

National Institute of Standards and Technology, December 14, 2015

# Density Functional Theory of Extreme Environments

R.J. Magyar



Sandia National Laboratories is a multi program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.



# Materials Properties are Needed to Model Complex Phenomena through Equations of State.

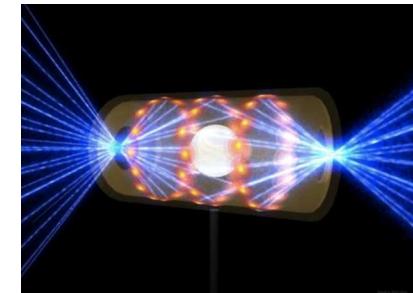
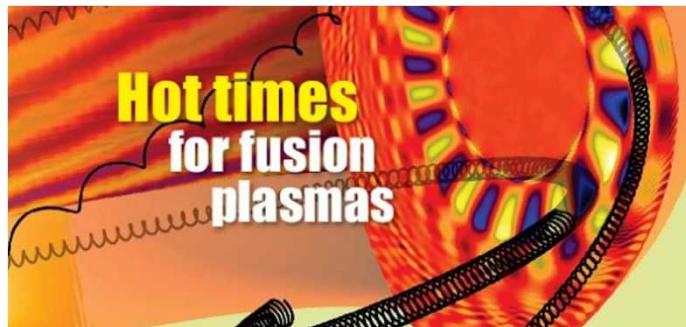
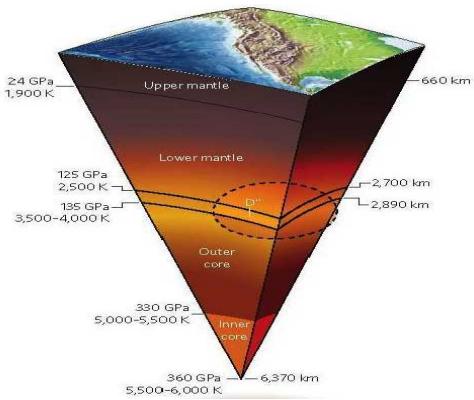


Pressure, density, temperature, phase....

- Materials science
- Planetary collision science
- Geoscience
- Inertial confinement fusion

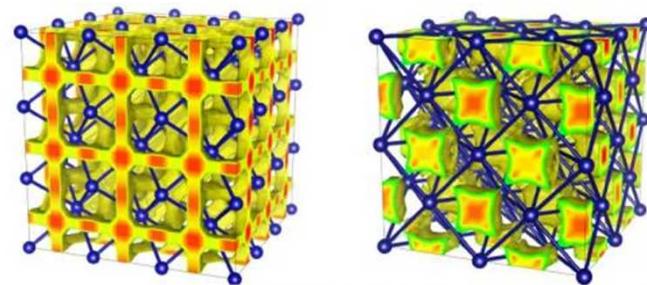
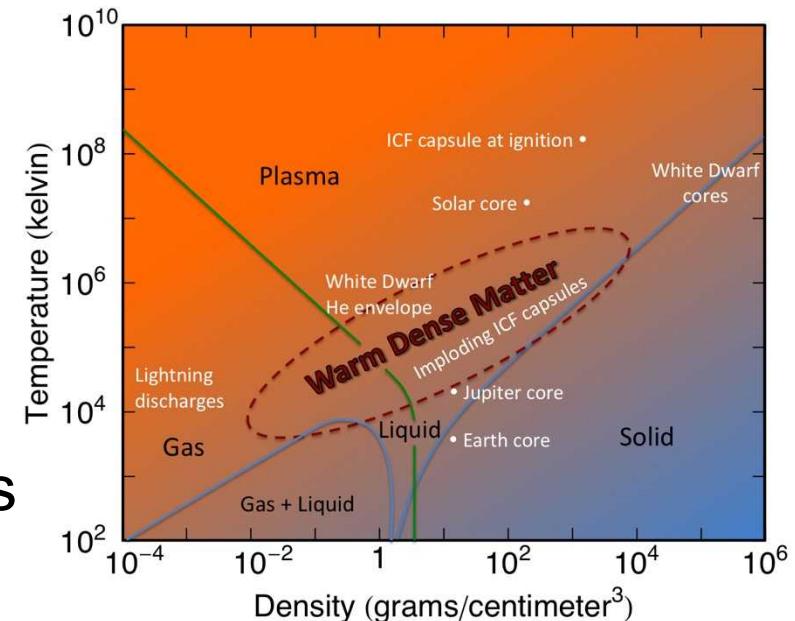
Information to build equations of state typically includes

- Low temperature experiments diamond anvil cell < a few kK
- High temperature plasma physics where degeneracies are negligible



# A Difficult Region of Phase Space to Access is the Warm Dense Matter Region.

- Highly compressed matter with electron densities of  $10^{21}$ - $10^{26}$  electrons / cm<sup>3</sup>
- Temperature on the order of several eVs, 10s of kK
- Electron degeneracy significant
- Bound-free electron correlations significant
- Accessible to experiment and theory - Warm dense matter near-solid (2-4x) density
- Mbars of pressure
- The plasmon energy,  $\omega_p \sim 1$ -4 eV

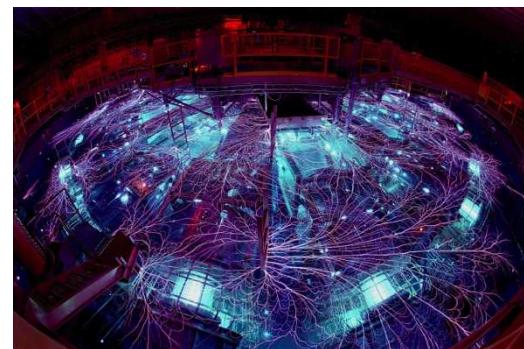
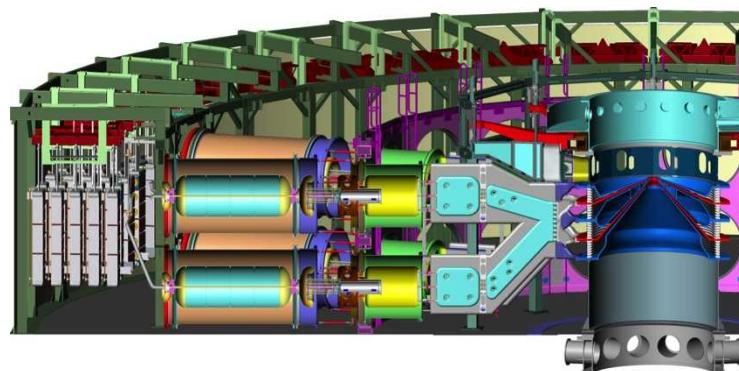


Super ionic water

# The Z-Machine can Probe this Region.

- The world's most powerful pulsed power machine
- Accelerates aluminum flyer plates to 40 km/sec.
- Delivers 27 MegaAmps in 95 nanoseconds.
- Achieves Pressures greater than 10 Mbar (1 TPa).
- Recent work on Xenon reached a state 840 GPa and 149kK
- Compare to diamond Anvil cell – up to 300 GPa and several kK

Indirectly but Accurately Measures **Pressures and Densities**



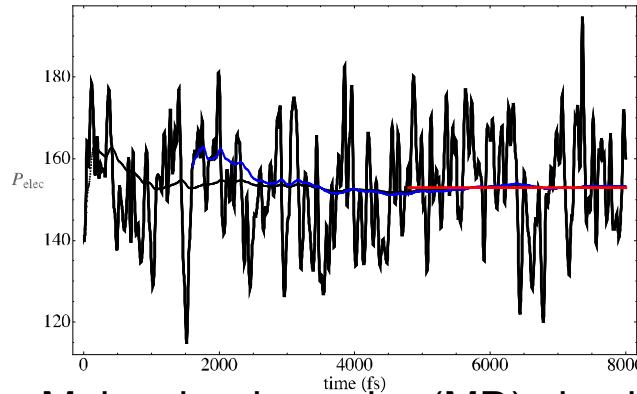
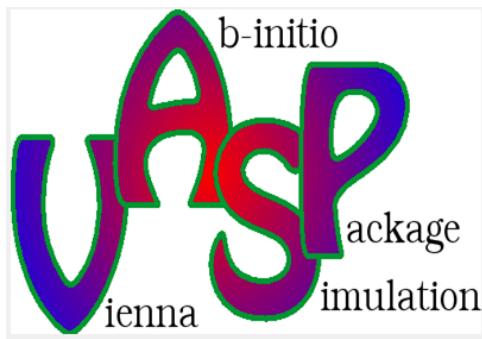
# First Principles Probes

- First principles approach to simulations of total energies, pressures, and other physical quantities
- Unbiased as to elemental species
- First-principles simulations using DFT
  - VASP – plane-wave code with PAW core-functions
  - Great care in convergence
    - A. E. Mattsson et. al. *Modelling and Simulation in Material Science and Engineering* **13**, R1 (2005)
  - Importance of exchange-correlation functional
    - A. E. Mattsson et al. *JCP* **128**, 084714 (2008)



## TOP10 November 2013

- 1 Tianhe-2 (MilkyWay-2) - TH-IVB  
FEP Cluster, Intel Xeon E5-2692  
12C 2.200GHz, TH Express-2,  
Intel Xeon Phi 31S1P  
NUDT
- 2 Titan - Cray XK7 , Opteron 6274  
16C 2.200GHz, Cray Gemini  
interconnect, NVIDIA K20x  
Cray Inc.
- 3 Sequoia - BlueGene/Q, Power  
BQC 16C 1.60 GHz, Custom  
IBM



Molecular dynamics (MD) simulations  
give thermo-physical properties

# DFT, DFT-MD, and TDDFT

Density functional theory (DFT):

- Electron degeneracy/correlation treated exactly .
- Many-body Schrodinger equation from  $R^{3N} \rightarrow R^3$ .
- Ground state or equilibrium thermal state.

Density functional theory molecular dynamics (DFT-MD):

- DFT electronic state  $\rightarrow$  forces on ions.
- Typically within Born-Oppenheimer approximation.

Time-dependent density functional theory (TDDFT):

- Exact treatment of electron dynamics.
- Excited states.
- Ehrenfest-TDDFT  $\rightarrow$  forces including excited electronic states.
- Electrons and ions do not have to be in equilibrium.

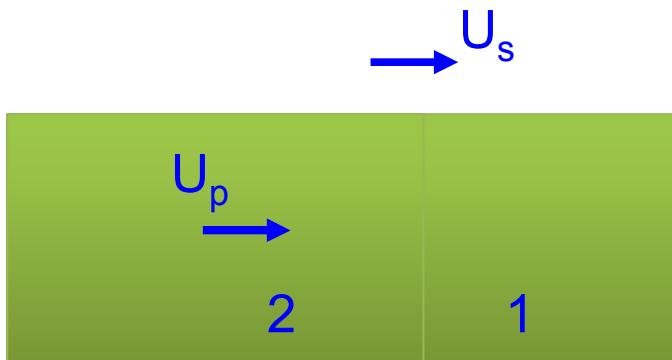
We have implemented Ehrenfest-TDDFT in an existing projector-augmented wave (PAW) code.

(Plane wave basis with a soft cutoff)

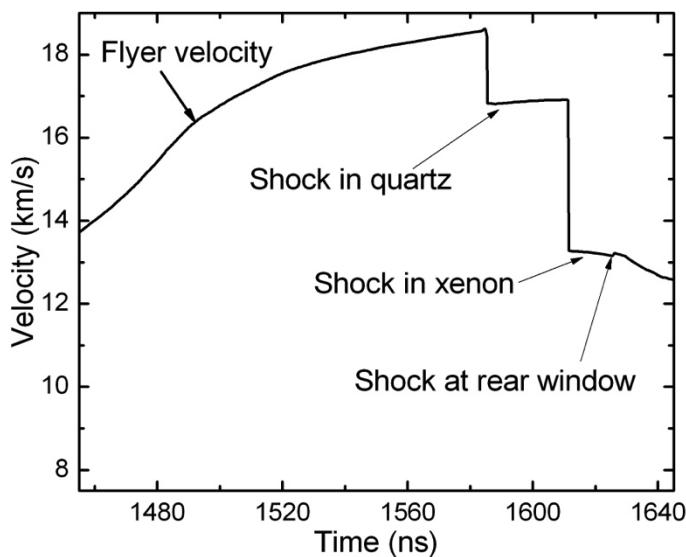
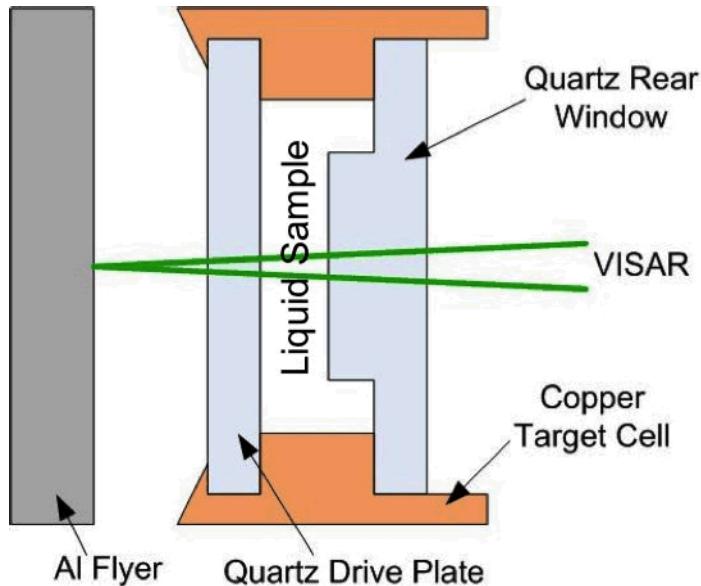
‘Most accurate’ treatment of electron-ion interaction

Approximations  
in DFT are not  
material  
specific.

# Validation of the DFT-MD Simulations

- Compare simulation results to Z-data
  - Convenient –especially in the warm dense matter regime – connection through the Hugoniot
  - Example successes Xe and Ethane
  - Note the dissociation of the latter
- *Conservation of mass, energy, and momentum* lead to the **Rankine-Hugoniot condition** for the initial (1) and final state (2).
- E - internal energy
  - P - pressure
  - v – specific volume
- $$2(E_2 - E_1) = (P_2 + P_1)(v_1 - v_2)$$
- *High accuracy measurement and/or calculations of thermo-physical properties* can be compared to validate understanding.
- 

# We Measure Shock Velocities in Materials with Sub-Percent Accuracy



Precision Accuracy and  
Reproducibility  
VISAR main diagnostics

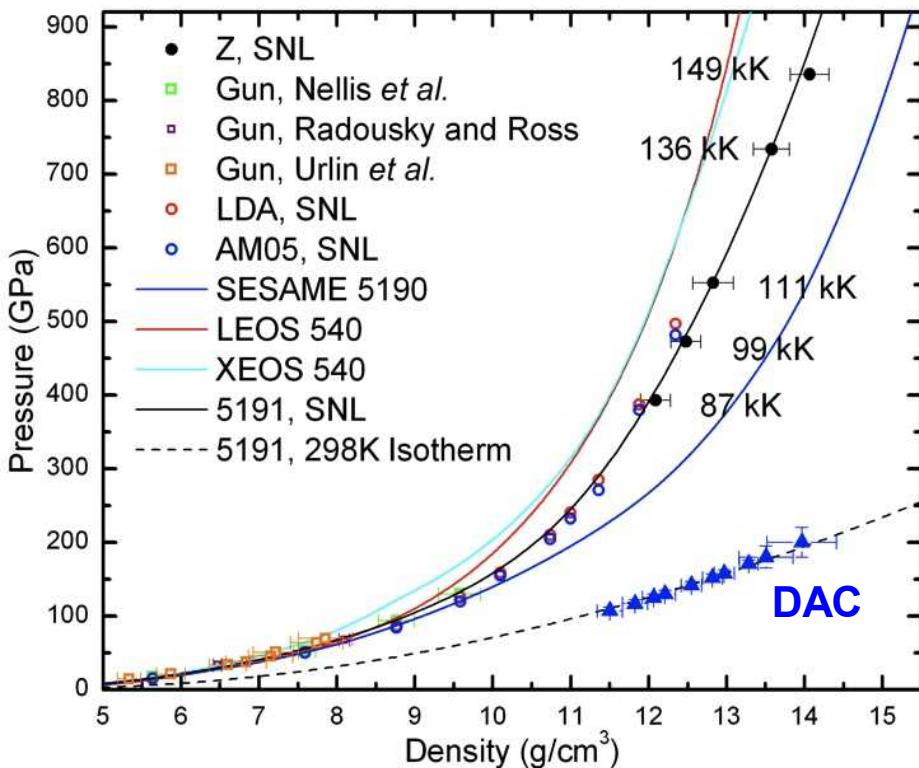
- Flyer velocity, time of impact
- Arrival at interfaces and breakout
- Shock velocity in samples

Monte-Carlo error analysis

- Accuracy of shock standards
- Correlation among parameters
- Error propagation

VISAR trace from a  
xenon experiment with  
18.5 km/s impact velocity

# Experiments on Sandia's Z Machine Obtained High-Precision Data for Xenon to 840 GPa/ 14 g/cm<sup>3</sup>



Seth Root et al Phys. Rev. Lett.  
**105**, 085501 (2010)

Neither LEOS 540 nor SESAME 5190 captures the behavior of xenon above 100 GPa

Demonstrated the need for validating EOS tables to enable high-fidelity simulations

Developed a new multi-phase wide-range EOS table: 5191 in the LANL database

AM05 GGA developed by Ann Mattsson (SNL) is highly accurate for WDM.

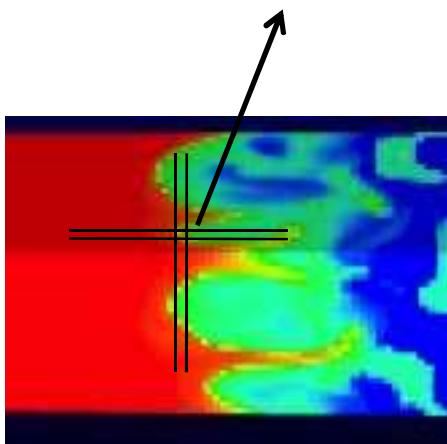
# Hydrocodes, Materials, and Mixtures

A cell in a hydro simulations with two materials “mixed cell”



Material  
1

Material  
2



- High-fidelity hydrodynamics simulations to solve solid dynamics problems
- Require high fidelity equation of state (EOS) models to describe the response of materials to external stimuli e.g.  $P[\rho, T]$
- Materials can mix.
- Dynamic mixing can occur for example through Rayleigh Taylor instabilities.
- For practical reasons, a rule must be used to combine EOS models of pure materials to EOS of mixtures.

Tom Haill  
Al Liner impacting on foam

# Classical Mixing Rules for Binary Mixtures Developed for Nineteenth Century Engineering Problems

$$x = \frac{\rho_L}{\rho_L + \rho_H} = \frac{\rho_L}{\rho}$$

- Ideal (Ideal gas law astrophysics)

$$P = x P_L [\rho, T] + (1-x) P_H [\rho, T]$$

- Volume (Dalton's law 1801 related to cell approaches)

$$P = P_L [x\rho, T] + P_H [(1-x)\rho, T]$$

- Pressure (Amagat's 1880 law of partial volumes some hydro-codes)

$$P_{MIX} = P_L [\tilde{\rho}_L, T] = P_H [\tilde{\rho}_H, T], \quad \frac{x}{\tilde{\rho}_L} + \frac{(1-x)}{\tilde{\rho}_H} = \frac{1}{\rho},$$

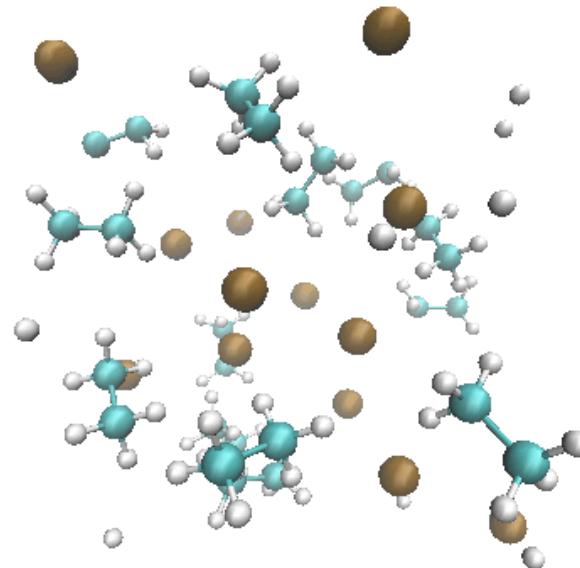
$$f_L \tilde{\rho}_L = \rho_L, \quad f_H \tilde{\rho}_H = \rho_H$$

- Relates total pressure of the mixture to equation of state models of the pure states



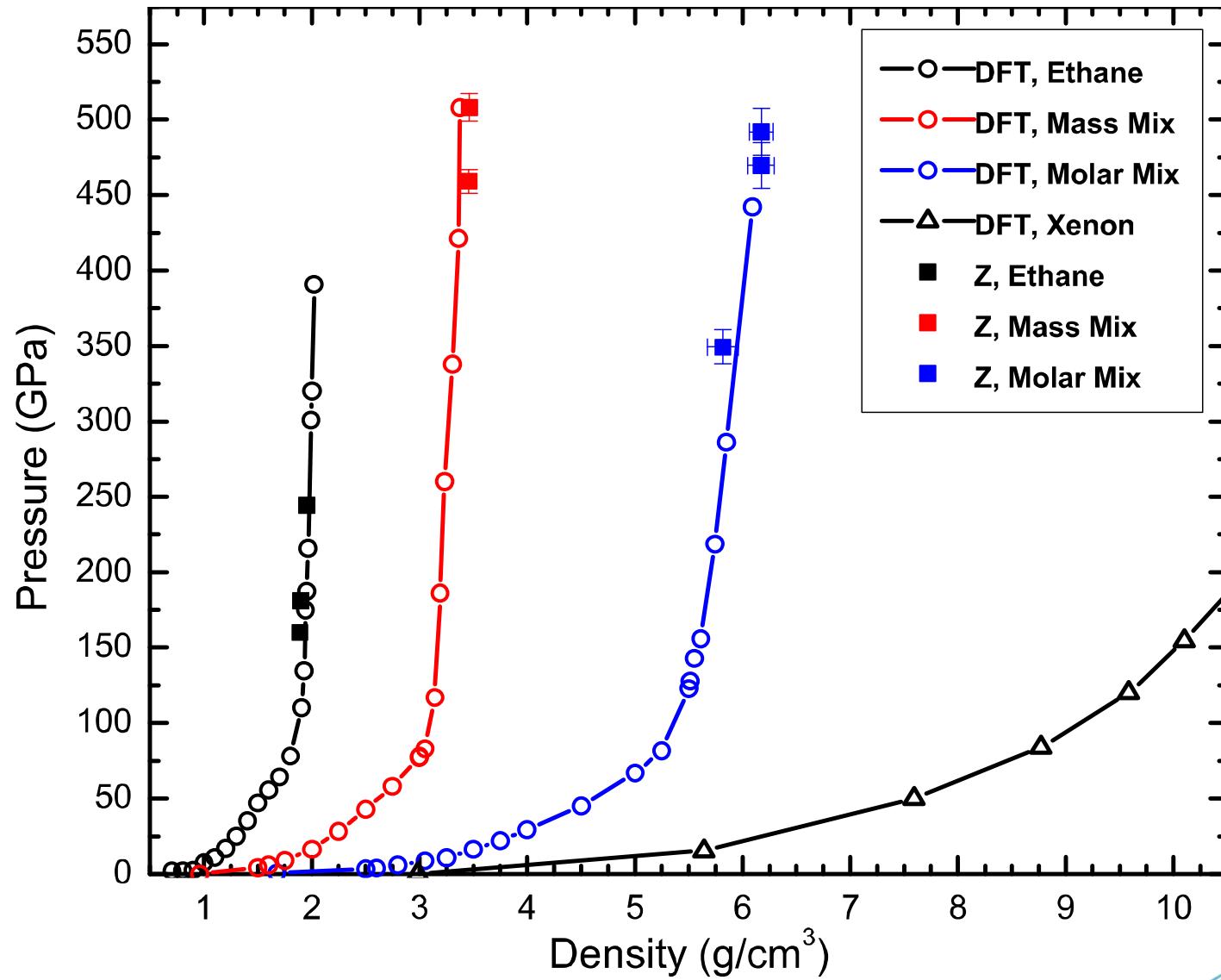
# Xe-Ethane ( $C_2H_6$ ) Mix Hugoniot Reference State

- $T=163.5$  K
- $\rho=1.5$  and  $1.7$  g/cc
- $P=16.8$  psi
- Molar mix ratios 42% and 50%
- Mass mix 5 Xe:18 Ethane (159 atoms per simulation)  $x=0.5$
- Molar mix 13 Xe:13 Ethane (117 atoms per simulation)  $x=0.19$
- Plane-wave energy cut off 900 eV
- Time steps 0.8-0.04 fs
- 8000 time steps
- Mean value point
- AM05 exchange-correlation results shown

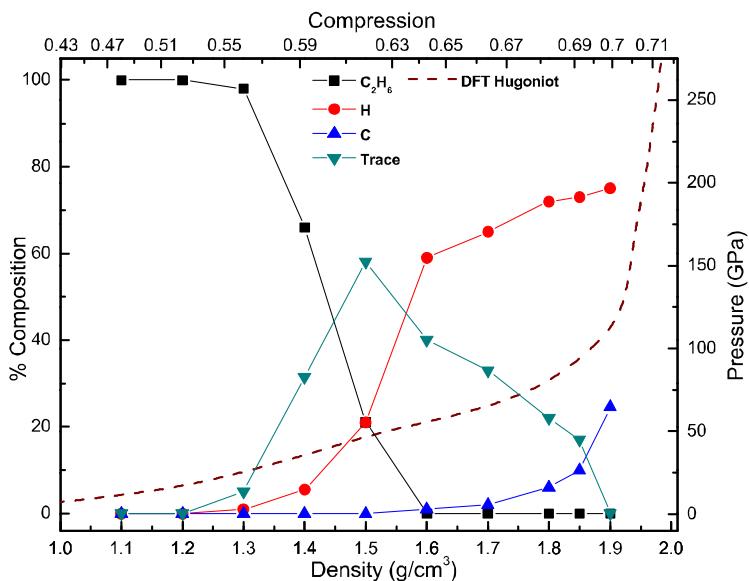
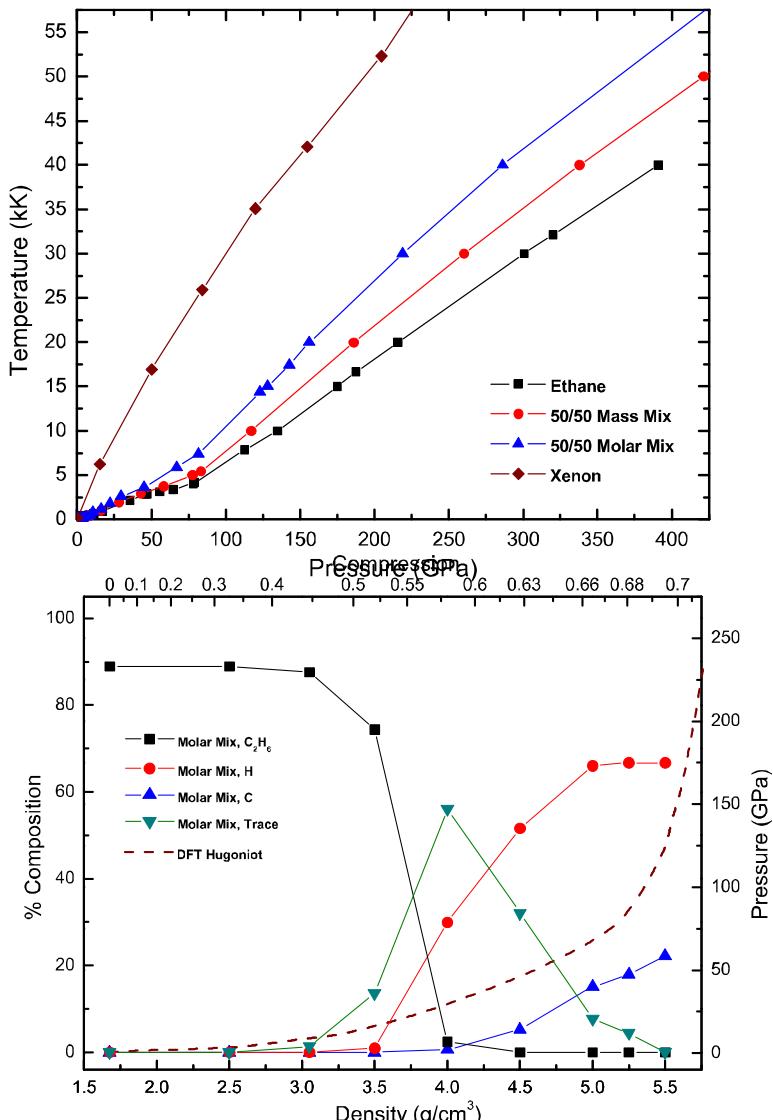


$$x = \frac{\text{Ethane mass}}{\text{Xenon and Ethane mass}}$$

# Xe-Ethane Mix Hugoniot

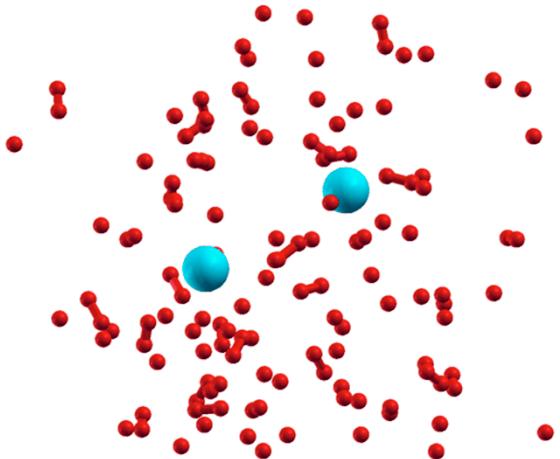


# Decomposition Along the Hugoniot



# Mixing Ratio for Binary Mixtures

High Z- low Z mixture used in gas puff experiments  
Difficult to mix experimentally



$$x = \frac{\text{Deuterium mass}}{\text{Xenon and Deuterium mass}}$$

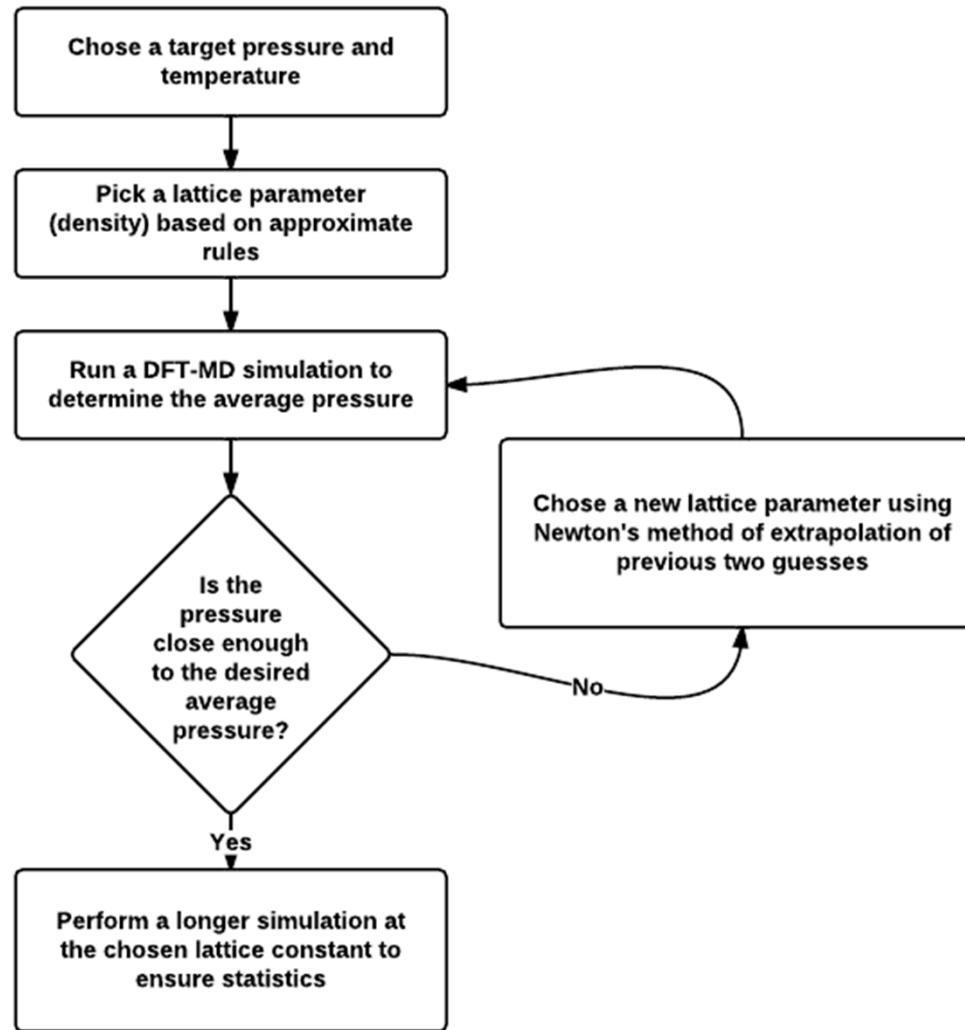
Mix Ratio	# of Xe Atoms / Cell	# of D Atoms / Cell
0.0	32	0
0.3	3	84
0.5	2	132
0.67	1	132
1.0	0	200

Note: Deuterium mass / Xenon mass  $\approx 0.015$

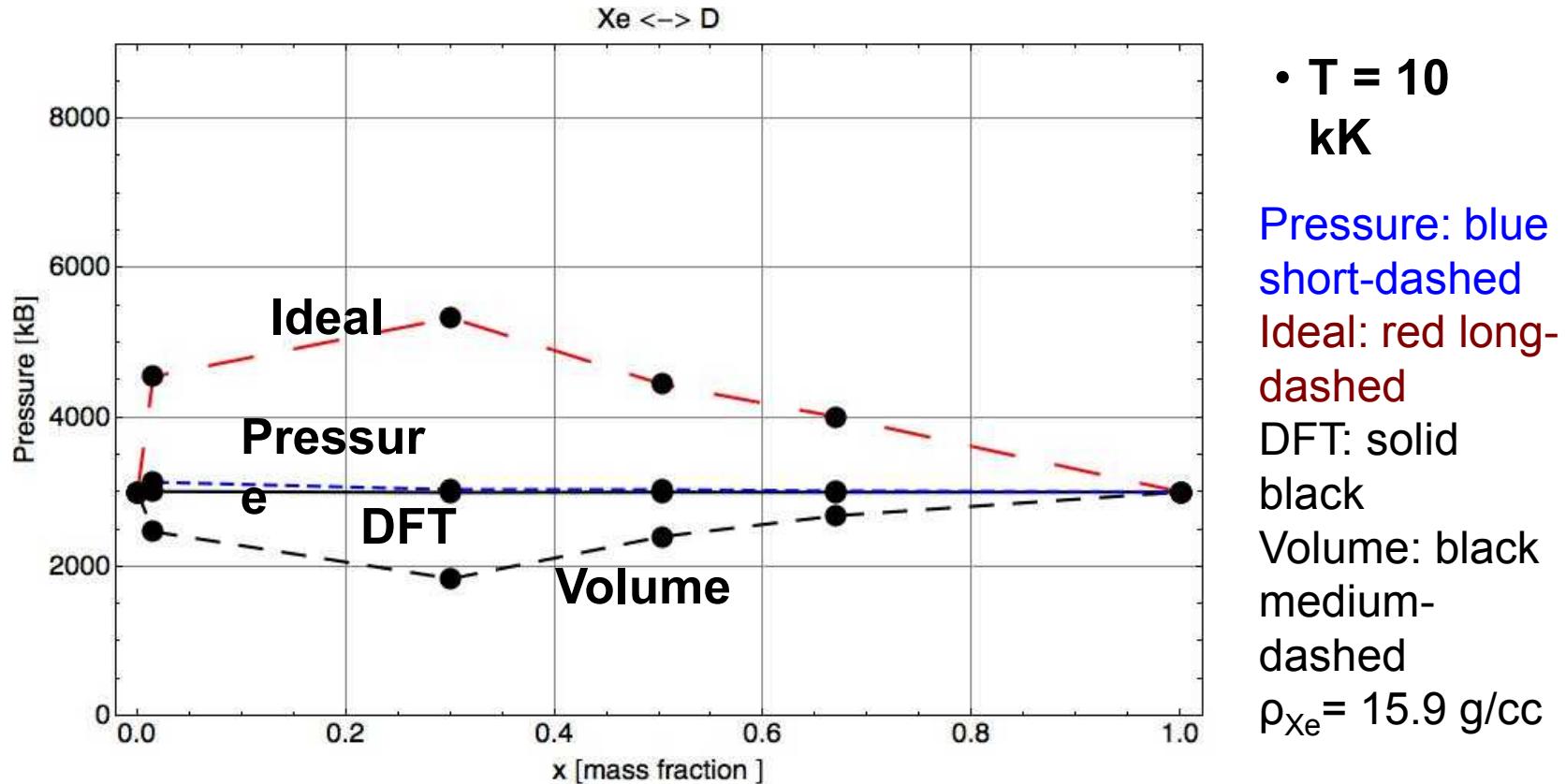
According to the ideal gas law:  $P$  is proportional to  $n$  the number density

To achieve similar pressures the mass densities are related  $\rho_{Xe} \approx 100 \rho_D$

# Constant Pressure Calculations Implementation at First Principles Simulations

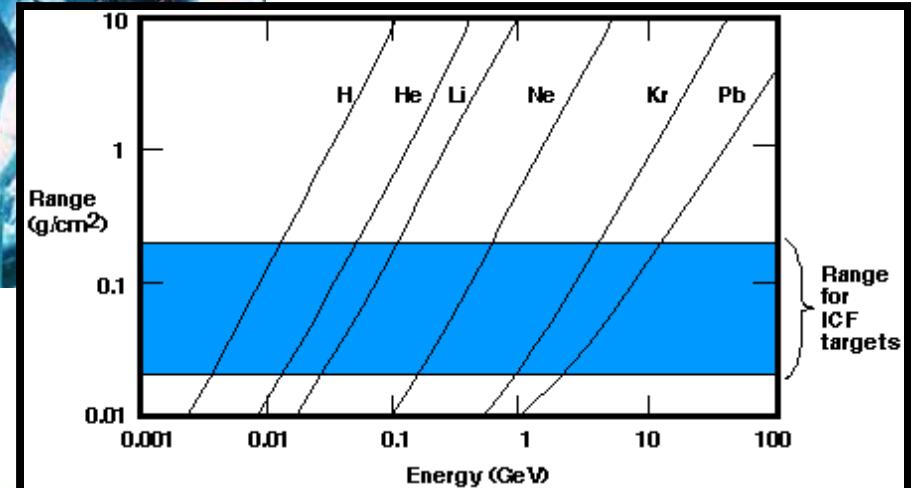
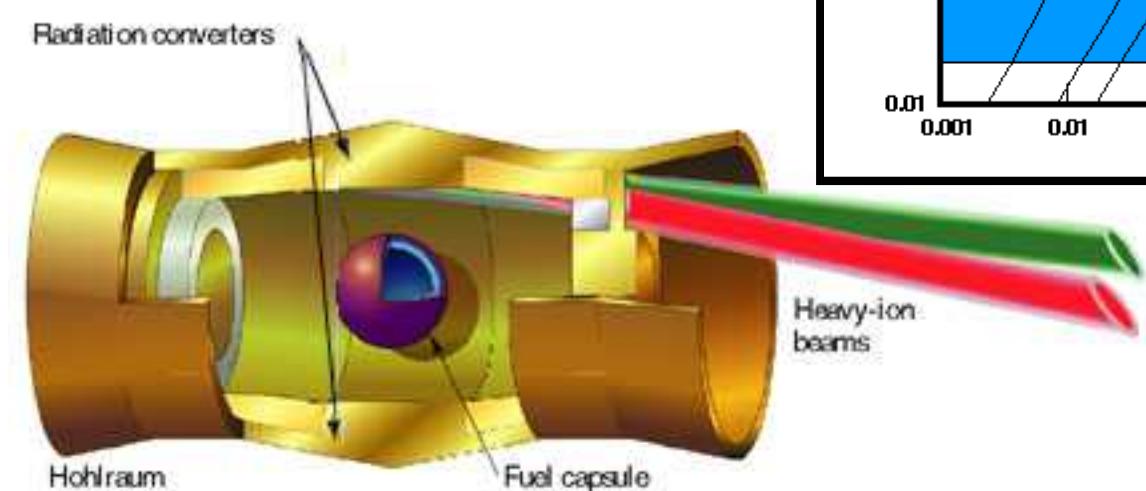
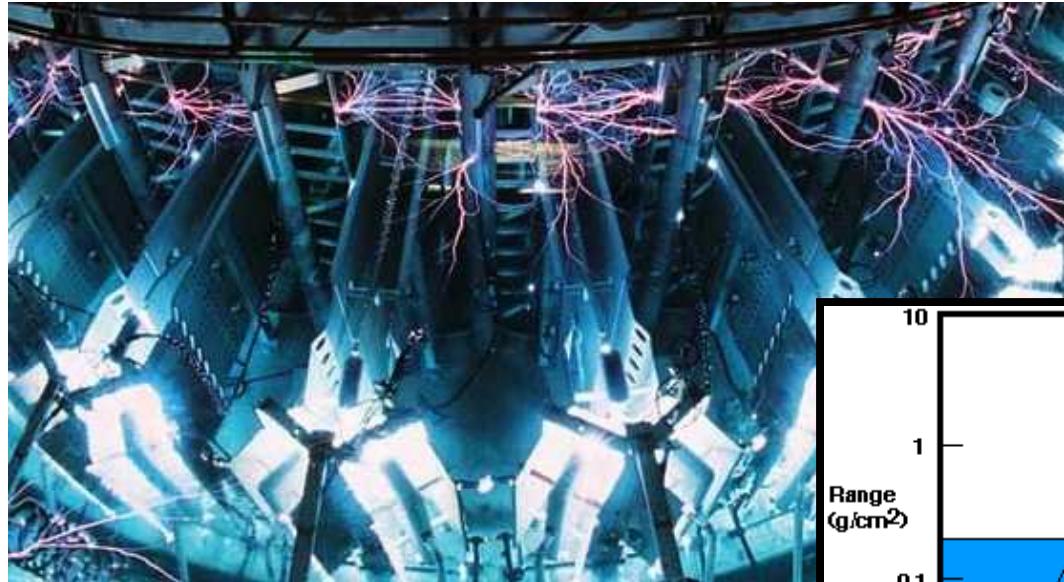


# Xe-D with fixed pressure: DFT/AM05, SESAME 5365 for D

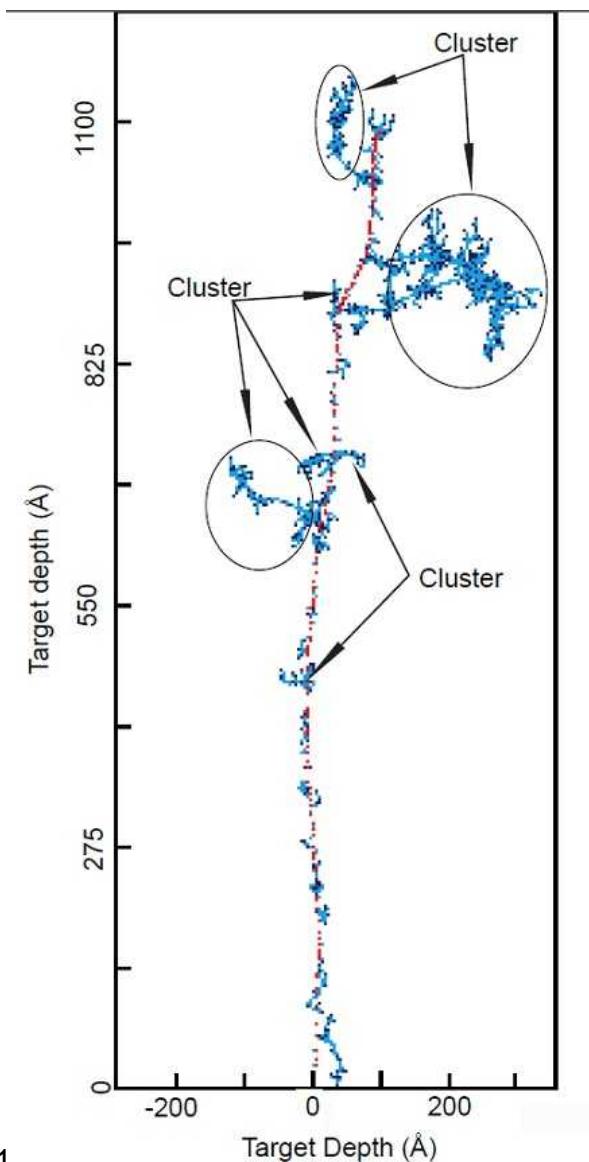


Magyar and Mattsson, Phys. Plasmas **20**, 032701 (2013)  
Notes: Ideal mixing rule is clearly flawed especially for small x.  
Volume mixing predicts lower pressures than DFT-MD.

# Stopping Powers for Inertial Confinement Fusion and Warm Dense Matter



# Stopping Power



$$S(E) = -dE_{\text{Projectile}} / dx$$

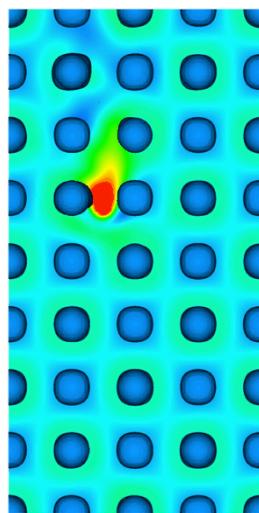
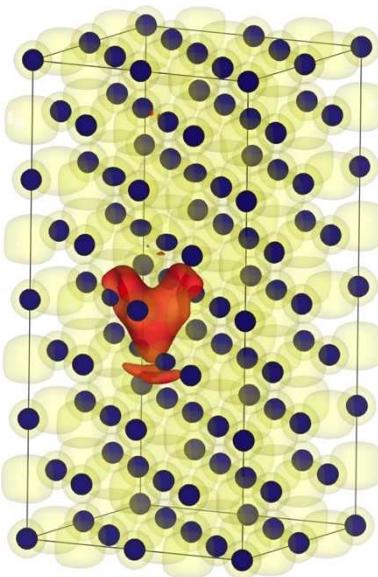
**Penetration Depth :**

$$\Delta x = \int_0^{E_0} dE \frac{1}{S(E)}$$

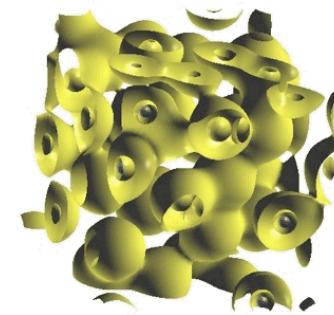
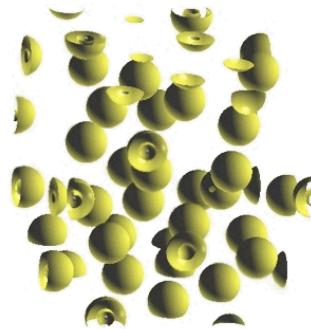
Common Materials Monte Carlo Data Tabulated:  
[www.srim.org](http://www.srim.org)

# Developments Required for TDDFT of WDM

- Extended system for dense disordered materials
- Real-time evolution to allow non-harmonic nuclear motion to couple
- Extended system optical or small  $q$  response
- Finite temperature theory
- Coupled-electron-ion motion
- Electron-ion energy transfer



$$i \frac{\partial}{\partial t} \phi_i(r, t) = \left[ -\frac{1}{2} \nabla^2 + v_{KS}[\Psi_0, \Phi_0, n](r, t) \right] \phi_i(r, t)$$



# Approaches to Stopping in Real-Time Electron Dynamics Simulations

1. Total energy – Constant velocity projectile, increasing total energy of system
2. Forces on nuclei – Direct solution of forces of projectile
3. Perturbative – Relationship to dielectric response of system

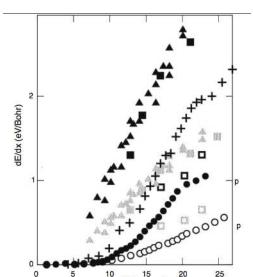
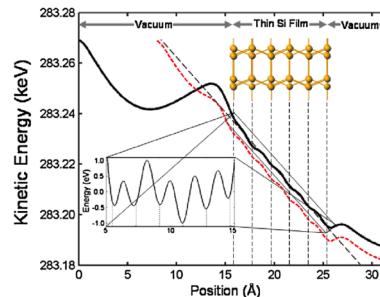


Fig. 1. Electronic stopping power  $S$  as a function of the particle velocity  $v$  for  $p$  (filled symbols) and  $p̂$  (empty symbols). Circles are the calculations while triangles and squares are the measured values scaled by 1/2. The solid line is for direct comparison with the calculations, which only considered channelling trajectories. Calculations include basis functions for  $p̂$  including additional basis functions along the projectile's path (see text).

J.M. Pruneda et al. Nuclear Instruments and Methods in Physics Research B 267 (2009) 590–593

J. M. Pruneda, D. Sánchez-Portal, A. Arnau, J. I. Juaristi, and E. Artacho, Electronic stopping power in LiF from first principles, [Phys. Rev. Lett. 99, 235501 \(2007\)](https://doi.org/10.1103/PhysRevLett.99.235501).



R. Hatcher, M. Beck, A. Tackett, and S.T. Pantelides, Phys. Rev. Lett. 100, 103201 (2008).

# Electron-Dynamics through TDDFT

Time-dependent KS Scheme Builds Upon the Highly Successful Ground-state Theory

$$i \frac{\partial}{\partial t} \phi_i(r, t) = \left[ -\frac{1}{2} \nabla^2 + v_{KS}[\Psi_0, \Phi_0, n](r, t) \right] \phi_i(r, t)$$

$$\phi_i(r, 0) = \phi_i^T(r) \quad \int d^3r \phi_i(r, t) \phi_j(r, t) = \delta_{ij}$$

$$n(r, t) = \sum_i^{\text{occ.}} |\phi_i(r, t)|^2$$

In the spirit of KS DFT, we postulate that a non-interacting system with a judiciously chosen potential can reproduce the time dependent density.

Non-linear and complex

$t_{\text{electron}} \ll t_{\text{nuclei}}$  for long simulations 50000 time steps typical > 5000 in DFT-MD

# Elevated-Temperature Time-Dependent Density Functional Theory (ET-TDDFT)

$$n(r, t) = \text{Tr} [\hat{n}(r) \hat{\rho}(t)] = \sum_{\text{norbs}} w_i(t) |\phi_i(r, t)|^2$$
$$w_{N,i} = f \left[ \beta (\varepsilon_{N,i} - \mu N) \right]$$

- Mermin formulation
- Ground-state exchange-correlation Functionals (local density and gradient approximations)
- Chemical bonds
- Thermostats
- Molecular dynamics of the nuclei

$$n(r, t) = \sum_i^{\text{occ.}} w_i |\phi_i(r, t)|^2, f_i \leq 1$$

# Electron-ion Equilibration

**Hot ions and cold electrons or Hot electrons and cold ions**

Often modeled in terms of a 2 temperature model

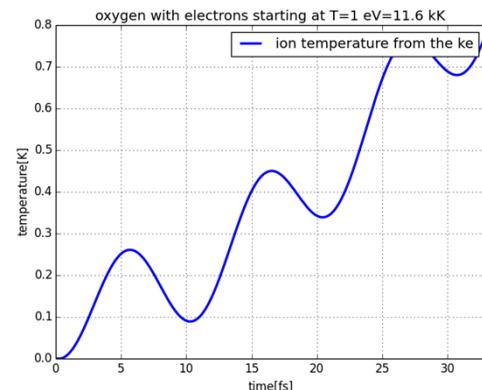
$$T_{\text{equilibration}} = 0.33 - 10 \text{ ps}$$

Runge-Gross Leaves the Question of Weights Open

- Different representations of TDDFT ensemble densities
- NVT thermal density but NVE propagation?!

$$\hat{\rho}^{\text{Exact}} = \sum_i W_{i,\beta} |\Psi_i\rangle\langle\Psi_i|$$

$$\hat{\rho}^{\text{Mermin}} = \sum_i w_{i,\beta} |\phi_i(w_{i,\beta})\rangle\langle\phi_i(w_{i,\beta})|$$



# Trouble with Von Neumann and Mermin States

- Assume for example non-interacting Fermions.
- Try to connect 2 different Mermin states through unitary propagation alone.
- Some mechanism to change occupations is required.

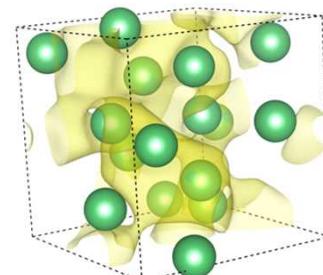
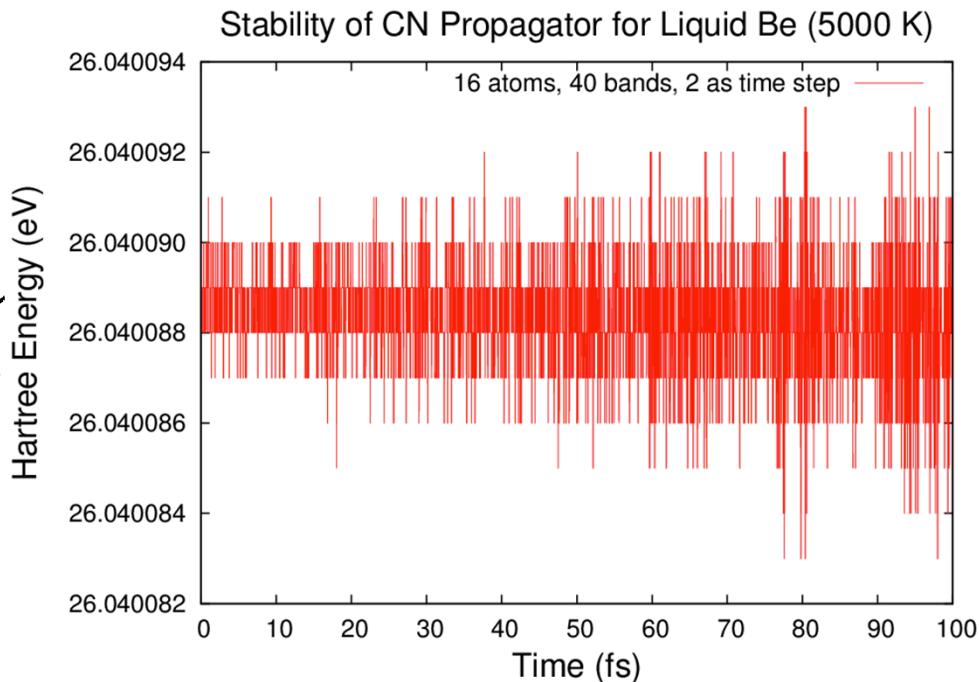
$$\hat{\rho}_1 = \sum_i w_i^{(1)} |\Phi_i\rangle\langle\Phi_i| \quad \hat{\rho}_2 = \sum_i w_i^{(2)} |\Phi_i\rangle\langle\Phi_i|$$

$$\hat{\rho}_2 = \sum_i w_i^{(1)} U(T) |\Phi_i\rangle\langle\Phi_i| U(T)$$

$$U(t) = \sqrt{w_i^{(2)} / w_i^{(1)}}$$

# Time-integration and Stability

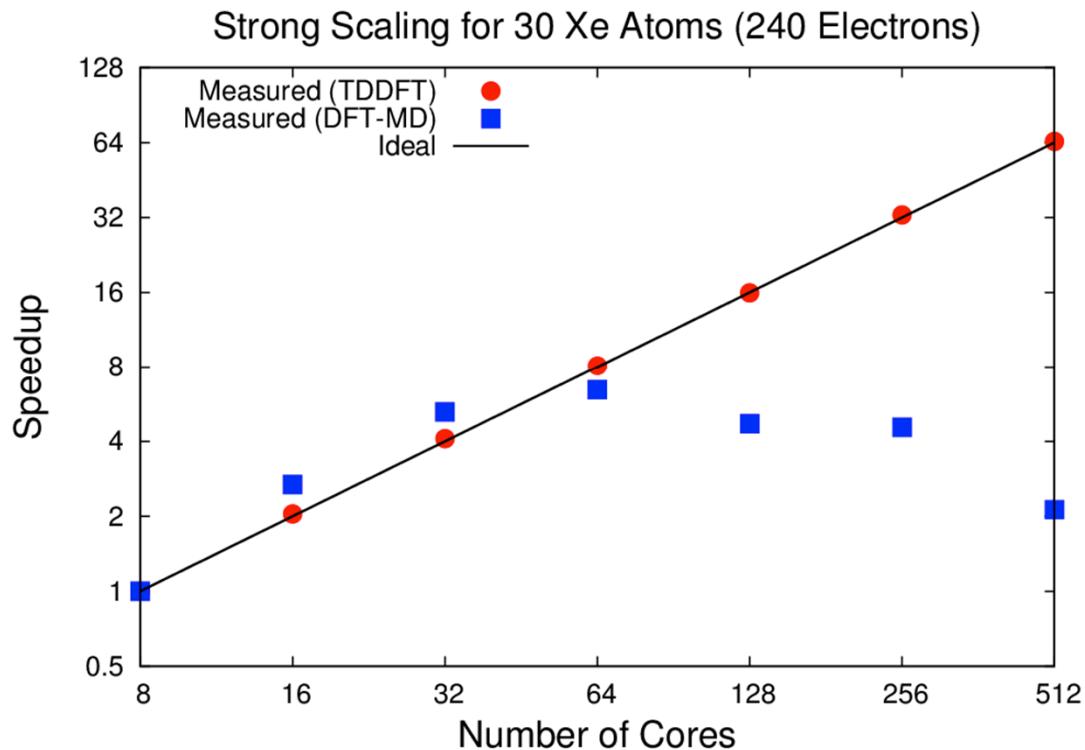
- Highly nonlinear equations
- Sources of trouble:
- Iterative solve at each step
- Hartree/XC  $\leftarrow n(r, t) \leftarrow |\Psi_m(r, t)|^2$
- Accumulation of floating-point error
- Validation: Does Mermin state stay in Mermin state?
- Crank-Nicolson proves robust :  
Exact unitary propagation
- Orbitals orthogonal for 50k+ steps
- Hartree energy conserved  $\pm 10\mu\text{eV}!$



$$\begin{aligned} & \left[ S(t) + \frac{i\Delta}{2} H_{\text{smooth}}(t + \frac{\Delta}{2}) \right] \Psi_{n,\text{smooth}}(t + \Delta) \\ &= \left[ S(t) - \frac{i\Delta}{2} H_{\text{smooth}}(t + \frac{\Delta}{2}) \right] \Psi_{n,\text{smooth}}(t) \end{aligned}$$

# Parallel Scalability

- Ehrenfest TDDFT: ‘more parallel’ than DFT-MD.
- Primary cost/step is iterative linear solve
- No orthogonalization
- Hierarchical parallelism
- The catch: time step in attoseconds
- Of course, we also capture influence of electronic excited states. . .



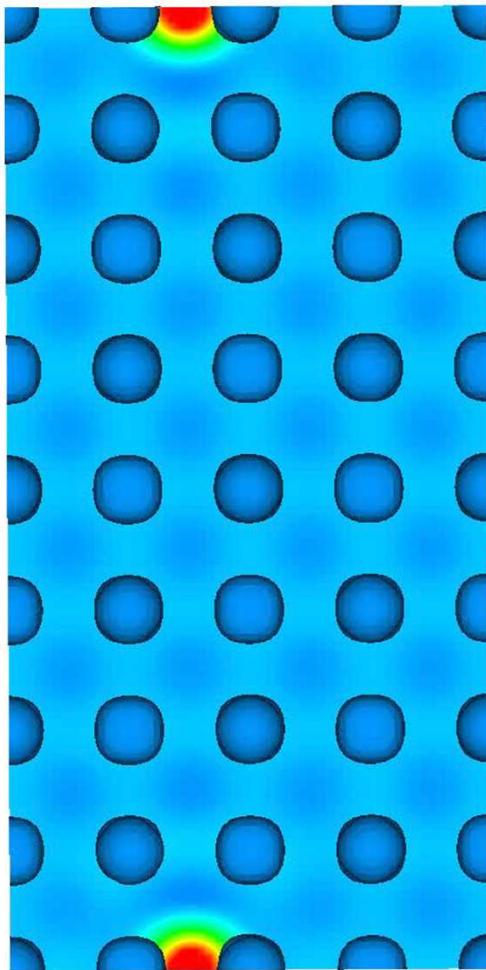
# Coupled Electrons and Moving Nuclei

$$H[\{R_I\}]\phi = \varepsilon\phi \quad \text{vs.} \quad H[\{R_I\}]\phi = i\frac{d}{dt}\phi$$
$$F_I = -\left\langle \nabla_I V(\{R_I\}) \right\rangle$$

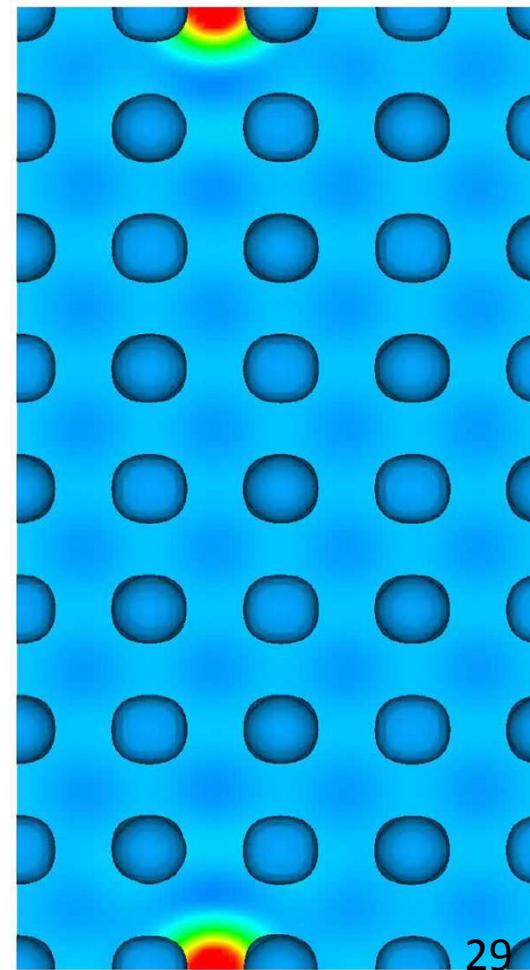
- **Separate model for coupled electron ion dynamics**
- No uncoupled electron dynamics Born-Oppenheimer
- Electron-dynamics in Ehrenfest
- Certain processes not described by even Ehrenfest such as photochemistry, discrete electron relaxation

# Born-Oppenheimer vs. Ehrenfest

Born-Oppenheimer

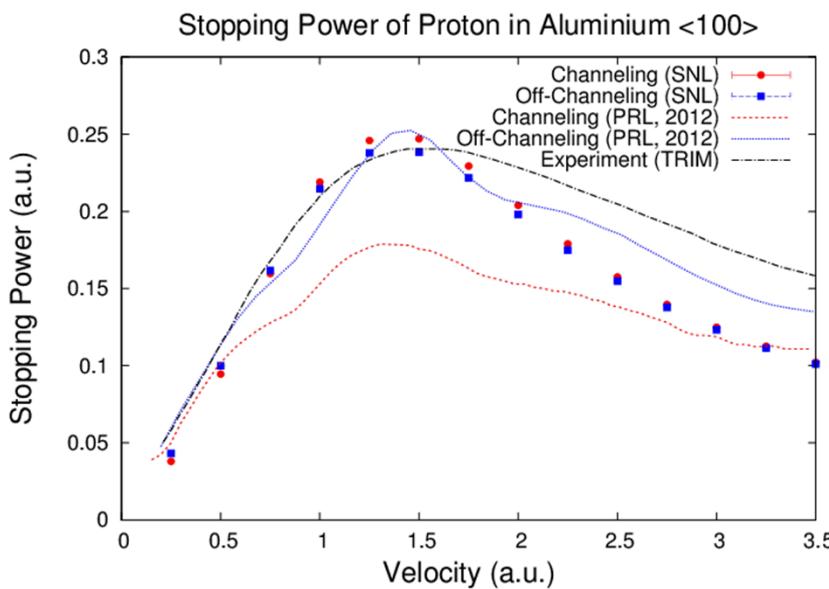
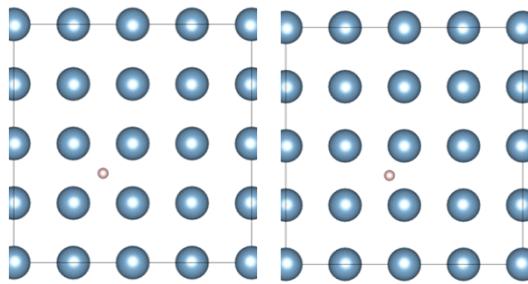


Ehrenfest



29

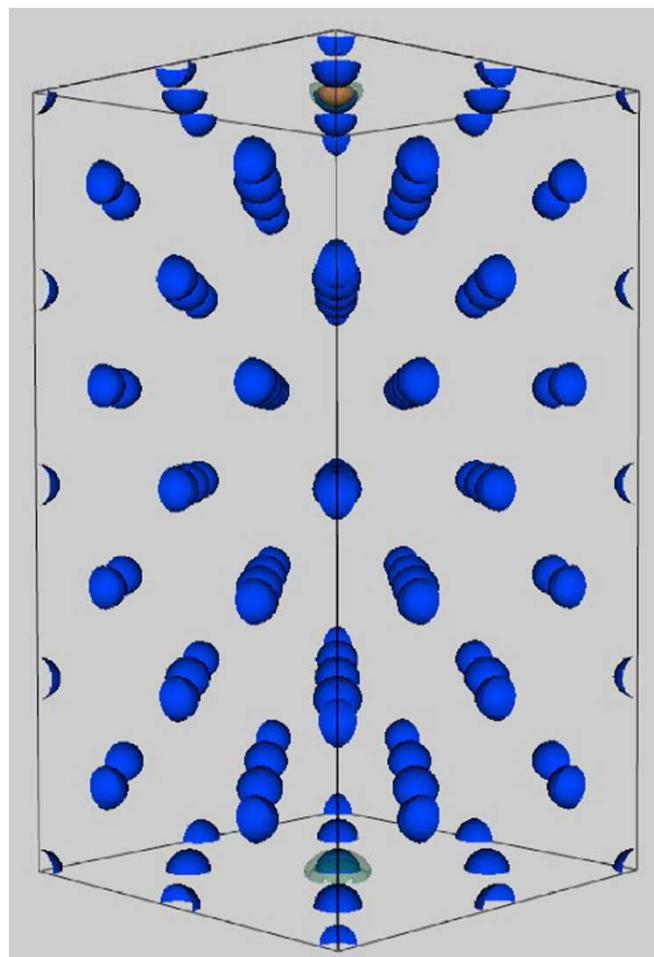
# Stopping Power Calculations Extended to WDM



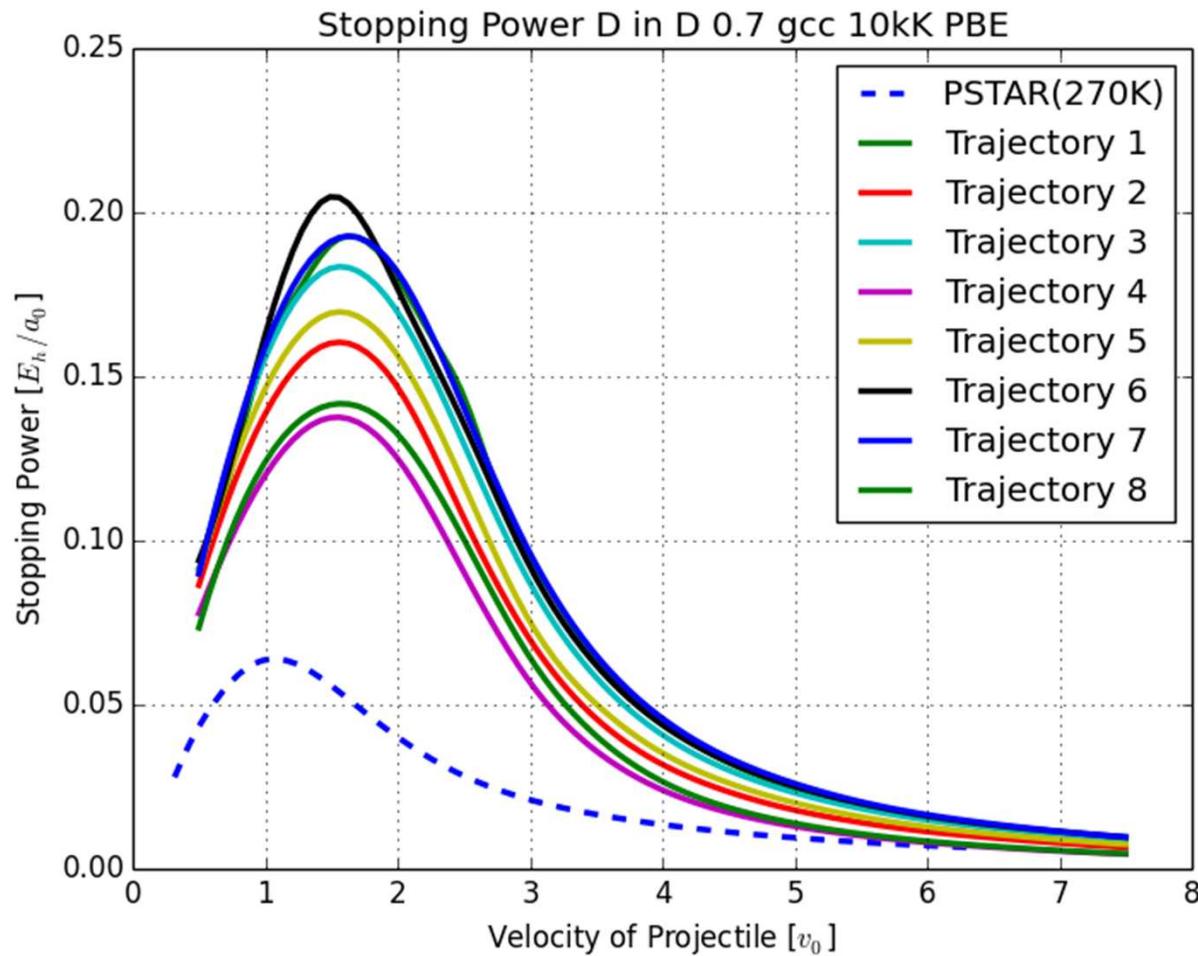
- Low energy  $v < 0.1$  a.u. ground-state or thermal electrons / adiabatic regime
- High energy  $v >> 0.1$  a.u. electron dynamics
- Intermediate regime: combined electron-nuclear dynamics, electron capture and ionization

André Schleife, Yosuke Kanai, and Alfredo A. Correa

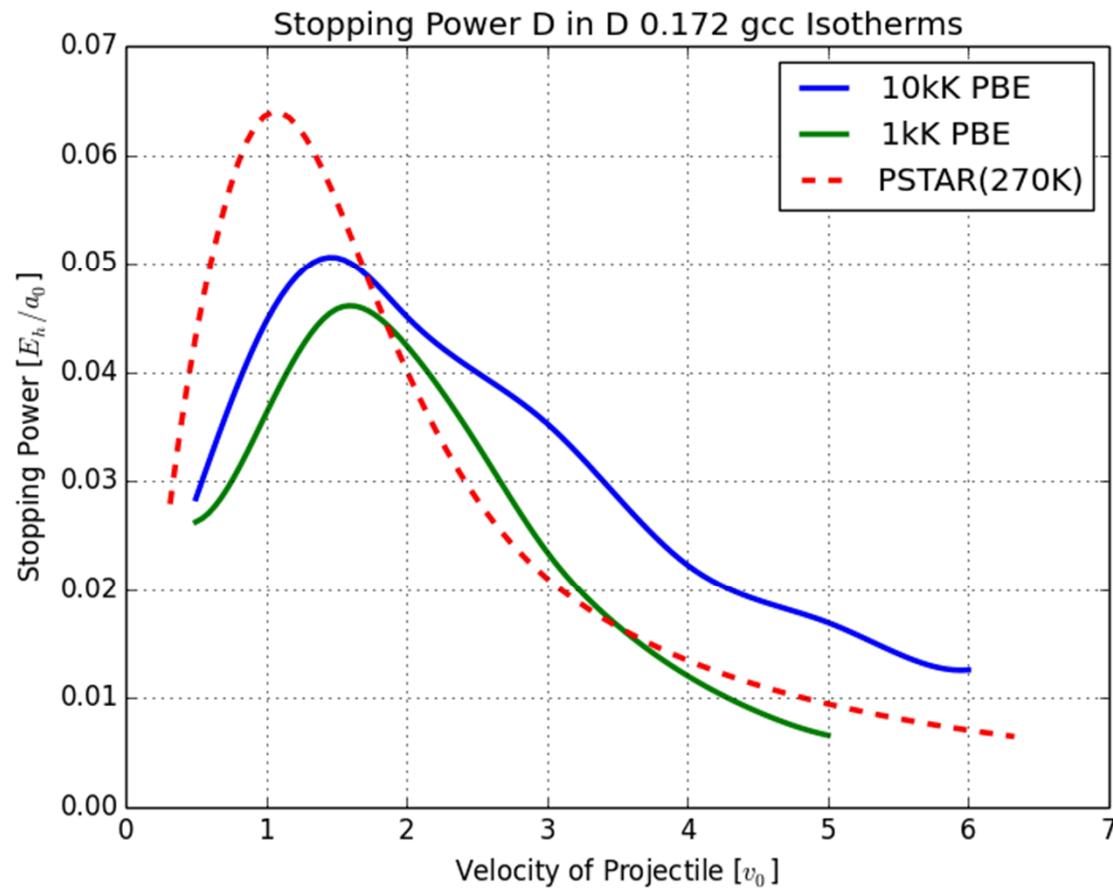
# Plasmons are Formed in the Wake.



# Stopping in Deuterium

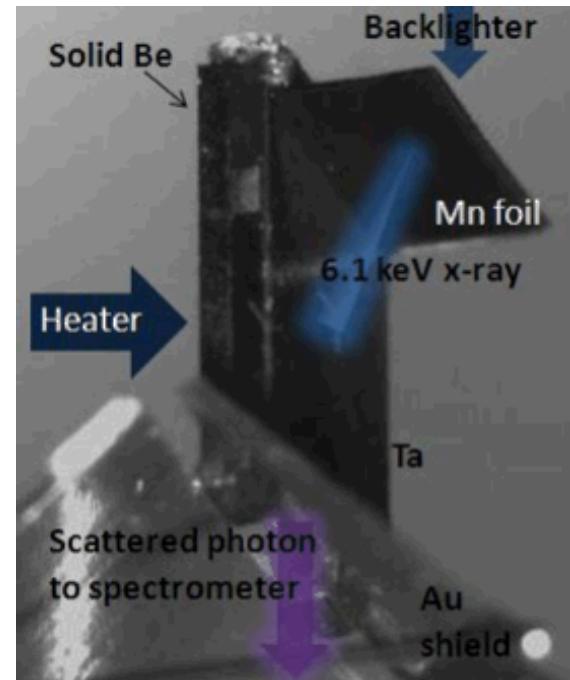


# D in D at four-fold compressed

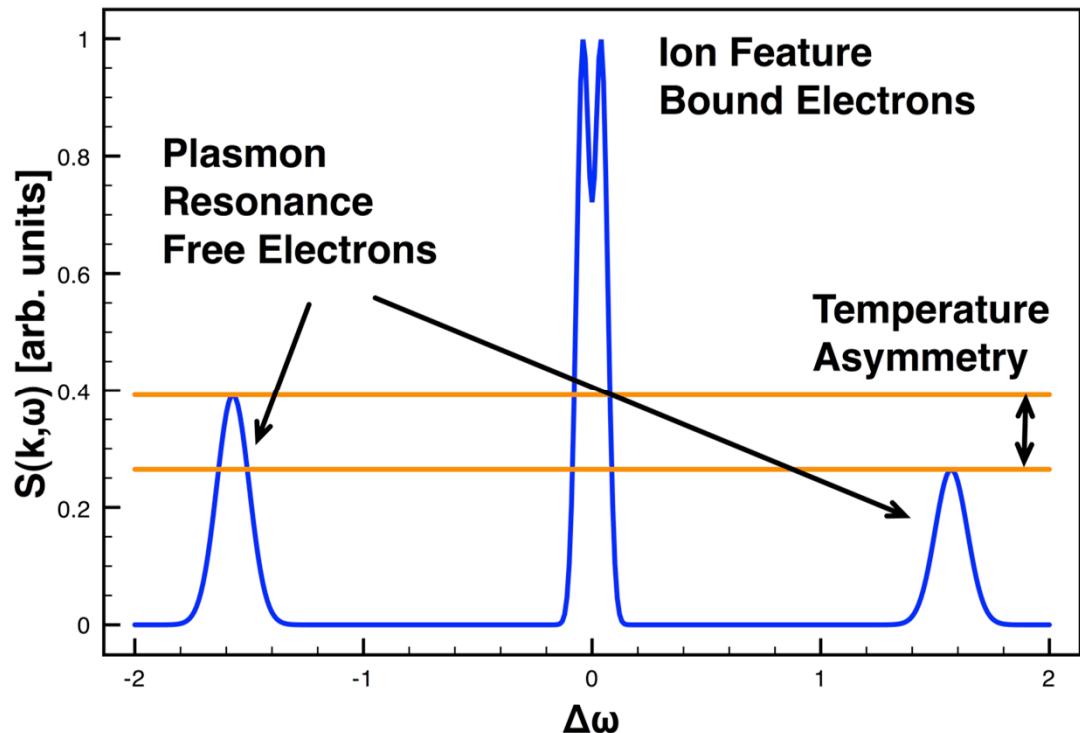


# X-Ray Thomson Scattering, a New Diagnostic, in Warm Dense Matter

- Diagnosing Warm Dense Matter
- X-Ray Thomson scattering can test EOS by providing a measure of bulk **temperature**, density, and ionization state (not surface limited)
- Used (or soon to be used) at several facilities:
- Z-Machine, Omega, DESY , Tsinghua, and many more



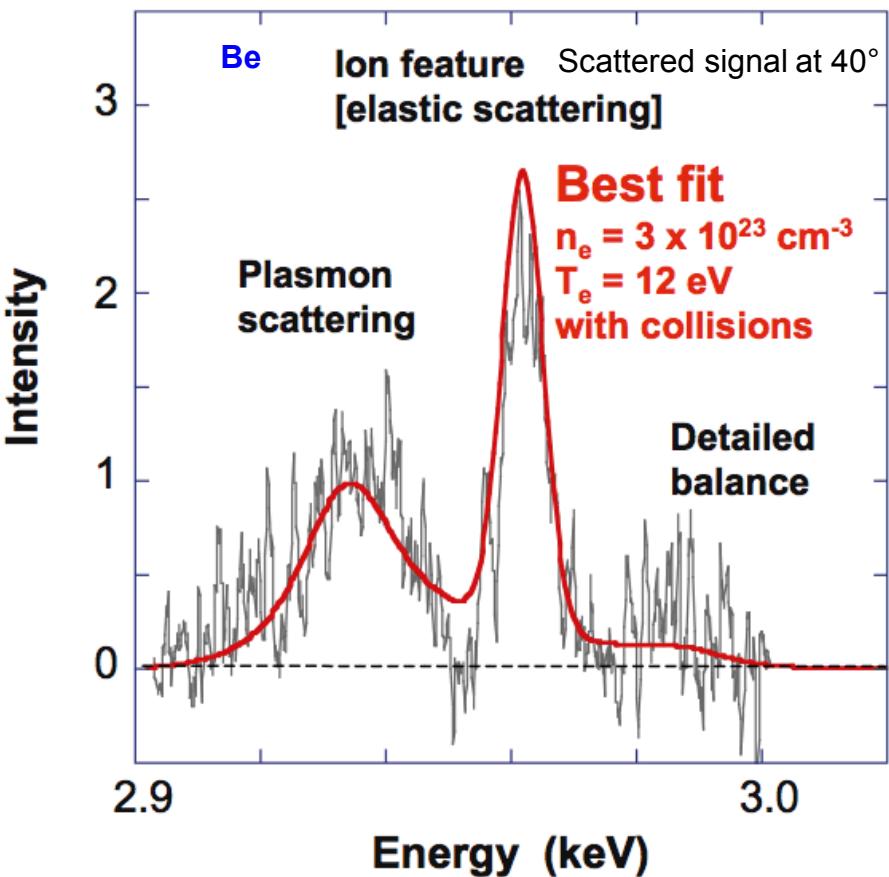
# Temperature Diagnostic X-Ray Thompson Scattering



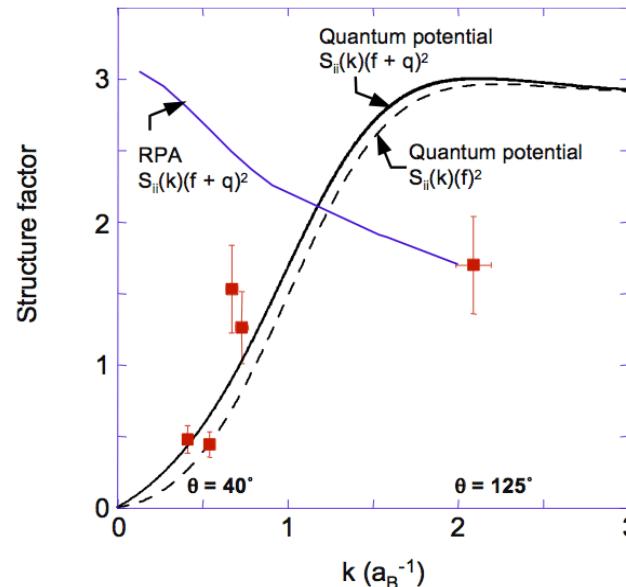
$$S^{tot}(k, -\omega) = \text{Exp}\left(-\hbar\omega / k_B T\right) S^{tot}(k, \omega)$$

- Based on fundamental principle of detailed balance
- Temperature diagnostic for warm dense matter
- Structural information about a material
- Works at low  $k$  based on models (Chihara) that use unphysical ion structure factors from classical plasma simulations with *effective quantum potentials*

# X-Ray Thomson scattering has delivered temperature measurements and questions



Beryllium data from Glenzer, *et al.*, Phys. Rev. Lett. 98 (2007)



$$S(k, \omega) = (f(k) + q(k)) S_{ii}(k) \delta(\omega) + Z_C S_{ee}(k, \omega) + S_{cv}(k, \omega)$$

The Chihara models that “work” at low  $k$  use unphysical ion structure factors from classical plasma simulations w effective “quantum potentials”.

Core-valence separation; frequency domains of validity

# Most Direct Simulation through the Dynamic Structure Factor

- Time-domain quantum mechanics simulations allows a direct calculation of the structure factor  $S(k, \omega)$  that
  - Includes quantum degeneracy
  - Correlations
  - Electrons and nuclei out of thermal equilibrium
  - Non Fermi-Dirac distributions
  - Collective excitations

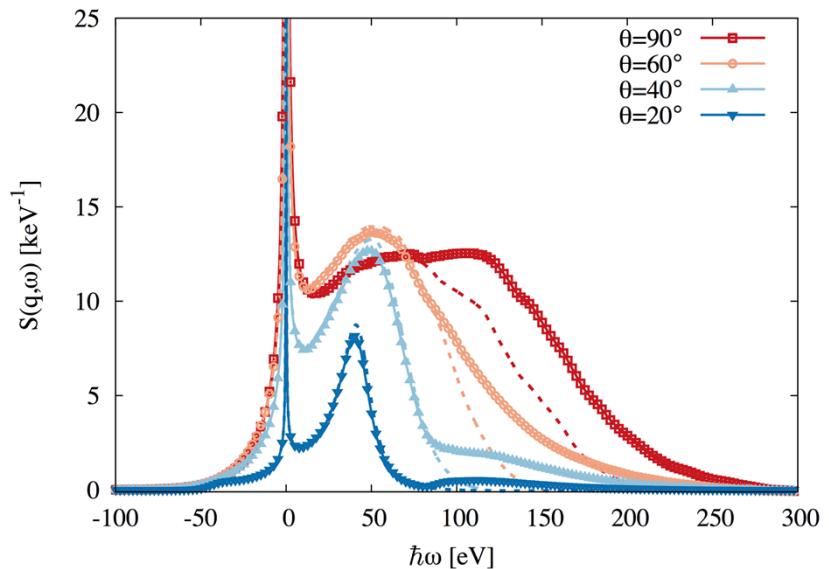
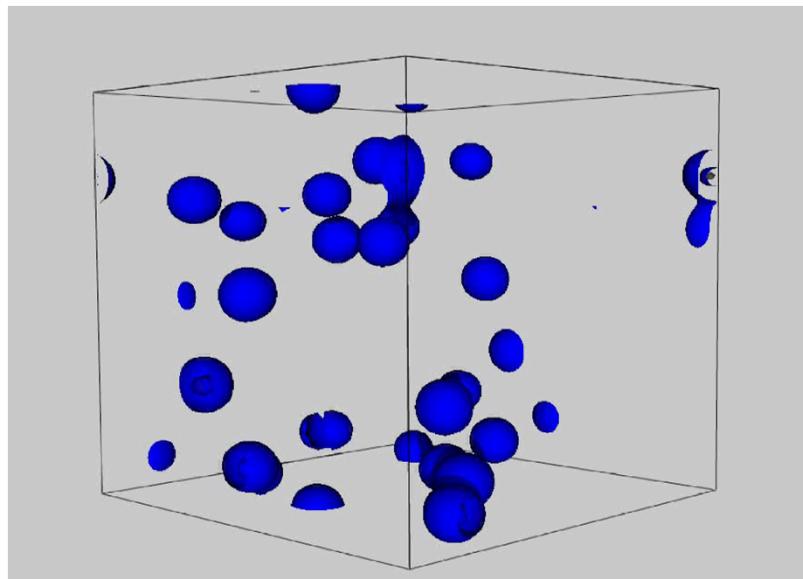
$$\frac{d\sigma}{d\omega d\Omega} = \sigma_T S^{tot}(k, \omega) \quad S_{ee}^{tot}(k, \omega) = \frac{1}{N_{\text{ion}}} \left\langle \left| \rho_e^{\text{tot}}(\mathbf{k}, \omega) \right|^2 \right\rangle$$

# Movie: X-Ray Thomson Scattering Calculation

$$\delta v_{pert.}(r, t) = v_0 e^{iq \cdot r} f(t)$$

$$\delta \rho(k, \omega) / v_0 f(\omega) = \chi(k, -k, \omega)$$

$$S(k, \omega) = -\frac{1}{\pi} \frac{\text{Im}[\chi(q, -q, \omega)]}{1 - e^{-\omega/kT}}$$



Compressed and heated Be  
mass density 5.5 g/cm<sup>3</sup> and Te = 13 eV

# The LDRD Team



BACZEWSKI, ANDREW



SHULENBURGER, LUKE



DESJARLAIS, MICHAEL P.

- The Z team
- Thomas Mattsson
- Stephanie Hansen
- Dawn Flicker
- Seth Root
- Kyle Cochrane
- Programmatic leadership
- The Cryogenic Team – D. L. Hanson
- Sandia High-Performing Computing (HPC) – S. Corwell
- Supported by the Laboratory Directed Research and Development program at Sandia National Laboratories, a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

# Summary and Future Work

- DFT based MD simulations to model shock compression of mixtures under WDM conditions
- Experimental validation through shots on the Z-machine
- New tools for TDDFT of WDM:
  - Ehrenfest-TDDFT for coupled electron-ion motion in bulk systems
  - Stable, accurate, and scalable PAW implementation
  - XRTS/DSF is primary goal
- Immediately: dielectric function of interesting WDM systems (SEQUOIA).
- Near term: direct calculation of dynamic structure factor.
- Challenge: Identify surface hopping model that gets non-adiabatic electron-ion energy transfer 'right'.



Sandia  
National  
Laboratories



# Direct Simulation Monte Carlo

What is DSMC?

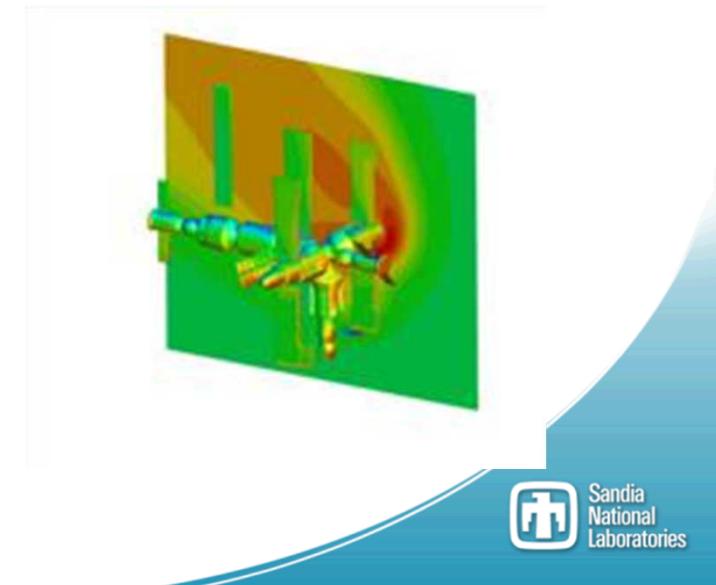
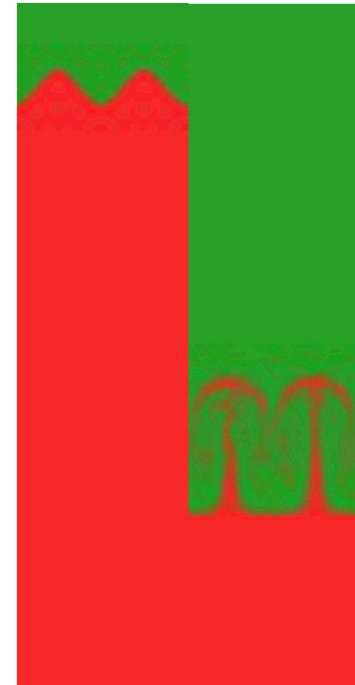
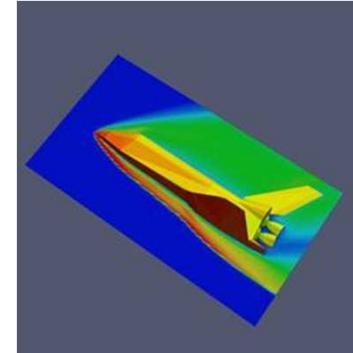
- Probabilistic (Monte Carlo) scattering for finite Knudsen number fluid flows (Prof. Graeme Bird)

Why do we need DSMC?

- Estimation of the Space Shuttle re-entry aerodynamics to the modeling of micro-electro-mechanical systems (MEMS)

At Sandia, SPARTA code

<http://sparta.sandia.gov>

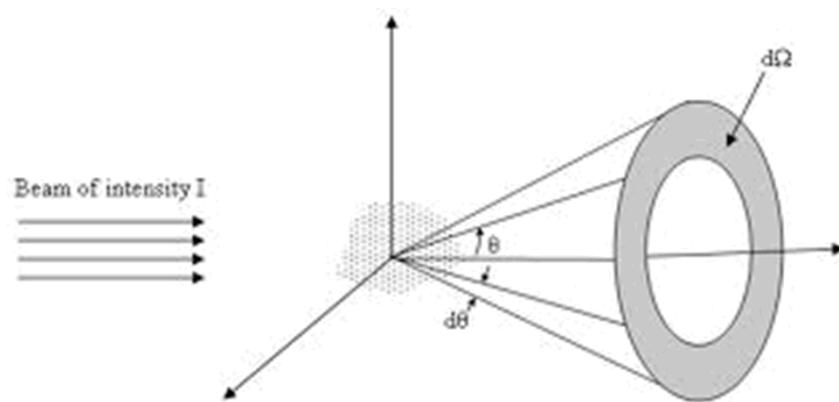


# Parameters Needed for DSMC

$$\lambda = \frac{1}{\sqrt{2n\sigma}} \quad \eta = \left( \frac{4mk_B T}{9\pi\sigma^2} \right)^{1/2}$$

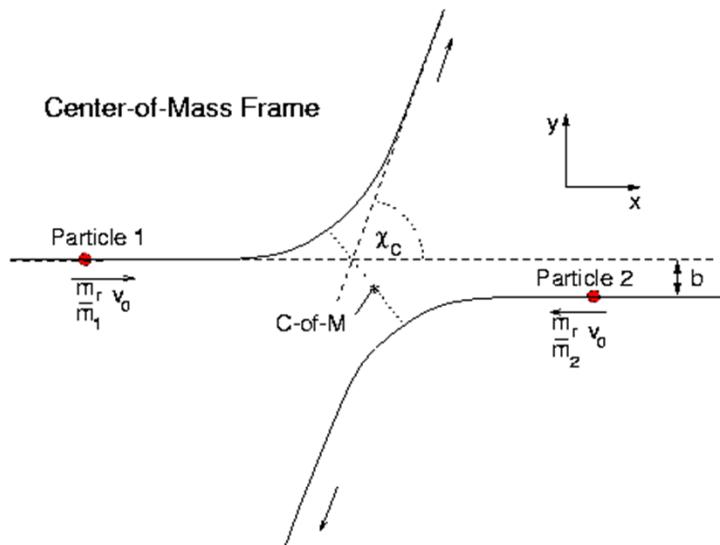
- The mean-free path is related to the cross-section.
- Viscosity can be calculated and compared to experiment with input of the cross section.
- Cross-section varies with material and temperature.
- The viscosity depends on the material and temperature, not on the density.

# Cross-Sections Related to Scattering Angles

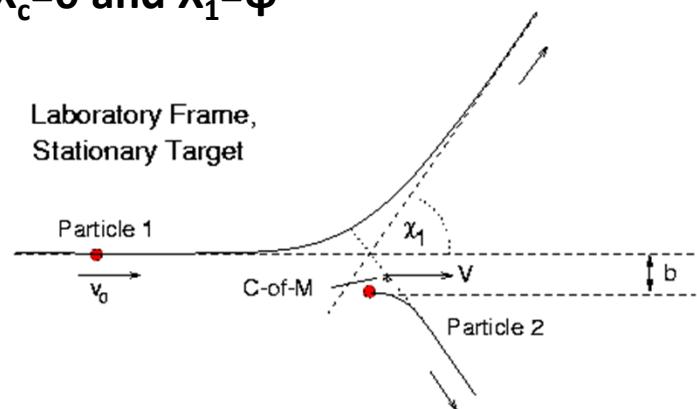


We need to model:

- Scatter and scattered particles
- Impact parameters
- Measures of charge transfer
- Statistics
- Exchange-correlation, external fields and changing potential landscapes

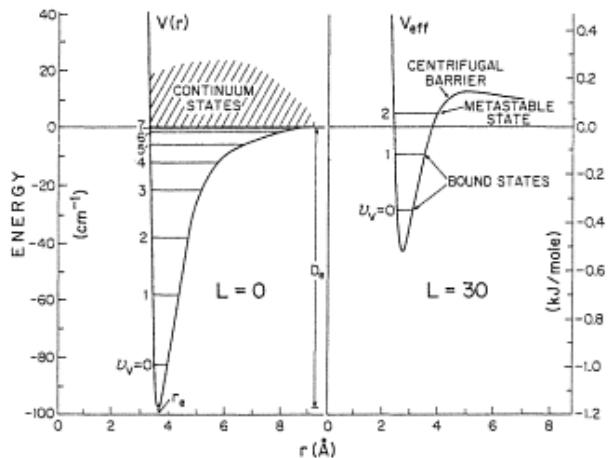


$$x_c = \theta \text{ and } x_1 = \psi$$



# Important Scales

Ar-Ar bond length 3.7 Å



$$v = \sqrt{2k_B T / m}$$

- $V$  is determined by thermal velocities at  $T=2,000\text{K}$
- Mean thermal velocity at  $300\text{K}$ ,  $394\text{ m/sec}$
- Approximately  $0.01\text{ \AA/fs}$
- $X$  displacement  $>$  Ar-Ar van der Waals Bond length
- Impact b recursive halving of initial  $x$  displacement

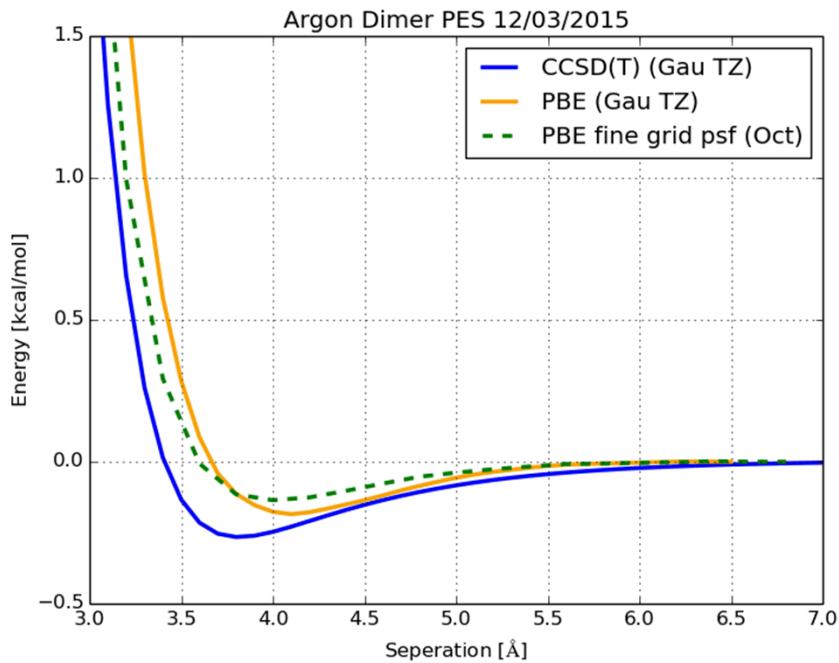
# Basic Set-Up of Calculation

- Octopus 4.1.2  
(<http://www.tddft.org/programs/octopus>) on 8 cores on UNO
- Time step conserves energy of stationary state
- Time-dependent propagation  
Approximated Enforced Time-Reversal Symmetry
- Total time greater than bounce time
- Ehrenfest coupling
- PBE GGA for XC – No van der Waals
- Ar Pseudo potential
- Spin-polarized

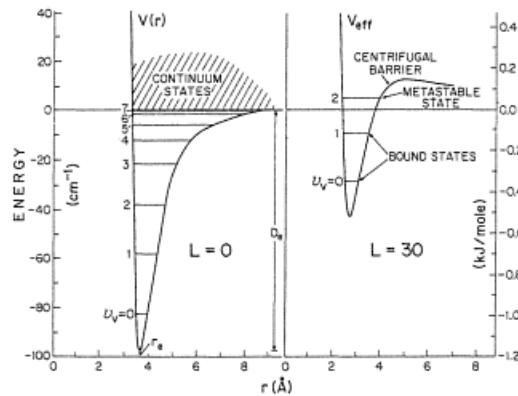


Uno Dell SNL-NM 201	3344	2.7 GHz Intel Sandy
Bridge:2S:8C/4S:8C RHEL 6	GigE	64 / 128 71 TF 29,293,440

# Distance of Initial Separation



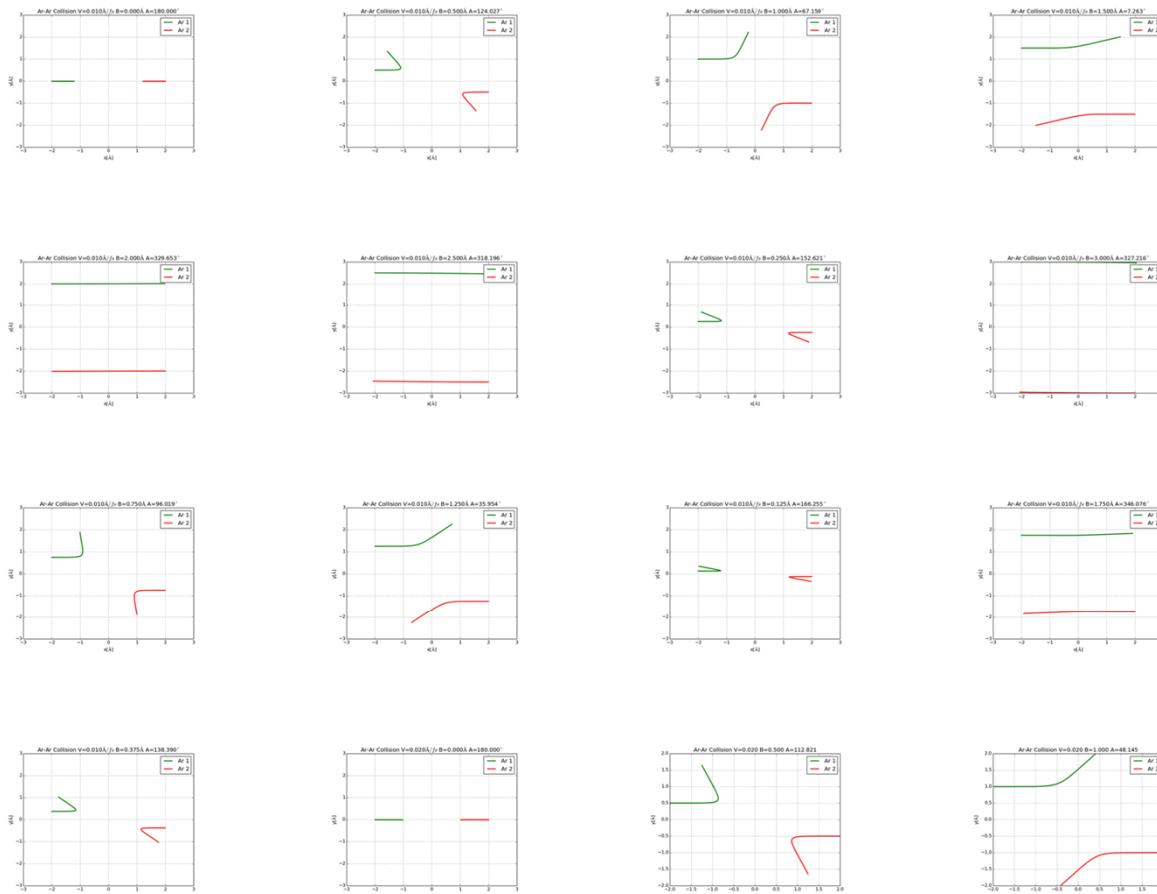
## DISSOCIATION OF VAN DER WAALS MOLECULES



1. The interatomic potential energy curve and energy states  $\text{Ar}_2$ . This figure is adapted from reference 2.

Ar-Ar bond length 3.7 Å

# Typical X-Y Scattering Trajectories, $\theta$ (b,v)



# Scattering Theory

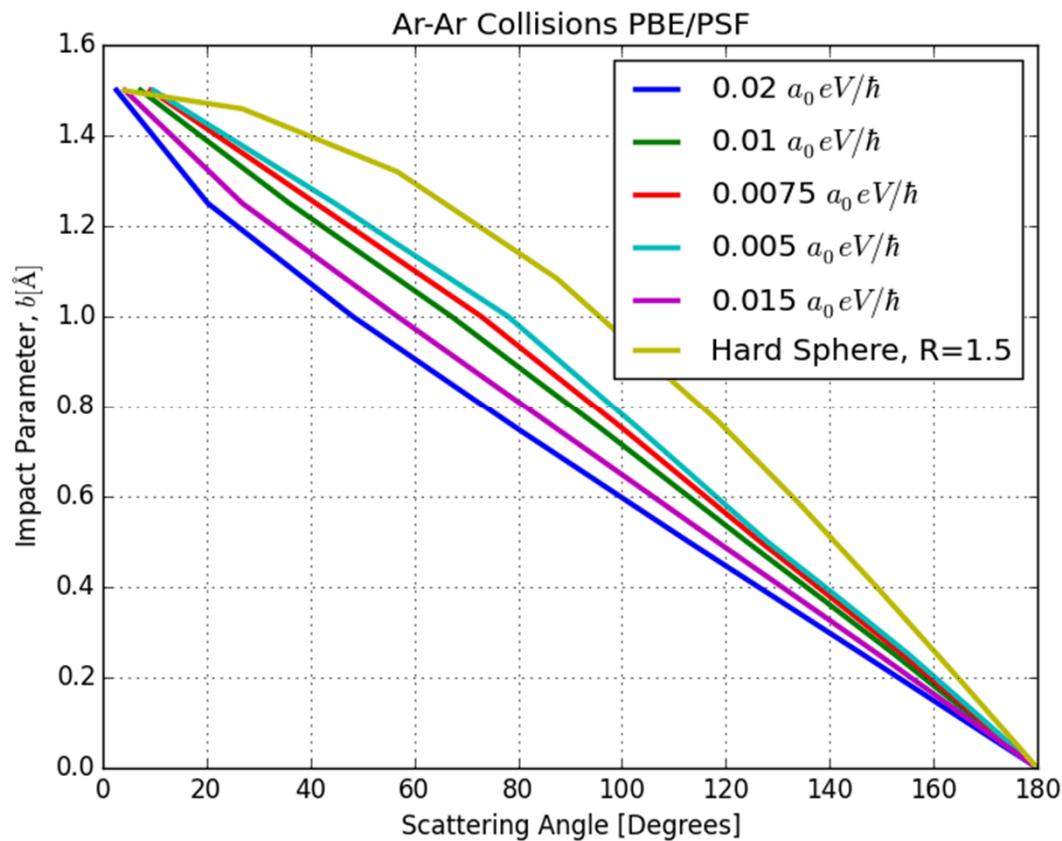
$$\frac{d\sigma}{d\Omega} = \frac{b}{\sin\theta} \left| \frac{db}{d\theta} \right| \quad \sigma = 2\pi \int_0^{180} d\theta \frac{b}{\sin\theta} \left| \frac{db}{d\theta} \right|$$

$$\lambda = \frac{1}{\sqrt{2n\sigma}}$$

Relates trajectories that we can calculate to the mean-free path used in simulations.

Thermal average of cross-sections

# Table of Scattering Angles, $b(\theta, v)$



$$b(\theta) = R_{\text{Hard Sphere}} \cos\left(\frac{\theta}{2}\right)$$

Quite linear in calculated region

Must curve to  $+\infty$  as angle goes to 0

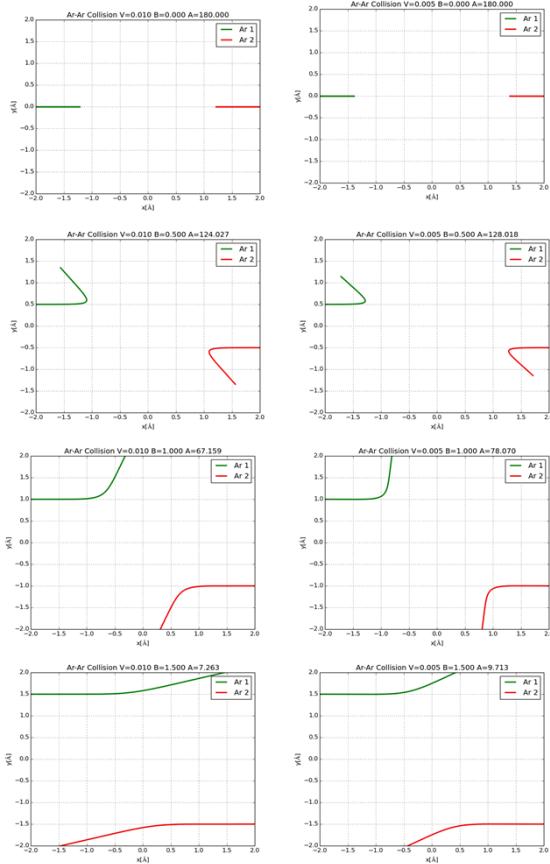
$b(\theta)/\sin \theta$  requires careful consideration as  $\theta \rightarrow 0$ .

Note 1  $a_0$  eV /  $\hbar$  = 0.804 Å/fs

I have run larger impact parameters but I am still testing the reliability of these runs.

# Summary

## TDDFT for DSMC



- TDDFT describes coupled electron-ion dynamics of scattering events without materials specific parameters.
- The approach is general and can be applied to charged species, other elements, and molecules.
- Technical challenges related to simulation cell size and computer power can be overcome at present.
- Accuracy is therefore limited by the choice of functional and pseudo-potential used. Future work will investigate their roles.
- Scattering angle versus impact parameter and velocity are extracted for time-dependent runs.
- Cross sections can be obtained in postposing.
- We have developed a general set of tools (python scripts) to create, to manage, to run, and to post process these simulations.