

An Active Thevenin Equivalent Network Approach to EMI/EMC Problems

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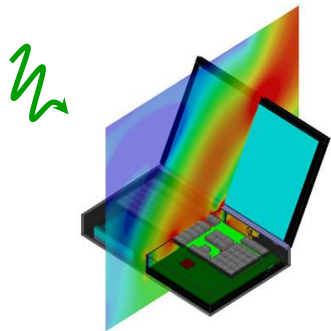
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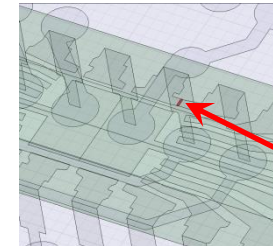
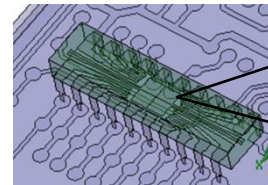
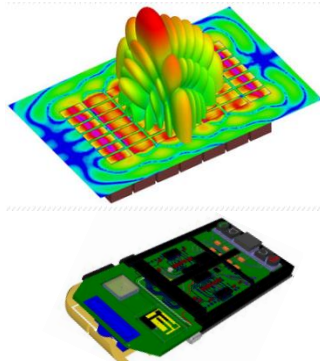
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EMI & IEMI Effects Process

Coupling

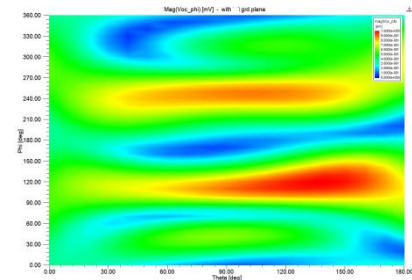


Energy Distribution



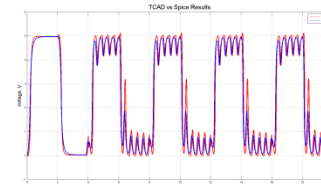
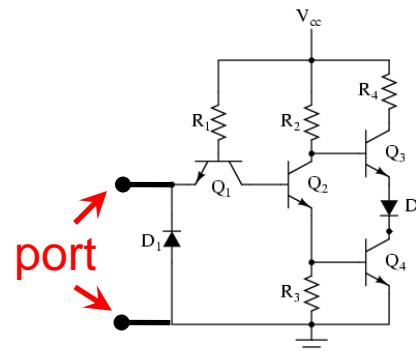
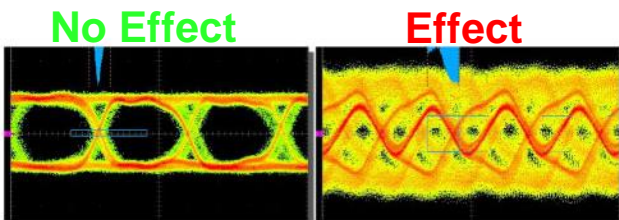
port

Device Response



available power at port

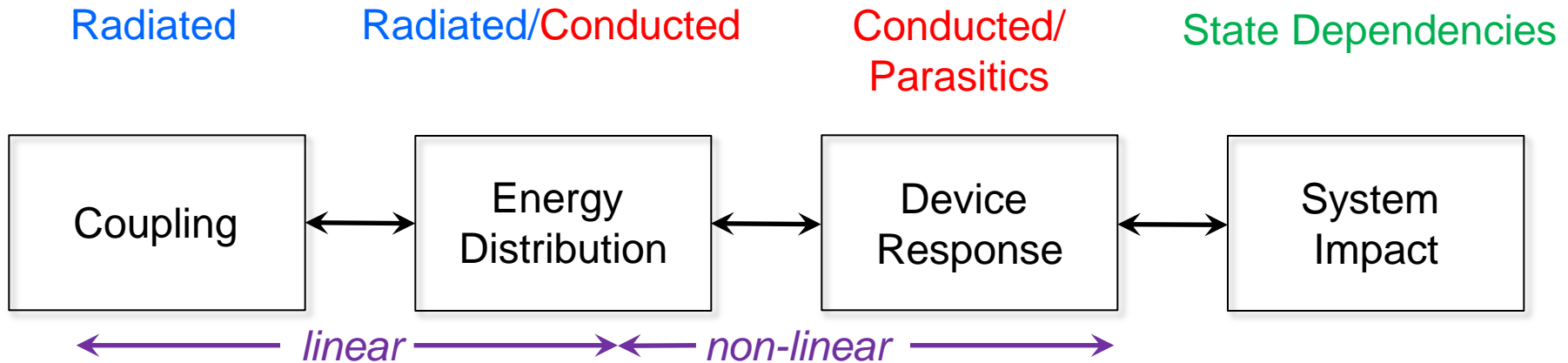
System Impact



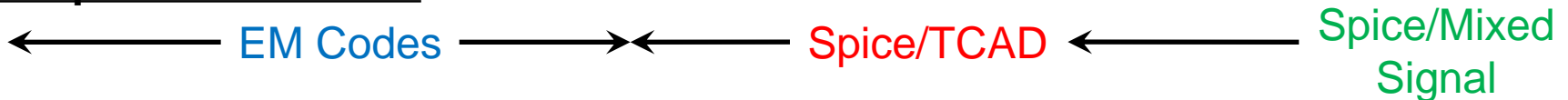
Computing EMI & IEMI Effects



Mechanisms:



Computational Tools:

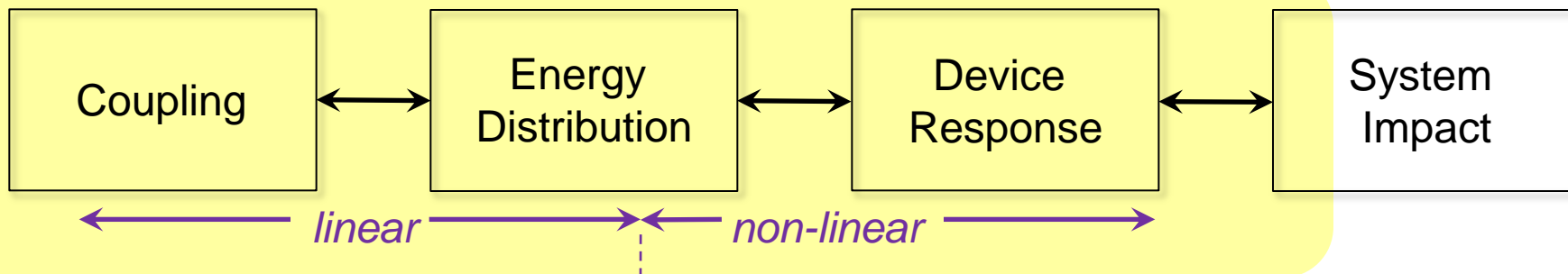
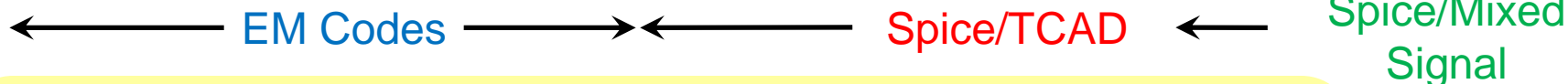


We need an efficient and accurate approach for linking these different computations together in a self-consistent manner.



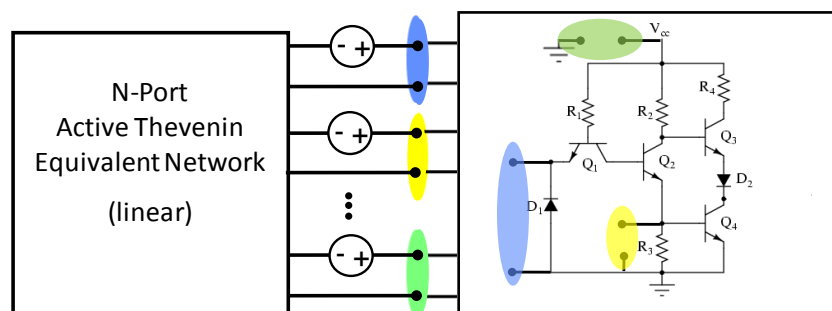
Our Approach: ATHENA

Computational Tools:



ATHENA

Active **T**Hevenin **E**quivalent **N**etwork Approach



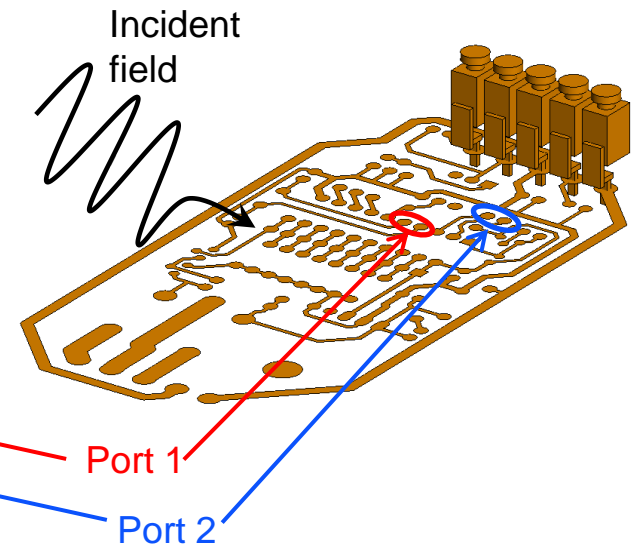
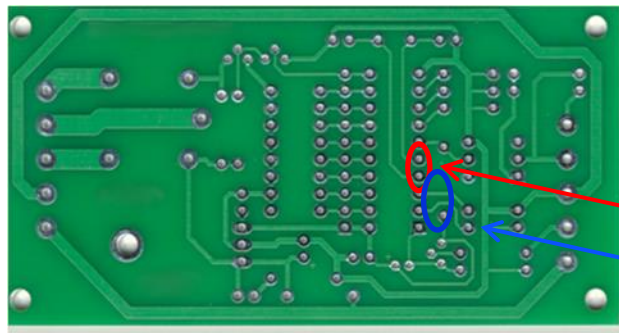
Circuit for demonstration only

Active Thevenin Equivalent Network

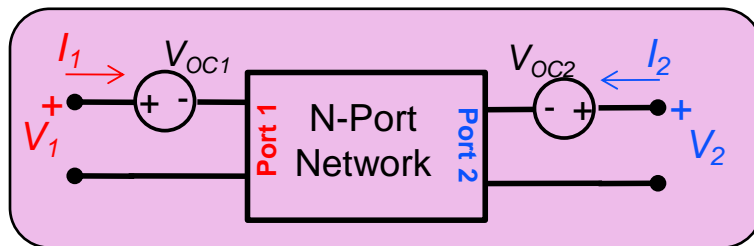


Ports are essentially terminal pairs defined at reference planes where quasi-static voltages and currents can be defined.

2-Port Example



Excluding the port loads, **linear** time or frequency domain EM simulators are used to determine the **open-circuit voltage** and **impedance parameters** at the ports.

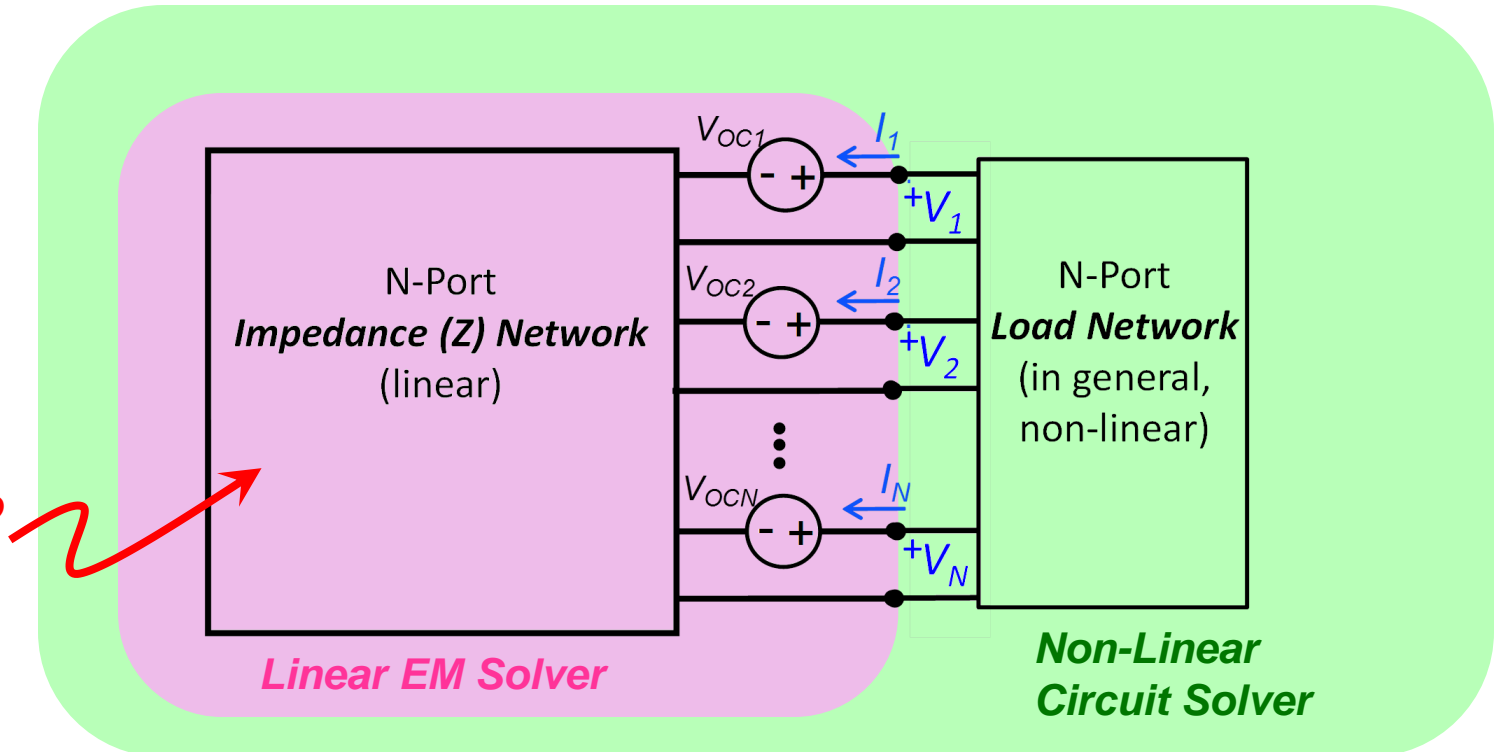


Active Thevenin Equivalent Network = “ATHENA device”

Coupling of ATHENA Device to a Load Network

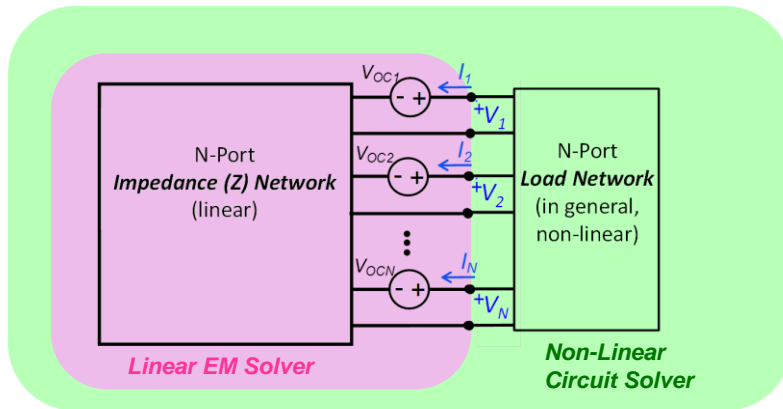


Only needs to be calculated once.



- Implicitly, for non-linear loads this coupling is performed in the time-domain. Hence, any frequency domain quantities have to be inverse-Fourier transformed to the time-domain.

Coupling of ATHENA Device to a Load Network



Using reciprocity, the open-circuit voltage at m^{th} -port due to a **p**-polarized, unit plane wave

$$V_m^{OC} = \frac{1}{j\omega\mu_0} (4\pi r e^{jk_0 r}) (\mathbf{p} \cdot \mathbf{E}_m^T(\theta, \phi))$$

Radiated field from unit current at port m.

Freq. Domain

$$[\mathbf{V}] = [\mathbf{Z}][\mathbf{I}] + [\mathbf{V}^{OC}]$$

Time Domain

$$[v(t)] = [z(t)] \otimes [i(t)] + [v^{OC}(t)]$$

Convolution operator

2-Port Example:

$$\begin{bmatrix} v_1(t) \\ v_2(t) \end{bmatrix} = \begin{bmatrix} \int_0^t z_{11}(t-\tau) i_1[v_1(\tau)] d\tau + \int_0^t z_{12}(t-\tau) i_2[v_2(\tau)] d\tau \\ \int_0^t z_{21}(t-\tau) i_1[v_1(\tau)] d\tau + \int_0^t z_{22}(t-\tau) i_2[v_2(\tau)] d\tau \end{bmatrix} + \begin{bmatrix} v_1^{OC}(t) \\ v_2^{OC}(t) \end{bmatrix}$$

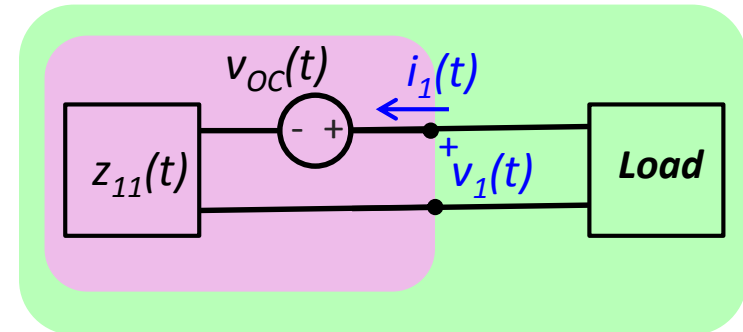
Relationships between port voltages and currents dictated by the Load Network

Coupling of ATHENA Device to a Load Network



To discuss details associated with the implementation, consider a **one-port network** example:

$$v_1(t) = \int_0^t z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$



For distributed coupling problems the self-impedances (z_{mm}) are impulsive near $t=0$.

$$v_1(t) - \int_{t_-}^t z_{11}(t - \tau) i_1[v_1(\tau)] d\tau = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

$$v_1(t) - z_{11}(t) i_1[v_1(t)] = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

$$t_- = \lim_{\delta \rightarrow 0} (t - \delta)$$

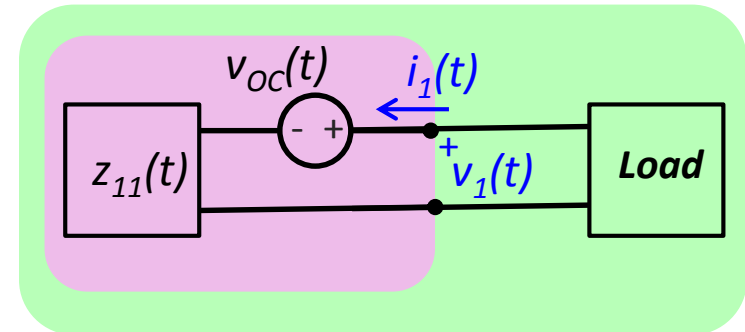
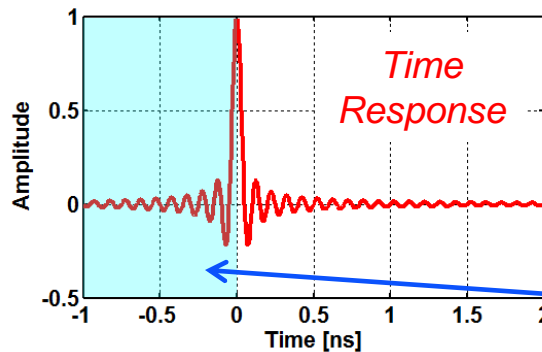
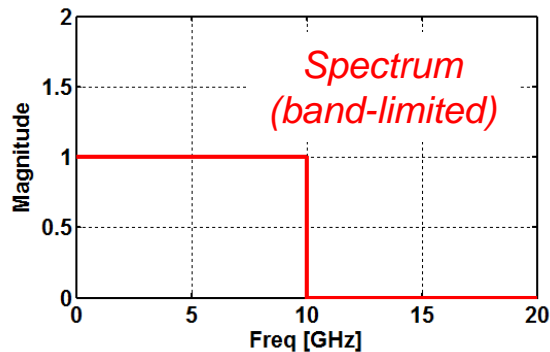
Surge impedance

- Time domain simulations capture this response.
- Frequency domain simulations must be corrected.

Coupling of ATHENA Device to a Load Network



Frequency domain simulations are band-limited.
Hence, impulse-like responses in the
time-domain appear as *sinc* functions.



Non-Causal

If the surge impedance is not corrected

- amplitude errors
- aliasing errors (causality)
- instability in non-linear solvers

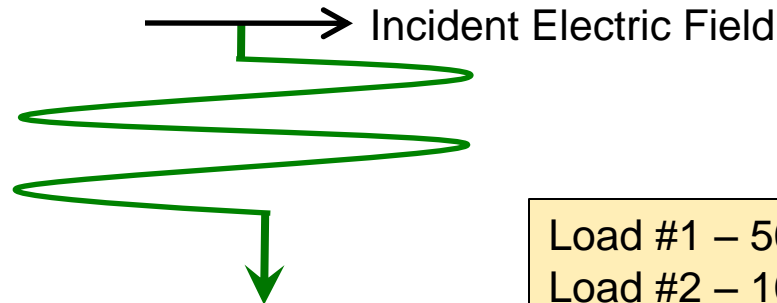
$$v_1(t) - z_{11}(t) i_1[v_1(t)] = \int_0^{t-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

Since the impulsive nature of surge impedance is known, it is evaluated analytically and *sinc* behavior is analytically removed.

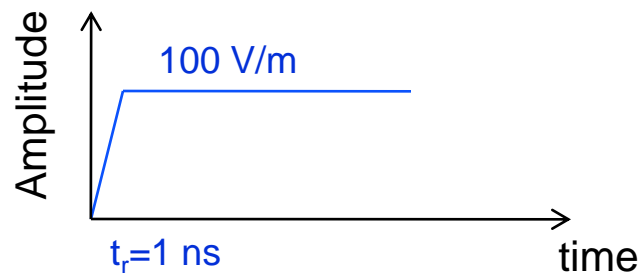
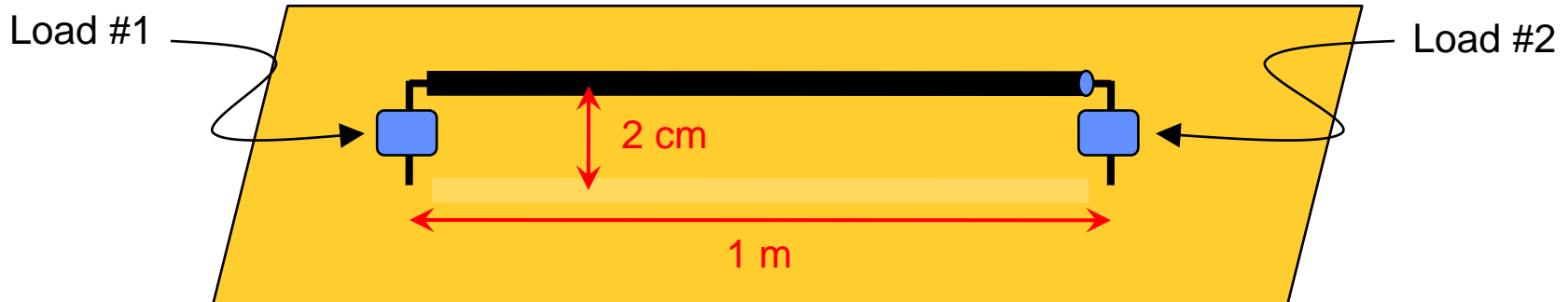
Example Problem Geometry (Intentionally Simple!)



Wire above ground plane
with end terminations



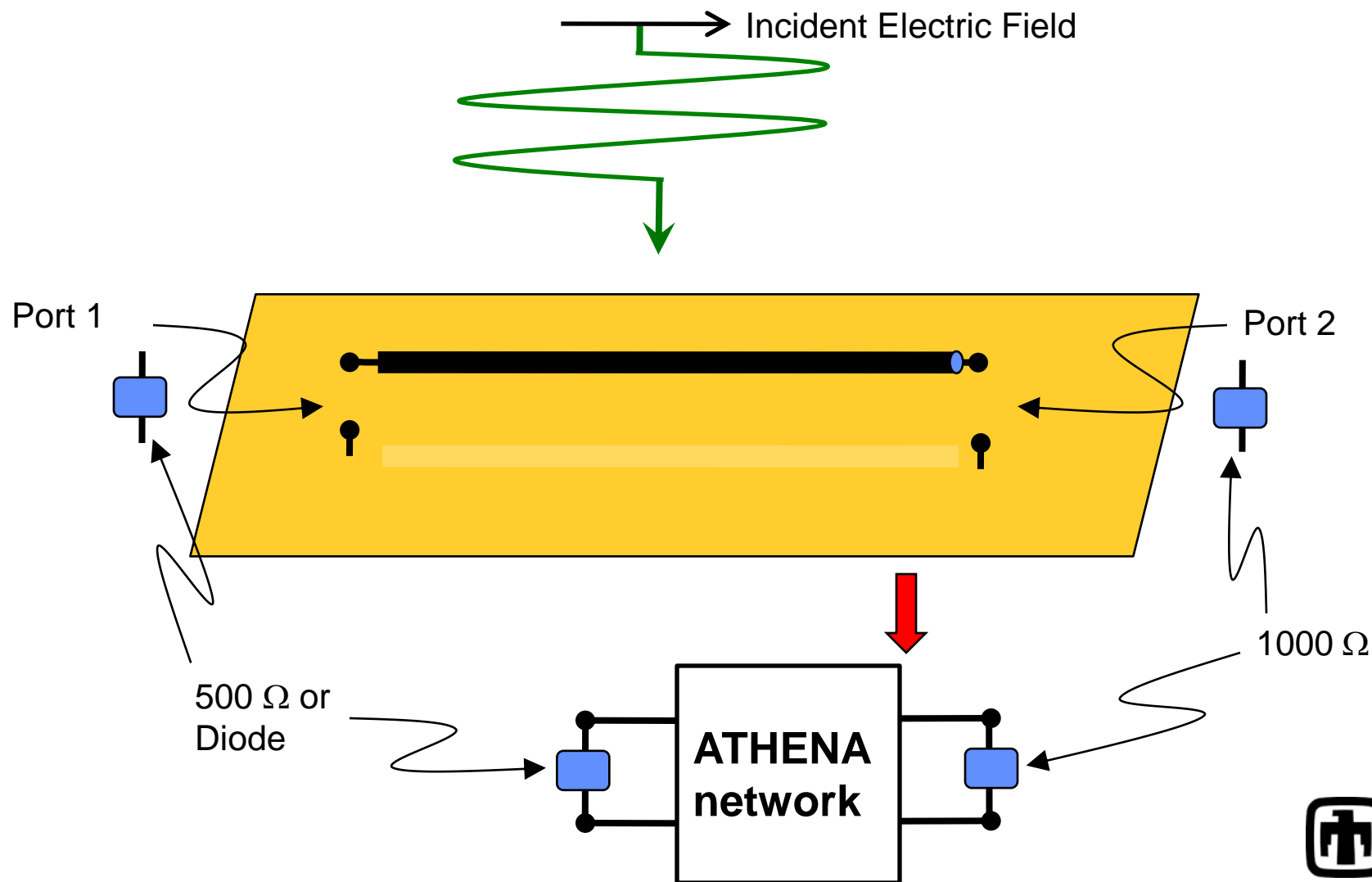
Load #1 – 500 Ω or Diode
Load #2 – 1000 Ω



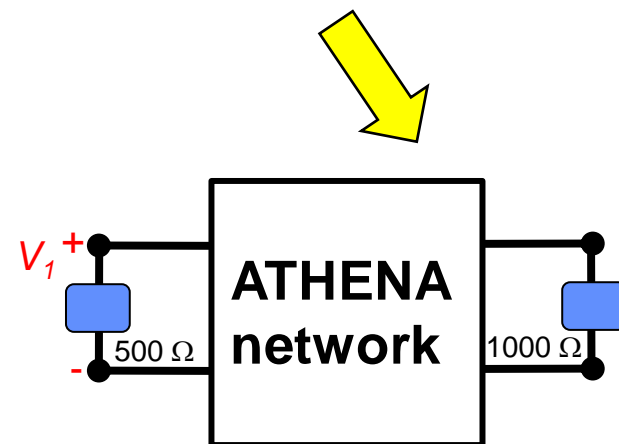
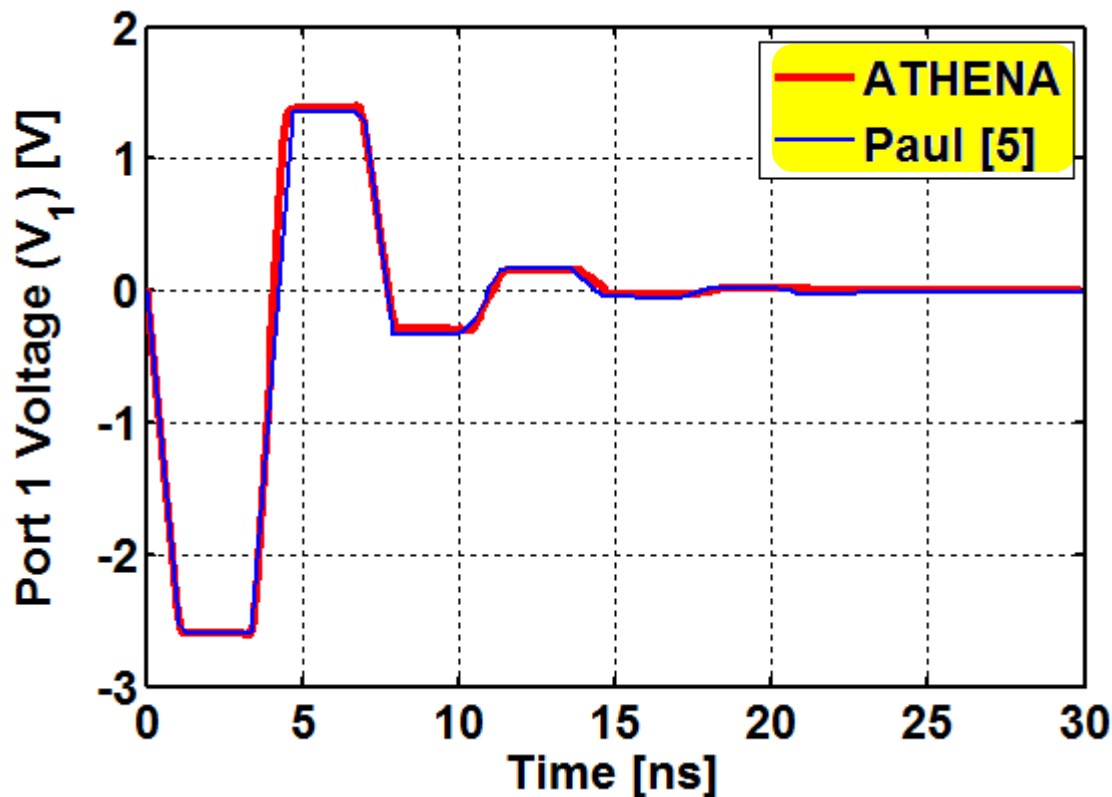
Not to scale



Example: 2-Port Network



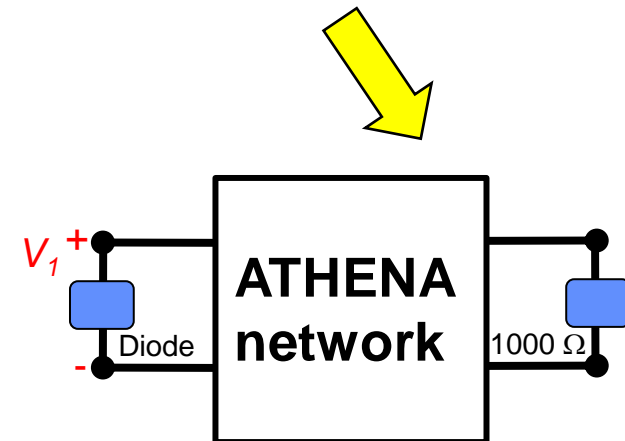
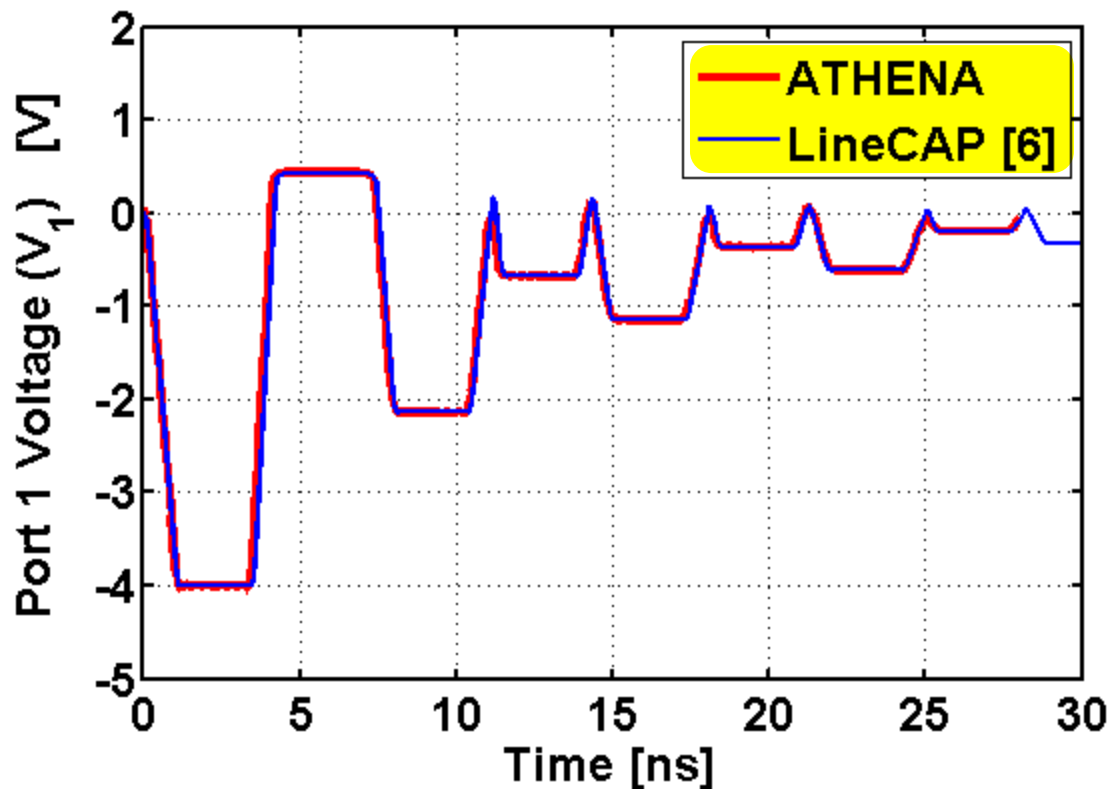
2-Port : Linear Loads (500 Ω and 1000 Ω)



$E_{\max} = 100$ V/m

ATHENA device in Xyce

2-Port : Linear ($500\ \Omega$) and Non-Linear (Diode) Loads



$E_{\max} = 100\ \text{V/m}$

ATHENA device in Xyce



Summary and Next Steps

- The **Active Thevenin Equivalent Network Approach (ATHENA)** allows us to link EMI & IEMI coupling to nonlinear circuit simulations in a fully consistent, bidirectional way.
- ATHENA is now implemented in the Spice code *ngspice* and Sandia's parallelized circuit code *Xyce*. Test cases have been successfully completed with good agreement with independent results.
- Validation measurements for test-cases are underway.