

Third harmonic generation in ultrathin epsilon-near-zero media

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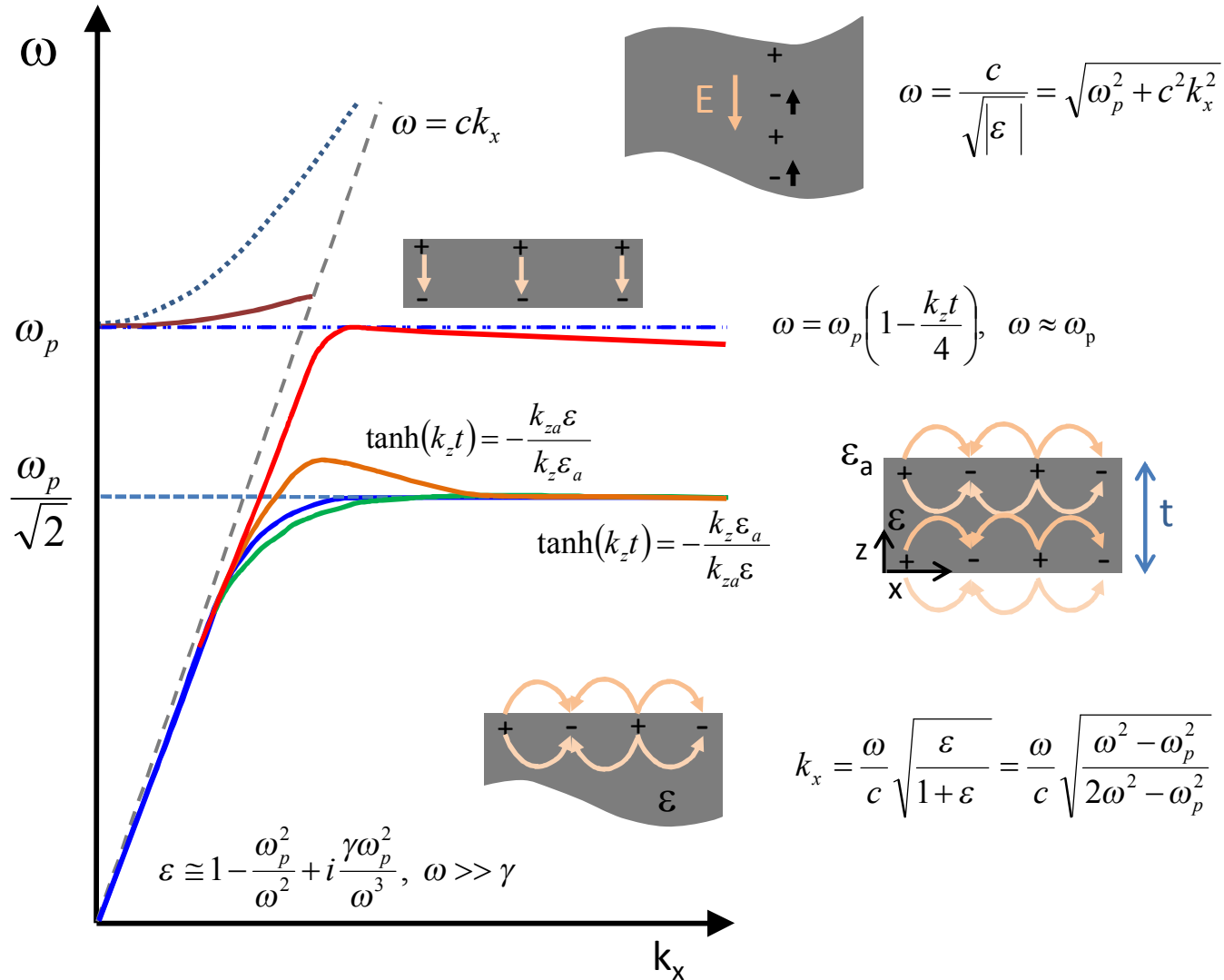
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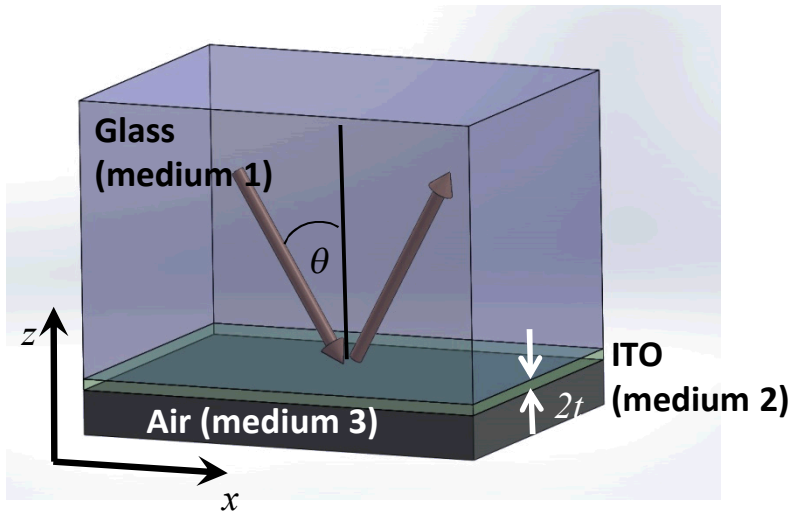
Outline

- ENZ mode in ultrathin film
- Critical coupling to the ENZ mode
- Results of enhanced THG using ENZ mode

ENZ mode and dispersion



ENZ mode dispersion and critical coupling

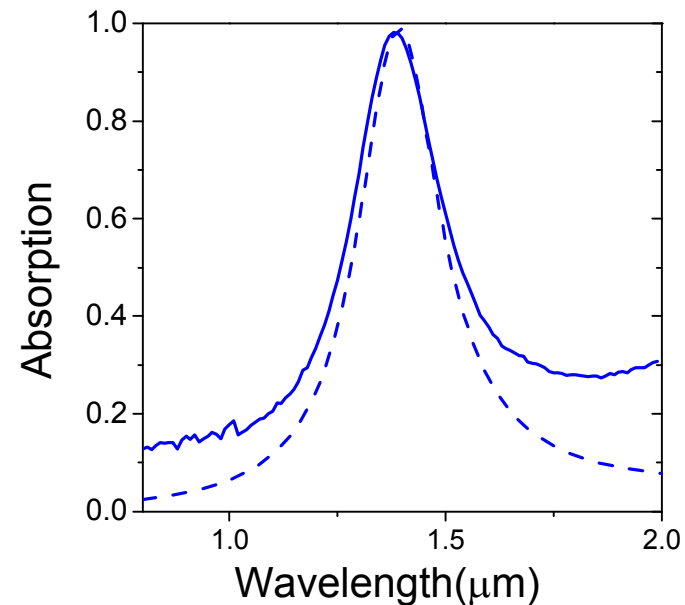
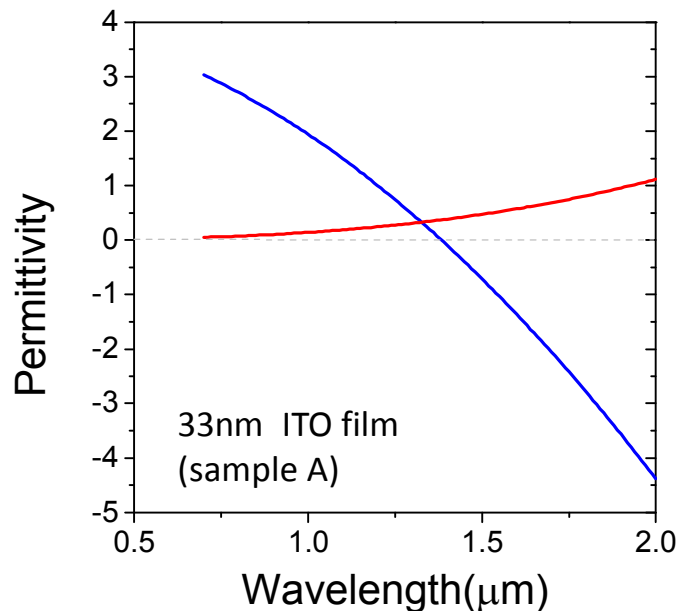


Airy Formula
$$\Gamma = \frac{r_{01} + r_{12}e^{2i\phi}}{1 + r_{01}r_{12}e^{2i\phi}} \quad \phi = k_{1\perp}t$$

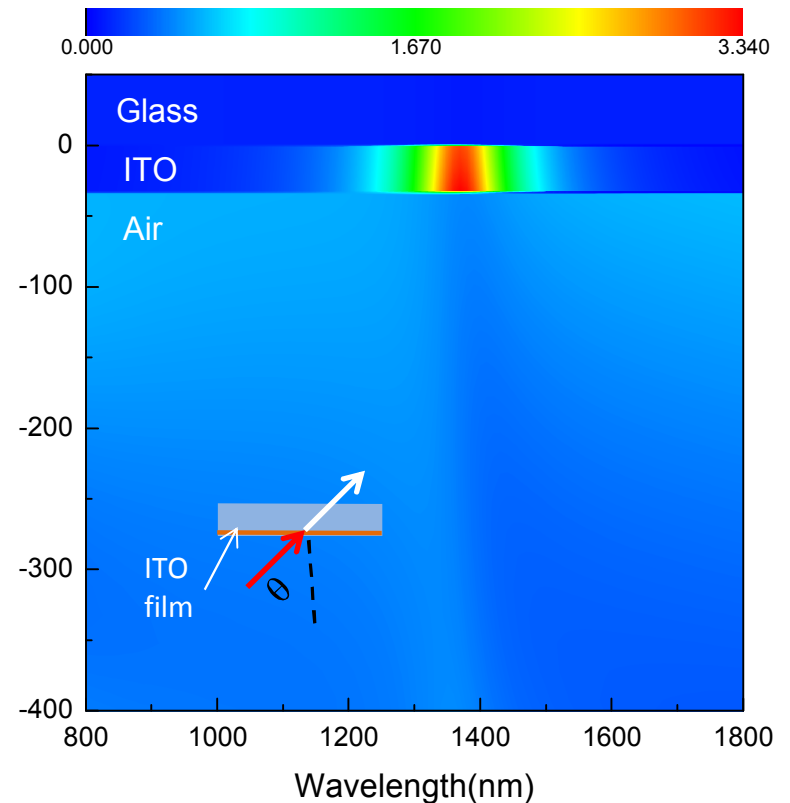
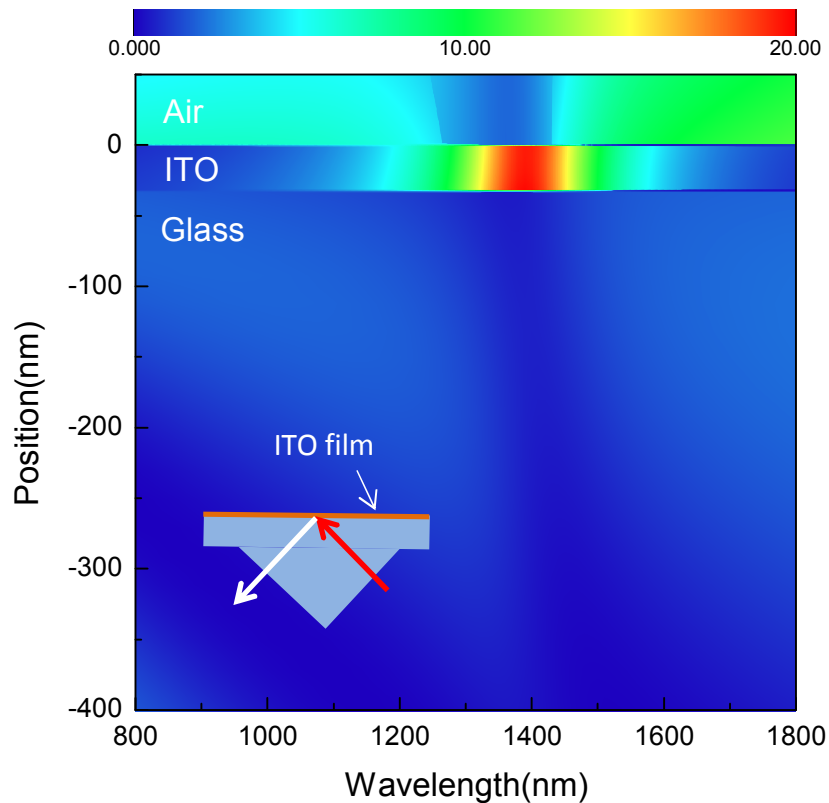
Mode dispersion:
$$r_{01}r_{12}e^{2i\phi} = -1$$

Critical coupling condition:
$$r_{01} = -r_{12}e^{2i\phi}$$

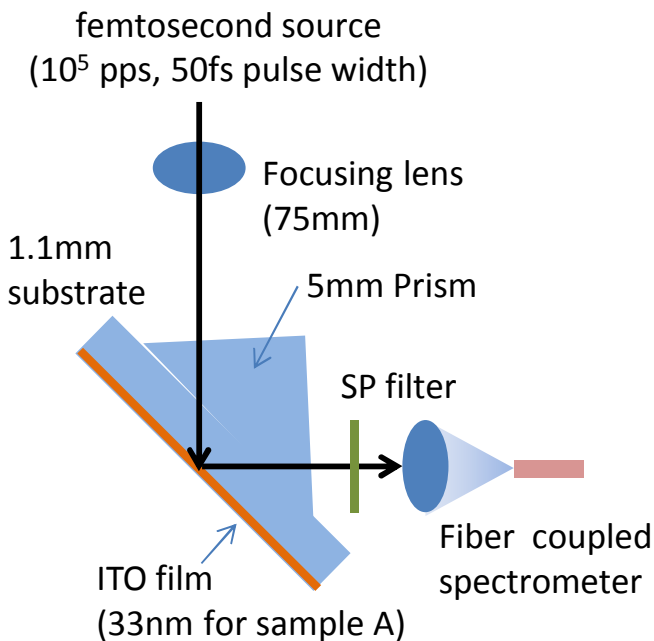
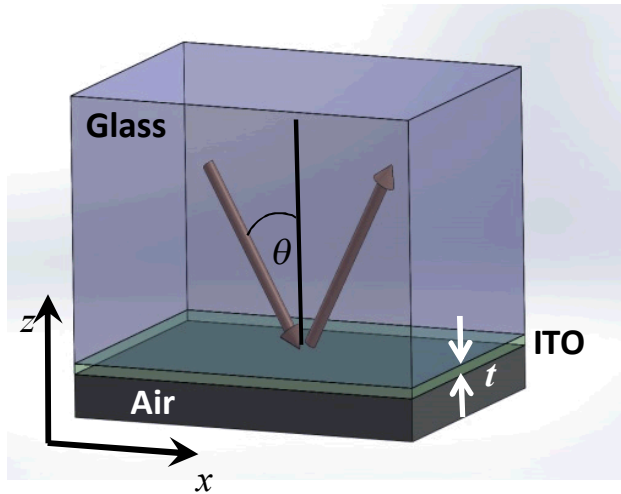
T. S. Luk et. al, *PRB*, (2014)



Field enhancement of ENZ mode



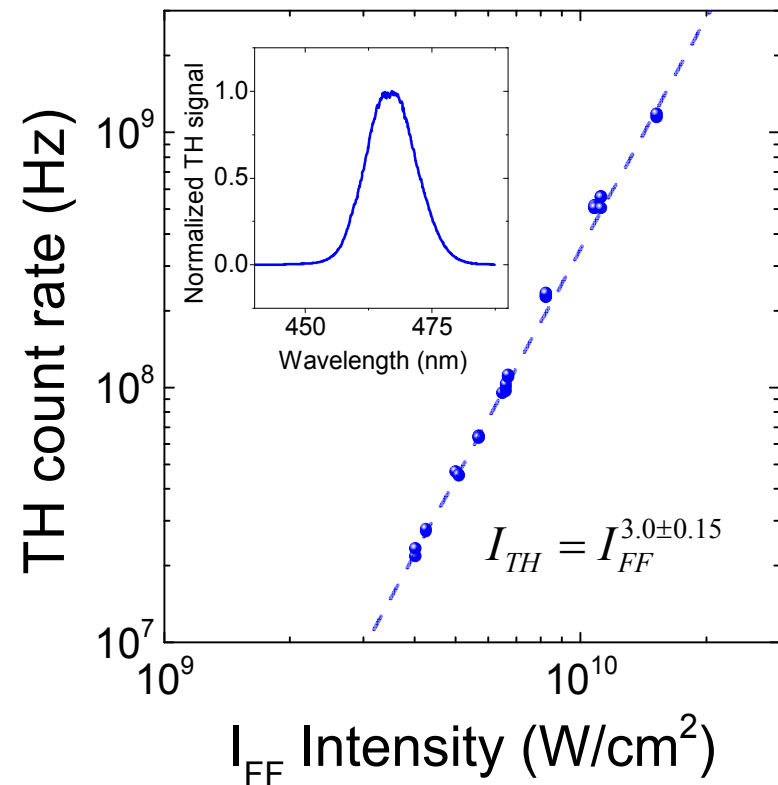
Third harmonic generation using ENZ mode



$$3\vec{k}_{FF} = \vec{k}_{TH}$$

Continuity condition: $3k_{FF\parallel} = k_{TH\parallel}$

TH emerges in specular direction: $\frac{k_{FF\parallel}}{k_{FF\perp}} = \frac{k_{TH\parallel}}{k_{TH\perp}}$



Nonlinear polarization

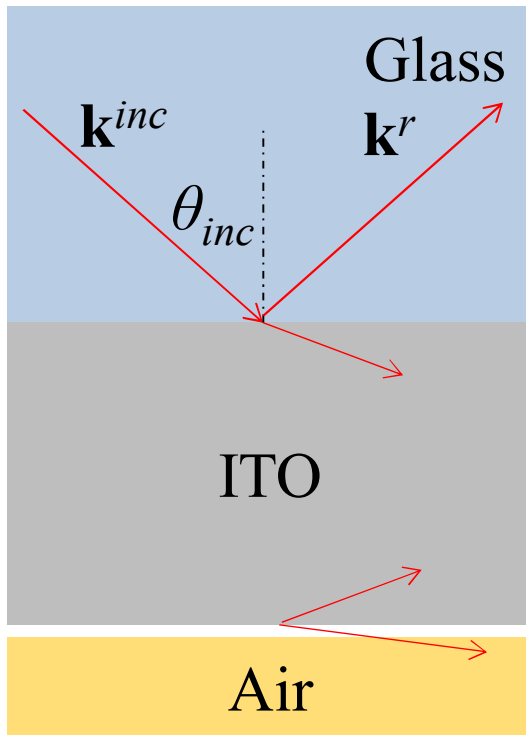
$$\nabla \times \nabla \times \vec{E}_{TH} - \frac{\omega_{TH}^2}{c^2} \vec{\epsilon} \cdot \vec{E}_{TH} = \mu_0 \omega_{TH}^2 \vec{P}_{TH}$$

$$\vec{P}_{TH} = e^{i3k_x x} \epsilon_0 \chi^{(3)}(\omega_{TH}, \omega_{FF}, \omega_{FF}, \omega_{FF}) \cdot \left[\vec{E}_+ \vec{E}_+ \vec{E}_+ e^{i3k_z z} + 3\vec{E}_+ \vec{E}_+ \vec{E}_- e^{ik_z z} + 3\vec{E}_+ \vec{E}_- \vec{E}_- e^{-ik_z z} + \vec{E}_- \vec{E}_- \vec{E}_- e^{-i3k_z z} \right]$$

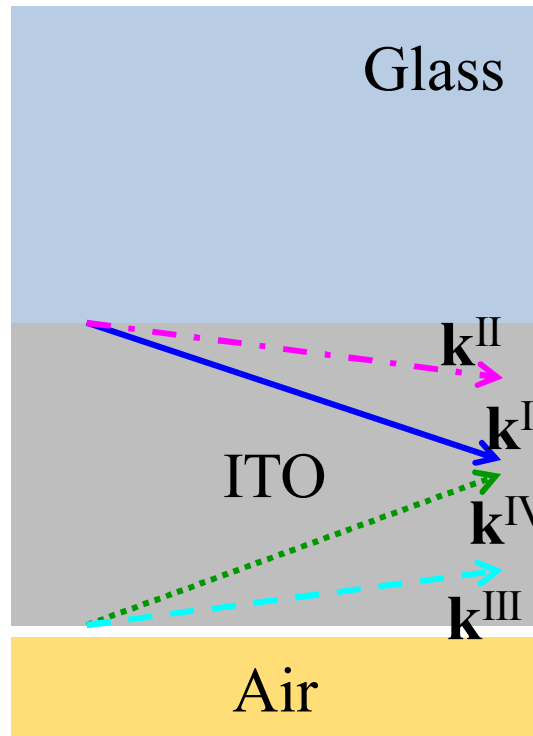
Inhomogeneous solution

Homogeneous solution

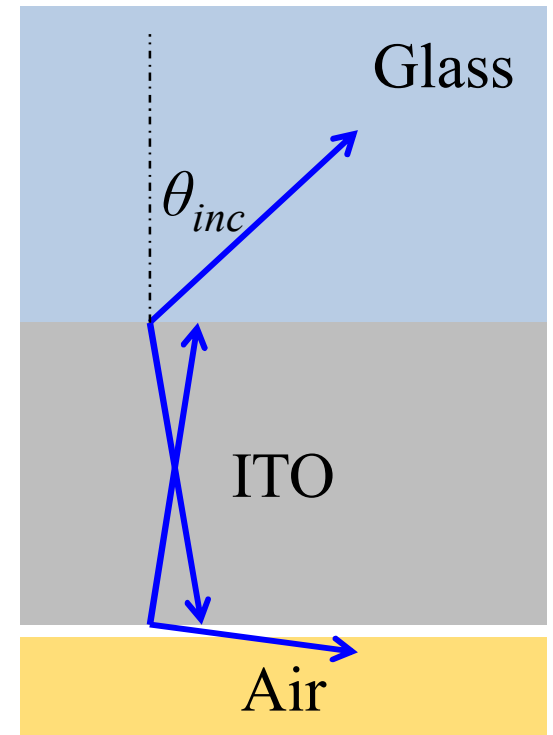
FF waves



Bound TH

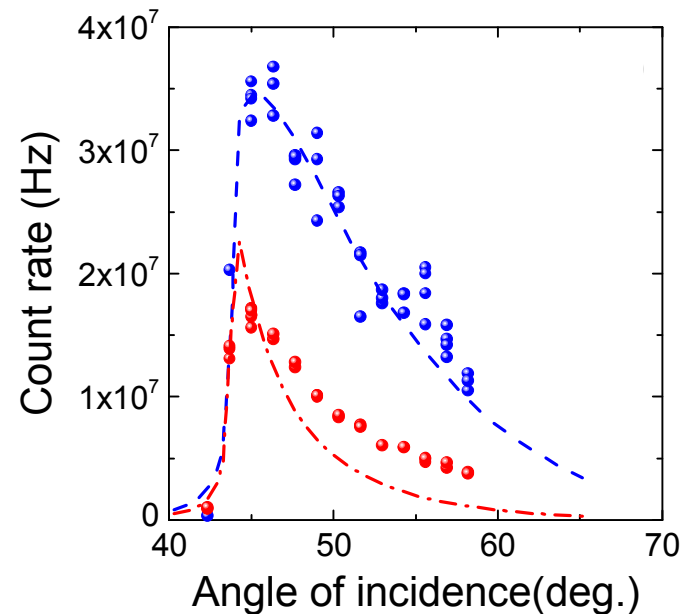
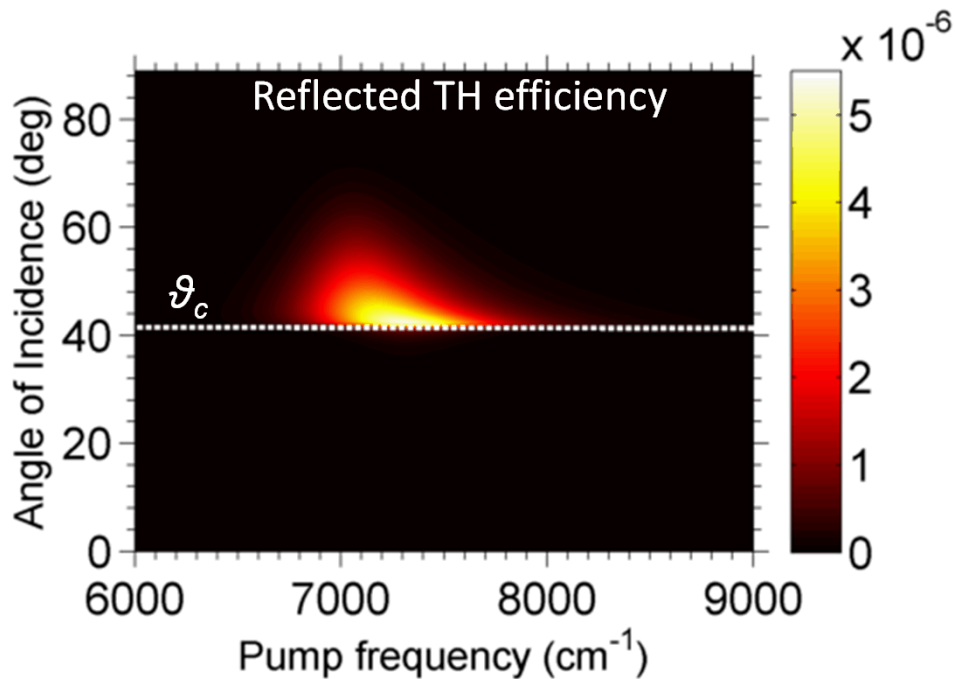


Free TH



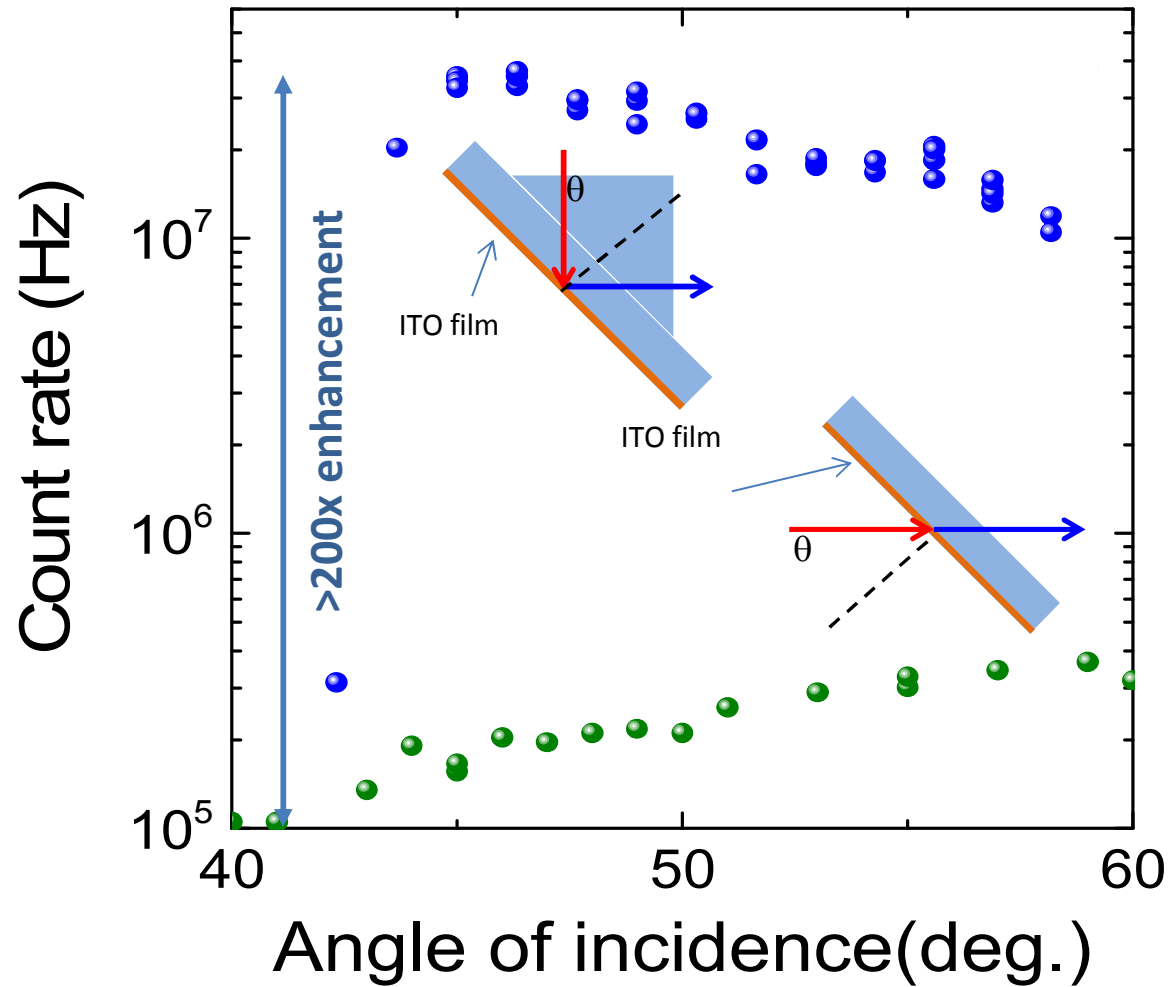
Angular dependence and conversion efficiency

Conversion efficiency at 2×10^{10} W/cm² pump is 3.3×10^{-6}



T. S. Luk et. al, *APL*, (2015)

ENZ mode effect



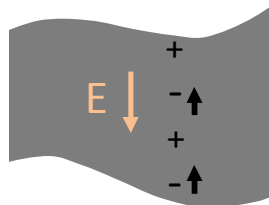
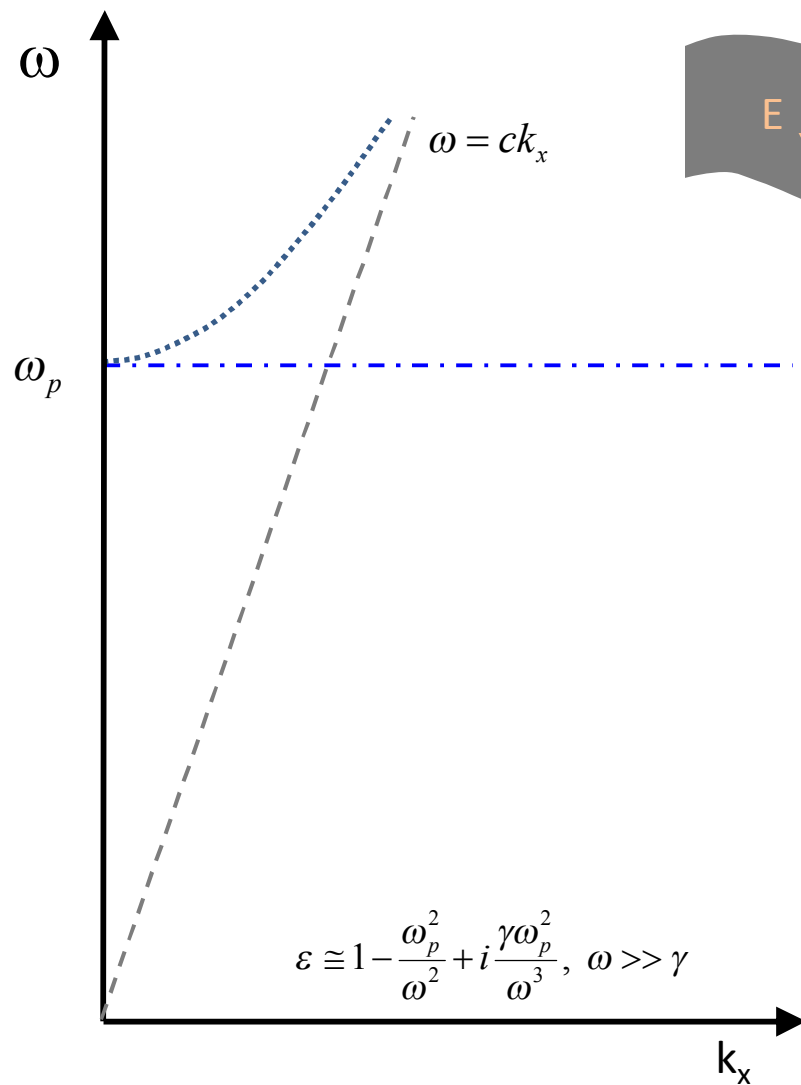
Summary

- Ultrathin film
 - ENZ mode
 - Efficient mode coupling
- 
- Efficient TH generation

Thank you for your attention

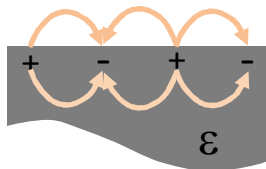
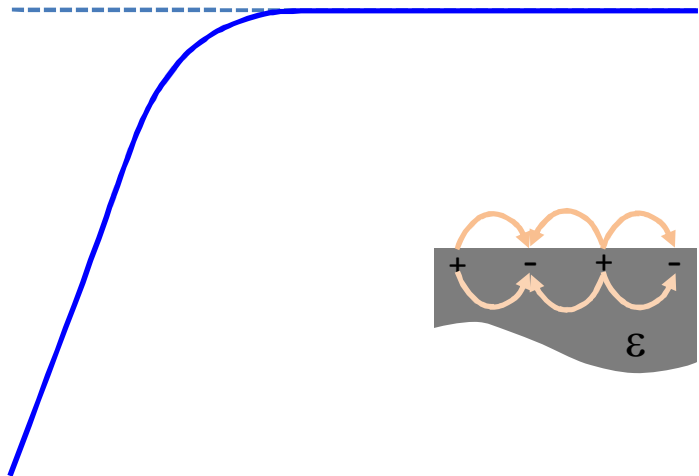
Storyline –

- This paper is a story about ultrathin film optics, ENZ optics and nonlinear optics.
- This work specifically illustrates a unique aspect of ultrathin film optics that goes hand-in-hand with ENZ material.
- Examples of ultrathin film optics: metasurfaces for phase front texturing, Salisbury screen for enhanced absorption, surface plasmon waves, ENZ for enhanced field and density of states.
- Brief history of ENZ:
 - Bulk plasmon
 - Coupling to EM planewave (Ferrell recognized that under thin film condition, bulk plasmon oscillation is radiative).
 - Field enhancement
 - Optical modes in ENZ material
 - Critical coupling and perfect absorption
- We illustrate how to exploit this optical structure in the form of nonlinear third harmonic generation.
- Ultrathin epsilon-near-zero material exhibits strong field enhancement.
- The mode properties enable critical coupling of external planewave to the mode leading to perfect absorption.
- I will provide evidence that this maximum utilization of the incident field produces enhanced third harmonic generation.



$$\omega = \frac{c}{\sqrt{|\varepsilon|}} = \sqrt{\omega_p^2 + c^2 k_x^2}$$

$$\frac{\omega_p}{\sqrt{2}}$$



$$k_x = \frac{\omega}{c} \sqrt{\frac{\epsilon}{1+\epsilon}} = \frac{\omega}{c} \sqrt{\frac{\omega^2 - \omega_p^2}{2\omega^2 - \omega_p^2}}$$

