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Density Functional Theory of Extreme Environments

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Materials Properties are Needed to Model Complex Phenomena through Equations of State.

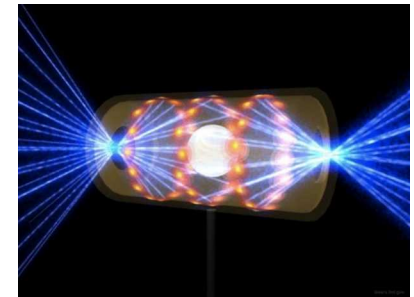
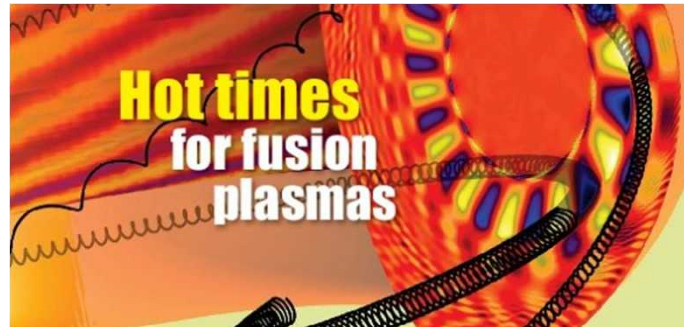
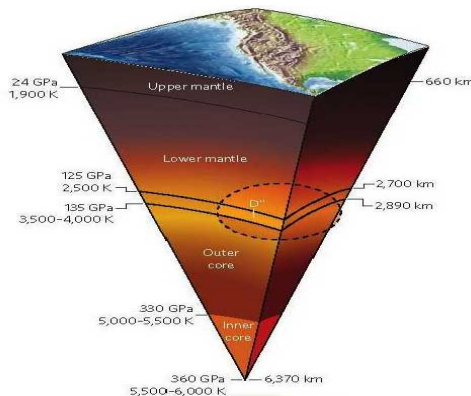


Pressure, density, temperature, phase....

- Materials science
- Planetary collision science
- Geoscience
- Inertial confinement fusion

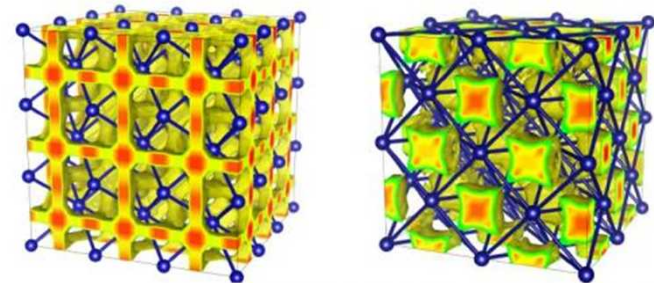
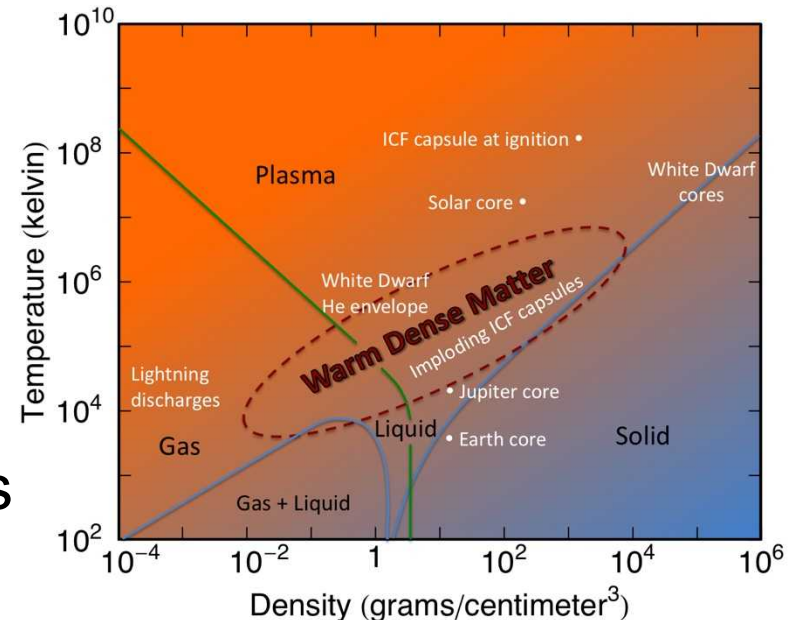
Information to build equations of state typically includes

- Low temperature experiments diamond anvil cell < a few kK
- High temperature plasma physics where degeneracies are negligible



A Difficult Region of Phase Space to Access is the Warm Dense Matter Region.

- Highly compressed matter with electron densities of 10^{21} - 10^{26} electrons / cm^3
- Temperature on the order of several eVs, 10s of kK
- Electron degeneracy significant
- Bound-free electron correlations significant
- Accessible to experiment and theory - Warm dense matter near-solid (2-4x) density
- Mbars of pressure
- The plasmon energy, $\omega_p \sim 1$ -4 eV

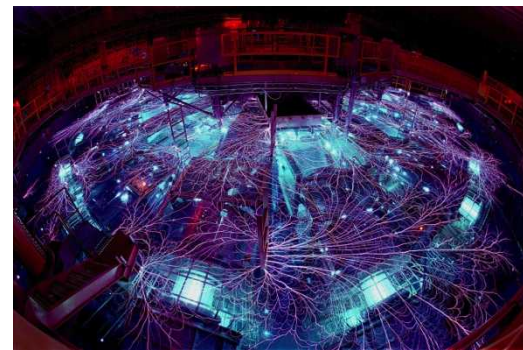
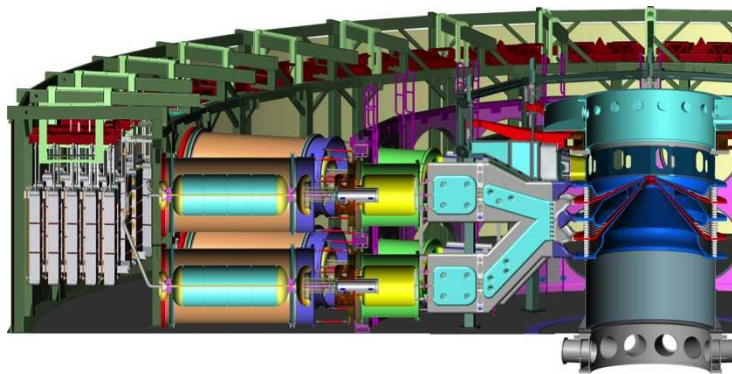


Super ionic water

The Z-Machine can Probe this Region.

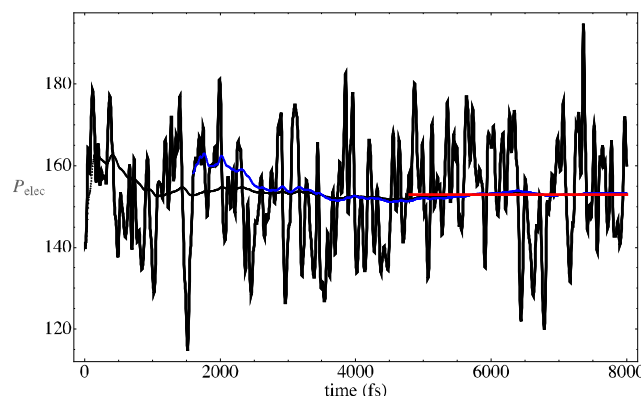
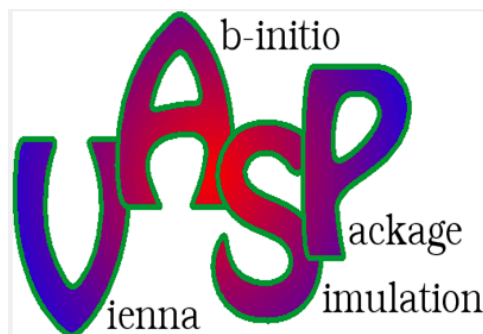
- The world's most powerful pulsed power machine
- Accelerates aluminum flyer plates to 40 km/sec.
- Delivers 27 MegaAmps in 95 nanoseconds.
- Achieves Pressures greater than 10 Mbar (1 TPa).
- Recent work on Xenon reached a state 840 GPa and 149kK
- Compare to diamond Anvil cell – up to 300 GPa and several kK

Indirectly but Accurately Measures **Pressures and Densities**



First Principles Probes

- First principles approach to simulations of total energies, pressures, and other physical quantities
- Unbiased as to elemental species
- **First-principles simulations using DFT**
 - VASP – plane-wave code with PAW core-functions
 - Great care in convergence
 - A. E. Mattsson et al. *Modelling and Simulation in Material Science and Engineering* **13**, R1 (2005)
 - Importance of exchange-correlation functional
 - A. E. Mattsson et al. *JCP* **128**, 084714 (2008)



Molecular dynamics (MD) simulations
give thermo-physical properties



TOP10 November 2013

- 1 **Tianhe-2 (MilkyWay-2)** - TH-IVB-FEP Cluster, Intel Xeon E5-2692 12C 2.200GHz, TH Express-2, Intel Xeon Phi 31S1P
NUDT
- 2 **Titan** - Cray XK7 , Opteron 6274 16C 2.200GHz, Cray Gemini interconnect, NVIDIA K20x
Cray Inc.
- 3 **Sequoia** - BlueGene/Q, Power BQC 16C 1.60 GHz, Custom
IBM

DFT, DFT-MD, and TDDFT

Density functional theory (DFT):

- Electron degeneracy/correlation treated exactly .
- Many-body Schrodinger equation from $R^{3N} \rightarrow R^3$.
- Ground state or equilibrium thermal state.

Density functional theory molecular dynamics (DFT-MD):

- DFT electronic state \rightarrow forces on ions.
- Typically within Born-Oppenheimer approximation.

Time-dependent density functional theory (TDDFT):

- Exact treatment of electron dynamics.
- Excited states.
- Ehrenfest-TDDFT \rightarrow forces including excited electronic states.
- Electrons and ions do not have to be in equilibrium.

We have implemented Ehrenfest-TDDFT in an existing projector-augmented wave (PAW) code.

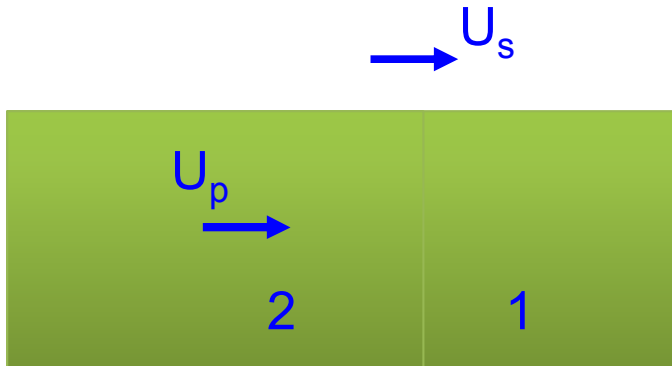
(Plane wave basis with a soft cutoff)

'Most accurate' treatment of electron-ion interaction

**Approximations
in DFT are not
material
specific.**

Validation of the DFT-MD Simulations

- Compare simulation results to Z-data
- Convenient –especially in the warm dense matter regime – connection through the Hugoniot
- Example successes Xe and Ethane
- Note the dissociation of the latter
- *Conservation of mass, energy, and momentum* lead to the **Rankine-Hugoniot condition** for the initial (1) and final state (2).

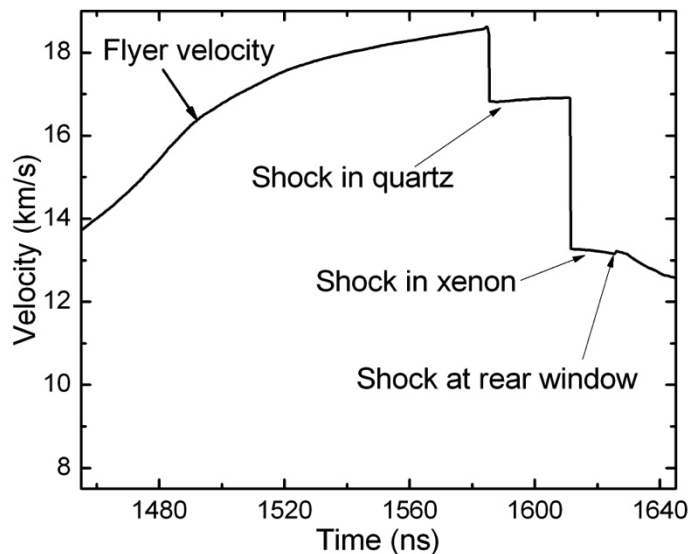
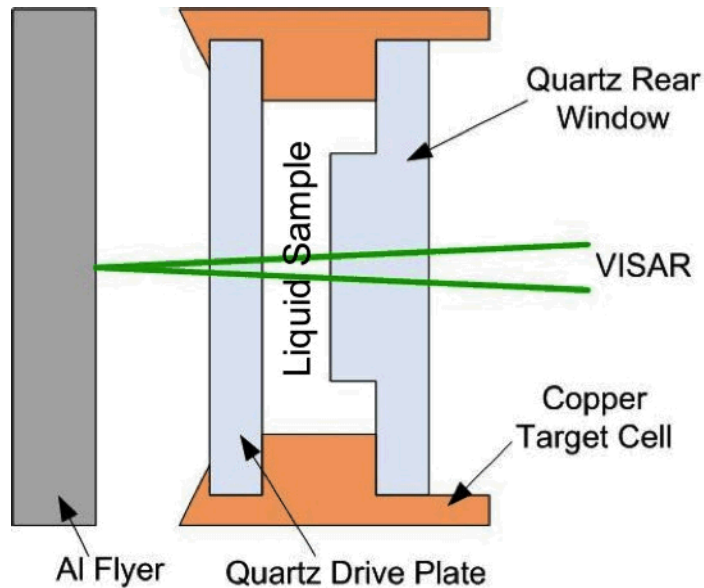


- E - internal energy
- P - pressure
- v – specific volume

$$2(E_2 - E_1) = (P_2 + P_1)(v_1 - v_2)$$

- *High accuracy measurement and/ or calculations of thermo-physical properties* can be compared to validate understanding.

We Measure Shock Velocities in Materials with Sub-Percent Accuracy



Precision Accuracy and
Reproducibility

VISAR main diagnostics

Flyer velocity, time of impact

Arrival at interfaces and breakout

Shock velocity in samples

Monte-Carlo error analysis

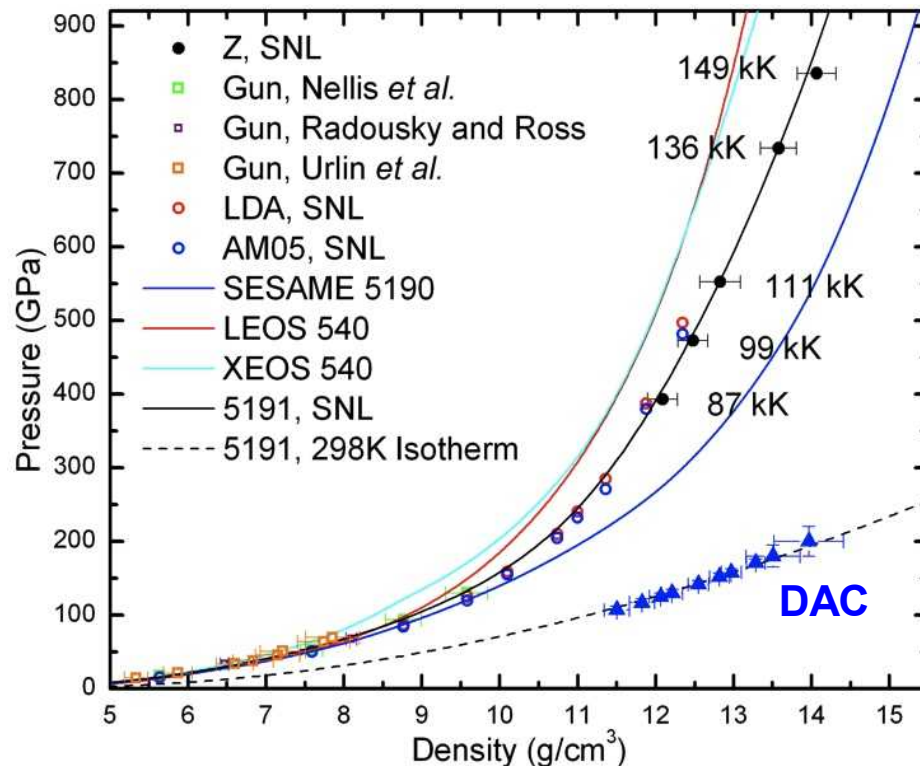
Accuracy of shock standards

Correlation among parameters

Error propagation

VISAR trace from a
xenon experiment with
18.5 km/s impact velocity

Experiments on Sandia's Z Machine Obtained High-Precision Data for Xenon to 840 GPa/ 14 g/cm³



Seth Root et al Phys. Rev. Lett.
105, 085501 (2010)

Neither LEOS 540 nor SESAME 5190 captures the behavior of xenon above 100 GPa

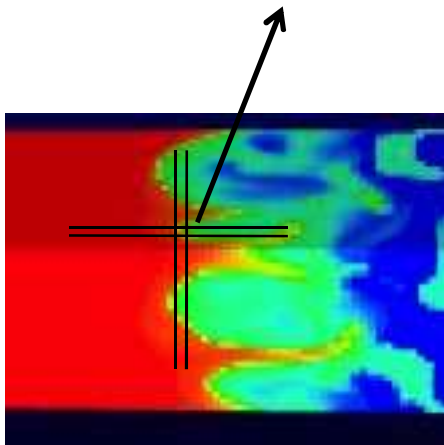
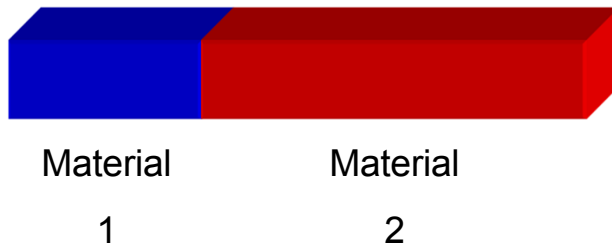
Demonstrated the need for validating EOS tables to enable high-fidelity simulations

Developed a new multi-phase wide-range EOS table: 5191 in the LANL database

AM05 GGA developed by Ann Mattsson (SNL) is highly accurate for WDM.

Hydrocodes, Materials, and Mixtures

A cell in a hydro simulations
with two materials “mixed cell”



- High-fidelity hydrodynamics simulations to solve solid dynamics problems
- Require high fidelity equation of state (EOS) models to describe the response of materials to external stimuli e.g. $P[\rho, T]$
- Materials can mix.
- Dynamic mixing can occur for example through Rayleigh Taylor instabilities.
- For practical reasons, a rule must be used to combine EOS models of pure materials to EOS of mixtures.

Tom Haill
Al Liner impacting on foam

Classical Mixing Rules for Binary Mixtures Developed for Nineteenth Century Engineering Problems

$$x = \frac{\rho_L}{\rho_L + \rho_H} = \frac{\rho_L}{\rho}$$

- Ideal (Ideal gas law astrophysics)

$$P = x P_L [\rho, T] + (1 - x) P_H [\rho, T]$$

- Volume (Dalton's law 1801 related to cell approaches)

$$P = P_L [x\rho, T] + P_H [(1 - x)\rho, T]$$

- Pressure (Amagat's 1880 law of partial volumes some hydro-codes)

$$P_{MIX} = P_L [\tilde{\rho}_L, T] = P_H [\tilde{\rho}_H, T], \quad \frac{x}{\tilde{\rho}_L} + \frac{(1 - x)}{\tilde{\rho}_H} = \frac{1}{\rho},$$

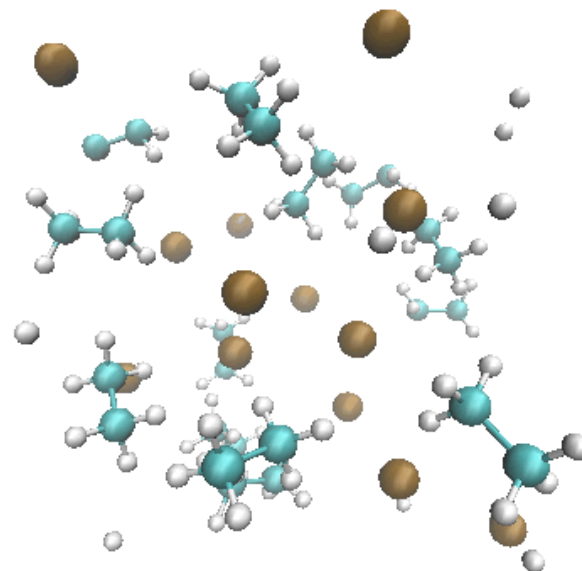
$$f_L \tilde{\rho}_L = \rho_L, \quad f_H \tilde{\rho}_H = \rho_H$$

- Relates total pressure of the mixture to equation of state models of the pure states



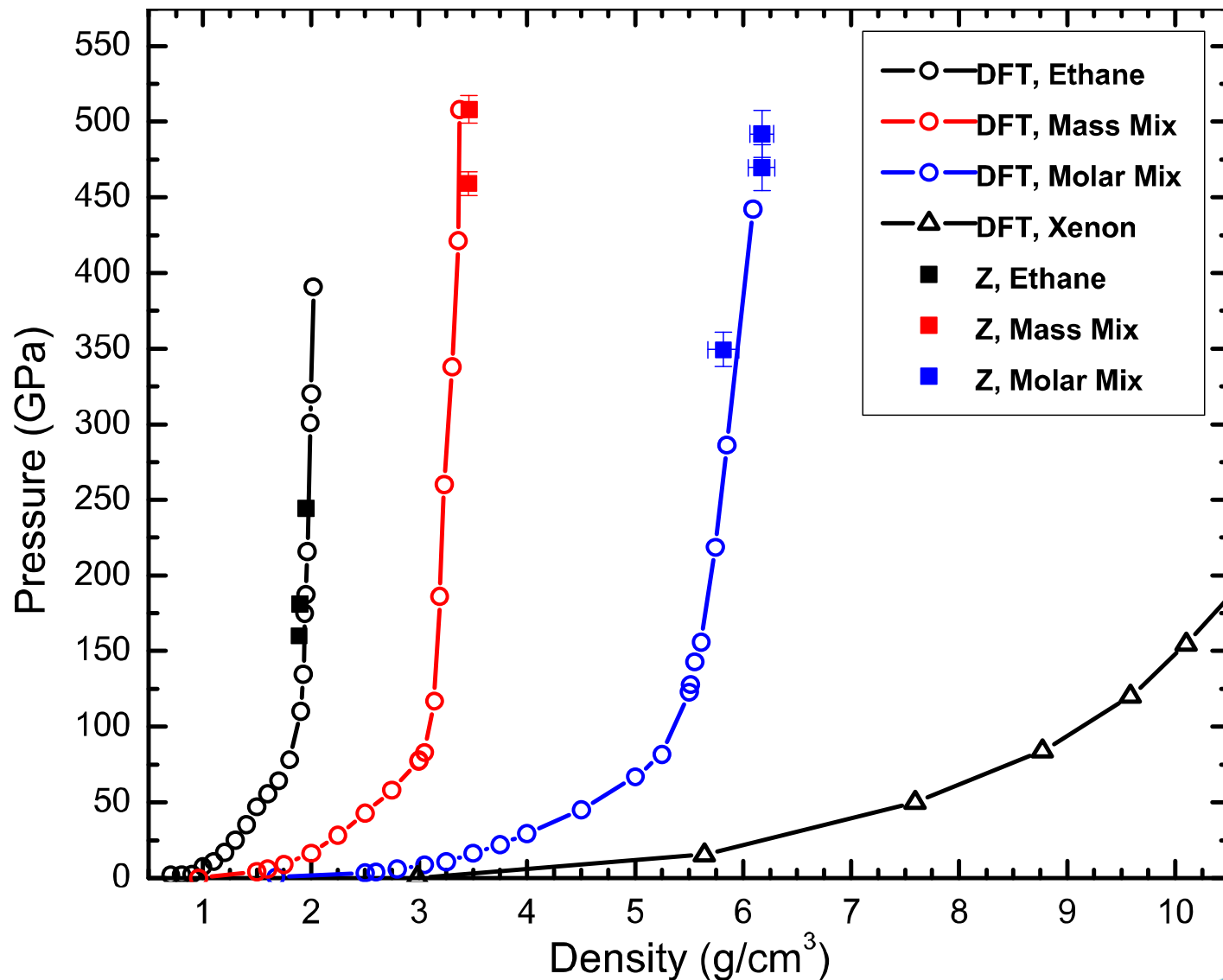
Xe-Ethane (C_2H_6) Mix Hugoniot Reference State

- $T=163.5$ K
- $\rho=1.5$ and 1.7 g/cc
- $P=16.8$ psi
- Molar mix ratios 42% and 50%
- Mass mix 5 Xe:18 Ethane (159 atoms per simulation) $x=0.5$
- Molar mix 13 Xe:13 Ethane (117 atoms per simulation) $x=0.19$
- Plane-wave energy cut off 900 eV
- Time steps 0.8-0.04 fs
- 8000 time steps
- Mean value point
- AM05 exchange-correlation results shown

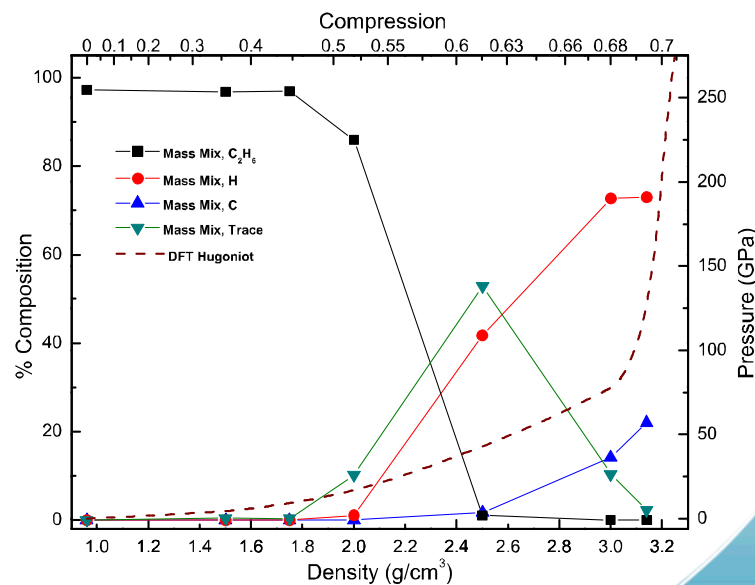
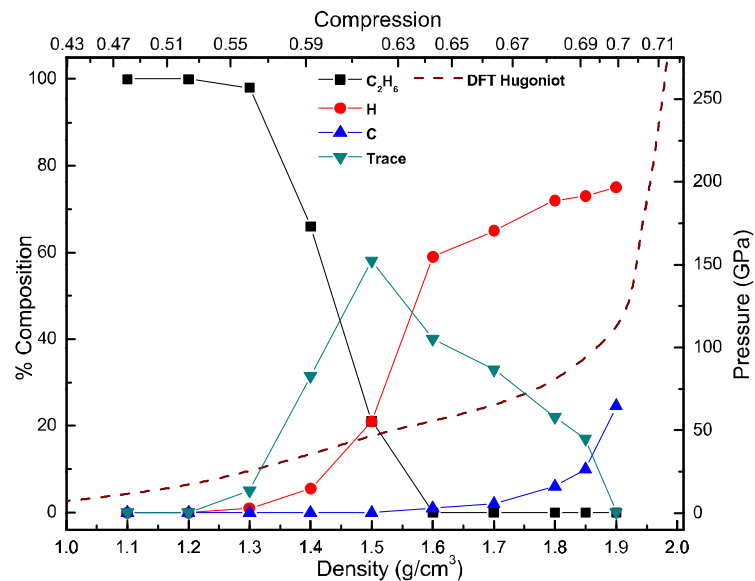
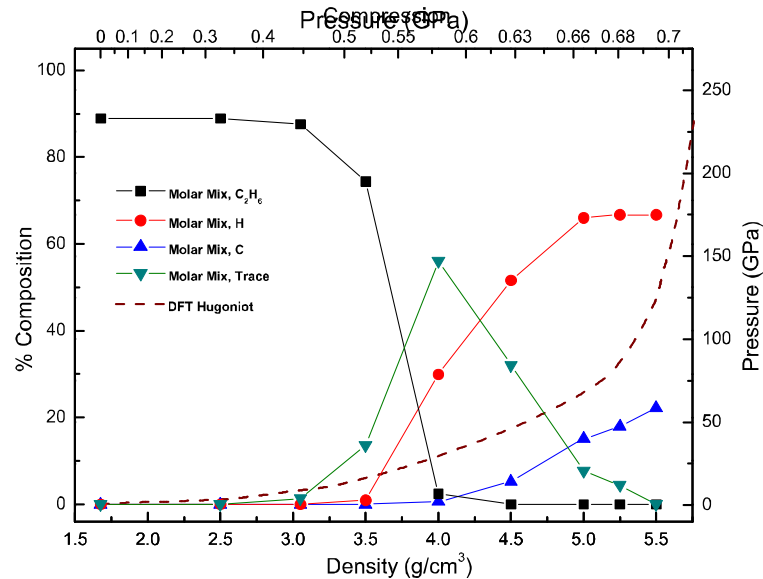
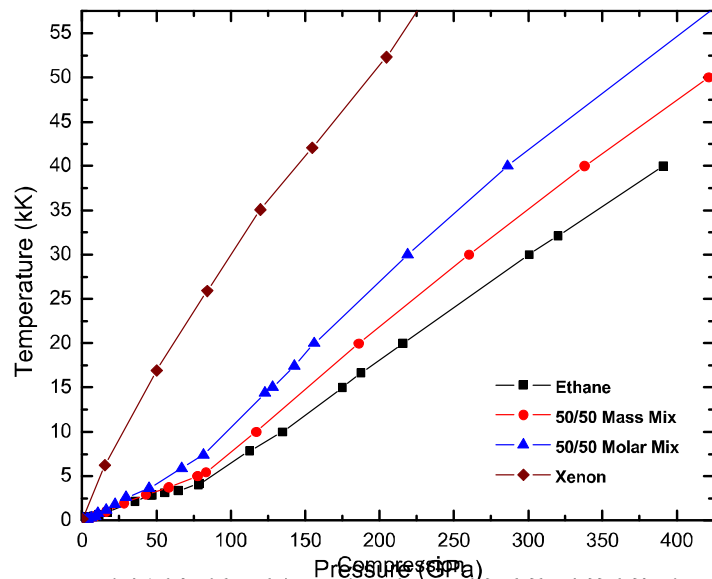


$$x = \frac{\text{Ethane mass}}{\text{Xenon and Ethane mass}}$$

Xe-Ethane Mix Hugoniot

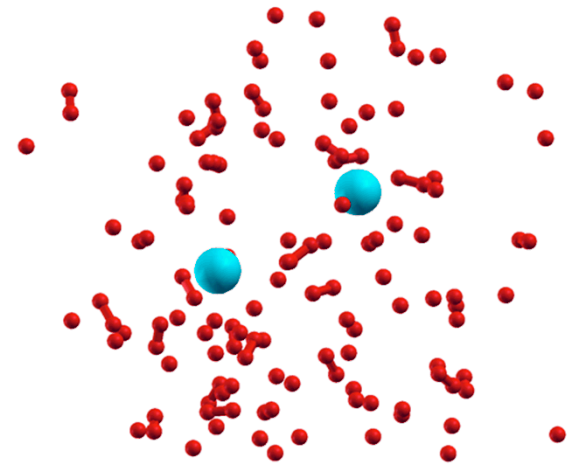


Decomposition Along the Hugoniot



Mixing Ratio for Binary Mixture

High Z- low Z mixture used in gas puff experiments
Difficult to mix experimentally



$$x = \frac{\text{Deuterium mass}}{\text{Xenon and Deuterium mass}}$$

Mix Ratio	# of Xe Atoms / Cell	# of D Atoms / Cell
0.0	32	0
0.3	3	84
0.5	2	132
0.67	1	132
1.0	0	200

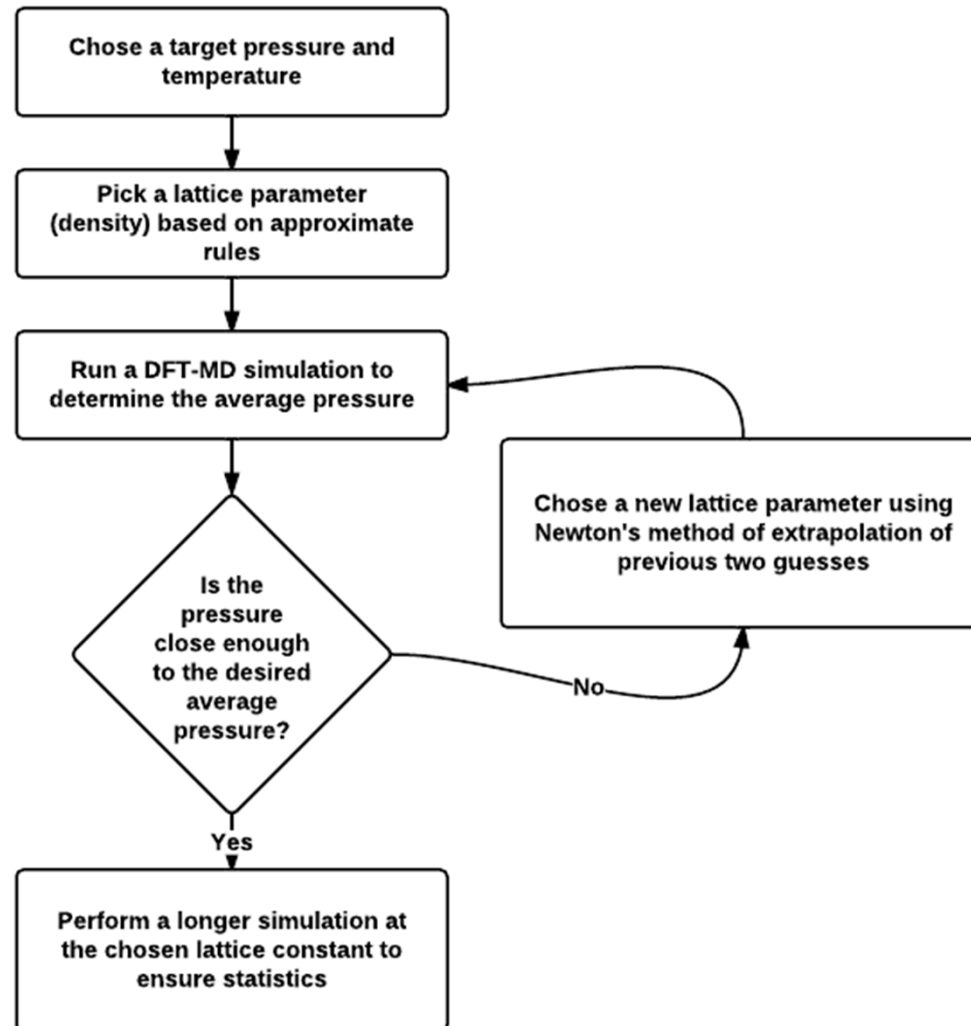
Note: Deuterium mass / Xenon mass ≈ 0.015

According to the ideal gas law: P is proportional to n the number density

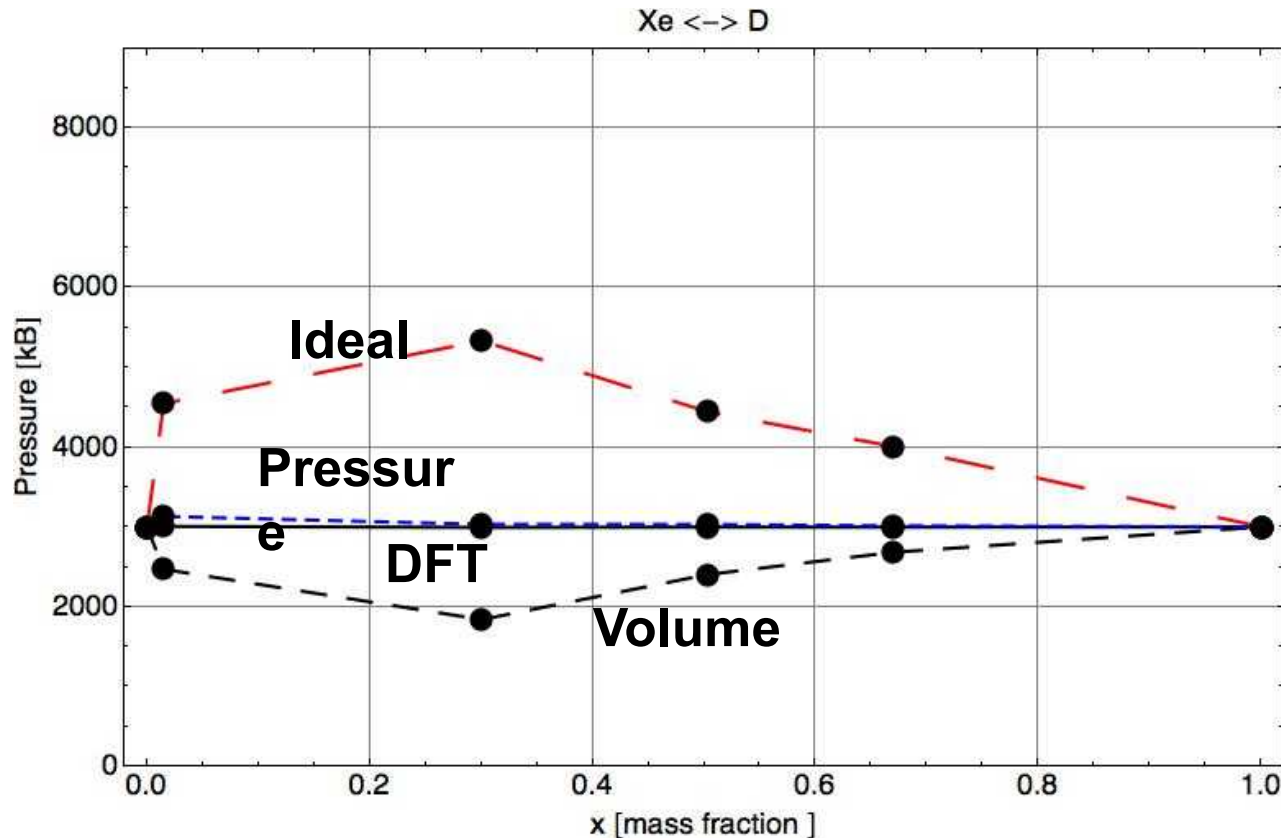
To achieve similar pressures the mass densities are related $\rho_{\text{Xe}} \approx 100 \rho_{\text{D}}$

Constant Pressure Calculations

Implementation at First Principles Simulations



Xe-D with fixed pressure: DFT/AM05, SESAME 5365 for D



• $T = 10$
kK

Pressure: blue
short-dashed
Ideal: red long-
dashed

DFT: solid
black
Volume: black
medium-
dashed

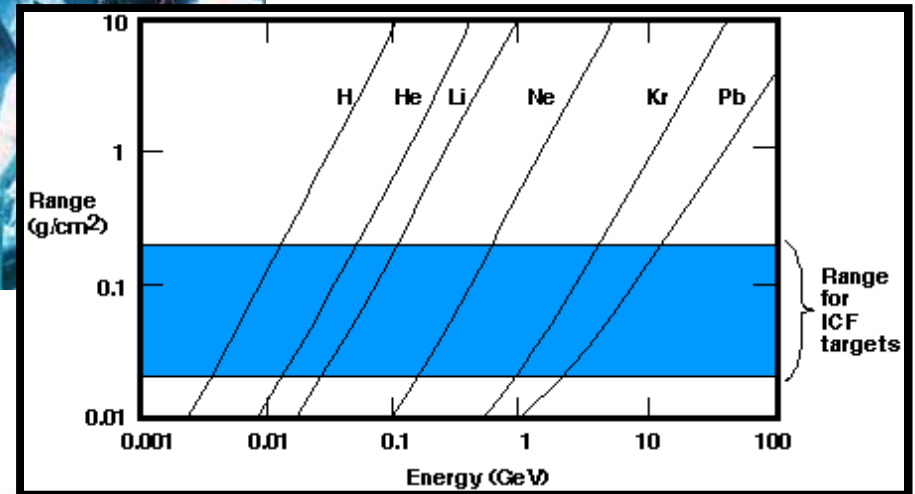
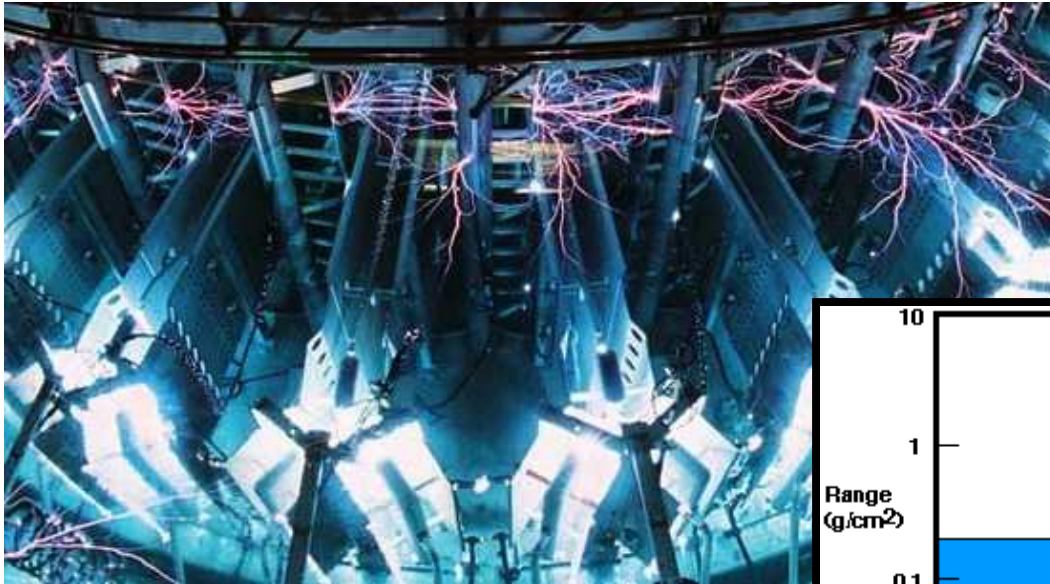
$\rho_{\text{Xe}} = 15.9 \text{ g/cc}$

Magyar and Mattsson, Phys. Plasmas **20**, 032701 (2013)

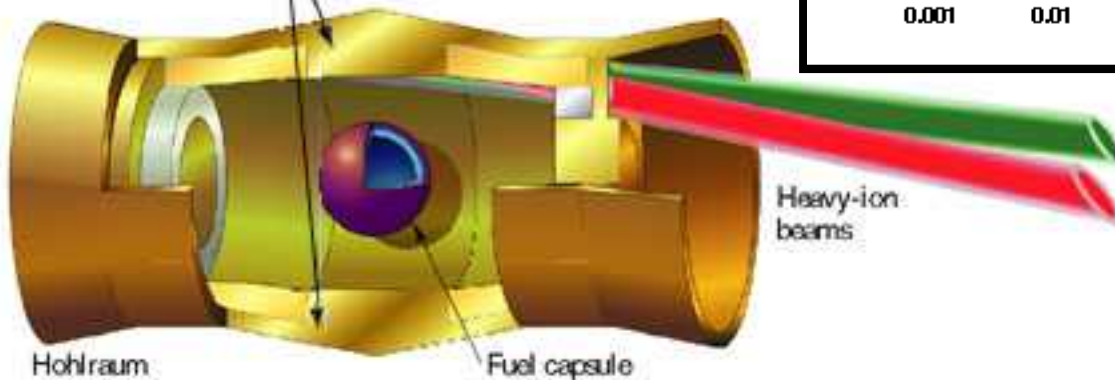
Notes: Ideal mixing rule is clearly flawed especially for small x .

Volume mixing predicts lower pressures than DFT-MD.

Stopping Powers for Inertial Confinement Fusion and Warm Dense Matter



Radiation converters

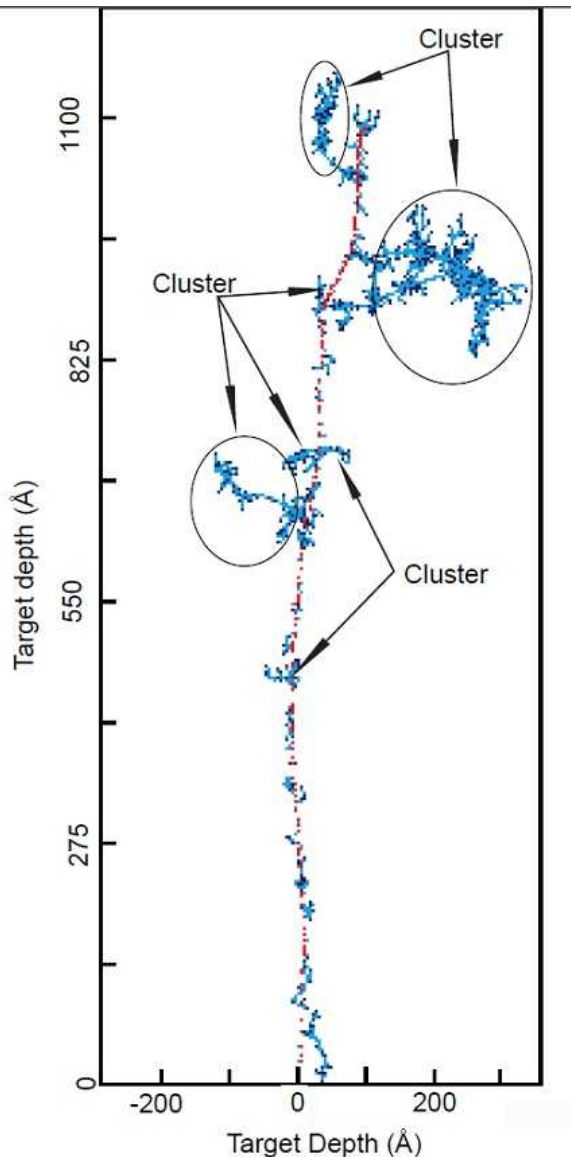


Heavy-ion
beams

Hohlraum

Fuel capsule

Stopping Power



$$S(E) = -dE_{\text{Projectile}} / dx$$

**Penetration
Depth :**

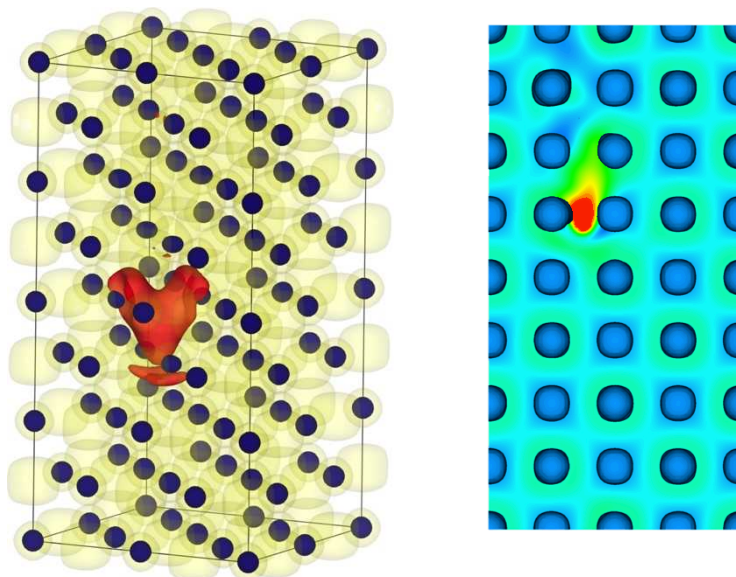
$$\Delta x = \int_0^{E_0} dE \frac{1}{S(E)}$$

Common Materials Monte Carlo Data Tabulated:

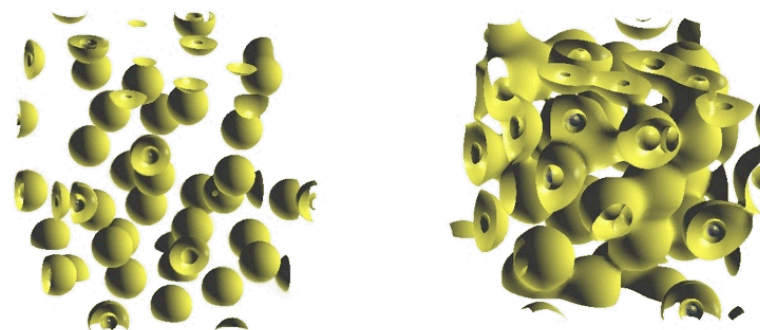
www.srim.org

Developments Required for TDDFT of WDM

- Extended system for dense disordered materials
- Real-time evolution to allow non-harmonic nuclear motion to couple
- Extended system optical or small q response
- Finite temperature theory
- Coupled-electron-ion motion
- Electron-ion energy transfer



$$i \frac{\partial}{\partial t} \phi_i(r, t) = \left[-\frac{1}{2} \nabla^2 + v_{KS}[\Psi_0, \Phi_0, n](r, t) \right] \phi_i(r, t)$$



Approaches to Stopping in Real-Time Electron Dynamics Simulations

1. Total energy – Constant velocity projectile, increasing total energy of system
2. Forces on nuclei – Direct solution of forces of projectile
3. Perturbative – Relationship to dielectric response of system

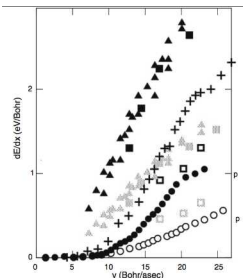
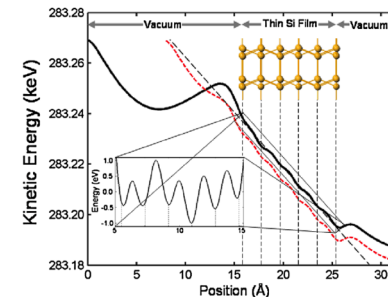


Fig. 1. Electronic stopping power dE/dx as a function of the particle velocity v for p (filled symbols) and α (empty symbols). Circles are the calculations while triangles and squares indicate, respectively, the measured values of 70 and 110. Grey triangles and squares are these measured values scaled by 1/2, for direct comparison with the calculations, which only considered channeling superlatoms. Crosses indicate calculations for p including additional basis orbitals along the projectile's path (see text).

J.M. Pruneda et al. Nuclear Instruments and Methods in Physics Research B 267 (2009) 590–593

J. M. Pruneda, D. Sánchez-Portal, A. Arnau, J. I. Juaristi, and E. Artacho, Electronic stopping power in LiF from first principles, [Phys. Rev. Lett. 99, 235501 \(2007\)](#).



R. Hatcher, M. Beck, A. Tackett, and S.T. Pantelides, Phys. Rev. Lett. 100, 103201 (2008).

Electron-Dynamics through TDDFT

Time-dependent KS Scheme Builds Upon the Highly Successful Ground-state Theory

$$i \frac{\partial}{\partial t} \phi_i(r, t) = \left[-\frac{1}{2} \nabla^2 + v_{KS}[\Psi_0, \Phi_0, n](r, t) \right] \phi_i(r, t)$$

$$\phi_i(\mathbf{r}, 0) = \phi_i^T(r) \quad \int d^3r \phi_i(r, t) \phi_j(r, t) = \delta_{ij}$$

$$n(r, t) = \sum_i^{occ.} |\phi_i(r, t)|^2$$

In the spirit of KS DFT, we postulate that a non-interacting system with a judiciously chosen potential can reproduce the time dependent density.

Non-linear and complex

$t_{\text{electron}} \ll t_{\text{nuclei}}$ for long simulations 50000 time steps typical > 5000 in DFT-MD

Elevated-Temperature Time-Dependent Density Functional Theory (ET-TDDFT)

$$n(r, t) = \text{Tr}[\hat{n}(r) \hat{\rho}(t)] = \sum_{\text{norbs}} w_i(t) |\phi_i(r, t)|^2$$

$$w_{N,i} = f\left[\beta(\varepsilon_{N,i} - \mu N)\right]$$

- Mermin formulation
- Ground-state exchange-correlation Functionals (local density and gradient approximations)
- Chemical bonds
- Thermostats
- Molecular dynamics of the nuclei

$$n(r, t) = \sum_i^{\text{occ.}} w_i |\phi_i(r, t)|^2, f_i \leq 1$$

Electron-Ion Equilibration

Hot ions and cold electrons or Hot electrons and cold ions

Often modeled in terms of a 2 temperature model

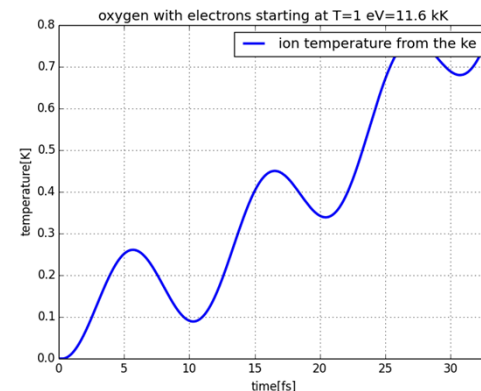
$T_{\text{equilibration}} = 0.33 - 10 \text{ ps}$

Runge-Gross Leaves the Question of Weights Open

- Different representations of TDDFT ensemble densities
- NVT thermal density but NVE propagation?!

$$\hat{\rho}^{Exact} = \sum_i w_{i,\beta} |\Psi_i\rangle\langle\Psi_i|$$

$$\hat{\rho}^{Mermin} = \sum_i w_{i,\beta} |\phi_i(w_{i,\beta})\rangle\langle\phi_i(w_{i,\beta})|$$



Trouble with Von Neumann and Mermin States

- Assume for example non-interacting Fermions.
- Try to connect 2 different Mermin states through unitary propagation alone.
- Some mechanism to change occupations is required.

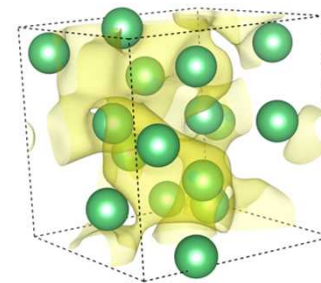
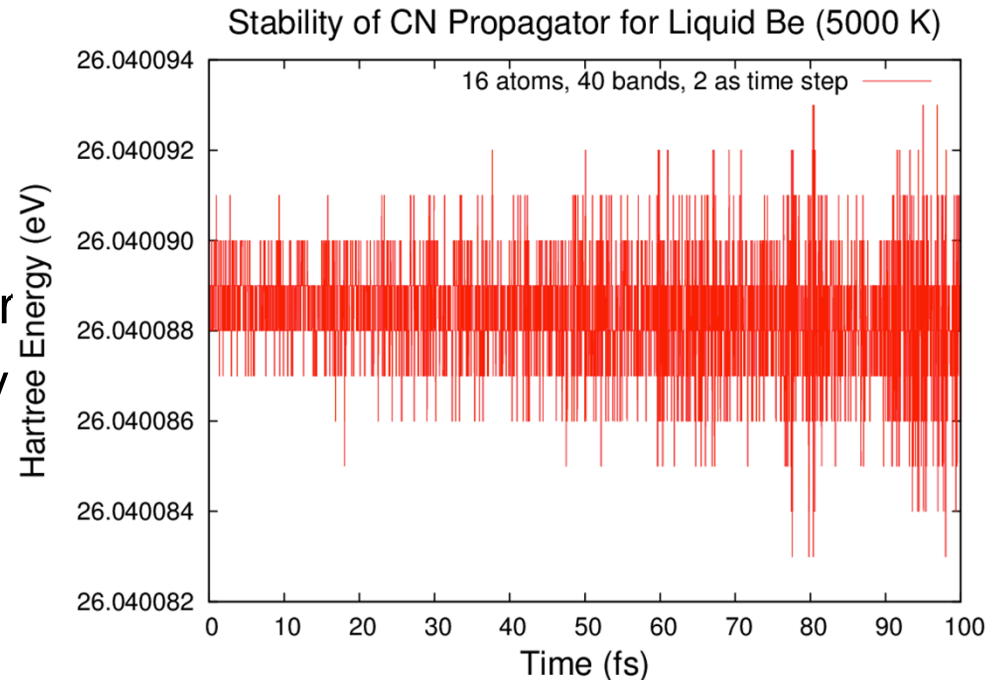
$$\hat{\rho}_1 = \sum_i w_i^{(1)} |\Phi_i\rangle\langle\Phi_i| \quad \hat{\rho}_2 = \sum_i w_i^{(2)} |\Phi_i\rangle\langle\Phi_i|$$

$$\hat{\rho}_2 = \sum_i w_i^{(1)} U(T) |\Phi_i\rangle\langle\Phi_i| U(T)$$

$$U(t) = \sqrt{w_i^{(2)} / w_i^{(1)}}$$

Time-integration and Stability

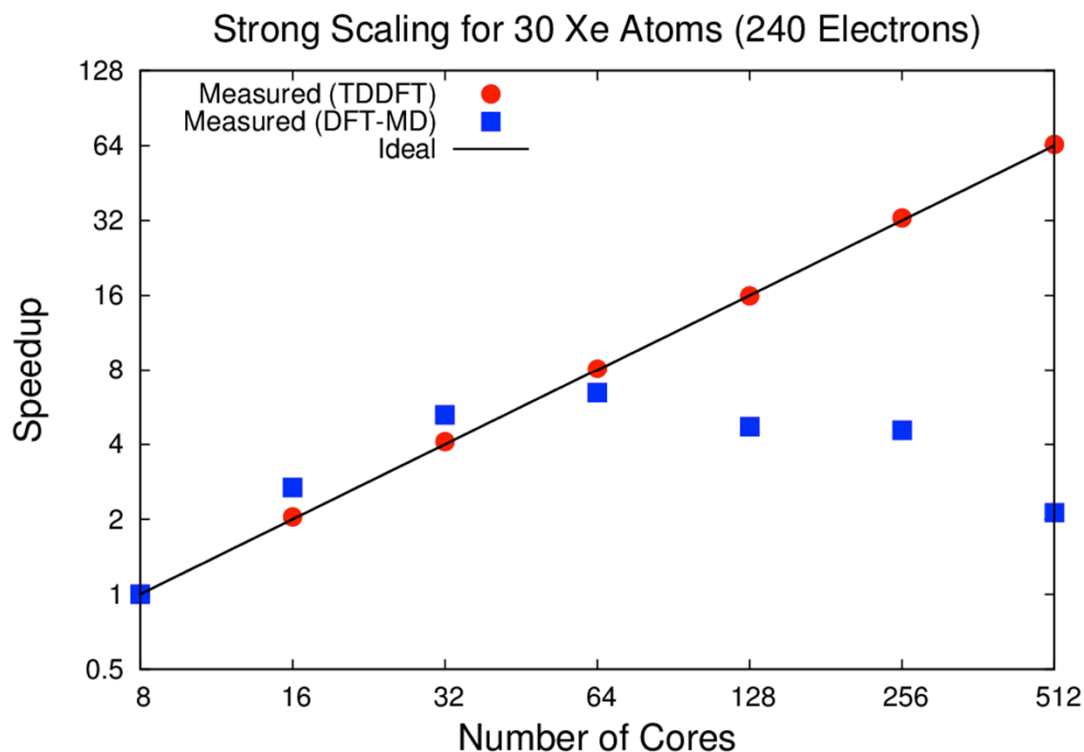
- Highly nonlinear equations
- Sources of trouble:
- Iterative solve at each step
- Hartree/XC $\leftarrow n(\mathbf{r}, t) \leftarrow |\psi_m(\mathbf{r}, t)|^2$
- Accumulation of floating-point error
- Validation: Does Mermin state stay in Mermin state?
- Crank-Nicolson proves robust :
Exact unitary propagation
- Orbitals orthogonal for 50k+ steps
- Hartree energy conserved $\pm 10\mu\text{eV}$!



$$\begin{aligned} & \left[S(t) + \frac{i\Delta}{2} H_{smooth} \left(t + \frac{\Delta}{2} \right) \right] \psi_{n,smooth} \left(t + \Delta \right) \\ &= \left[S(t) - \frac{i\Delta}{2} H_{smooth} \left(t + \frac{\Delta}{2} \right) \right] \psi_{n,smooth} (t) \end{aligned}$$

Parallel Scalability

- Ehrenfest TDDFT: 'more parallel' than DFT-MD.
- Primary cost/step is iterative linear solve
- No orthogonalization
- Hierarchical parallelism
- The catch: time step in attoseconds
- Of course, we also capture influence of electronic excited states. .



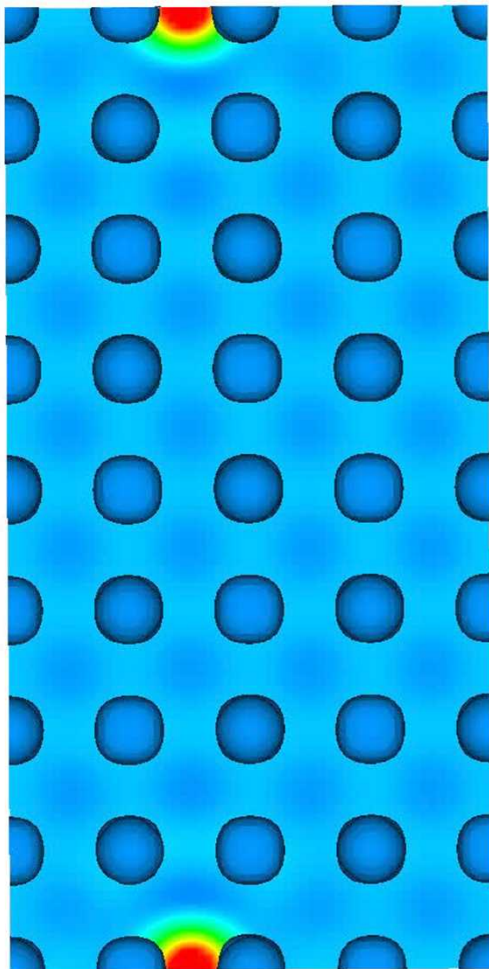
Coupled Electrons and Moving Nuclei

$$H[\{R_I\}]\phi = \varepsilon\phi \quad \text{vs.} \quad H[\{R_I\}]\phi = i\frac{d}{dt}\phi$$
$$F_I = -\left\langle \nabla_I V(\{R_I\}) \right\rangle$$

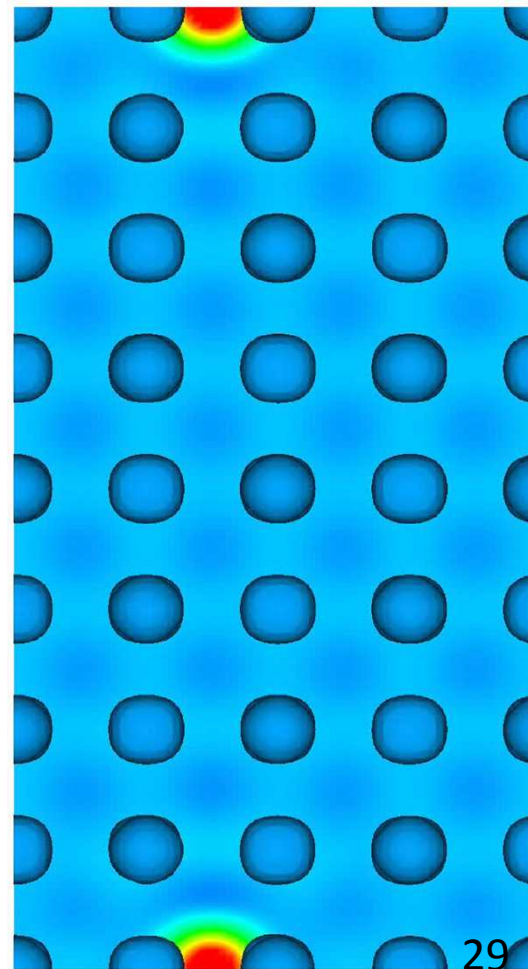
- **Separate model for coupled electron ion dynamics**
- No uncoupled electron dynamics Born-Oppenheimer
- Electron-dynamics in Ehrenfest
- Certain processes not described by even Ehrenfest such as photochemistry, discrete electron relaxation

Born-Oppenheimer vs. Ehrenfest

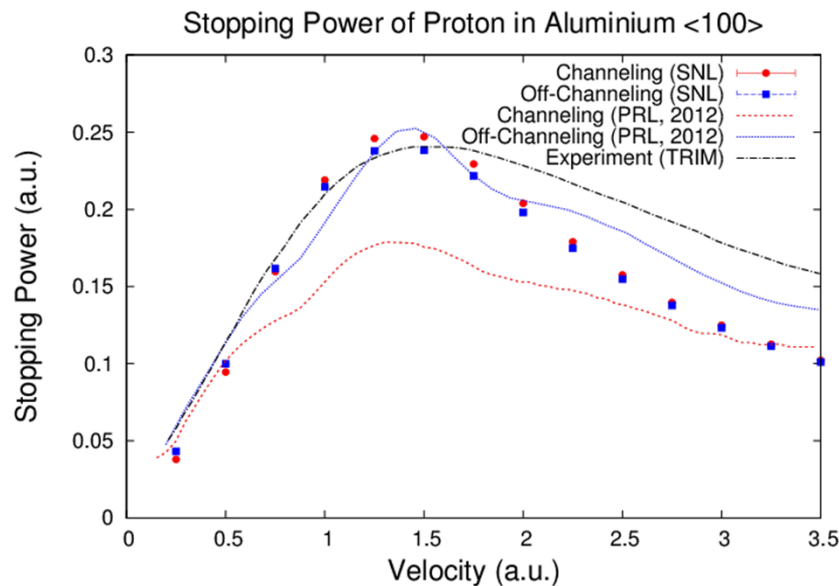
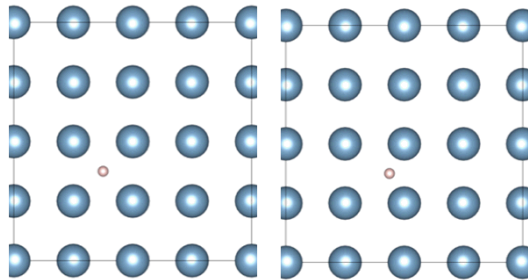
Born-Oppenheimer



Ehrenfest



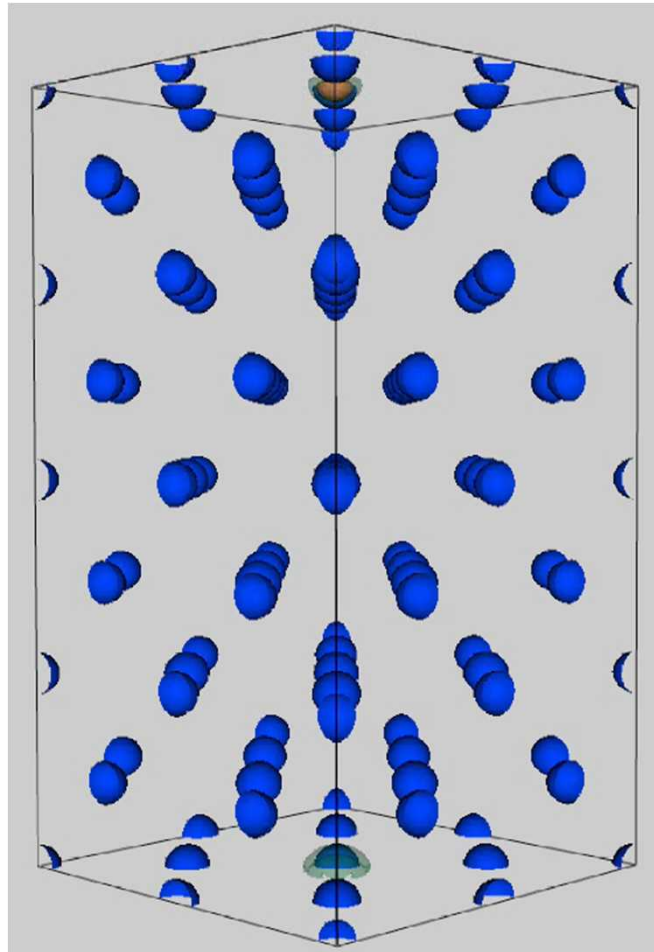
Stopping Power Calculations Extended to WDM



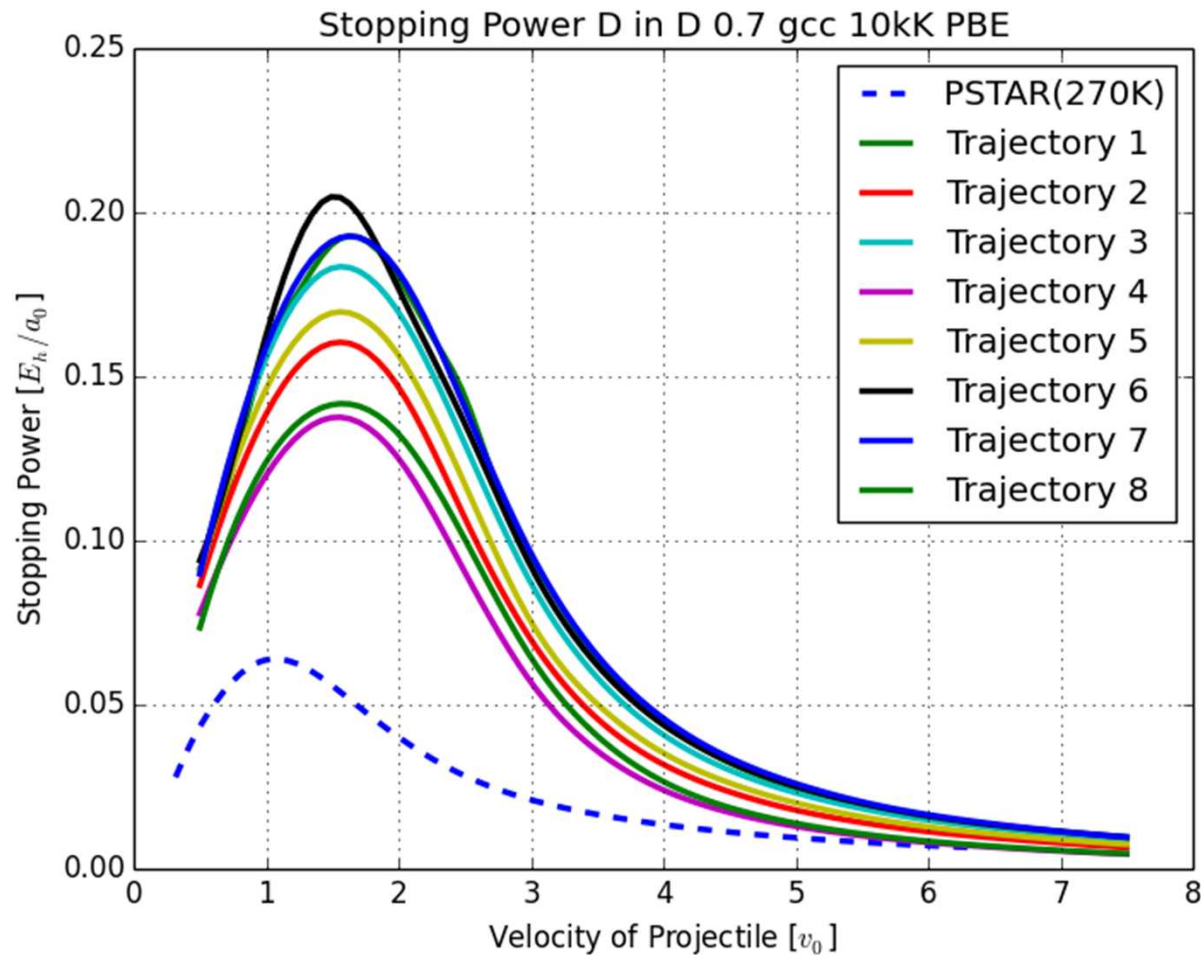
André Schleife, Yosuke Kanai, and Alfredo A. Correa

- Low energy $v < 0.1$ a.u.
ground-state or thermal
electrons / adiabatic
regime
- High energy $v \gg 0.1$ a.u.
electron dynamics
- Intermediate regime:
combined electron-
nuclear dynamics,
electron capture and
ionization

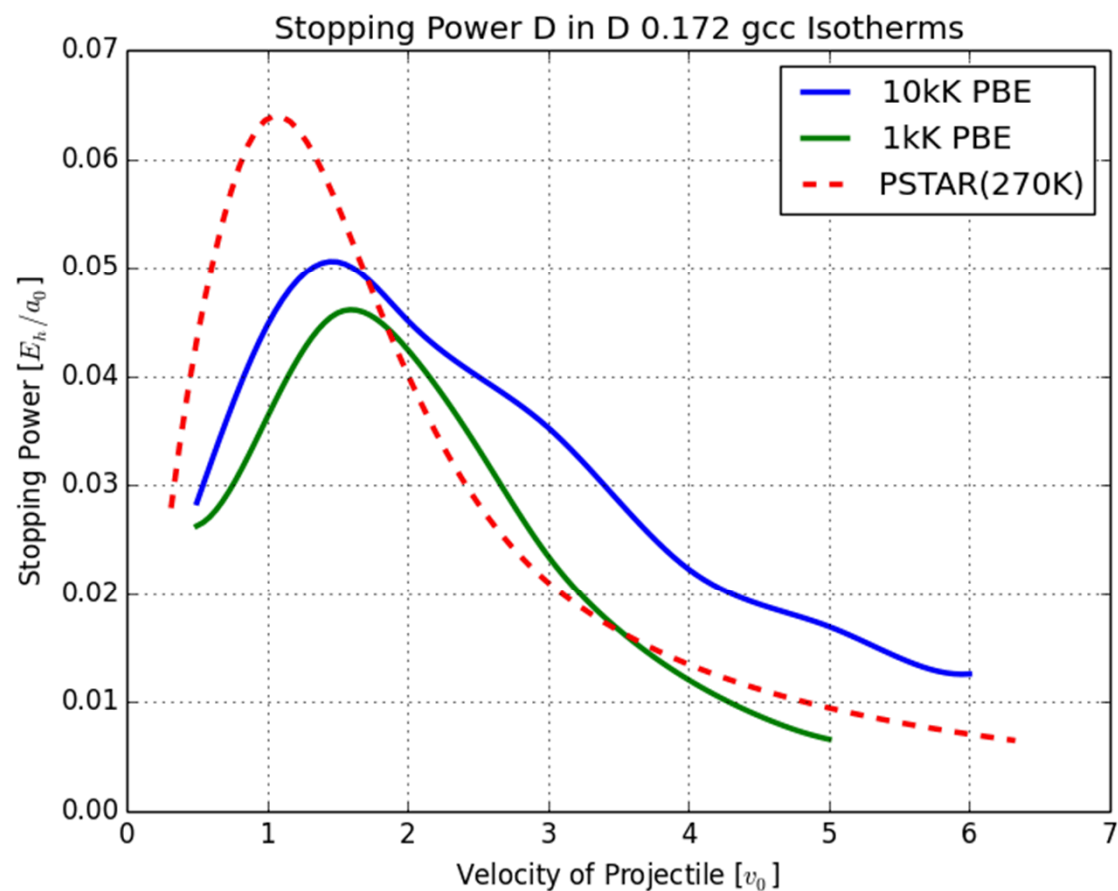
Plasmons are Formed in the Wake.



Stopping in Deuterium

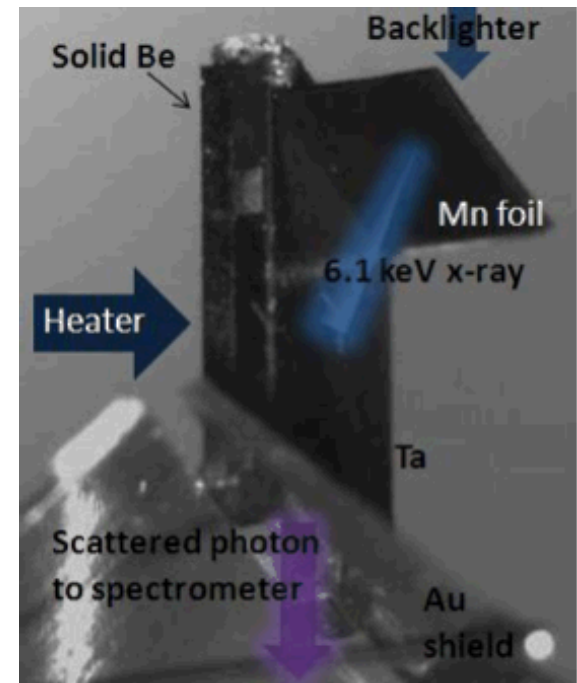


D in D at four-fold compressed

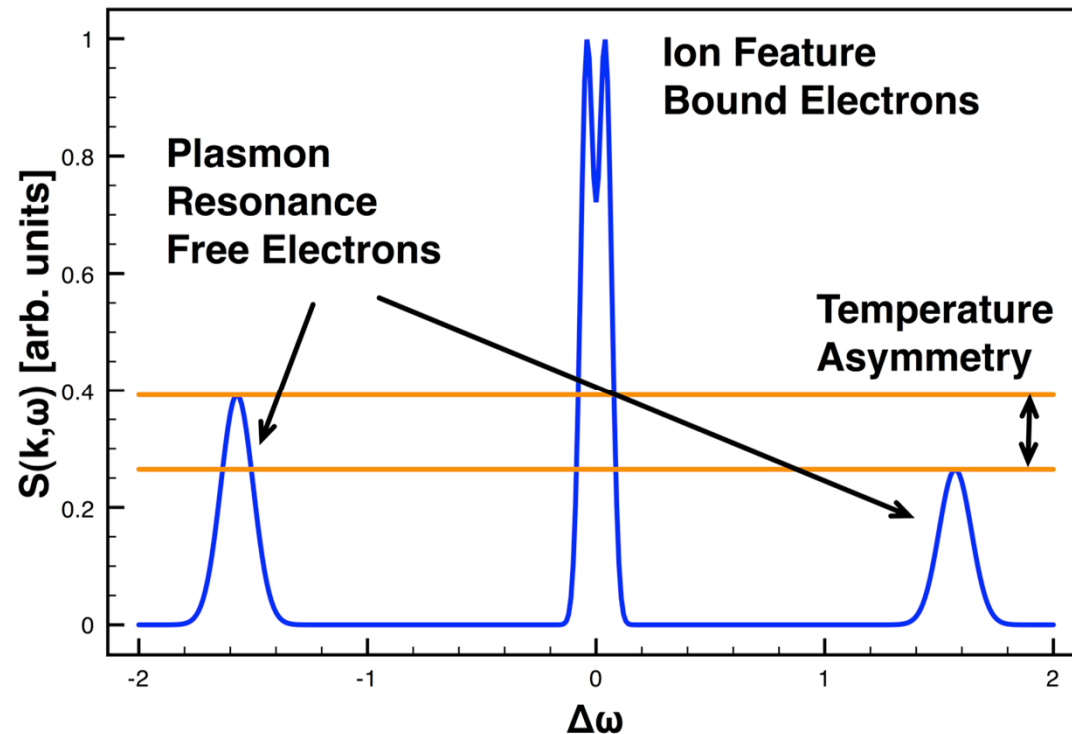


X-Ray Thomson Scattering, a New Diagnostic, in Warm Dense Matter

- Diagnosing Warm Dense Matter
- X-Ray Thomson scattering can test EOS by providing a measure of bulk **temperature**, density, and ionization state (not surface limited)
- Used (or soon to be used) at several facilities:
- Z-Machine, Omega, DESY , Tsinghua, and many more



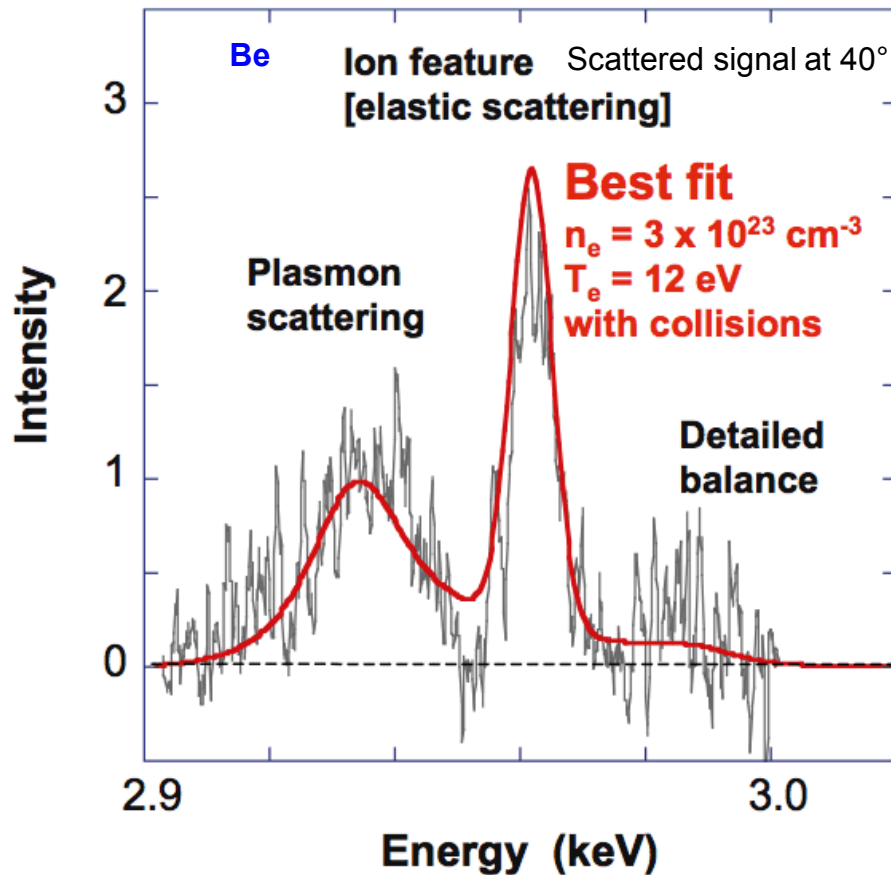
Temperature Diagnostic X-Ray Thompson Scattering



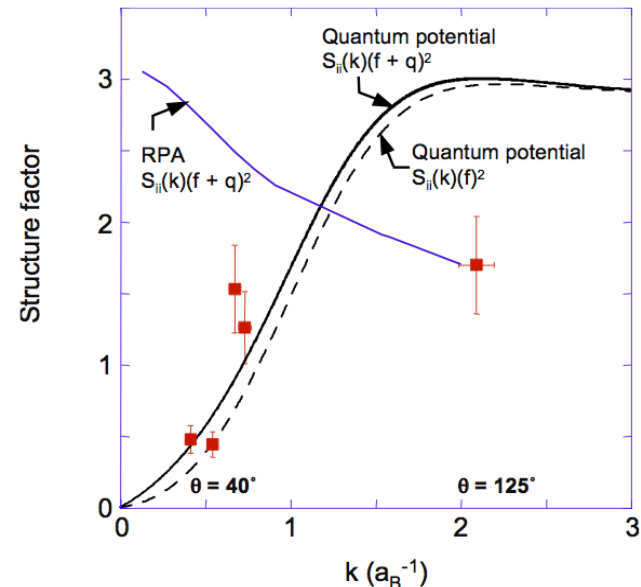
$$S^{tot}(k, -\omega) = \text{Exp}(-\hbar\omega / k_B T) S^{tot}(k, \omega)$$

- Based on fundamental principle of detailed balance
- Temperature diagnostic for warm dense matter
- Structural information about a material
- *Works* at low k based on models (Chihara) that use unphysical ion structure factors from classical plasma simulations with *effective quantum potentials*

X-Ray Thomson scattering has delivered temperature measurements and questions



Beryllium data from Glenzer, *et al.*, Phys. Rev. Lett. 98 (2007)



$$S(k, \omega) = (f(k) + q(k)) S_{ii}(k) \delta(\omega) + Z_C S_{ee}(k, \omega) + S_{cv}(k, \omega)$$

The Chihara models that “work” at low k use unphysical ion structure factors from classical plasma simulations w effective “quantum potentials”.

Core-valence separation; frequency domains of validity

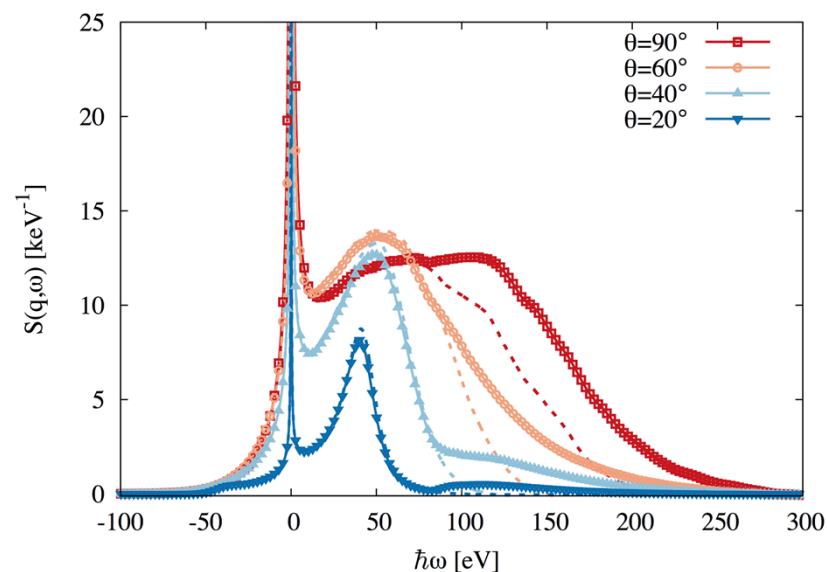
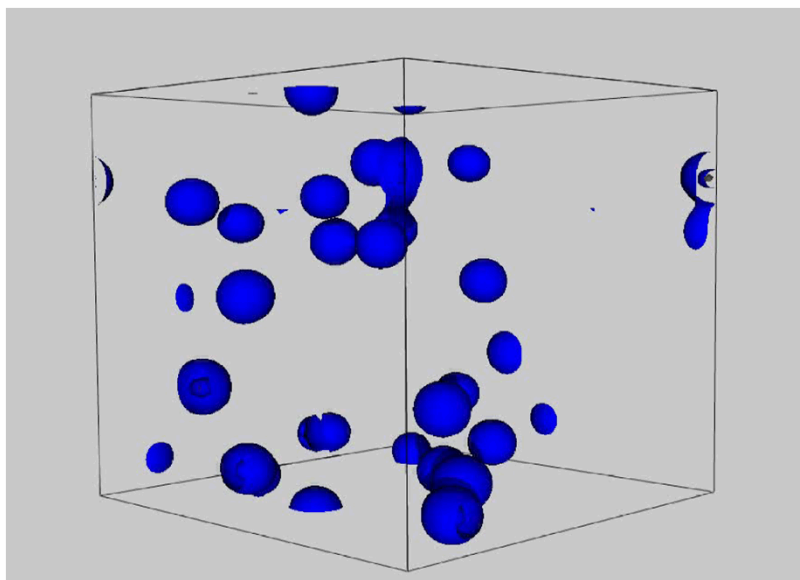
Most Direct Simulation through the Dynamic Structure Factor

- Time-domain quantum mechanics simulations allows a direct calculation of the structure factor $S(k, \omega)$ that
 - Includes quantum degeneracy
 - Correlations
 - Electrons and nuclei out of thermal equilibrium
 - Non Fermi-Dirac distributions
 - Collective excitations

$$\frac{d\sigma}{d\omega d\Omega} = \sigma_T S^{tot}(k, \omega) \quad S_{ee}^{tot}(k, \omega) = \frac{1}{N_{ion}} \left\langle \left| \rho_e^{tot}(\mathbf{k}, \omega) \right|^2 \right\rangle$$

Movie: X-Ray Thomson Scattering Calculation

$$\delta v_{pert.}(r, t) = v_0 e^{iq \cdot r} f(t) \quad \delta \rho(k, \omega) / v_0 f(\omega) = \chi(k, -k, \omega) \quad S(k, \omega) = -\frac{1}{\pi} \frac{\text{Im}[\chi(q, -q, \omega)]}{1 - e^{-\omega/kT}}$$

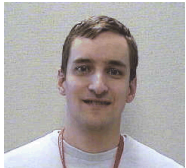


Compressed and heated Be
mass density 5.5 g/cm³ and $T_e = 13\text{eV}$

The LDRD Team



BACZEWSKI, ANDREW



SHULENBURGER, LUKE

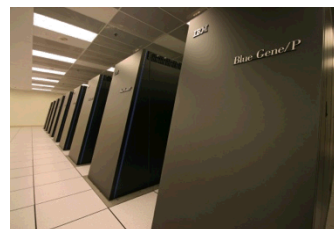


DESJARLAIS, MICHAEL P.

- The Z team
- Thomas Mattsson
- Stephanie Hansen
- Dawn Flicker
- Seth Root
- Kyle Cochrane
- Programmatic leadership
- The Cryogenic Team – D. L. Hanson
- Sandia High-Performing Computing (HPC) – S. Corwell
- Supported by the Laboratory Directed Research and Development program at Sandia National Laboratories, a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

Summary and Future Work

- DFT based MD simulations to model shock compression of mixtures under WDM conditions
- Experimental validation through shots on the Z-machine
- New tools for TDDFT of WDM:
 - Ehrenfest-TDDFT for coupled electron-ion motion in bulk systems
 - Stable, accurate, and scalable PAW implementation
 - XRTS/DSF is primary goal
- Immediately: dielectric function of interesting WDM systems (SEQUOIA).
- Near term: direct calculation of dynamic structure factor.
- Challenge: Identify surface hopping model that gets non-adiabatic electron-ion energy transfer 'right'.



Direct Simulation Monte Carlo

What is DSMC?

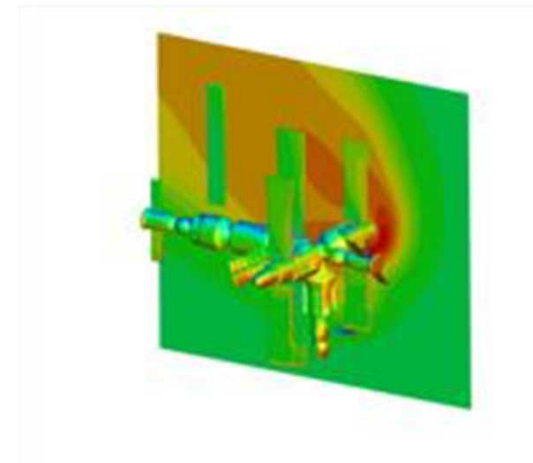
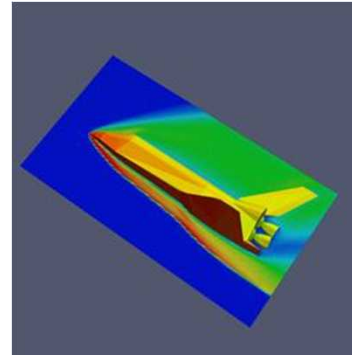
- Probabilistic (Monte Carlo) scattering for finite Knudsen number fluid flows (Prof. Graeme Bird)

Why do we need DSMC?

- **E**stimation of the Space Shuttle re-entry aerodynamics to the modeling of micro-electro-mechanical systems (MEMS)

At Sandia, SPARTA code

<http://sparta.sandia.gov>

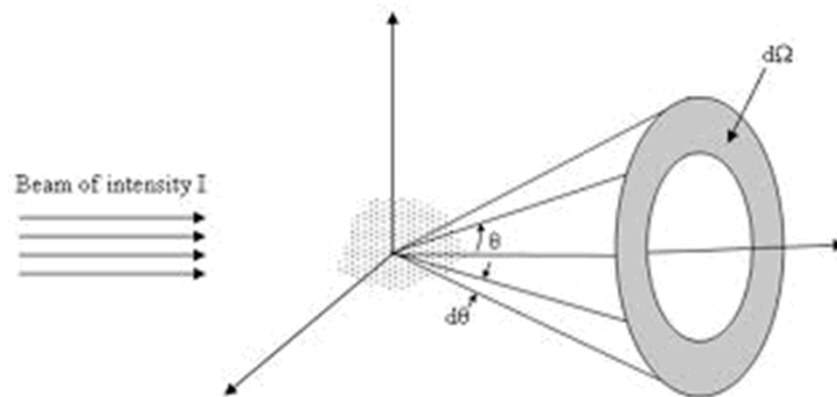


Parameters Needed for DSMC

$$\lambda = \frac{1}{\sqrt{2}n\sigma} \quad \eta = \left(\frac{4mk_B T}{9\pi\sigma^2} \right)^{1/2}$$

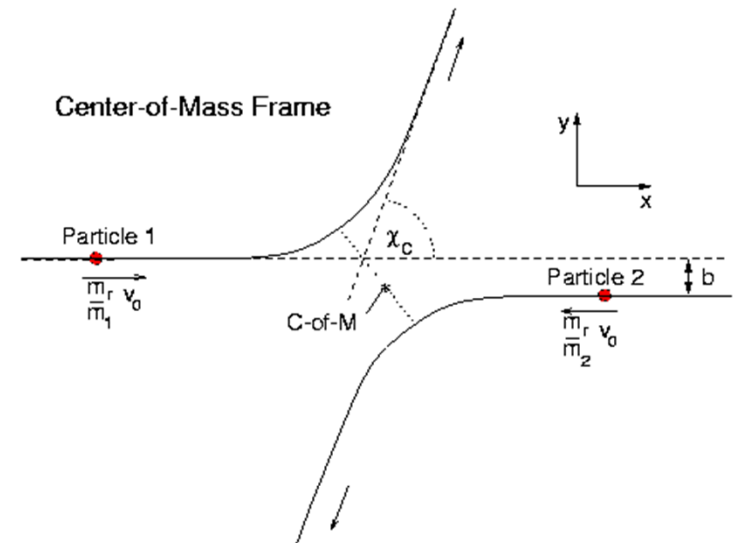
- The mean-free path is related to the cross-section.
- Viscosity can be calculated and compared to experiment with input of the cross section.
- Cross-section varies with material and temperature.
- The viscosity depends on the material and temperature, not on the density.

Cross-Sections Related to Scattering Angles

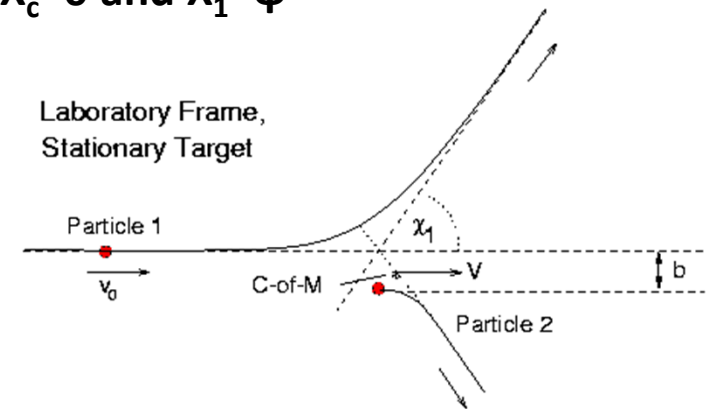


We need to model:

- Scatter and scattered particles
- Impact parameters
- Measures of charge transfer
- Statistics
- Exchange-correlation, external fields and changing potential landscapes

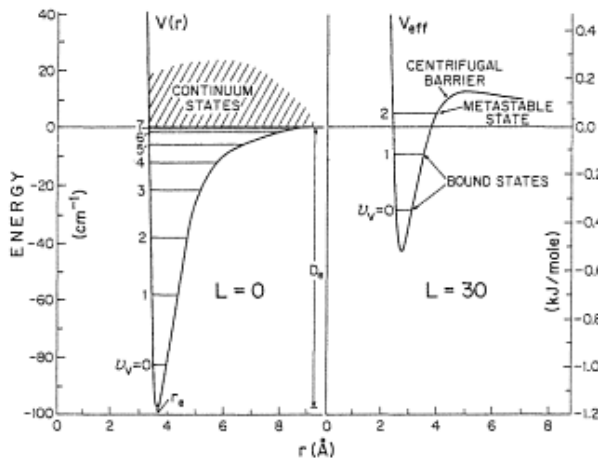


$$\chi_c = \theta \text{ and } \chi_1 = \psi$$



Important Scales

Ar-Ar bond length 3.7 Å

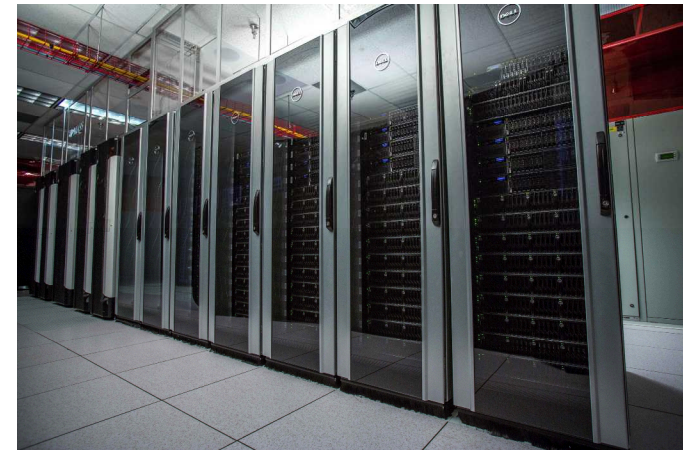


$$v = \sqrt{2k_B T / m}$$

- V is determined by thermal velocities at $T=2,000\text{K}$
- Mean thermal velocity at 300K, 394 m/sec
- Approximately 0.01 Å/fs
- X displacement > Ar-Ar van der Waals Bond length
- Impact b recursive halving of initial x displacement

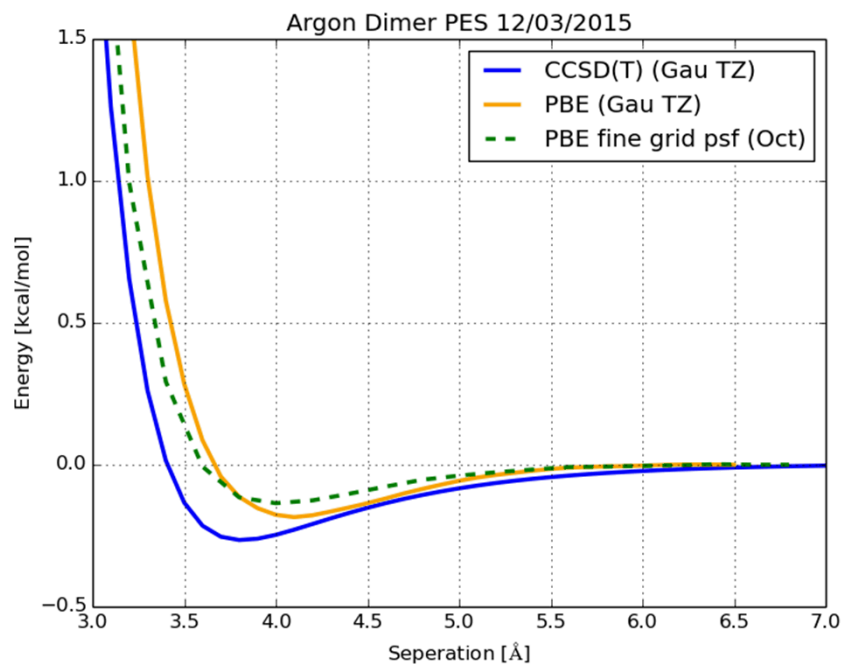
Basic Set-Up of Calculation

- Octopus 4.1.2
(<http://www.tddft.org/programs/octopus>) on 8 cores on UNO
- Time step conserves energy of stationary state
- Time-dependent propagation
Approximated Enforced Time-Reversal Symmetry
- Total time greater than bounce time
- Ehrenfest coupling
- PBE GGA for XC – No van der Waals
- Ar Pseudo potential
- Spin-polarized



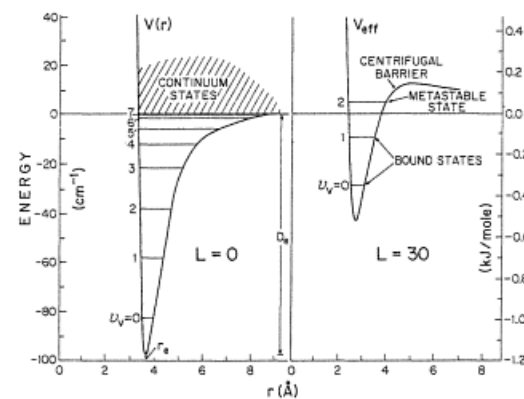
Uno Dell	SNL-NM	201	3344	2.7 GHz Intel Sandy		
Bridge:2S:8C/4S:8C	RHEL 6	GigE	64 / 128	71 TF	29,293,440	

Distance of Initial Separation



DISSOCIATION OF VAN DER WAALS MOLECULES

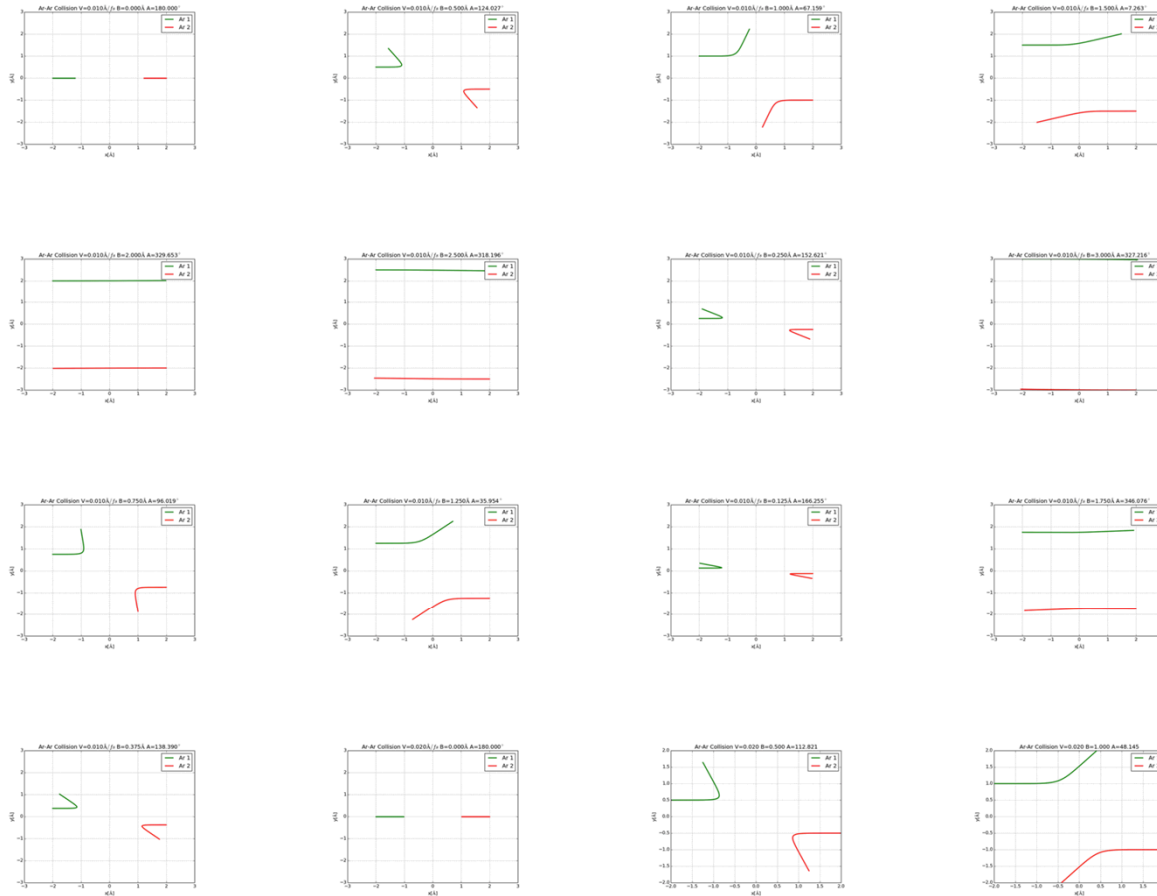
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1. The interatomic potential energy curve and energy states
2. This figure is adapted from reference 2.

Ar-Ar bond length 3.7 Å

Typical X-Y Scattering Trajectories, θ (b,v)



Scattering Theory

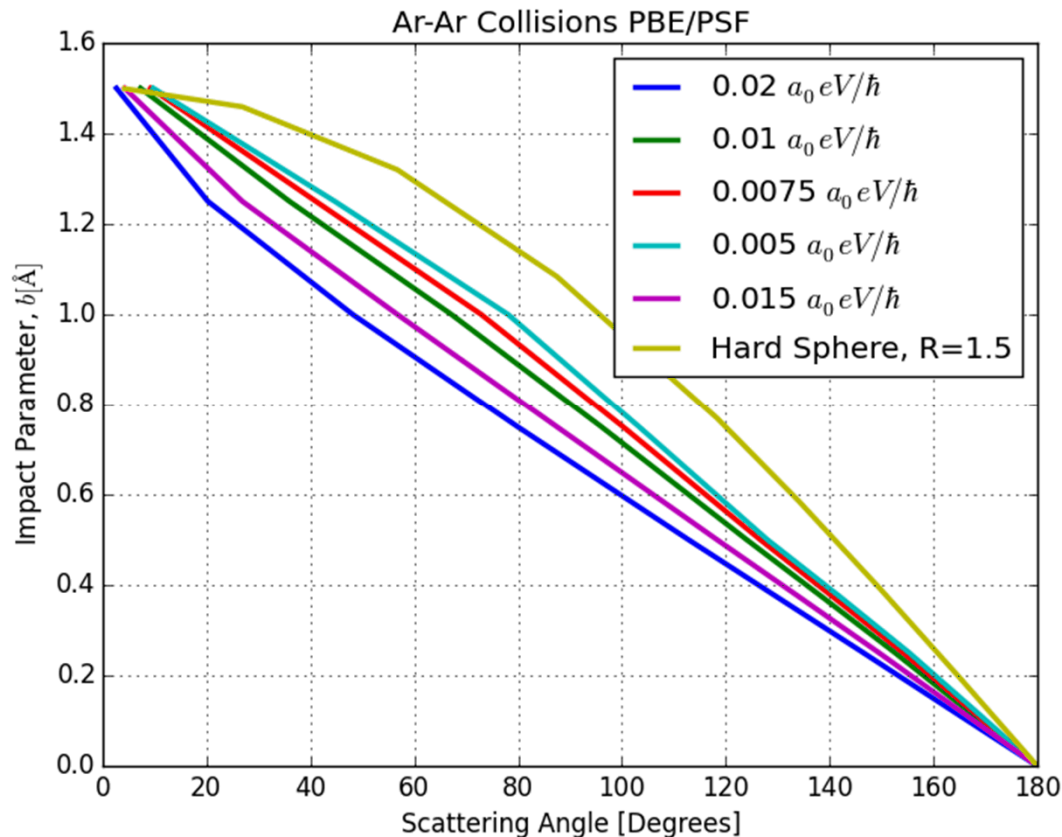
$$\frac{d\sigma}{d\Omega} = \frac{b}{\sin\theta} \left| \frac{db}{d\theta} \right| \quad \sigma = 2\pi \int_0^{180} d\theta \frac{b}{\sin\theta} \left| \frac{db}{d\theta} \right|$$

$$\lambda = \frac{1}{\sqrt{2}n\sigma}$$

Relates trajectories that we can calculate to the mean-free path used in simulations.

Thermal average of cross-sections

Table of Scattering Angles, $b(\theta, v)$



$$b(\theta) = R_{\text{Hard Sphere}} \cos\left(\frac{\theta}{2}\right)$$

Quite linear in calculated region

Must curve to $+\infty$ as angle goes to 0

$b(\theta)/\sin \theta$ requires careful consideration as $\theta \rightarrow 0$.

Note 1 $a_0 eV / \hbar = 0.804 \text{ \AA/fs}$

I have run larger impact parameters but I am still testing the reliability of these runs.

Summary

TDDFT for DSMC

- TDDFT describes coupled electron-ion dynamics of scattering events without materials specific parameters.
- The approach is general and can be applied to charged species, other elements, and molecules.
- Technical challenges related to simulation cell size and computer power can be overcome at present.
- Accuracy is therefore limited by the choice of functional and pseudo-potential used. Future work will investigate their roles.
- Scattering angle versus impact parameter and velocity are extracted for time-dependent runs.
- Cross sections can be obtained in postprocessing.
- We have developed a general set of tools (python scripts) to create, to manage, to run, and to post process these simulations.

