

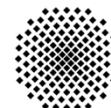
# Project 2: Numerical Round Robin for Prediction of the Behavior of Lap Joints

SAND2015-6184D

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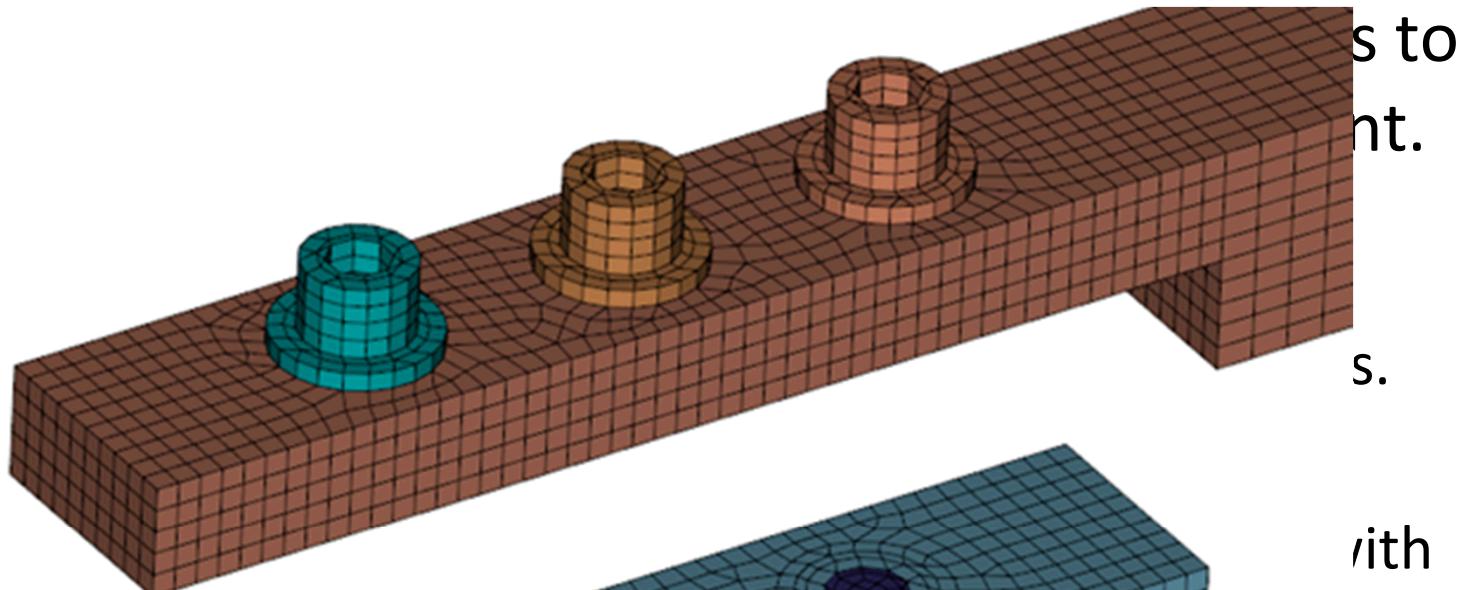
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# Objective

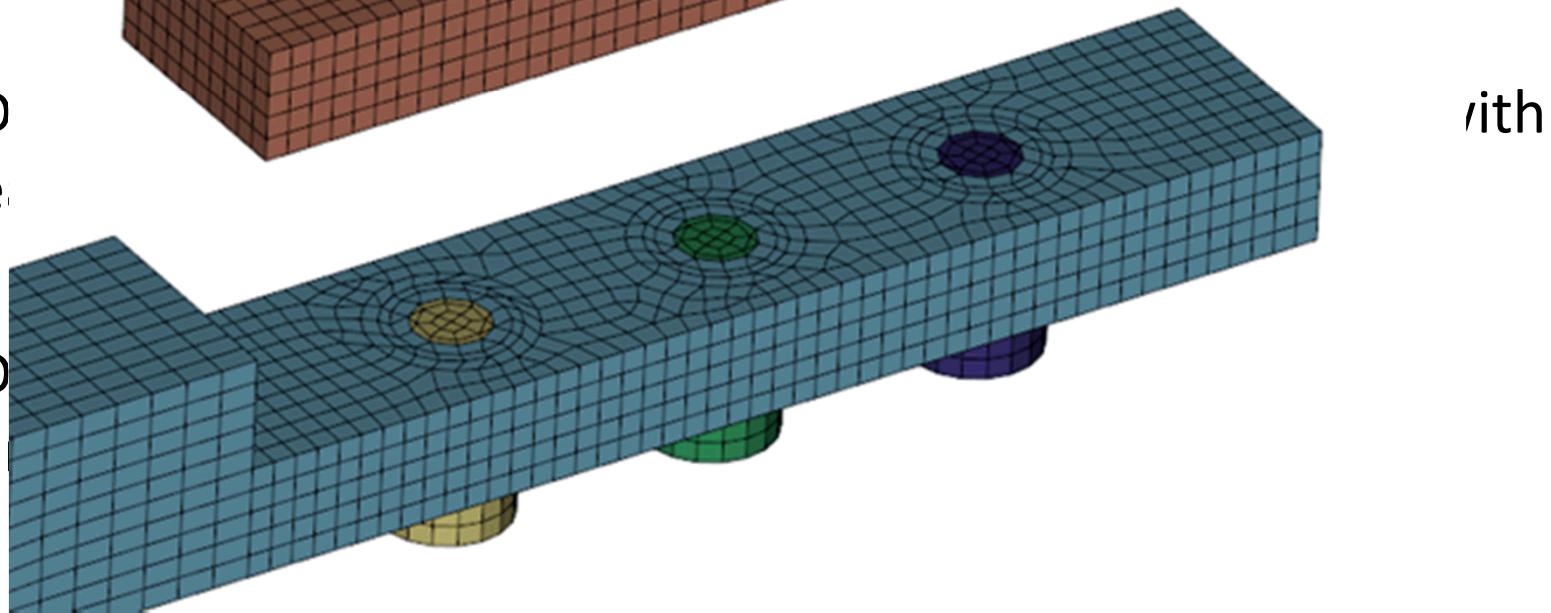
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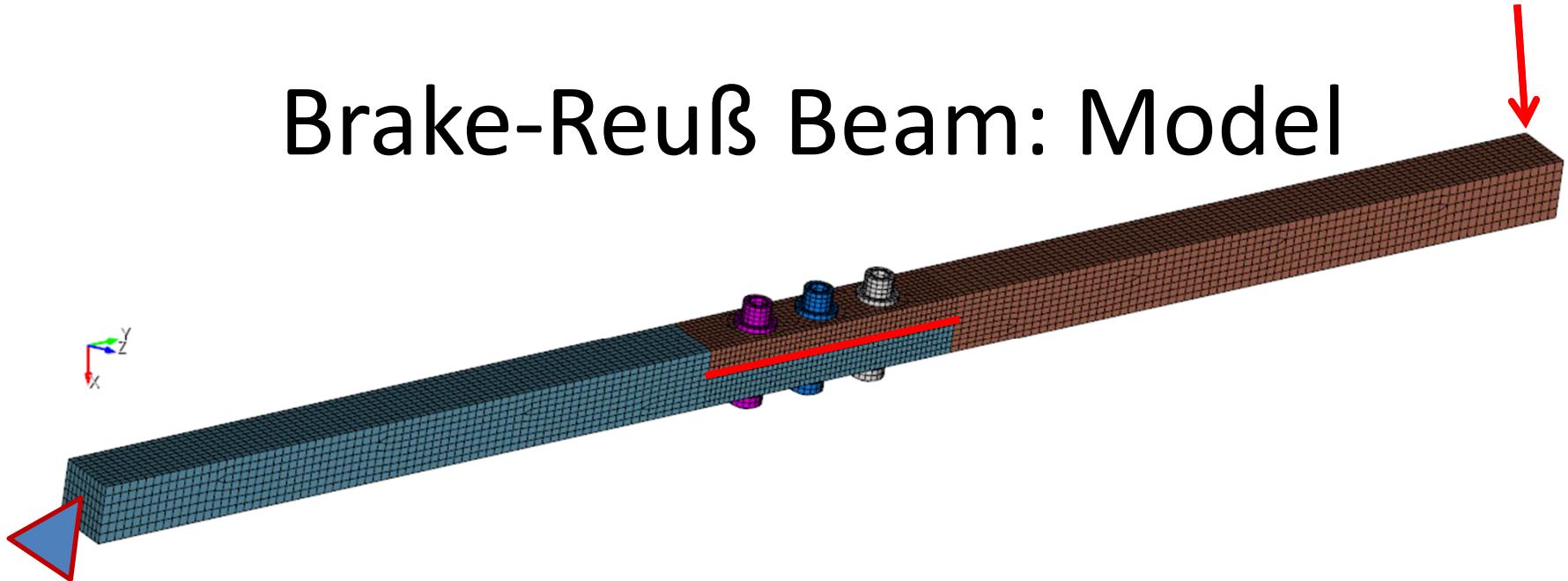
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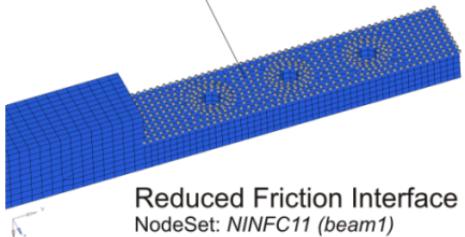
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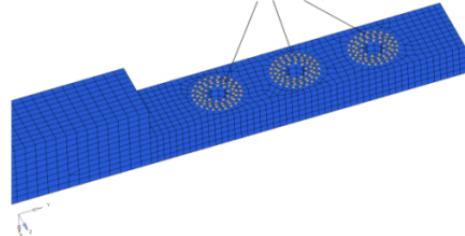
# Brake-Reuß Beam: Model



Full Friction Interface  
NodeSet: *NINFC1* (beam1)  
*NINFC2* (beam2)



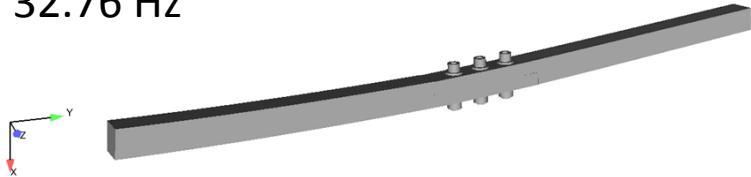
Reduced Friction Interface  
NodeSet: *NINFC11* (beam1)  
*NINFC22* (beam2)



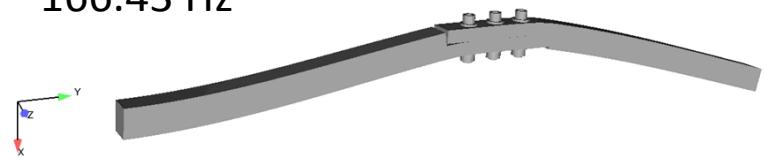
Finite Element Discretization	
# nodes	24512
# elements	19368
Element type	C3D8I / C3D6
Material Parameter	Value
Young's Modulus	182480.0[N/mm <sup>2</sup> ]
Poisson's Ratio	0.29 [-]
Density	7.9e-9 [t/mm <sup>3</sup> ]

# Linear System: Cantilevered Mode Shapes

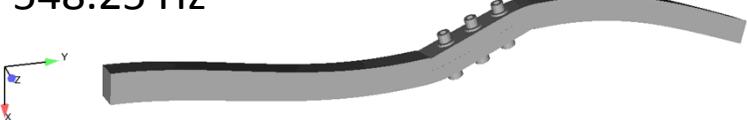
32.76 Hz



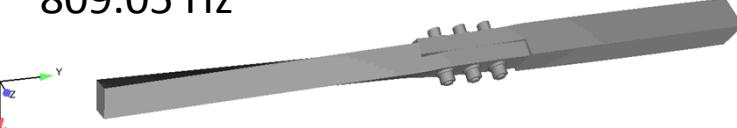
166.43 Hz



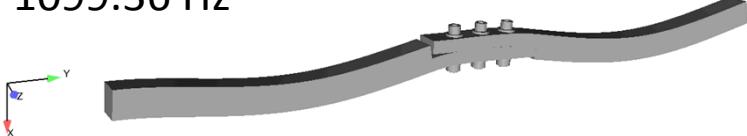
548.25 Hz



809.05 Hz



1099.36 Hz



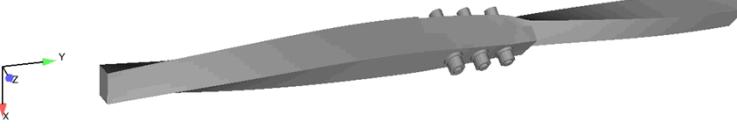
1219.72 Hz



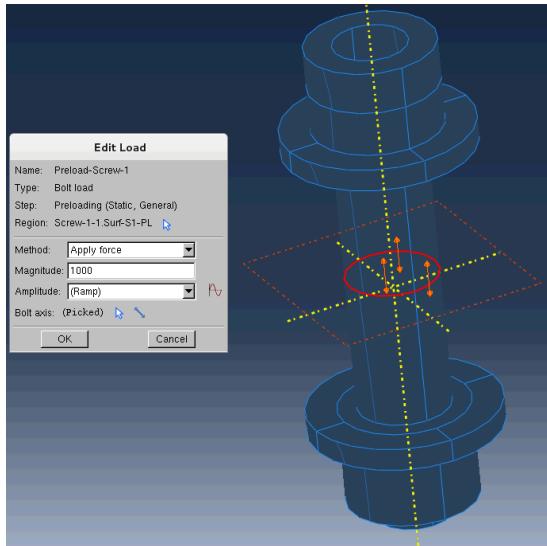
1833.39 Hz



2428.24 Hz



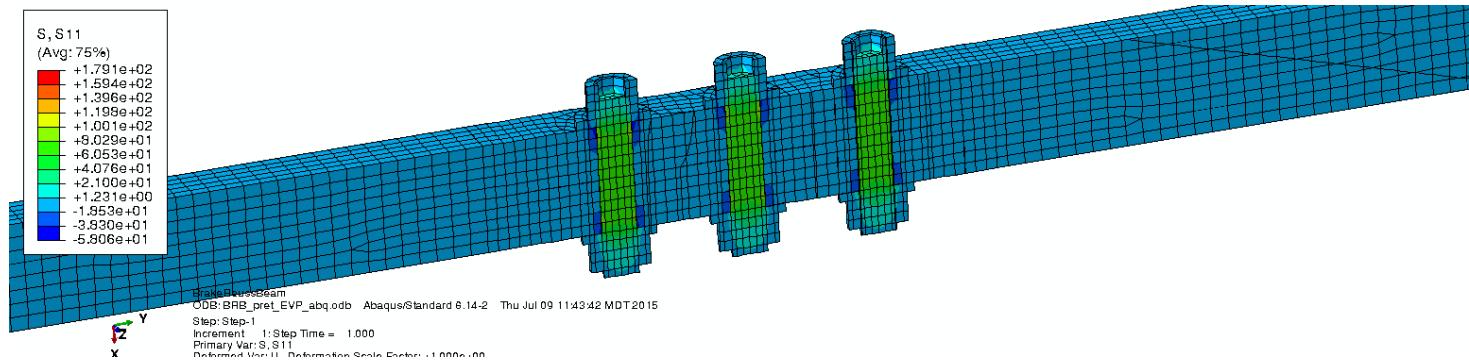
# Nonlinear Static Analysis: Modeling



## Contact properties in the friction interface:

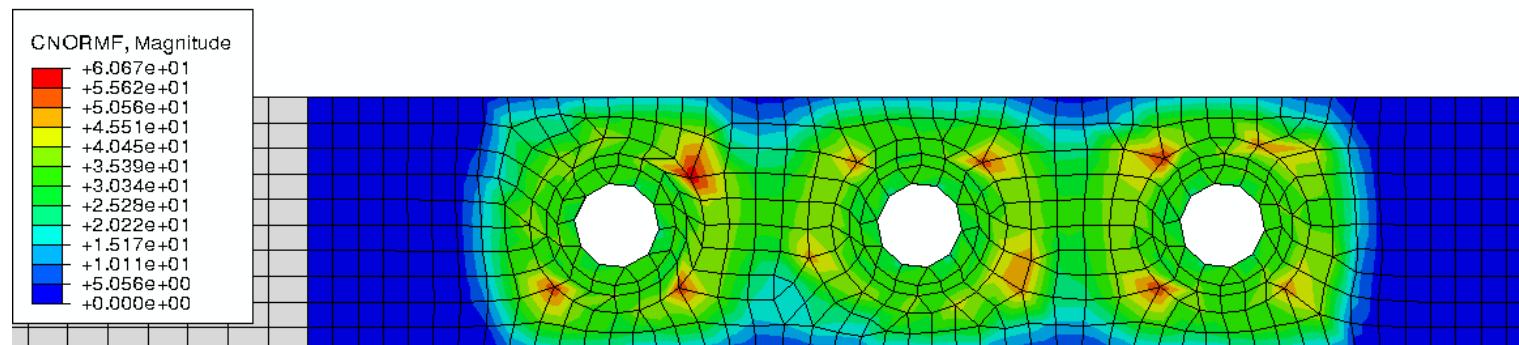
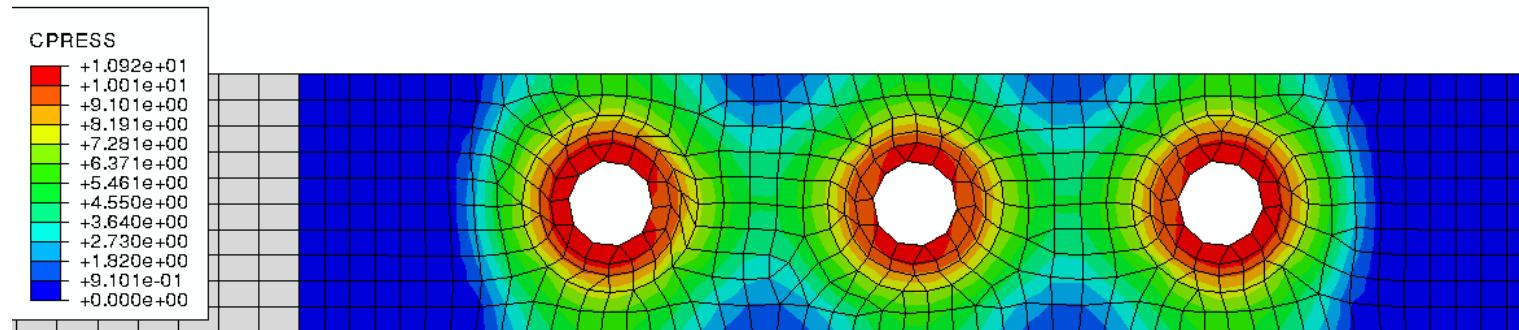
- Surface-to-surface approach
- Pressure-overclosure: hard contact
- Constraint enforcement: Lagrange multipliers
- Friction formulation: penalty method,  $\mu=0.6$  [-]
- Applied force per screw: 4kN

## Normal stress distribution in the bolts due to pre-tension

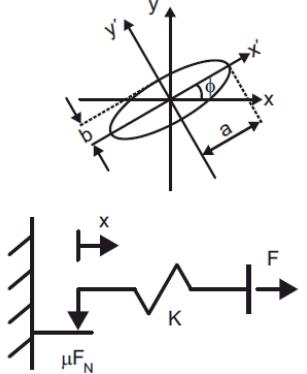
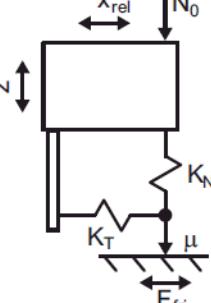
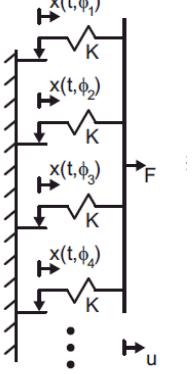


# Nonlinear Static Analysis: Results

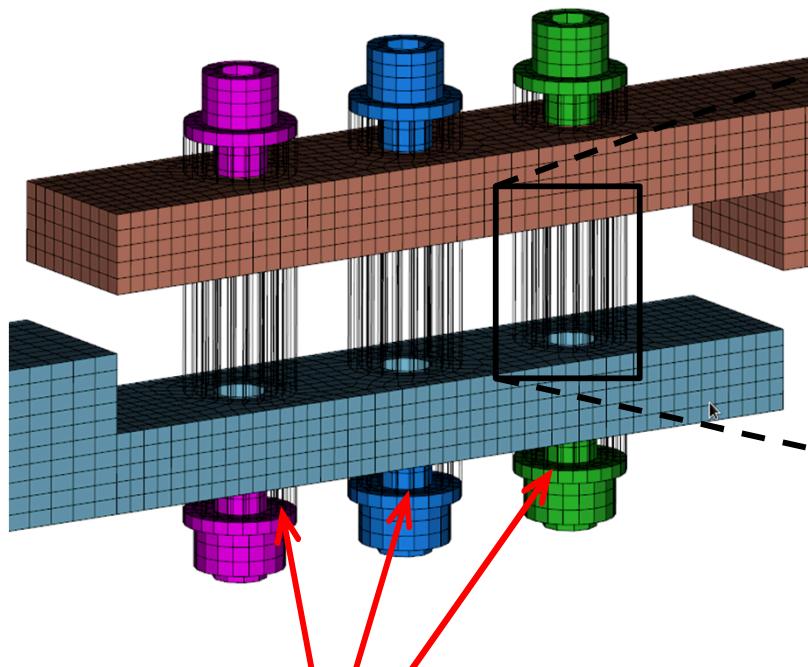
- Contact pressure and contact normal force distributions (Abaqus)



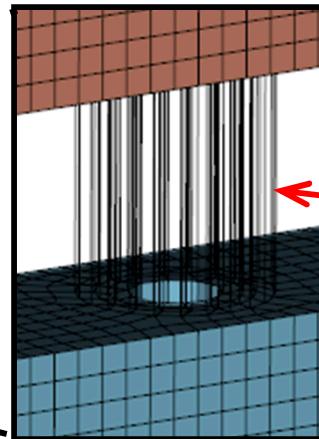
# Considered Approaches for Modeling Joints

	Stuttgart Approach	Imperial Approach	Sandia Approach
FE Tool	CalculiX	NASTRAN	SIERRA/SD
Model Fidelity	Craig-Bampton ROM	Hybrid ROM	Craig-Bampton ROM
Nonlinear Element	<p>2D Jenkins Element</p> 	<p>3D Contact Element</p> 	<p>Iwan Element</p> 
Nonlinear Solver	ROCMAN	FORSE	ROMULIS
Solver Type	Harmonic Balance	Multi-Harmonic Balance	Transient Integration

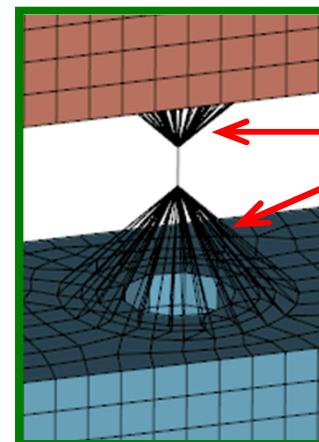
# Contact Interface Modeling



Tie coincident nodes on beam-screw interfaces with MPC's



Stuttgart/Imperial Approach  
Tie coincident nodes on the friction interface with Jenkins/3D contact elements.



Sandia Approach

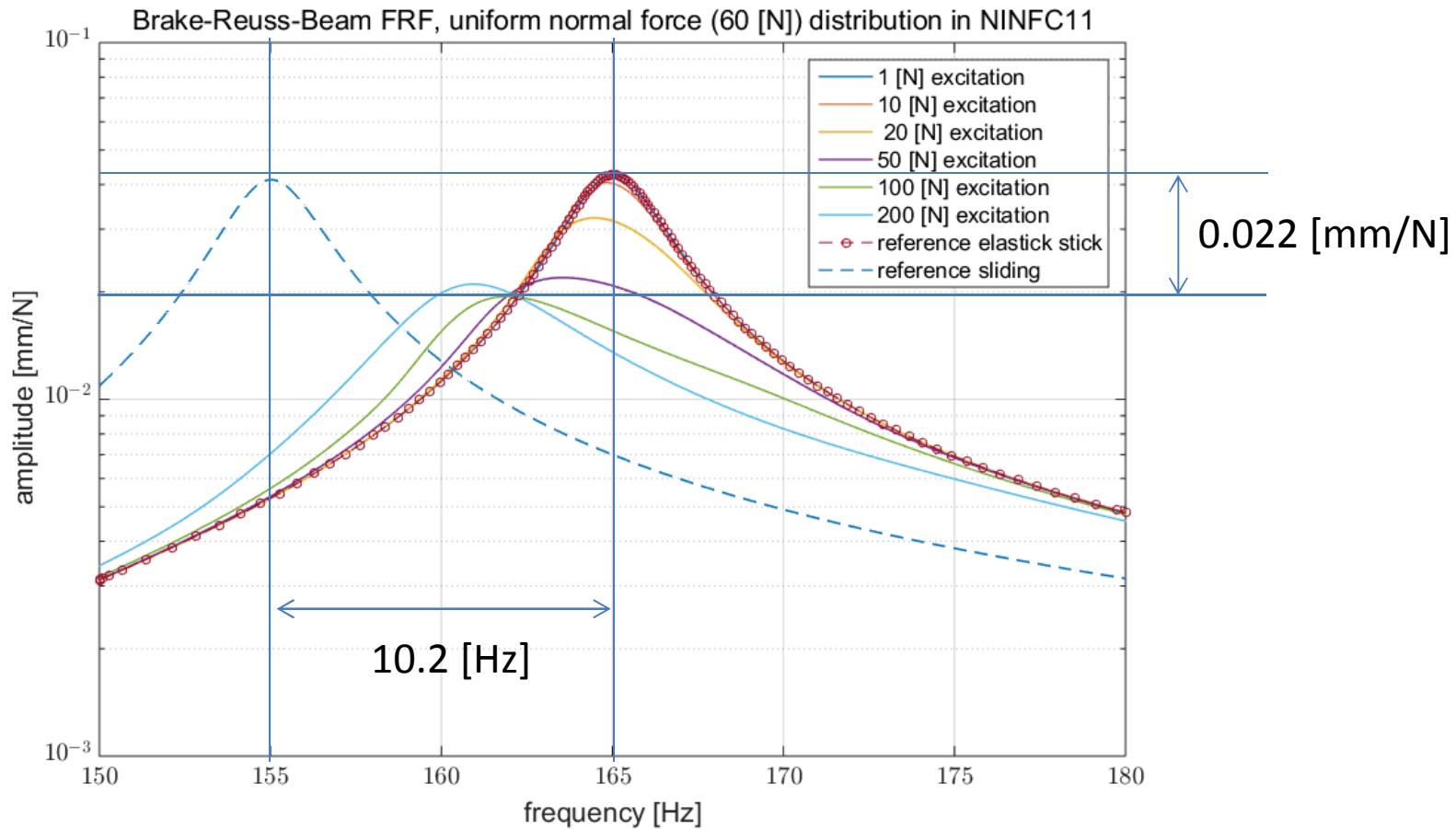
Connect interface nodes to a virtual node with NASTRAN RBE3 element spider.  
Tie virtual nodes with an Iwan element.

# Nonlinear Element Parameterization

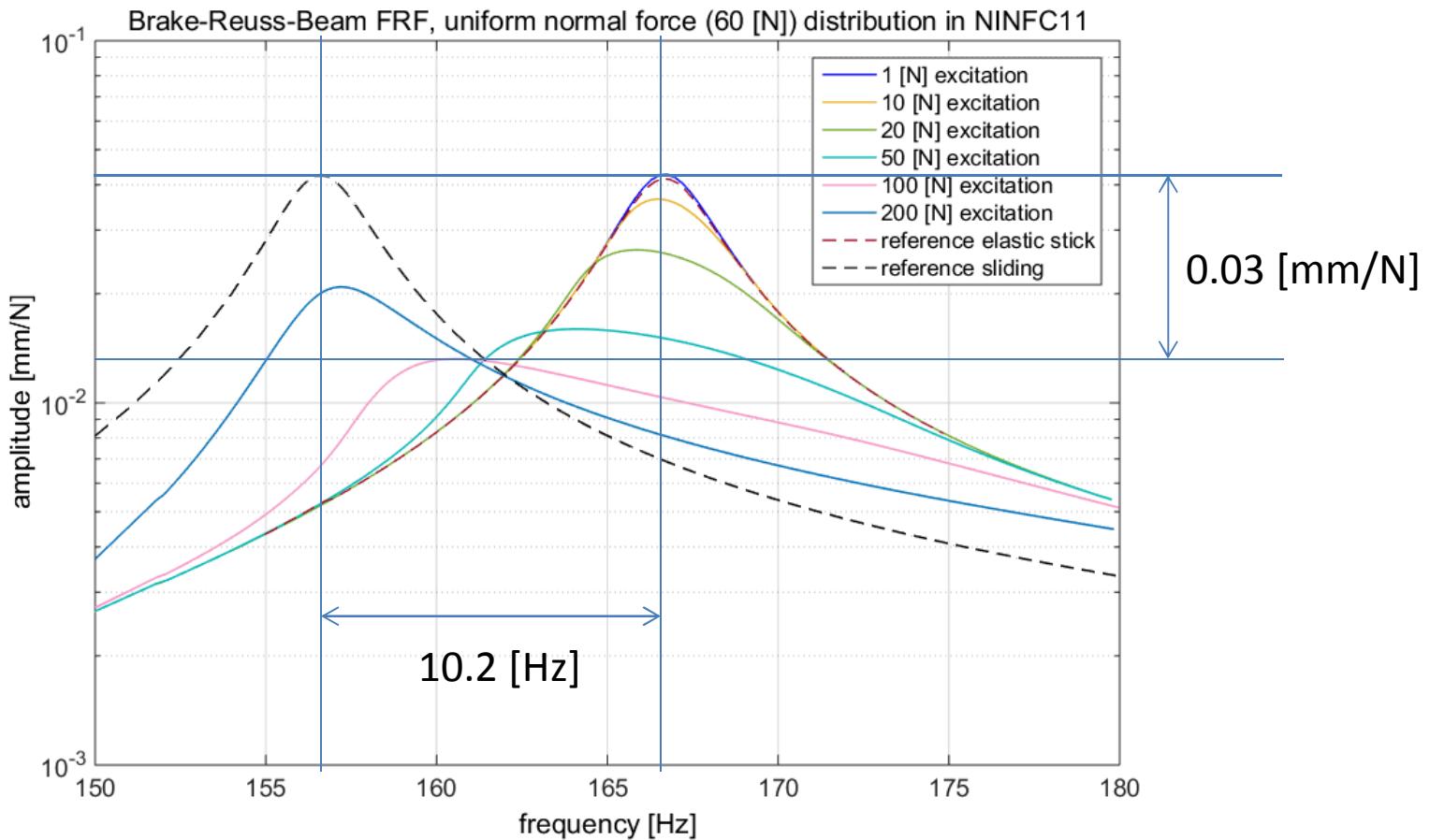
Parameter	Imperial	Stuttgart
Normal Force [N] (Uniform Distribution)	60	60
Coulomb Friction Coefficient	0.6	0.6
Tangential Stiffness [N/mm]	5e4	5e4
Normal Contact Stiffness [N/mm]	1e6	MPCs
Number of Harmonics	1	1
Number of Nonlinear DOFs	603	402

Parameter	Sandia
Slip Force [N]	2400
Tangential Stiffness [N/mm]	3.35e6
Power Law Slope ( $\chi$ )	-0.5
Power Law Intercept ( $\beta$ )	0.05
Normal Contact Stiffness [N/mm]	1e10
Number of Nonlinear DOFs	12

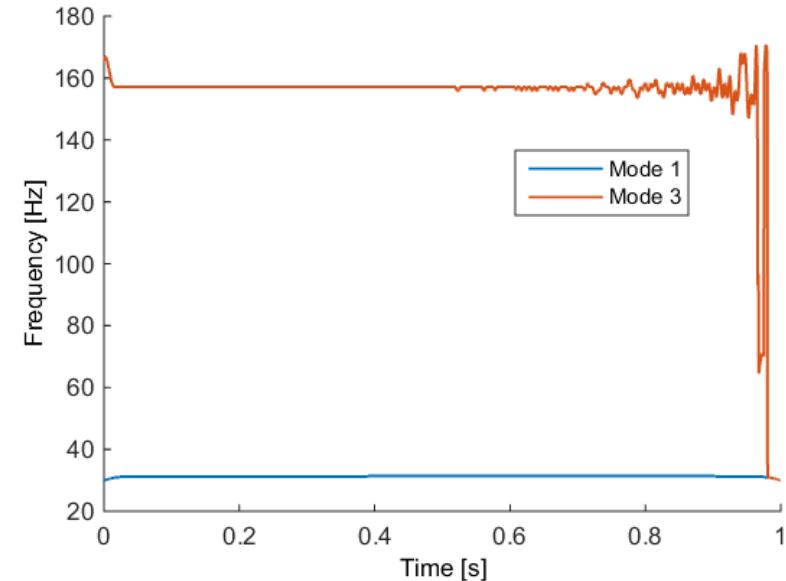
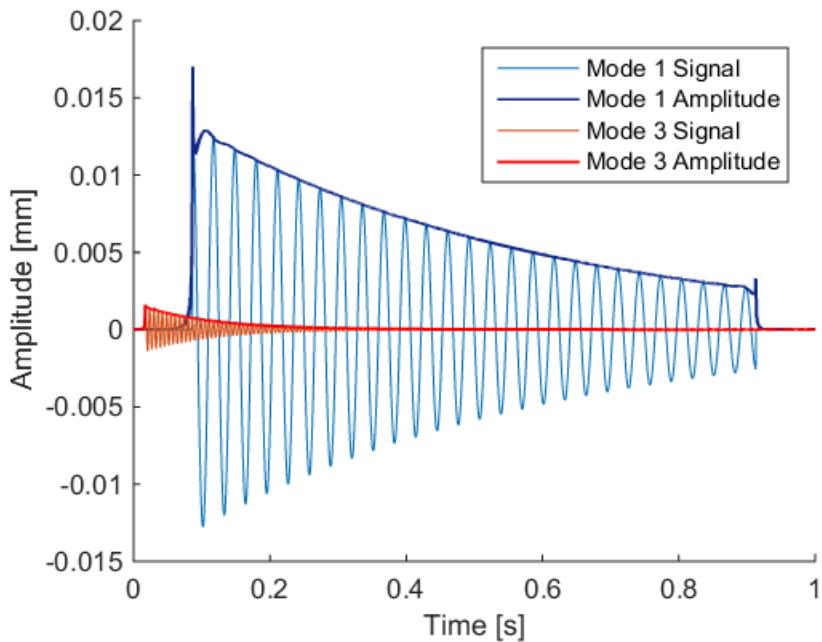
# Preliminary Results: FORSE



# Preliminary Results : ROCMAN



# Preliminary Results : ROMULIS



Simulate the free response to an impulse that excites the mode of interest.

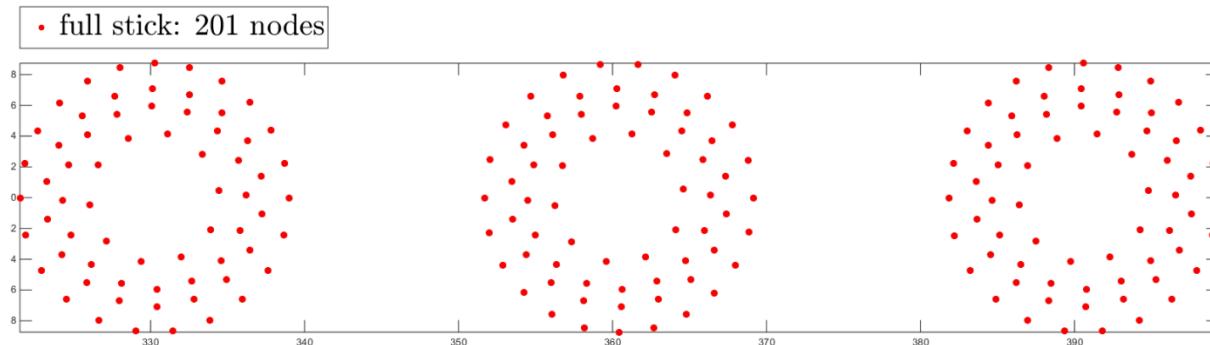
Calculate amplitude-dependent damping and natural frequency from the signal using the methods in [1].

Compare damping and frequency results with those of harmonic results.

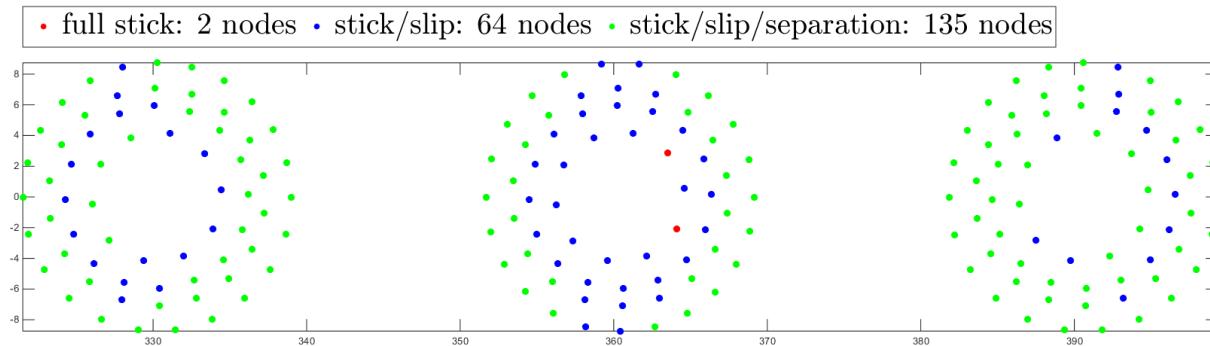
[1] Deaner, B.J., Allen, M.S., Starr, M.J., Segalman, D.J. (2015). "Application of Viscous and Iwan Modal Damping Models to Experimental Measurements from Bolted Structures," SAND2015-2643J. Sandia National Laboratories.

# Preliminary Results (FORSE): Contact States

1 [N] excitation at resonance (2nd z-Bending):

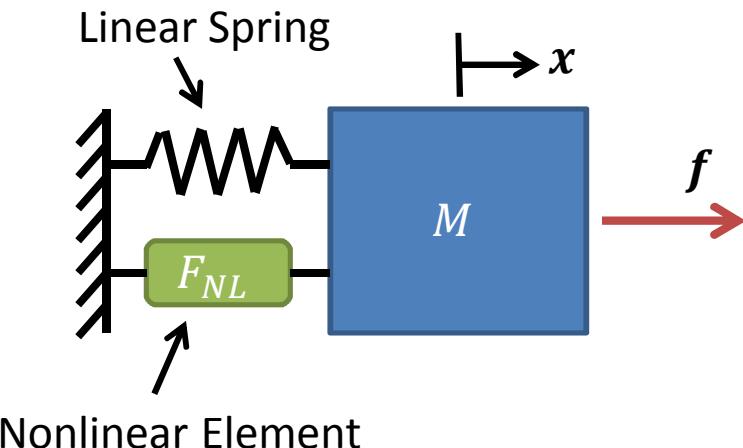


200 [N] excitation at resonance (2nd z-Bending):



# A Method to Tune Nonlinear Element Parameters to Give Similar Dissipation Characteristics

Observe the damping due to the nonlinear element in a 1-DOF system based on the dynamic response to a harmonic excitation at resonance.



Set Jenkins element parameters as constant and tune the parameters of the other elements to match its damping.

$$M = 1 \text{ [t]}$$

$$K_{linear} = 40000 \text{ [N/mm]}$$

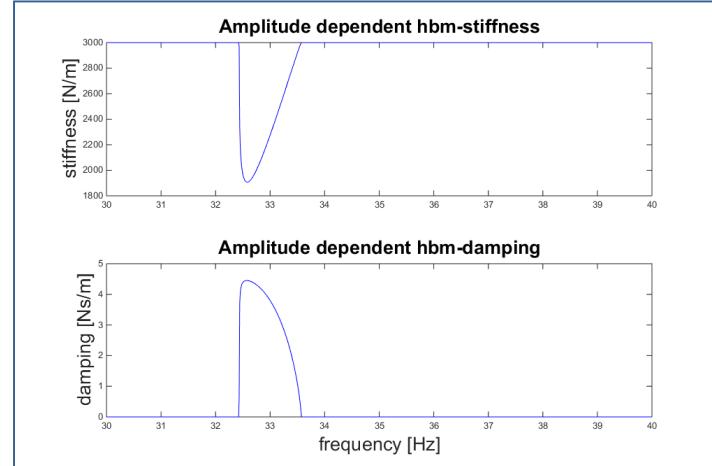
$$F_{slip} = 100 \text{ [N]}$$

$$K_{tangent} = 3000 \text{ [N/mm]}$$

# How Each Approach Calculates Damping

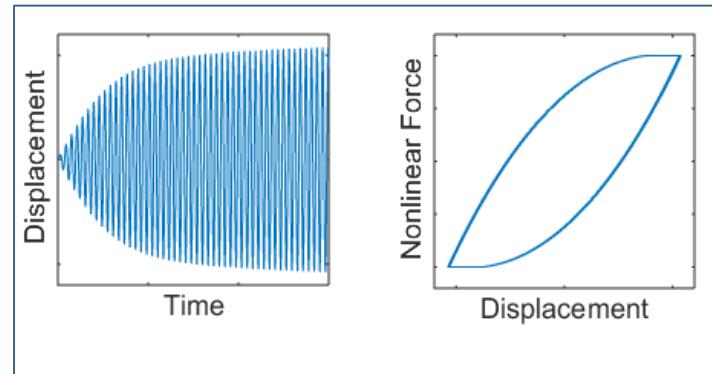
## Stuttgart Approach (Jenkins)

The amplitude dependent nonlinear force contributions at every frequency can be substituted by equivalent linearized stiffness and damping terms. The damping value is extracted at resonance point.



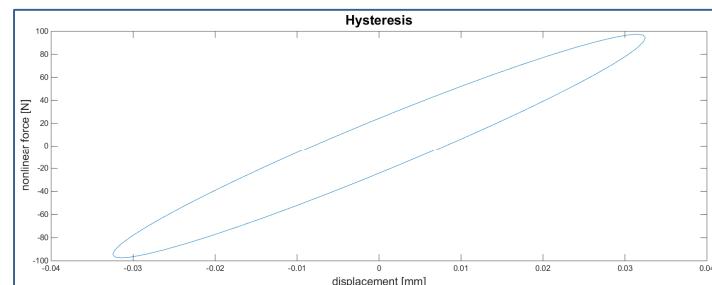
## Sandia Approach (Iwan)

Simulate the transient response to a resonance harmonic excitation until steady-state is achieved. Use the area in the steady-state hysteresis curve to determine damping.

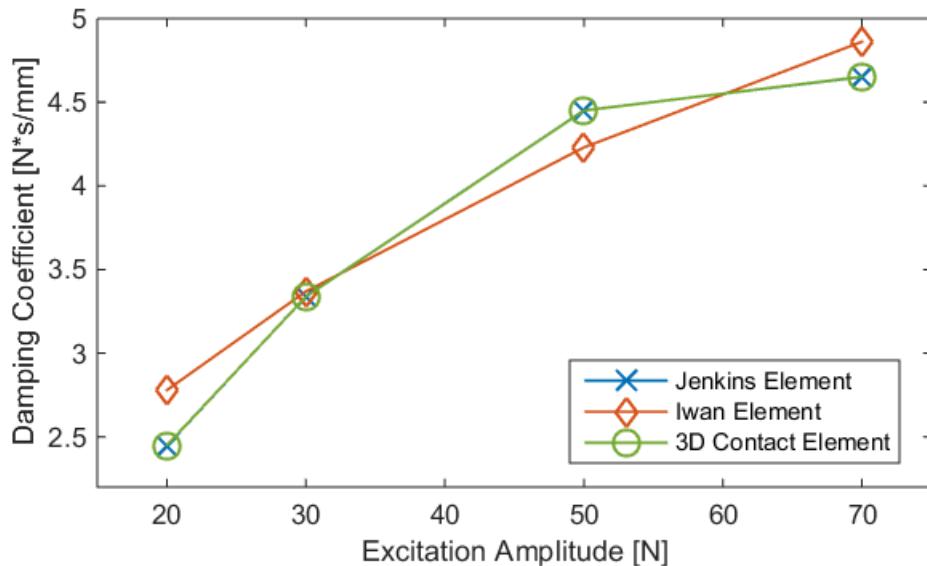


## Imperial Approach (3D Contact)

Generate a hysteresis curve based on the element constitutive model using the time domain DFT of displacement frequency response at resonance. One half the ratio of dissipated energy to kinetic energy is the damping ratio.  $\left( \zeta = \frac{E_d}{2 * \max(E_k)} \right)$



# Preliminary Results



## Iwan Parameters

$F_s = 100$  [N]  
 $K_t = 4.5e3$  [N/mm<sup>2</sup>]  
 $\chi = -0.15$  [-]  
 $\beta = 0.05$  [-]

The formulations for an Iwan element and a single friction slider are too phenomenologically different to allow a perfect match.

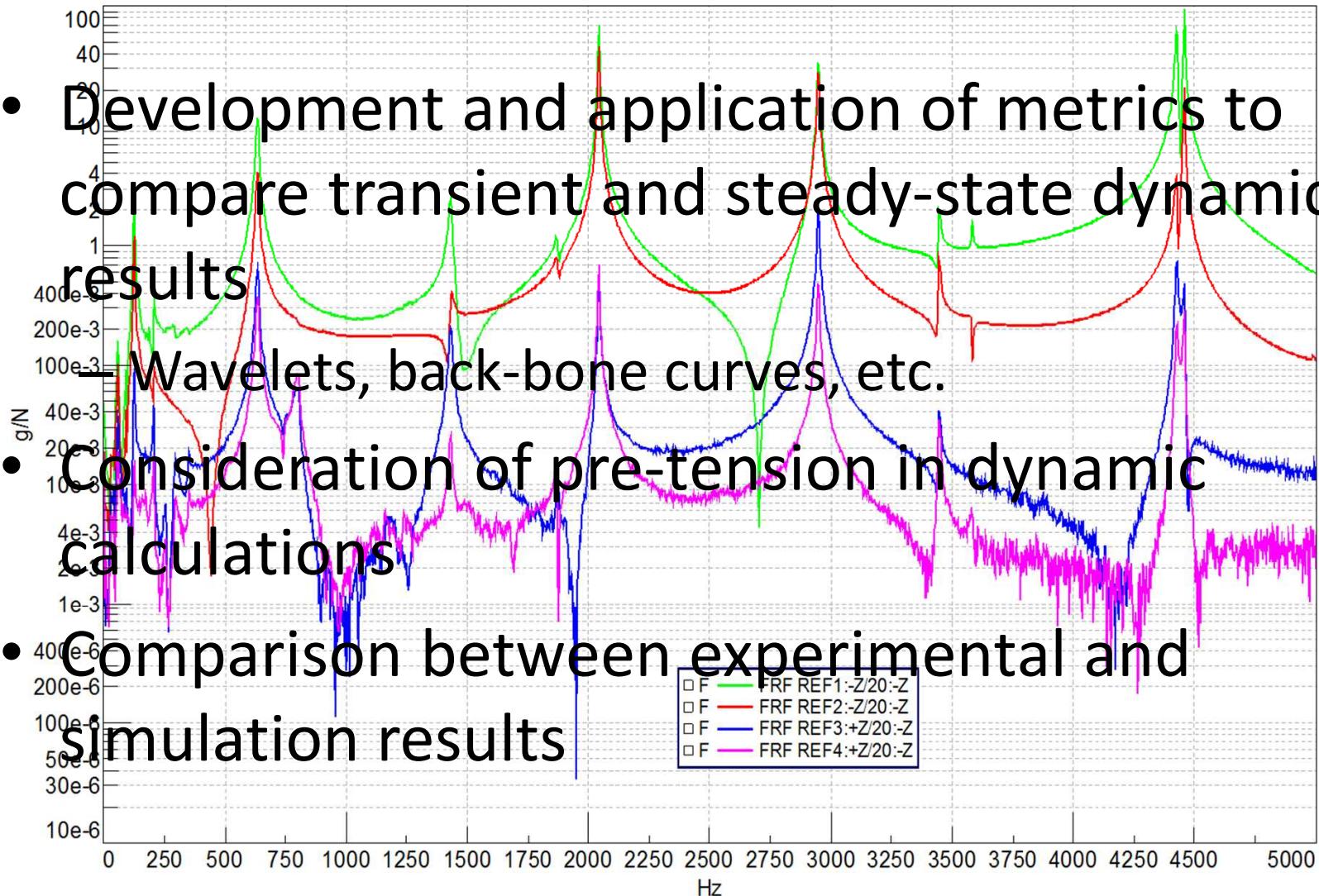
This exercise demonstrates the ability to compare nonlinear elements from both time domain approaches and frequency domain approaches by tracking damping as a function of amplitude.

# Initial Conclusions

- Brake-Reuss-Beam benchmark is suitable as Round-Robin system.
- The elasticity of the interface between the beams must be well represented to capture accurately the stick-slip-separation phenomena.
- Synthesized comparison metrics (e.g. damping vs. amplitude) must be used for the quantification of damping properties.
- Nonlinear FRFs generation is prohibitively expensive for transient methods, and may not be practical as a comparison metric.

# Future Work

- Development and application of metrics to compare transient and steady-state dynamic results
  - Wavelets, back-bone curves, etc.
- Consideration of pre-tension in dynamic calculations
- Comparison between experimental and simulation results



# POSTER LAYOUT

