

# Ubiquitous signatures of nematic quantum criticality in optimally doped Fe-based superconductors

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**A key actor in the conventional theory of superconductivity is the induced interaction between electrons mediated by the exchange of virtual collective fluctuations, originally phonons. Other collective modes that can play the same role, especially spin-fluctuations, have been widely discussed in the context of high-temperature and heavy Fermion superconductors. The strength of such collective fluctuations is measured by the associated susceptibility. Here we use**

**differential elastoresistance measurements on five optimally doped Fe-based superconductors to reveal that a diverging *nematic* susceptibility appears to be a generic feature in the optimal doping regime of these materials. The observation motivates consideration of the effects of nematic fluctuations on the**

**superconducting pairing interaction in this family of compounds, and possibly beyond.**

A growing body of evidence suggests the possibility of an intimate connection between electronic nematic phases (*1*) and high-temperature superconductivity. However, it is currently unclear to what extent there is any causal relationship between nematic fluctuations and superconductivity. Strongly anisotropic electronic phases have been found in the underdoped regime of both cuprate (*2, 3, 4, 5, 6*) and Fe-based (*7, 8, 9, 10, 11, 12*) high-temperature superconductors. For underdoped Fe-based systems, recent measurements of the elastoresistance (*13, 14, 15*), Raman spectroscopy (*16, 17, 18*), and elastic moduli (*19, 20*) for the representative electron-doped system  $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$  reveal a divergence of the electronic nematic susceptibility upon approach to the tetragonal-to-orthorhombic structural phase transition, definitively establishing that the phase transition is driven by electronic correlation. For the cuprates, recent x-ray diffraction (*21, 22, 23, 24*) and NMR (*25*) measurements have revealed evidence for short-range charge density wave order in “underdoped” crystals. Although details of the charge ordered state(s) are still being established, these initial observations have at least motivated discussion of a possible “vestigial” nematic order (*26*). Perhaps significantly, in the phase diagrams of both families of compounds, optimal doping is located close to putative quantum critical points (*27, 28, 29*) which potentially have a nematic character (*13, 26, 30*).

From a theoretical perspective, recent treatments indicate that nematic quantum criticality, (i.e. quantum critical fluctuations caused by proximity to a nematic quantum critical point) can provide an enhancement of the existing pairing interaction. In particular, a pure nematic phase does not break the translational symmetry of the original crystal lattice; consequently the  $q=0$  nematic fluctuations enhance  $T_c$  in all symmetry channels (*31, 32, 33*). It is therefore of considerable interest to empirically establish whether nematic fluctuations are a characteristic feature of optimally doped high temperature superconductors, as well as to probe



the extent to which these nematic fluctuations show intrinsically quantum behavior. In the present paper, we show that this is the case for Fe-pnictide and chalcogenide superconductors by considering the representative materials  $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$  and  $\text{Ba}(\text{Fe}_{1-x}\text{Ni}_x)_2\text{As}_2$  (i.e. electron-doped “122”),  $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$  (hole-doped),  $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$  (isovalent substitution) and  $\text{FeTe}_{1-x}\text{Se}_x$  (“11”). Furthermore, we find that the nematic susceptibility obeys a simple Curie-Weiss power law for all five optimally doped Fe-based superconductors over a wide temperature range. For the electron and hole-doped 122 pnictides a sub-Curie-Weiss deviation was observed at low temperatures, which we tentatively attribute to an enhanced sensitivity to disorder in a quantum critical regime.

Nematic order couples linearly to anisotropic strain of the same symmetry. Consequently, the nematic susceptibility of a material can be measured by considering the electronic anisotropy that is induced by anisotropic in-plane strain. In the regime of infinitesimal strains, all forms of electronic anisotropy are linearly proportional. Hence, the rate of change of resistivity anisotropy with respect to anisotropic strain, defined in the limit of vanishing strain, is linearly proportional to the nematic susceptibility (34). The proportionality constant depends on microscopic physics, but away from any quantum critical point does not contain any singular behavior. Consequently, the induced resistivity anisotropy reveals the essential divergence of the nematic susceptibility upon approach to a thermally-driven nematic phase transition (14, 15).

For a tetragonal material, nematic order has either  $d_{xy}$  symmetry (i.e. the  $B_{2g}$  irreducible representation of the  $D_{4h}$  point group, corresponding to nematic order oriented along a nearest-neighbor Fe-Fe bond – the  $[110]$  or  $[1\bar{1}0]$  crystal axes), or  $d_{x^2-y^2}$  symmetry ( $B_{1g}$ , corresponding to the  $[100]$  or  $[010]$  crystal axes). Anisotropic strains with appropriate symmetry are then  $\epsilon_6 = (\epsilon_{xy} + \epsilon_{yx})/2$  and  $\epsilon_1 - \epsilon_2 = \epsilon_{xx} - \epsilon_{yy}$  respectively. The strain-induced changes in resistivity can be described using the dimensionless elastoresistivity tensor,  $m_{ij}$  (14):

$$(\Delta\rho/\rho)_i = \sum_{j=1}^6 m_{ij}\epsilon_j \quad (1)$$

where  $1 = xx$ ,  $2 = yy$  etc. Consequently, the corresponding components of the nematic susceptibility tensor are given by:

$$\chi_{N(B_{2g})} = c \times 2m_{66} \quad (2)$$

$$\chi_{N(B_{1g})} = c' \times (m_{11} - m_{12}) \quad (3)$$

where  $c$  and  $c'$  are proportionality constants, which depend on microscopic physics (34).

We measure elastoresistivity by applying an in-situ tunable anisotropic strain using a piezo-electric PZT stack. A square plate sample (typical dimension  $750 \times 750 \times 20 \mu\text{m}$ ) is glued on the side wall of the PZT stack using a commercial two part epoxy. The PZT stack deforms when a voltage is applied and hence strains the sample glued on top of it (35). The amount of strain can be measured by a strain gauge glued either on the backside of the PZT stack or on the top surface of a larger sample (the latter case enabling a full determination of the strain transmission (36)). The in-plane resistivity tensor of the sample is measured via the Montgomery technique, with electrical contacts made at the four corners of the square sample (36). Representative data taken using this new technique are shown in Figure 1 for the specific case of  $\text{BaFe}_2\text{As}_2$ . As has been previously demonstrated (14, 15), the data can be fit very well by a Curie-Weiss temperature dependence:

$$2m_{66} = 2m_{66}^0 + \lambda/[a(T - T^*)]. \quad (4)$$

In Figure 2 we show  $B_{2g}$  elastoresistance data for a range of optimally doped materials, including  $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$  (isovalently substituted),  $\text{Ba}(\text{Fe}_{1-x}\text{Ni}_x)_2\text{As}_2$  (electron-doped),

$\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$  (hole-doped) and  $\text{FeTe}_{1-x}\text{Se}_x$ . In all cases,  $2m_{66}$  rises strongly with decreasing temperature, with comparably large values for each compound. The observation of such an effect for this wide variety of ways of doping, including the case of the iron chalcogenide  $\text{FeTe}_{0.6}\text{Se}_{0.4}$ , is highly suggestive that a divergence of the nematic susceptibility in the  $B_{2g}$  channel is a generic feature of optimally doped Fe-based superconductors. This is our main result. Regardless of microscopic models, from a purely empirical perspective it is apparent that the optimally-doped superconductor is born out of an electronic state that is characterized by strongly fluctuating orientational (nematic) order in this specific symmetry channel. This result is especially notable for  $\text{FeTe}_{0.6}\text{Se}_{0.4}$  given that the orientation of both the magnetic ordering wave vector and the in-plane component of the structural distortion of undoped FeTe is 45 degrees away from the orientation of those in the iron arsenide materials.

The  $m_{66}$  coefficient of optimally doped  $\text{BaFe}_2(\text{As}_{0.68}\text{P}_{0.32})_2$  (Fig. 2A) follows a perfect Curie-Weiss temperature dependence from  $T = 250\text{K}$  (the highest temperature where strain can be effectively transmitted by the epoxy) down to  $T_c$  (below which temperature the resistance is zero), with a Weiss temperature ( $T^*$ ) close to zero. For  $\text{FeTe}_{0.6}\text{Se}_{0.4}$ , the  $m_{66}$  coefficient can be perfectly fitted with Curie-Weiss down to  $T_c$  but shows a significant deviation for temperatures greater than 100K, possibly related to the loss of quasi particle coherence due to its extremely small Fermi energy as observed in photoemission spectroscopy and transport (37,38). Intriguingly, for the electron and hole doped 122 pnictides, a downward deviation from Curie-Weiss behavior is observed below a characteristic temperature that is different for each of the materials. The quality of fit to the Curie-Weiss functional form for  $\text{BaFe}_2(\text{As}_{0.68}\text{P}_{0.32})_2$  in comparison to all of the other optimally doped compositions studied can be readily appreciated if the data are plotted on log axes (Fig. S11). Only the data for the P-substituted system can be fit by a single power law  $[(2m_{66} - 2m_{66}^0)] \sim (T - T^*)^{-\gamma}$  over the entire temperature range, yielding  $\gamma = 0.985 \pm 0.005$  and  $T^* = 11.7 \pm 3.1$ .

A slightly overdoped  $\text{BaFe}_2(\text{As}_{0.64}\text{P}_{0.36})_2$  sample has also been measured; the elastoresistivity coefficient  $m_{66}$  of this sample can also be well fitted by Curie-Weiss temperature dependence over the entire temperature range, with a negative Weiss temperature  $T^* = -11.5 \pm 2.3$  (Fig. S14). The small value of the Weiss temperature observed in  $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$  near optimally doping, and the fact that it crosses zero as doping increases, motivates consideration of the nematic susceptibility in the context of a quantum critical point. An Ising nematic phase transition in an insulator would generally be expected to have dynamical exponent  $z = 1$ , so the effective dimensionality of the system would be  $d + z = 3+1$ . As the materials in question are metallic, the situation is more complicated (39); the Hertz-Millis paradigm is expected to break down in the case of electronic nematic order in metallic systems, for which Landau damping associated with the gapless Fermions leads to a larger value of the dynamical exponent,  $z = 3$ . Although the analysis of this problem is not straightforward, both analytic (40) and numerical studies (41) indicate that the nematic susceptibility at criticality should diverge in proportion to  $1/T$  (up to possible logarithmic corrections), consistent with the observed behavior of the  $B_{2g}$  elastoresistance of optimally doped  $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$ .

To gain insight into the physical origin of the low temperature downward deviation from Curie-Weiss behavior in the electron and hole doped pnictides, we consider the evolution of the  $B_{2g}$  elastoresistance as a function of composition for the specific case of Co-doped  $\text{BaFe}_2\text{As}_2$ . Figure 3 A-D show the progression of  $2m_{66}$  as a function of Co doping for several representative compositions (more were measured, see (36)), from underdoped (A,B), through optimal doping (C), to the overdoped regime (D). For the heavily underdoped compositions ( $x = 0.025$ ),  $2m_{66}$  can be well described by mean field Curie-Weiss T-dependence down to  $T_s$ . It has been previously established that this behavior is essentially independent of disorder, at least comparing undoped  $\text{BaFe}_2\text{As}_2$  with different Residual Resistance Ratios (RRR), and Co and Ni substituted crystals with the same  $T_N$  (15). The Weiss temperature  $T^*$  extracted from high-

temperature fits to Curie-Weiss behavior crosses zero close to optimal doping (Fig. 4). However, for lightly underdoped  $\text{Ba}(\text{Fe}_{0.553}\text{Co}_{0.047})_2\text{As}_2$ , a downward deviation from mean-field behavior at low temperatures begins to be noticeable, and becomes more pronounced for optimally doped  $\text{Ba}(\text{Fe}_{0.93}\text{Co}_{0.07})_2\text{As}_2$ ; similar deviations are observed in optimally Ni and K doped  $\text{BaFe}_2\text{As}_2$ . A similar effect has been observed in recent measurements of the sheer modulus via three-point bending experiments (20). The deviation from Curie-Weiss behavior diminishes again as the doping is further increased: for the overdoped composition (Fig. 3D) the data can be fit to Curie-Weiss to a lower temperature than for optimal doping, and the magnitude of the deviation below  $\sim 45$  K is smaller than for optimal doping.  $2m_{66}$  of four additional Co dopings has also been measured, showing a similar non-monotonic doping dependence of the deviation from Curie-Weiss behavior. The fact that the effect is maximal near optimal doping where  $T^* \sim 0$ , suggests that it is associated with proximity to the putative nematic quantum phase transition.

P-substituted  $\text{BaFe}_2\text{As}_2$  is the “cleanest” of all of the known 122 Fe-pnictide families, evidenced by the fact that quantum oscillations can be observed across the phase diagram (42, 43). The deviation from Curie-Weiss behavior for optimally doped compositions of all other dopants in  $\text{BaFe}_2\text{As}_2$  suggests that disorder plays an important role in the quantum critical regime. All forms of quenched disorder produce locally anisotropic effective strains, which thus couple to the orientation of the nematic order; this is “random-field” disorder (26). Analysis of the random-field Ising model yields several generically expected effects of random field disorder, including suppression of the nematic susceptibility below mean field expectations for a clean system, and, for the case of a quantum phase transition, the enhanced sensitivity of quantum critical phenomena to disorder. (36).

The temperature dependence of the nematic susceptibility can also be extracted from measurements of the elastic moduli (20). The two measurements (elastoresistance and elastic moduli) are in broad agreement, for example in terms of the Curie-Weiss T-dependence of  $\chi_N$  for

underdoped compositions of  $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ , and also in terms of the deviation from Curie-Weiss behavior near optimal doping. However, there is an important distinction in terms of the relative magnitude of the measured quantities as a function of doping. In particular, the normalized lattice softening  $[c_{66}^0 - c_{66}]/c_{66}^0$  extracted in (20) monotonically decreases in magnitude and extent in temperature as a function of  $x$ . In contrast, the quantity  $|(2m_{66} - 2m_{66}^0)| = c\chi_N$  initially increases with  $x$ , peaking for lightly underdoped compositions  $x \simeq 0.05$ . The apparent enhancement of the elastoresistance  $2m_{66}$  over the softening of the elastic modulus for compositions near optimal doping is potentially related to renormalization of the quasiparticle effective mass in the quantum critical regime, as has been seen in P-substituted  $\text{BaFe}_2\text{As}_2$  (29). Such a mass renormalization is an expected consequence of nematic quantum critical fluctuations (39). Significantly, it is precisely these low-energy quasiparticles that are also involved in the eventual superconductivity.

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## **Acknowledgments**

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## **Supplementary Materials**

Materials and Methods

Supplementary Text

Table S1

Figs. S1 to S16

References (45–62)

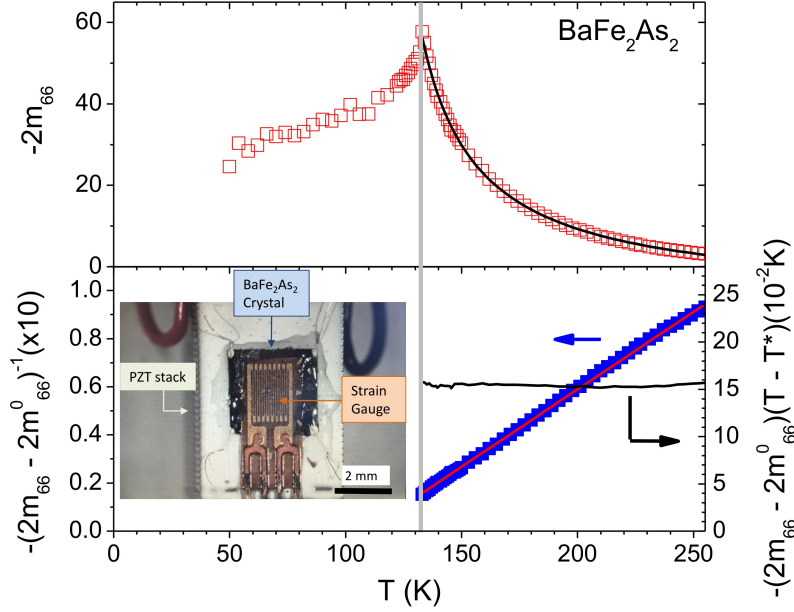


Figure 1: **Temperature dependence of the  $B_{2g}$  elastoresistance of  $\text{BaFe}_2\text{As}_2$ .** The data follow a Curie-Weiss behavior, which is the anticipated mean-field temperature dependence of the nematic susceptibility of a material approaching a thermally driven nematic phase transition (13, 14, 15). Upper panel shows  $-2m_{66}$ , proportional to the nematic susceptibility  $\chi_{N(B_{2g})}$ . Black line shows the Curie-Weiss fit. The quality of fit can be better appreciated by considering the inverse susceptibility,  $-(2m_{66} - 2m_{66}^0)^{-1}$  which is perfectly linear (left axis of lower panel; fit shown by red line), and the Curie constant  $-(2m_{66} - 2m_{66}^0)^{-1}(T - T^*)$  (right axis of lower panel), which is independent of temperature. The Weiss temperature obtained from the Curie-Weiss fit, which gives the bare mean field nematic critical temperature, yields a value  $T^* = 109 \pm 1.4$  K. Coupling to the lattice renormalizes the critical temperature, leading to a nematic-structural phase transition at  $T_s = 134$  K (vertical gray line). Inset shows a photograph of a square crystal glued on a PZT piezoelectric stack for differential elastoresistance measurements using Montgomery's geometry. Four electrical contacts were made at the corners and a strain gauge was glued on the top surface (36).

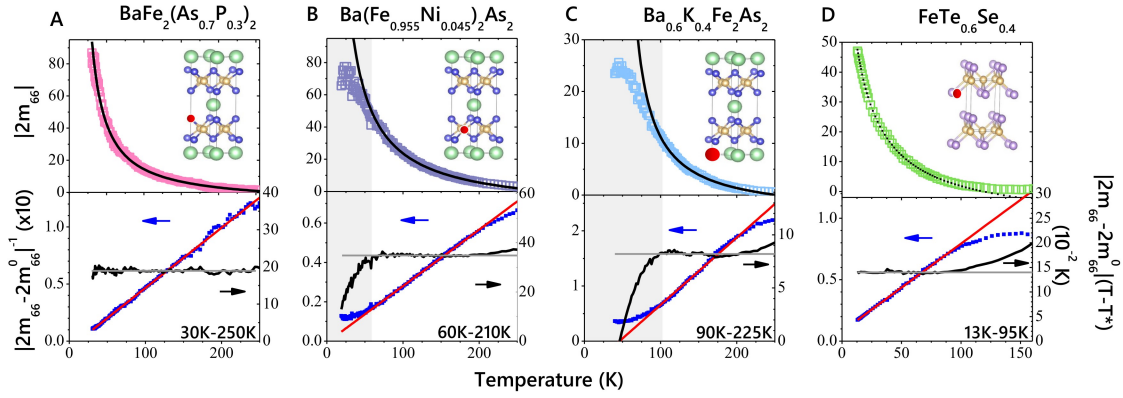


Figure 2: **Divergence of the  $B_{2g}$  elastoresistance  $2m_{66}$  of several different families of optimally doped Fe pnictide and chalcogenide superconductors.** (A) optimally doped  $\text{BaFe}_2(\text{As}_{0.7}\text{P}_{0.3})_2$  (isovalent substitution), (B) optimally doped  $\text{Ba}(\text{Fe}_{0.955}\text{Ni}_{0.045})_2\text{As}_2$  (electron doped), (C) optimally doped  $\text{Ba}_{0.58}\text{K}_{0.42}\text{Fe}_2\text{As}_2$  (hole doped), and (D) optimally doped  $\text{FeTe}_{0.58}\text{Se}_{0.42}$ . Insets indicate the dopant site (red) in the respective unit cells of each material. Comparable magnitude induced resistivity anisotropies are observed for each case (36). Upper panels show  $|2m_{66}|$ , whereas lower panels show  $|(2m_{66} - 2m_{66}^0)|^{-1}$  (left axes of lower panels, blue symbols) and  $|(2m_{66} - 2m_{66}^0)|(T - T^*)$  (right axes of lower panels, black curves). Black(upper panels) and red(lower panels) lines shows fits to Curie-Weiss behavior of  $m_{66}$  and  $|(2m_{66} - 2m_{66}^0)|^{-1}$  respectively. Grey horizontal lines (low panels) shows the average values of  $|(2m_{66} - 2m_{66}^0)|(T - T^*)$  in the fitting temperature range. Regions of deviation from Curie-Weiss behavior in (B) and (C) are indicated by gray shaded regions. For (A) and (B),  $2m_{66}$  is negative. For (C) and (D),  $2m_{66}$  is positive. Fit parameters are listed in (36, 44).

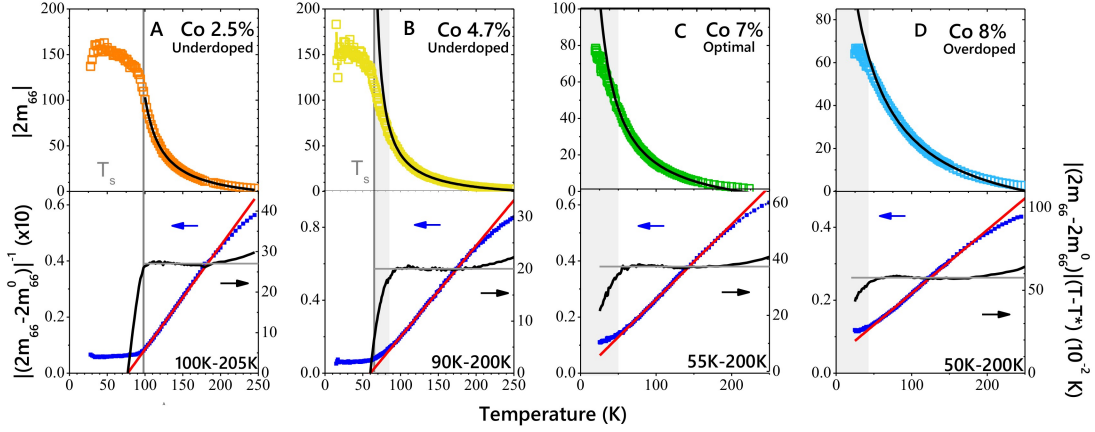


Figure 3: **Variation of the  $B_{2g}$  elastoresistance of  $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$  for four representative compositions.** (A,B) underdoped compositions  $\text{Ba}(\text{Fe}_{0.975}\text{Co}_{0.025})_2\text{As}_2$  and  $\text{Ba}(\text{Fe}_{0.953}\text{Co}_{0.047})_2\text{As}_2$ ; (C) optimal-doped  $\text{Ba}(\text{Fe}_{0.93}\text{Co}_{0.07})_2\text{As}_2$ ; and (D) overdoped  $\text{Ba}(\text{Fe}_{0.92}\text{Co}_{0.08})_2\text{As}_2$ . The heavily underdoped composition is very well described by a Curie-Weiss temperature dependence over the entire temperature range (black lines in upper panels). For the compositions near optimally-doping,  $2m_{66}$  can be well fit by a Curie-Weiss  $T$ -dependence at high temperatures. Below a characteristic temperature scale (different for each compositions, indicated by shade gray region), a strong downward deviation from Curie Weiss behavior is observed, also seen in the inverse susceptibility (upward curvature) and in  $|(2m_{66} - 2m_{66}^0)/(T - T^*)| \propto \chi_N(T - T^*)$  (strong downturn), which are shown in the lower panels. The deviation from Curie-Weiss behavior is the strongest at the optimal doping, and diminishes on either side of the phase diagram. Curie-Weiss fit parameters for each composition are listed in (36).



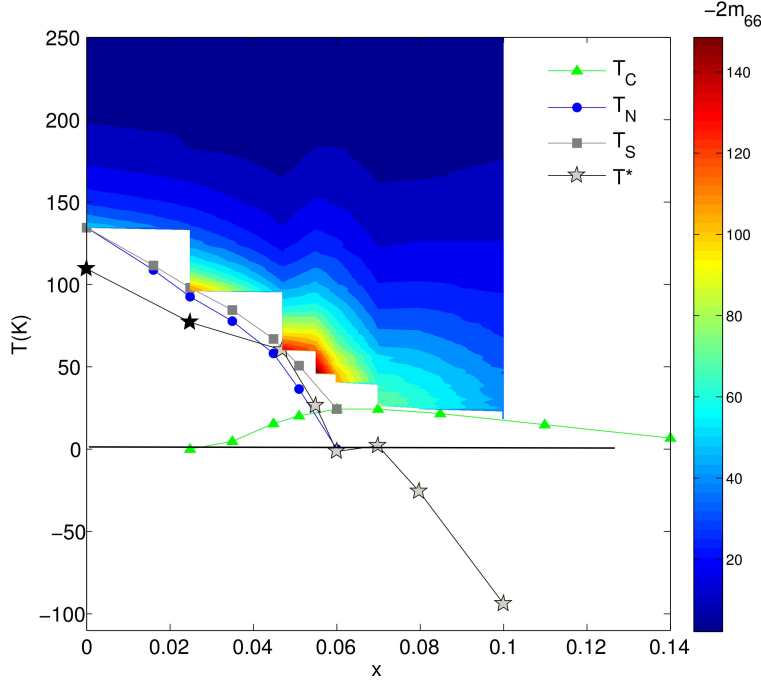


Figure 4: **Phase diagram of  $\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$ , showing the variation of  $2m_{66}$  in the  $x - T$  plane (color scale).** Squares, circles and triangles indicate  $T_s$ ,  $T_N$ , and  $T_c$  respectively. Stars indicate the bare mean-field nematic critical temperatures,  $T^*$ , extracted from the Curie-Weiss fits of  $2m_{66}$  above the temperature at which disorder effects suppress the nematic susceptibility (see text; light grey symbols are used for the cases for which deviations from Curie Weiss behavior are observed at low temperatures). As has been previously determined via longitudinal elastoresistance measurements (13), but established here by the full  $B_{2g}$  differential elastoresistance, the Weiss temperature,  $T^*$  goes through zero as a function of  $x$  close to optimal doping. Color scale shows the magnitude of  $-2m_{66}$ , which peaks between lightly underdoped to optimally doped compositions.