



SAND2015-6928PE

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Frequency Response of Shock Mitigation through Foam Materials

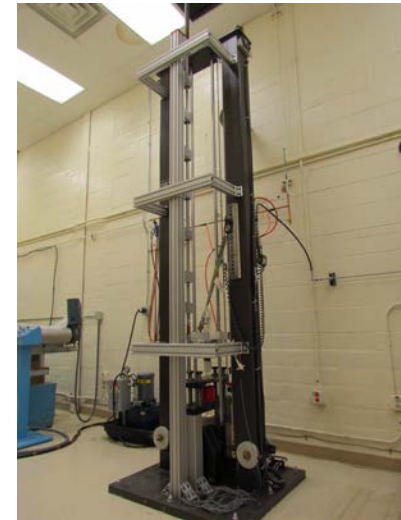
Bo Song (1558)



Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

Experimental Impact Mechanics Lab. (EIML)

- Location: B860/122B
- Lead/Principal Investigator: Bo Song (1558)
- Facilities:
 - 1"-diameter split Hopkinson compression bar (*Kolsky compression bar*)
 - 1"-diameter split Hopkinson tension bar (*Kolsky tension bar*)
 - 1"-diameter "dropkinson" bar for intermediate-rate tensile testing
 - 3"-diameter split Hopkinson compression bar (*Kolsky compression bar*)
- Instrument/Equipment
 - Teledyne LeCroy 4-channel high-speed digital oscilloscope
 - Teledyne LeCroy 8-channel high-speed digital oscilloscope
 - Keyence VHX-5000 digital microscope (20X-5000X)
 - Vishay 4-channel signal conditioner
 - Custom made laser displacement measurement system
 - 1200°C electrical furnace
 - MTI 15kW induction heater
 - Instron environmental chamber (-100 - 350°C)
 - Buehler diamond saw
 - Thermocouple welder
 - Kirana ultra-high speed digital camera (coming soon)
 - NI acquisition and control system (coming soon)
- Partnership with:
 - Terminal Ballistic Hopkinson Bar Lab
 - Structure Mechanics Lab (MTS)
 - Shock Mechanics Lab (Drop tables)
 - Area III – Mechanical Shock Facility (Gas gun, horizontal actuator)
 - Area III – Terminal Ballistic Lab



EIML Capabilities (What Can We Do?)

- **Dynamic Characterization of Materials**

- *Dynamic stress-strain response of materials in compression or tension (shear coming soon)*
- *Dynamic failure and fracture of materials*
- *Strain-rate Range: $\sim 100 - 10,000 \text{ s}^{-1}$*
- *Temperature Range: $-100 - 1200^\circ\text{C}$*
- *Stress state: uniaxial stress; triaxial stress (in compression only)*
- *Materials covered: ceramics, alloys, composites, glasses, polymers, foams, biological tissues, concretes, sands, soil, etc*

- **Dynamic Characterization of Component/Small Structures**

- *Dynamic structural testing with preload capability (compression or tension)*
- *Wave Propagation/Interaction*
- *Shock Mitigation*
- *Dynamic Interface Problem*
- *Component/Device Functionality/Survivability in Abnormal Mechanical Environments*
 - *High-g, high-frequency impact and vibration*
- *Impact Sensor characterization*

- **Rate-dependent Model Validation**

- *High rate, high frequency, etc*



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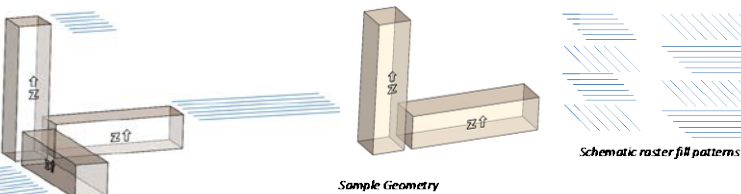
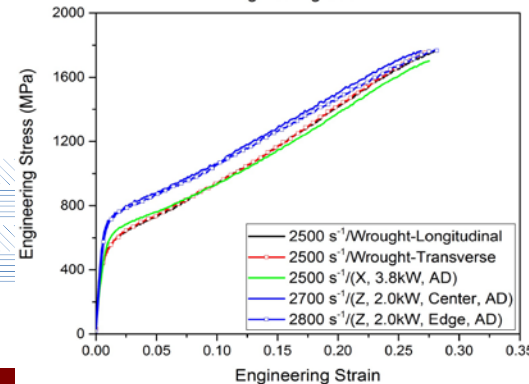
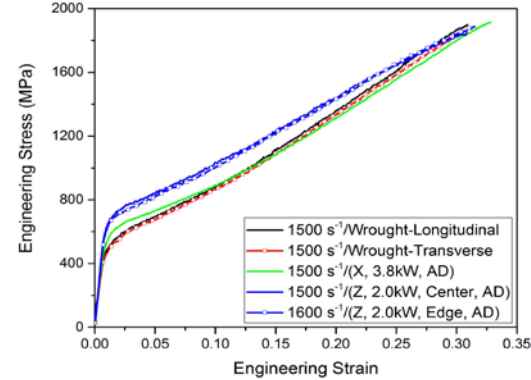
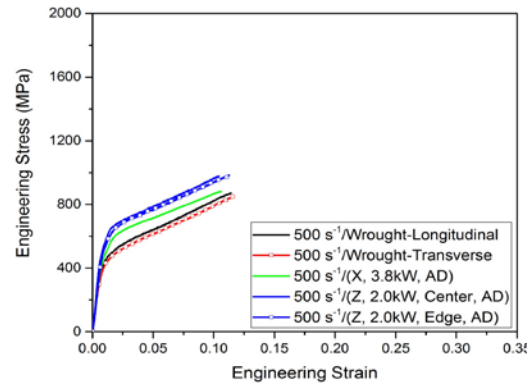
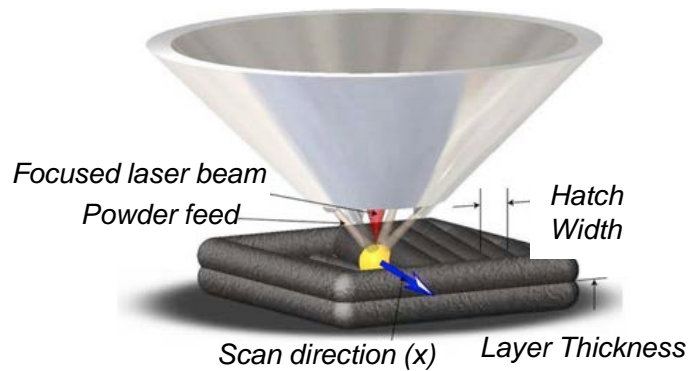
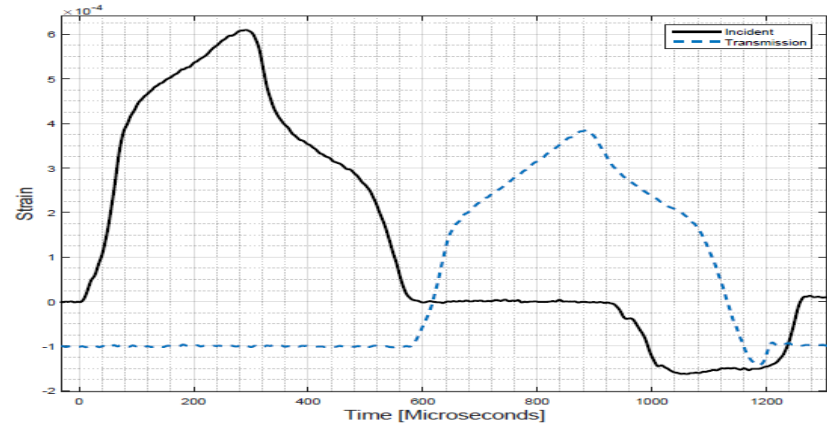
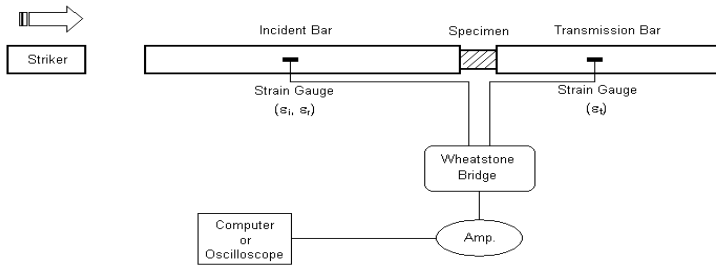


Brett Sanborn

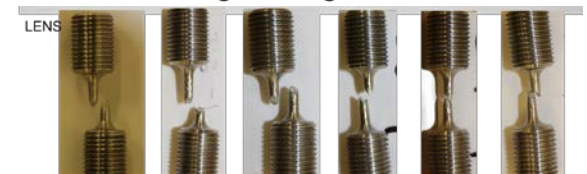
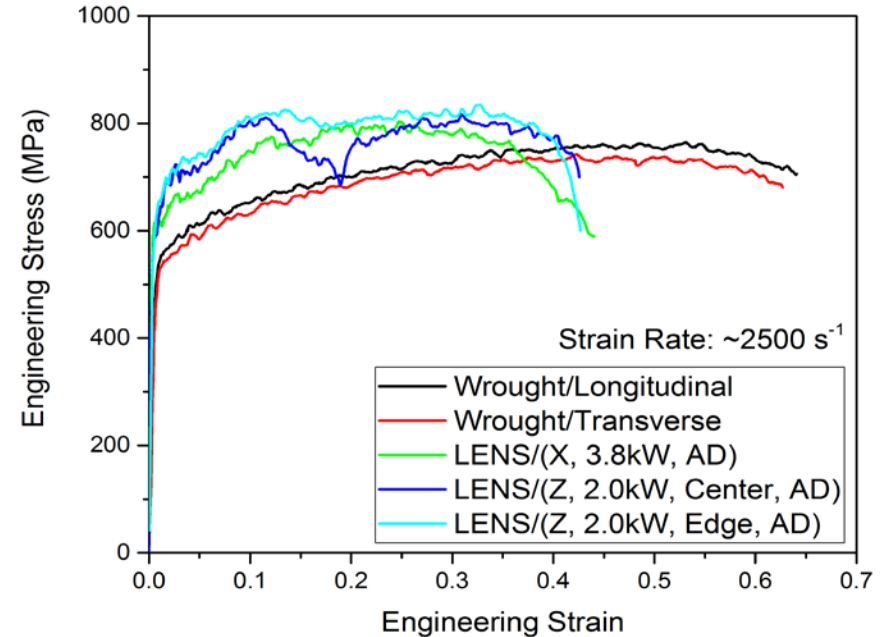
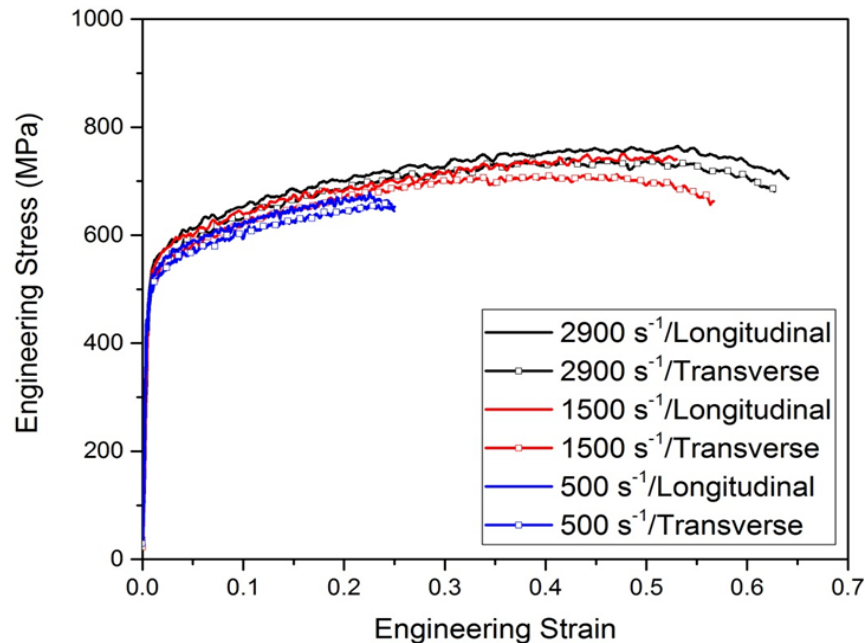
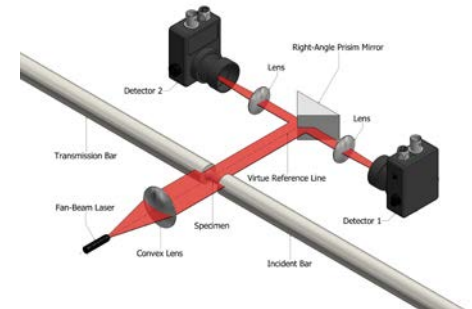
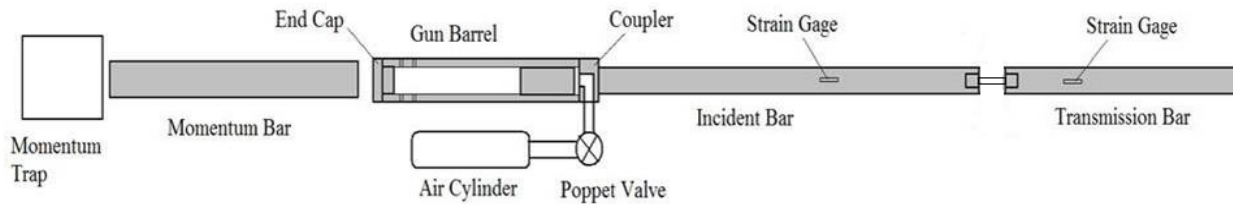
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Dynamic Material Characterization Examples

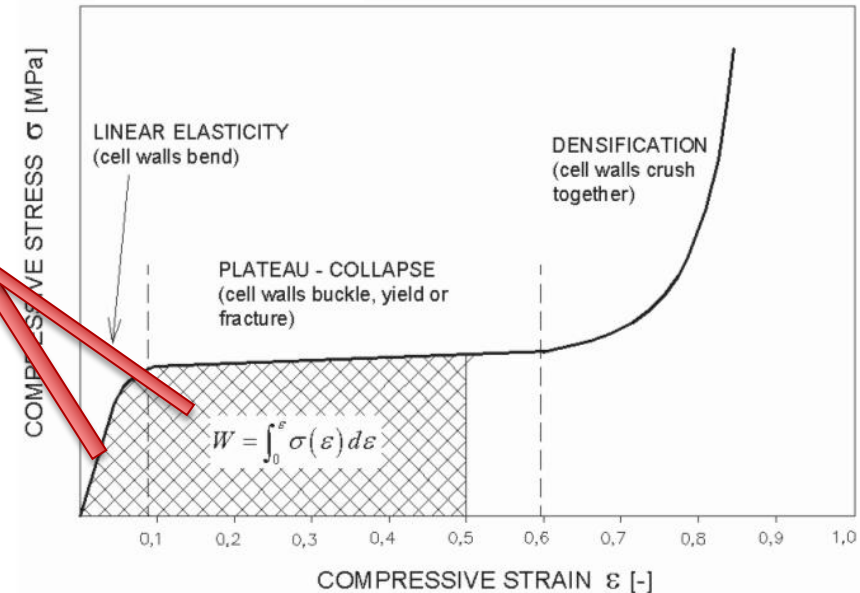


Dynamic Material Characterization Examples



Characteristics and Applications of Foam Materials

- ▶ **Light weight (low density)**
 - Good for transportation
- ▶ **Excellent vibration damper**
 - Comfort
 - Protection (sensitive devices)
- ▶ **Excellent shock/impact energy absorber**
 - Protection (human, sensitive devices, hazard materials, etc)
- ▶ **Application-orientated materials design**
 - Material properties, particularly under impact loading
 - Structural response in abnormal (shock/impact) mechanical environments

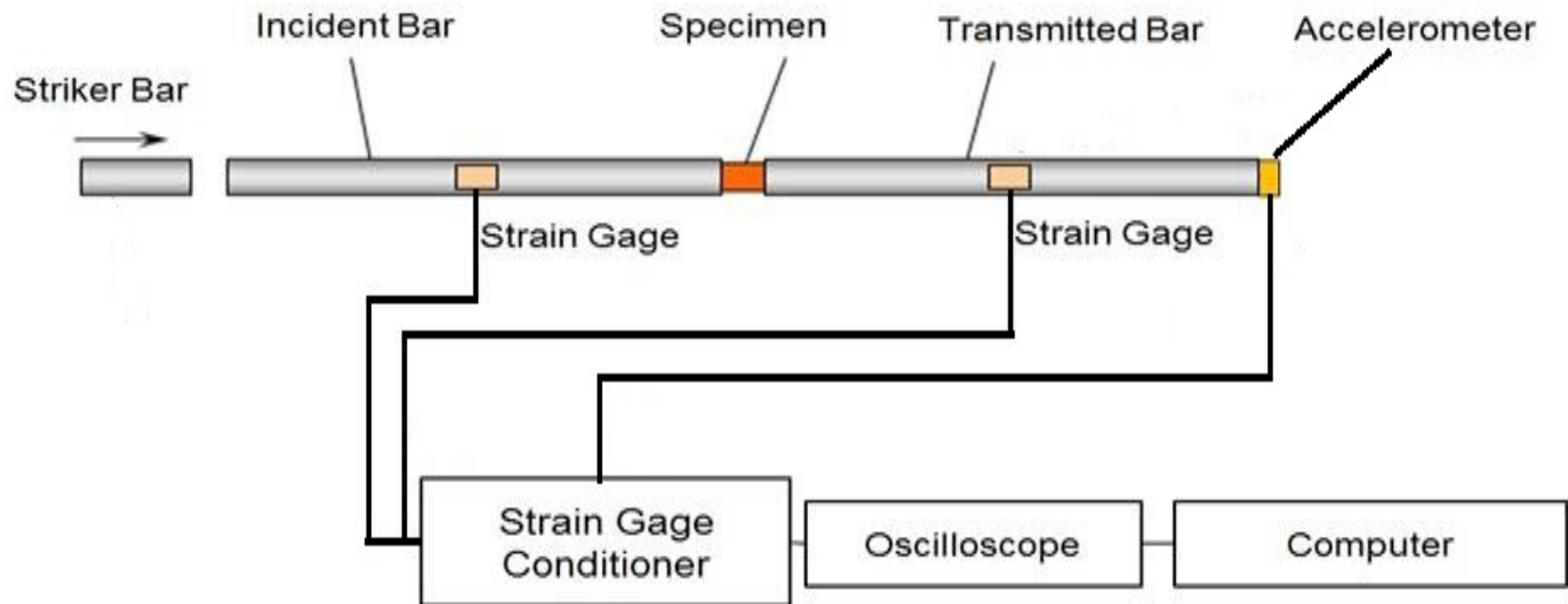


➡ **Size/geometry independent**

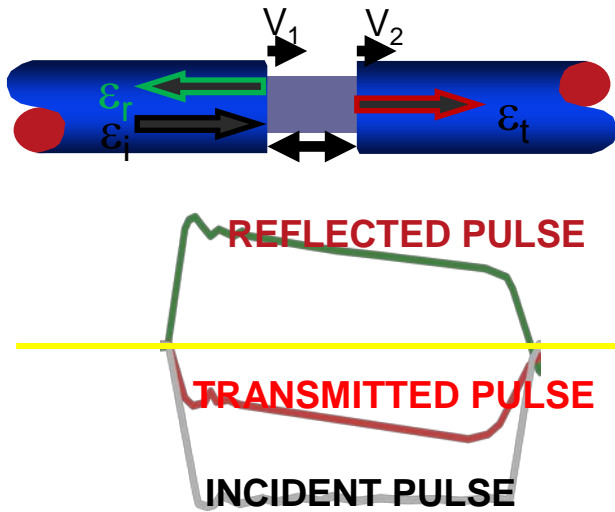
➡ **Size/geometry dependent**

Shock Mitigation Characterization of Polymeric Foams

► Time- and Frequency-Based Shock Mitigation Analyses



Time-Based Shock Mitigation Analysis



Incident Energy $E_i(t) = A_0 C_0 E_0 \int_0^t \epsilon_i(t)^2 dt$

Reflected Energy $E_r(t) = A_0 C_0 E_0 \int_0^t \epsilon_r(t)^2 dt$

Transmitted Energy $E_t(t) = A_0 C_0 E_0 \int_0^t \epsilon_t(t)^2 dt$

Input Energy

$$E_{input}(t) = E_i(t) - E_r(t) = A_0 C_0 E_0 \int_0^t [\epsilon_i^2(t) - \epsilon_r^2(t)] dt$$

Output Energy $E_{output}(t) = E_t(t) = A_0 C_0 E_0 \int_0^t \epsilon_t(t)^2 dt$

Energy Dissipation (Absorbed Energy) $\Delta E(t) = E_{input}(t) - E_{output}(t)$

$$= A_0 C_0 E_0 \int_0^t [\epsilon_i^2(t) - \epsilon_r^2(t) - \epsilon_t^2(t)] dt$$

Energy Dissipation Ratio

$$\delta(t) = \frac{\Delta E(t)}{E_{input}(t)}$$

Frequency-Based Shock Mitigation Analysis

$$\varepsilon(f) = B(f)e^{-j(2\pi f + \phi)}$$

Incident Energy Spectrum Density $S_i(f) = A_0 C_0 E_0 |B_i(f)|^2$

Reflected Energy Spectrum Density $S_r(f) = A_0 C_0 E_0 |B_r(f)|^2$

Transmitted Energy Spectrum Density $S_t(f) = A_0 C_0 E_0 |B_t(f)|^2$

$$E(f) = \int_f^{f+\Delta f} S(f) df = A_0 C_0 E_0 \int_f^{f+\Delta f} |B(f)|^2 df \approx A_0 C_0 E_0 |B(f)|^2 \Delta f$$

Parseval's theorem $E = A_0 C_0 E_0 \int_0^\infty \varepsilon(t)^2 dt = A_0 C_0 E_0 \int_{-\infty}^{+\infty} |B(f)|^2 df$

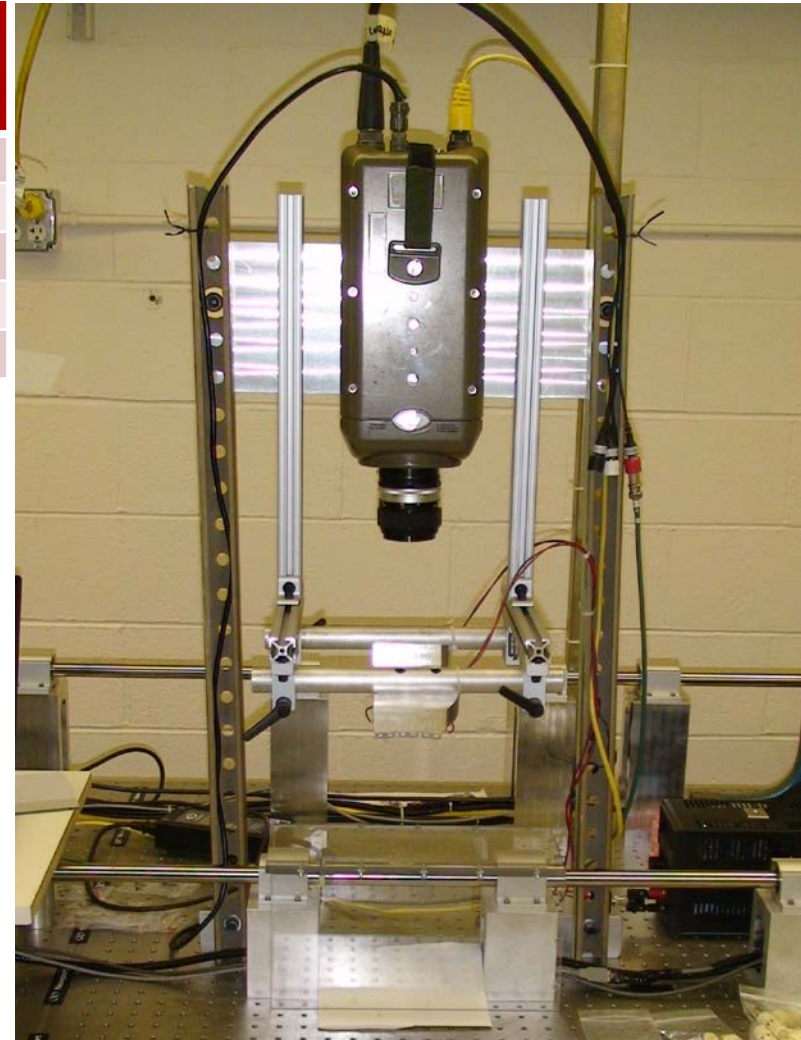
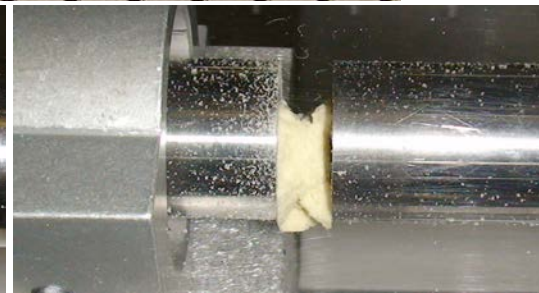
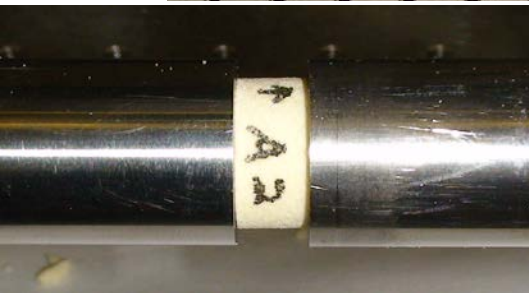
Energy Dissipation (Absorbed Energy) $\Delta(f) = E_i(f) - E_r(f) - E_t(f)$
 $= A_0 C_0 E_0 (|B_i(f)|^2 - |B_r(f)|^2 - |B_t(f)|^2) \Delta f$

Energy Dissipation Ratio

$$\delta(f) = \frac{\Delta(f)}{E_i(f) - E_r(f)} = 1 - \frac{|B_t(f)|^2}{|B_i(f)|^2 - |B_r(f)|^2}$$

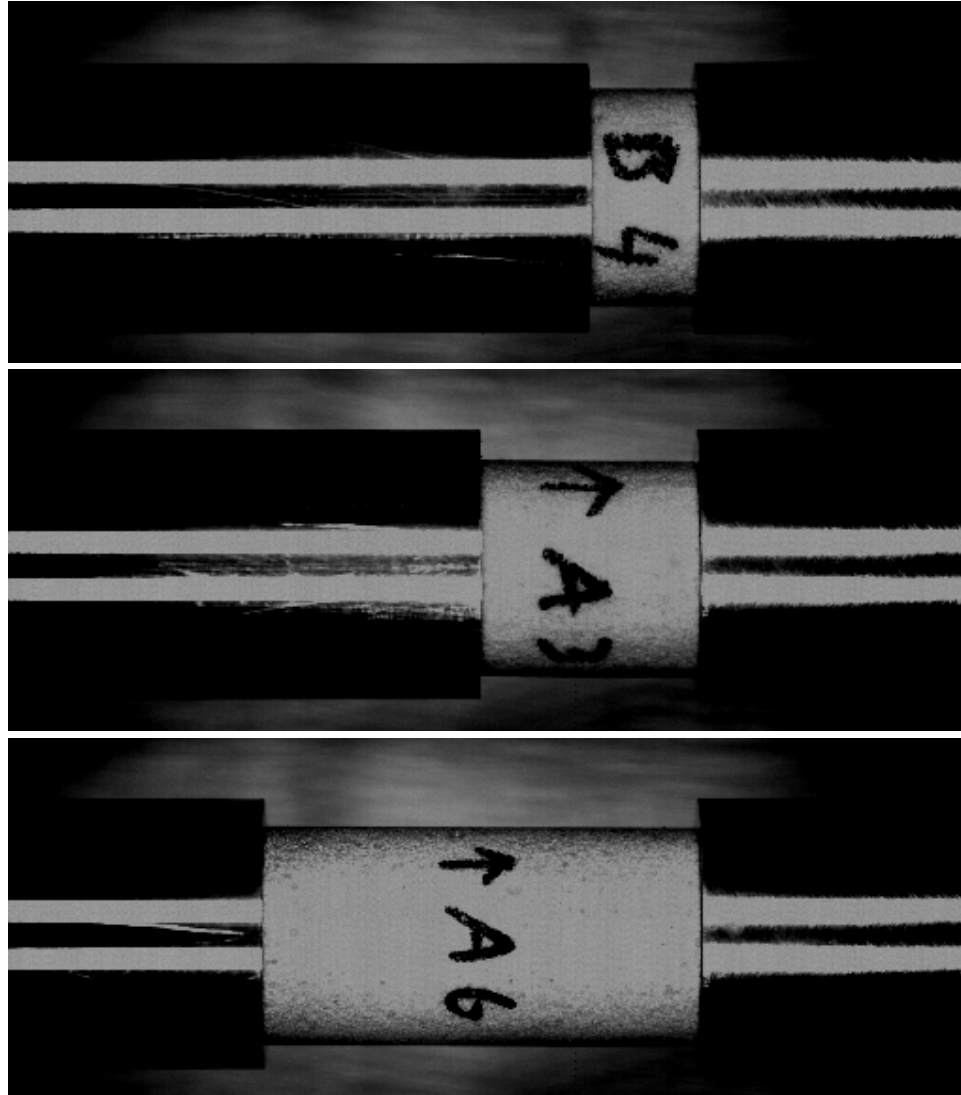
Frequency-Based Shock Mitigation Analysis on 20-PCF PMDI Foam

Sample No.	Diameter (mm)	Thickness (mm)	Density ($\times 10^3$ kg/m ³)	Impact Speed (m/s)
B-4	15.3	7.6	0.31	16
B6-1	15.4	7.6	0.31	38
A-3	15.2	15.3	0.34	16
B-5	15.4	15.3	0.31	16
A-6	15.3	30.5	0.32	16

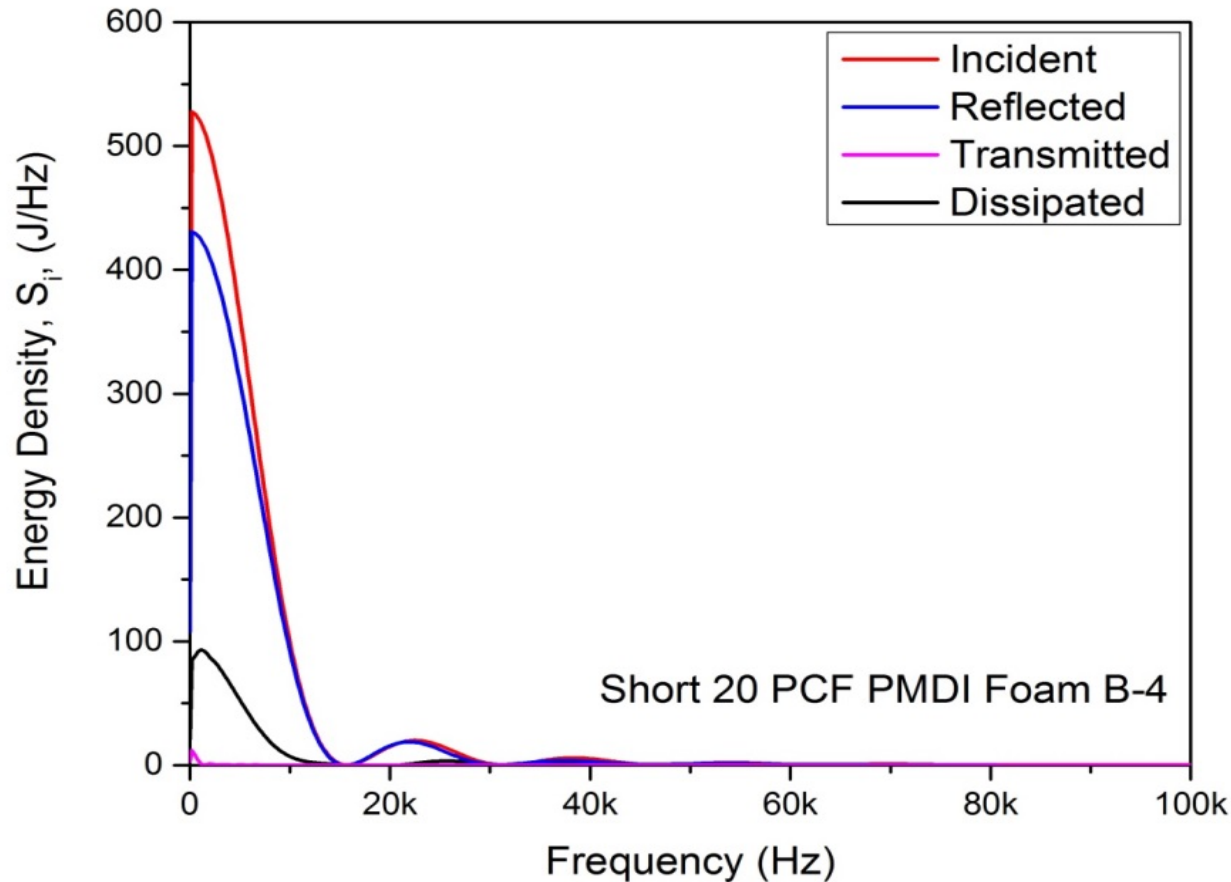


Frequency-Based Shock Mitigation Analysis on 20-PCF PMDI Foam

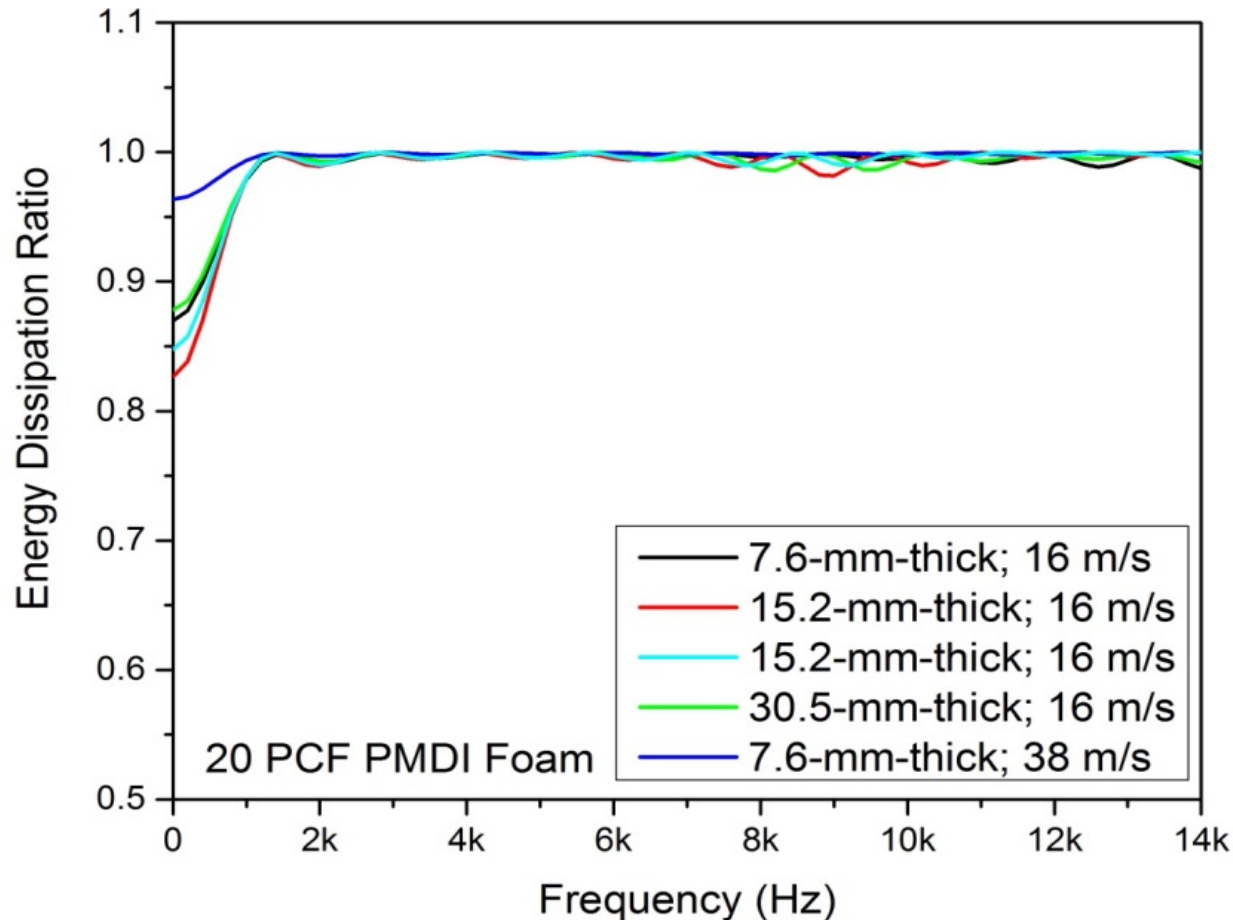
$V = 16 \text{ m/s}$



Frequency-Based Shock Mitigation Analysis on 20-PCF PMDI Foam

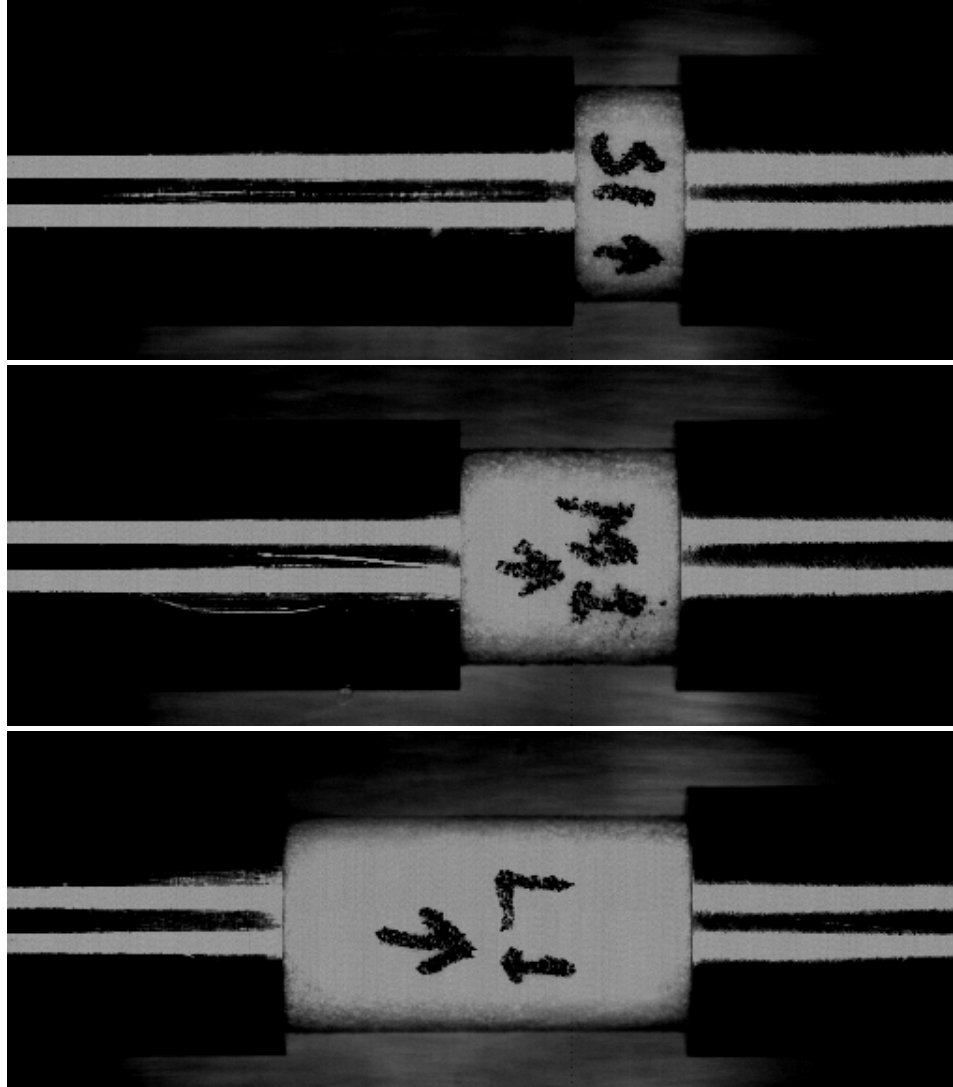


Frequency-Based Shock Mitigation Analysis on 20-PCF PMDI Foam

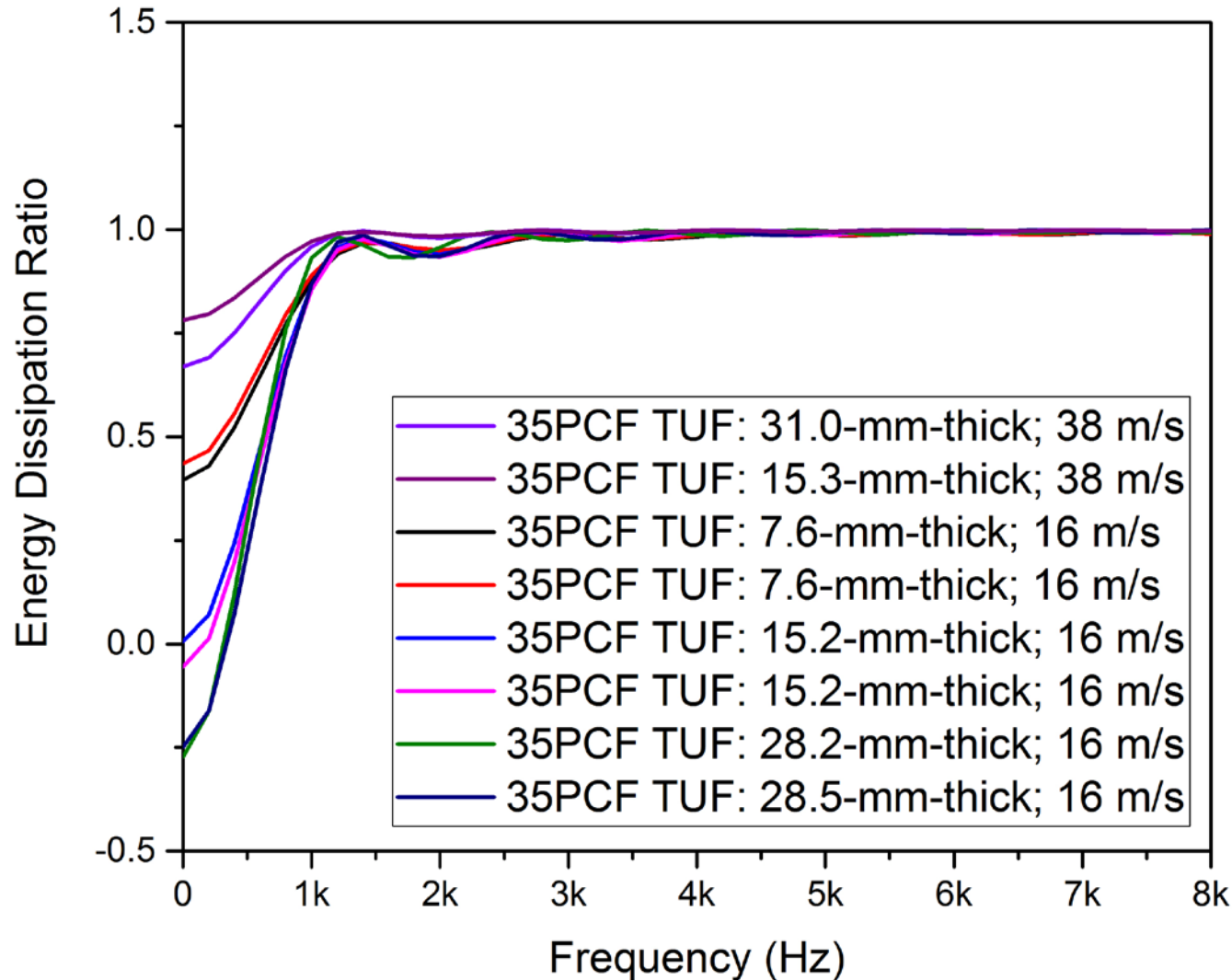


Frequency-Based Shock Mitigation Analysis on 35-PCF Tuf-Foam

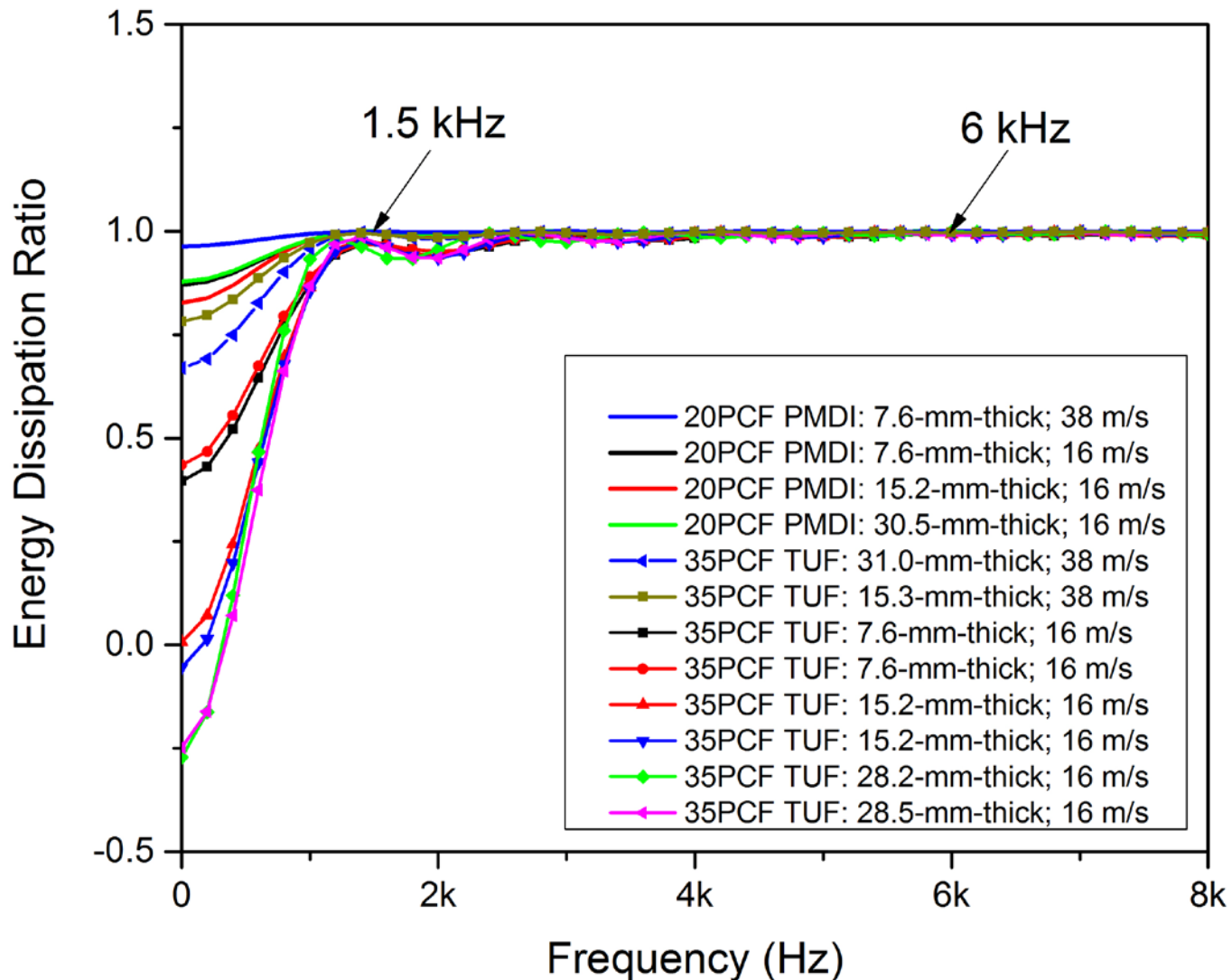
$V = 16 \text{ m/s}$



Frequency-Based Shock Mitigation Analysis on 35-PCF Tuf-Foam



Shock Mitigation Comparison between 20-PCF PMDI and 35-PCF Tuf-Foam



This Presentation

- Frequency-based analysis on shock mitigation characteristics of foam materials
 - Extended to several other shock mitigation/isolation materials and structures

Our Mission

- Develop advanced experimental and diagnostic techniques for scientific discovery
- Provide high-fidelity experimental data on dynamic response of materials and structures for rate-dependent material model development and validation

We are highly motivated and looking forward to any kind of internal and/or external collaboration/partnership, particularly with universities, on fundamental research and applications