

A Channelized Hotelling Observer for Treaty-Verification Tasks

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Outline

- Background on arms-control-treaty verification & project summary
- GEANT4 simulations to acquire data on inspection objects
- Applying mathematical observer models developed by medical imaging community to arms-control-treaty verification
 - Observer: human or mathematical model that makes decisions

Arms-Control-Treaty Verification

- Current treaties holds accountable number of delivery systems
 - New START treaty limits US to 1550 warheads on 700 delivery systems
- Future treaties may want to count warheads.
- Monitor wants to verify presence of warhead, host wants to preserve sensitive information on construction.
- Many current proposed methods utilize an information barrier (IB)
 - IB: hardware or software

Verification task

Is it really a warhead?



Photo from National Museum
of the USAF

Verification Task

Is it really a warhead?

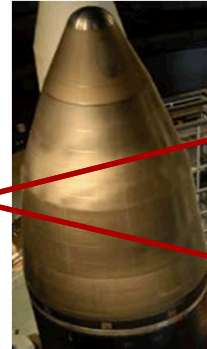


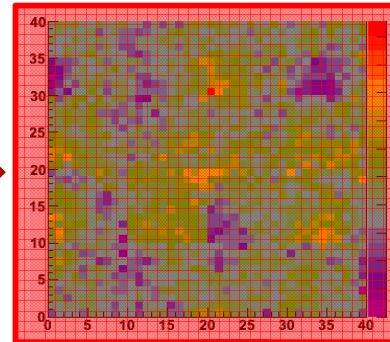
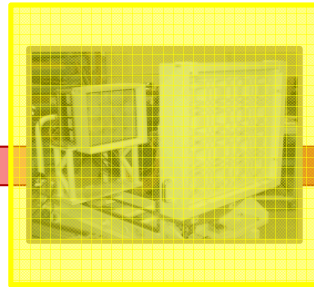
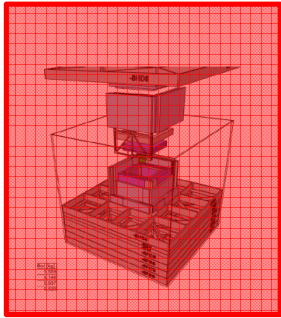
Photo from National Museum
of the USAF

Is it warhead A or warhead B?



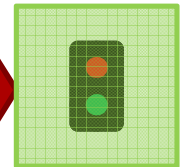
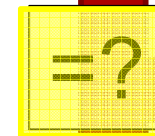
“Traditional” Template Matching

Trusted object

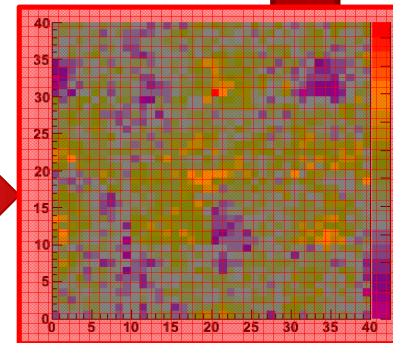
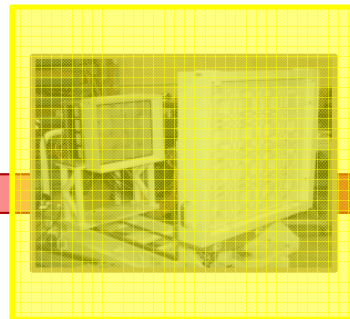
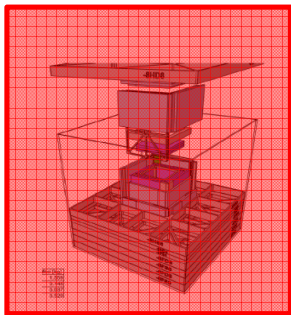


Calibration data is sensitive
IB required

LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access



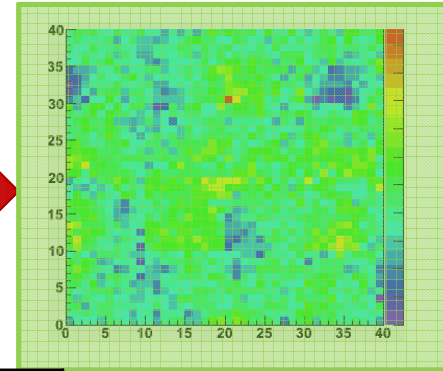
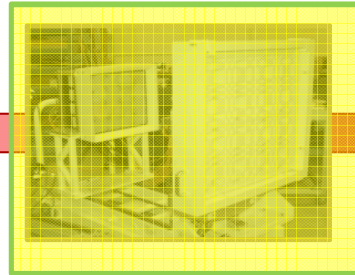
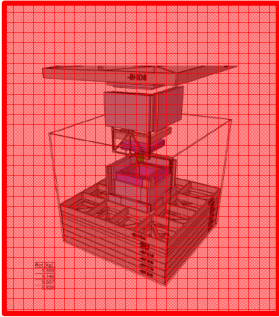
Tested object



Tested detector data is sensitive
IB required

Our proposal

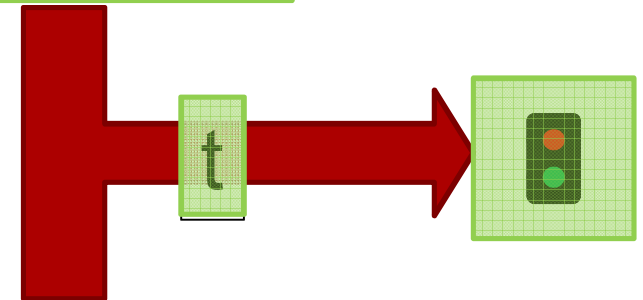
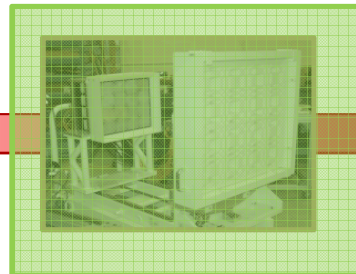
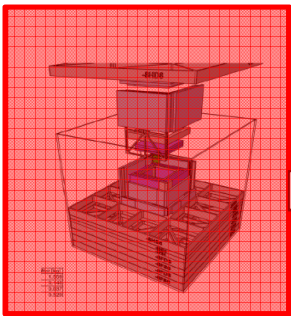
Trusted object



Hypothetical observer stores info sufficient for confirmation but not sensitive

LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access

Tested object



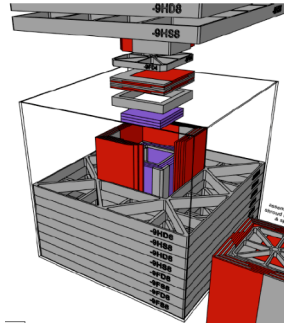
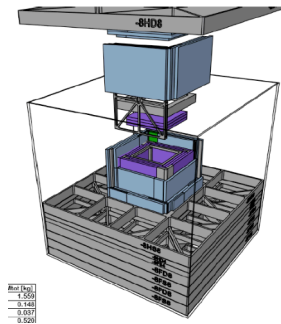
Testing data is processed event by event, only updating test statistic.

Data not aggregated

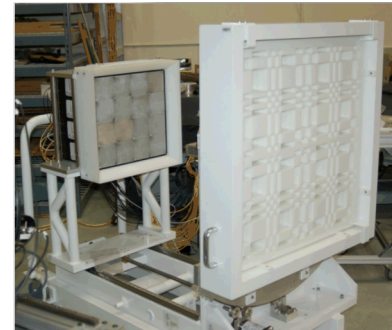
Think snapchat!

Task – Discriminate Idaho Inspection Objects

- Binary discrimination using spectral information.
 - Distinguish objects 8 (Pu surrounded by DU) and 9 (Pu surrounded by HEU) developed by Idaho National Laboratory.
 - Fast-neutron coded-aperture detector with liquid scintillator.



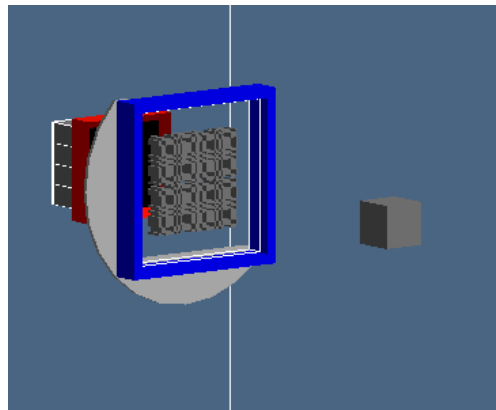
INL/EXT-11-20876



- Rotational variability included (simulated grid of orientations)

GEANT4 Simulations

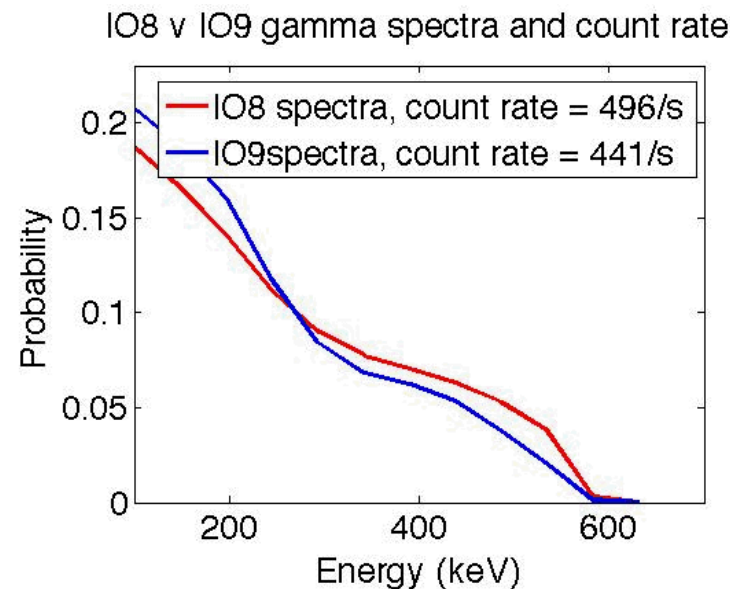
- Models built into transport application using GEANT4 toolkit to acquire testing and training data.



- Difficult to simulate gamma transport in plutonium objects with thick high-Z shielding.
 - Set gamma-energy threshold, applied linear energy bias
 - Used multithreaded capability of GEANT4.10
 - Ran on high-performance-computing clusters at SNL.

Simulation Data

- Similar geometries, no significant spatial difference in detector data.
- Observers make decisions based on gamma spectra differences
 - Data is summed over pixels



Definitions

- List-mode data A_n :
 - Estimated energy, pixel, and particle type (photon or neutron) for event n . Define N to be total number of detected events.
- Nuisance parameters :
 - Characteristics of the objects being imaged that affect the data but are of no interest
 - Examples include orientation, material age, construction, storage container characteristics.

Linear Template Observers

- Testing and training event data $\{A_n\}$ binned into data vector \mathbf{g} ($P \times 1$).

$$g_p = \sum_{n=1}^N f_p(A_n)$$

- \mathbf{g} is binned detector data – image, spectra or both.
- Linear template \mathbf{W} ($P \times 1$) acts on \mathbf{g}_{test} , result is thresholded to make a decision

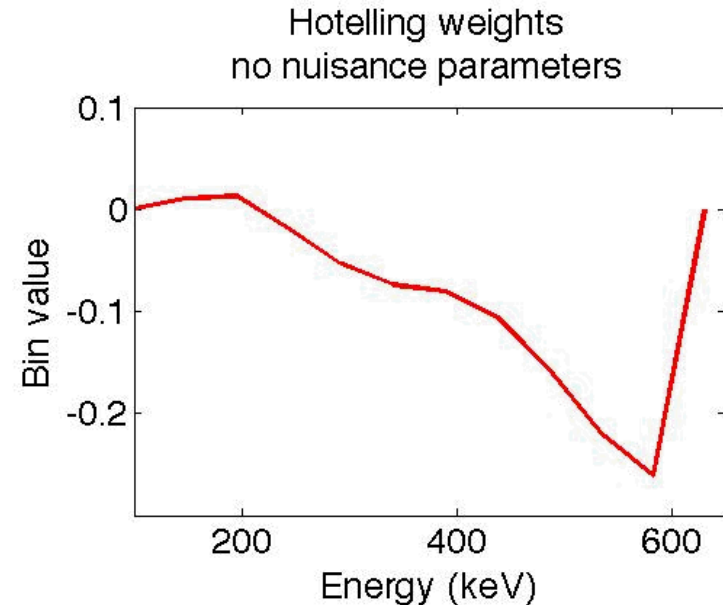
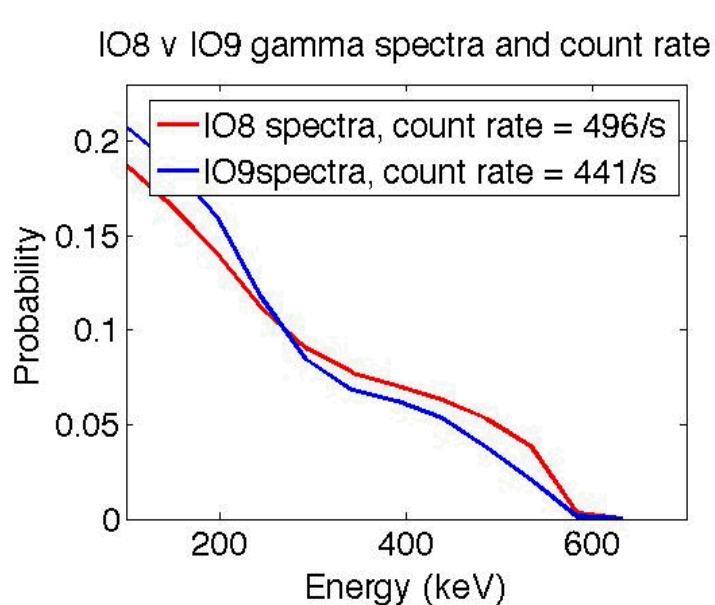
$$t = \mathbf{W}^\dagger \mathbf{g}_{test} \quad t \gtrless t_{thresh}$$

Hotelling Observer

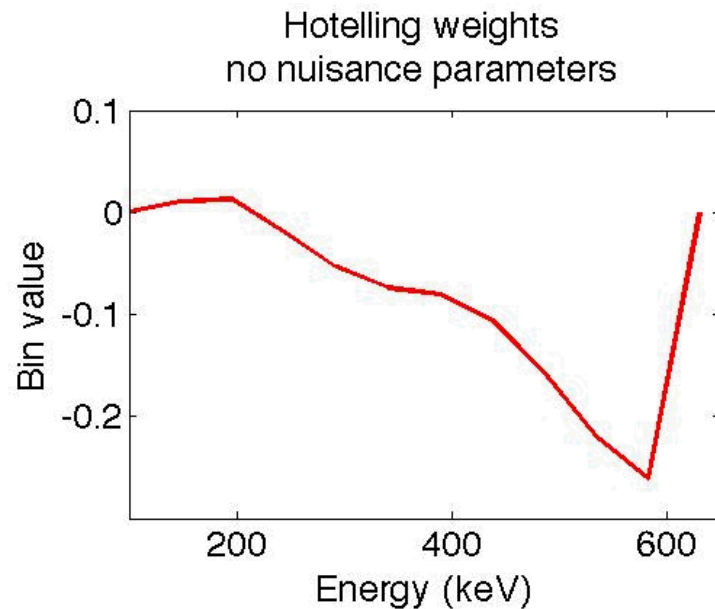
- Hotelling observer is **sensitive template W** defined as:

$$W = K_g^{-1} \overline{\Delta g}$$

- W is optimal template when data statistics are Gaussian.

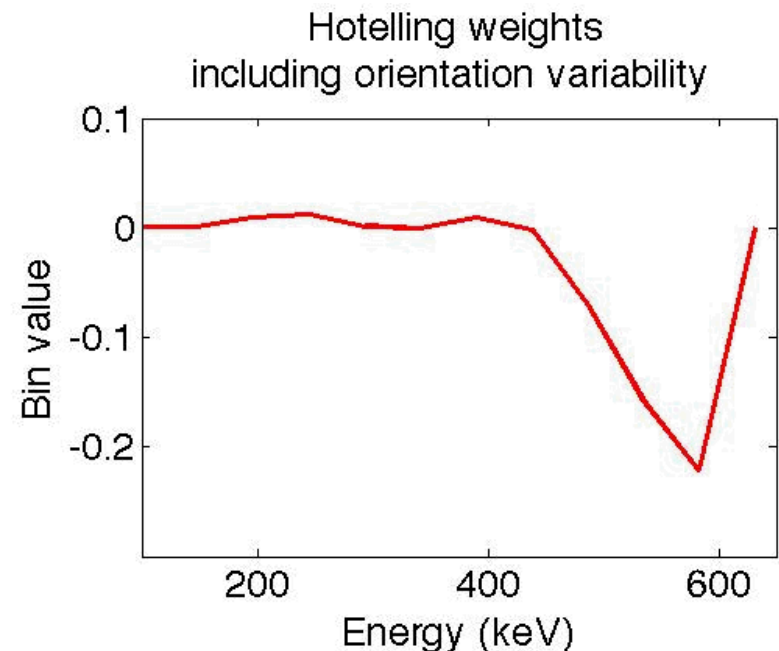


Hotelling Observer with Nuisance Parameters



Slight difference due to dense
K matrix

Relates directly to spectra



+/- of Hotelling Observer

Positives

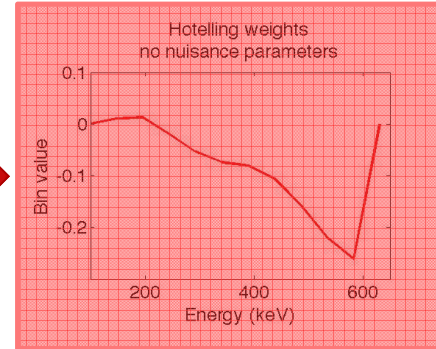
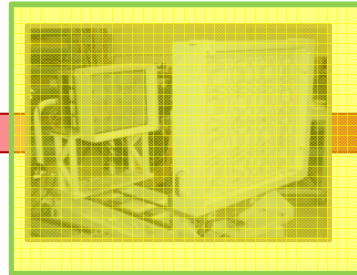
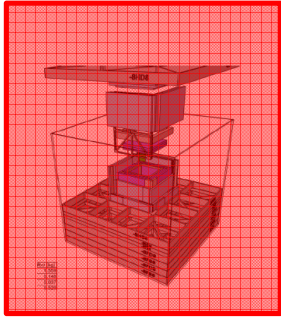
- Only storage is Hotelling template W – not image data g .
- Average over nuisance parameters smears out data.
- Analogous to secondary imaging system that filters out information other than the differences between objects.
 - Impossible to reconstruct g , only W .

Negatives

- Template contains product of first and second order statistics, but still (likely) constitutes sensitive information

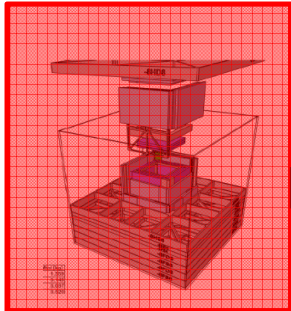
Hotelling Observer in Practice

Trusted object

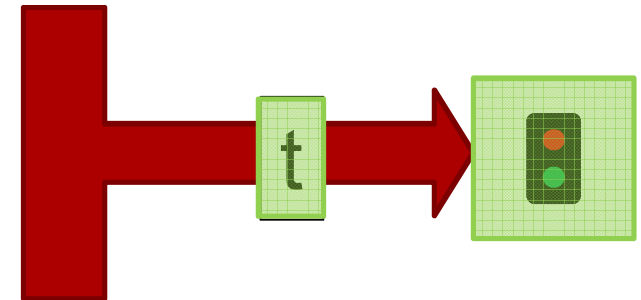
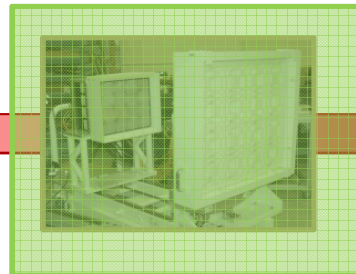


Hotelling template probably sensitive, but can't reconstruct object from t

Tested object



LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access



Testing data is processed event by event, only updating test statistic.

Channelized Hotelling Observer (CHO)

- Can we channelize data into non-sensitive channel values that monitor can work with?
- Channelize data vector \mathbf{g} ($P \times 1$) with channelizing matrix \mathbf{T} ($Q \times P$) into much smaller vector \mathbf{v} ($Q \times 1$).

$$\mathbf{v} = \mathbf{T}\mathbf{g}$$
$$Dim(\mathbf{v}) \ll Dim(\mathbf{g})$$

$$\mathbf{W}_{\mathbf{v}} \mathbf{v}_{test} \lesssim t_{thresh}$$

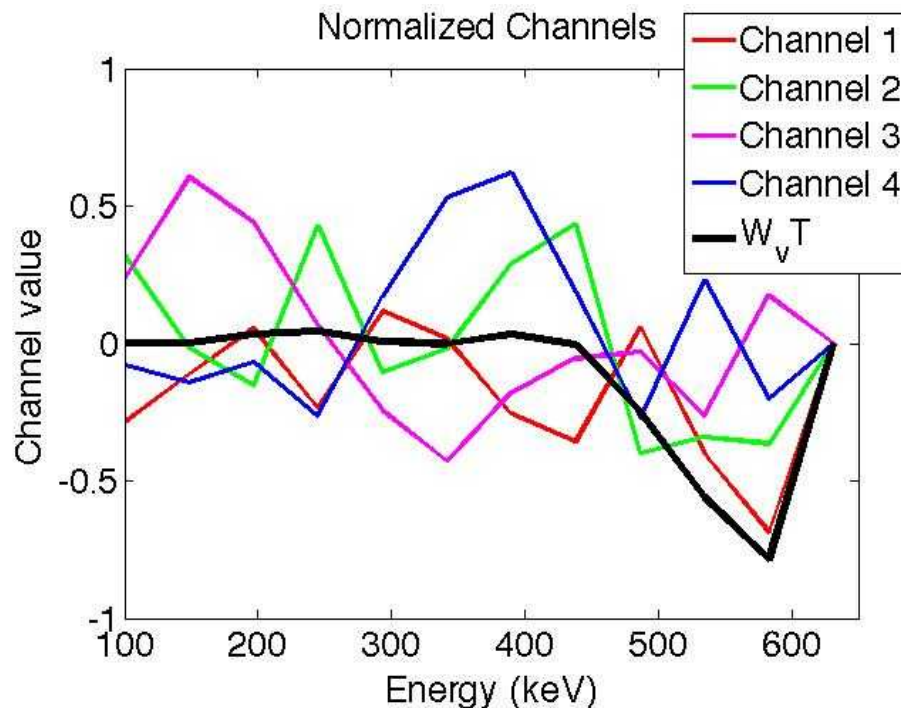
Optimizing \mathbf{T}

- \mathbf{T} can be optimized to maximize SNR^2 of test statistic distributions for best performance.
 - Gradient descent with backtrack

$$\begin{aligned} f_{obj}(\mathbf{T}) &= \text{SNR}^2(\mathbf{T}) \\ &= \overline{\Delta \mathbf{v}(\mathbf{T})}^\dagger \mathbf{K}_{\mathbf{v}}(\mathbf{T})^{-1} \overline{\Delta \mathbf{v}(\mathbf{T})} \end{aligned}$$

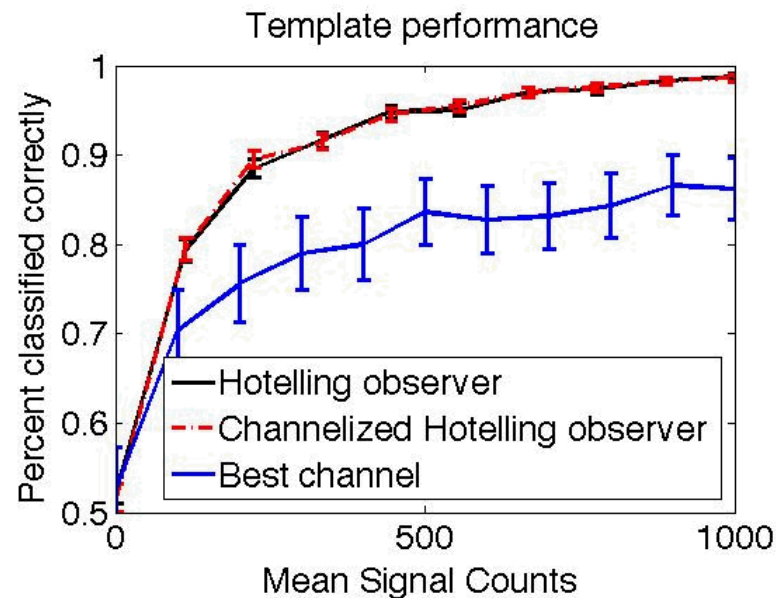
Example Channelization

- Standard optimization leads to fairly nonsensitive channels.
- Optimal performance requires sum of optimally weighted channels to equal **Hotelling weights**.



Performance of HO & CHO

- Task is to discriminate IO8 and IO9 when orientation is unknown



- However, best channel in other tasks has equal performance to CHO

+/- of CHO

Positives

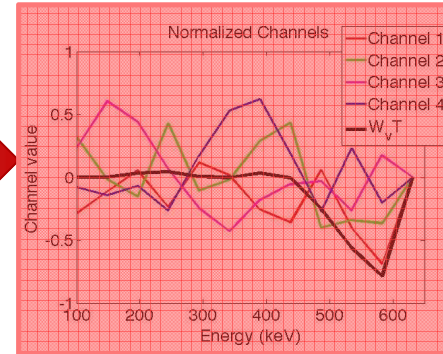
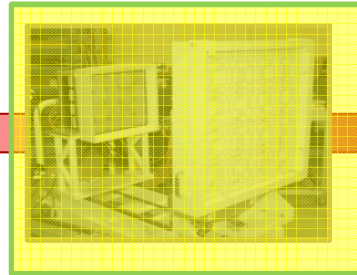
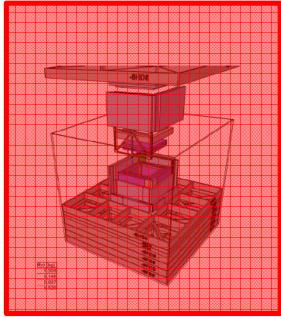
- Q non-sensitive channel values that monitor can use to make decisions
 - More channels = improved ability to verify tested sources is one of two in discrimination task, and not a spoof
- Optimizing SNR² results in optimal performance
 - Impossible to reconstruct *image*, only *Hotelling weights (difference in images)*.

Negatives

- Optimally weighted sum is sensitive information
- *Channelizing matrix itself* often sensitive, cannot be shared.

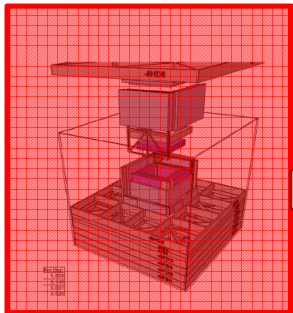
CHO in practice

Trusted object

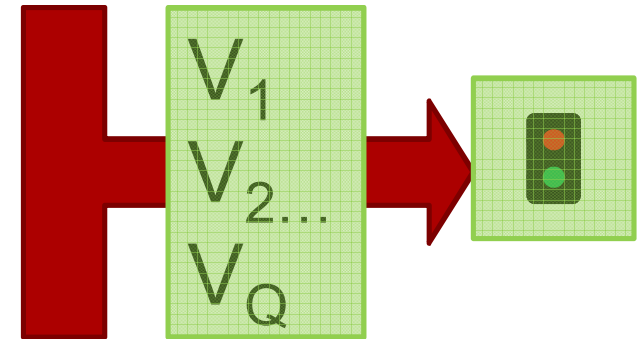
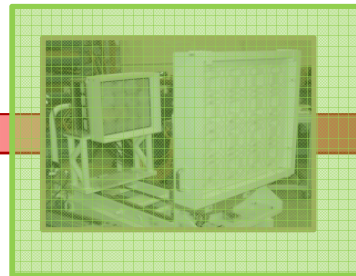


Channels may/may not be sensitive, but $W_v T$ is

Tested object



LEGEND	
Red	No Access
Yellow	Access Before & After
Green	Full Access



Testing data is processed event by event, updating Q channelized values

Current/Future work

- Build off channelized Hotelling observer groundwork

- Create nonsensitive channels by penalizing channel performance

$$f_{obj} = SNR_{Q_{channels}}^2 - \eta \sum_{q=1}^Q SNR_{channel\ q}^2$$

- Add noise to channels to reduce sensitive storage and performance.
- If host defines sensitive parameters in geometry construction, we can penalize the ability to discriminate between slight differences in the object

Summary

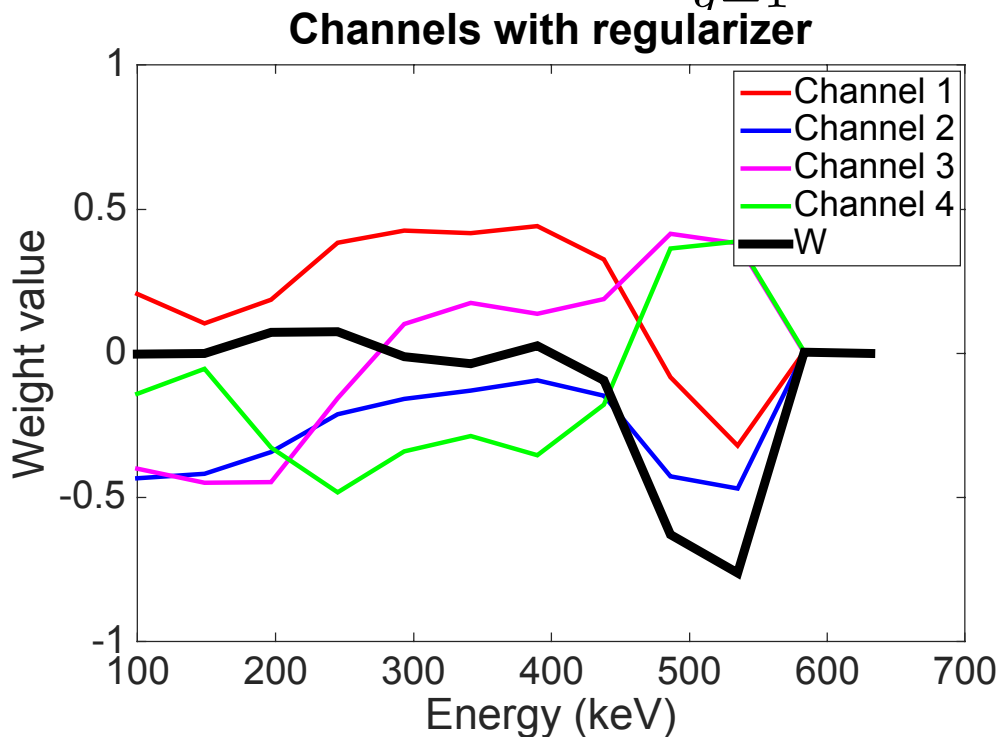
- Applying methods developed by medical imaging community to arms-control-treaty verification tasks
- Modeled inspection objects in transport application using GEANT4 toolkit to simulate data
- Hotelling observer gives optimal results while only storing differences between objects
- Channelized Hotelling observer gives monitor access to more information
 - Adding terms to optimization routine offers paths to non-sensitive storage

Extra slides

CHO with penalty

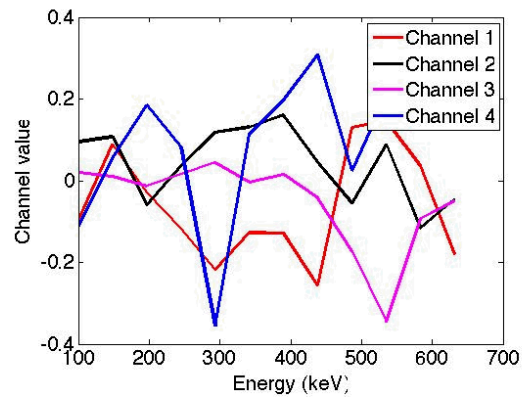
- Use penalty term in optimization to **limit channel performance**

$$f_{obj} = SNR_{Qchannels}^2 - \eta \sum_{q=1}^Q SNR_{channel\ q}^2$$



CHO inverse problem

T

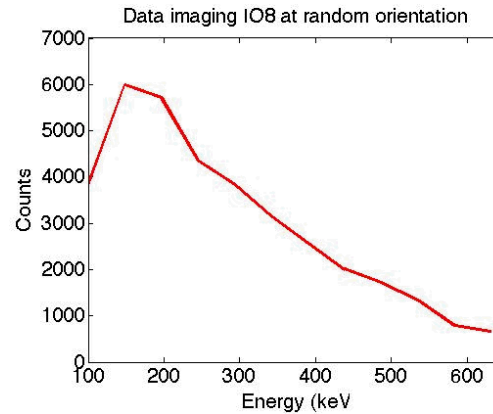


x

g

$=$

v



-365
-5589
223
-3030

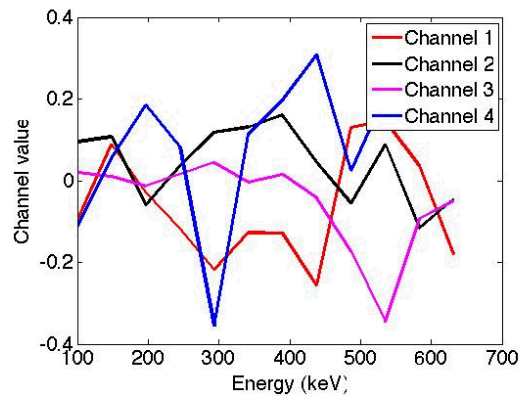
T^{-1}

x

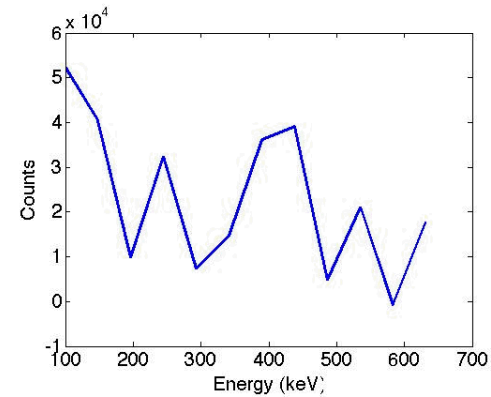
v

$=$

g_{rec}



-365
-5589
223
-3030

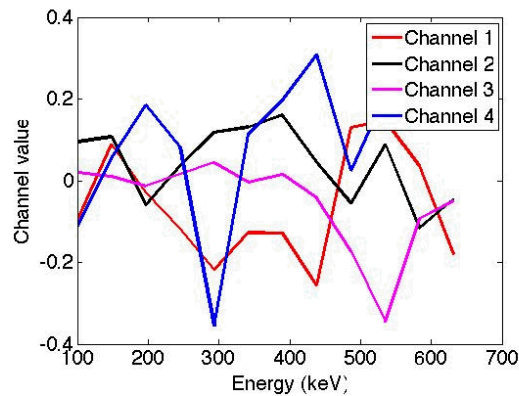


CHO inverse problem

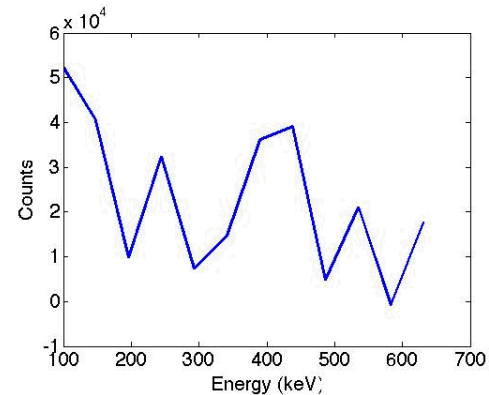
$$T \quad x \quad g \quad = \quad v$$

Channel value

Channels, singular vectors, reconstruction are all very noisy,
But channel 3 looks like W

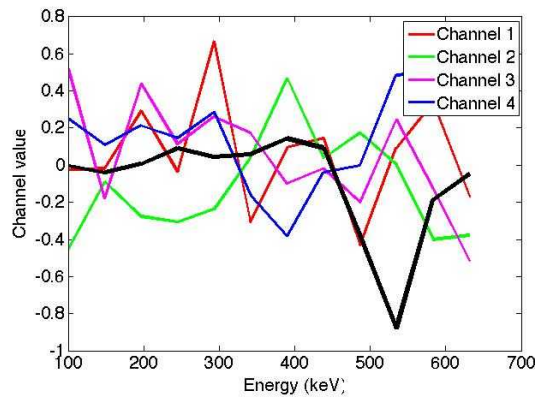


-365
-5589
223
-3030



CHO inverse problem w/ perform. penalty

T

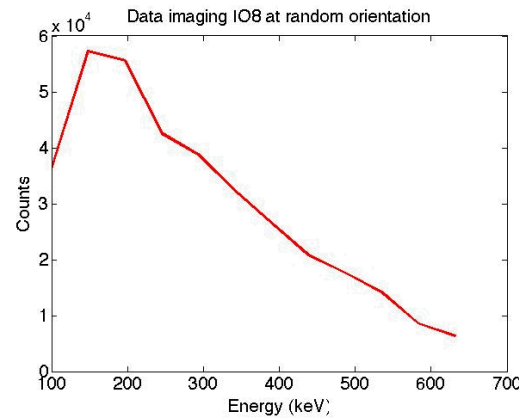


x

g

$=$

v



1.38e4
-2.25e4
2.26e4
2.19e4

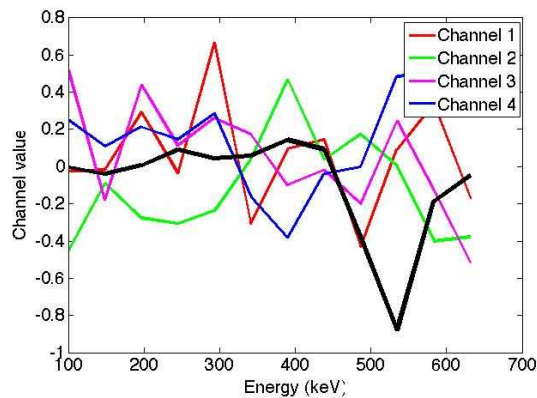
T^{-1}

x

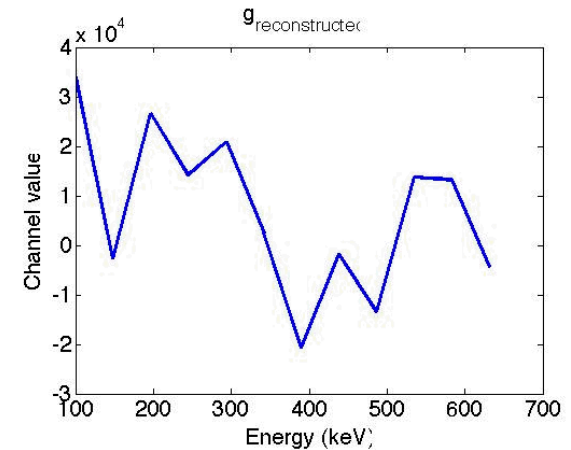
v

$=$

g_{rec}

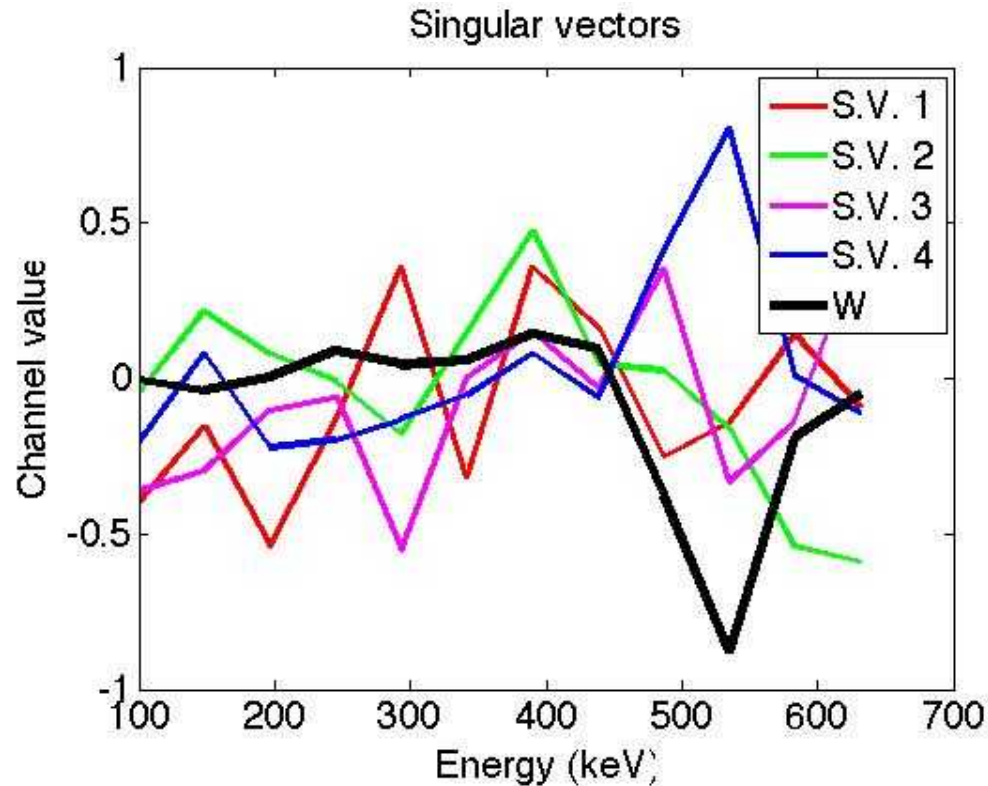


1.38e4
-2.25e4
2.26e4
2.19e4



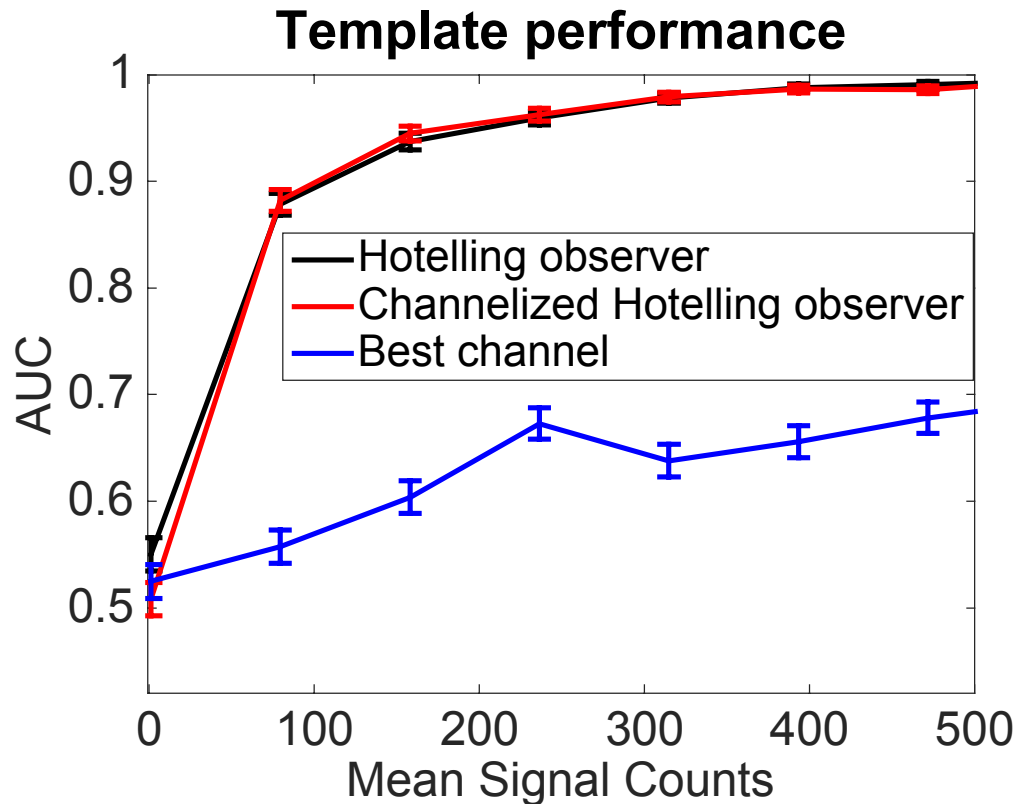
CHO inverse problem w/ perform. penalty

- SVD of channelizing matrix: S.V. 4 looks like Hotelling weights



Channelized Hotelling penalty

- Hotelling and channelized Hotelling perform well
- Individual channels perform poorly



Future work – reducing sensitive info

- Example: Source A is a BeRP ball with 1" of poly shielding. The host country doesn't want the monitor to know what source A's poly thickness is down to a tolerance of Δt

$$f_{obj} = SNR_{(B-A)}^2 - \eta SNR_{(A_{(1''+\Delta t)} - A_{(1'')})}^2$$

- Will lead to drop in performance with benefit that host needn't worry.

Future work – reducing sensitive Info

$$f_{obj} = SNR_{(B-A)}^2 - \eta SNR_{(A_{(1''+\Delta t)} - A_{(1'')})}^2$$

- A channelizing matrix that optimizes this objective function wouldn't be based on sensitive data
- Likewise, sensitive data could not be gained through the inverse problem

Future work – null hypothesis test

- Need an observer to address “Is this source A or not source A?”
- We developed a model based on likelihood expression, but it is spoofable.
- Standard tests based on distance metrics
- Is there a linear model similar to the Hotelling observer?