

SAND2015-10729C

# Low-Level Track Finding and Completion using Random Fields

Tu-Thach Quach    Rebecca Malinas    Mark W. Koch

Sandia National Laboratories

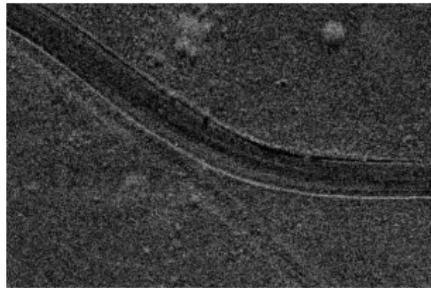
February 18, 2016



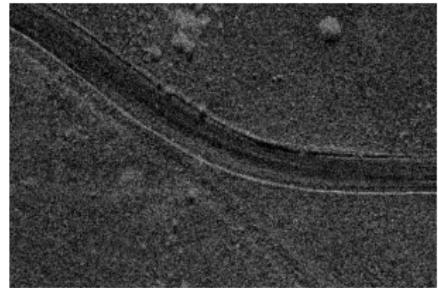
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# Coherent Change Detection (CCD) Image

Morning

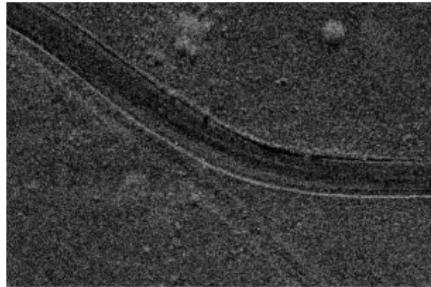


Afternoon

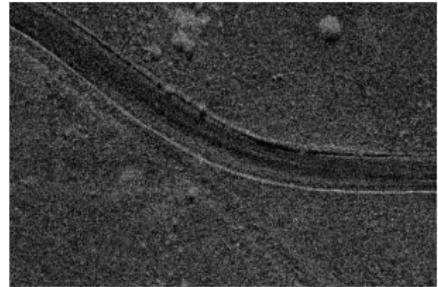


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- 4 Form CDT graph using obtained tracks as *constrained* edges
- 5 Optimize energy function:

$$\sum_{i \in E} f_i(x_i) + \sum_{i, j \in N} [x_i \neq x_j][i \in E_C \vee j \in E_C] g_{ij}(x_i, x_j)$$

## Forming Initial Binary Image

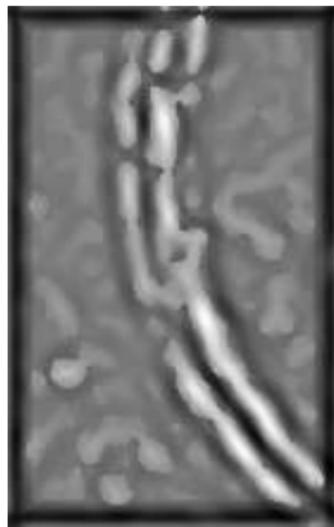


Input CCD Image

## Forming Initial Binary Image



Input CCD Image

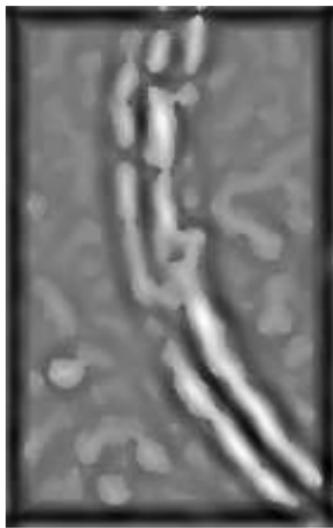


Ridge Feature

## Forming Initial Binary Image



Input CCD Image

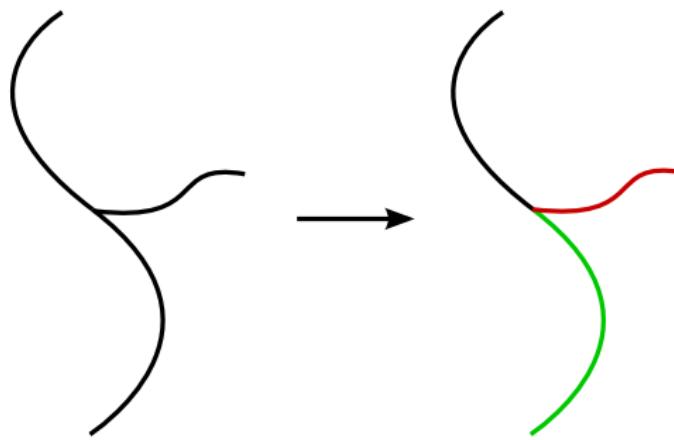


Ridge Feature

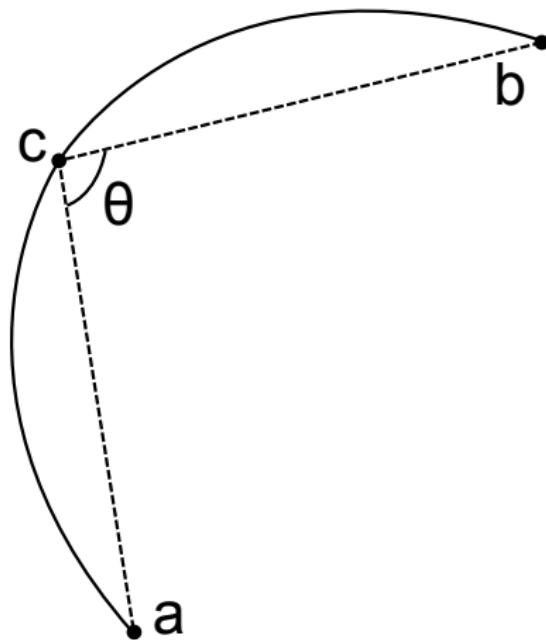


Thresholded Image

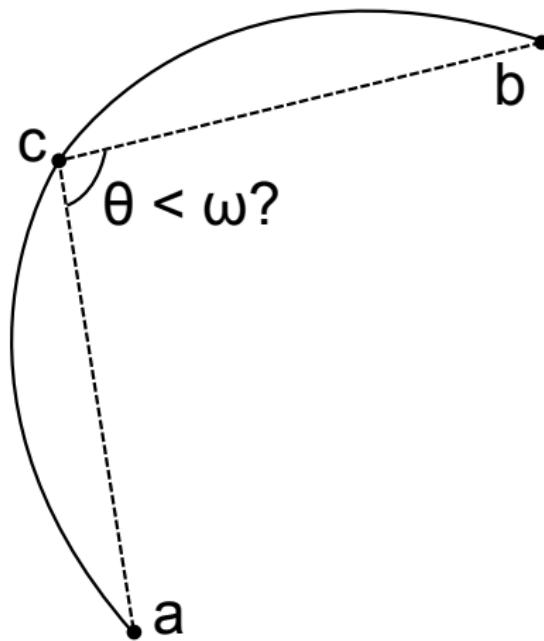
# Branching



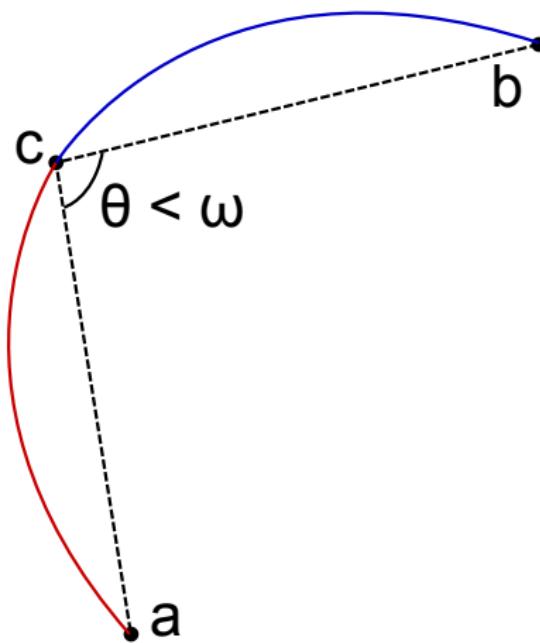
# Linearization



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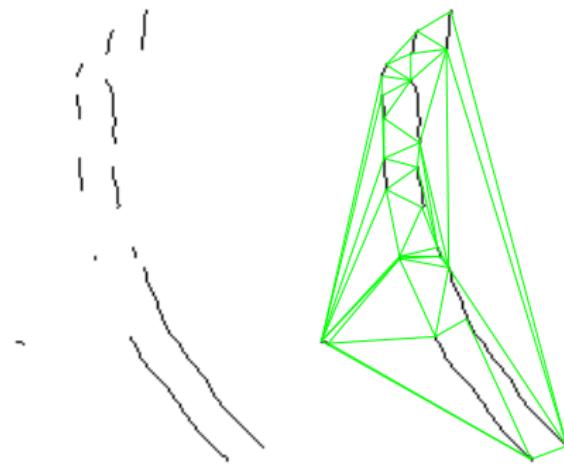
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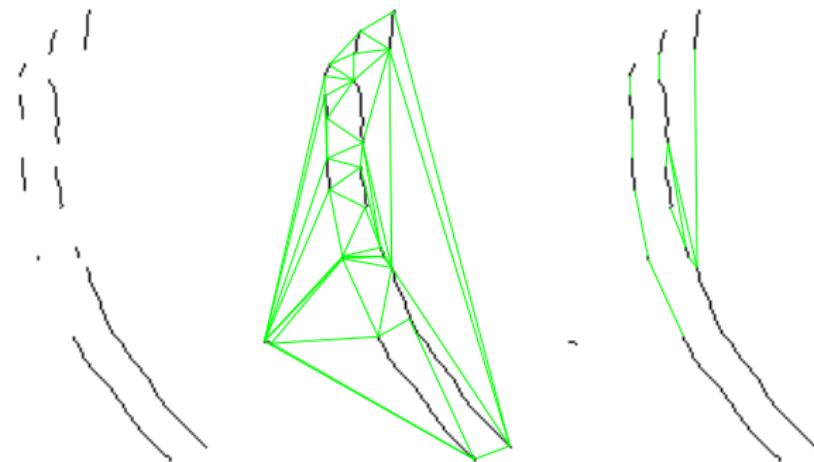
# Constrained Delaunay Triangulation (CDT) Graph



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# Optimization

$E$ : edges of CDT graph

$E_C \subset E$ : constrained edges

$N \subset E \times E$ : neighborhood system

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$E_C \subset E$ : constrained edges

$N \subset E \times E$ : neighborhood system

Minimize binary energy function ( $x_i \in \{0, 1\}$ ):

$$\sum_{i \in E} \underbrace{f_i(x_i)}_{\text{Unary}} + \sum_{i, j \in N} \underbrace{[x_i \neq x_j][i \in E_C \vee j \in E_C]g(i, j)}_{\text{Pairwise}}$$

## Unary Cost

$\mathcal{P}(i)$ : set of pixels corresponding to edge  $i$

$\lambda^i = \frac{1}{|\mathcal{P}(i)|} \sum_{j \in \mathcal{P}(i)} \lambda_j$ : average ridge feature along edge  $i$

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By central limit theorem,

$$p(\lambda^i | x_i = 0) \approx \mathcal{N}(\mu_0, \sigma_0 / \sqrt{|\mathcal{P}(i)|}),$$

$$p(\lambda^i | x_i = 1) \approx \mathcal{N}(\mu_1, \sigma_1 / \sqrt{|\mathcal{P}(i)|}),$$

$\mu_0$  and  $\sigma_0$ : mean and standard deviation of background ridge feature

$\mu_1$  and  $\sigma_1$ : mean and standard deviation of track ridge feature

## Pairwise Cost

$\theta_{ij}$ : angle formed by edges  $i$  and  $j$

$$g(i, j) = \frac{\alpha}{1 + \exp(-\beta(\theta_{ij} - \theta_0))}$$

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Edges with large angles should have the same class

## Sub-Modular Energy Function

Minimize binary energy function:

$$\sum_{i \in E} f_i(x_i) + \sum_{i,j \in N} [x_i \neq x_j] [i \in E_C \vee j \in E_C] g(i,j)$$

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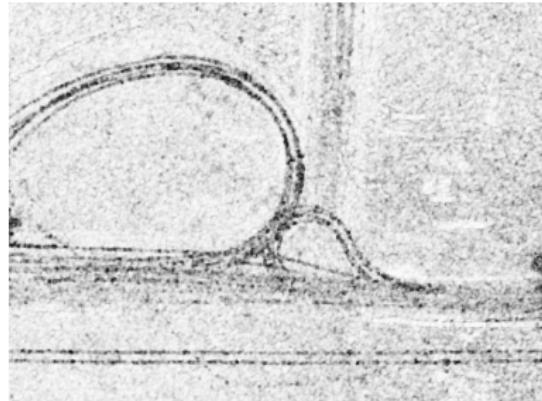
Pairwise cost is sub-modular  $\rightarrow$  global solution obtained via graph cut

Sub-modular:  $\psi(0,0) + \psi(1,1) \leq \psi(0,1) + \psi(1,0)$

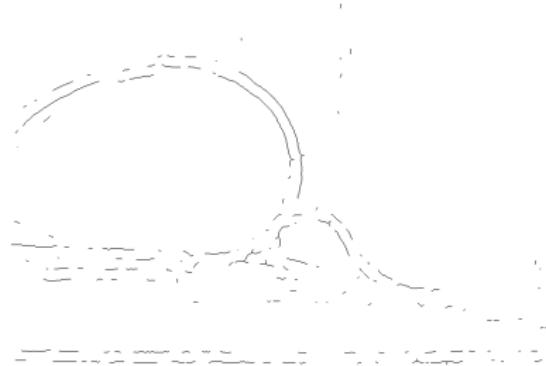
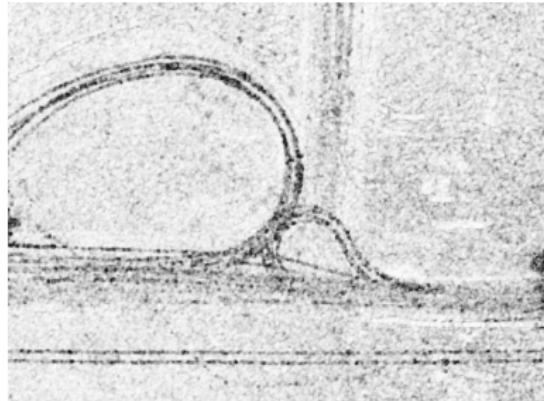
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Kolmogorov, V., Zabih, R., "What Energy Functions Can Be Minimized via Graph Cuts," *IEEE Trans. Pattern Anal. Mach. Intell.*, 2004.

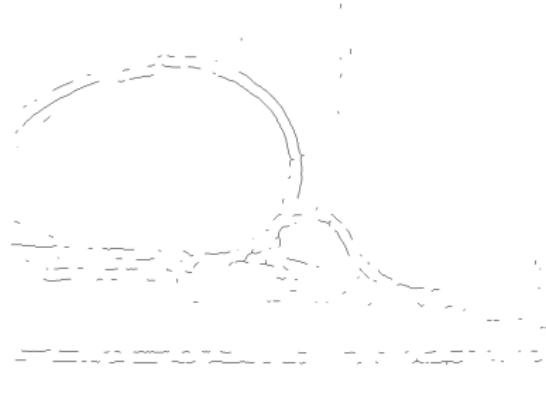
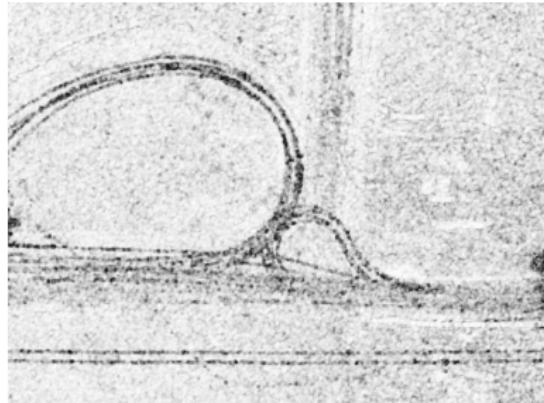
## Qualitative Results



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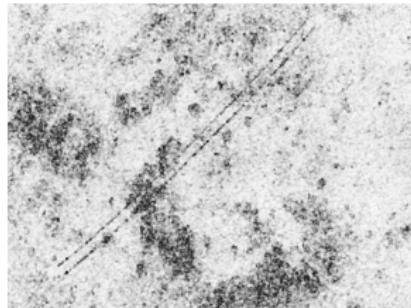
## Quantitative Results

## Data sets:

Dark



Medium



Accuracy:

$$\frac{TP}{GT + FA}$$

## Quantitative Results

	Model-Based <sup>1</sup>	Current
<i>dark</i>	0.9767	<b>0.9941</b>
<i>medium</i>	0.8429	<b>0.9822</b>

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<sup>1</sup>Quach et al., "A Model-Based Approach to Finding Tracks in SAR CCD Images," *IEEE CVPR Workshops*, 2015.

# Conclusion

- Track completion via CDT + random field is useful in completing tracks
- Approach is fast: less than 1 second on 600-by-800 image
- Future work: leverage parallel nature of tracks

Thank You

tong@sandia.gov