

Verification & Validation: Measured Credibility, on Demand, for Stockpile Applications

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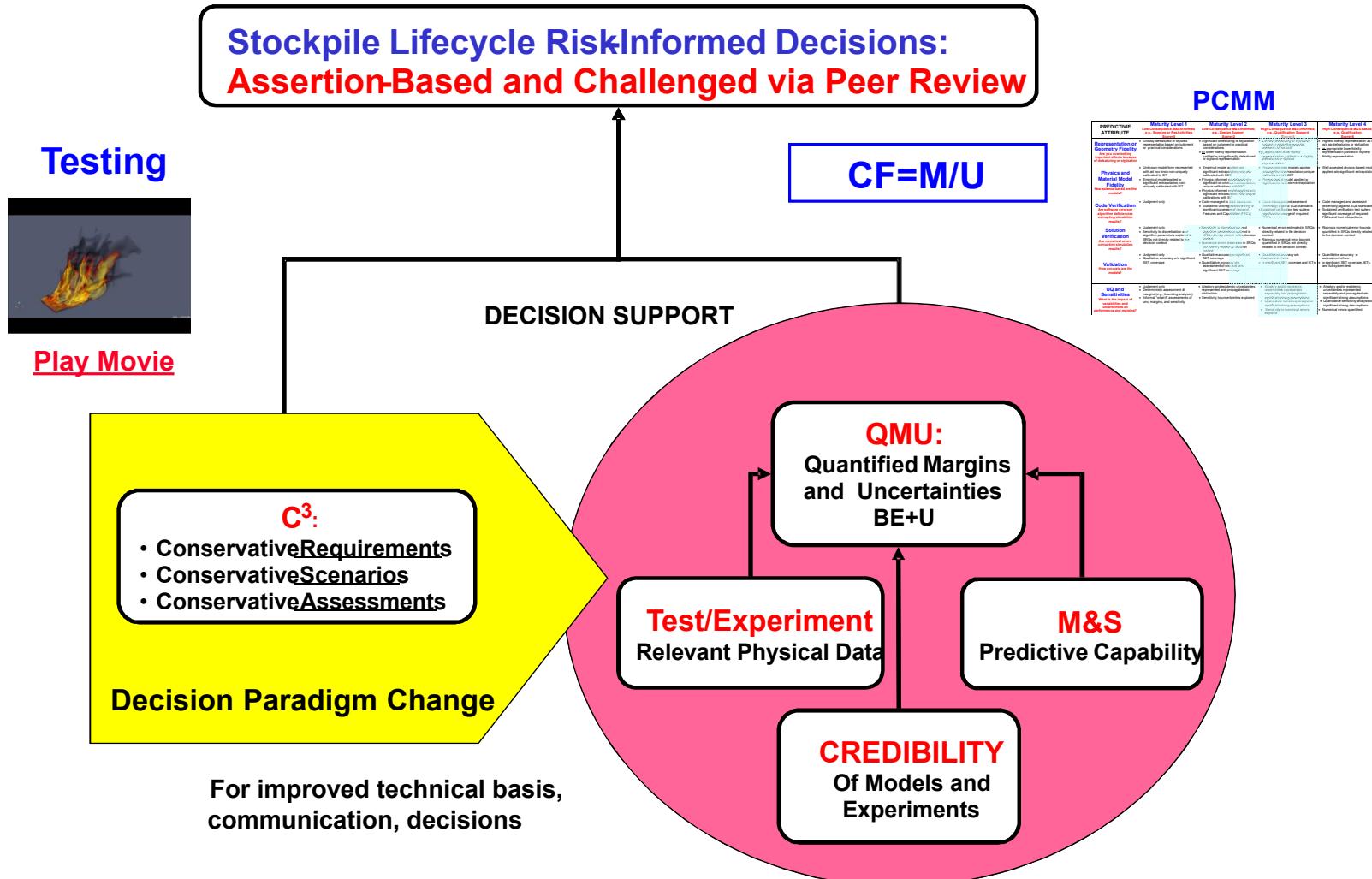


We Need V&V Because We Care!



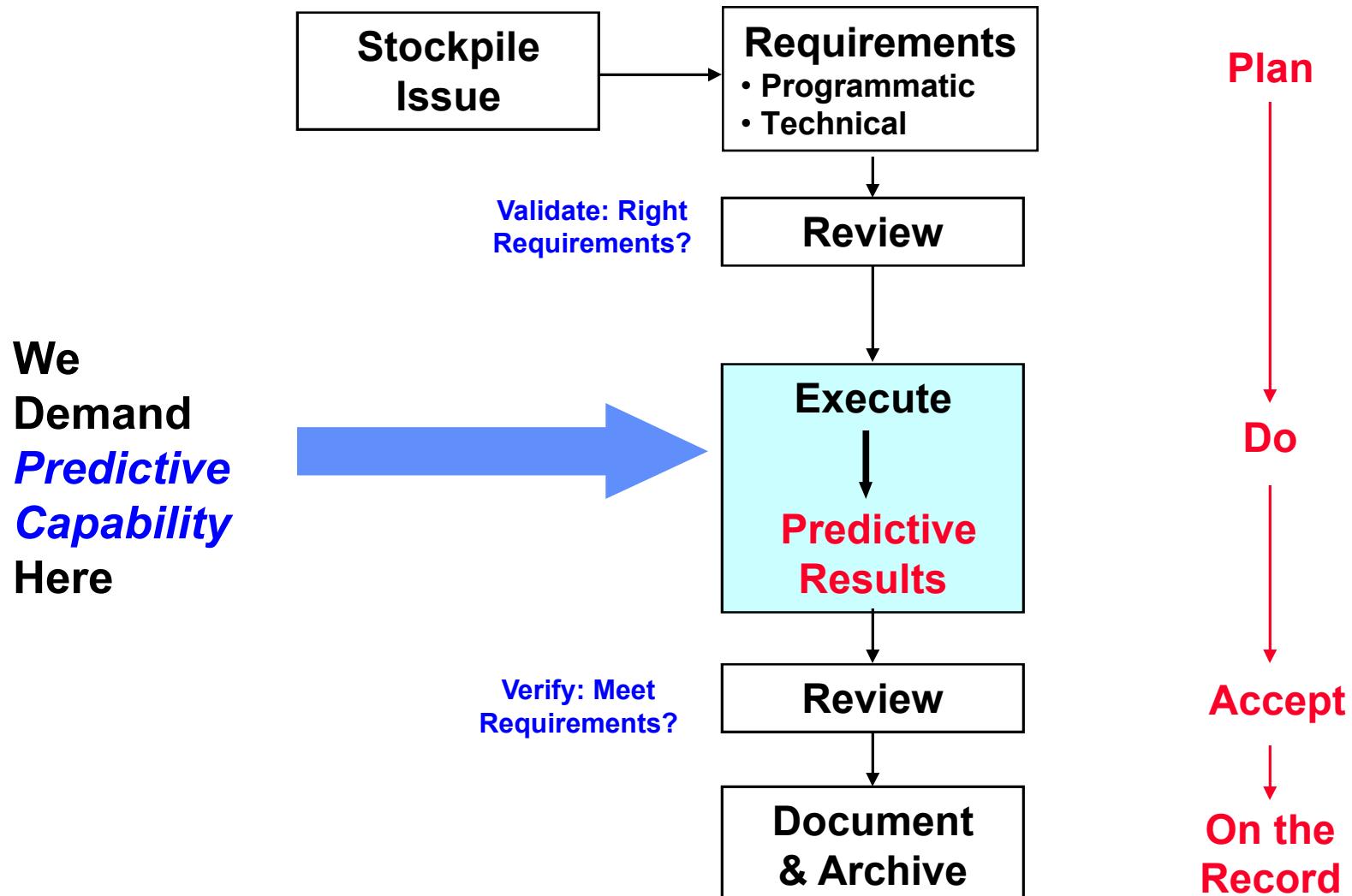
- **Stockpile Applications**
 - There *is* a decision context: High consequence design and decision making associated with nuclear weapons
- **On Demand**
 - Agility and responsiveness are critical to the nuclear weapons complex of the future
- **Measured Credibility**
 - What's the “certificate of credibility” that accompanies M&S results

M&S Increasingly Contributes to Risk-Informed Decisions at Sandia



High Consequence Issues Demand Predictive Capability

Concepts of Stockpile Computing: SAND2004-2479





What Does it Mean “to Predict”?

American Heritage Dictionary:

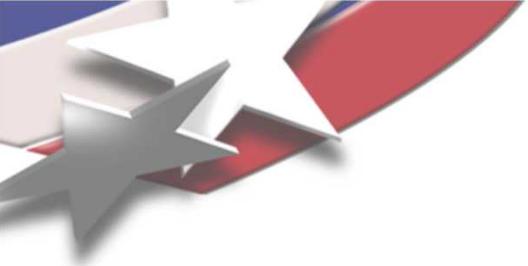
- **Predict:** To state, tell about, or make known in advance, especially on the basis of *special knowledge**

**What *special knowledge* do we demand
of M&S to assert a predictive capability
and how do we communicate it?**



You Can't Measure and Communicate "it" Unless You Know What "it" Is

- **Some Attributes of Predictive Capability**
 - Representation or geometric fidelity
 - Physics and material model fidelity (predictive science)
 - Code verification
 - Solution verification
 - Validated models
 - Uncertainty quantification with sensitivity analysis



How Much is Enough?

Increasing Rigor
Expected

- Sufficiency can only be discussed in an application context
- Graded approach
 - Maturity Level 1:
 - Low-consequence, M&S-informed (e.g., scoping studies)
 - Maturity Level 2:
 - Low-consequence, M&S-informed (e.g., design support)
 - Maturity Level 3:
 - High-consequence, M&S-informed (e.g., qual support)
 - Maturity Level 4:
 - High-consequence, M&S-based (e.g., qualification)
- Negotiate expectations for future work or communicate maturity for work already done

This is Where We Are Going

Predictive Capability Maturity Model (PCMM)

PREDICTIVE ATTRIBUTE	Maturity Level 1 Low-Consequence M&S-Informed, e.g., Scoping or Res Activities Score=0	Maturity Level 2 Low-Consequence M&S-Informed, e.g., Design Support Score=2	Maturity Level 3 High-Consequence M&S-Informed, e.g., Qualification Support, Score=4	Maturity Level 4 High-Consequence M&S-Based, e.g., Qualification Score=6
Representation or Geometry Fidelity <i>Are you overlooking important effects because of defeaturing or stylization</i>	<ul style="list-style-type: none"> Grossly defeatured or stylized representation based on judgment or practical considerations 	<ul style="list-style-type: none"> Significant defeaturing or stylization based on judgment or practical considerations or lower fidelity representation justified w a significantly defeatured or stylized representation 	<ul style="list-style-type: none"> Limited defeaturing or stylization judged to retain the essential elements of "as built" or appropriate lower fidelity representation justified w a slightly defeatured or stylized representation 	<ul style="list-style-type: none"> Highest fidelity representation "as is" w/o sig defeaturing or stylization or appropriate lower fidelity representation justified w highest fidelity representation
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Why PCMM?

- Educate the decision maker about what should be expected from M&S
- Measure/communicate process maturity (not adequacy of results) associated with M&S in a decision context
- Provide program vision so that technical and infrastructure needs can be leveraged across multiple funding lines to enhance the credibility of M&S results
- Speak to the *whats*, not dictate the *hows*

Setting the National Agenda in V&V

Representation or Geometric Fidelity

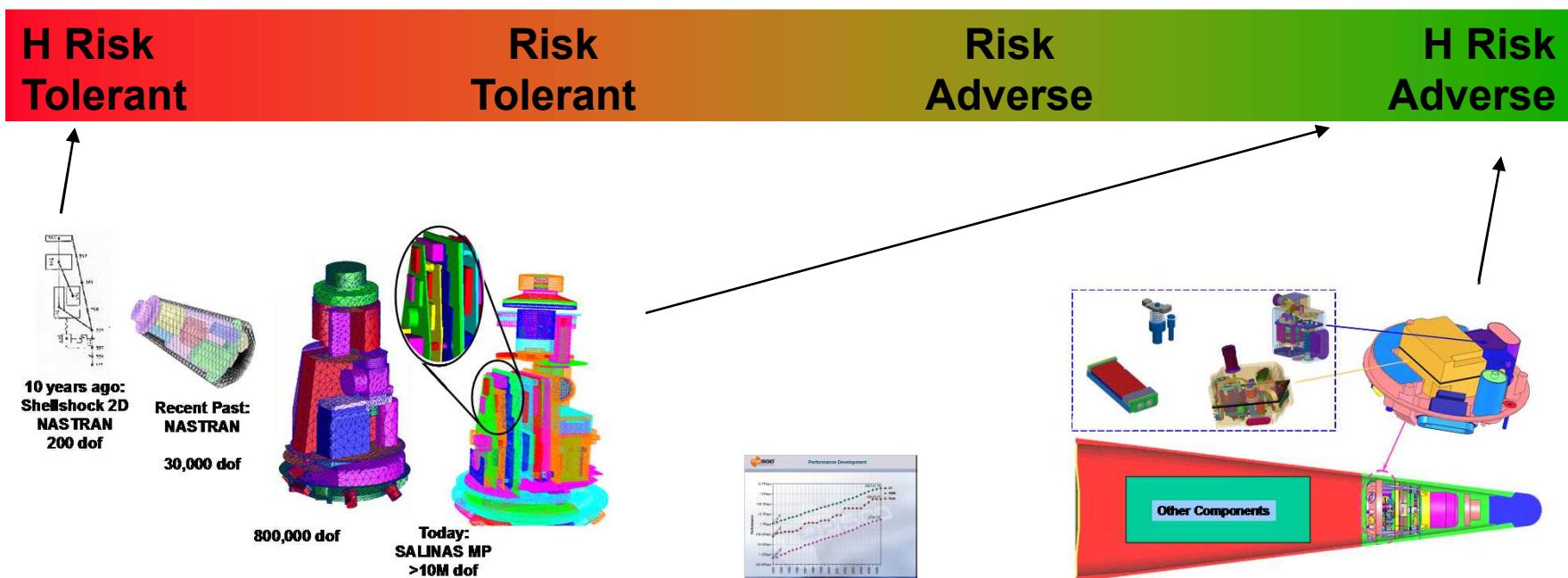
Are you overlooking important effects because of judgment-based Defeaturing or Stylization?

Grossly defeatured or stylized

Significant D&S based on judgment

Limited D&S judged to retain the essential elements of "as built"

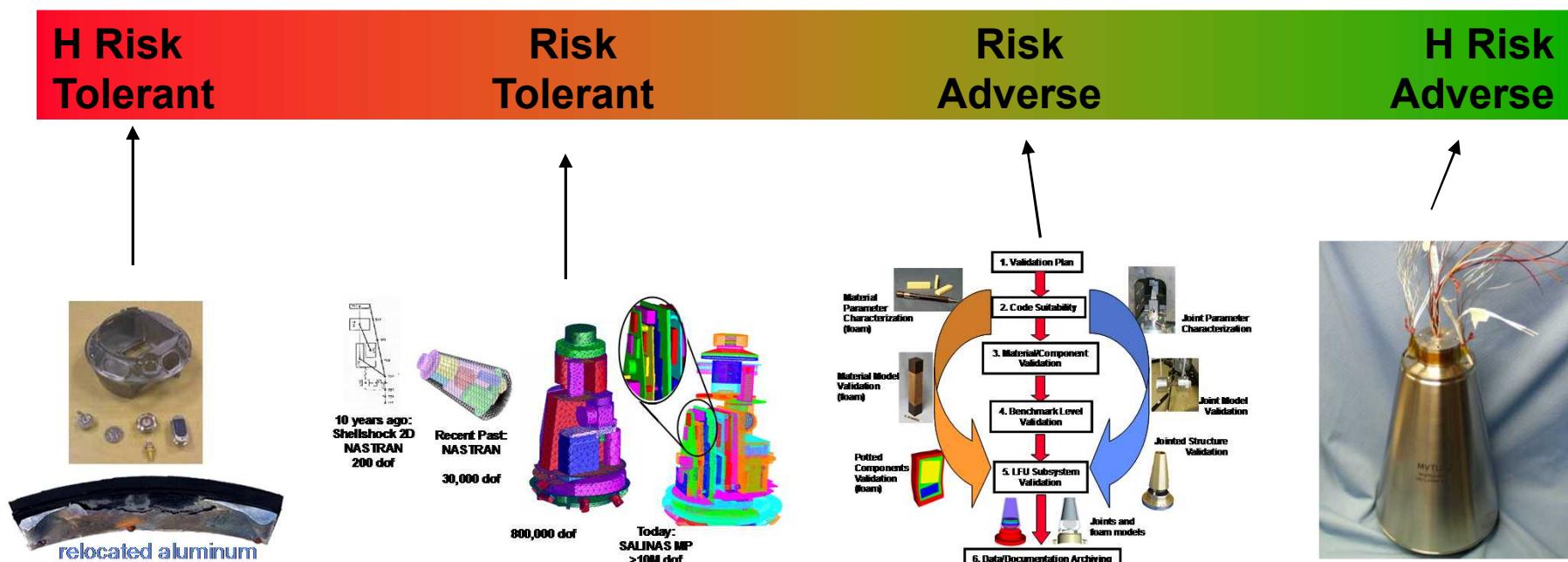
Highest fidelity representation "as built" w/o significant D&S



Physics and Material Model Fidelity

Are the models science-based?

Unknown model form or empirical model form applied w sig extrap	Empirical model form applied w/o sig extrap or physics informed model applied w sig/unk extrap	Physics-informed model applied w/o sig extrap or physics based model applied w sig/unk extrap	Physics-based model applied w/o sig extrap
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Code Verification

Are software errors or algorithm deficiencies corrupting simulation results?

Judgment only

Code managed to SQE standards

Sustained unit/regression tests w sig coverage of F&C

SQE +assessment + sustained VERTS w sig coverage of F&C

SQE(A) + VERTS w sig coverage of F&C interactions

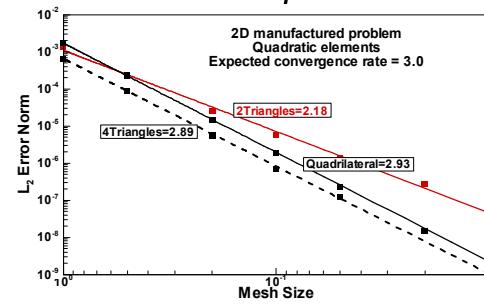
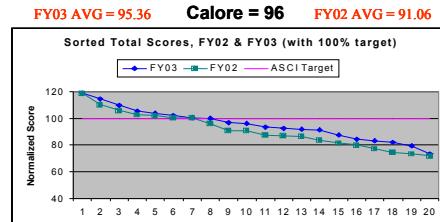
H Risk Tolerant

Risk Tolerant

Risk Adverse

H Risk Adverse

Code/Code Comparisons



		Verification Test Suite		
	Features & Capabilities	Unit Tests	VERT 1	VERT 2
Code A	FC1	UT1	VT1	
	FC2	UT1	VT1	
	FC3	UT2	VT1	
	FC4	UT3	VT1	
	FC5			
Code B	FC6	UT4		VT2
	FC7	UT5		VT2
	FC8	UT6		
	FC9	UT7		VT3
	FC10	UT8		VT3
Code or Applic Perspective		$f = \frac{\sum_{r=1}^{NFC} \left(\sum_{i=1}^{Nv} C_r \right)}{NFC \sum_{r=1}^{NFC} C_r}$		
Line or Cap Coverage		80%		
		Capability+Interaction Coverage		
		3.22%		

Solution Verification

Are numerical errors corrupting simulation results?

Judgment only

Explore sensitivity to discretization and algorithm parameters

Estimate numerical errors

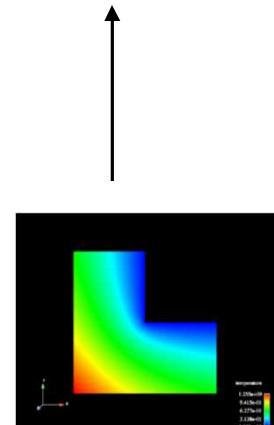
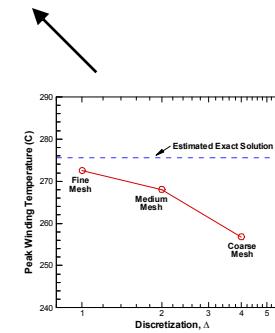
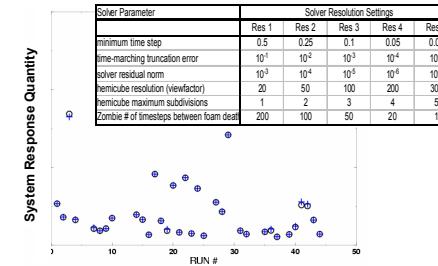
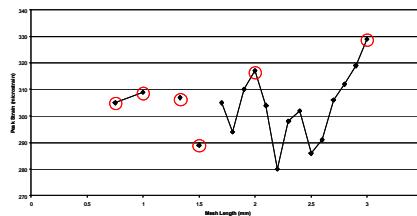
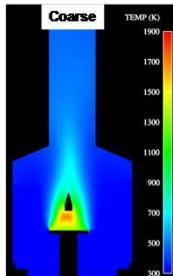
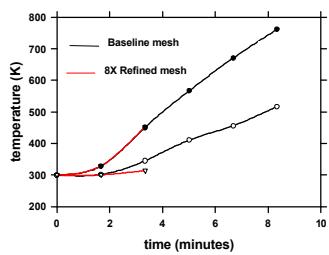
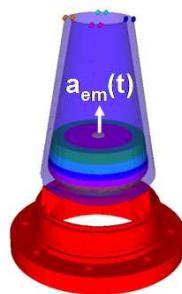
Quantify rigorous numerical error bounds

H Risk Tolerant

Risk Tolerant

Risk Adverse

H Risk Adverse



Validation

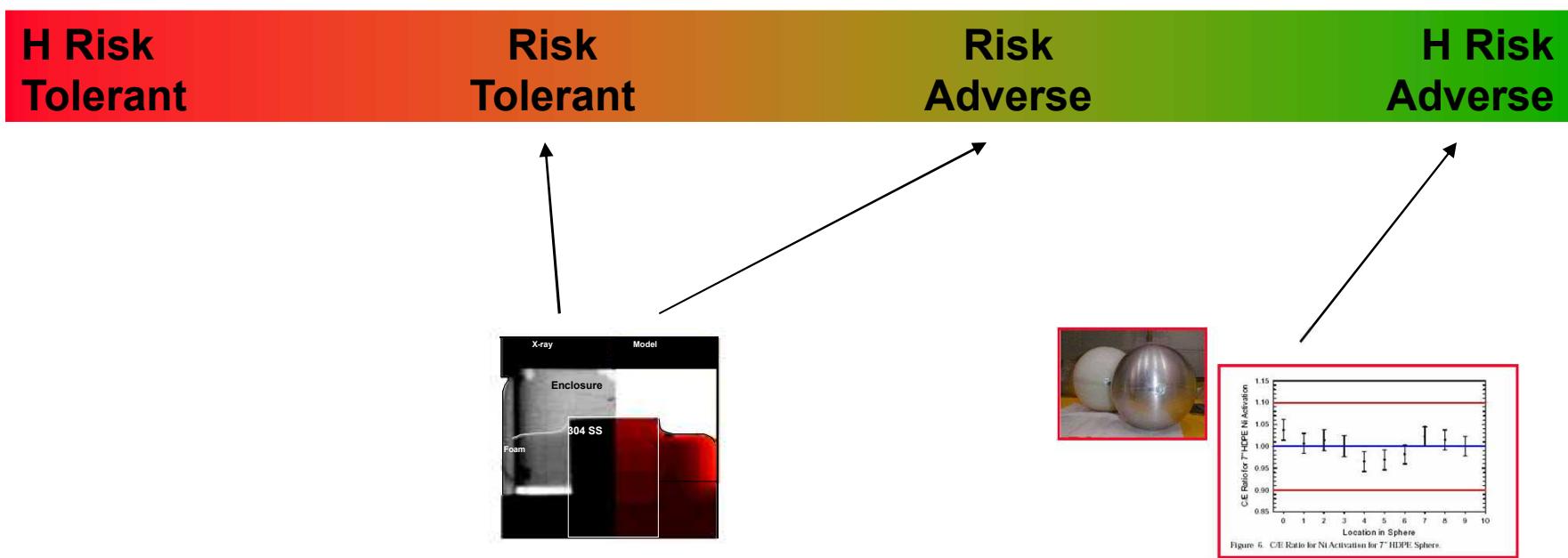
How accurate are the models?

Judgment only

Qual accuracy w SET coverage

Quantitative accuracy w/o assessment of unc and w SET coverage and IETs

Quantitative accuracy w assessment of unc and SET coverage and IETs and full system



Uncertainty Quantification and Sensitivities

What is the impact of variabilities and uncertainties on performance and margins?

Judgment only
Deterministic assessment of margins or informal “what if” studies

Aleatory and epistemic unc represented w/o distinction
Sensitivities explored

Aleatory/epistemic unc interpreted separately w strong assumptions
Sensitivities w strong assumptions
Sensitivity to numerical errors exp

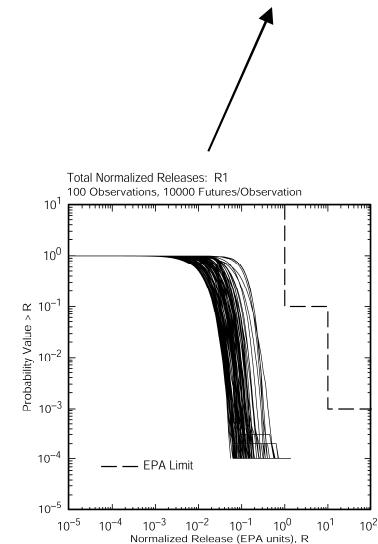
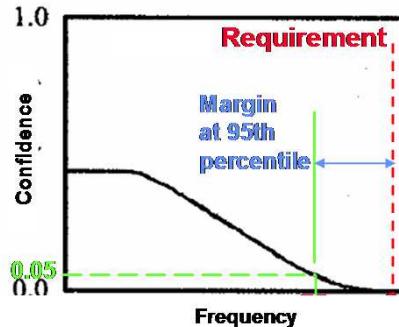
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Numerical errors quantified

H Risk Tolerant

Risk Tolerant

Risk Adverse

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ASC Projects Should Map to Capability/Agility Needs

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V&V Methods

DART

PEM

Adaptivity

Codes and Platforms

Predictive Capability Maturity Model (PCMM)

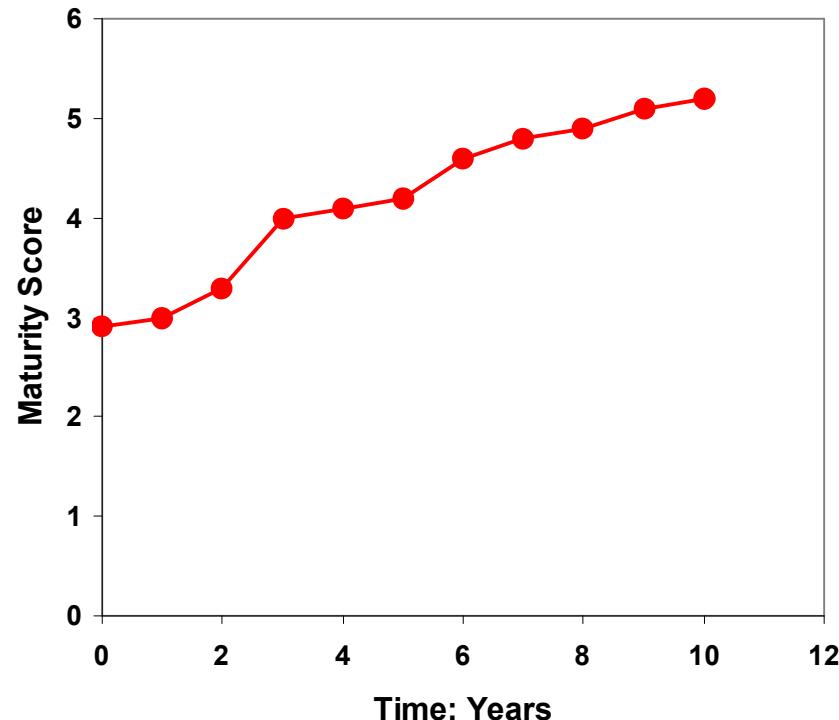
Communicating Credibility

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Measure Progress Over Time

Application: Legacy Weapon in Fuel Fire

	Rollup Scores	Avg/Avg Score	Avg/Min Score
Representation or Geometric Fidelity			
Fire Environment	4.5	4.0	4.0
Weapon	5.0	5.0	5.0
Physics and Material Model Fidelity			
Fire Environment	3.2	3.0	1.0
Fuel vaporization from spill	2.0	2.0	2.0
Fluid mechanics	4.0	4.0	4.0
Turbulent mixing	3.0	3.0	3.0
Combustion	4.0	4.0	4.0
Emmission	2.0	2.0	2.0
Radiative transport to weapon	4.0	4.0	4.0
Convective transport to weapon	2.0	2.0	2.0
Weapon Thermal Response	3.3	3.3	0.0
Code Verification			
Fire Environment	2.0	2.0	2.0
Weapon Thermal Response	2.0	2.0	2.0
Solution Verification			
Fire environment	1.5	1.0	1.0
Weapon thermal response	2.0	2.0	2.0
Validation			
Fire Environment	2.1	1.6	0.0
Weapon Thermal Response	2.3	2.3	0.0
UQ/SA		4.0	4.0



Note: all scores are notional



***Measured Credibility*, on Demand, for Stockpile Applications**

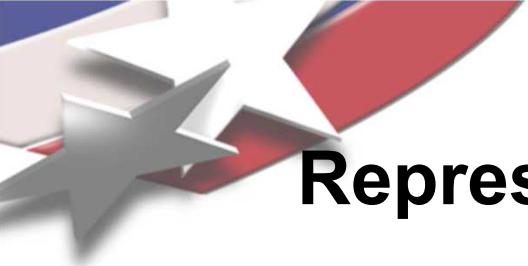
- Decision makers need to understand predictive capability in order to make informed decisions and to efficiently leverage and make use of research dollars
- Progress in predictive capability needs to be measured in each individual decision context
 - Predictive capability is more than geometric fidelity or even physics fidelity
 - There is a need to define sufficiency (or adequacy) in each attribute of predictive capability
- The **Predictive Capability Maturity Model** provides a graded approach to assessing and measuring predictive capability for specific applications



The Credibility of M&S is Critical



“Due diligence means asking *all* the questions, even if you don’t think you’ll like the answers.”

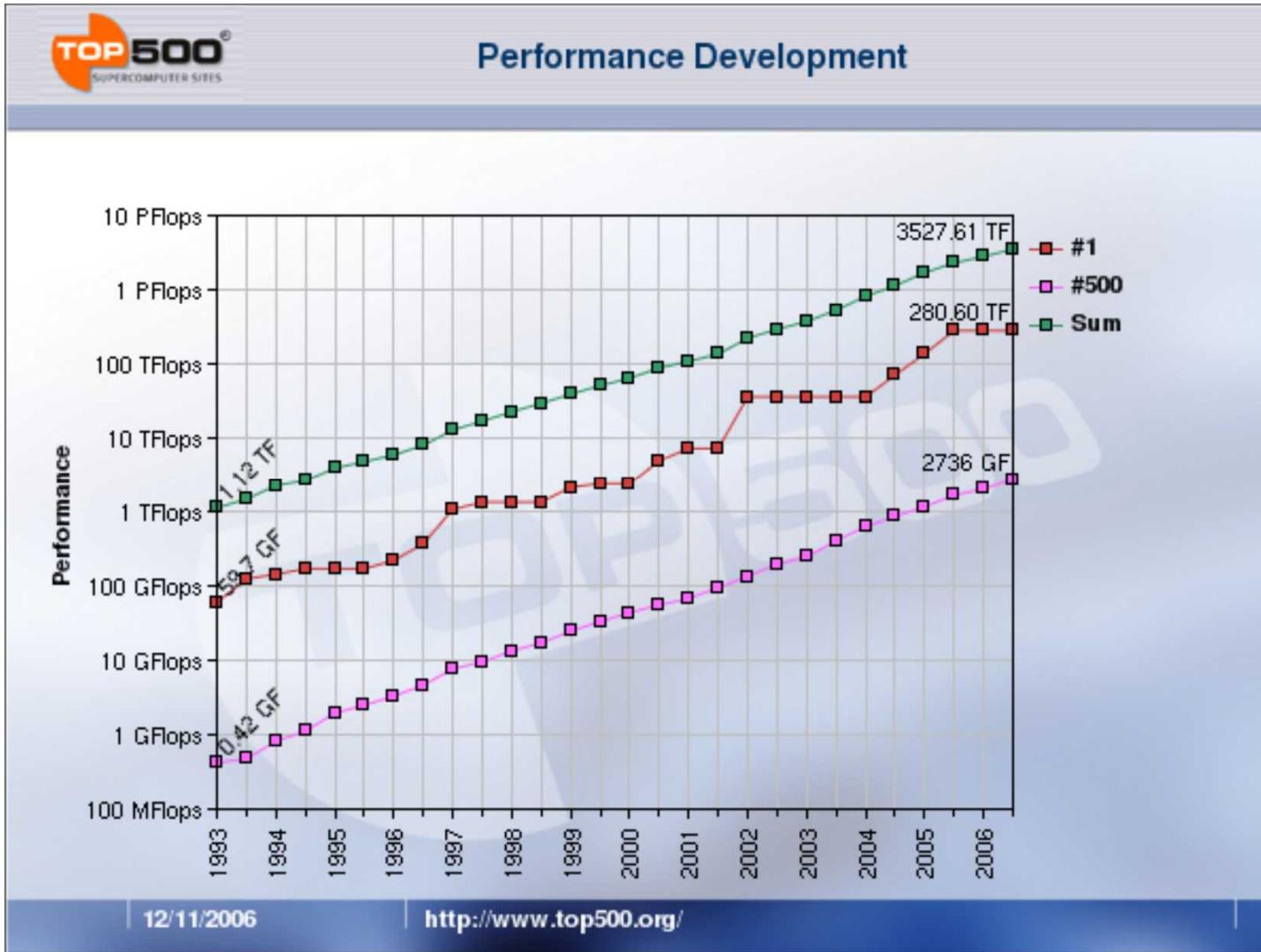


Representational (Geometric) Fidelity

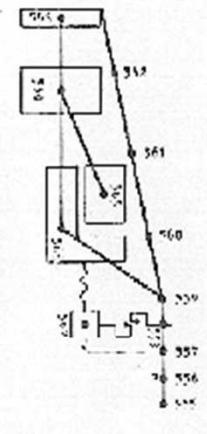
Hyperlinks

Imagine the Future!

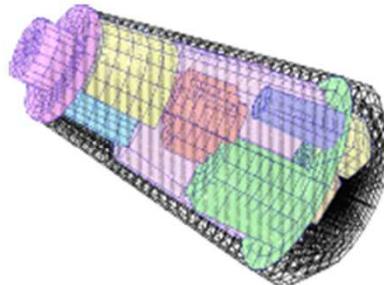
Computing Speed - Dec. 2006



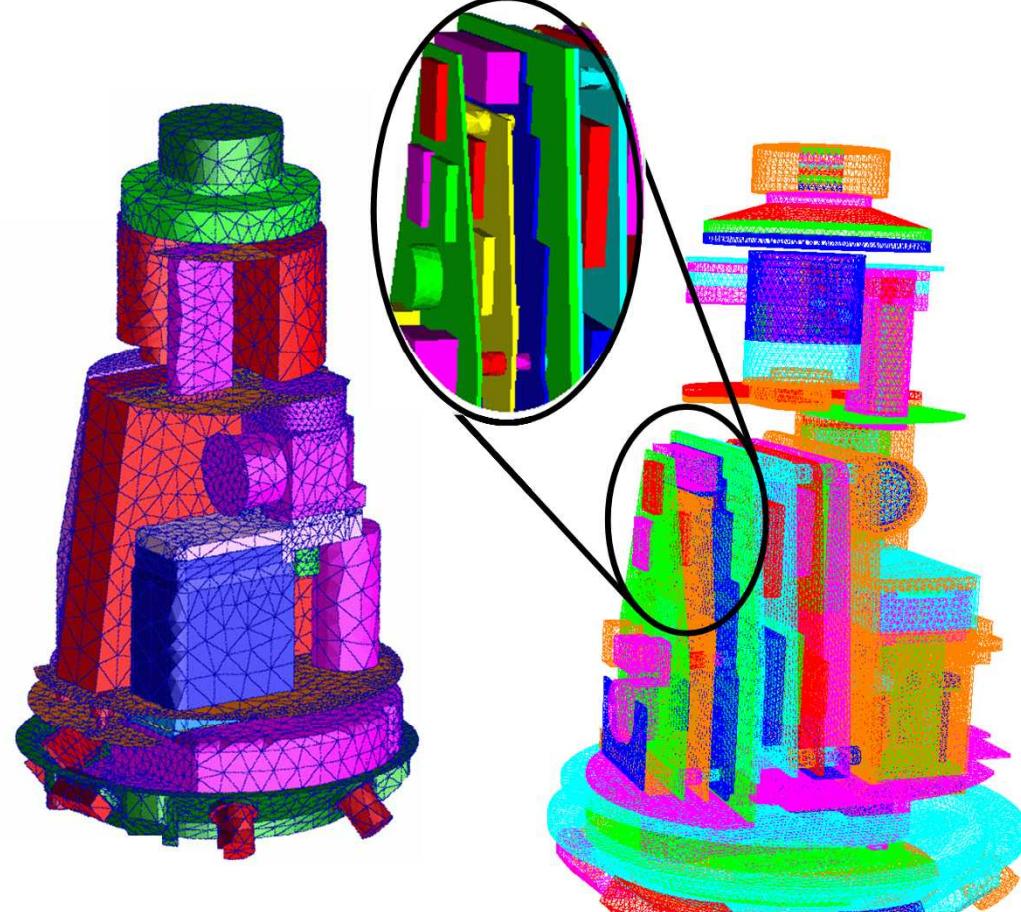
Progress in Representational Fidelity in Structural Dynamics



**10 years ago:
Shellshock 2D
NASTRAN
200 dof**



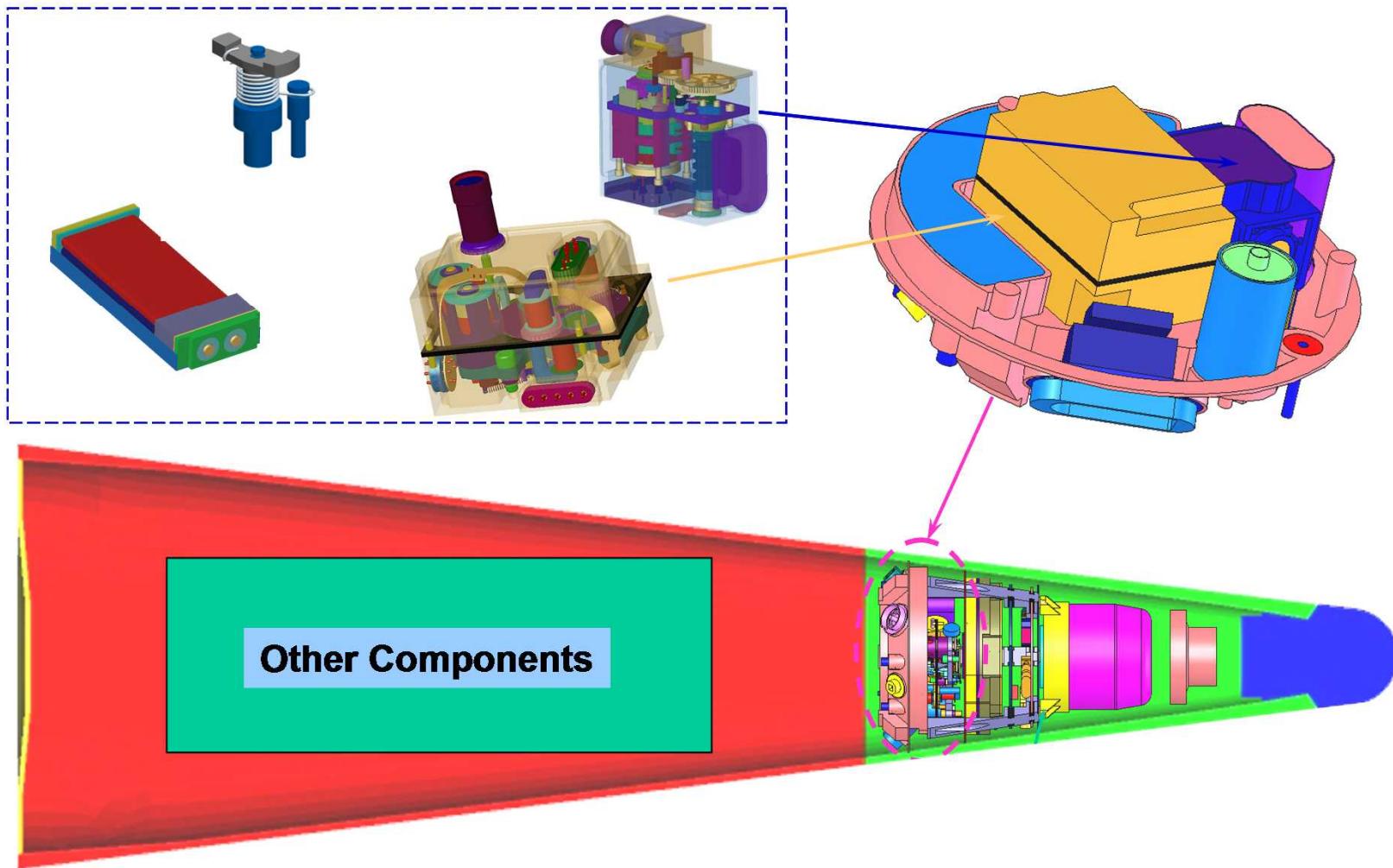
**Recent Past:
NASTRAN
30,000 dof**

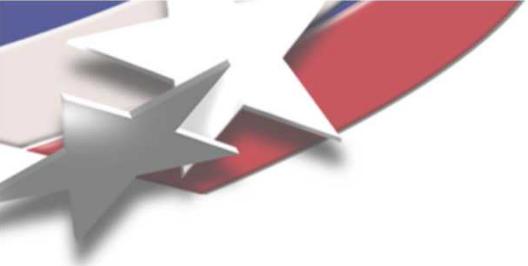


**Today:
SALINAS MP
>10M dof**



Progress in Representational Fidelity Thermal Modeling





Physics Fidelity

Hyperlinks

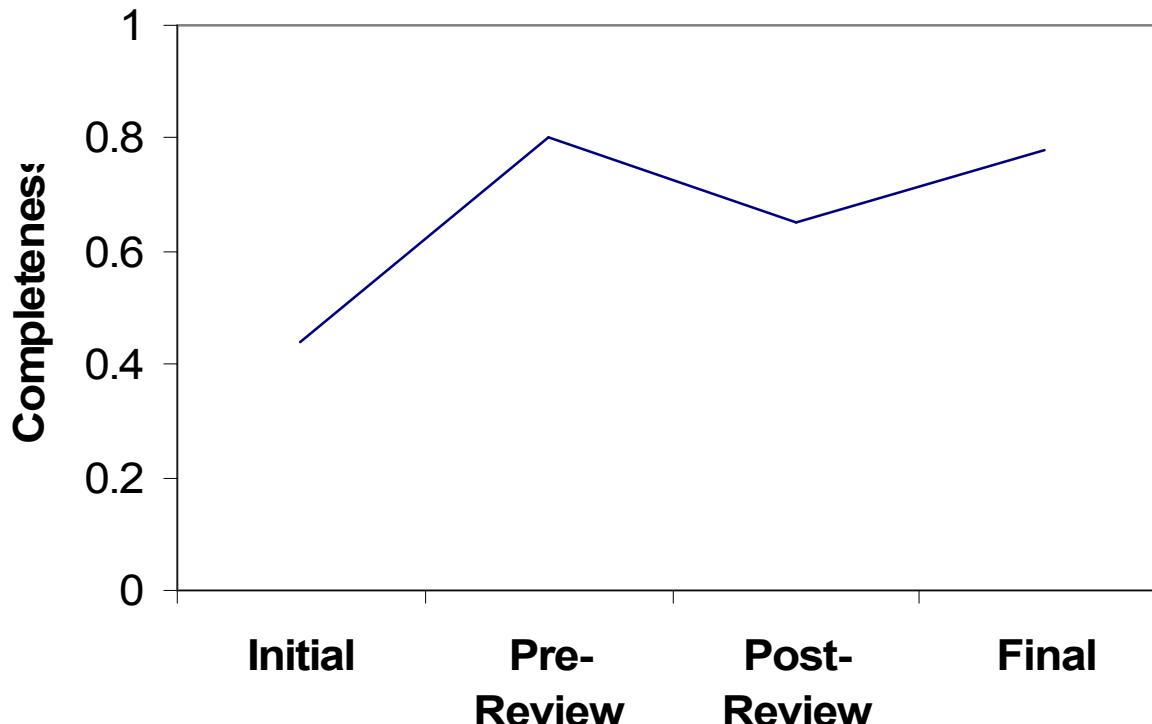
Phenomena Identification and Ranking Tables (PIRT)

Establish efficiency and sufficiency of activities

Phenomena	Importance	Adequacy		
		Model	Code	Validation
P1	H	H	M	L
P2	M	M	L	L
P3	L	L	L	L

Gap = 5

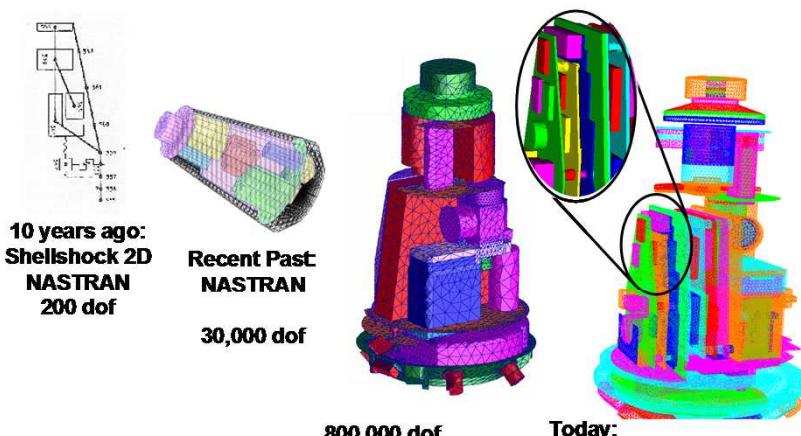
Completeness = 0.44



Low Physics Fidelity

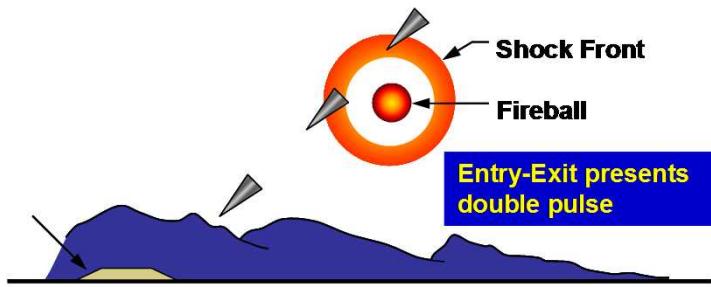


- Conduct blast test

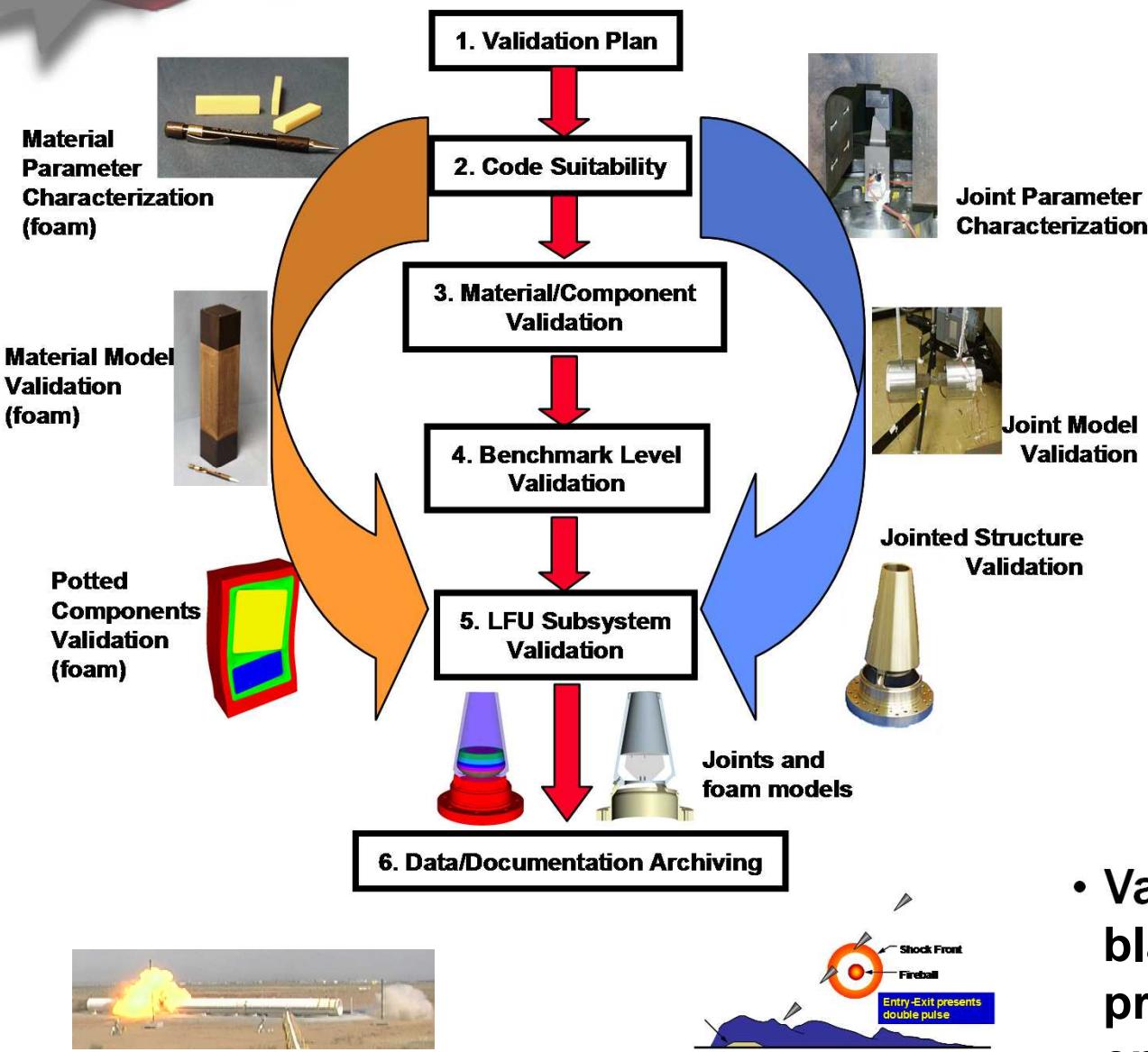


- Calibrate model to blast test using global **stiffness** and **damping** parameters: **knobs that act as surrogates for missing or unknown physics**

- Use calibrated model to make prediction in tactical environments



Improving Physics Fidelity



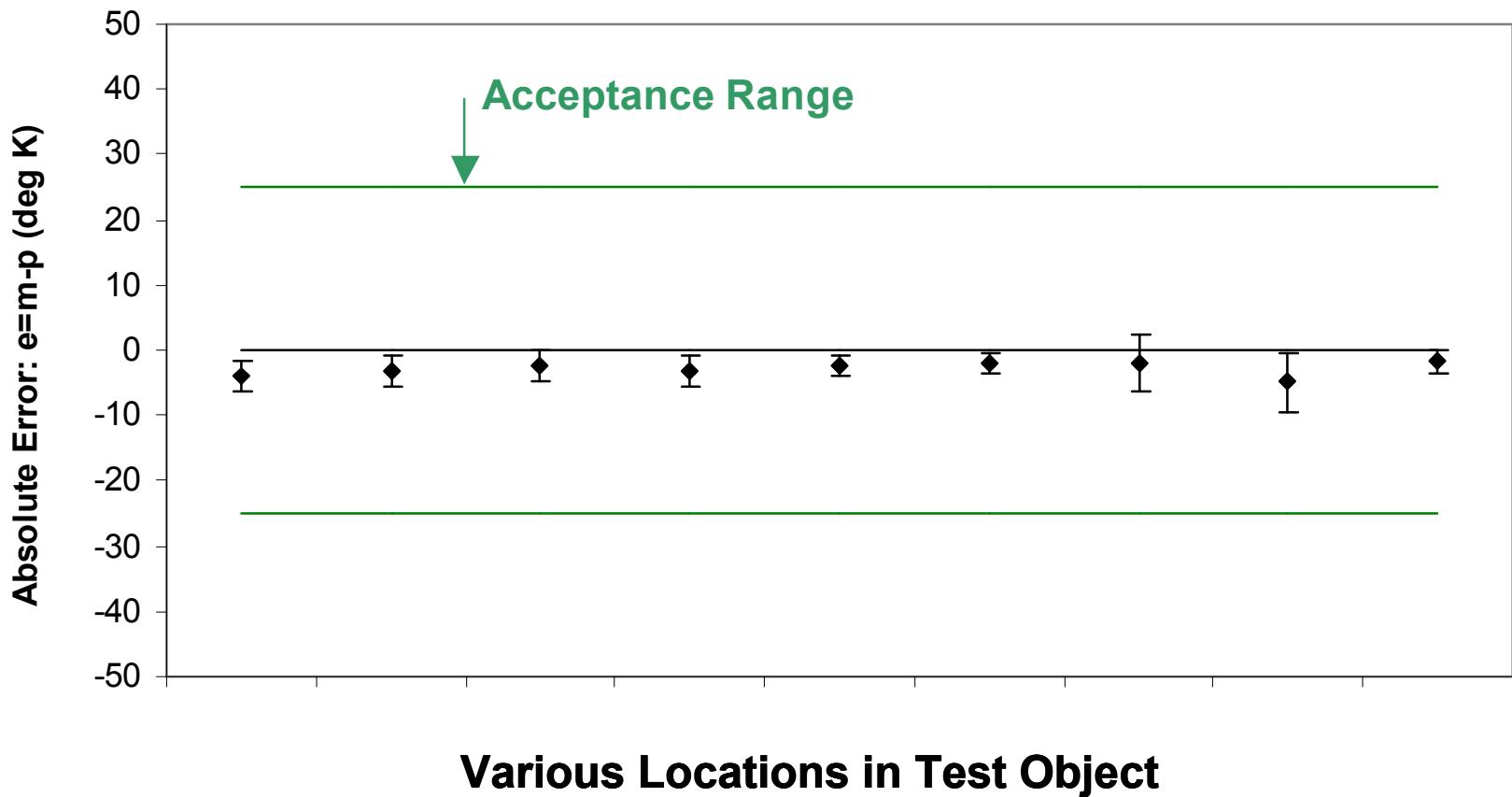
- Physics-informed models validated against separate effects tests

- Validate against blast test and make prediction in tactical environments



Well Established Physics Fidelity

$e \sim 2K$ for conduction





Code Readiness

Hyperlinks

Attributes of Verification

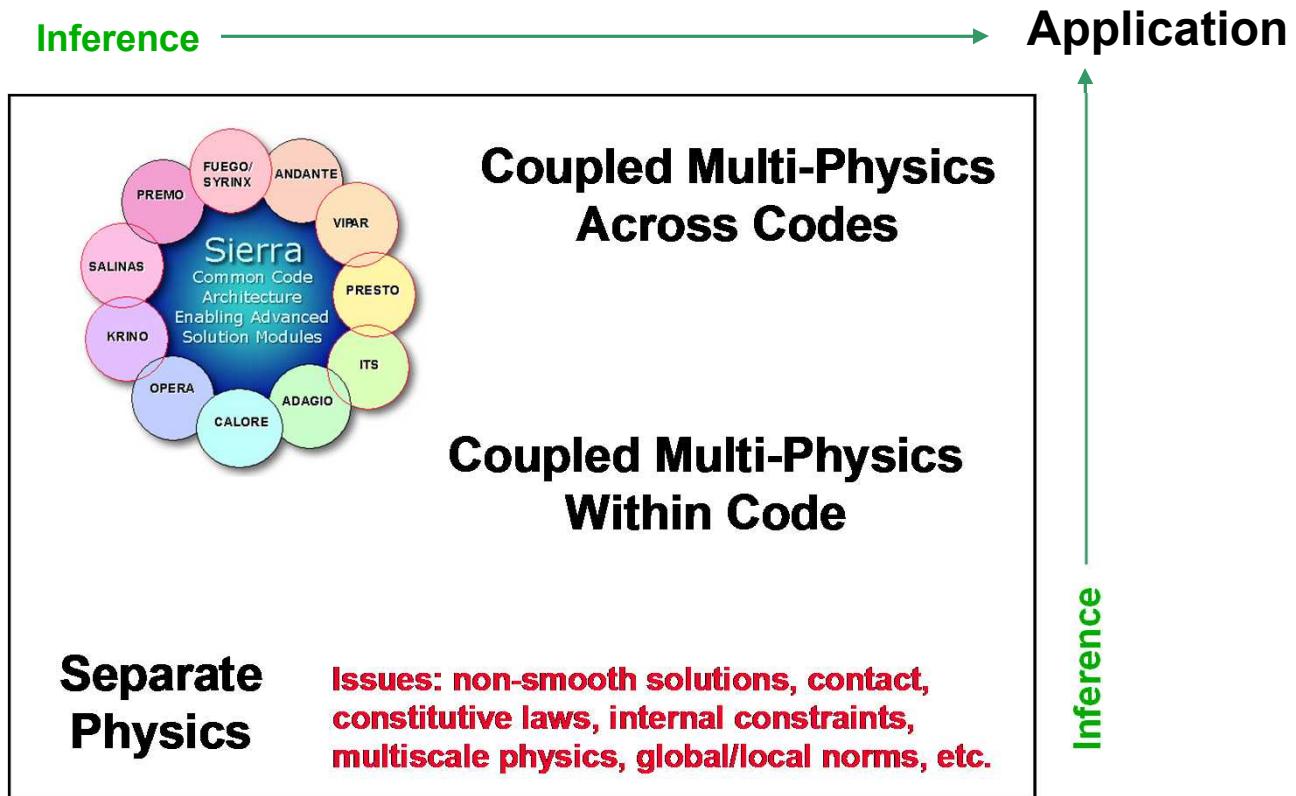
Demonstrating **Convergence to Correct Answer**
for the **Intended Application**

- Solution Verification: **Convergence for intended application, but is it the right answer?**
- **Address adequacy of spatial AND temporal AND other discretizations AND numerical knobs**

Regression Testing

SQE(A)

Pilch – VV 2007



Code Verification: **Convergence to correct answer, wrong application**

- **Eliminate code bugs AND inadequate algorithms**



Code to Code Comparisons Are a Poor Substitute for Formal Verification

Code Comparison Principle (CCP)

Code 1 = assessed code Code 2 = benchmark code

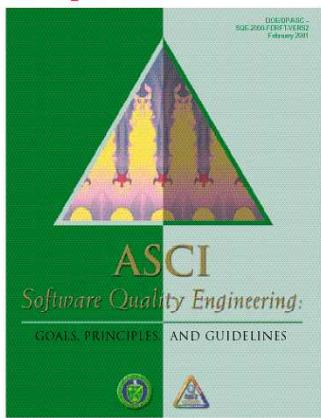
$$\| \text{Code 1} - \text{Truth} \| \leq \| \text{Code 1} - \text{Code 2} \| + \| \text{Code 2} - \text{Truth} \|$$

- $\| \text{Code 1} - \text{Code 2} \|$ - **What if this term is not negligible?**
 - Could be that Code 1 models are different from Code 2 models
 - Could be a bug in Code 1 or Code 2
 - Could be an algorithm flaw in Code 1 or Code 2
 - Could be that Code 1 or Code 2 model is not converged

Points to path for better code-to-code comparisons; but if Code 2 is formally verified, why not verify Code 1 to the same verification test suite? And if not, why bother with the code-to-code comparison?

SQE(A): Demonstrated Due Diligence in the Stewardship of Codes

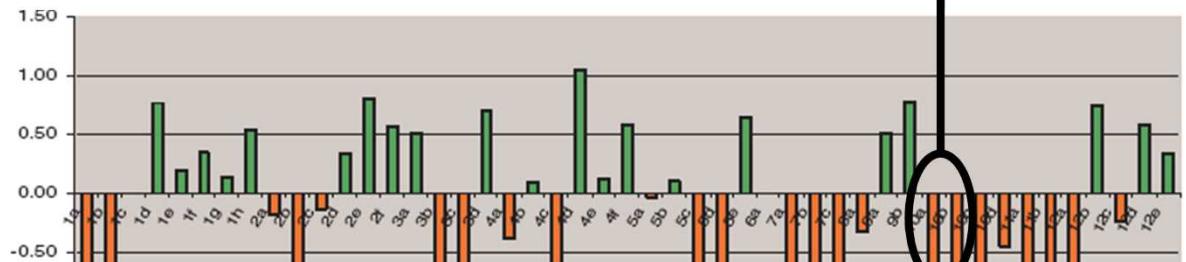
Requirements



FY03 AVG = 95.36

SourceForge: Issue Tracking

Improvement

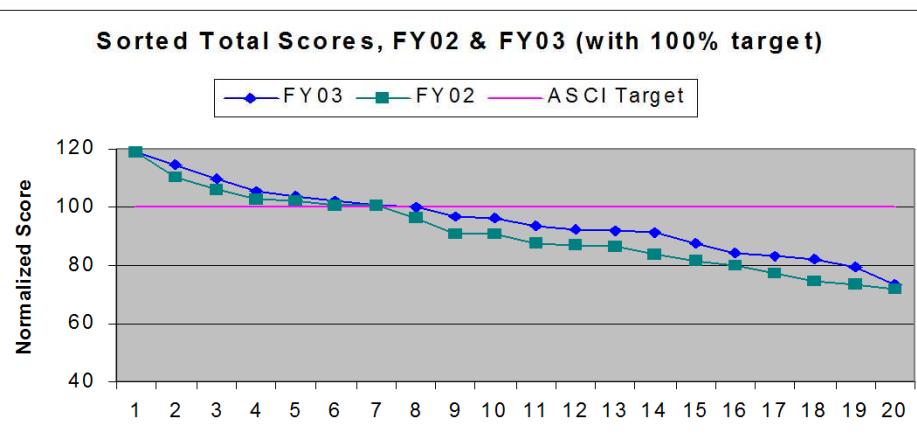


Calore = 96

FY02 AVG = 91.06

Sorted Total Scores, FY02 & FY03 (with 100% target)

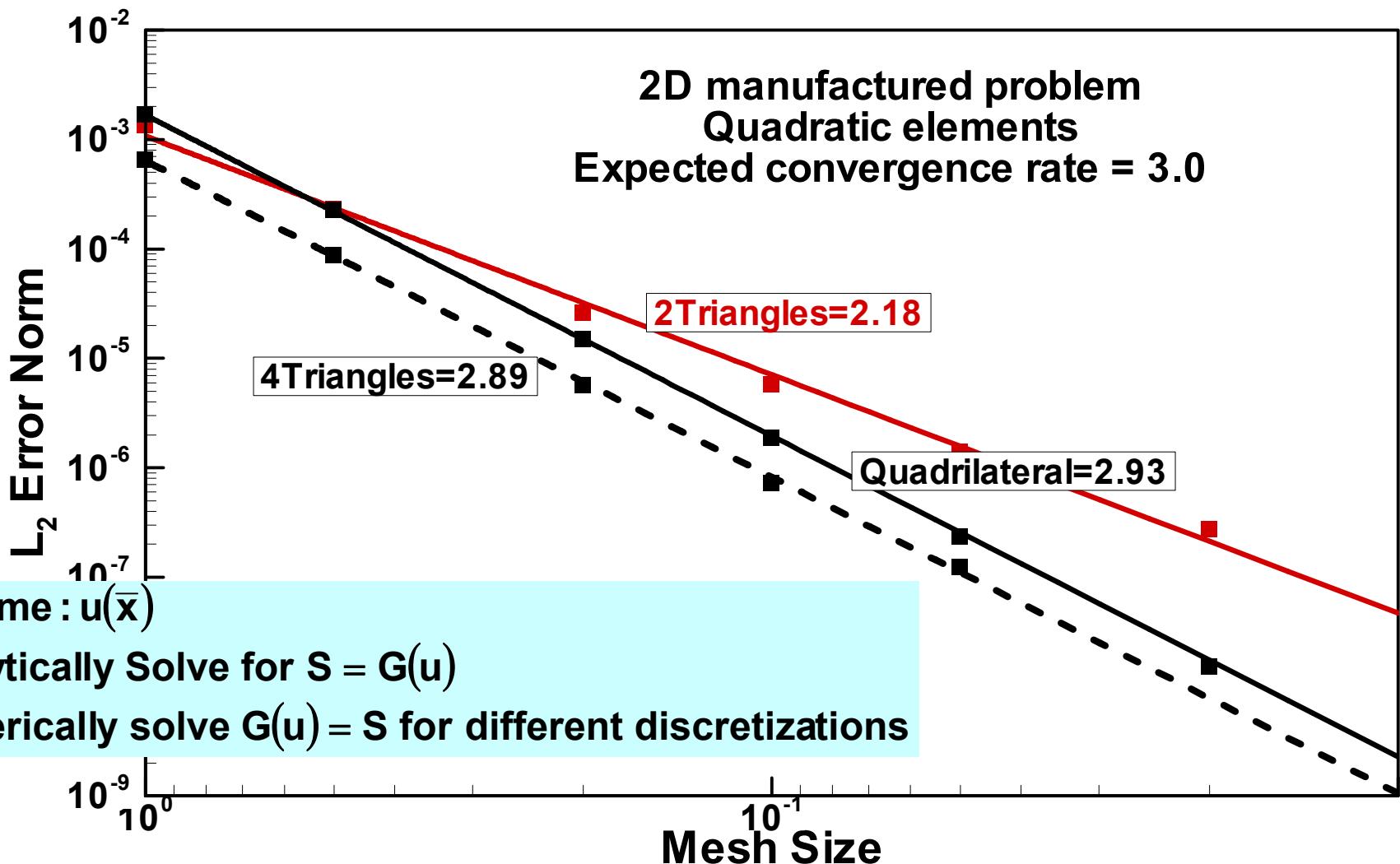
— FY03 ■ FY02 — ASCI Target



Assessments

Verification with Manufactured Solution

CEPTRE: Radiation Transport



Measuring Progress in Code Verification Coverage and Interactions

		Verification Test Suite				
Features & Capabilities		Unit Tests	VERT 1	VERT 2	VERT 3	Ideal
Code A	FC1		VT1			
	FC2	UT1	VT1			
	FC3	UT2	VT1			
	FC4	UT3	VT1			
	FC5			VT2		
Code B	FC6	UT4		VT2		
	FC7	UT5		VT2		
	FC8	UT6				VT3
	FC9	UT7				VT3
	FC10	UT8				VT3
Code or Appl Perspective		Line or Cap Coverage	$f = \frac{\sum_{i=1}^{Nverts} \left(\sum_{r=1}^{nv} C_r \right)_i}{\sum_{r=1}^{NFC} NFC C_r}$			
		80%	Capability+Interaction Coverage 3.22%			



Solution Verification

Hyperlinks

Attributes of Verification

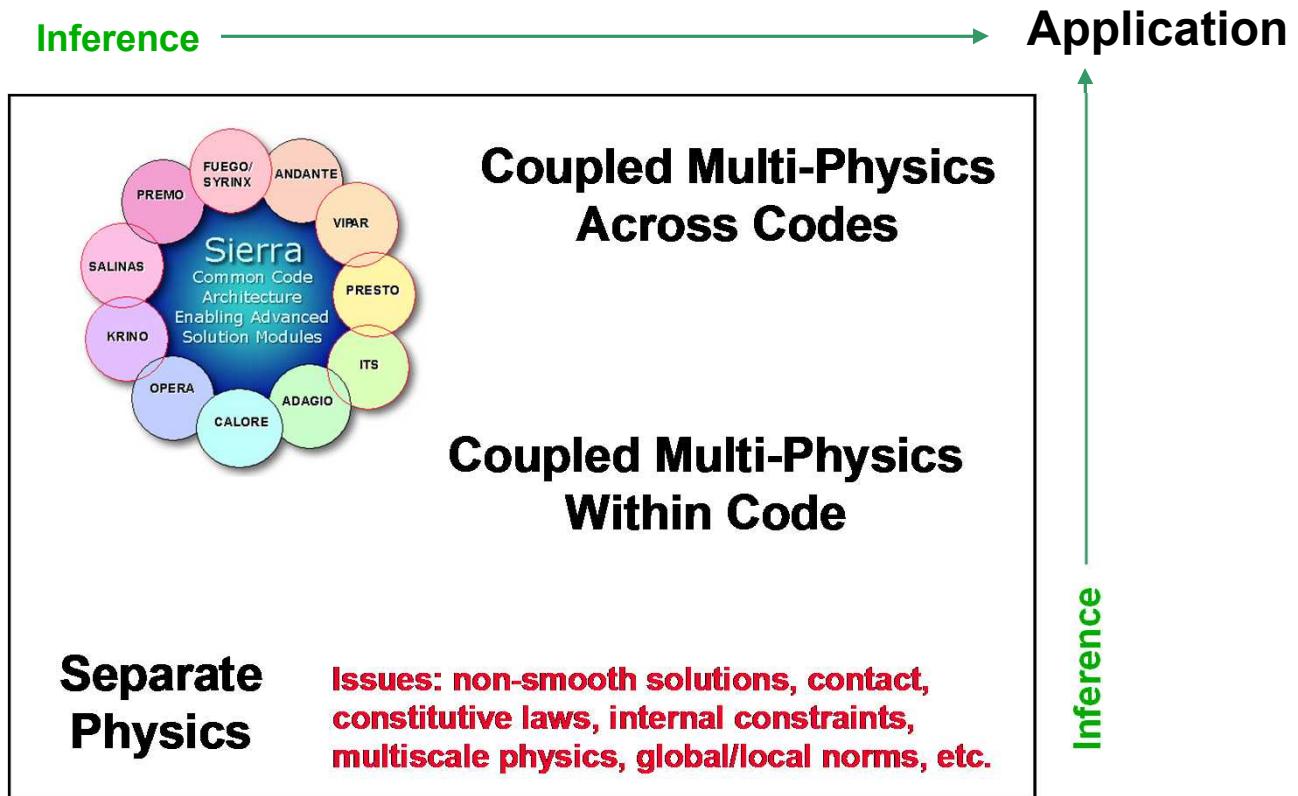
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SQE(A)

Pilch – VV 2007



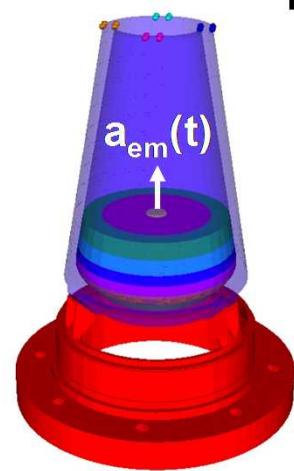
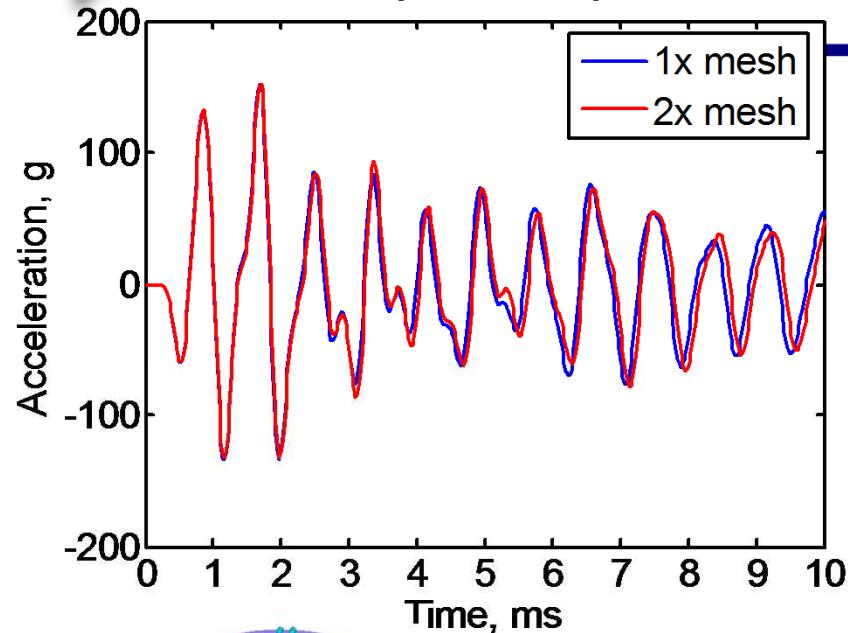
Code Verification: **Convergence to correct answer, wrong application**

- Eliminate code bugs **AND** inadequate algorithms

Sensitivity to Mesh Parameters

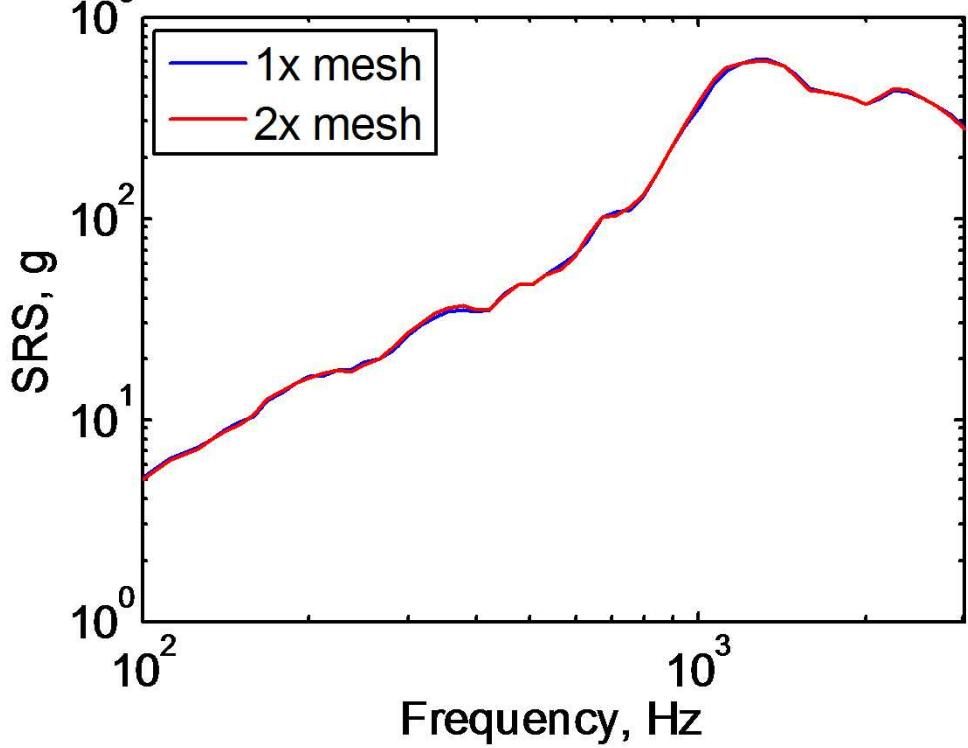
Structural Dynamics

Acceleration response at top of enc. mass



Max. relative error between SRS: +/- 5%

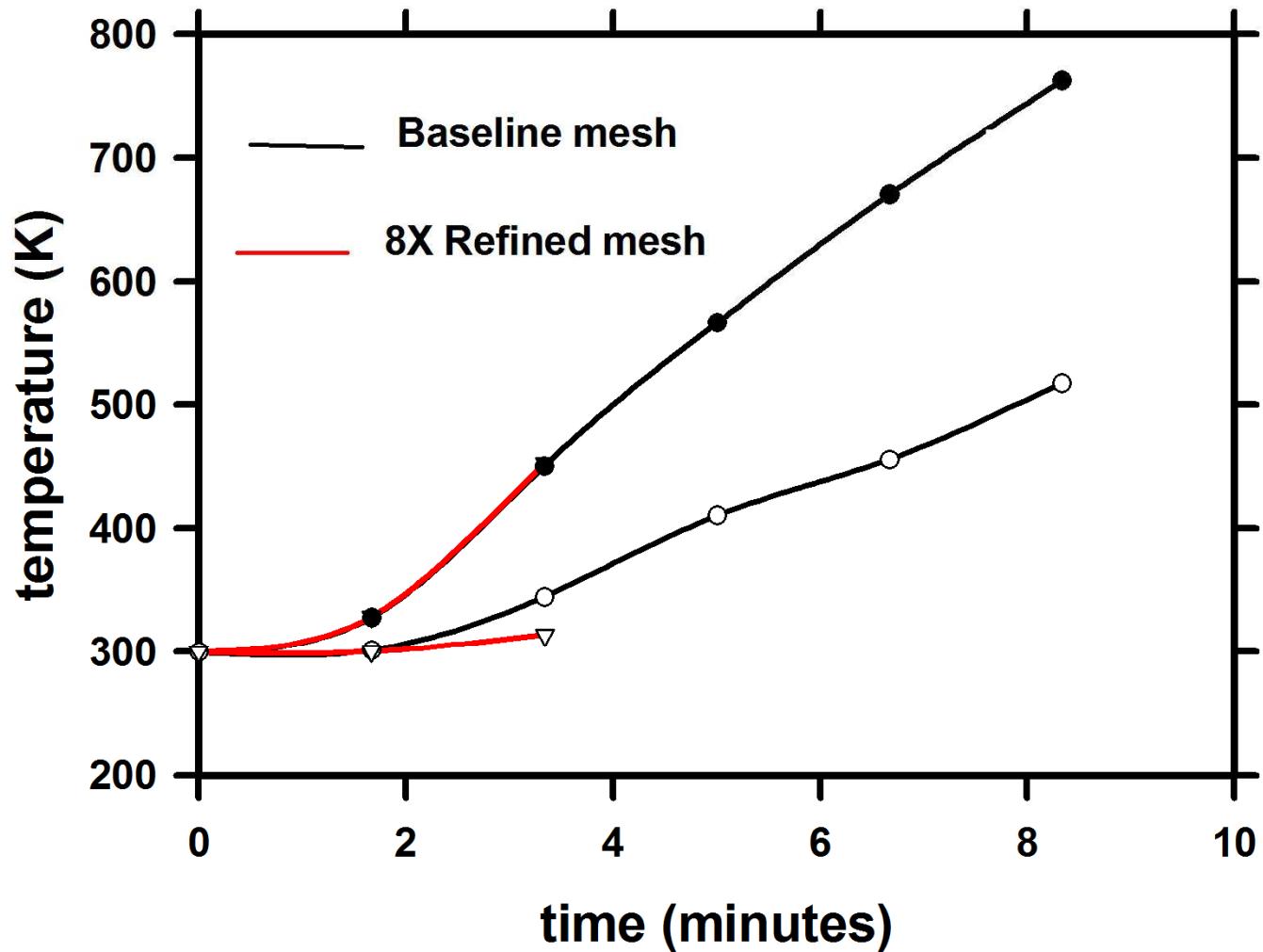
Shock response spectra at top of enc. mass

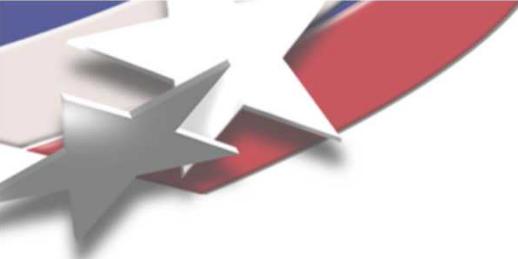




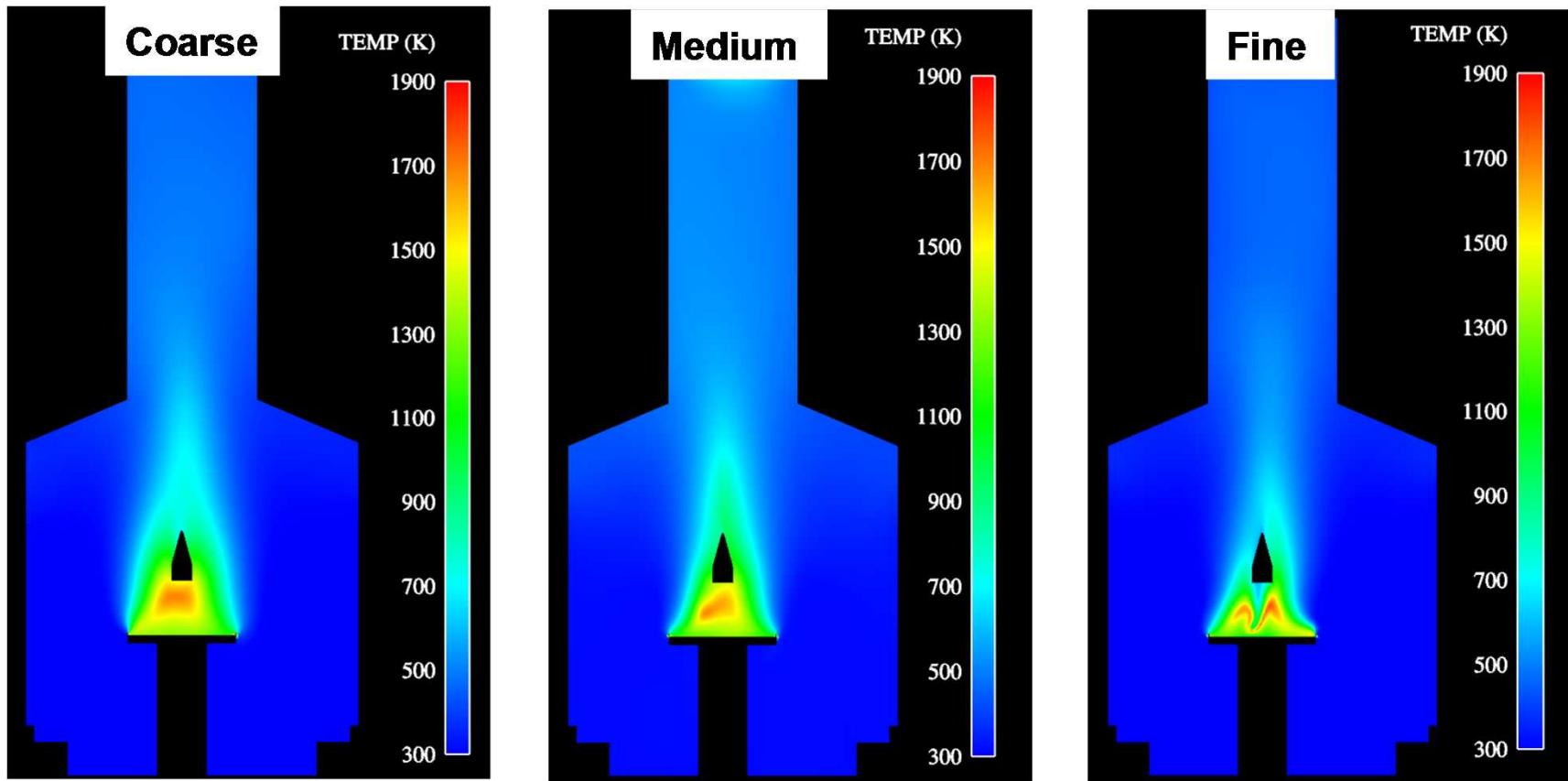
Solution Verification on High Fidelity Models is Hard

Solution Verification: Is the Discretization Adequate?



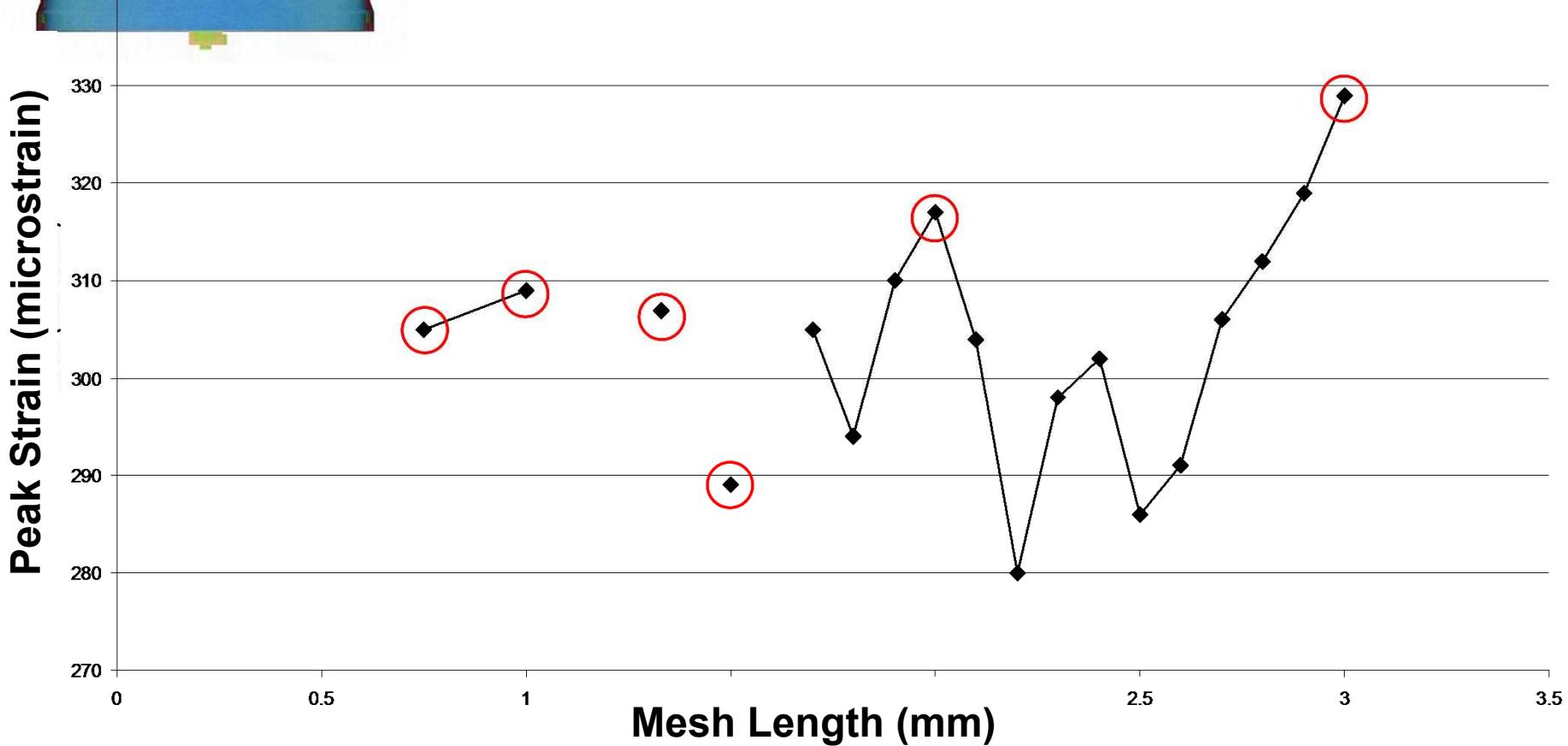


Calorimeter Fire BVG Solutions



Calculation Verification for a Threaded Assembly

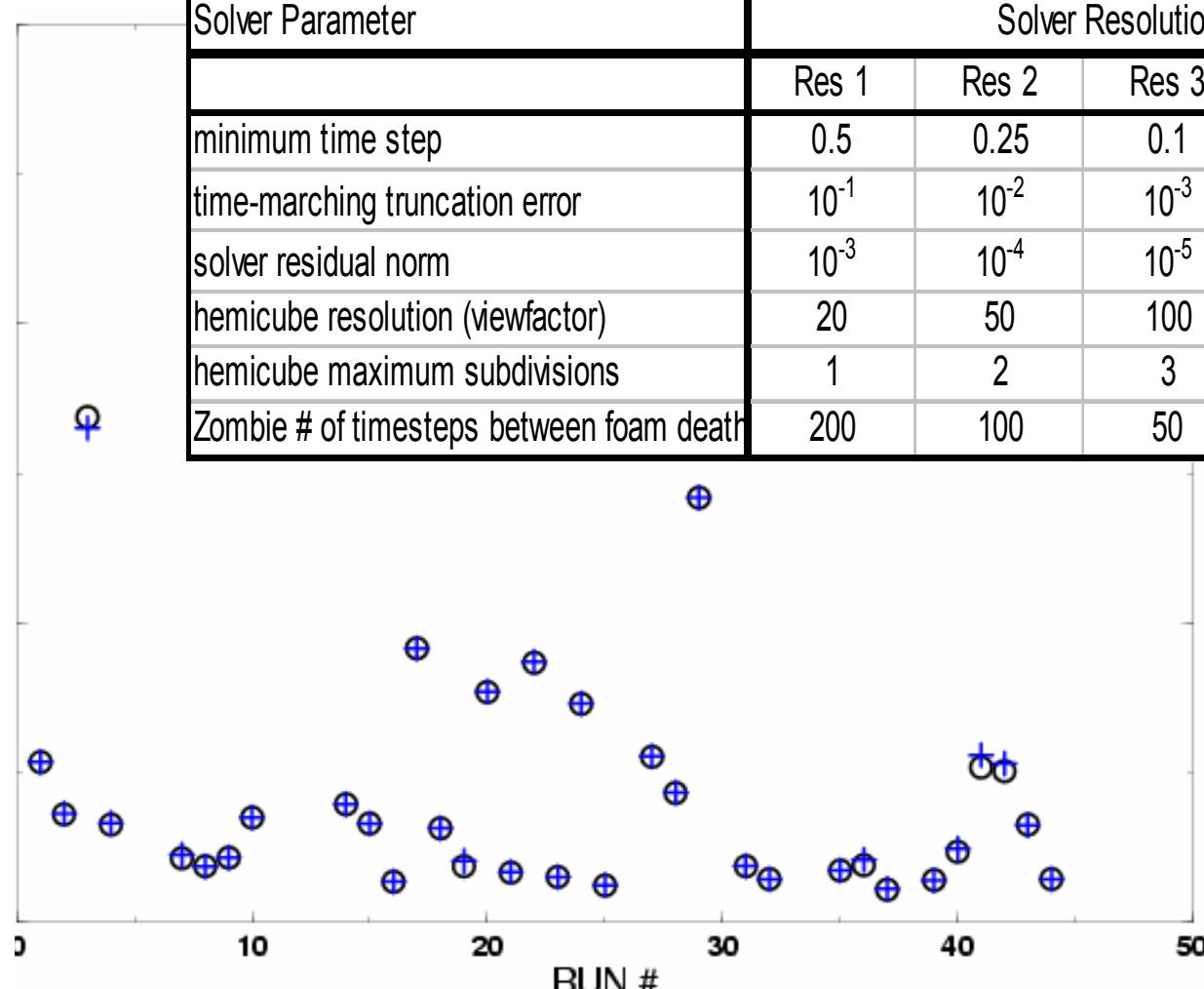
Ryan Maupin, ESA-WR, LANL: IMAC-XXIV 1/31/06



Solver Resolution Over UQ Parameter Space

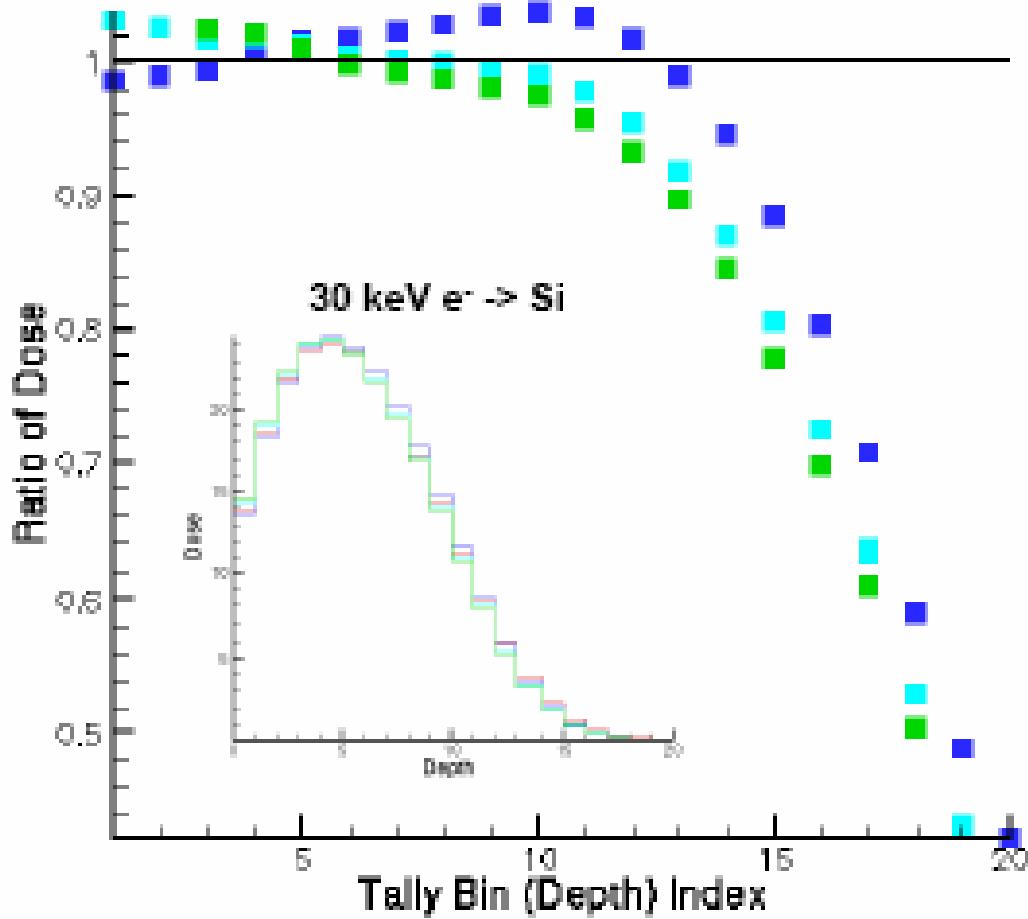
Solution Verification: Are the solver settings adequate?

System Response Quantity



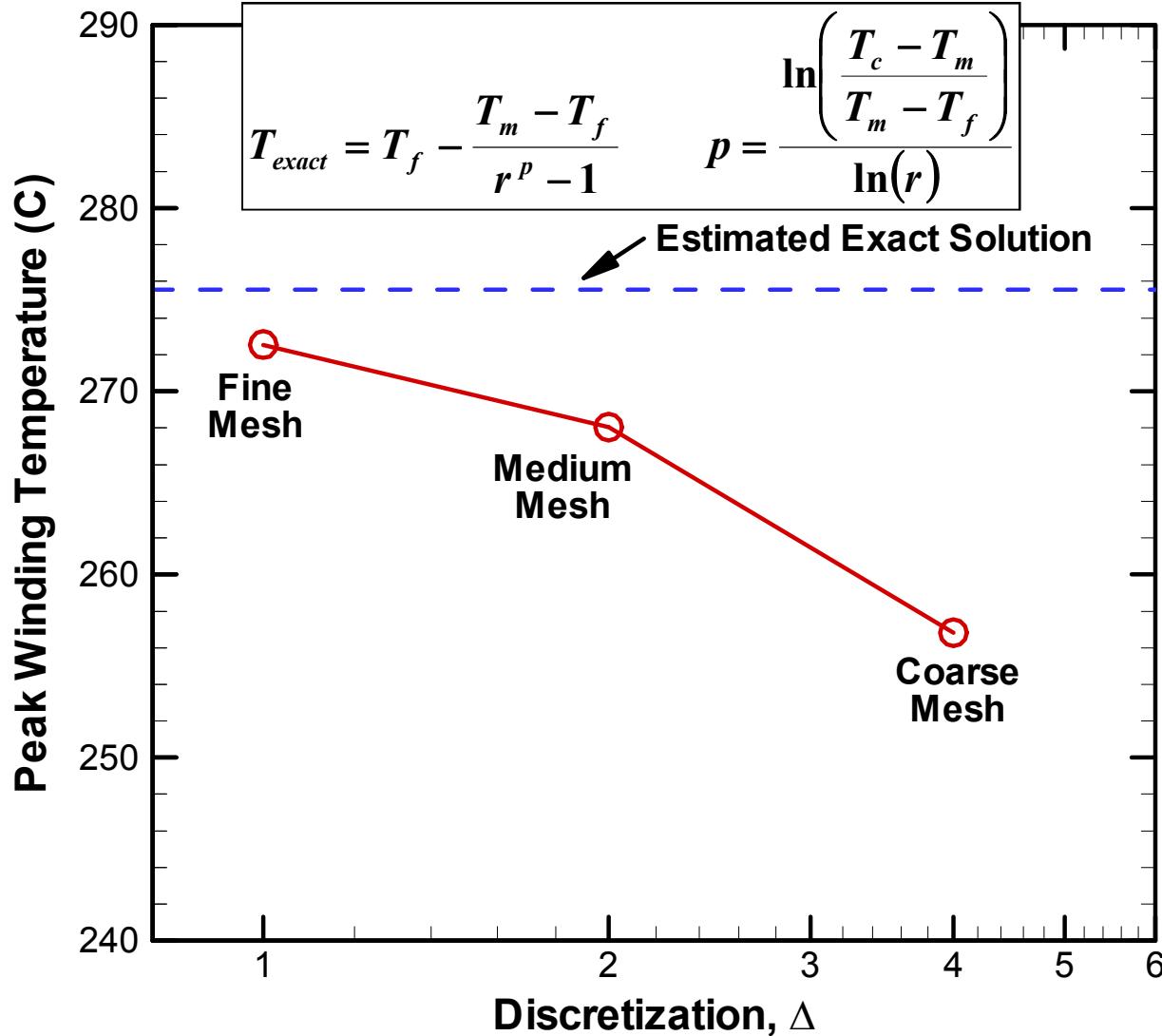
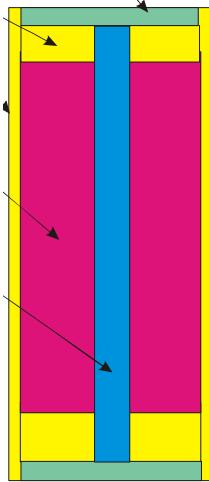
Solver Parameter	Solver Resolution Settings				
	Res 1	Res 2	Res 3	Res 4	Res 5
minimum time step	0.5	0.25	0.1	0.05	0.01
time-marching truncation error	10^{-1}	10^{-2}	10^{-3}	10^{-4}	10^{-5}
solver residual norm	10^{-3}	10^{-4}	10^{-5}	10^{-6}	10^{-7}
hemicube resolution (viewfactor)	20	50	100	200	300
hemicube maximum subdivisions	1	2	3	4	5
Zombie # of timesteps between foam death	200	100	50	20	1

Dose Sensitivity to Electron Boundary Crossing Algorithm



- Evaluation of ITS electron boundary-crossing error: (All with respect to no internal boundaries, default substep size.)
- Blue: internal boundaries, default substep size
- Cyan: Internal boundaries half-default substep size
- Green: Internal boundaries quarter-default substep size

Numerical Errors Pollute Validation Assessments



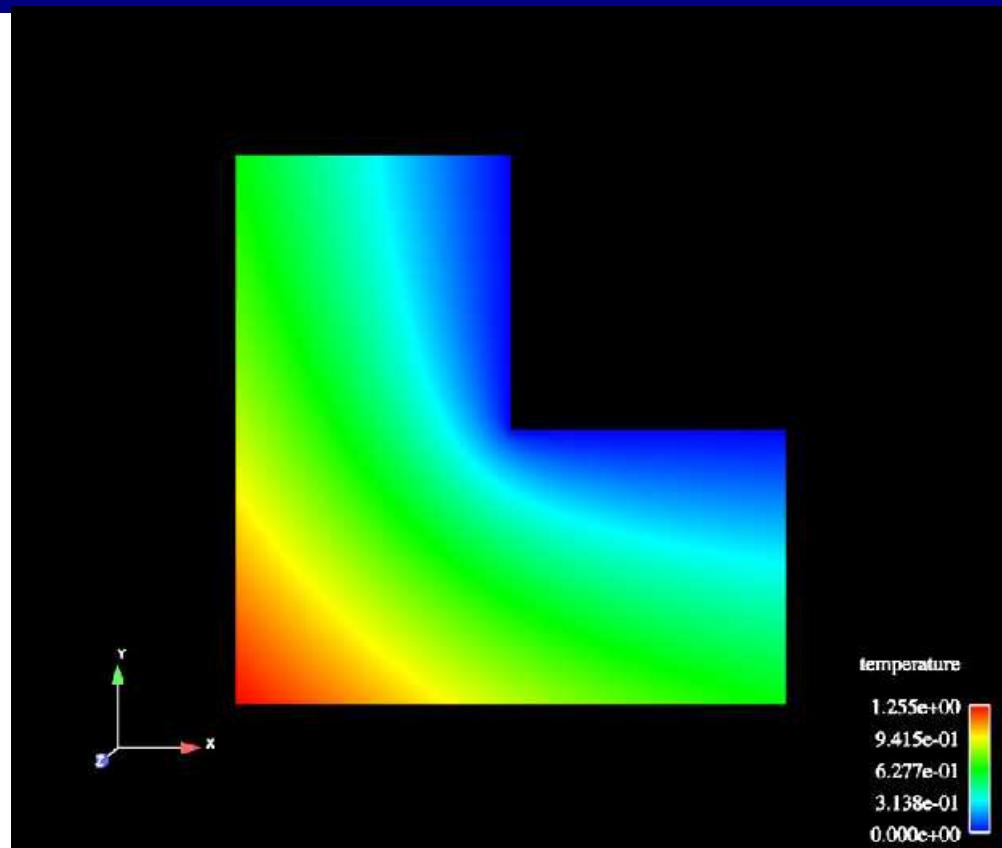
Verification of Error Estimator and Adaptive Algorithm

- 2D Exact Solution:

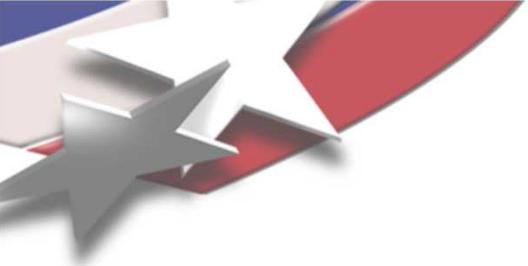
$$u = r^{2/3} \sin\left(\frac{2}{3}\theta\right)$$

- Linear elements
- ZZ error estimator

- Feedback adaptive algorithm:



if $\left(||e^*||_{H_1(\omega_j)} > 0.995 \max_{1 \leq i \leq N_\omega} ||e^*||_{H_1(\omega_i)} \right)$ then refine ω_j

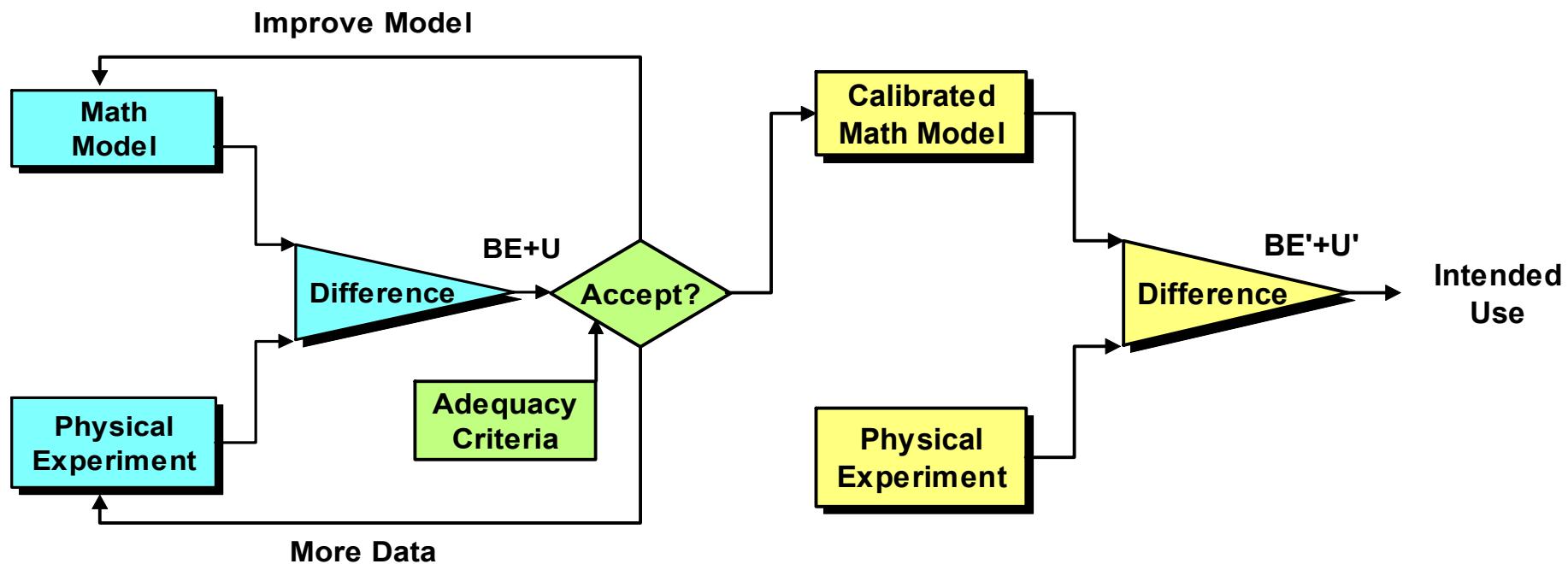


Validation

Hyperlinks

Validation is Assessment

Calibration is not Validation

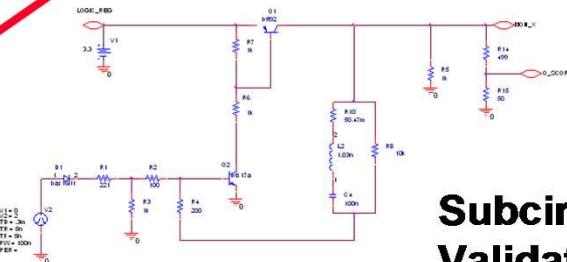


Science-Based Validation Experiments

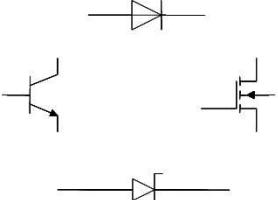
Validation: Are You Solving the Right Equations?

Hierachal Validation: Right answer for the right reason

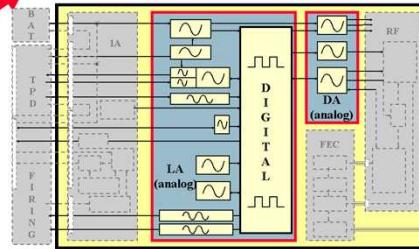
Increasing complexity,
Decreasing number of tests



Subcircuit Validation



Single Device Characterization and Validation



Single ASIC Validation

System-Level Circuit Validation

- Application relevant parameter space
- Formal DOE and replicate tests
- Attention to diagnostic bias and precision

Science-Based Validation Experiments

Validation: Are You Solving the Right Equations?

Hierachal Validation: Right answer for the right reason

Increasing complexity,
Decreasing number of tests



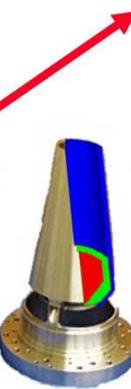
Joint parameter characterization



Single joint validation



Jointed structure validation



Full System Test

Mockup with jointed structure and foam embedded object

- Application relevant parameter space
- Formal DOE and replicate tests
- Attention to diagnostic bias and precision

Science-Based Validation Experiments

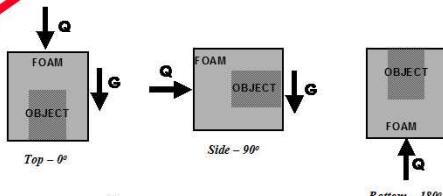
Validation: Are You Solving the Right Equations?

Hierachal Validation: Right answer for the right reason

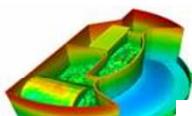
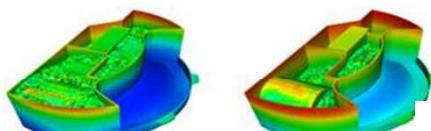


Full System Test

Increasing complexity,
Decreasing number of tests



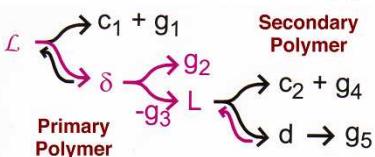
Validation with
mockups



Validation
Real Sub-systems

Foam recession

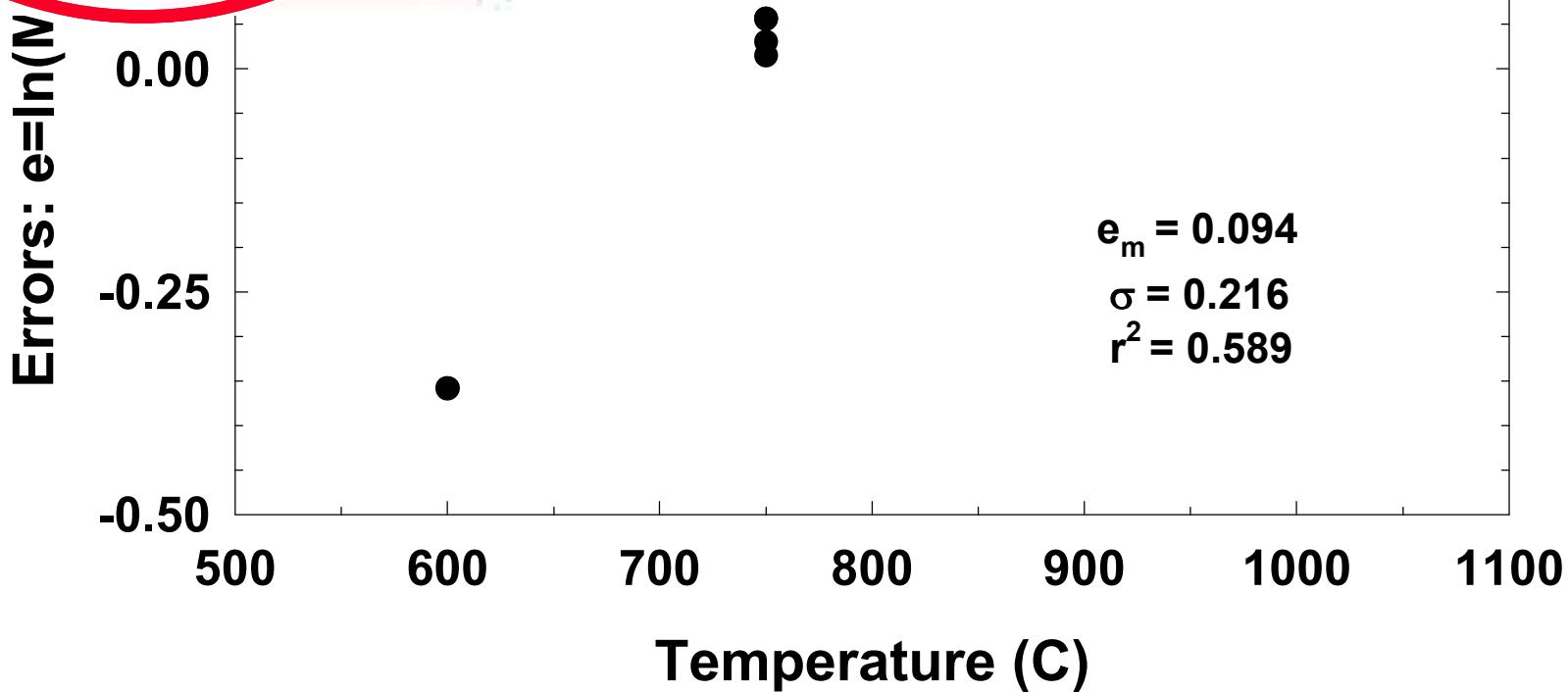
Chemistry
characterization/validation



- Application relevant parameter space
- Formal DOE and replicate tests
- Attention to diagnostic bias and precision

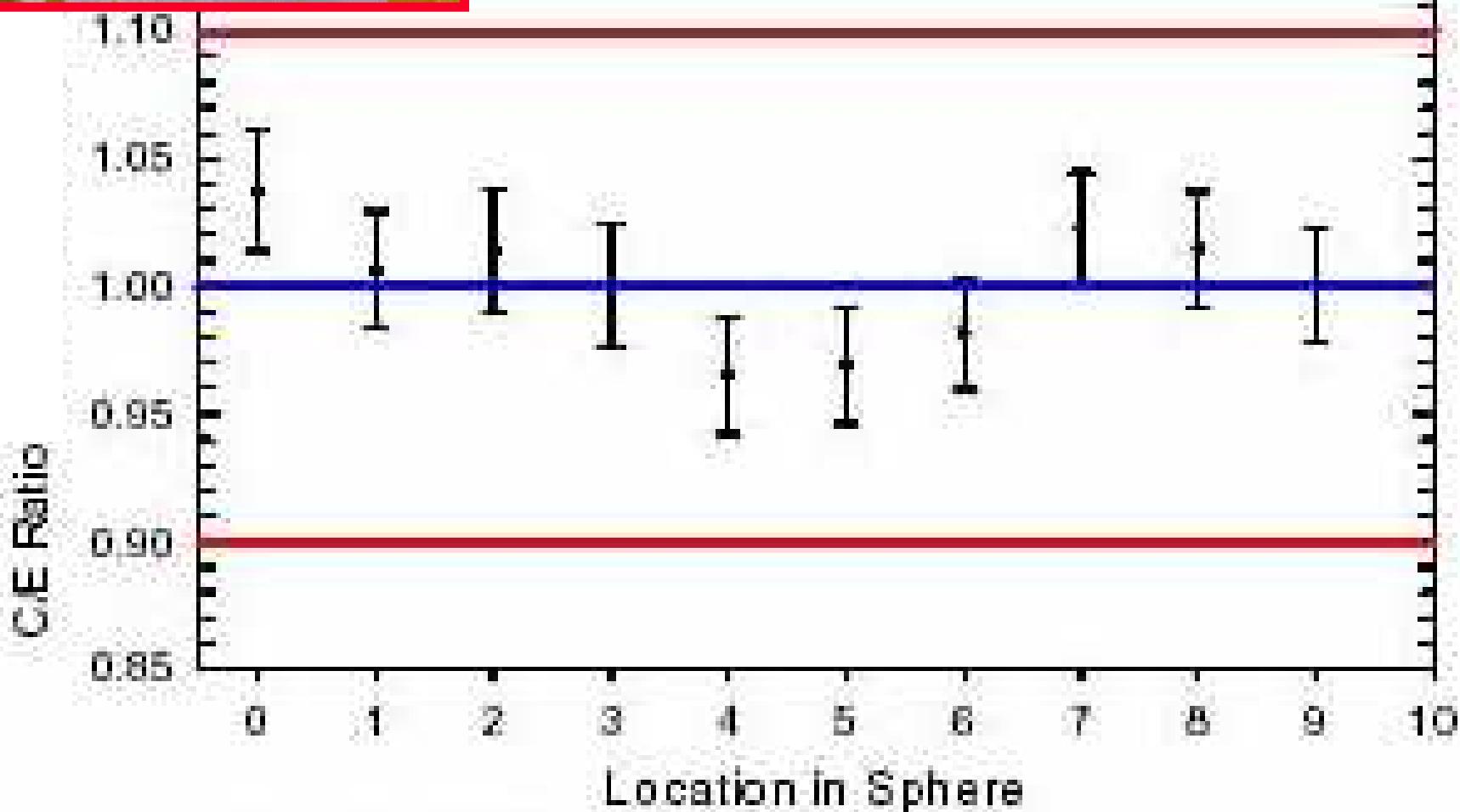
Validation is Statistical

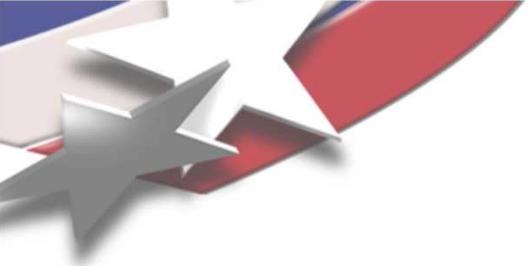
Vugraph Norms Are Not Adequate





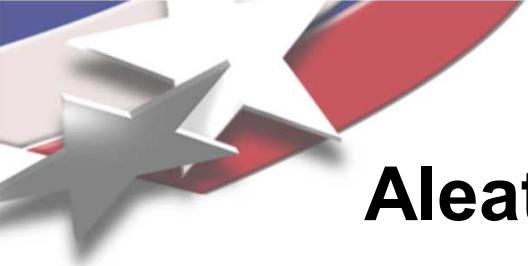
Neutron Attenuation in Test Objects





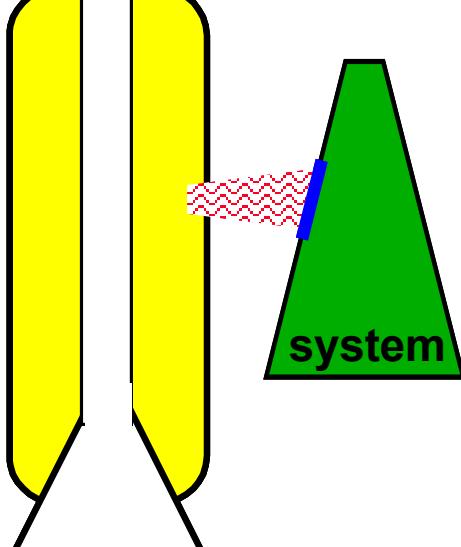
QMU and Sensitivities

Hyperlinks

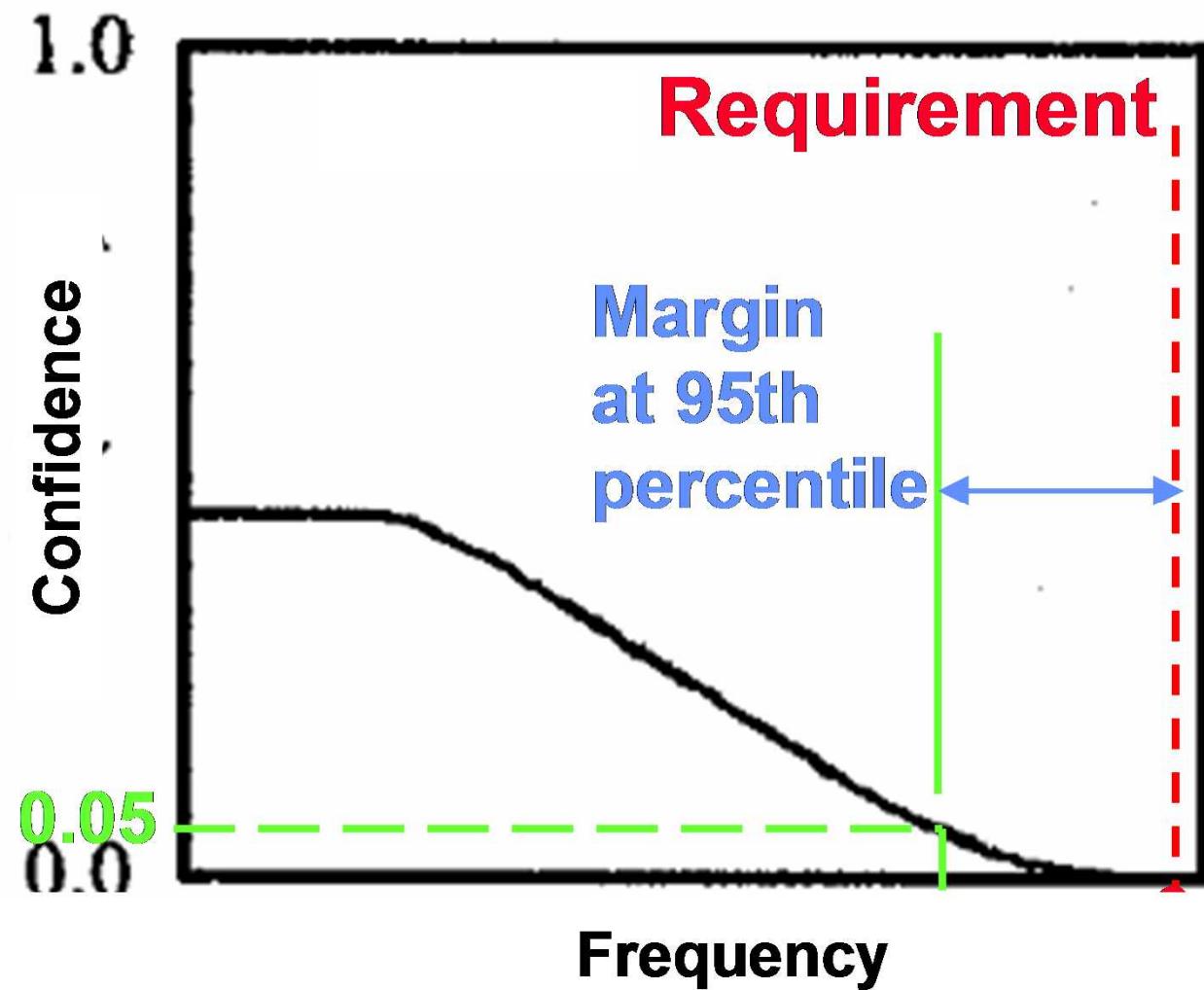


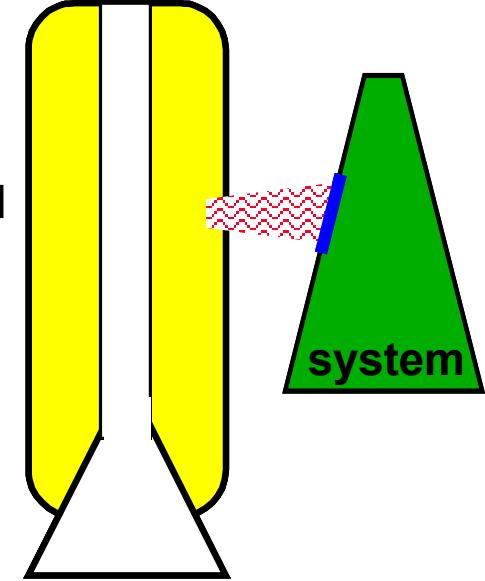
Aleatory and Epistemic Uncertainties

- **Aleatory uncertainty:** Inherent randomness in behavior of system under study (**frequency interpretation**)
 - Alternatives: Variability, stochastic uncertainty, irreducible uncertainty, type A uncertainty
 - Examples: component failures or material properties derived from statistically significant testing under conditions relevant to intended application
- **Epistemic uncertainty:** Lack of knowledge about appropriate value to use for a quantity that is assumed to have a fixed value in the context of a specific analysis (**confidence or belief interpretation**)
 - Alternatives: state of knowledge uncertainty, subjective uncertainty, reducible uncertainty, type B uncertainty
 - Examples: representative scenarios, unknown parameters in frequency distributions, parameters or models with defensible bounds but no sense of frequency



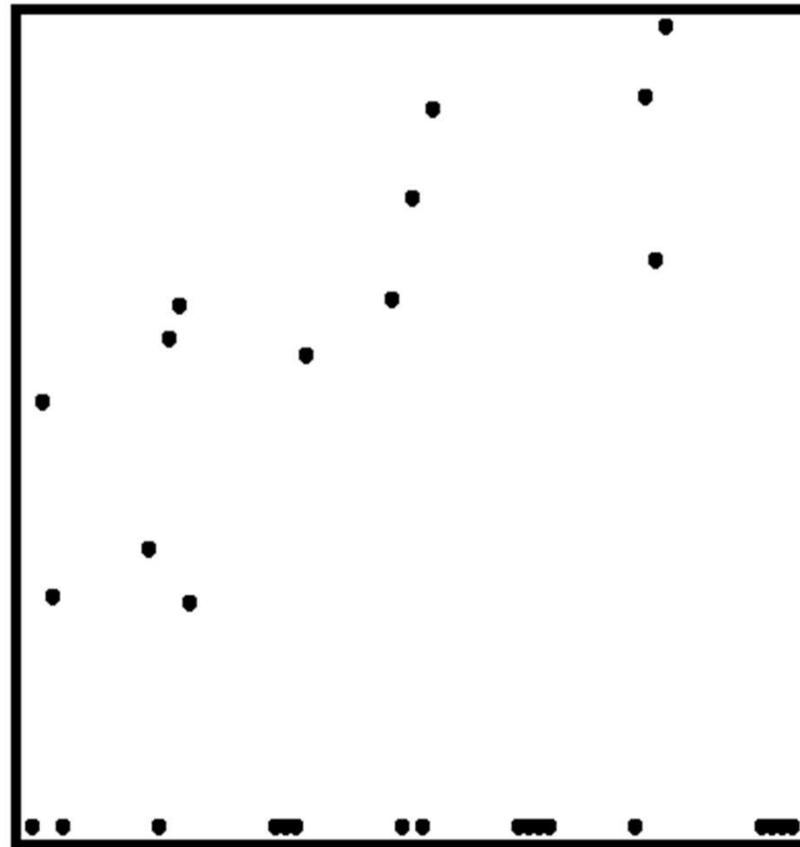
Quantified Margins and Uncertainties

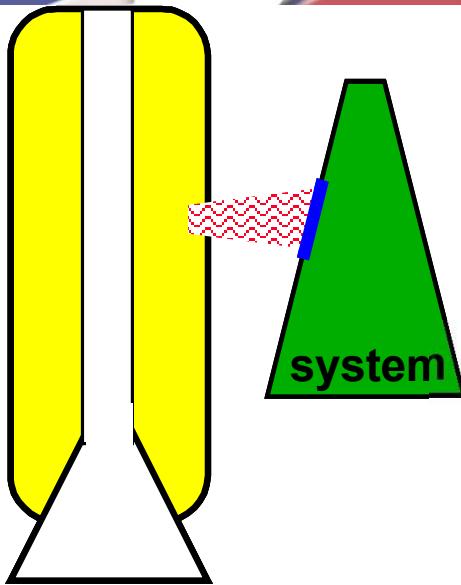




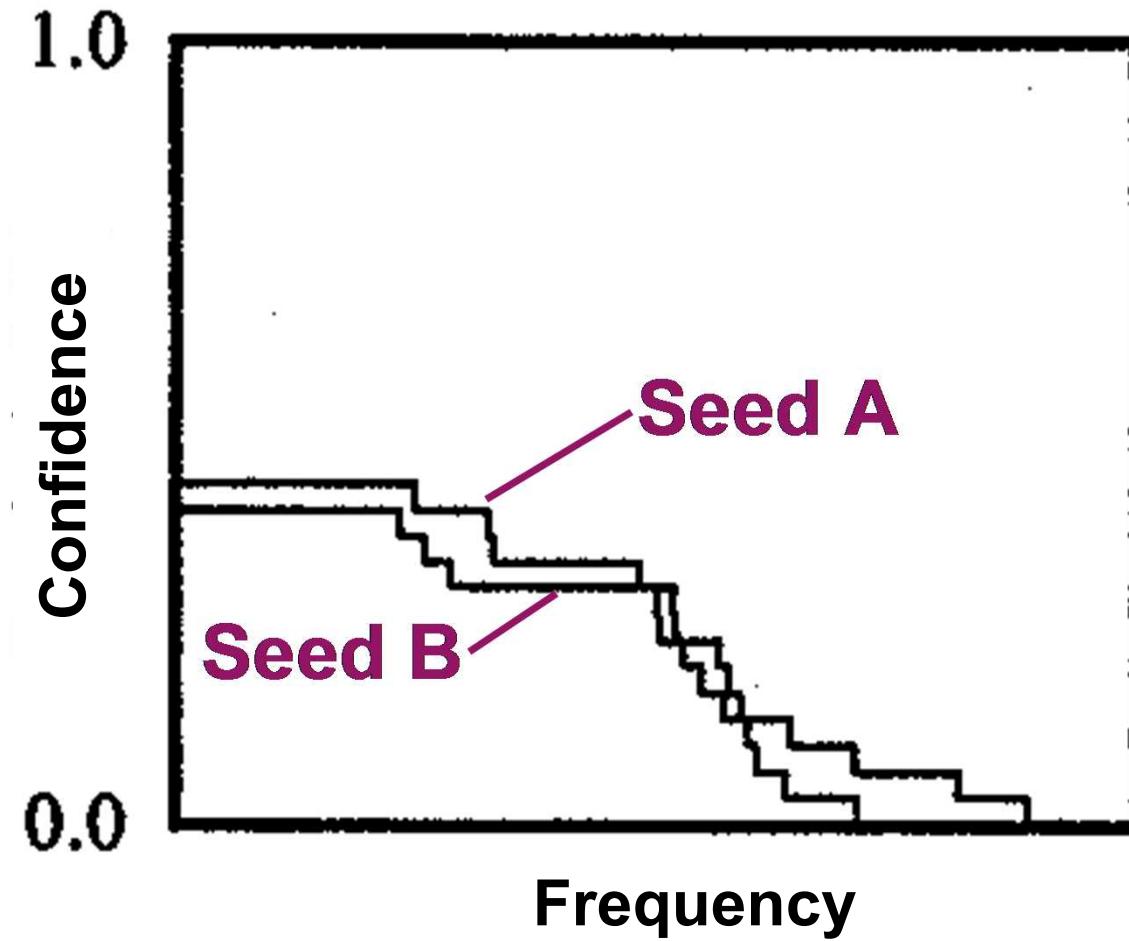
Sensitivity Analysis

SCorr = 0.809





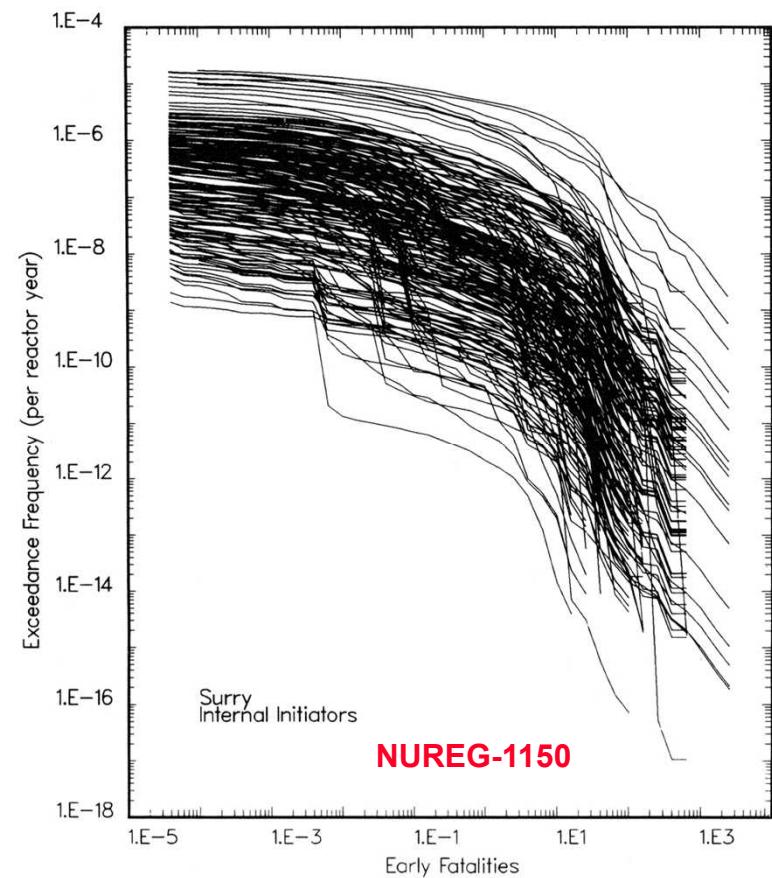
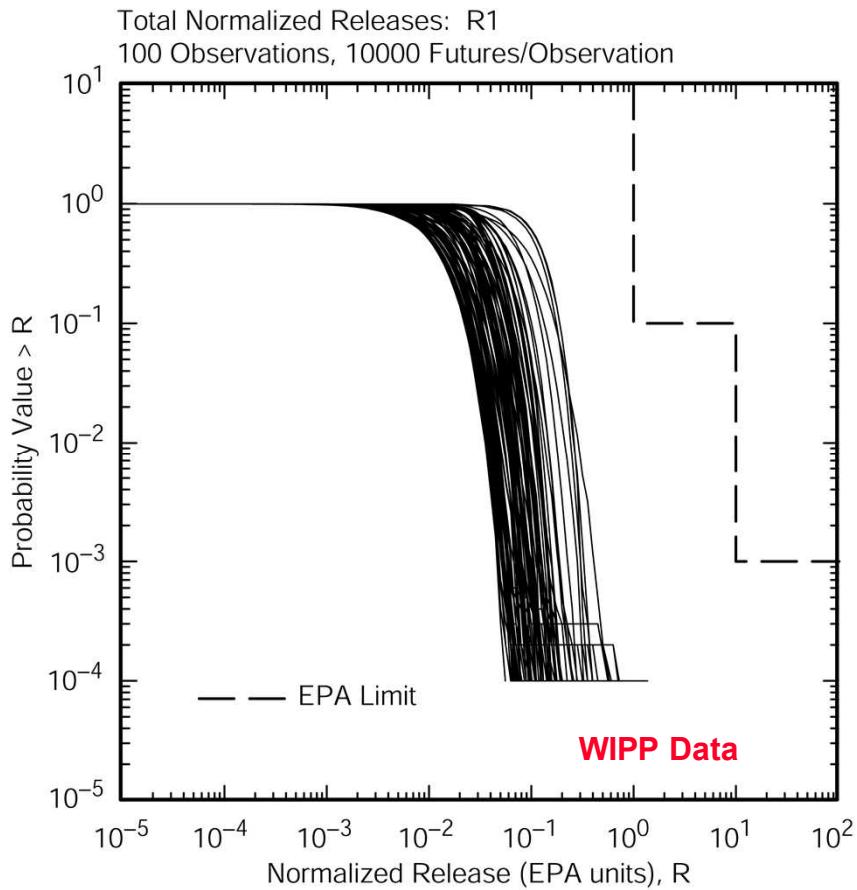
UQ Solution Verification



Seed Effects from limited sampling

WIPP and NUREG-1150 Precedents

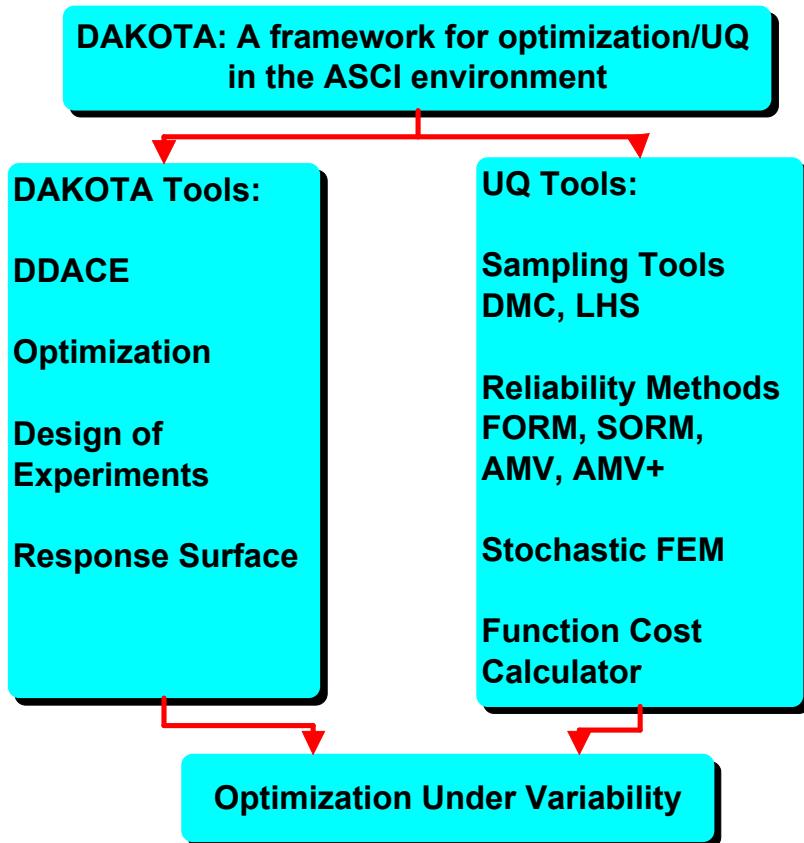
High Consequence Regulatory Issues in the National Interest
Addressed Primary Through Modeling and Simulation



Lessons Learned: (1) Seek BE + Uncertainty

(2) It takes more than one shot to get it right

Infrastructure for ASC-Scale UQ Analyses



1. **Algorithmic coarse-grained parallelism:** independent concurrent fn. evaluations
2. **Algorithmic fine-grained parallelism:** parallel computation of internal linear algebra
3. **Function evaluation coarse-grained parallelism:** concurrent execution of separable simulations within a fn. eval. (e.g., multiple loading cases)
4. **Function evaluation fine-grained parallelism:** parallelization of the solution steps within a single analysis code (e.g., SALINAS, MPSalsa)

