

A Channelized Hotelling Observer for Treaty-Verification Tasks

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Outline

- Background on arms-control-treaty verification & project summary
- GEANT4 simulations to acquire data on inspection objects
- Applying mathematical observer models developed by medical imaging community to arms-control-treaty verification
 - Observer: human or mathematical model that makes decisions

Arms-Control-Treaty Verification

- Current treaties holds accountable number of delivery systems
 - New START treaty limits US to 1550 warheads on 700 delivery systems
- Future treaties may want to count warheads.
- Monitor wants to verify presence of warhead, host wants to preserve sensitive information on construction.
- Many current proposed methods utilize an information barrier (IB)
 - IB: hardware or software

Verification task

Is it really a warhead?



Photo from National Museum
of the USAF

Verification Task

Is it really a warhead?

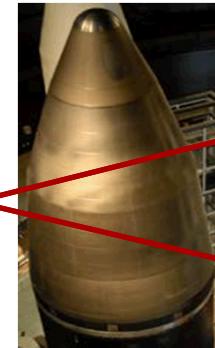


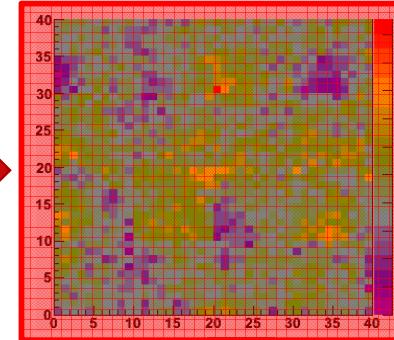
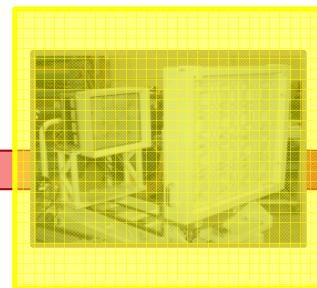
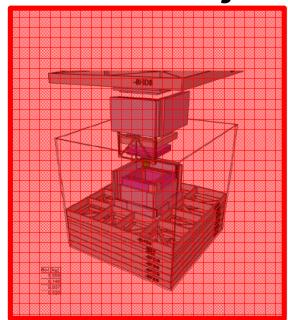
Photo from National Museum
of the USAF

Is it warhead A or warhead B?



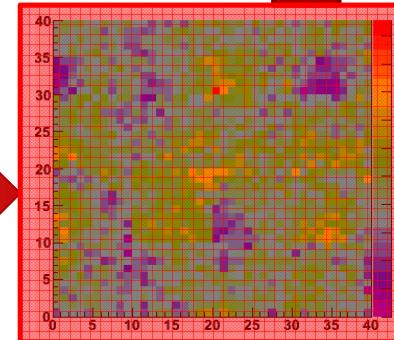
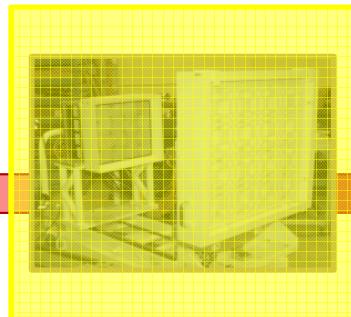
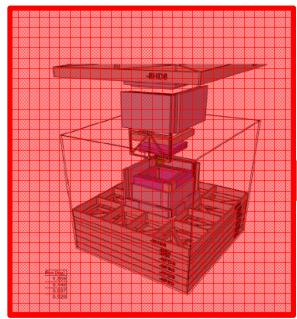
“Traditional” Template Matching

Trusted object



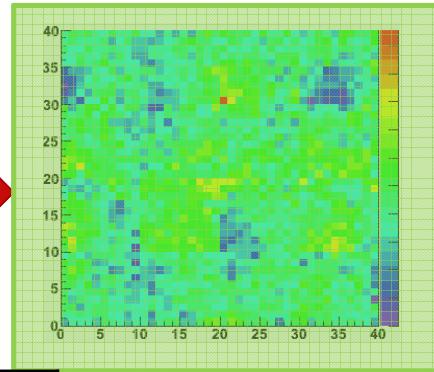
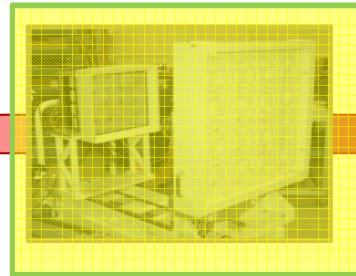
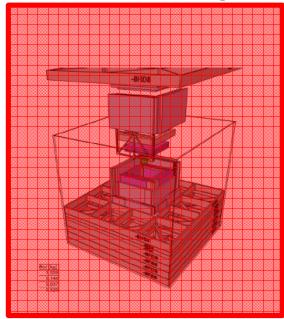
LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access

Tested object



Our proposal

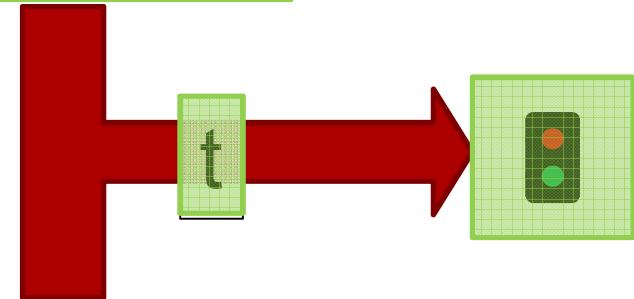
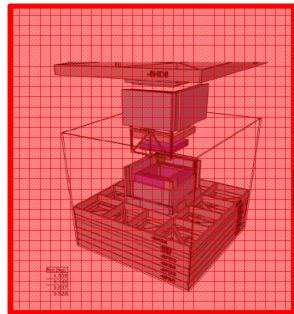
Trusted object



Hypothetical observer stores info sufficient for confirmation but not sensitive

LEGEND	
Red	No Access
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Tested object



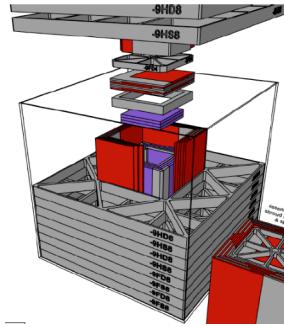
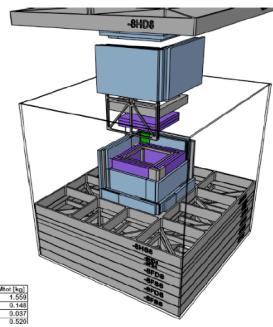
Testing data is processed event by event, only updating test statistic.

Data not aggregated

Think snapchat!

Task – Discriminate Idaho Inspection Objects

- Binary discrimination using spectral information.
 - Distinguish objects 8 (Pu surrounded by DU) and 9 (Pu surrounded by HEU) developed by Idaho National Laboratory.
 - Fast-neutron coded-aperture detector with liquid scintillator.

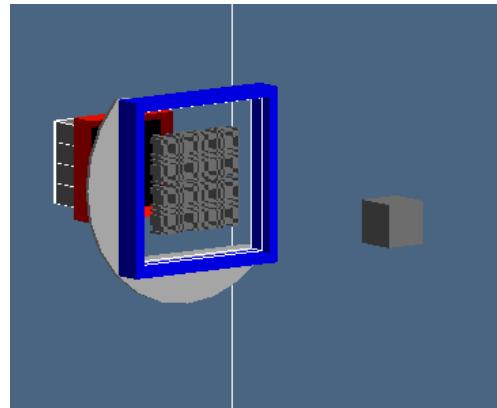


INL/EXT-11-20876

- Rotational variability included (simulated grid of orientations)

GEANT4 Simulations

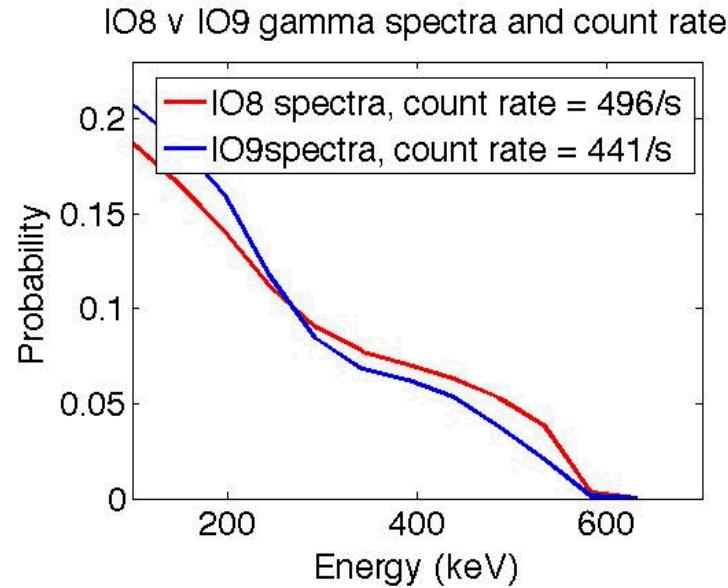
- Models built into transport application using GEANT4 toolkit to acquire testing and training data.



- Difficult to simulate gamma transport in plutonium objects with thick high-Z shielding.
 - Set gamma-energy threshold, applied linear energy bias
 - Used multithreaded capability of GEANT4.10
 - Ran on high-performance-computing clusters at SNL.

Simulation Data

- Similar geometries, no significant spatial difference in detector data.
- Observers make decisions based on gamma spectra differences
 - Data is summed over pixels



Definitions

- List-mode data A_n :
 - Estimated energy, pixel, and particle type (photon or neutron) for event n . Define N to be total number of detected events.
- Nuisance parameters :
 - Characteristics of the objects being imaged that affect the data but are of no interest
 - Examples include orientation, material age, construction, storage container characteristics.

Linear Template Observers

- Testing and training event data $\{A_n\}$ binned into data vector \mathbf{g} ($P \times 1$).

$$g_p = \sum_{n=1}^N f_p(A_n)$$

- \mathbf{g} is binned detector data – image, spectra or both.
- Linear template \mathbf{W} ($P \times 1$) acts on \mathbf{g}_{test} , result is thresholded to make a decision

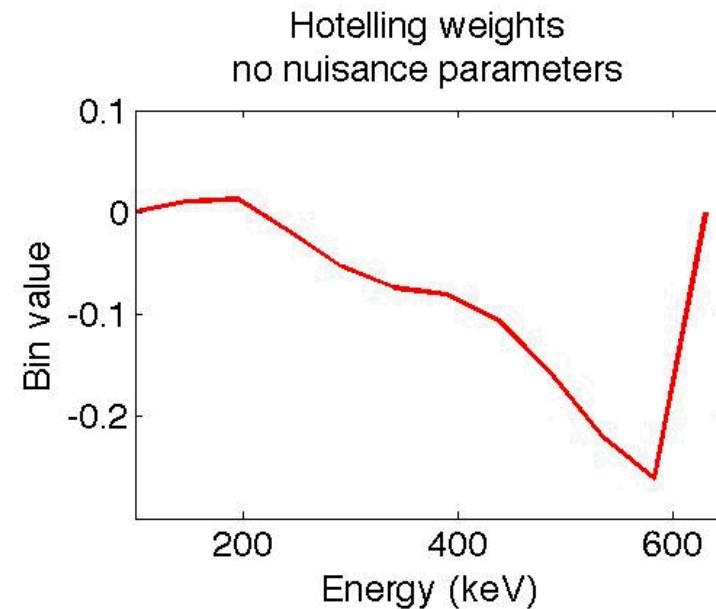
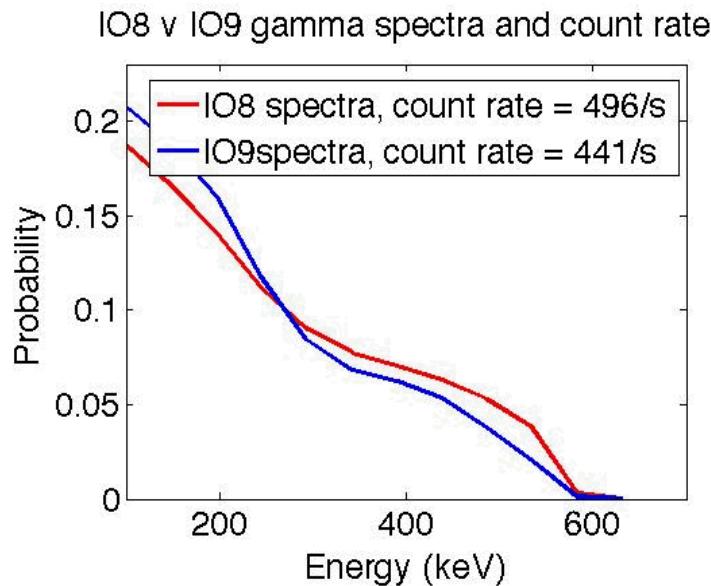
$$t = \mathbf{W}^\dagger \mathbf{g}_{test} \quad t \gtrless t_{\text{thresh}}$$

Hotelling Observer

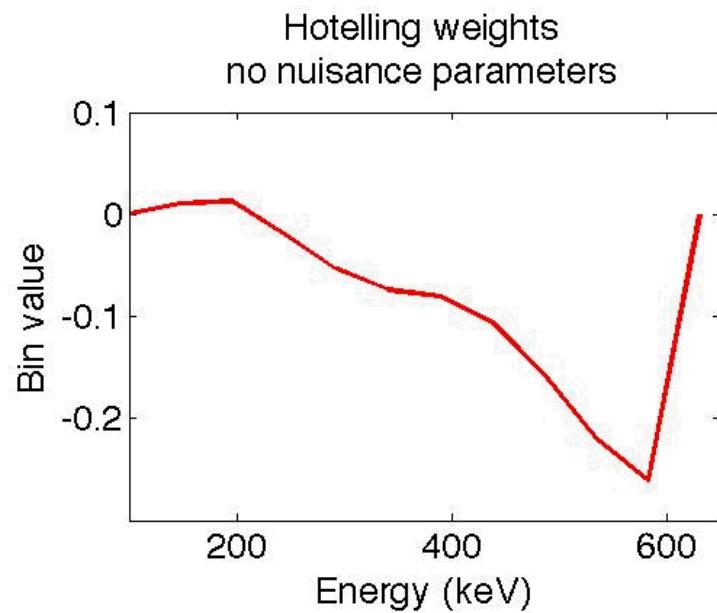
- Hotelling observer is **sensitive template W** defined as:

$$W = K_g^{-1} \overline{\Delta g}$$

- W is optimal template when data statistics are Gaussian.

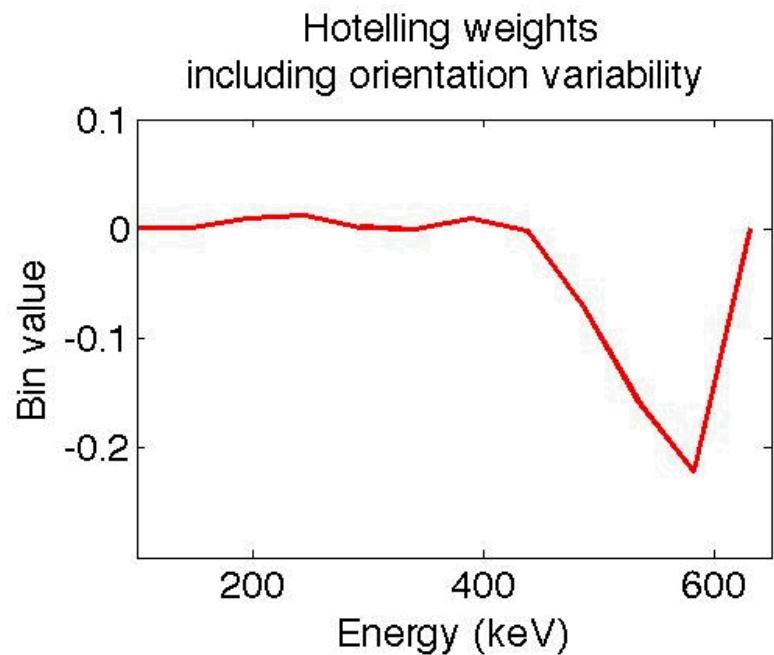


Hotelling Observer with Nuisance Parameters



Slight difference due to dense
 \mathbf{K} matrix

Relates directly to spectra



+/- of Hotelling Observer

Positives

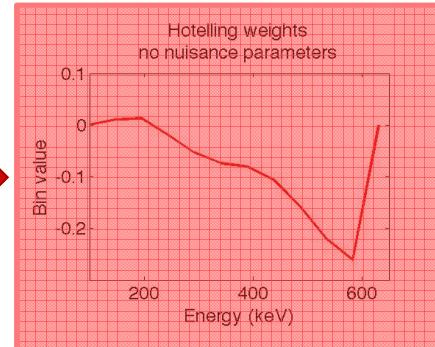
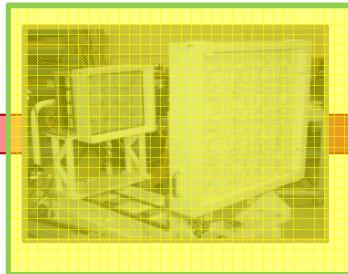
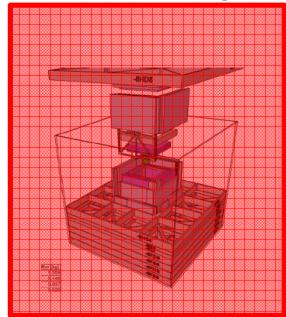
- Only storage is Hotelling template W – not image data g .
- Average over nuisance parameters smears out data.
- Analogous to secondary imaging system that filters out information other than the differences between objects.
 - Impossible to reconstruct g , only W .

Negatives

- Template contains product of first and second order statistics, but still (likely) constitutes sensitive information

Hotelling Observer in Practice

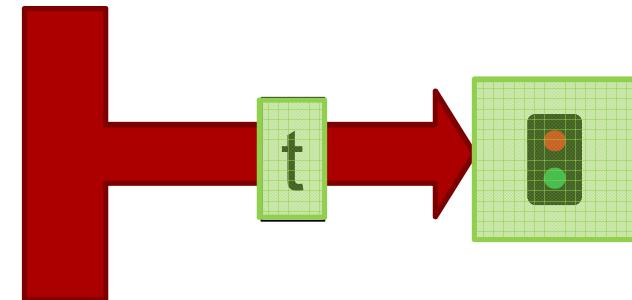
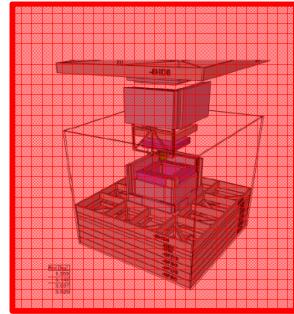
Trusted object



Hotelling template probably sensitive, but can't reconstruct object from t

LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access

Tested object



Testing data is processed event by event, only updating test statistic.

Channelized Hotelling Observer (CHO)

- Can we channelize data into non-sensitive channel values that monitor can work with?
- Channelize data vector \mathbf{g} ($P \times 1$) with channelizing matrix \mathbf{T} ($Q \times P$) into much smaller vector \mathbf{v} ($Q \times 1$).

$$\mathbf{v} = \mathbf{T}\mathbf{g}$$
$$Dim(\mathbf{v}) \ll Dim(\mathbf{g})$$

$$\mathbf{W}_v \mathbf{v}_{test} \leq t_{thresh}$$

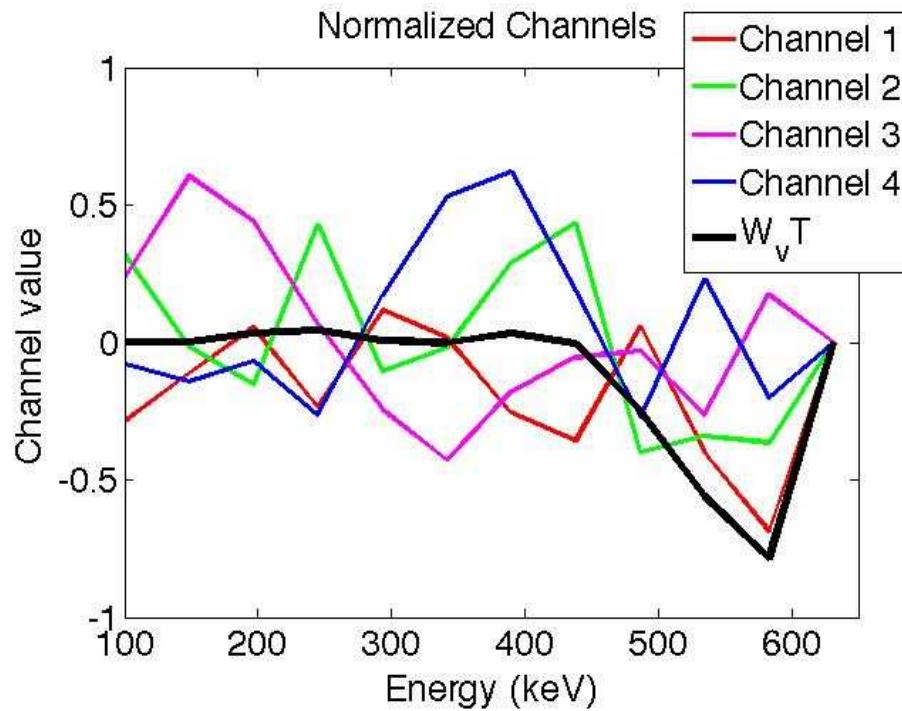
Optimizing \mathbf{T}

- \mathbf{T} can be optimized to maximize SNR^2 of test statistic distributions for best performance.
 - Gradient descent with backtrack

$$\begin{aligned}f_{obj}(\mathbf{T}) &= SNR^2(\mathbf{T}) \\&= \overline{\Delta \mathbf{v}(\mathbf{T})}^\dagger \mathbf{K}_\mathbf{v}(\mathbf{T})^{-1} \overline{\Delta \mathbf{v}(\mathbf{T})}\end{aligned}$$

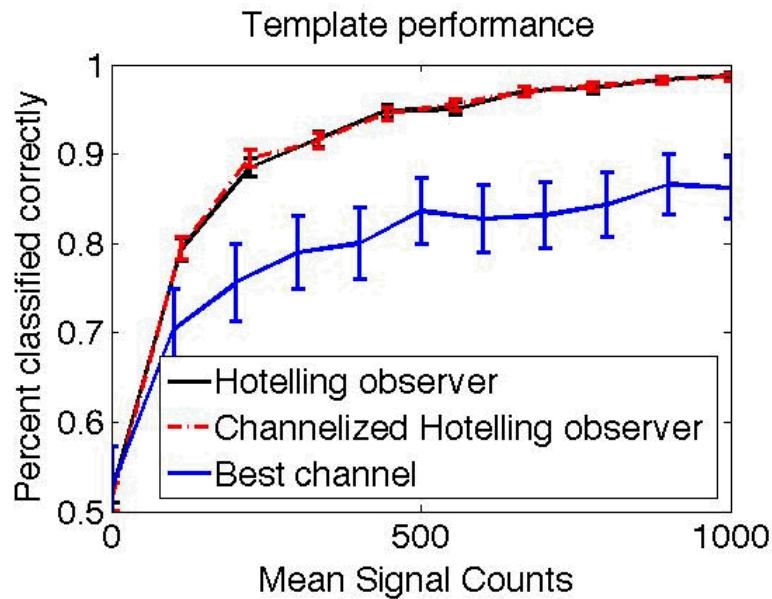
Example Channelization

- Standard optimization leads to fairly nonsensitive channels.
- Optimal performance requires sum of optimally weighted channels to equal **Hotelling weights**.



Performance of HO & CHO

- Task is to discriminate IO8 and IO9 when orientation is unknown



- However, best channel in other tasks has equal performance to CHO

Positives

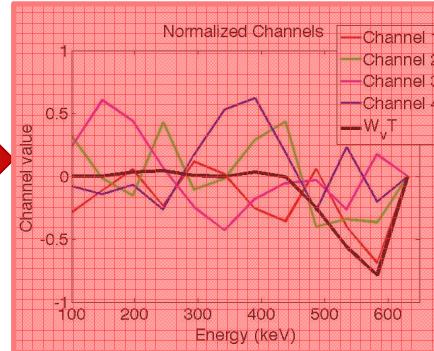
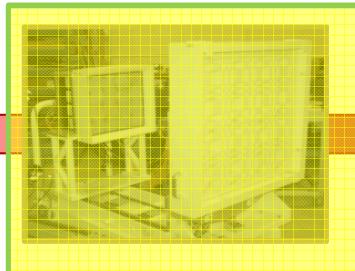
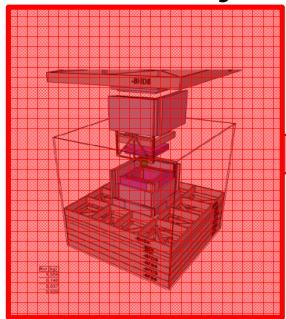
- Q non-sensitive channel values that monitor can use to make decisions
 - More channels = improved ability to verify tested sources is one of two in discrimination task, and not a spoof
- Optimizing SNR^2 results in optimal performance
 - Impossible to reconstruct *image*, only ***Hotelling weights (difference in images)***.

Negatives

- Optimally weighted sum is sensitive information
- ***Channelizing matrix itself*** often sensitive, cannot be shared.

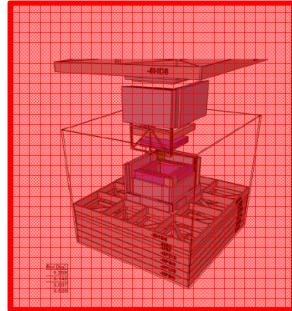
CHO in practice

Trusted object

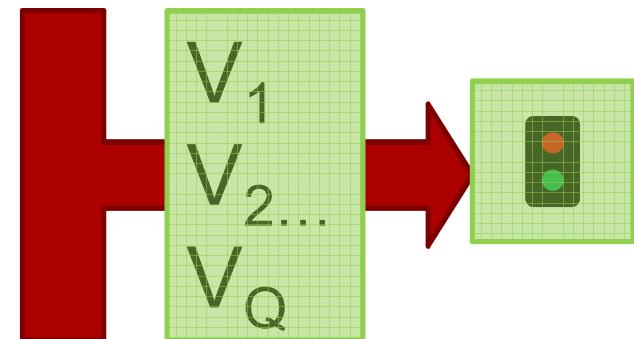


Channels
may/may not be
sensitive, but
 W_v^T is

Tested object



LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access



Testing data is processed event
by event, updating Q
channelized values

Current/Future work

- Build off channelized Hotelling observer groundwork
- Create nonsensitive channels by penalizing channel performance

$$f_{obj} = SNR_{Qchannels}^2 - \eta \sum_{q=1}^Q SNR_{channel \ q}^2$$

- Add noise to channels to reduce sensitive storage and performance.
- If host defines sensitive parameters in geometry construction, we can penalize the ability to discriminate between slight differences in the object

Summary

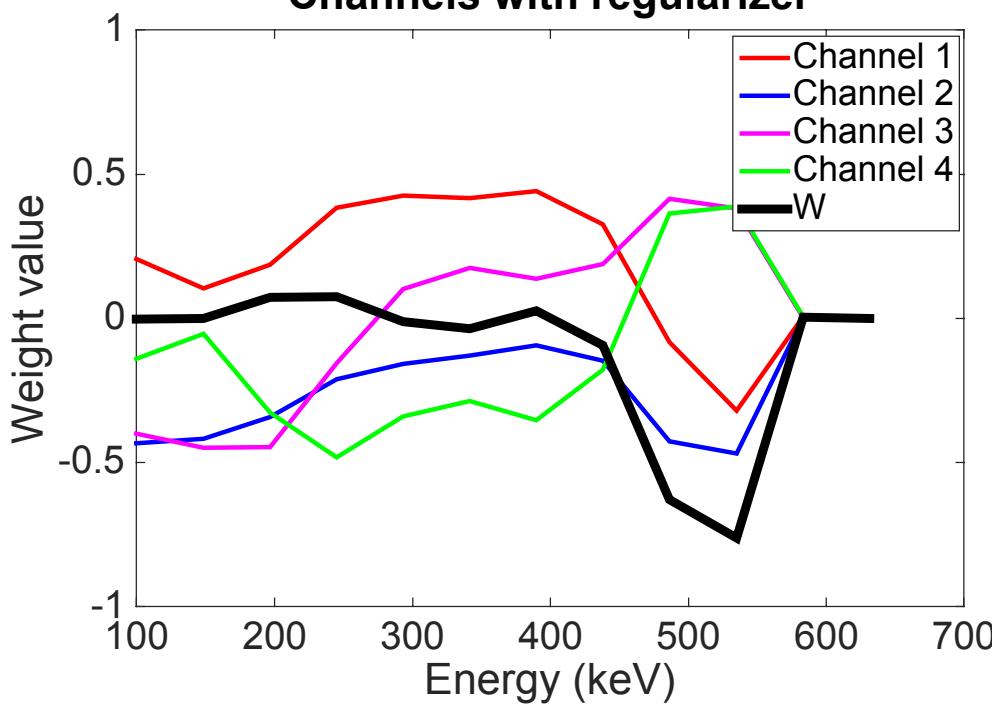
- Applying methods developed by medical imaging community to arms-control-treaty verification tasks
- Modeled inspection objects in transport application using GEANT4 toolkit to simulate data
- Hotelling observer gives optimal results while only storing differences between objects
- Channelized Hotelling observer gives monitor access to more information
 - Adding terms to optimization routine offers paths to non-sensitive storage

Extra slides

CHO with penalty

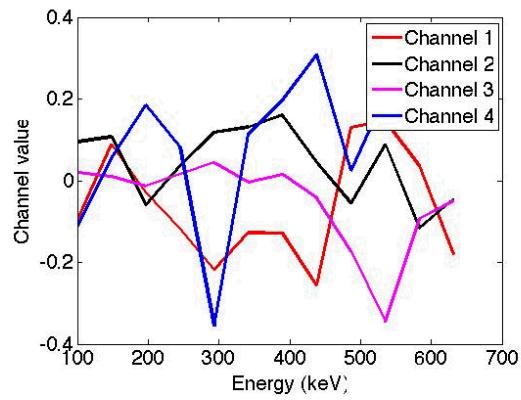
- Use penalty term in optimization to limit channel performance

$$f_{obj} = SNR_{Q\text{channels}}^2 - \eta \sum_{q=1}^Q SNR_{\text{channel } q}^2$$

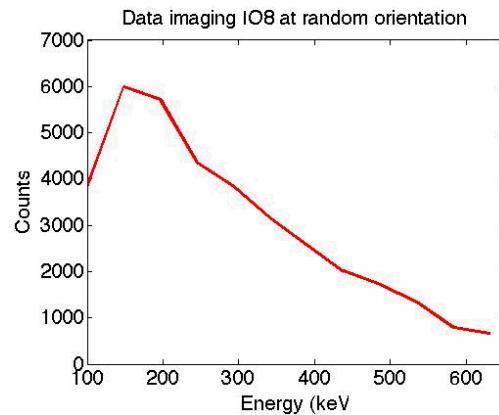


CHO inverse problem

T

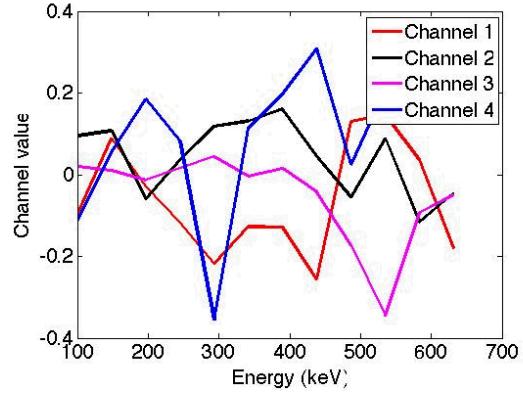


X g = V



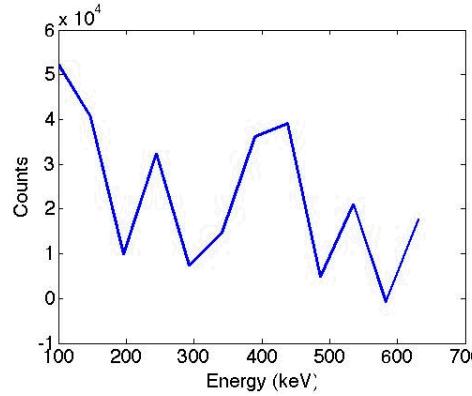
-365
-5589
223
-3030

T^{-1}



X V = g_{rec}

-365
-5589
223
-3030

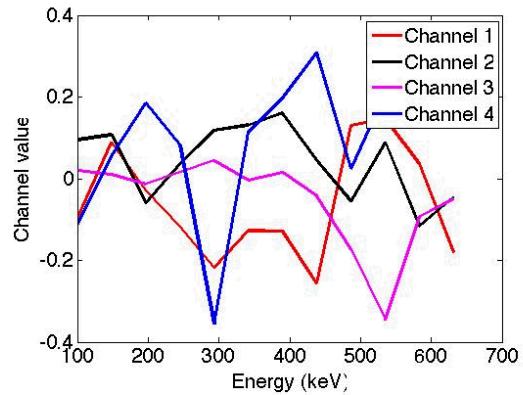


CHO inverse problem

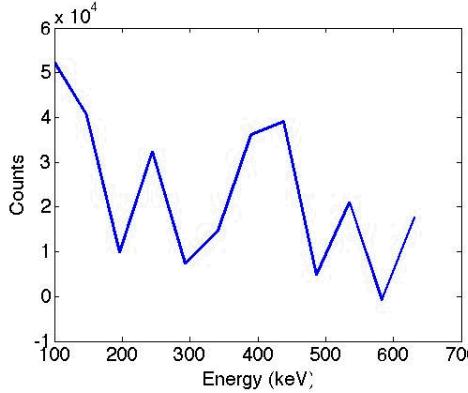
$$T \quad x \quad g \quad = \quad v$$

channel value

Channels, singular vectors, reconstruction are all very noisy,
But channel 3 looks like W

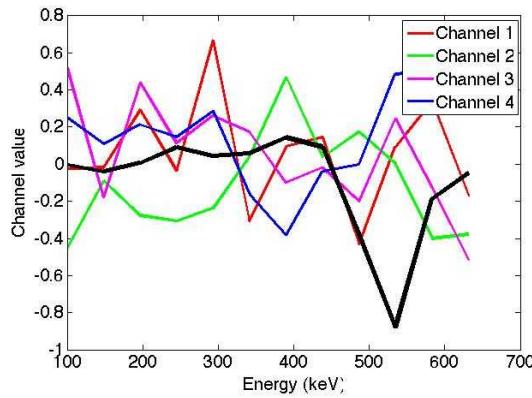


-365
-5589
223
-3030

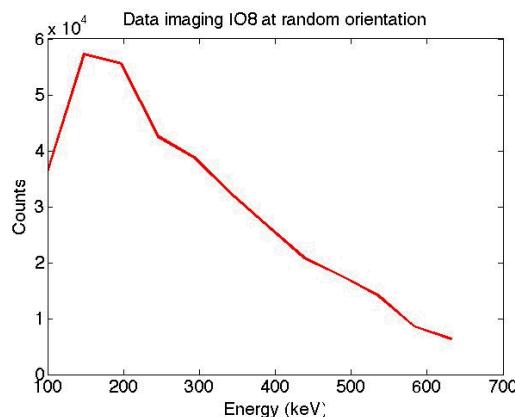


CHO inverse problem w/ perform. penalty

T



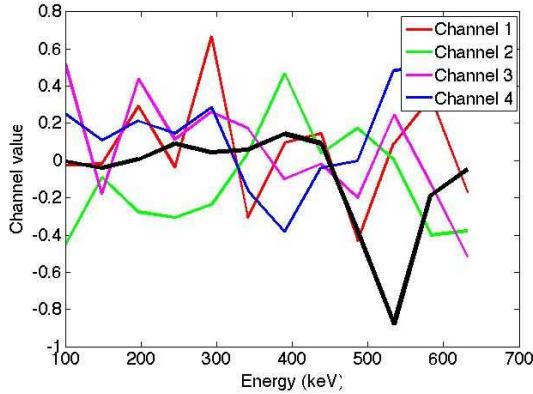
X g = V



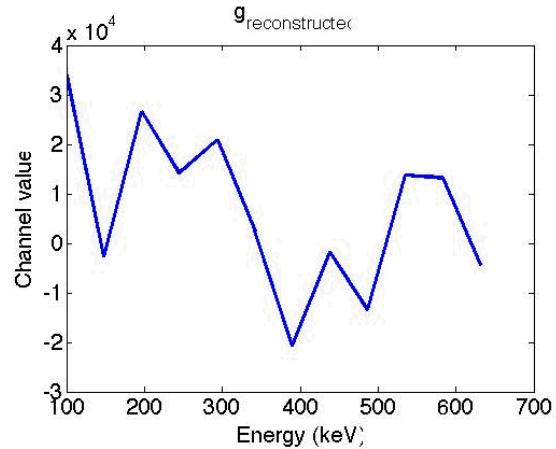
1.38e4
-2.25e4
2.26e4
2.19e4

T^{-1}

X V = g_{rec}

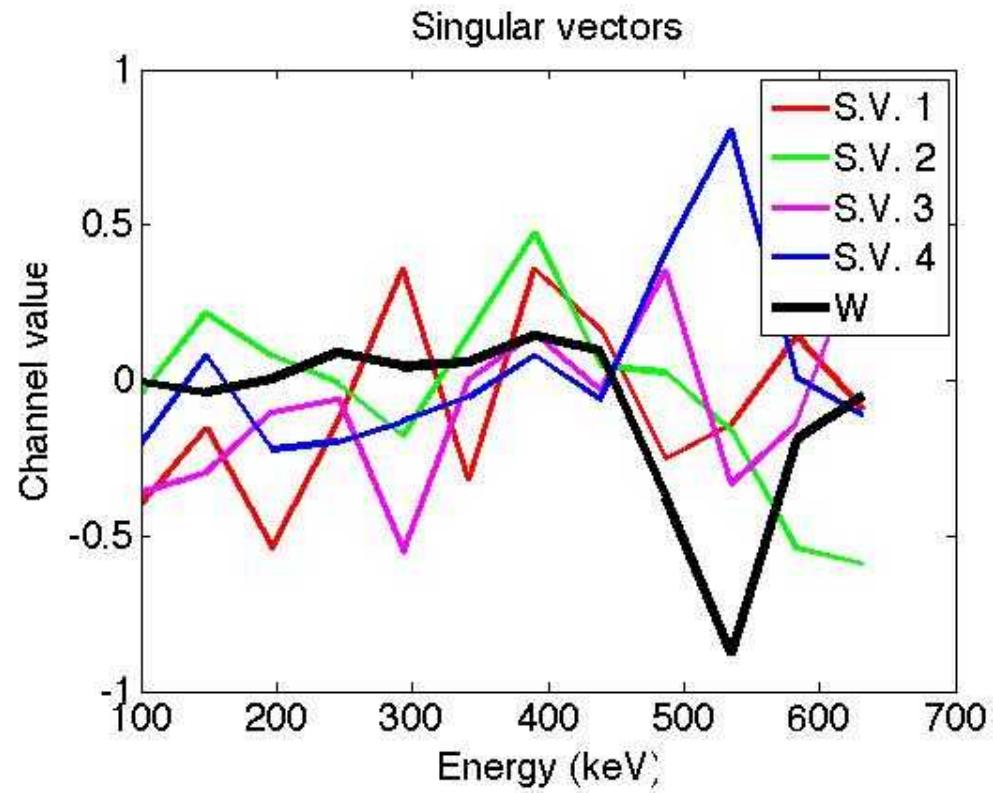


1.38e4
-2.25e4
2.26e4
2.19e4



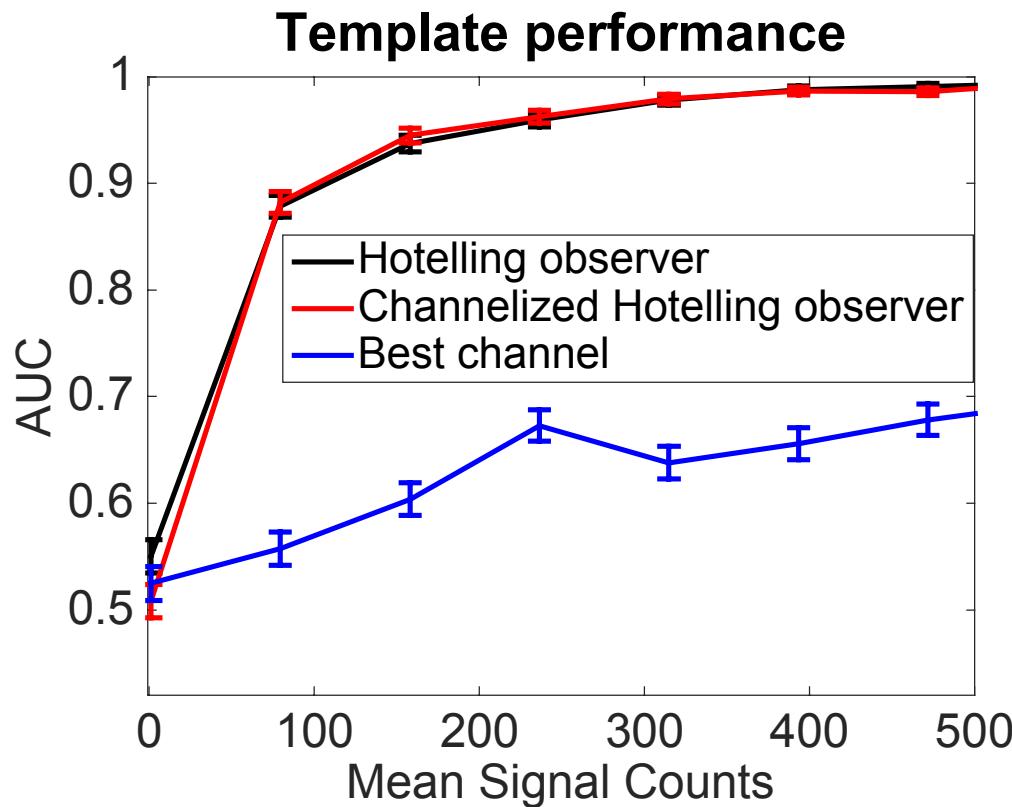
CHO inverse problem w/ perfom. penalty

- SVD of channelizing matrix: S.V. 4 looks like Hotelling weights



Channelized Hotelling penalty

- Hotelling and channelized Hotelling perform well
- Individual channels perform poorly



Future work – reducing sensitive info

- Example: Source A is a BeRP ball with 1" of poly shielding. The host country doesn't want the monitor to know what source A's poly thickness is down to a tolerance of Δt

$$f_{obj} = SNR_{(B-A)}^2 - \eta SNR_{(A_{(1''} + \Delta t) - A_{(1'')})}^2$$

- Will lead to drop in performance with benefit that host needn't worry.

Future work – reducing sensitive Info

$$f_{obj} = SNR_{(B-A)}^2 - \eta SNR_{(A_{(1'')} + \Delta t) - A_{(1'')}}^2$$

- A channelizing matrix that optimizes this objective function wouldn't be based on sensitive data
- Likewise, sensitive data could not be gained through the inverse problem

Future work – null hypothesis test

- Need an observer to address “Is this source A or not source A?”
- We developed a model based on likelihood expression, but it is spoofable.
- Standard tests based on distance metrics
- Is there a linear model similar to the Hotelling observer?