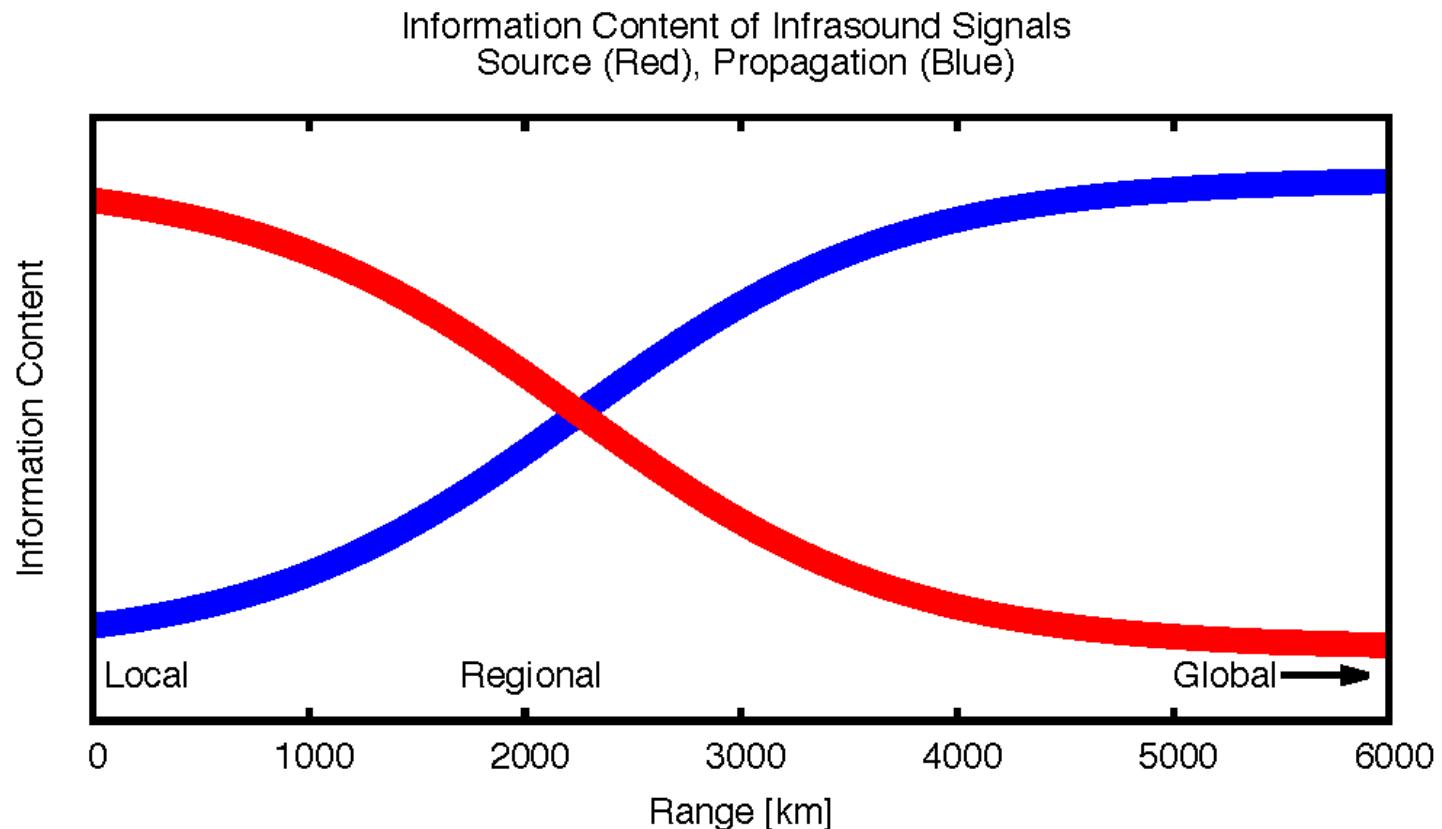




# Infrasound Event Detection

# Infrasound Event Detection



- An inherent assumption of global infrasound data processing is that there is little source information that is extractable at global distances.
- Thus, event detectors are based almost exclusively on coherence at arrays, and on agreement of arrival times and azimuths at spatially-separated arrays

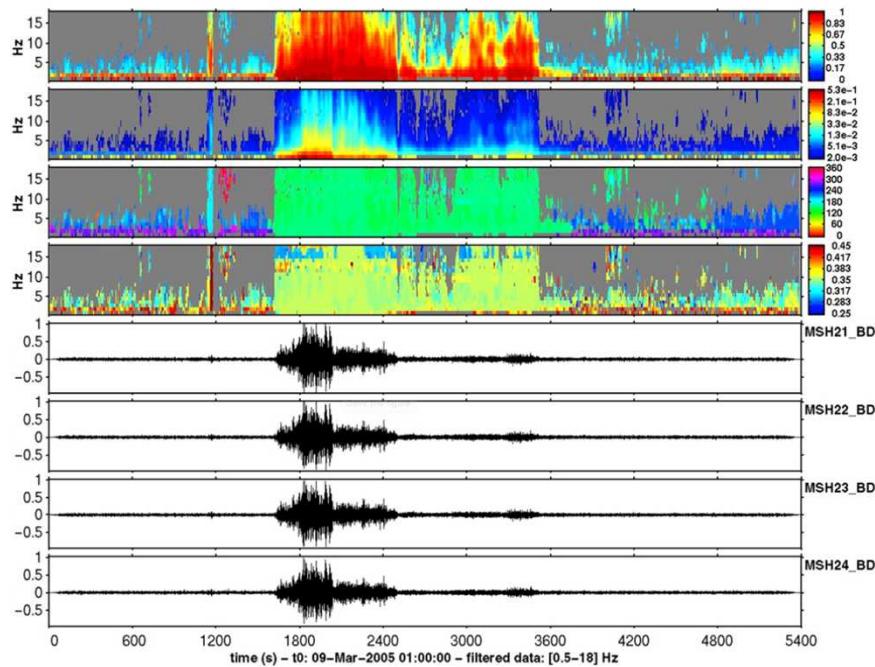
# Infrasound Event Detection: PMCC

## Ground-based Nuclear Explosion Monitoring R&D

Basic hypothesis:  $x_i(t) = s(t - \mathbf{r} \cdot \mathbf{u}) + w_i(t)$

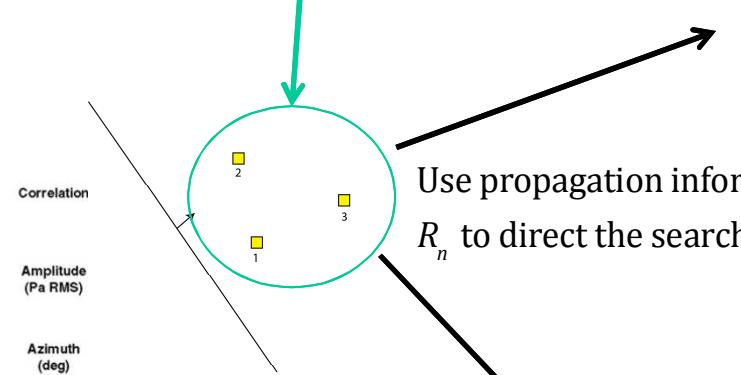
- ‘Clutter’ or ‘correlated noise’ under this definition is a signal
- Use of multiple narrowband filters to separate simultaneous signals in the f-domain
- Progressive  $\rightarrow$  Handles noisy channels
- Requires extensive post-processing

PMCC detections from the eruption of Mt. St. Helens.  
Different colored pixels represent detections in time/frequency space.



$$r_{ijk} = \Delta t_{ij} + \Delta t_{jk} + \Delta t_{ki}$$

$$c_n = \sqrt{\frac{6}{n(n-1)(n-2)} \sum_{i>j>k} r_{ijk}^2} \quad \left. \right\} i, j, k \in R_n$$



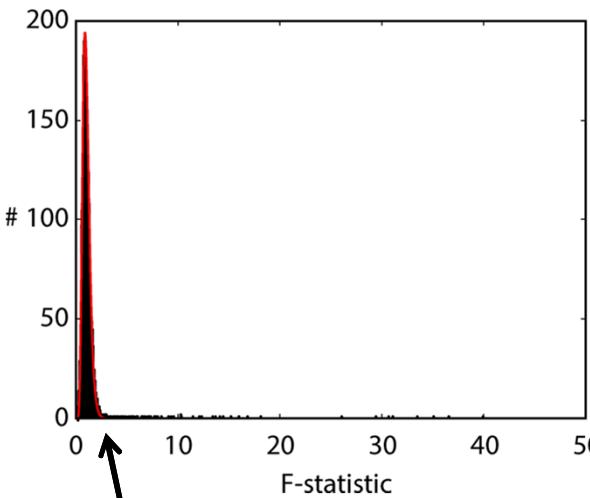
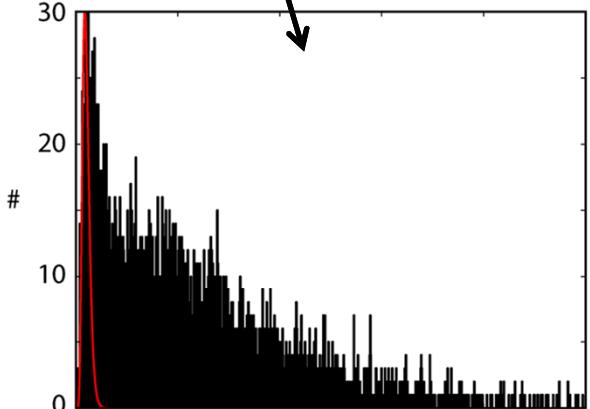
Use propagation information from  $R_n$  to direct the search at other sensors

Pixels are coalesced into families (‘detections’) using distance metrics

$$d(P_1, P_2) = \sqrt{\frac{\Delta t^2}{\sigma_t^2} + \frac{\Delta f^2}{\sigma_f^2} + \frac{\Delta v^2}{\sigma_v^2 v_2 v_1} + \frac{\Delta \theta^2}{\sigma_t^2}} < d_{\text{thres}}$$

# Infrasound Event Detection: AFD

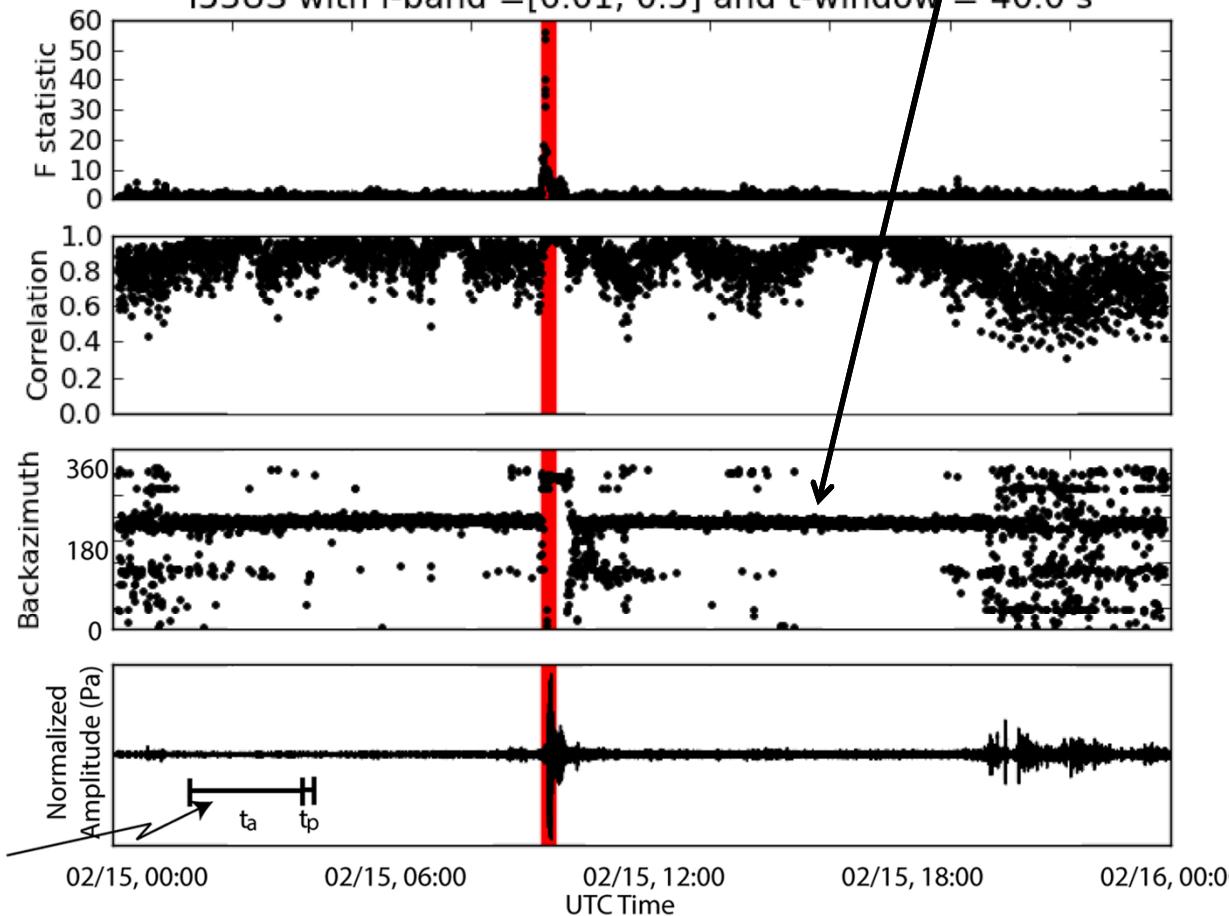
$F$  does not follow  $H_0$



Basic hypothesis:  $x_i(t) = s(t - \mathbf{r}_s \cdot \mathbf{u}_s) + n(t - \mathbf{r}_n \cdot \mathbf{u}_n) + w_i(t)$

Background coherence  
from oceans

I53US with f-band = [0.01, 0.5] and t-window = 40.0 s



$F / C$  follows  $H_0$

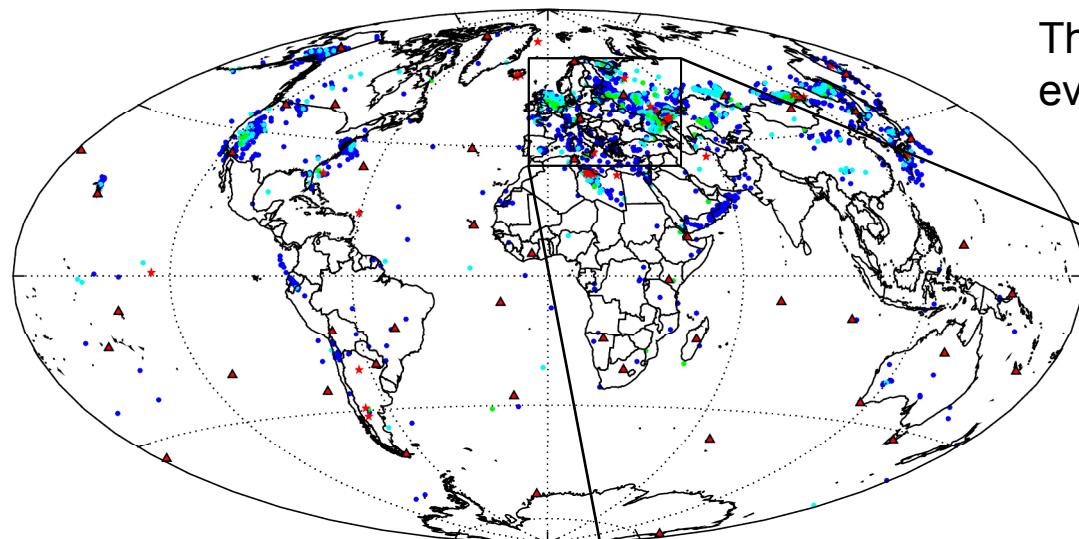
As shown by Shumway:  $F_{|H_0} \square F_{2BT, 2BT(N-1)\lambda} \approx CF_{2BT, 2BT(N-1)}$

## Infrasound Event Detection: Limitations

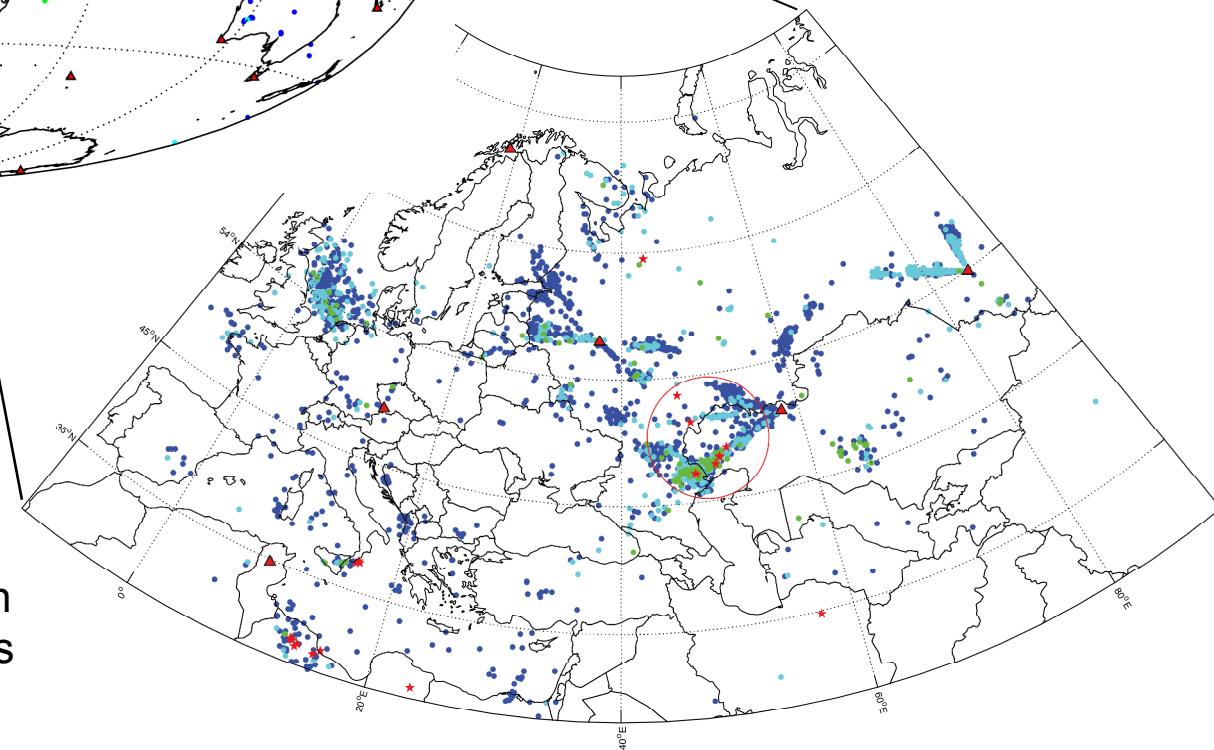


- Existing infrasound hypothesis tests are based on coherence only
- Post-processing is employed to sift through detections to identify possible explosion signals
  - Interesting signals could be associated at multiple arrays
  - Interesting signals may have certain characteristics at an individual array
- How might we identify explosion signals?
  - Explosions are broadband
  - Explosions have finite duration that typically increases with range
  - ...
- What about formulating detectors that exploit these properties from the outset?

## A Dataset for Testing some improvements

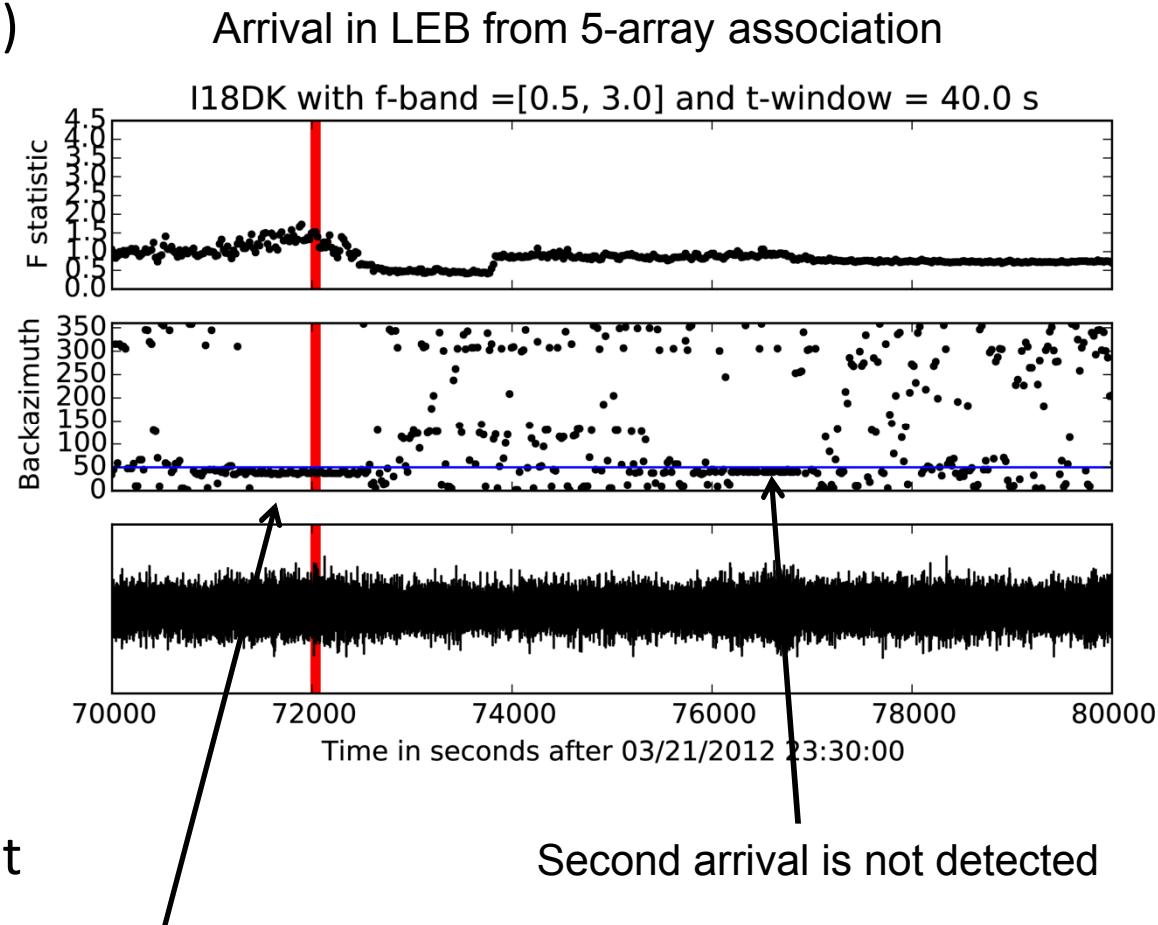


The largest density of infrasound events in the LEB is in Eurasia



# The need for detector improvements

- Adaptive F detector (AFD) insensitive to coherent noise but can miss low SNR signals.
- Can we combine the AFD with additional constraints to lower the detection threshold, while preserving the advantages of the AFD?
- Initial testing of a simple 'Hough-like' (line) detector
- Initial testing of Fishers Combined Probability test



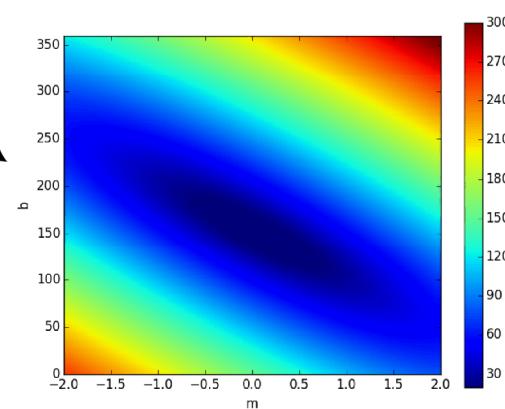
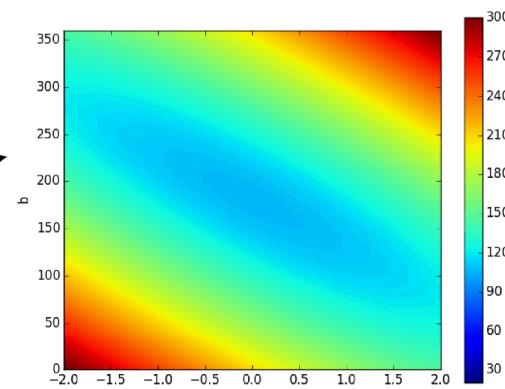
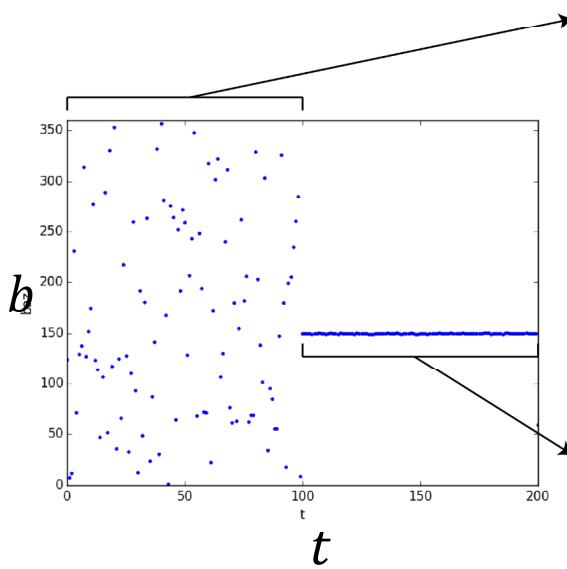
Consistent backazimuth over some time interval  
but weak F-statistic barely above ambient

# A 'Hough-like' detector



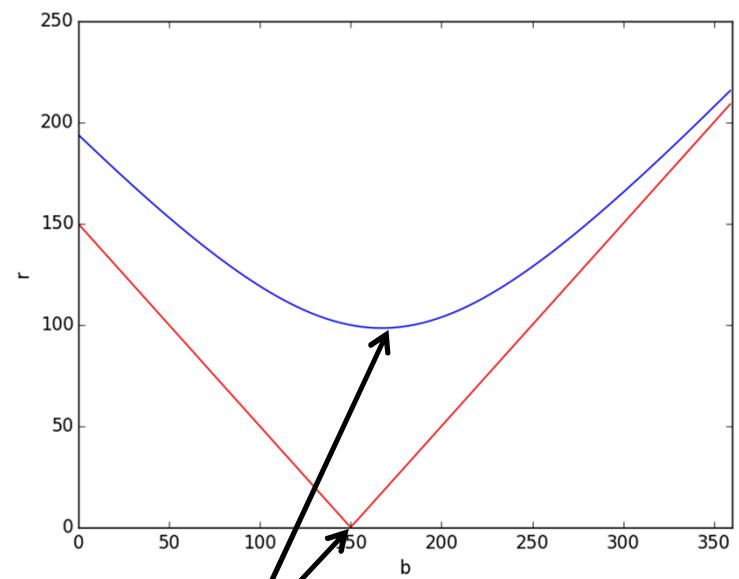
Detecting lines in backazimuth, time space:

Model:  $y_{pi} = mt_i + b$     Residual:  $r = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_{pi} - y_i)^2}$



At long distances, we only want to search for horizontal lines:

Model:  $y_{pi} = b$



$$r_{\min} = \min \left( \sqrt{\frac{1}{N} \sum_{i=1}^N (b - b_i)^2} \right)$$
$$b \in [0, 360]$$

# Combining detectors



How to combine detections from different detectors?

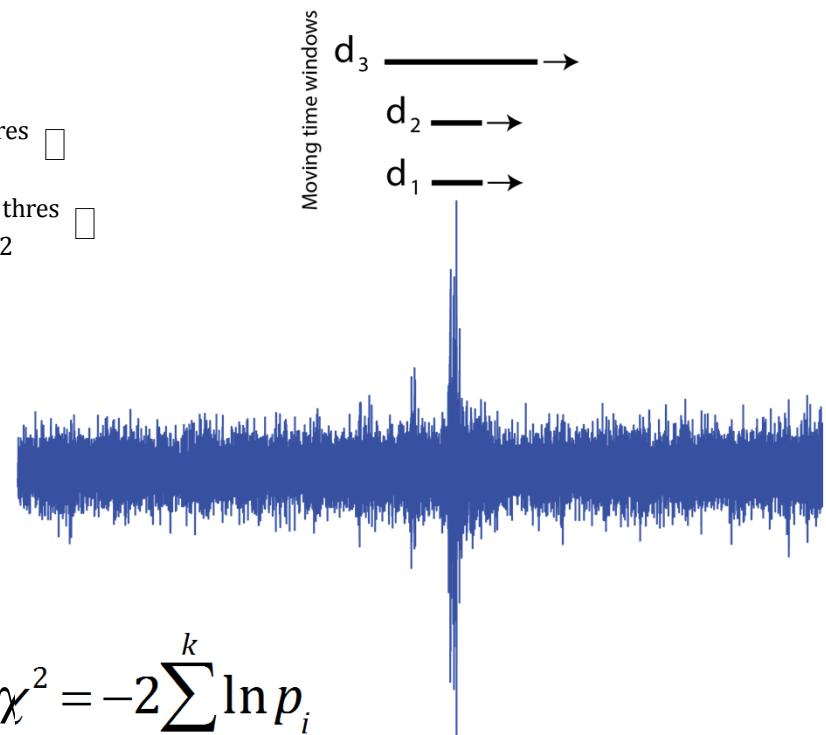
- Logical
  - Doesn't fully exploit the combined effects of two detectors
- Arithmetic
  - Doesn't use noise distribution information
- Fishers Combined Probability Test
  - Uses distributional properties of  $H_0$
  - requires a probability model
- ...

$$\begin{aligned} d_1 > d_1^{\text{thres}} \text{ OR } d_2 > d_2^{\text{thres}} & \square \\ d_1 > d_1^{\text{thres}} \text{ AND } d_2 > d_2^{\text{thres}} & \square \end{aligned}$$

$$\sum_{i=1}^k w_i d_i > \text{thres}$$

$$p_i = \int_{d_i}^{\infty} p(x; H_0) \quad \chi^2 = -2 \sum_{i=1}^k \ln p_i$$

Moving time windows

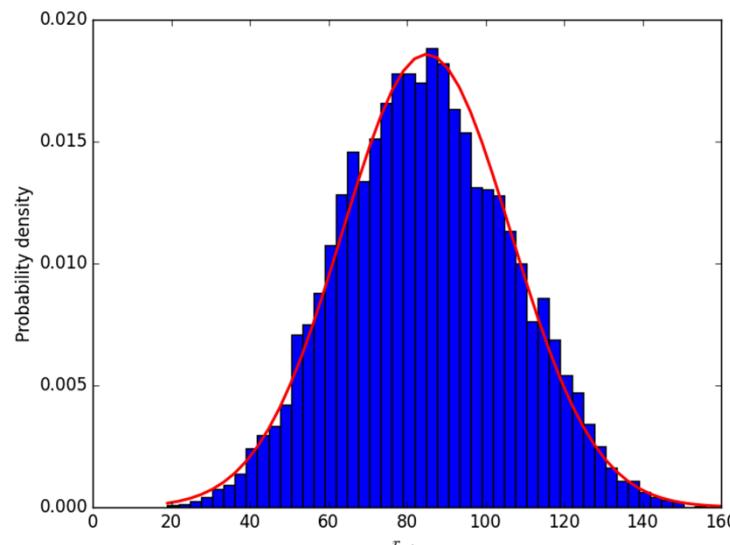


Detectors should ideally exploit different signal characteristics

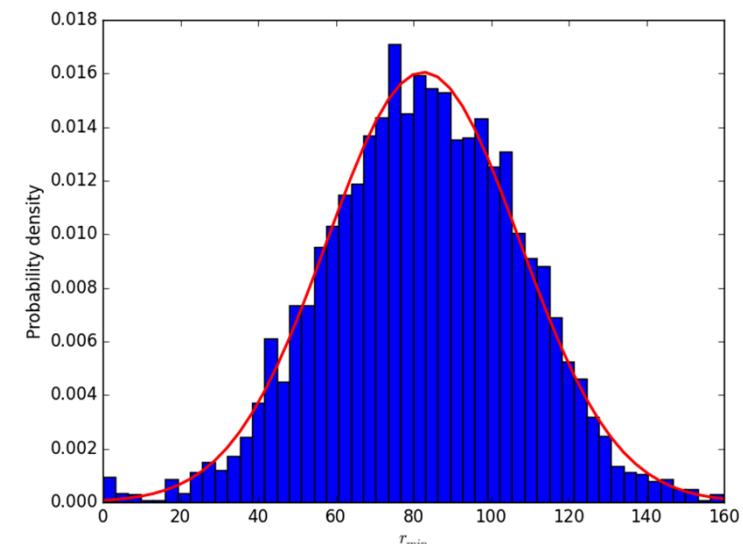
# Fishers Combined Probability Test

Distributional properties of

$$r_{\min} = \min \left( \sqrt{\frac{1}{N} \sum_{i=1}^N (b - b_i)^2} \right)$$

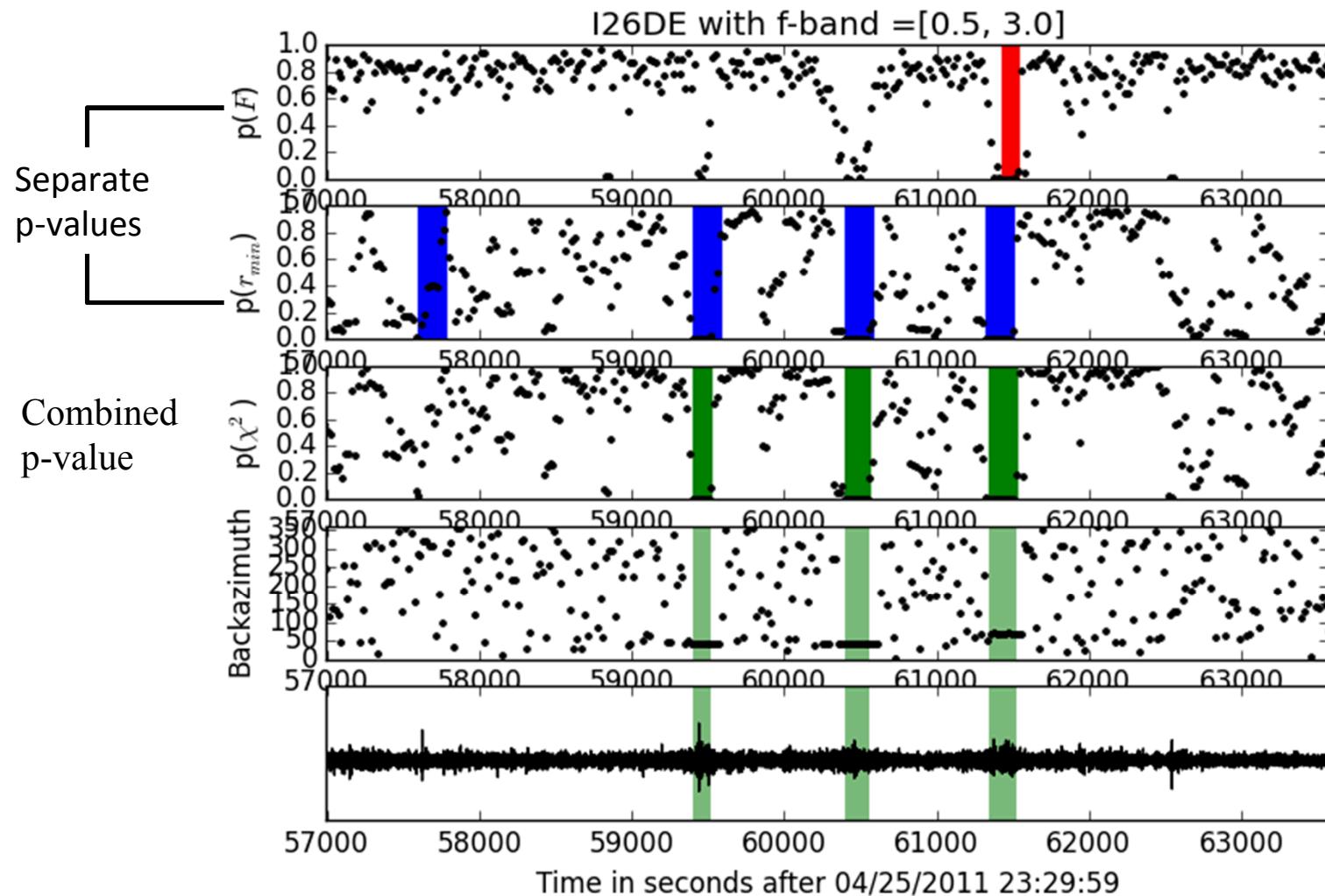


Uniformly distributed noise  
 $U[0, 360]$



1-day interval at I26DE

# An initial multivariate detector result



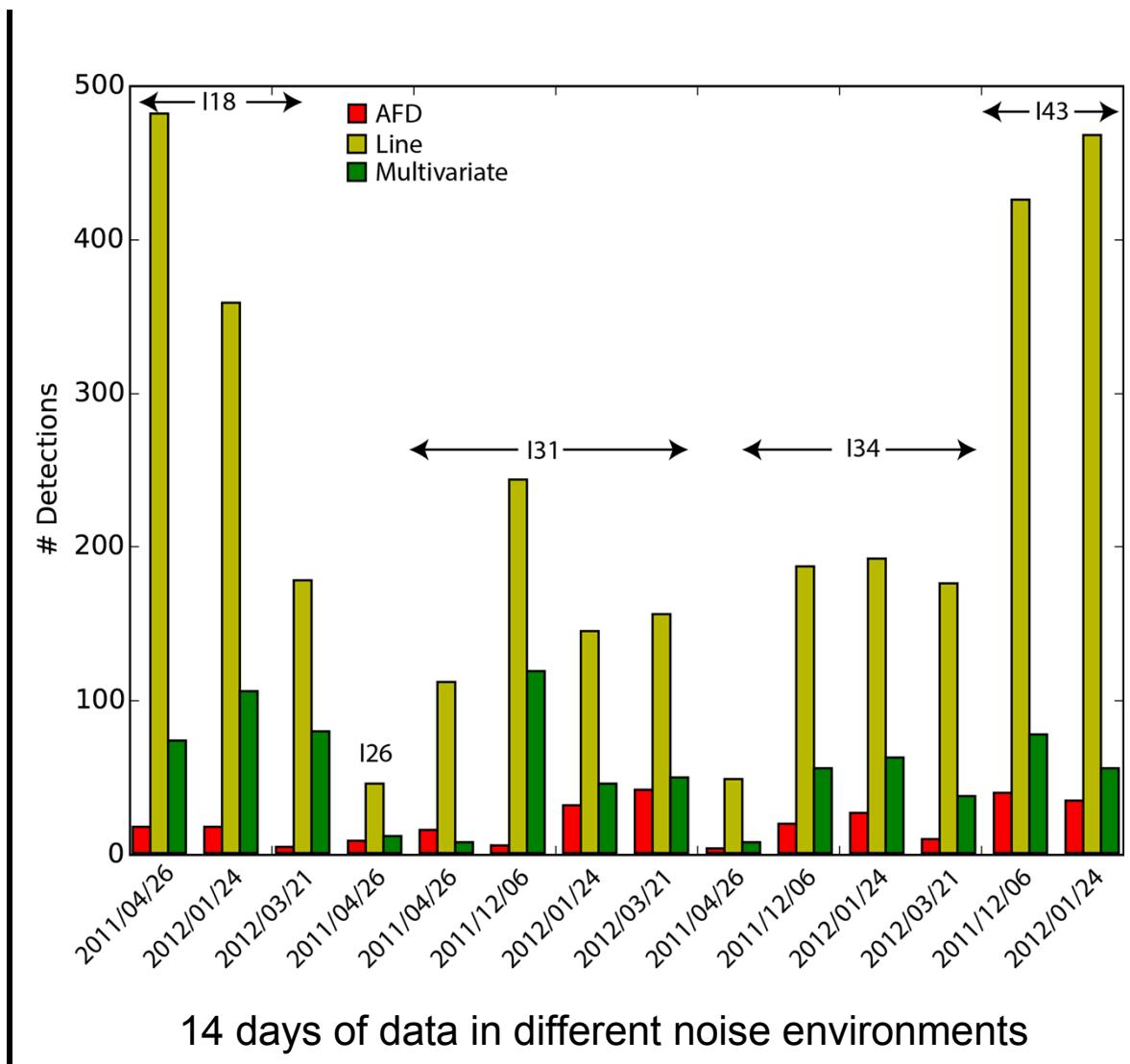
Combining AFD and line detector results in a much stronger detection of the first arrival, and weak detection of the second arrival.

# Some initial detection statistics

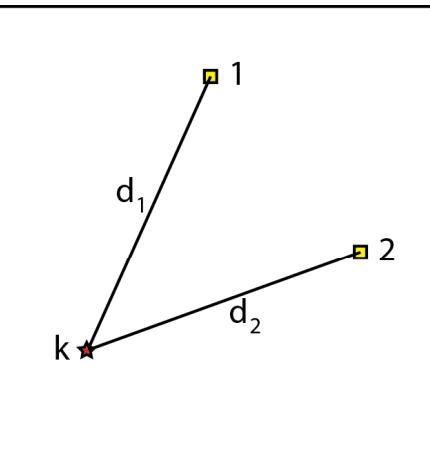
Detections of LEB arrivals  
from test events

# detections	Catalog
17	LEB
13	AFD
15	Multivariate

- Multivariate detector find two LEB arrivals from AFD
- Missing two arrivals are not observed in broadband FK processing



# Association



Forward model observations for each grid node...

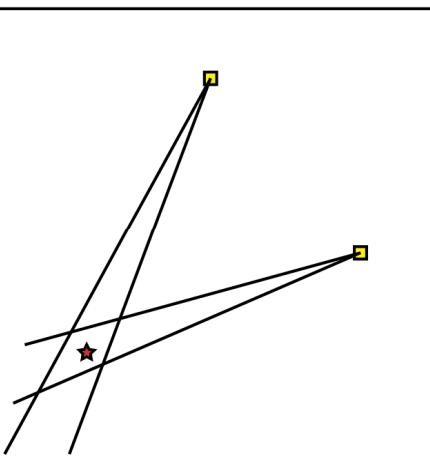
$$\Phi_k = (\phi_1^k, \phi_2^k, \dots) \quad dT_{\max}^k = \left[ \frac{(d_1 - d_2)}{v_{\min}}, \frac{(d_1 - d_3)}{v_{\min}}, \dots \right] \quad dT_{\min}^k = \left[ \frac{(d_1 - d_2)}{v_{\max}}, \frac{(d_1 - d_3)}{v_{\max}}, \dots \right]$$

Loop over GRID NODES...

- Find detection pairs that are compatible
- Cluster detection pairs based on ARID linkages

e.g., GA, InfraMonitor

Slower/greater memory load



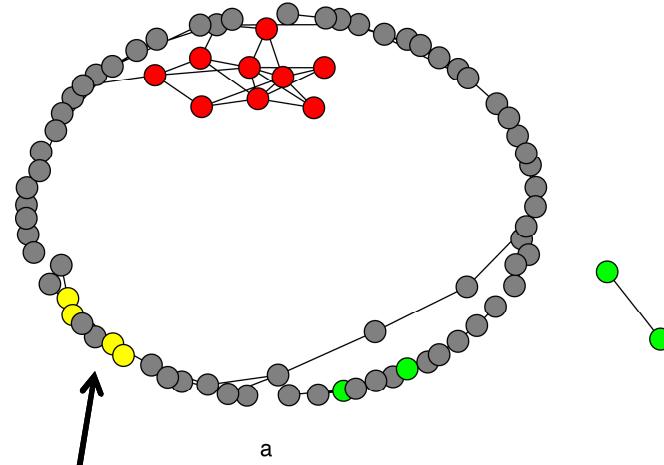
Loop over DETECTION PAIRS...

- Find detection pairs that are compatible
- Cluster detection pairs based on ARID linkages
- Process cluster (or 'graph') using physical criteria
- Search for associated signals at remaining arrays

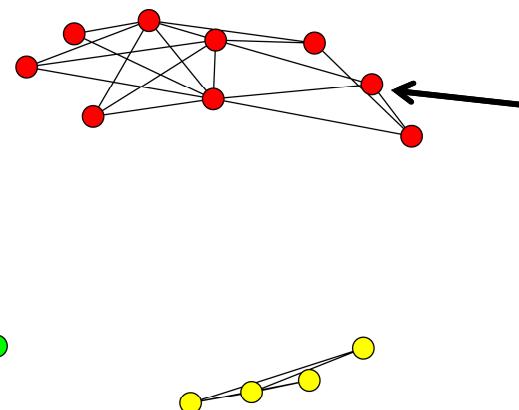
e.g., CEA algorithm, InfraPy

Existing methods fall under two basic categories. Criteria are basically azimuth/time but GA may include additional empirical constraints

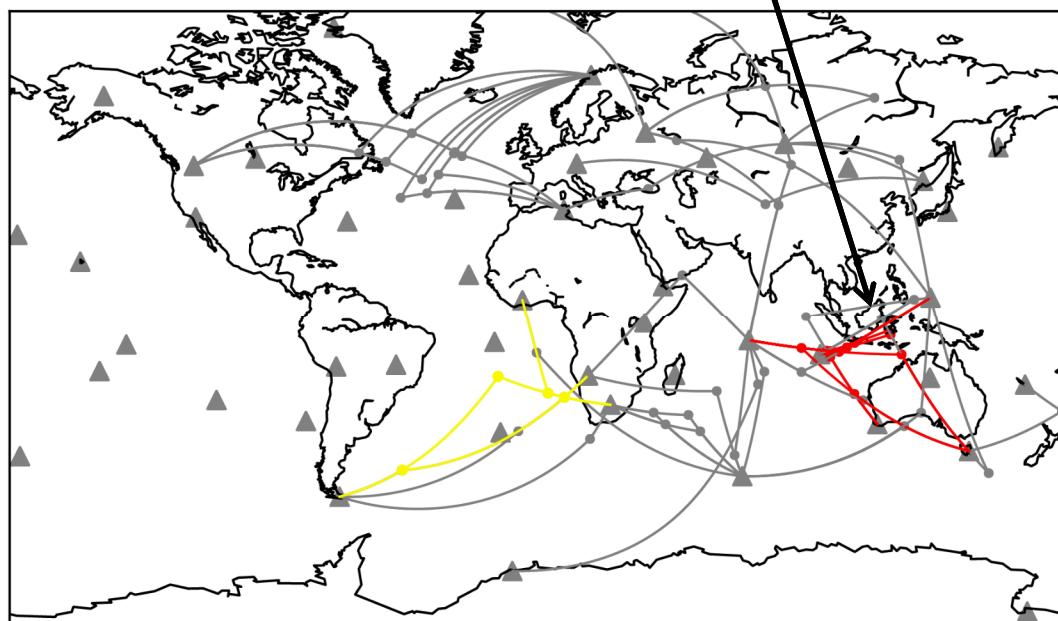
## Association – Looping over detection pairs



Compatible detection pairs plotted as 16 separate graphs. Three graphs are highlighted separately.

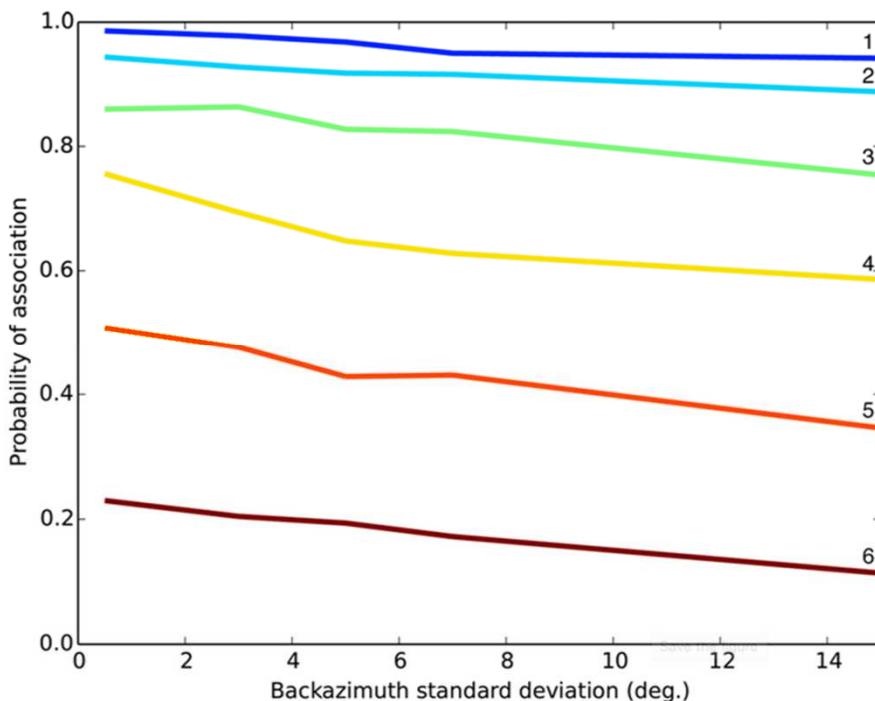


Eruption of Kelud  
volcano

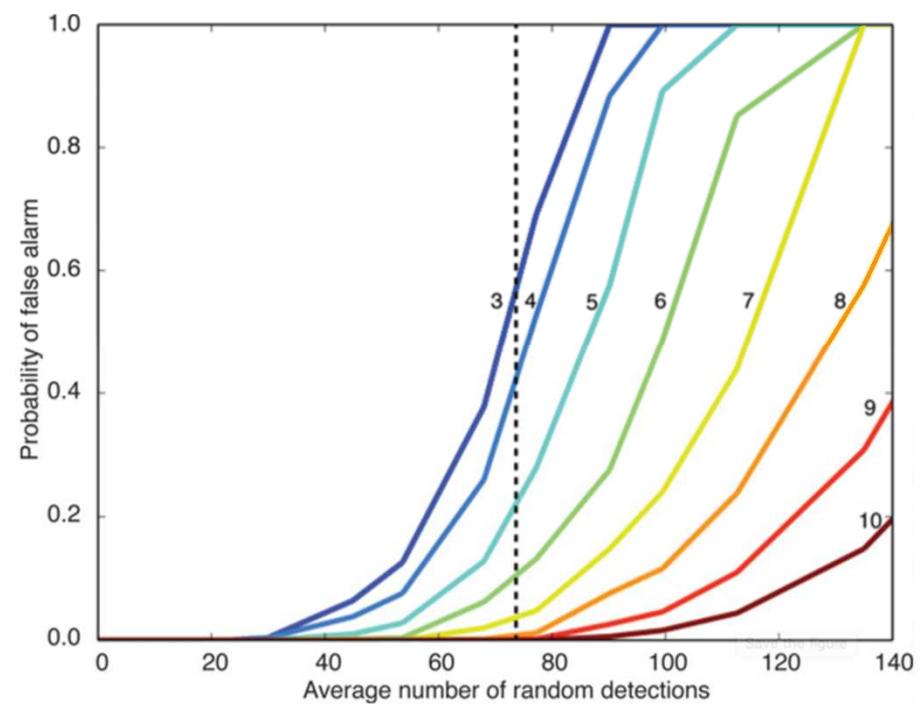


The geographic consistency of each graph is used to develop a robust event hypothesis

# Association synthetic tests

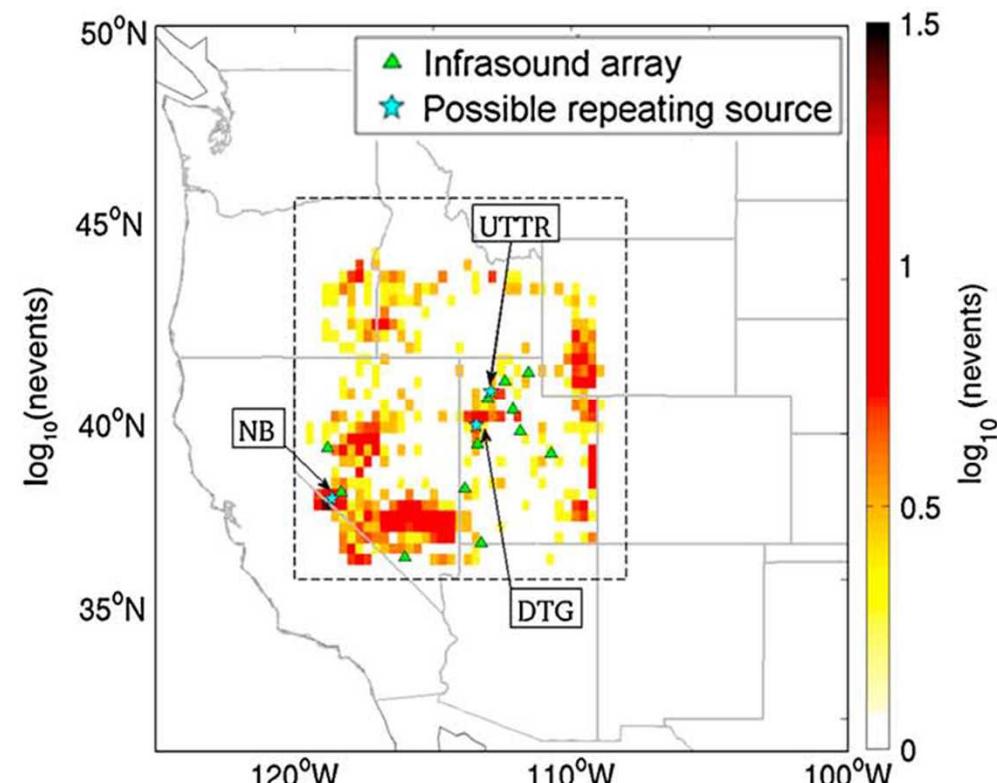
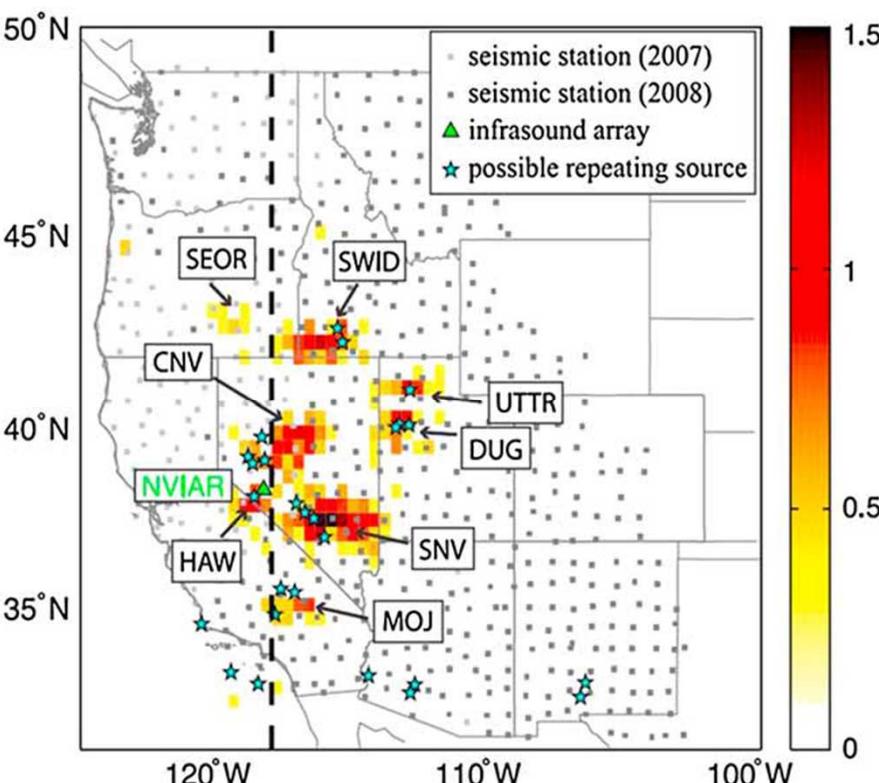


Probability of association (1 = all synthetic events associated, 0 = no synthetic events associated) as a function of event size (# of detecting stations) and noise added to backazimuths



Probability of false association as a function of event size (# of detecting stations) and # of detections

## Association – Looping over grid nodes



Comparison between reverse-time migration on 100's of seismic sensors (left) and node-based association results using 12 infrasound arrays (right)

## Summary



- Infrasound event detection is a challenging endeavor that has historically been hampered by the use of very simple models
- The main consequence of these simple models is a big false positive problem.
  - Moving towards more realistic signal and noise models should reduce the false positive problem
  - Adding physics-based constraints via propagation modeling should reduce the false positive problem at the network level.