



# **Coupled Multiphase Flow and Geomechanics for Analysis of Caprock Damage**

**MJ Martinez, P Newell and JE Bishop**

**Engineering Sciences Center  
Sandia National Laboratories  
Albuquerque, NM, USA**

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# Outline

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1. Technical Challenges for CO<sub>2</sub> Sequestration
2. Potential leakage paths
3. Goal of predictive assessment of caprock integrity
4. Coupled flow and geomechanics analyses
5. Future work
6. Summary

# Technical Challenges for CO<sub>2</sub> Sequestration

## 1. Subsurface

- uncertain materials
- uncertain structures

## 2. Multiple scales

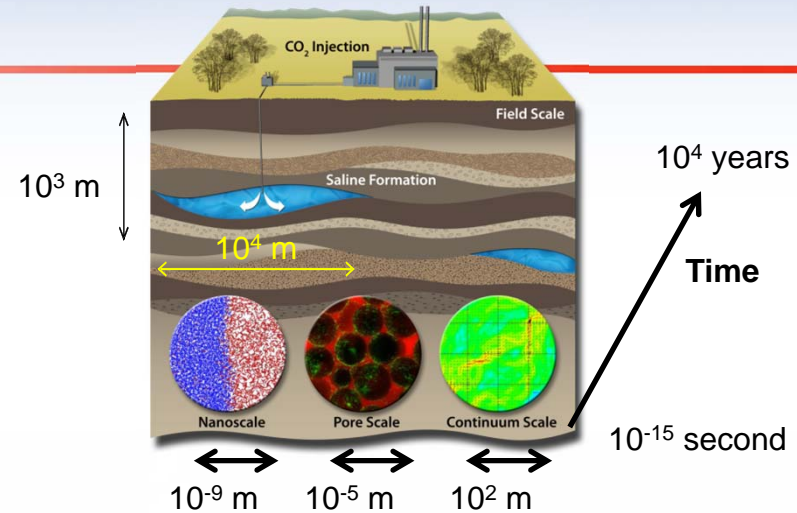
- time, space
- multi-scale analysis (e.g. homogenization) attempts to exploit any scale separation
- may not have scale separation → scale embedding with 'mortars'
- fracture is inherently multi-scale

## 3. Multiple physics

- geomechanics, geochemistry, biology
- solid mechanics, porous flow, chemical and biological reactions
- phase changes, localization, fracture

## 4. Dynamic, highly nonlinear

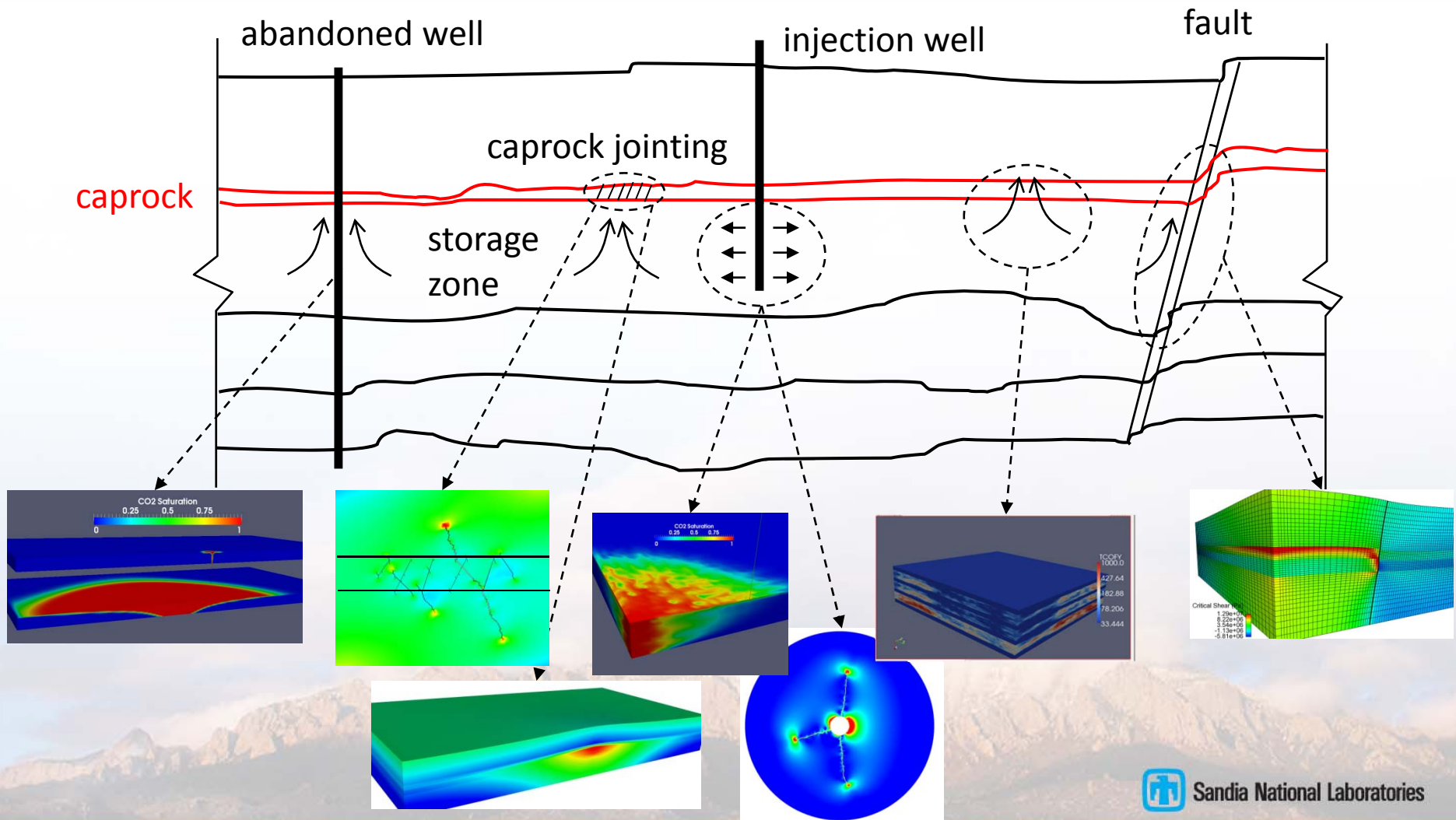
- instabilities, bifurcation phenomena, limit cycles, aperiodic behavior
- emergent phenomena



# Potential Leakage Paths for CO<sub>2</sub>

Primary CO<sub>2</sub> trapping mechanism is structural.

Scale: 1 km





# Goals

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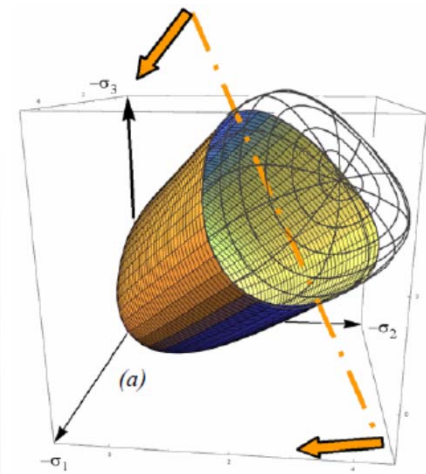
1. Predictive modeling capability for assessing caprock integrity
  - various field sites, general stratigraphy
  - assess injection scenarios
2. Assess potential leakage rate as a function of site characteristics and injection schedules
3. Assessment of mitigation scenarios
  - refine injection criteria



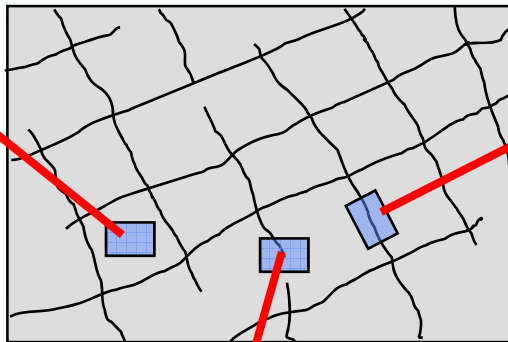
# Hydromechanical Coupling in Fractured Rock

## Bulk Constitutive Properties

- plasticity model
- limit surface
- effective stress, Biot coeff.



## Fractured Caprock



## Fracture contact properties

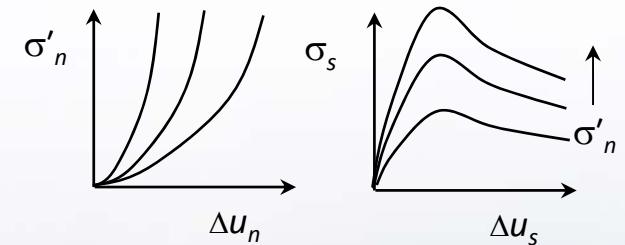
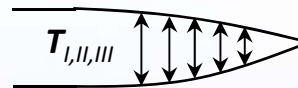
$$\sigma'_n = \sigma_n - p$$

A diagram showing a fracture contact under normal stress  $\sigma_n$  and shear stress  $\sigma_s$ . The normal stress is represented by downward arrows, and the shear stress by horizontal arrows. The displacement components are  $\Delta u_s$  (shear) and  $\Delta u_n$  (normal). The contact is shown as two blocks, one on top of the other, with a blue base.

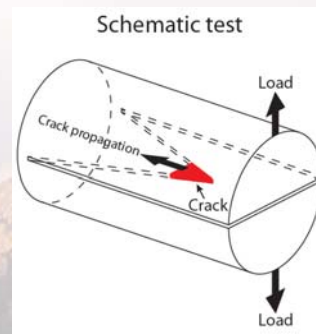
$$\sigma_s = \sigma_s \{\Delta u_s, \Delta u_n\}$$

$$\sigma'_n = \sigma'_n \{\Delta u_s, \Delta u_n\}$$

## Crack-tip Properties



## Fracture Toughness



## Cohesive Properties



# Hydromechanical Coupling Scheme In Sierra Mechanics

## Solid Mechanics (Sierra/Adagio)

Large strain finite element  
nonlinear elastic/plastic solid  
mechanics; Sandia GeoModel

Effective stress  
 $\sigma'_n = \sigma_n - \lambda p$

- Displacement field
- Effective permeability

## Transfer Function

- Pore pressure field

## Fluid Mechanics (Sierra/Aria)

Vertex-centered control  
volume method for multiphase  
flows in heterogeneous porous  
media

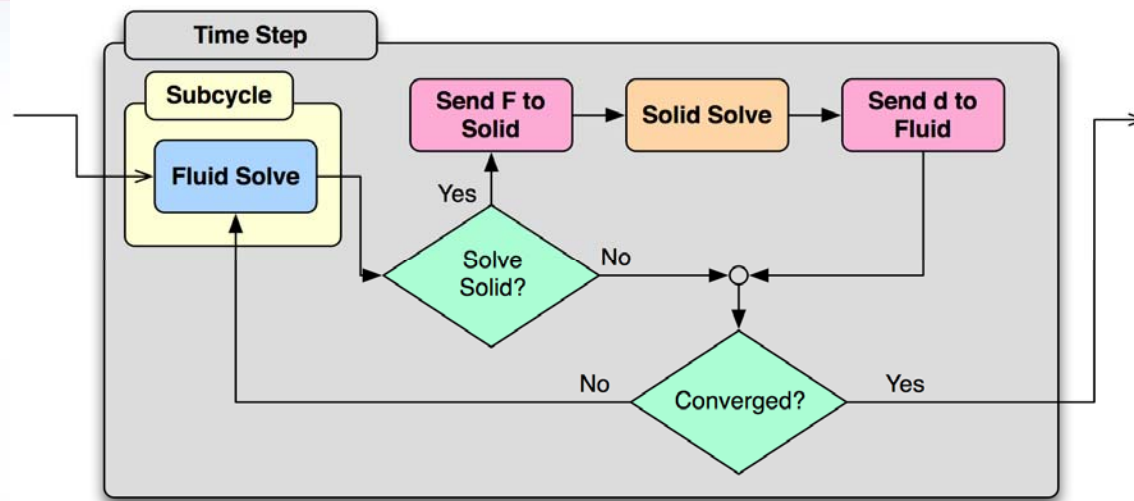
$k_{eff}(\sigma_n)$   
 $\phi(\det F)$



- Transfer function facilitates data movement between Sierra modules
- Sierra modules can use different grids
- Both solve on deforming grid systems



# Conditional Loose Coupling with Nonlinear Iteration and Subcycling



```

Begin System Main
  Use Initialize MyInit
  Begin Transient MyTransient
    Begin Nonlinear MyNonlinearLoop
      Begin Subcycle MySubcycle
        Advance AriaRegion
      End
      Transfer ForceAriaForceAdagio when "Solve_Solid()"
      Advance AdagioRegion when "Solve_Solid()"
      Transfer DispAdagioDispAria when "Solve_Solid()"
    End
  End
End
  
```



# CO<sub>2</sub> Leakage Through an Abandoned Well

## Flow Benchmark Problem

### Reference Problem Description:

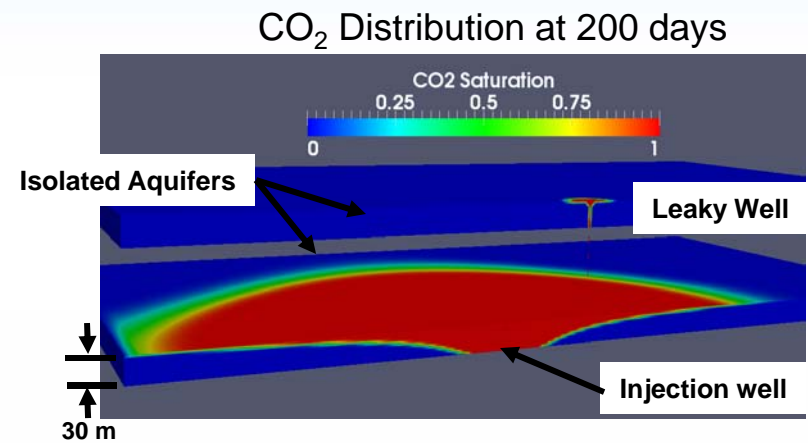
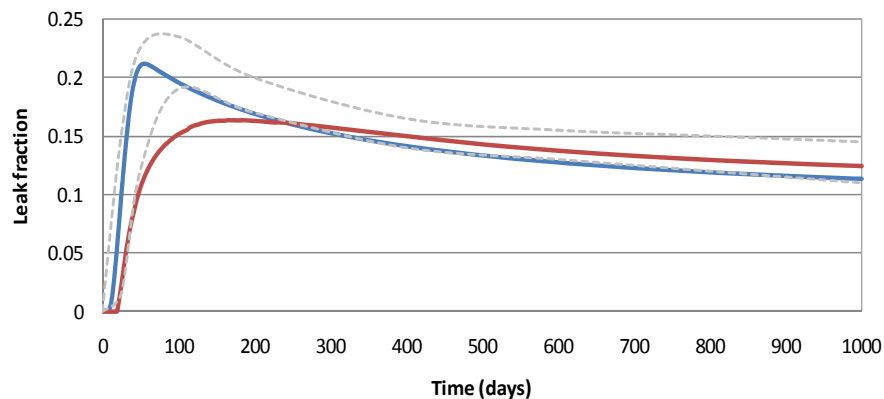
- 3D model of leakage during supercritical CO<sub>2</sub> injection into a brine aquifer
- Single CO<sub>2</sub> injection well
- Two aquifers separated by an aquitard
- One leaky well, 100 m from injection well
- 1200 day injection

### Assumptions:

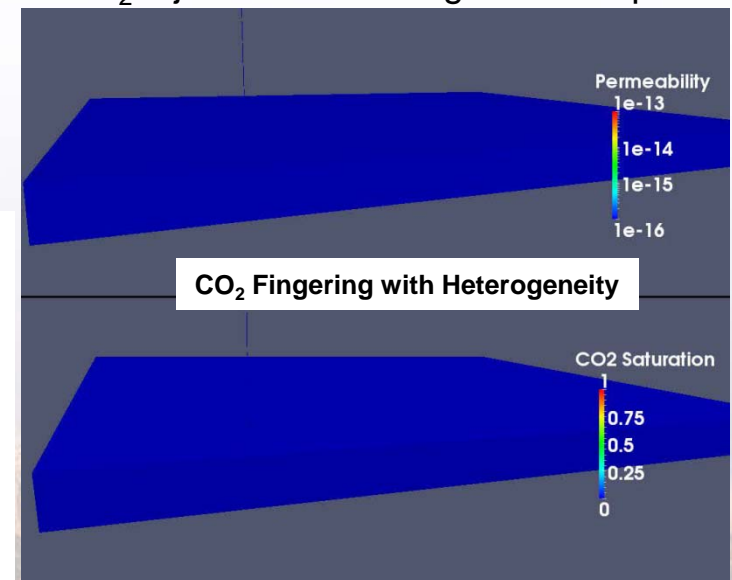
- Isothermal injection process
- CO<sub>2</sub> and brine immiscible phases
- Isotropic formation
- Neglect capillary pressure

### Results:

- Computed leakage rate and arrival times compare well with benchmark study:
- Max leakage: 0.214% at 56 days
- Leakage at 1000 days: 0.116%
- Arrival time: 11.5 days



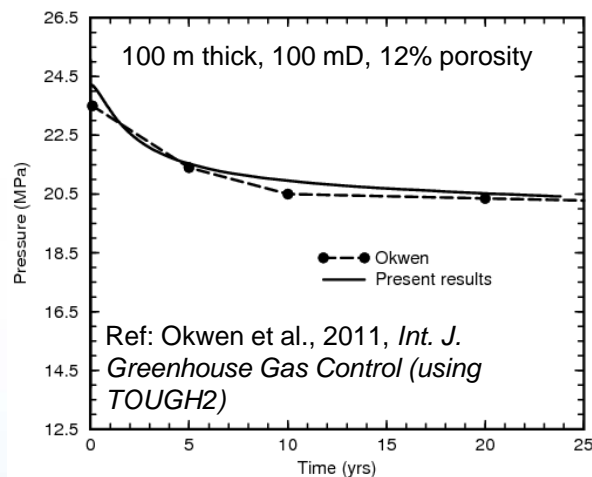
### CO<sub>2</sub> Injection in Heterogeneous Aquifer



# Verification Problems

## CO2 Injection into a Confined Saline Aquifer

Near-Wellbore Pressure

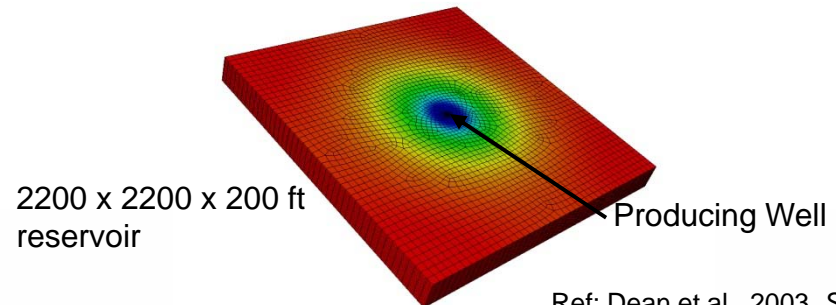


### Features:

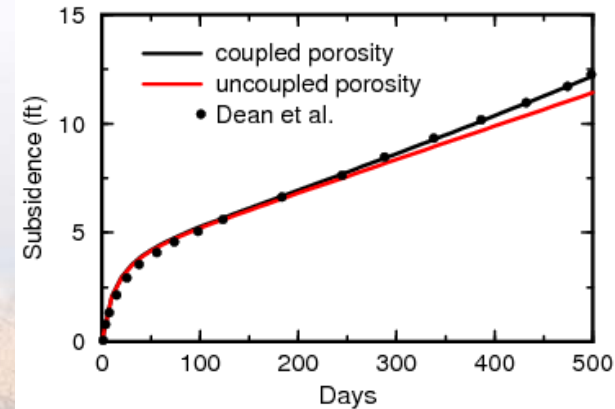
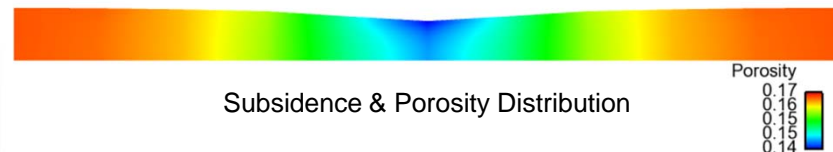
- fluid properties @ 45C (Okwen: TOUGH2)
- 100 kg/s ( 3.16 MMT/yr)
- Cap. Pressure: van Genuchten  $P_0=19.6$  kPa
- $k_{rl}$ : Van Genuchten,  $Slr=0.3$ ,  $\lambda=0.457$
- $k_{rg}$ : cubic  $Slr=0.3$  (Okwen: Brooks-Corey)

## Subsidence due to Fluid Withdrawal

Coupled Flow and Geomechanics

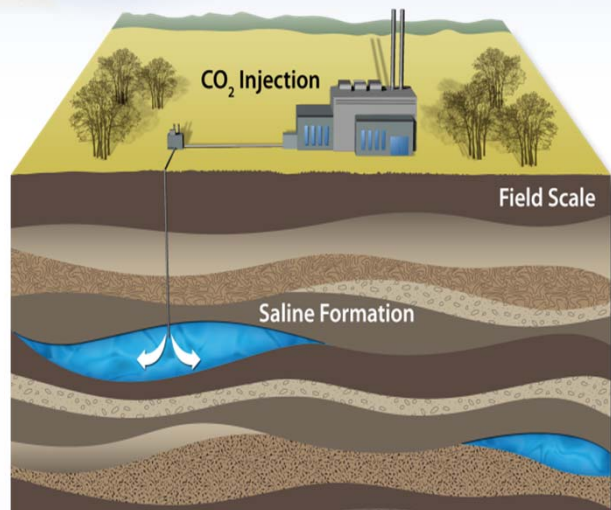


Ref: Dean et al., 2003, *SPE -79709*

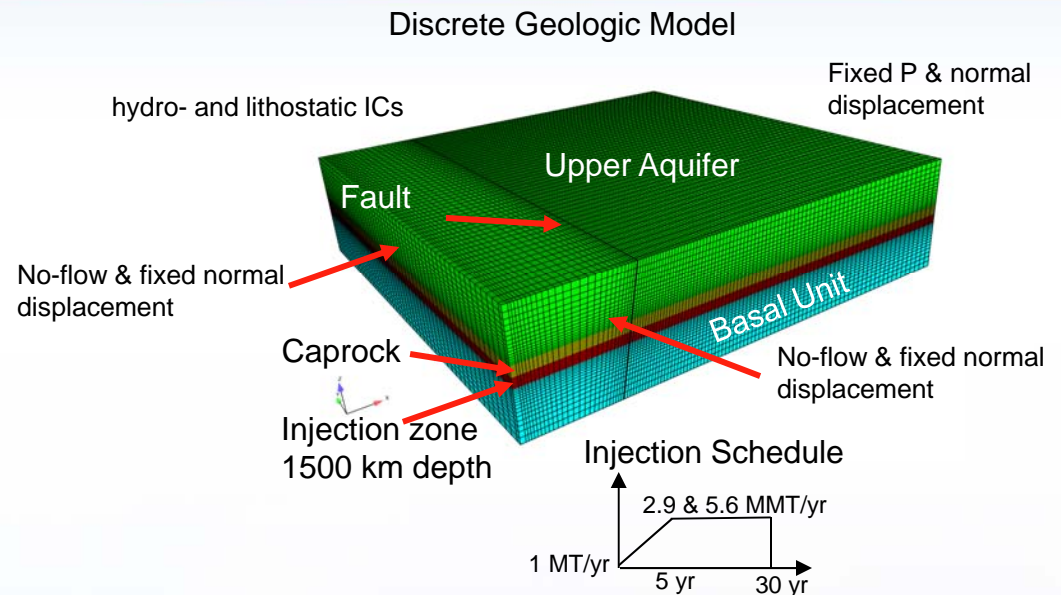
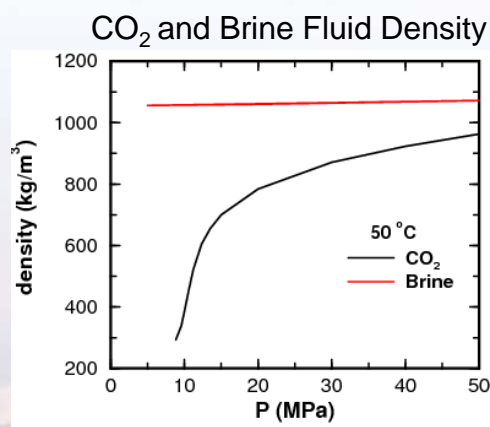


# Flow and Geomechanics in Jointed Rock

## Model Problem



Model problem definition showing conceptual stratigraphy (left), and model problem geometry.



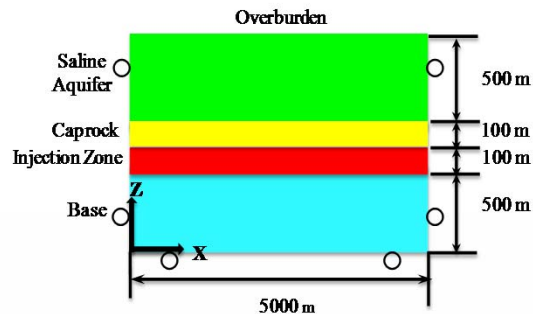
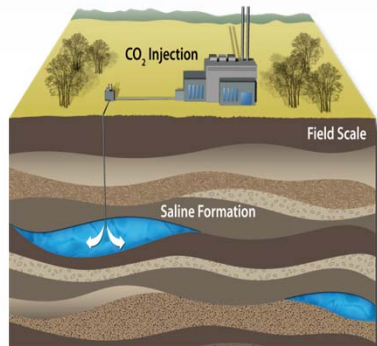
Overburden

Layer	$\phi$	$k$ (mD)	$E$ (GPa)	$\nu$	Thickness (m)
Upper Aquifer	0.15	20-100	20	0.20	500
Caprock	0.05	0.001	50	0.12	100
Injection Zone	0.15	20-100	20	0.20	100
Base	0.1	0.01	50	0.12	500

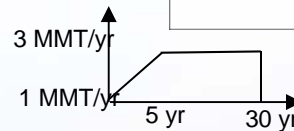
15 km

# Coupled Flow and Geomechanics

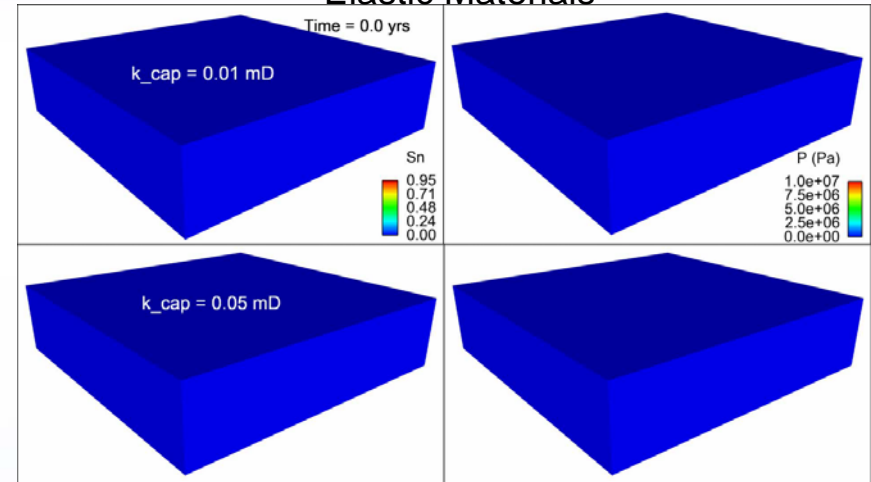
## Flow, CO<sub>2</sub> Transport and Deformation



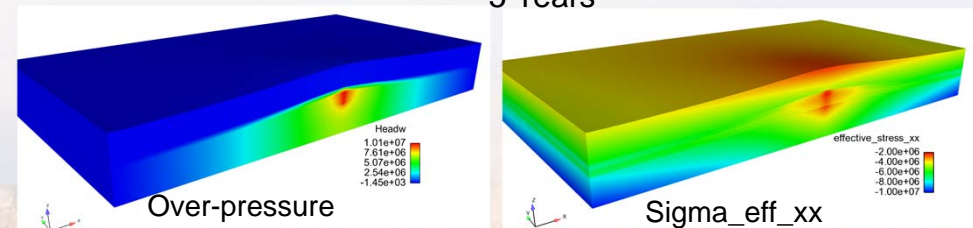
Model problem definition showing conceptual stratigraphy (left), and model problem geometry (right, not to scale).



### CO<sub>2</sub> saturation, Overpressure & Displacement Elastic Materials



### CO<sub>2</sub> Leakage in Jointed Caprock 5 Years

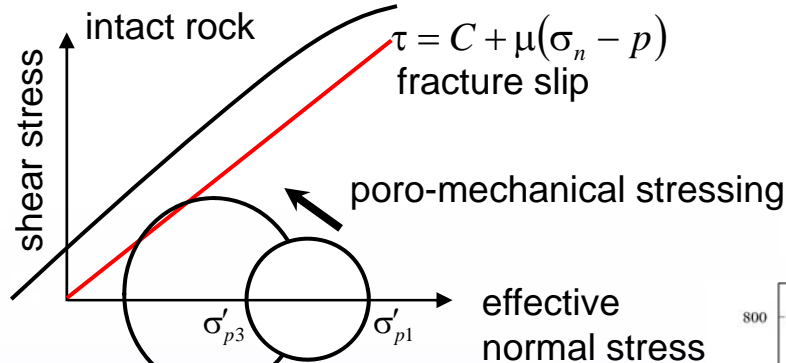




# Coupled Flow and Geomechanics

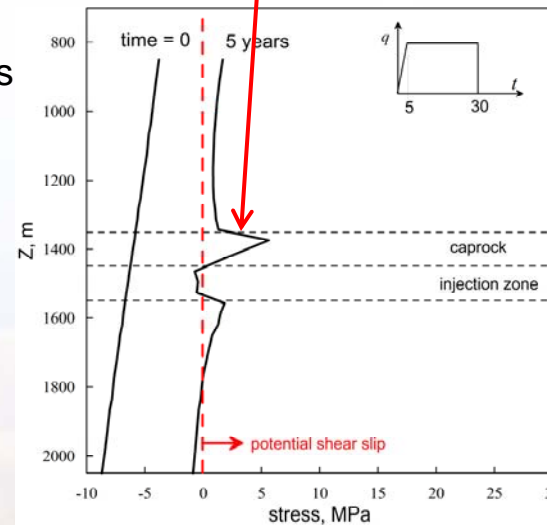
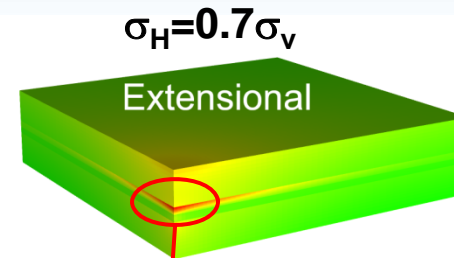
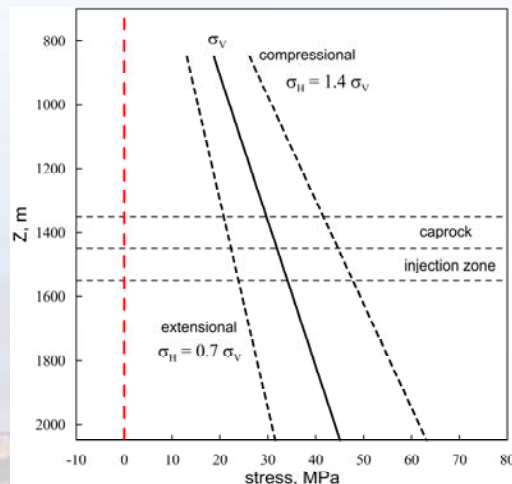
## Effect of Regional Stress State

### Linear Mohr-Coulomb

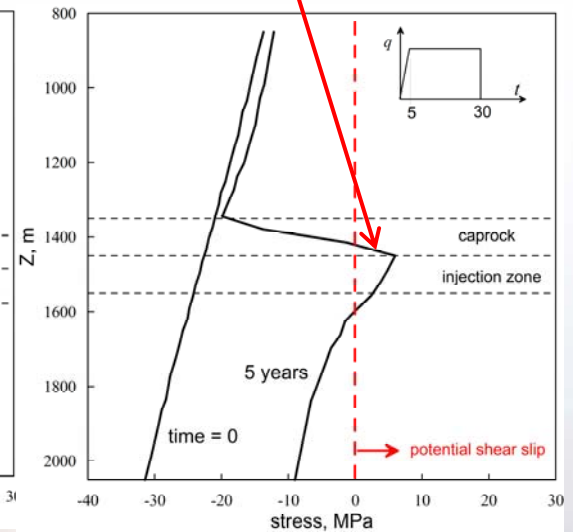
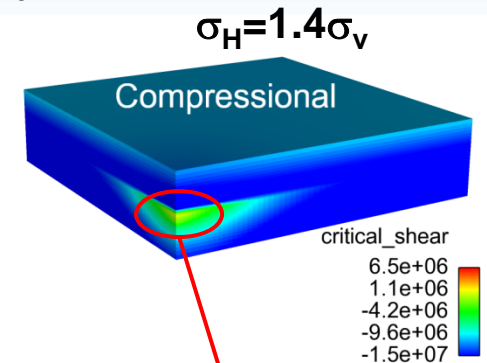


Critical Shear

$$\sigma'_{p1} - 3\sigma'_{p3} > 0$$



Year 5



Extensional regional stresses are more dangerous to caprock integrity

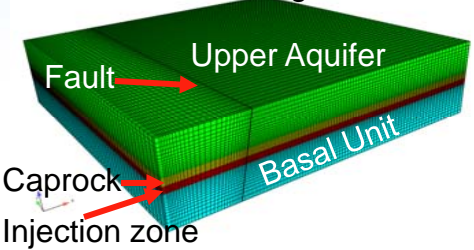


# Coupled Flow and Geomechanics

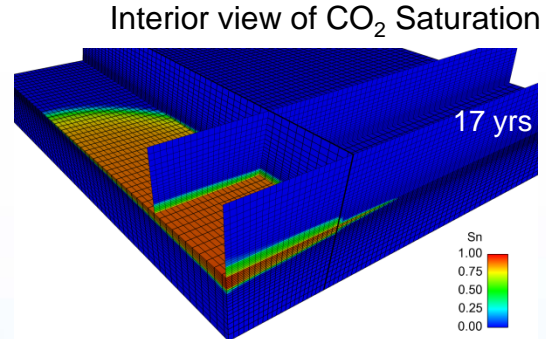
## *Hydromechanical Effects of Faults*

Some faults could go undetected and may pose a risk to sequestration of CO<sub>2</sub> by reactivation due to injection pressures. This study considers possible hydromechanical effects due to a low and high permeability fault.

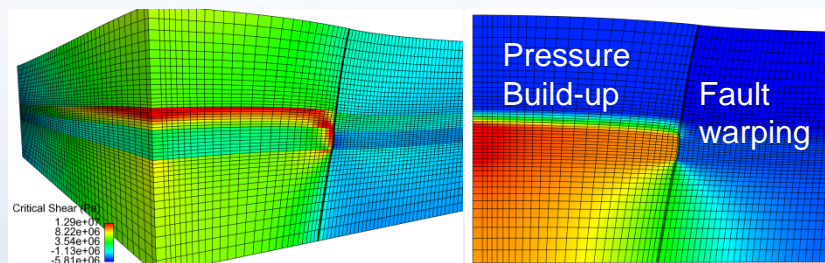
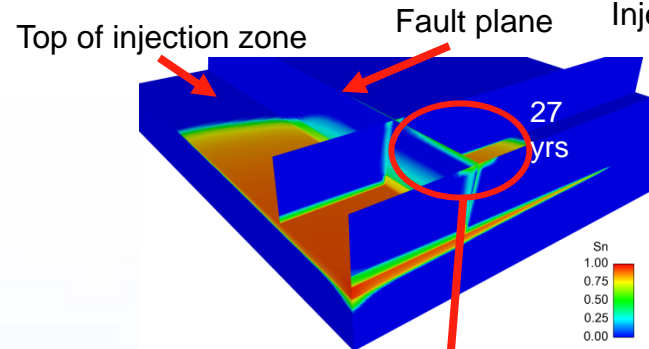
Discrete Geologic Model



Low Permeability Fault

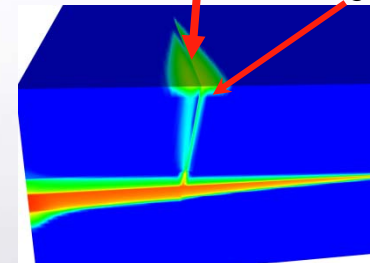


High Permeability Fault



Exterior view

Leaking Fault

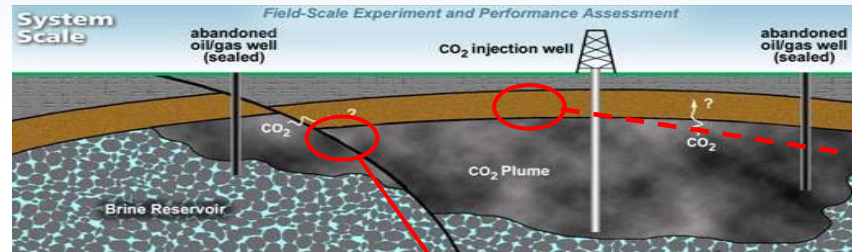


**Low permeability** fault impedes CO<sub>2</sub> injection, diverts flow along fault and builds pressure behind the fault, thereby shearing/warping the fault and inducing critical shear failure in both the caprock and fault.

**High permeability** fault creates a pathway for leakage of CO<sub>2</sub> through the caprock, ultimately pooling at the top of the upper aquifer, which is capped by an impermeable boundary.

# Deformation Dependent Caprock Permeability due to Jointing

Change in joint aperture due to CO<sub>2</sub> injection causes a change in caprock permeability (anisotropic).

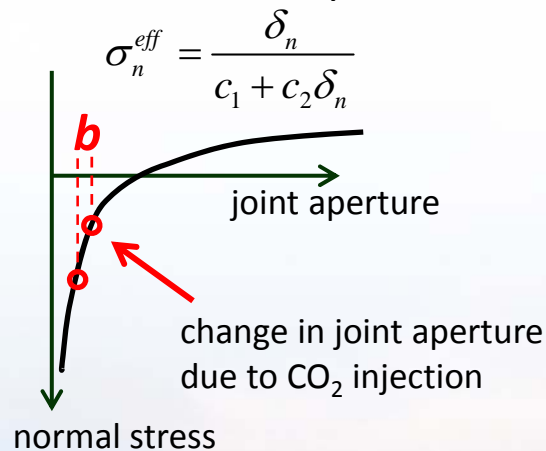


faulting

Caprock jointing

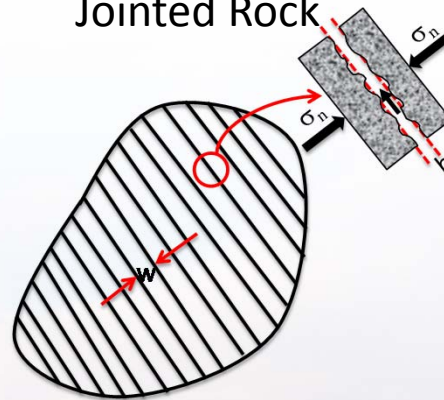


Stress vs. Joint aperture



$$\mathbf{k}_{eff} = k\mathbf{I} + \frac{b^3}{12W}(\mathbf{I} - \mathbf{n} \otimes \mathbf{n})$$

Conceptual Model of Jointed Rock



Multiple joints sets can be modeled

Change in effective stress with CO<sub>2</sub> injection causes a change in caprock stiffness, normal to fracture plane.

$$K_n = K_{ni} \left( 1 - \frac{\sigma_n^{eff}}{K_{ni} V_m} \right)^2$$

$$\dot{\boldsymbol{\epsilon}}^{joint} = \frac{1}{W K_n} \mathbf{P} \bullet \dot{\boldsymbol{\sigma}} \bullet \mathbf{P}$$

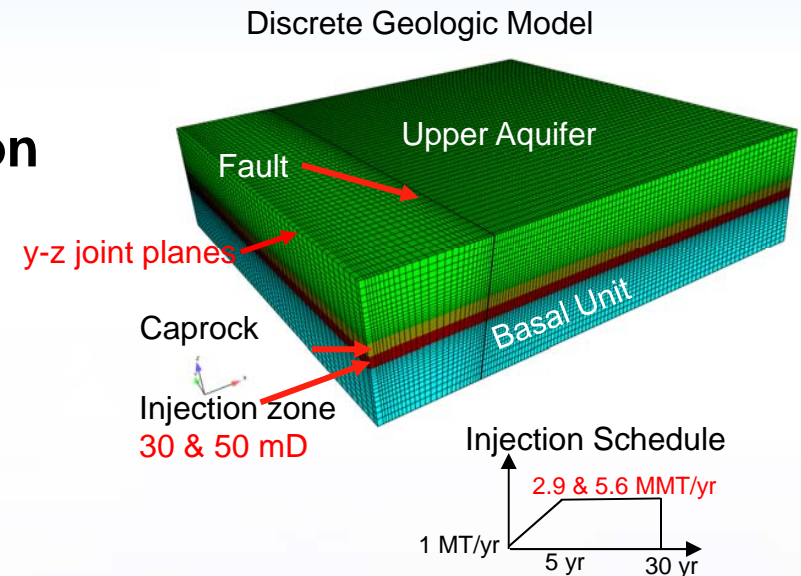
$$\mathbf{P} = \mathbf{n} \otimes \mathbf{n}$$

# ***CO<sub>2</sub> Injection with a Jointed Caprock***

## ***Effect of injection rate and permeability***

**Investigate the relationship between injection zone permeability and injection rate**

- single joint set (vertical joints in y-z plane)
- two injection rates: 2.85 & 5.6 MMT/yr
- two injection zone permeabilities:
  - 30 and 50 mD
- Van Genuchten capillary pressure
  - $P_{\text{entry}} = 5\text{kPa}$  all layers
- Cubic relative permeability



Overburden

	$\phi$	$k$ (mD)	$E$ (GPa)	$\nu$	
Upper Aquifer	0.15	20-100	20	0.20	500 m
Caprock	0.05	0.001	50	0.12	100 m
Injection Zone	0.15	20-100	20	0.20	100 m
Base	0.1	0.01	50	0.12	500 m

15 km

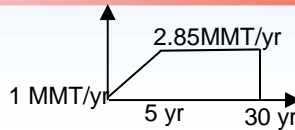


# Simulation Results

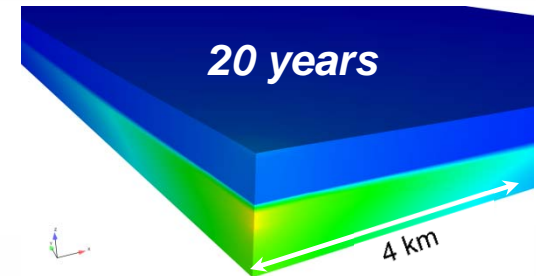
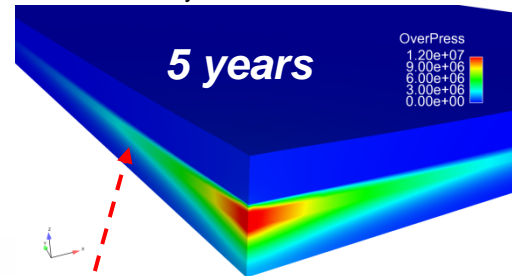
## Joint Activation Case

### Features:

- Single joint set in **y-z** plane
  - $K_n=15$  Gpa,  $W = 1$  m
- Injection zone perm: **30 mD**
- Max. injection rate: **2.85 MMT/yr**

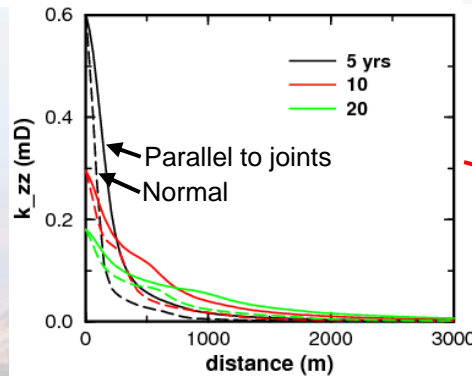
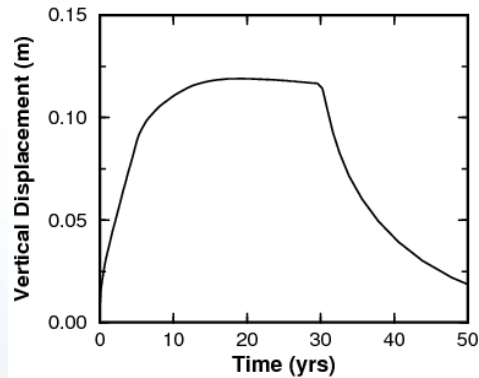
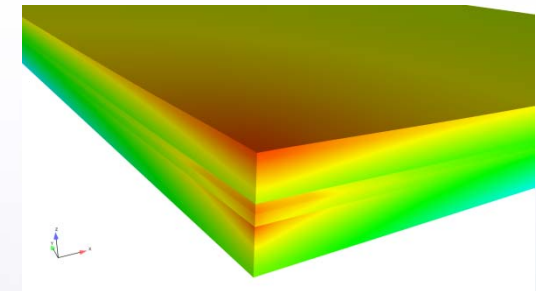
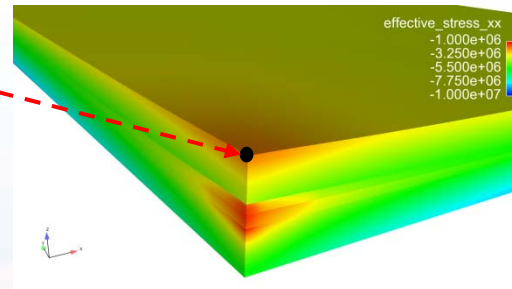


### Over-Pressure

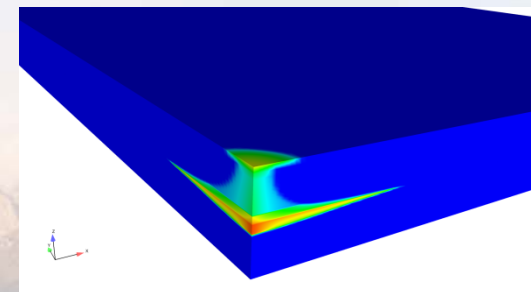
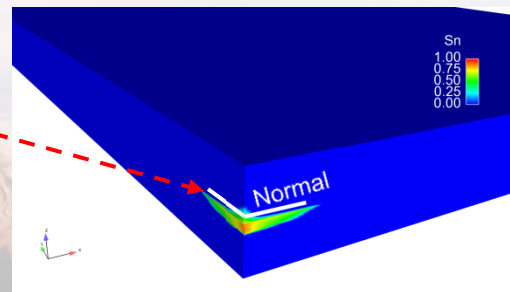


y-z joint planes

### $\Sigma_{eff\_xx}$

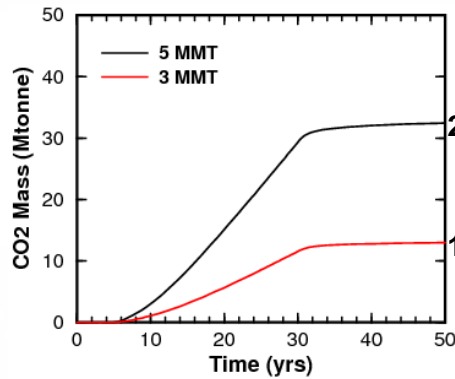


### CO2 Saturation



# Pressure, Mass Budget and Leakage

Cumulative CO<sub>2</sub> Leaked

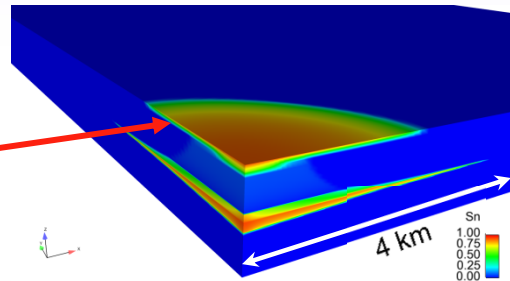


20%

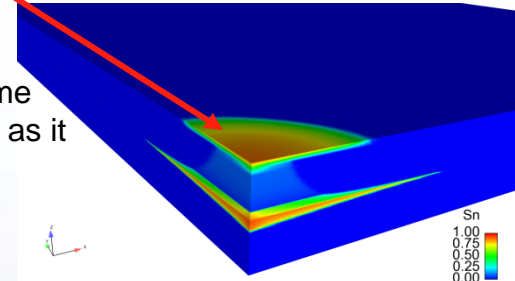
16%

CO<sub>2</sub> volume increases as it rises

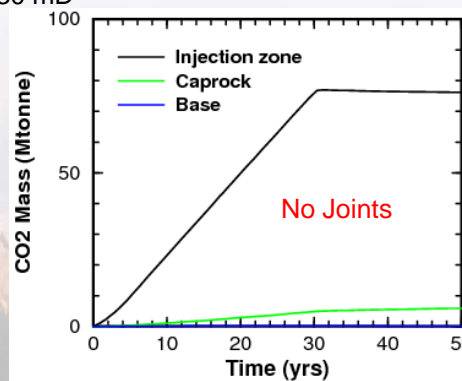
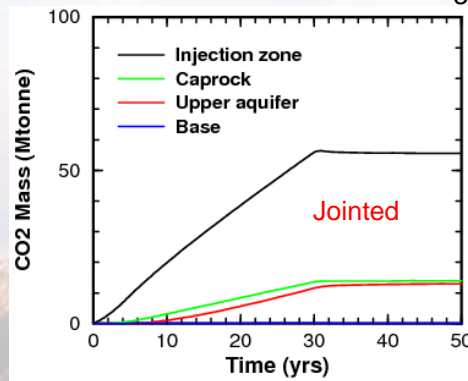
5 MMT 50 mD



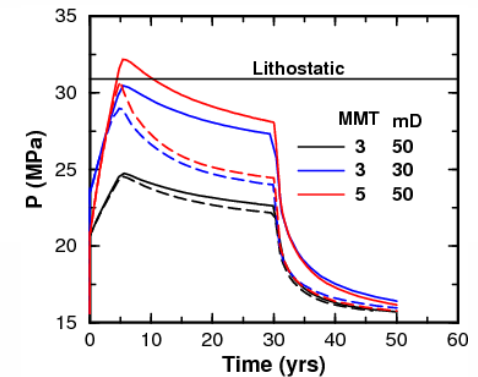
3 MMT 30 mD



CO<sub>2</sub> Mass Budget  
3 MMT 30 mD



Near-Wellbore Pressure

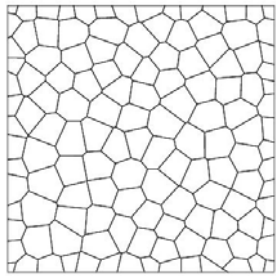


- Joints activated near the tension limit
- Joint activation relieves pressure

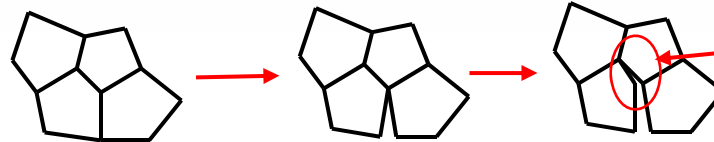


# Future Directions: Methods for Modeling Fracture Growth in Disordered Materials

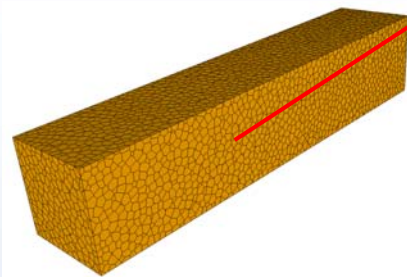
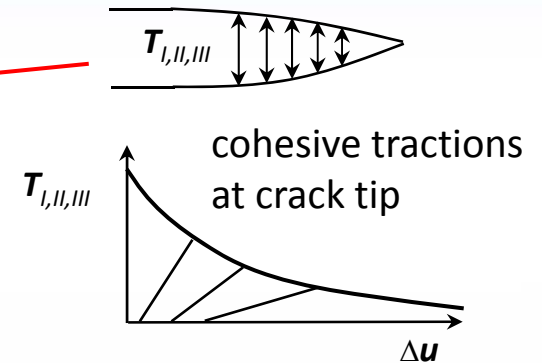
(JE Bishop)



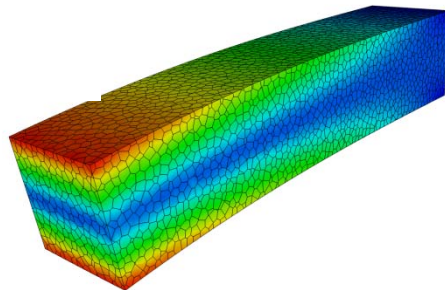
randomly closed packed Voronoi mesh



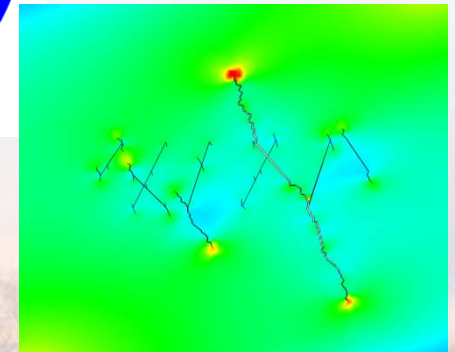
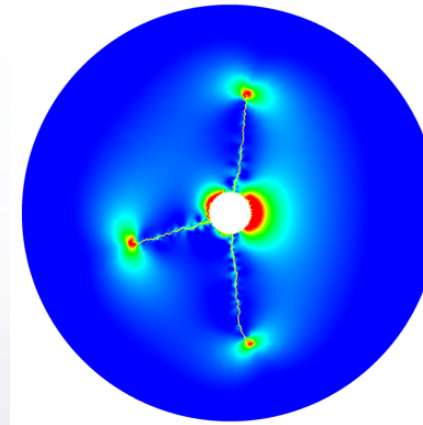
changing mesh connectivity



finite-element shape function

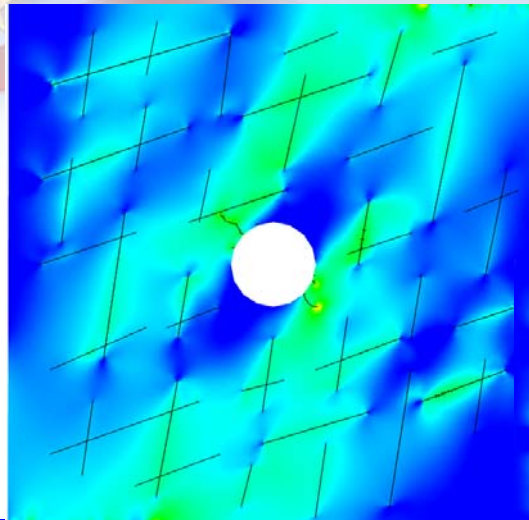


beam-bending verification problem

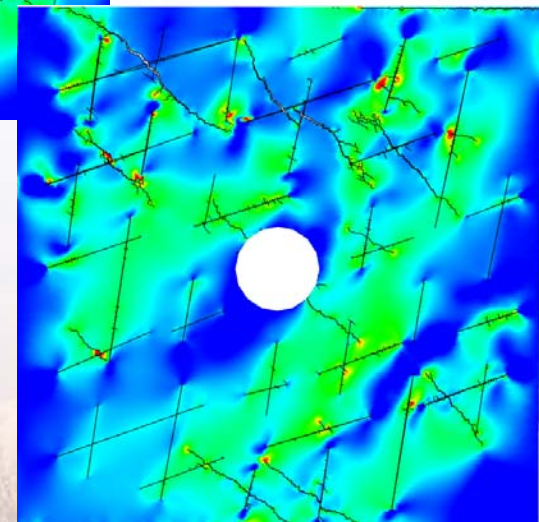
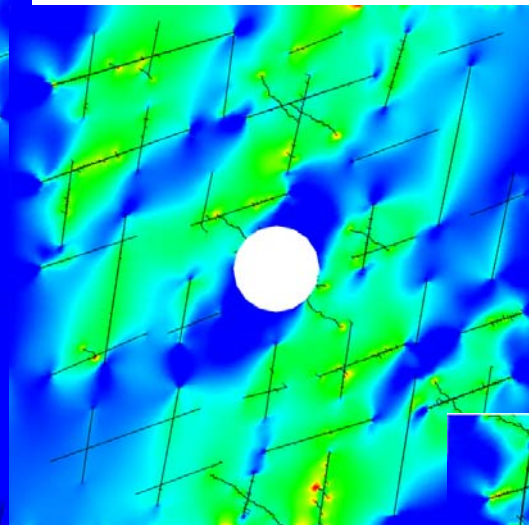


fluid-induced fracture simulations

# Dynamic Fracture Growth in Disordered Materials



increasing stress



play movie

max\_p

8.00

6.00

4.00

2.00

0.00



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# Summary

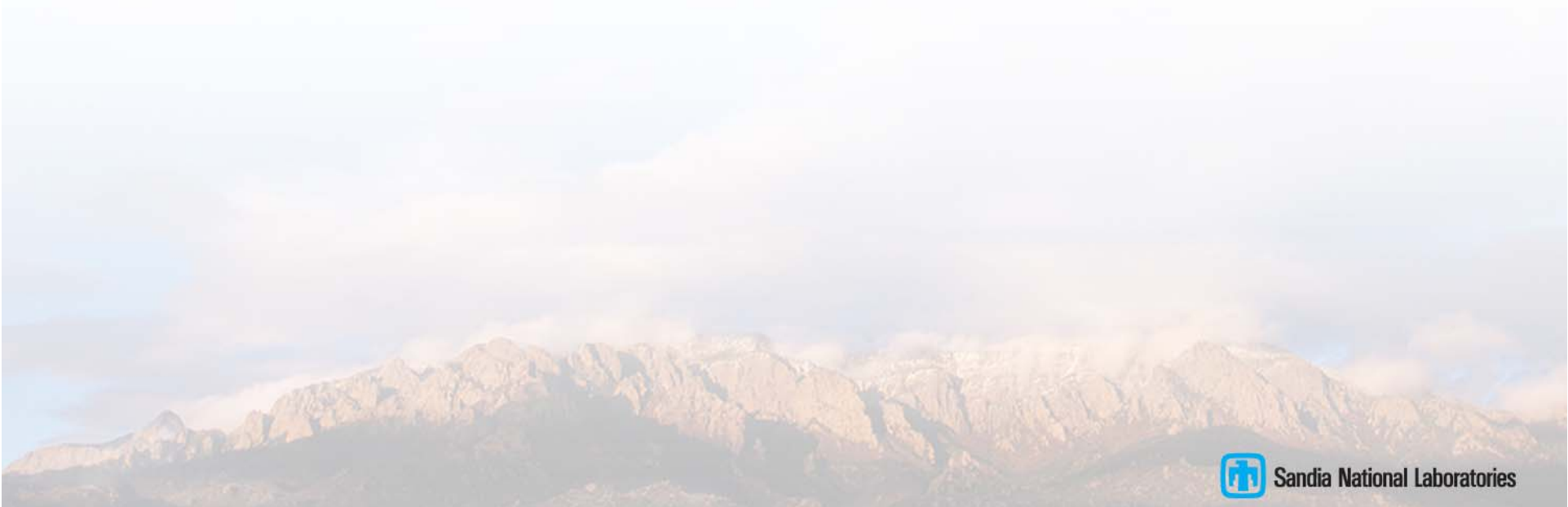
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1. An important scientific research question for the feasibility of CO<sub>2</sub> sequestration is assessment of the integrity of the caprock.
2. Problem is inherently multi-physics and multi-scale (space and time). Fluid-structure interaction is important, both at the field scale and micro-scale. Requires a multi-disciplinary team of researchers.
3. A number of new numerical methods are under development for modeling fracture activation, nucleation and propagation in heterogeneous media with coupled fluid flow for continuum and/or discrete representations of fractures.



# Backup Slides

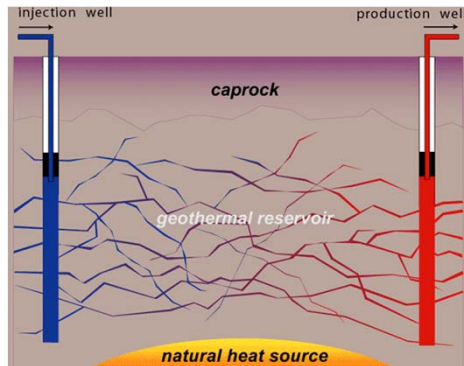
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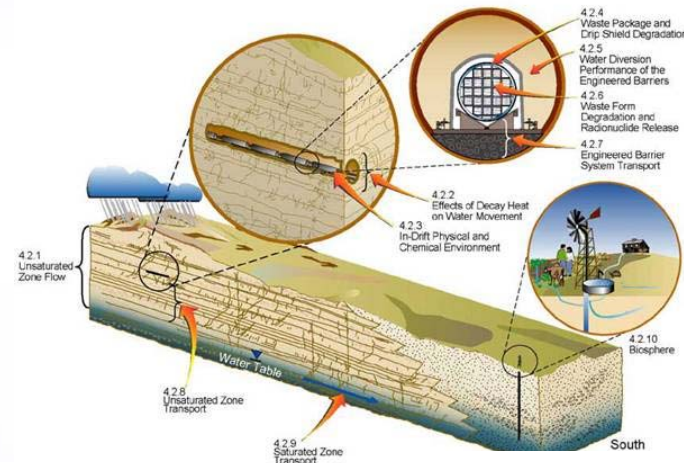


# Geoscience Applications at SNL

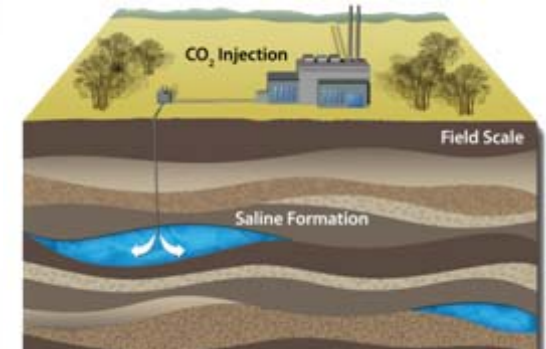
## Engineered Geothermal



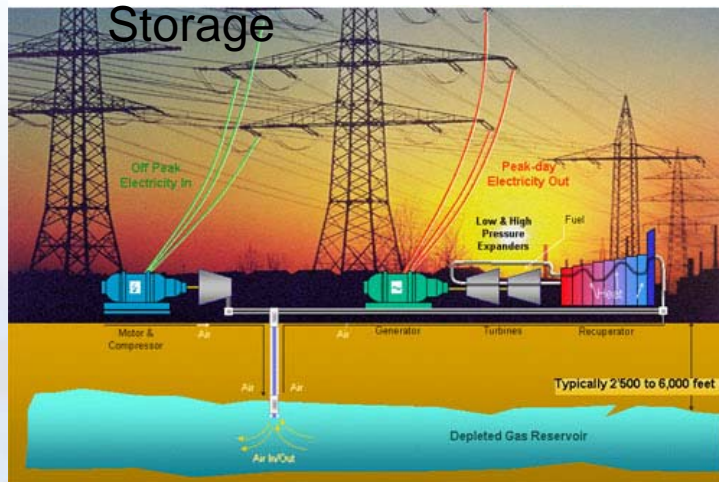
## Nuclear Waste Isolation



## CO<sub>2</sub> Sequestration

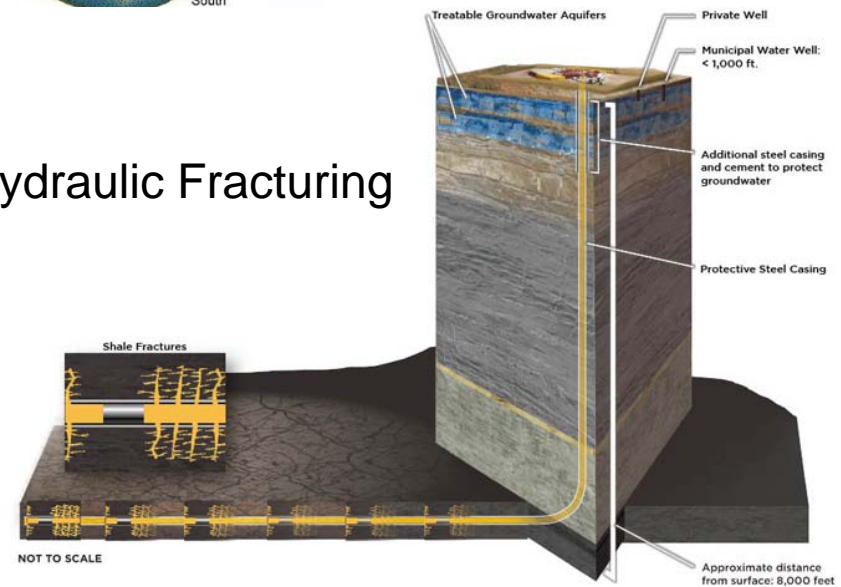


## Compressed Air Energy Storage



Derek Sept. 2009

## Hydraulic Fracturing



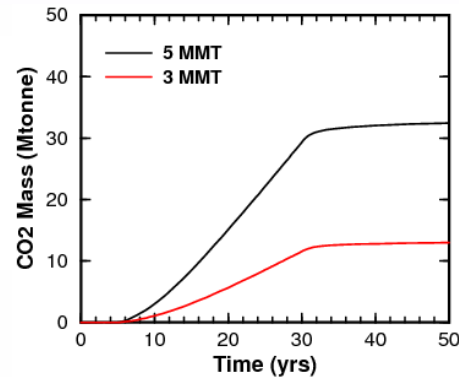
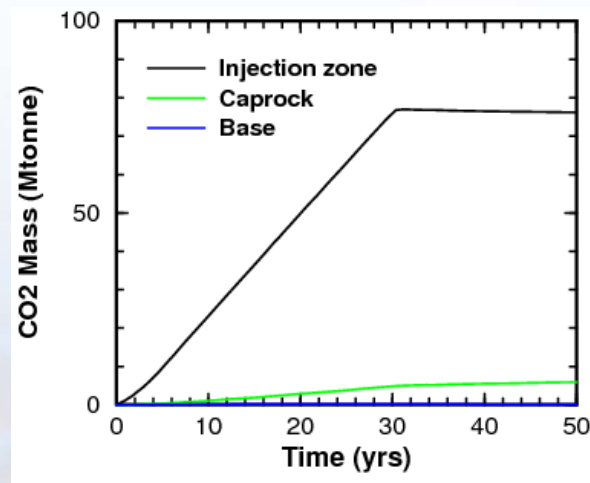
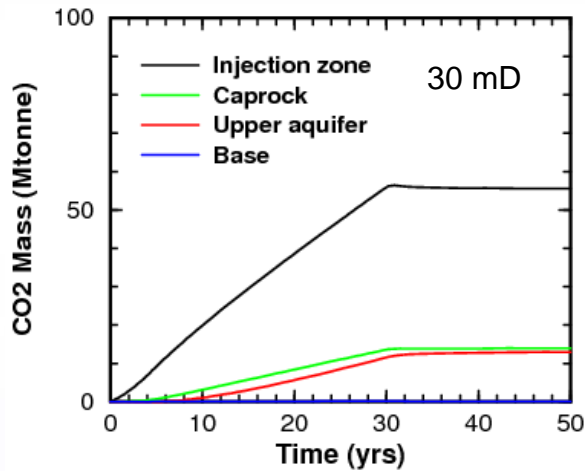
<http://www.hydraulicfracturing.com>

Sandia National Laboratories

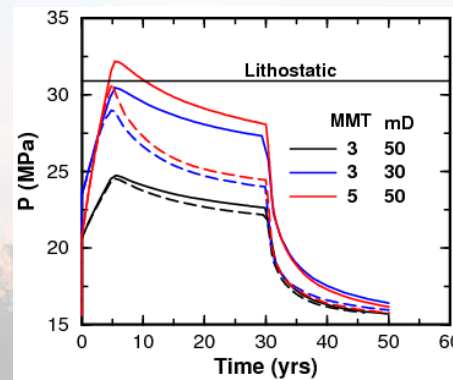


# Mass Budget and Leakage

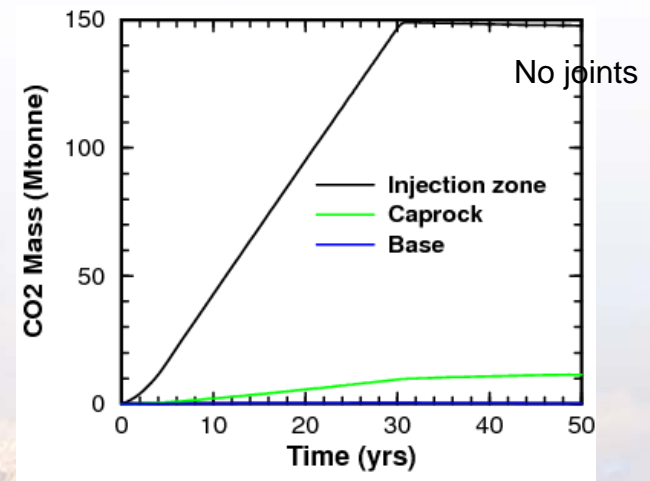
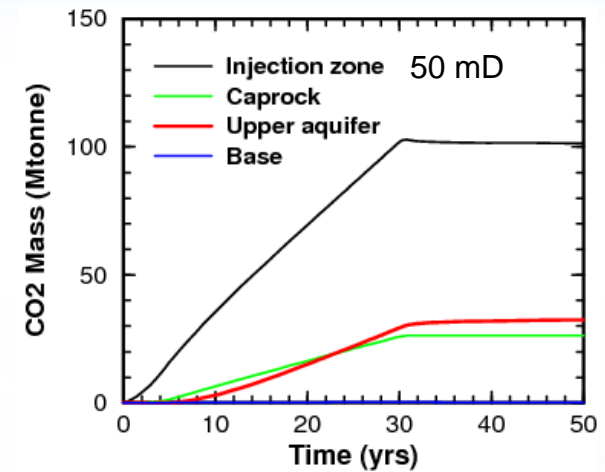
3.1 MMT/yr



No joints



5.6 MMT/yr



# Aria Porous Flow Physics

## Immiscible Flow

### Mathematical Model

- **Two-Phase Immiscible Mass Balances:**

$$\frac{\partial(\rho_w \phi S_w)}{\partial t} = \nabla \cdot \left( \rho_w \frac{k_{rw}}{\mu_w} \mathbf{k} \cdot (\nabla p - \rho_w \mathbf{g}) \right) + Q_w$$

$$\frac{\partial(\rho_n \phi S_n)}{\partial t} = \nabla \cdot \left( \rho_n \frac{k_{rn}}{\mu_n} \mathbf{k} \cdot (\nabla p + \nabla p_c - \rho_n \mathbf{g}) \right) + Q_n$$

- **Thermophysical property models (new models are easily incorporated):**

$$\rho_w = \rho_{w,0} (1 + \kappa_{Tw} (p - p_o))$$

$$\rho_n = \rho_{n,0} (1 + \kappa_{Tn} (p_n - p_{n,o}))$$

$$p_n = p + p_c(S_w)$$

$$S_w = 1 - S_n$$

$$\phi = \phi_0 (1 + C_r (p - p_0))$$

# Overview of Geomechanics in Adagio

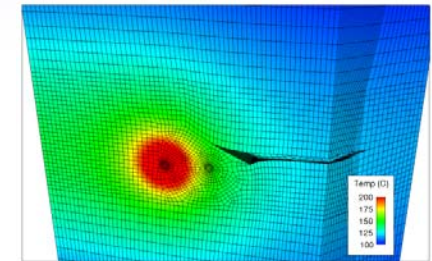
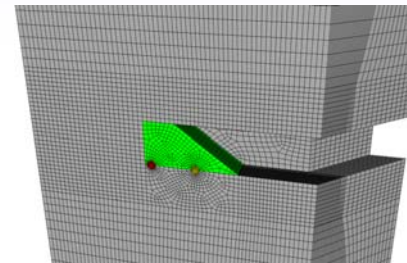
## Features:

- Large deformation, large strain kinematics
- Robust contact algorithms (both detection and application)
- Based on iterative (matrix-free) solvers with low order hourglass stabilized 8-node hexahedron element
- Efficient constitutive model implementations

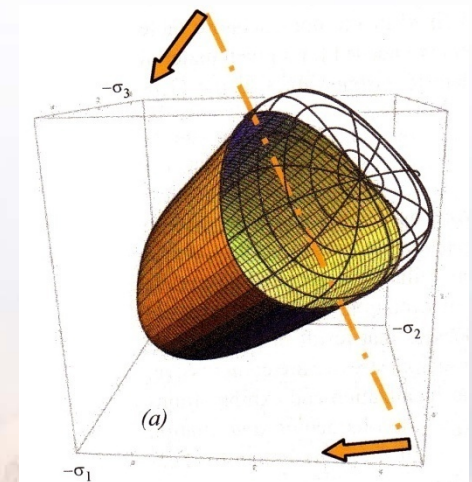
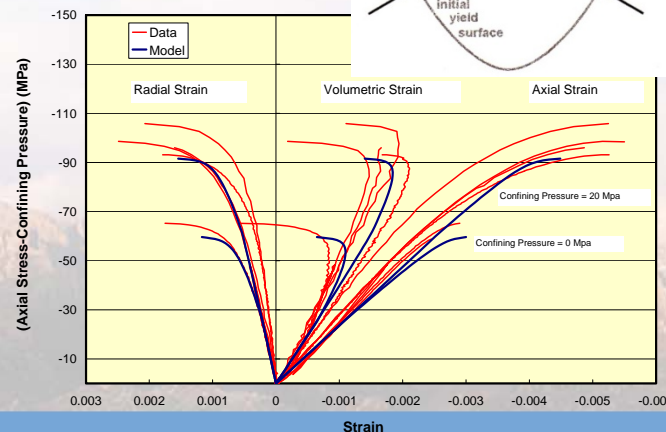
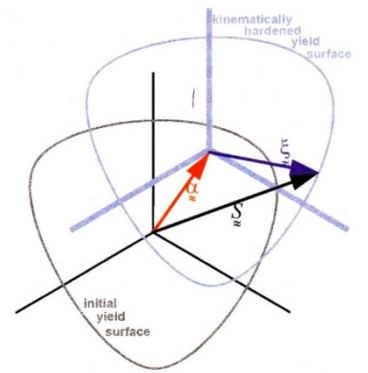
## Models for Geomechanics:

- Elastic
- Elastic/Plastic
- Soil Foam
- Power Law Creep
- MD Creep Model
- Crushed Salt Creep Model
- Clay
- GeoModel

## Thermally Enhanced Creep Closure

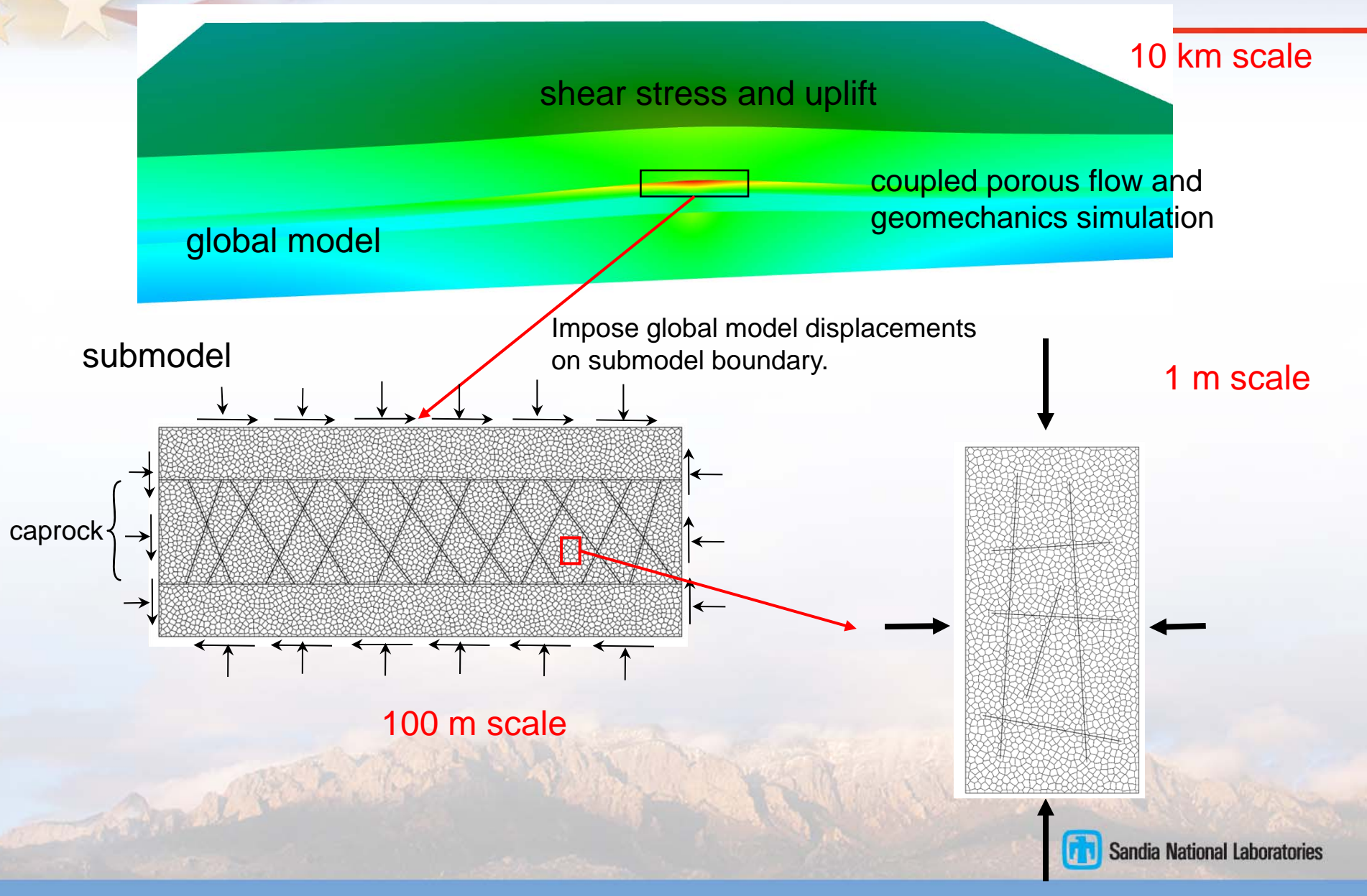


## Undeformed and Deformed Storage Tunnels in a Heated Salt Repository





# Multiscale analysis of caprock integrity during CO<sub>2</sub> injection



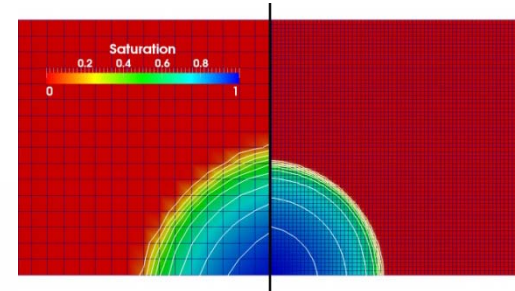
# Aria Multiphase Porous Flow Physics

## Two-Phase Immiscible Flow

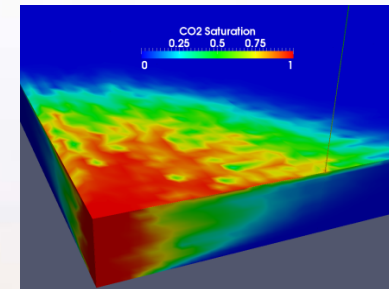
- Compressible (fluids and/or formation), buoyancy effects
- General dependence of thermophysical and transport properties on solution vector
- Capillary pressure (optional)
- Relative permeability
- Specification of heterogeneous transport property fields (e.g. permeability, porosity)
- Can be coupled to energy equation

### Benchmark Problem

Displacement of oil by water flood without capillary pressure or gravitational effects.



Grid effects using upwind CVFEM scheme



Injected CO<sub>2</sub> saturation levels in a brine filled reservoir represented with heterogeneous permeability