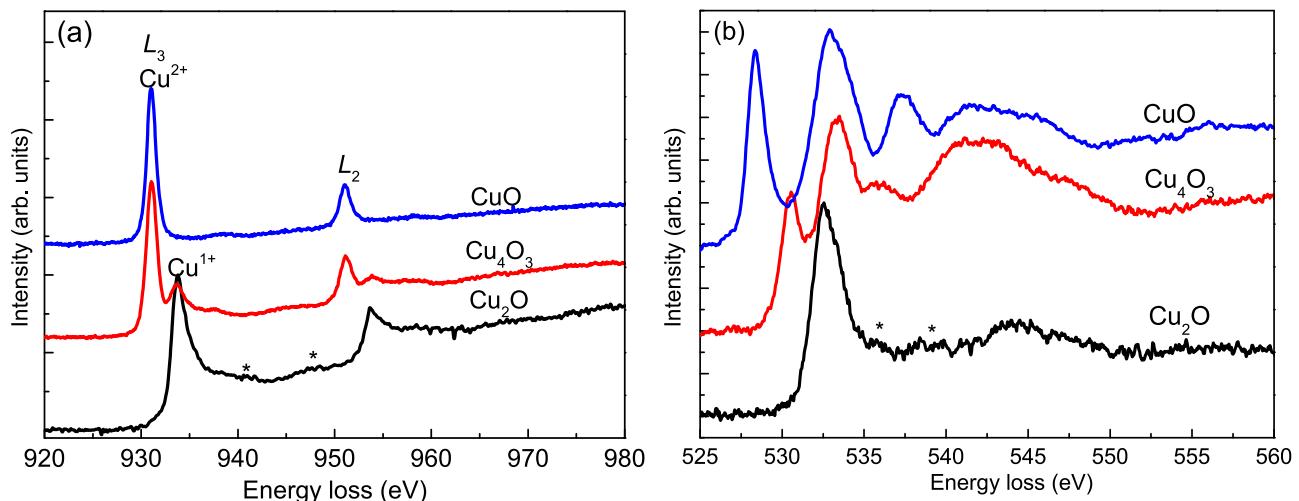


FIG. 5. (a) Cu $L_{2,3}$ edges and (b) O K edge ELNES spectra of Cu_2O , Cu_4O_3 , and CuO , normalized to the peak height.

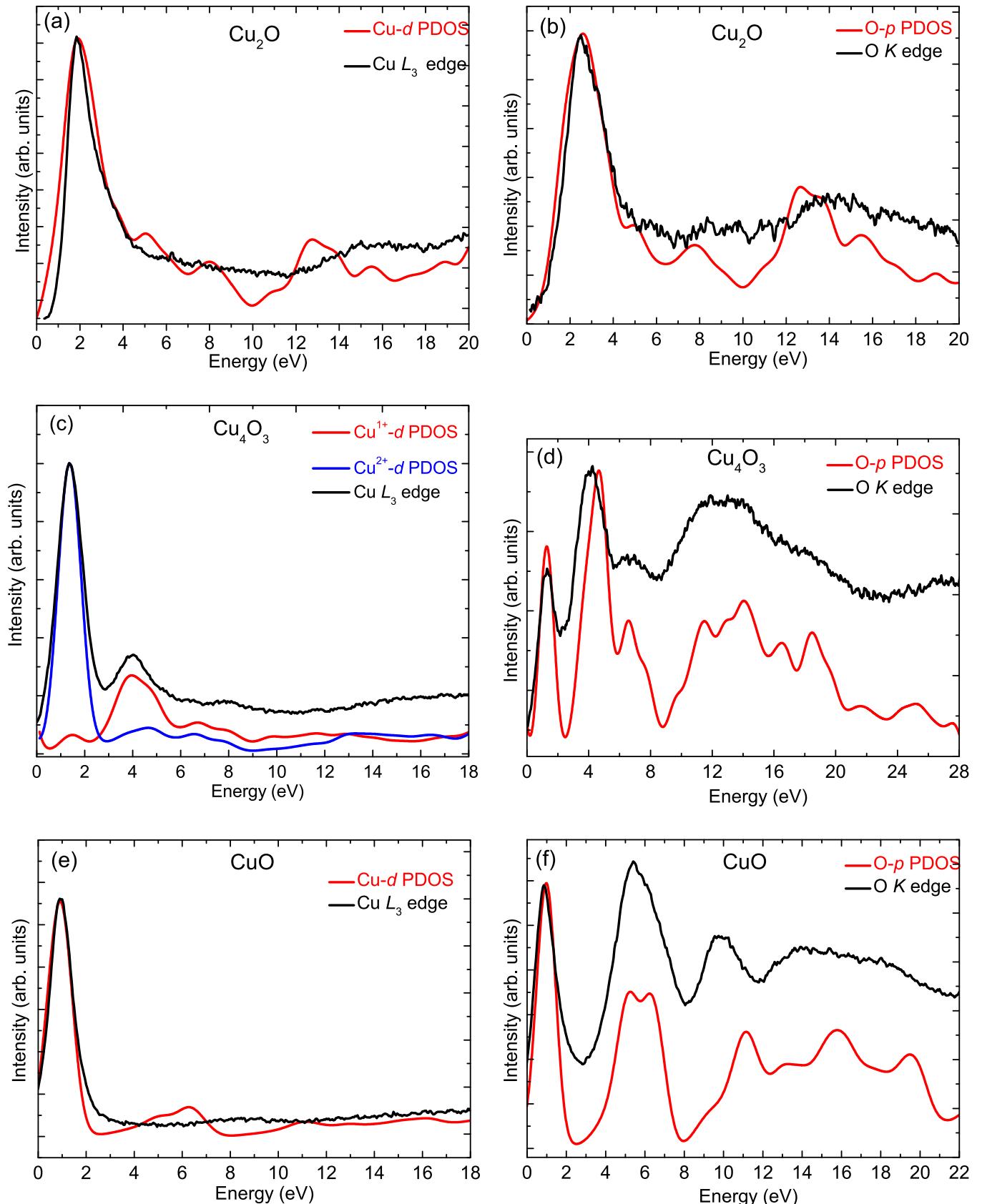


FIG. 6. The comparison between experimental Cu L_3 edge ELNES spectrum and Cu- d PDOS in conduction band for (a) Cu_2O , (c) Cu_4O_3 , and (e) CuO . The comparison between experimental O K edge ELNES spectrum and O- p PDOS in conduction band for Cu_2O , Cu_4O_3 , and CuO is displayed in (b), (d), and (f), respectively. The experimental spectra are shifted to align with the leading peak of PDOS.

600 Cu_4O_3 , respectively, based on the comparison with the GW 641 calculations. Similarly, the features in the $\text{O } K$ spectrum are 642 well described by the PDOS up to energies of about 20 eV 643 above the conduction band minimum (CBM) [Fig. 6(d)].

604 The comparisons for CuO are shown in Figs. 6(e) and 6(f), 644 which demonstrates that also here most of the experimental 605 features are well reproduced by the theory, even though some 645 minor differences are observed, e.g. the peak at about 4 eV 606 in $\text{O } K$ edge of Cu_4O_3 has a shift with theoretical position 646 [see Fig. 6(d)], or the peak at 6 eV in $\text{Cu-}d$ PDOS of CuO is 607 not clearly observed in the experiments [see Fig. 6(e)]. Such 647 differences could well result from the simple PDOS model 608 that does not fully account for the optical transition matrix 648 element and for the energy dependence of the electron-core 609 hole interaction.

615 IV. CONCLUSIONS

616 A joint experimental and theoretical study has been carried 649 out to investigate the electronic structures of Cu_2O , Cu_4O_3 , and 650 CuO thin films. Optical absorption, photoemission, and EELSS 651 have been employed to determine the band gap, valence, and 652 conduction band structures, respectively, which are compared 653 with theoretical results from many-body GW calculations 654 employing an additional onsite potential for the $\text{Cu-}d$ orbital 655 energies. Applying this approach to the less studied oxide 656 Cu_4O_3 , we predict an indirect band gap of 0.84 eV and a 657 direct band gap of 1.59 eV. For CuO , we obtain an indirect 658 band gap of 1.24 eV and a direct band gap of 1.46 eV. The 659 consistency between the calculated and measured absorption 660 spectra corroborates the prediction of indirect band gaps in 661 these Cu^{2+} containing oxides.

662 X-ray photoemission spectroscopy and UPS have been 662 combined together to study the valence band structure. In 663 combination with the theoretical electronic structure results, a 664 consistent picture was obtained where the $\text{Cu-}d$ photoemission 665 peaks of Cu^{2+} and Cu^{1+} lie around -4 and -3 eV relative to 666 the VBM, respectively, across all three oxides. Fully accounting 667 for hybridization effects and band dispersion, the GW 668 calculations reveal that the $\text{O-}p$ DOS straddles the DOS peak 669 of the $\text{Cu-}d^9$ manifold. Thus, CuO cannot be unambiguously 670 described as either Mott or charge transfer insulator, but has 671 features of both. An important finding for the interpretation of

672 photoemission data is that CuO and Cu_4O_3 seem to be subject 673 to surface reduction under vacuum conditions, leading to the 674 attenuation of the Cu^{2+} peak at -4 eV and to a shift of the 675 apparent peak position between XPS and UPS. As a result of 676 the surface reduction, the photoemission spectra of CuO and 677 Cu_4O_3 are hardly distinguishable.

678 The comparative study across the three Cu oxides benefited 678 greatly from the application of EELS, which resolves the rich 679 structure of electronic structure features in the conduction 680 band. Since EELS is much less surface sensitive, it offered a 681 significant advantage over XPS to distinguish the three phases 682 in the $\text{Cu } L_{2,3}$ edges or $\text{O } K$ edge spectra. The predicted PDOS 683 in the conduction band agrees remarkably well with the EELS 684 spectra, providing further confidence in the computational 685 description of the overall electronic structure.

686 Notwithstanding the use of the V_d onsite potential, which 686 acts as a simple potential offset of equal magnitude for 687 all three oxides, it is remarkable that the GW method 688 provides a consistent electronic structure picture across both 689 correlated Mott/charge-transfer insulators (CuO , Cu_4O_3) and 690 band insulators (Cu_2O). This is not possible, for example, 691 in hybrid functional calculations without a materials specific 692 parameter adjustment. This finding strongly suggests that 693 electron correlation effects are rather well captured in GW . 694 Thus, addressing current technical limitations, such as the 695 quality of input wave functions, the convergence of RPA 696 response functions, and vertex corrections, will likely enable 697 fully parameter-free predictions of band structures and optical 698 properties in correlated materials.

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