



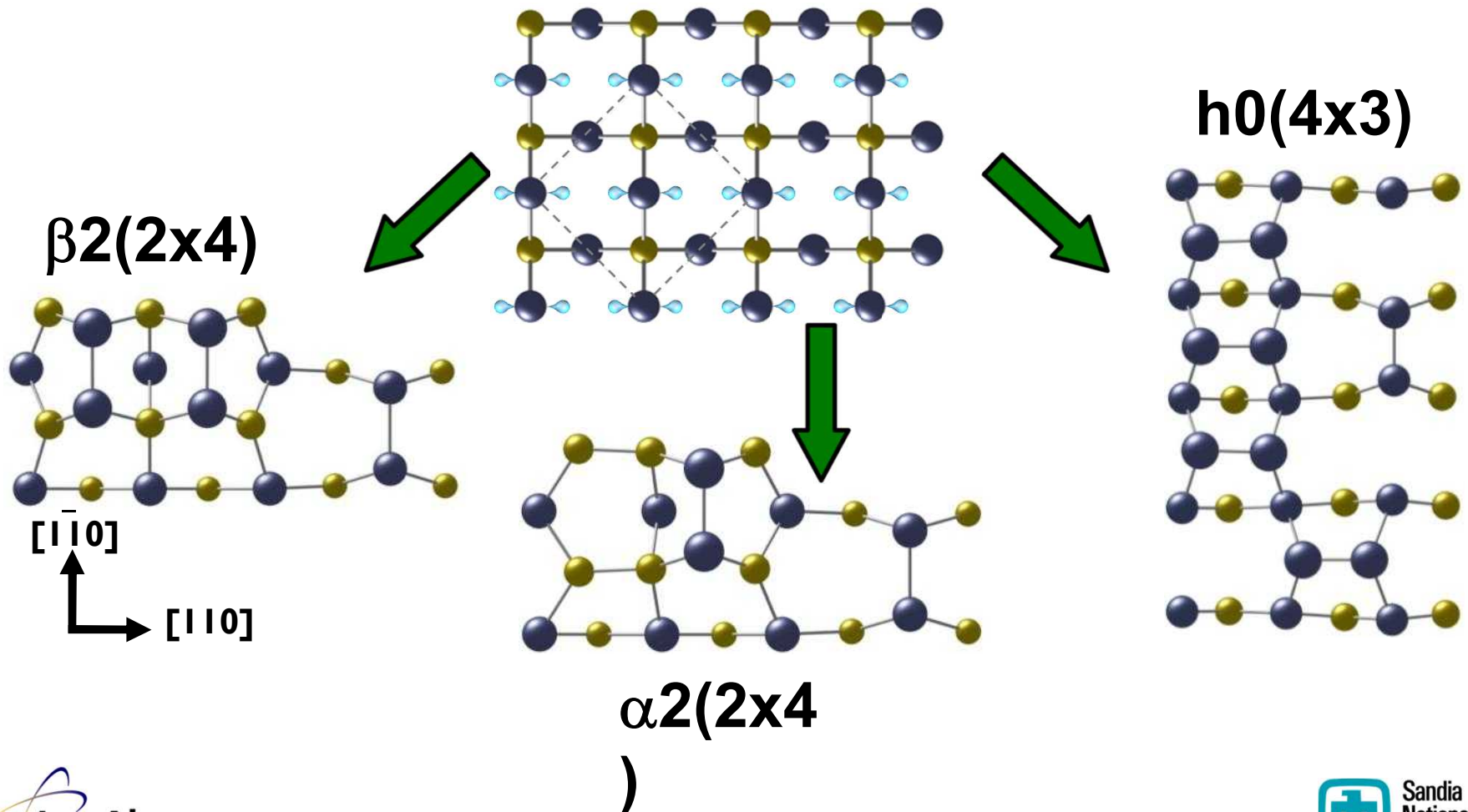
Reconstruction and Disorder at Compound Semiconductor Surfaces

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Sandia National Laboratories

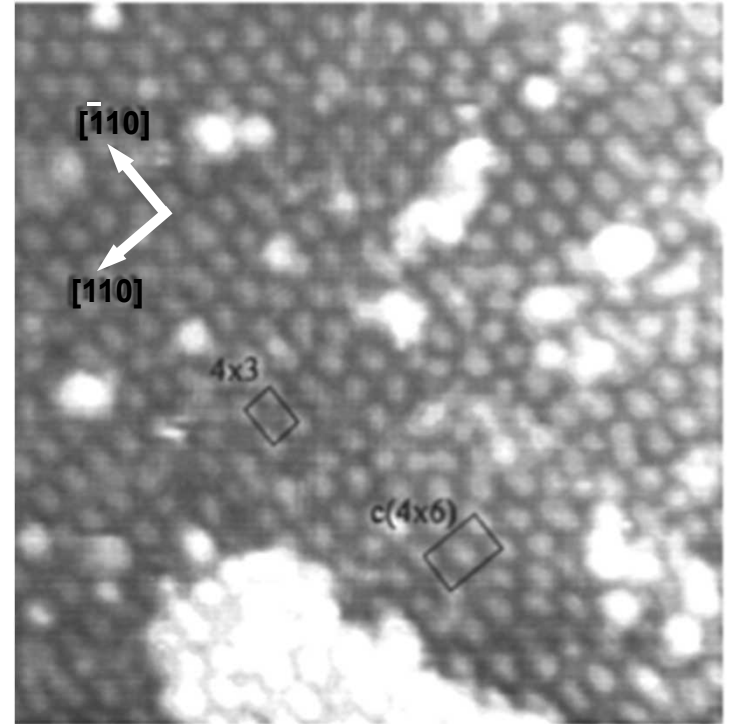
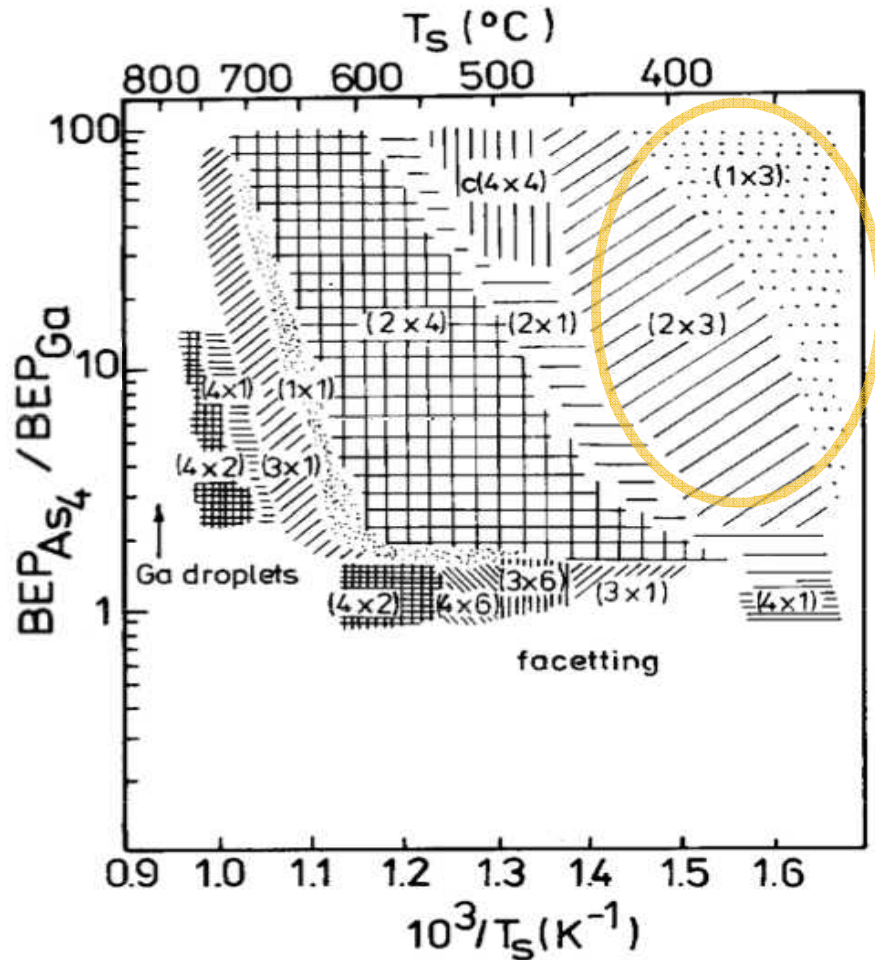
J.C. Thomas, A. Duzik,
J. Mirecki Millunchick, and A. Van der Ven
University of Michigan

This work was performed, in part, at the Center for Integrated Nanotechnologies, a U.S. Department of Energy, Office of Basic Energy Sciences user facility. Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

Surface Reconstruction



Reconstruction Stability Diagram

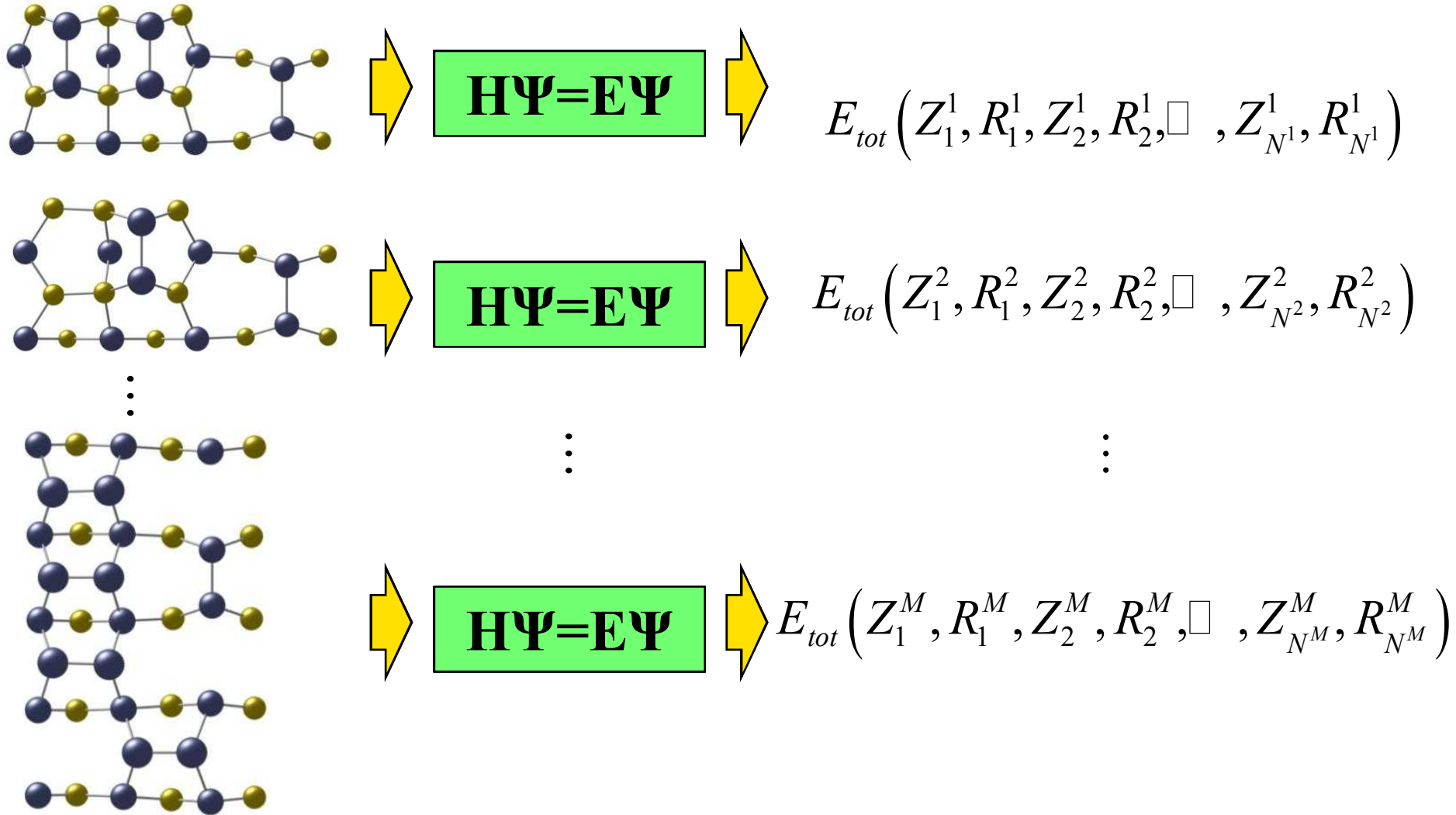


The (2x3)/(4x3)/c(6x4) reconstruction observed on GaAs (001)

Chizhov, Lee, Willis, Lubyshev, and Miller, *Phys. Rev. B*, 56, 1013 (1997).

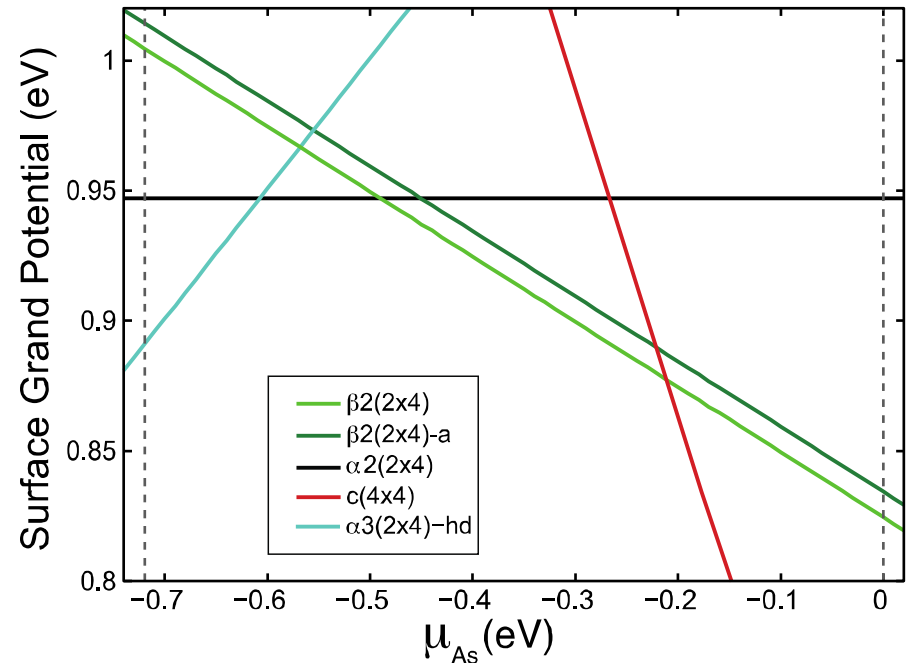
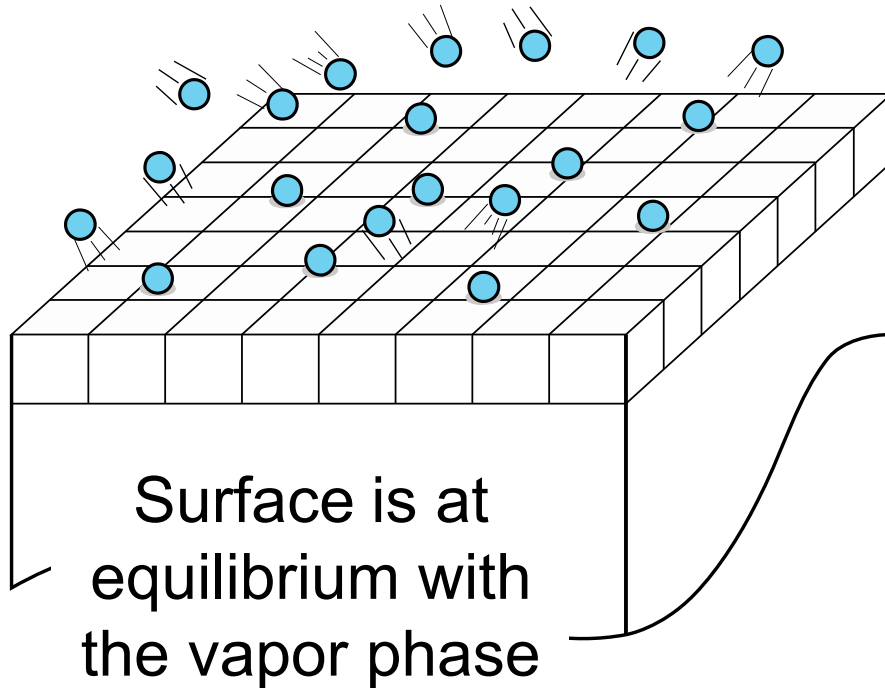


Ab Initio Calculations – Kohn Sham Density Functional Theory





Chemical Potentials Account For Variable Numbers of Each Species



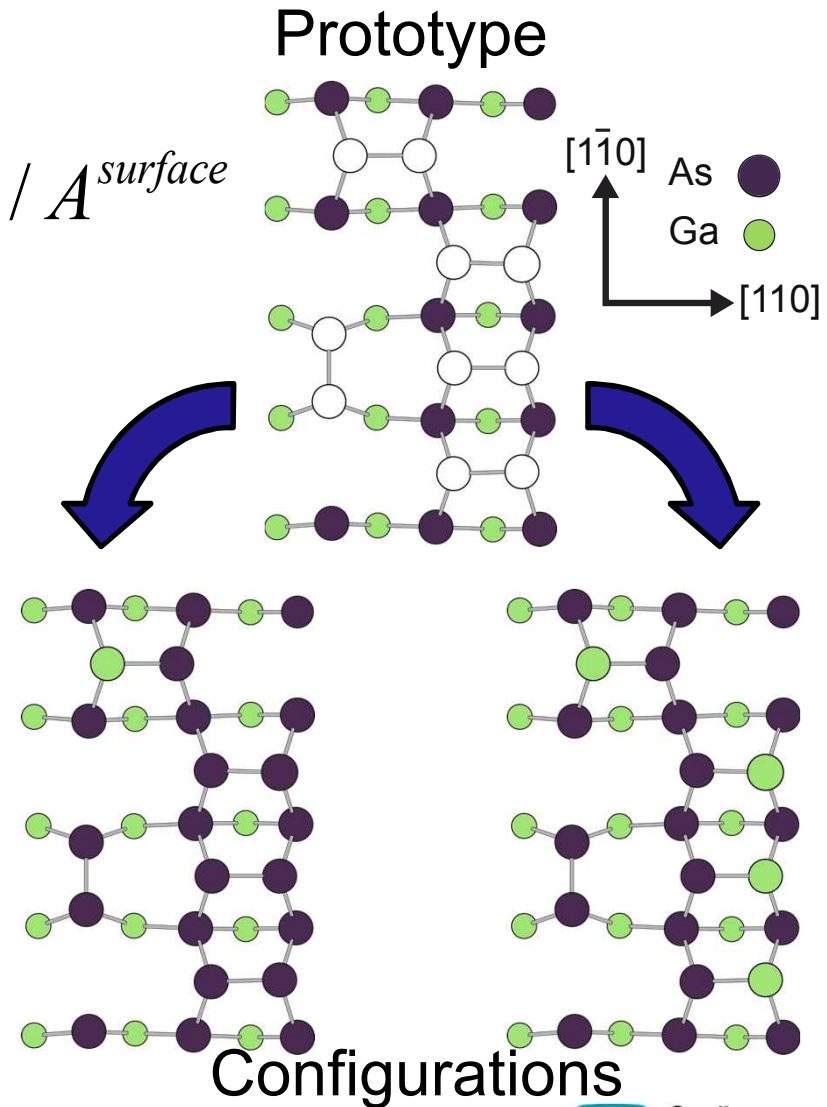
Surface Grand Potential

$$\sigma(\mu_1, \dots, \mu_n) = \left(E_{tot} - N^{bulk} E_{bulk} - \sum_{\alpha} \mu_{\alpha} (N_{\alpha} - N_{\alpha}^{bulk}) \right) / A^{surface}$$

Nonzero Temperature and Disorder

$$\sigma(T, \mu_1, \dots, \mu_n) = \sigma(\mu_1, \dots, \mu_n) - TS / A^{\text{surface}}$$

- **Energy**
 - Structure
 - Species configuration
- **Entropy**
 - Vibrational entropy
 - Configurational entropy





Systematic Enumeration of Low Energy Prototypes

Identify rules that describe observed structural trends



Enumerate all distinct prototypes that obey rules

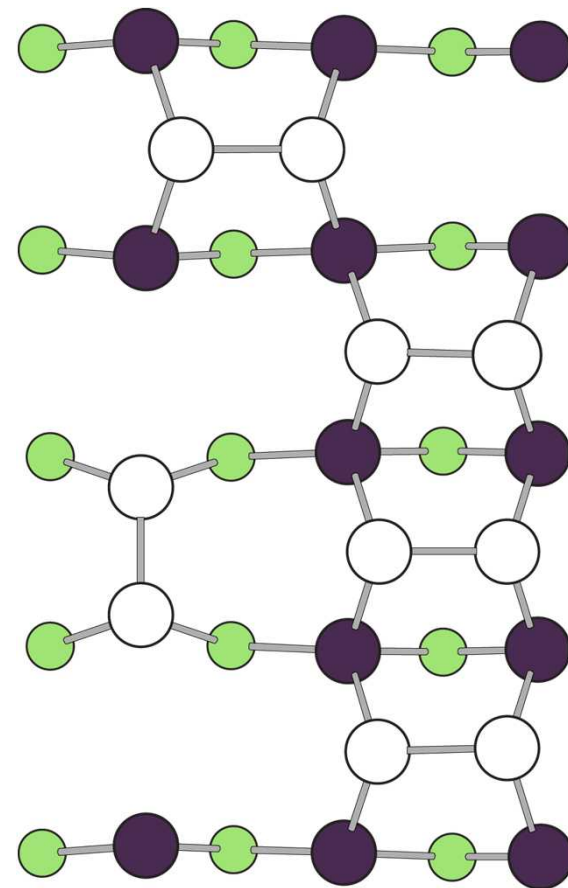


Calculate energies of promising structures from first principles



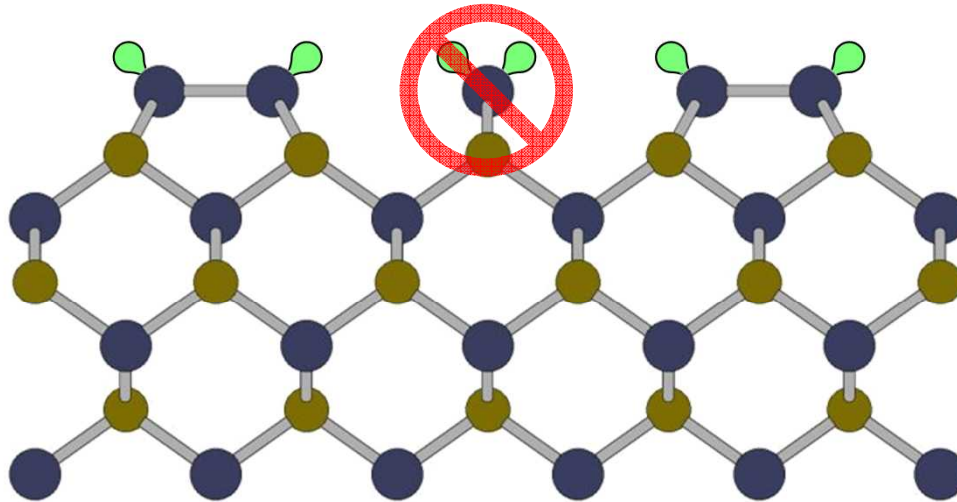
Collect low-energy prototypes to study configurations

Prototype



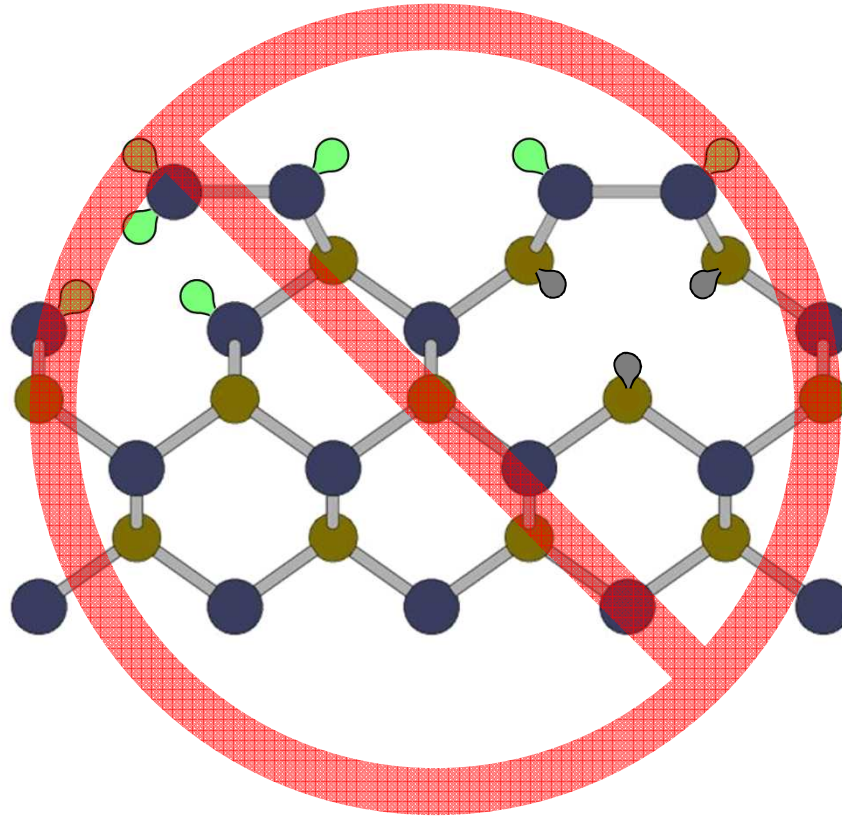


Structural trends



1. Only three-fold and four-fold coordination is allowed.

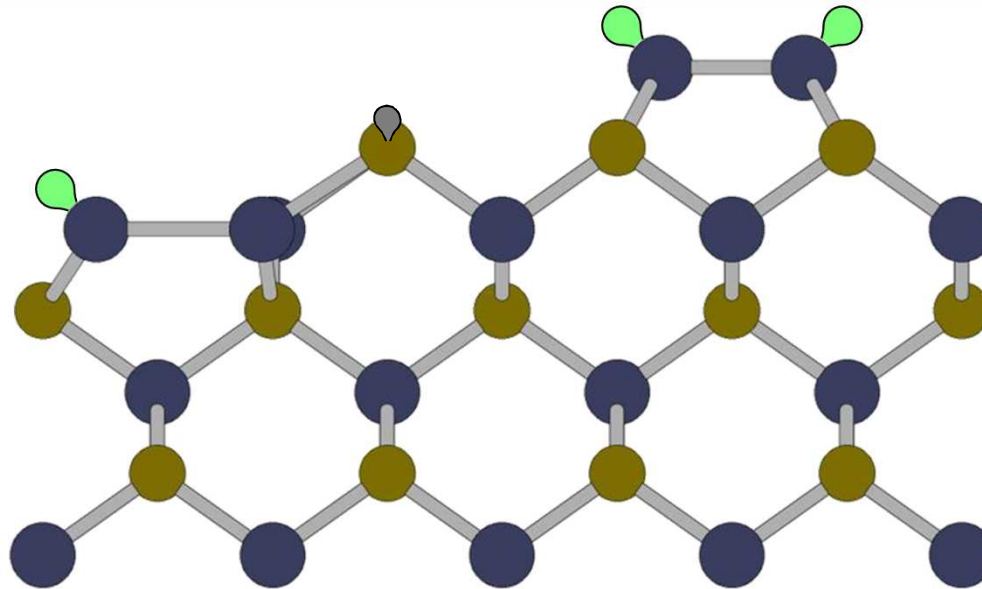
Structural trends



II. There are no subsurface vacancies.

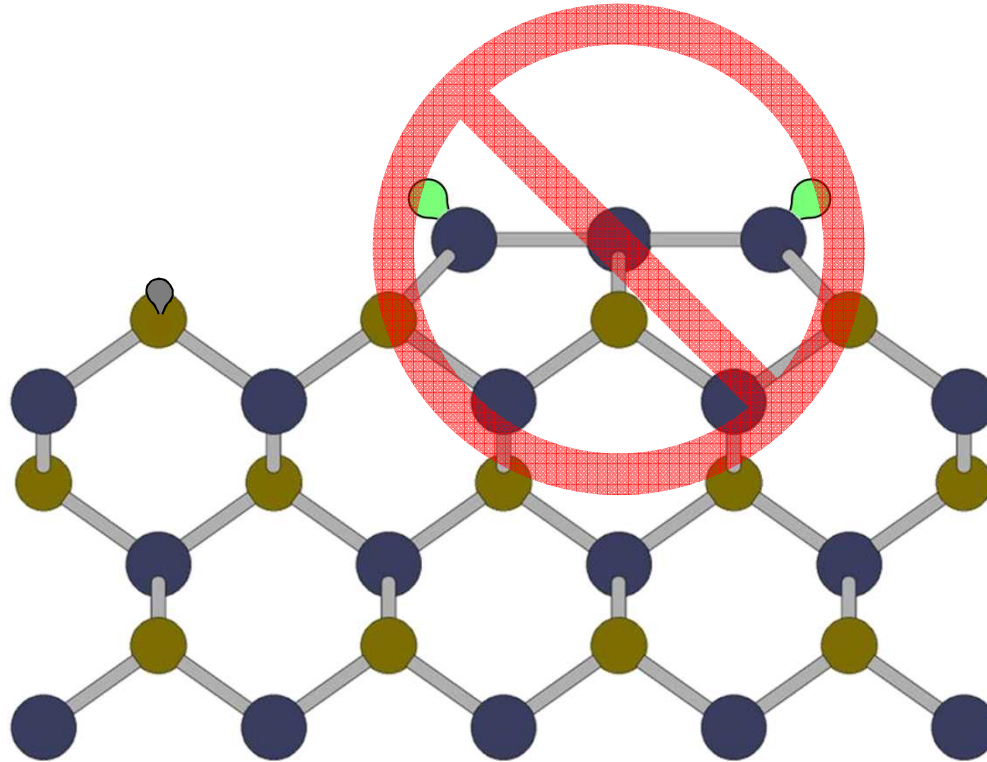


Structural trends



III. Under-coordinated atoms can bond to in-plane neighbors.

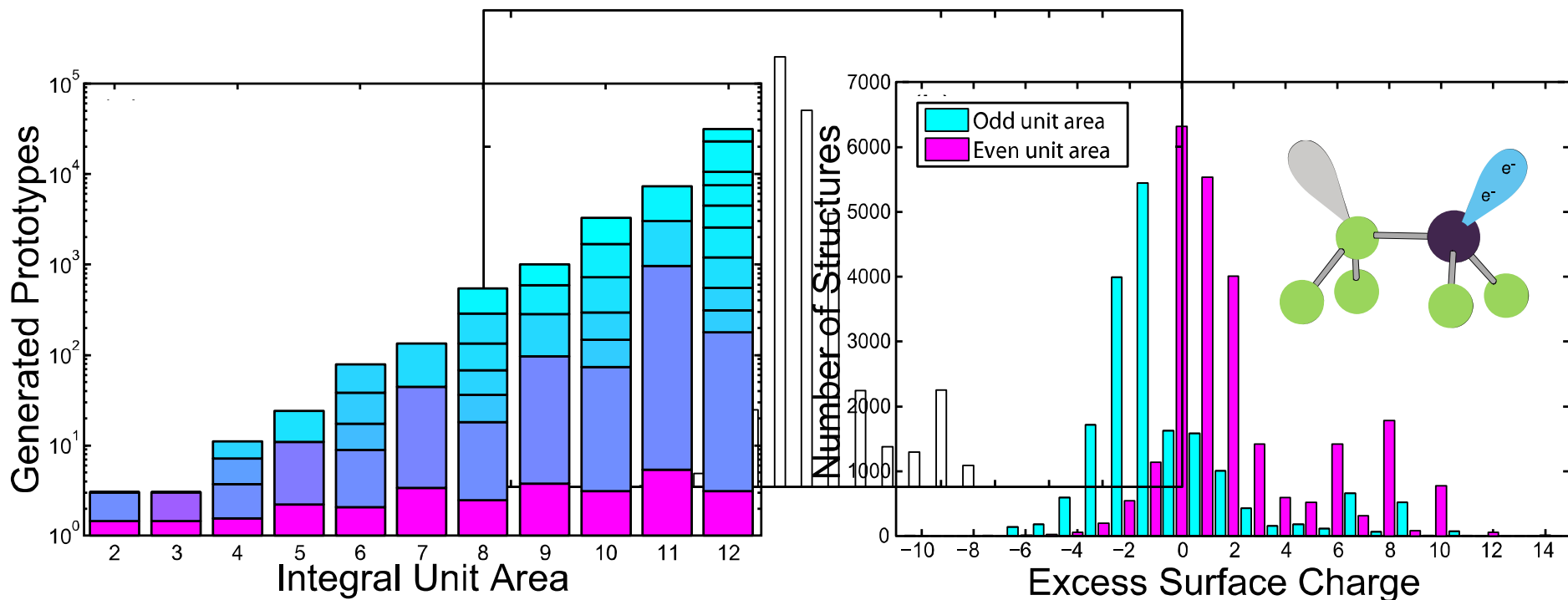
Structural trends



IV. An atom can have no more than one in-plane bond.



Screen Results Using the “Electron Counting Model”



There are over 40,000 new structural prototypes with unit area ≤ 12 .

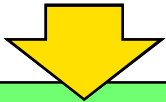
Charge neutral prototypes make up only about 15% of those generated.

J. Thomas *et al.*, *Phys. Rev. B*, 82, 165434, (2010).



GaAs (001) Groundstate Search

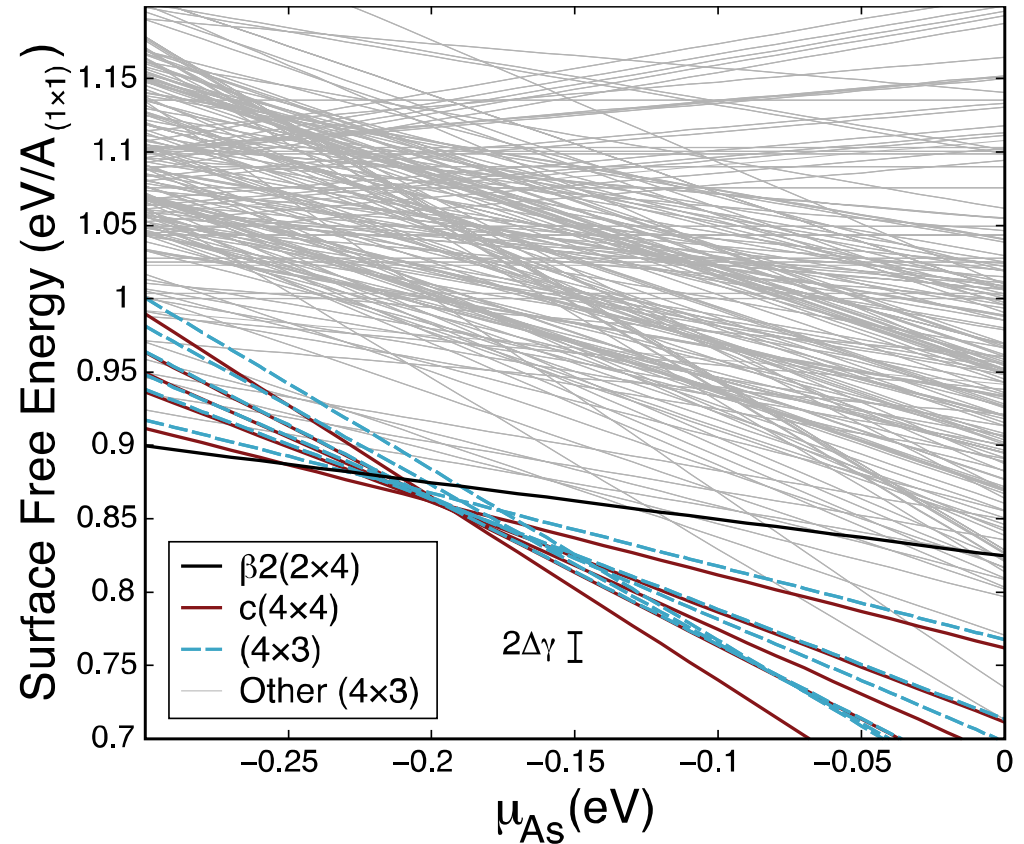
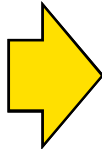
Experimentally
Observed Unit Cells



124 Reconstruction
Prototypes



$H\Psi = E\Psi$



Charge-neutral structural prototypes for observed geometries:
20 c(8x2), 20 c(4x4), 23 (4x2), 23 (2x4), and 124 (4x3).

DFT calculations performed using Vienna *ab initio* Simulation Package



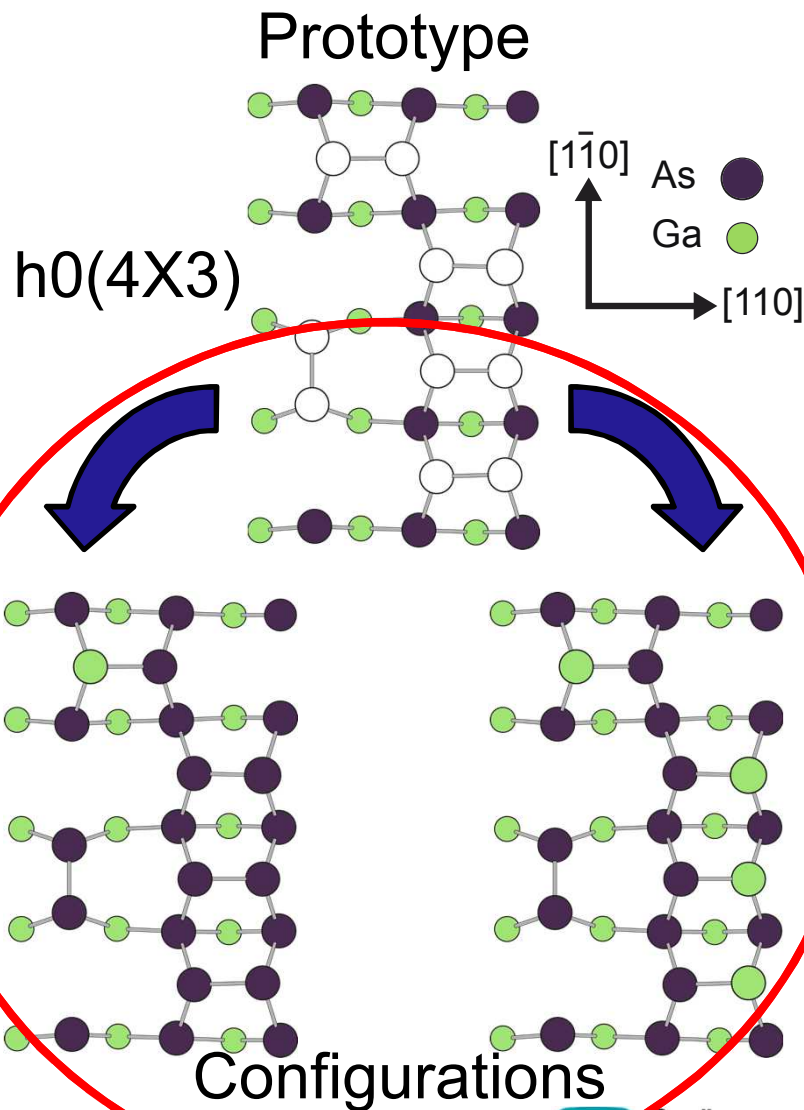
Systematic Sampling of Configurations For Low Energy Prototypes

Build a training set of configurations using DFT

Fit the cluster expansion to the training set

Perform Monte-Carlo using cluster expansion energies

Calculate quantities of interest (composition, free energy, ...)



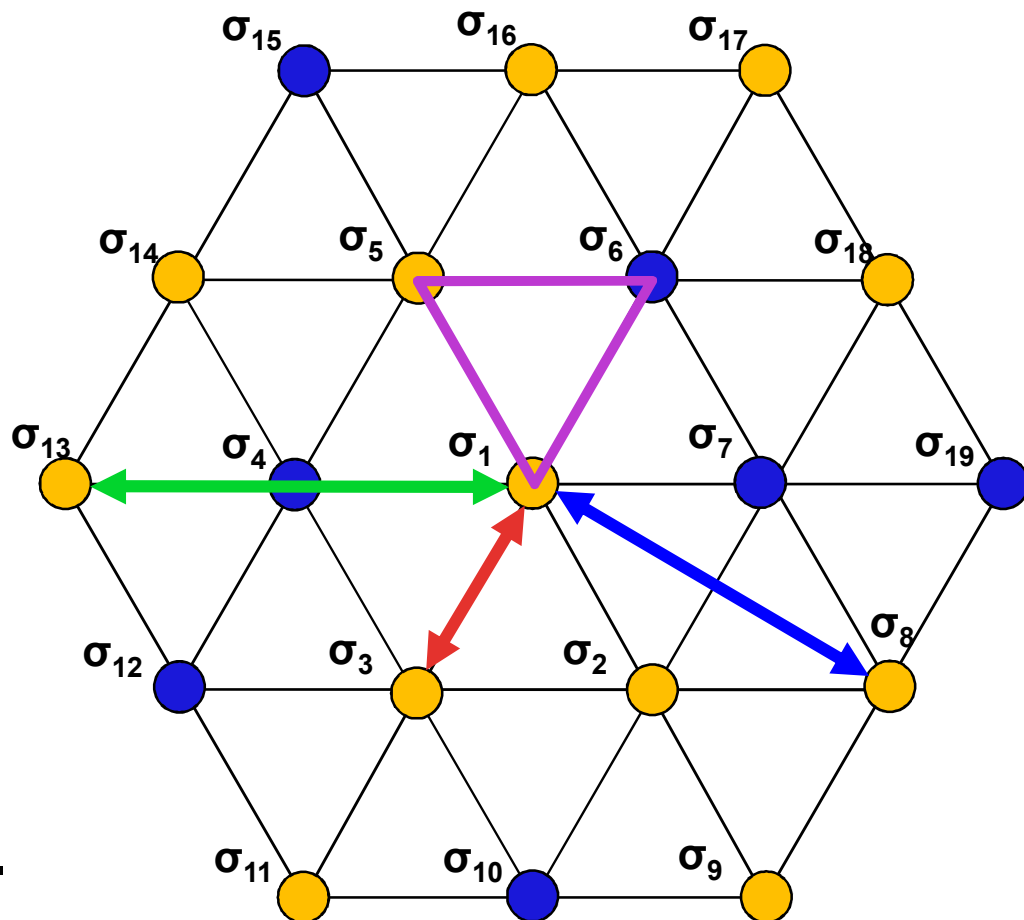


The Cluster Expansion

Interactions between sites are described by products of σ_i .

Fit interaction parameters to a database of DFT energies.

Monte-Carlo used to sample configurations.

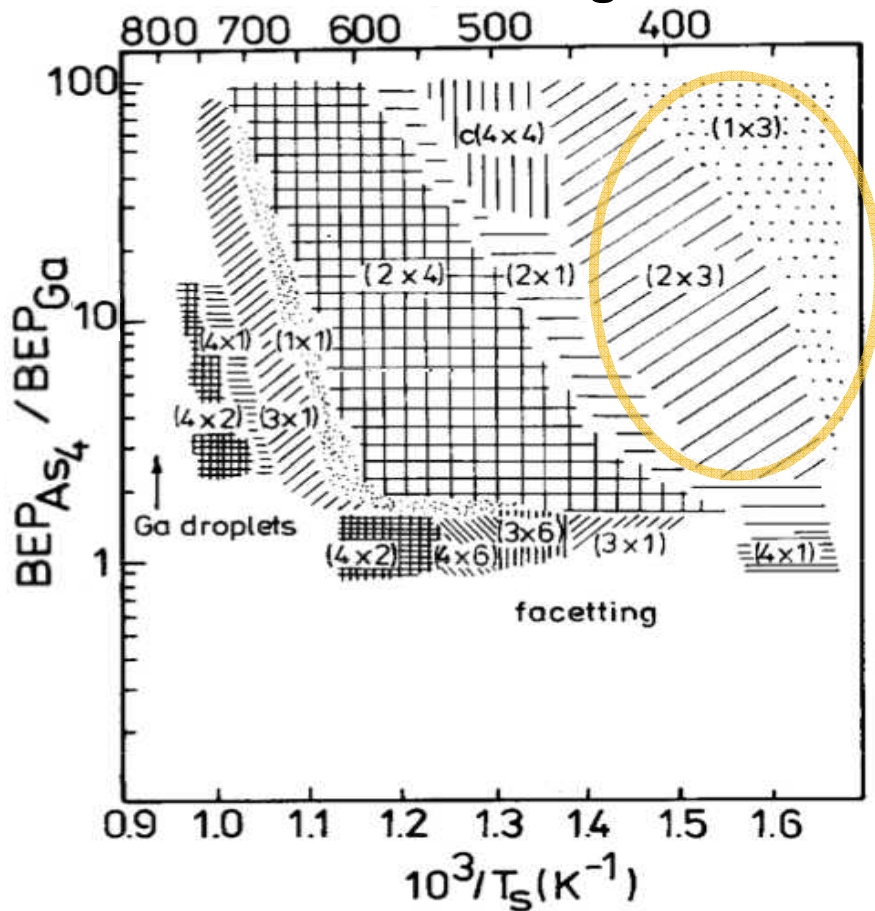


$$E = J_1 \sigma_1 + \textcolor{red}{J}_{1,3} \sigma_1 \sigma_3 + \textcolor{blue}{J}_{1,8} \sigma_1 \sigma_8 + \textcolor{violet}{J}_{1,5,6} \sigma_1 \sigma_5 \sigma_6 + \dots$$

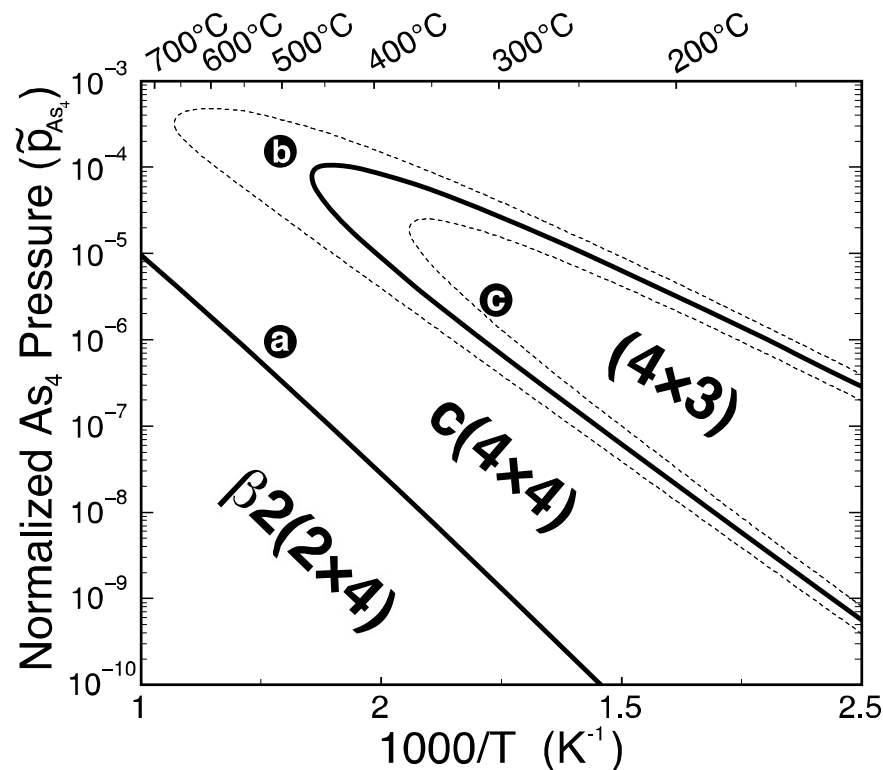


Theoretical (4X3) Consistent with Experiment

**Observed GaAs (001)
Phase Diagram**



**Calculated GaAs (001)
Phase Diagram**



Chizhov, Lee, Willis, Lubyshev, and Miller, *Phys. Rev. B*, 56, 1013 (1997).

J.C. Thomas, J.M. Millunchick, N.A. Modine, A. Van der Ven, Submitted to PRL.



Conclusions

- **We have developed a systematic method for predicting equilibrium surface atomic structure based on coupling DFT, rule-based enumeration, the Cluster Expansion, and Monte-Carlo**
- **A complete surface structure consists of a “Prototype” and a “Configuration”**
- **Our approach captures the effects of disorder due to non-zero temperature and alloying**
- **NEXT: We aim to systematically couple surface reconstruction and strain**