

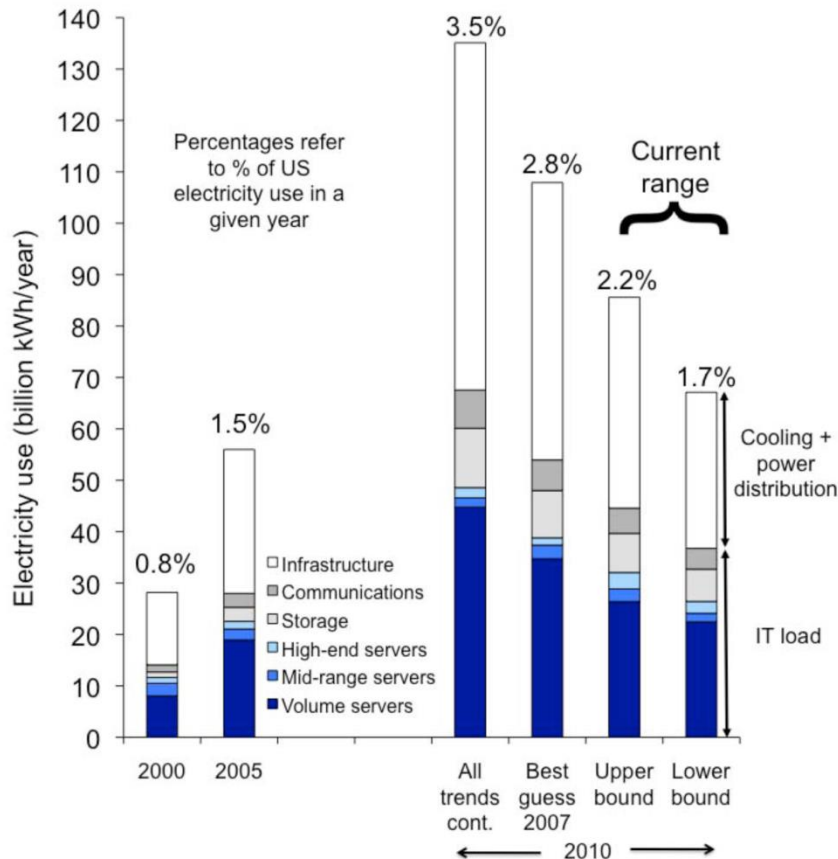
Exceptional service in the national interest



The Low Voltage TFET Demands Higher Perfection than Previously Required in Electronics

Sapan Agarwal, Eli Yablonovitch

Data Center Electricity Usage



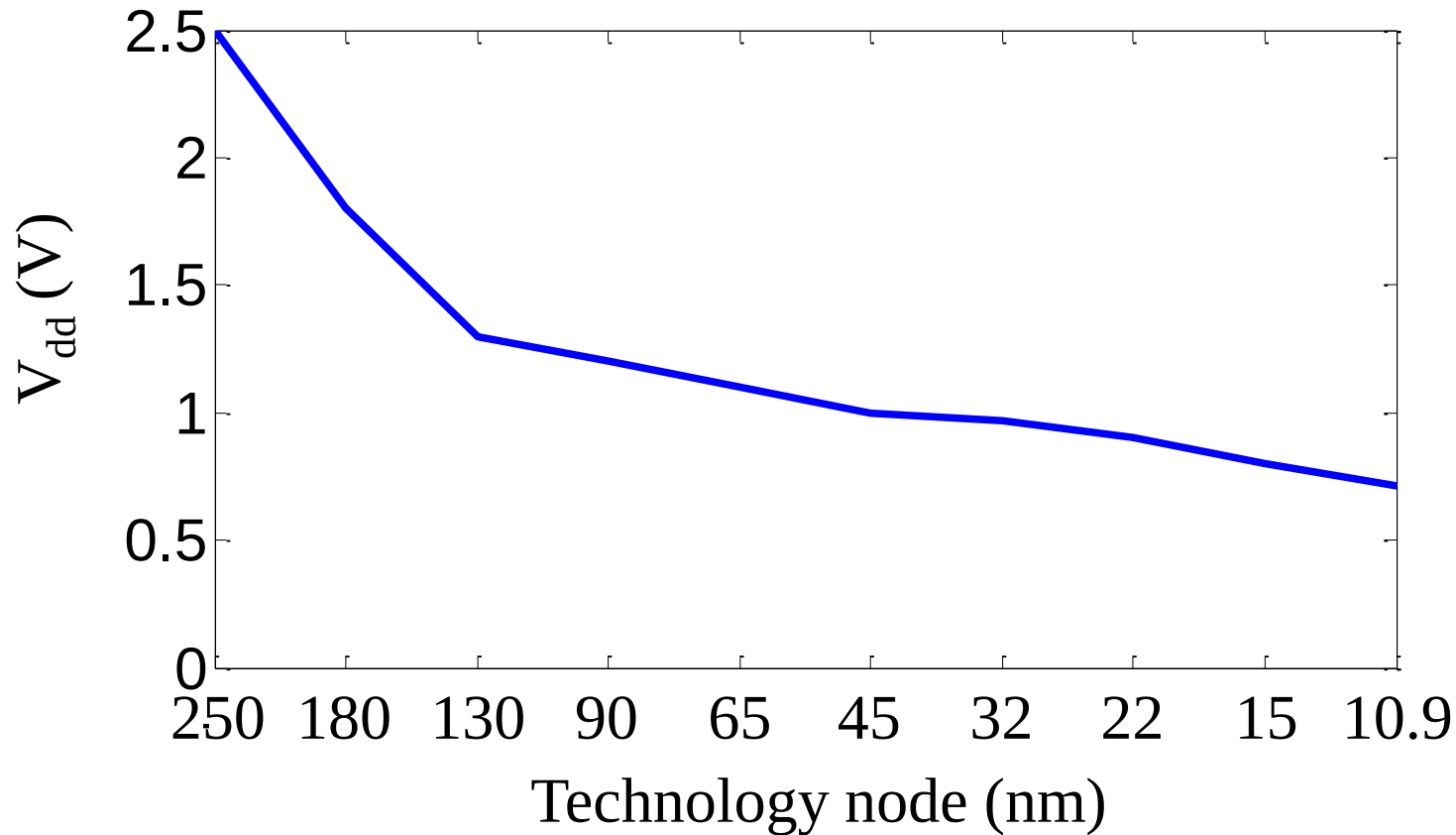
- In 2010, data centers accounted for ~1.3% of all electricity use worldwide, ~2% of all electricity use in the U.S.



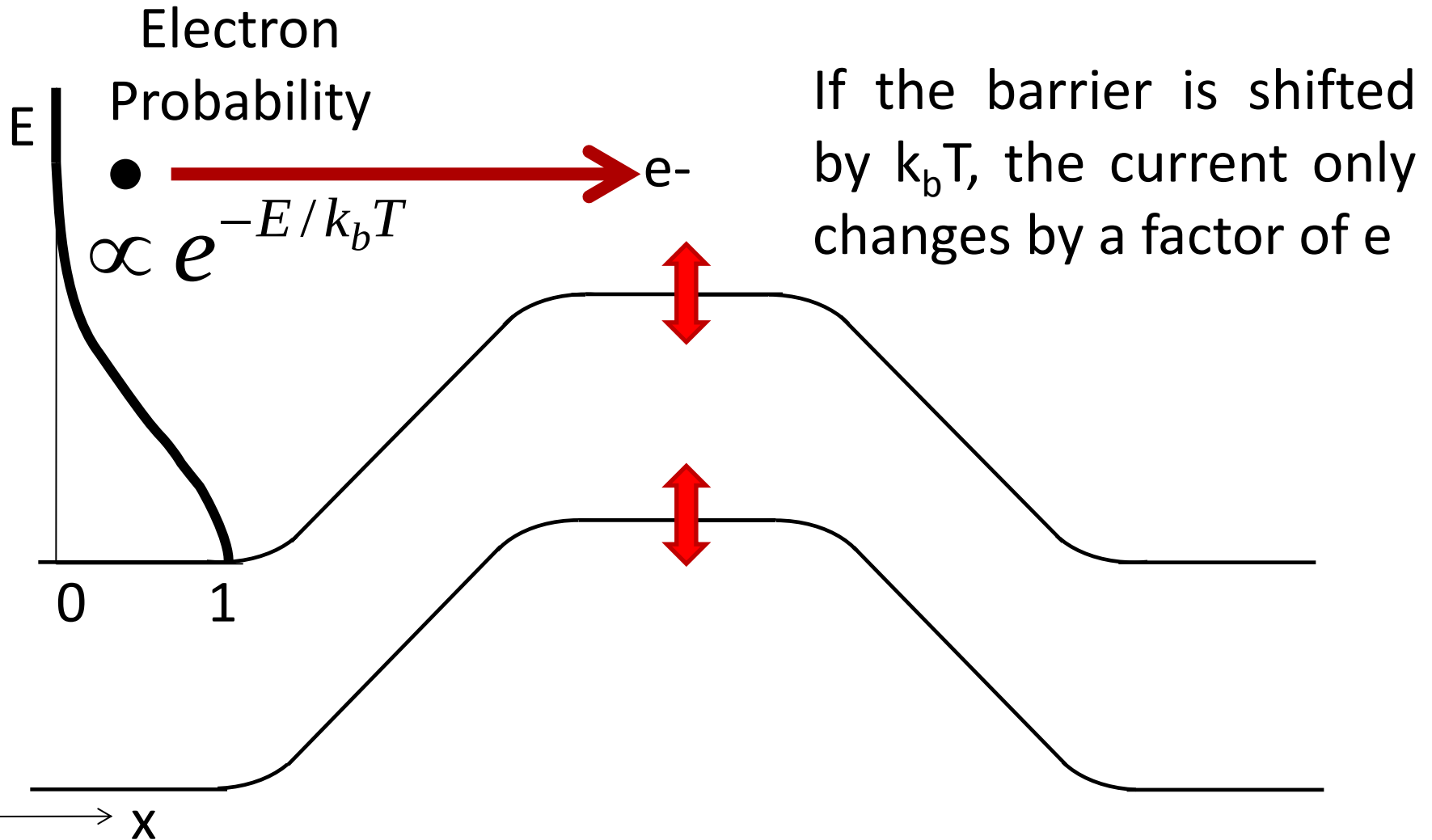
Google's new data center in Hamina, Finland, has an energy-efficient cooling system that uses seawater from a nearby bay.

Power Usage Rising

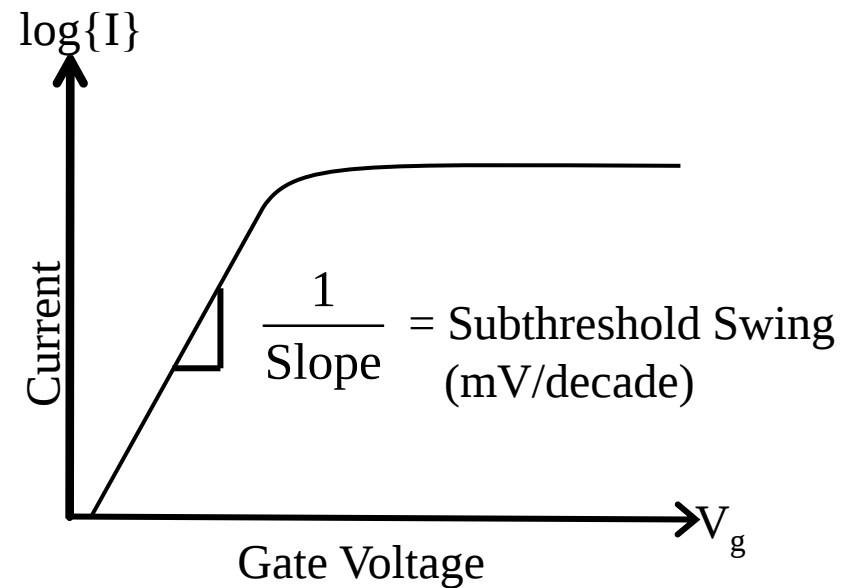
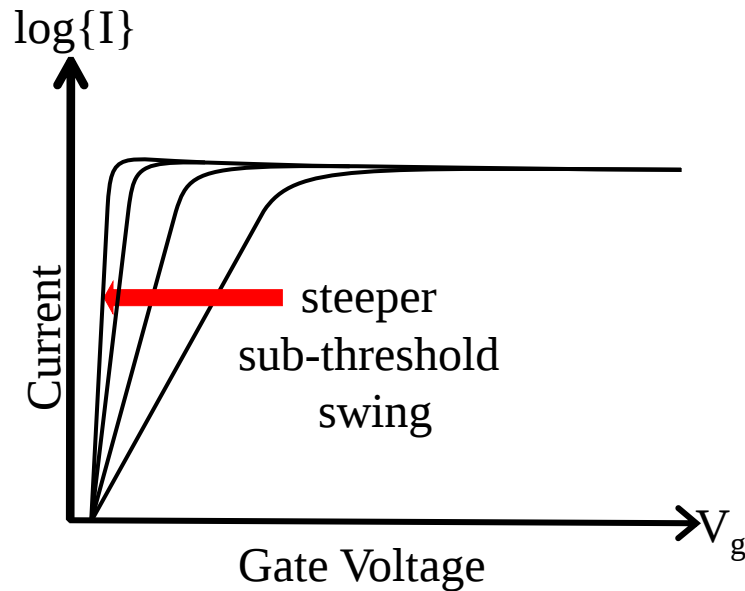
- Power consumption is $\propto V_{dd}^2$ and V_{dd} (operation voltage) scaling has slowed.



What's Wrong With Current Transistors?



Need a New, More Sensitive Switch



The New Switch has to Satisfy Three Specifications

1. Steepness (or sensitivity)

switches with only a few milli-volts
 $60\text{mV/decade} \Rightarrow \mathbf{1\text{mV/decade}}$

2. On/Off ratio. $10^6 : 1$

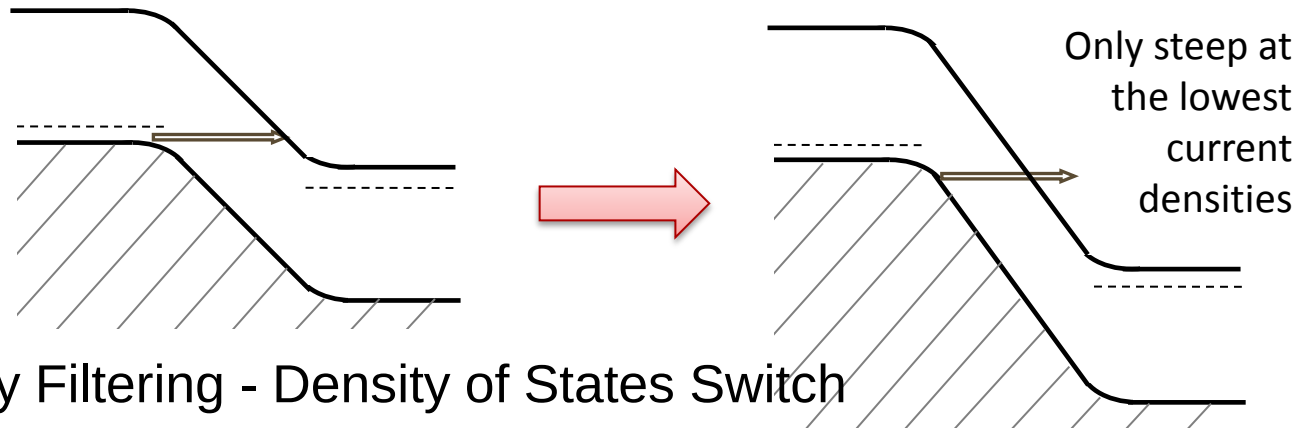
3. Current Density or Conductance Density (for miniaturization)

old spec at 1V: 1 mAmp/micron

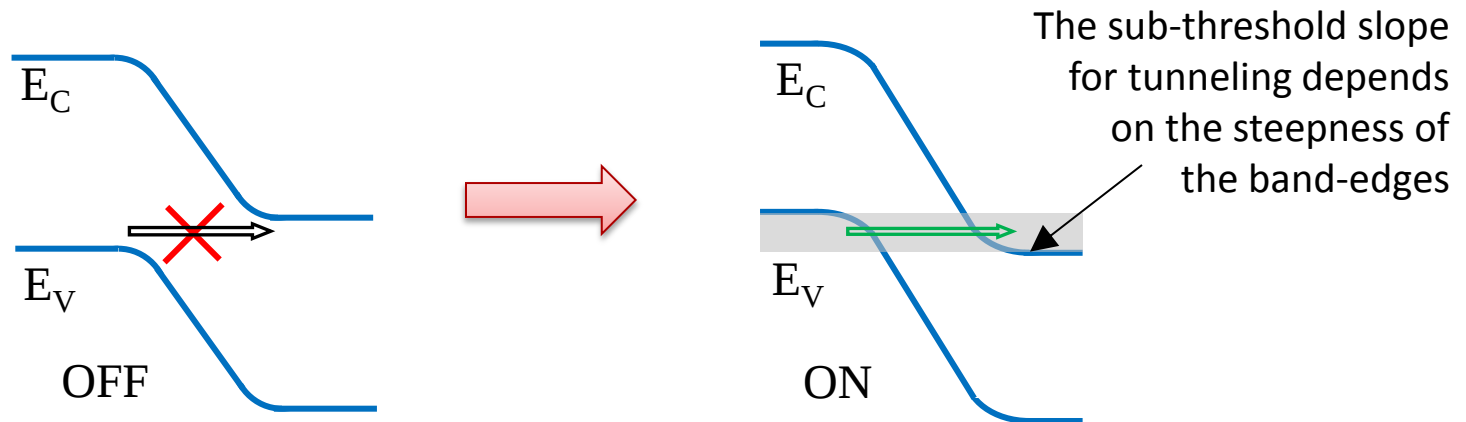
our spec: **1 milli-Siemen/micron**

2 Ways to Obtain Steepness

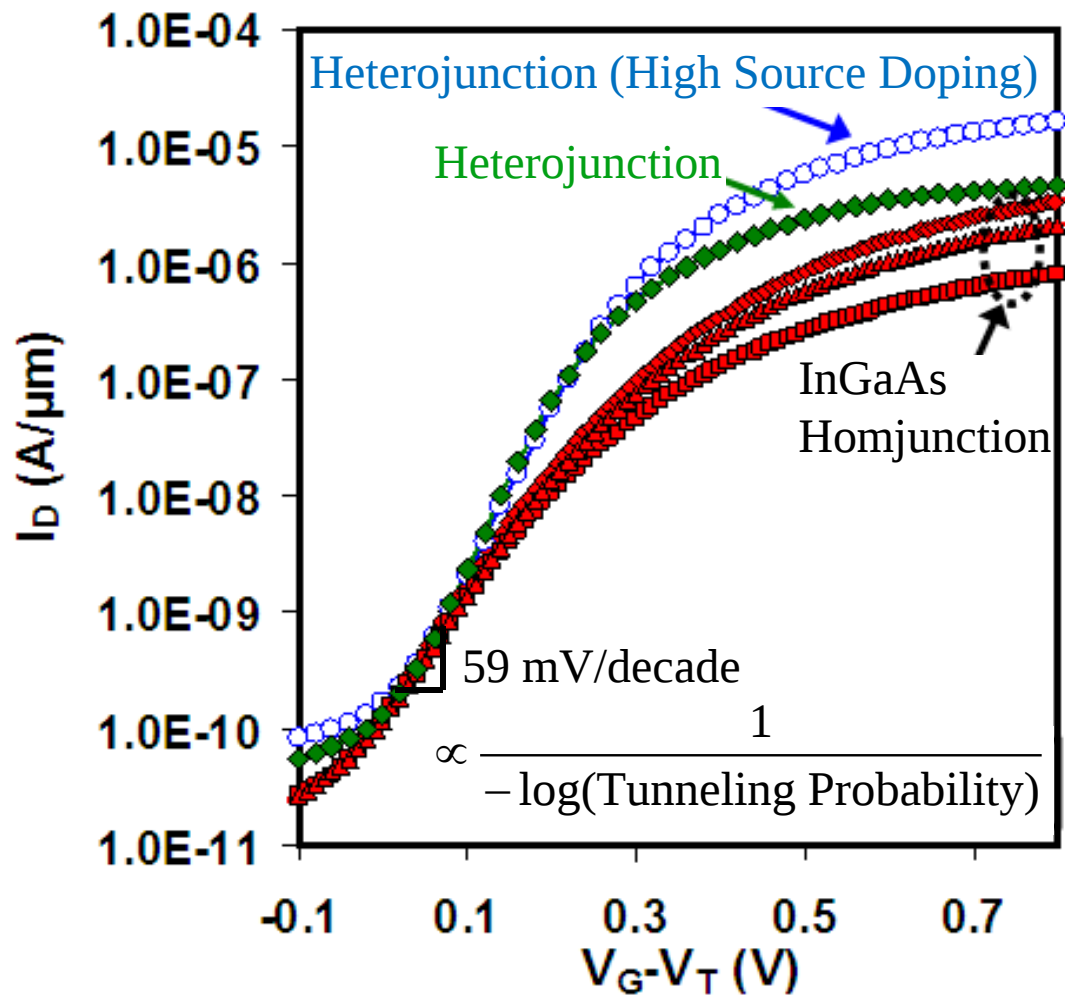
- Modulate the Tunneling Barrier Thickness



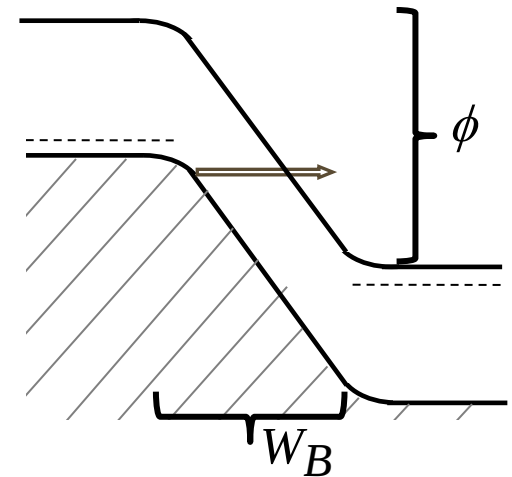
- Energy Filtering - Density of States Switch



Barrier Width Modulation Explains all Steep TFET Results and it's not Good Enough



G.Dewey, et al, *IEDM 2011* pp. 785-788, 2011



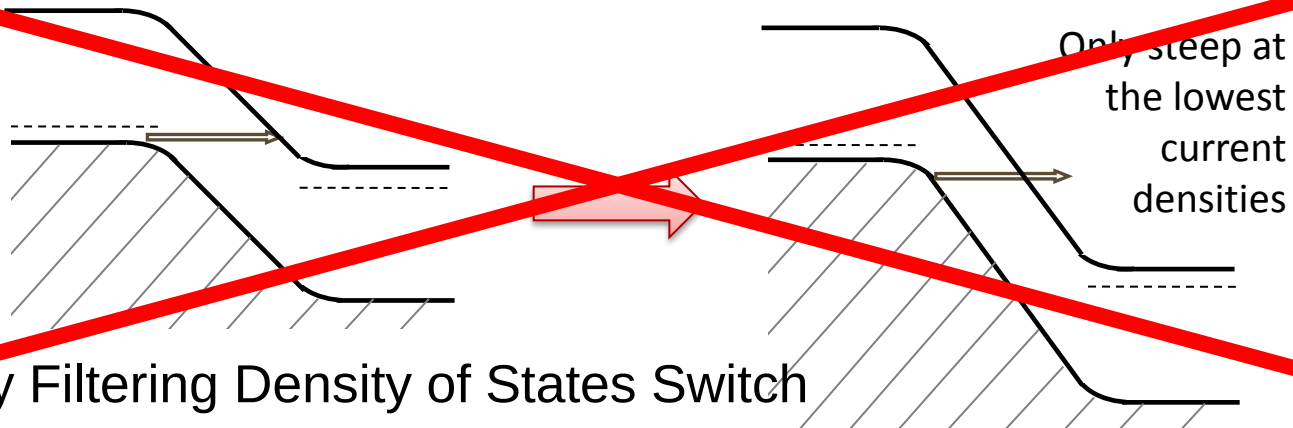
$$\text{Subthreshold Swing(SS)} \approx \frac{d\phi}{d \log(T)}$$

$$T = \exp\left(\frac{-\alpha}{|\vec{F}|}\right) \quad |\vec{F}| = \frac{\phi}{W_B}$$

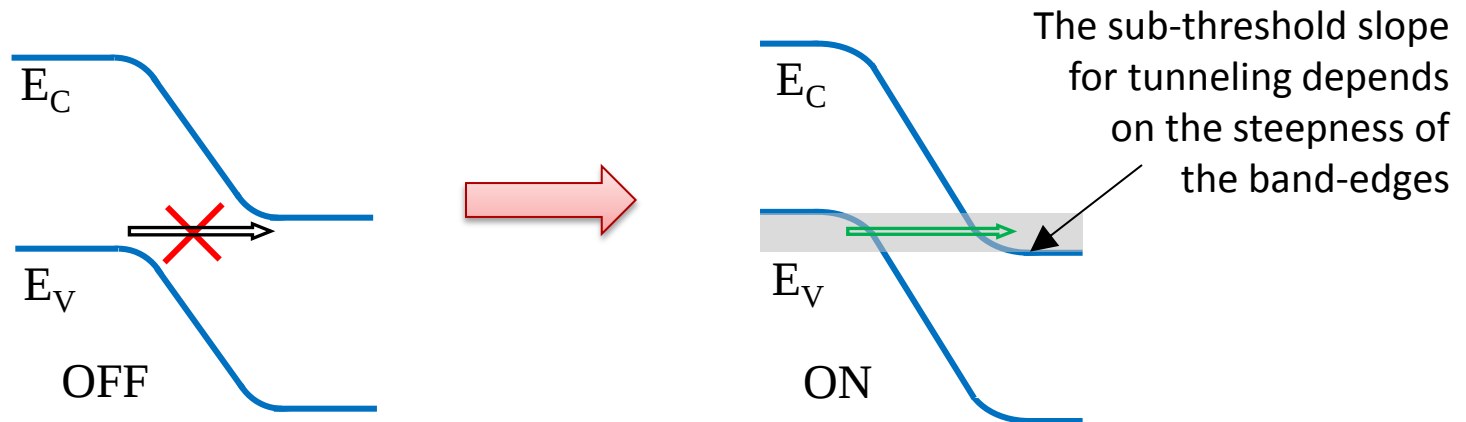
$$\begin{aligned}
 SS &\approx \left| \frac{1}{\log(T)} \times \frac{F}{dF(\phi)/d\phi} \right| \\
 &= \frac{\phi}{|\log(T)|}
 \end{aligned}$$

2 Ways to Obtain Steepness

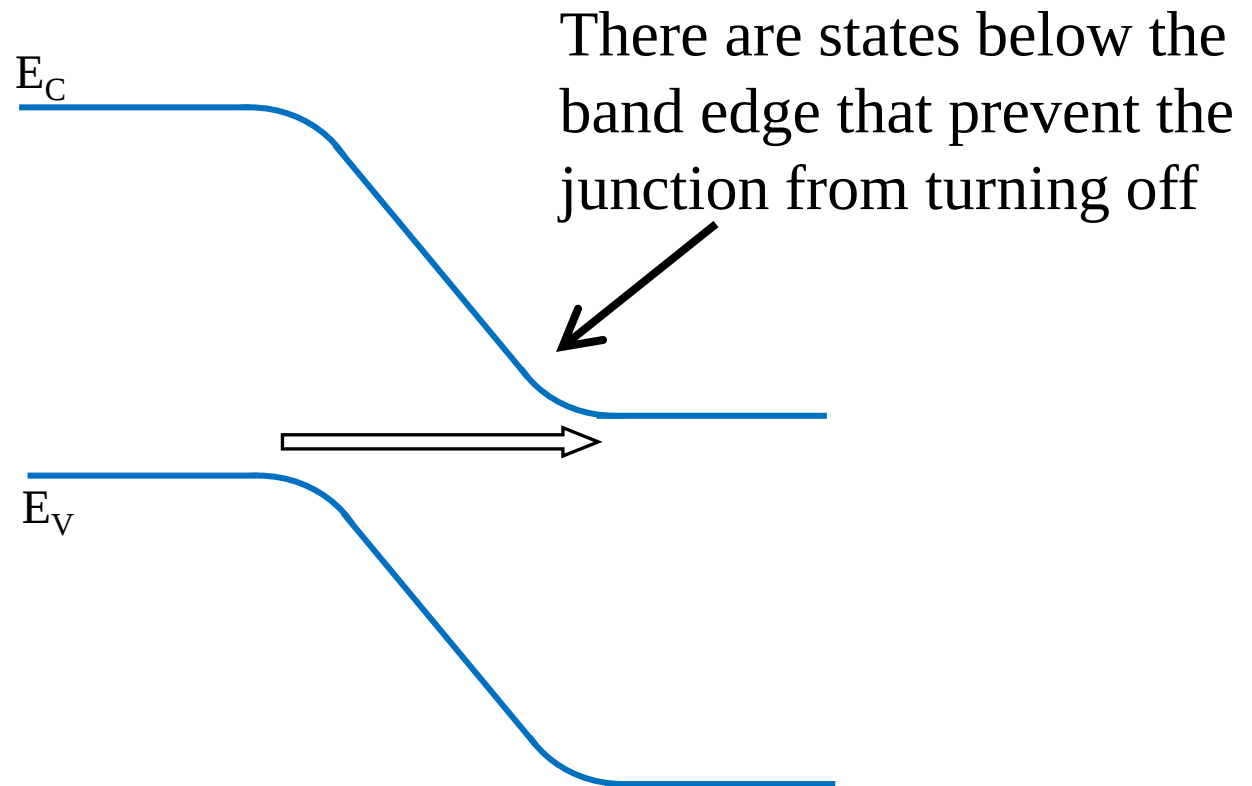
- Modulate the Tunneling Barrier Thickness



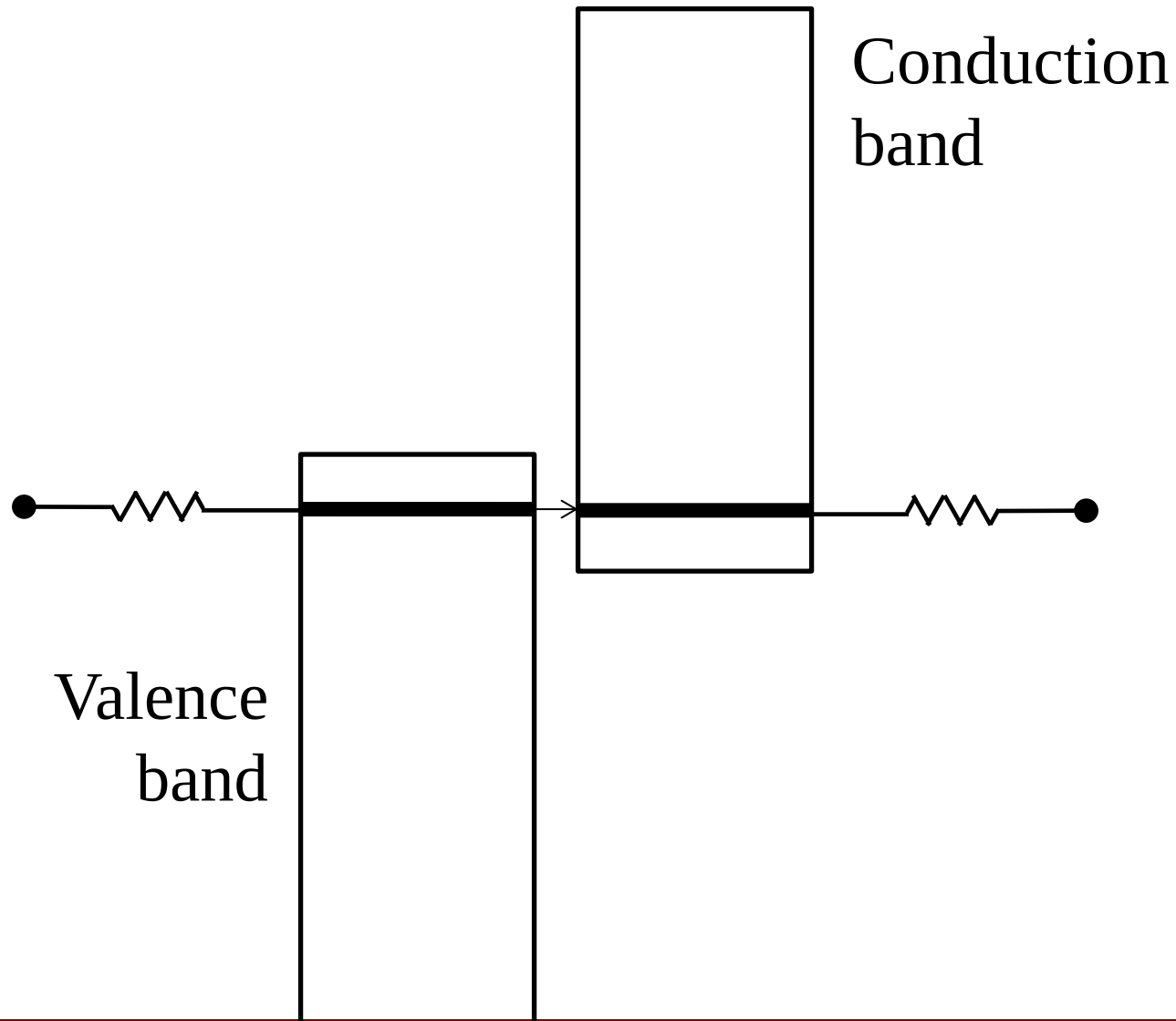
- Energy Filtering Density of States Switch



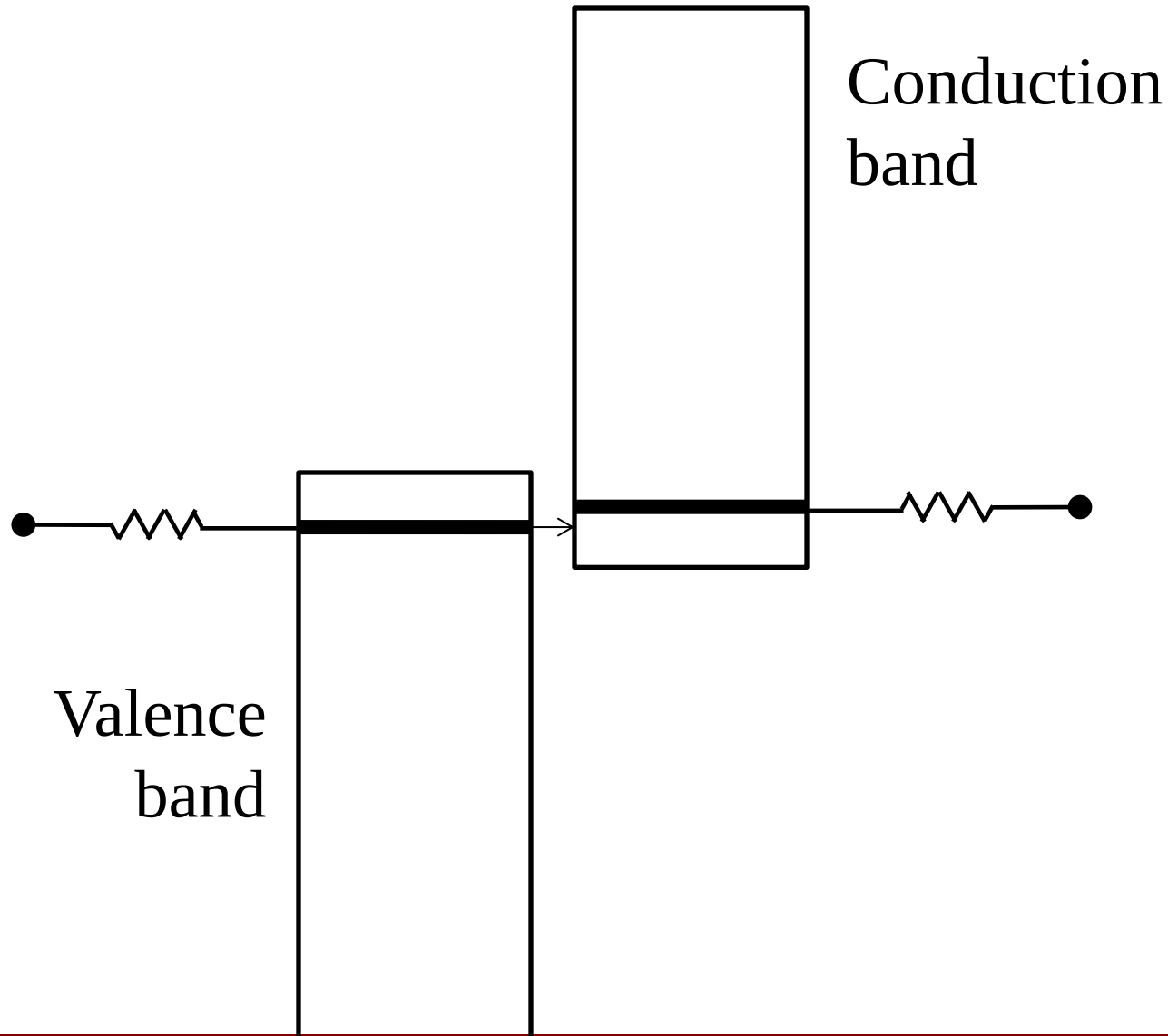
Band Tails Prevent a Steep Swing



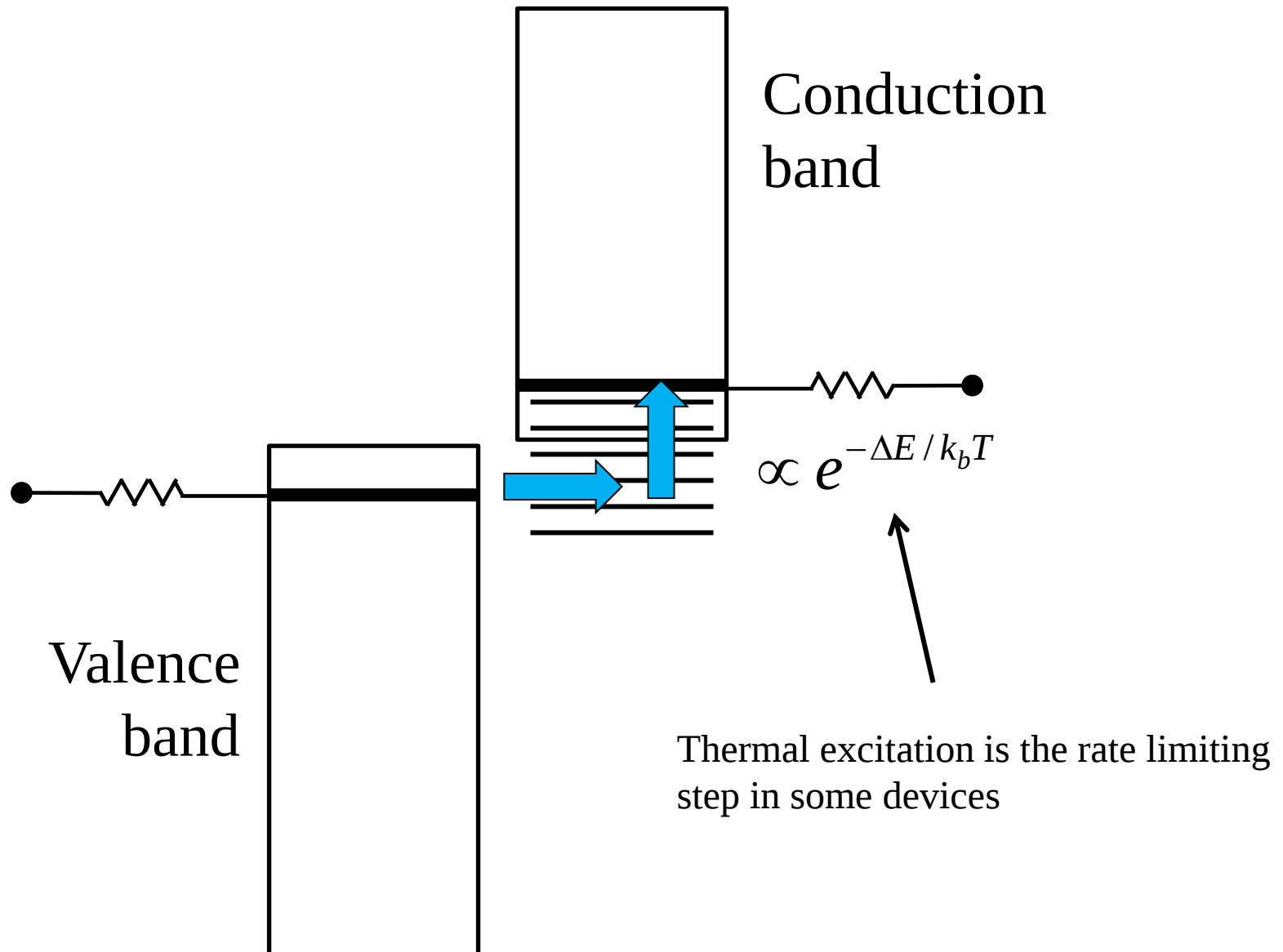
Switching Principle:



Switching Principle:



A problem arises from states where they should not be:

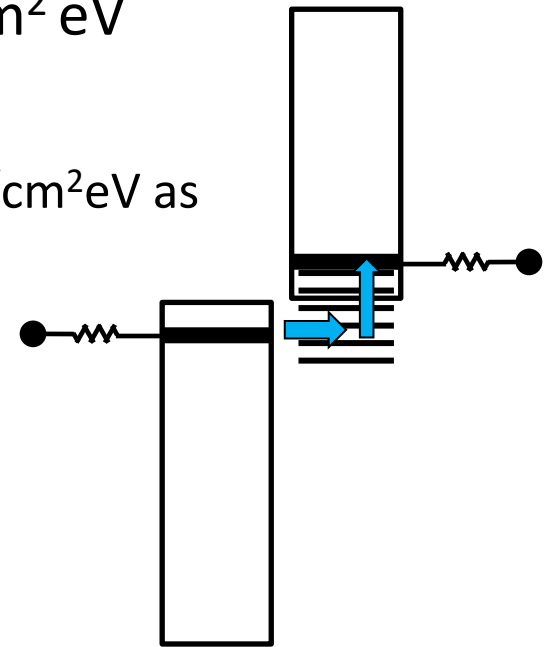


Interface Traps are Disastrous

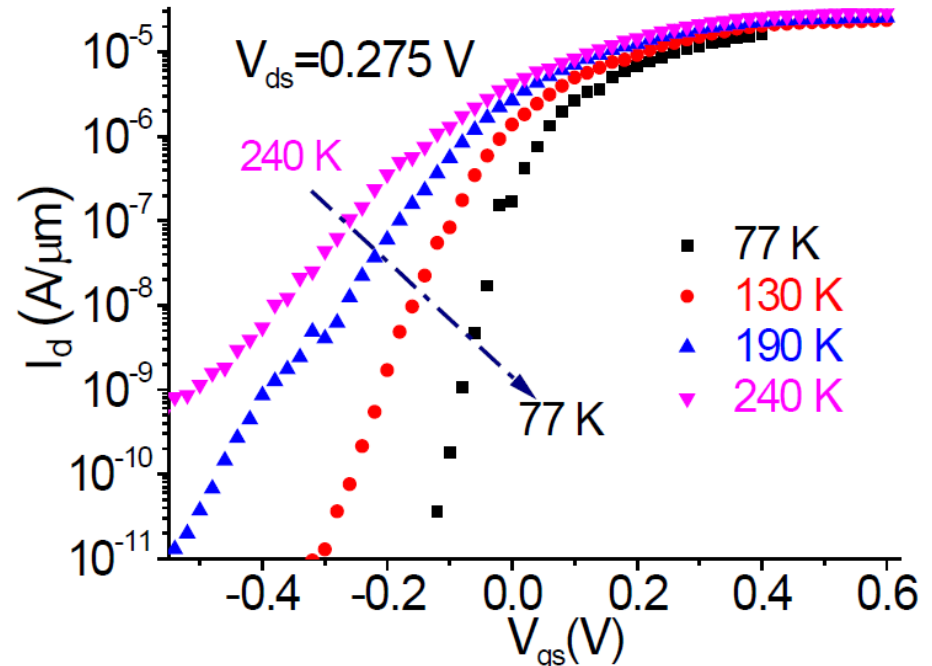
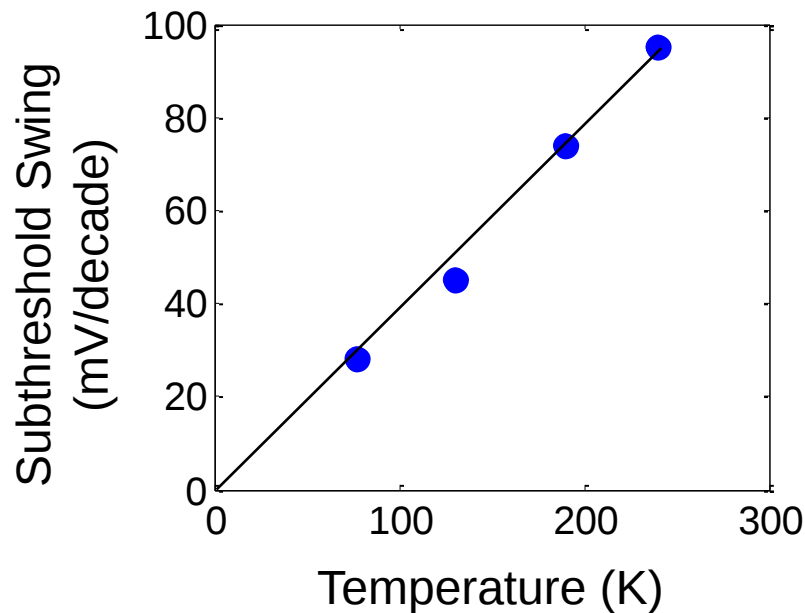
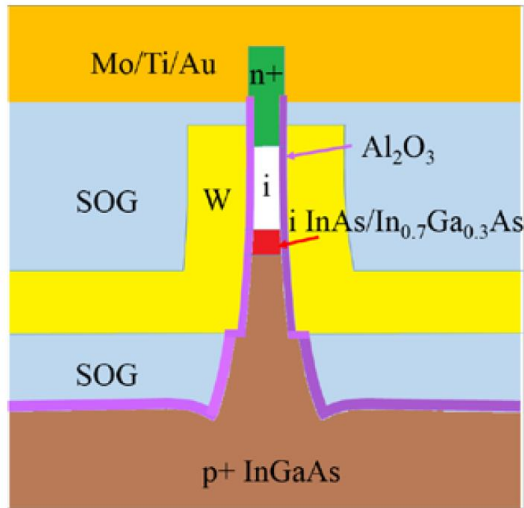
- Desired: Band-to-Band Tunneling –
Quantum Density of States $\sim 10^{12}/\text{cm}^2 \text{ eV}$

- Undesired: Tunneling into gate insulator States
 $D_{\text{IT}} \sim 10^{11}/\text{cm}^2 \text{ eV}$

- Interface state density might have to be lowered $< 10^8/\text{cm}^2 \text{ eV}$ as one of many pre-requisites to get a good On/Off ratio.
- This translates also into purity and reproducibility

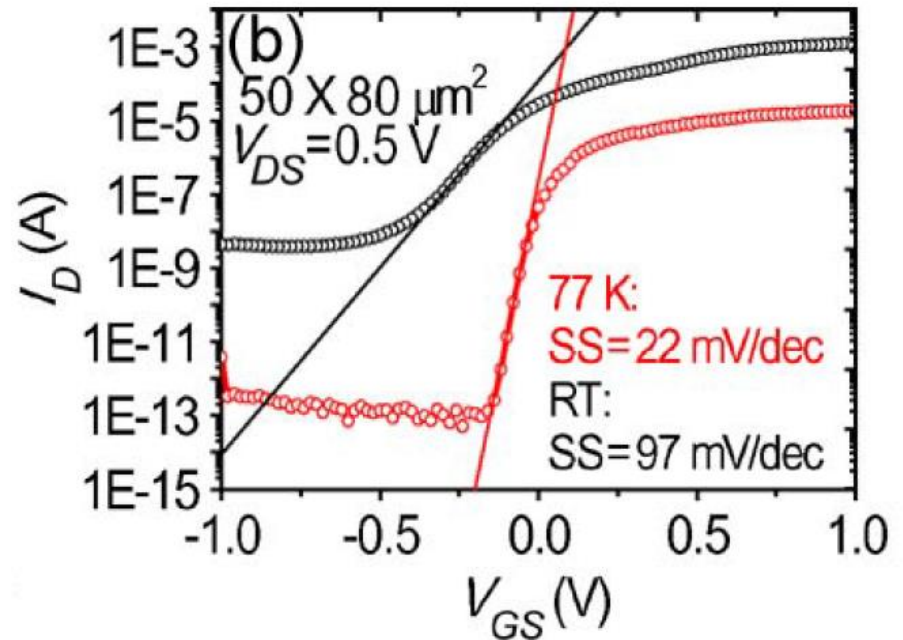
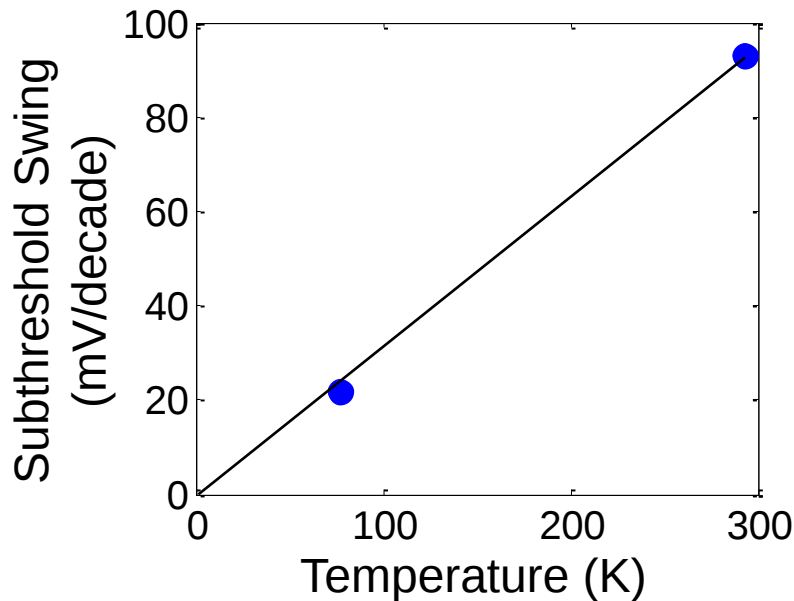
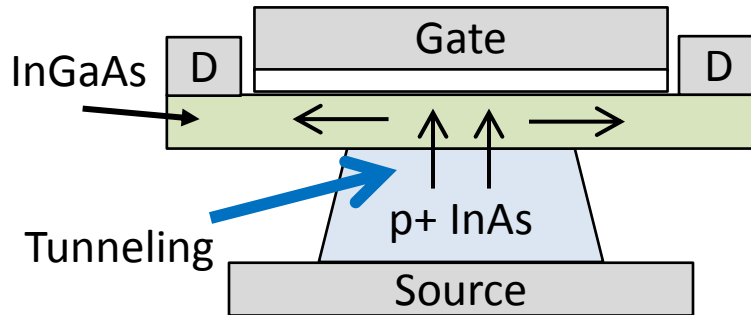


Thermally Activated Tunneling



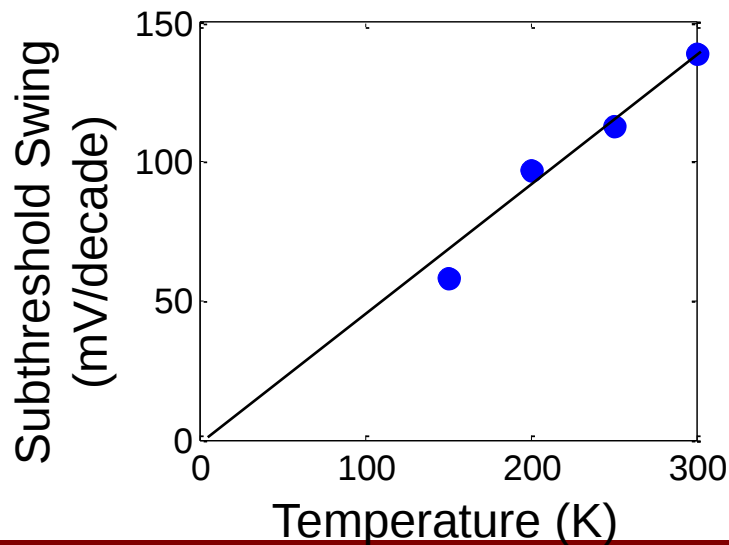
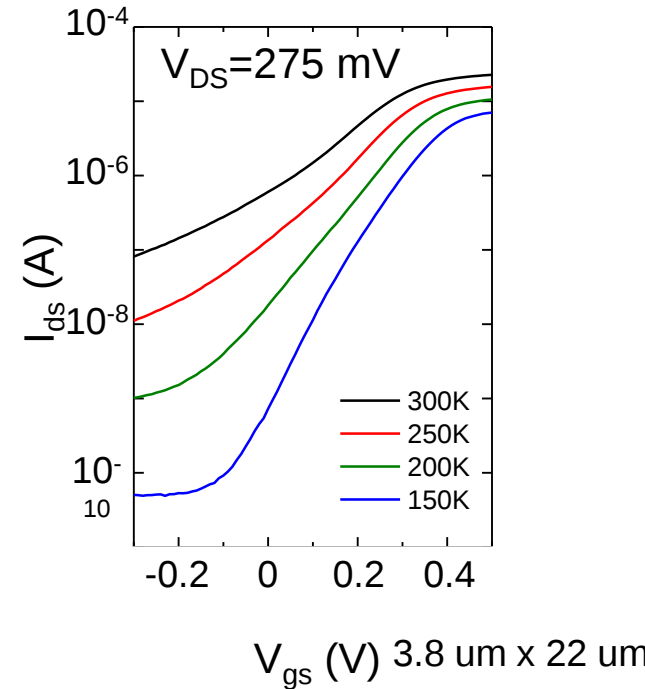
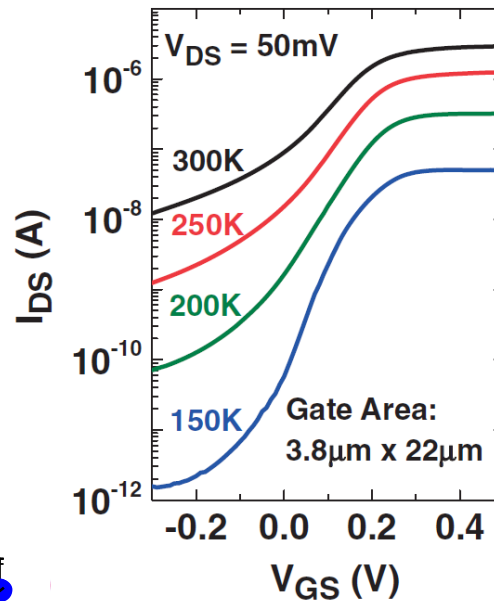
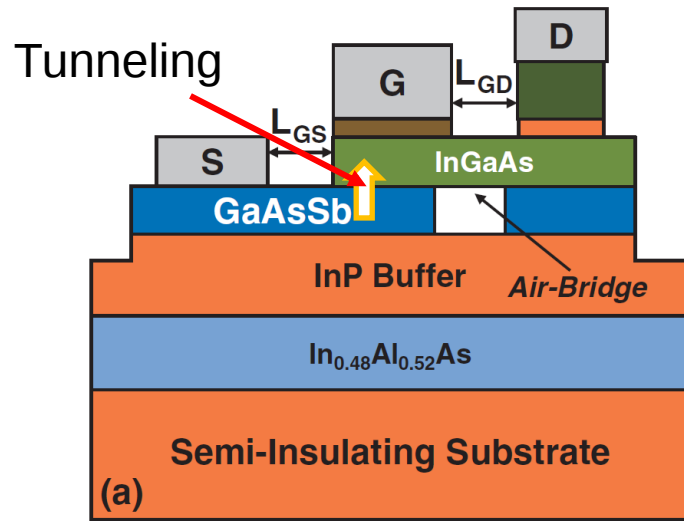
Zhao, Vardi, del Alamo, IEDM 2014

Thermally Activated Tunneling



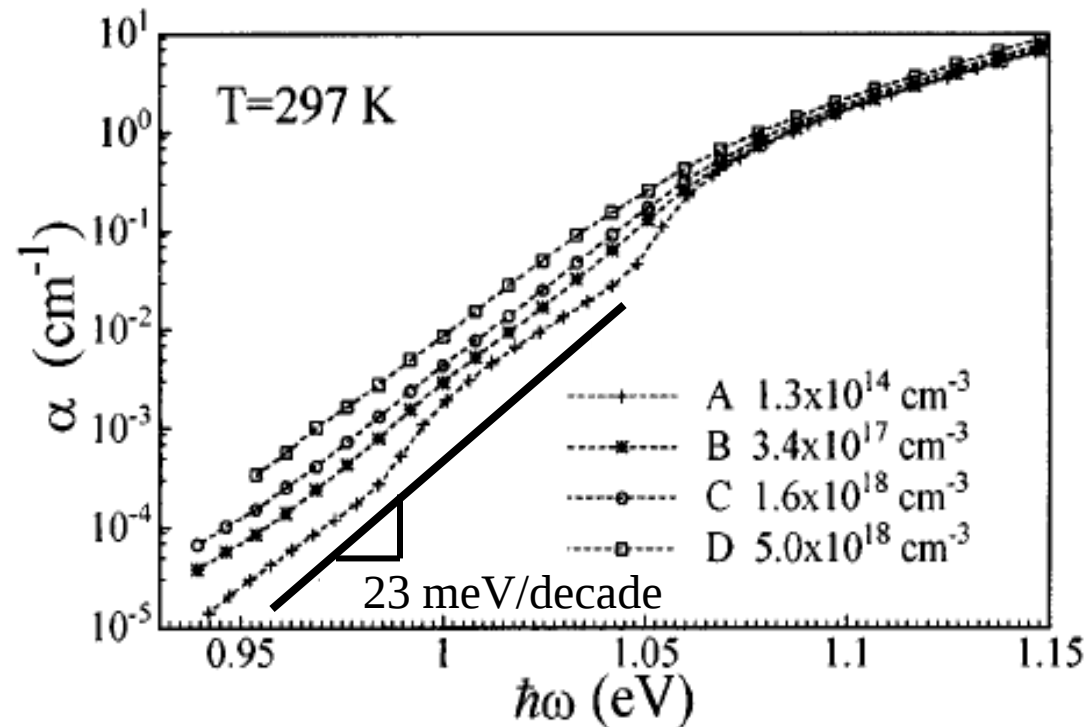
Guangle Zhou, et al, IEEE EDL 2012

Thermally Activated Tunneling

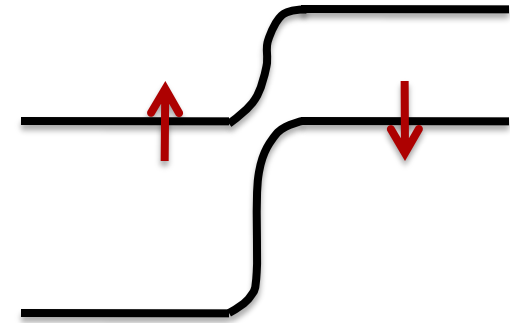


T. Yu, J. T. Teherani, D. A. Antoniadis, J. L. Hoyt, Applied Physics Express 2014

Use Optical Absorption Measurements to Measure the Band Edge Density of States



The absorption curves of Silicon at different doping levels

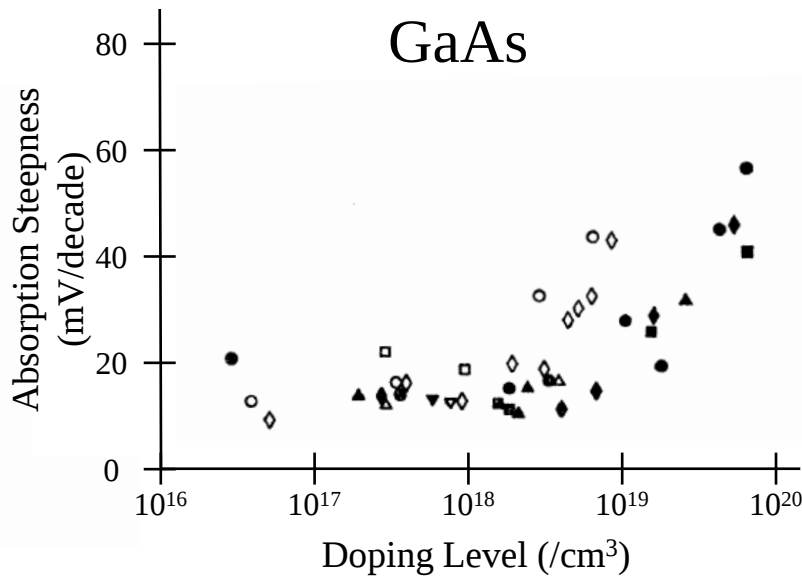


$$\alpha(h\nu) \sim \exp\{(h\nu - E_g)/E_o\}$$

$$E_o \sim 10\text{ meV for Silicon}$$

$$\sim 23\text{ meV /decade}$$

Optical Absorption Slope Gets Worse With Doping



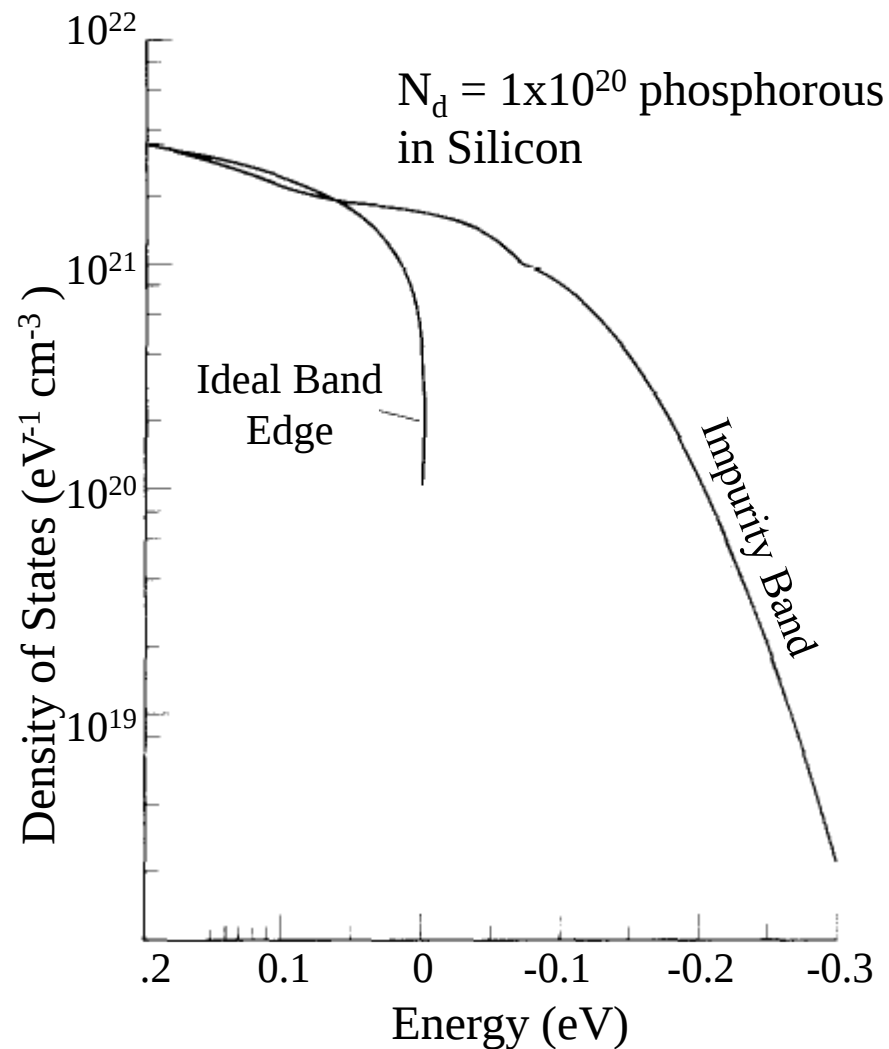
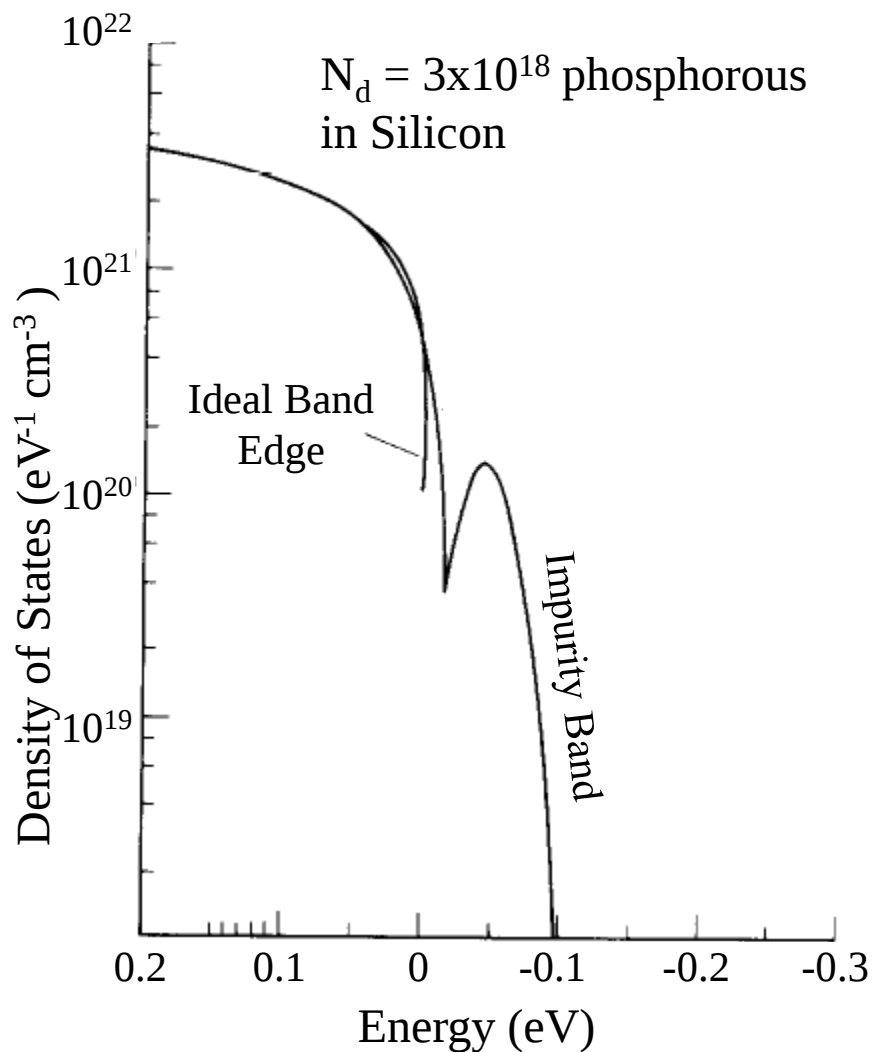
Undoped
~ 17 mV/decade

Heavily Doped
~ 60 mV/decade

J. I. Pankove, "Absorption Edge of Impure Gallium Arsenide"
Physical Review, vol 140 pp A2059-A2065, 1965

The doping induced potential variations are screened by free carriers. The slope will be far worse in a depletion region

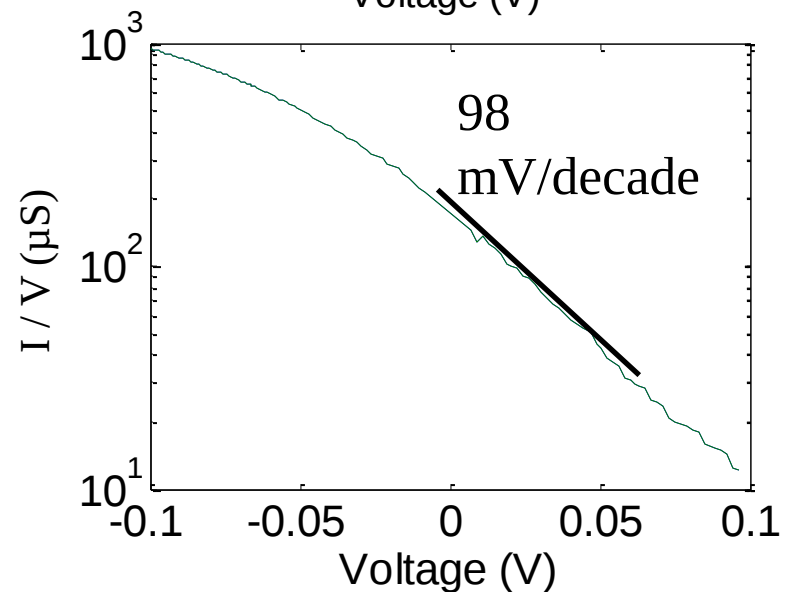
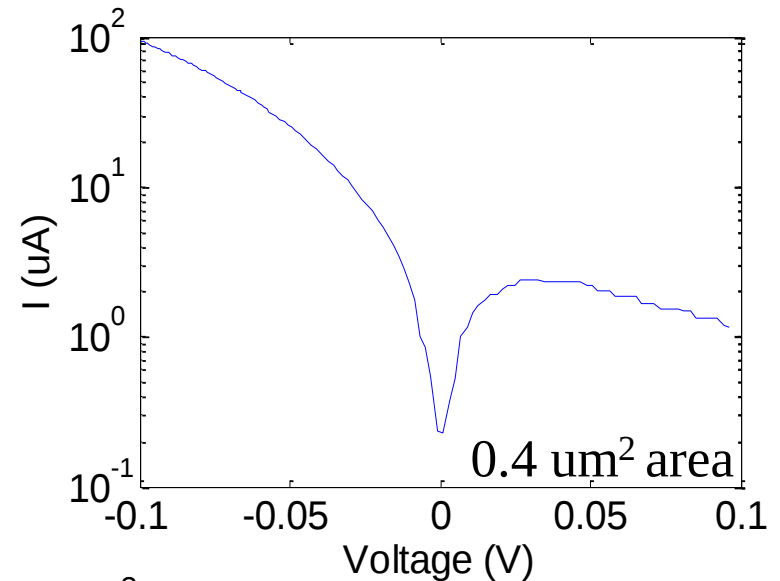
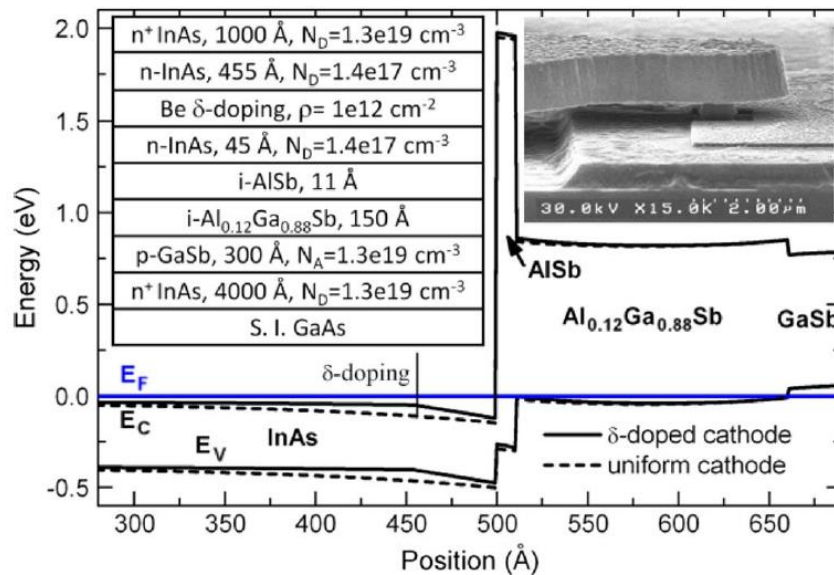
What's Going on?



Kleppinger and Lindholm, Solid State Electronics Vol 14, pp 407-416 (1971)

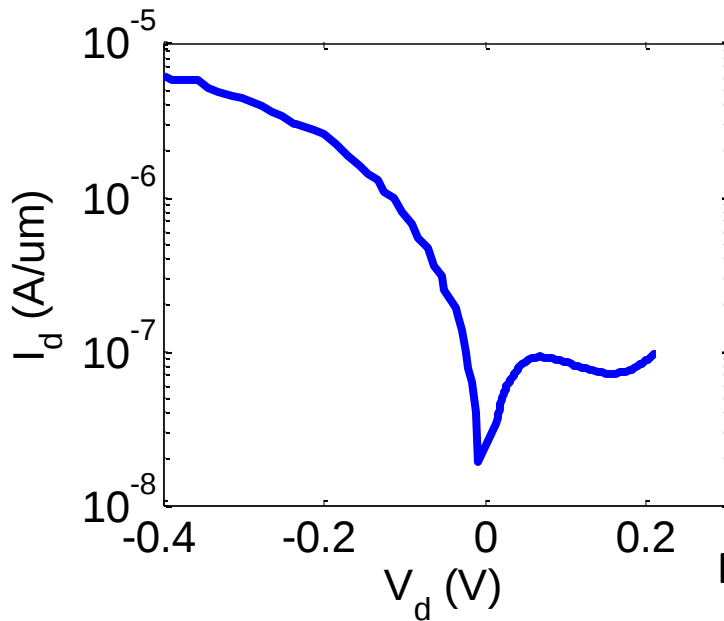
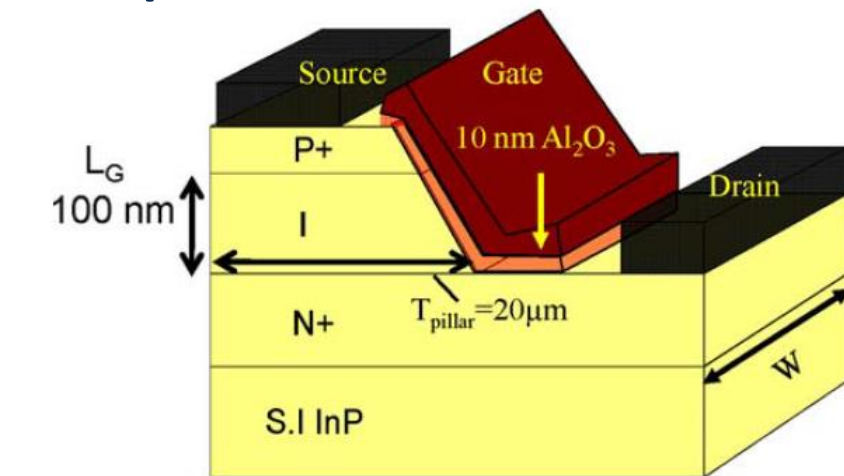
Analyze the Diode Conductance to Measure Steepness

InAs / AlGaSb Backward Diode

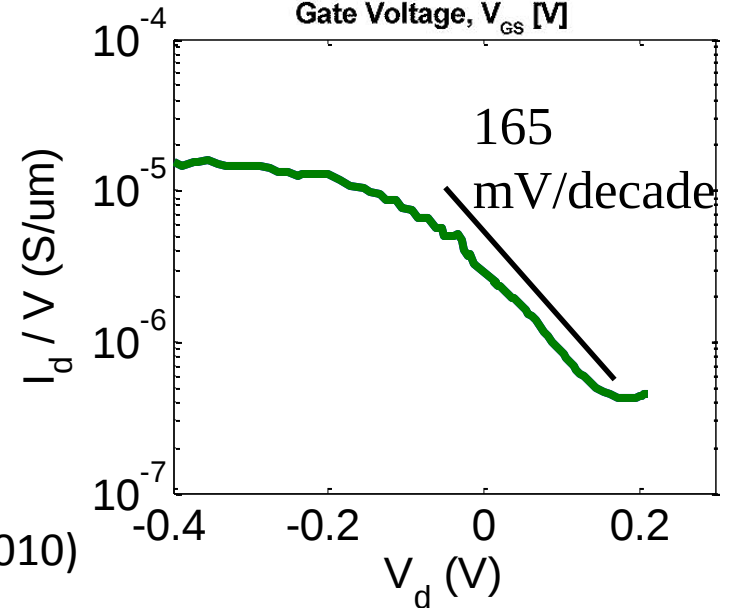
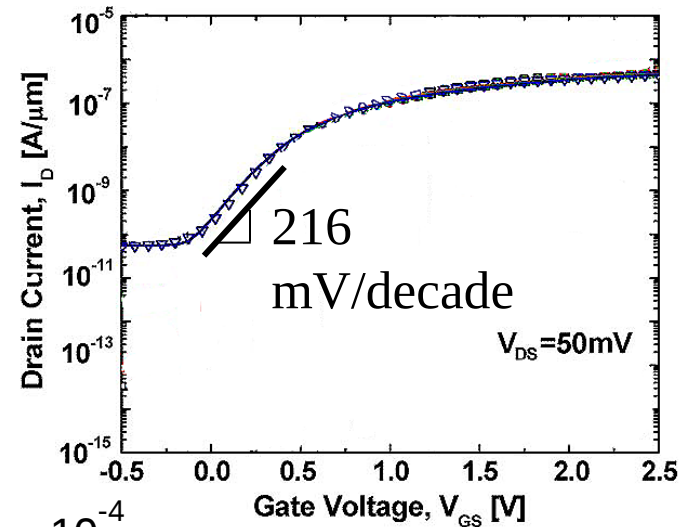


Zhang, Rajavel, Deelman, and Fay (2011)

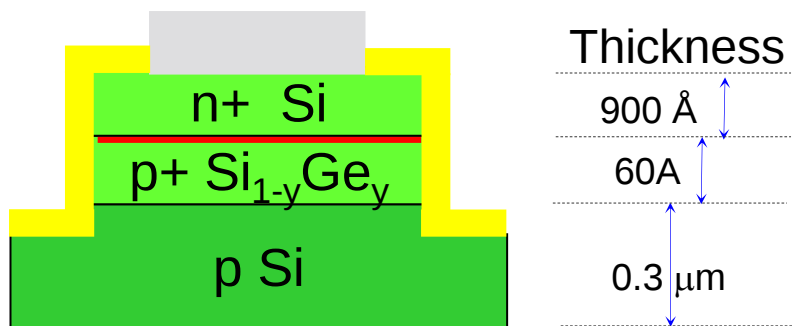
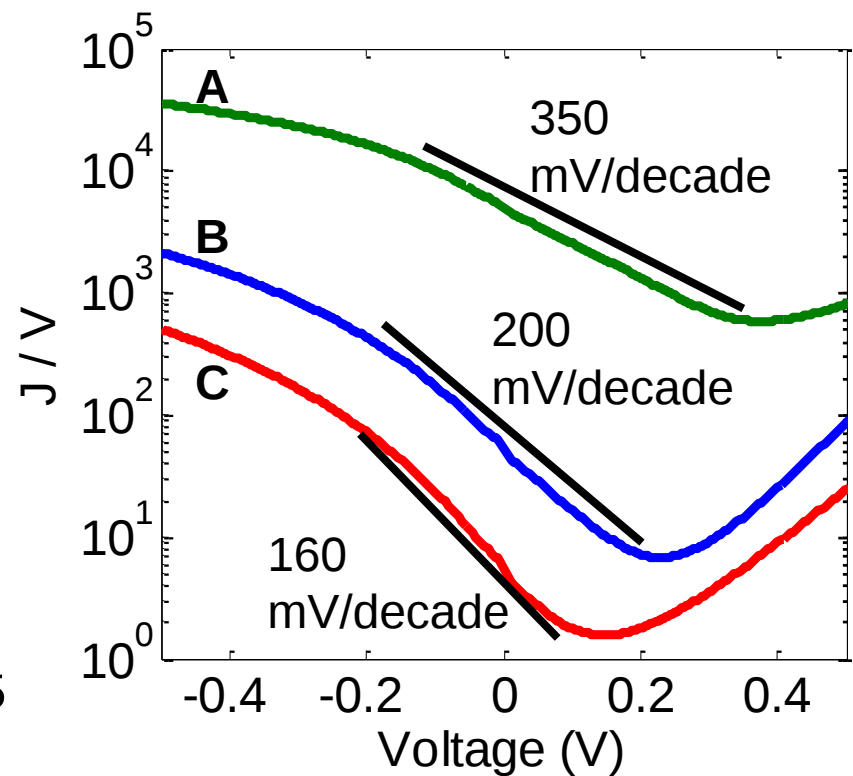
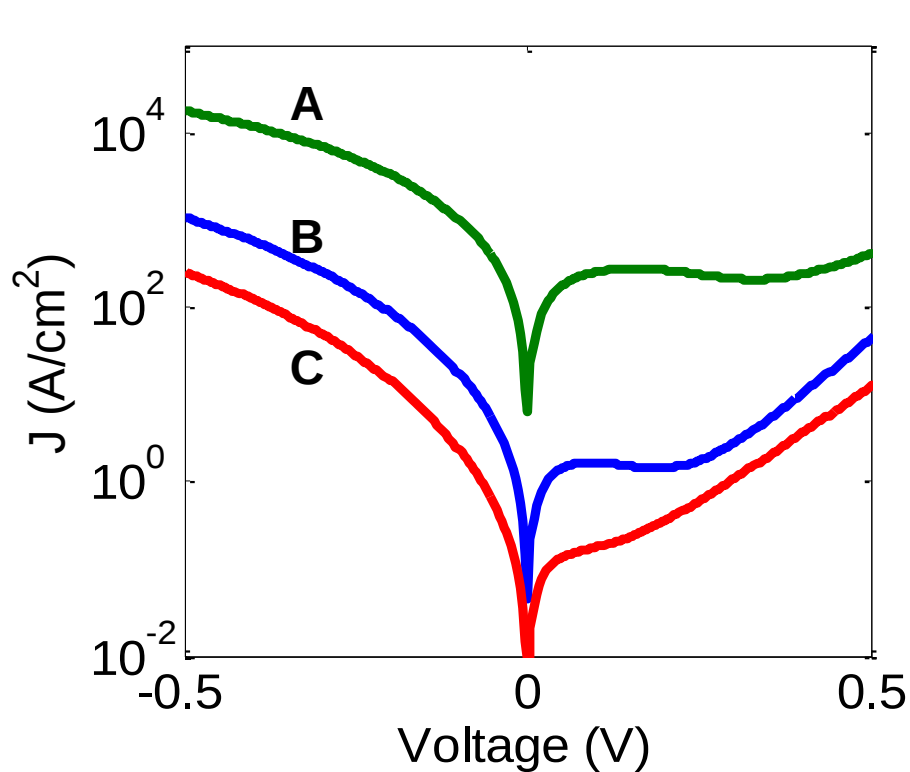
In_{0.53}Ga_{0.47}As PIN Diode Characteristics Steeper than TFET!



Mookerjea, (2010)

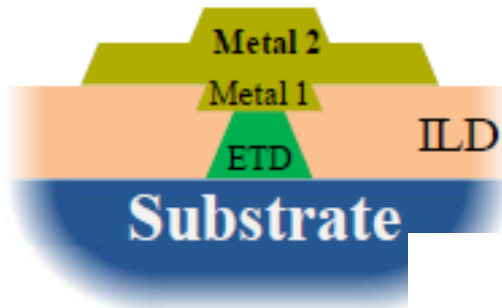


SiGe Epi Diodes Steeper at Lower Doping

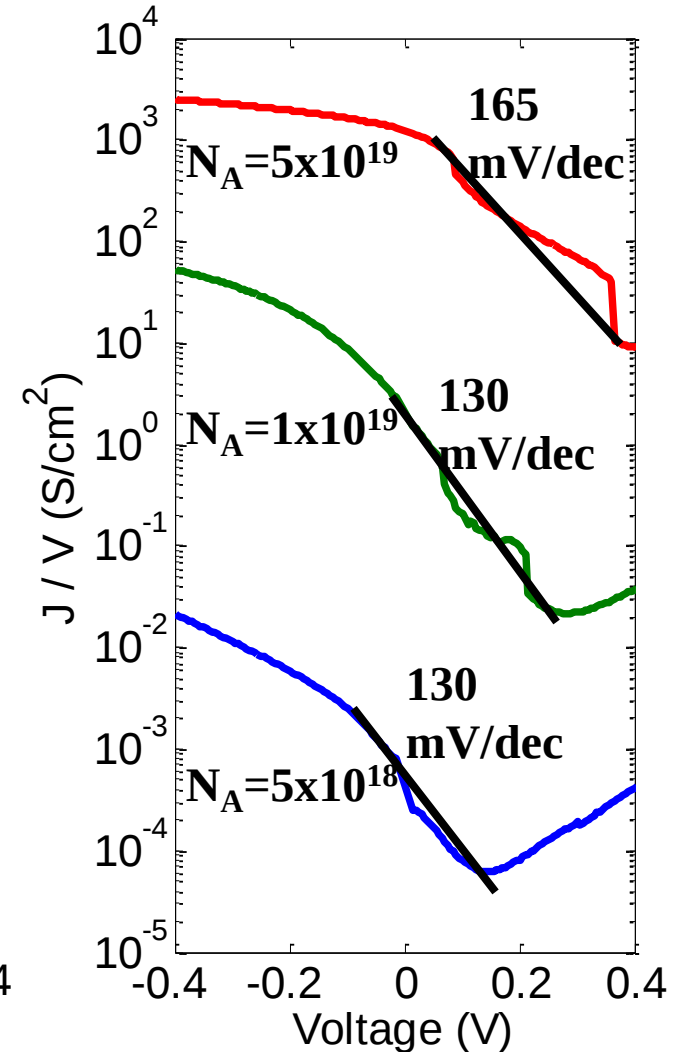
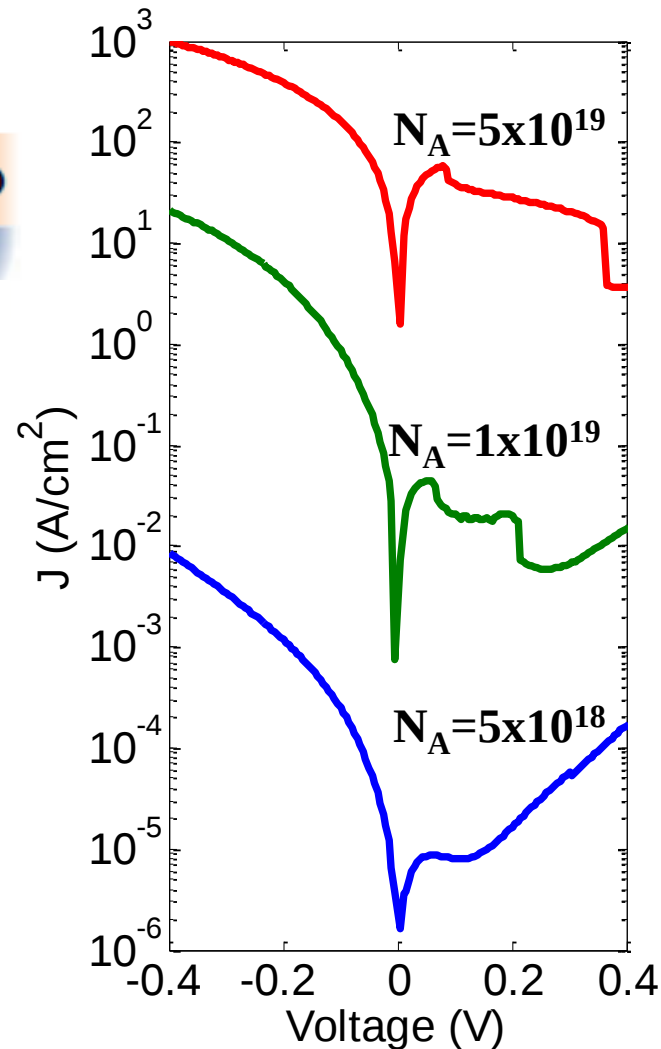


- | | |
|----------------------|---------|
| (A) 5e19/3e20/3e19 | n+/p+/p |
| (B) 1e19/1e20/3e19 | n+/p+/p |
| (C) 1e19/1.5e20/1e17 | n+/p+/p |

GaAs Homojunction Diodes

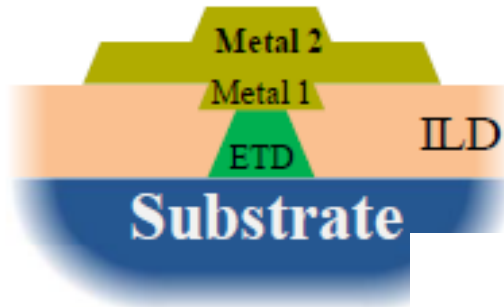


$$N_D = 3 \times 10^{19}$$

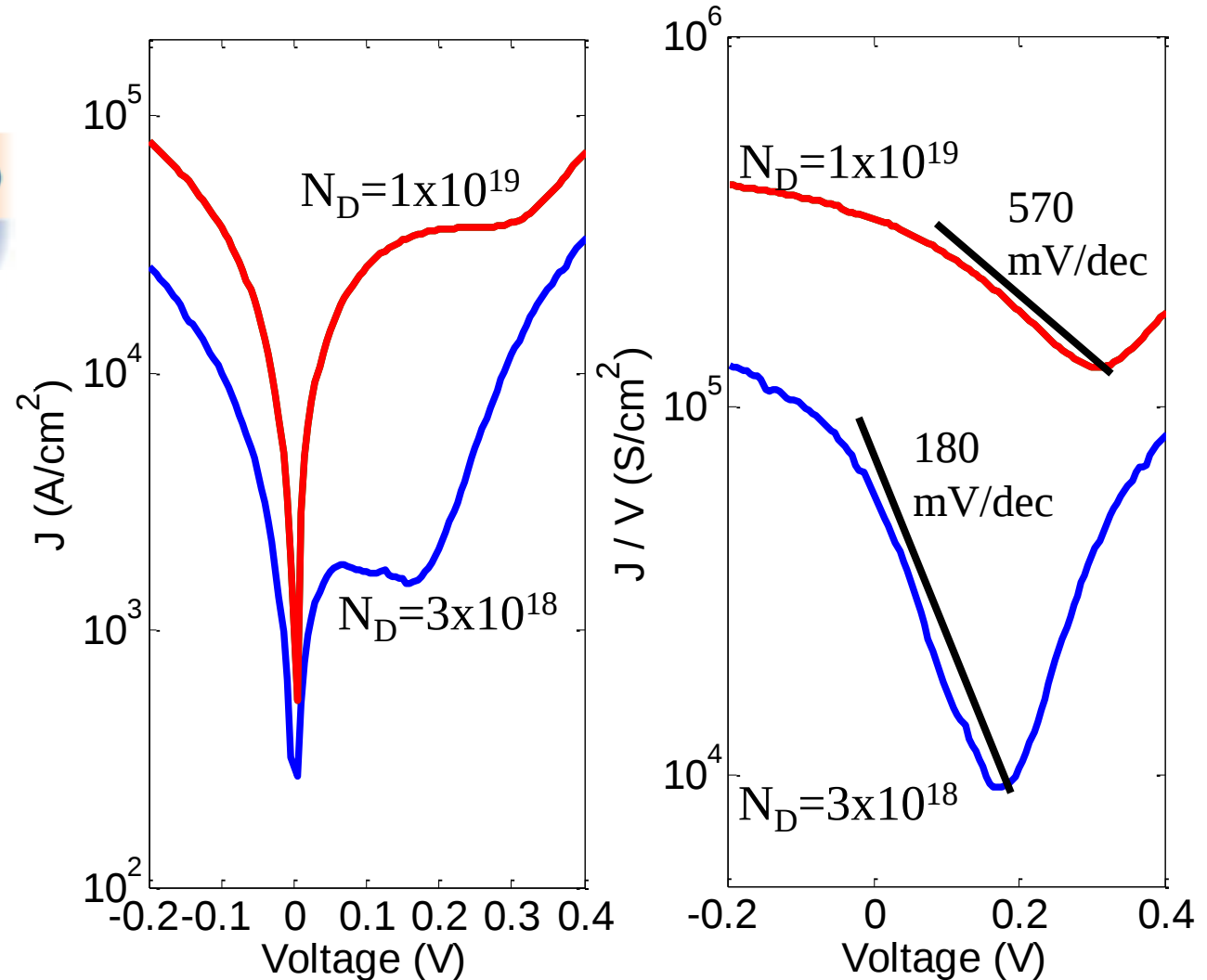


From Pawlik et al, "Benchmarking and Improving III-V Esaki Diode Performance with a Record 2.2 MA/cm² Peak Current Density to Enhance TFET Drive Current" IEDM 2012, pp. 812-814

InAs Homojunction Diodes



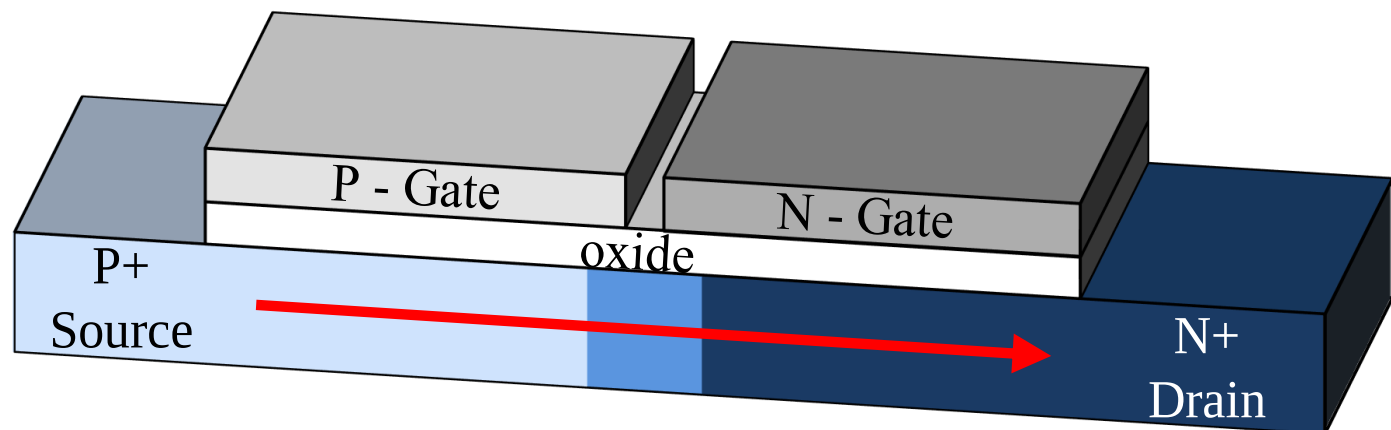
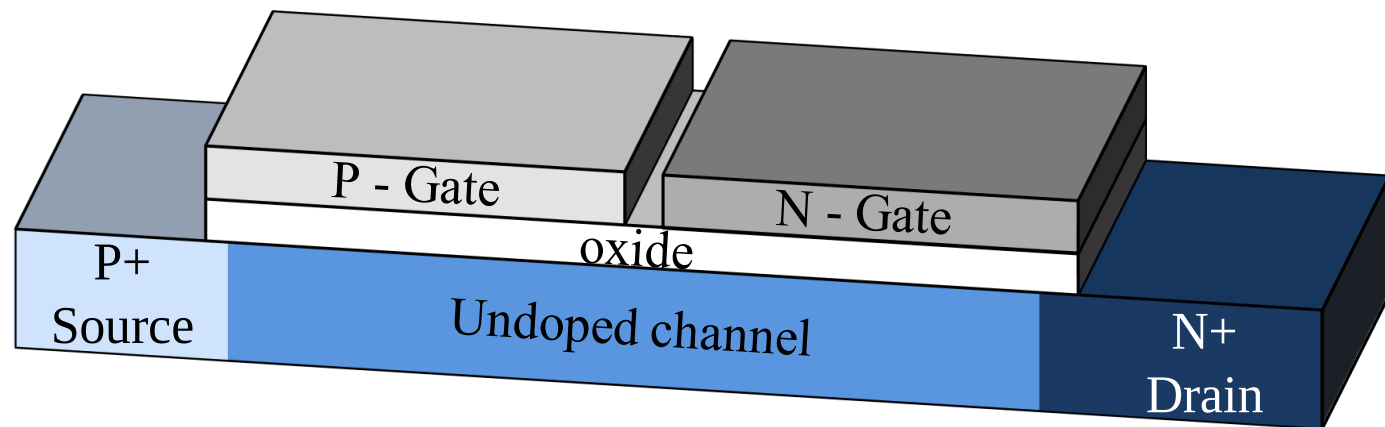
$$N_A = 1.8 \times 10^{19}$$



From Pawlik et al, "Benchmarking and Improving III-V Esaki Diode Performance with a Record 2.2 MA/cm² Peak Current Density to Enhance TFET Drive Current" IEDM 2012, pp. 812-814

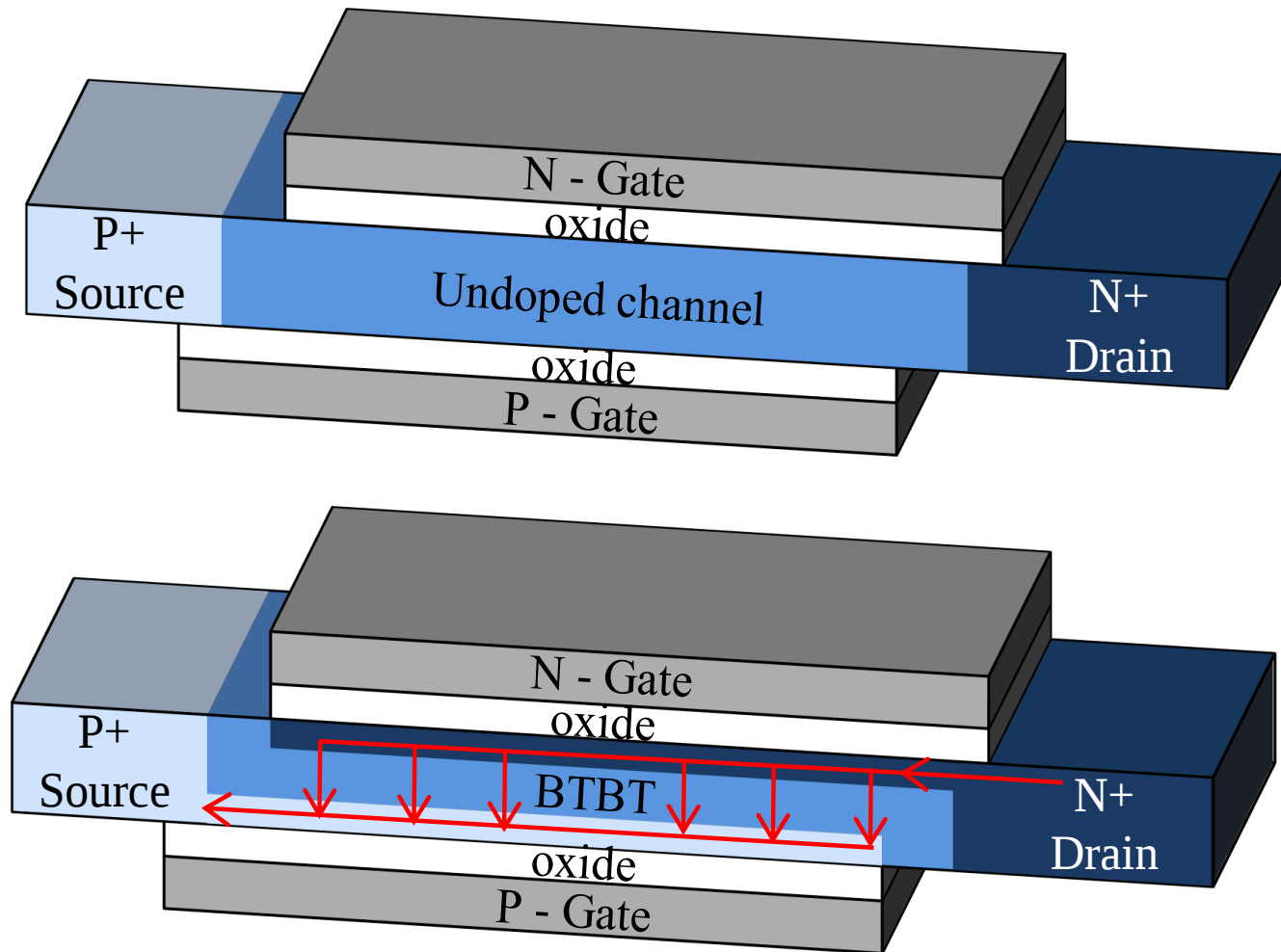
How to Eliminate Doping

Lateral Double Gate TFET

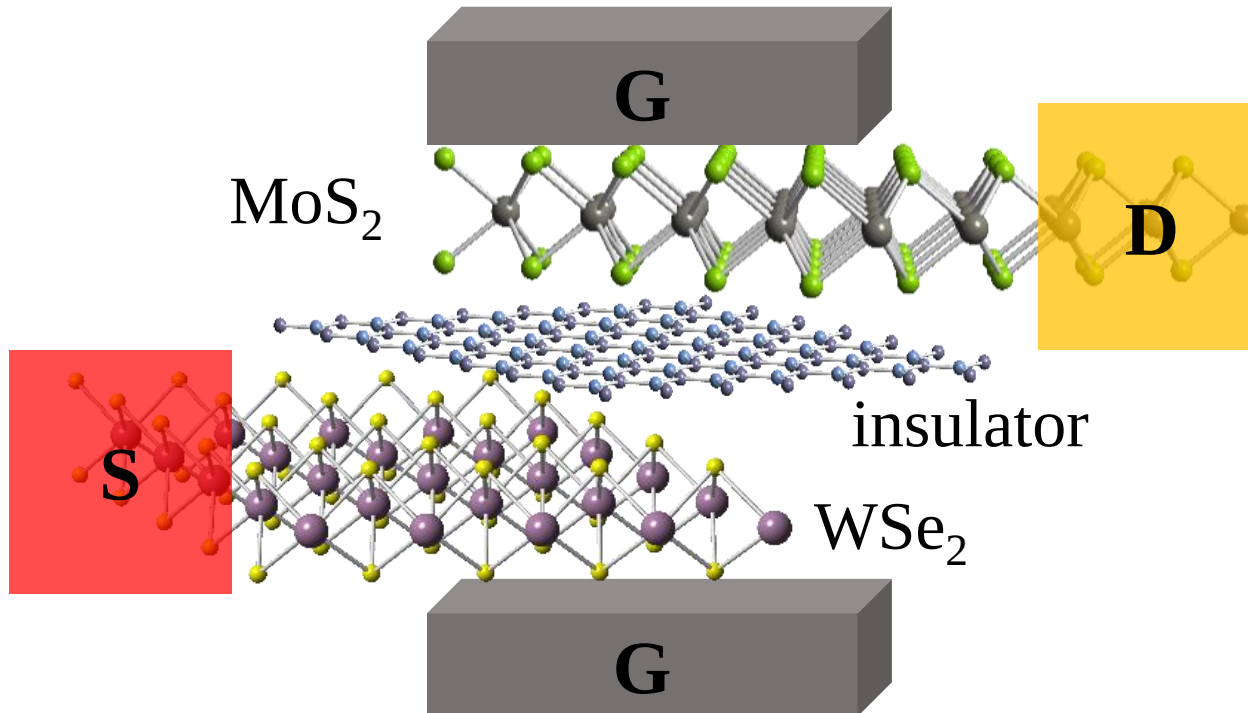


How to Eliminate Doping

Bilayer TFET

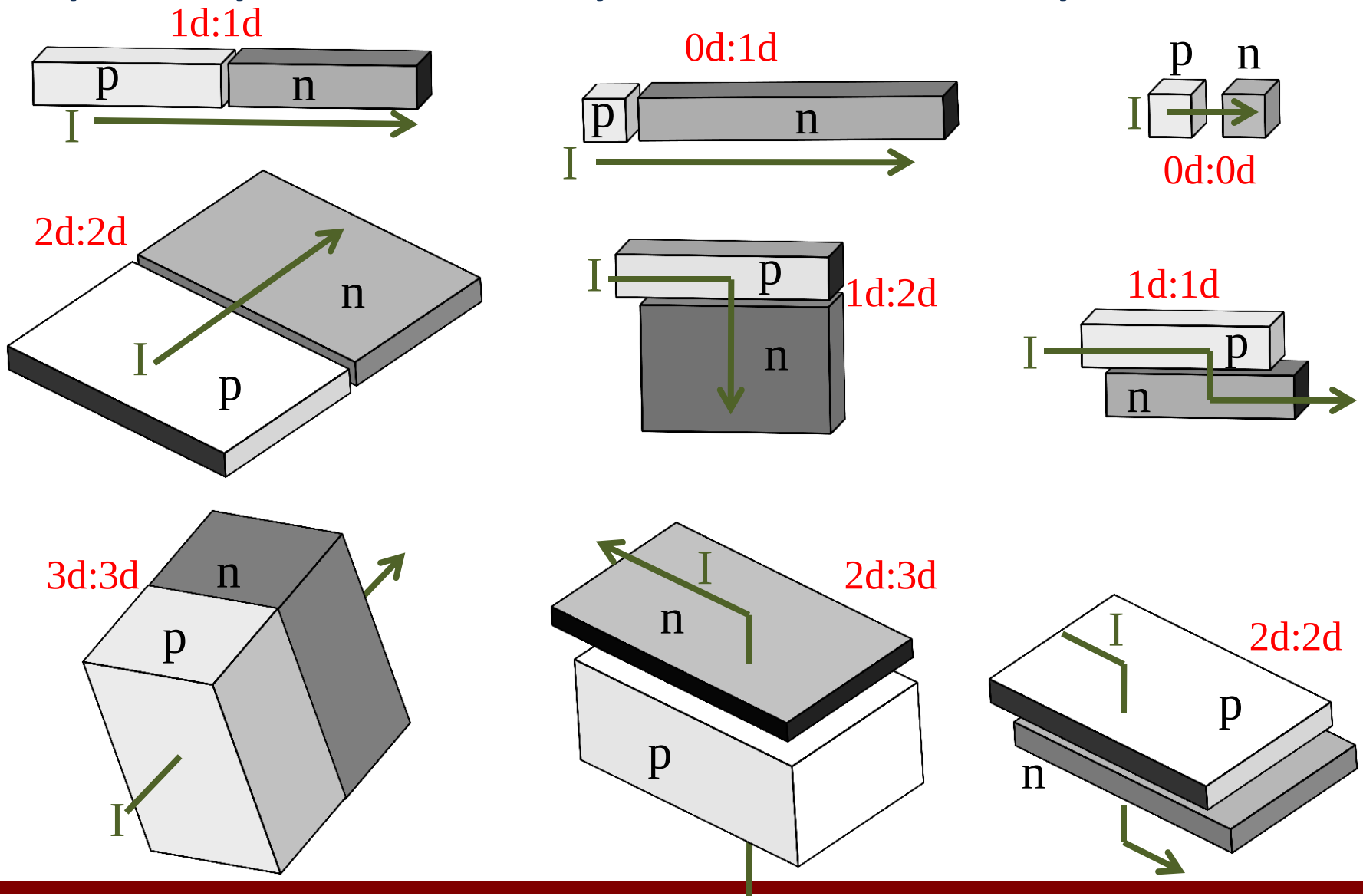


Layered chalcogenides: atomic level flatness and new opportunities



- Scalable down to a single monolayer (~ 7 Angstroms)
- Lack dangling bonds; no native oxide
- van der Waals bonding/interfaces – reduced lattice matching constraints
- Uniform thickness at the atomic level – sharp band edges

An Ideal Density of States Switch is Explicitly Affected by Dimensionality:



Fermi's Golden Rule Approach

$$I = \sum_{k_x, k_y, k_z} \frac{4q\pi}{\hbar} |M_{fi}|^2 \delta(E_i - E_f)$$

Now include all possible
states

Explicitly include
conservation of
transverse momentum

$$I = \sum_{\substack{k_{xi}, k_{yi}, k_{zi} \\ k_{xf}, k_{yf}, k_{zf}}} \frac{4q\pi}{\hbar} |M_{fi}|^2 \delta(E_i - E_f) \delta_{k_{xi}, k_{xf}} \delta_{k_{yi}, k_{yf}}$$

The number of
sums is reduced
for reduced
dimensionality

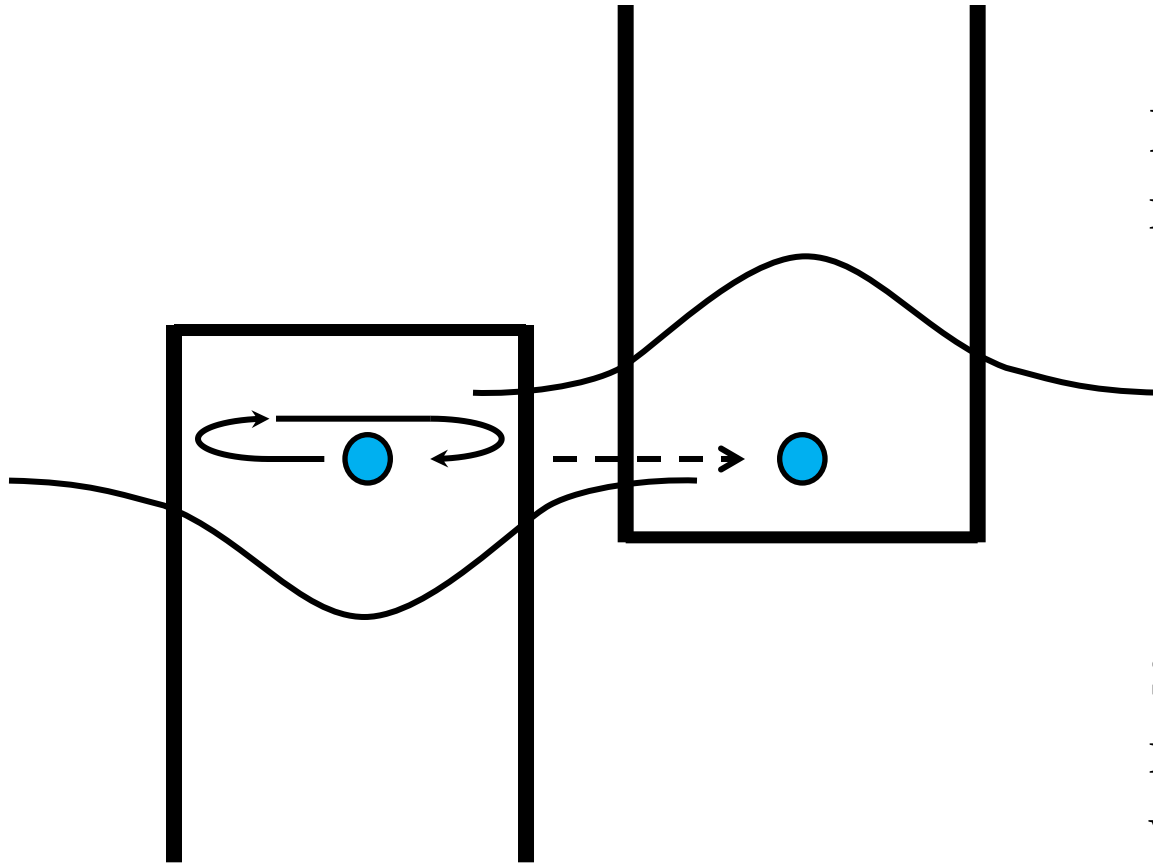
$$M_{fi} = \frac{\hbar^2}{2m} \sqrt{\left(\frac{k_{zi} k_{zf}}{L_{zi} L_{zf}} \right)} \sqrt{T}$$

References:

W. A. Harrison, "Tunneling from an independent-particle point of view," *Physical Review*, vol. 123, pp. 85-89, 1 July 1961.

C. B. Duke, *Tunneling in Solids*. New York: Academic Press, Inc, 1969.

Confinement in the Tunneling Direction Increases Conductance

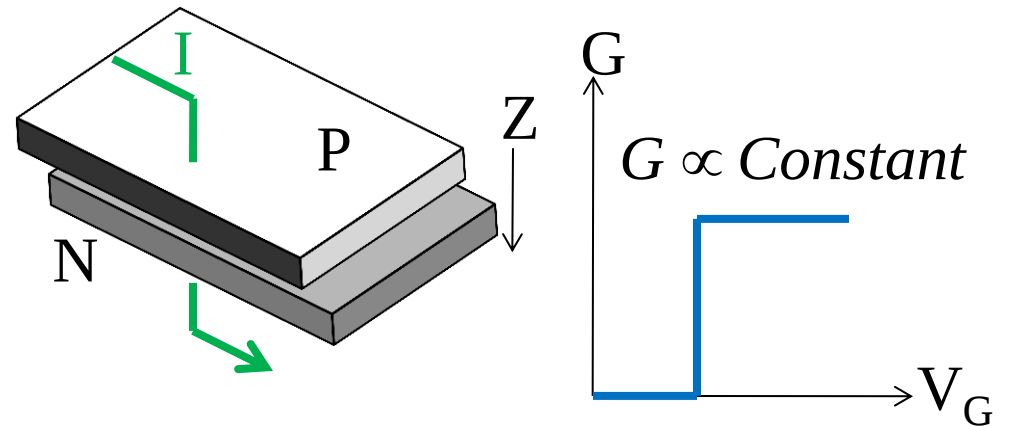
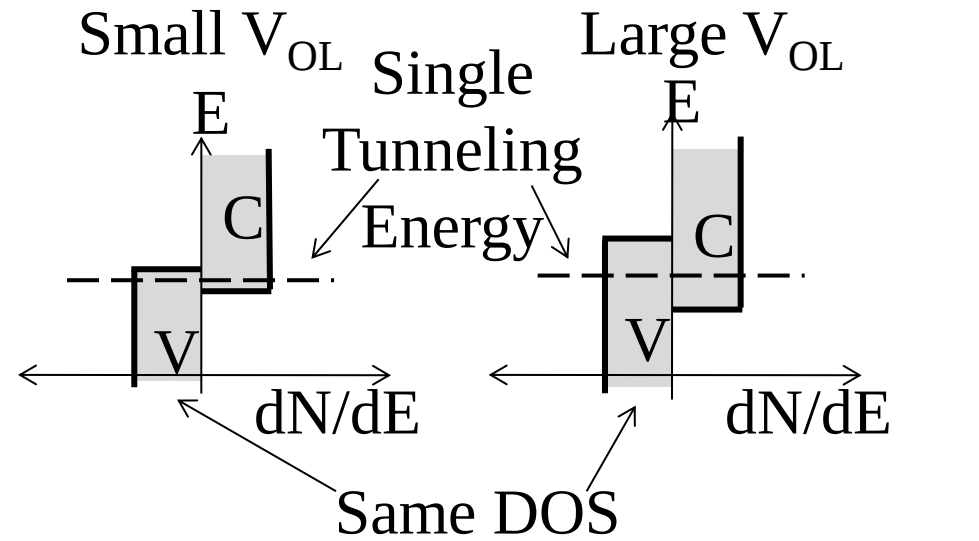
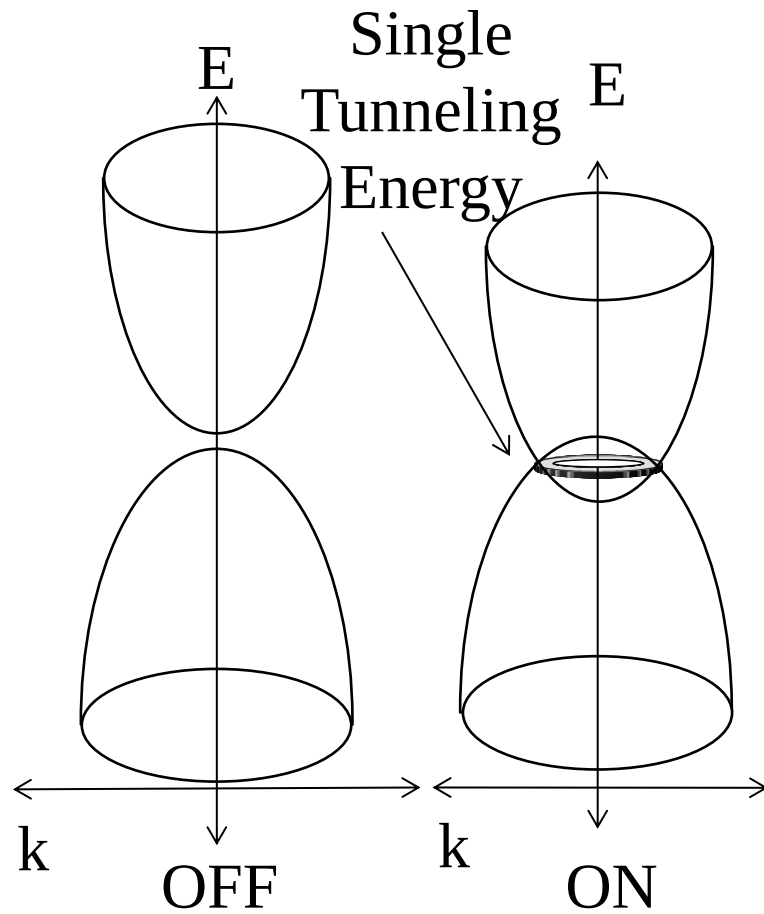


Higher energy results in more tunneling attempts

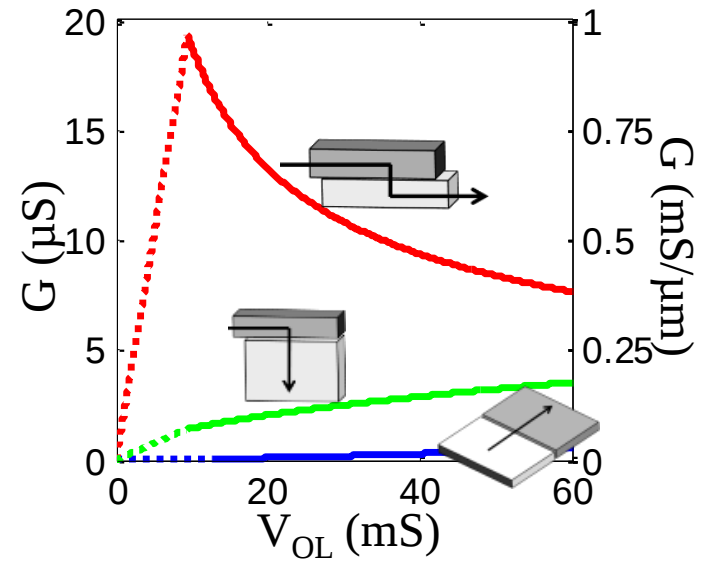
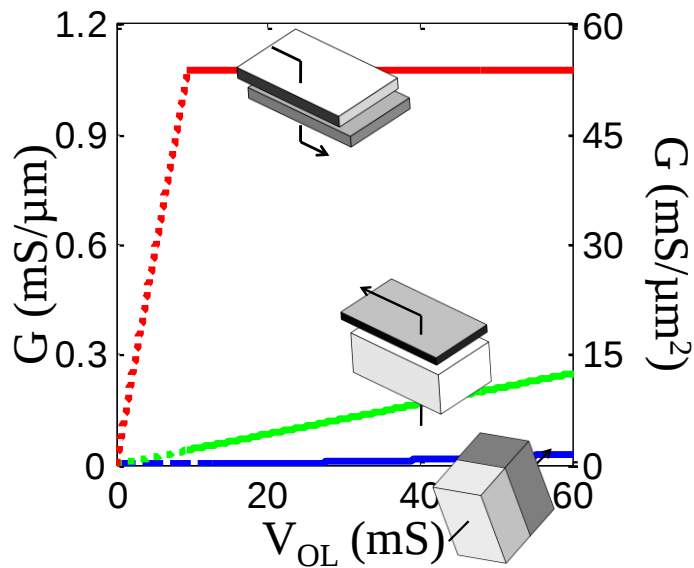
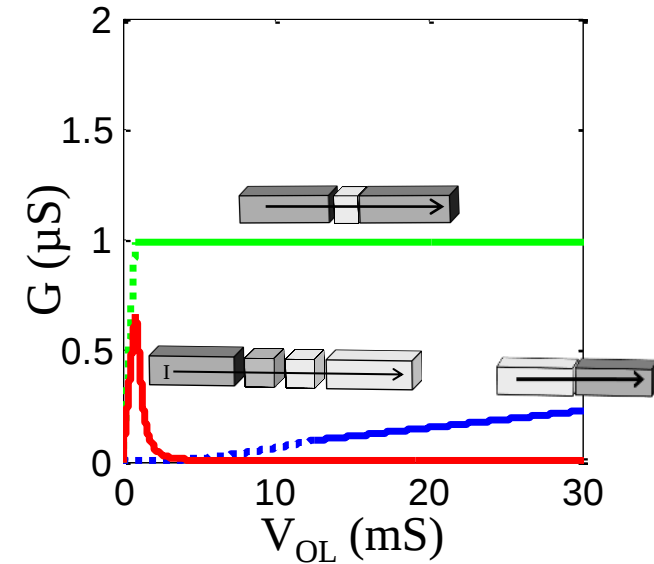
Smaller quantum well results in a larger wavefunction overlap

$$E_z = \frac{1}{2} m v_z^2$$

2d-2d Bilayer



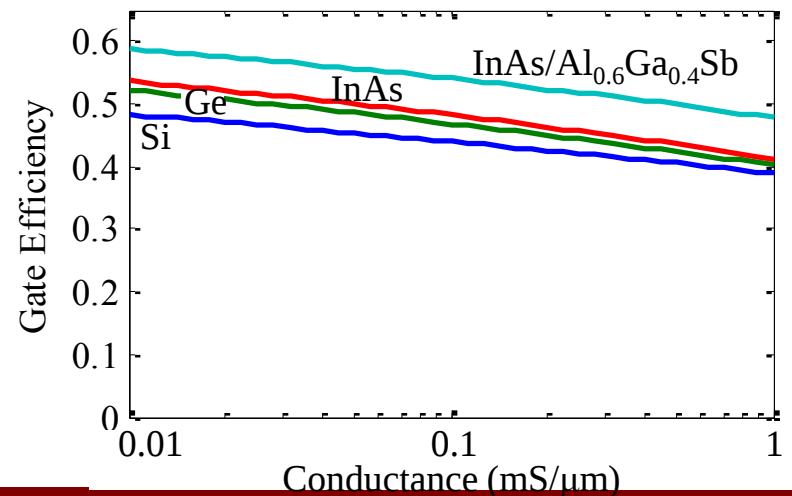
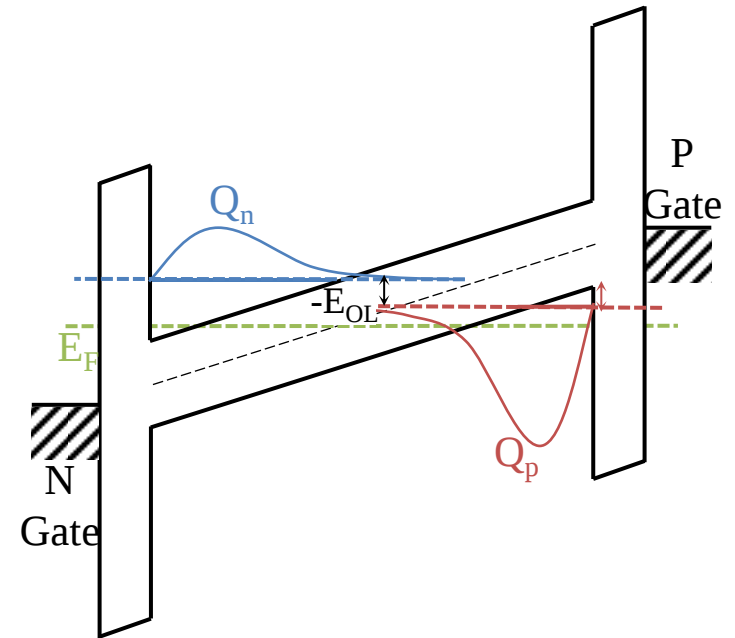
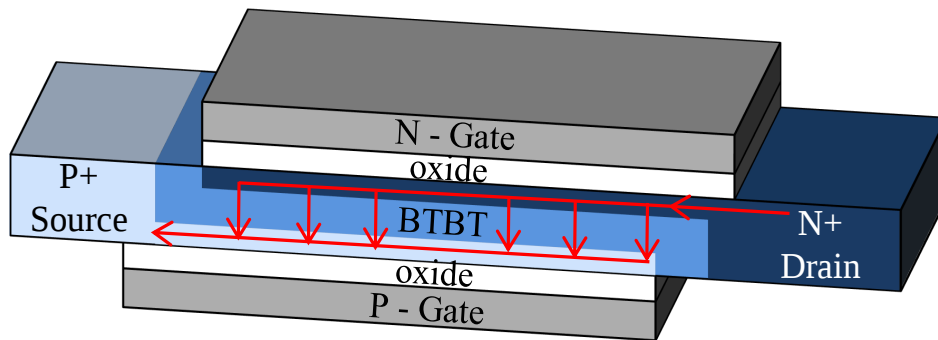
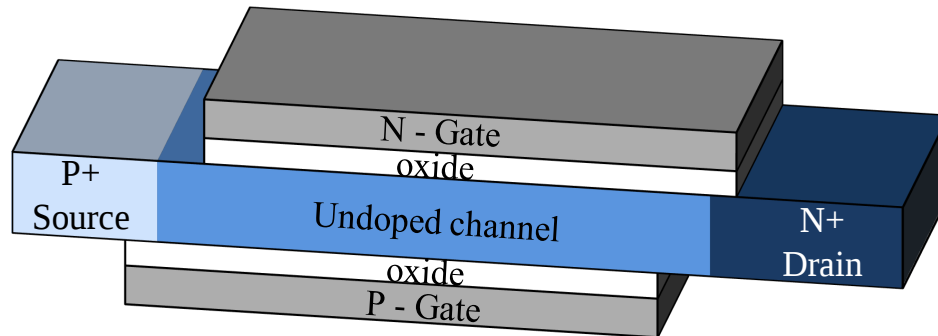
Compare the Dimensionalities



$T=1\%$, $m^*=0.1m_e$
Overlap Lengths=20 nm
Confinement Energies=130 meV

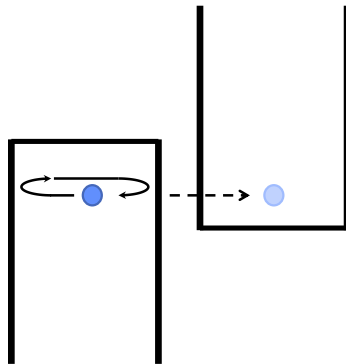
Conductance increase verified by NEGF

Putting it All Together: Bilayer TFET



The Low Voltage TFET Demands Higher Perfection than Previously Required

- Need a steep density of states to get a steep subthreshold swing
- Must drastically reduce the interface state trap density
 - Quantum Well DOS $\sim 10^{12}/\text{cm}^2 \text{ eV}$, $D_{\text{IT}} \sim 10^{11}/\text{cm}^2 \text{ eV}$
- No doping – use gates to electrostatically control the Fermi level
- Use Quantum Confinement

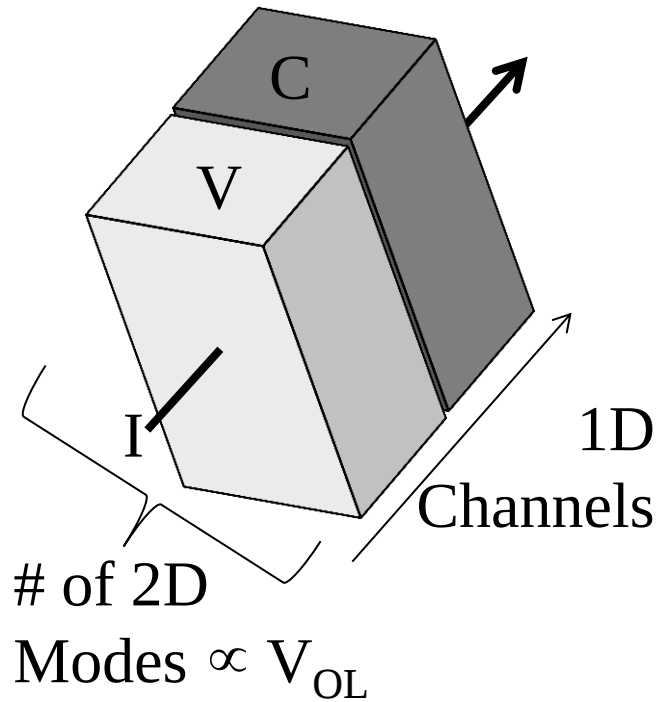


Reduce the voltage to $< 100 \text{ mV}$

**10X reduction in voltage
100X reduction in power**

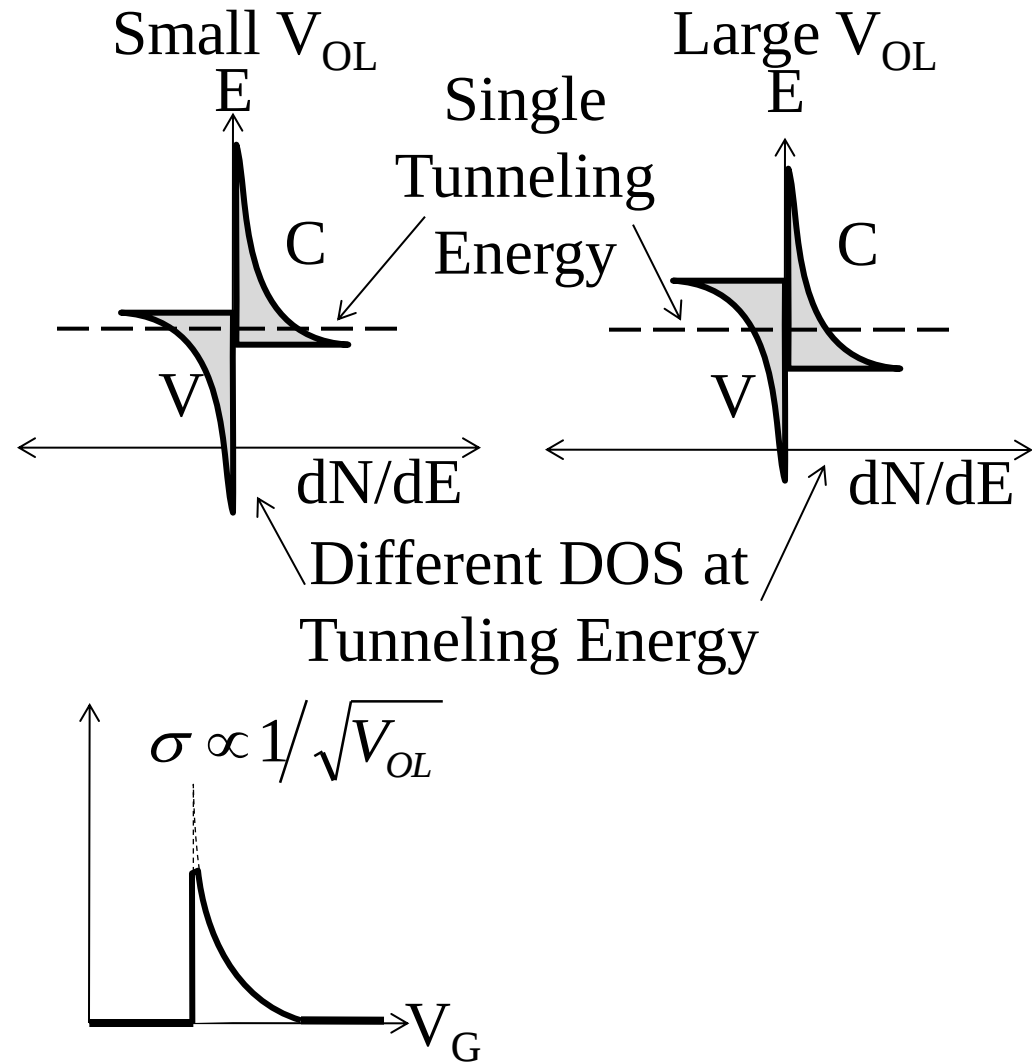
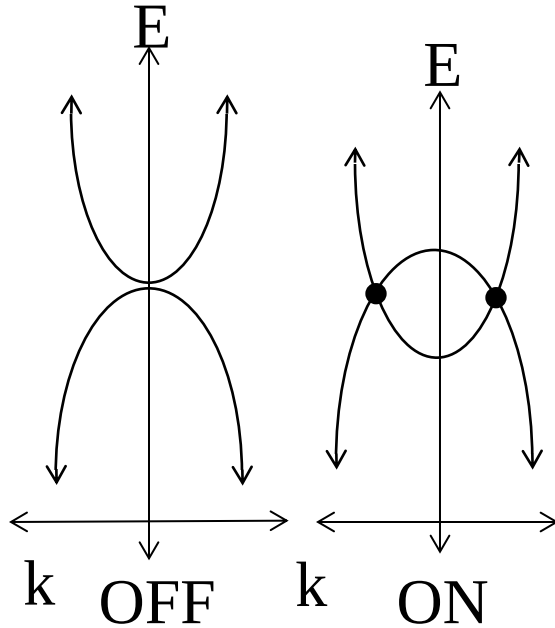
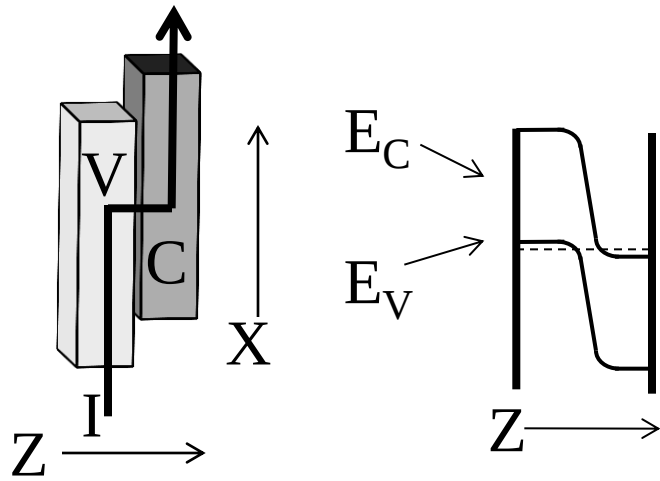
Extra Slides

3d-3d Tunneling

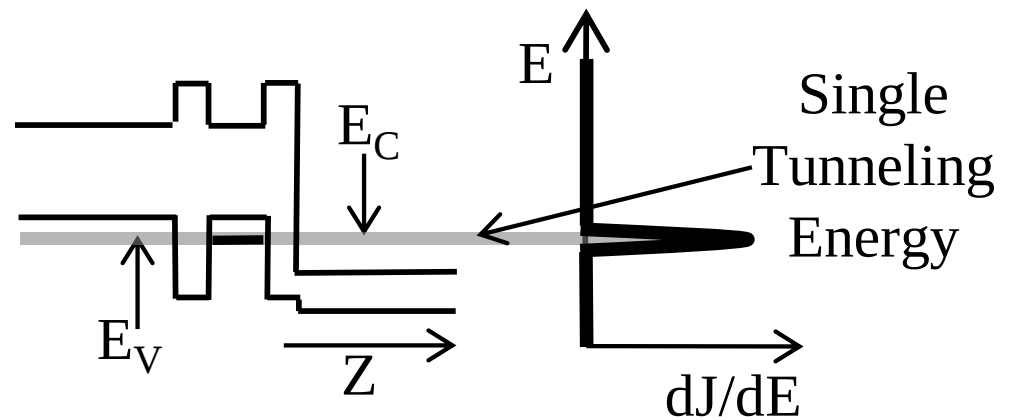
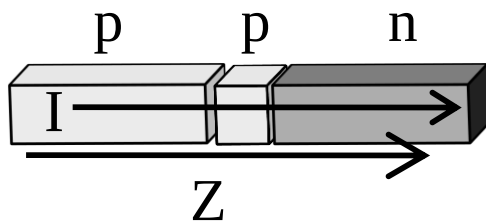
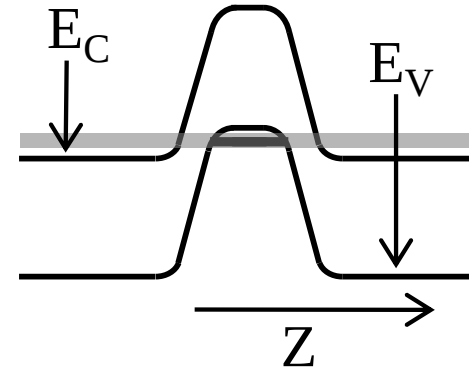
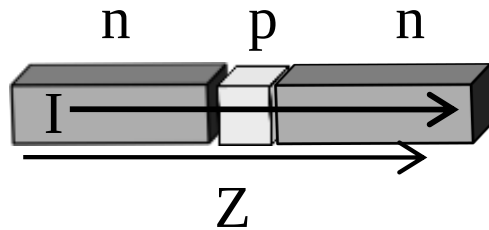


$$\partial I = N_{\perp \text{ States}} \times \frac{2e}{h} \times T \times (f_c - f_v) \times \partial E$$

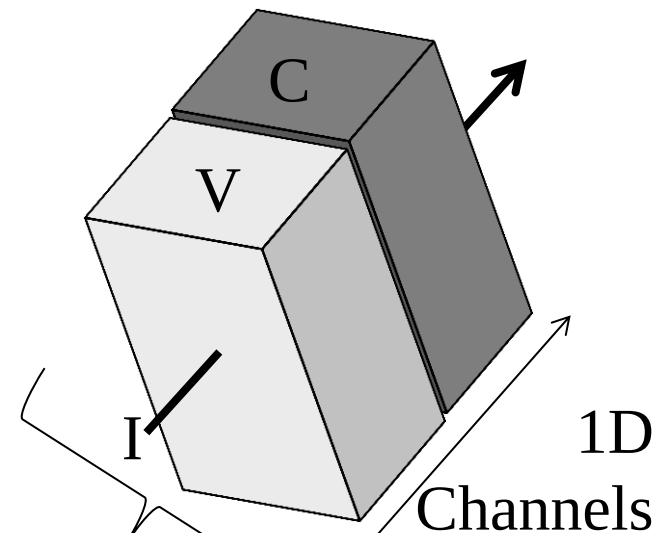
1d-1d Edge Overlap



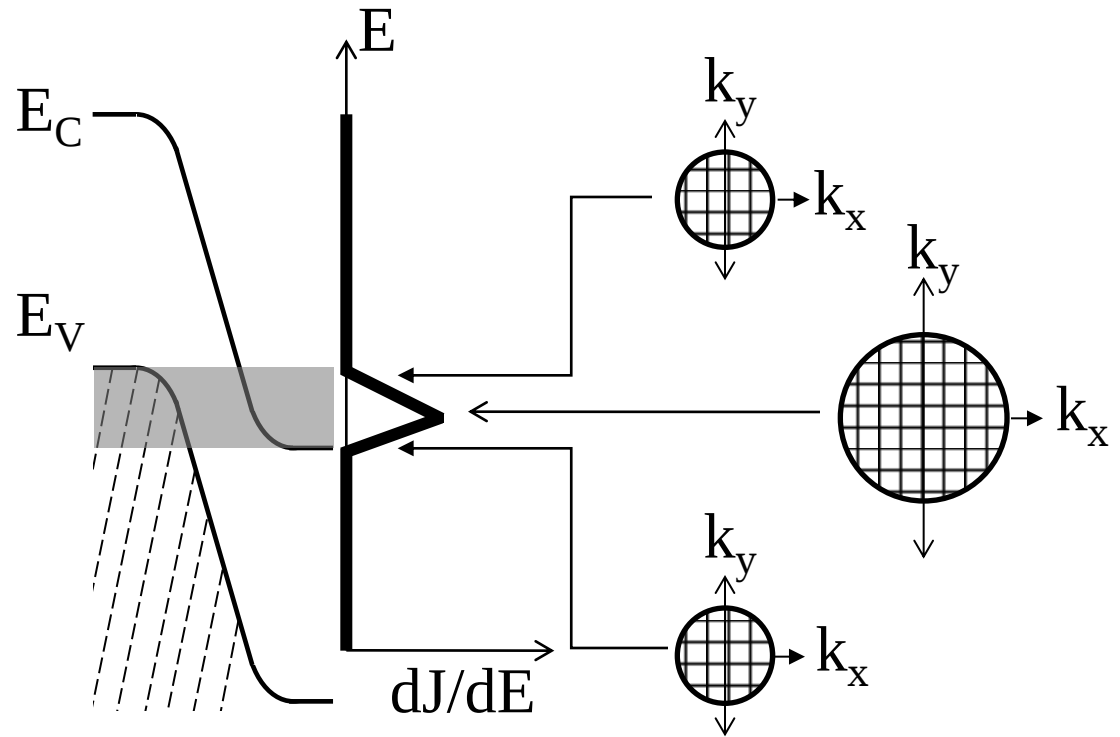
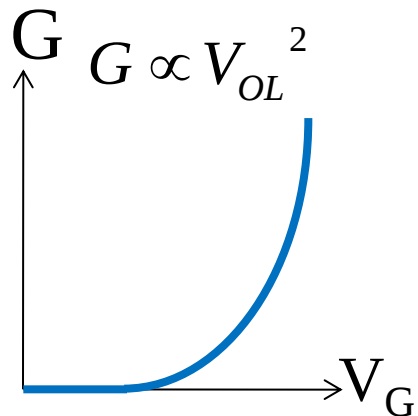
0d-1d Junction



3d-3d Tunneling



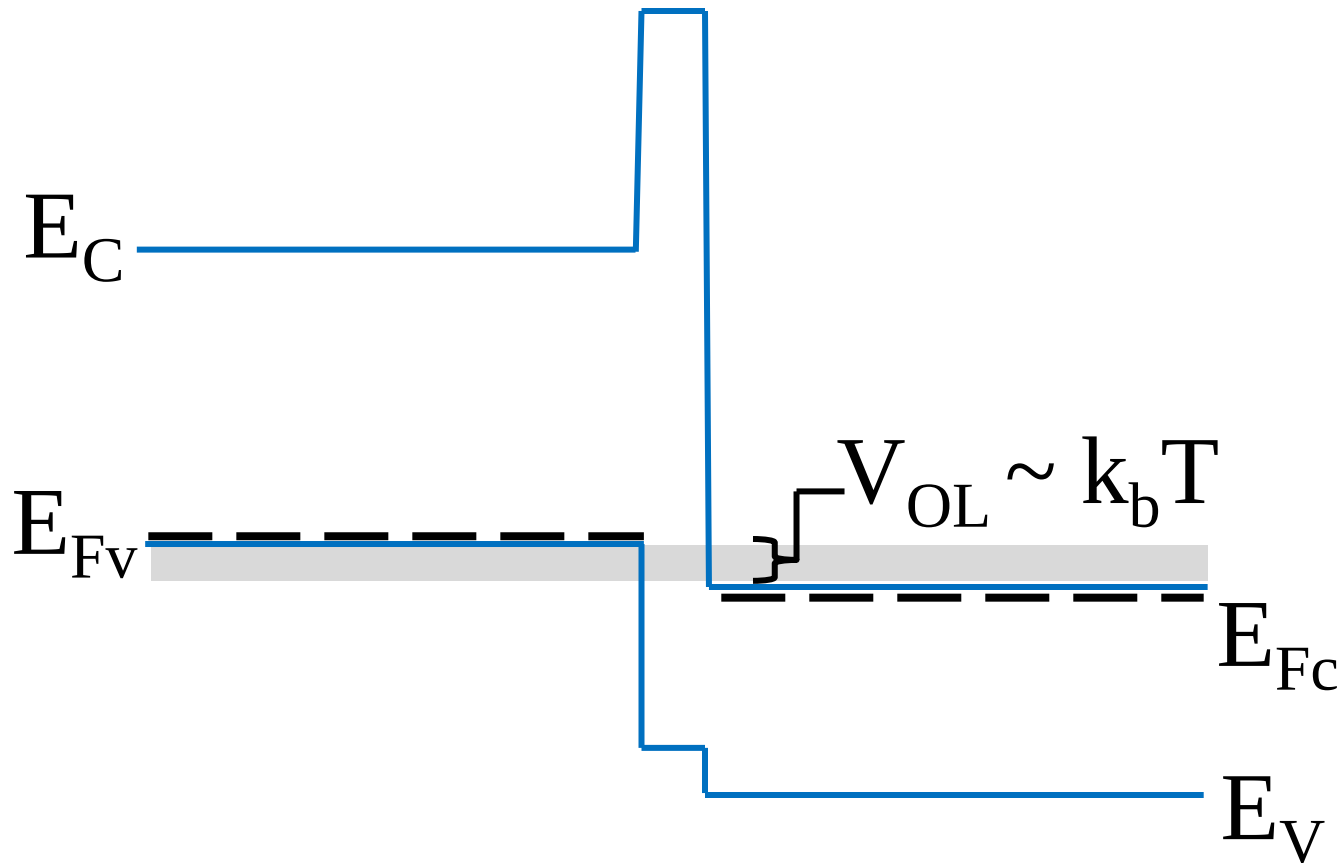
$\text{\# of 2D Modes} \propto V_{OL}$



$$I_{3d-3d} \approx \left(\frac{Am^*}{4\pi\hbar^2} \times \frac{qV_{OL}}{2} \right) \times \left(\frac{2q^2}{h} V_{OL} \times T \right)$$

= # of 2D Channels $\times$ 1D Conductance

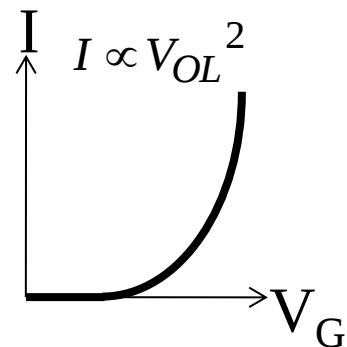
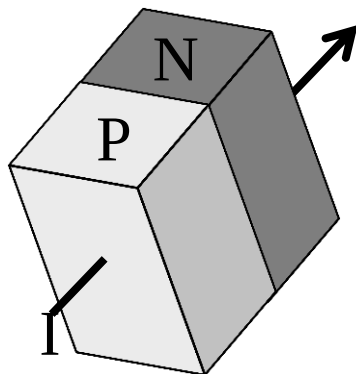
Consider an Ideal Density of States Switch



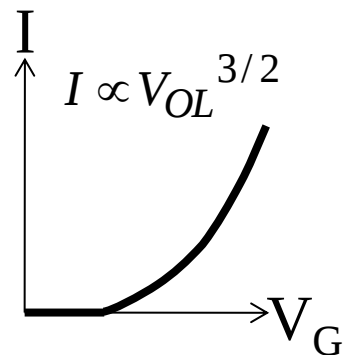
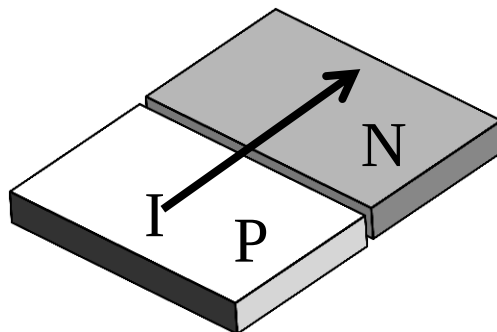
$T \approx \text{constant}$

Compare the Dimensionalities

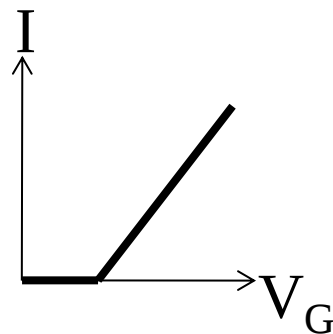
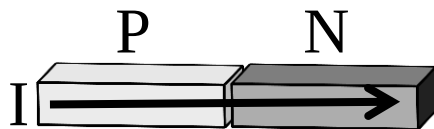
3d-3d



2d-2d_{edge}

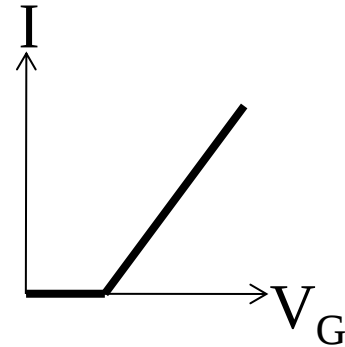
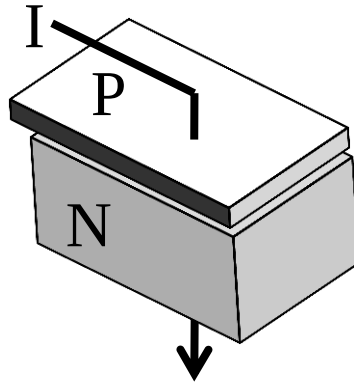


1d-1d_{point}

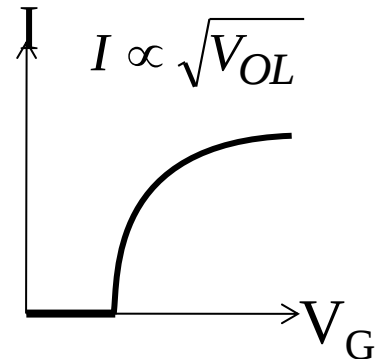
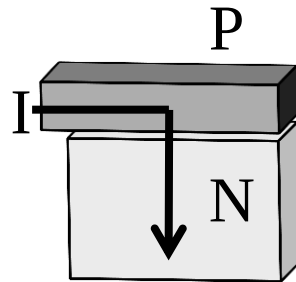


Compare the Dimensionalities

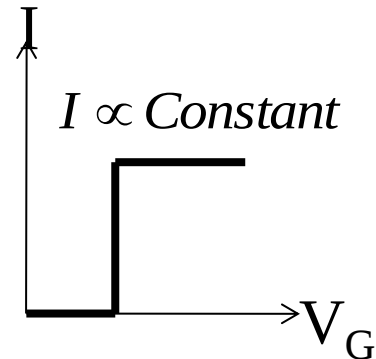
2d-3d



1d-2d

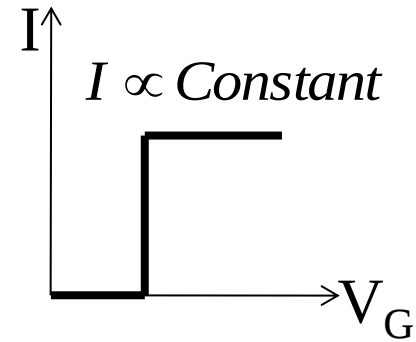
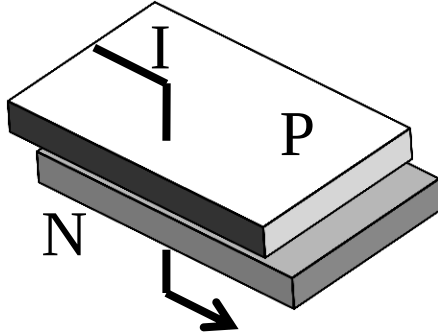


0d-1d

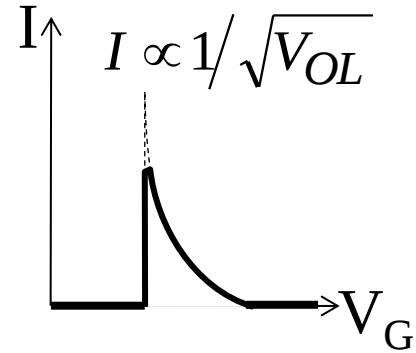
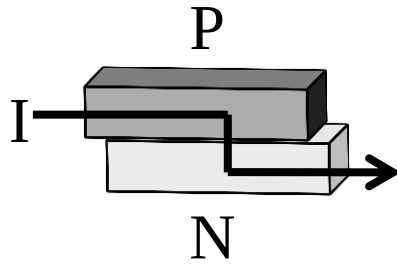


Compare the Dimensionalities

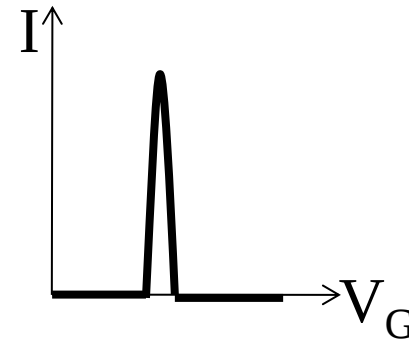
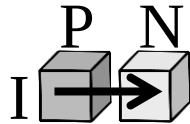
2d-2d_{face}



1d-1d_{edge}



0d-0d



Why so many Non-Steep Results?

Technological:

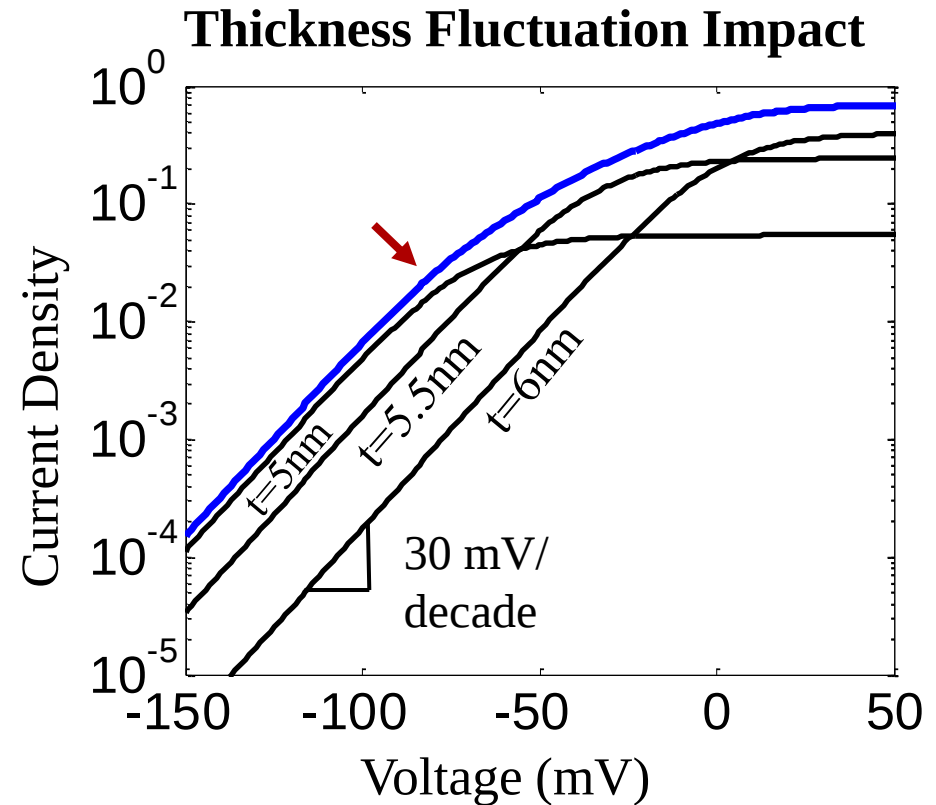
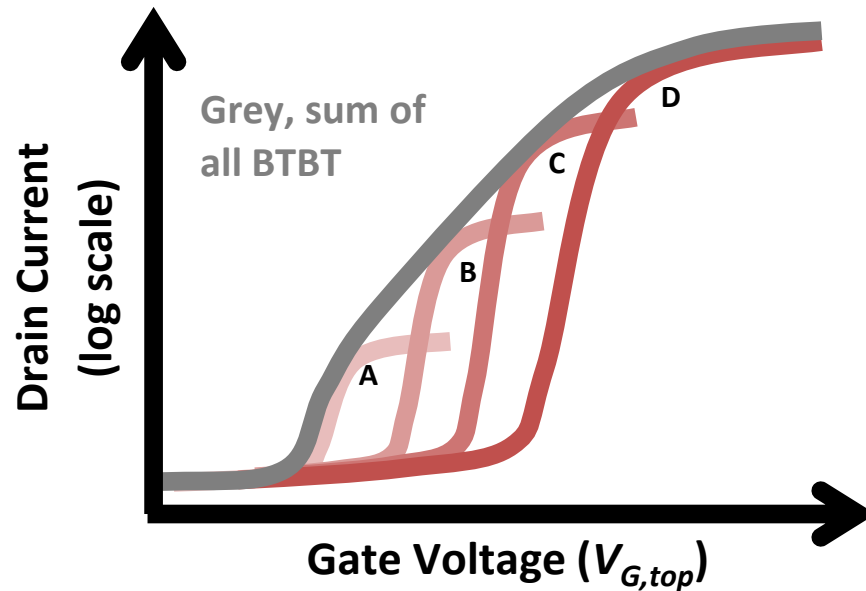
- Band-tails caused by heavy doping
- Interface traps
- Mid-gap traps
- Electrostatic design (parasitic paths)
- Spatial Inhomogeneity of semiconductor--
 - Doping & Thickness

Fundamental

- Inherent level broadening (source to drain tunneling)
- Phonon effects

Eliminate Spatial Inhomogeneity

- Make the Devices Very Small.
 - The threshold may not be reproducible, but so far the field doesn't have a single steep device.



Can we use S_{Barrier} ?

$$S_{\text{Barrier}} \approx \left| \frac{\phi_s}{\log(T)} \right|$$

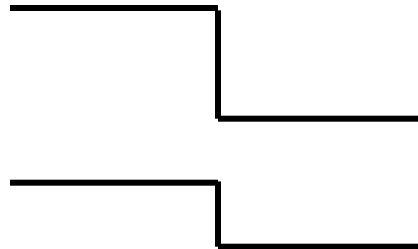
Consider $T \sim 1\%$

$$\log(T) = -2$$

For $S_{\text{Barrier}} = 60 \text{ mV/decade}$, need ϕ_s of 120 meV

Is this reasonable?

$$\log(I_{\text{ON}}/I_{\text{OFF}}) = 120 \text{ meV} / S_{\text{DOS}}$$



For 5 orders of magnitude on/off need $S_{\text{DOS}} < 24 \text{ mV/decade}$

Use steep S_{DOS} for steep subthreshold swing

Find $S_{Barrier}$

$$S_{Barrier} \approx \frac{d\phi_s}{d \log(T)}$$

$$T(\vec{F}) = \exp\left(\frac{-\pi(m_{tunnel}^*)^{1/2} E_g^{3/2}}{2\sqrt{2}\hbar q |\vec{F}|}\right) = \exp\left(\frac{-\alpha}{|\vec{F}|}\right)$$

$$S_{Barrier} \approx \left(\log(e) \times \alpha \times \frac{1}{|\vec{F}|^2} \times \frac{d\vec{F}(\phi_s)}{d\phi_s} \right)^{-1}$$

$$\text{use } |\vec{F}| = -\frac{\log(e) \times \alpha}{\log(T)}$$

$$S_{Barrier} \approx \left| \frac{1}{\log(T)} \times \frac{F}{d\vec{F}(\phi_s) / d\phi_s} \right|$$

Lateral/point TFET

$$|\vec{F}| = \frac{\phi_s}{l_{screening}}$$

$$\frac{|\vec{F}|}{dF / d\phi_s} = \phi_s$$

Bilayer TFET

$$|\vec{F}| = \frac{\phi_s}{t_{body}}$$

$$\frac{|\vec{F}|}{dF / d\phi_s} = \phi_s$$

$$S_{Barrier} \approx \left| \frac{\phi_s}{\log(T)} \right|$$

Find $S_{Barrier}$

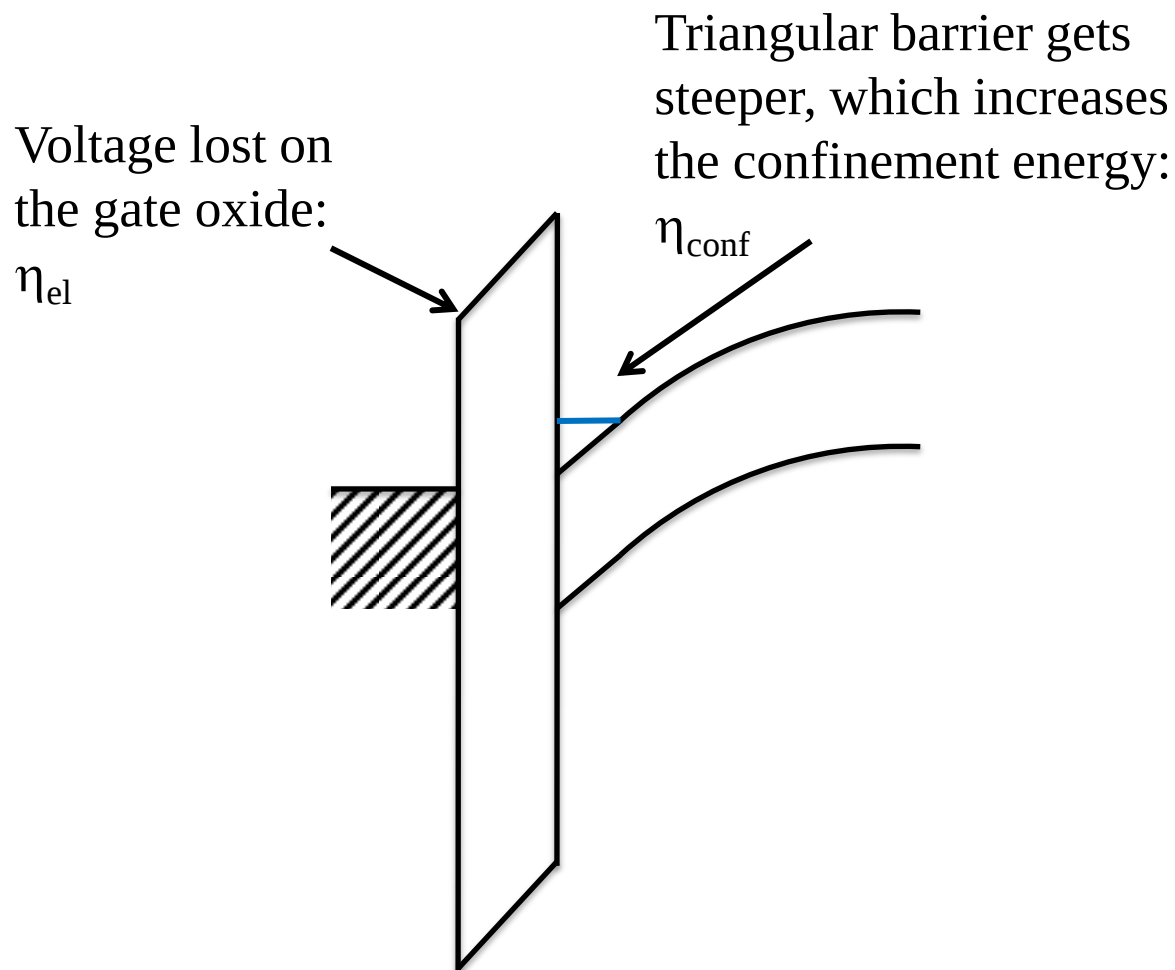
Vertical TFET

$$|\vec{F}| = \frac{\phi_s}{W_{depletion}} \frac{= \phi_s}{\sqrt{\epsilon_s \phi_s / 2qN_d}}$$

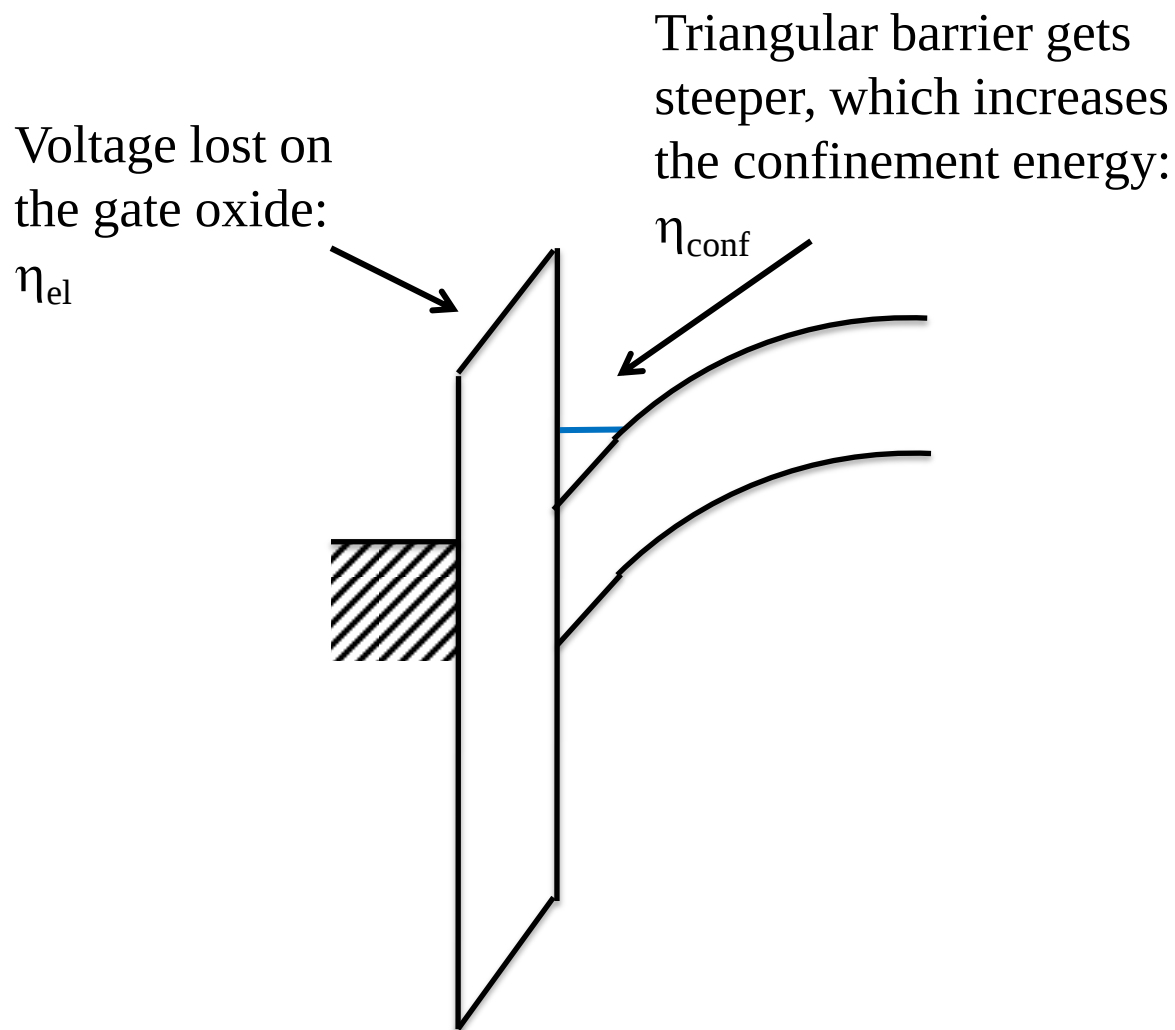
$$\frac{d\vec{F}}{\phi_s} = \frac{1}{2} \sqrt{\frac{2qN_d}{\epsilon_s}} \phi_s^{-1/2} = \frac{1}{2\phi_s} \vec{F}$$

$$S_{Barrier} \approx \left| \frac{2 \times \phi_s}{\log(T)} \right|$$

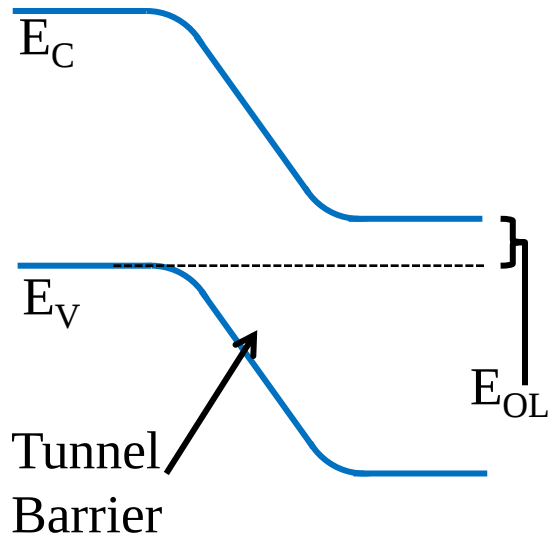
Need to Maximize Gate Efficiency



Need to Maximize Gate Efficiency



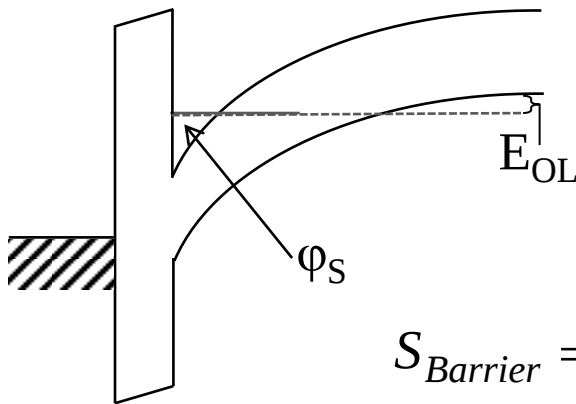
Four Factors Determine The Subthreshold Swing



$$I \propto DOS \times \text{Tunneling Probability}$$

$$SS = \left(\frac{d \log(I)}{dV_G} \right)^{-1}$$

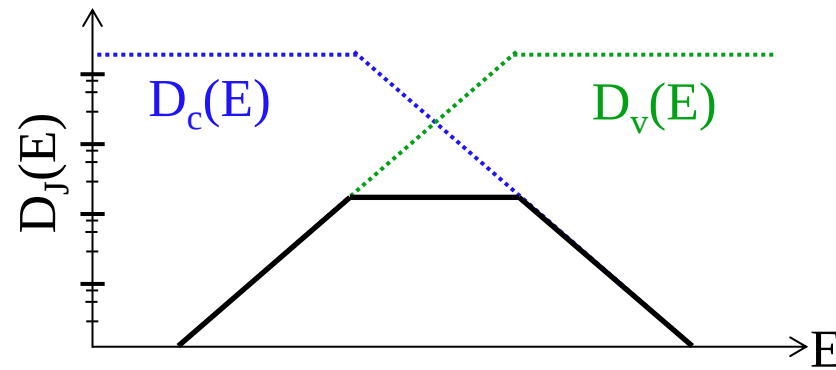
$$= \frac{1}{\eta_{el}} \left(\frac{\eta_{conf}}{S_{DOS}} + \frac{1}{S_{Barrier}} \right)^{-1}$$



$$S_{Barrier} = \frac{d \log(T)}{d\phi_s} \quad S_{DOS} = \frac{d \log(DOS)}{dE_{OL}} \quad \eta_{conf} = \frac{dE_{OL}}{d\phi_s} \quad \eta_{el} = \frac{d\phi_s}{dV_G}$$

Modeling the Tunneling Current

$$I \propto \int (f_C - f_V) \times T \times D_J(E) \times \partial E$$

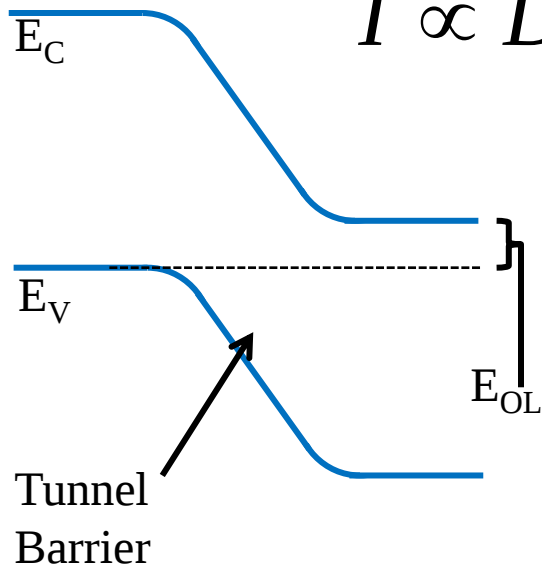


$$I \propto e^{-|E_{OL}|/qV_0} \times \int_{E_V'}^{E_C'} (f_C - f_V) \times T \times D_0 \times \partial E$$

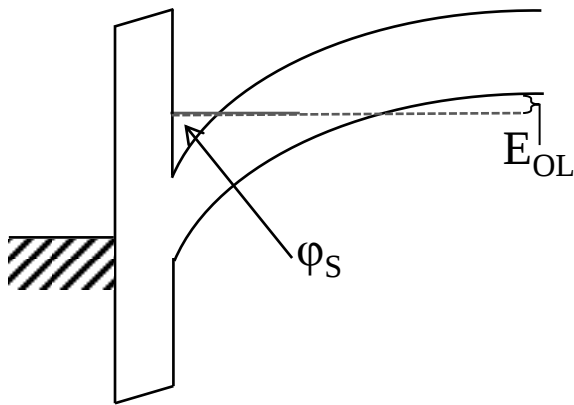
$$I \propto DOS \times \text{Tunneling Current}$$

Four Factors Determine The Subthreshold Swing

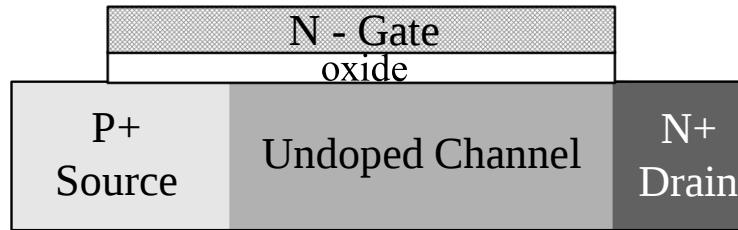
$I \propto DOS \times \text{Tunneling Probability}$



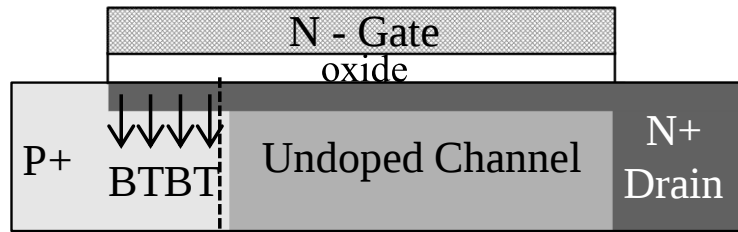
$$\begin{aligned}
 SS &= \left(\frac{d \log(I)}{dV_G} \right)^{-1} = \left(\frac{d \log(DOS)}{dV_G} + \frac{d \log(T)}{dV_G} \right)^{-1} \\
 &= \left(\frac{d\phi_s}{dV_G} \frac{dE_{OL}}{d\phi_s} \frac{d \log(DOS)}{dE_{OL}} + \frac{d\phi_s}{dV_G} \frac{d \log(T)}{d\phi_s} \right)^{-1} \\
 &= \left(\frac{\eta_{el} \eta_{conf}}{S_{DOS}} + \frac{\eta_{el}}{S_{Barrier}} \right)^{-1} \\
 &= \frac{1}{\eta_{el}} \left(\frac{\eta_{conf}}{S_{DOS}} + \frac{1}{S_{Barrier}} \right)^{-1}
 \end{aligned}$$



Vertical TFET



(b)



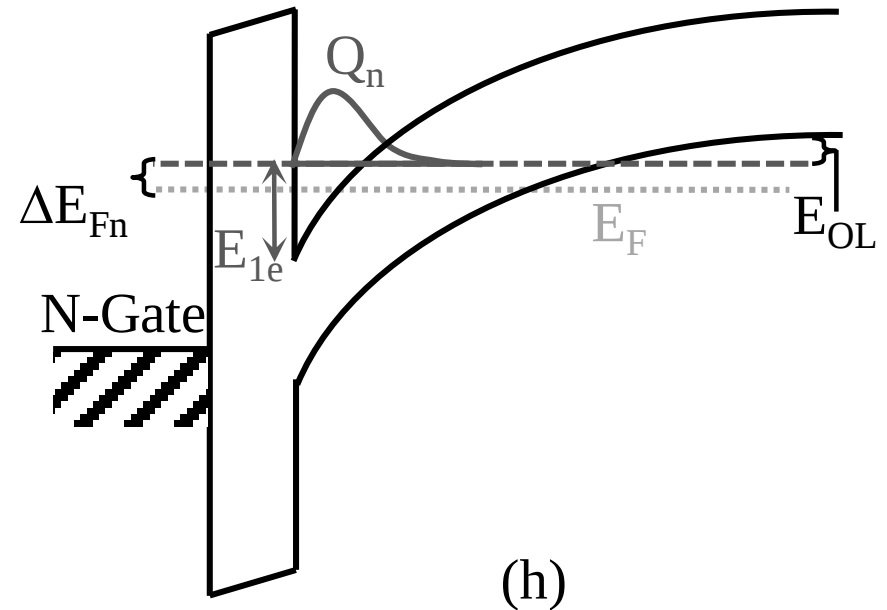
Cut shown in (h)

(e)

$$\eta_{conf} \approx \frac{1}{3} \left(\frac{9\pi}{8} \right)^{2/3} \times \left(\frac{N_d \hbar^2}{m_{e,z}^* \epsilon_s} \right)^{1/3} \times \phi_s^{-2/3}$$

~ 80 – 90%

η_{el} is standard planar MOSFET
gate efficiency

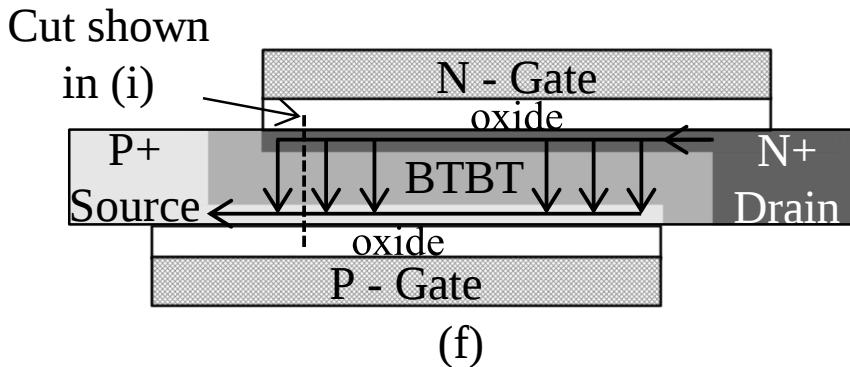
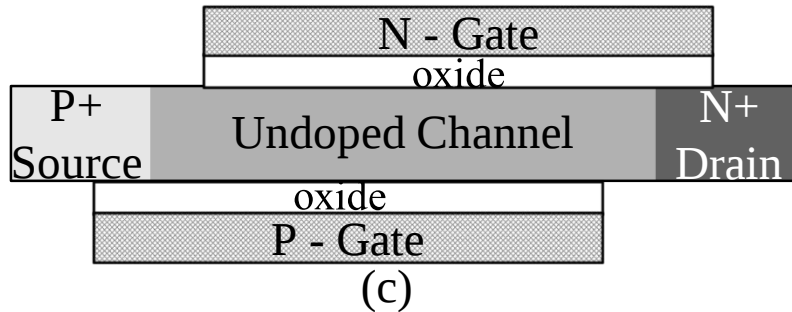


(h)

Higher I_{ON}

Always requires doping to get
band bending -> poor S_{DOS}

Bilayer TFET



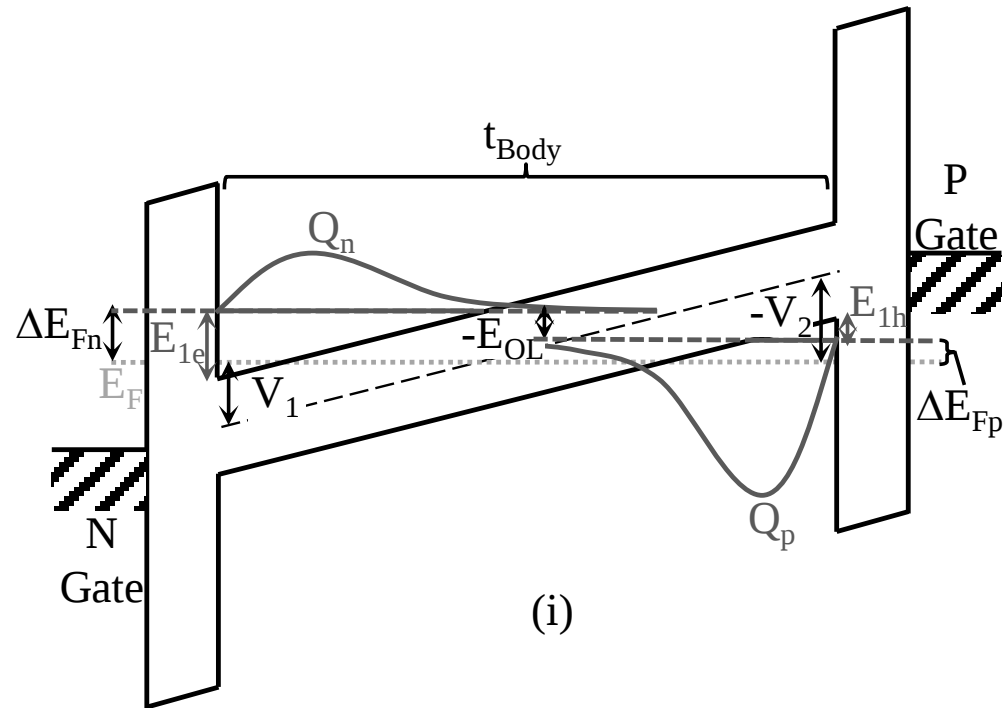
Two gate oxides and thin body

→ $\eta_{el} \sim 60\text{-}70\%$

Confined Electron and Hole Levels

→ $\eta_{conf} \sim 60\text{-}70\%$

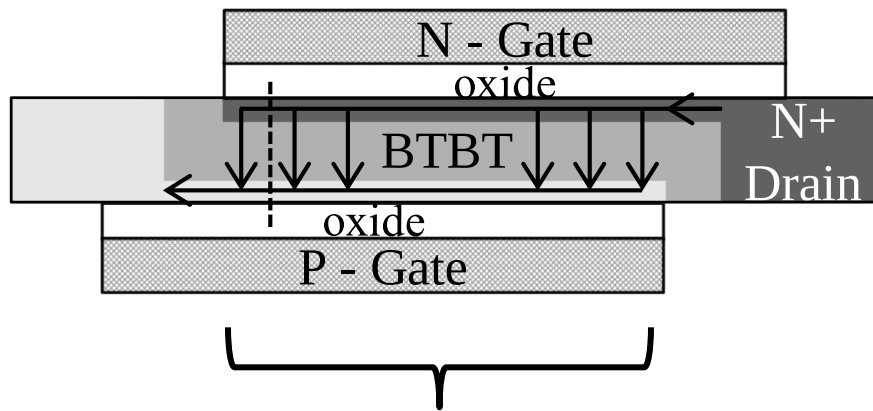
$\eta_{conf} \times \eta_{el} \sim 40\text{-}50\%$



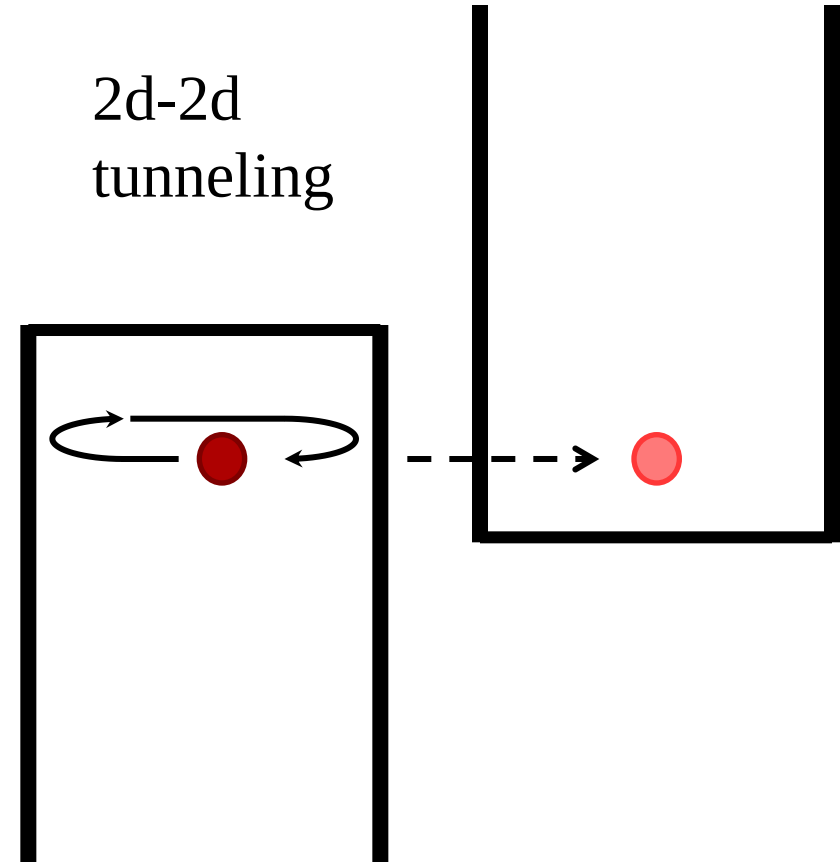
Highest I_{ON}

Lowest Overdrive Voltage

High Bilayer Conductance



Large Tunneling Area



$$E_z = \frac{1}{2} m v_z^2$$

What is Happening in a Diode at Small Bias?

$$I \propto \int (f_C - f_V) \times T \times D_J(E) \times \partial E$$

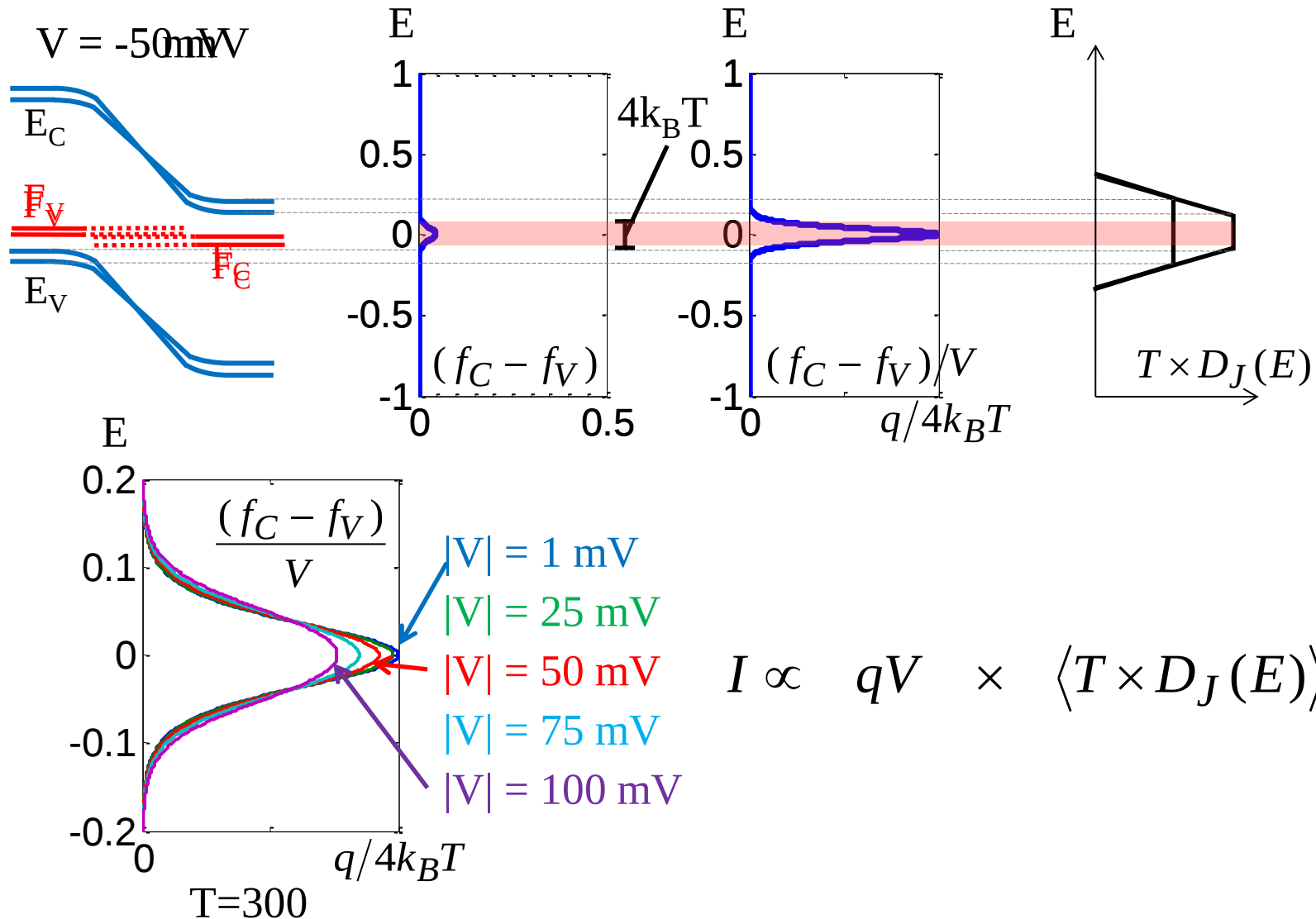
Fermi Functions
Tunneling probability
Joint Density of States

Consider Small Bias

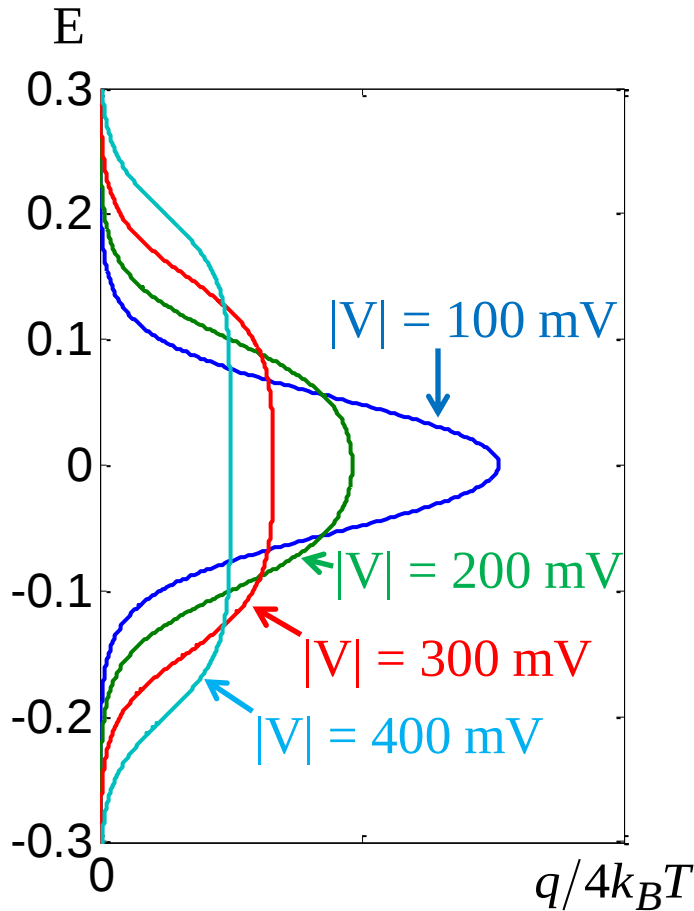
$$I \propto \int (f_C - f_V) \times \partial E \times \frac{\int (f_C - f_V) \times T \times D(E) \times \partial E}{\int (f_C - f_V) \times \partial E}$$

$$= qV \times \langle T \times D(E) \rangle \Big|_{-2k_BT}^{2k_BT}$$

What is Happening in a Diode at Small Bias?



What is Happening in a Diode at Large Bias $> 4k_B T$?



$$(f_C - f_V)/V$$

$$I \propto \int (f_C - f_V) \partial E \times \frac{\int (f_C - f_V) \times T \times D(E) \times \partial E}{\int (f_C - f_V) \partial E}$$

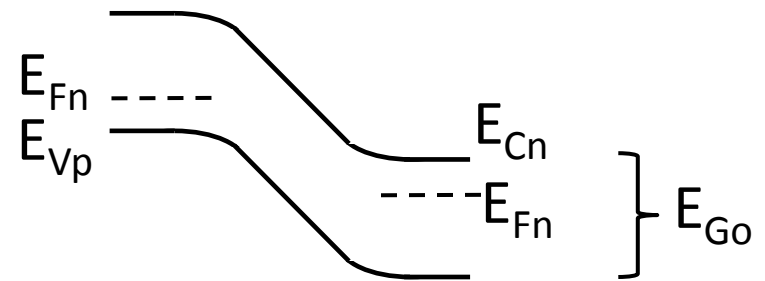
$$= qV \times \left\langle T \times D(E) \right\rangle \Big|_{-V/2}^{V/2}$$

The Band Tails Can be Modeled

$$J = J_0 \int \partial E \times T \times (f_C - f_V) \times D_n(E) \times D_p(E)$$

$$D_p(E) = \begin{cases} 1, & E < E_{vp} \\ e^{-(E-E_{vp})/qV_o}, & E > E_{vp} \end{cases}$$

$$D_n(E) = \begin{cases} 1, & E > E_{cn} \\ e^{+(E-E_{cn})/qV_o}, & E \leq E_{cn} \end{cases}$$



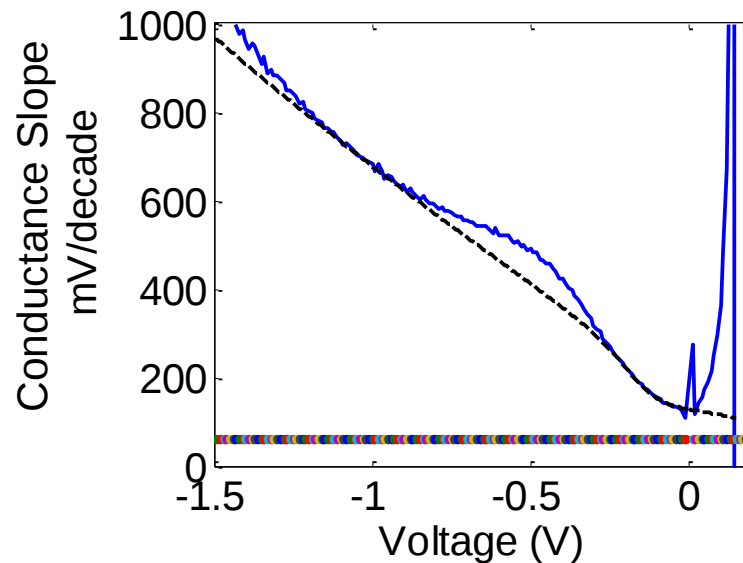
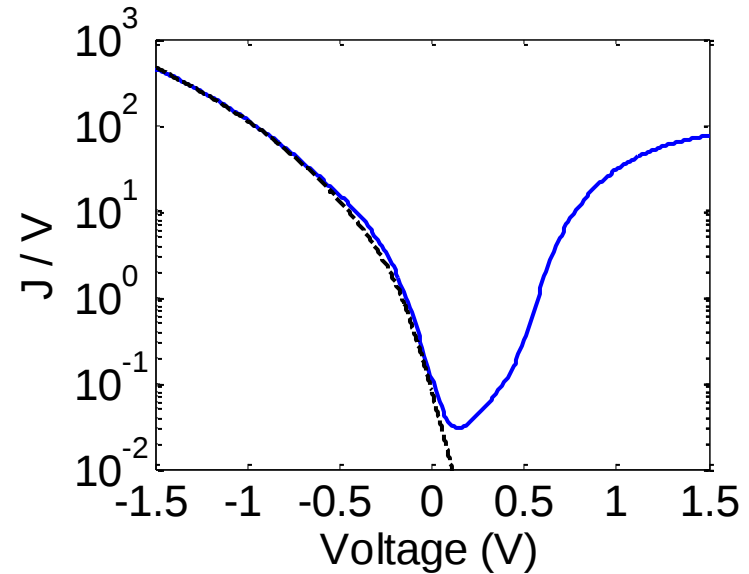
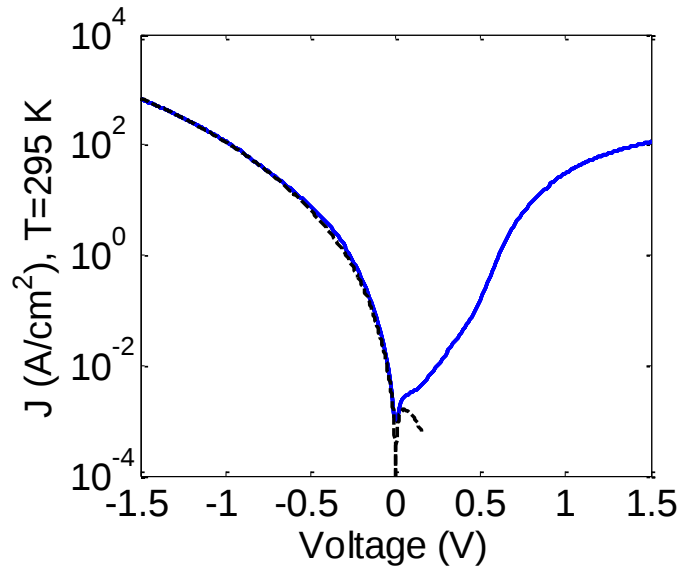
$$f_c = \frac{1}{1 + e^{(E-E_{fn})/k_b T}}$$

$$f_v = \frac{1}{1 + e^{(E-E_{fp})/k_b T}}$$

$$T(V_{SD}) = e^{\frac{-\alpha}{(V_{bi}-V_{SD})^{1/2}}}$$

$$\begin{aligned} V_{bi} &= 0.91 \text{ V} \\ E_{go} &= 1.12 \text{ eV} \\ V_o &= 0.126 \text{ V} \\ J_0 &= 3.84 \times 10^7 \\ \alpha &= 0.843 \end{aligned}$$

I-V Fits Band Tail Model Well



Band Edge Tunneling Current

$$j_t \propto \int \partial E * T * (f_C - f_V) * D_{\text{BandEdge}}(E)$$

Band Edge
Density of States

Fixed by source-drain
bias in a transistor
and is a **CONSTANT**
with gate voltage

Varies with voltage in a diode
At small bias:

$$(f_C - f_V) \approx \left(\frac{1}{2} - \frac{E - F_C}{4K_B T} \right) - \left(\frac{1}{2} - \frac{E - F_V}{4K_B T} \right) = \frac{F_C - F_V}{4k_b T} = \frac{qV}{4k_b T}$$

At larger biases it becomes energy dependent, but

$$\int (f_C - f_V) dE = qV_{SD}$$

**Simply dividing the diode current by voltage will
approximately give the transistor response!**

Polycrystalline Silicon is Very Bad!

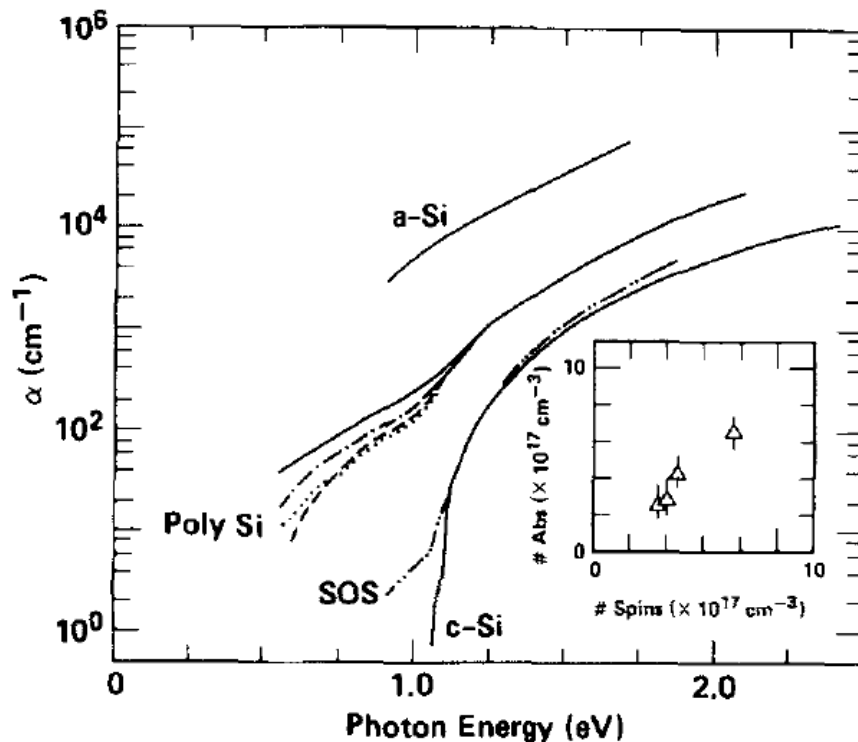


FIG. 1. Absorption vs photon energy for different intervals of atomic hydrogenation exposure. Evaporated amorphous silicon (*a*-Si) from Ref. 16. Fine grained polysilicon, unhydrogenated (solid), 60 min (dot-dash), 120 min (dash), 30 min (dotted), silicon-on-sapphire (SOS). Bulk crystalline silicon (*c*-Si) from Ref. 17. Inset shows the integrated density of optically absorbing defects with a cross section of $1.2 \times 10^{-16} \text{ cm}^{-2}$ (Ref. 8) vs the dangling bond spin density.

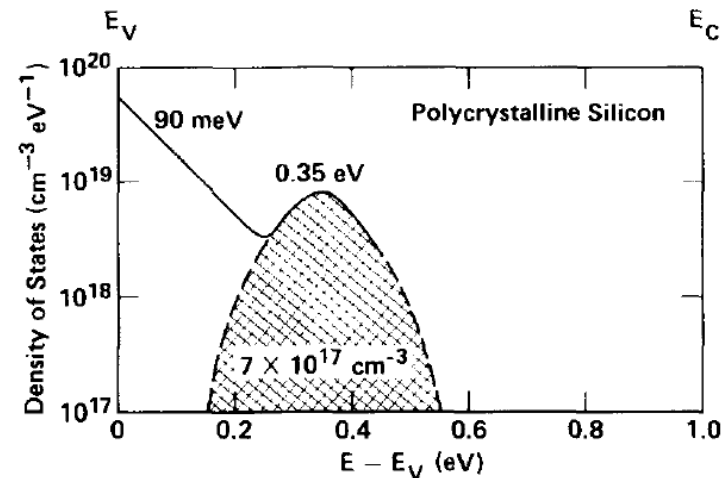
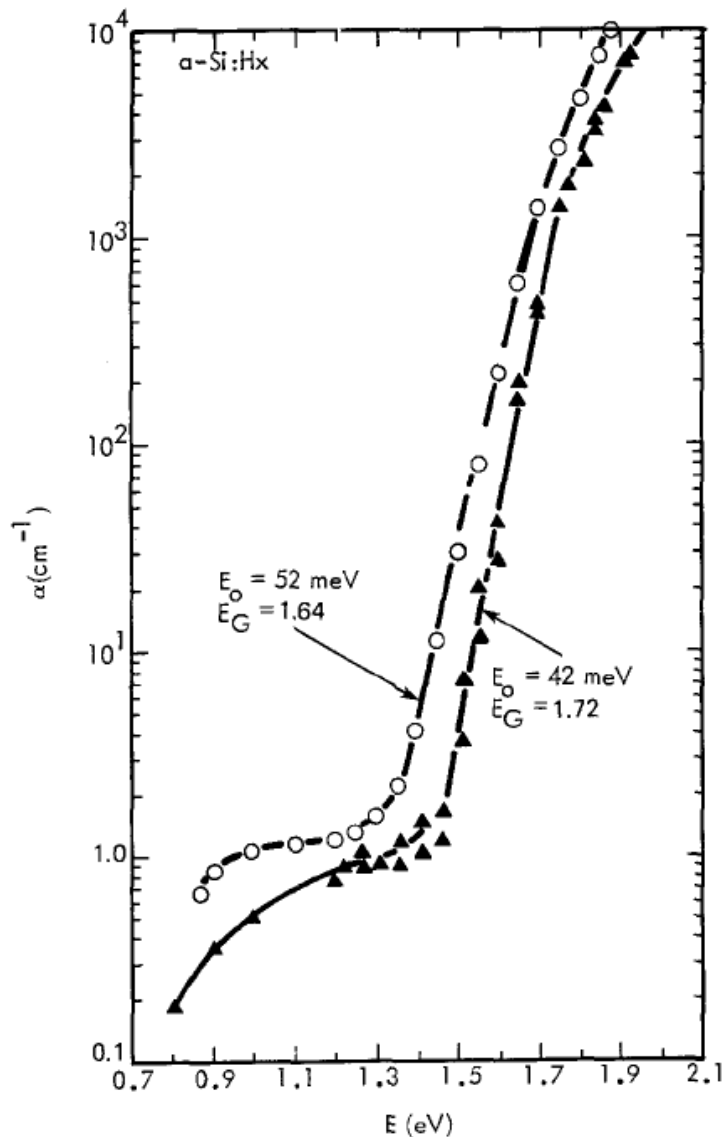


FIG. 3. Features of the grain boundary density of states derived from optical absorption and ESR measurements.

Jackson, Johnson and Biegelsen,
“Density of Gap States of Silicon Grain
boundaries Determined by Optical
Absorption,” 1982

Amorphous Silicon is Very Bad!

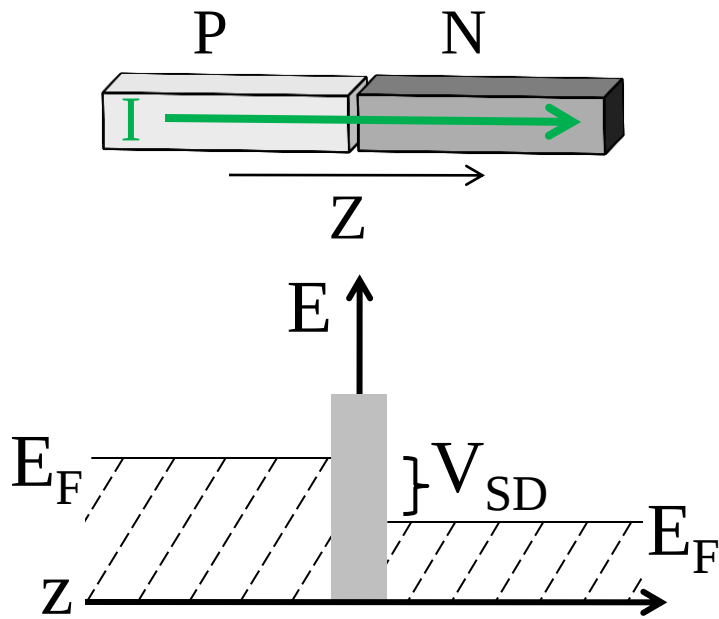


$$\alpha = \alpha_0 \exp[E - E_F/E_0(T, X)]$$

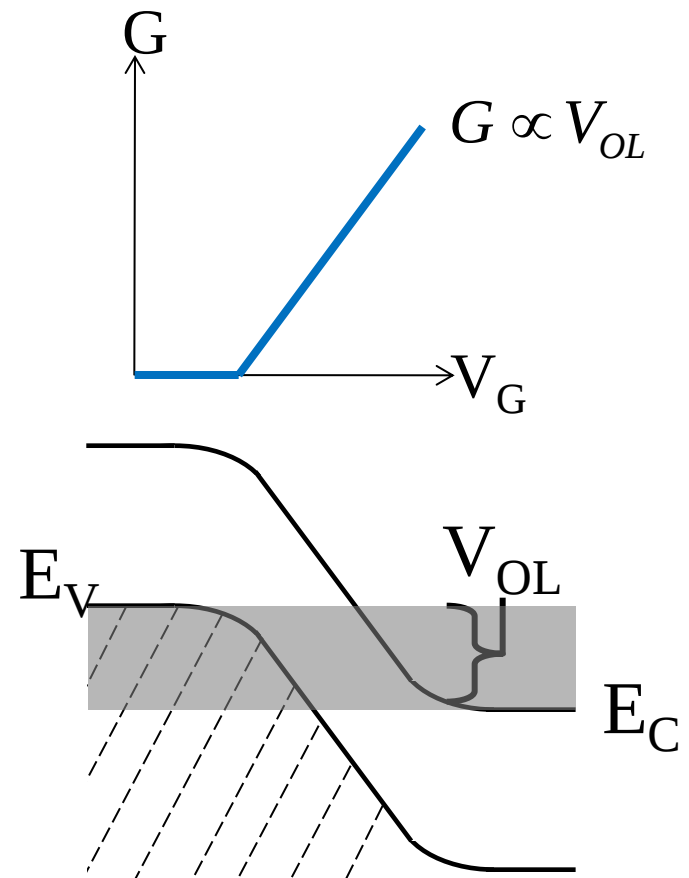
Fig. 1. Absorption edge of two films of amorphous silicon hydride (a-Si:H). The film with the higher Tauc gap was grown at a substrate temperature of 250°C compared with 200°C for the lower gap film. It has a hydrogen content of 14 at.% compared with 9 at.% for the lower gap film (adapted from ref. [2]).

Cody, "Urbach Edge of crystalline and amorphous silicon: a personal review" (1992)

1d-1d Point Overlap



$$I_{1d-1d, \text{Point}} = \frac{2e^2}{h} \times V_{OL} \times T$$



Consider a Very Small V_{SD}

- We are interested in the case where all voltages $< kT$
- All states are roughly half occupied,
and current flows both ways according
to the difference in occupation probability:

$$f_c = \frac{1}{e^{(E - E_{Fc})/kT} + 1}$$

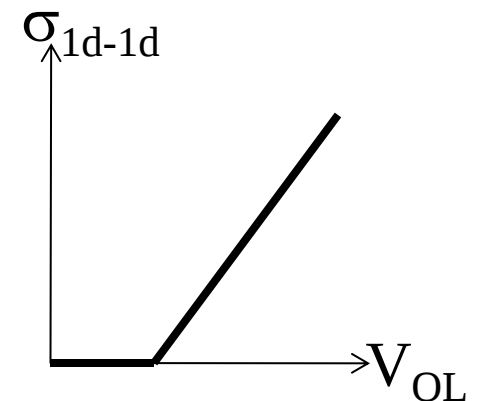
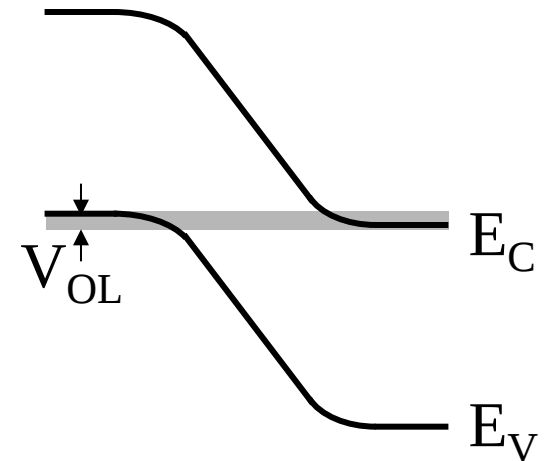
$$f_c - f_v \approx \frac{(E_{Fc} - E_{Fv})}{4kT} \approx \frac{qV_{SD}}{4kT}$$

- Take the cold current and multiply by $qV_{SD}/4kT$

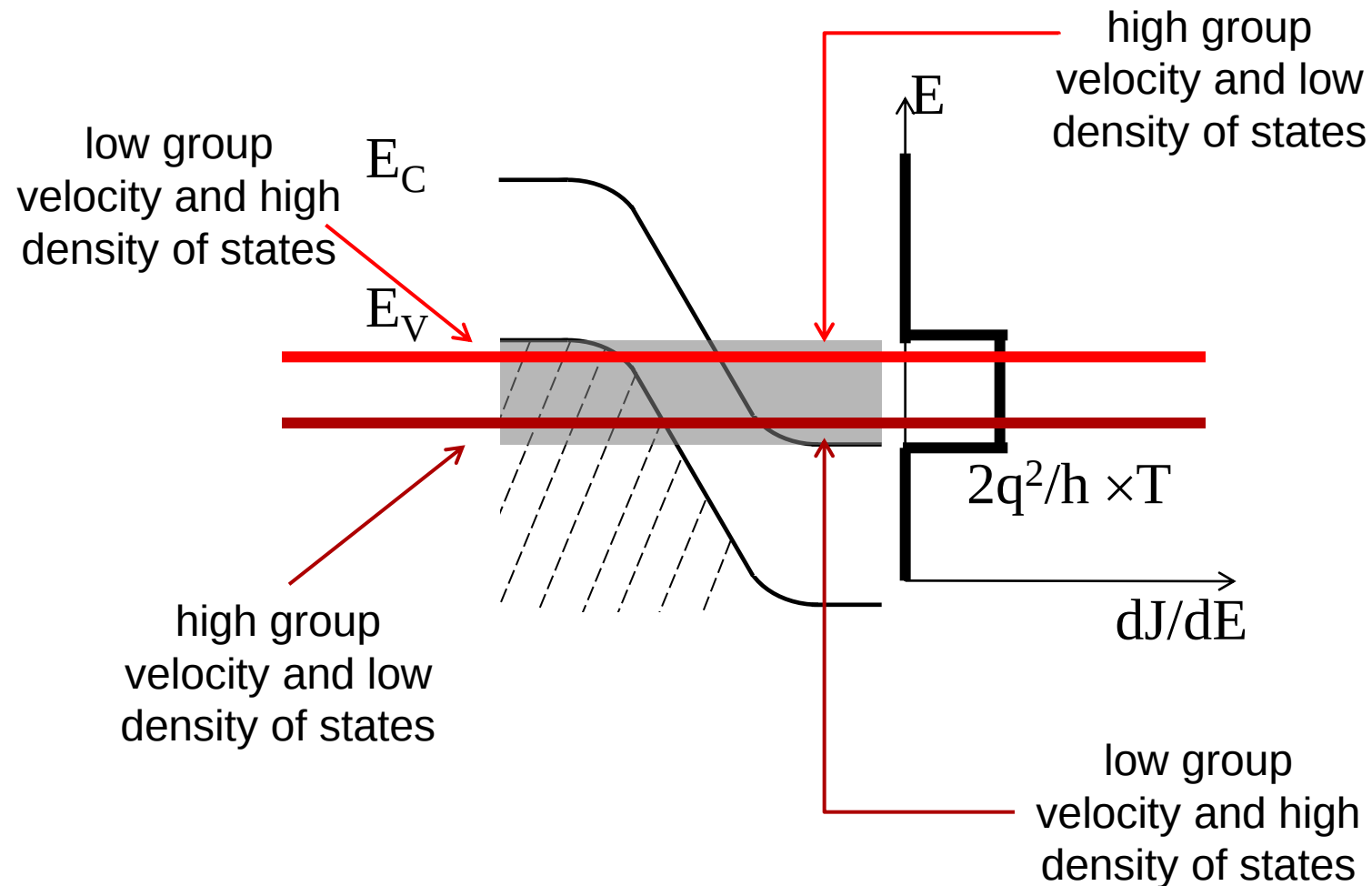
$$I_{1d-1d,Point} \times \frac{qV_{SD}}{kT} = \frac{2q^2}{h} \times V_{OL} \times \frac{qV_{SD}}{4kT}$$

- Therefore conductance of the diode is:

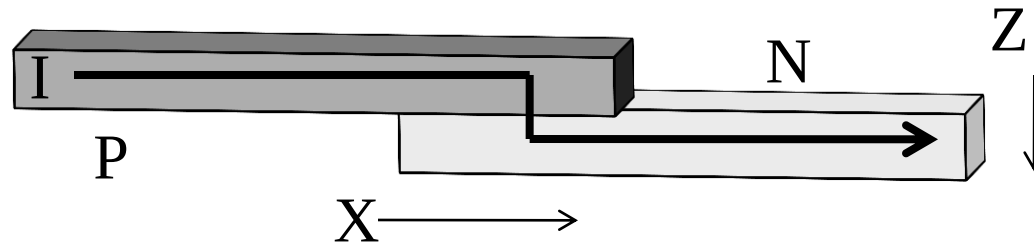
$$\sigma_{1d-1d,Point} = \frac{2q^2}{h} \times V_{OL} \times \frac{q}{4kT}$$



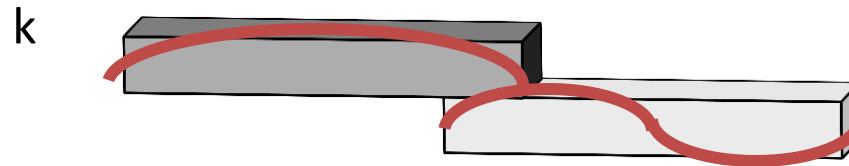
Why is it Still a Quantum of Conductance?



Turn on Broadening



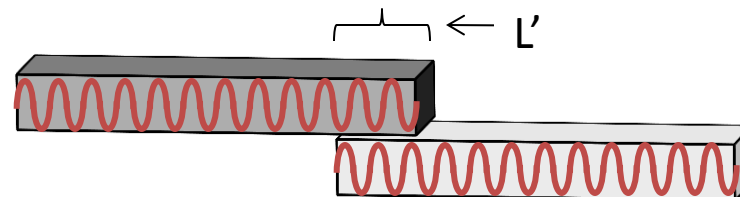
Transverse Momentum is NOT Conserved at Low



$$k_1 \neq k_2$$

overlap integral is
NOT zero

Transverse Momentum is Conserved at High k

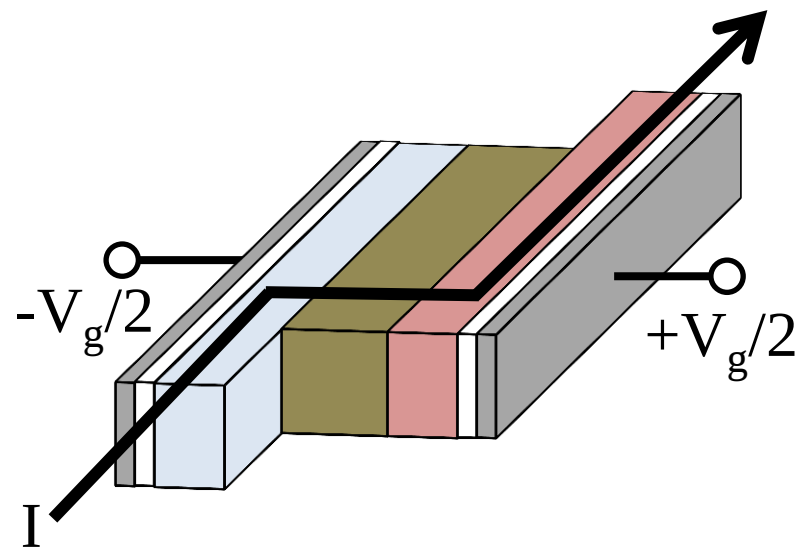
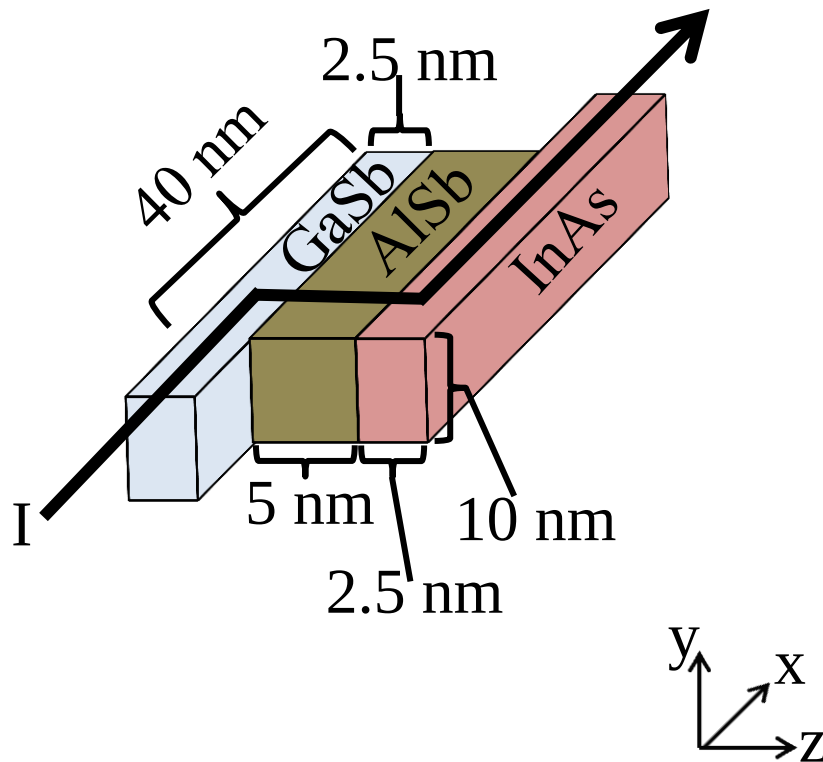


Transverse momentum conserved once $\lambda \sim L'$

Case	Picture	Current http://arxiv.org/abs/1109.0096	Conductance, G	Maximum G for pert. theory to be valid	Maximum G for end contacts $\gamma = (2/\pi)E_x$
1d-1d		$\frac{2q^2}{h} \times V_{OL} \times \mathcal{T}_{device}$	$\frac{2q^2}{h} \times V_{OL} \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	N/A	N/A
3d-3d		$\frac{Am^*}{4\pi\hbar^2} \times \frac{qV_{OL}}{2} \times \frac{2q^2}{h} V_{OL} \times \mathcal{T}_{device}$	$\frac{Am^*}{4\pi\hbar^2} \times \frac{qV_{OL}}{2} \times \frac{2q^2}{h} V_{OL} \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	N/A	N/A
2d-2d _{edge}		$\frac{2L_x \sqrt{qm^*V_{OL}}}{3\pi\hbar} \times \frac{2q^2}{h} \times V_{OL} \times \mathcal{T}_{device}$	$\frac{2L_x \sqrt{qm^*V_{OL}}}{3\pi\hbar} \times \frac{2q^2}{h} \times V_{OL} \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	N/A	N/A
0d-1d		$\frac{2q}{h} \times E_Z \times \mathcal{T}_{device}$	$\frac{2q}{h} \times E_Z \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	N/A	N/A
2d-3d		$\frac{Am}{2\pi\hbar^2} \times \frac{qV_{OL}}{2} \times \frac{4q}{h} \times E_Z \times \mathcal{T}_{device}$	$\frac{Am}{2\pi\hbar^2} \times \frac{qV_{OL}}{2} \times \frac{4q}{h} \times E_Z \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	N/A	N/A
1d-2d		$\frac{L_x}{\pi\hbar} \times \sqrt{qm^*V_{OL}} \times \frac{4q}{h} \times E_Z \times \mathcal{T}_{device}$	$\frac{L_x}{\pi\hbar} \times \sqrt{qm^*V_{OL}} \times \frac{4q}{h} \times E_Z \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	N/A	N/A
0d-0d		$\frac{4q}{h} E_{Z,i} \times \frac{\mathcal{T}_{device}}{\mathcal{T}_{contact}}$	$\frac{4q}{h} E_{Z,i} \times \frac{\mathcal{T}_{device}}{\mathcal{T}_{contact}} \times \frac{q}{4k_b T}$	$\frac{2q^2}{h} \times \pi^2 \times \frac{\gamma}{k_b T}$	$\frac{2q^2}{h} \times \pi^2 \times \frac{\gamma}{k_b T}$
2d-2d _{face}		$\frac{qmA}{\pi^2\hbar^3} \times E_{Z,i} \times E_{Z,f} \times \mathcal{T}_{device}$	$\frac{qmA}{\pi^2\hbar^3} \times E_{Z,i} \times E_{Z,f} \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	$\frac{2q^2}{h} \times \frac{\pi^3}{2} \times \gamma^2 \times \frac{1}{4k_b T} \times \frac{2mA}{\hbar^2\pi^2}$	$\frac{2q^2}{h} \times \frac{\pi^2}{4} \times \frac{W}{L_x} \times \frac{\gamma}{k_b T}$
1d-1d _{edge}		$2 \frac{qL_x}{\pi^2\hbar^2} E_{Z,i} \times E_{Z,f} \times \sqrt{\frac{m}{qV_{OL}}} \times \mathcal{T}_{device}$	$2 \frac{qL_x}{\pi^2\hbar^2} E_{Z,i} \times E_{Z,f} \times \sqrt{\frac{m}{qV_{OL}}} \times \mathcal{T}_{device} \times \frac{q}{4k_b T}$	$\frac{2q^2}{h} \times \sqrt{2}\pi^2 \times \gamma^{3/2} \times \frac{1}{4k_b T} \times \sqrt{\frac{2mL_x^2}{\pi^2\hbar^2}}$	$\frac{2q^2}{h} \times \frac{2\pi^{3/2}}{4} \times \frac{\gamma}{k_b T}$

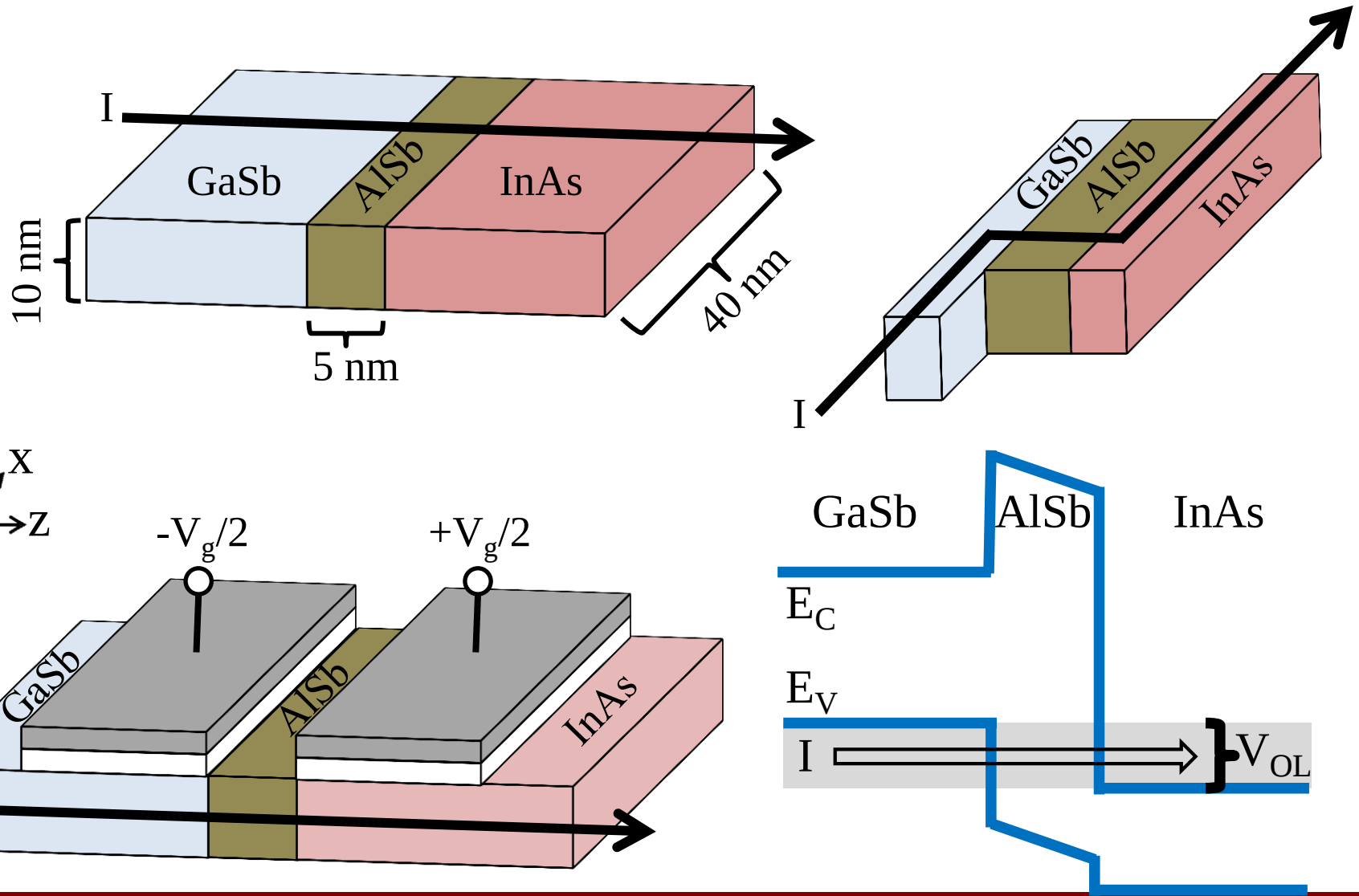
Use NEGF to Model a 1d-1d Edge Overlapped Junction

- Define a 1d-1d_{edge} Geometry
 - Let contacts extend to infinity

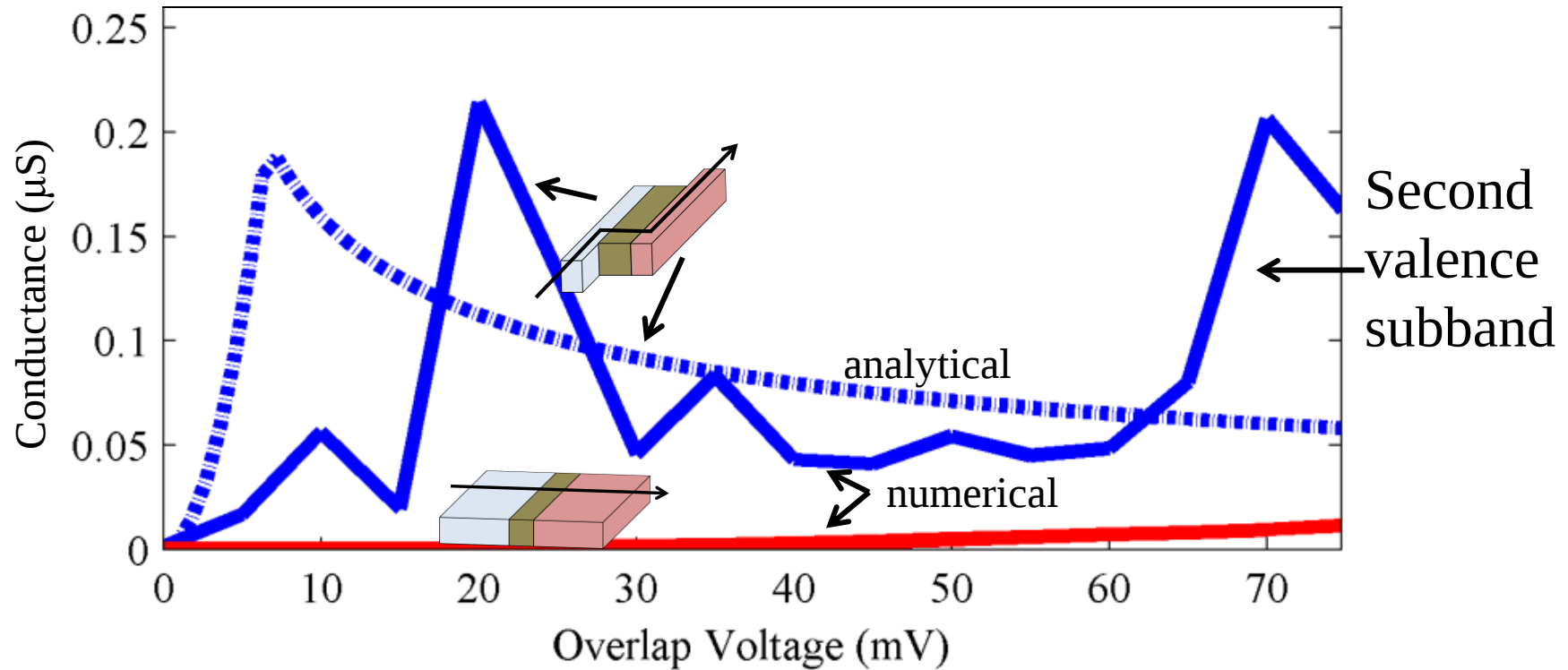


Use an 8 band k.p based
basis for the NEGF Modeling

Compare to an Unconfined 2d-2d edge

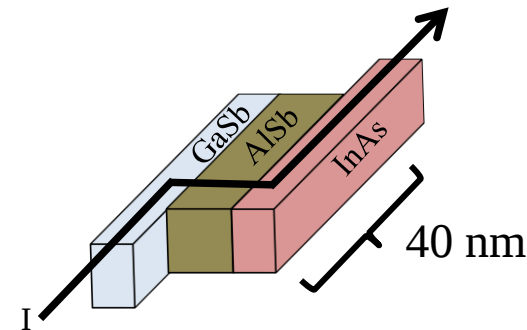
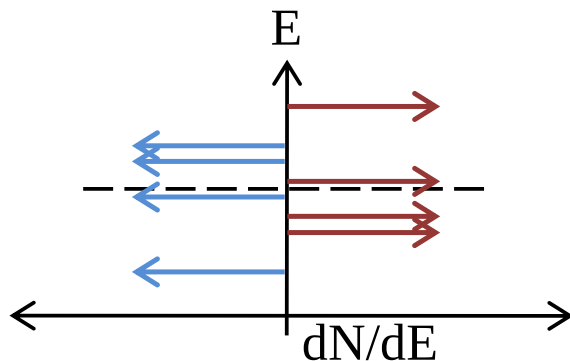
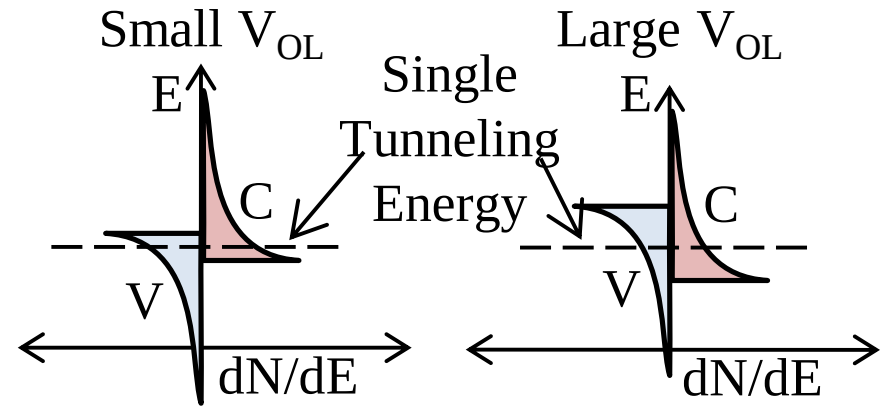
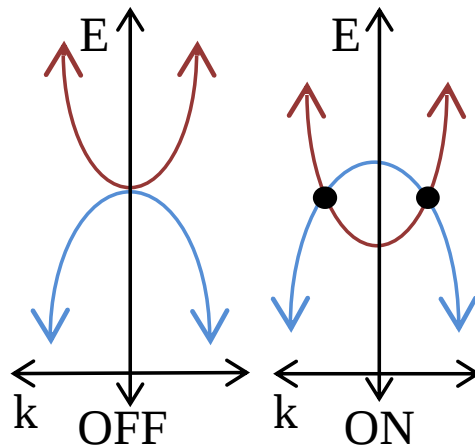


Compare the Structures



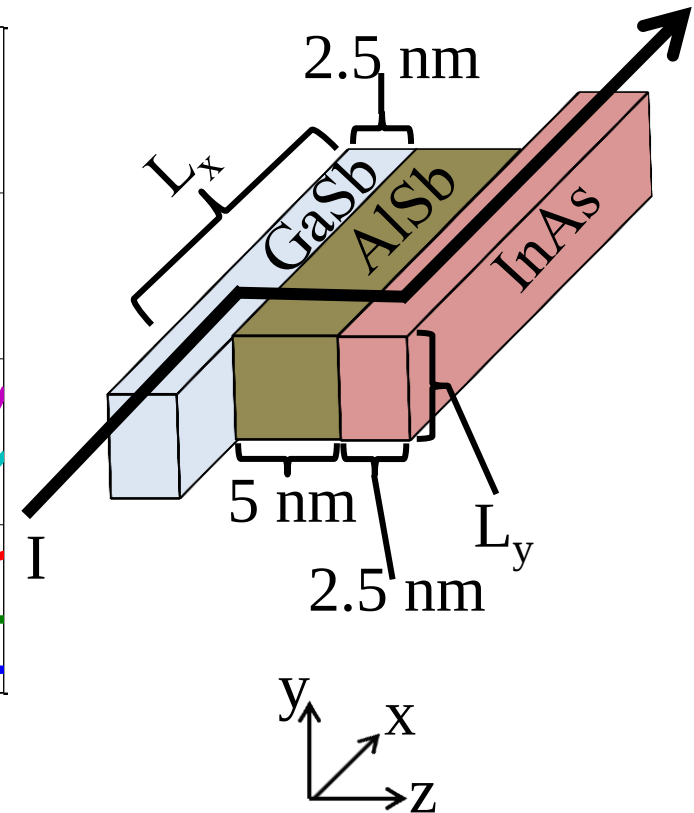
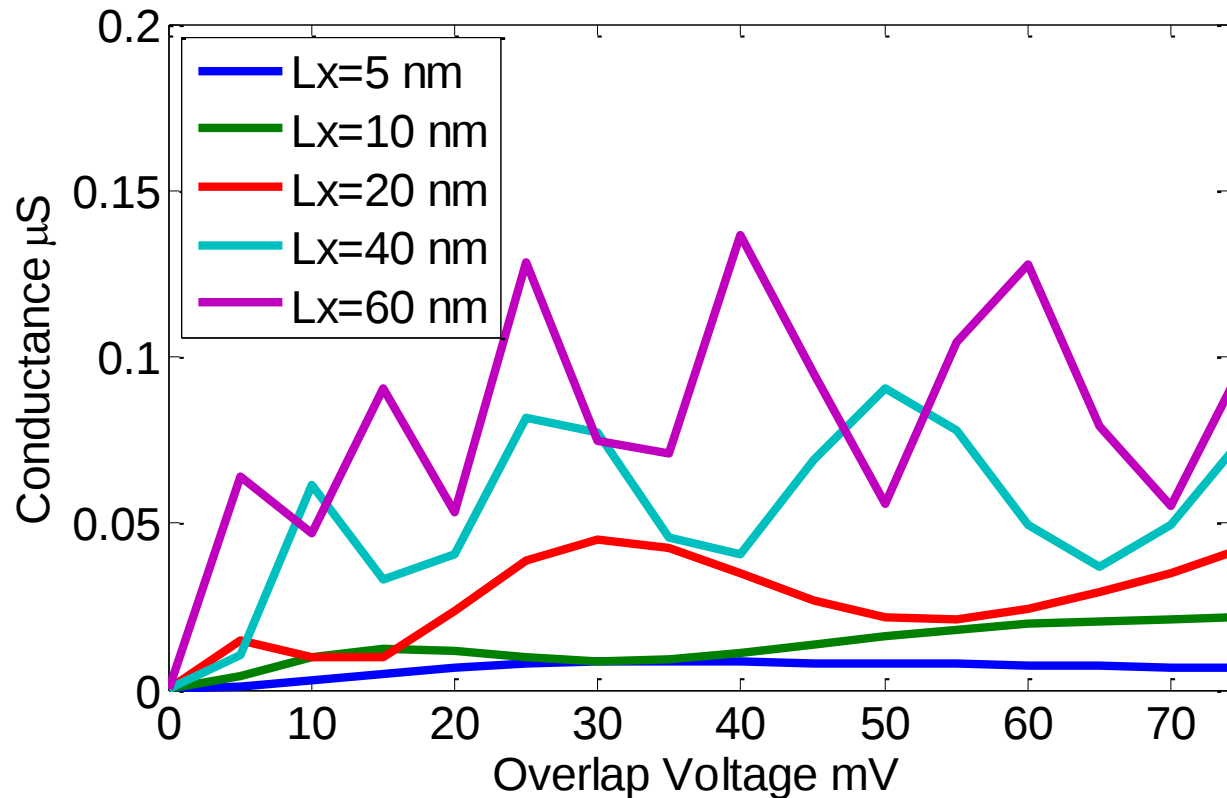
$G_{1\text{d-1d, edge}}$ is 10 times larger than $G_{2\text{d-2d, edge}}$!

What is the Difference Between the Analytic Model and Simulation?



Need to account for discrete transverse states

What Happens When the Overlap is Increased?



Assumed $k_y = 0$

Define a Hamiltonian for the System

- Start with an 8 band k.p Hamiltonian

$$H = \begin{bmatrix} H_{\text{int}} & 0 \\ 0 & H_{\text{int}} \end{bmatrix} + H_{\text{S.O.}} \quad H_{\text{int}} = \begin{bmatrix} E_C + \frac{\hbar^2 k^2}{2m_o} & +iP_o k_x & +iP_o k_y & +iP_o k_z \\ -iP_o k_x & E_V + \hbar^2 k^2 / 2m_o + M(k_y^2 + k_z^2) + L'k_x^2 & N'k_x k_y & N'k_x k_z \\ -iP_o k_y & N'k_x k_y & E_V + \hbar^2 k^2 / 2m_o + M(k_x^2 + k_z^2) + L'k_y^2 & N'k_y k_z \\ -iP_o k_z & N'k_x k_z & N'k_y k_z & E_V + \hbar^2 k^2 / 2m_o + M(k_x^2 + k_y^2) + L'k_z^2 \end{bmatrix}$$

- Convert k to a discrete spatial derivative

$$k_x x_n = -i \frac{\partial}{\partial x} x_n = \frac{-i}{2a} (x_{nx+1} - x_{nx-1})$$

- Write Hamiltonian for each grid point to get spatial variation

$$H_{\text{S.O.}} = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & -i & 0 & 0 & 0 & 0 & 1 \\ 0 & i & -1 & 0 & 0 & 0 & 0 & -i \\ 0 & 0 & 0 & -1 & 0 & -1 & i & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & -1 & i & 0 \\ 0 & 0 & 0 & -i & 0 & -i & -1 & 0 \\ 0 & 1 & i & 0 & 0 & 0 & 0 & -1 \end{bmatrix}$$

Principles Behind NEGF Calculation

Electron density is given by a sum of delta functions

$$D(E) = \sum_{\alpha} \delta(E - \varepsilon_{\alpha})$$

Write the delta function as a limit

$$\begin{aligned} 2\pi \times \delta(E - \varepsilon_{\alpha}) &= \frac{2\eta}{(E - \varepsilon_{\alpha})^2} \Big|_{\eta \rightarrow 0^+} \\ &= i \left[\frac{1}{E - \varepsilon_{\alpha} + i\eta} - \frac{1}{E - \varepsilon_{\alpha} - i\eta} \right]_{\eta \rightarrow 0^+} \end{aligned}$$

Converting this to a matrix gives the spectral density function, A

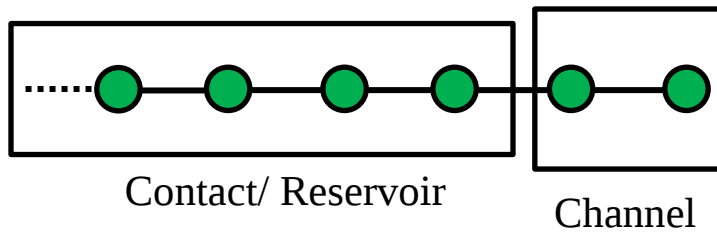
-Consider the eigenstates of H as the basis

$$A = i [G(E) - G^+(E)]$$

$$\text{where } G(E) = \frac{1}{E - \varepsilon_{\alpha} + i\eta}$$

Thus we have defined the Green's function as a convenient way to express a delta function

How to deal with an infinite contact?



Channel Hamiltonian (Size $d \times d$) ← Small

$$\bar{H} = \begin{bmatrix} H & \tau \\ \tau^\dagger & H_R \end{bmatrix}$$

← Coupling between channel and contact (Size $d \times R$)

← Contact Hamiltonian (Size $R \times R$) ← Huge!!

$$\bar{G} = [(E + i0^+)I - \bar{H}]^{-1} = \begin{bmatrix} (E + i0^+)I - H & -\tau \\ -\tau^\dagger & (E + i0^+)I - H_R \end{bmatrix}^{-1}$$

$$= \begin{bmatrix} A & B \\ C & D \end{bmatrix}^{-1} = \begin{bmatrix} G & G_{dR} \\ G_{Rd} & G_{RR} \end{bmatrix}^{-1}$$

← Only care about the electron density in the channel and thus G

$$G = (A - BD^{-1}C)^{-1}$$

$$= \left(\underbrace{(E + i0^+)I - H}_{\text{Invert the channel part}} - \underbrace{\Sigma}_{\text{Subtract out the effect of the contact/reservoir}} \right)^{-1}$$

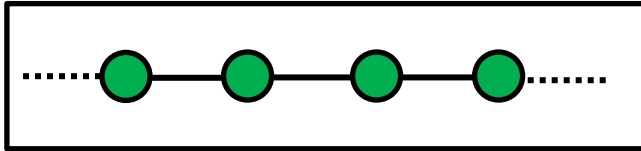
where $\Sigma = \tau G_R \tau^\dagger$, $G_R = [(E + i0^+)I - H_R]^{-1}$

Invert the
channel part

Subtract out the effect of
the contact/reservoir

If we know the self energy, Σ ,
finding G is easy

Trick to finding Σ



Contact/
Reservoir

In the contact adjacent atoms are identical and have the same electron density

$$G = \left[(E + i0^+)I - H - \Sigma \right]^{-1}$$



$$\Sigma = \tau G_R \tau^+$$

$$G_R = \left[(E + i0^+)I - H_R \right]^{-1}$$

$$G = G_R$$

Solve the equation self consistently for G

How to Find Current

Weight the electron density from the left contact by f_1
and the electron density from the right contact by f_2

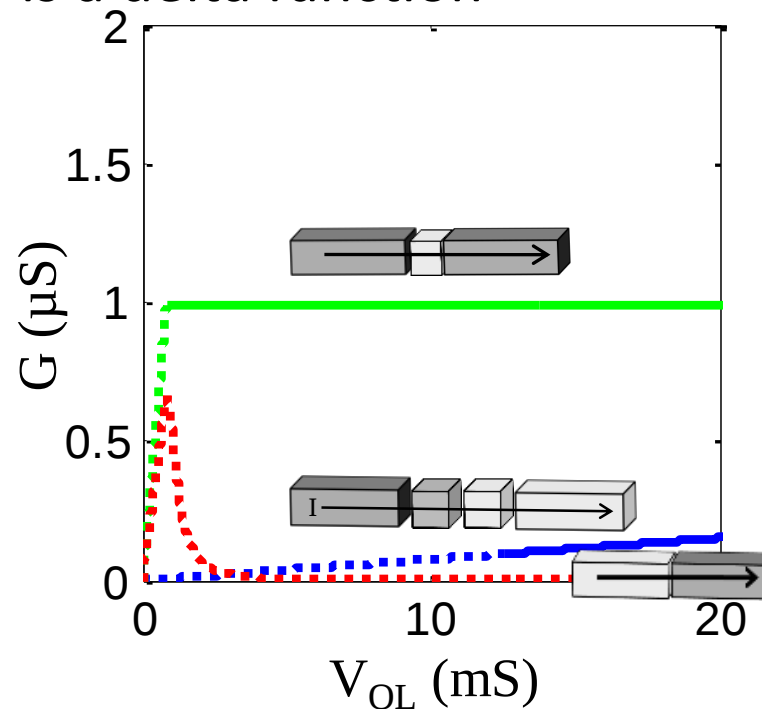
$$\text{Evaluate } I = \frac{d}{dt} \psi^+ \psi$$
$$\text{using } i\hbar \frac{d\{\psi\}}{dt} = [H]\{\psi\}$$

What do We Know So Far

- Need a steep density of states to get a steep subthreshold swing
 - Must eliminate doping: Use bilayer or double gate lateral FET
 - Vertical FET needs doping and so it will not work
- Lateral FET has a gate efficiency ~ 1
- Bilayer has a gate efficiency ~ 0.5
- Bilayer has a higher I_{ON} and lower overdrive voltage

Can we Improve the Lateral Structure?

- Increase T from $\sim 1\%$ to 50%
 - How?
 - Would reduce the required overdrive voltage and increase I_{ON}
- If we can't increase T , use quantum confinement in a lateral structure I-V is a delta function



Gate Controls Band Overlap

