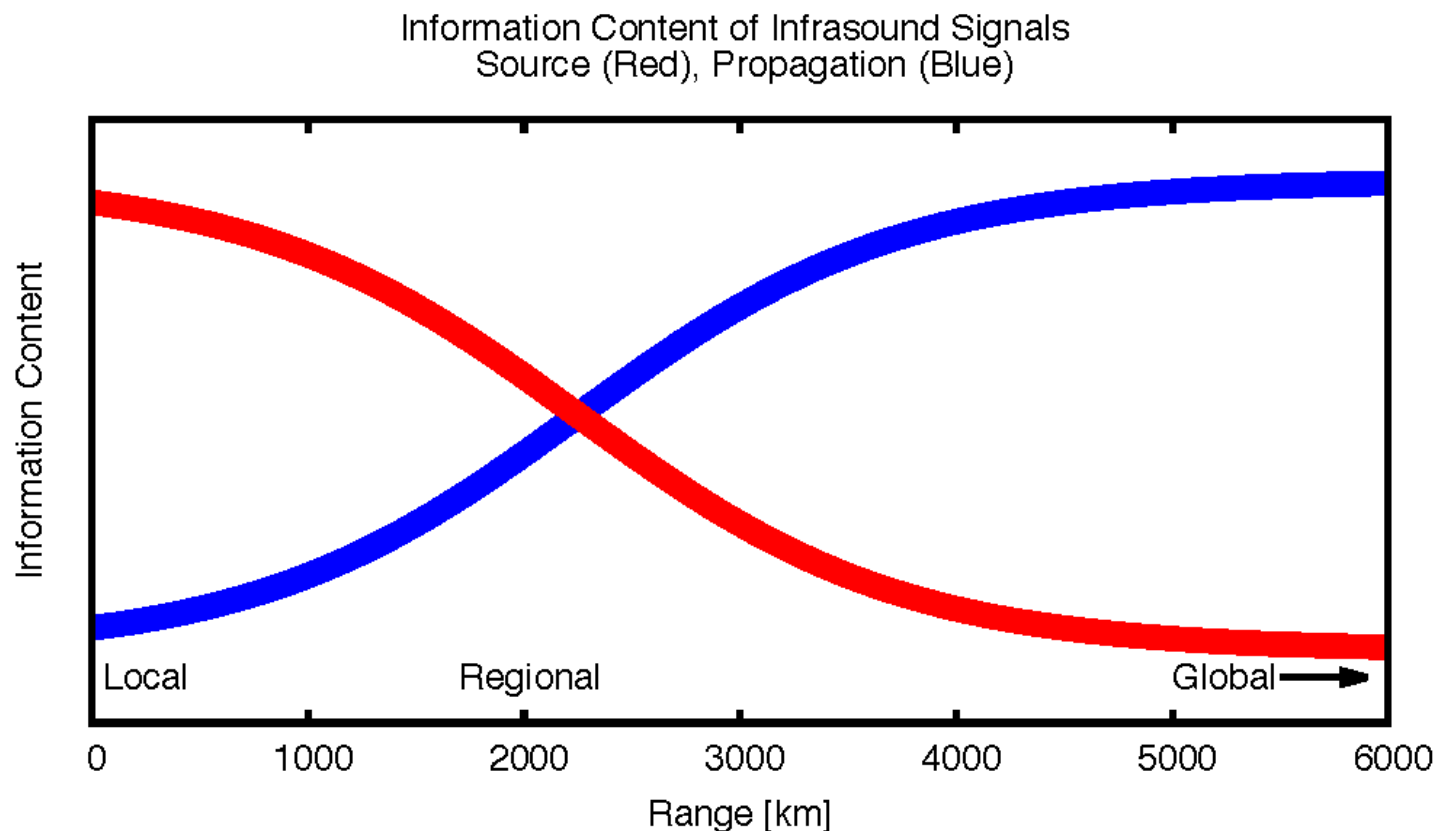


Infrasound Event Detection

Infrasound Event Detection



- An inherent assumption of global infrasound data processing is that there is little source information that is extractable at global distances.
- Thus, event detectors are based almost exclusively on coherence at arrays, and on agreement of arrival times and azimuths at spatially-separated arrays

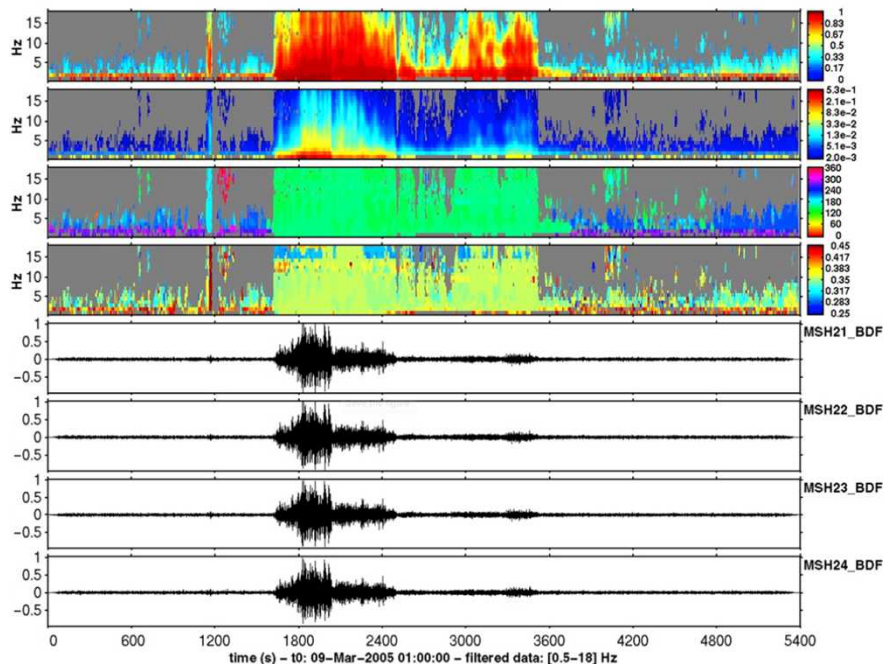
Infrasound Event Detection: PMCC

Ground-based Nuclear Explosion Monitoring R&D

Basic hypothesis: $x_i(t) = s(t - \mathbf{r} \cdot \mathbf{u}) + w_i(t)$

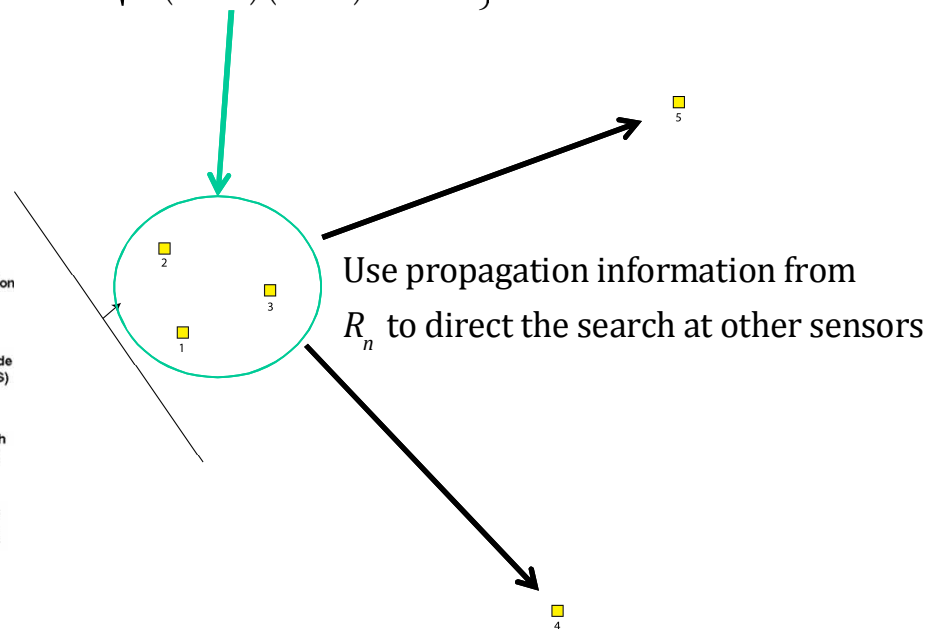
- 'Clutter' or 'correlated noise' under this definition is a signal
- Use of multiple narrowband filters to separate simultaneous signals in the f-domain
- Progressive -> Handles noisy channels
- Requires extensive post-processing

PMCC detections from the eruption of Mt. St. Helens.
Different colored pixels represent detections in time/frequency space.



$$r_{ijk} = \Delta t_{ij} + \Delta t_{jk} + \Delta t_{ki}$$

$$c_n = \sqrt{\frac{6}{n(n-1)(n-2)} \sum_{i>j>k} r_{ijk}^2} \quad \left. \vphantom{\sum_{i>j>k}} \right\} i, j, k \in R_n$$



Pixels are coalesced into families ('detections') using distance metrics

$$d(P_1, P_2) = \sqrt{\frac{\Delta t^2}{\sigma_t^2} + \frac{\Delta f^2}{\sigma_f^2} + \frac{\Delta v^2}{\sigma_v^2 v_2 v_1} + \frac{\Delta \theta^2}{\sigma_t^2}} < d_{\text{thres}}$$

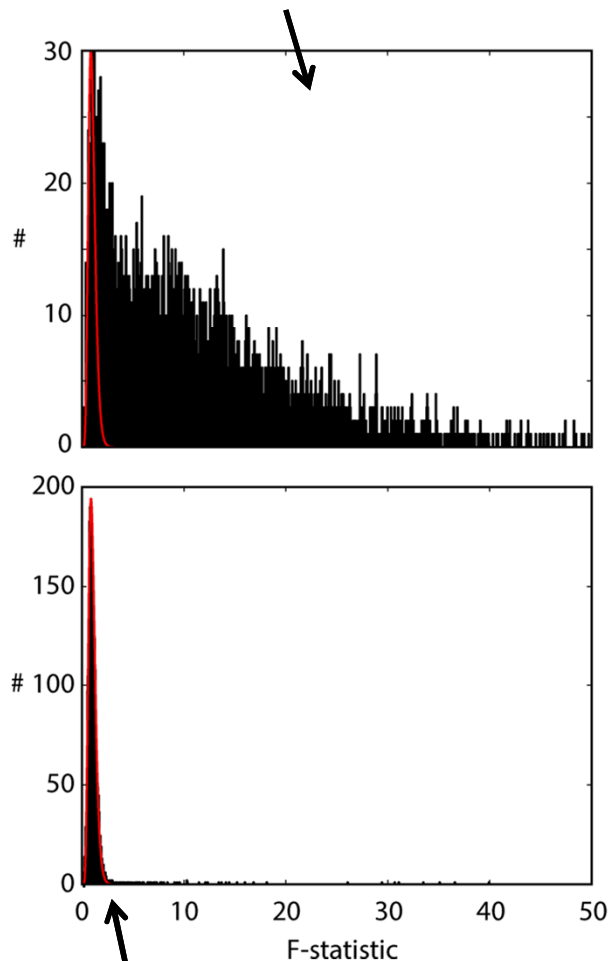
Infrasound Event Detection: AFD



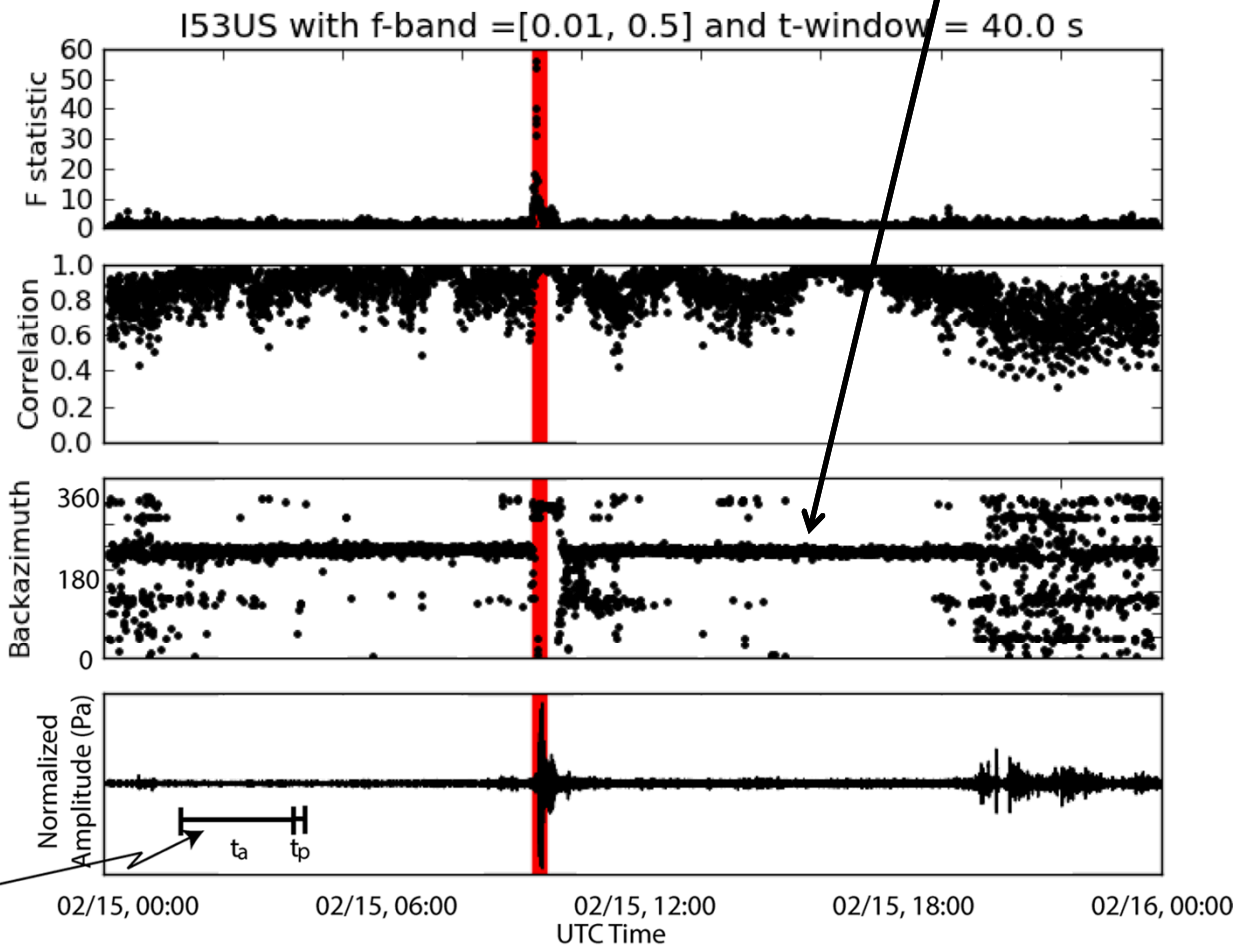
F does not follow H_0

$$\text{Basic hypothesis: } x_i(t) = s(t - \mathbf{r}_s \cdot \mathbf{u}_s) + n(t - \mathbf{r}_n \cdot \mathbf{u}_n) + w_i(t)$$

Background coherence from oceans



F/C follows H_0



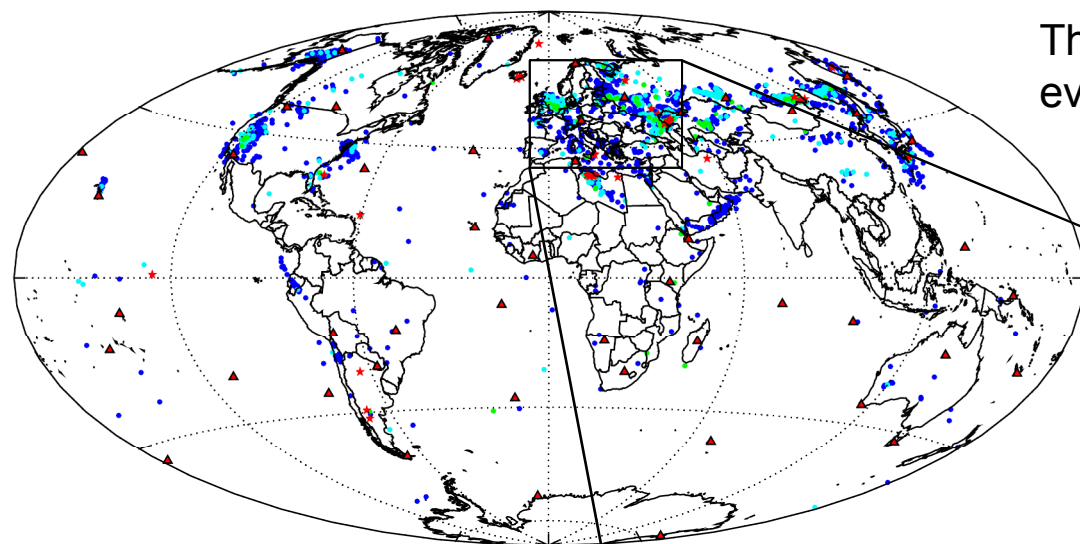
As shown by Shumway: $F_{|H_0} \square F_{2BT, 2BT(N-1)\lambda} \approx CF_{2BT, 2BT(N-1)}$

Infrasound Event Detection: Limitations

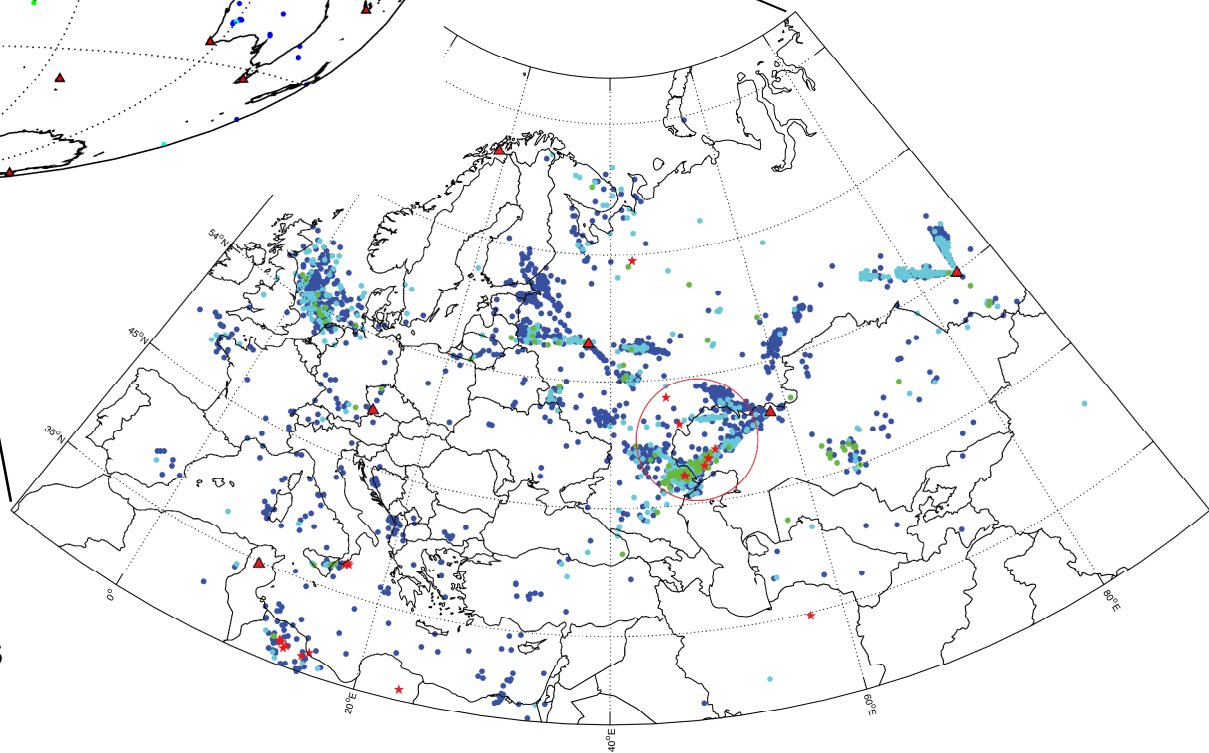


- Existing infrasound hypothesis tests are based on coherence only
- Post-processing is employed to sift through detections to identify possible explosion signals
 - Interesting signals could be associated at multiple arrays
 - Interesting signals may have certain characteristics at an individual array
- How might we identify explosion signals?
 - Explosions are broadband
 - Explosions have finite duration that typically increases with range
 - ...
- What about formulating detectors that exploit these properties from the outset?

A Dataset for Testing some improvements



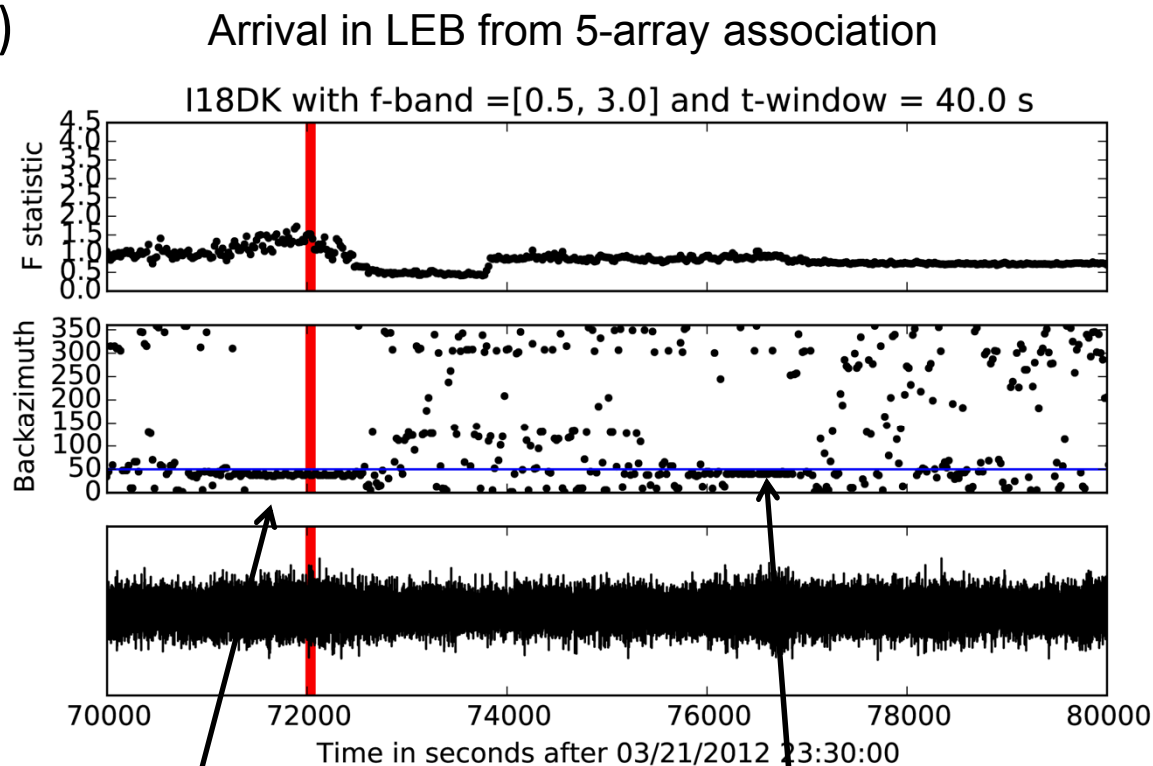
The largest density of infrasound events in the LEB is in Eurasia



8 events located near I31 are each recorded at 5 arrays -> Test events

The need for detector improvements

- Adaptive F detector (AFD) insensitive to coherent noise but can miss low SNR signals.
- Can we combine the AFD with additional constraints to lower the detection threshold, while preserving the advantages of the AFD?
- Initial testing of a simple 'Hough-like' (line) detector
- Initial testing of Fishers Combined Probability test



Consistent backazimuth over some time interval
but weak F-statistic barely above ambient

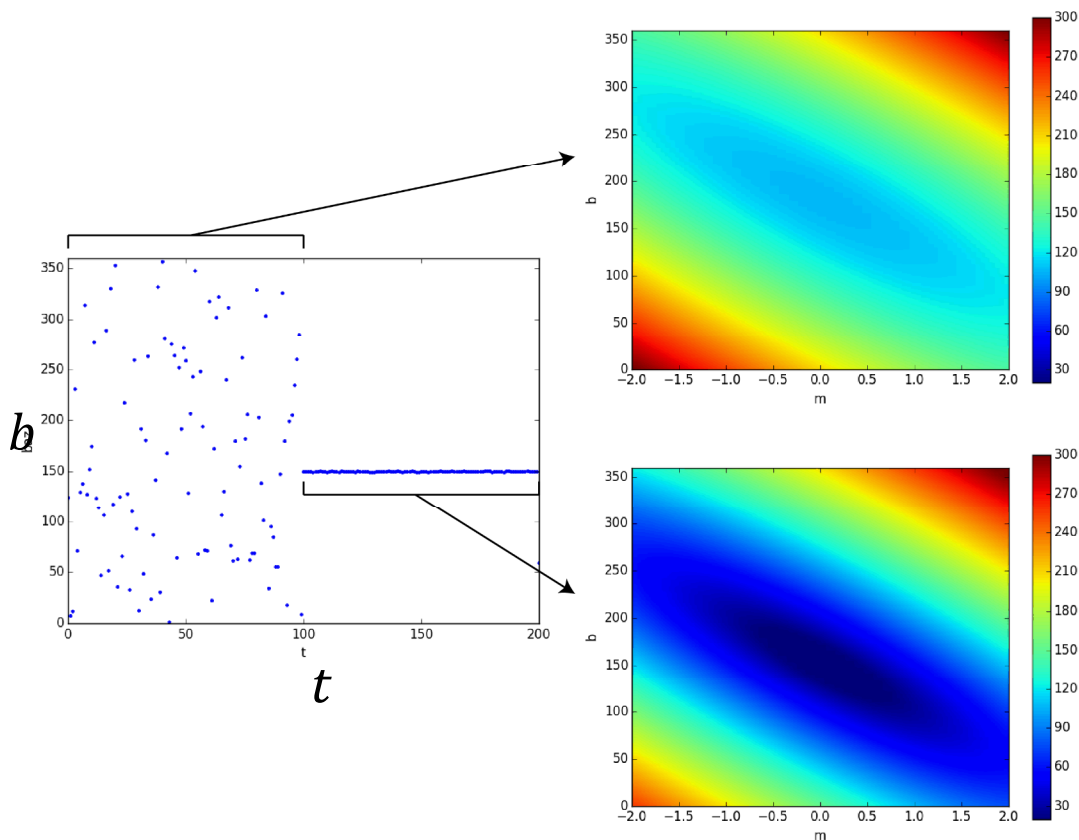
Second arrival is not detected

A 'Hough-like' detector



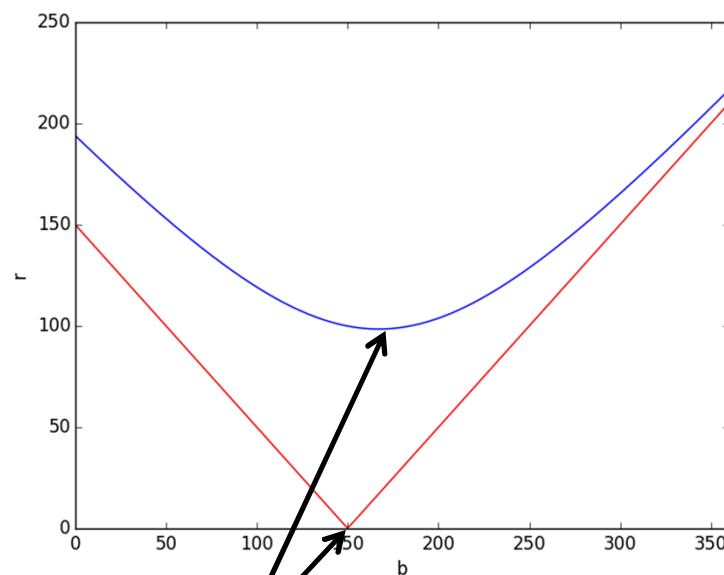
Detecting lines in backazimuth, time space:

Model: $y_{pi} = mt_i + b$ Residual: $r = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_{pi} - y_i)^2}$



At long distances, we only want to search for horizontal lines:

Model: $y_{pi} = b$



$$r_{\min} = \min \left(\sqrt{\frac{1}{N} \sum_{i=1}^N (b - b_i)^2} \right)$$

$$b \in [0, 360]$$

Combining detectors

How to combine detections from different detectors?

- Logical
 - Doesn't fully exploit the combined effects of two detectors

$$d_1 > d_1^{\text{thres}} \text{ OR } d_2 > d_2^{\text{thres}} \quad \square$$

$$d_1 > d_1^{\text{thres}} \text{ AND } d_2 > d_2^{\text{thres}} \quad \square$$

- Arithmetic
 - Doesn't use noise distribution information

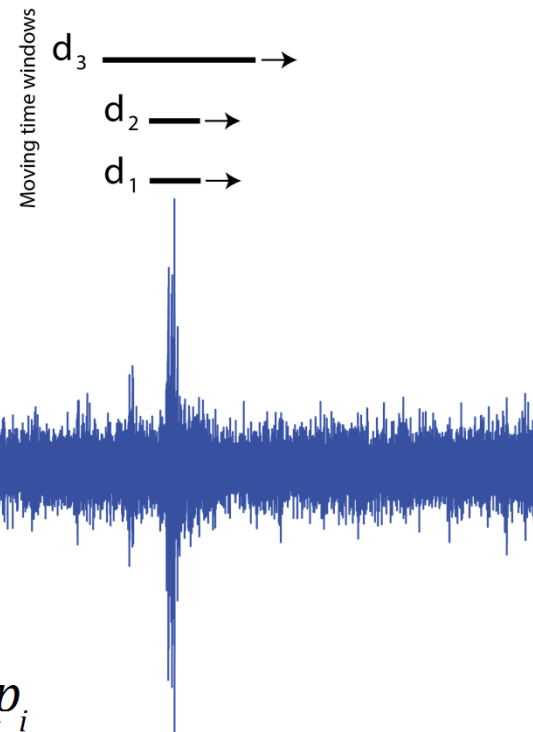
$$\sum_{i=1}^k w_i d_i > \text{thres}$$

- Fishers Combined Probability Test

- Uses distributional properties of H_0
- requires a probability model

$$p_i = \int_{d_i}^{\infty} p(\mathbf{x}; H_0) \quad \chi^2 = -2 \sum_{i=1}^k \ln p_i$$

- ...

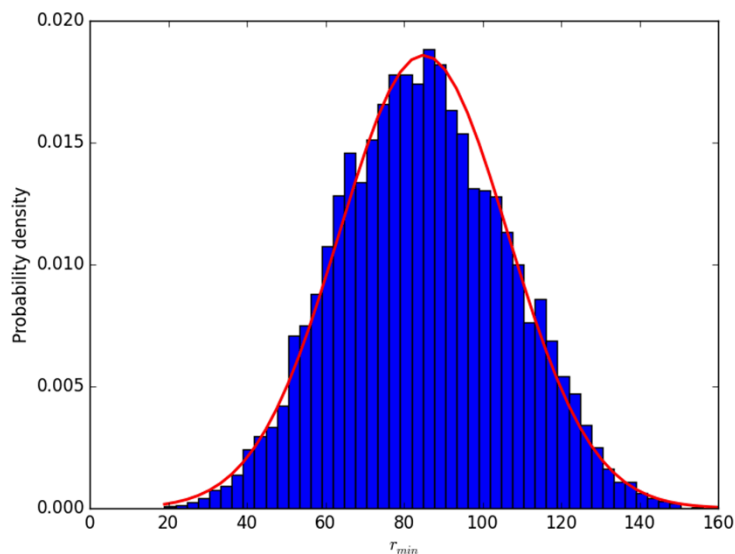


Detectors should ideally exploit different signal characteristics

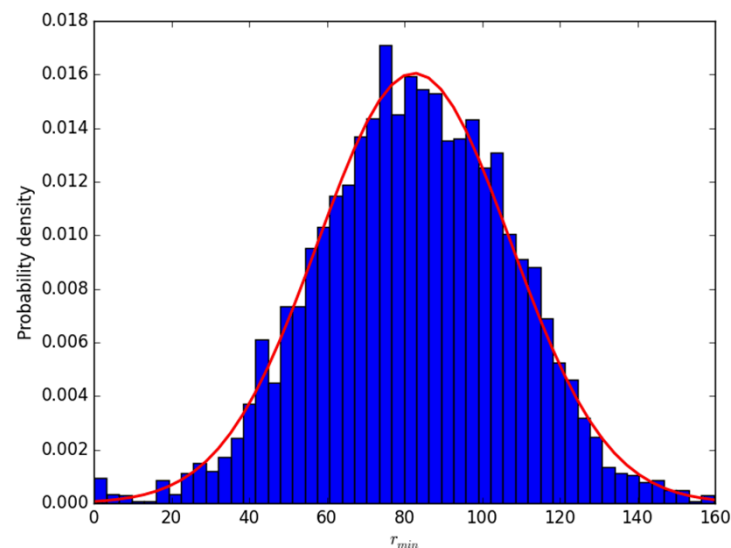
Fishers Combined Probability Test



Distributional properties of $r_{\min} = \min \left(\sqrt{\frac{1}{N} \sum_{i=1}^N (b - b_i)^2} \right)$

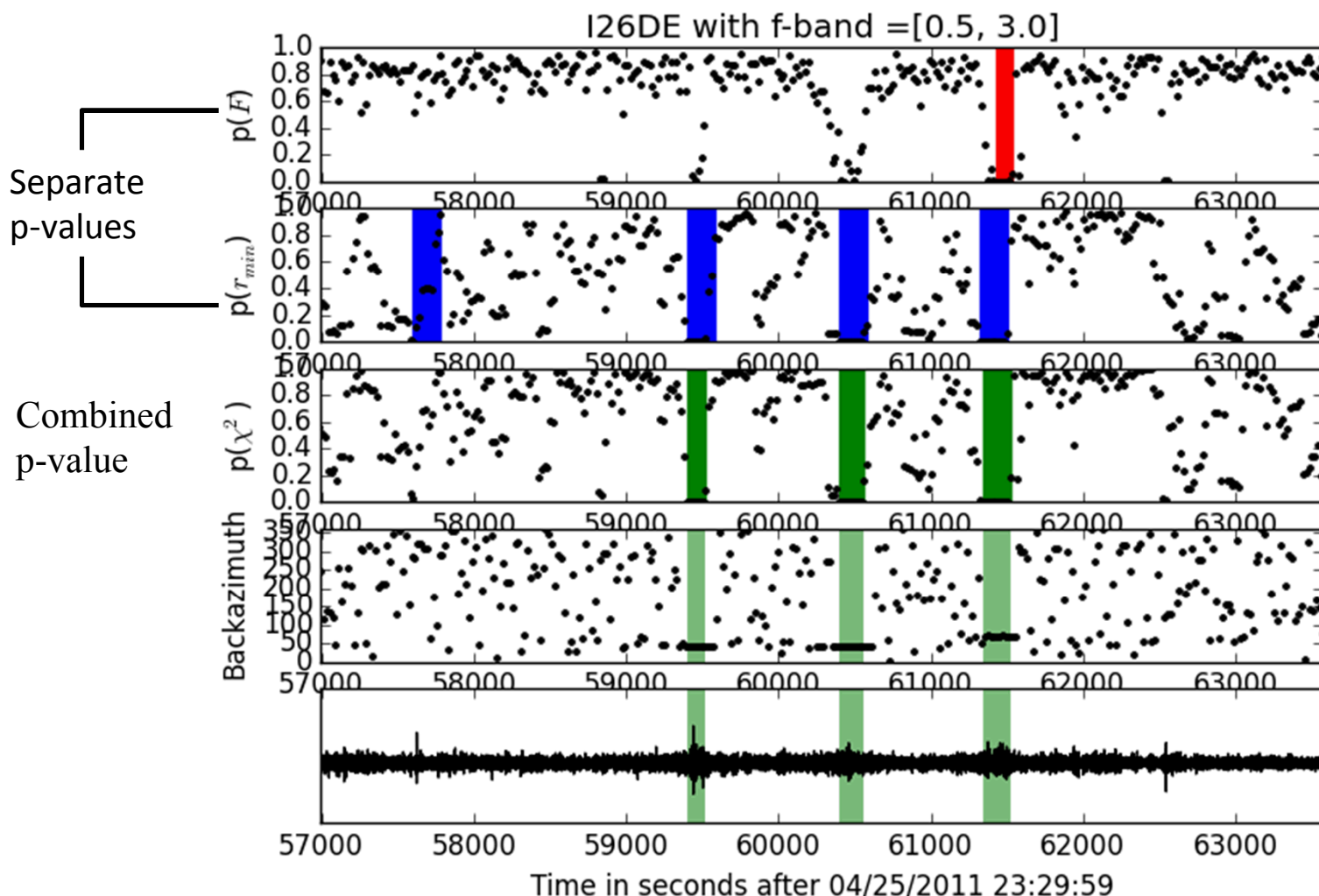


Uniformly distributed noise
 $U[0,360]$



1-day interval at I26DE

An initial multivariate detector result



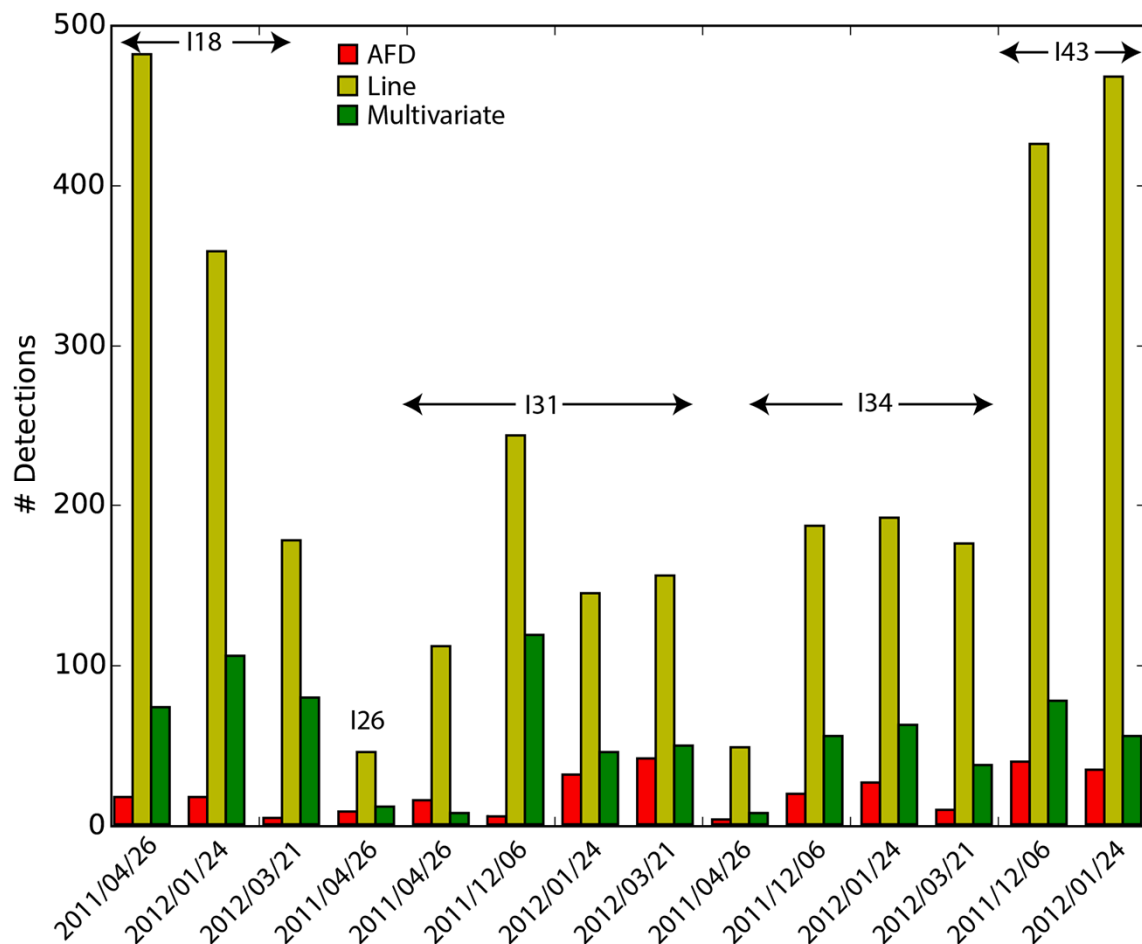
Combining AFD and line detector results in a much stronger detection of the first arrival, and weak detection of the second arrival.

Some initial detection statistics

Detections of LEB arrivals
from test events

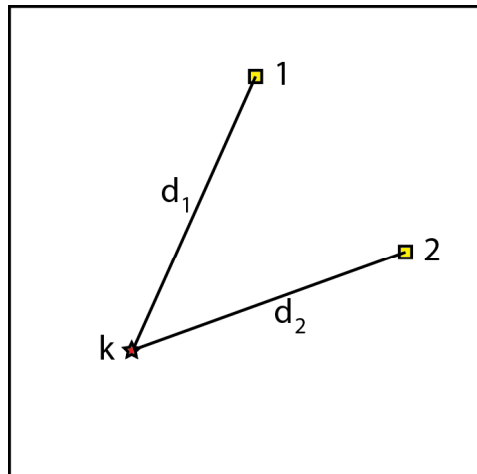
# detections	Catalog
17	LEB
13	AFD
15	Multivariate

- Multivariate detector find two LEB arrivals from AFD
- Missing two arrivals are not observed in broadband FK processing



14 days of data in different noise environments

Association



Forward model observations for each grid node...

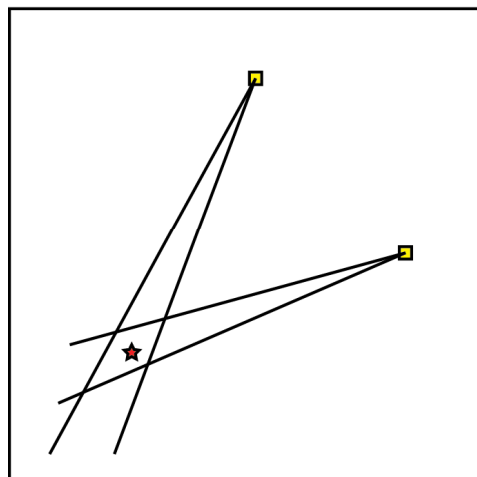
$$\Phi_k = (\phi_1^k, \phi_2^k, \dots) \quad dT_{\max}^k = \left[\frac{(d_1 - d_2)}{v_{\min}}, \frac{(d_1 - d_3)}{v_{\min}}, \dots \right] \quad dT_{\min}^k = \left[\frac{(d_1 - d_2)}{v_{\max}}, \frac{(d_1 - d_3)}{v_{\max}}, \dots \right]$$

Loop over GRID NODES...

- Find detection pairs that are compatible
- Cluster detection pairs based on ARID linkages

e.g., GA, InfraMonitor

Slower/greater memory load



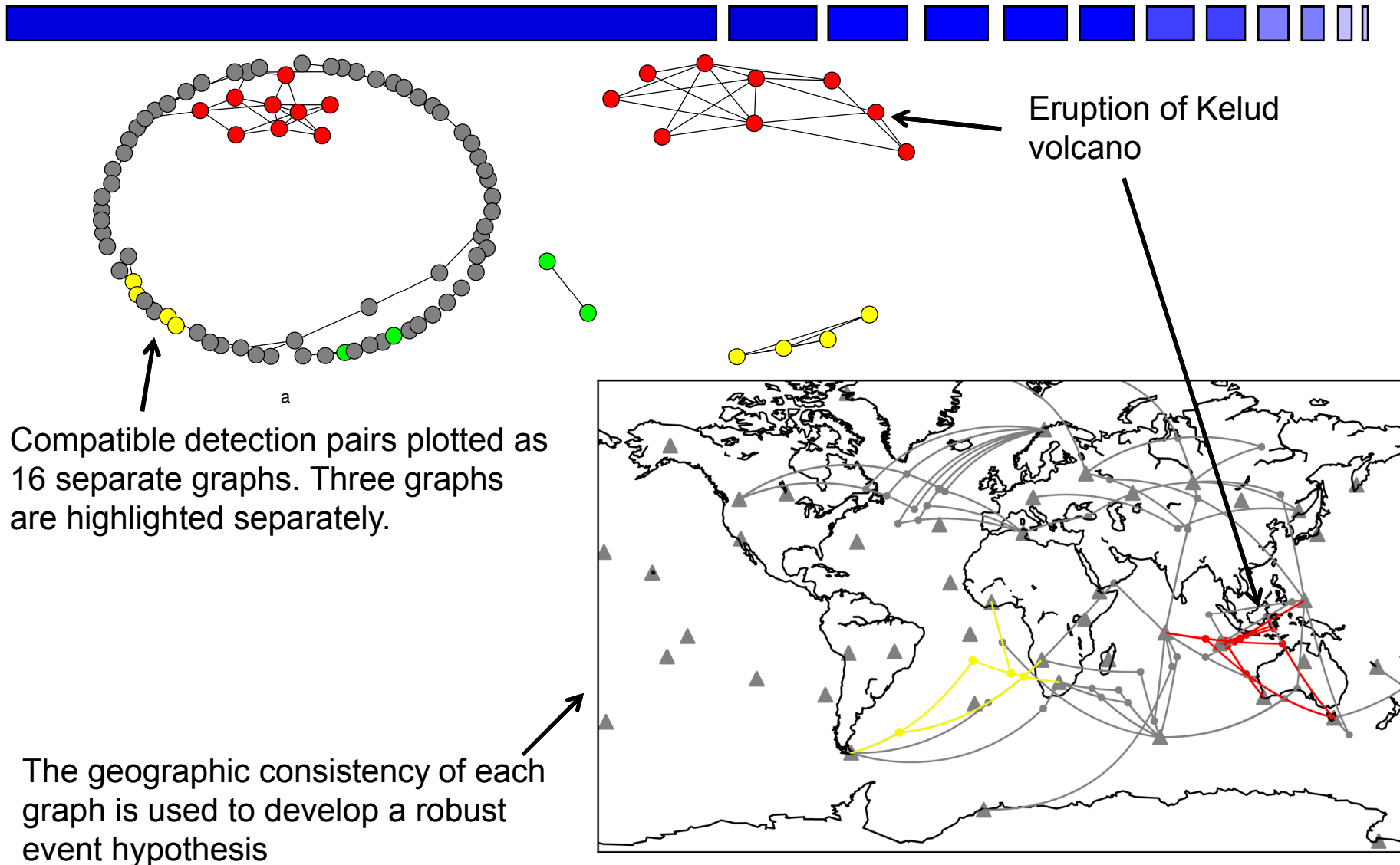
Loop over DETECTION PAIRS...

- Find detection pairs that are compatible
- Cluster detection pairs based on ARID linkages
- Process cluster (or 'graph') using physical criteria
- Search for associated signals at remaining arrays

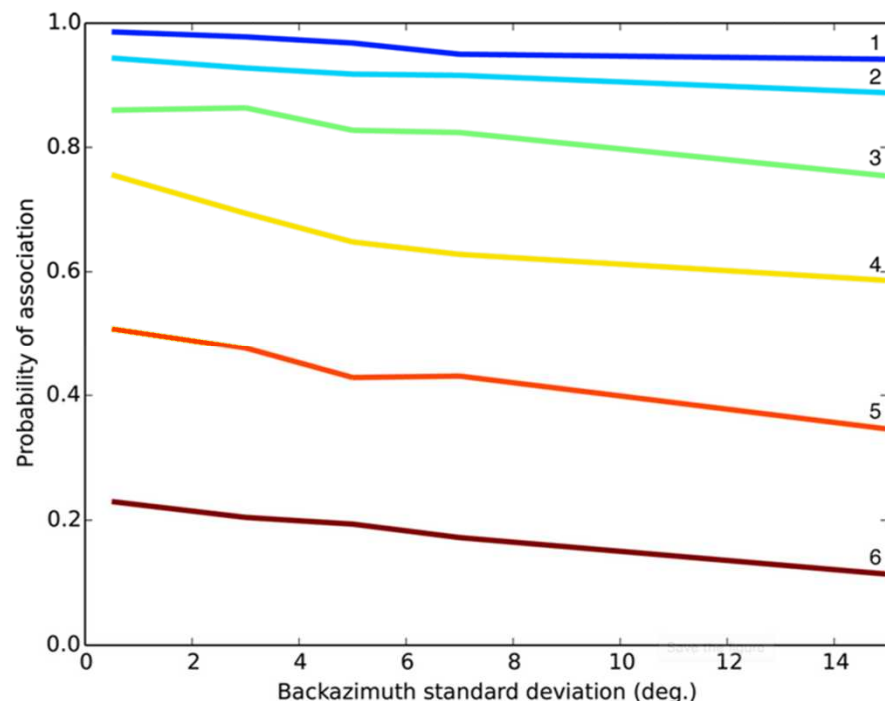
e.g., CEA algorithm, InfraPy

Existing methods fall under two basic categories. Criteria are basically azimuth/time but GA may include additional empirical constraints

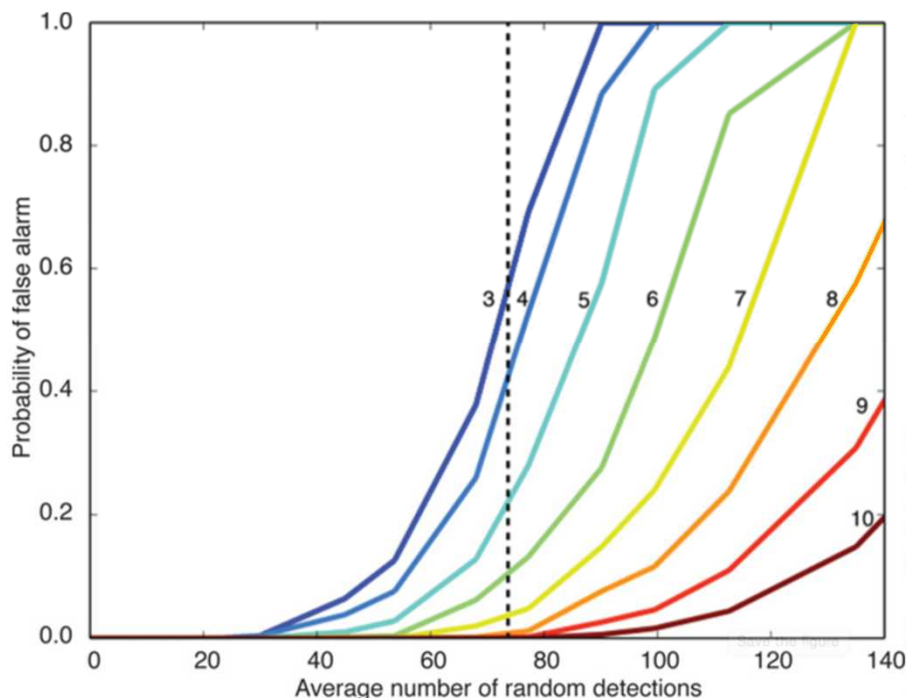
Association – Looping over detection pairs



Association synthetic tests

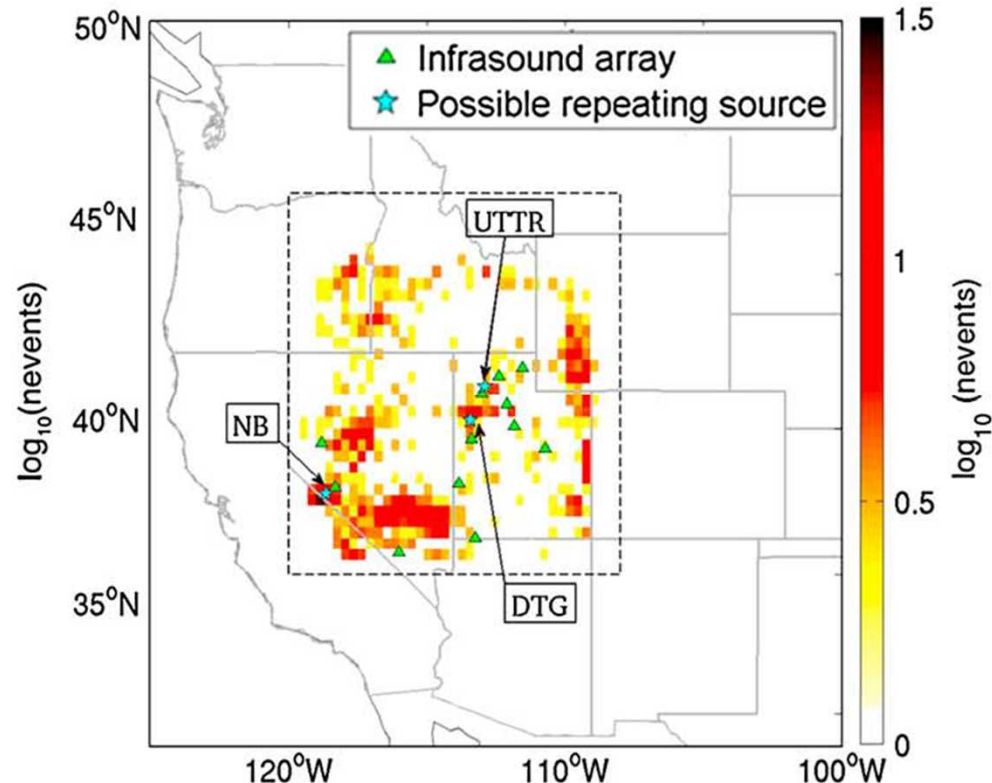
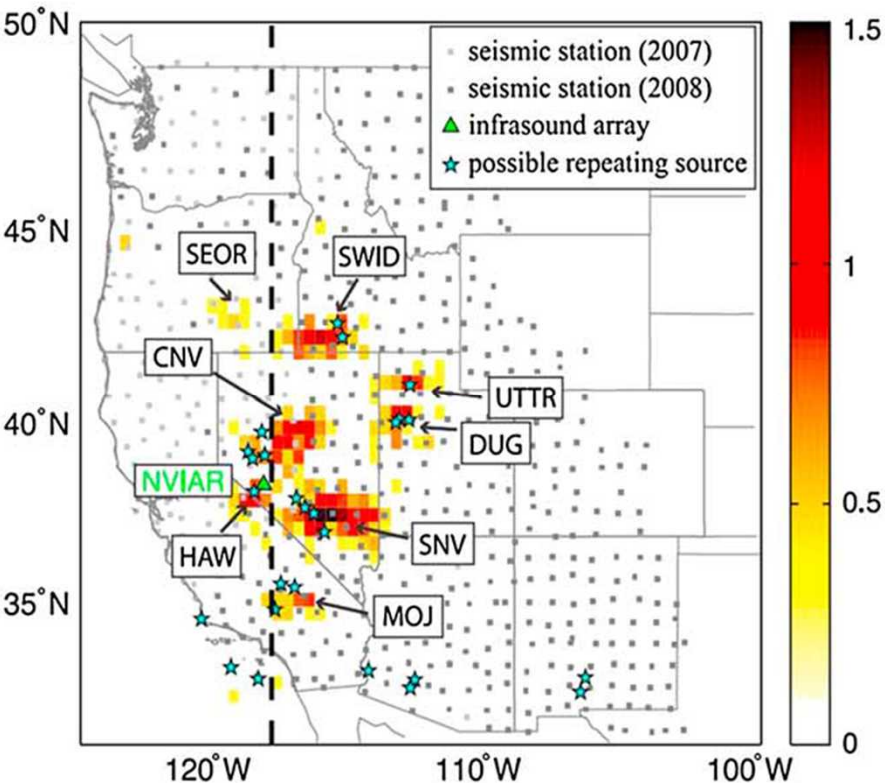


Probability of association (1 = all synthetic events associated, 0 = no synthetic events associated) as a function of event size (# of detecting stations) and noise added to backazimuths



Probability of false association as a function of event size (# of detecting stations) and # of detections

Association – Looping over grid nodes



Comparison between reverse-time migration on 100's of seismic sensors (left) and node-based association results using 12 infrasound arrays (right)

Summary



- Infrasound event detection is a challenging endeavor that has historically been hampered by the use of very simple models
- The main consequence of these simple models is a big false positive problem.
 - Moving towards more realistic signal and noise models should reduce the false positive problem
 - Adding physics-based constraints via propagation modeling should reduce the false positive problem at the network level.