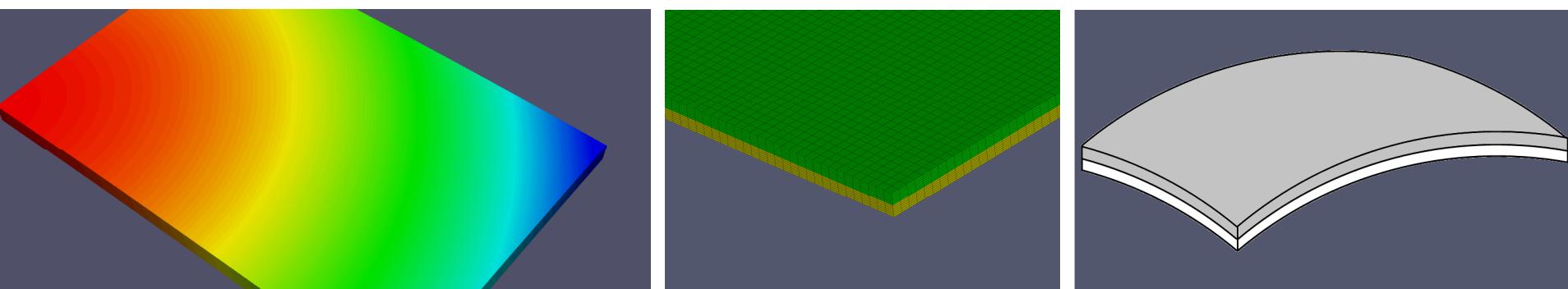


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# ASC V&V: Residual Stress Modeling

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ORG. 8259, Multi-Physics Modeling and Simulation



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# Outline

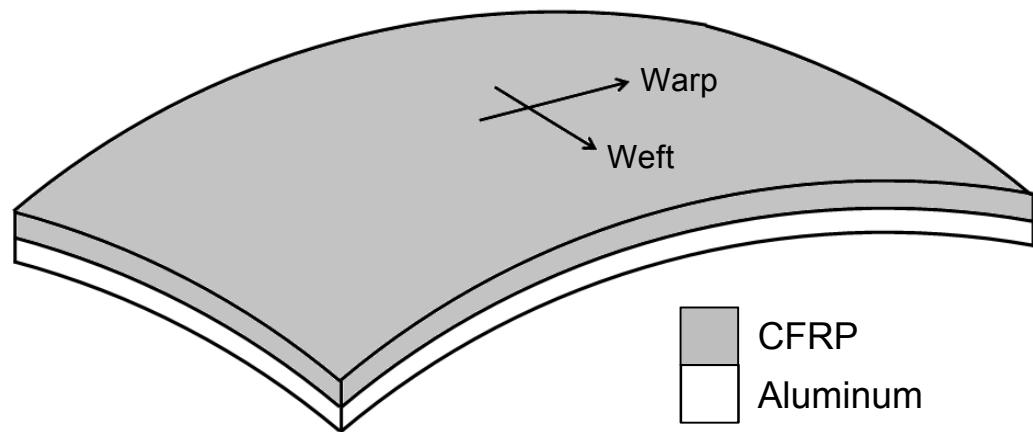
- Current Presentation Objectives
- Preliminary Model Details
  - Test specimen description and measured experimental data
  - Finite element model description
    - Material properties
    - Discretization study
    - Sample results and post-processing methodology
- Modeling Approaches
  - CTE mismatch only
  - CTE mismatch + “shrinkage”
  - Additional curing cycle considerations
- Conclusions & Future Considerations

# Current Presentation Objectives

- Develop modeling methodology that can be used to simulate the formation of residual stresses in co-cured and co-bonded composite structures
- Preliminary efforts are based a simple, co-bonded Al and CFRP plate
  - Determine ideal material models (elastic vs. elastic-orthotropic)
  - Determine an approach for simulating an approximation of a composite's rheological behavior during curing
  - Determine an optimum approach while minimizing model complexity
    - Planned sensitivity study, material model calibration, and uncertainty quantification require a robust and computationally inexpensive modeling method

# Preliminary Model

- Co-bonded Aluminum-  
CFRP plate
  - 4.0 x 6.0 inch plate
  - Aluminum
    - AL 6061-T6
    - thickness = 0.0625 inch
  - CFRP
    - 4 plies of an 8 harness satin weave prepreg
    - thickness = 0.063 inch



Location	Radius of Curvature (in)
Warp, Center	38
Warp, Edge	33
Weft, Center	38
Weft, Edge	28

# Material Model Consideration

- Aluminum
  - Elastic-Isotropic
- CFRP
  - Elastic-Isotropic
  - Elastic-Orthotropic

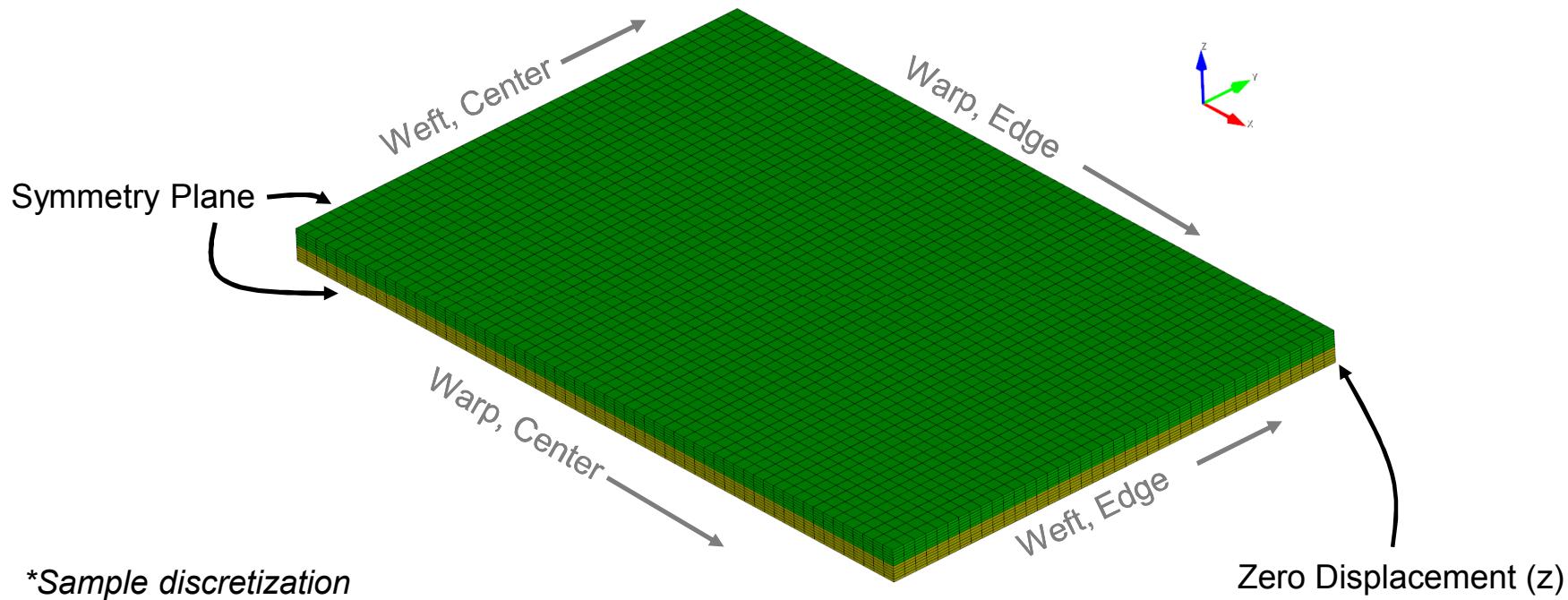
Property	Aluminum	CFRP
$E_{11}$		63.86 (GPa)
$E_{22}$	71.3 (GPa)	62.74 (GPa)
$E_{33}$		8.59 (GPa)
$G_{12}$		3.44 (GPa)
$G_{23}$	26.9 (GPa)	3.27 (GPa)
$G_{31}$		3.25 (GPa)
$v_{12}$		0.048
$v_{23}$	0.33	0.408
$v_{31}$		0.055
$CTE_{11}$		3.40e-6 <sup>1</sup> / 1.13e-6 <sup>2</sup> (1/K)
$CTE_{22}$	23.4e-6 (1/K)	3.36e-6 <sup>1</sup> / 1.13e-6 <sup>2</sup> (1/K)
$CTE_{33}$		72.0e-6 <sup>1</sup> / 28.3e-5 <sup>2</sup> (1/K)

<sup>1</sup> Glassy Region

<sup>2</sup> Rubbery Region

# Model Description

- Quarter symmetry conditions were applied for efficiency
- Applied Thermal boundary conditions simulate heating requirements of the prepreg's cure cycle



# Mesh Convergence Study

- Confirm that simulated solutions converge to the same continuum value
- Determine appropriate mesh size for all ensuing models

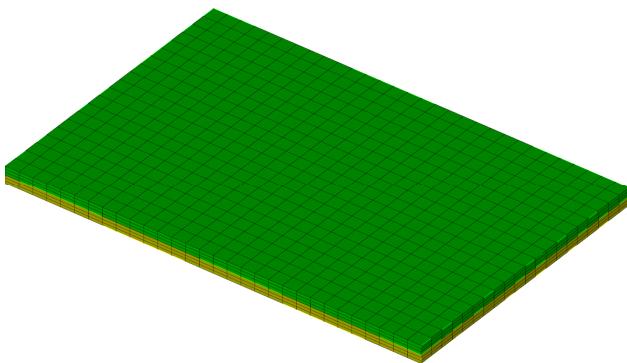


Plate-I

- 3,600 elements
- 3 elements through each layer

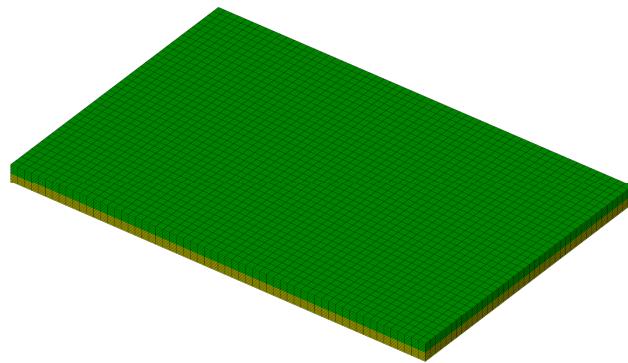


Plate-II

- 28,800 elements
- 6 elements through each layer

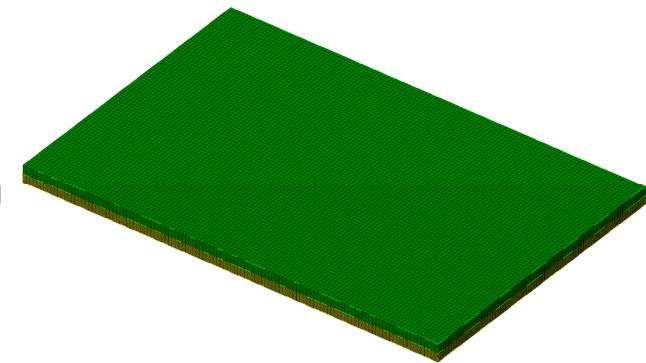


Plate-III

- 230,400 elements
- 12 elements through each layer

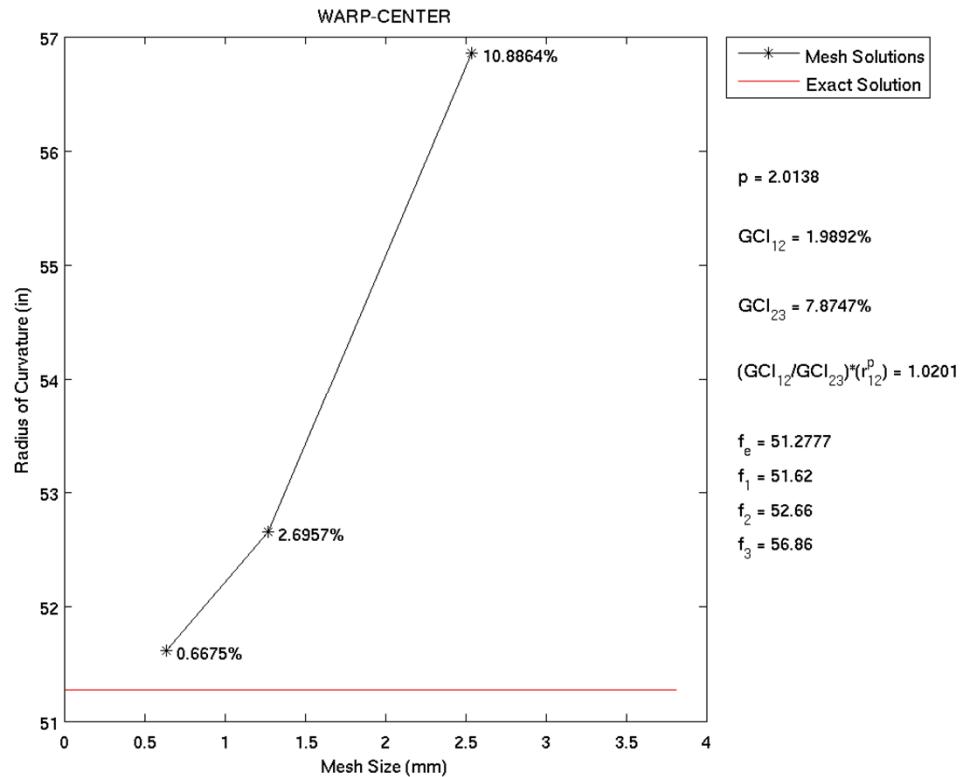
# Mesh Convergence Study

- Richardson's Extrapolation

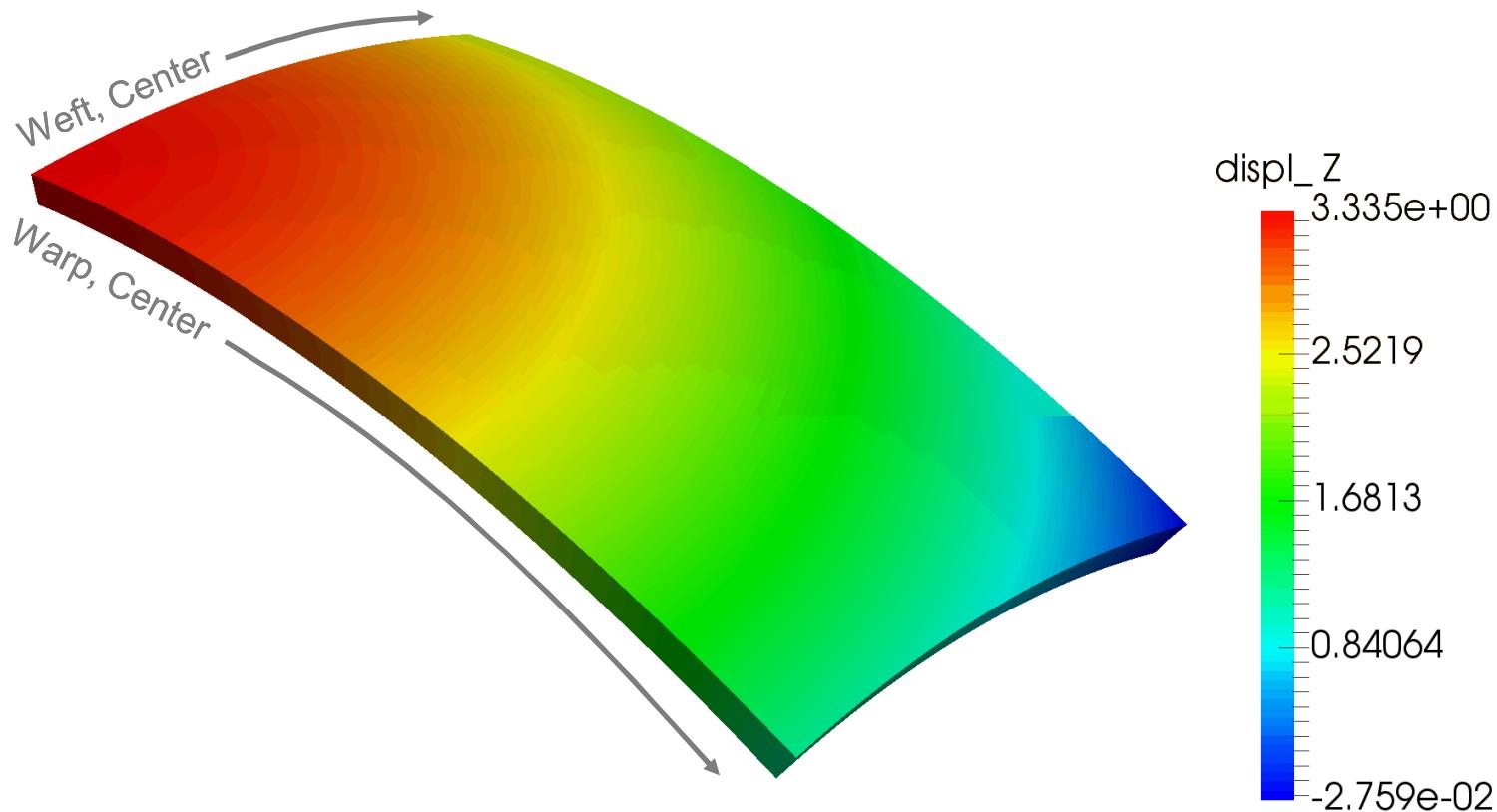
$$f_{exact} = f_1 + \frac{f_1 - f_2}{r^p - 1}$$

- Mesh Convergent

- plate-II
- 2.7% error (center)
- 3.3% error (edge)
- < 4 min runtime (12 cores)



# Sample Results



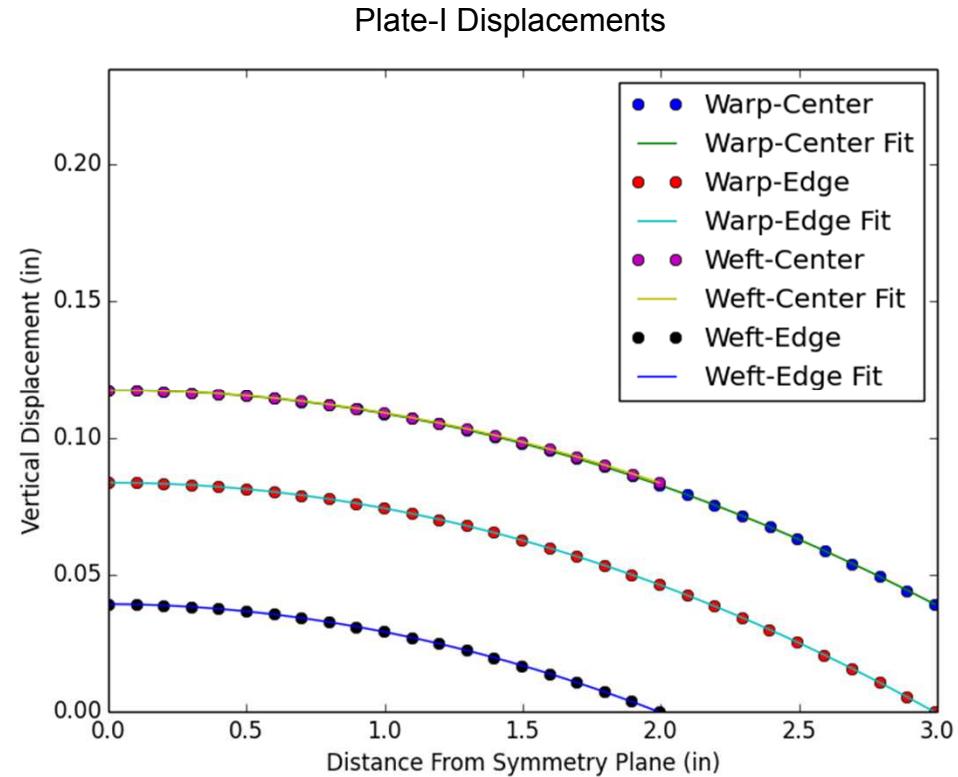
# Post-Processing Methodology

- Quadratic Fit

$$f(x) = Ax^2 + Bx + C$$

$$\kappa = \frac{f''}{(1 + f'^2)^{3/2}}$$

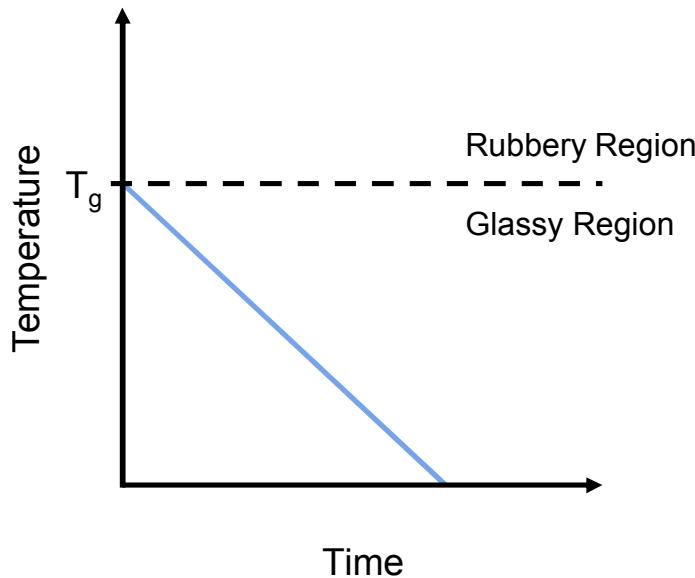
$$r = \frac{1}{\kappa} = \frac{(1 + (2Ax + B)^2)^{3/2}}{2A}$$



# Modeling Approach #1

## Cooldown Only

- Begin at  $T_g$  and cool to room temperature
- CFRP modeled as elastic, isotropic
- Simplest approach
- Considers CTE effects only

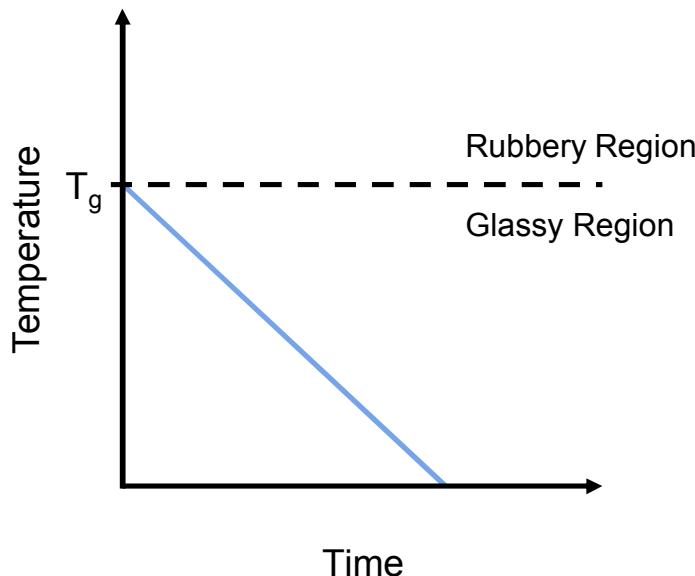


Location	Radius of Curvature (in)	
	Experiment	Model
Warp, Center	38	44.7
Warp, Edge	33	44.6
Weft, Center	38	44.8
Weft, Edge	28	44.1

# Modeling Approach #2

## Cooldown Only

- Same as Approach #1
- CFRP modeled as elastic, 3D orthotropic

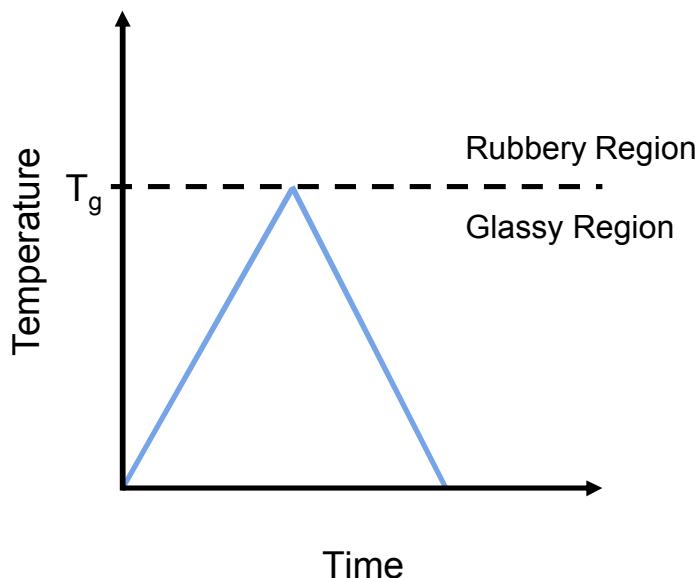


Location	Radius of Curvature (in)	
	Experiment	Model
Warp, Center	38	52.7
Warp, Edge	33	49.1
Weft, Center	38	53.4
Weft, Edge	28	47.4

# Modeling Approach #3

## Heatup and Cooldown

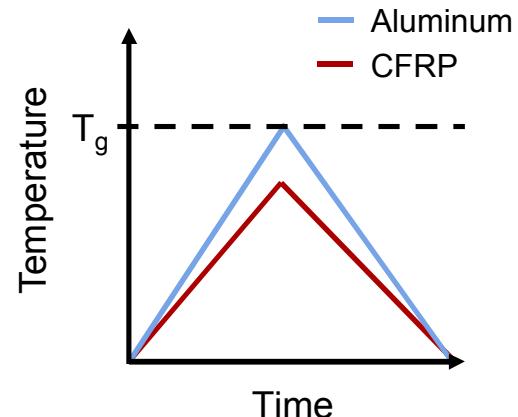
- Heat from room temperature to  $T_g$  then return
- Requires element ‘birth’ to change material properties
- Considers CTE effects only



Location	Radius of Curvature (in)	
	Experiment	Model
Warp, Center	38	53.0
Warp, Edge	33	49.3
Weft, Center	38	53.7
Weft, Edge	28	47.6

# Approximating Cure Shrinkage

- Adjust the temperature of the CFRP
  - Historical method
  - Good agreement predicting delamination
  - Generally an adjustment of  $\sim 10^{\circ}\text{C}$



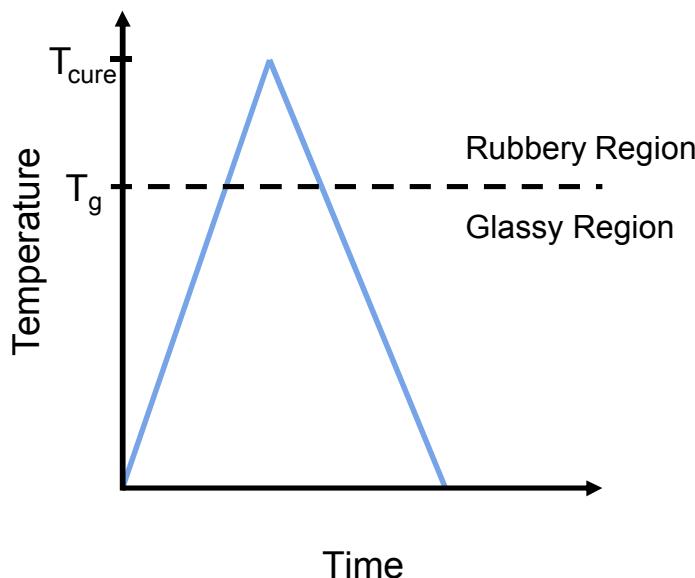
## Approach #2

Location	Radius of Curvature (in)			
	Experiment	Adj = 0°C	Adj = 10°C	Adj = 100°C
Warp, Center	38	52.7	51.4	40.9
Warp, Edge	33	49.1	47.8	37.1
Weft, Center	38	53.4	52.1	41.9
Weft, Edge	28	47.4	46.1	35.6

# Modeling Approach #4

## Cure Cycle

- Heat from room temperature to  $T_{\text{cure}}$  then return
- Requires element ‘birth’ to change material properties
- Considers CTE effects in both regions



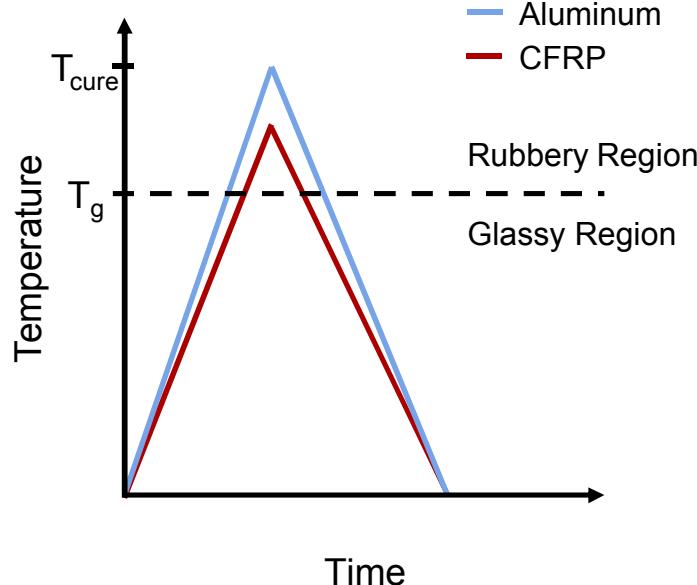
Location	Radius of Curvature (in)	
	Experiment	Model <sup>1</sup>
Warp, Center	38	40.3
Warp, Edge	33	36.5
Weft, Center	38	41.2
Weft, Edge	28	34.9

<sup>1</sup>  $T_{\text{cure}} = 154^{\circ}\text{C}$

# Modeling Approach #5

## Cure Cycle

- Same as Approach #4
- Adjusted CFRP temperature ( $50^{\circ}\text{C}$ ) for cure shrinkage



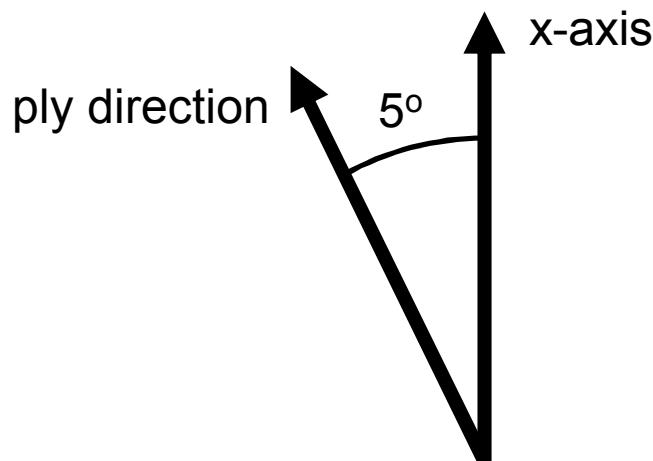
Location	Radius of Curvature (in)	
	Experiment	Model <sup>1</sup>
Warp, Center	38	38.1
Warp, Edge	33	34.3
Weft, Center	38	39.1
Weft, Edge	28	32.7

<sup>1</sup>  $T_{\text{cure}} = 154^{\circ}\text{C}$

# Skew Sensitivity

## Cure Cycle

- Same as Approach #5
- Rotated ply direction by 5°



Location	Radius of Curvature (in)	
	Experiment	Model <sup>1</sup>
Warp, Center	38	38.7
Warp, Edge	33	35.4
Weft, Center	38	39.1
Weft, Edge	28	31.8

<sup>1</sup>  $T_{cure} = 154^\circ\text{C}$

# Current Conclusions

- The accurate simulation of residual stresses formed during a composite's cure cycle requires consideration beyond CTE mismatch
  - Cannot rely on  $T_g$  and CTE alone
  - Cure shrinkage is not negligible
  - It may be important to account for both the glassy and rubbery regions during the post-cure cool down
- Uncertainties in the relevant model parameters significantly effect the simulated response
  - $T_g$ , cure temperature, and % shrinkage
  - Current simulations assume a “perfect” composite
    - Consideration of skew angle, void content, etc. may be important

# Planned Future Work

- Apply sensitivity study and uncertainty quantifications techniques to a variation of modeling approach #5
  - Initialize the simulated composite material with an initial strain
    - More accurate method of simulating shrinkage
    - Determine model parameters most relevant for the simulation of residual stresses
    - Account for uncertainty of sensitive parameters in simulated responses
- Apply validated modeling technique to simulate new residual stress experiments
  - Quantify the composite CTE + shrinkage
  - Simulate residual stress formation in both simple and complex structures
    - Bi-material strips (analytical solution for validation)
    - Bi-material plates
    - Bi-material cylinders
- Investigate methods for modeling interlaminar delamination due to large residual stresses
  - Cohesive zone methods
  - Model validation with planned DCB experiments conducted in different environments