

Exceptional  
service in the  
national  
interest

# Mesh Scaling

Generation of Incrementally finer meshes for Solution Verification

Matt Staten, Brian Carnes

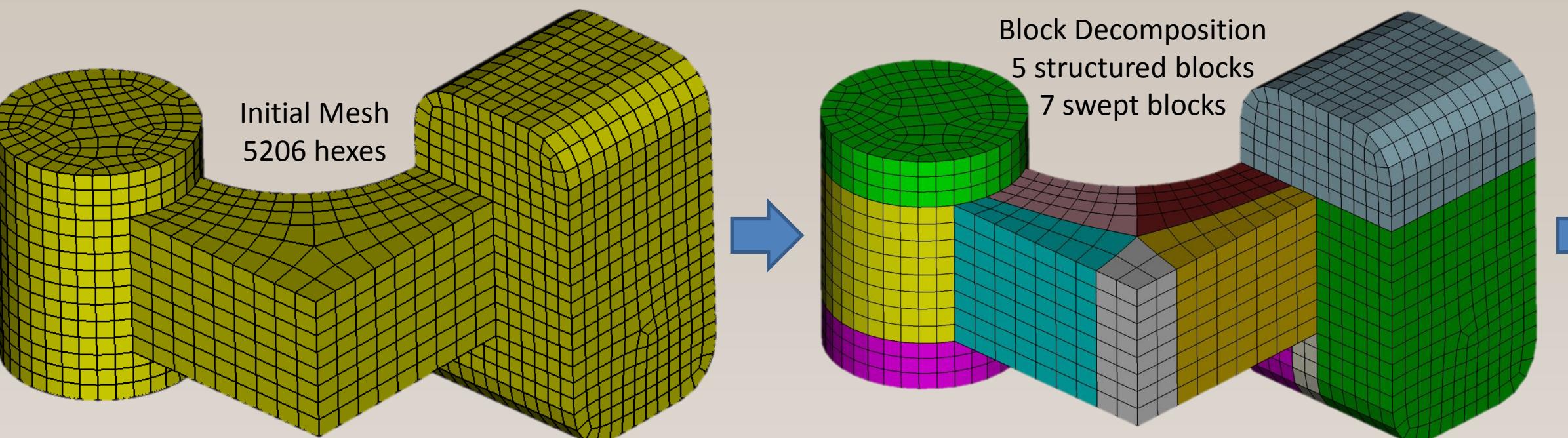


Sandia  
National  
Laboratories

## What is Mesh Scaling?

Mesh Scaling is a new mesh modification algorithm which, given an input all-hex mesh and a desired element count multiplier,  $N$ , will generate a new hex mesh with approximately  $N$  times more/less hex elements, while honoring element size grading and element orientations. Mesh Scaling offers an alternative to traditional uniform mesh refinement (UMR), without the 8X multiplier limitation.

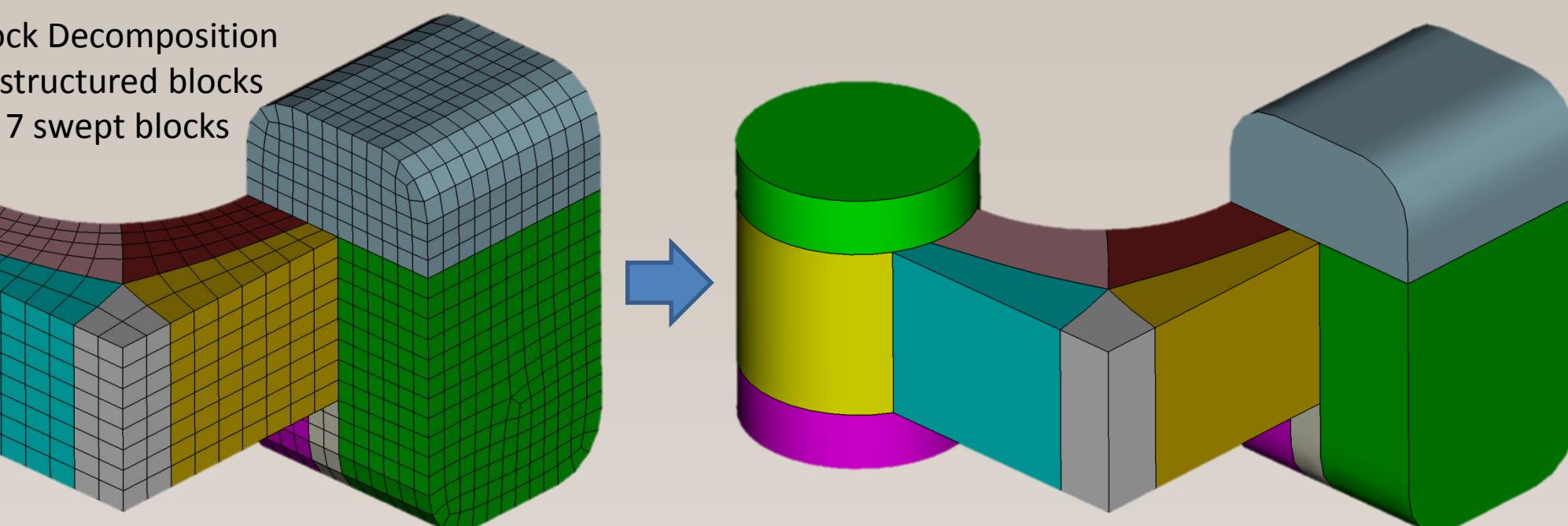
## How Does Mesh Scaling Work?



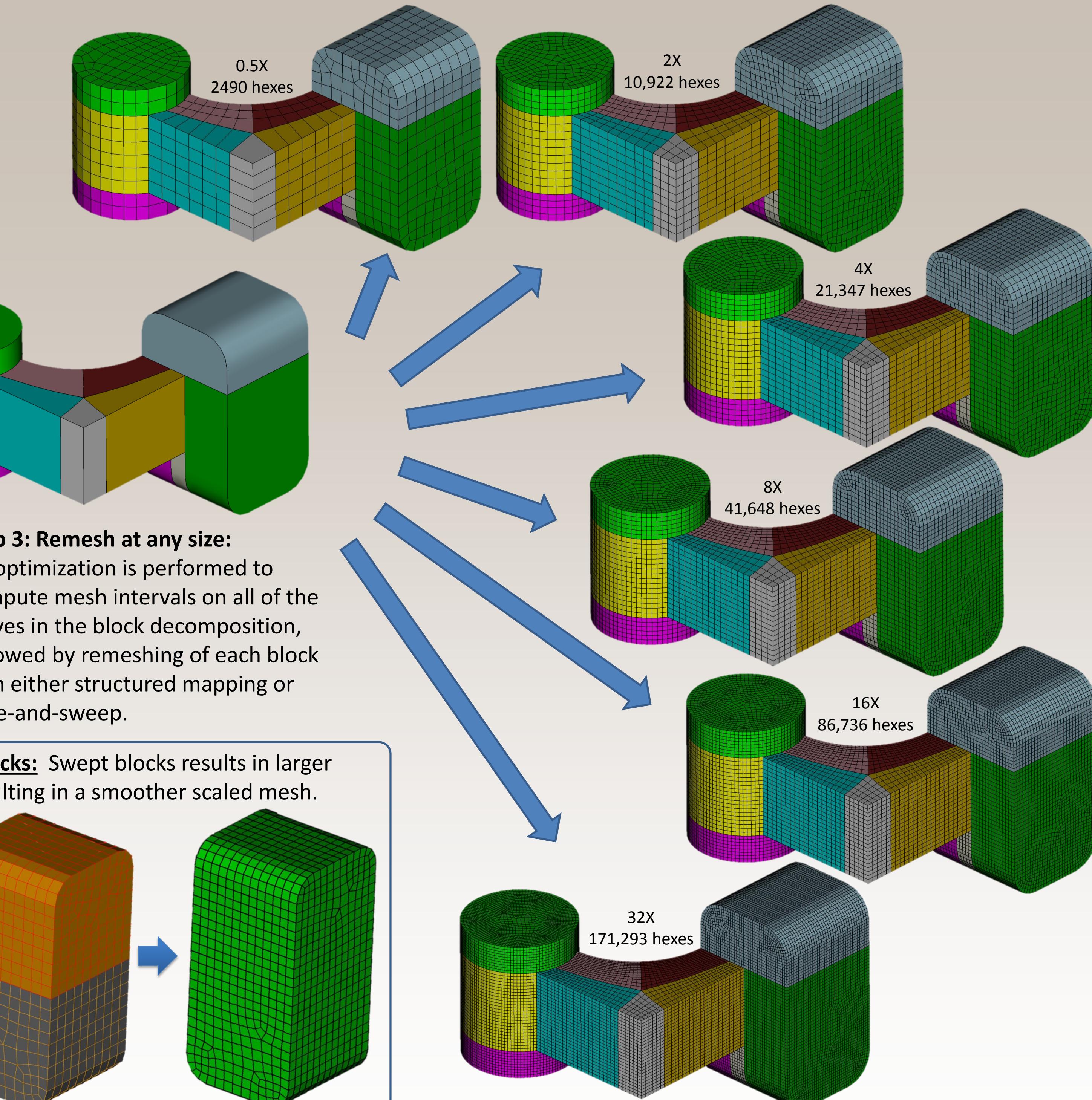
**Step 1: Extract the Block Decomposition:**  
Hex mesh topology is traversed looking for:

1. Swept mesh connectivity, AND
2. Structured zones separated by mesh singularities

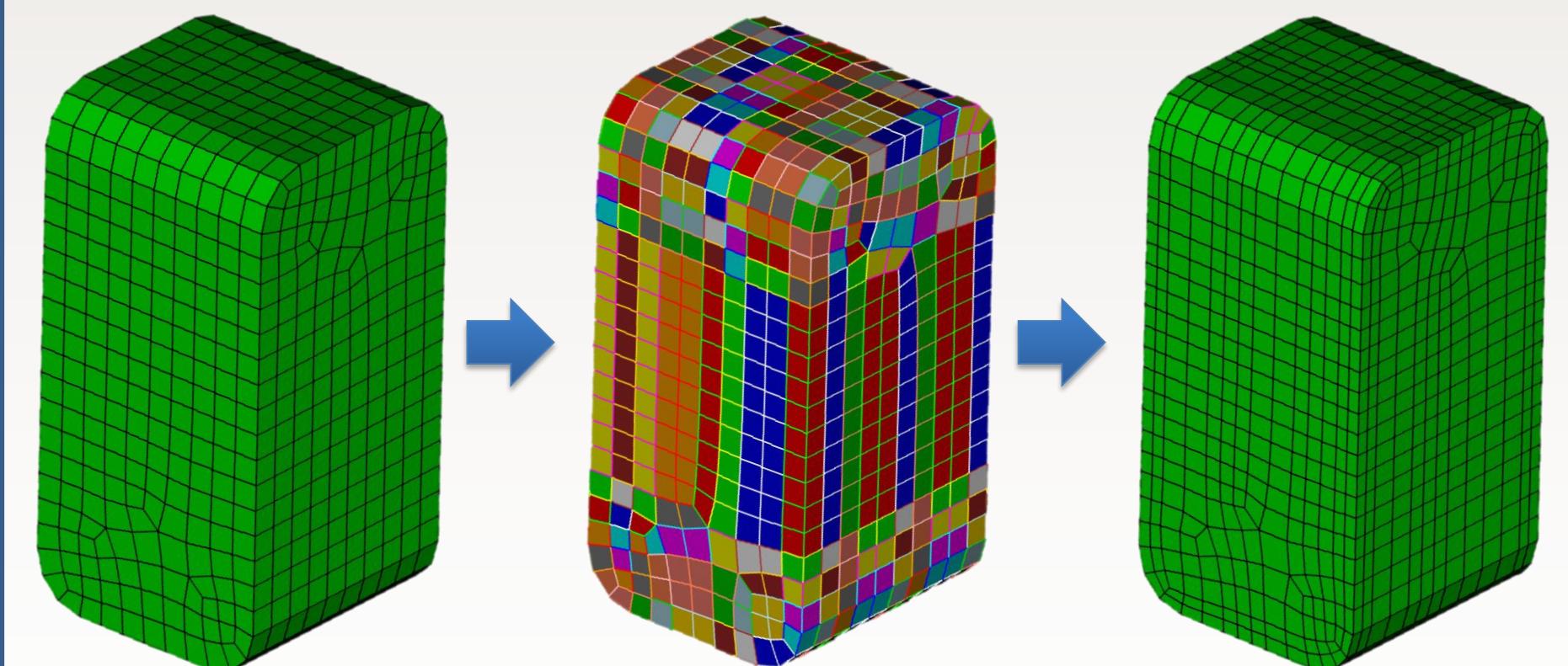
The mesh is then decomposed into both structured and swept blocks



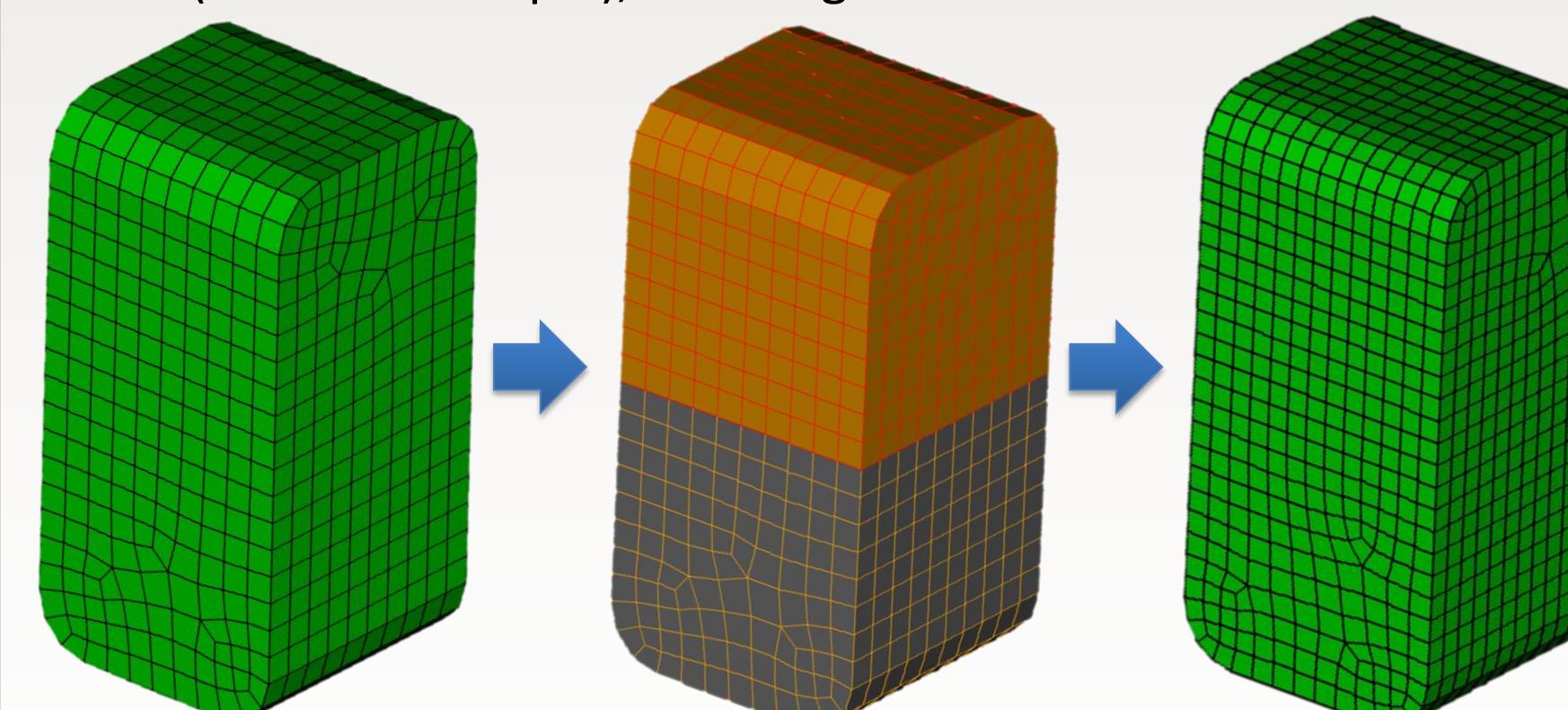
**Step 2: Delete Initial Mesh:**  
Mesh sizing, grading, orientation, and BC loading are extracted from the mesh and stored in the block decomposition. The original mesh is then deleted.



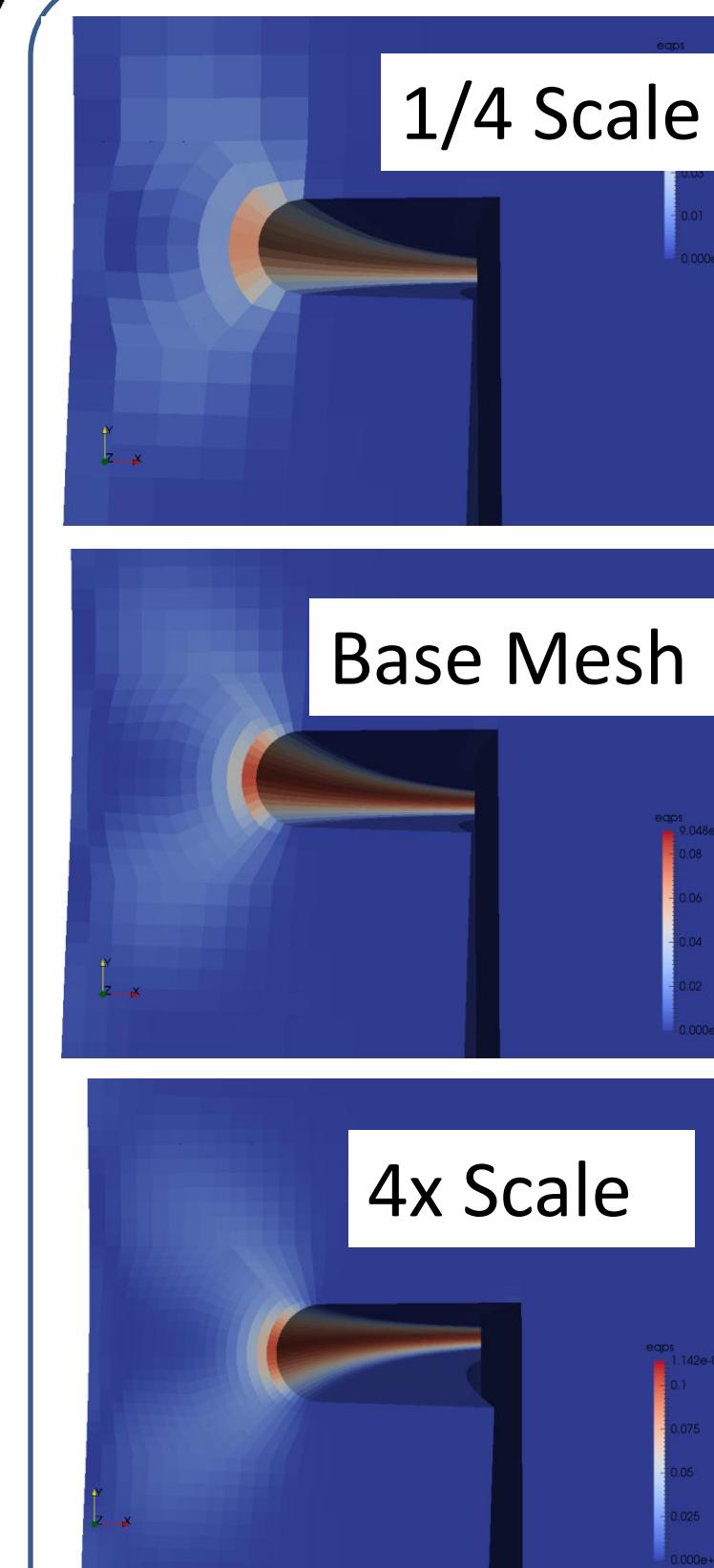
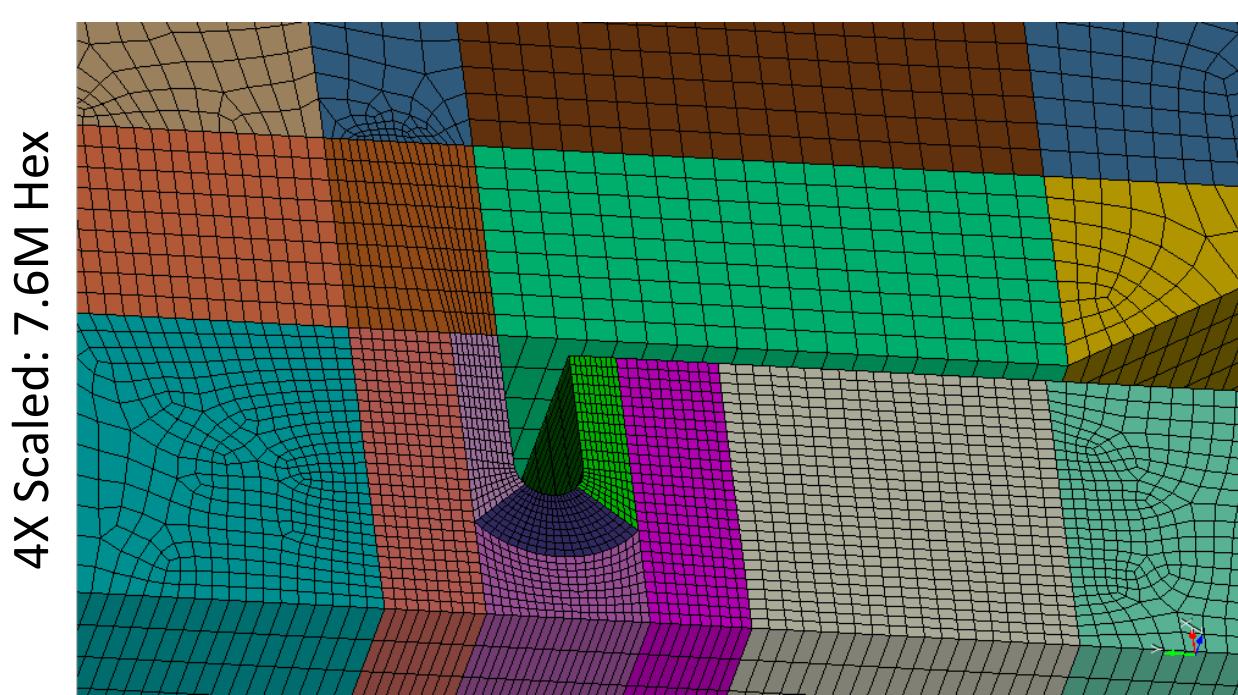
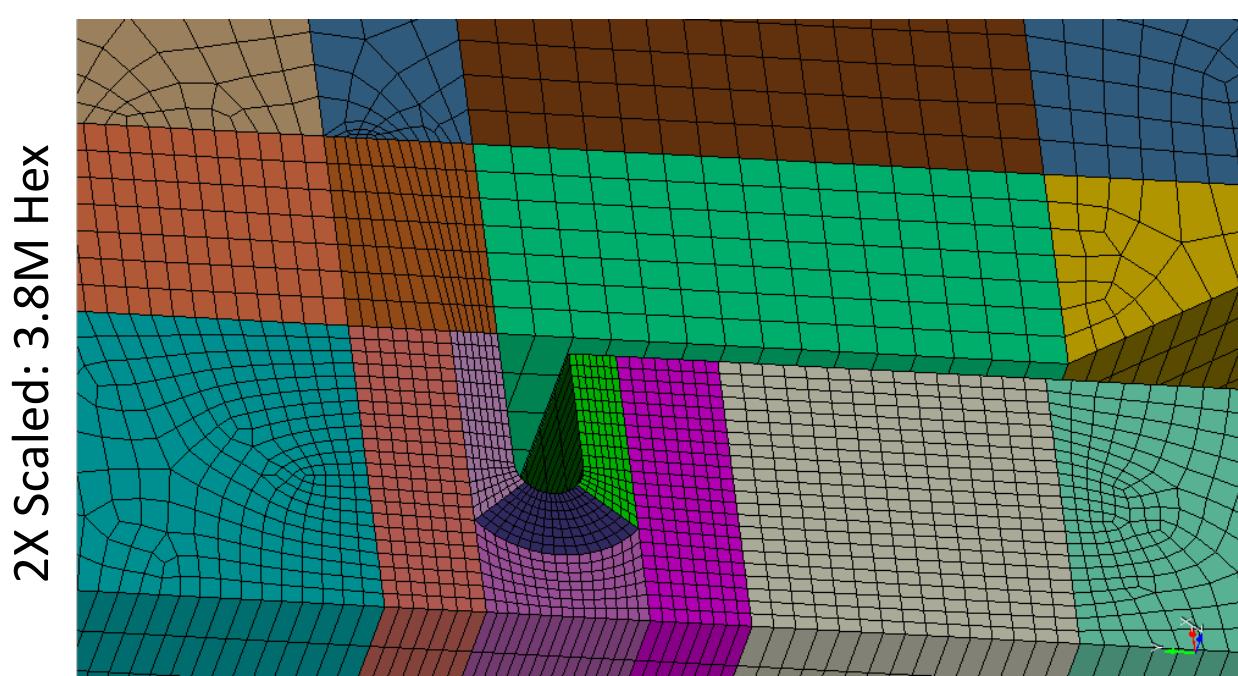
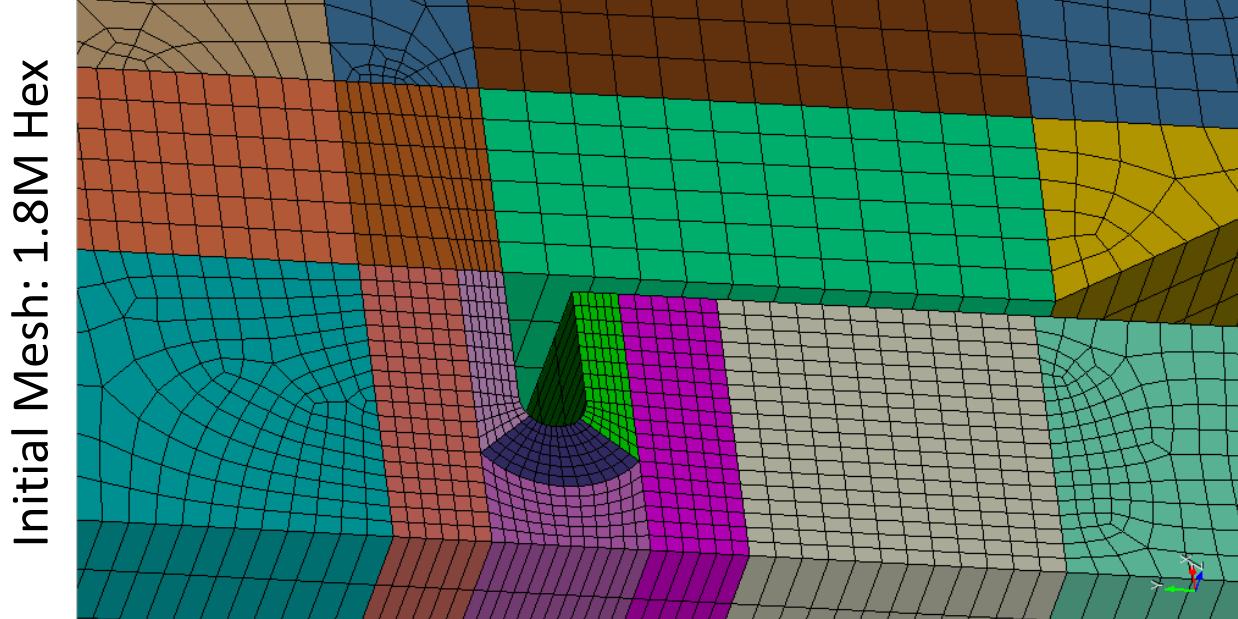
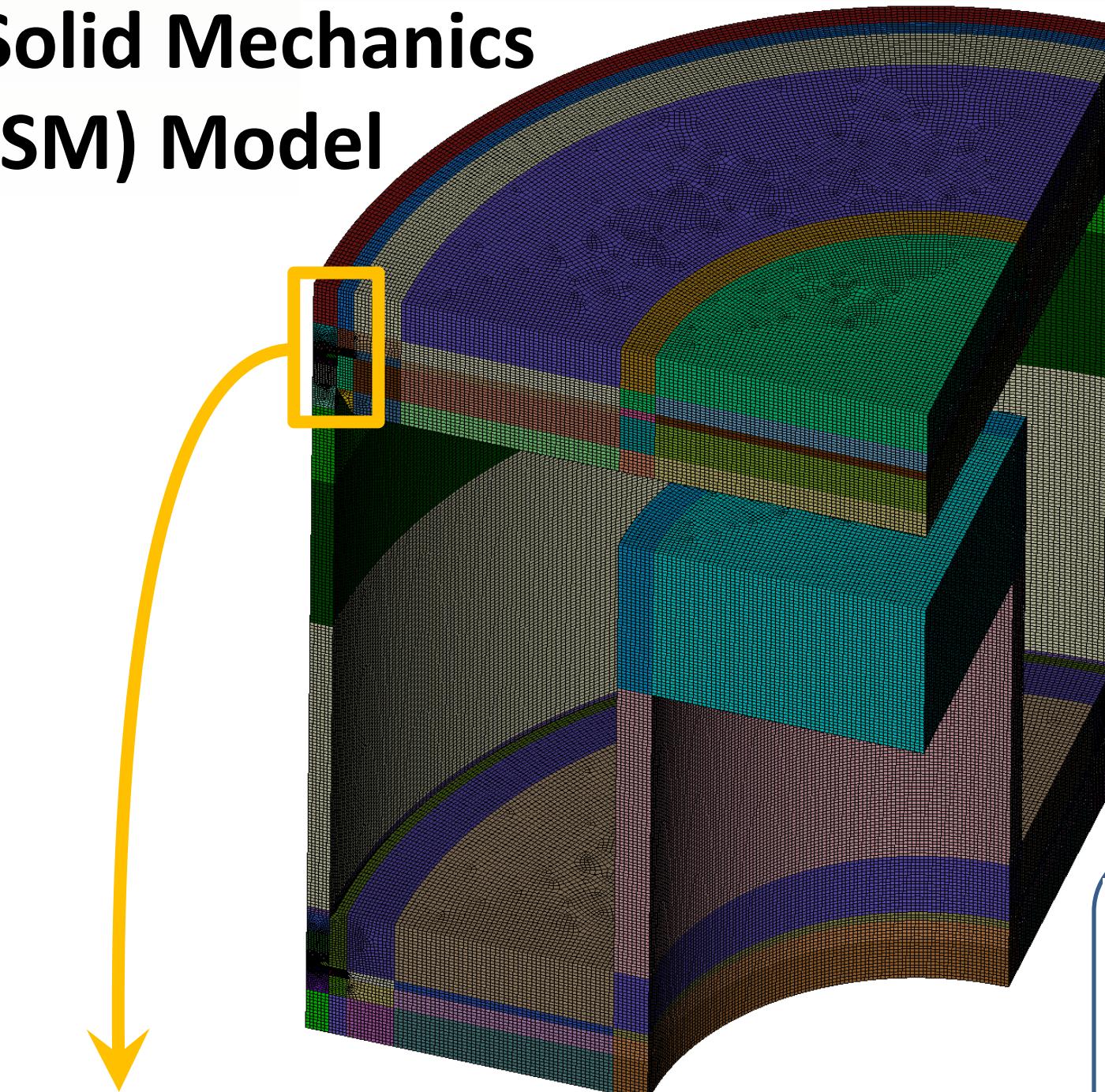
**Using Structured Blocks Only:** Honoring all mesh singularities results in 736 blocks in the decomposition and an unevenly scaled mesh.



**Mesh Scaling Using Swept Blocks:** Swept blocks results in larger blocks (2 in this example), resulting in a smoother scaled mesh.

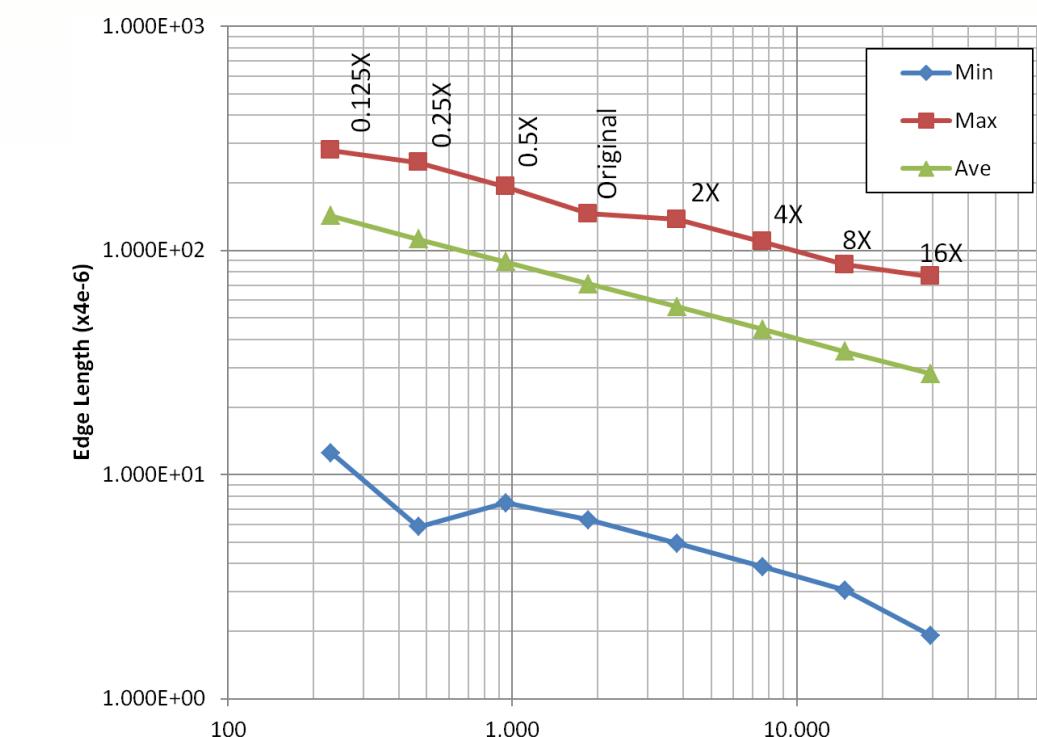


# Solid Mechanics (SM) Model

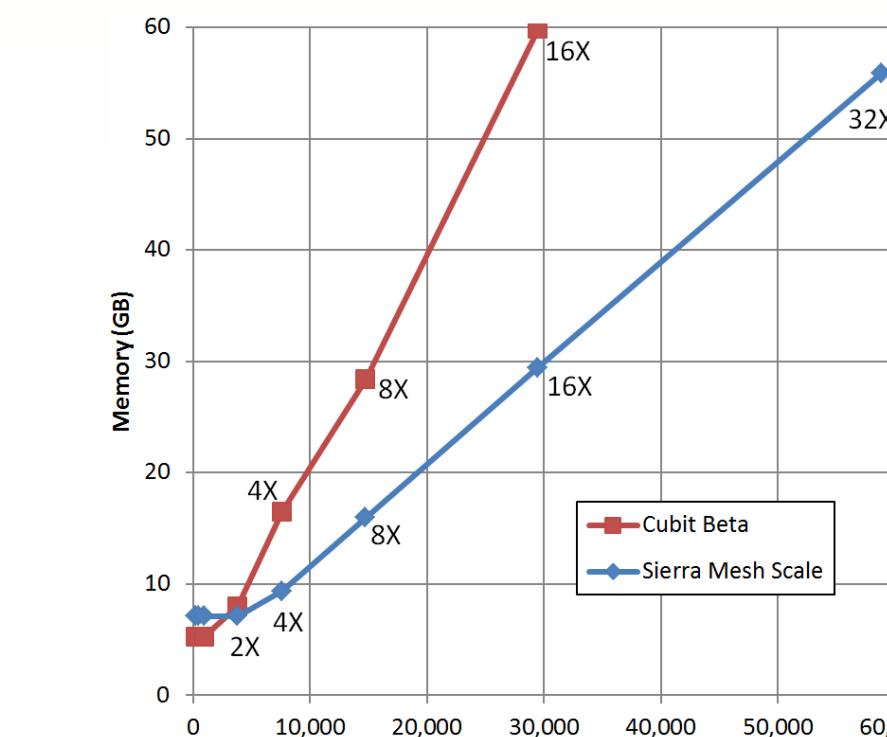


The model simulates weld failure from thermal/mechanical loading. The main output is the maximum equivalent plastic strain (EQPS), an indicator of weld failure.

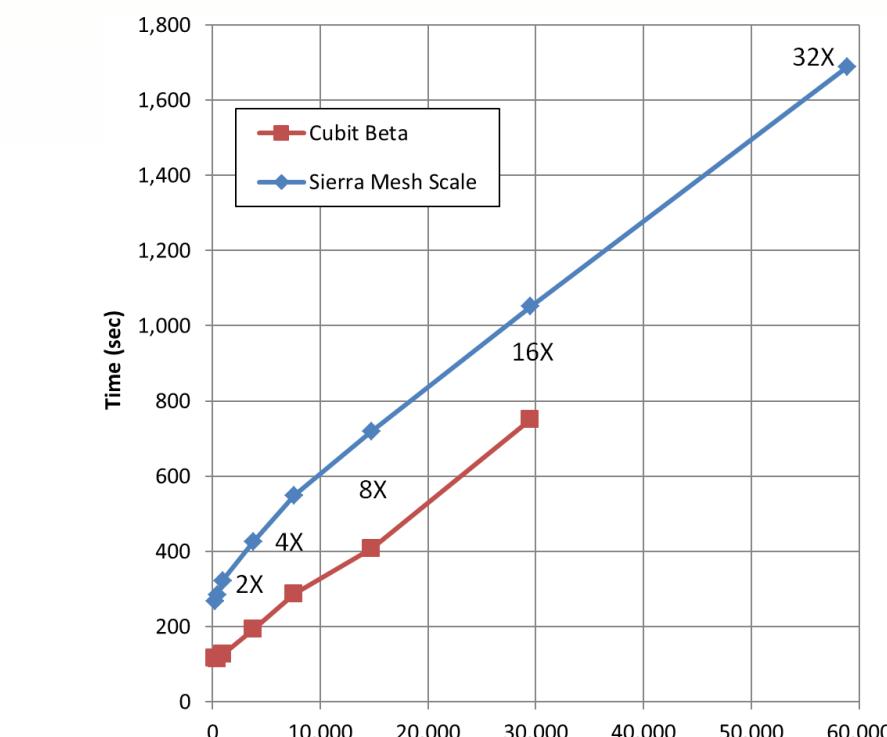
## Edge Lengths



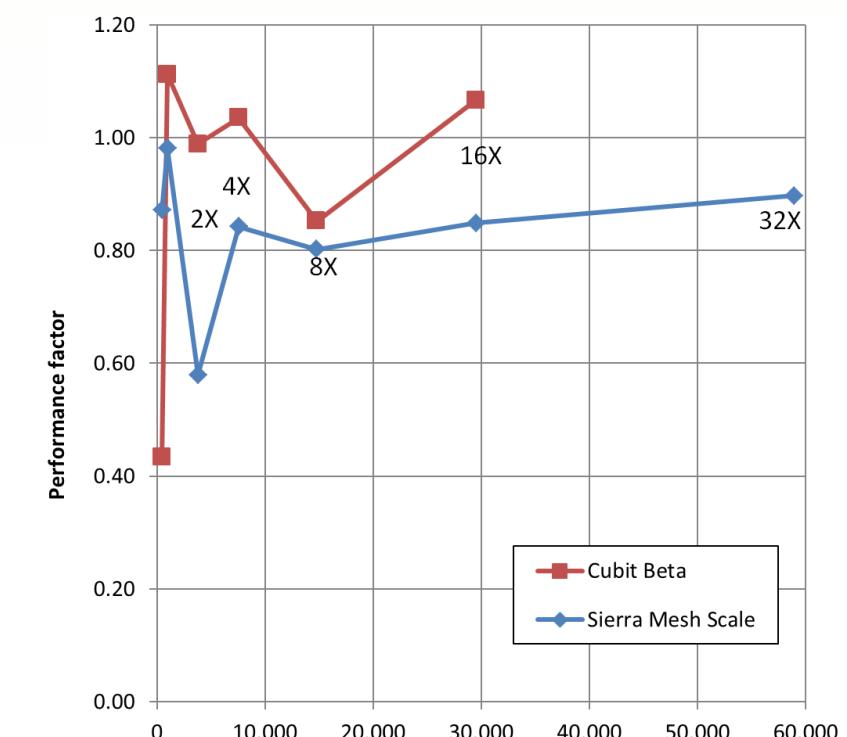
## Memory



## Performance



## Performance Factor



Run on: 64 GB, 16 proc Intel(R) Xeon(R) CPU E5-2670 0 @ 2.60GHz

$$\text{Performance Factor}_i = \frac{\text{Time}_{i-1}/\text{Time}_i}{\#\text{Elem}_{i-1}/\#\text{Elem}_i} = \frac{\text{time to remesh block decomposition doubles}}{\#\text{elems in scaled mesh doubles}} \approx 1.0$$

## Solution Verification and Mesh Scaling

Solution verification (quantified numerical error estimation)

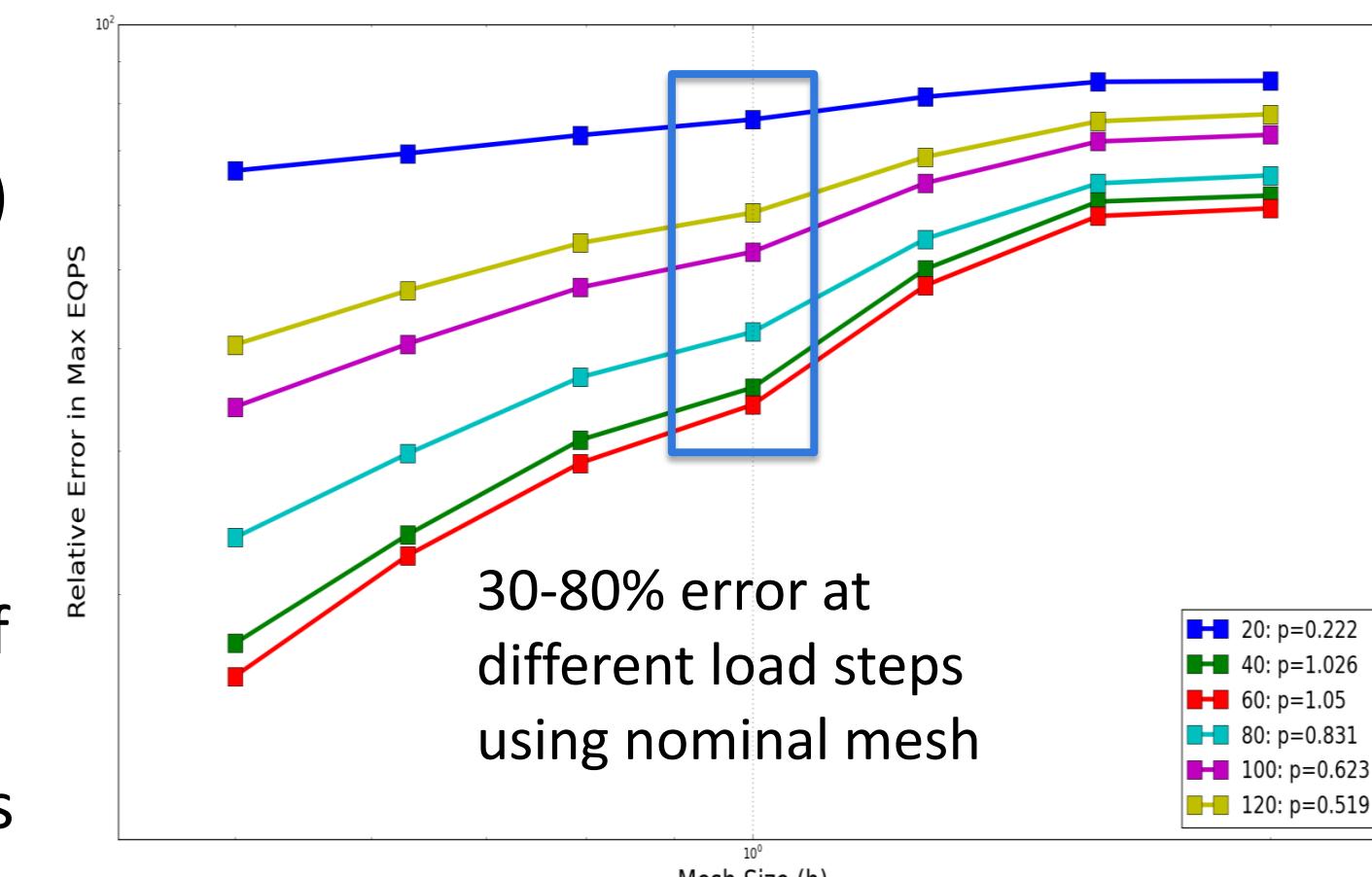
- is required for simulation prediction uncertainty
- typically requires a >100x increase in cost for a 3 grid sequence (using 8x, 64x scale factors)

The Mesh Scaling alternative:

- provides fine grained capability to generate a sequence of meshes – including coarsening
- Is used in solution verification with significant cost savings

Impact of Mesh Scaling:

- has enabled solution verification of models that primarily use hex meshes - solid mechanics and structural dynamics
- future work will increase impact to all mesh-based simulation models (tet meshes)



Above: Error estimates as a function of mesh size from extrapolation using mesh scaling (at selected points on the load history). Below: Nominal model response with error bars

