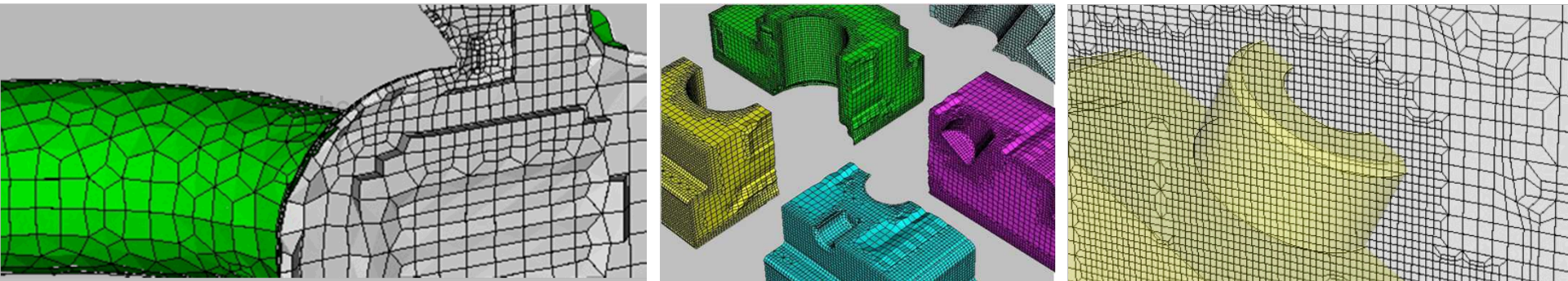


Exceptional service in the national interest



A Template-Based Approach for Parallel Hexahedral Two-Refinement

Steven J. Owen, Ryan M. Shih

24th International Meshing Roundtable

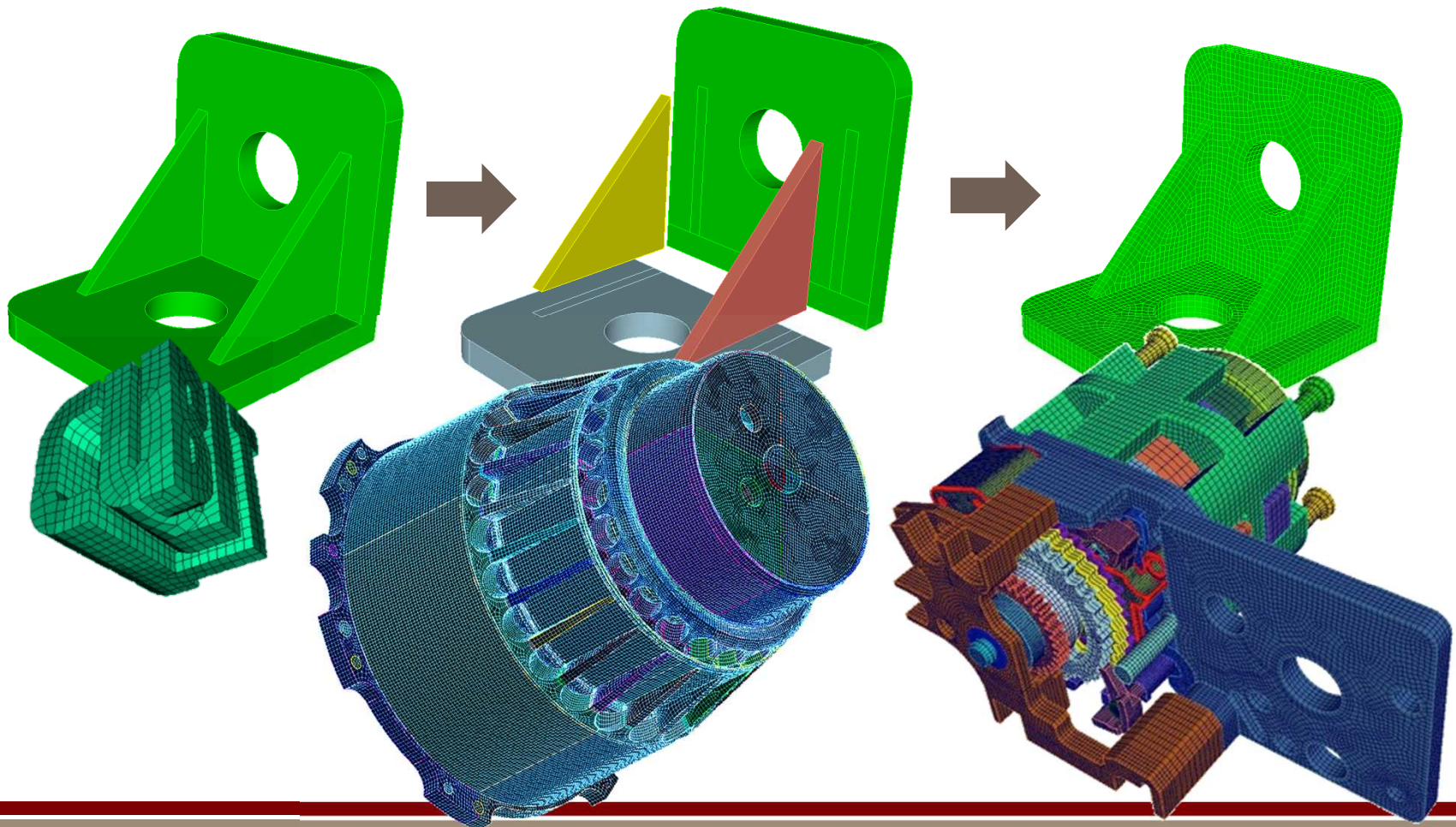
October 12-14, 2015

Austin, Texas

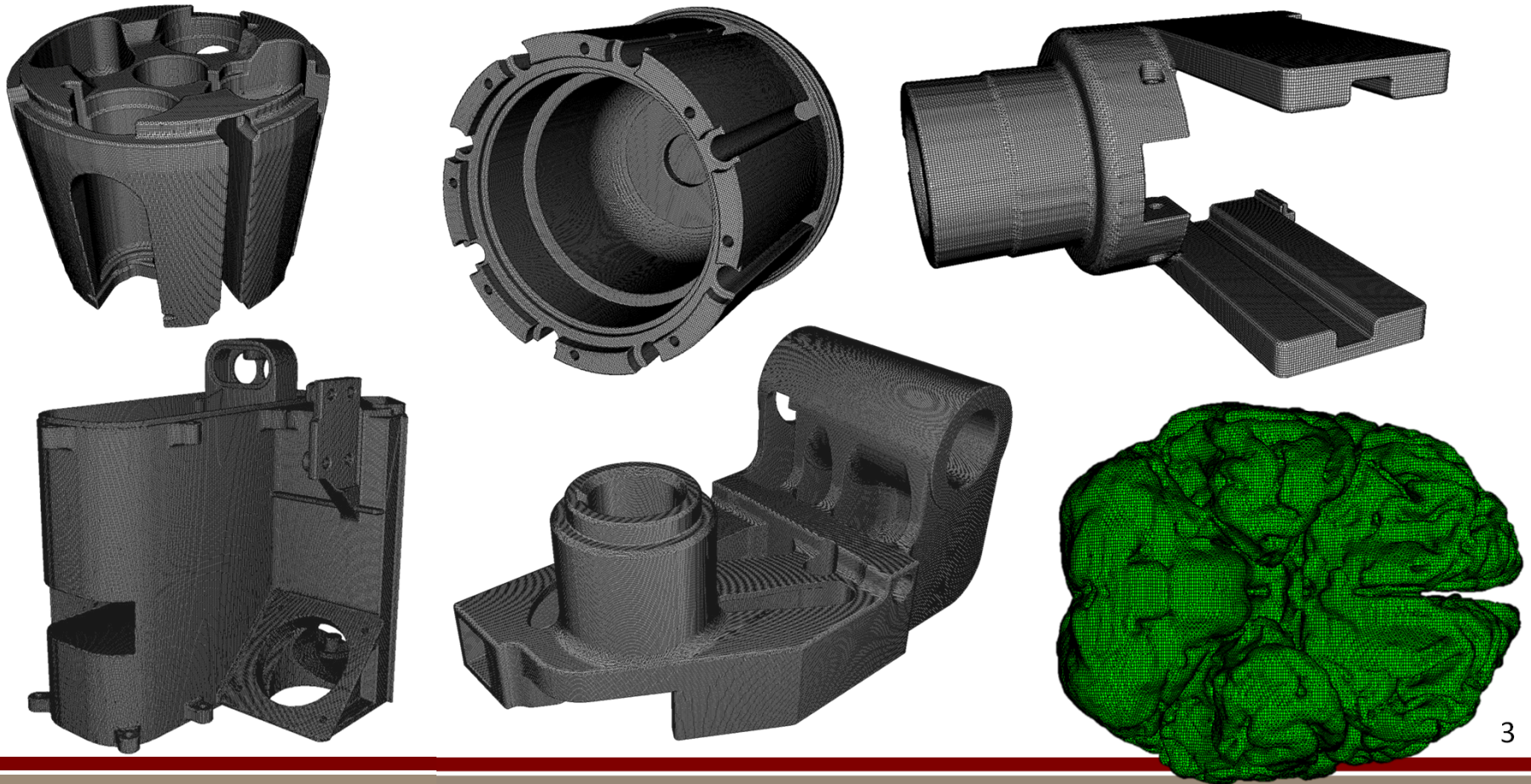


Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000. SAND NO. 2011-XXXXP

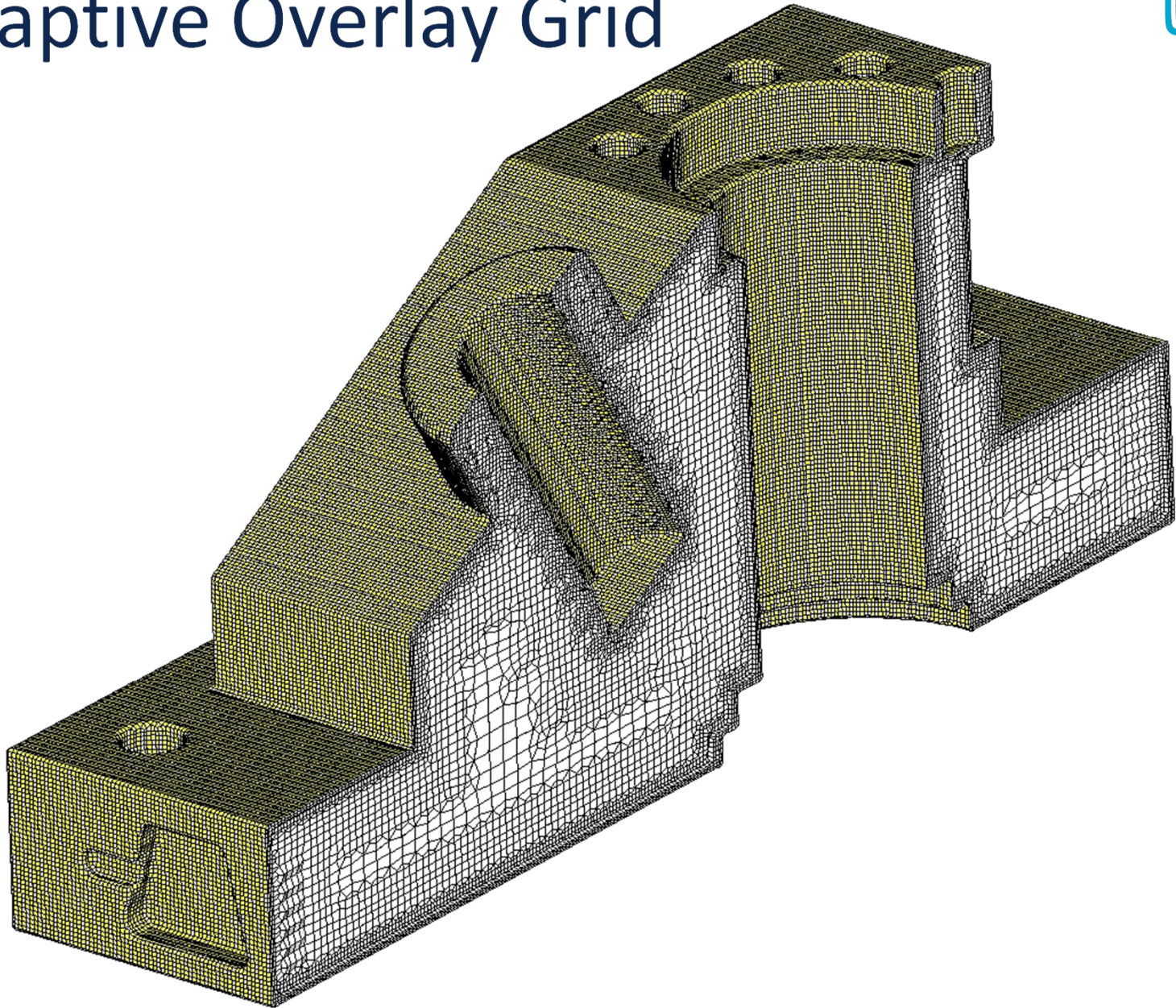
Hex Meshing



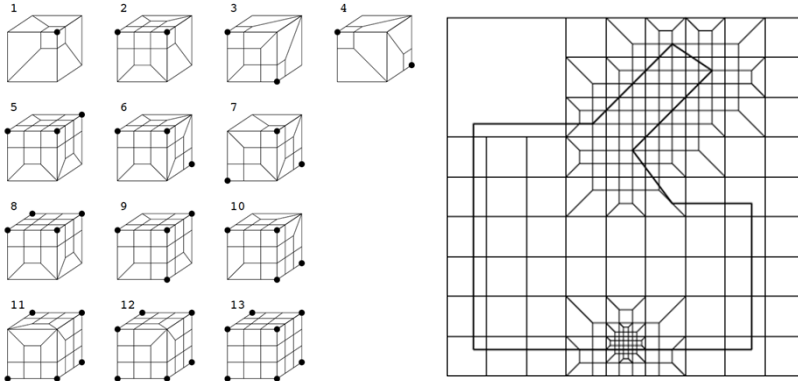
Hex Meshing for Next Generation Platforms



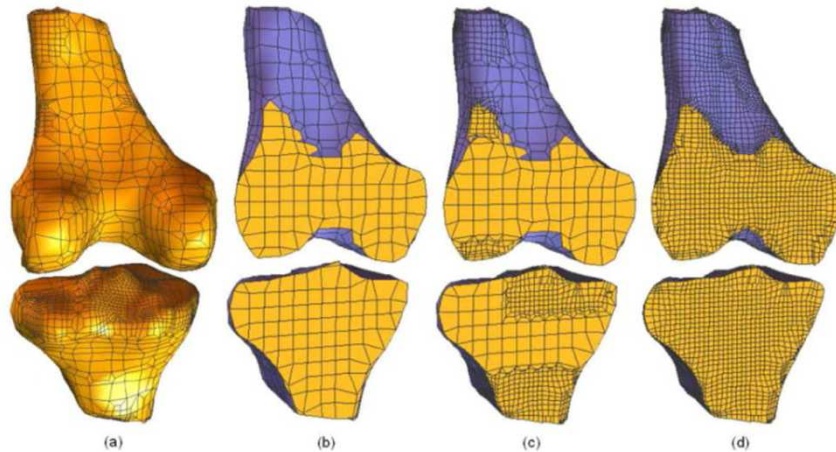
Adaptive Overlay Grid



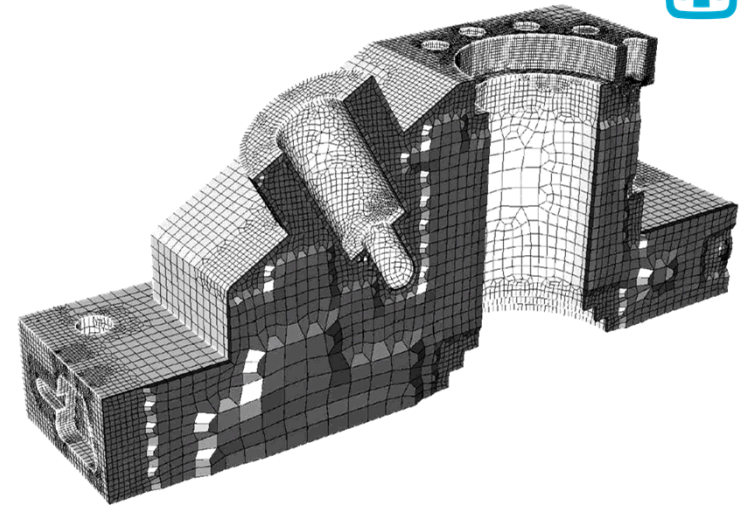
Background



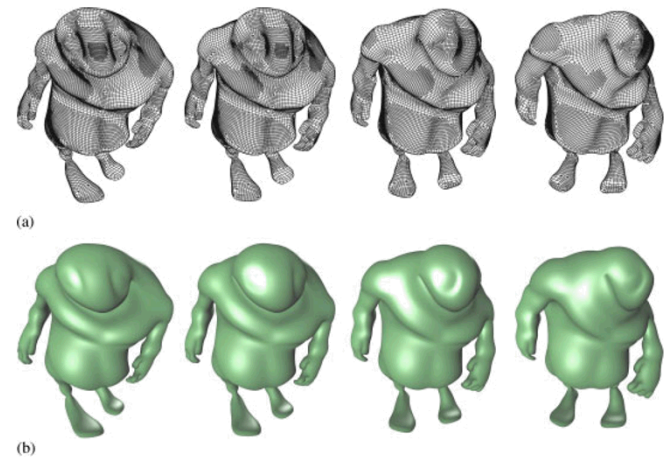
Robert Schneiders, Algorithms for quadrilateral and hexahedral mesh generation. In: Proceedings of the VKI lecture series on computational fluid dynamics (2000)



Yongjie Zhang and Chandrajit Bajaj, Adaptive and Quality Quadrilateral/Hexahedral Meshing from Volumetric Data Comput Methods Appl Mech Eng. 2006 Feb 1; 195(9): 942–960

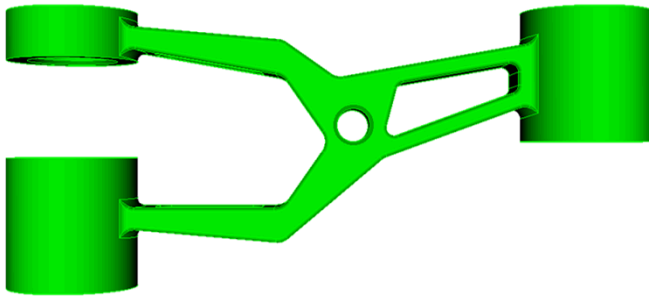


Loic Marechal, Advances in Octree-Based All-Hexahedral Mesh Generation: Handling Sharp Features, Proceedings of the 18th International Meshing Roundtable pp. 65-84

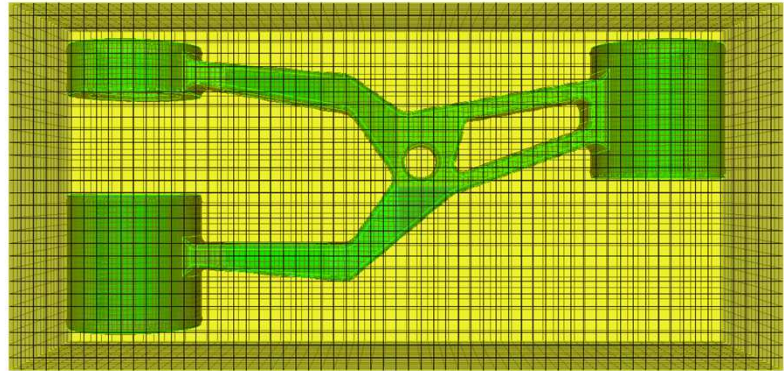


Mohamed S. Ebeida, Anjul Patney, John D. Owens and Eric Mestreau, Isotropic conforming refinement of quadrilateral and hexahedral meshes using two-refinement templates, Int. J. Numer. Meth. Engng 2011; 88:974–985

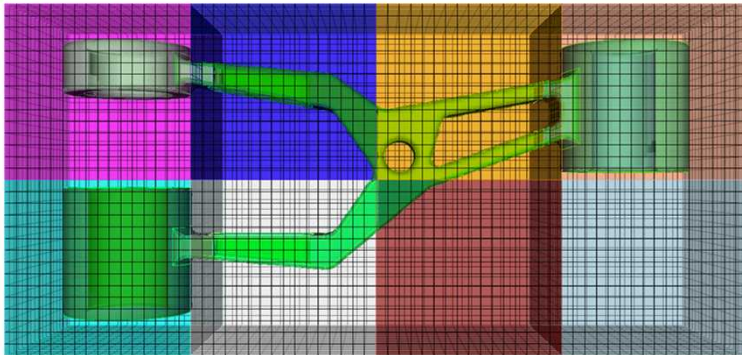
Sculpt



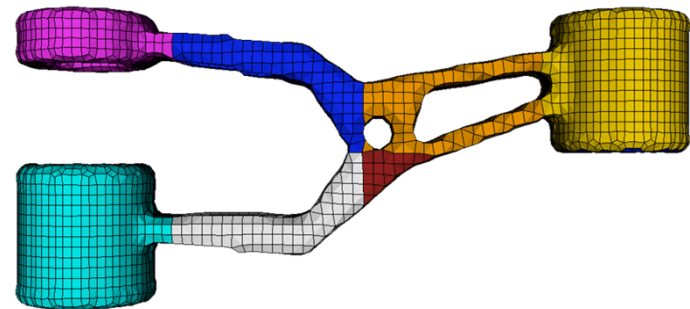
CAD geometry



Global overlay Cartesian grid



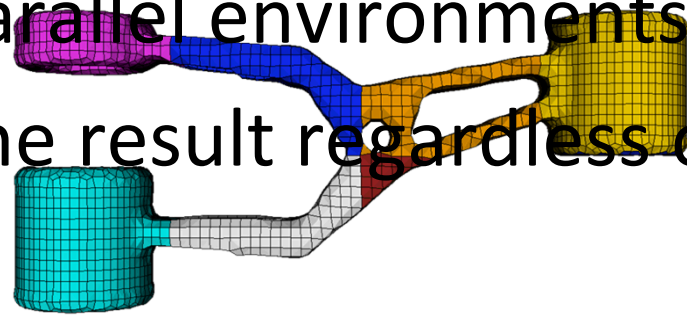
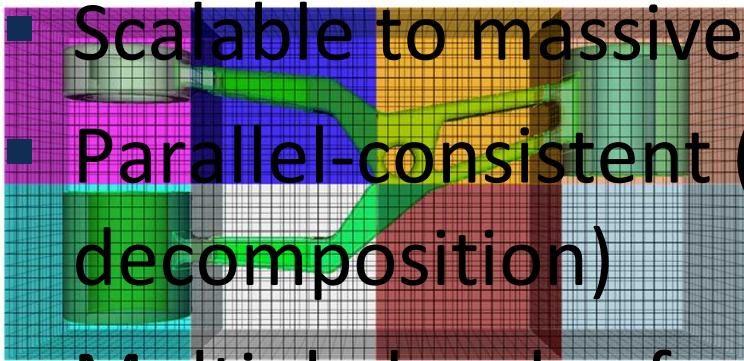
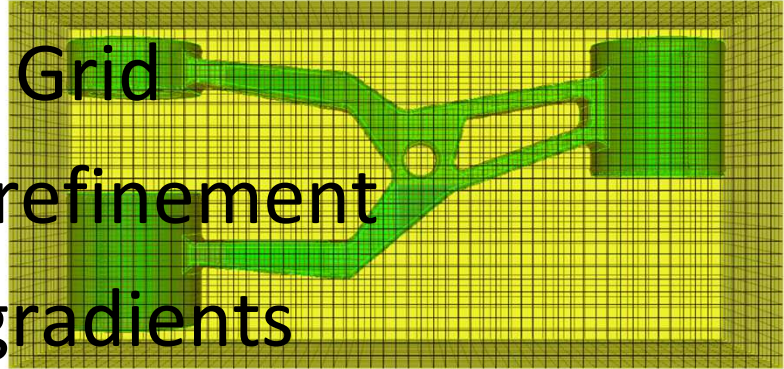
Cartesian grid decomposed and
distributed amongst many
processors



Each processor independently
meshes its portion of Cartesian grid

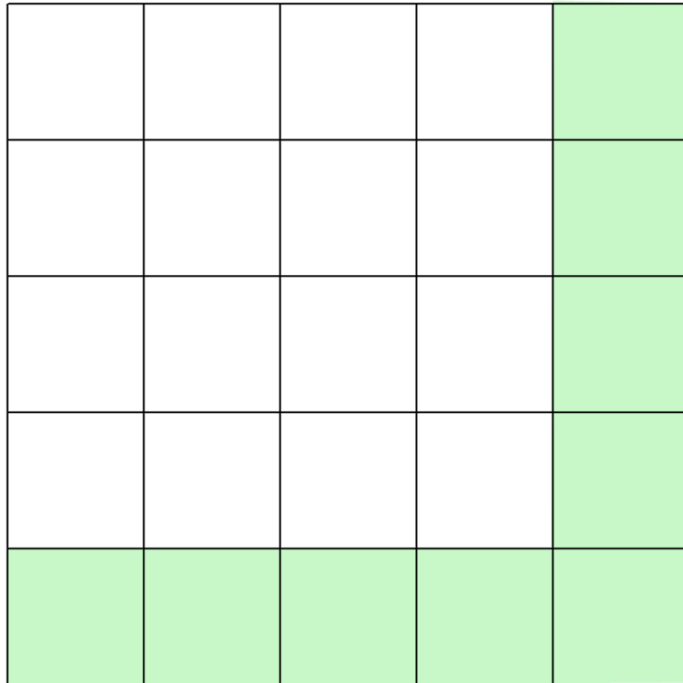
Refinement Requirements

- Structured (Cartesian) Grid
- One-to-eight uniform refinement
- Controlled mesh size gradients
- Computable Quality
- Scalable to massively parallel environments
- Parallel-consistent (Same result regardless of decomposition)
- Multiple levels of refinement

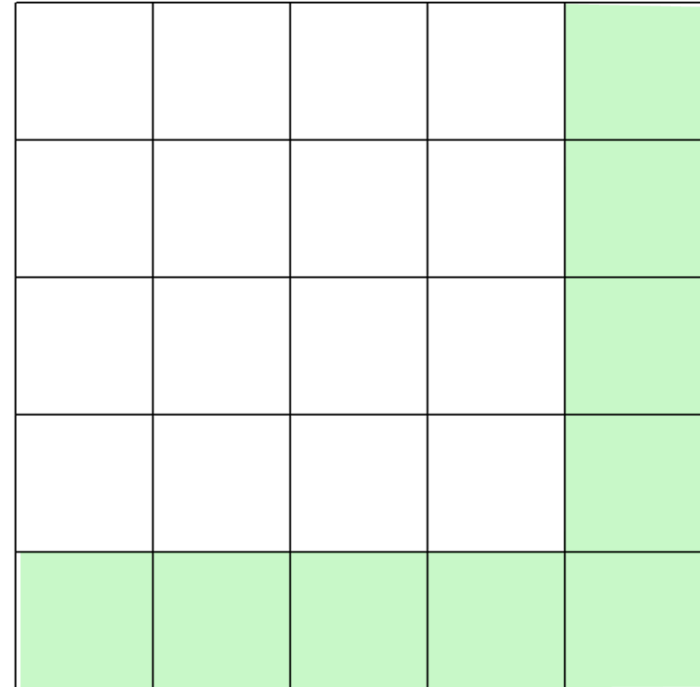


Hex Refinement

3-Refinement

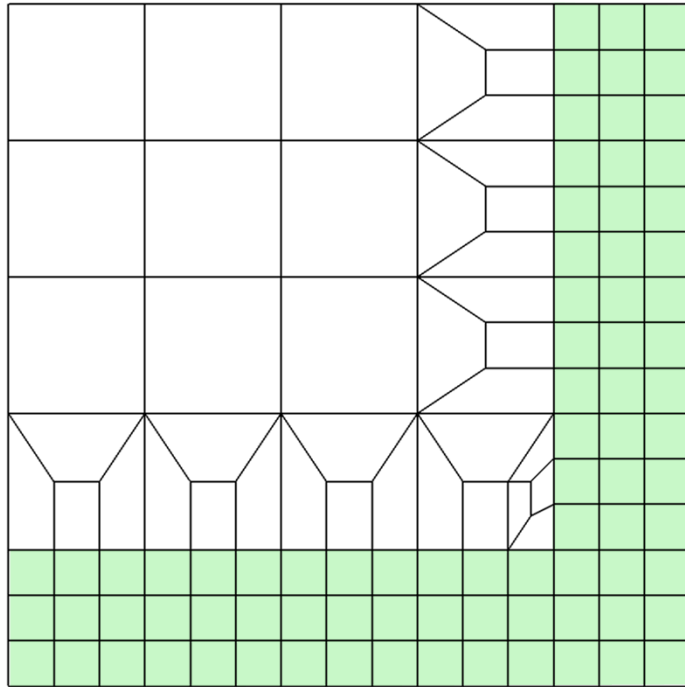


2-Refinement

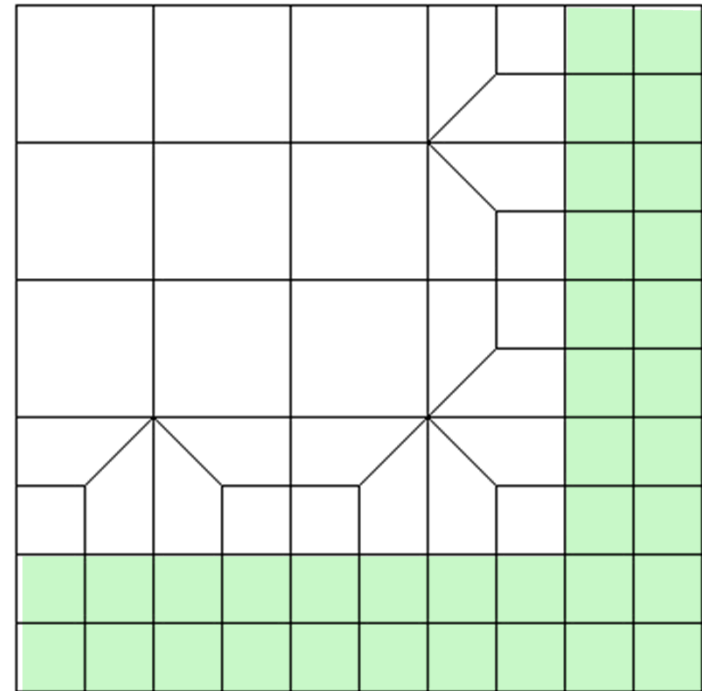


Hex Refinement

3-Refinement

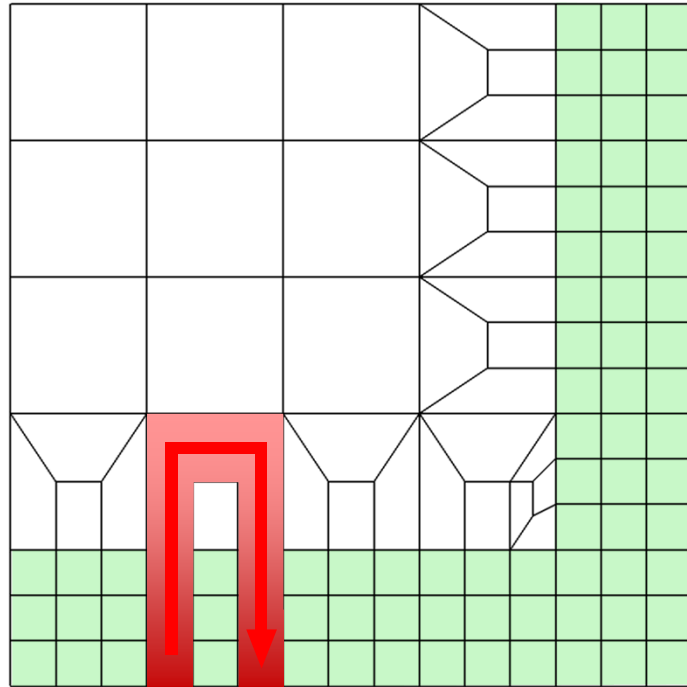


2-Refinement



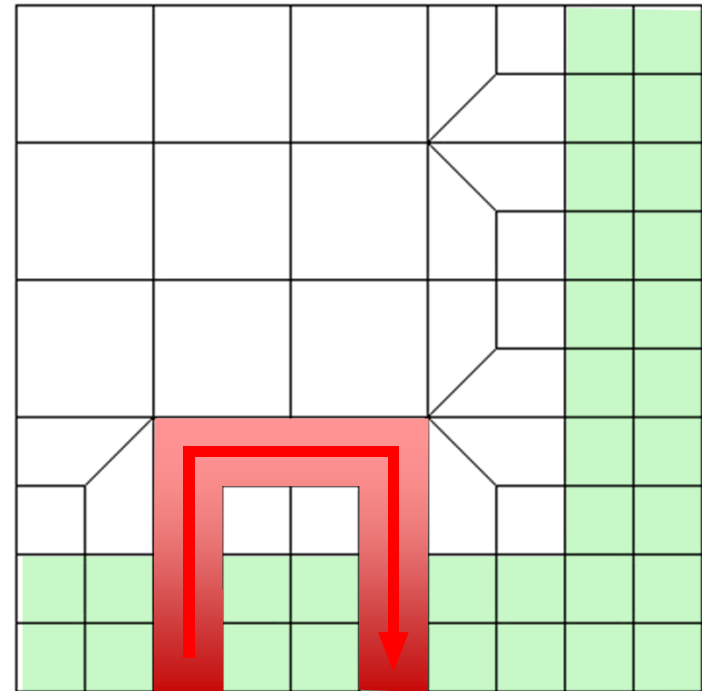
Hex Refinement

3-Refinement



single element
layer

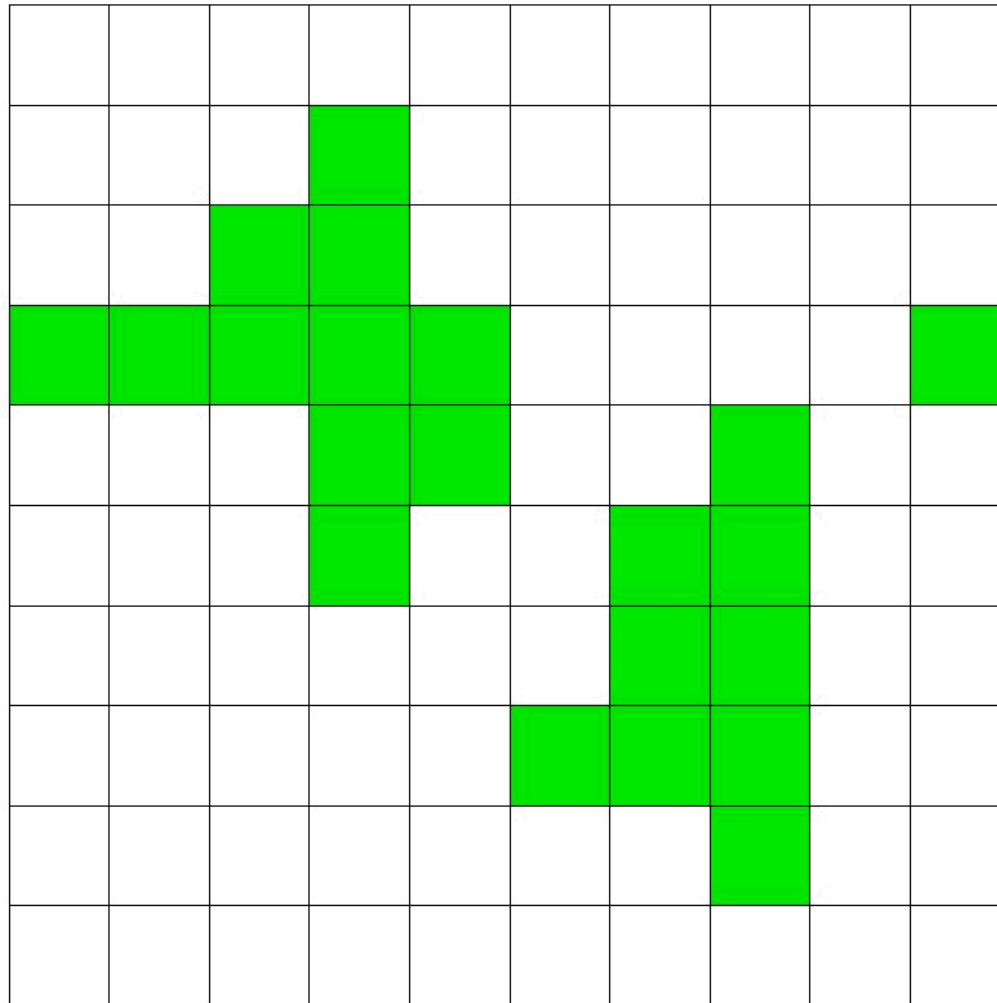
2-Refinement



element
layer pair

2-Refinement Procedure

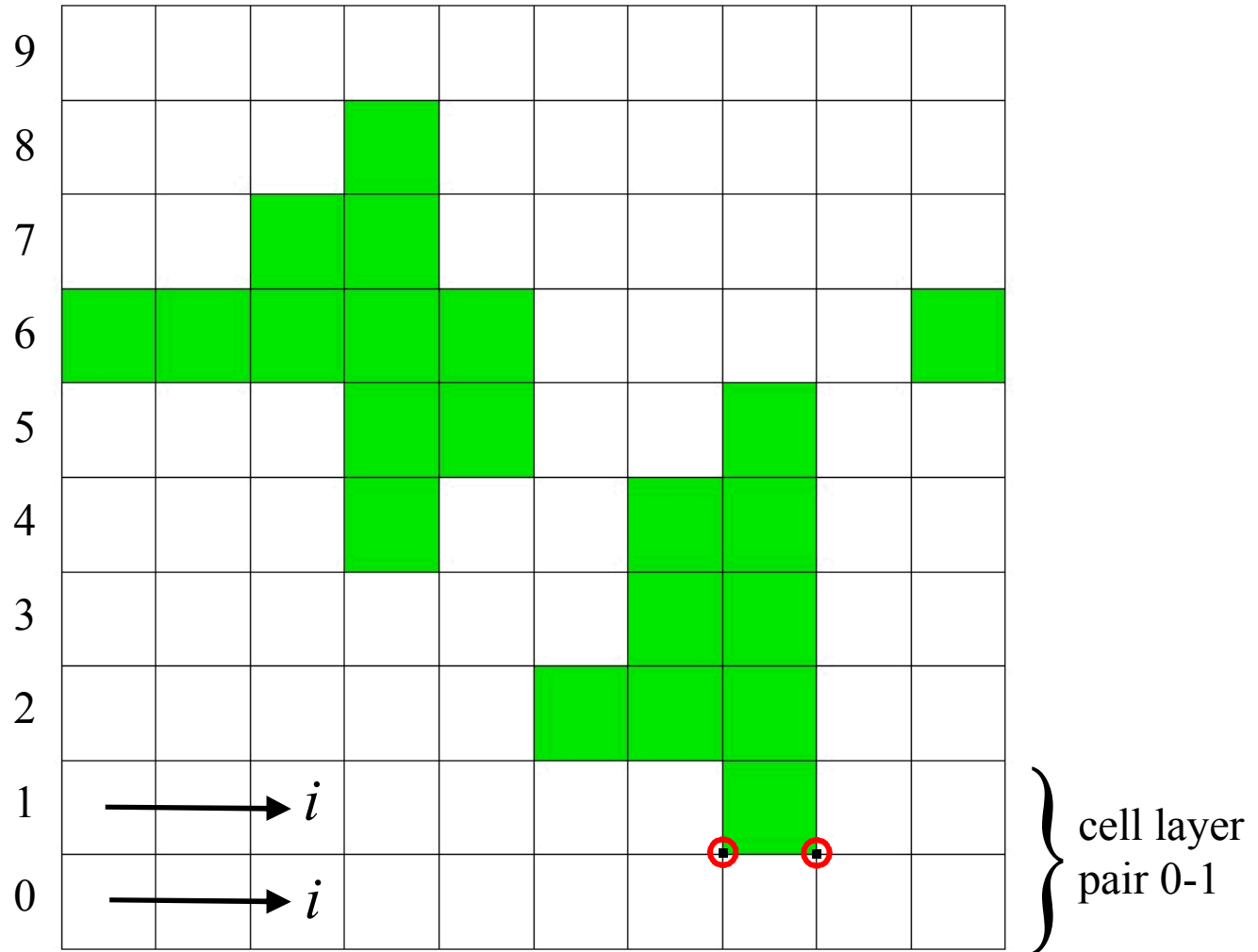
2D Example



A 10x10 grid representing a cell layer pair 0-1. The grid has rows indexed 0 to 9 and columns indexed 0 to 9. Green cells are located at (0,7), (1,7), (2,6), (2,7), (2,8), (3,0), (3,1), (3,2), (3,3), (3,4), (3,9), (4,3), (4,4), (5,7), (6,7), (6,8), (7,7), (7,8), (8,3), and (8,4). The grid is labeled with row indices 0-9 on the left and column indices 0-9 on the bottom. A bracket on the right indicates the grid represents 'cell layer pair 0-1'.

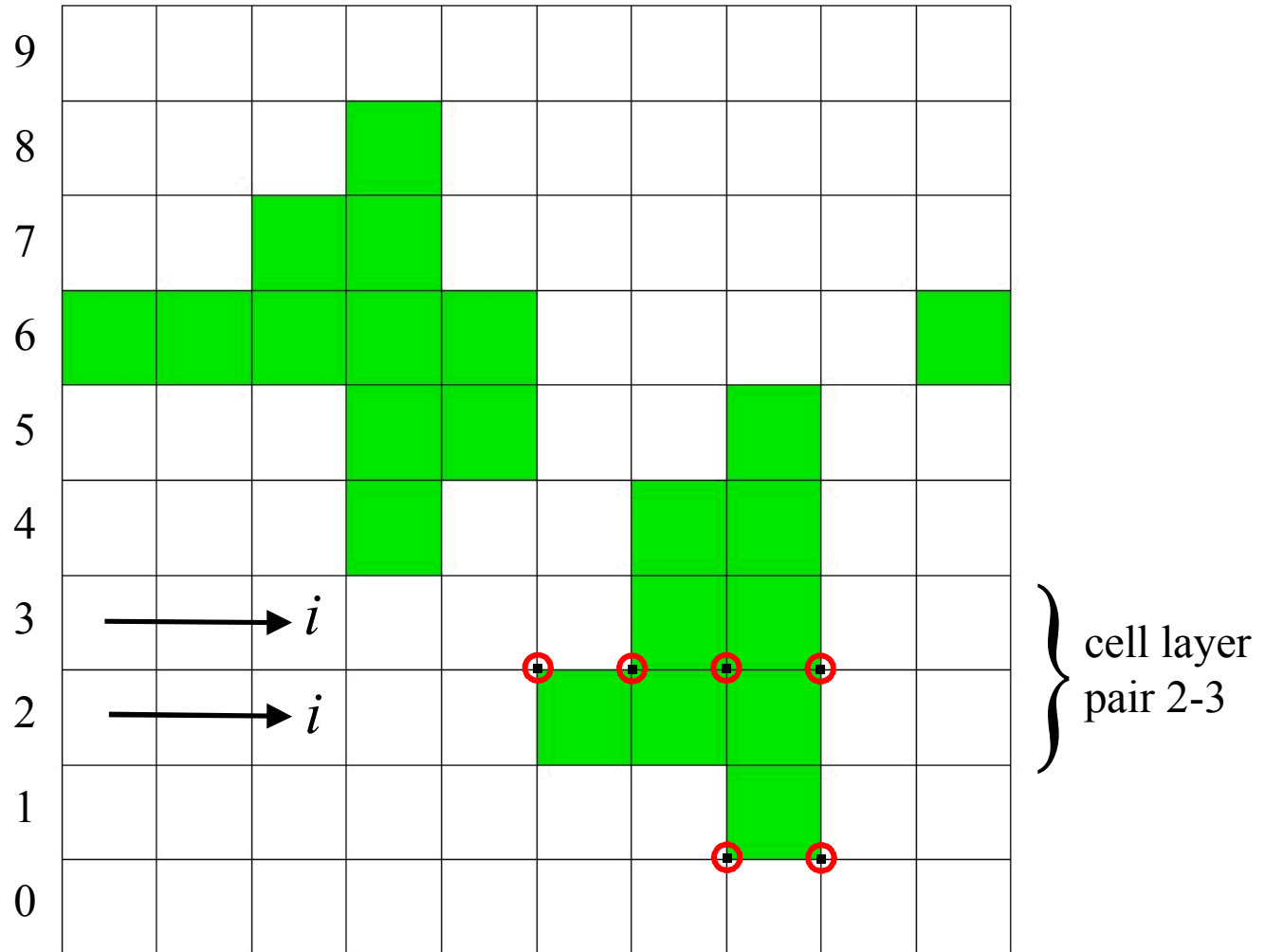
2-Refinement Procedure

2D Example



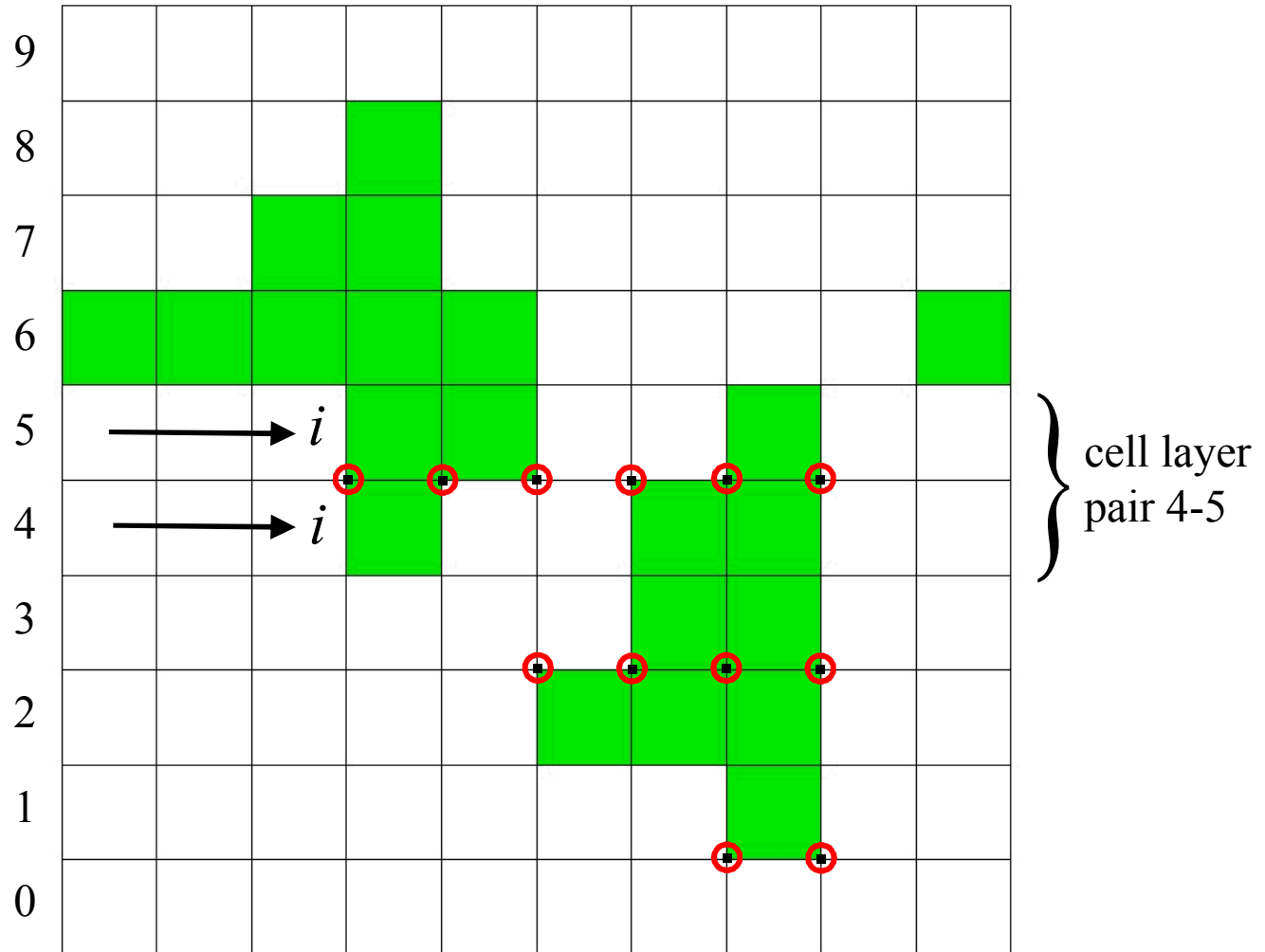
2-Refinement Procedure

2D Example



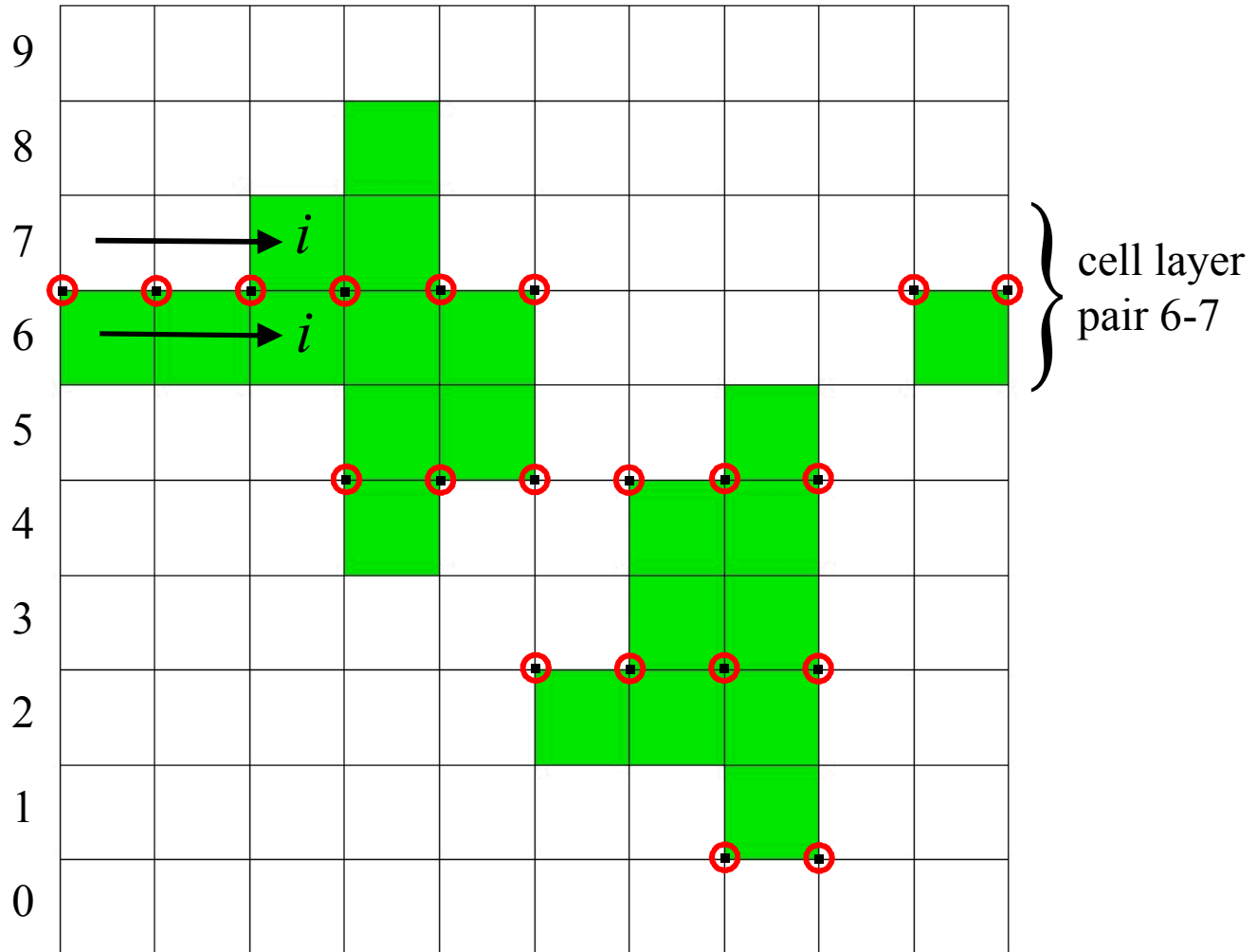
2-Refinement Procedure

2D Example



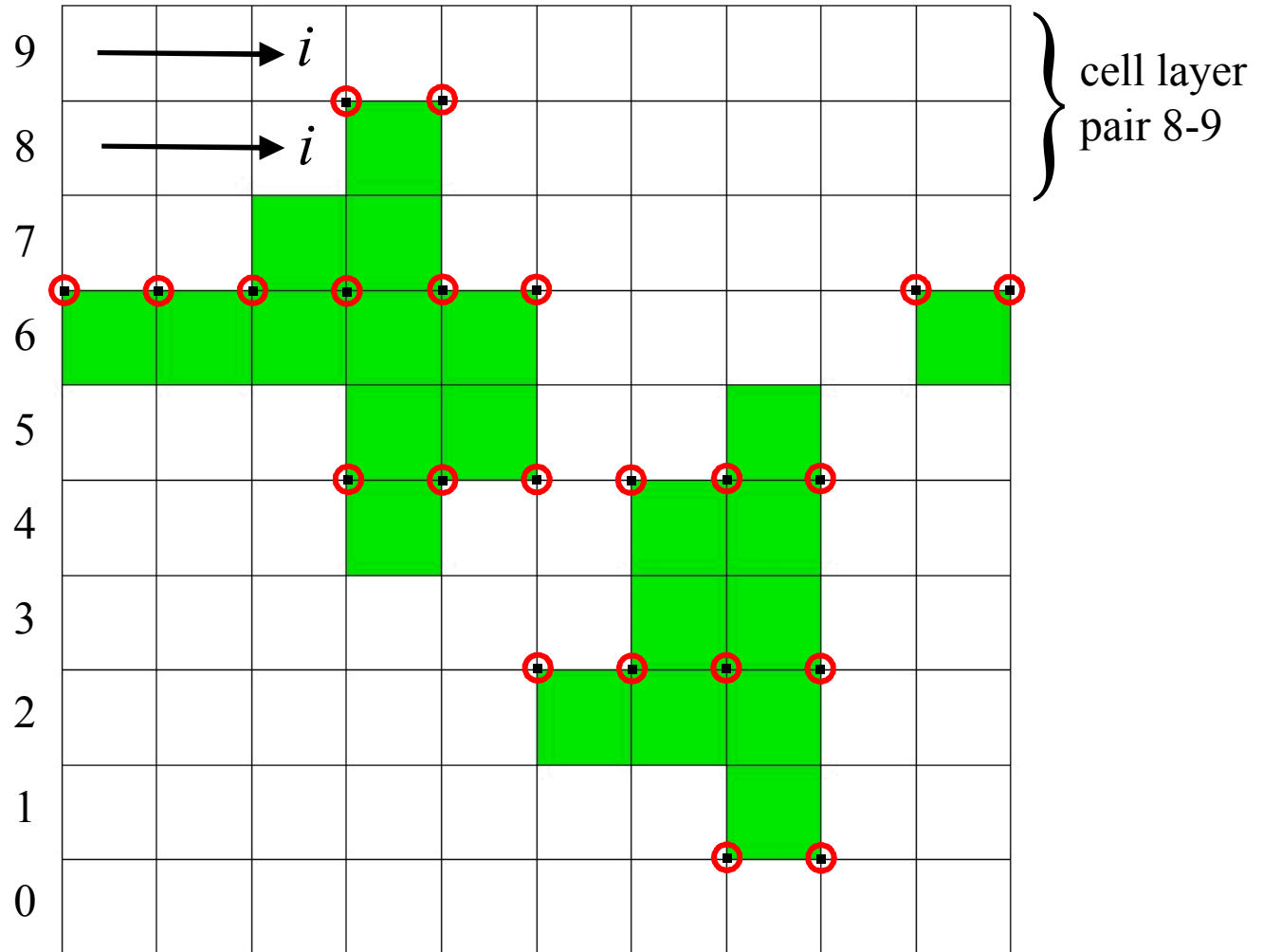
2-Refinement Procedure

2D Example

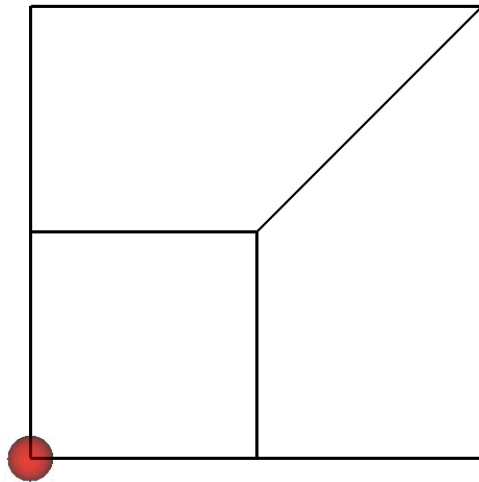


2-Refinement Procedure

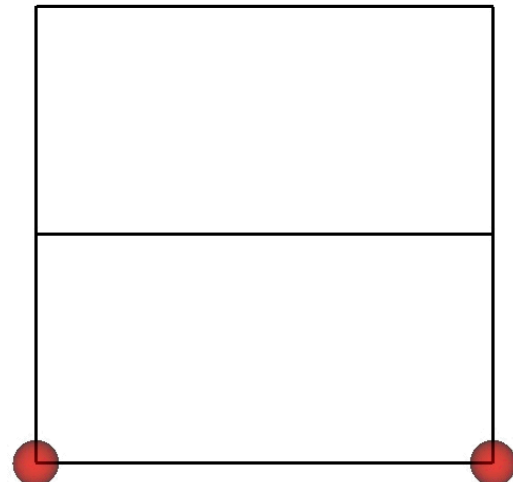
2D Example



2D Templates



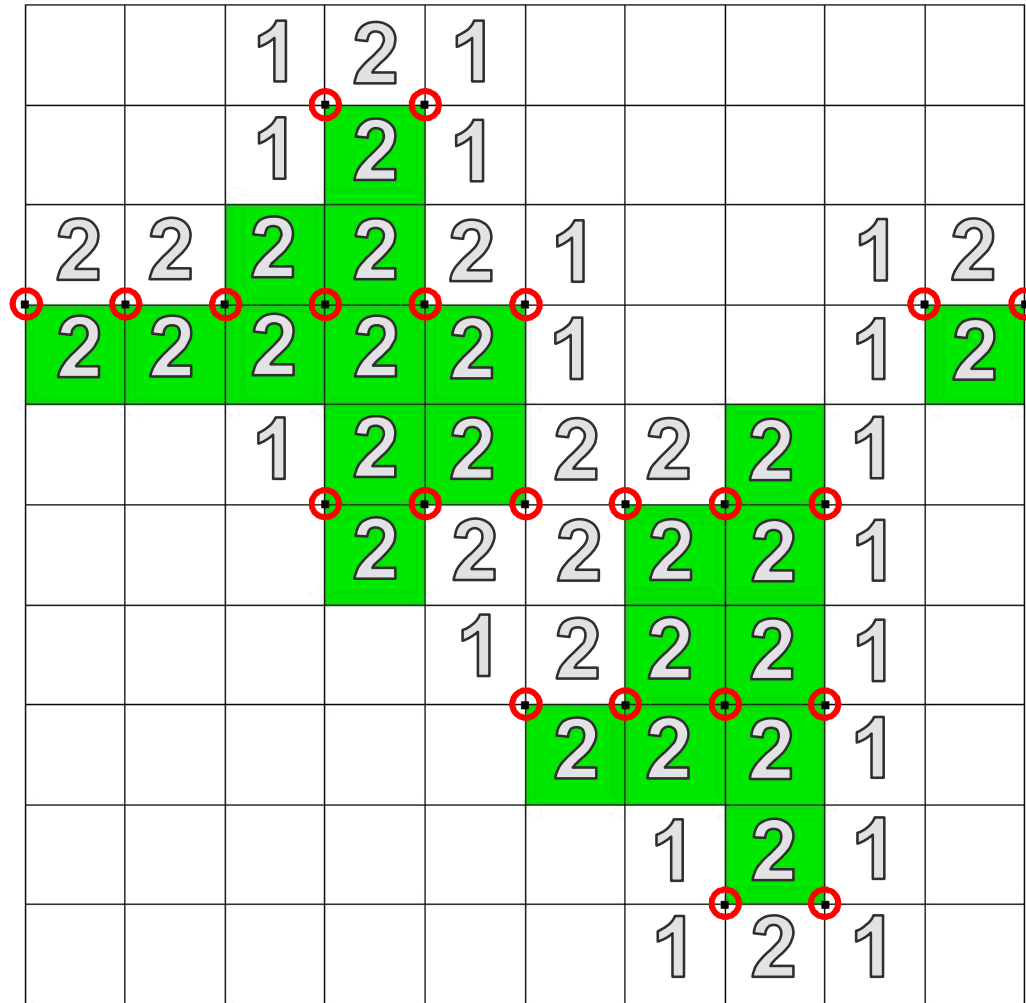
1



2

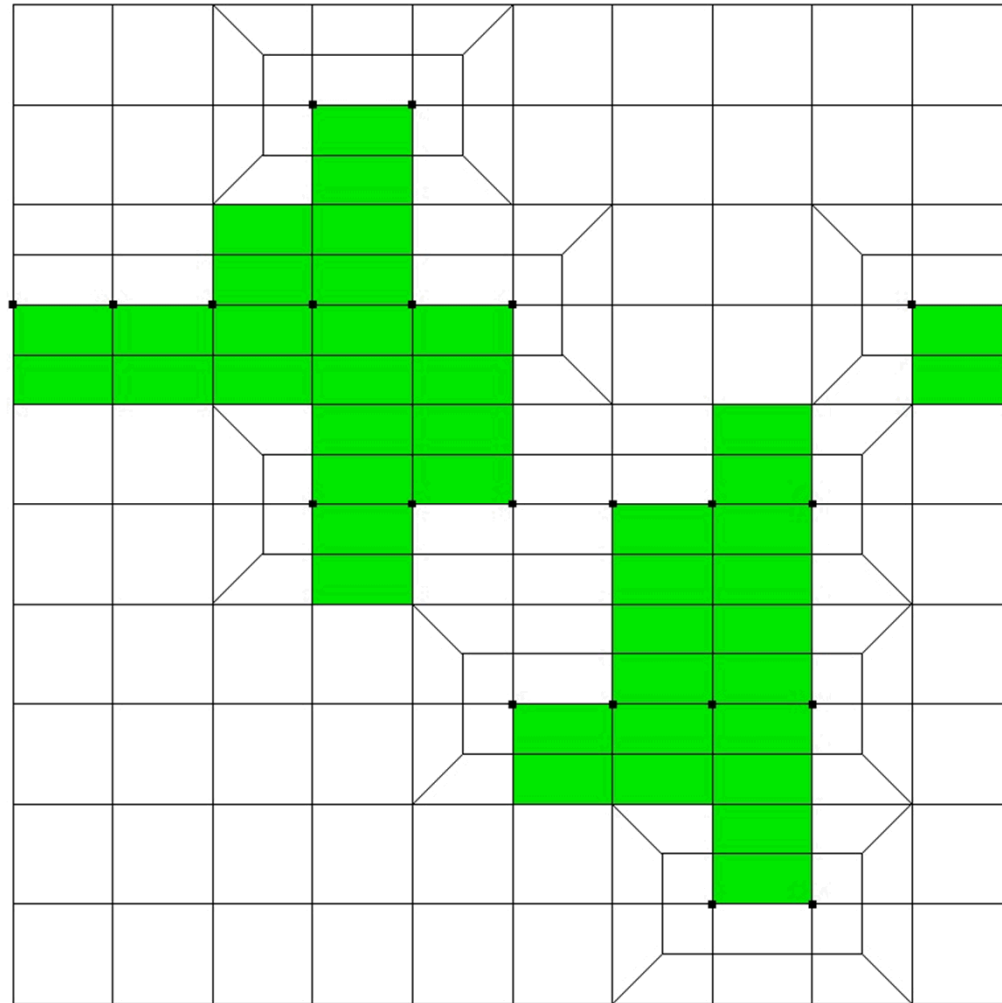
2-Refinement Procedure

2D Example



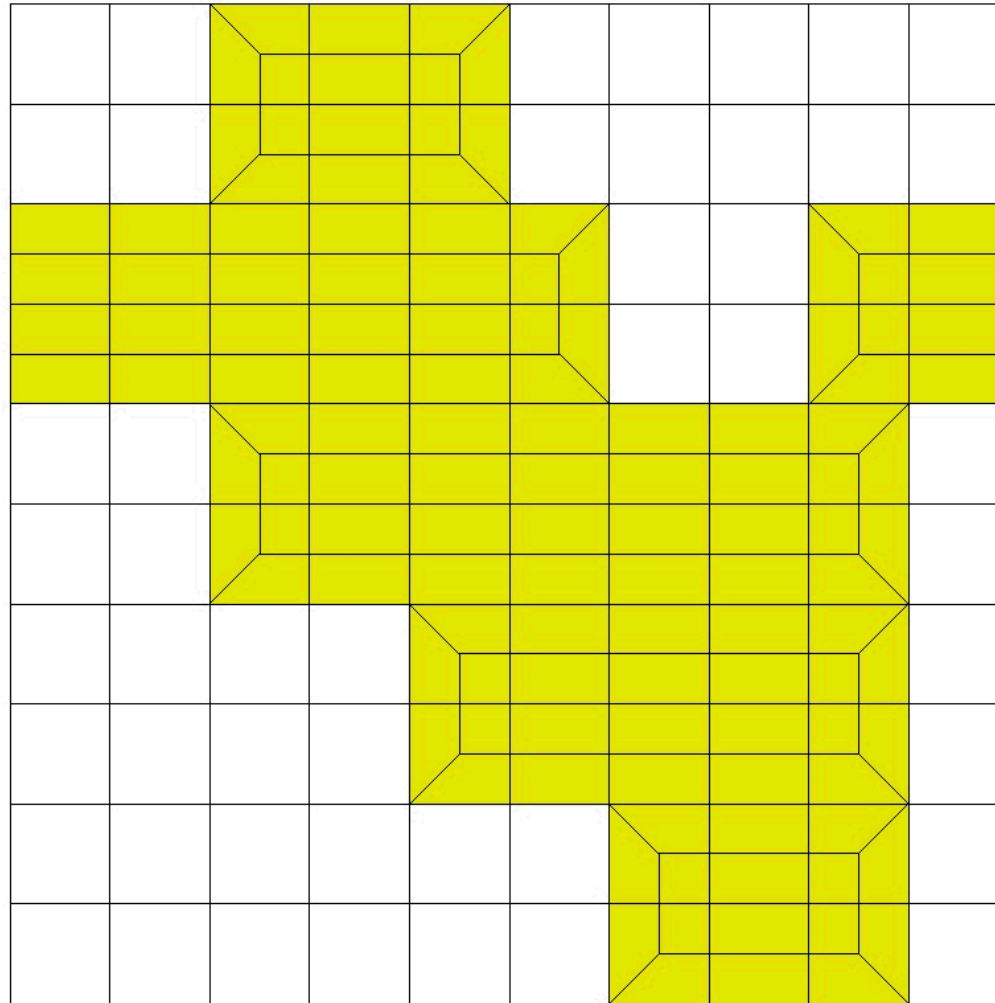
2-Refinement Procedure

2D Example

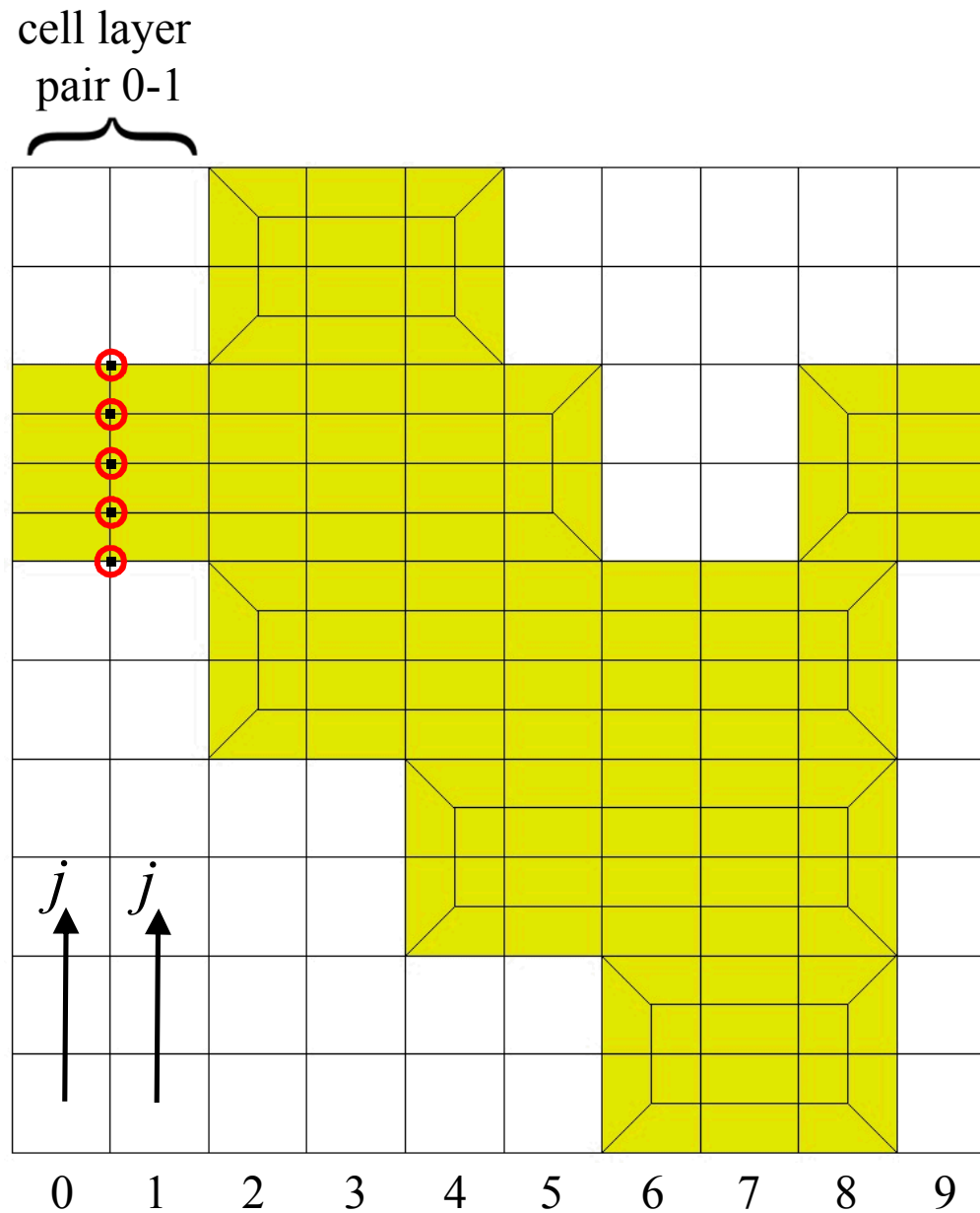


2-Refinement Procedure

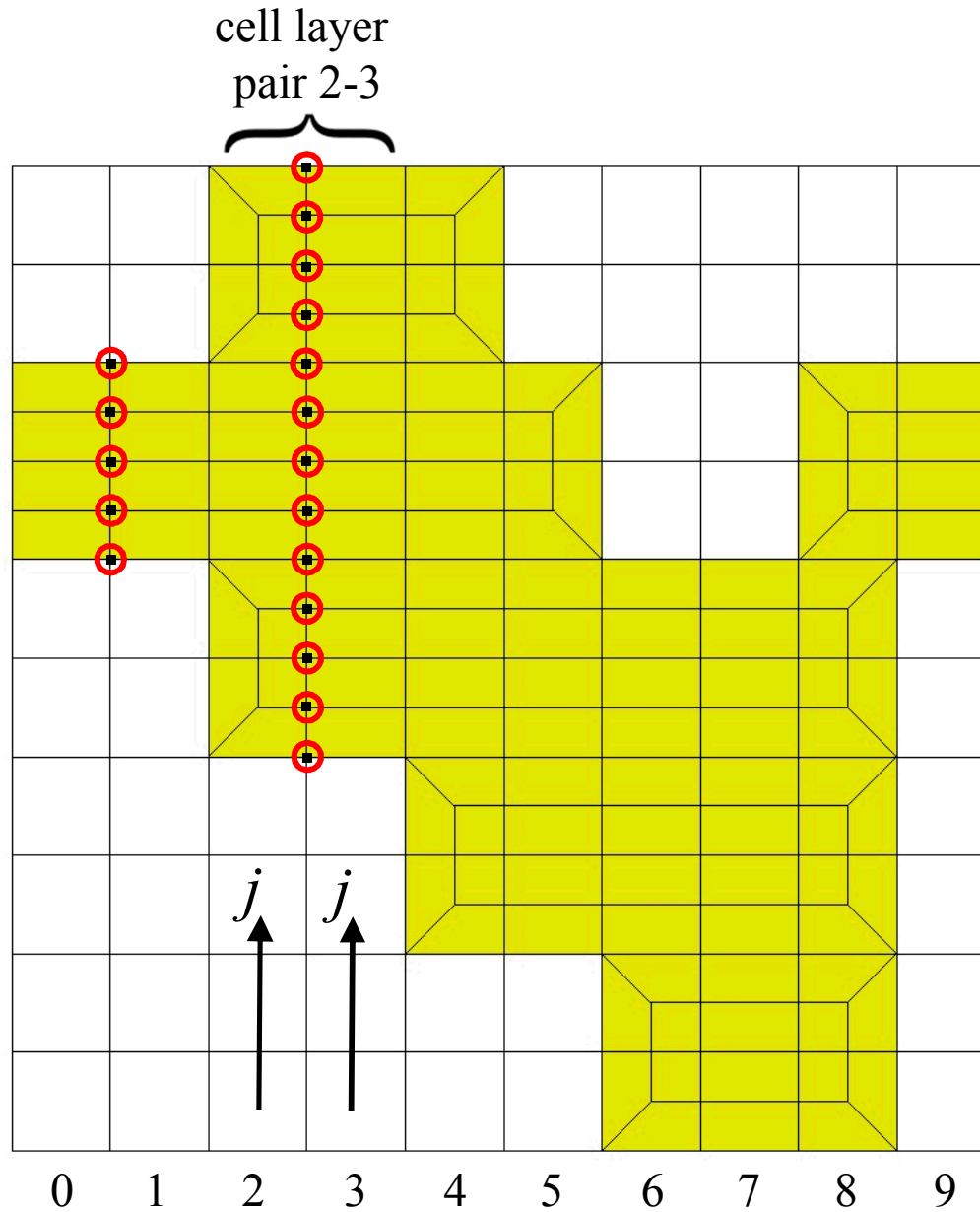
2D Example



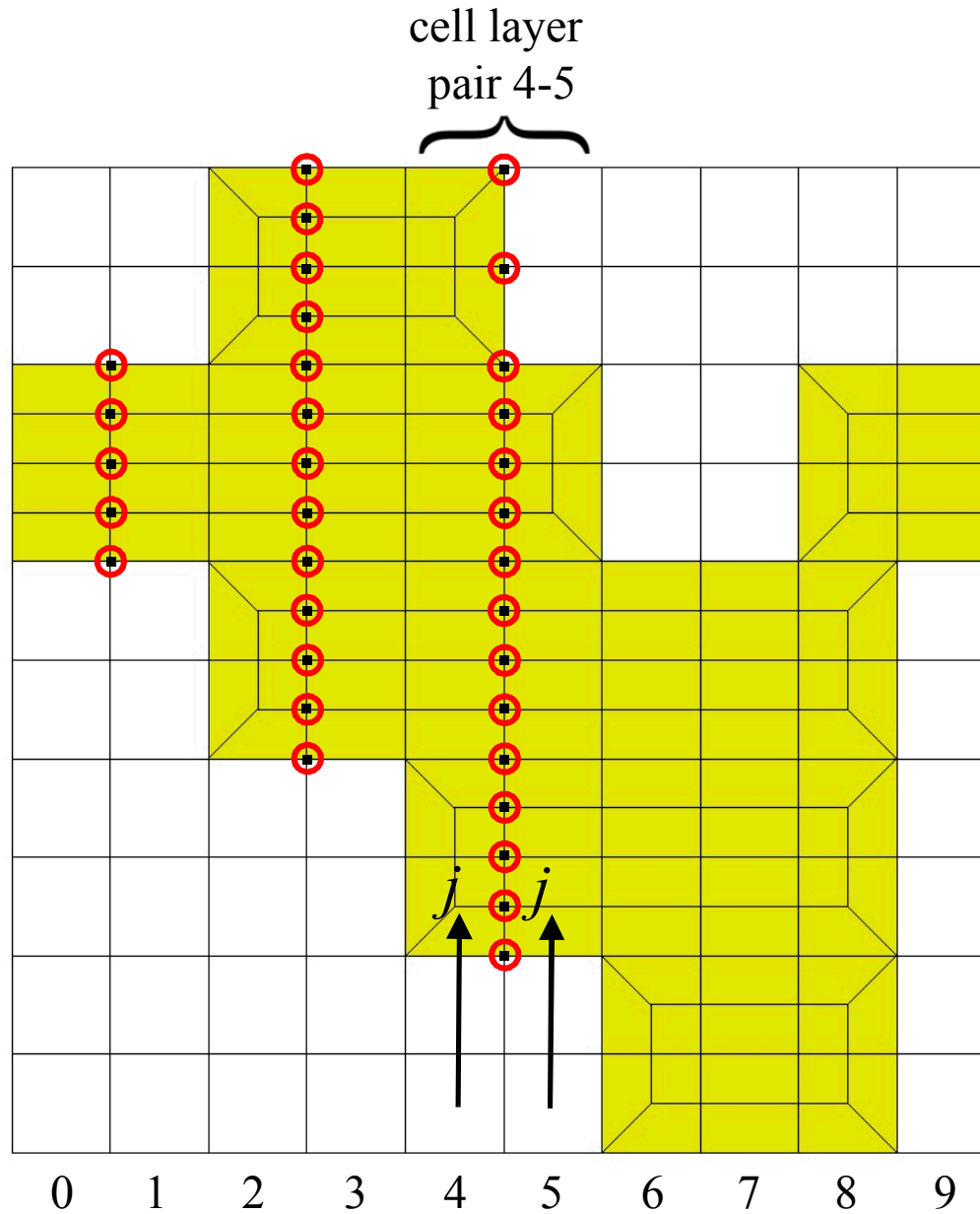
2D Example



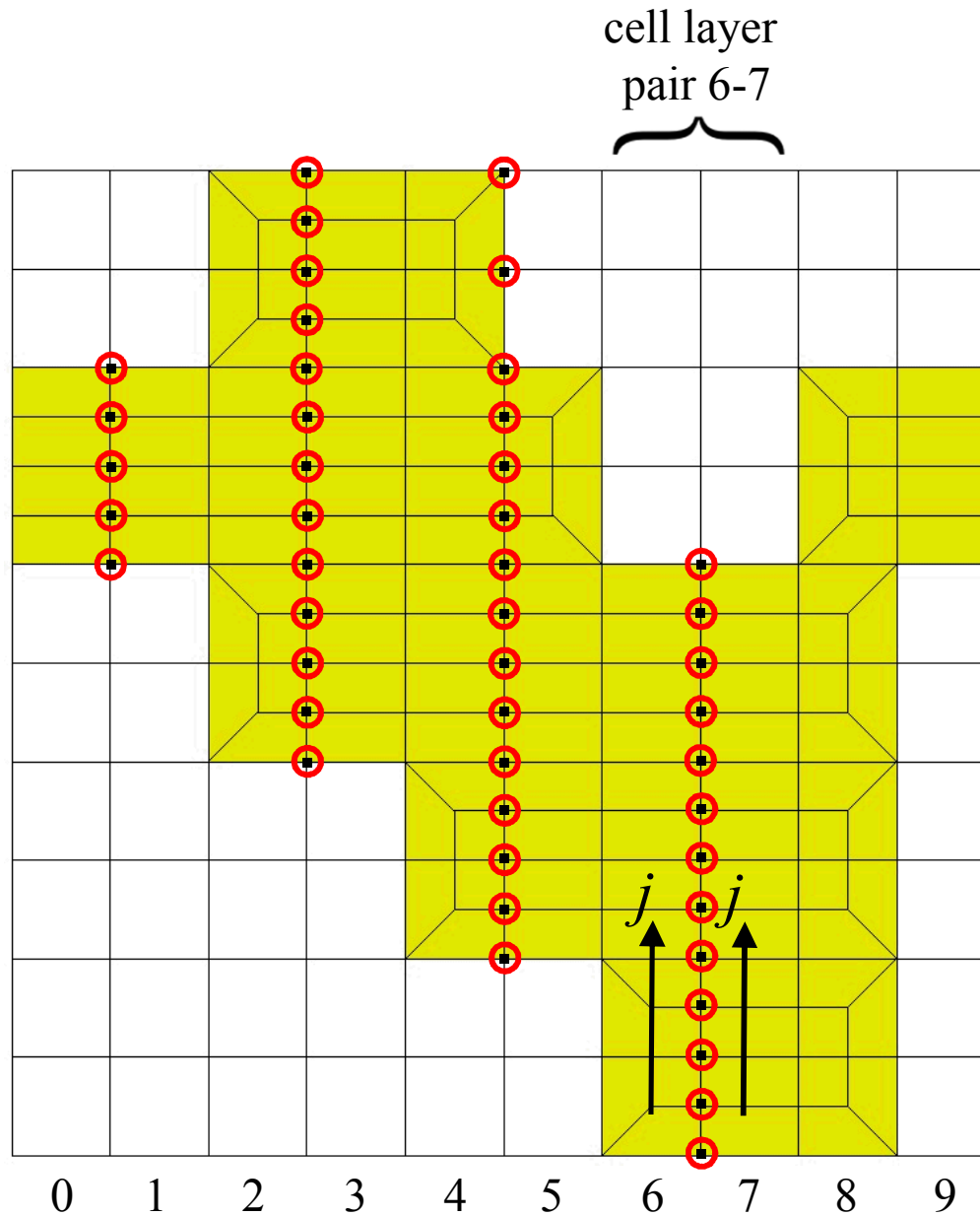
2D Example



2D Example

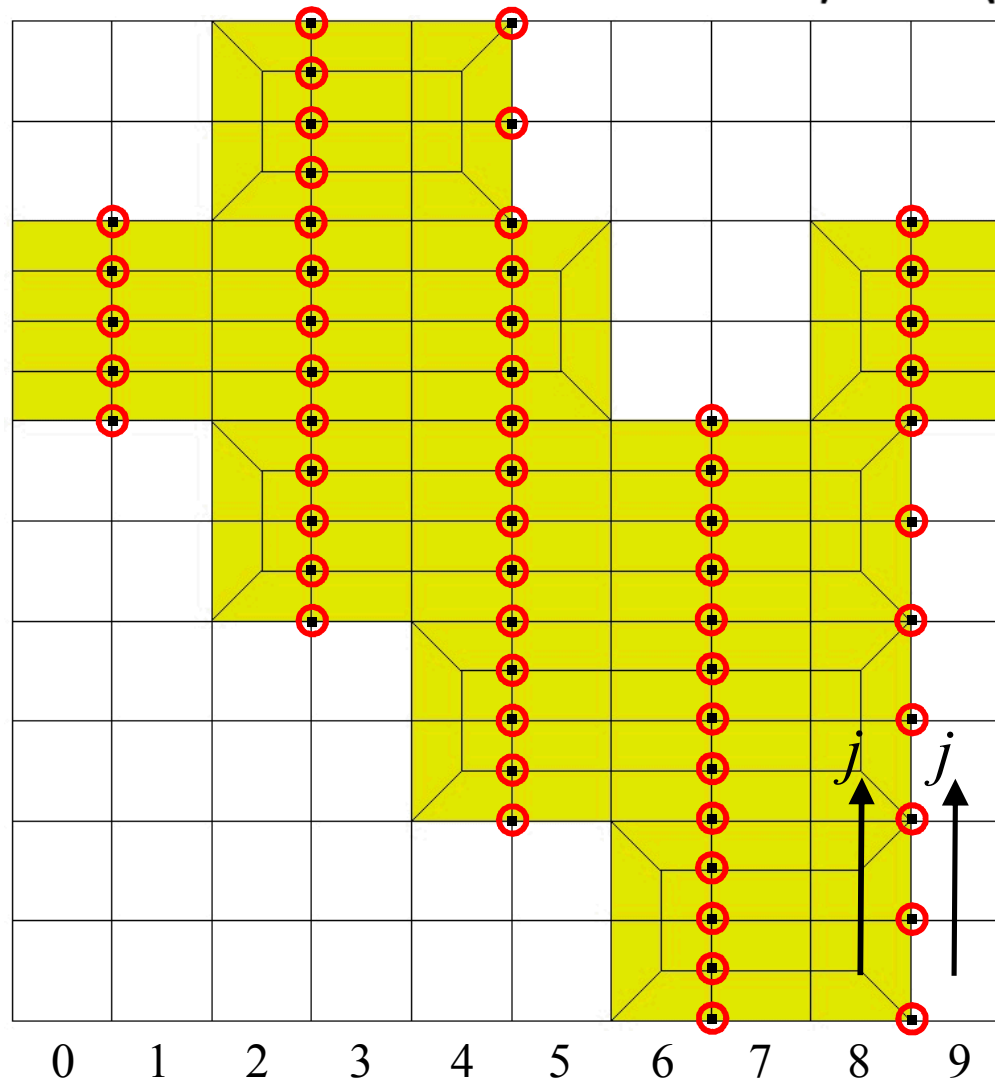


2D Example

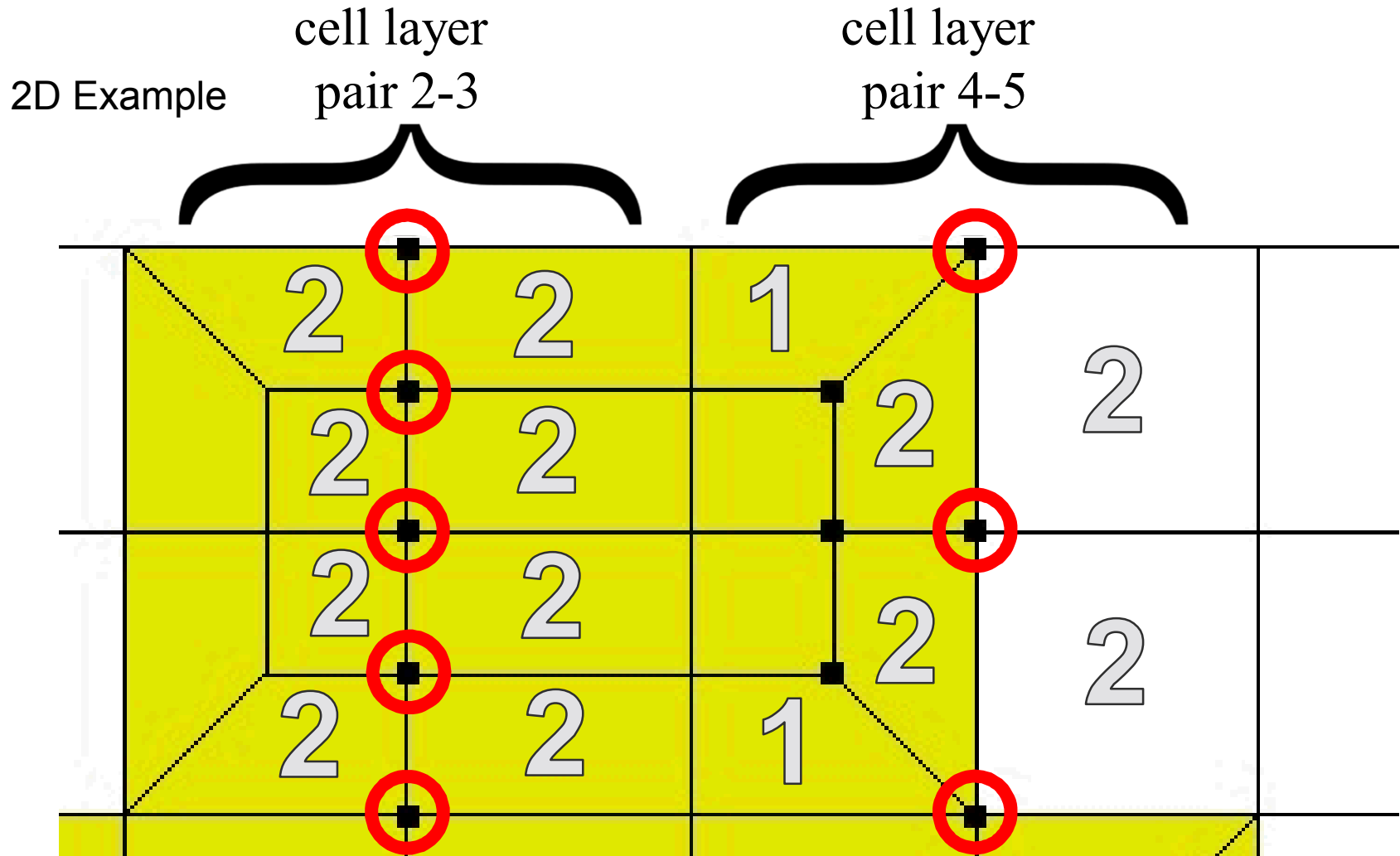


cell layer
pair 8-9

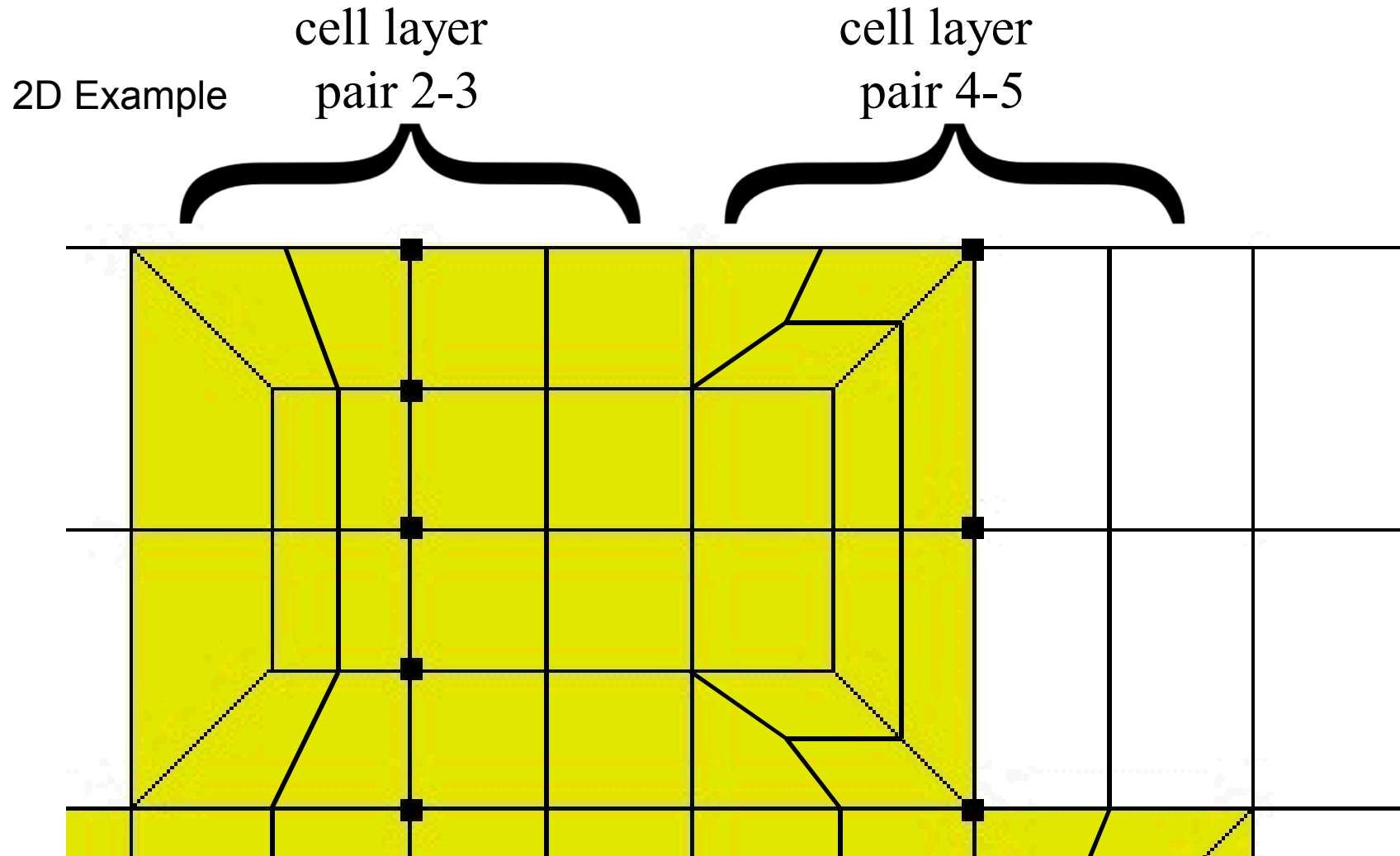
2D Example



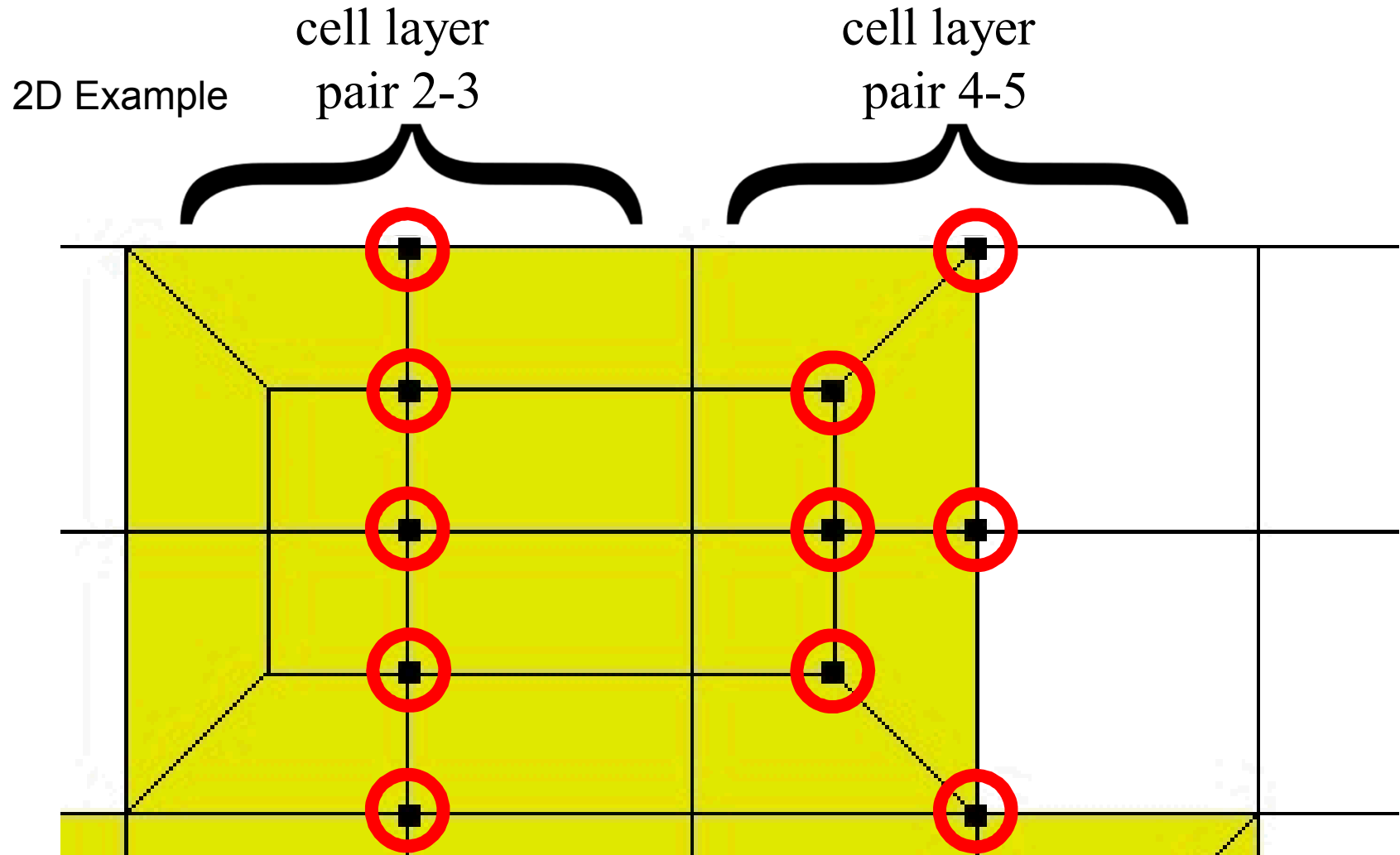
Node Marking Propagation



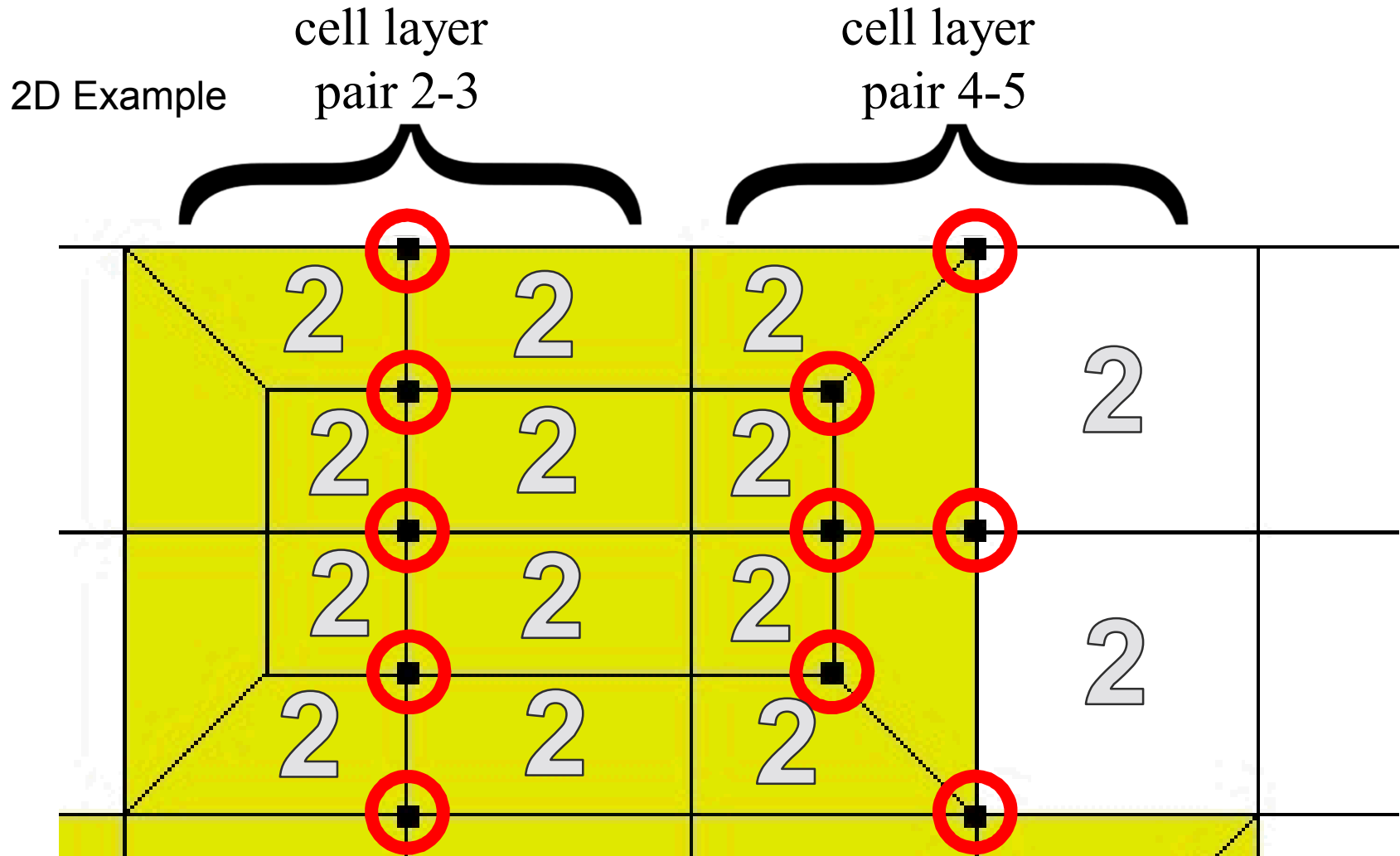
Node Marking Propagation



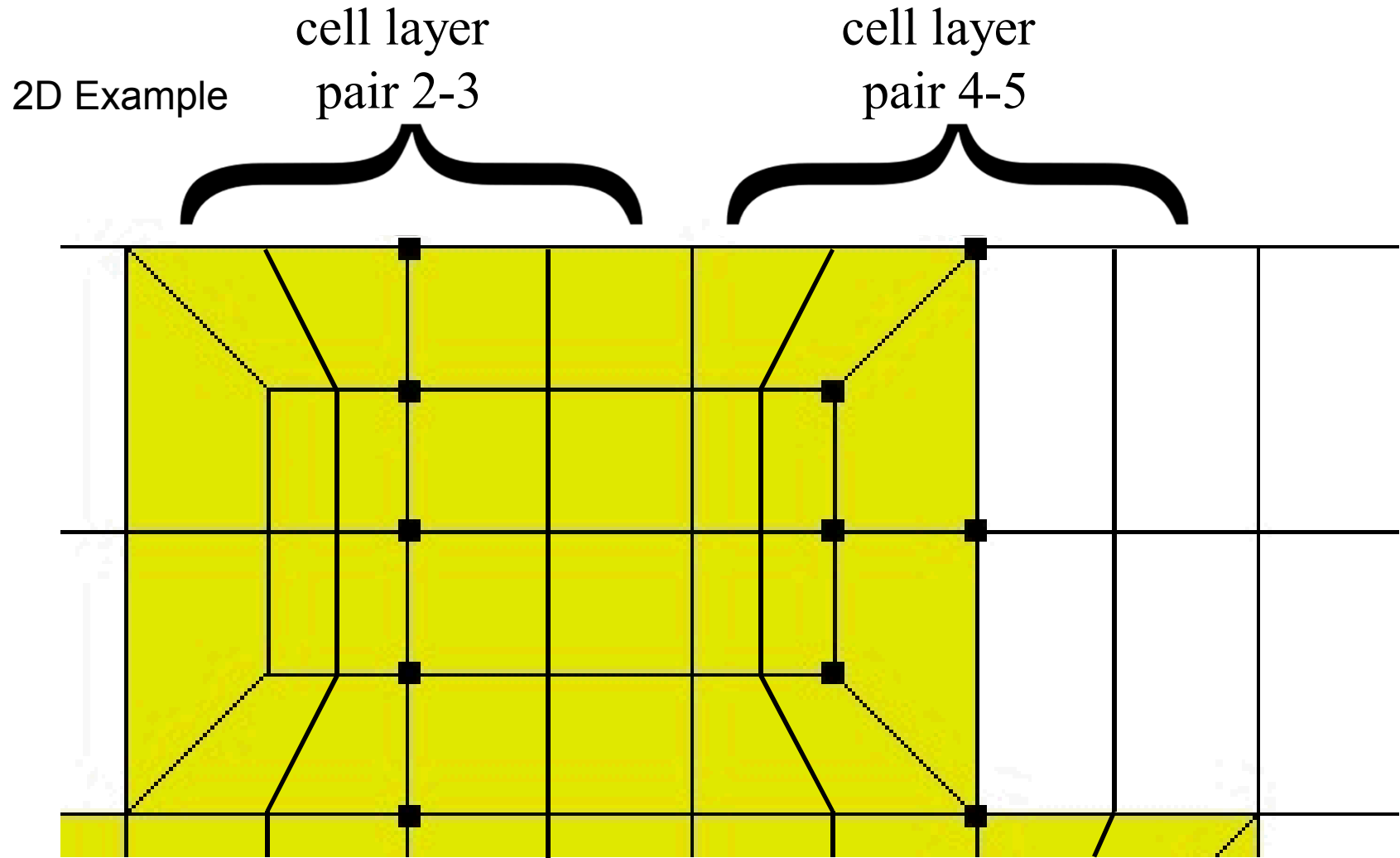
Node Marking Propagation



Node Marking Propagation

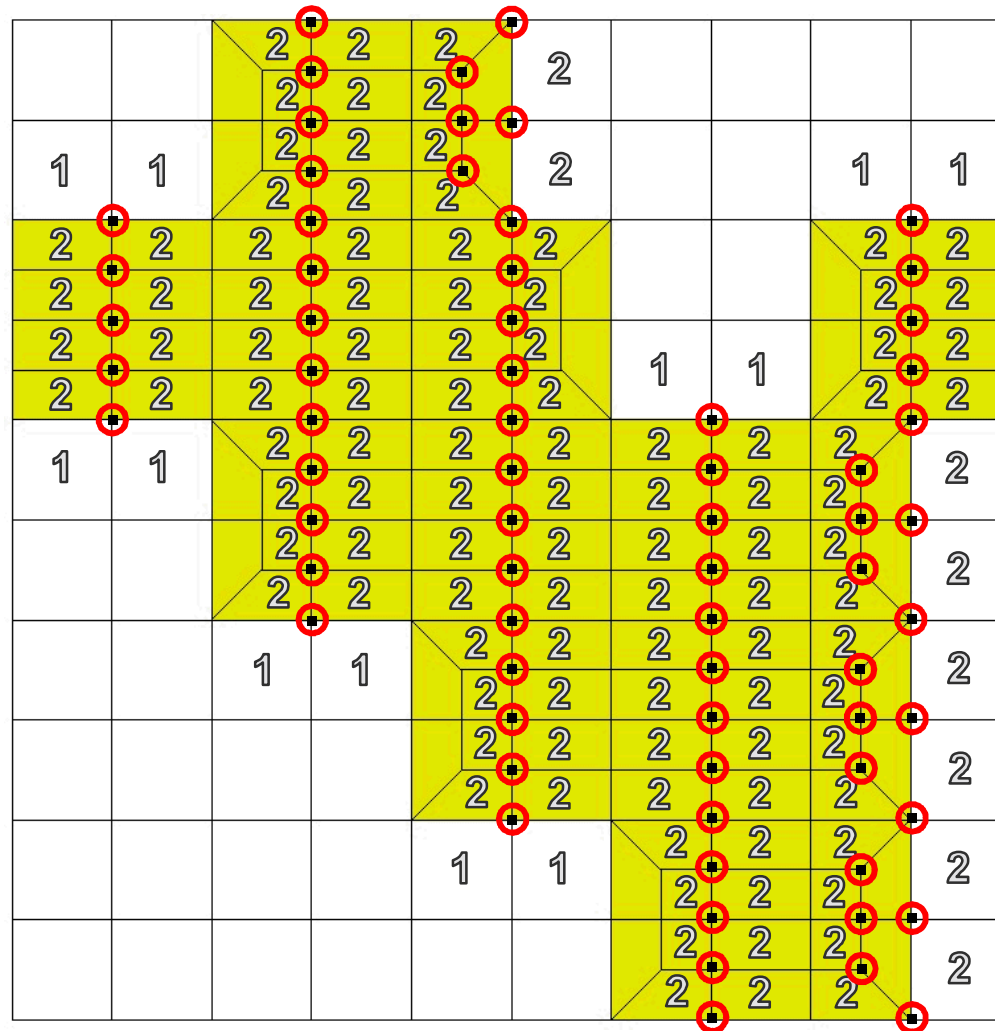


Node Marking Propagation



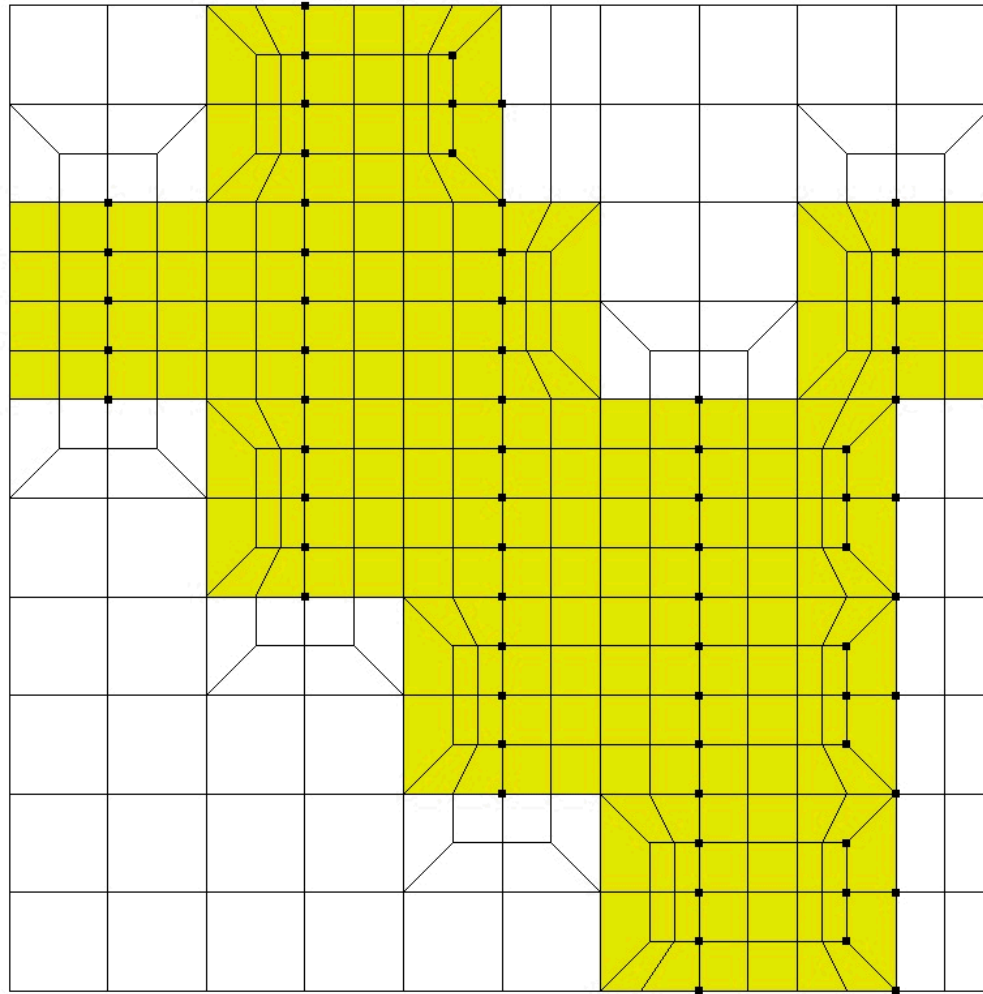
2-Refinement Procedure

2D Example



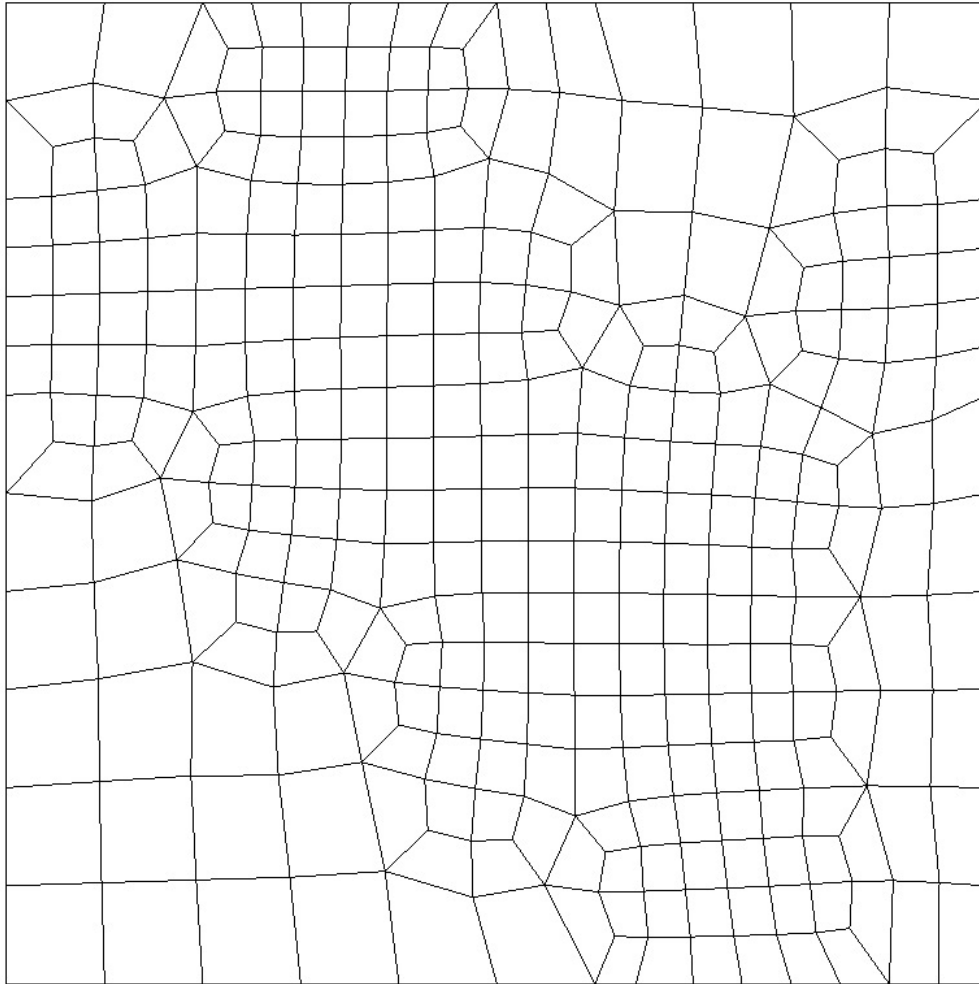
2-Refinement Procedure

2D Example



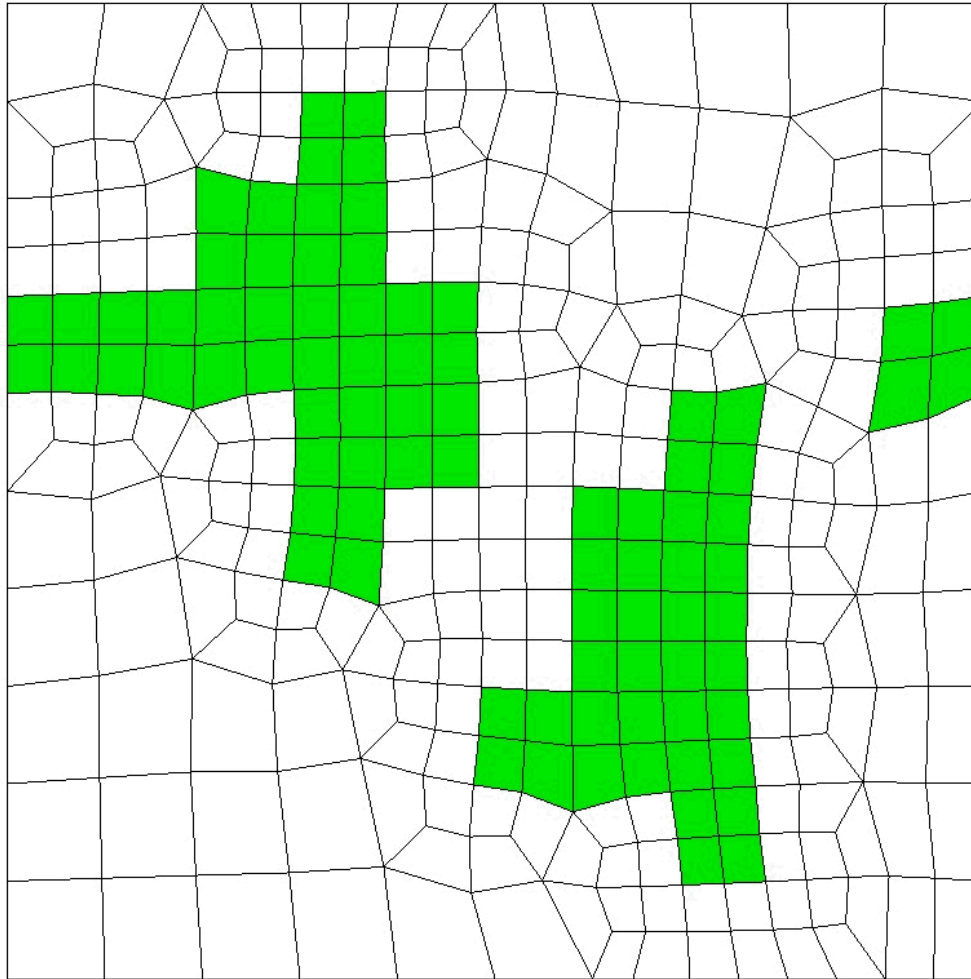
2-Refinement Procedure

2D Example



2-Refinement Procedure

2D Example



2-Refinement Algorithm

Enumerate Cartesian grid

Identify and mark elements to be uniformly refined

For each direction I, J, K do

 Mark nodes between odd-even layers at marked elements

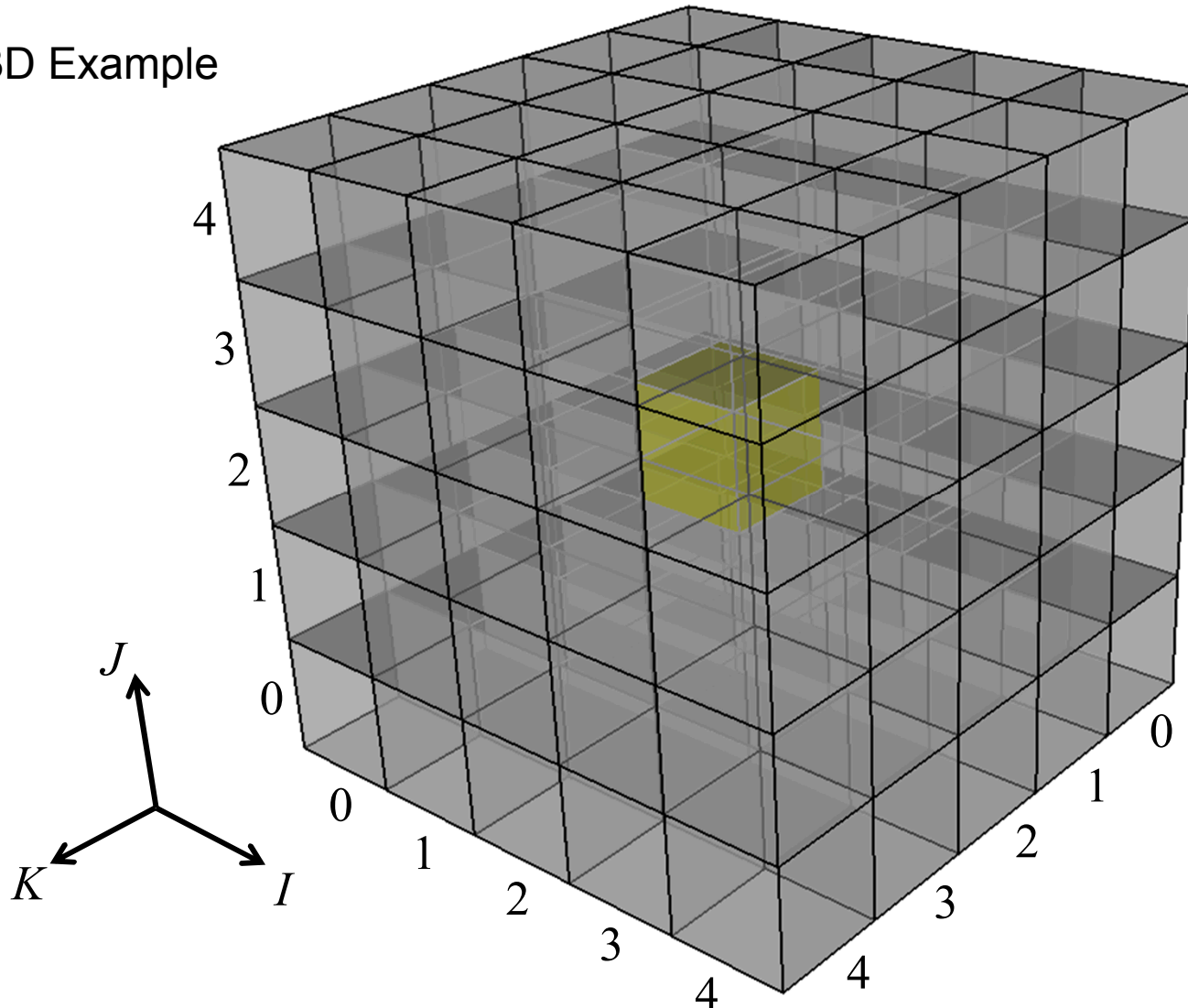
 Apply refinement templates to elements with marked nodes

 Expand marked elements to include refined elements

End For

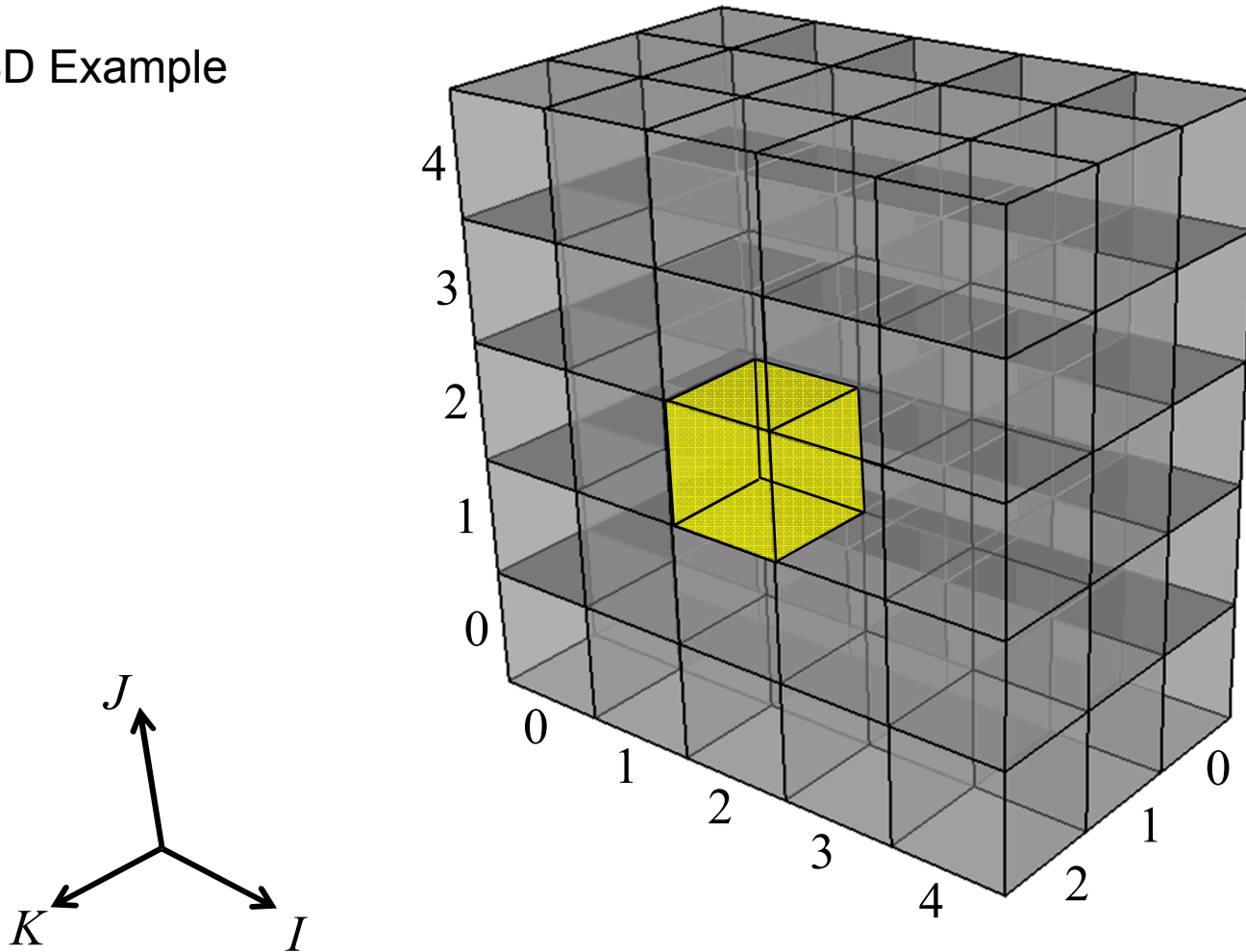
2-Refinement Procedure

3D Example



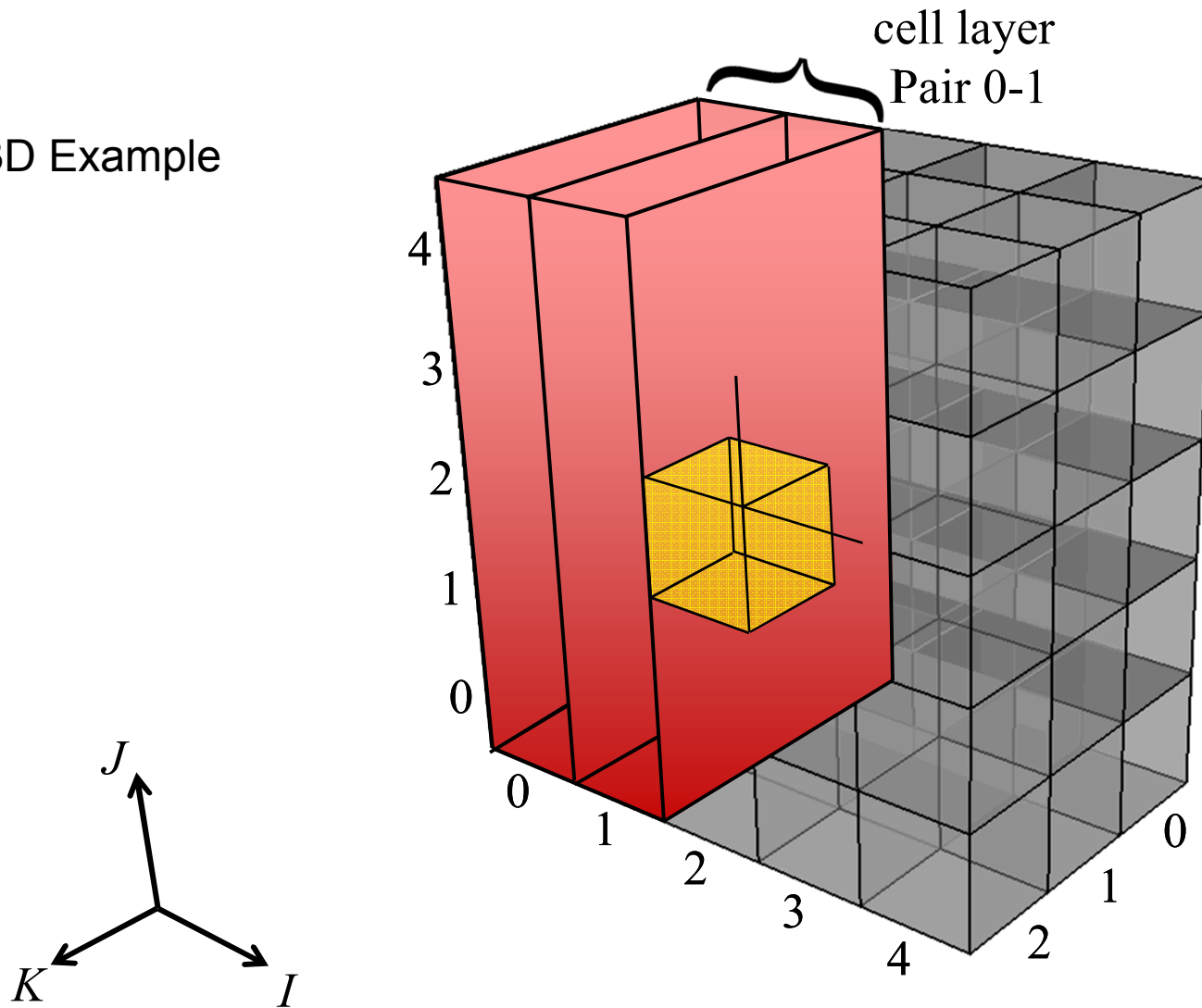
2-Refinement Procedure

3D Example



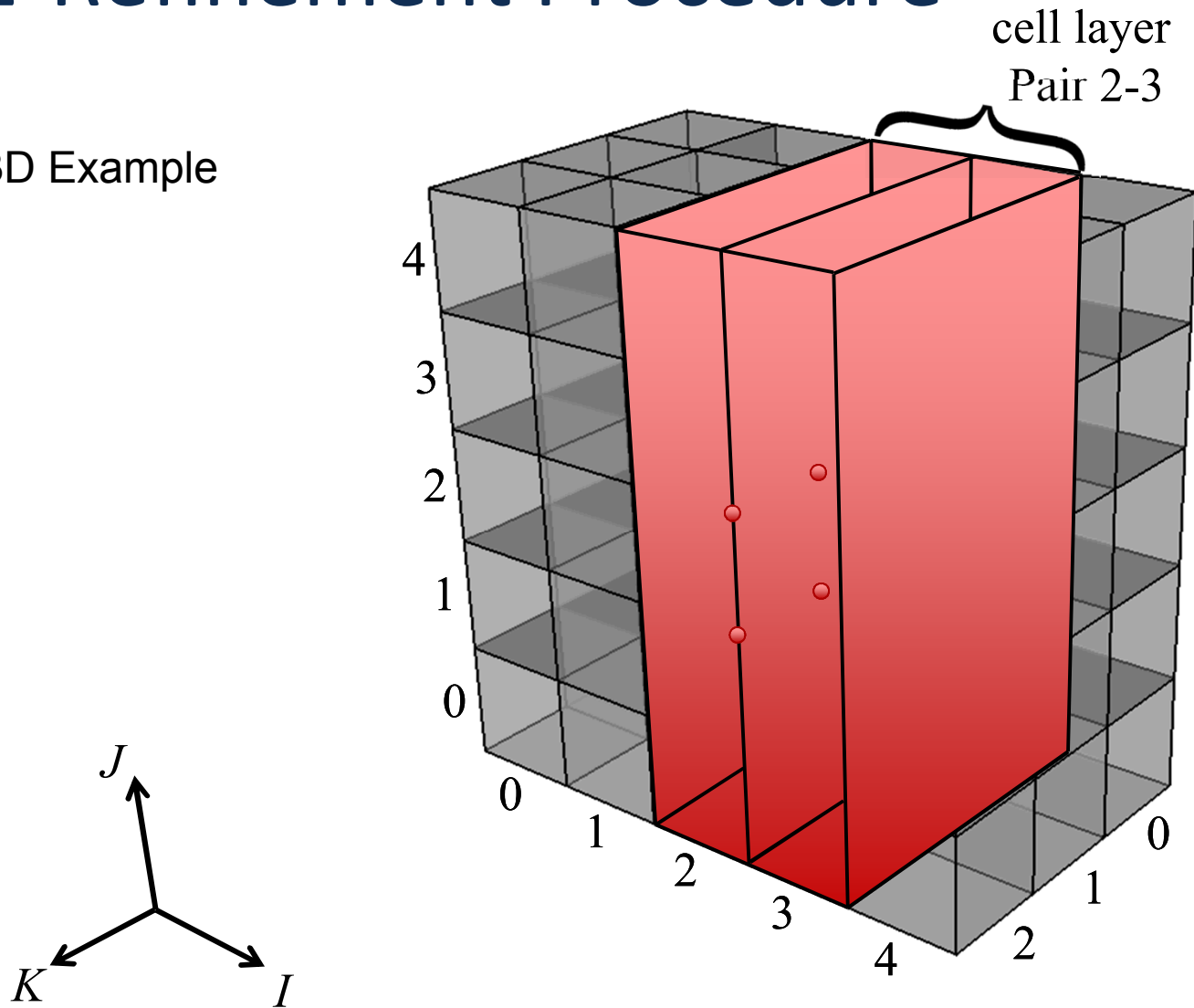
2-Refinement Procedure

3D Example



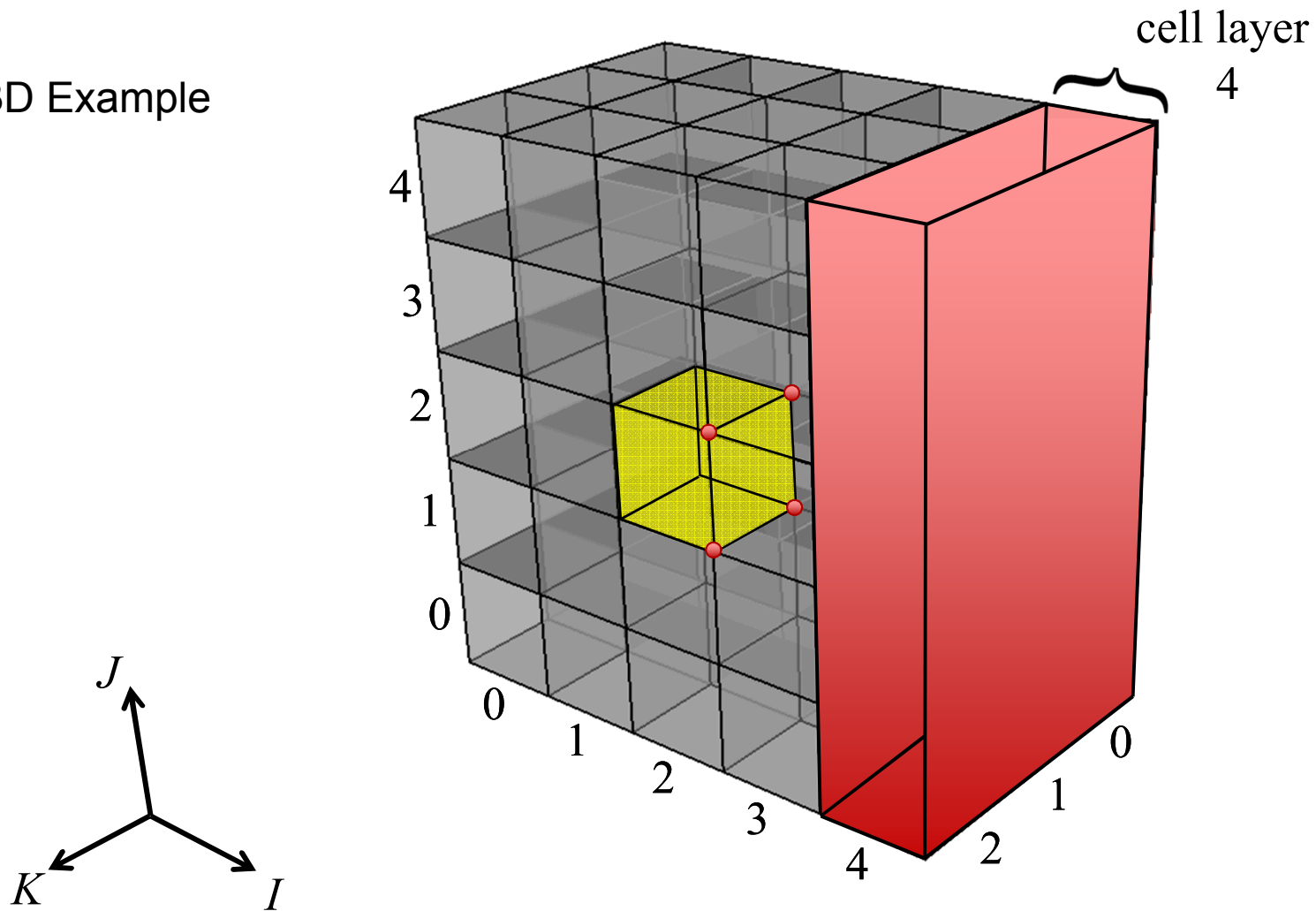
2-Refinement Procedure

3D Example

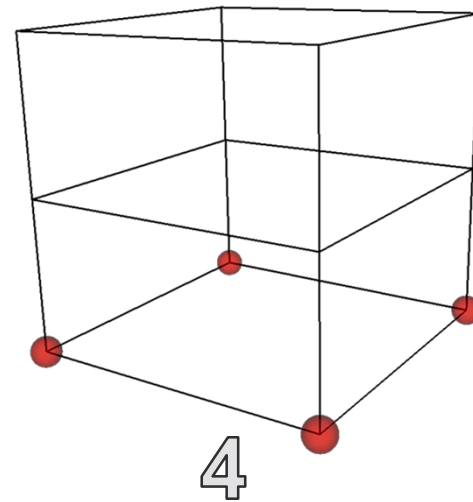
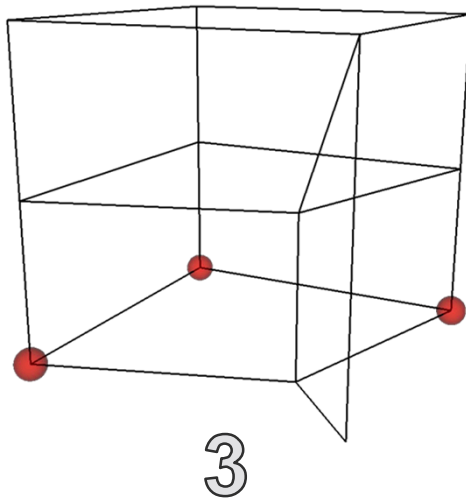
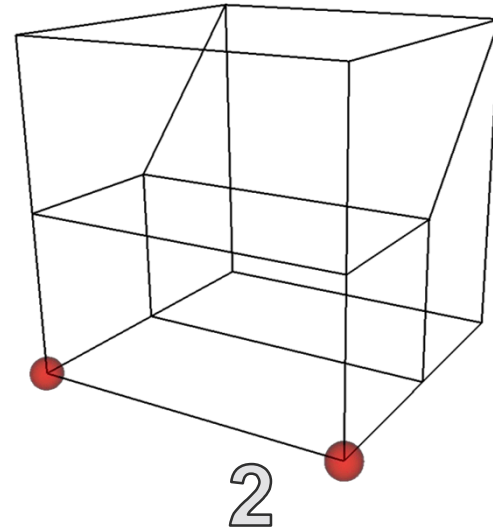
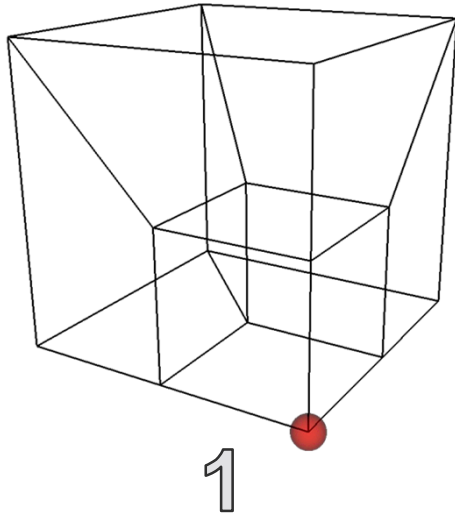


2-Refinement Procedure

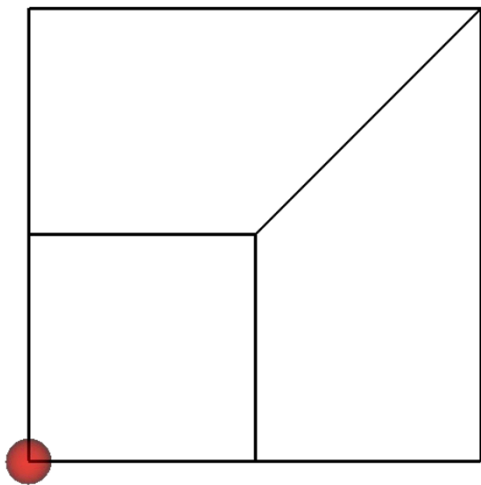
3D Example



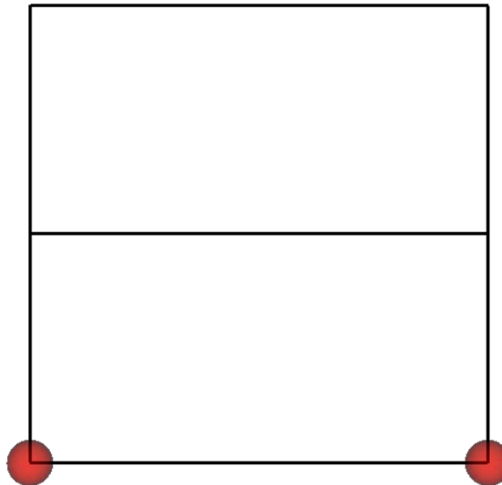
3D Templates



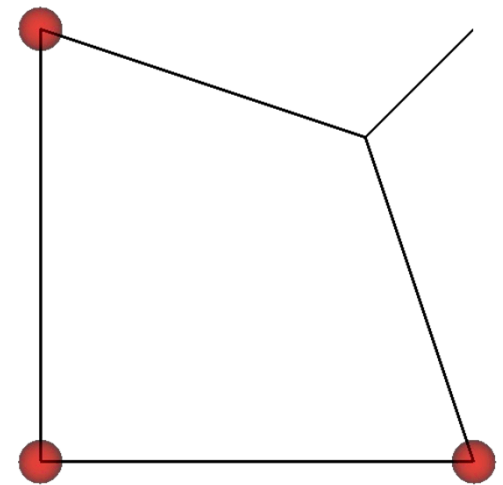
3D Face Templates



1



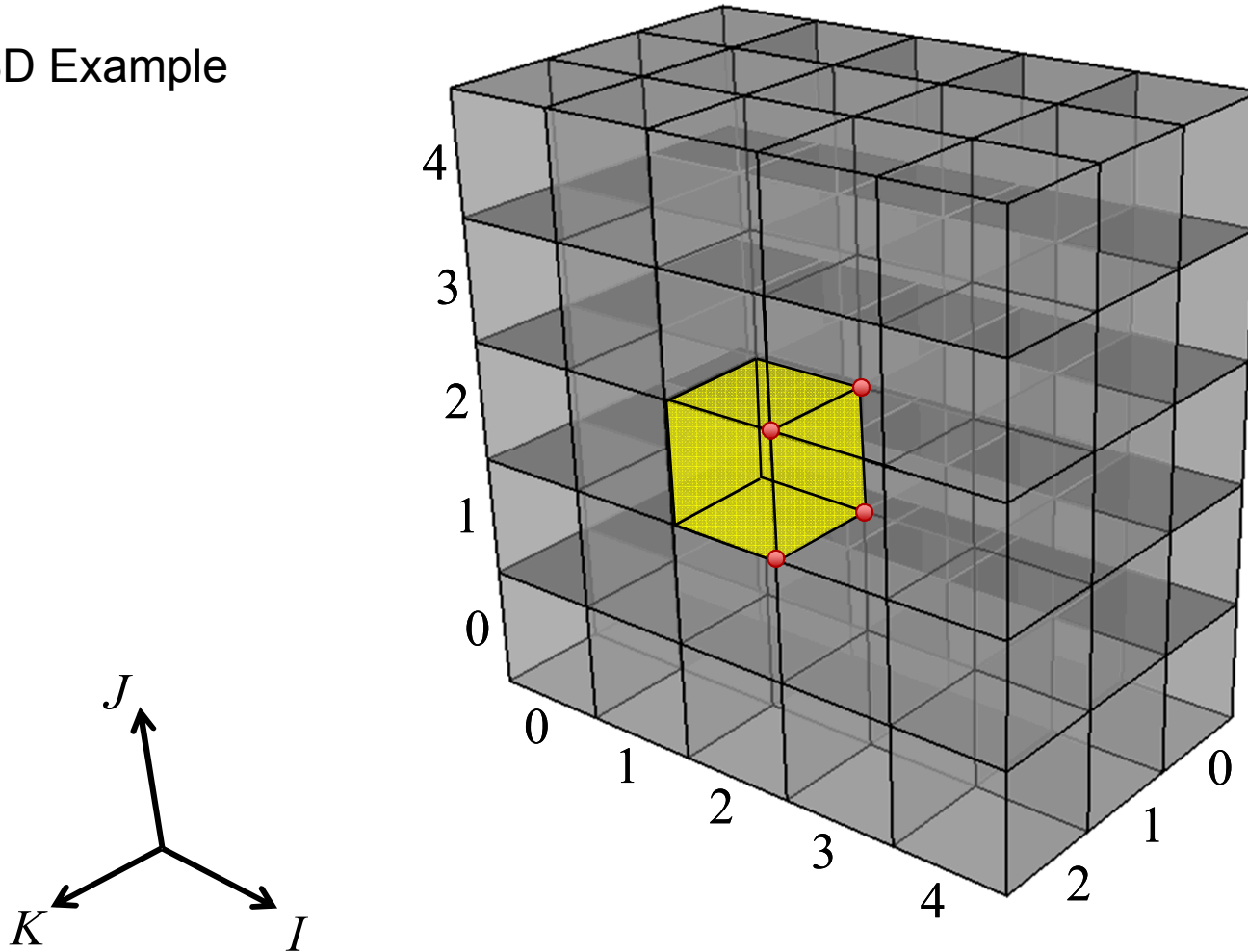
2



3

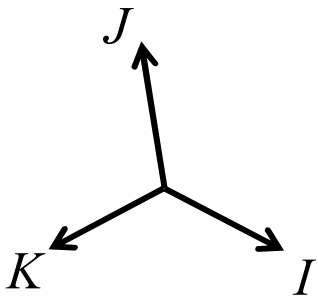
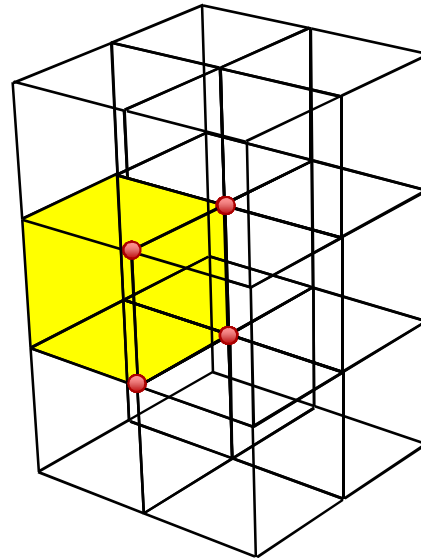
2-Refinement Procedure

3D Example



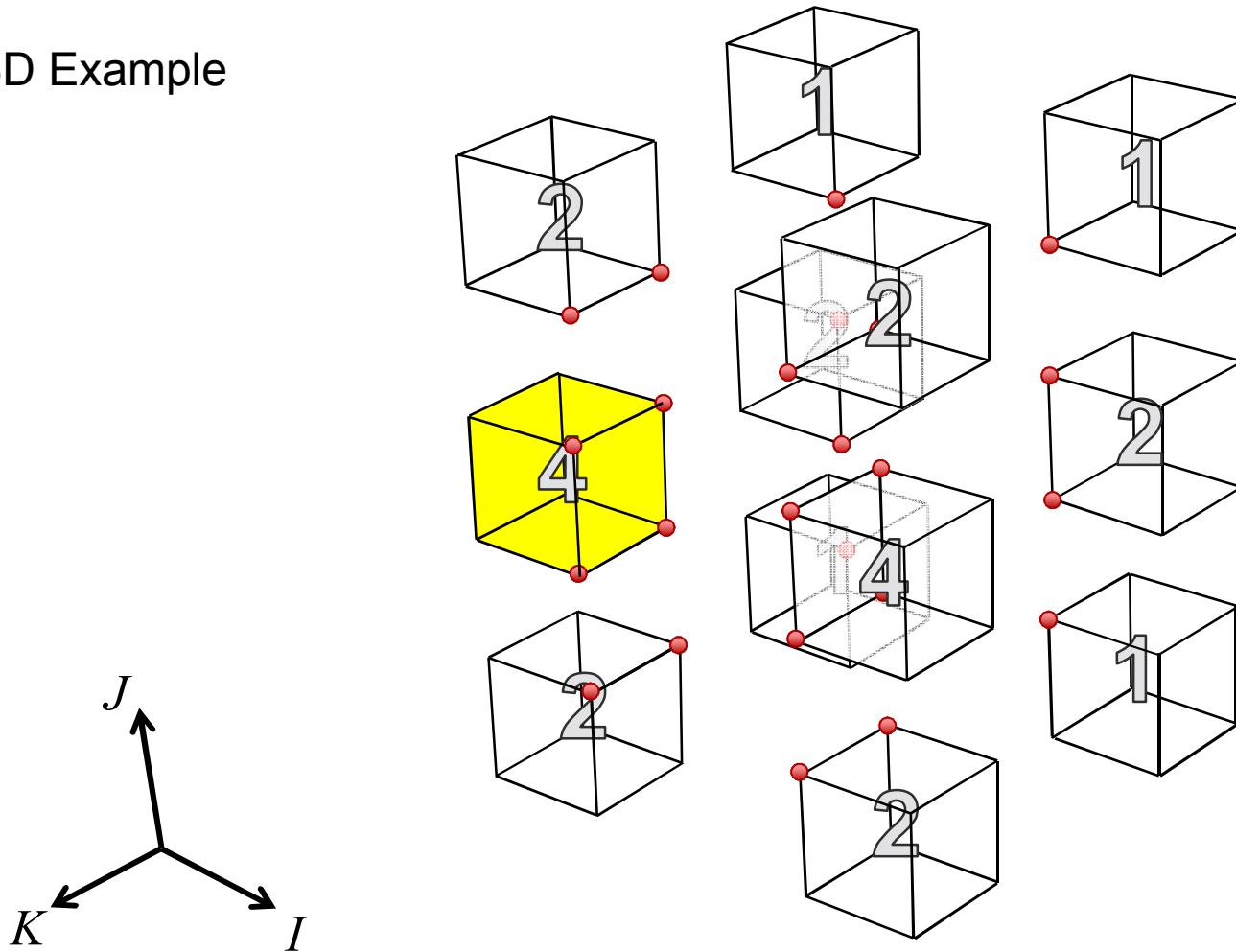
2-Refinement Procedure

3D Example



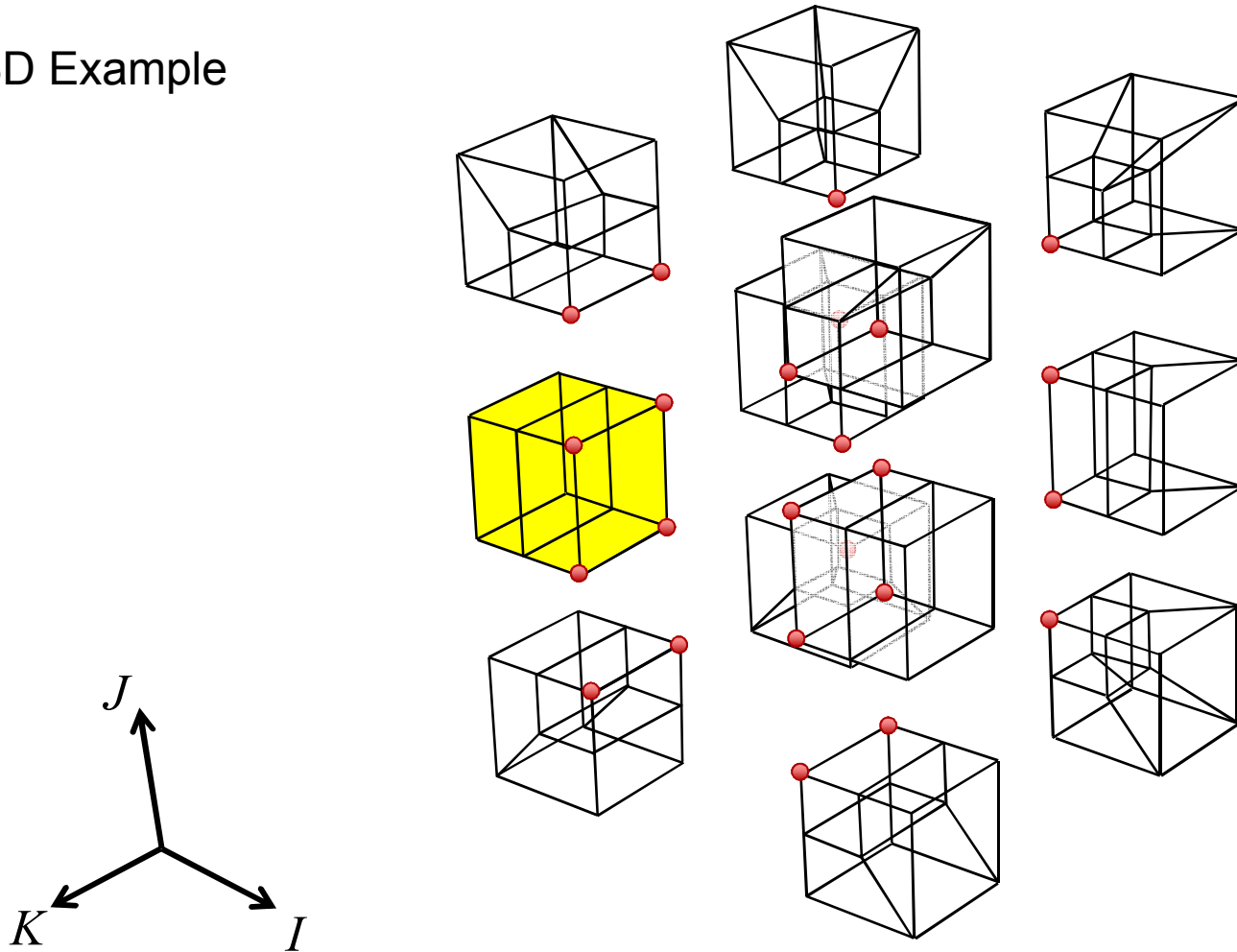
2-Refinement Procedure

3D Example



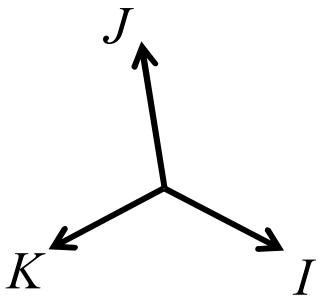
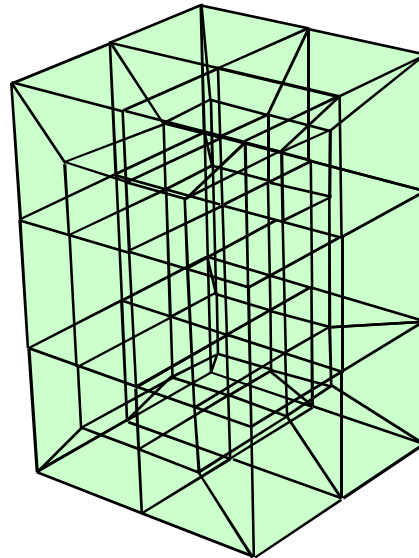
2-Refinement Procedure

3D Example



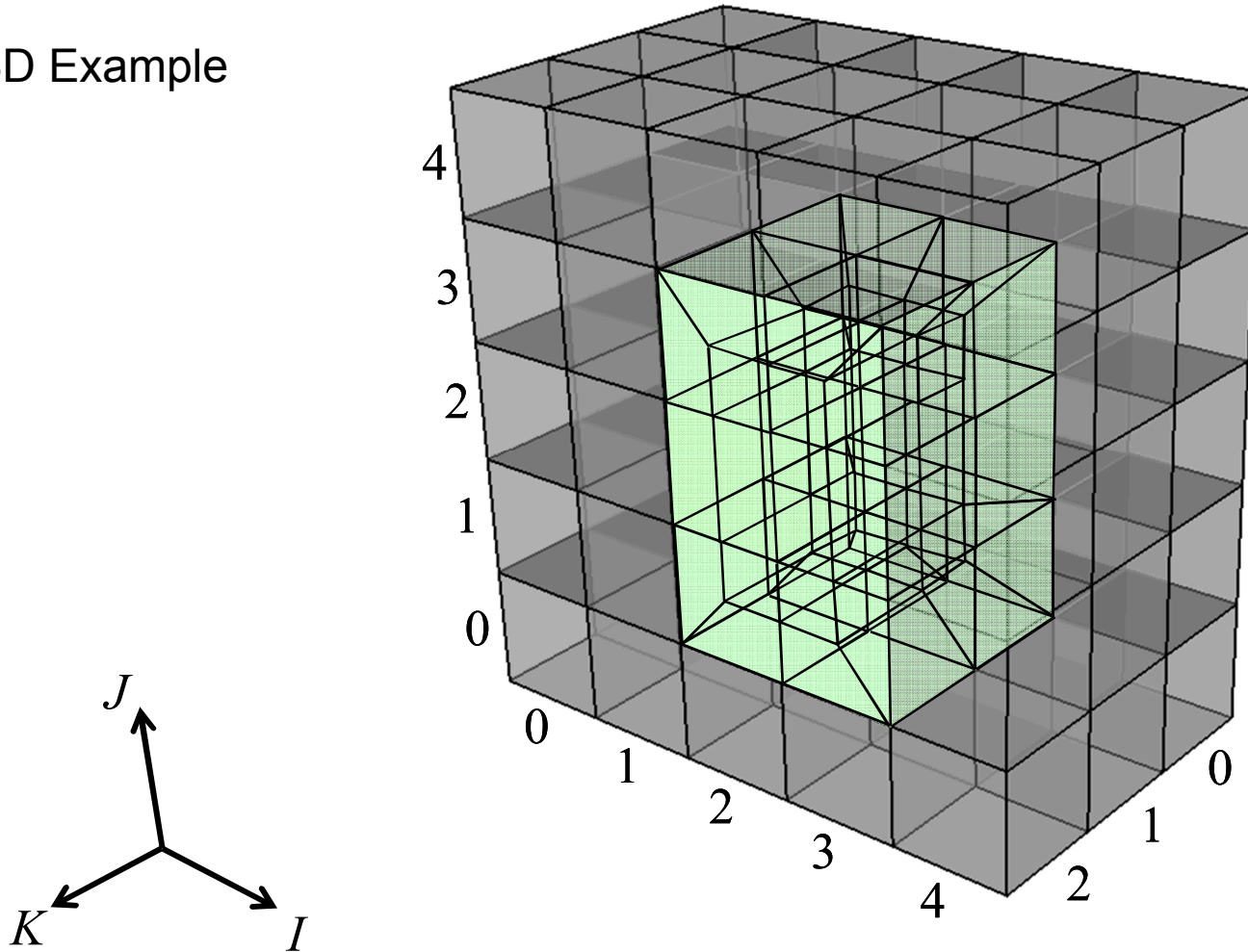
2-Refinement Procedure

3D Example



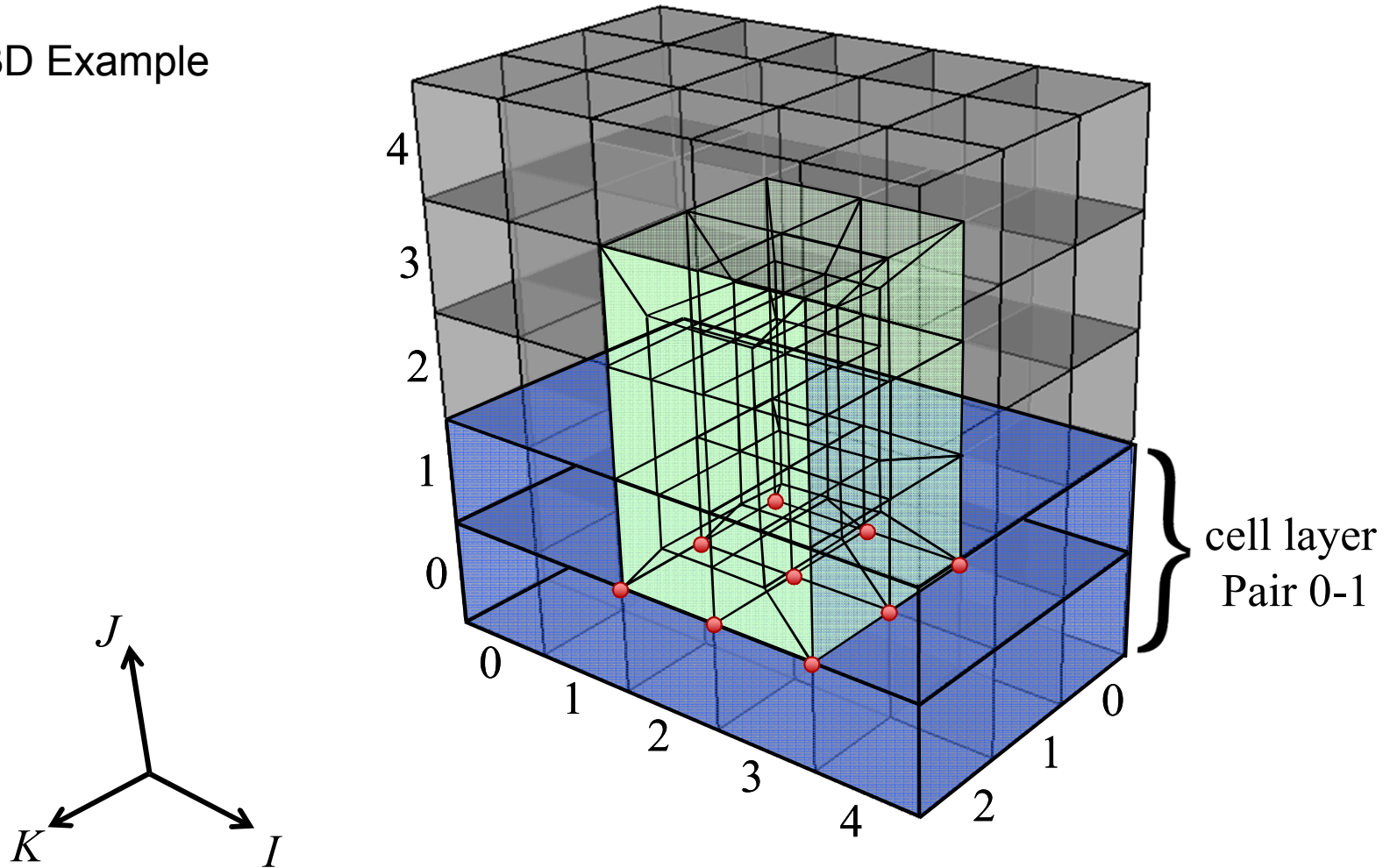
2-Refinement Procedure

3D Example



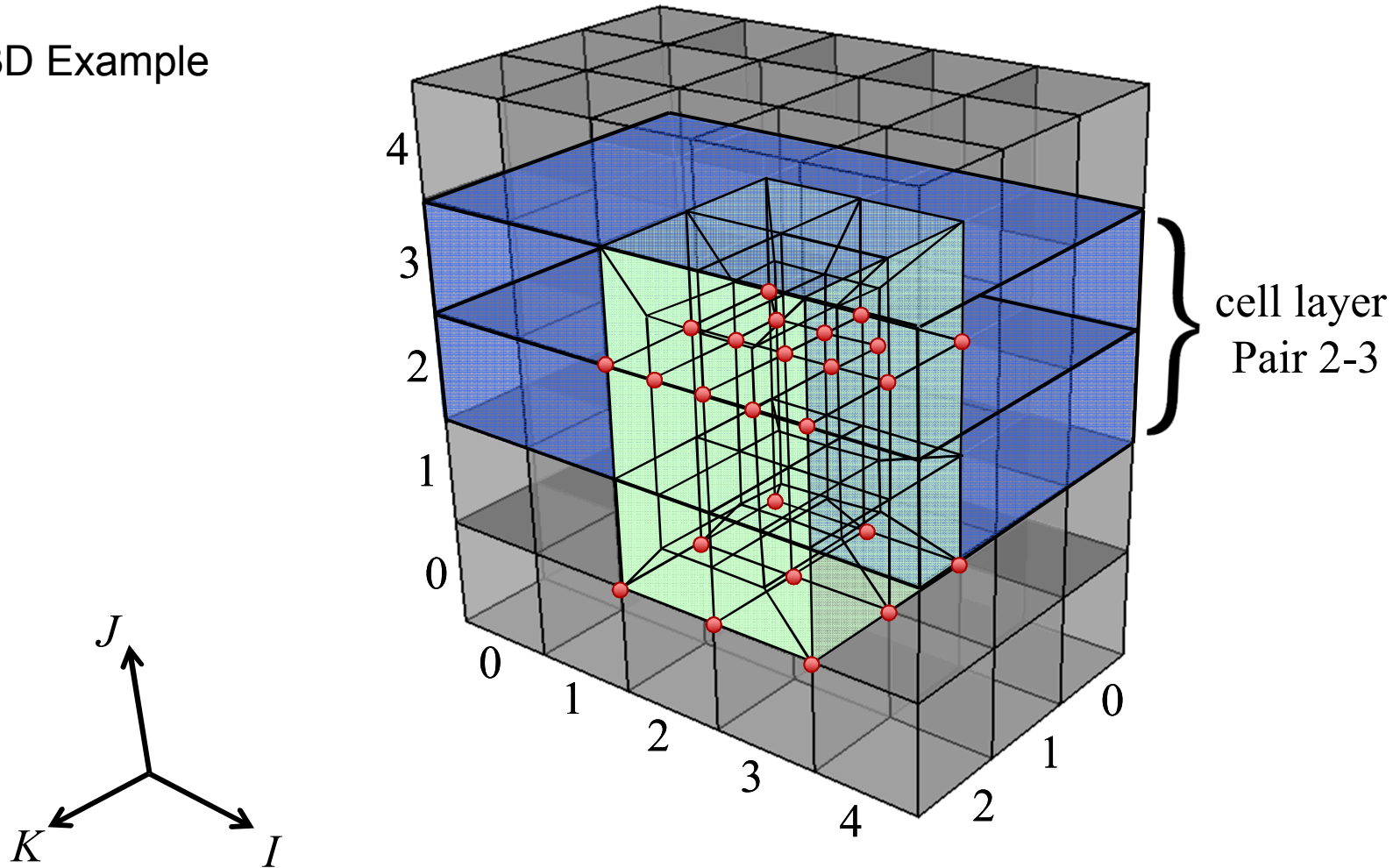
2-Refinement Procedure

3D Example



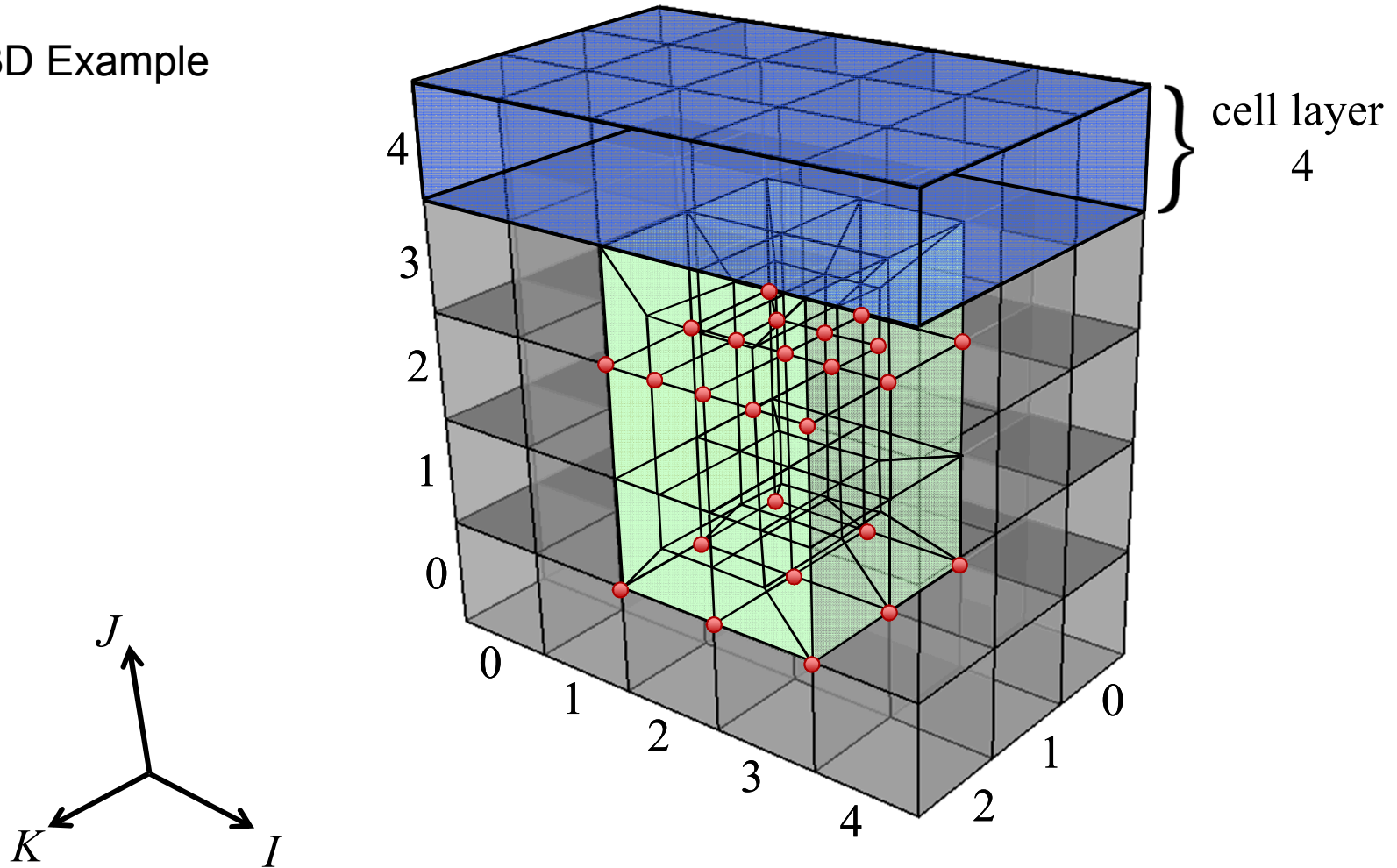
2-Refinement Procedure

3D Example



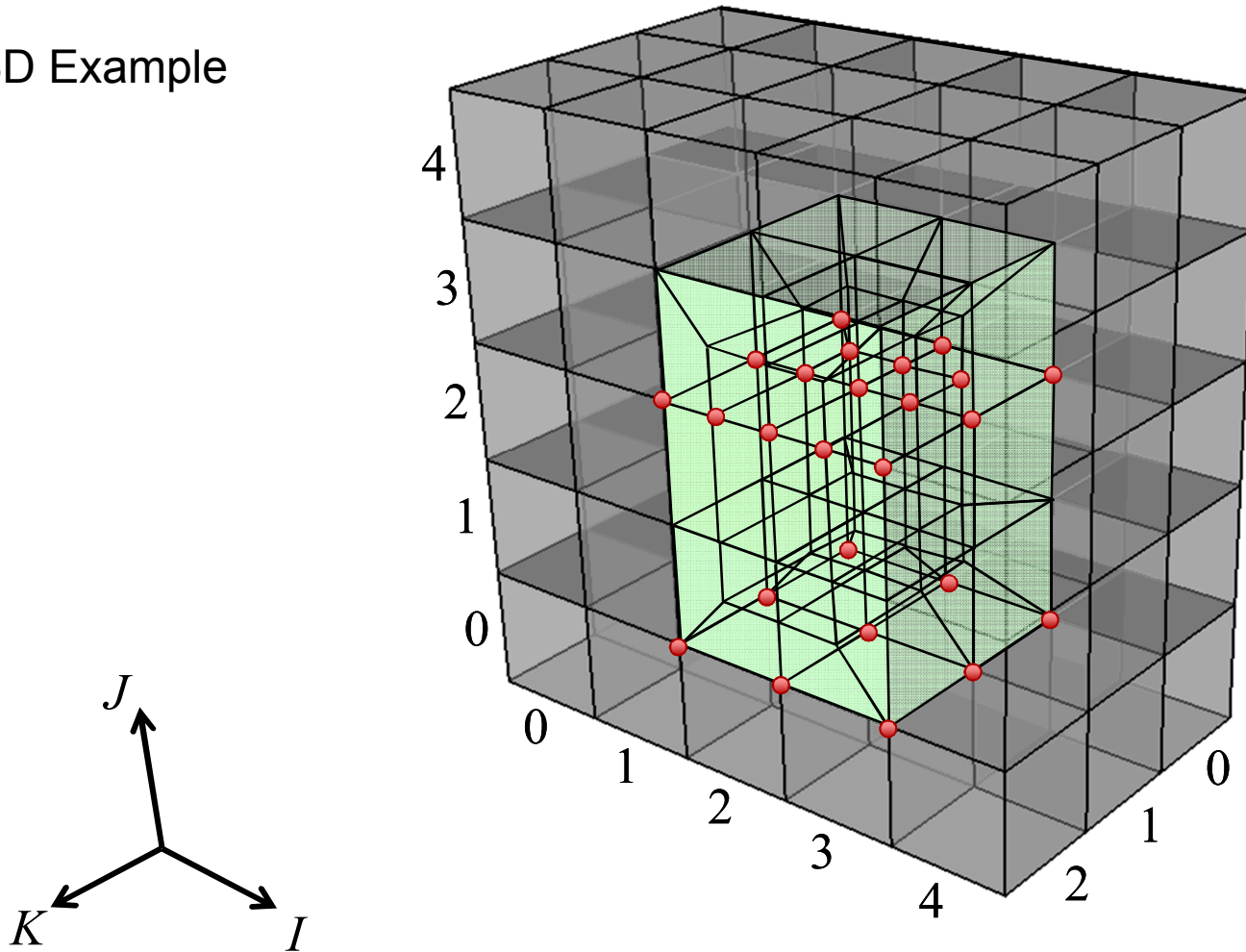
2-Refinement Procedure

3D Example



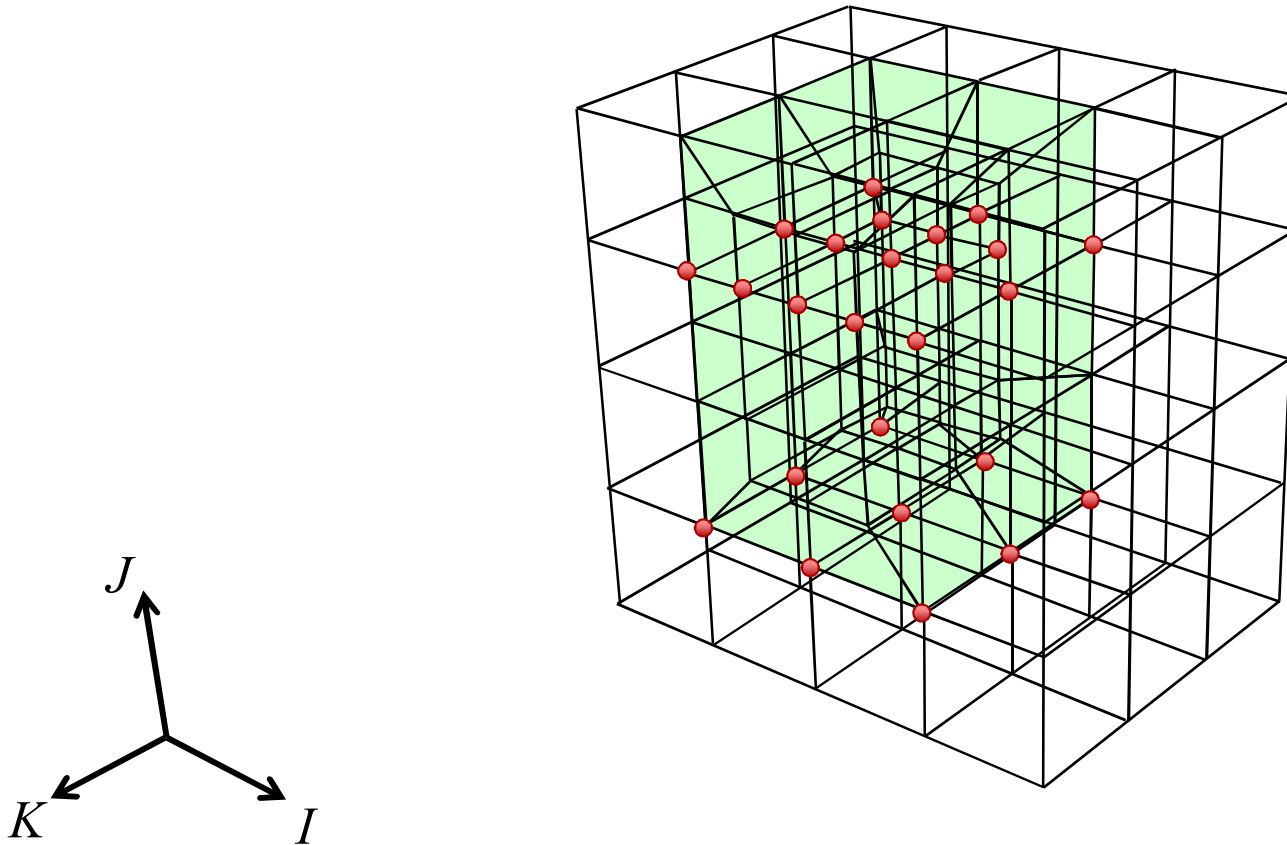
2-Refinement Procedure

3D Example



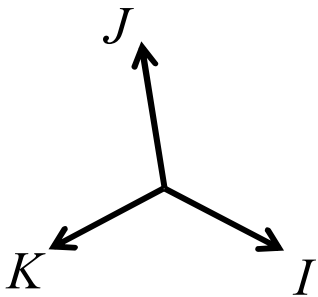
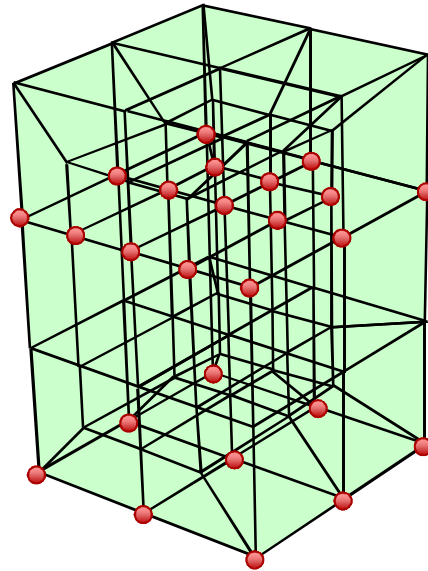
2-Refinement Procedure

3D Example



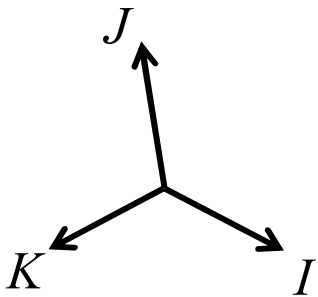
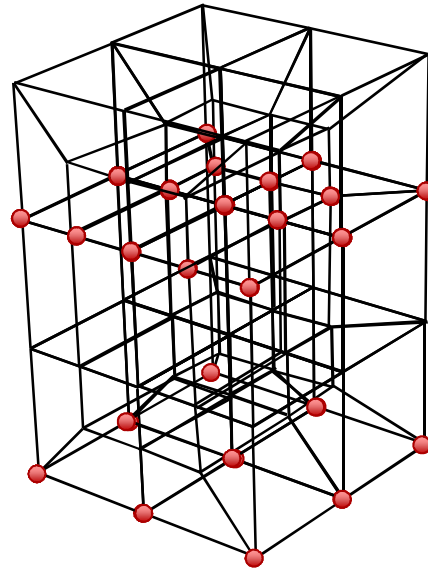
2-Refinement Procedure

3D Example



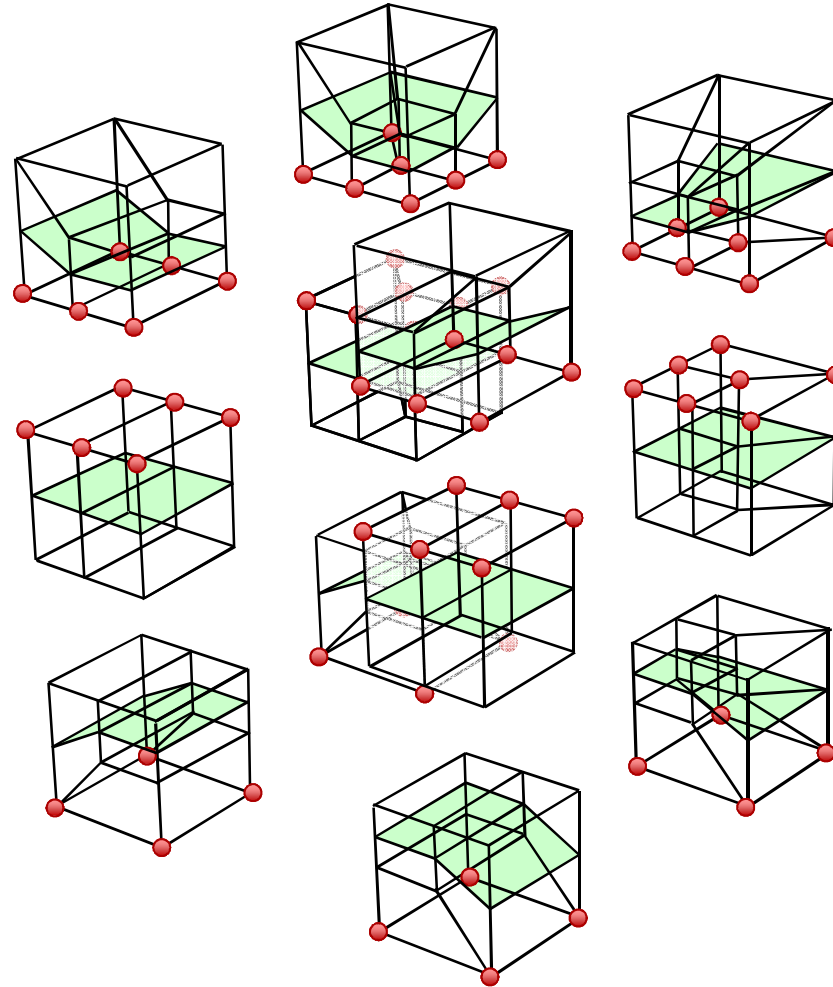
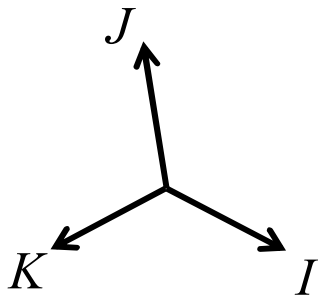
2-Refinement Procedure

3D Example



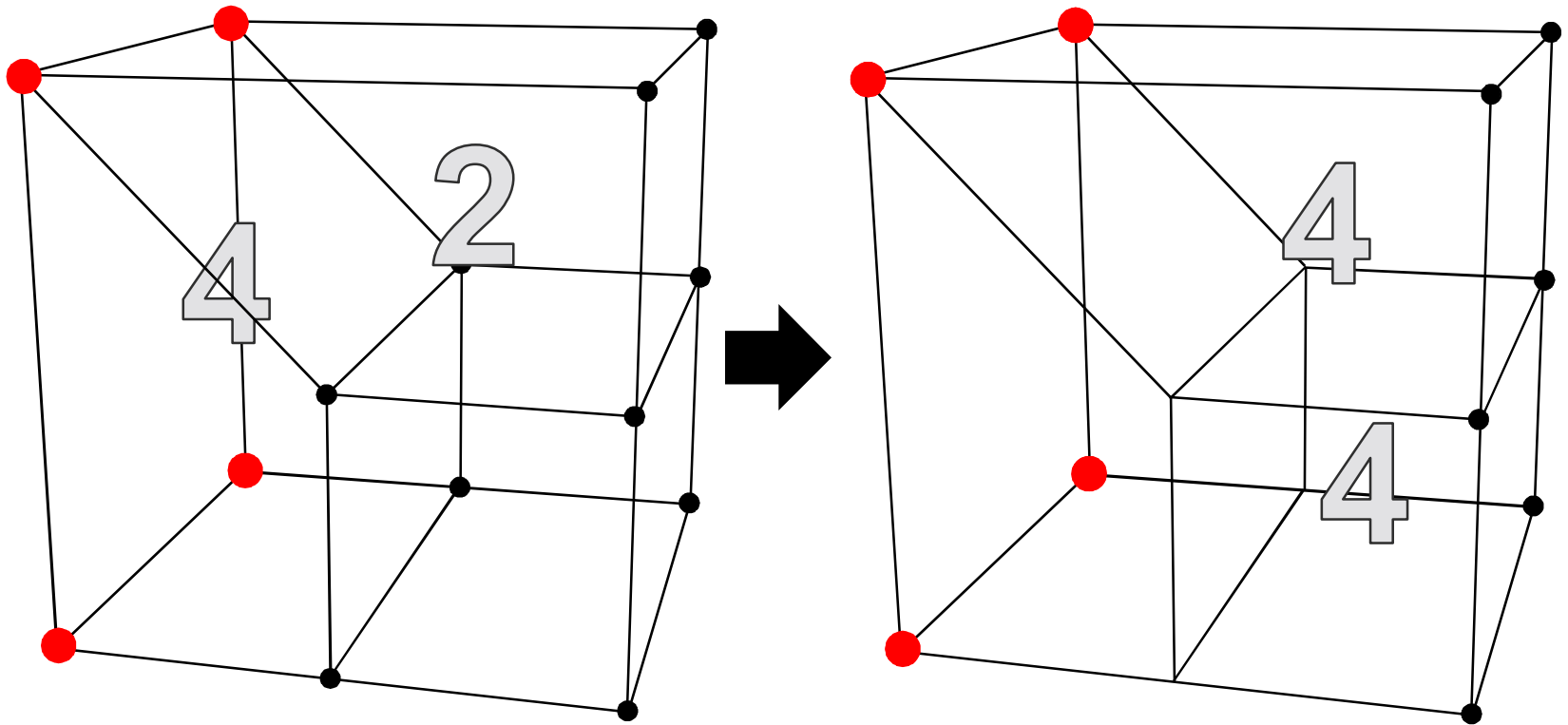
2-Refinement Procedure

3D Example



Node Marking Propagation

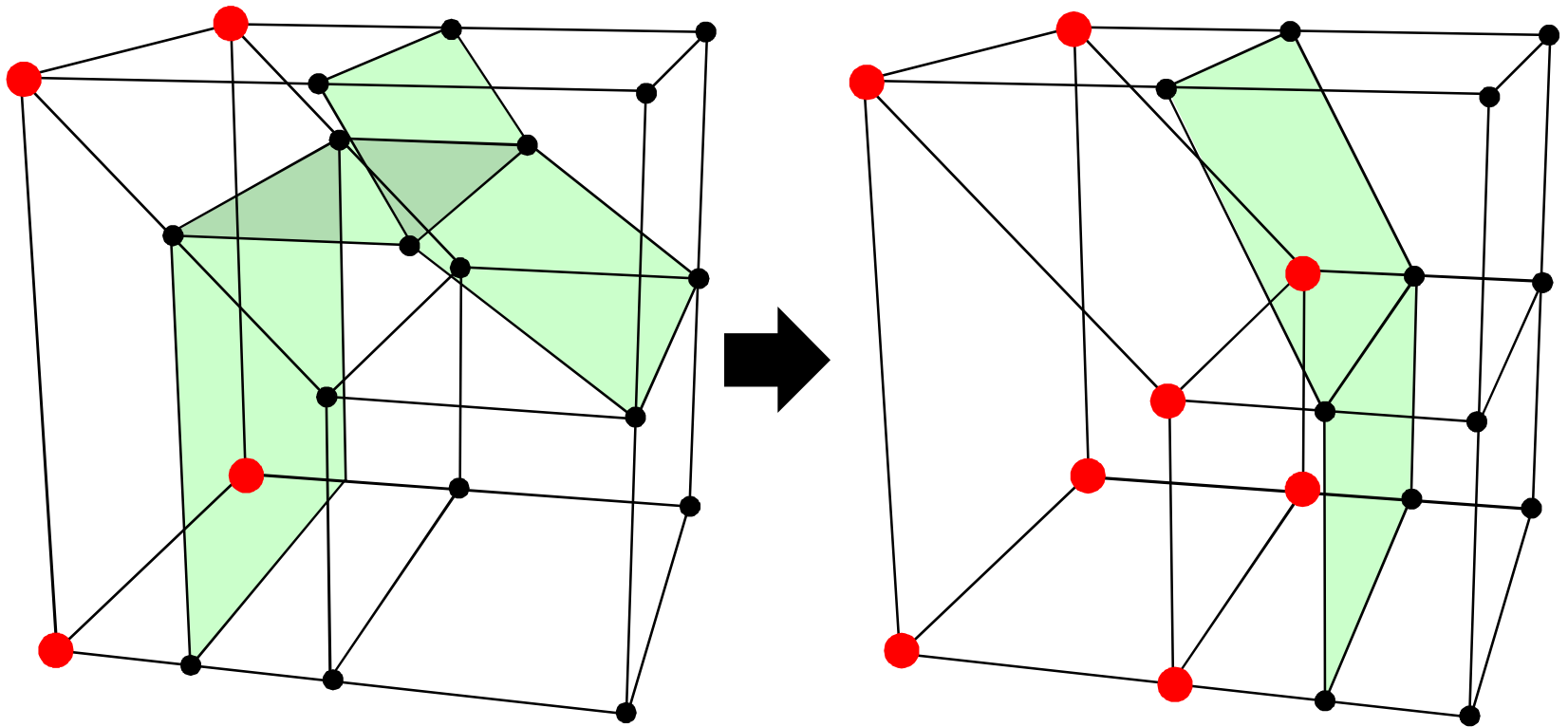
3D Example



From Refined *2-Template*

Node Marking Propagation

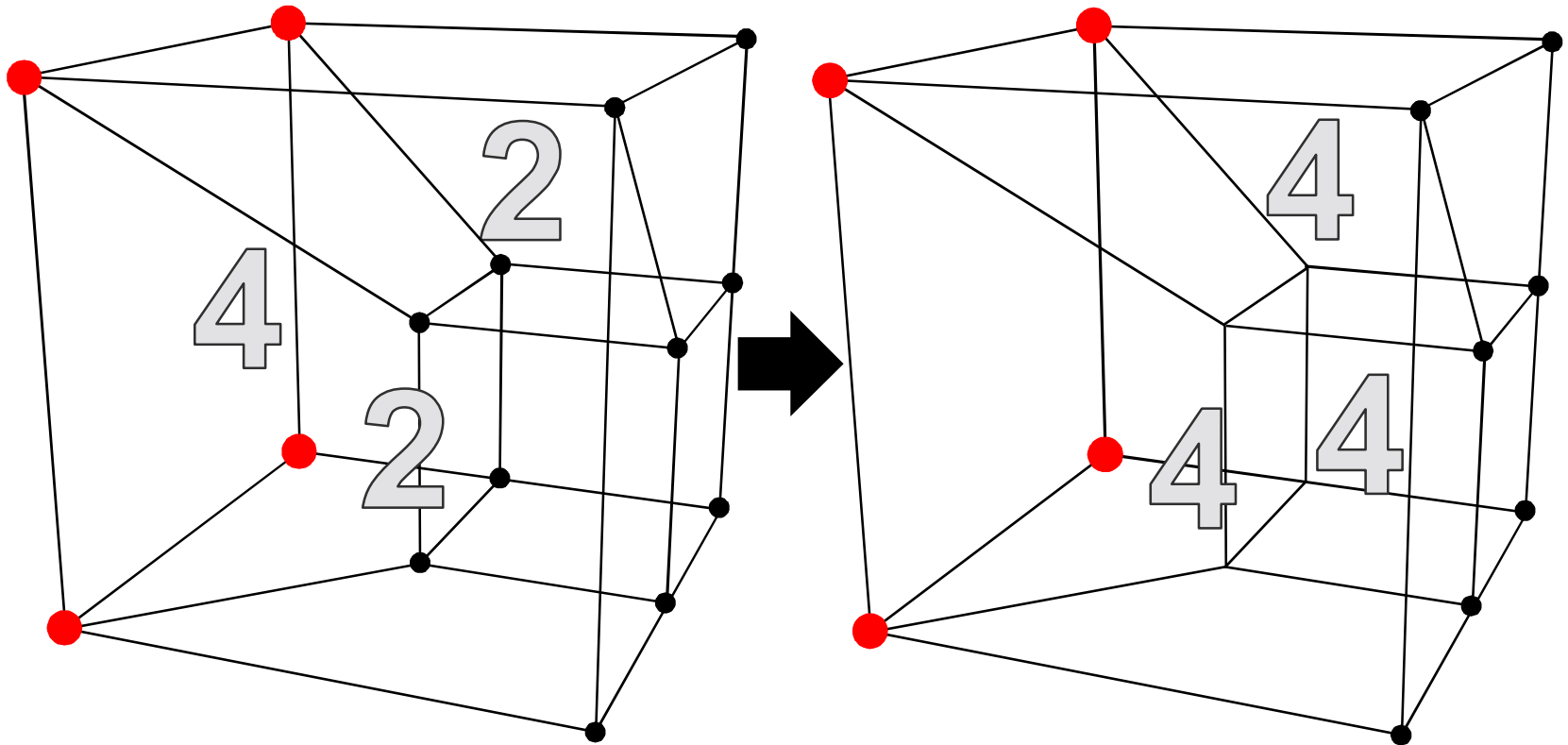
3D Example



From Refined *2-Template*

Node Marking Propagation

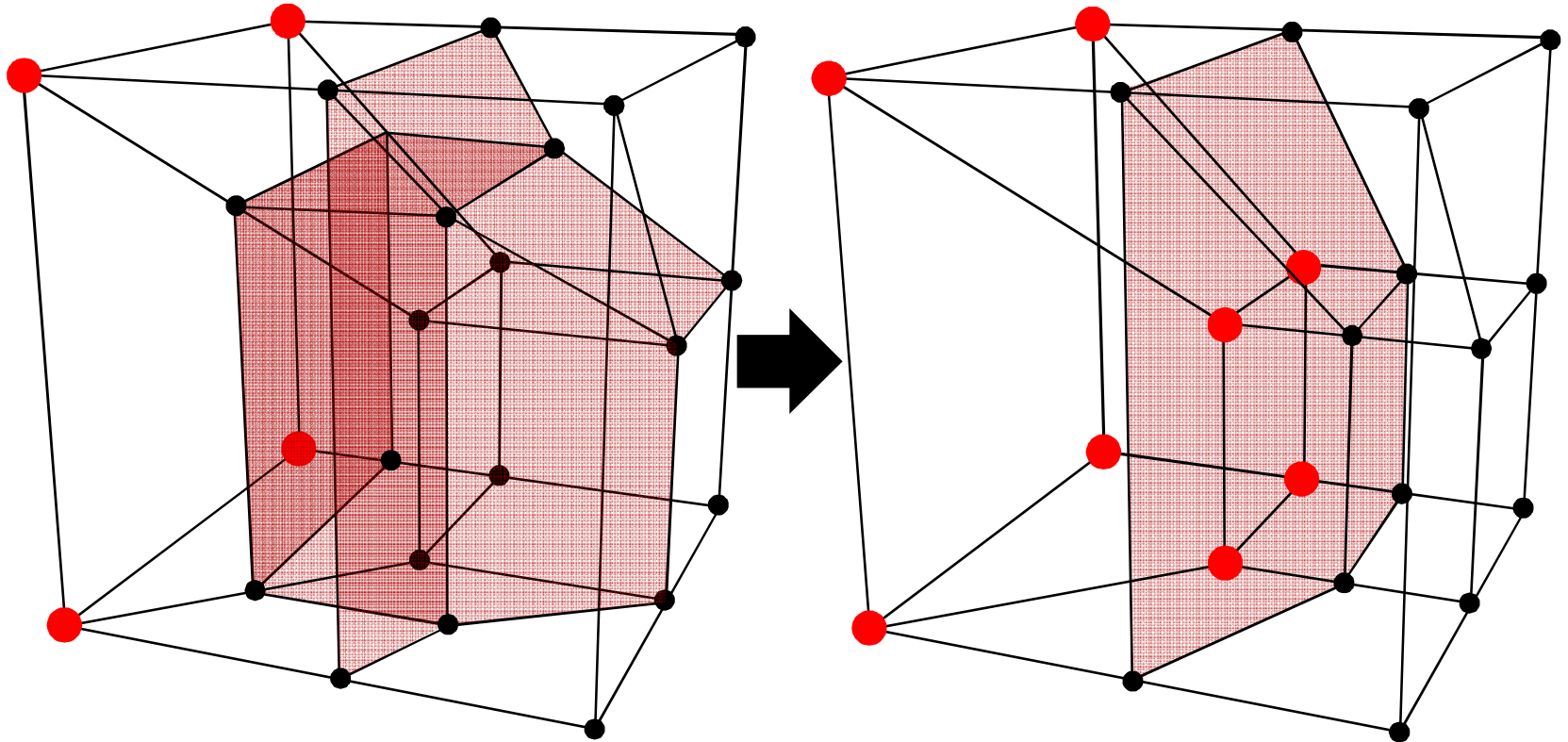
3D Example



From Refined *1-Template*

Node Marking Propagation

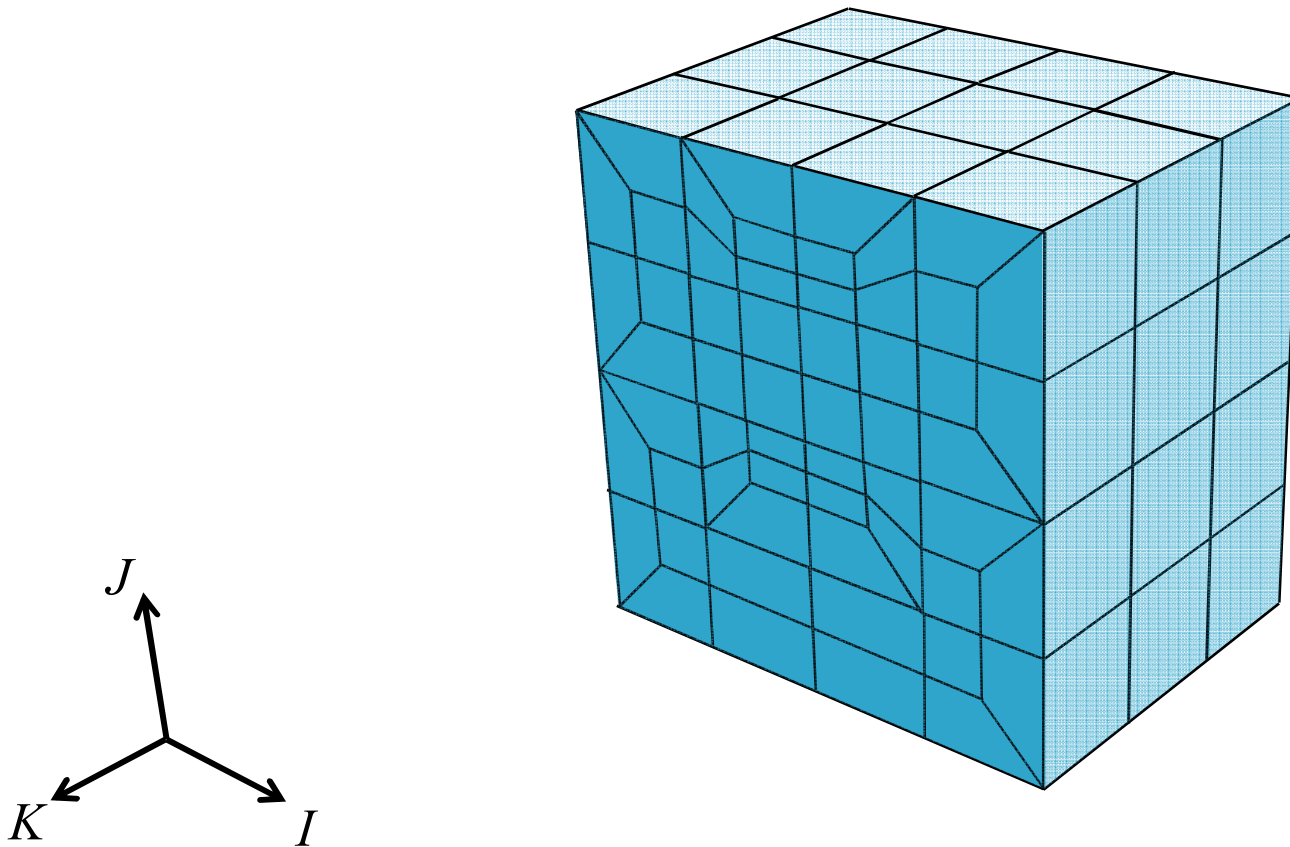
3D Example



From Refined *1-Template*

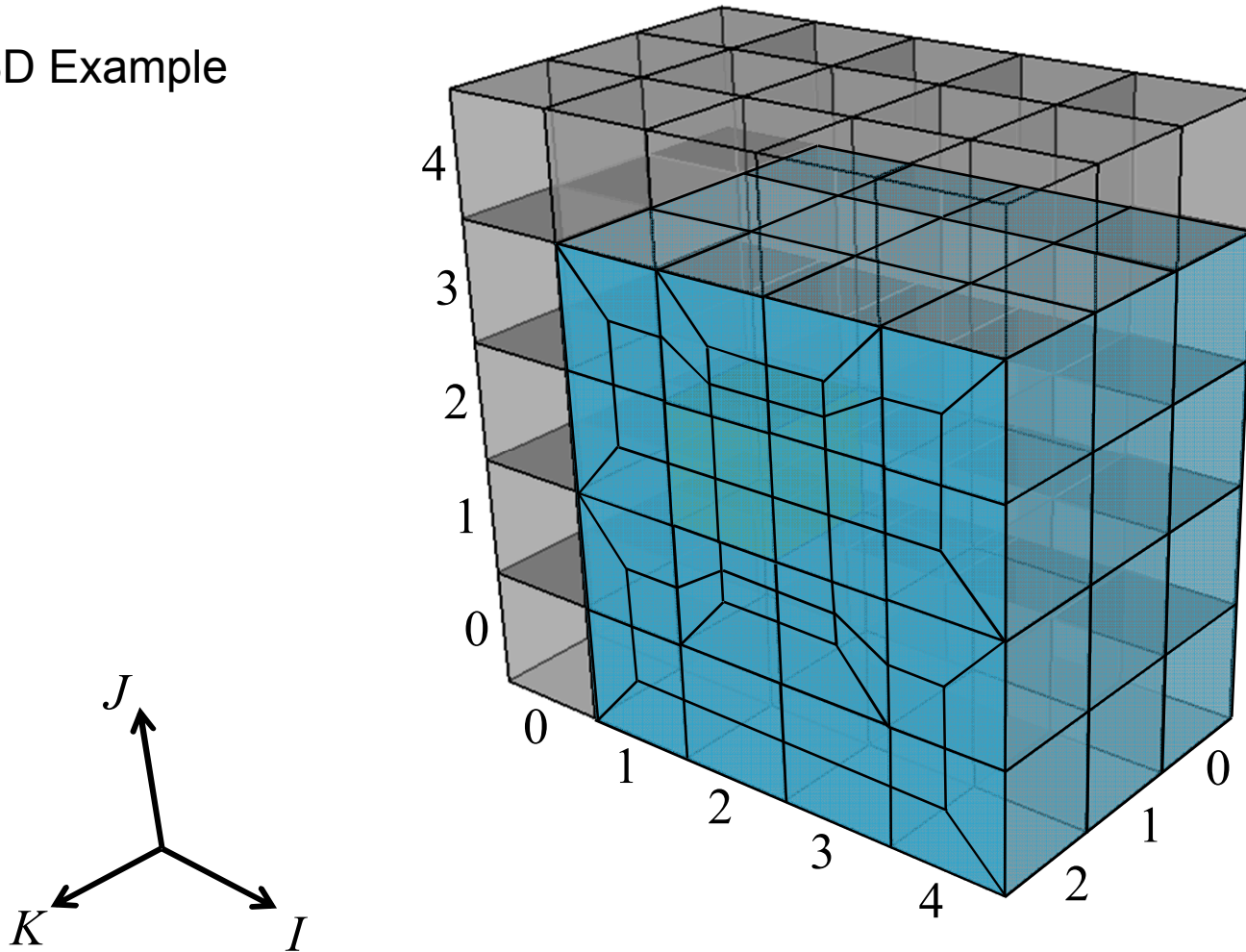
2-Refinement Procedure

3D Example



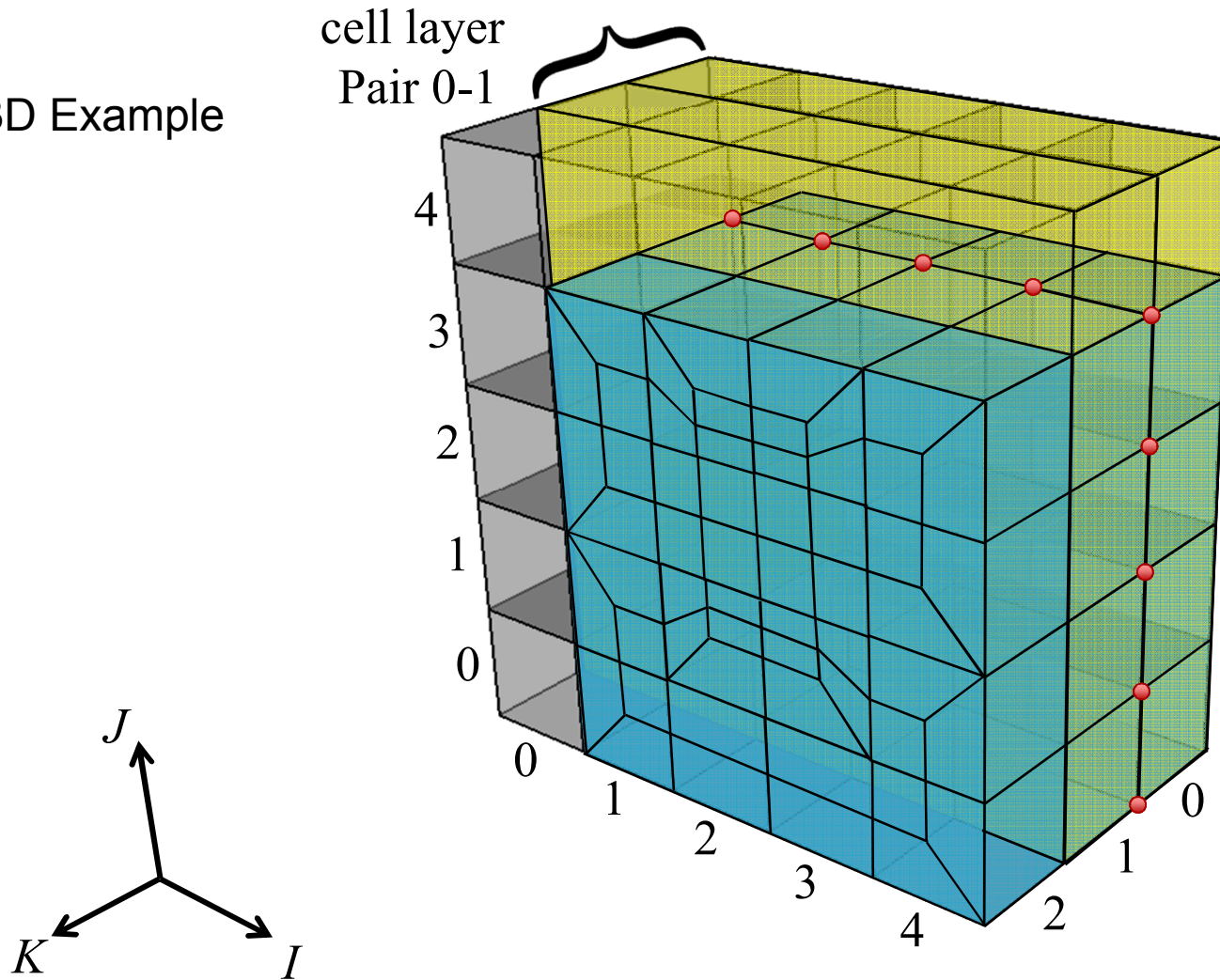
2-Refinement Procedure

3D Example



2-Refinement Procedure

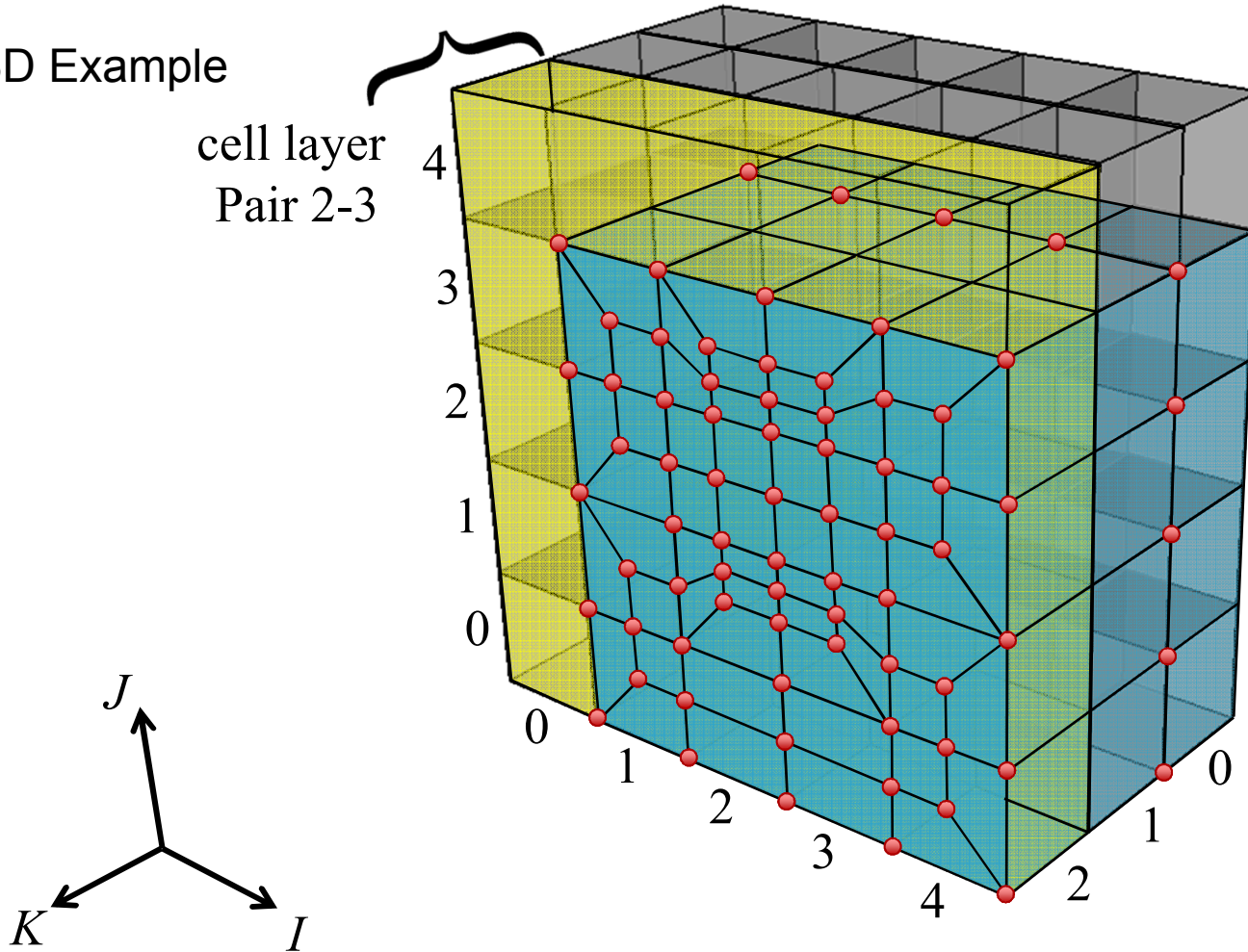
3D Example



2-Refinement Procedure

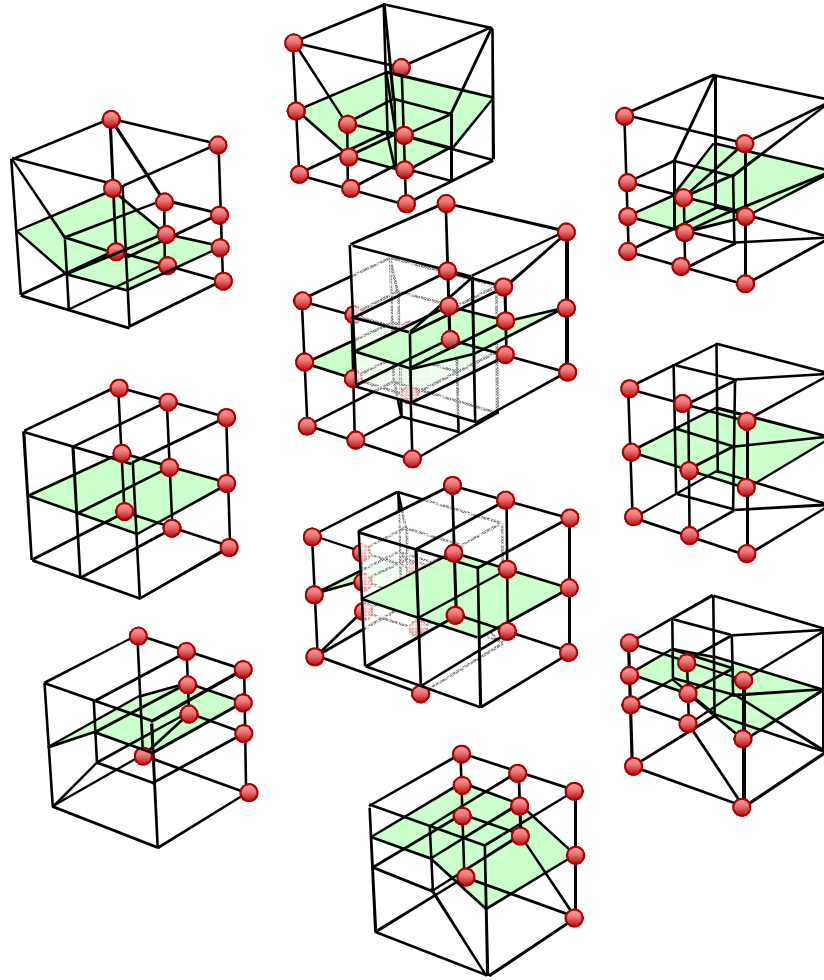
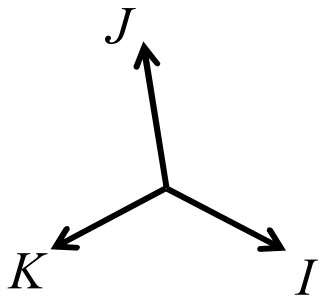
3D Example

cell layer
Pair 2-3



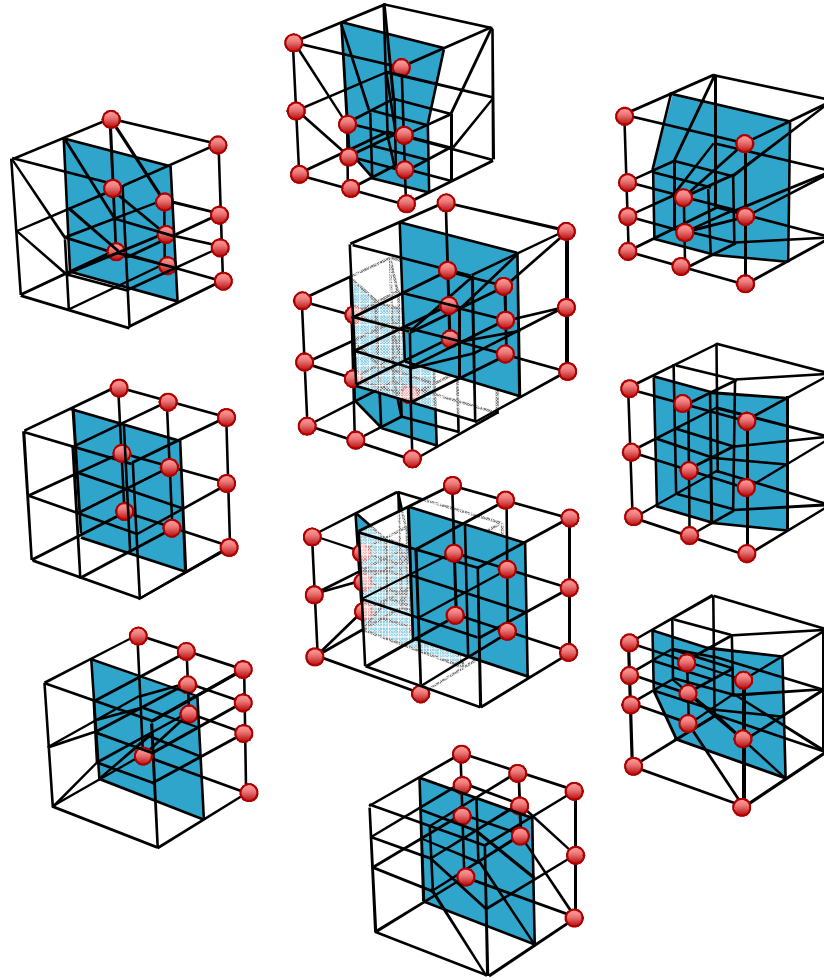
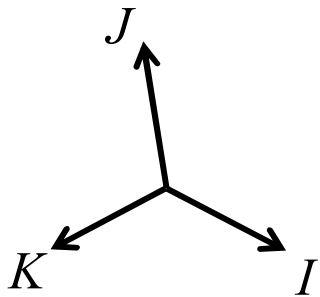
2-Refinement Procedure

3D Example



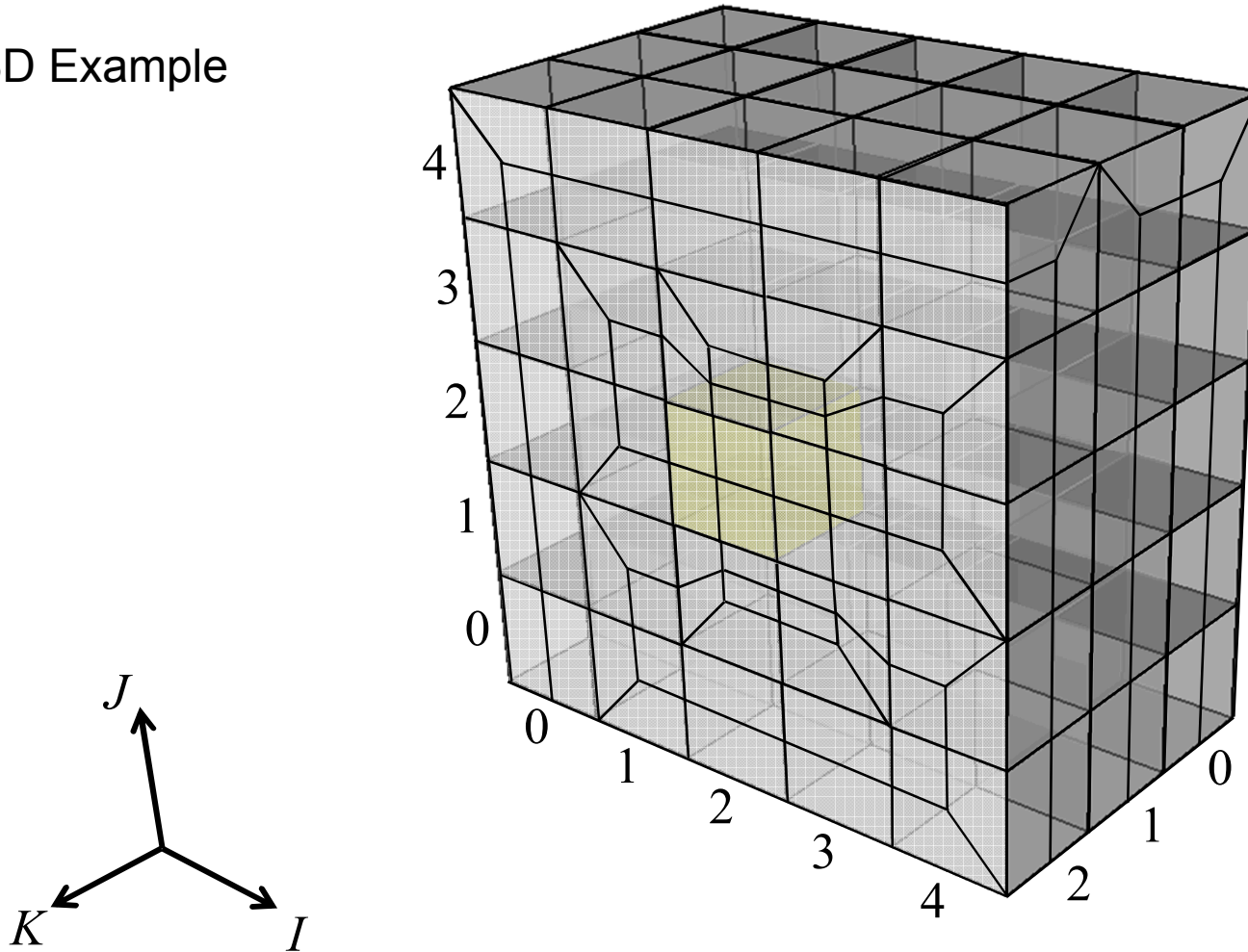
2-Refinement Procedure

3D Example

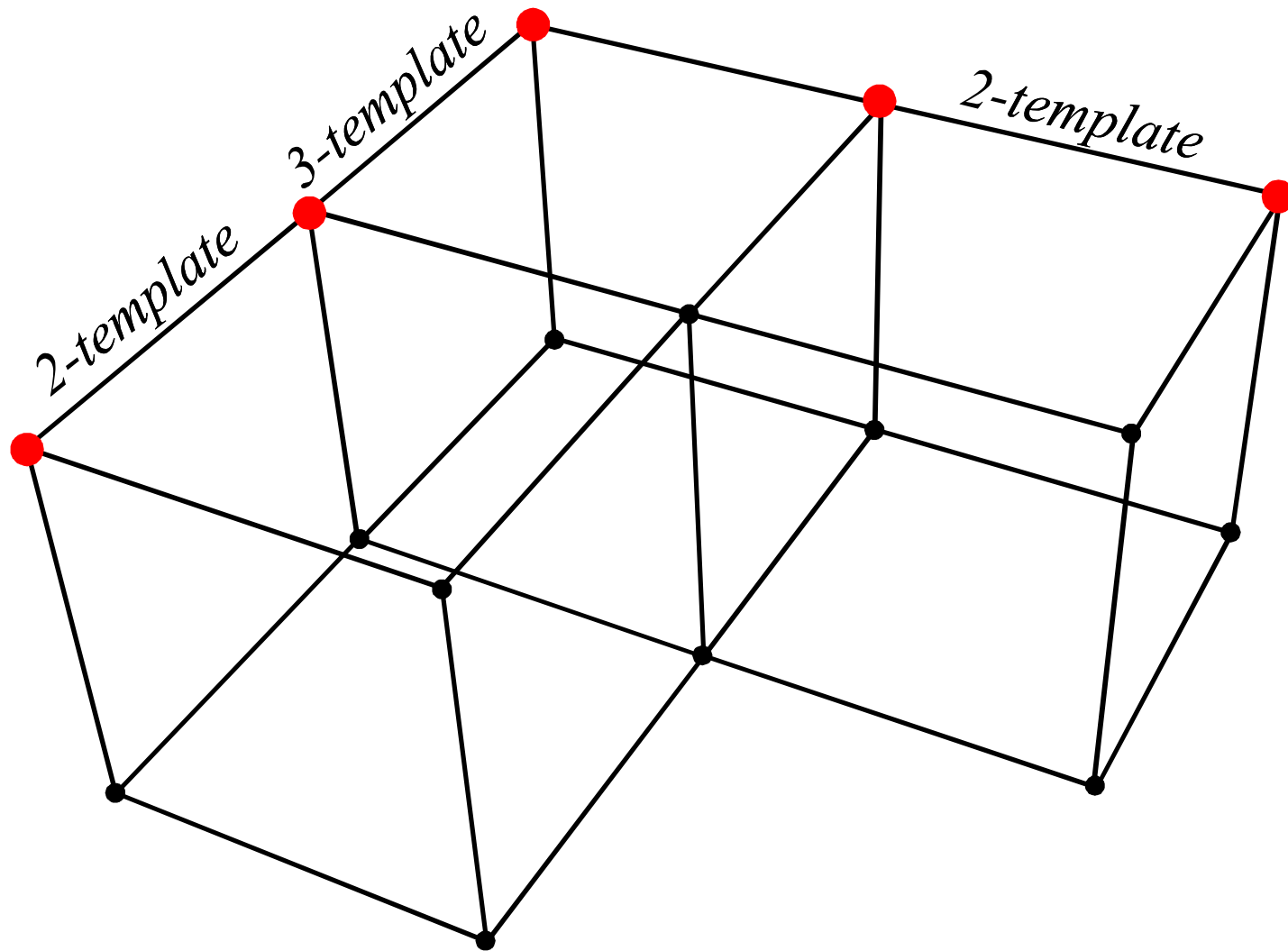


2-Refinement Procedure

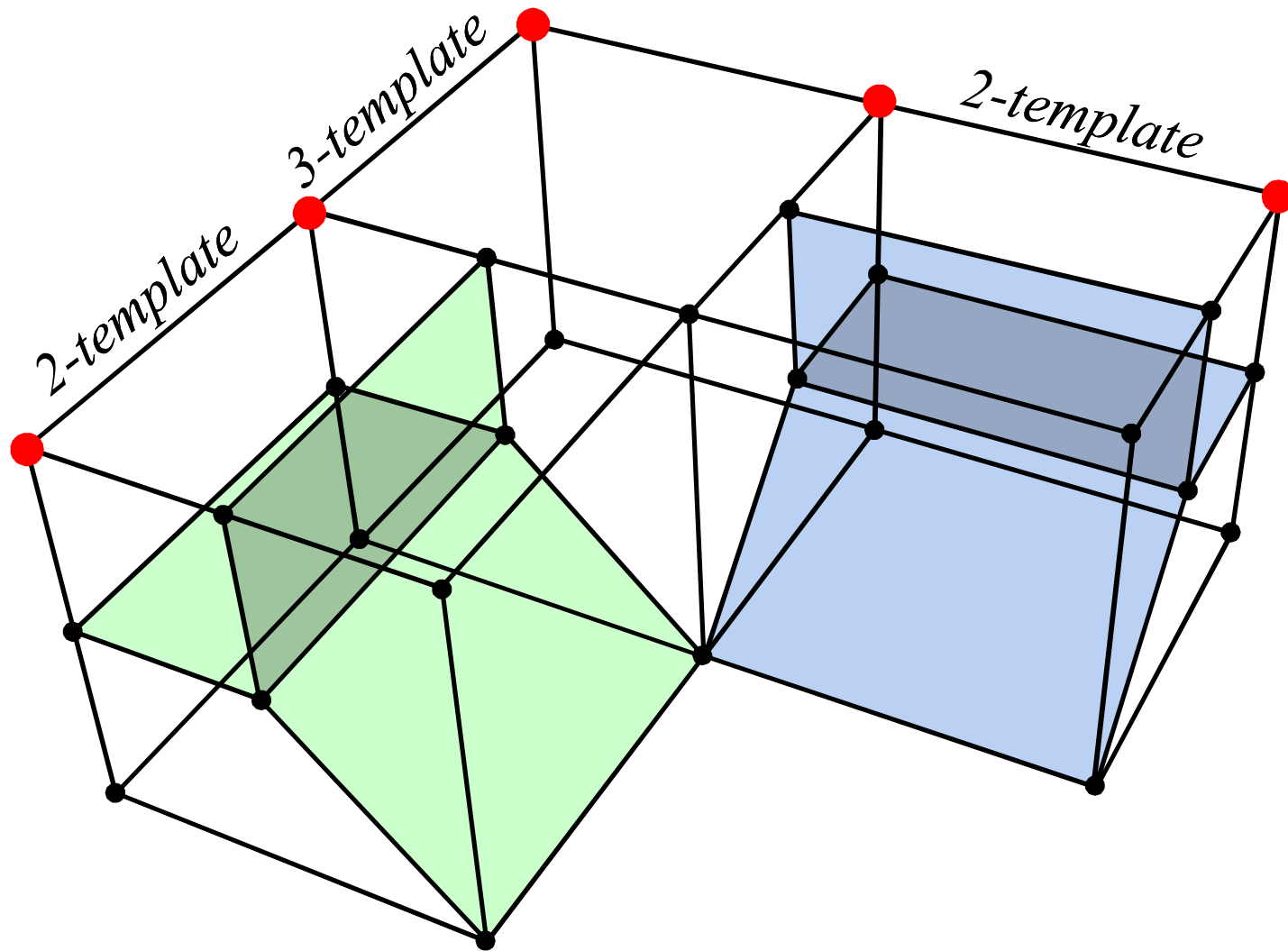
3D Example



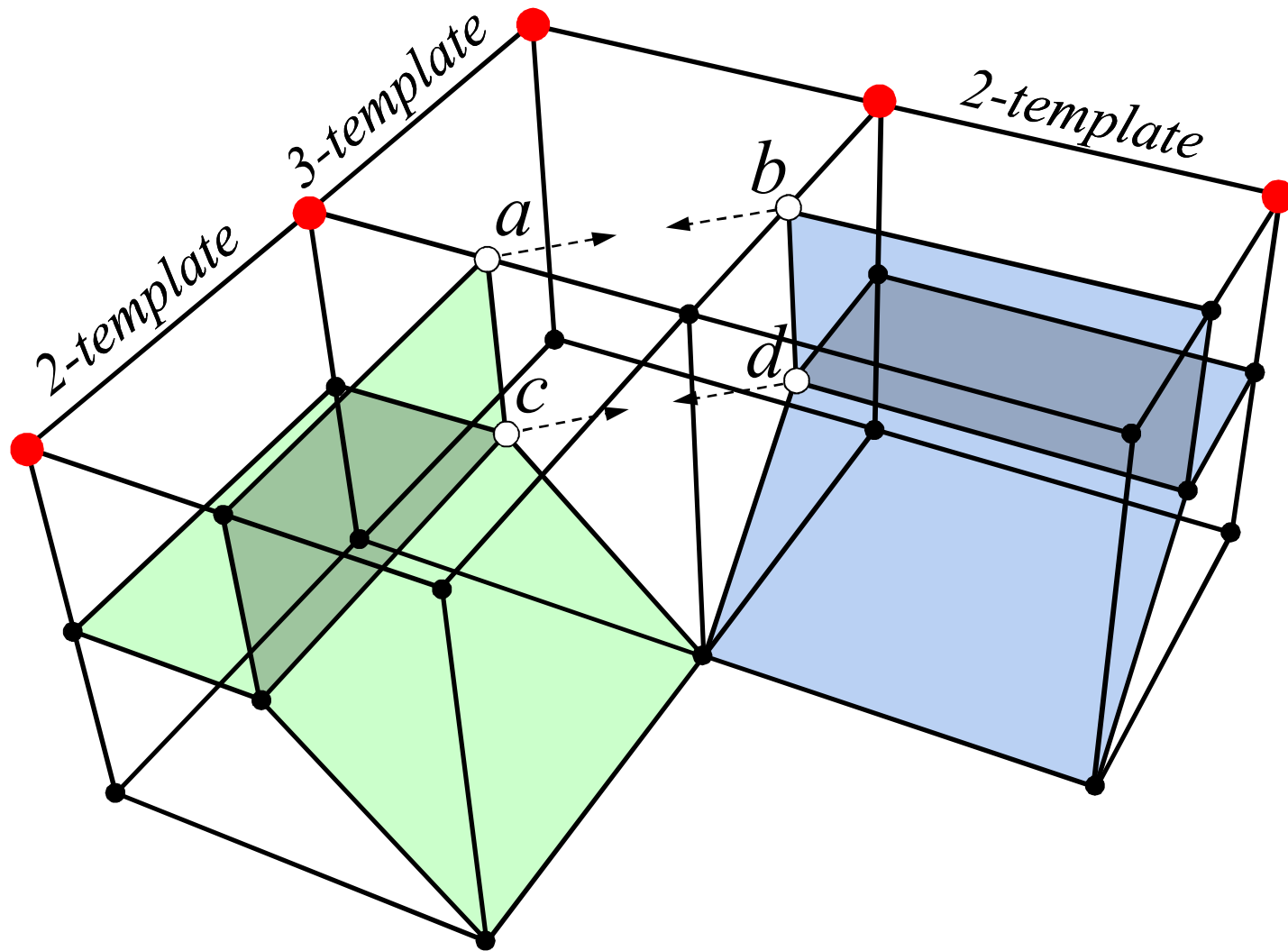
3-Template



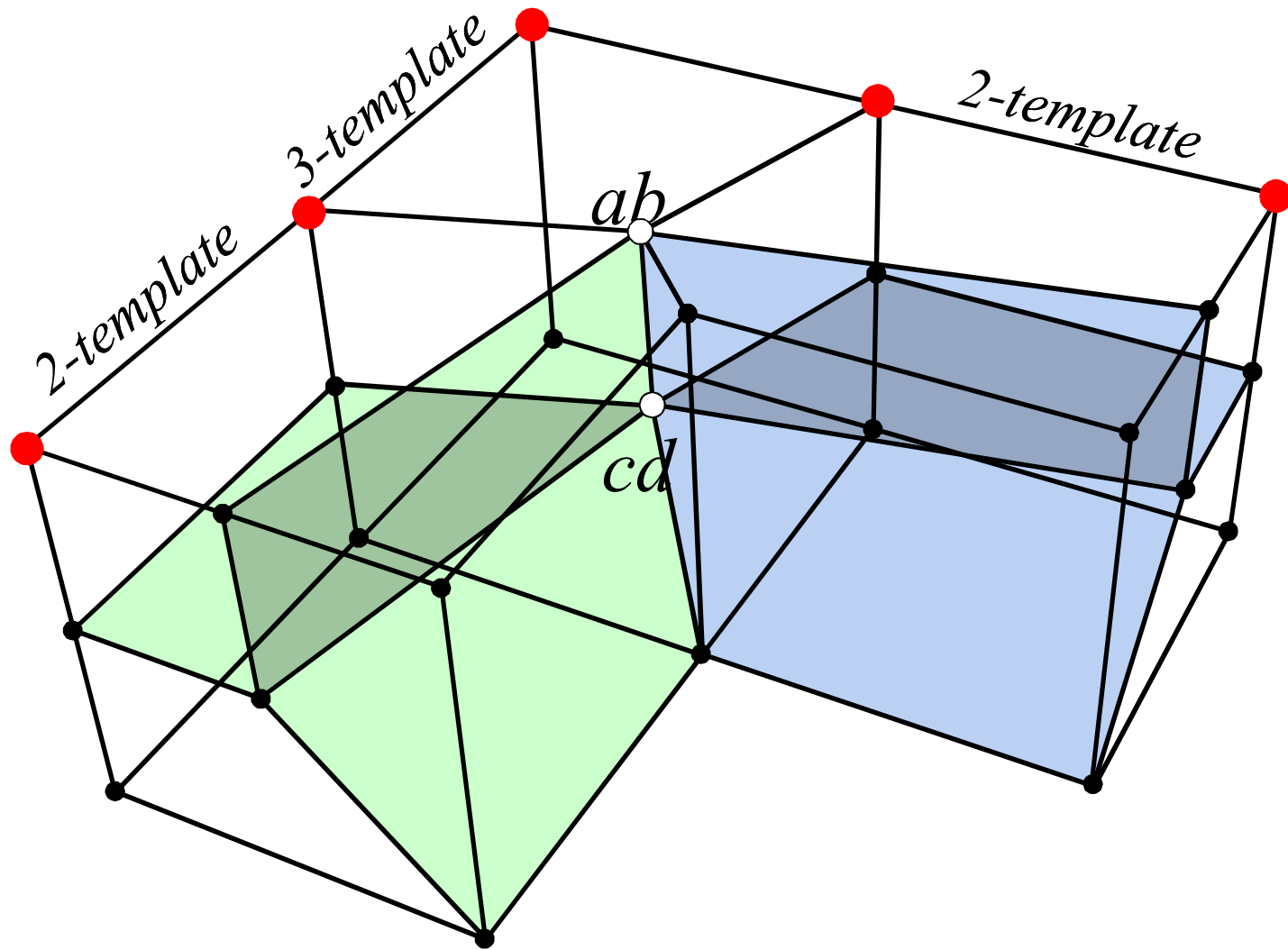
3-Template



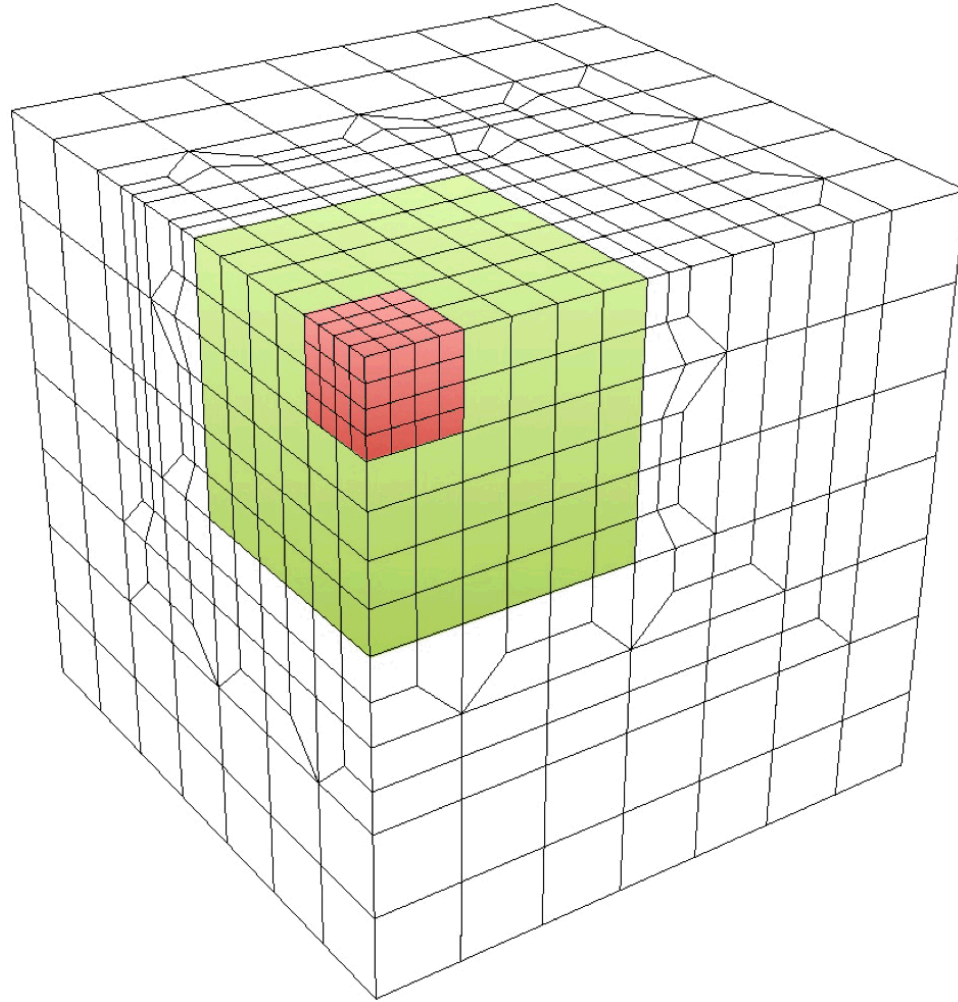
3-Template



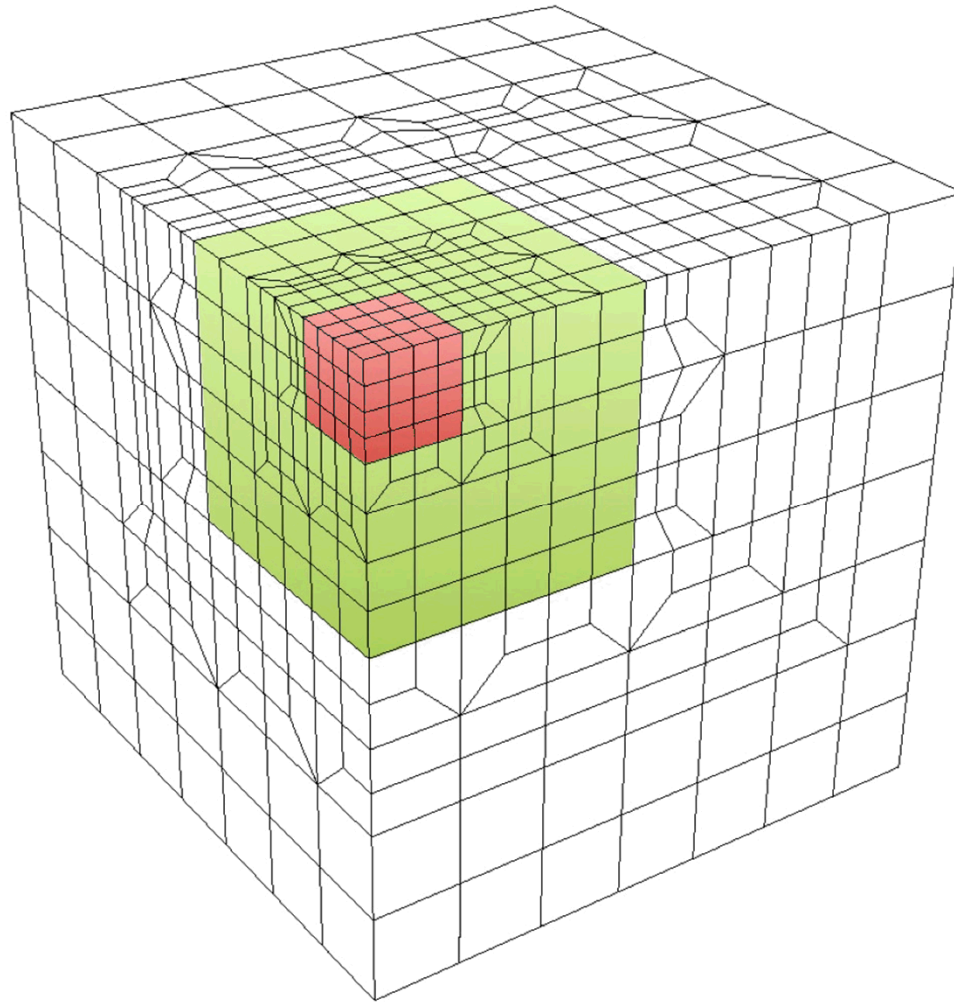
3-Template



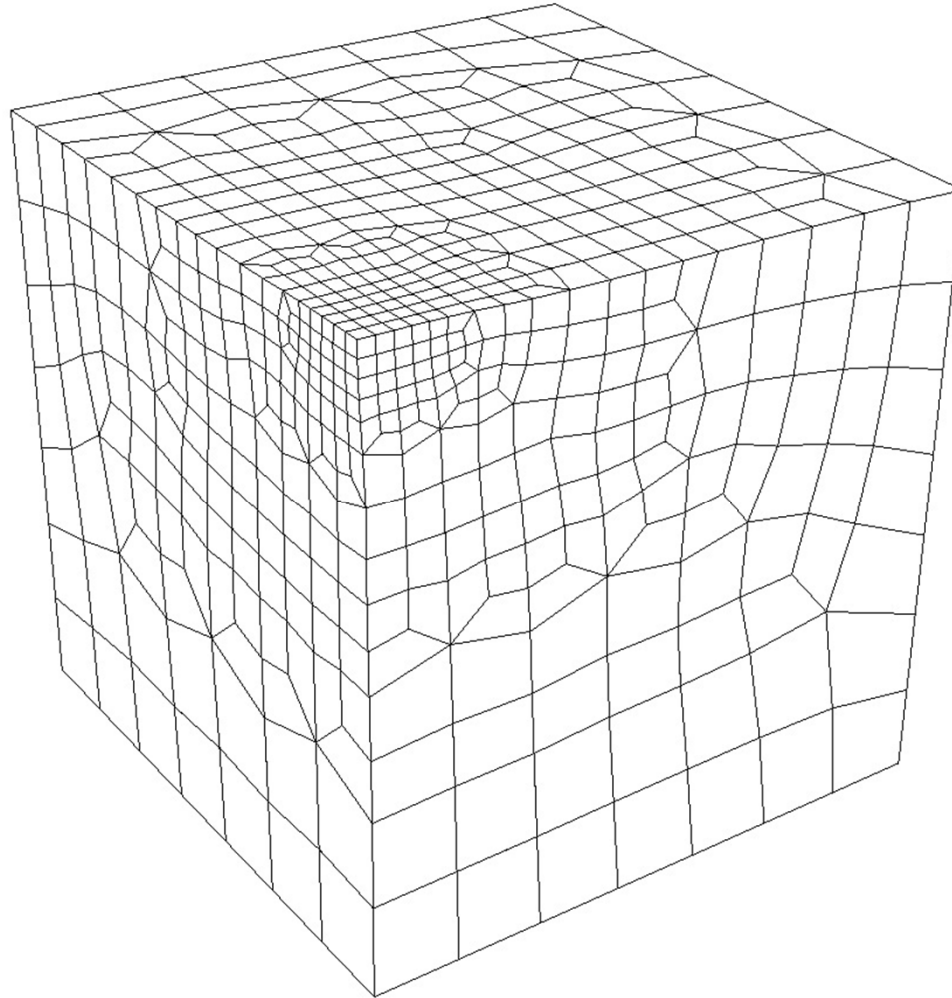
Multi-level Refinement



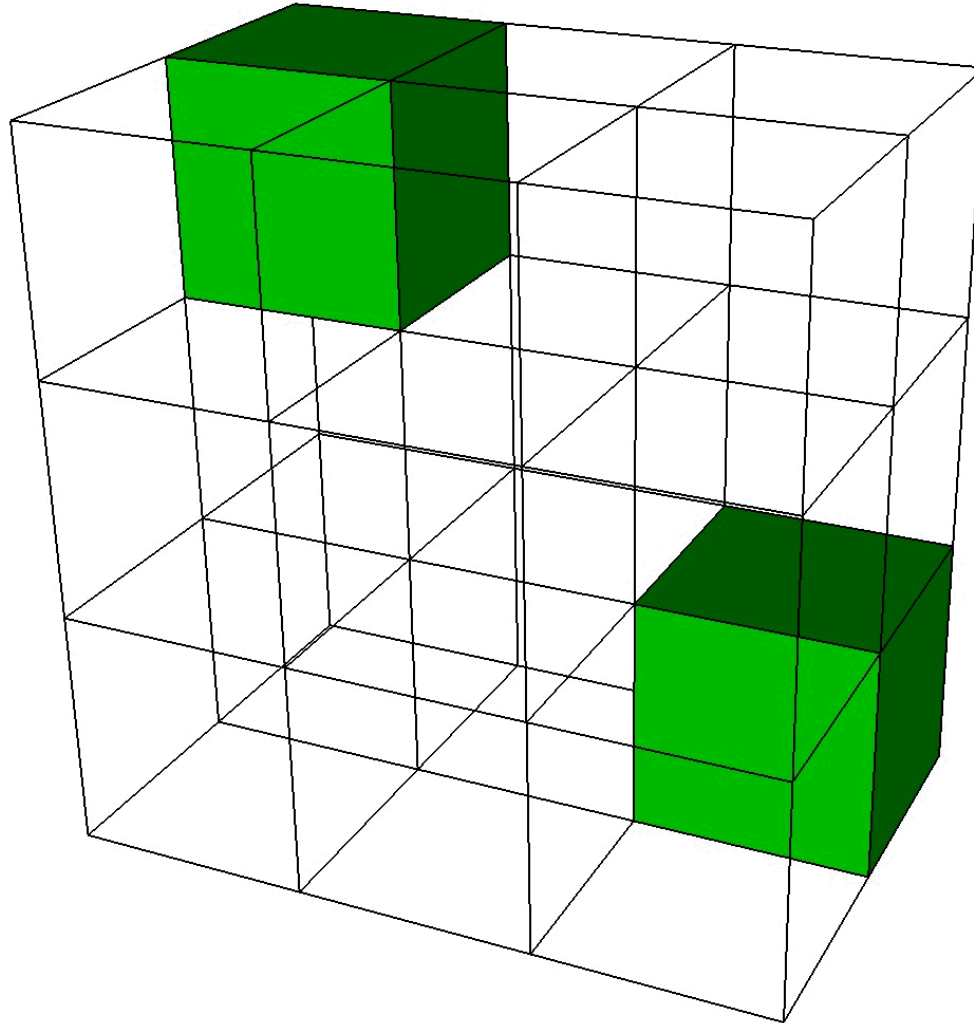
Multi-level Refinement



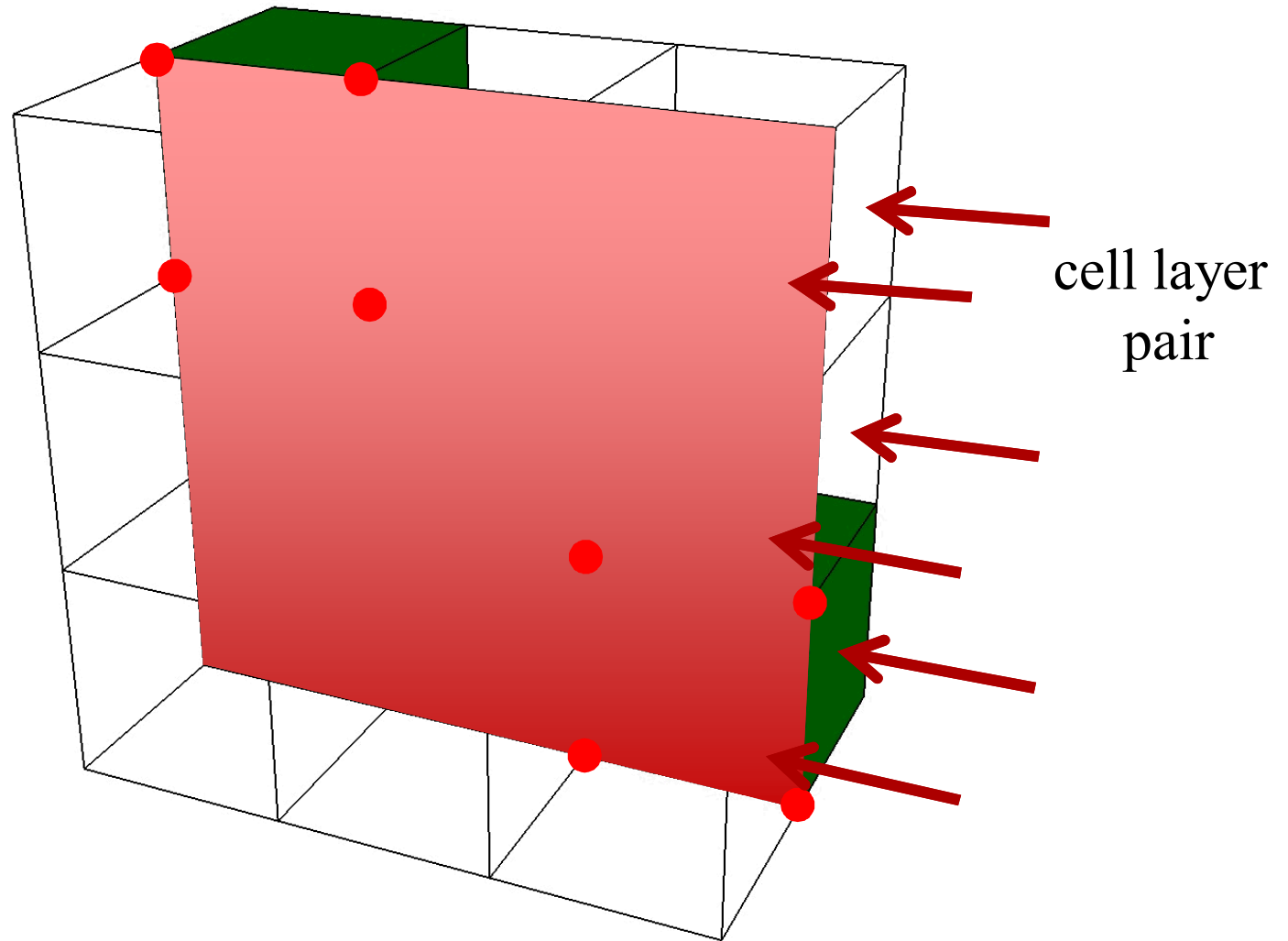
Multi-level Refinement



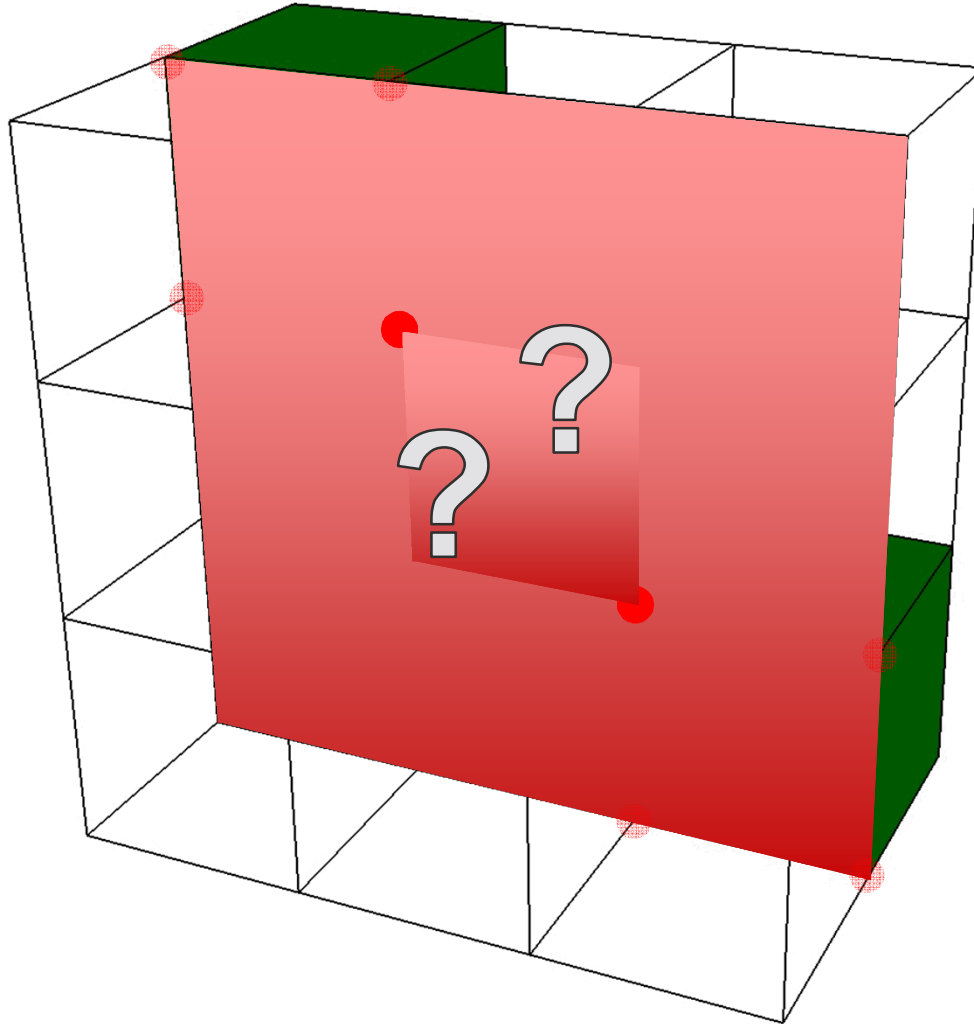
Additional 3D Node Marking



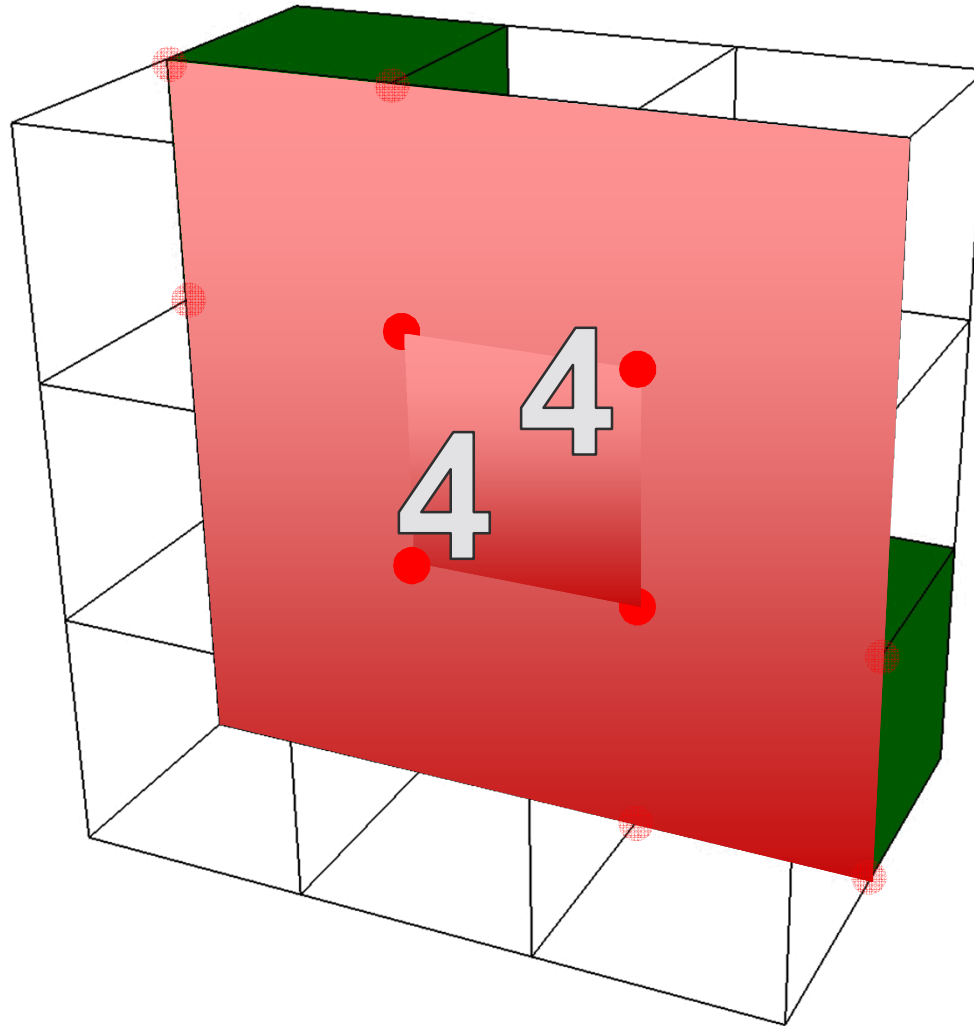
Additional 3D Node Marking



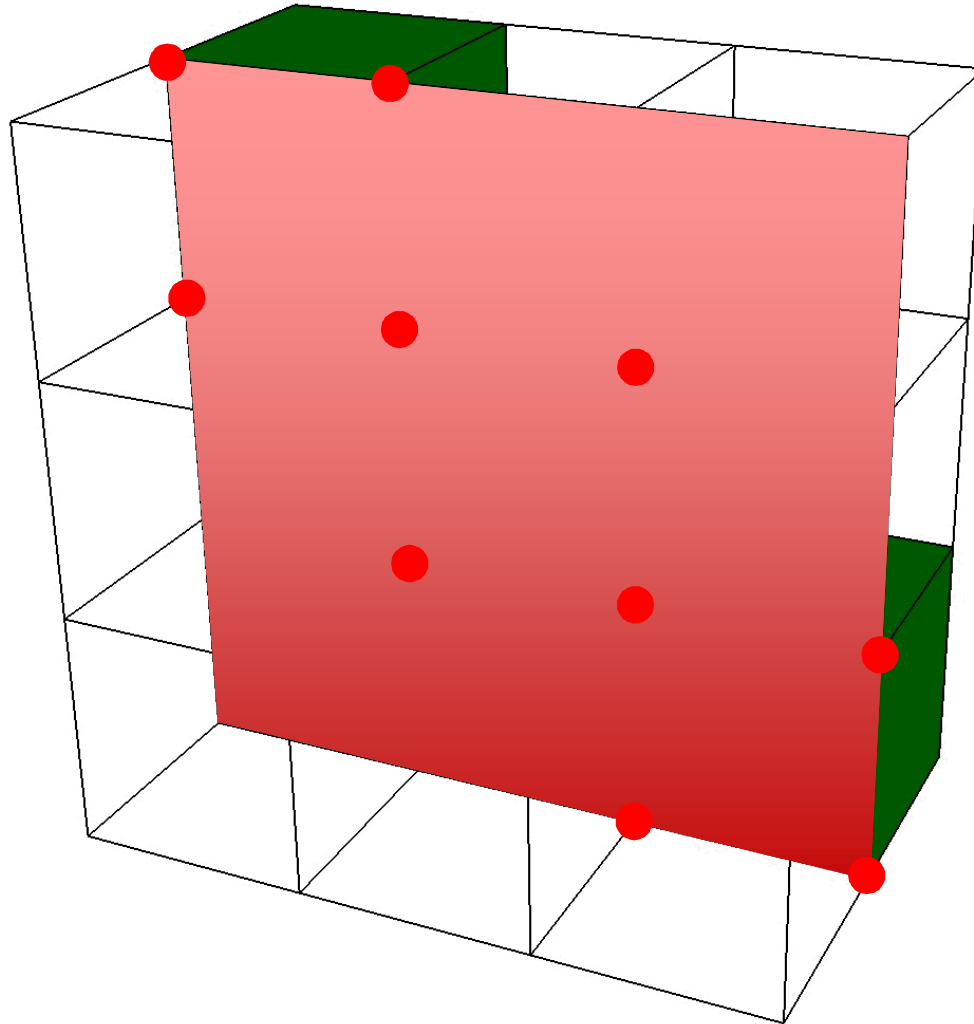
Additional 3D Node Marking



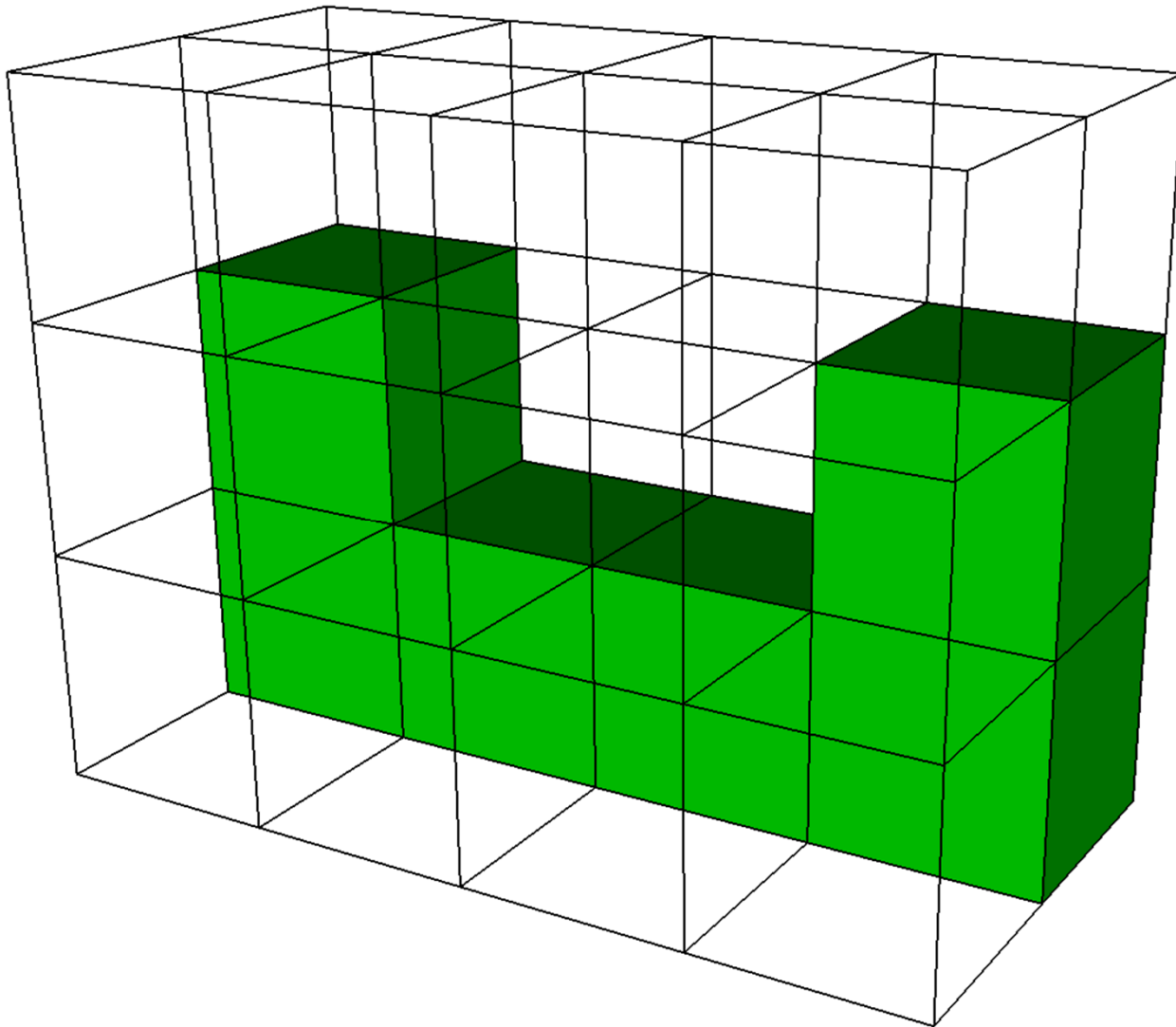
Additional 3D Node Marking



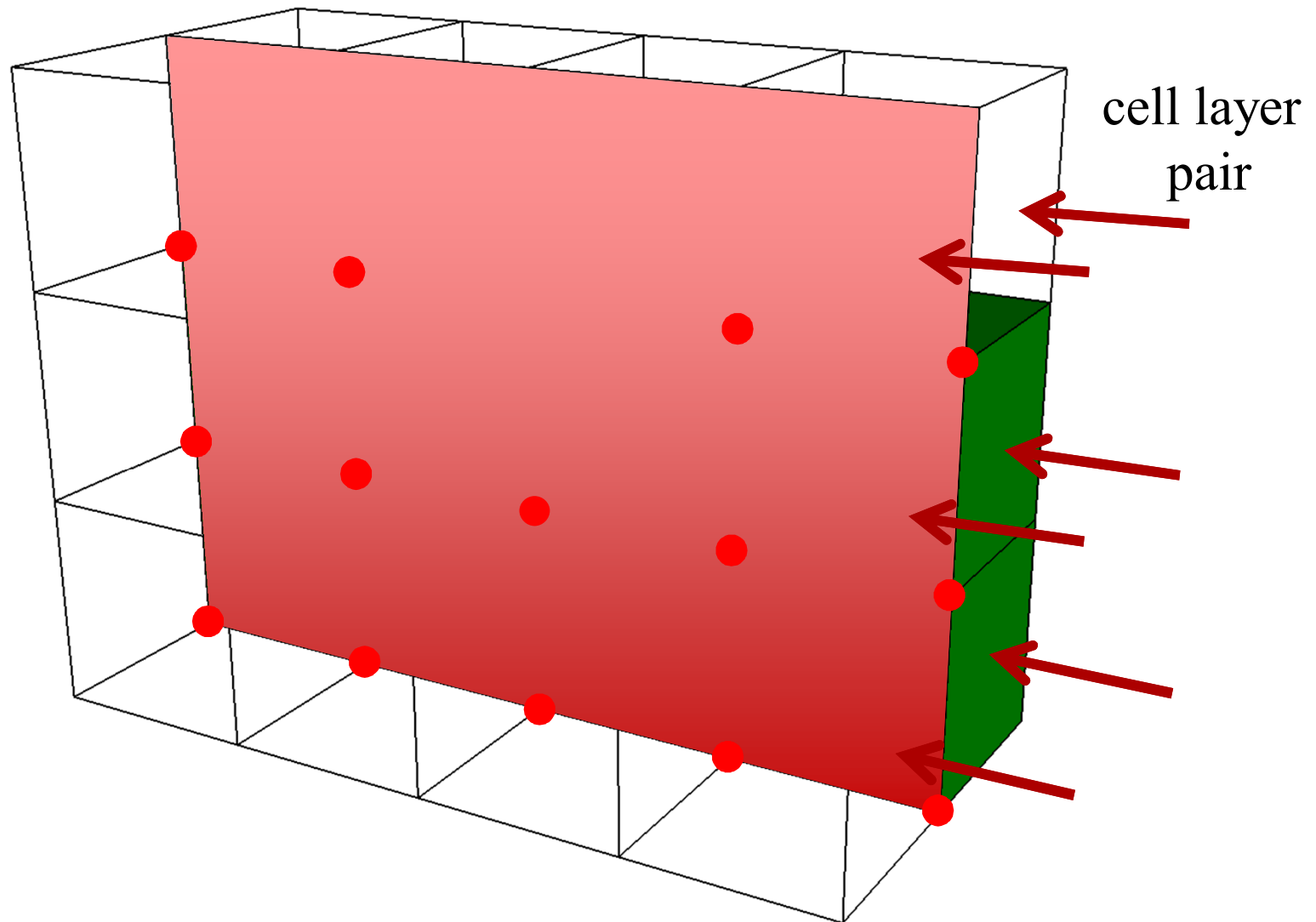
Additional 3D Node Marking



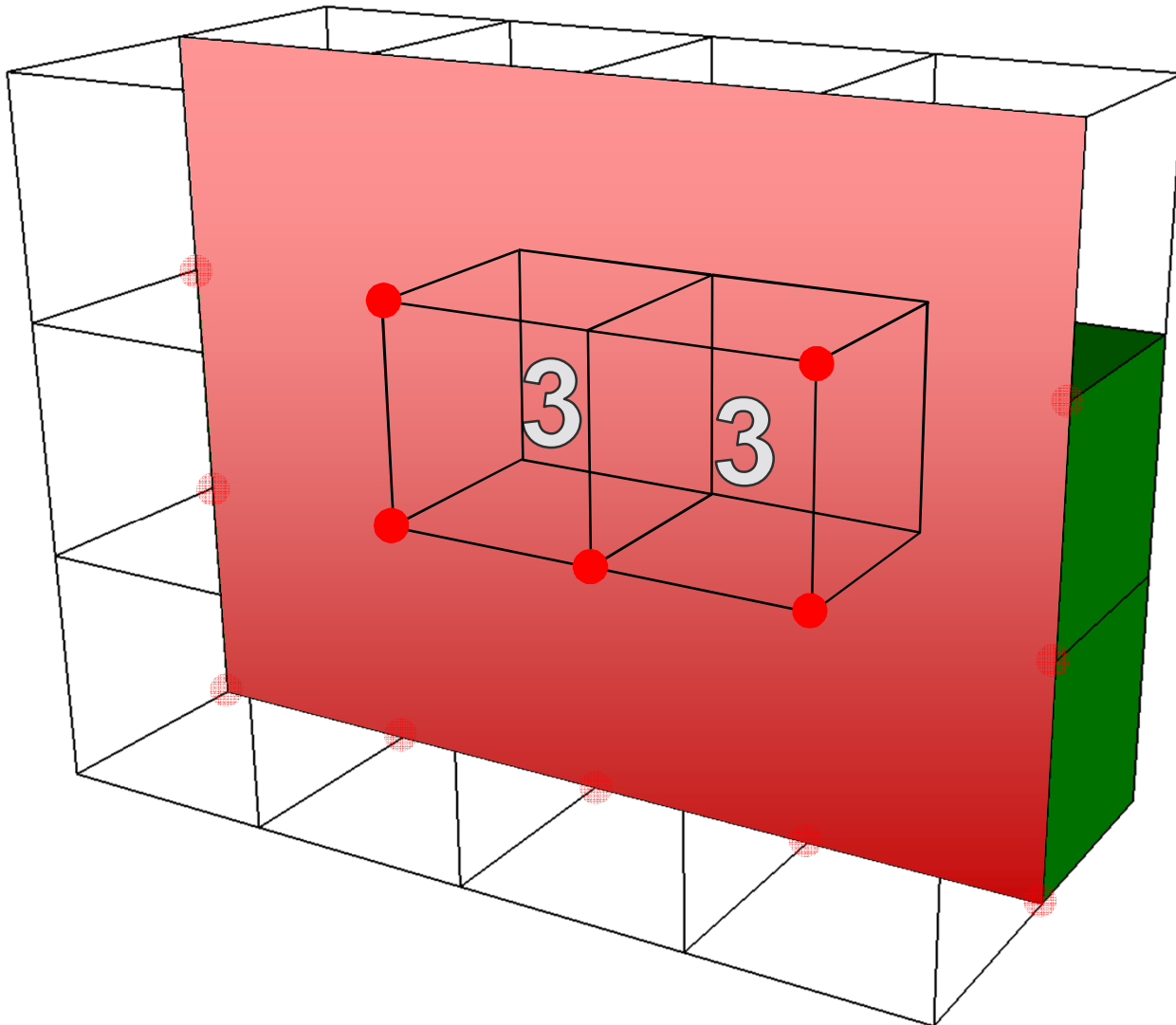
Additional 3D Node Marking



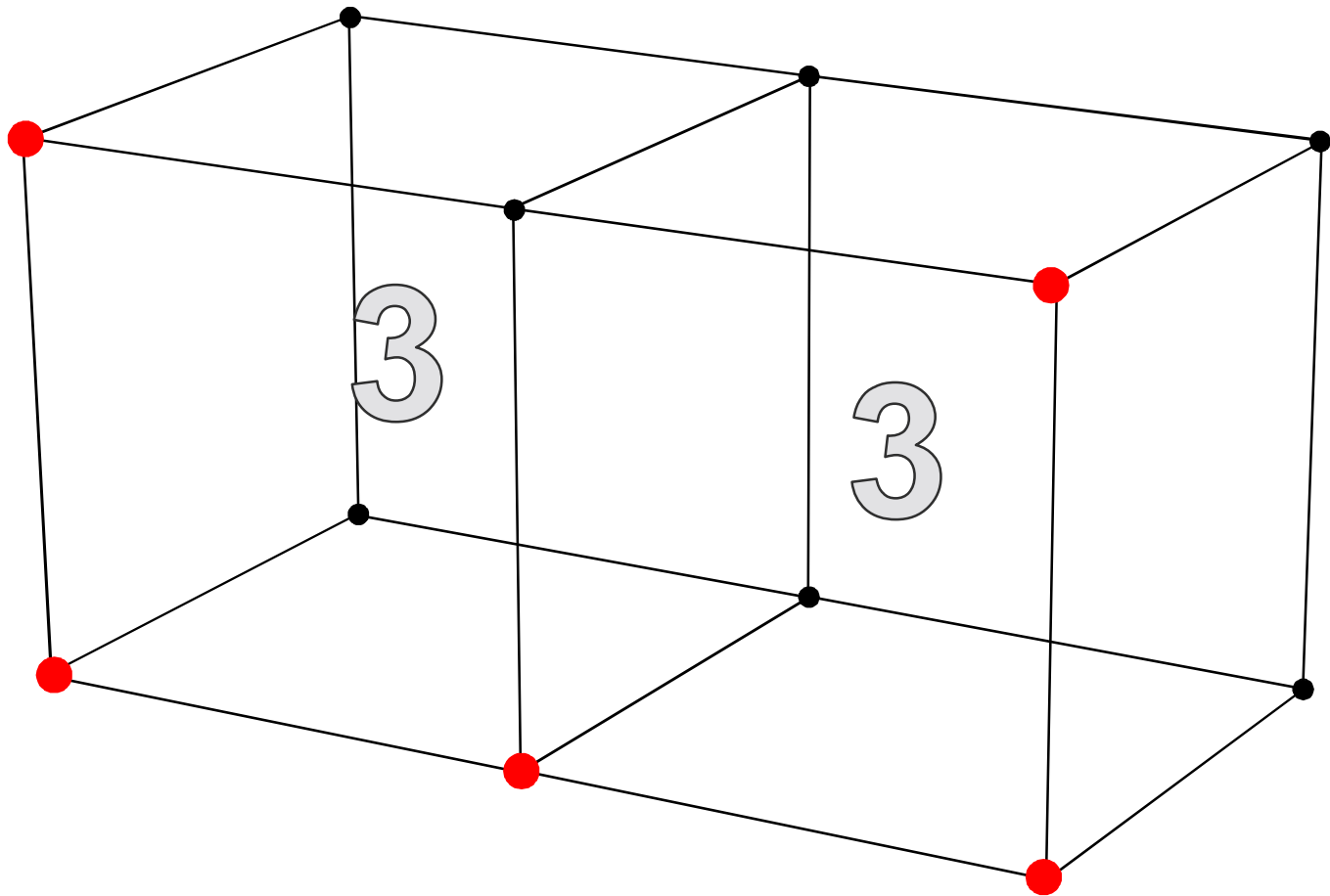
Additional 3D Node Marking



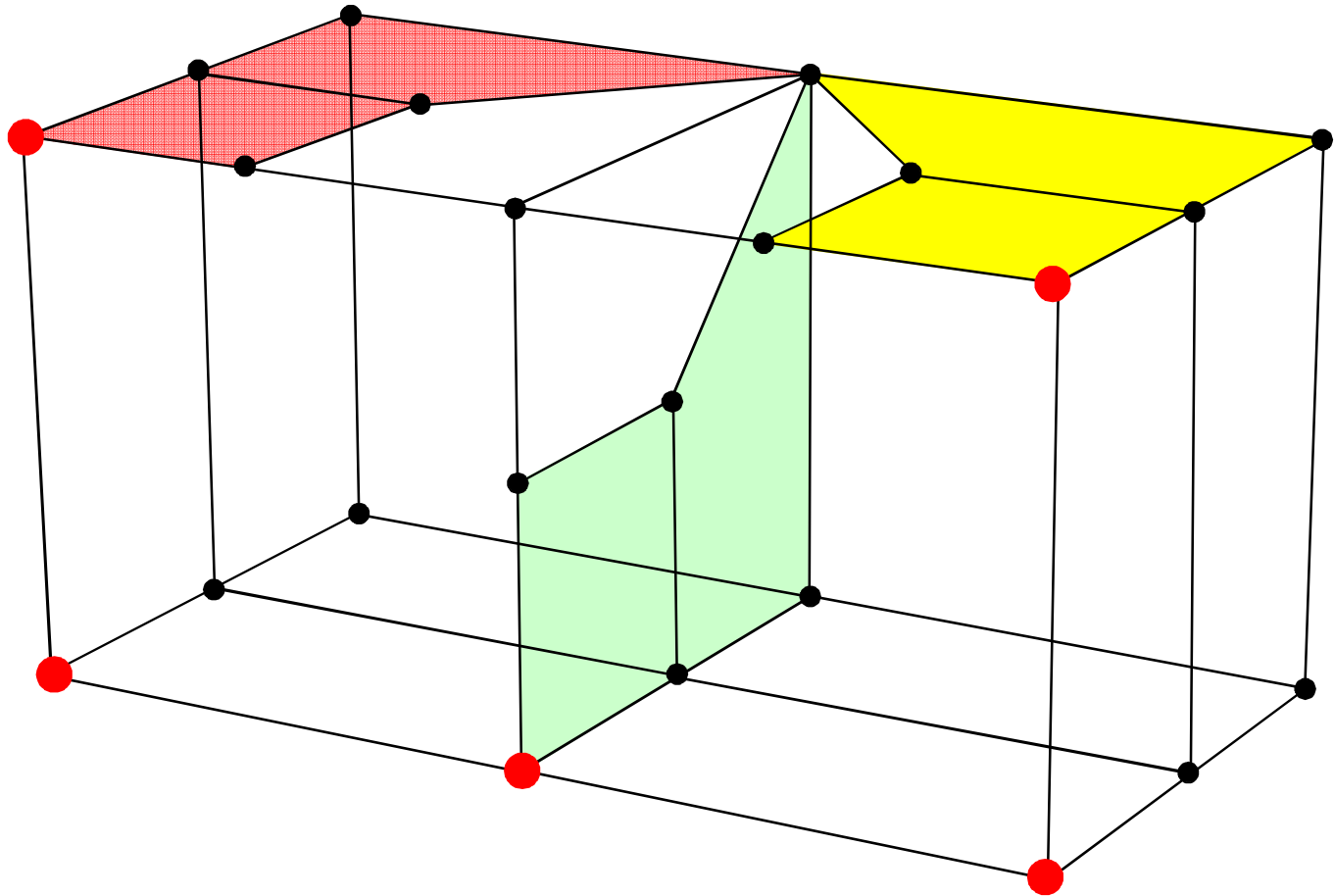
Additional 3D Node Marking



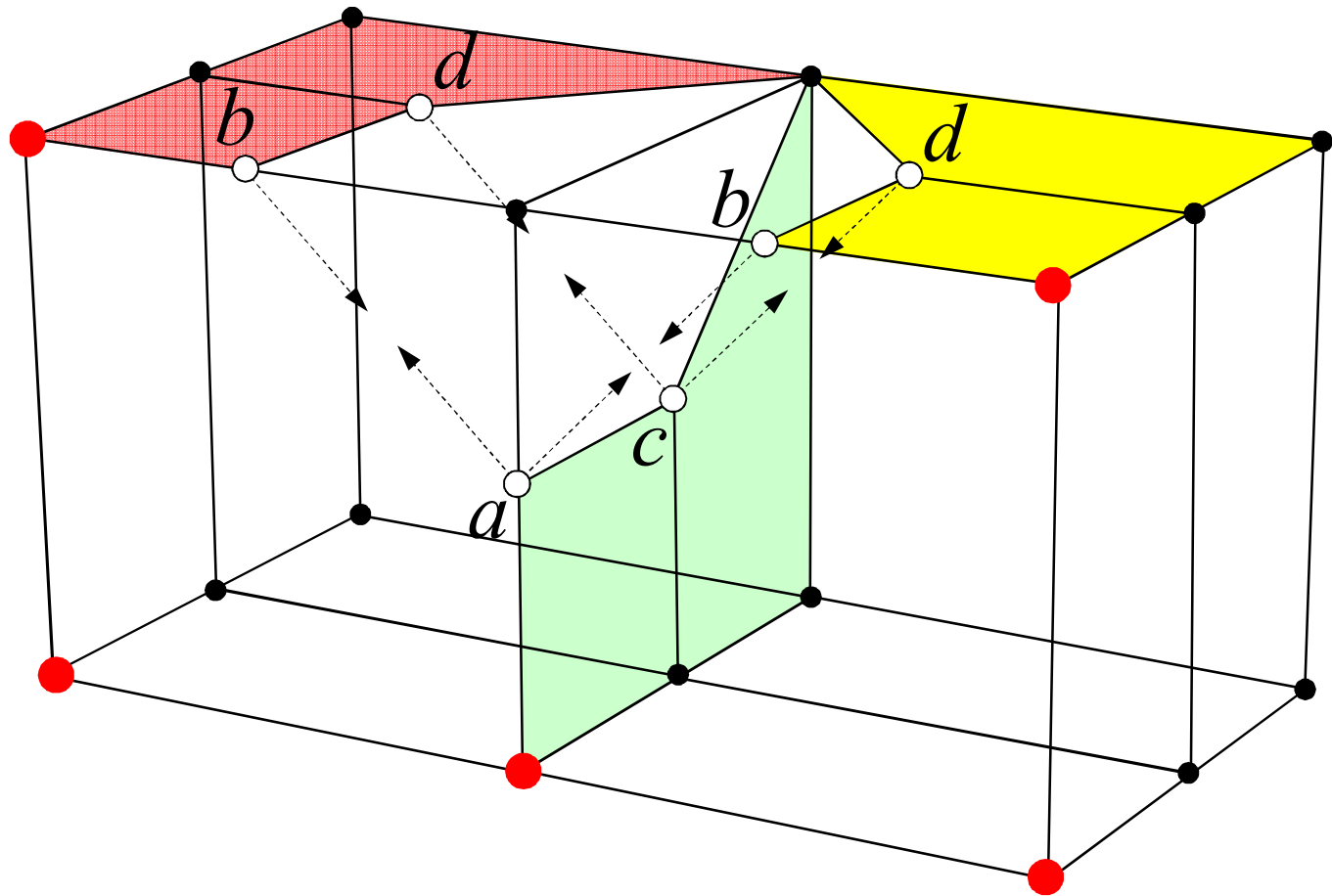
Additional 3D Node Marking



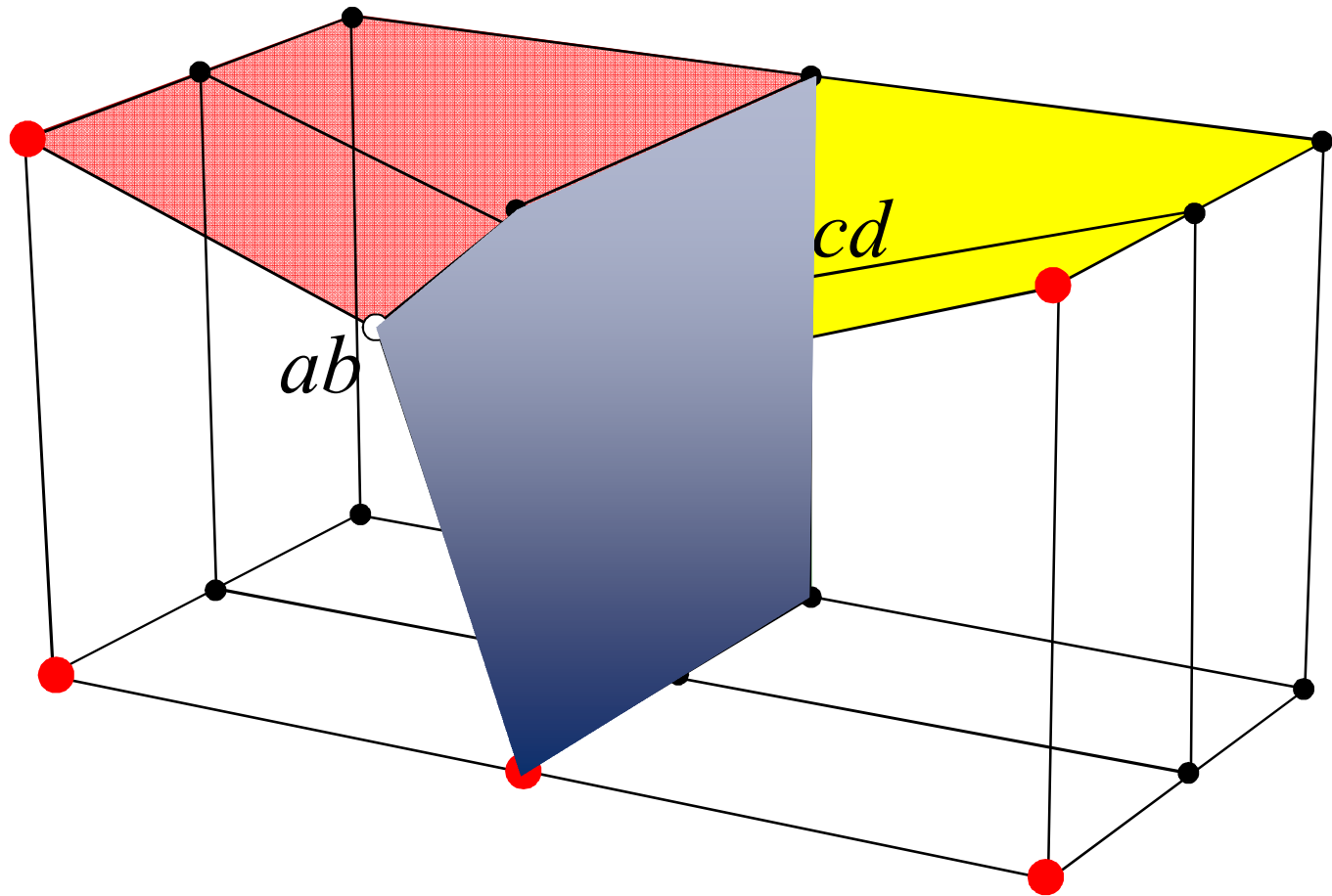
Additional 3D Node Marking



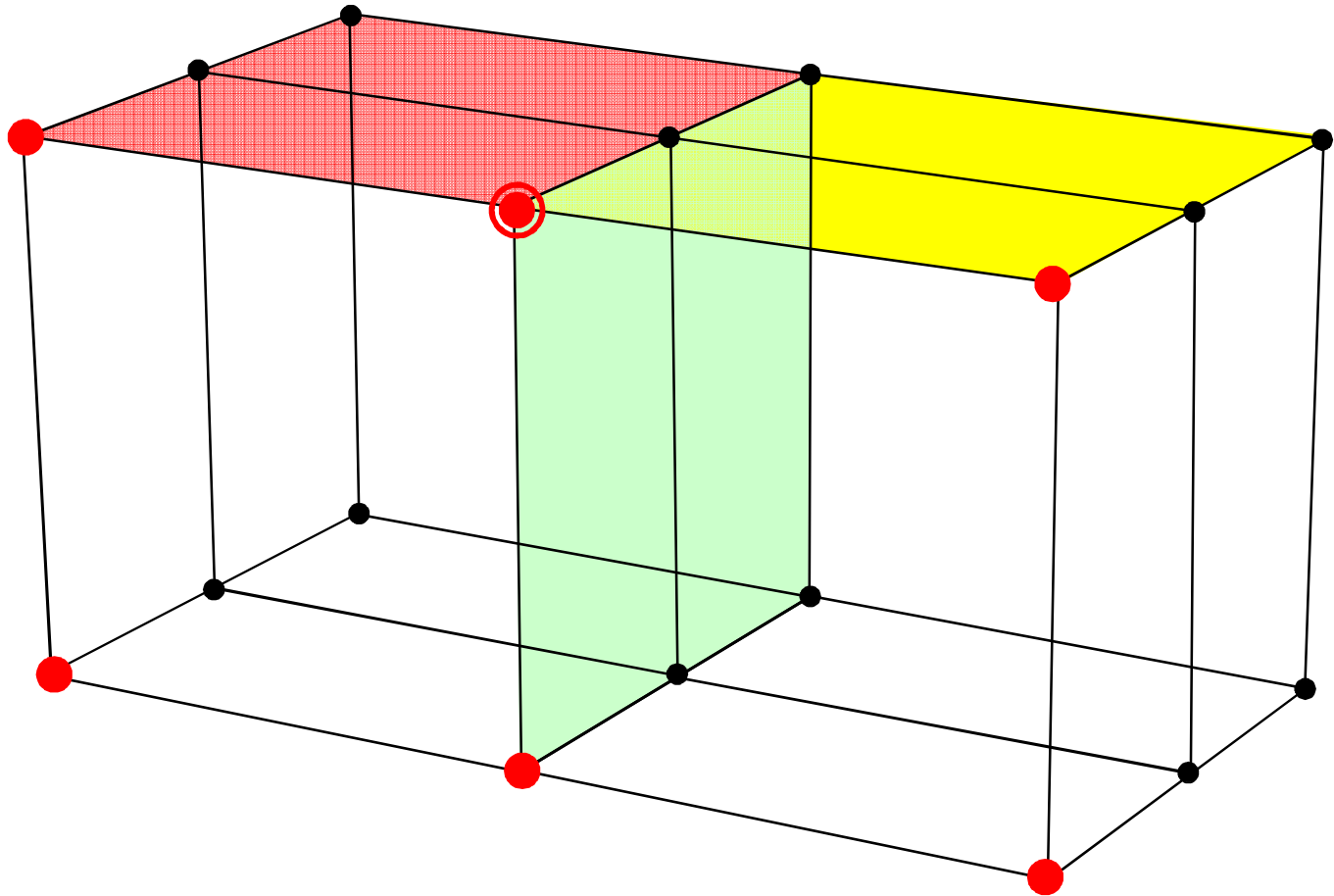
Additional 3D Node Marking



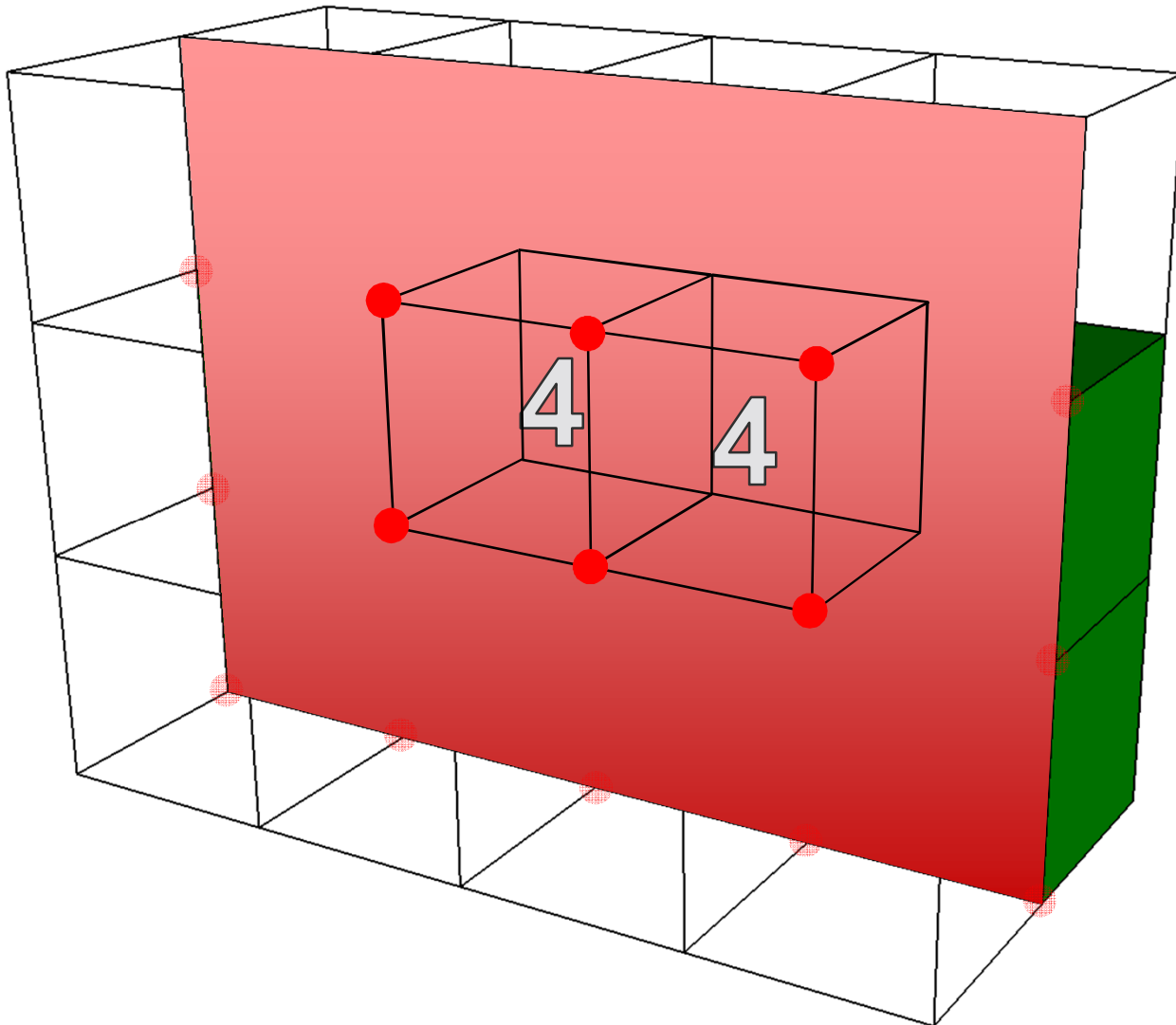
Additional 3D Node Marking



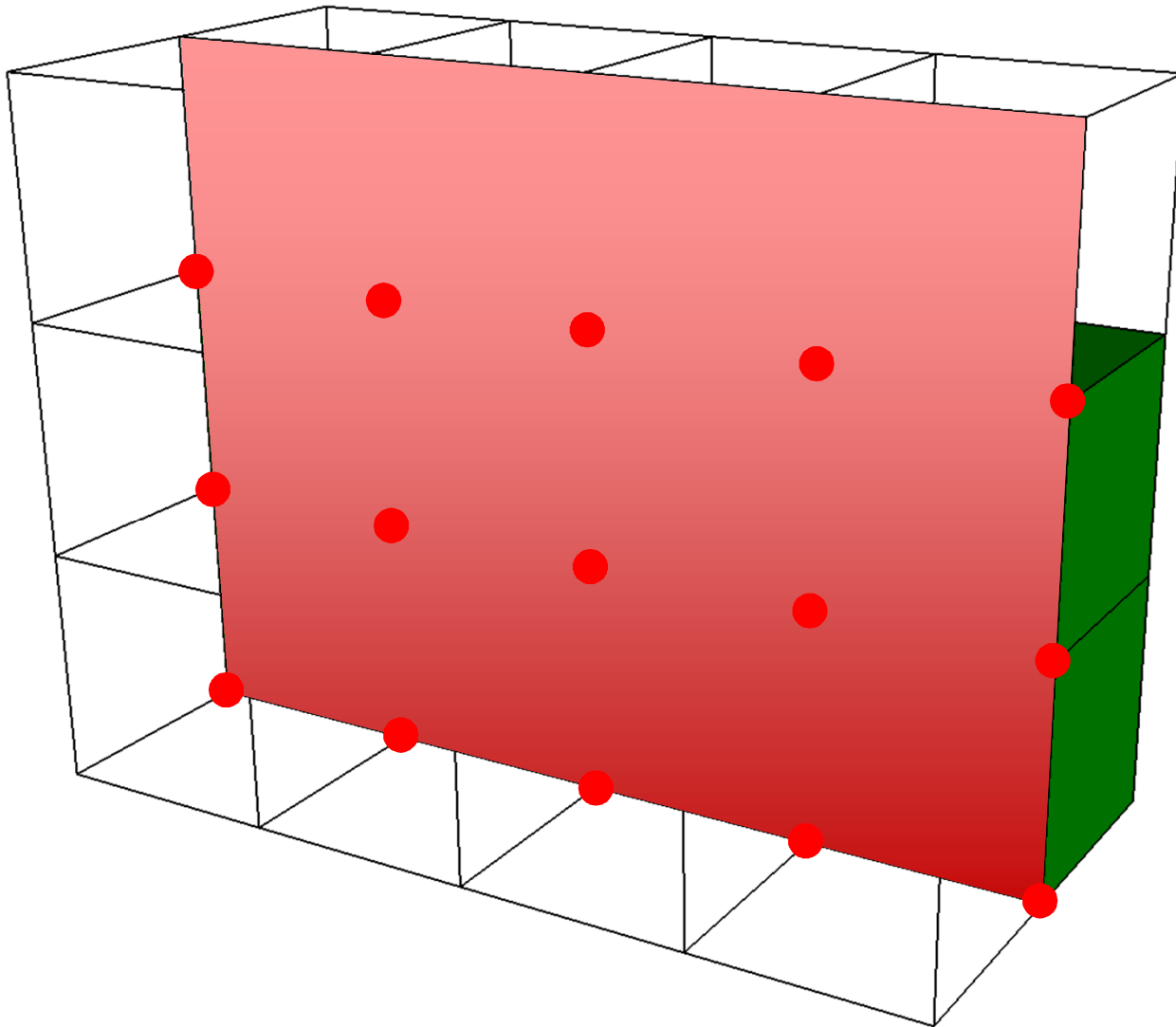
Additional 3D Node Marking



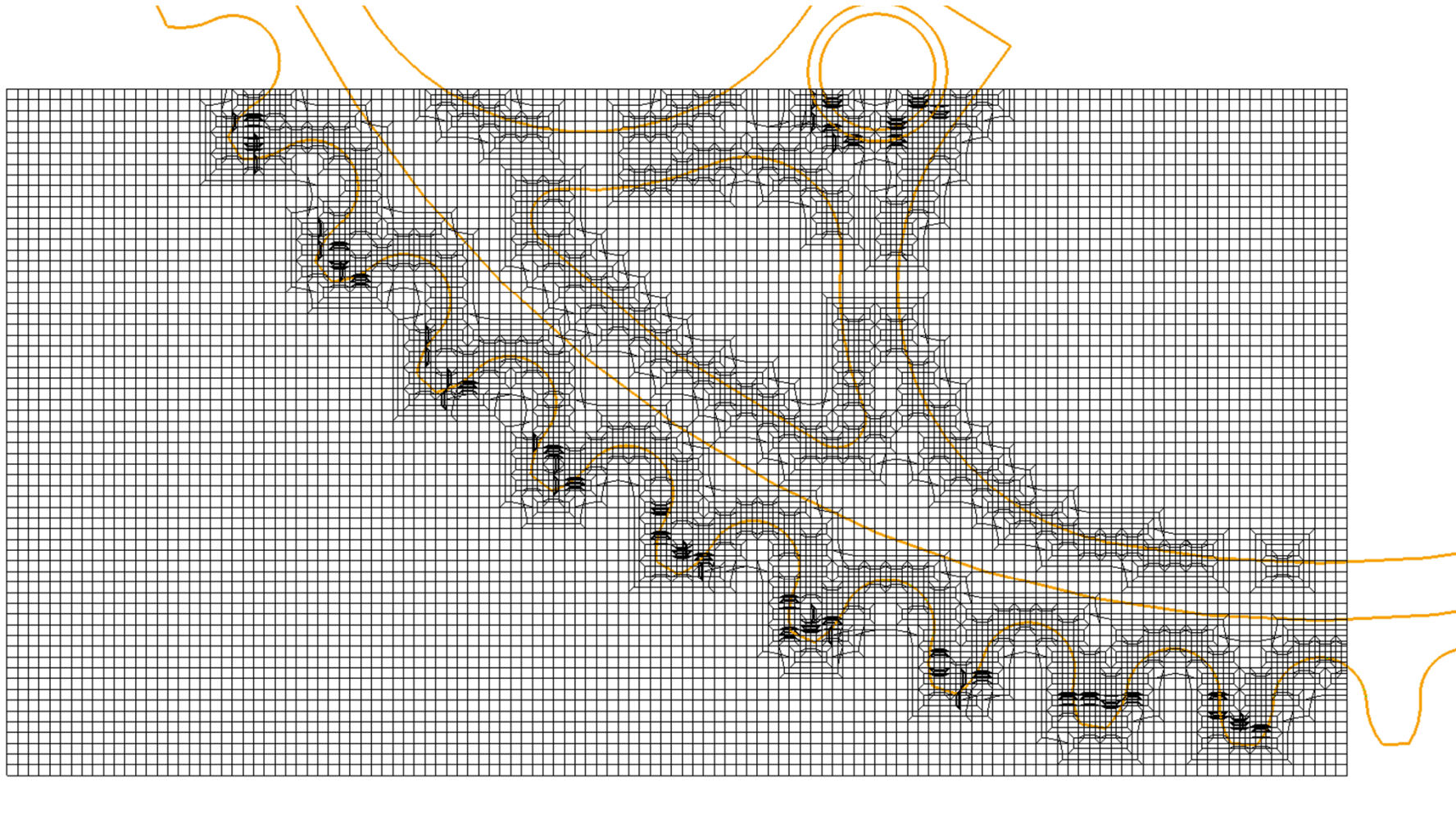
Additional 3D Node Marking



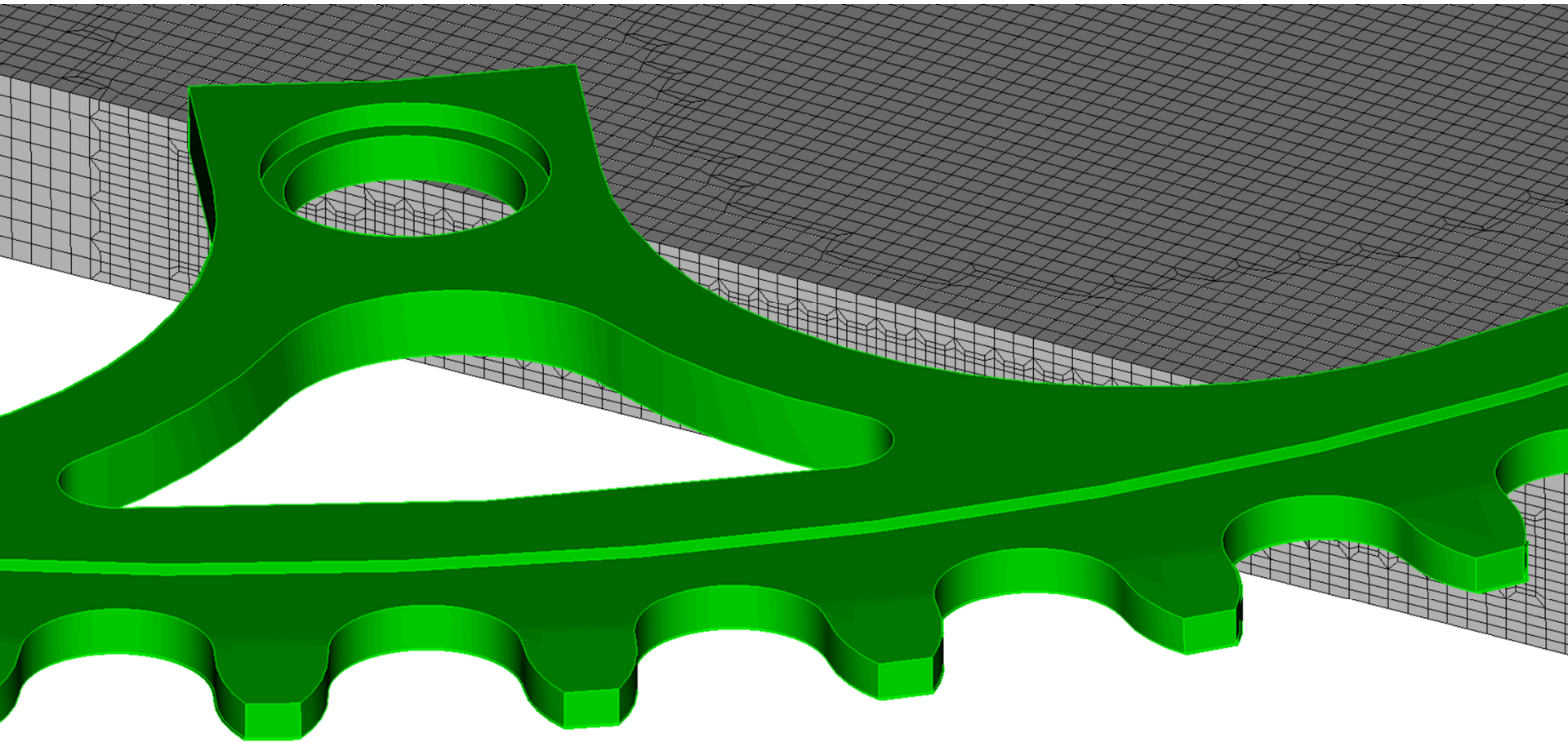
Additional 3D Node Marking

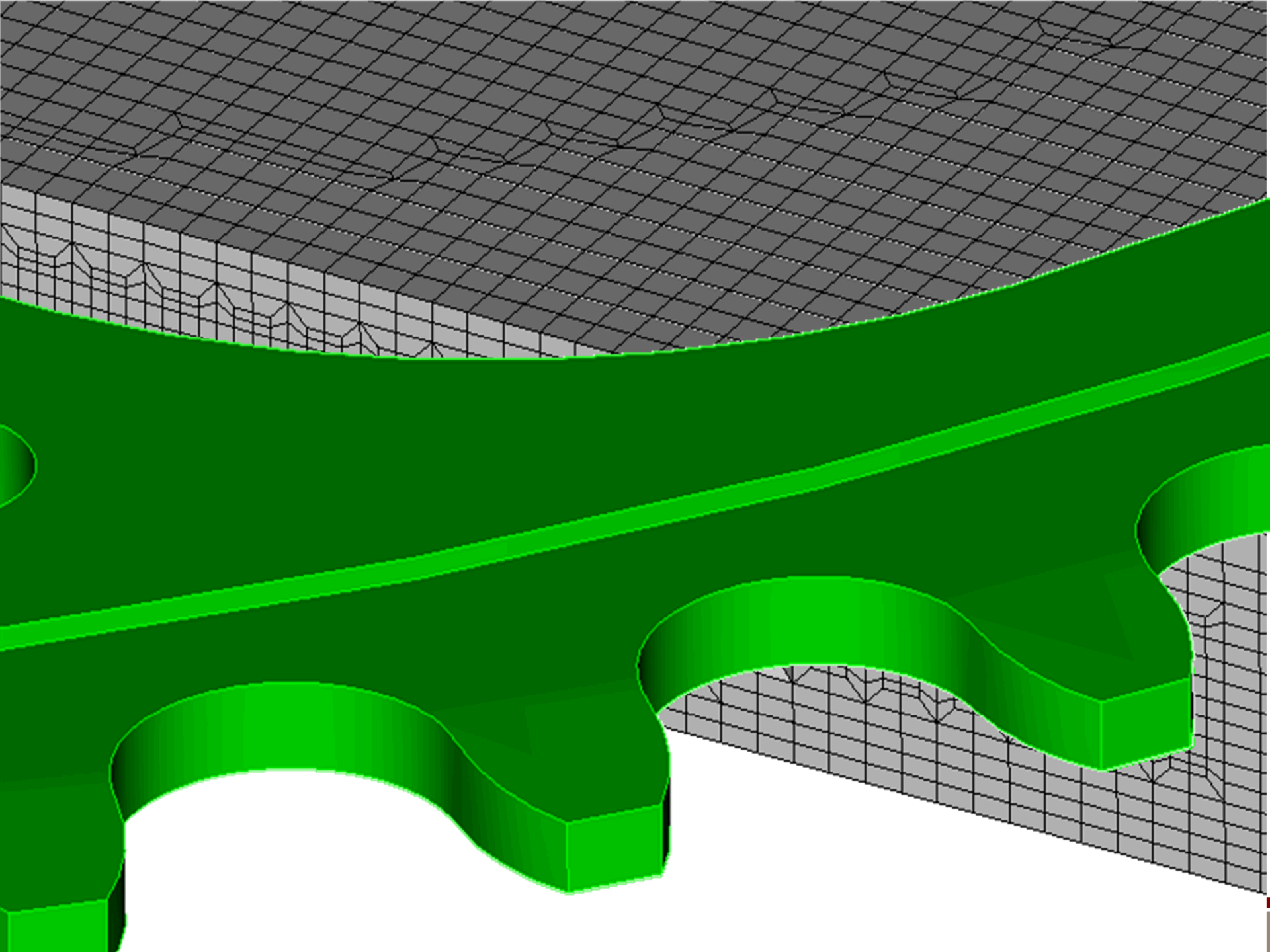


Example Refinement

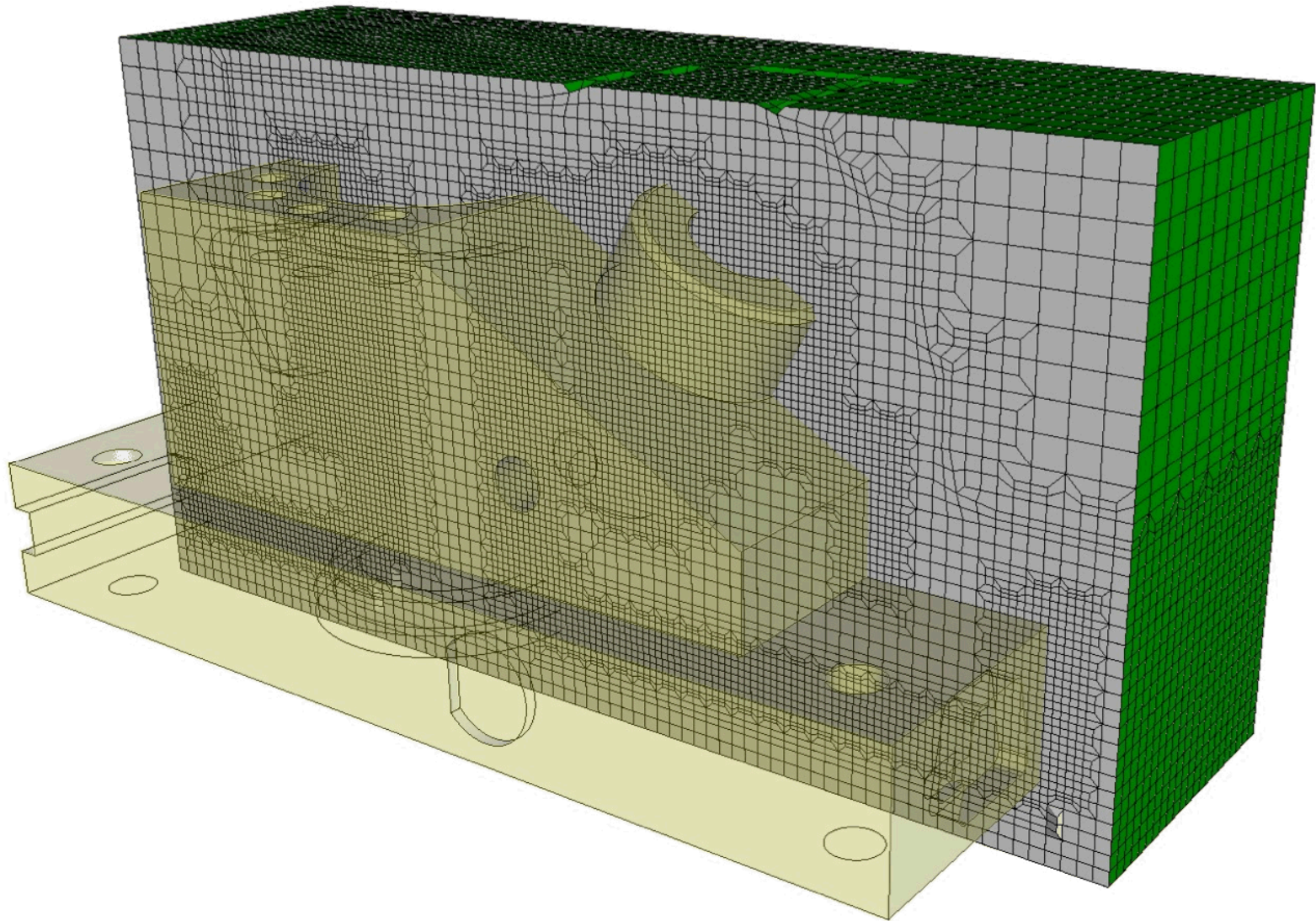


Example Refinement

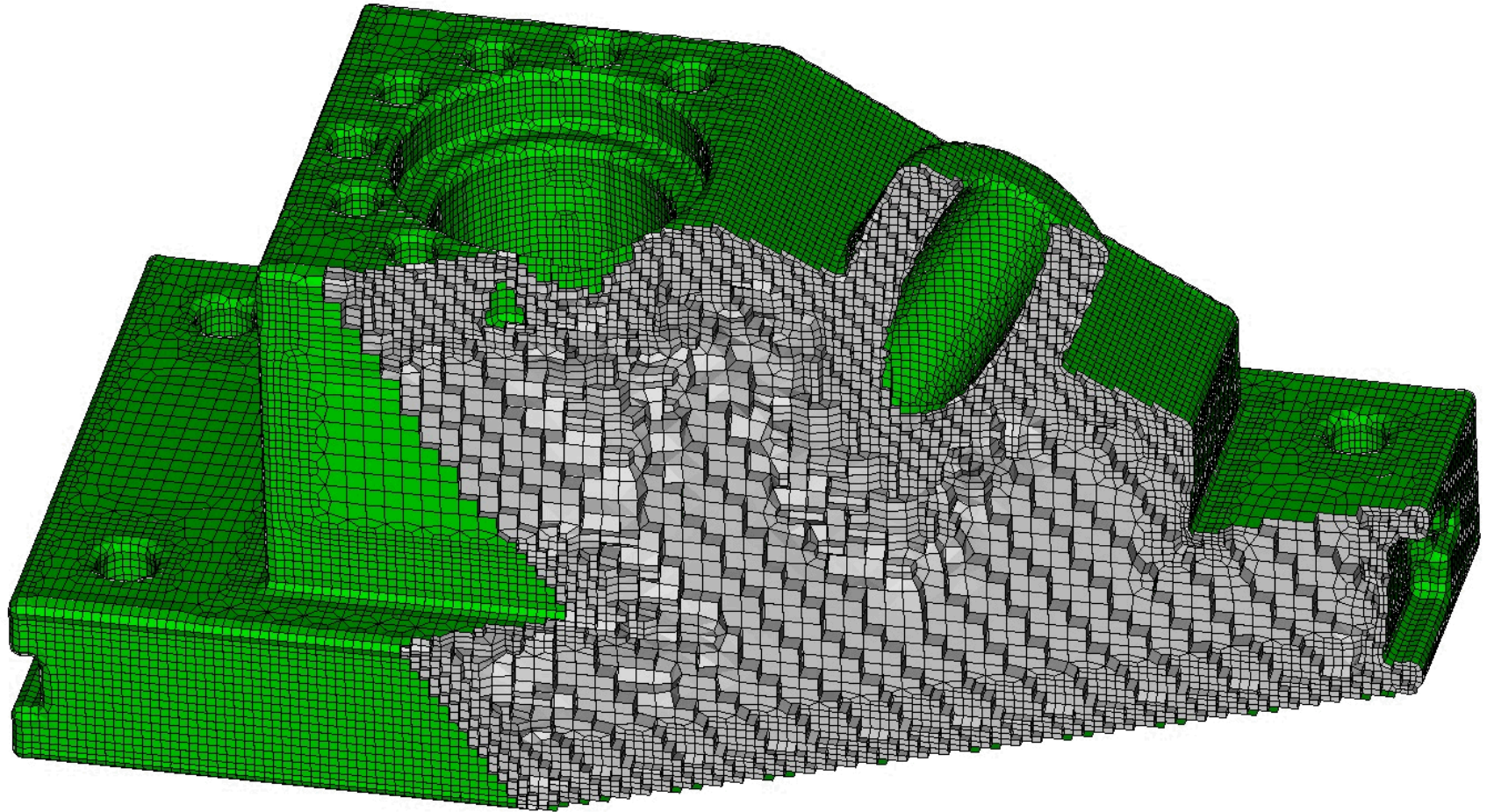




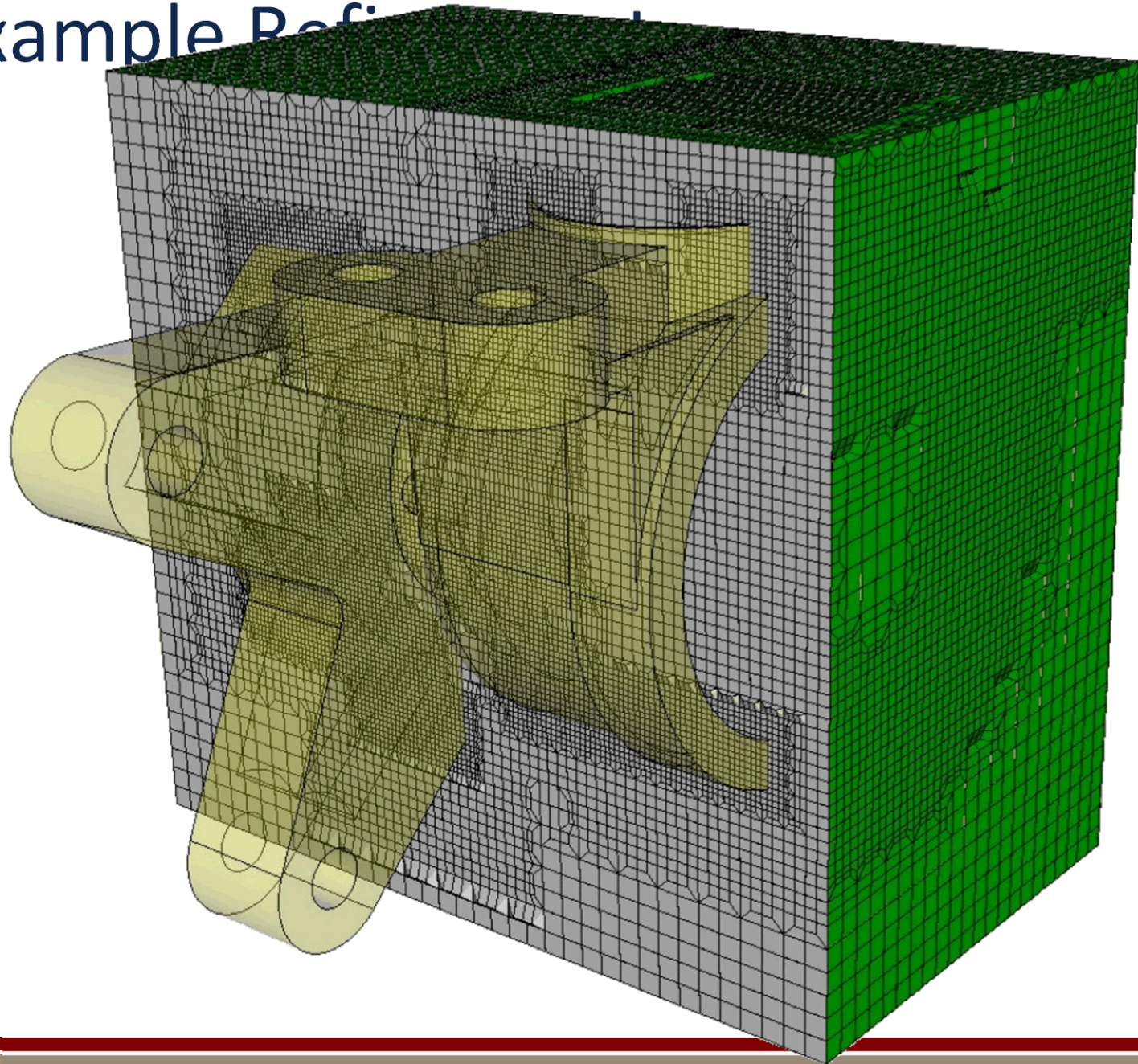
Example Refinement



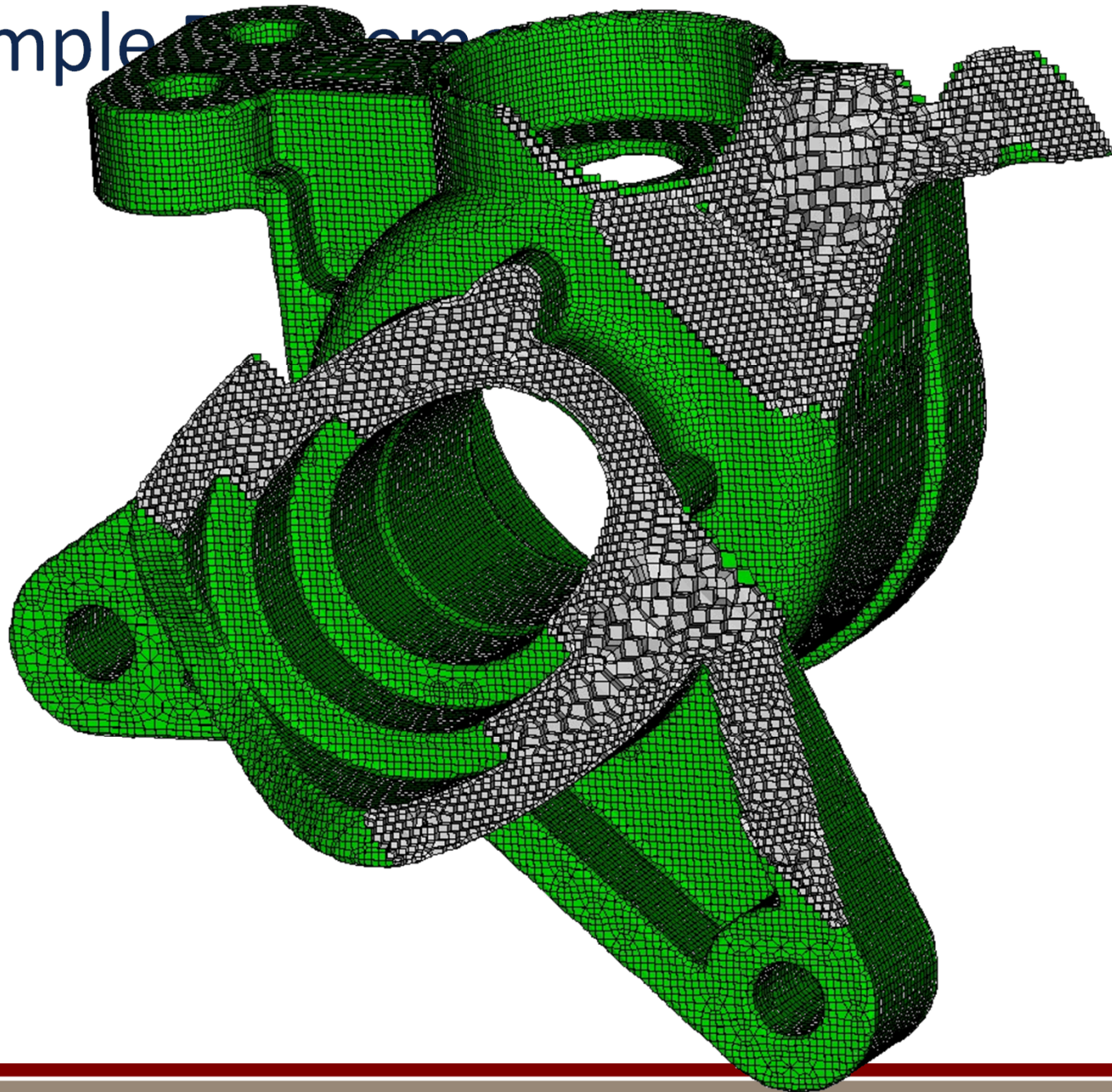
Example Refinement



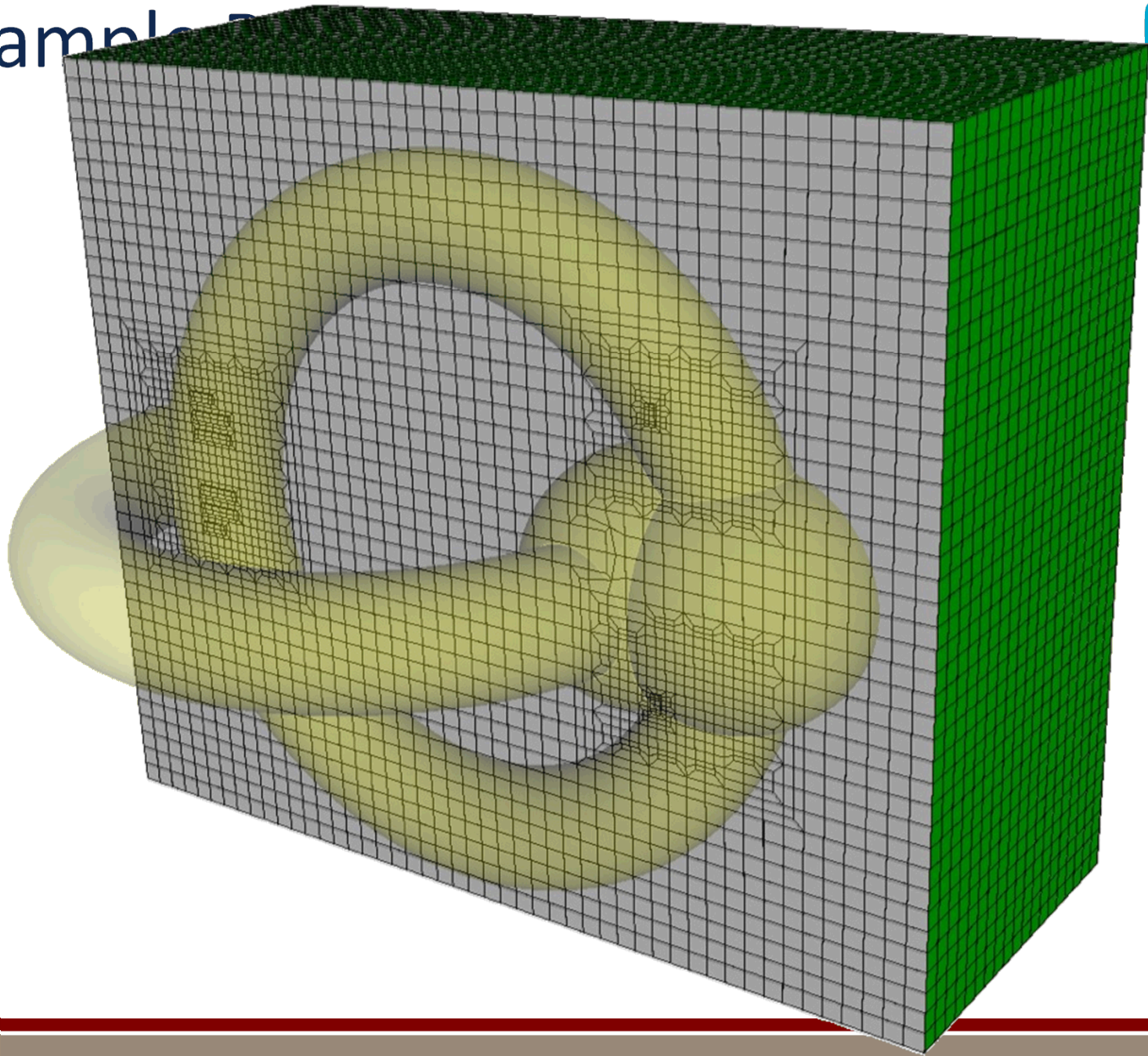
Example Refinement



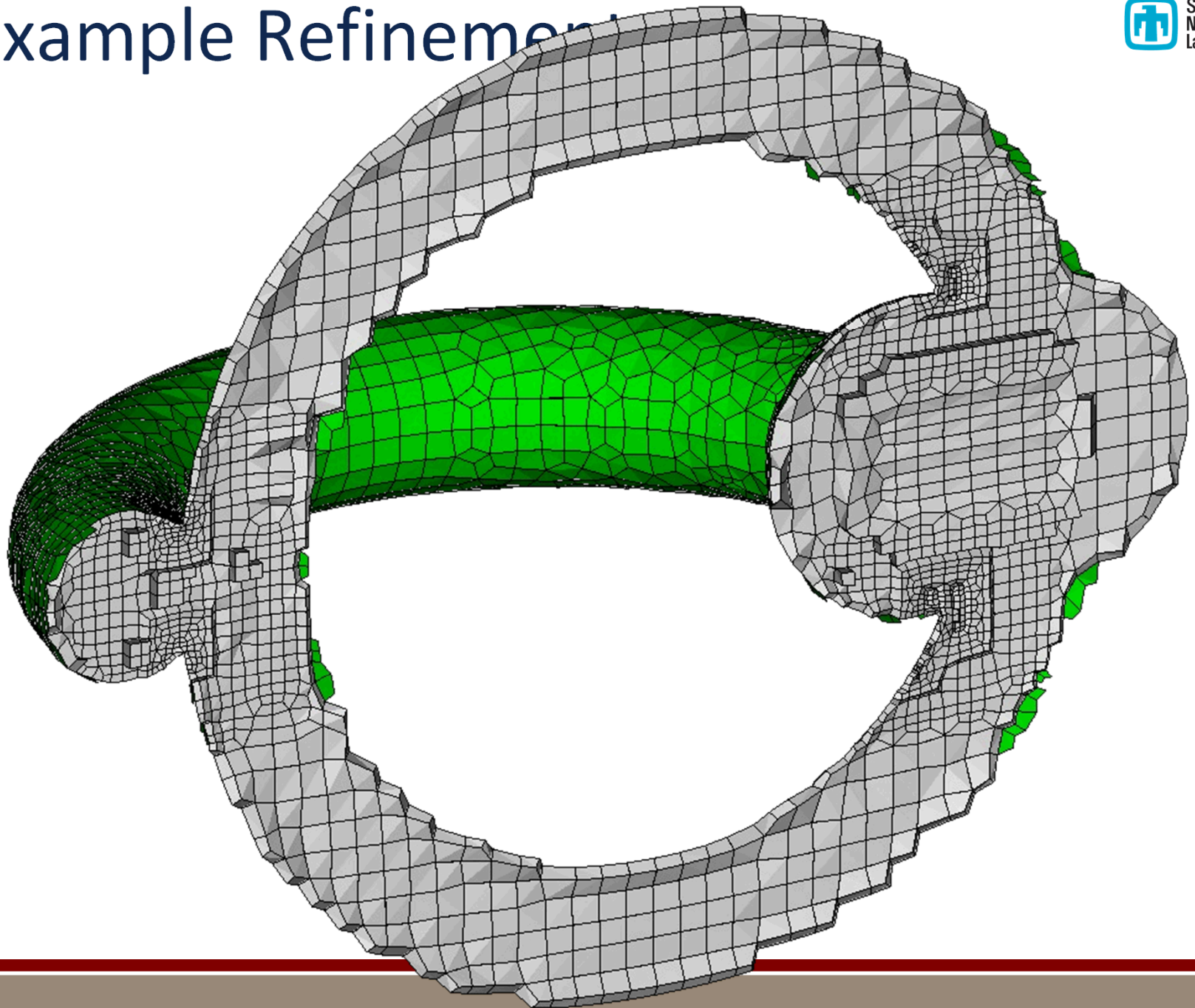
Example 2



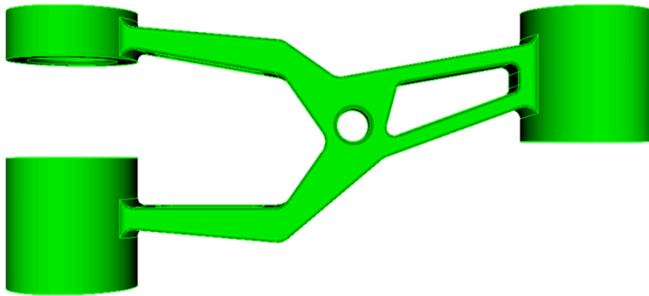
Example 2



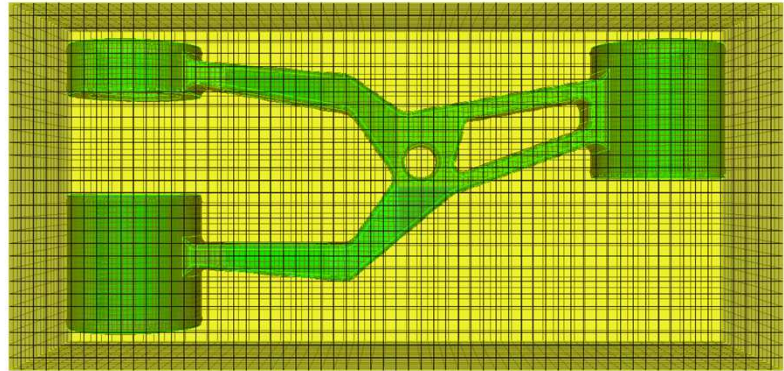
Example Refinement



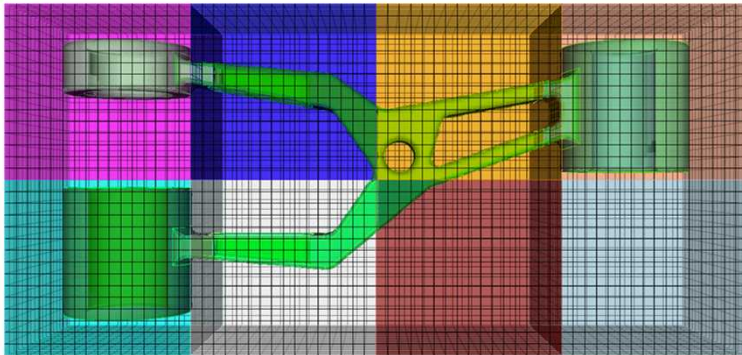
Distributed Parallel



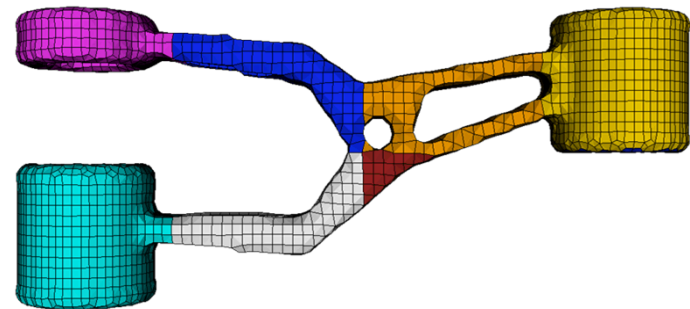
CAD geometry



Global overlay Cartesian grid

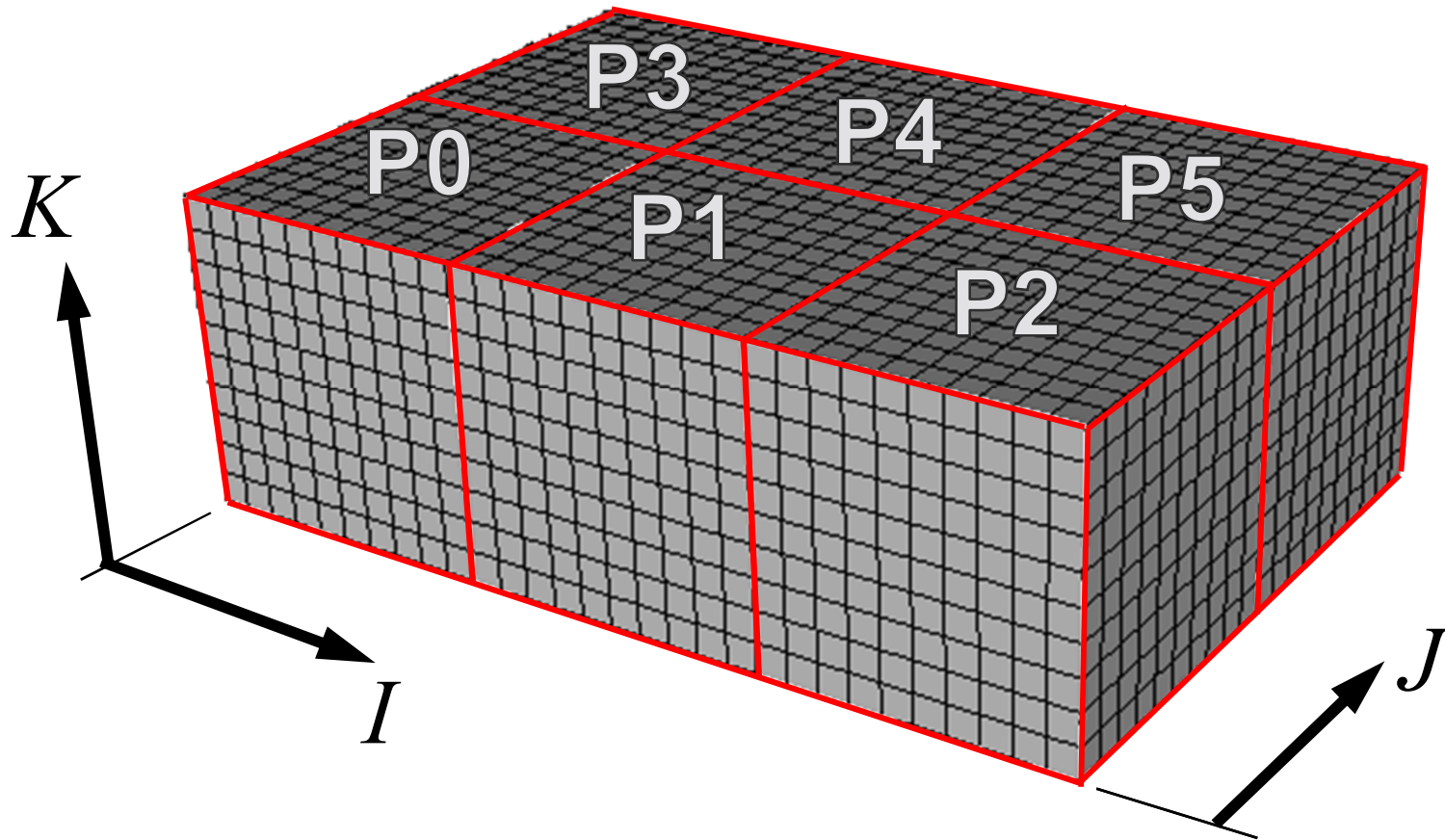


Cartesian grid decomposed and distributed amongst many processors

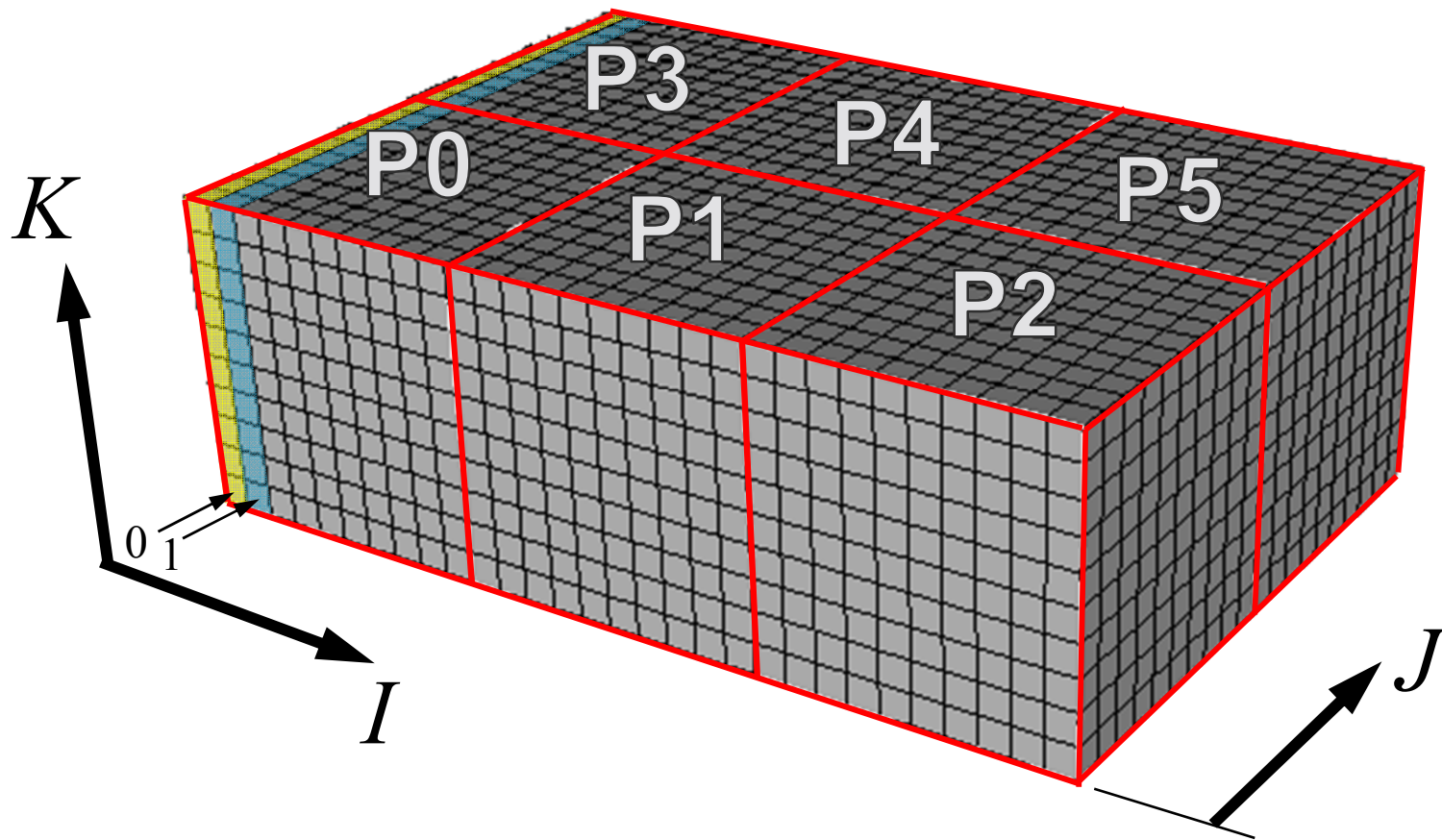


Each processor independently meshes its portion of Cartesian grid

Distributed Parallel



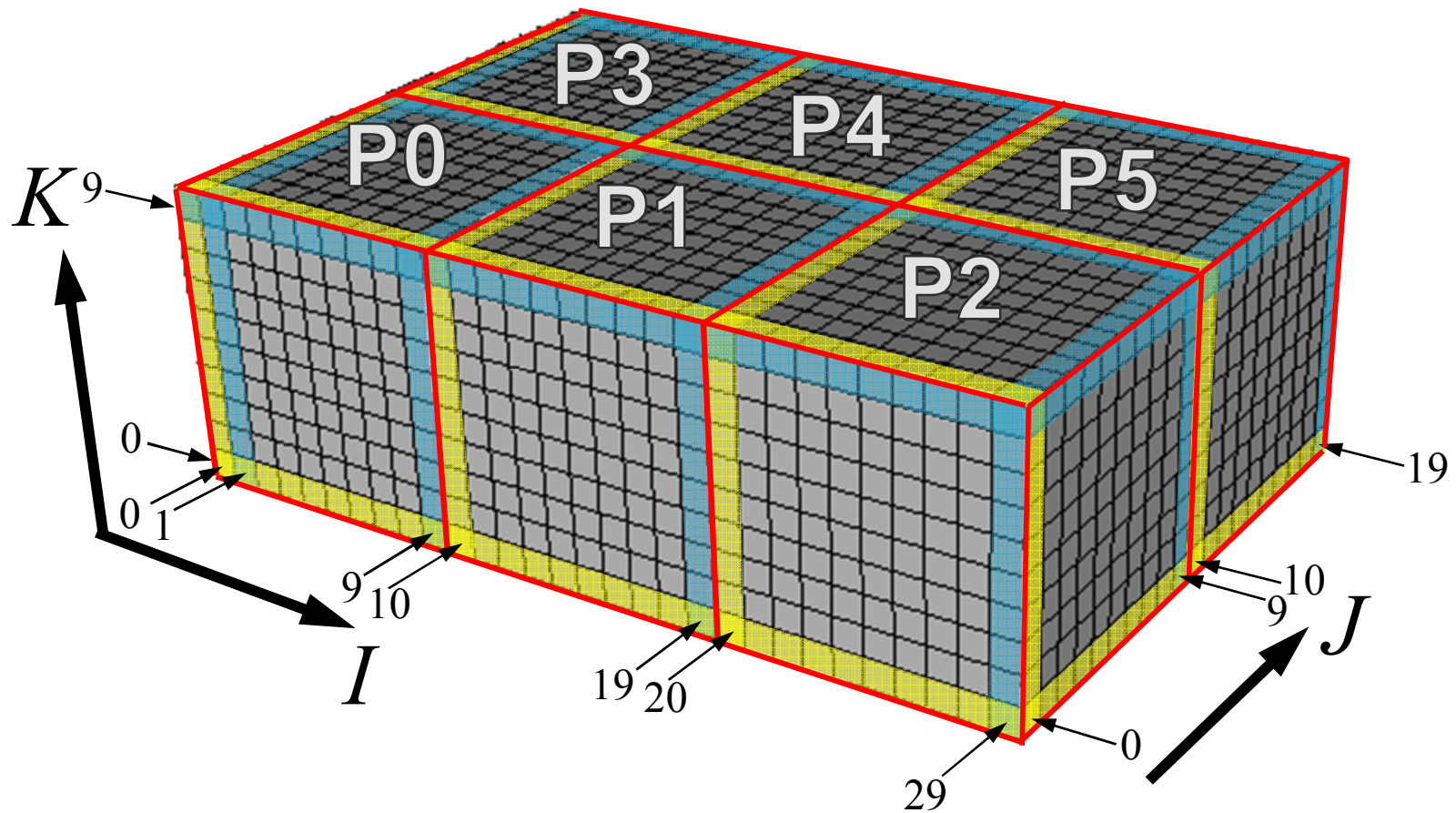
Distributed Parallel



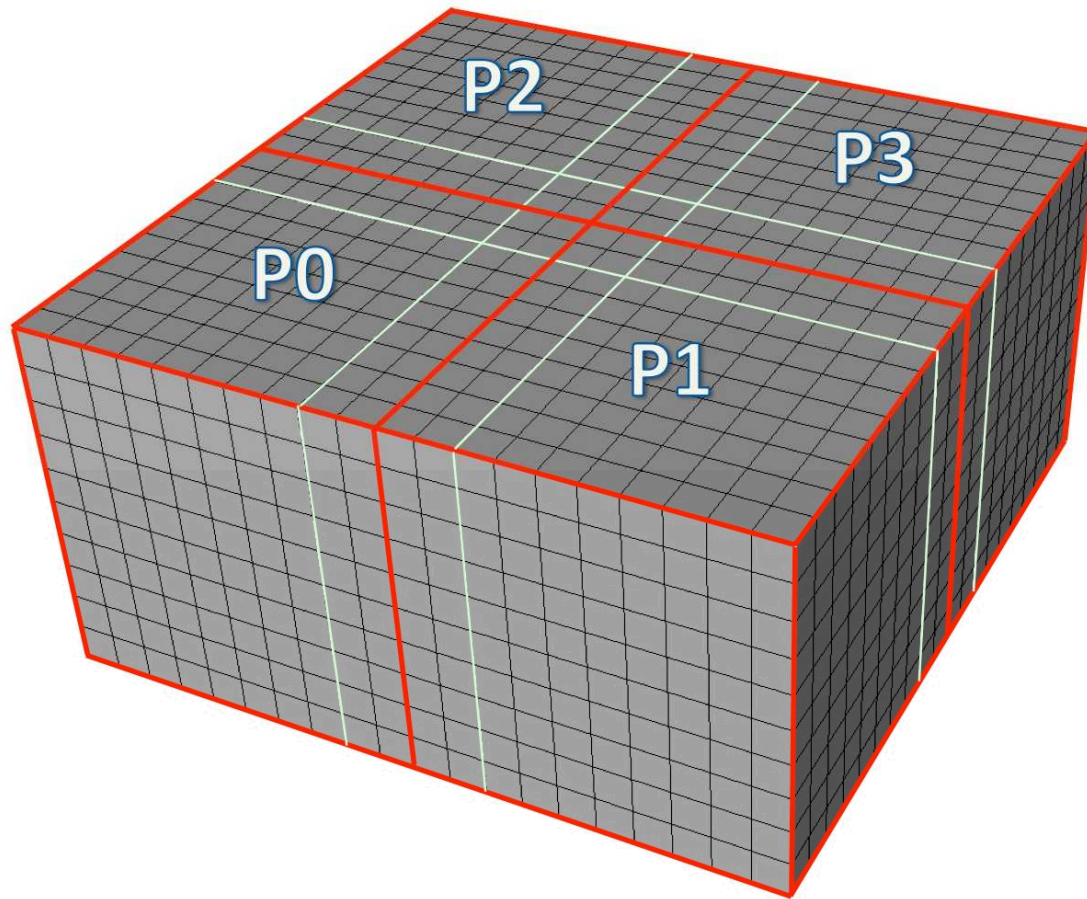




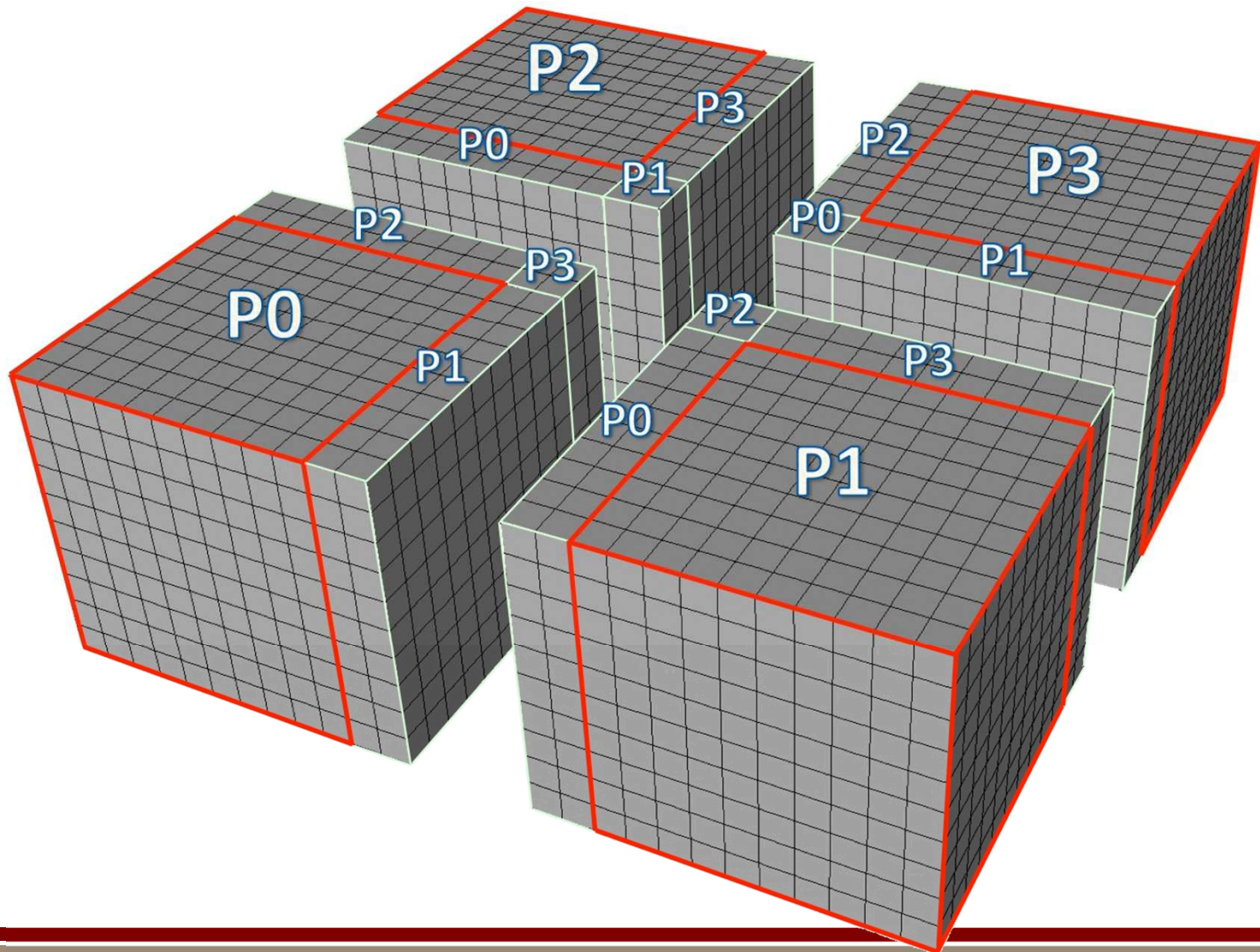
Distributed Parallel



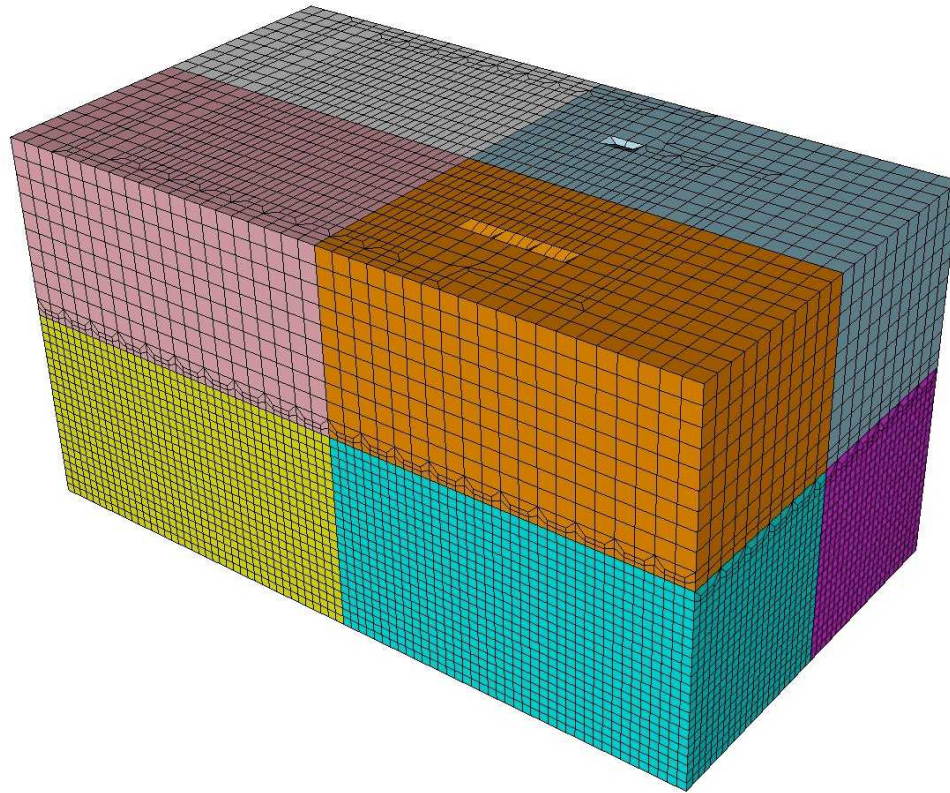
Distributed Parallel

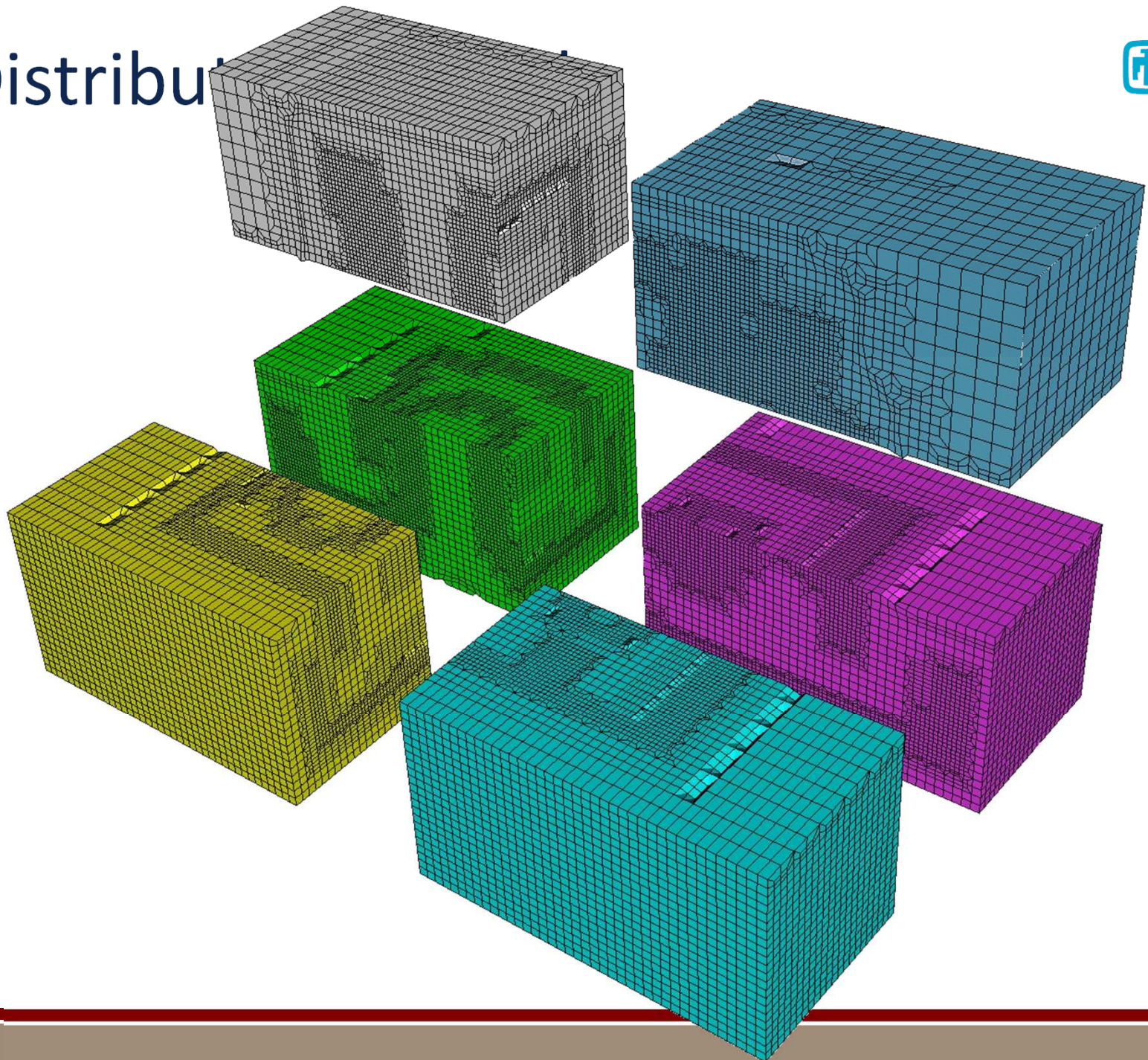


Distributed Parallel

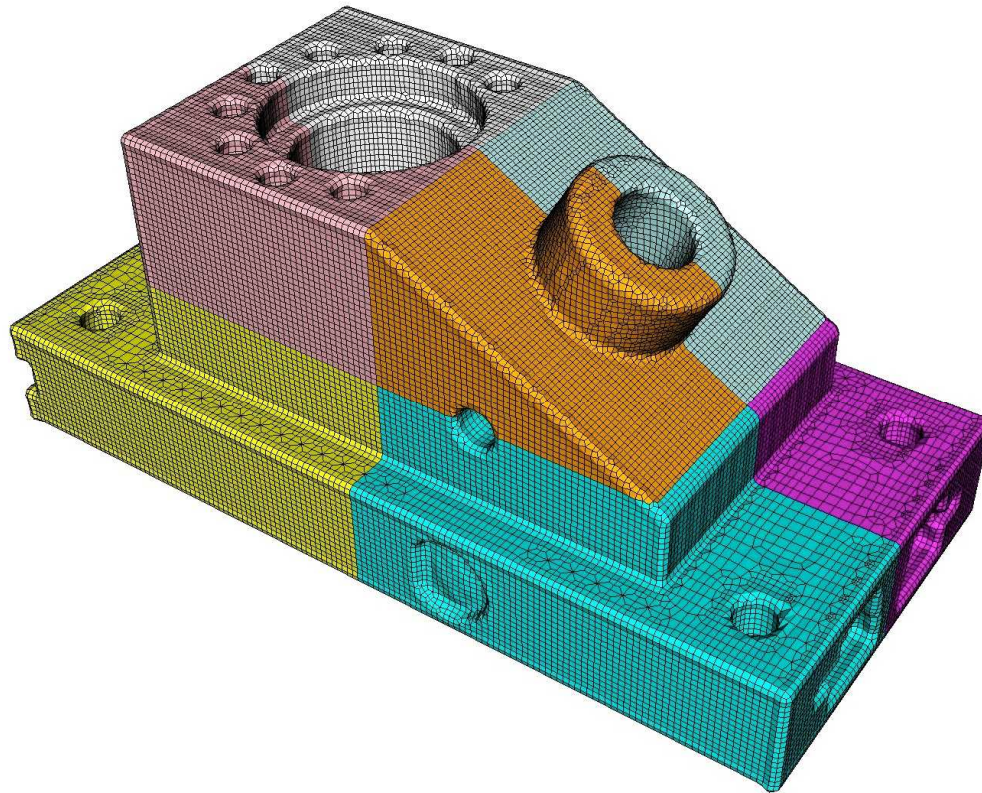


Distributed Parallel

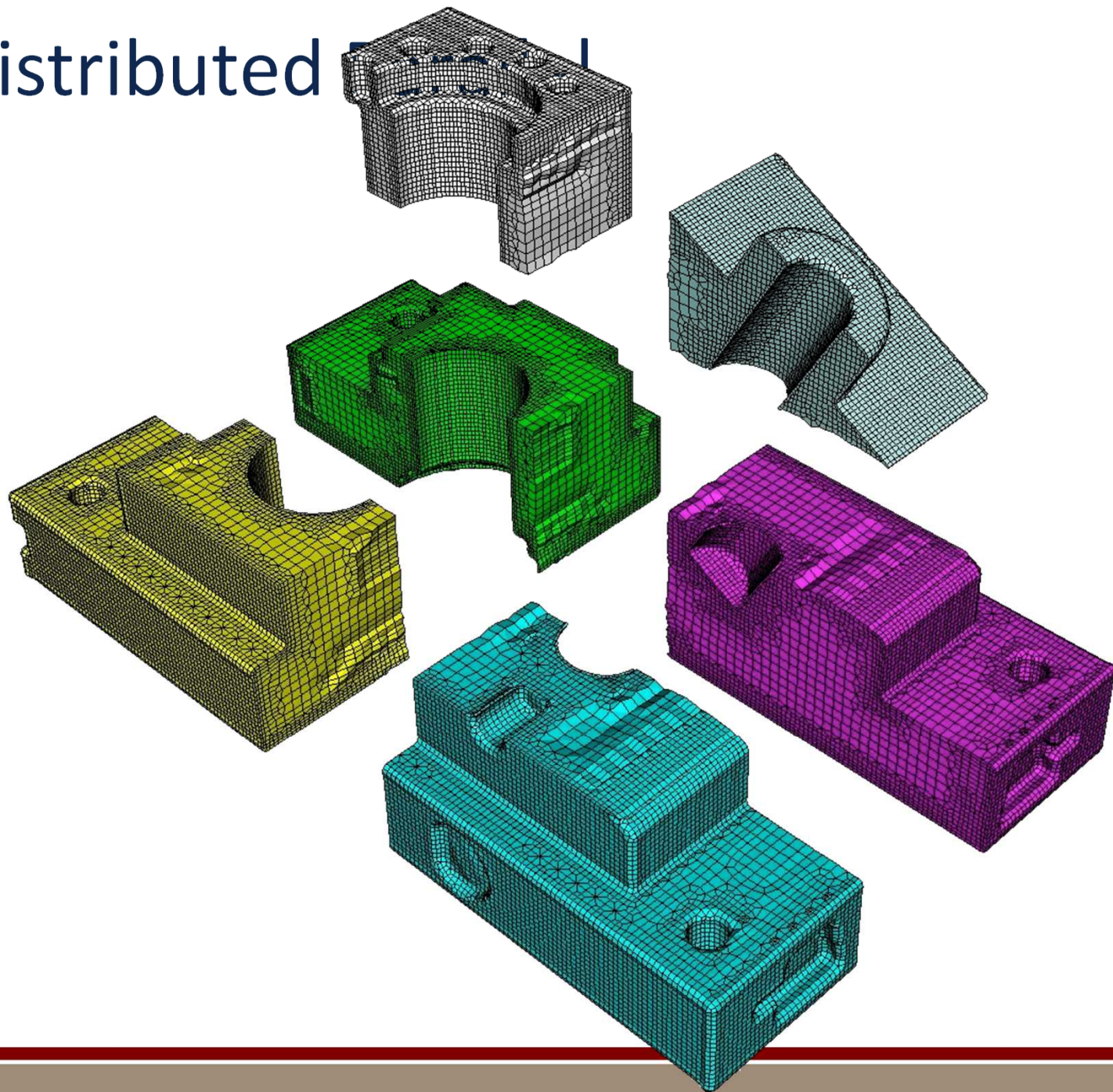




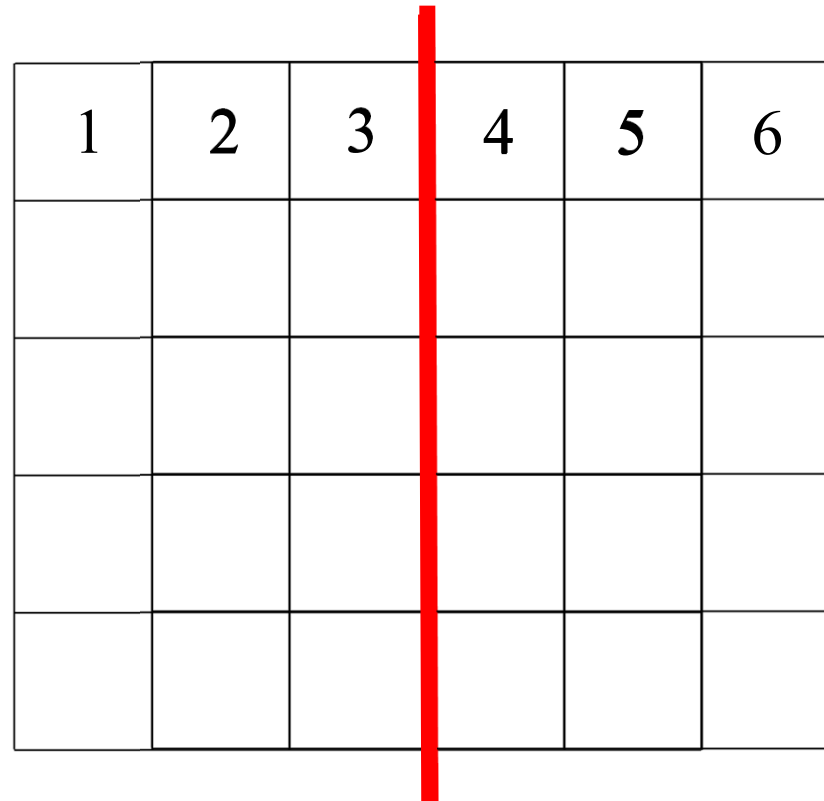
Distributed Parallel



Distributed



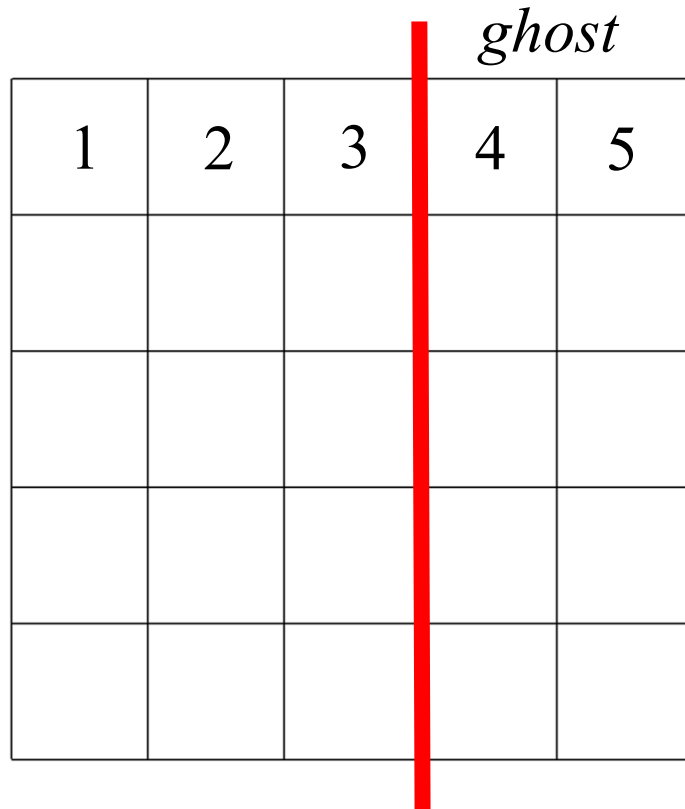
Parallel Communication



Processor 0

Processor 1

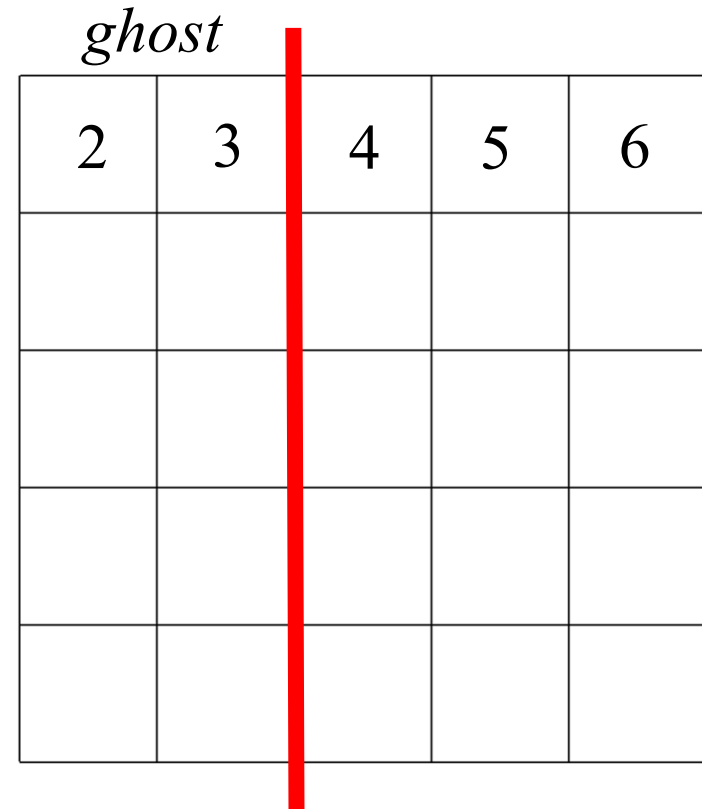
Parallel Communication



A 5x5 grid representing a data distribution on Processor 0. The top row contains the values 1, 2, 3, 4, and 5. A thick red vertical line is positioned between the third and fourth columns. The word "ghost" is written in italics above the fourth column, indicating that the data in this column is replicated (ghosted) for communication purposes.

1	2	3	<i>ghost</i> 4	5

Processor 0

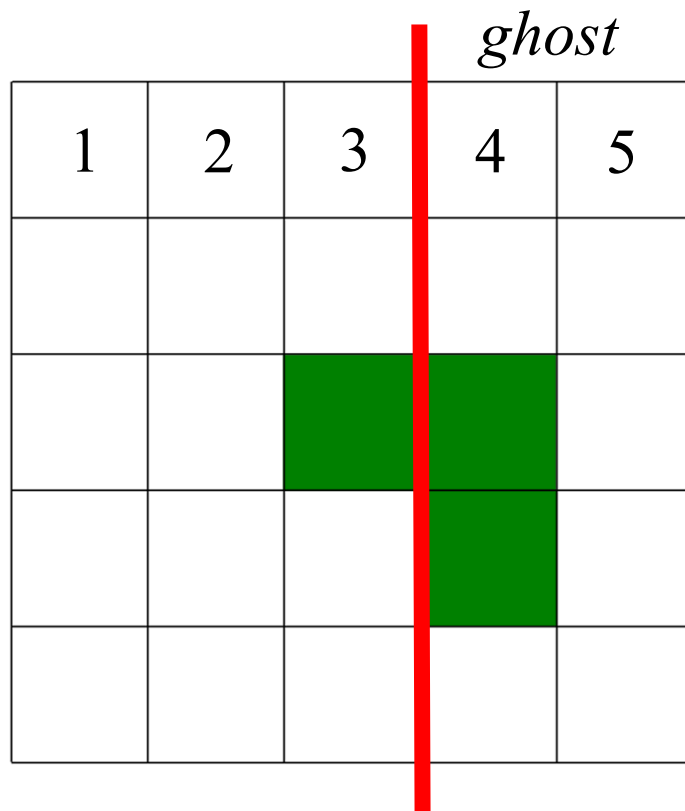


A 5x5 grid representing a data distribution on Processor 1. The top row contains the values 2, 3, 4, 5, and 6. A thick red vertical line is positioned between the second and third columns. The word "ghost" is written in italics above the second column, indicating that the data in this column is replicated (ghosted) for communication purposes.

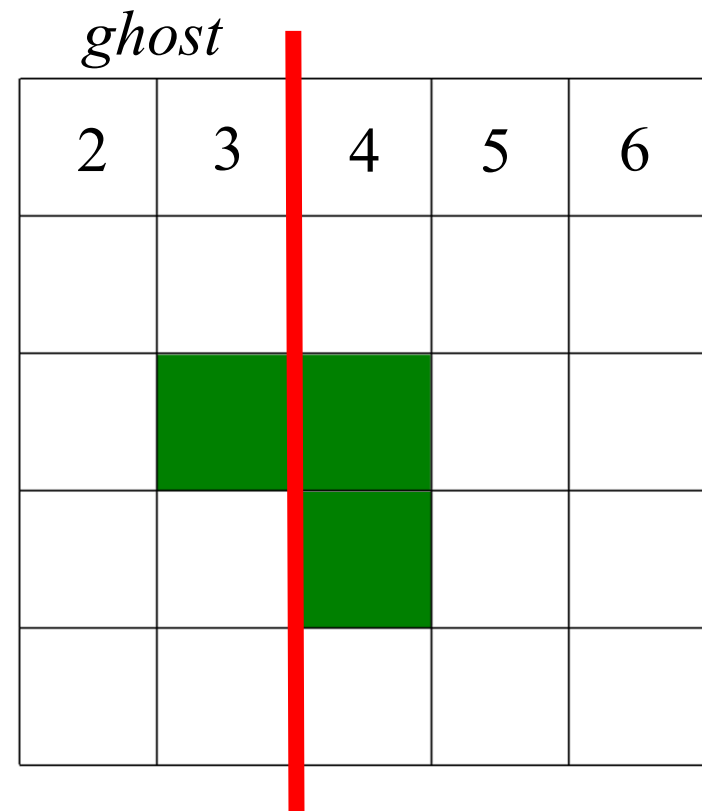
<i>ghost</i> 2	3	4	5	6

Processor 1

Parallel Communication

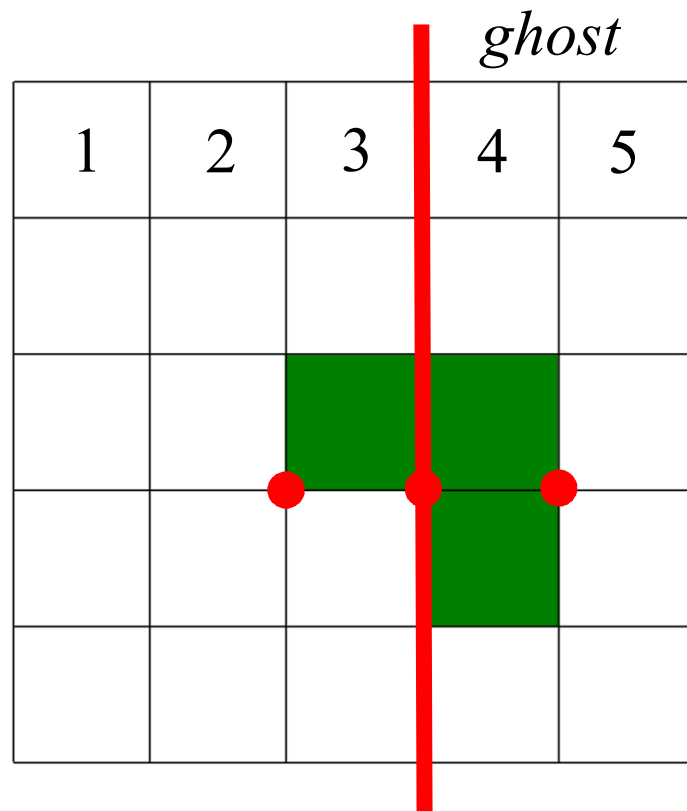


Processor 0

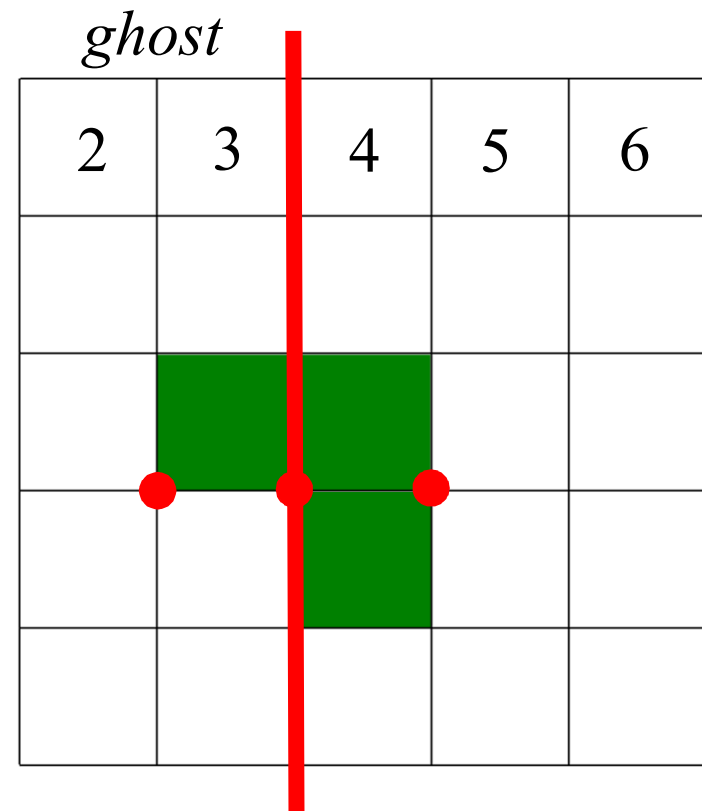


Processor 1

Parallel Communication

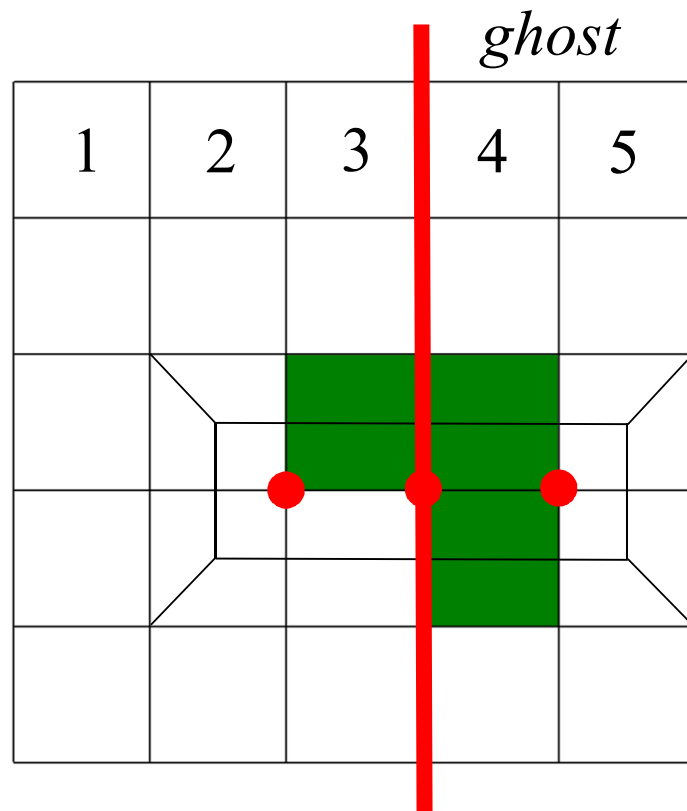


Processor 0

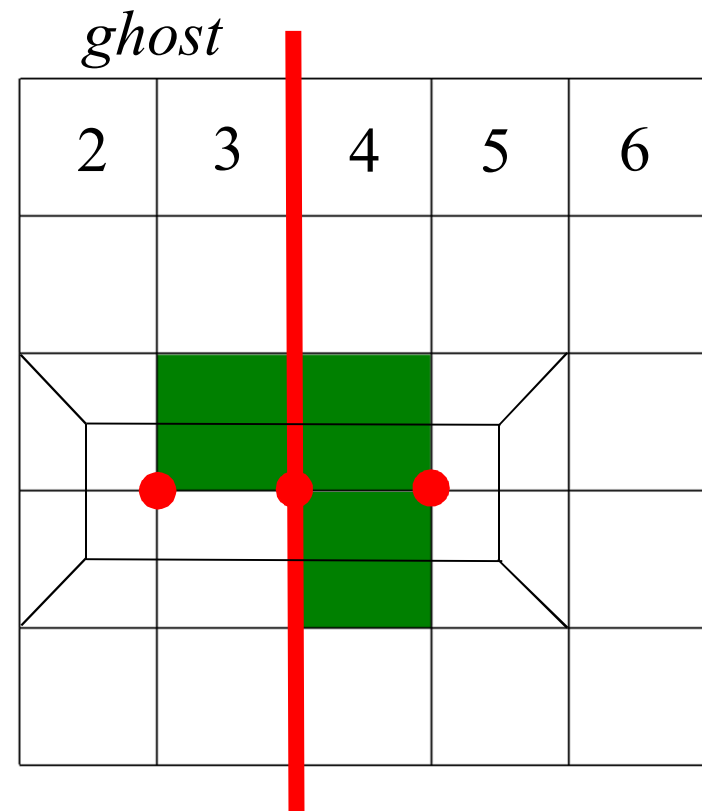


Processor 1

Parallel Communication

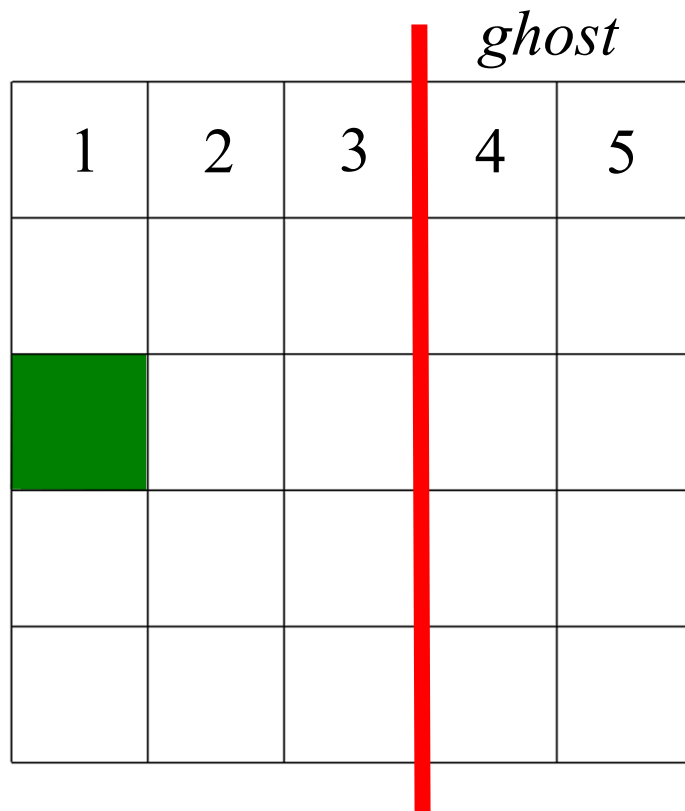


Processor 0

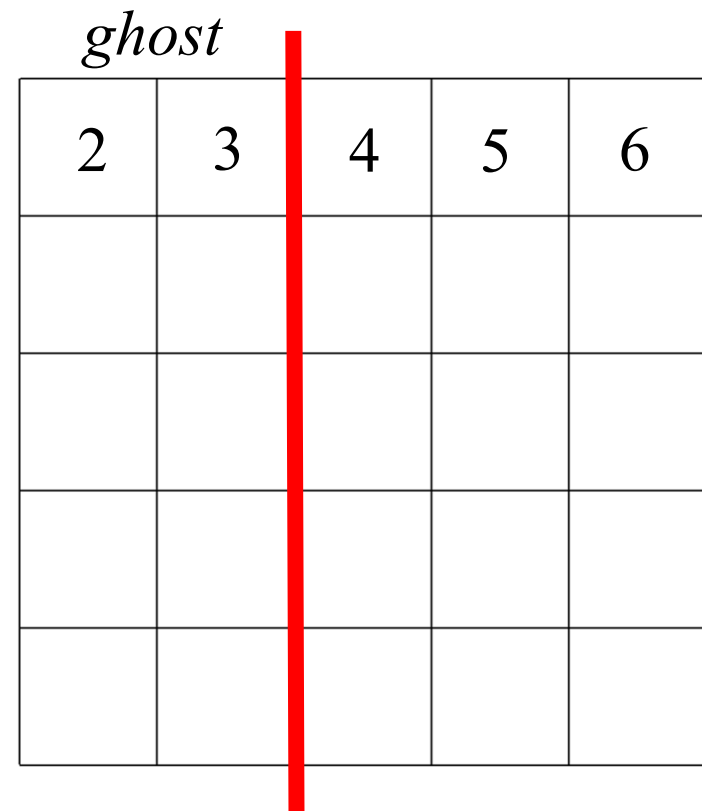


Processor 1

Parallel Communication

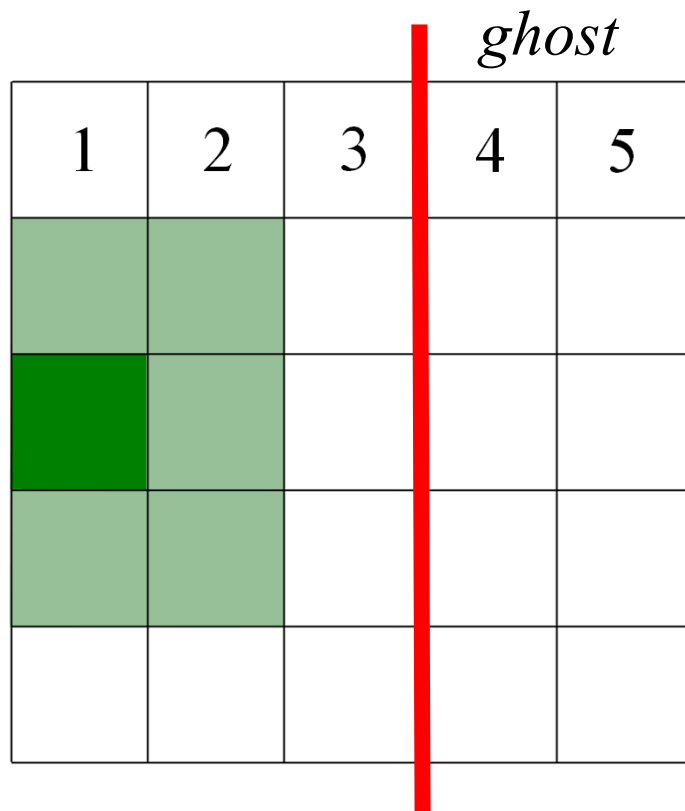


Processor 0

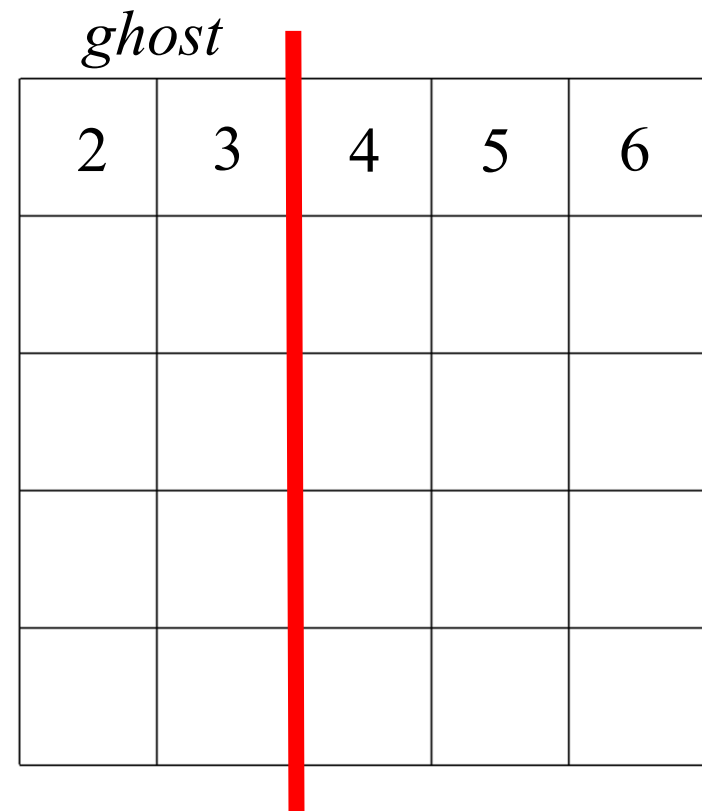


Processor 1

Parallel Communication

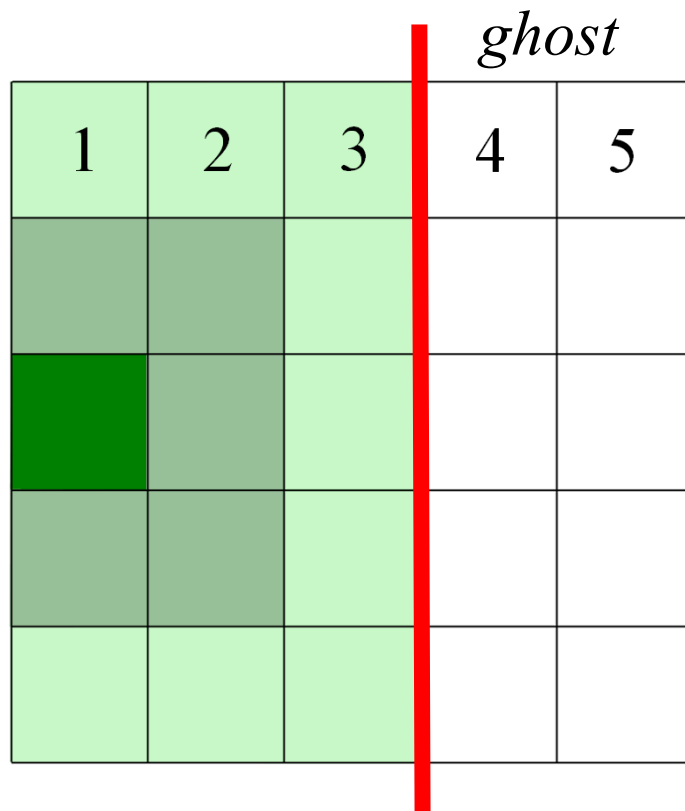


Processor 0

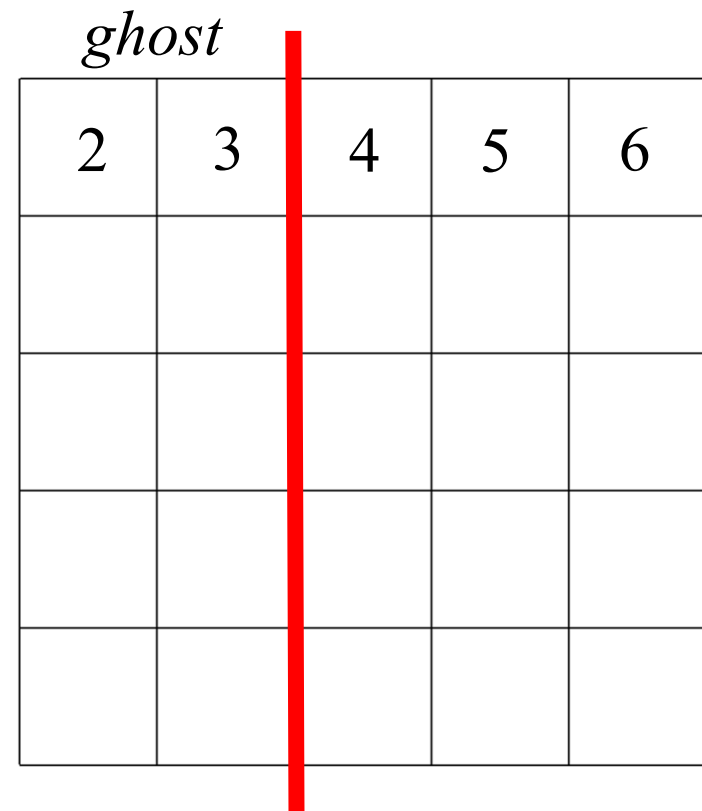


Processor 1

Parallel Communication

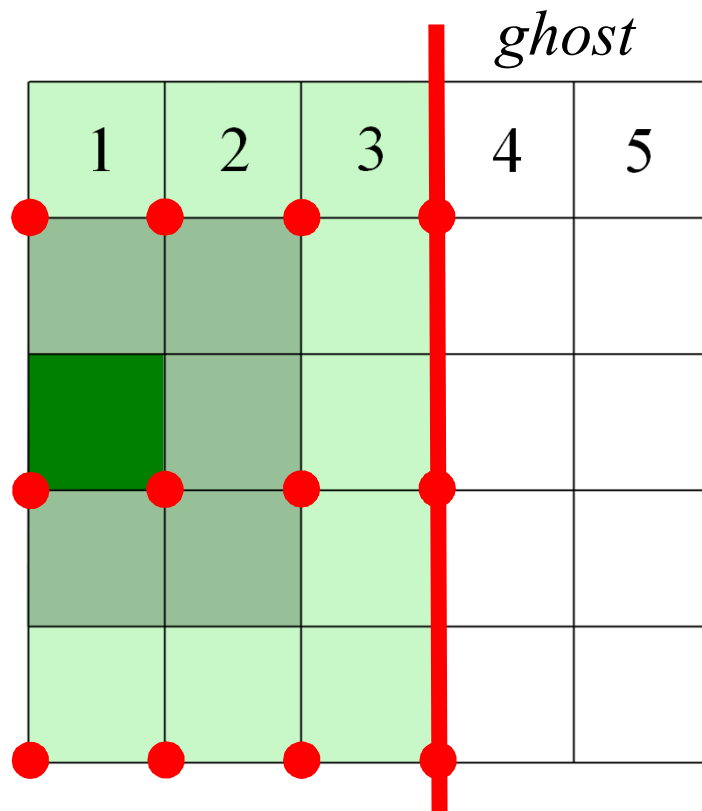


Processor 0

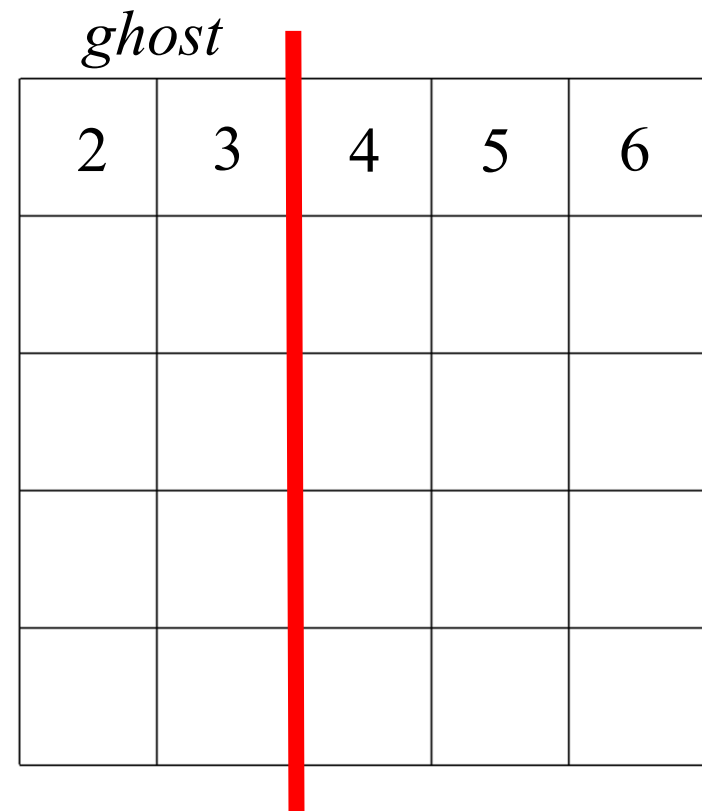


Processor 1

Parallel Communication

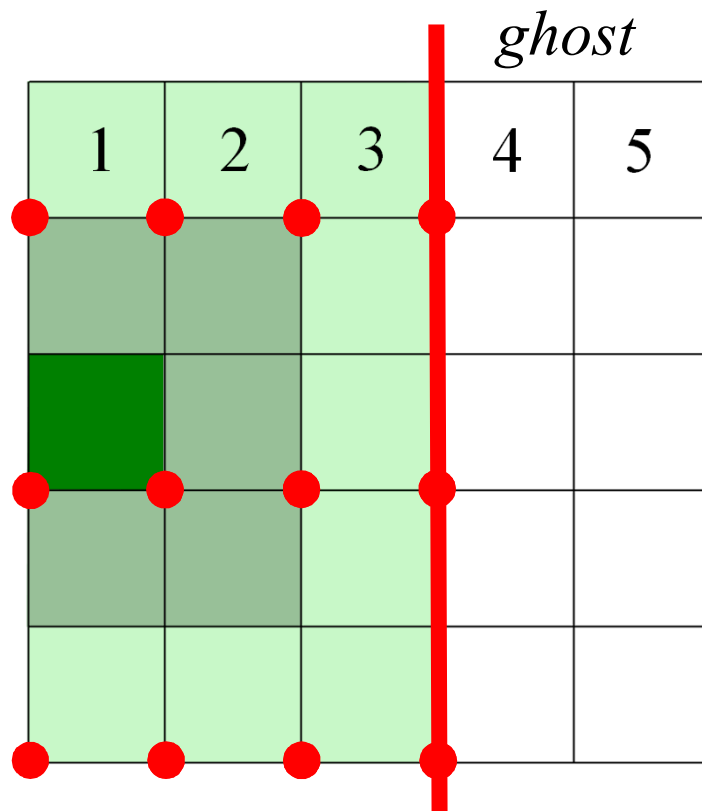


Processor 0

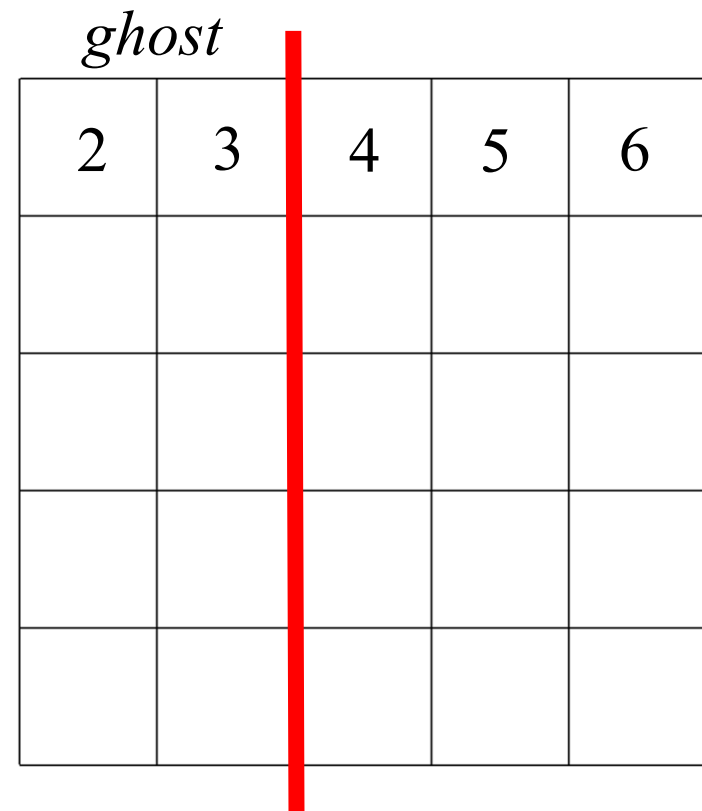


Processor 1

Parallel Communication

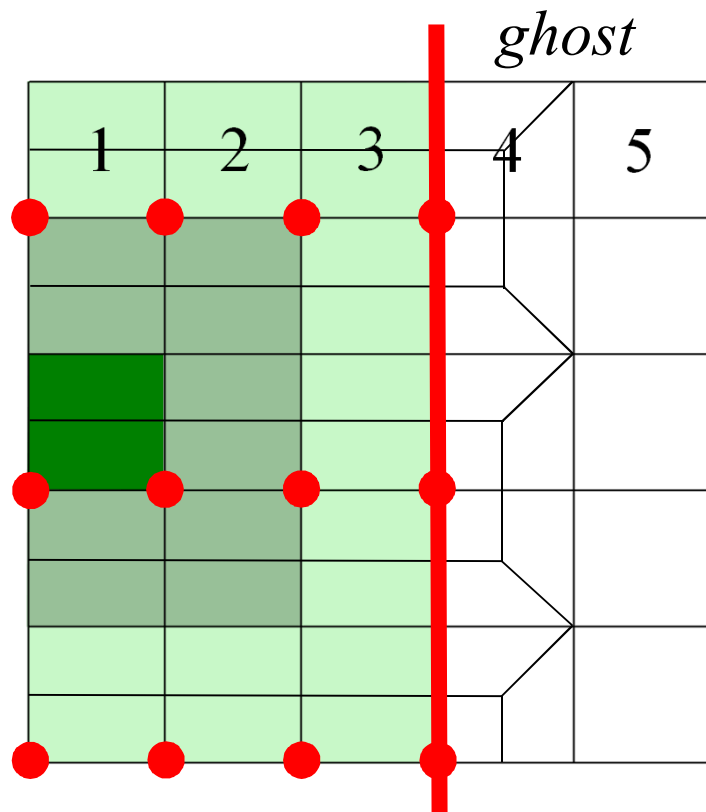


Processor 0

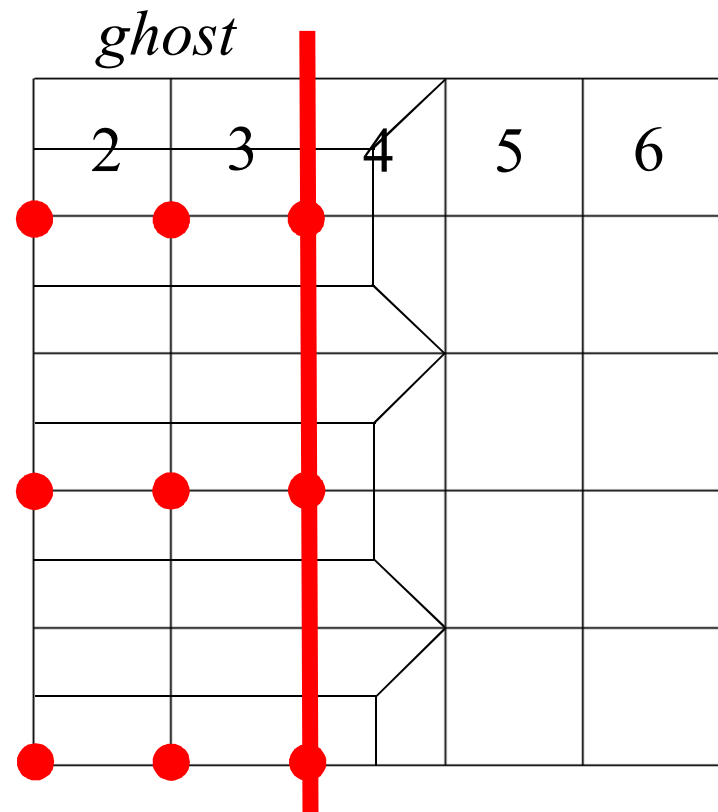


Processor 1

Parallel Communication

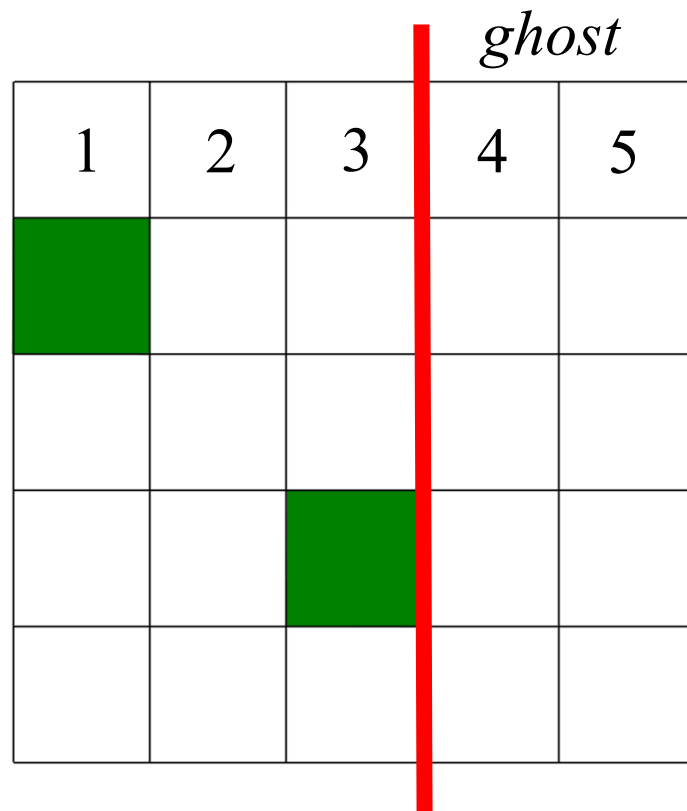


Processor 0

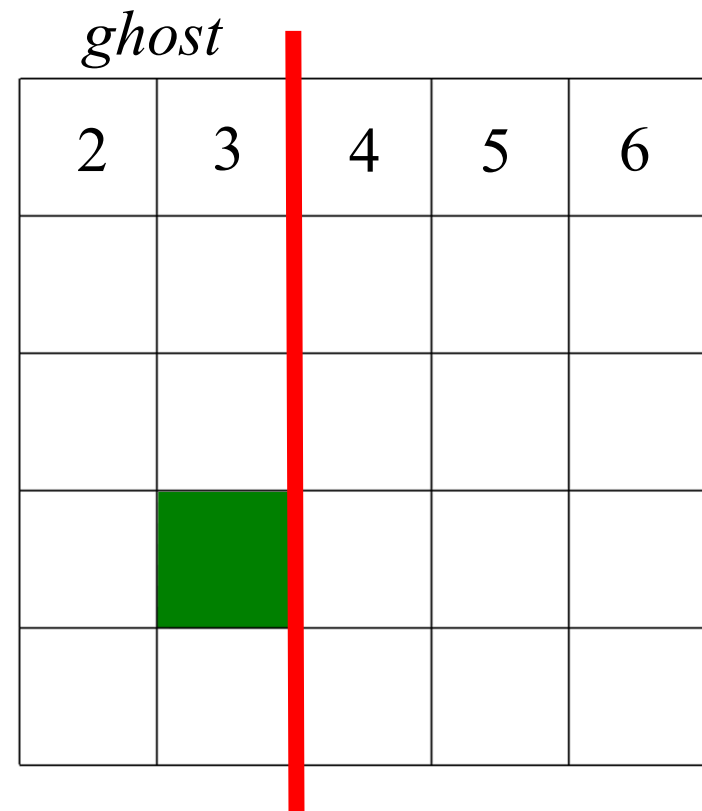


Processor 1

Parallel Communication

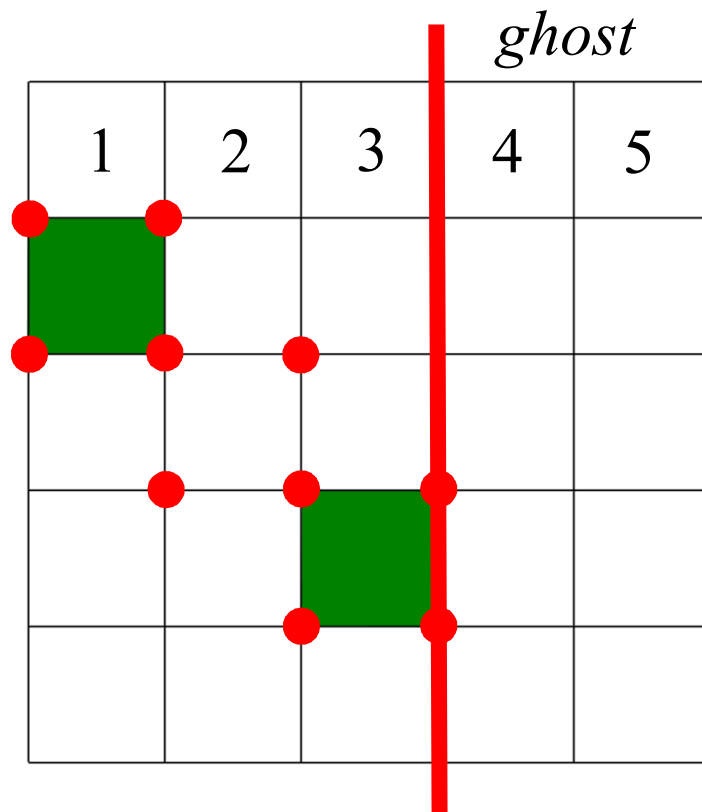


Processor 0

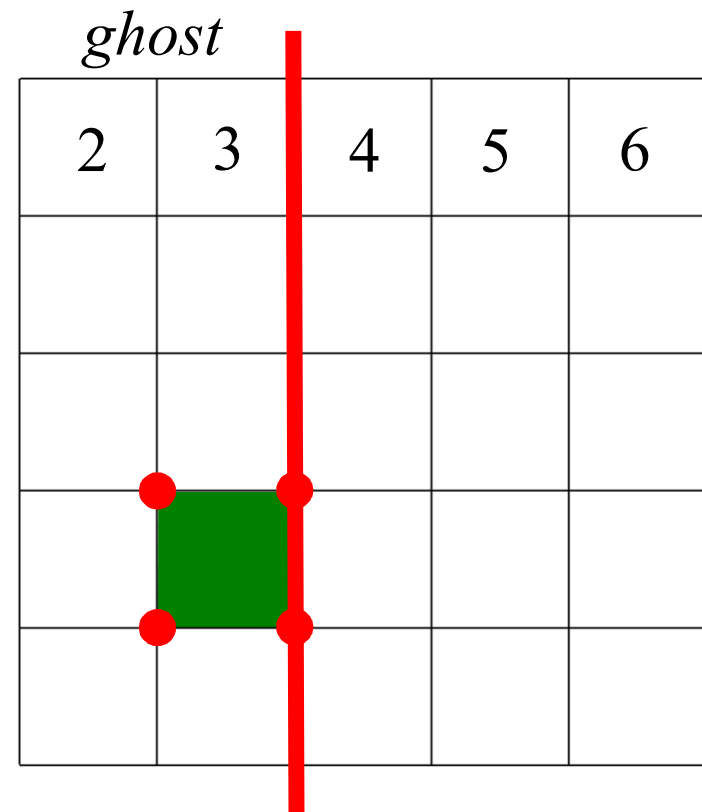


Processor 1

Parallel Communication

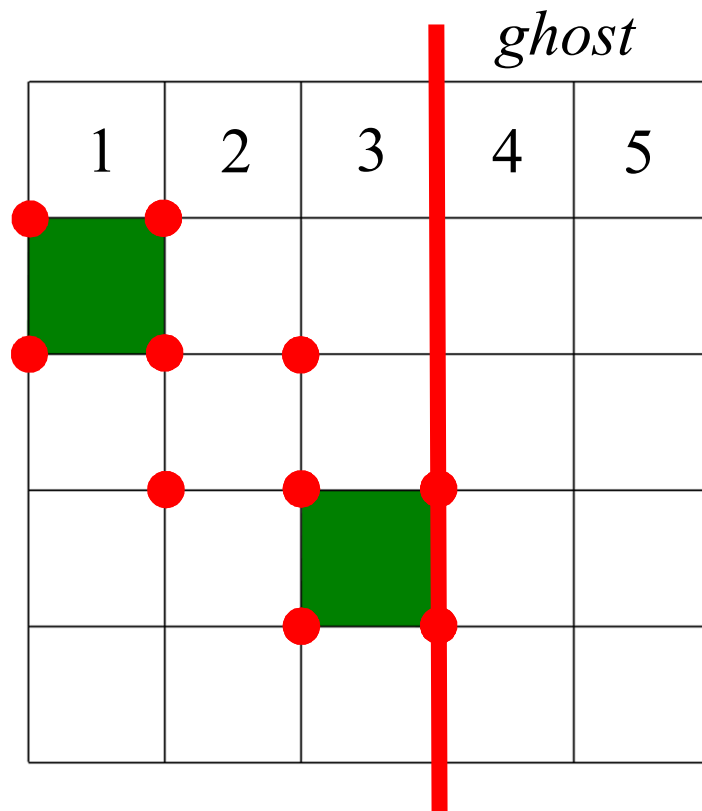


Processor 0

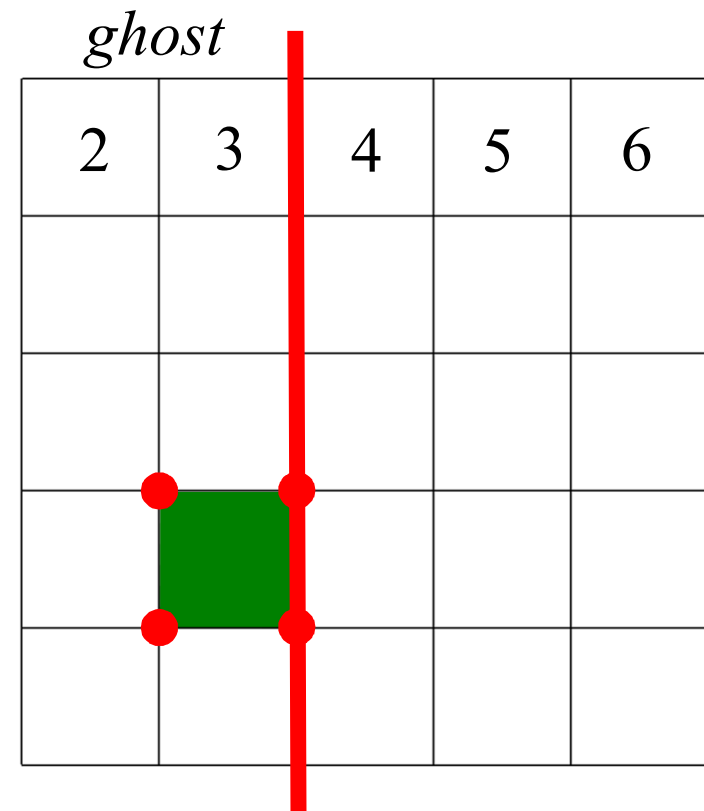


Processor 1

Parallel Communication

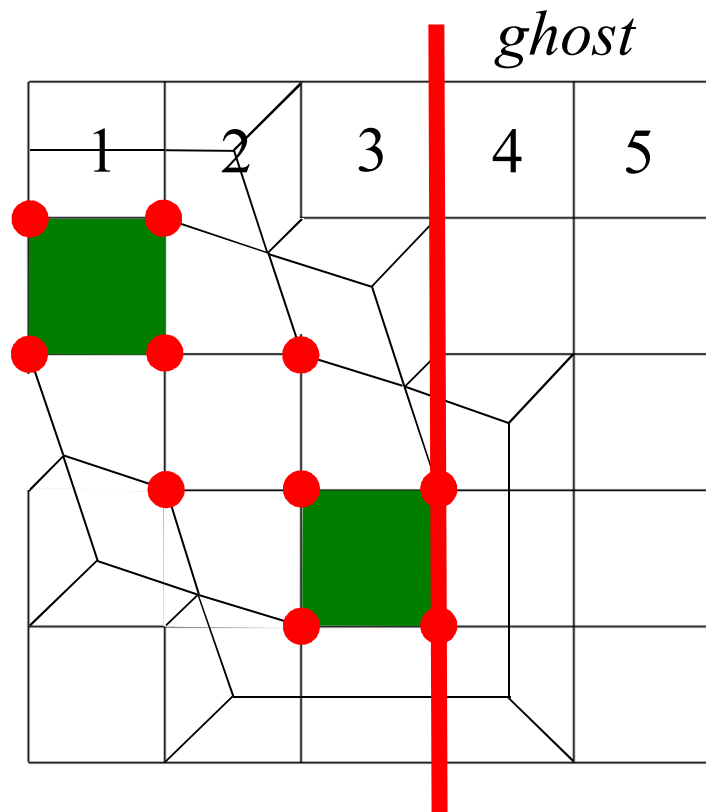


Processor 0

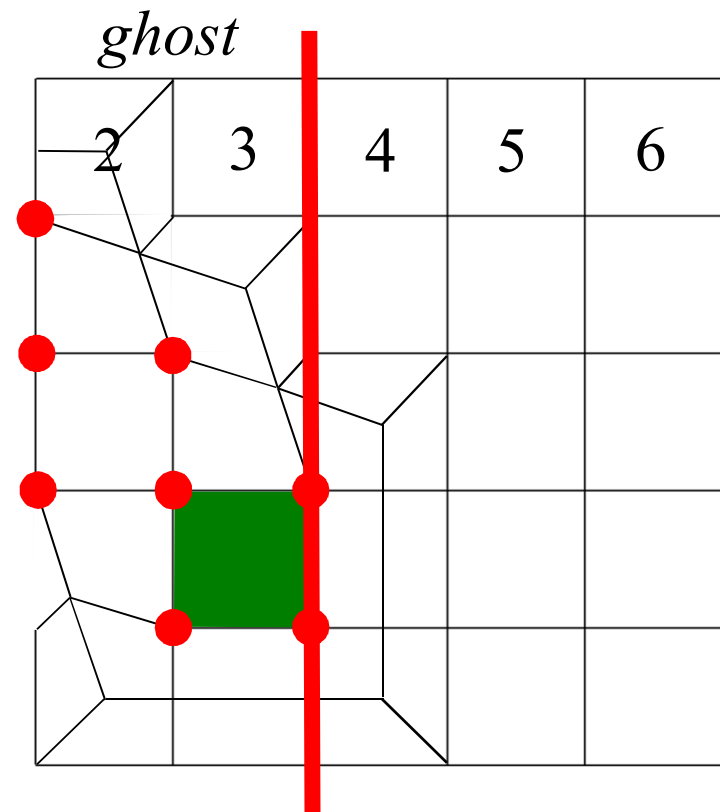


Processor 1

Parallel Communication

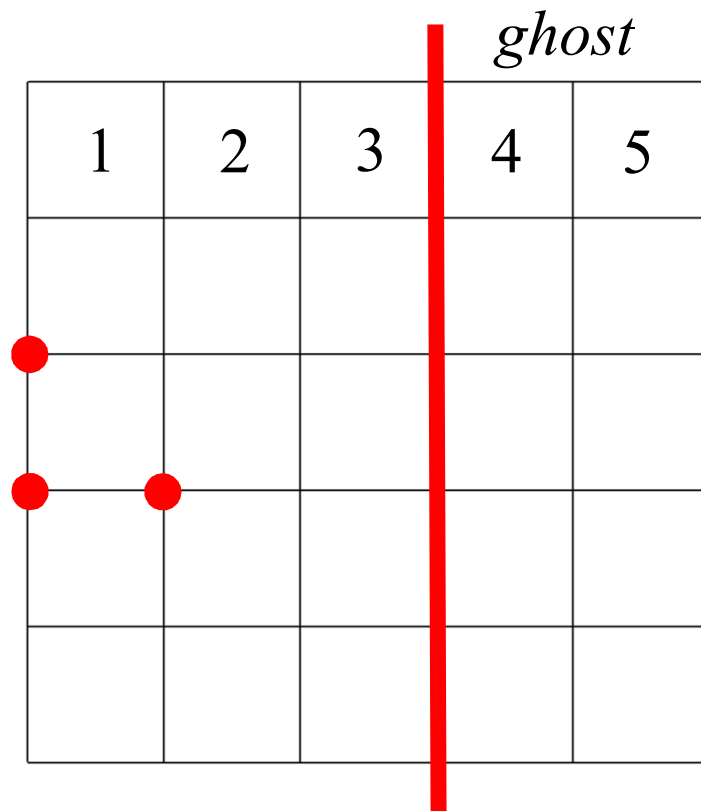


Processor 0

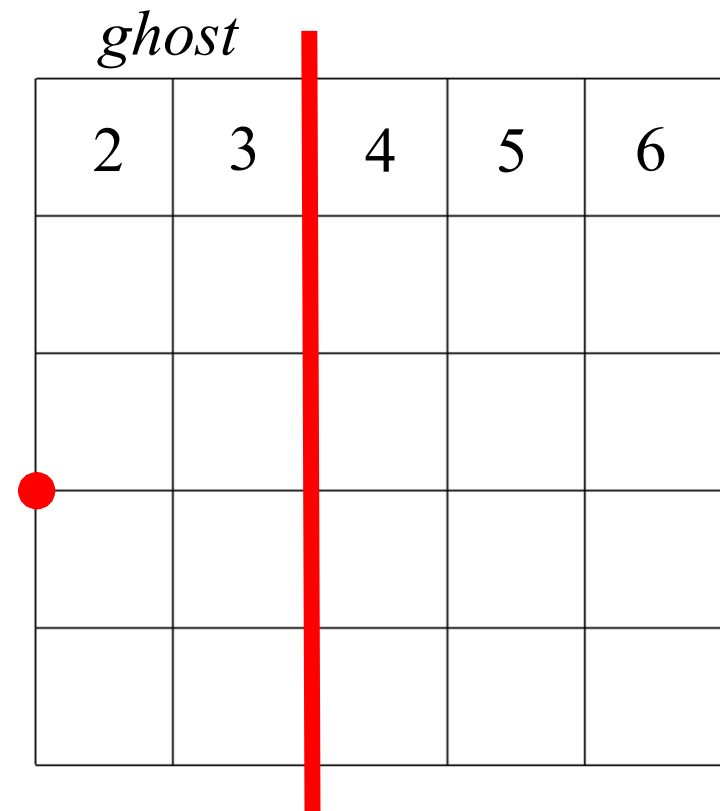


Processor 1

Parallel Communication

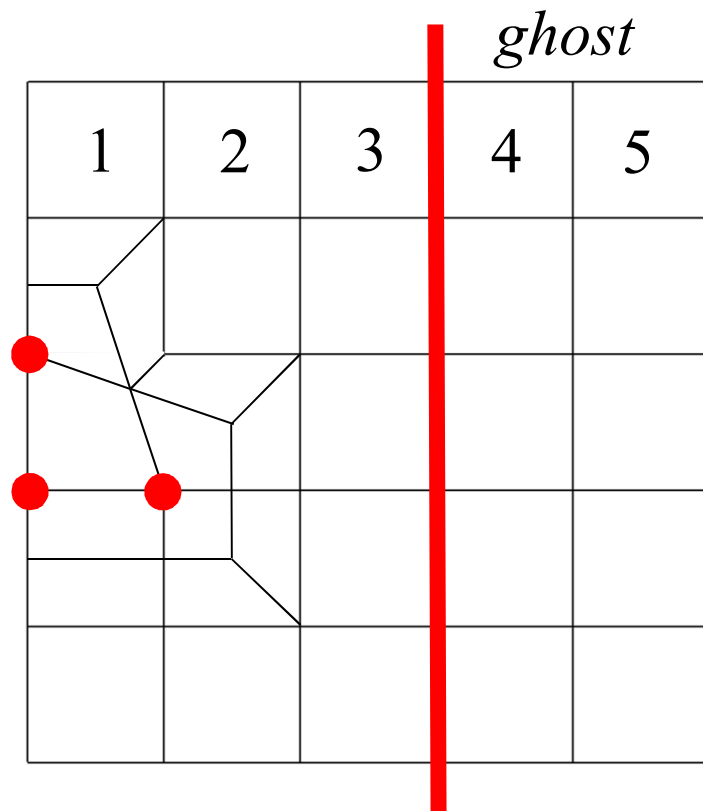


Processor 0

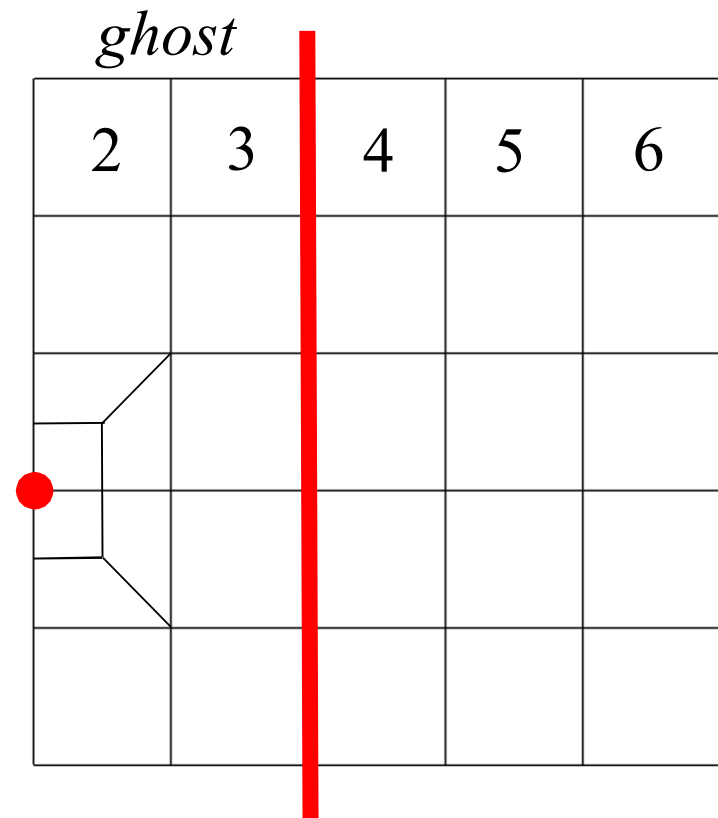


Processor 1

Parallel Communication

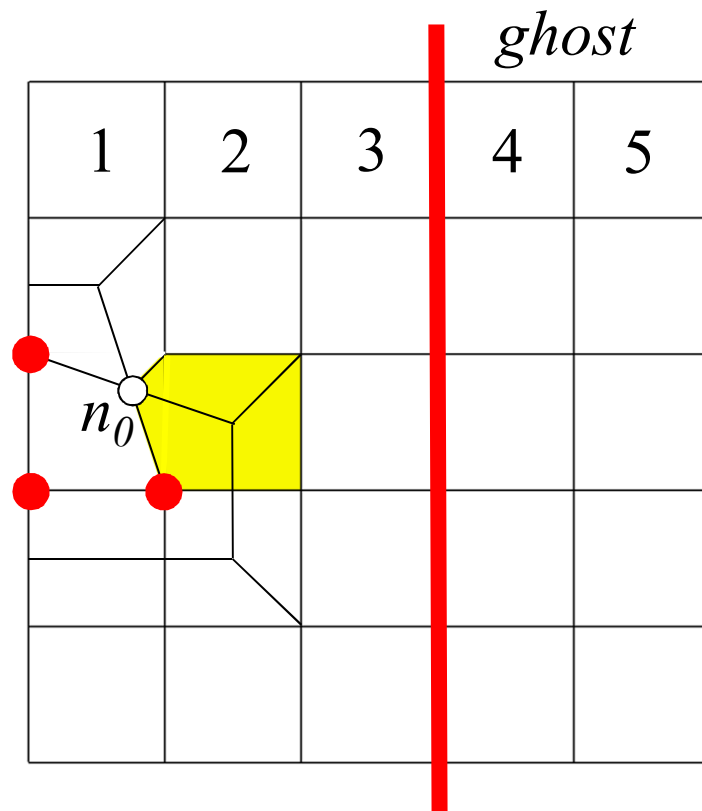


Processor 0

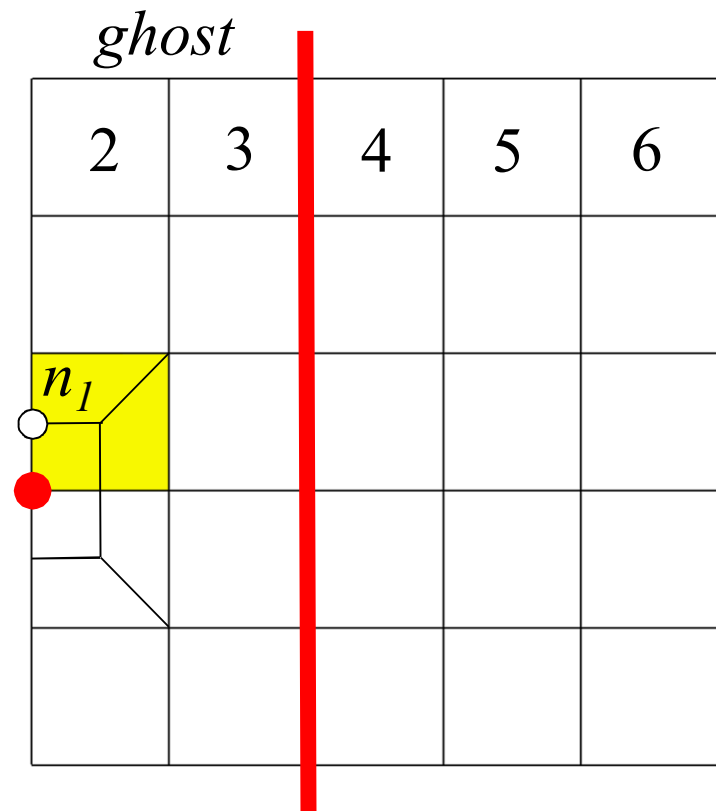


Processor 1

Parallel Communication

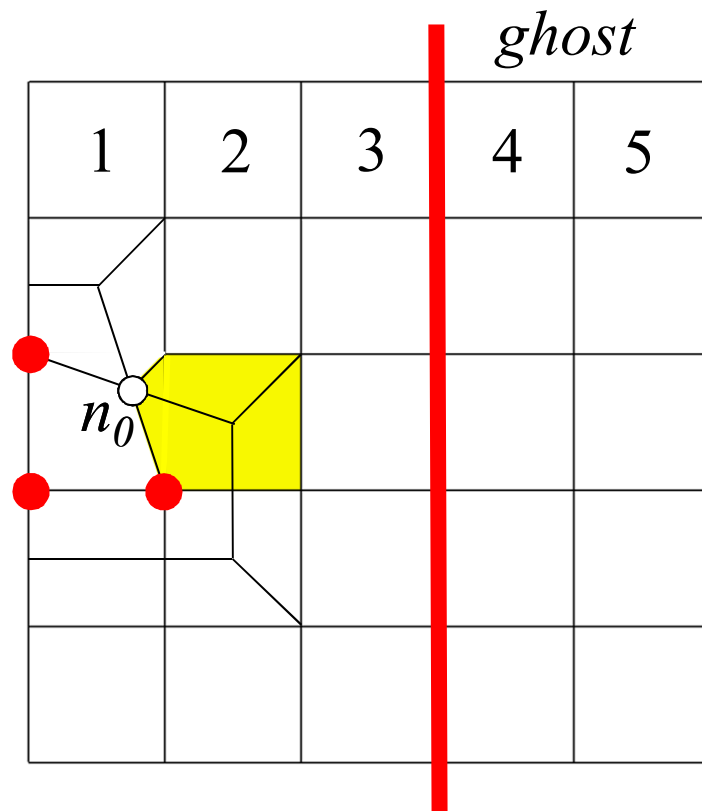


Processor 0

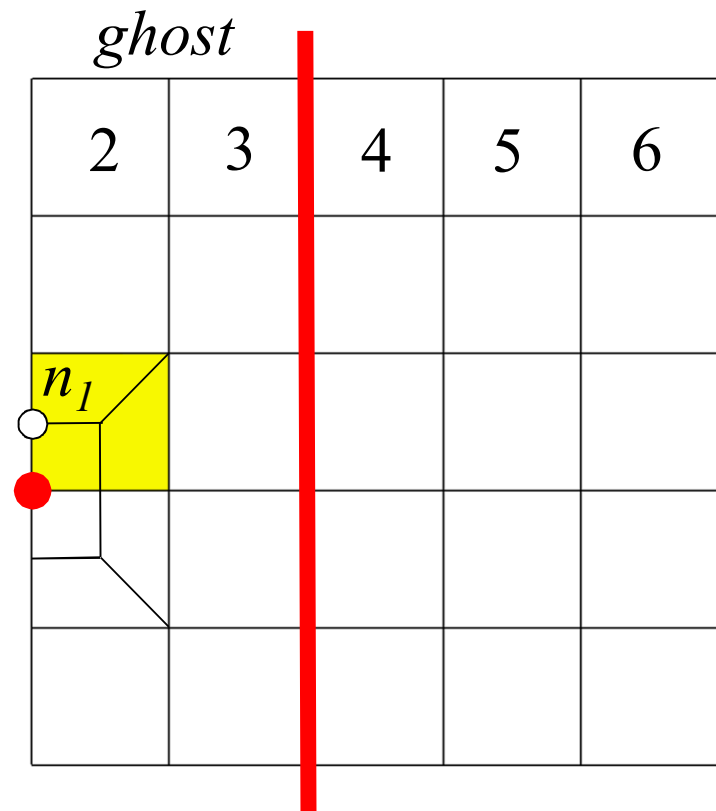


Processor 1

Parallel Communication

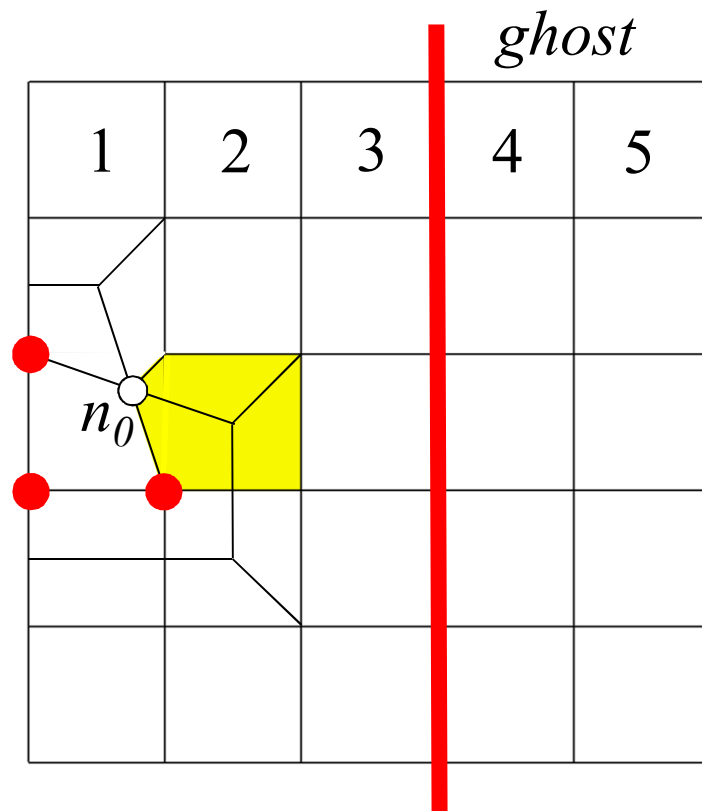


Processor 0

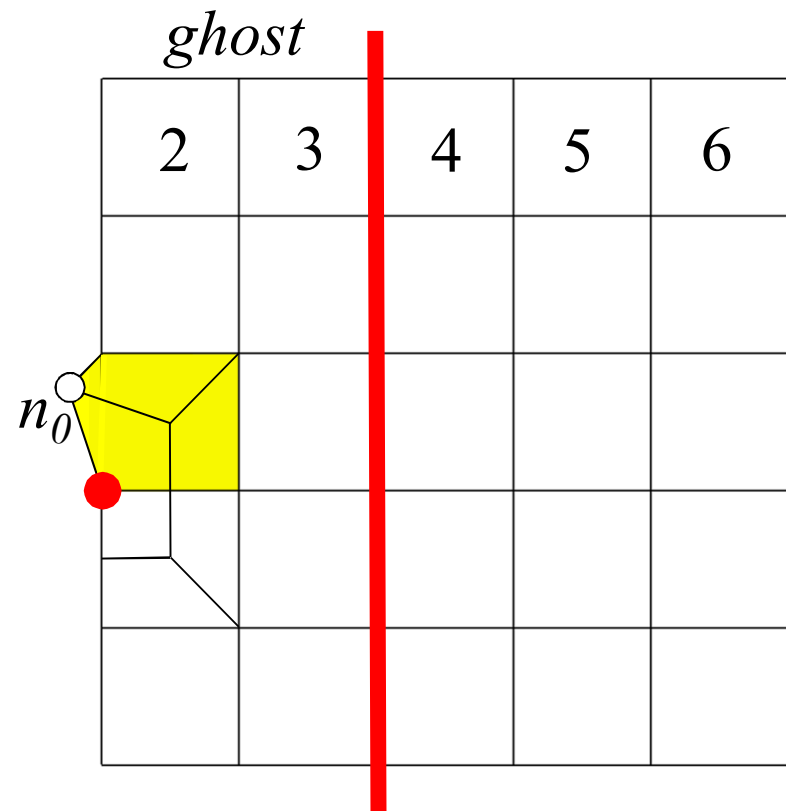


Processor 1

Parallel Communication

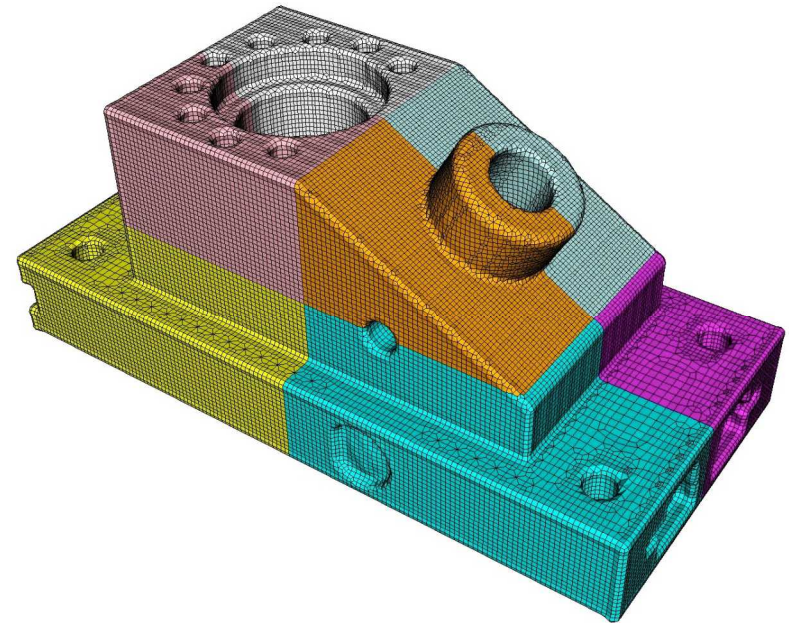
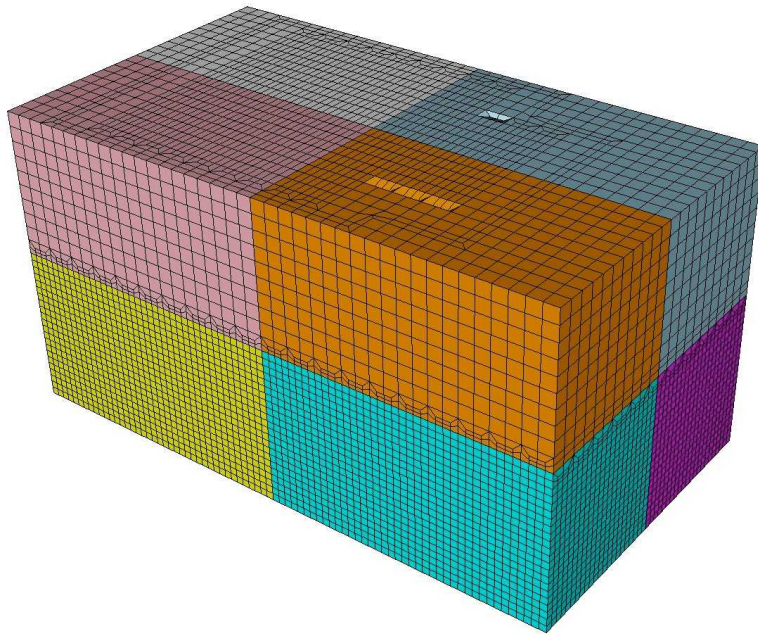


Processor 0



Processor 1

Parallel Results



Redsky

519/4,152 nodes/cores
2.93GHz Intel, 12GB/node

Chama

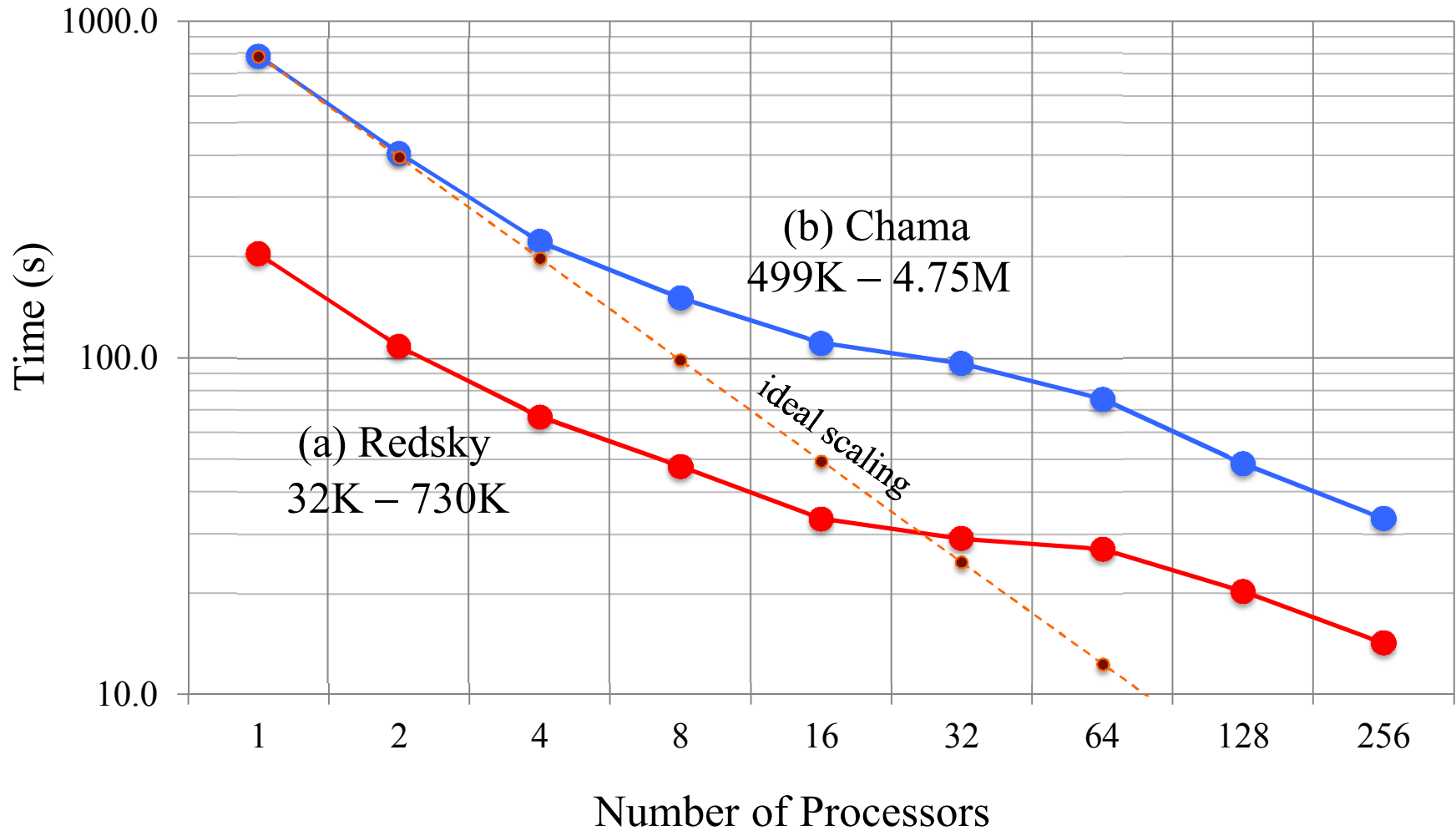
1,232/19,712 nodes/cores
2.6GHz Intel, 64GB/node

Initial Hexes in Cartesian Grid
Hexes in Refined Grid
Minimum Scaled Jacobian

32,400
730,512
0.408

498,960
4,750,848
0.408

Time to Refine model anc101



Conclusions

- 2-Refinement based on node marking procedure and 4 templates (3D)
- Uses up to 3 layers to transition
- Minimum Scaled Jacobian 0.408
- Distributed Parallel Implementation with Sculpt
- Parallel-consistent (Same result regardless of decomposition)
- Multiple levels of refinement

