

# **Verification & Validation:**

## **Measured Credibility, on Demand, for Stockpile Applications**

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**Albuquerque, New Mexico**  
**February 6, 2007**



# **We Need V&V Because We Care!**

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- **Stockpile Applications**

- There *is* a decision context: High consequence design and decision making associated with nuclear weapons

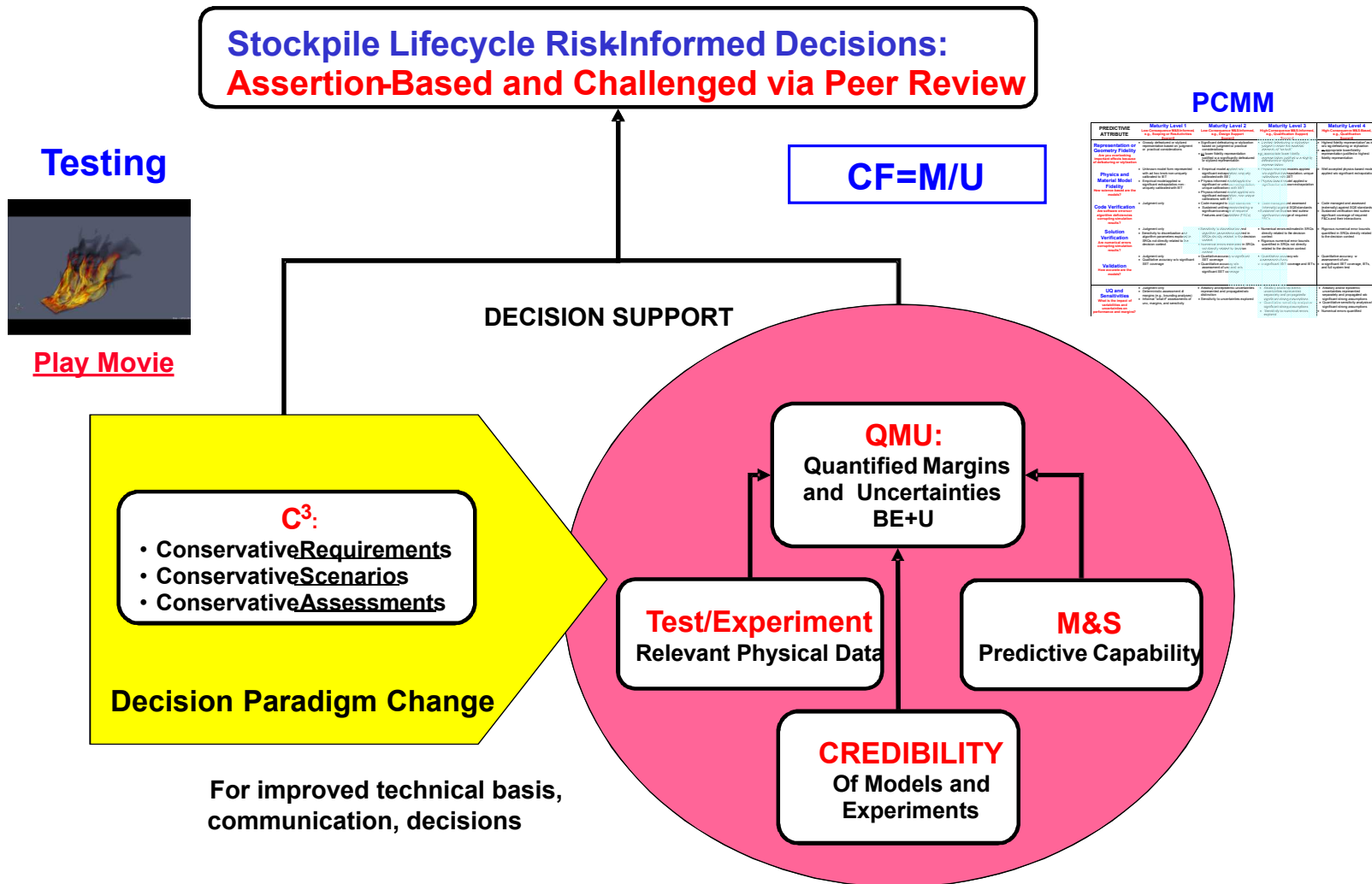
- **On Demand**

- Agility and responsiveness are critical to the nuclear weapons complex of the future

- **Measured Credibility**

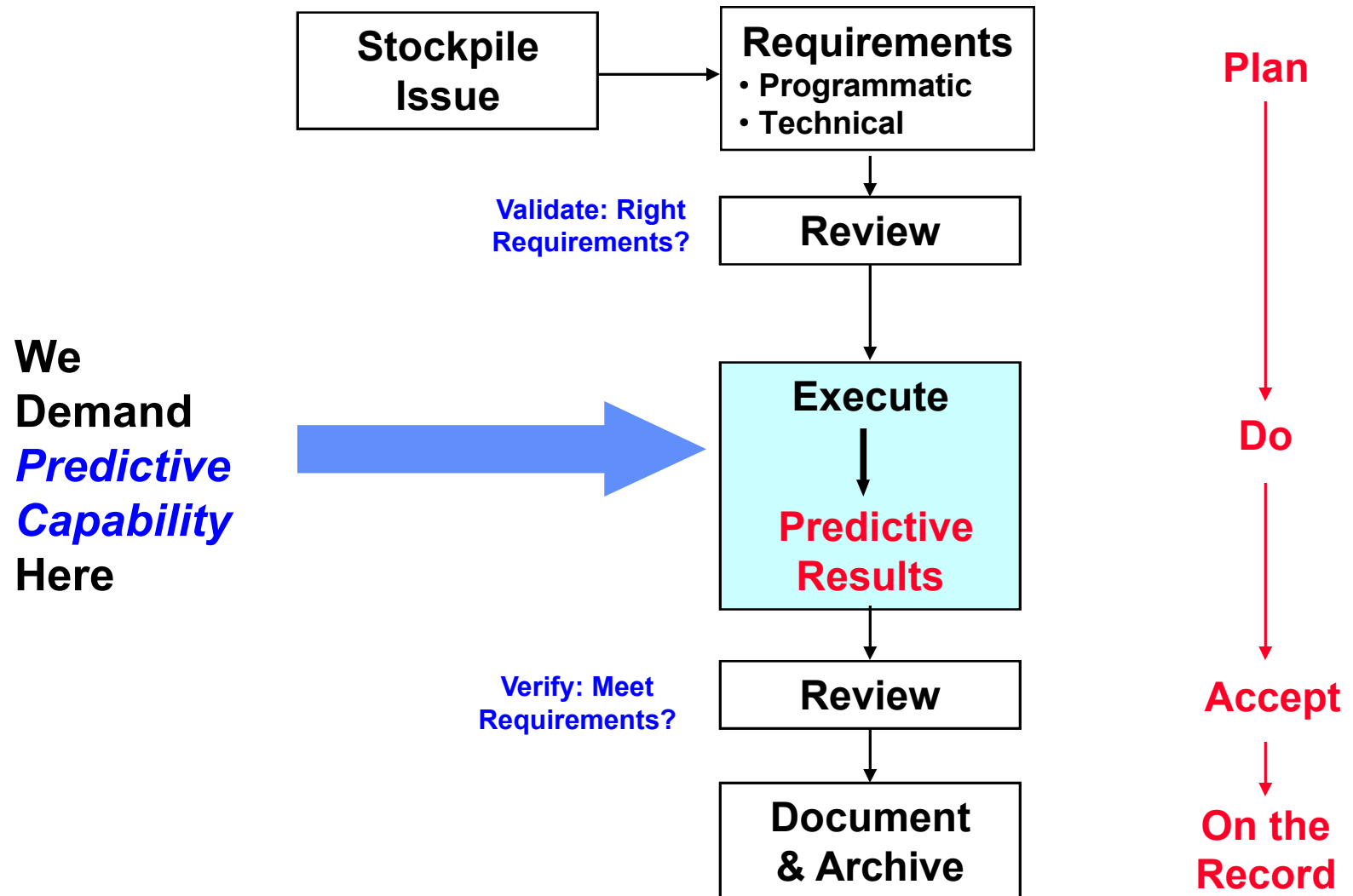
- What's the “certificate of credibility” that accompanies M&S results

# M&S Increasingly Contributes to *Risk-Informed Decisions* at Sandia



# High Consequence Issues Demand Predictive Capability

Concepts of Stockpile Computing: SAND2004-2479



# What Does it Mean “to Predict”?

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## American Heritage Dictionary:

- **Predict**: To state, tell about, or make known in advance, especially on the basis of *special knowledge*\*

**What *special knowledge* do we demand of M&S to assert a predictive capability and how do we communicate it?**



# **You Can't Measure and Communicate “it” Unless You Know What “it” Is**

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- **Some Attributes of Predictive Capability**
  - Representation or geometric fidelity
  - Physics and material model fidelity (predictive science)
  - Code verification
  - Solution verification
  - Validated models
  - Uncertainty quantification with sensitivity analysis



# How Much is Enough?

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- Sufficiency can only be discussed in an application context
- Graded approach
  - Maturity Level 1:
    - Low-consequence, M&S-informed (e.g., scoping studies)
  - Maturity Level 2:
    - Low-consequence, M&S-informed (e.g., design support)
  - Maturity Level 3:
    - High-consequence, M&S-informed (e.g., qual support)
  - Maturity Level 4:
    - High-consequence, M&S-based (e.g., qualification)
- Negotiate expectations for future work or communicate maturity for work already done

Increasing Rigor  
Expected



# This is Where We Are Going

## Predictive Capability Maturity Model (PCMM)

| PREDICTIVE ATTRIBUTE  | <b>Maturity Level 1</b><br>Low-Consequence M&S-Informed,<br>e.g., Scoping or Res Activities<br>Score=0  | <b>Maturity Level 2</b><br>Low-Consequence M&S-Informed,<br>e.g., Design Support<br>Score=2  | <b>Maturity Level 3</b><br>High-Consequence M&S-Informed,<br>e.g., Qualification Support,<br>Score=4   | <b>Maturity Level 4</b><br>High-Consequence M&S-Based,<br>e.g., Qualification<br>Score=6  |
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# Why PCMM?

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- Educate the decision maker about what should be expected from M&S
- Measure/communicate process maturity (not adequacy of results) associated with M&S in a decision context
- Provide program vision so that technical and infrastructure needs can be leveraged across multiple funding lines to enhance the credibility of M&S results
- Speak to the *whats*, not dictate the *hows*

**Setting the National Agenda in V&V**

# Representation or Geometric Fidelity

## Are you overlooking important effects because of judgment-based Defeaturing or Stylization?

Grossly defeatured or stylized

Significant D&S based on judgment

Limited D&S judged to retain the essential elements of “as built”

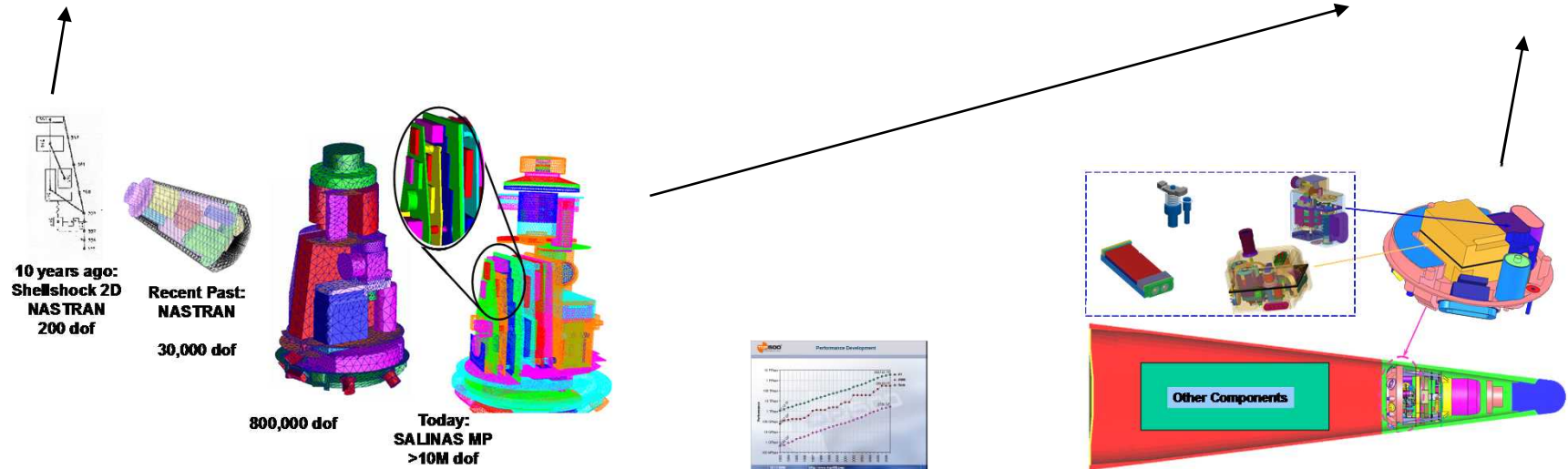
Highest fidelity representation “as built” w/o significant D&S

H Risk Tolerant

Risk Tolerant

Risk Adverse

H Risk Adverse



# Physics and Material Model Fidelity

## Are the models science-based?

Unknown model form or empirical model form applied w sig extrap

Empirical model form applied w/o sig extrap or physics informed model applied w sig/unk extrap

Physics-informed model applied w/o sig extrap or physics based model applied w sig/unk extrap

Physics-based model applied w/o sig extrap

H Risk Tolerant

Risk Tolerant

Risk Adverse

H Risk Adverse

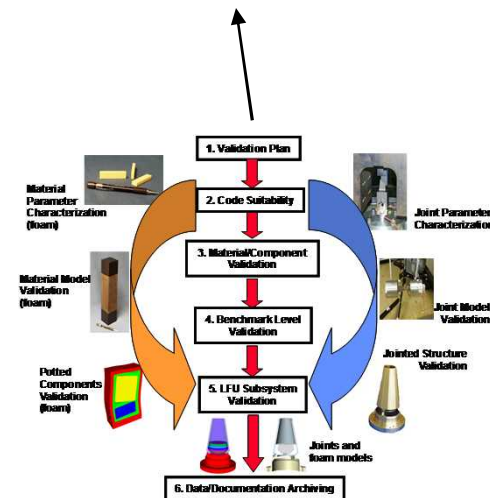


10 years ago:  
Shellshock 2D  
NASTRAN  
200 dof

Recent Past:  
NASTRAN  
30,000 dof

800,000 dof

Today:  
SALINAS MP  
>10M dof



# Code Verification

Are software errors or algorithm deficiencies corrupting simulation results?

Code managed to SQE standards

Sustained unit/regression tests w sig coverage of F&C

SQE +assessment + sustained VERTS w sig coverage of F&C

SQE(A) + VERTS w sig coverage of F&C interactions

Judgment only

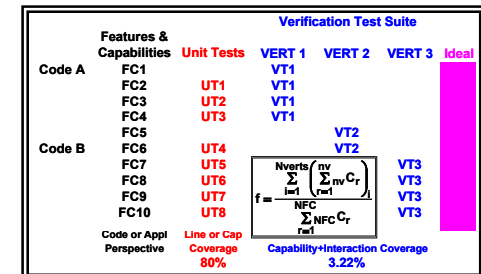
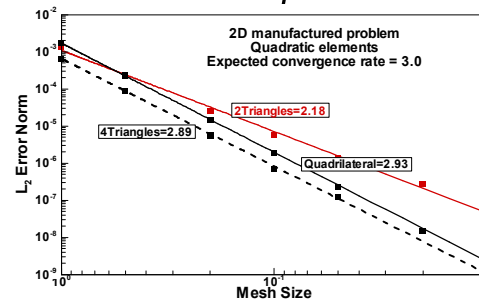
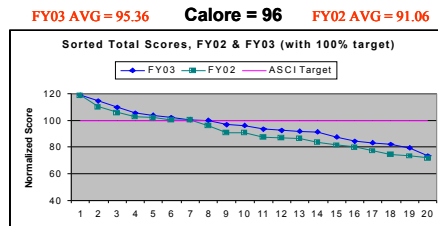
H Risk Tolerant

Risk Tolerant

Risk Adverse

H Risk Adverse

Code/Code Comparisons





# Solution Verification

## Are numerical errors corrupting simulation results?

Judgment  
only

Explore  
sensitivity to  
discretization and  
algorithm  
parameters

Estimate  
numerical  
errors

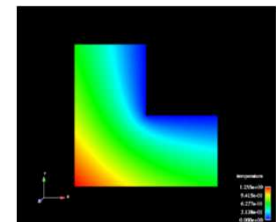
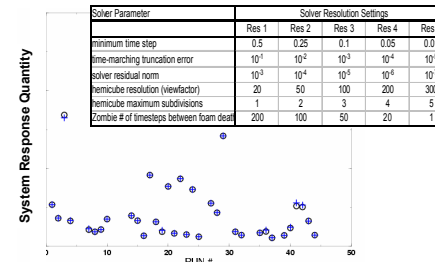
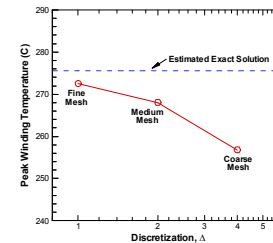
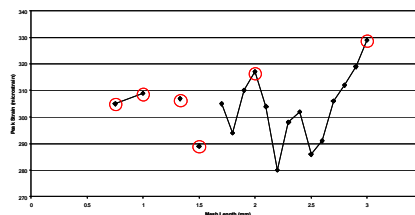
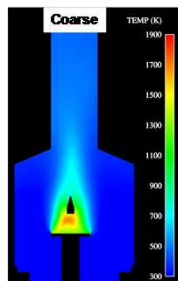
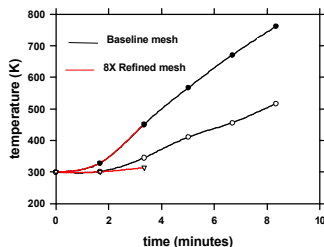
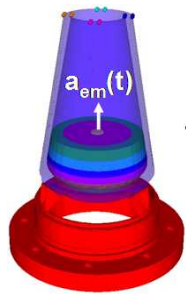
Quantify  
rigorous  
numerical  
error bounds

**H Risk  
Tolerant**

**Risk  
Tolerant**

**Risk  
Adverse**

**H Risk  
Adverse**



# Validation

## How accurate are the models?

Judgment  
only

Qual accuracy w  
SET coverage

Quantitative accuracy  
w/o assessment of unc  
*and* w SET coverage  
and IETs

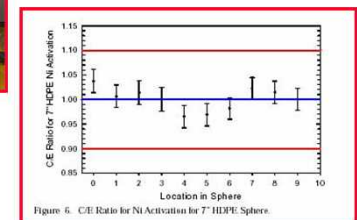
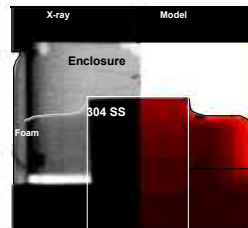
Quantitative  
accuracy w  
assessment of unc  
*and* SET coverage  
and IETs and full  
system

H Risk  
Tolerant

Risk  
Tolerant

Risk  
Adverse

H Risk  
Adverse



# Uncertainty Quantification and Sensitivities

## What is the impact of variabilities and uncertainties on performance and margins?

Judgment only  
Deterministic  
assessment of  
margins or informal  
“what if” studies

Aleatory and epistemic  
unc represented w/o  
distinction  
  
Sensitivities explored

Aleatory/epistemic unc  
interpreted separately  
w strong assumptions  
  
Sensitivities w strong  
assumptions  
  
Sensitivity to  
numerical errors exp

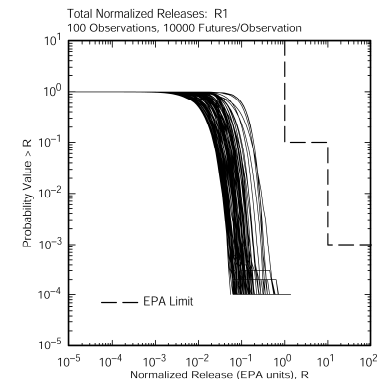
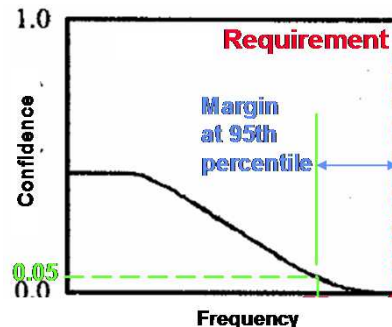
Aleatory/epistemic  
unc interpreted  
separately w strong  
assumptions  
Sensitivities w  
strong assumptions  
Numerical errors  
quantified

**H Risk  
Tolerant**

**Risk  
Tolerant**

**Risk  
Adverse**

**H Risk  
Adverse**





# ASC Projects Should Map to Capability/Agility Needs

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**DART**

**Wisdom**

**PEM**

**SQE**

**V&V Methods**

**Adaptivity**

**Codes and Platforms**



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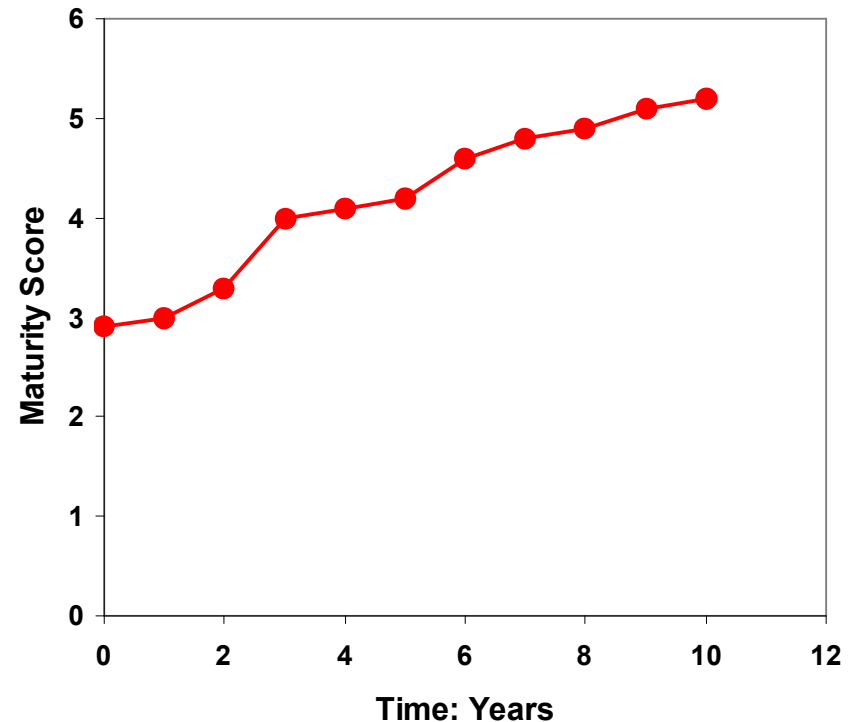
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| <b>Solution Verification</b><br>Are numerical errors corrupting simulation results?                                     | <ul style="list-style-type: none"> <li>Judgment only</li> <li>Sensitivity to discretization and algorithm parameters explored in SRQs not directly related to the decision context</li> </ul>                                   | <ul style="list-style-type: none"> <li>Sensitivity to discretization and algorithm parameters explored in SRQs directly related to the decision context</li> <li>Numerical errors estimated in SRQs not directly related to decision context</li> </ul>  | <ul style="list-style-type: none"> <li>Numerical errors estimated in SRQs directly related to the decision context</li> <li>Rigorous numerical error bounds quantified in SRQs not directly related to the decision context</li> </ul>   | <ul style="list-style-type: none"> <li>Rigorous numerical error bounds quantified in SRQs directly related to the decision context</li> </ul>   |
| <b>Validation</b><br>How accurate are the models?   | <ul style="list-style-type: none"> <li>Judgment only</li> <li>Qualitative accuracy w/o significant SET coverage</li> </ul>  | <ul style="list-style-type: none"> <li>Qualitative accuracy w significant SET coverage</li> <li>Quantitative accuracy w/o assessment of unc and w/o significant SET coverage</li> </ul>  | <ul style="list-style-type: none"> <li>Quantitative accuracy w/o assessment of unc</li> <li>w significant SET coverage and IETs</li> </ul>   | <ul style="list-style-type: none"> <li>Quantitative accuracy w assessment of unc</li> <li>w significant SET coverage, IETs, and full system test</li> </ul>   |
| <b>UQ and Sensitivities</b><br>What is the impact of variabilities and uncertainties on performance and margins?        | <ul style="list-style-type: none"> <li>Judgment only</li> <li>Deterministic assessment of margins (e.g., bounding analyses)</li> <li>Informal "what if" assessments of unc, margins, and sensitivity</li> </ul>                 | <ul style="list-style-type: none"> <li>Aleatory and epistemic uncertainties represented and propagated w/o distinction</li> <li>Sensitivity to uncertainties explored</li> </ul>   | <ul style="list-style-type: none"> <li>Aleatory and/or epistemic uncertainties represented separately and propagated w significant strong assumptions</li> <li>Quantitative sensitivity analysis w significant strong assumptions</li> <li>Sensitivity to numerical errors explored</li> </ul> | <ul style="list-style-type: none"> <li>Aleatory and/or epistemic uncertainties represented separately and propagated w/o significant strong assumptions</li> <li>Quantitative sensitivity analysis w/o significant strong assumptions</li> <li>Numerical errors quantified</li> </ul> |

# Measure Progress Over Time

## Application: Legacy Weapon in Fuel Fire

|                                      | Avg/Avg<br>Score | Avg/Min<br>Score |
|--------------------------------------|------------------|------------------|
| <b>Rollup Scores</b>                 | <b>2.9</b>       | <b>2.0</b>       |
| Representation or Geometric Fidelity | 4.5              | 4.0              |
| Fire Environment                     | 4.0              |                  |
| Weapon                               | 5.0              |                  |
| Physics and Material Model Fidelity  | 3.2              | 1.0              |
| Fire Environment                     | 3.0              | 2.0              |
| Fuel vaporization from spill         | 2.0              |                  |
| Fluid mechanics                      | 4.0              |                  |
| Turbulent mixing                     | 3.0              |                  |
| Combustion                           | 4.0              |                  |
| Emission                             | 2.0              |                  |
| Radiative transport to weapon        | 4.0              |                  |
| Convective transport to weapon       | 2.0              |                  |
| Weapon Thermal Response              | 3.3              | 0.0              |
| Code Verification                    | 2.0              | 2.0              |
| Fire Environment                     | 2.0              |                  |
| Weapon Thermal Response              | 2.0              |                  |
| Solution Verification                | 1.5              | 1.0              |
| Fire environment                     | 1.0              |                  |
| Weapon thermal response              | 2.0              |                  |
| Validation                           | 2.1              | 0.0              |
| Fire Environment                     | 1.6              | 0.0              |
| Weapon Thermal Response              | 2.3              | 0.0              |
| UQ/SA                                | 4.0              | 4.0              |



**Note: all scores are notional**



## ***Measured Credibility*, on Demand, for Stockpile Applications**

---

- **Decision makers need to understand predictive capability in order to make informed decisions and to efficiently leverage and make use of research dollars**
- **Progress in predictive capability needs to be measured in each individual decision context**
  - **Predictive capability is more than geometric fidelity or even physics fidelity**
  - **There is a need to define sufficiency (or adequacy) in each attribute of predicative capability**
- **The *Predictive Capability Maturity Model* provides a graded approach to assessing and measuring predictive capability for specific applications**

# The Credibility of M&S is Critical

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**“Due diligence means asking *all* the questions, even if you don’t think you’ll like the answers.”**



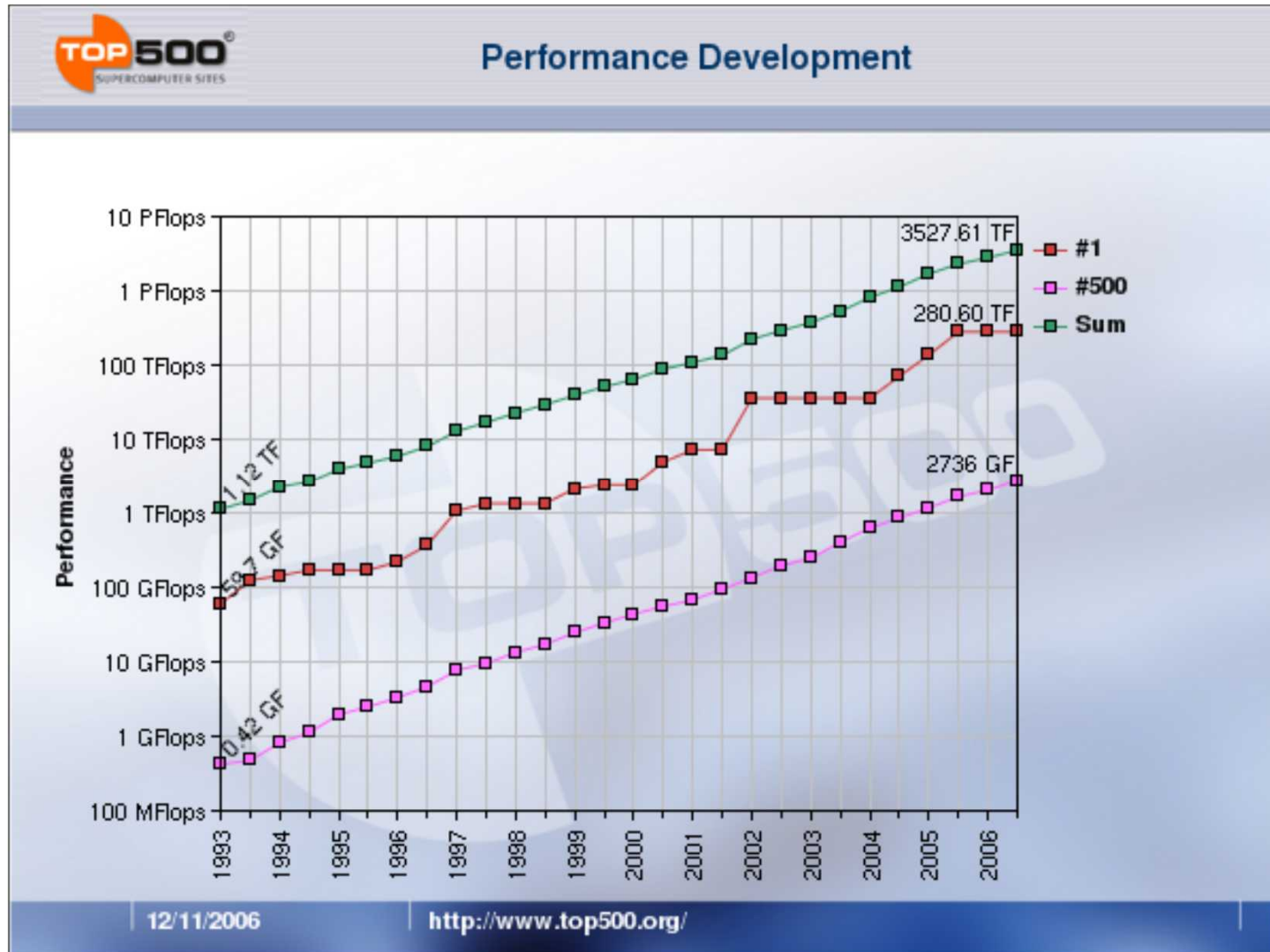
# Representational (Geometric) Fidelity

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**Hyperlinks**

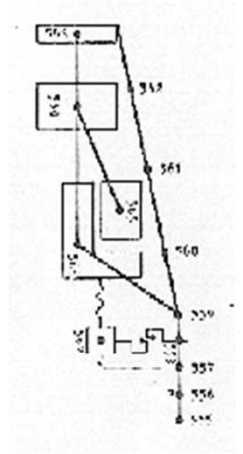
# Imagine the Future!

## Computing Speed - Dec. 2006

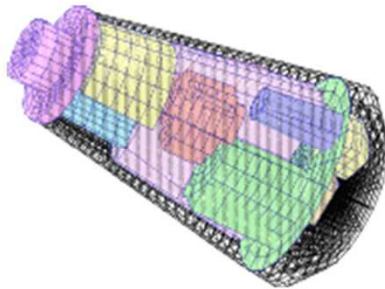




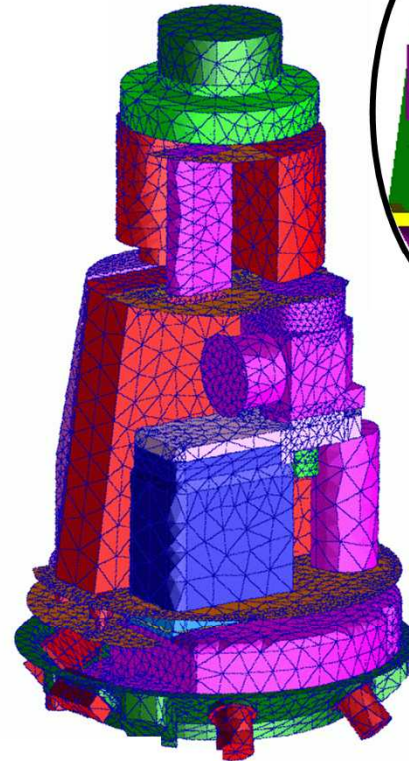
# Progress in Representational Fidelity in Structural Dynamics



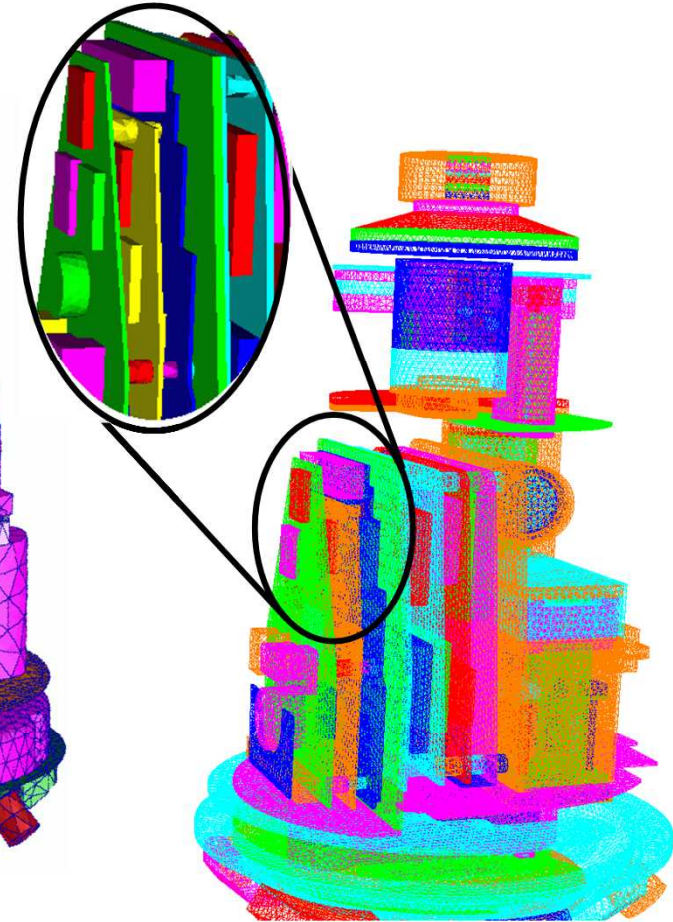
**10 years ago:**  
**Shellshock 2D**  
**NASTRAN**  
**200 dof**



**Recent Past:**  
**NASTRAN**  
**30,000 dof**

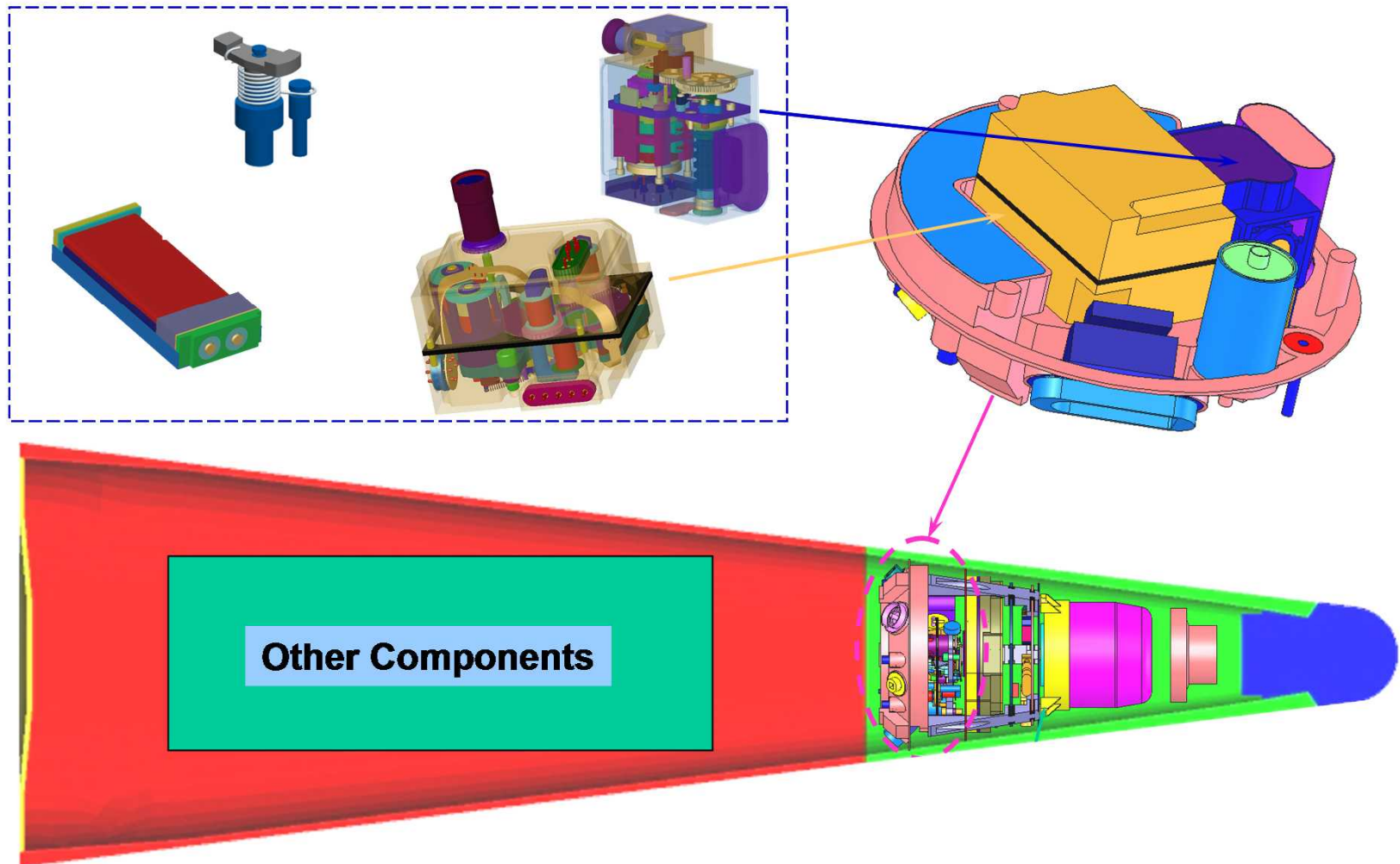


**800,000 dof**



**Today:**  
**SALINAS MP**  
**>10M dof**

# Progress in Representational Fidelity Thermal Modeling







# Physics Fidelity

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**Hyperlinks**

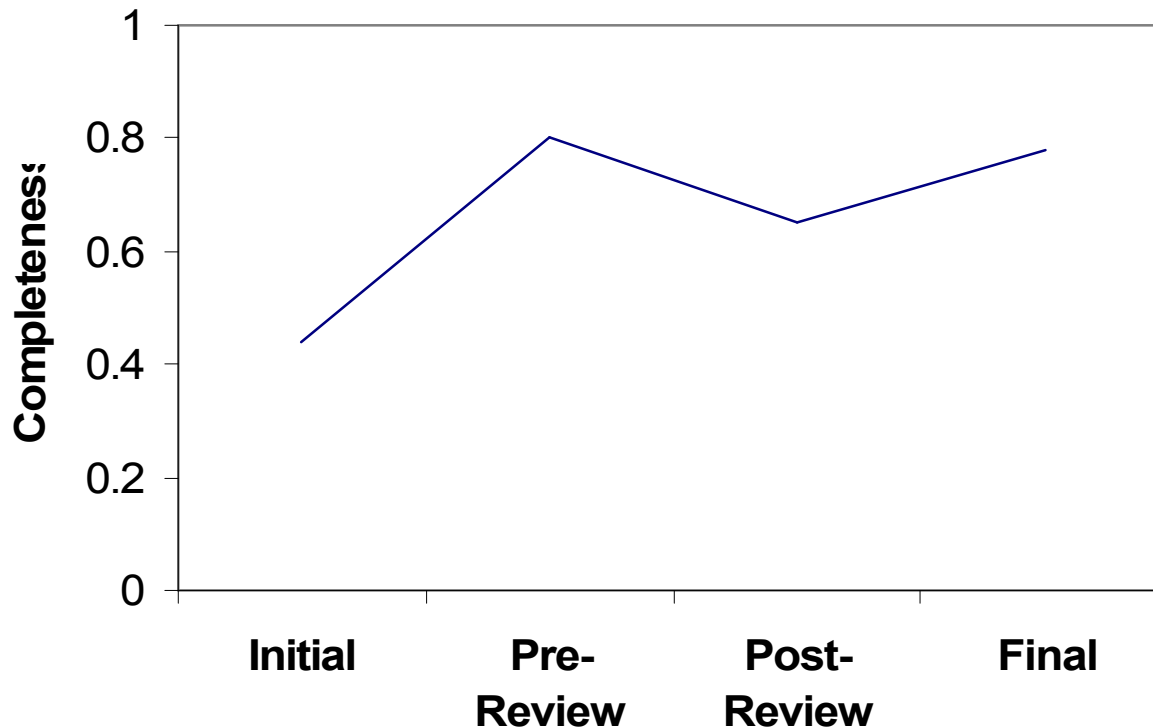
# Phenomena Identification and Ranking Tables (PIRT)

Establish efficiency and sufficiency of activities

| Phenomena | Importance | Model | Adequacy |            |
|-----------|------------|-------|----------|------------|
|           |            |       | Code     | Validation |
| P1        | H          | H     | M        | L          |
| P2        | M          | M     | L        | L          |
| P3        | L          | L     | L        | L          |

Gap = 5

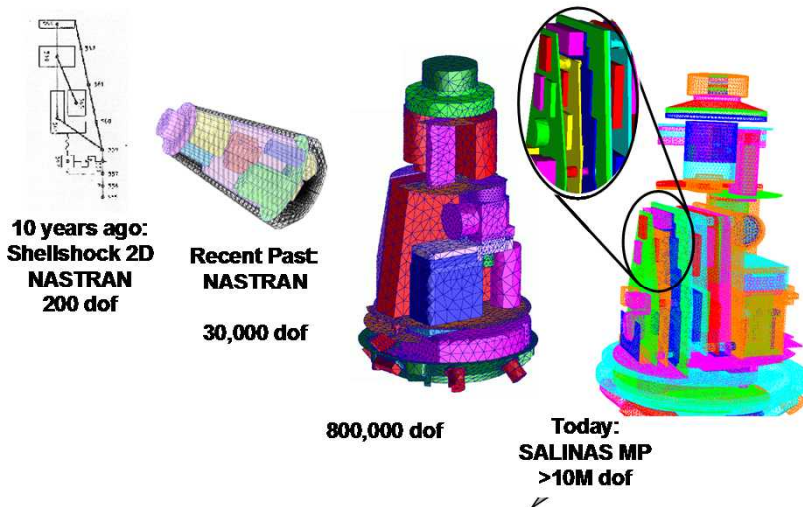
Completeness = 0.44



# Low Physics Fidelity

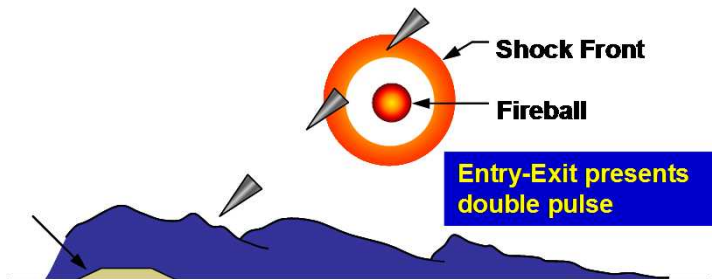


- Conduct blast test

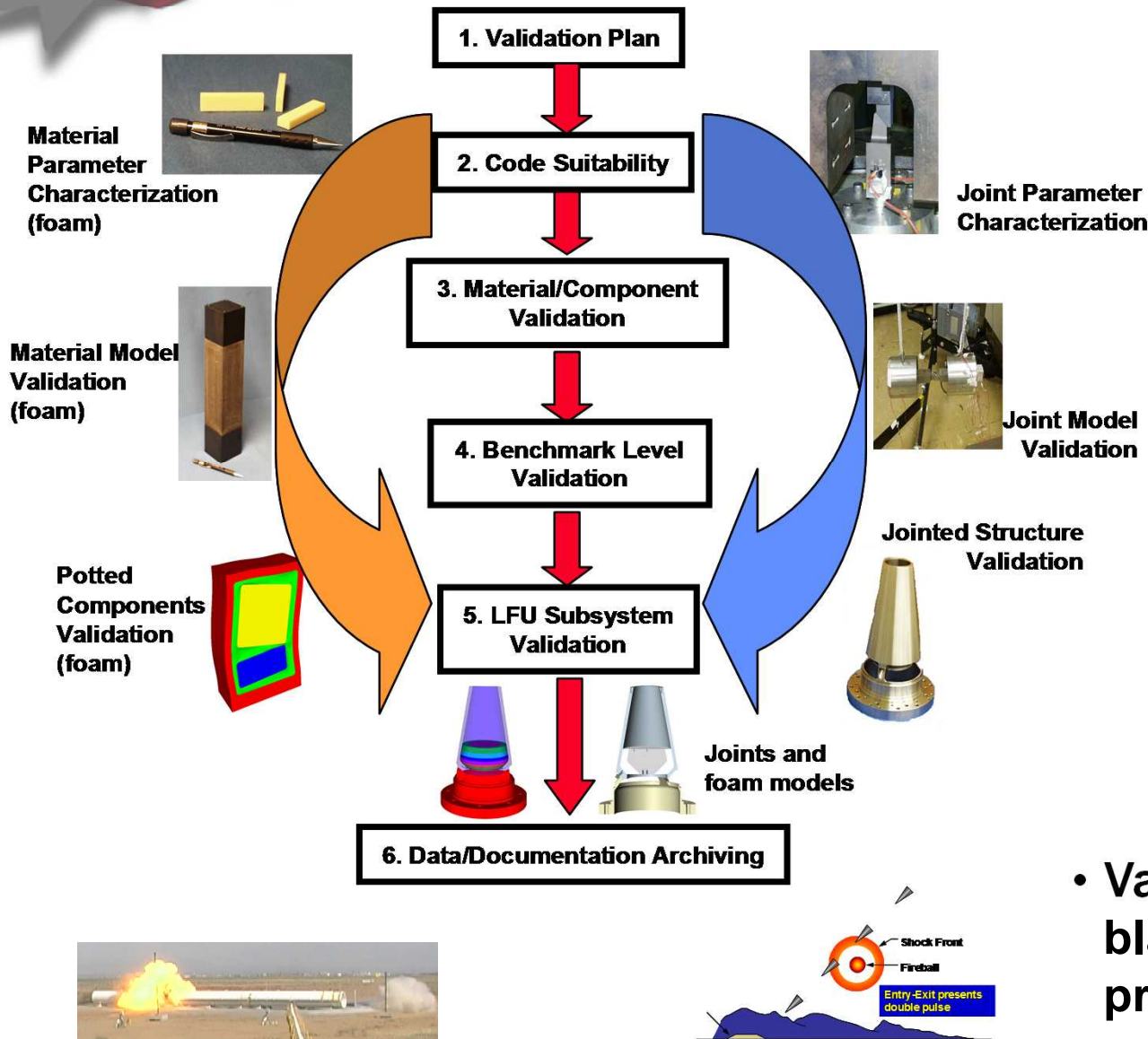


- Calibrate model to blast test using global **stiffness** and **damping** parameters: **knobs that act as surrogates for missing or unknown physics**

- Use calibrated model to make prediction in tactical environments



# Improving Physics Fidelity



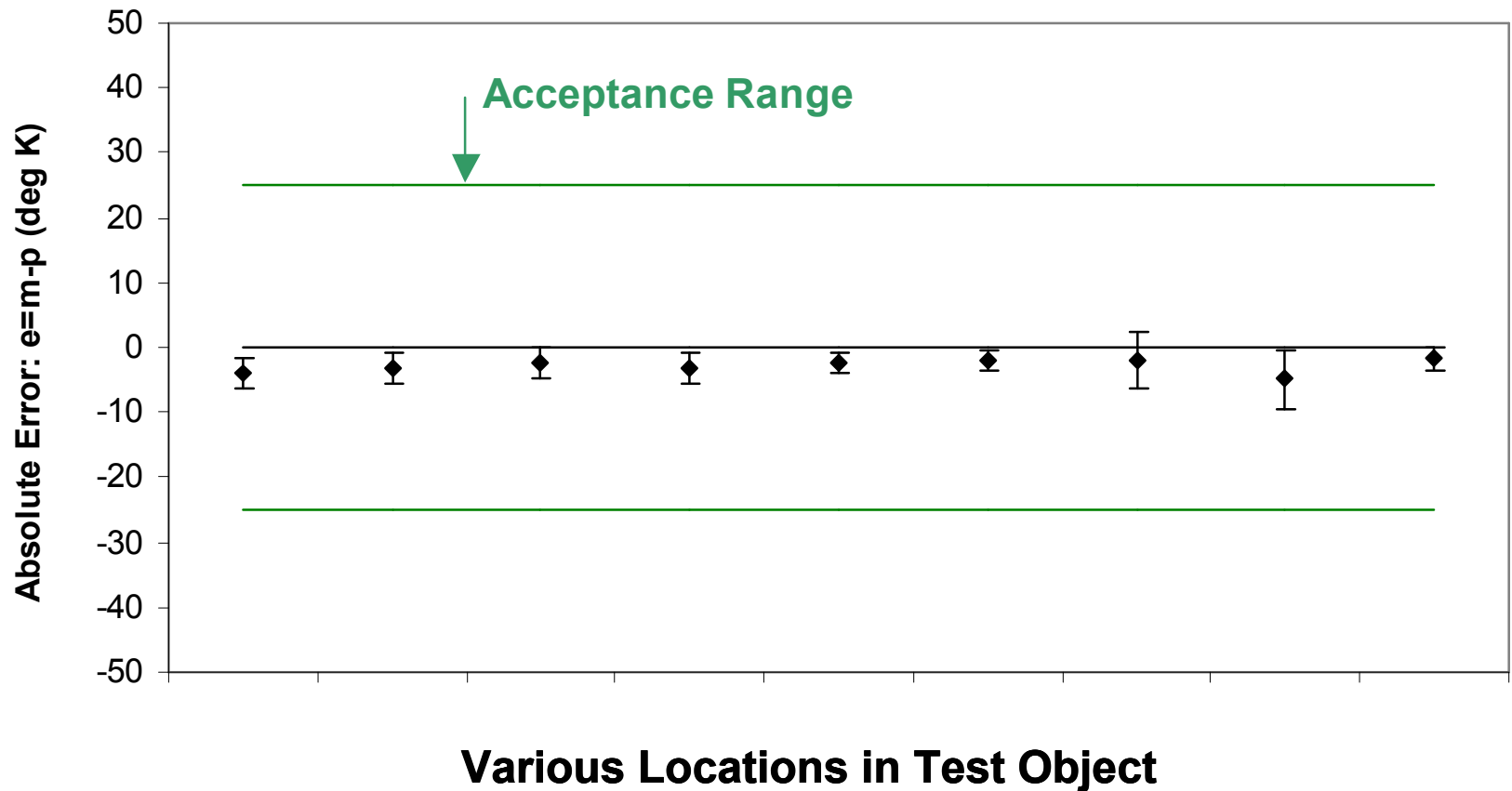
- Physics-informed models validated against separate effects tests

- Validate against blast test and make prediction in tactical environments



# Well Established Physics Fidelity

$e \sim 2K$  for conduction





# Code Readiness

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**Hyperlinks**

# Attributes of Verification

Demonstrating **Convergence** to **Correct Answer**  
for the **Intended Application**

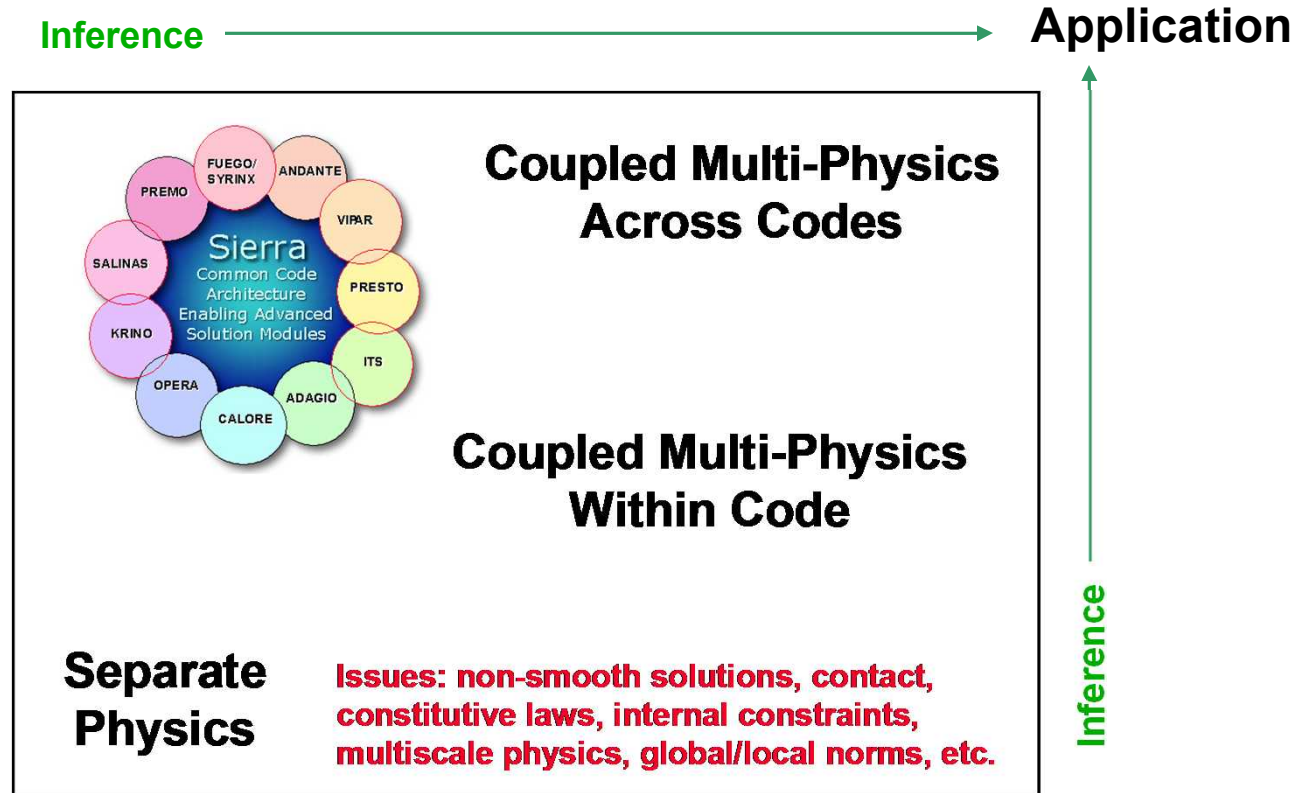
**Solution Verification: Convergence for intended application, but is it the right answer?**

**• Address adequacy of spatial AND temporal AND other discretizations AND numerical knobs**

**Regression Testing**

**SQE(A)**

Pilch – VV 2007



**Code Verification: Convergence to correct answer, wrong application**

**• Eliminate code bugs AND inadequate algorithms**



# Code to Code Comparisons Are a Poor Substitute for Formal Verification

## Code Comparison Principle (CCP)

**Code 1 = assessed code      Code 2 = benchmark code**

$$\|\text{Code 1} - \text{Truth}\| \leq \|\text{Code 1} - \text{Code 2}\| + \|\text{Code 2} - \text{Truth}\|$$

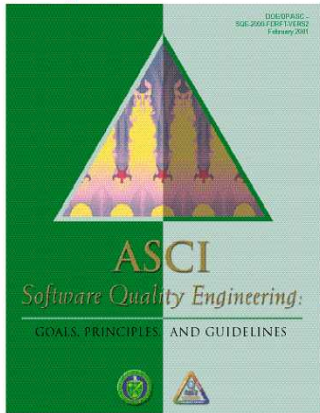
- $\|\text{Code 1} - \text{Code 2}\|$  . What if this term is not negligible?**
- Could be that Code 1 models are different from Code 2 models**
  - Could be a bug in Code 1 or Code 2**
  - Could be an algorithm flaw in Code 1 or Code 2**
  - Could be that Code 1 or Code 2 model is not converged**

**Points to path for better code-to-code comparisons; but if Code 2 is formally verified, why not verify Code 1 to the same verification test suite? And if not, why bother with the code-to-code comparison?**



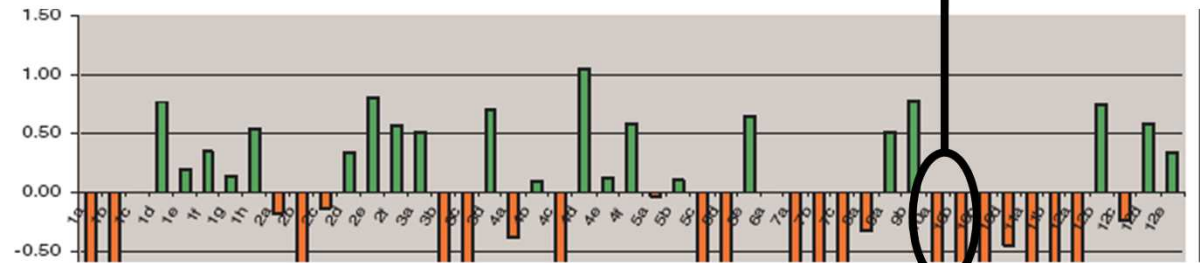
# SQE(A): Demonstrated Due Diligence in the Stewardship of Codes

## Requirements



## SourceForge: Issue Tracking

## Improvement

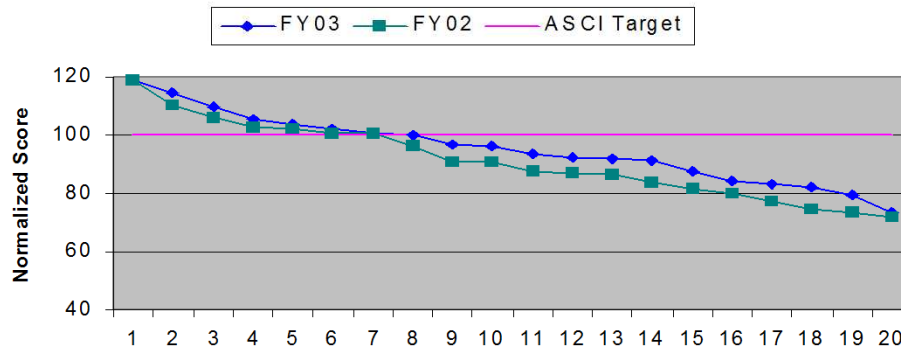


**FY03 AVG = 95.36**

**Calore = 96**

**FY02 AVG = 91.06**

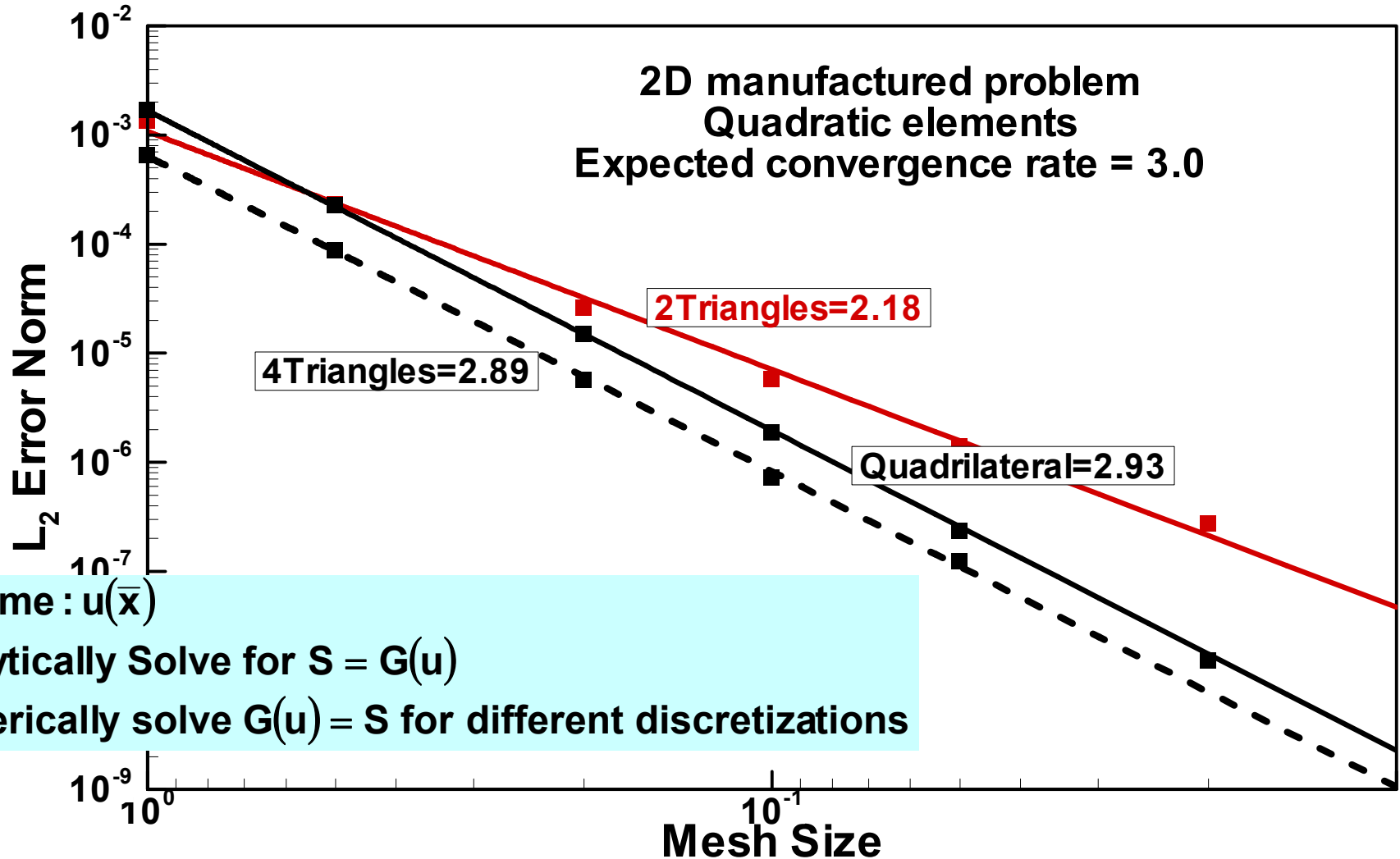
Sorted Total Scores, FY02 & FY03 (with 100% target)



## Assessments

# Verification with Manufactured Solution

## CEPTRE: Radiation Transport



Assume :  $u(\bar{x})$

Analytically Solve for  $S = G(u)$

Numerically solve  $G(u) = S$  for different discretizations

# Measuring Progress in Code Verification Coverage and Interactions

|                          |                         | Verification Test Suite         |  |        |        |       |     |
|--------------------------|-------------------------|---------------------------------|--|--------|--------|-------|-----|
|                          | Features & Capabilities | Unit Tests                      | VERT 1   | VERT 2 | VERT 3 | Ideal |     |
| Code A                   | FC1                     |                                 | VT1  |        |        |       |     |
|                          | FC2                     | UT1                             | VT1  |        |        |       |     |
|                          | FC3                     | UT2                             | VT1  |        |        |       |     |
|                          | FC4                     | UT3                             | VT1  |        |        |       |     |
|                          | FC5                     |                                 |  | VT2    |        |       |     |
| Code B                   | FC6                     | UT4                             |  | VT2    |        |       |     |
|                          | FC7                     | UT5                             | <div><math display="block">f = \frac{\sum_{i=1}^{N_{\text{verts}}} \left( \sum_{r=1}^{n_v} C_r \right)_i}{\sum_{r=1}^{N_{\text{FC}}} C_r}</math></div> |        |        |       | VT3 |
|                          | FC8                     | UT6                             |  |        |        |       | VT3 |
|                          | FC9                     | UT7                             |  |        |        |       | VT3 |
|                          | FC10                    | UT8                             |  |        |        |       | VT3 |
| Code or Appl Perspective | Line or Cap Coverage    | Capability+Interaction Coverage |  |        |        |       |     |
|                          | 80%                     | 3.22%                           |  |        |        |       |     |



# Solution Verification

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**Hyperlinks**

# Attributes of Verification

Demonstrating **Convergence** to **Correct Answer**  
for the **Intended Application**

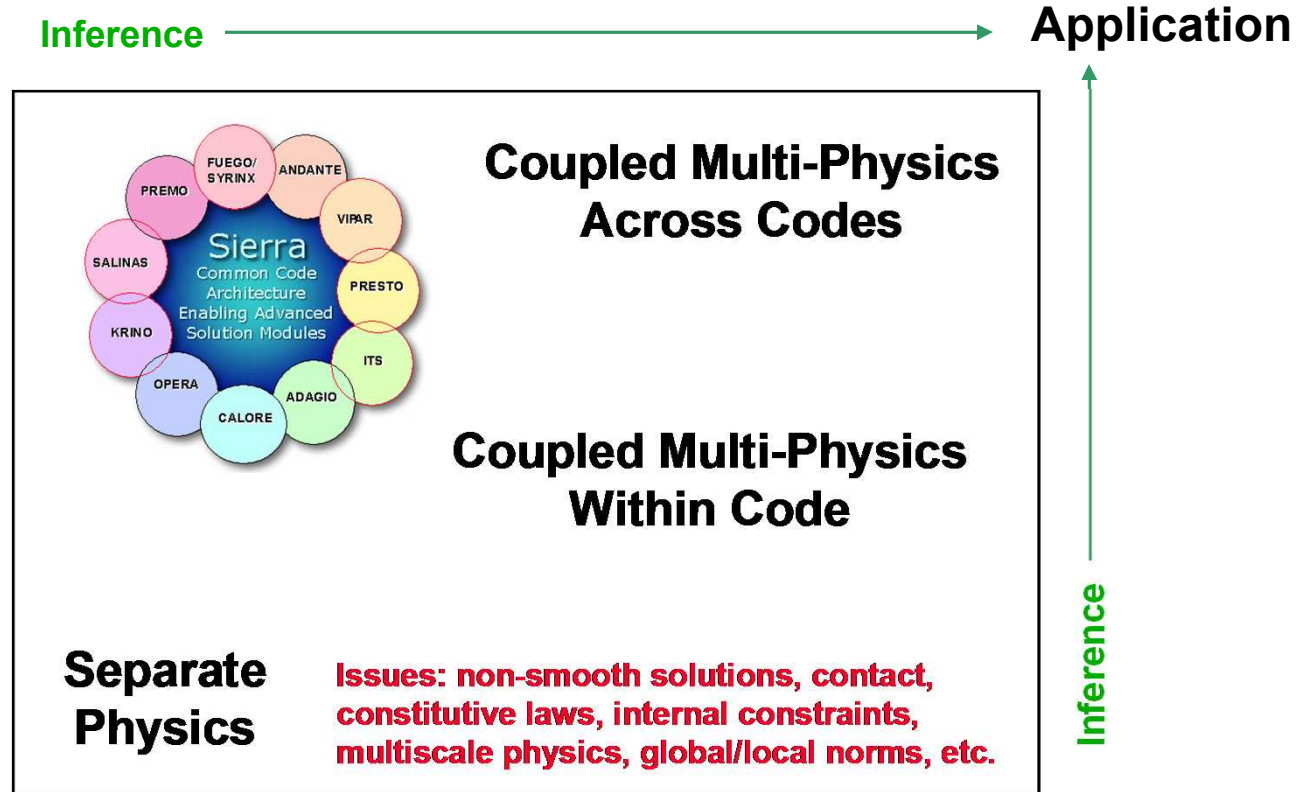
Solution Verification: **Convergence** for  
**intended application**, *but is it the right  
answer?*

• Address adequacy of spatial **AND** temporal  
**AND** other discretizations **AND** numerical  
knobs

Regression  
Testing

SQE(A)

Pilch – VV 2007



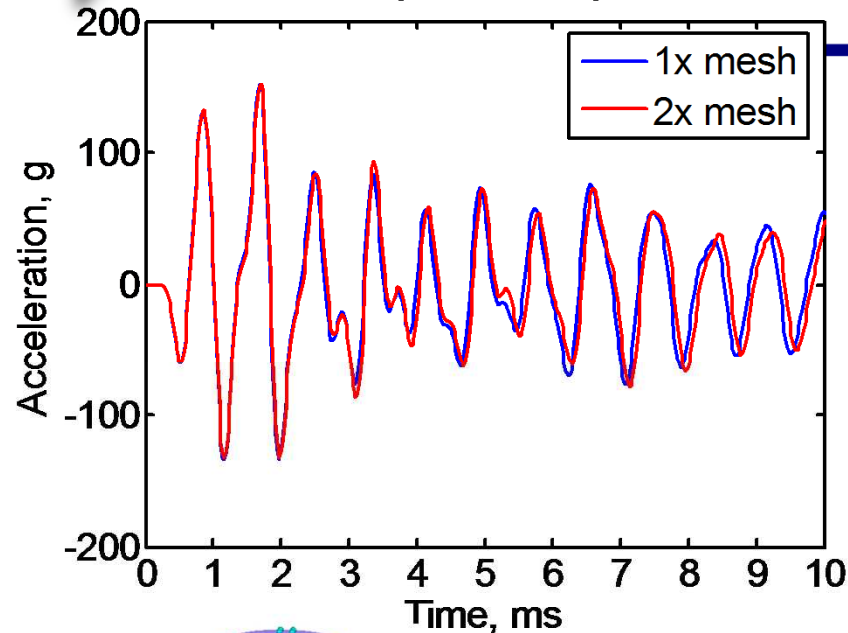
Code Verification: **Convergence** to correct answer, *wrong application*

• Eliminate code bugs **AND** inadequate algorithms

# Sensitivity to Mesh Parameters

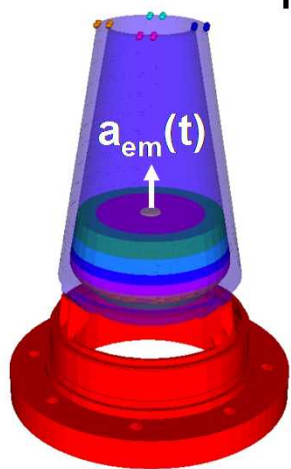
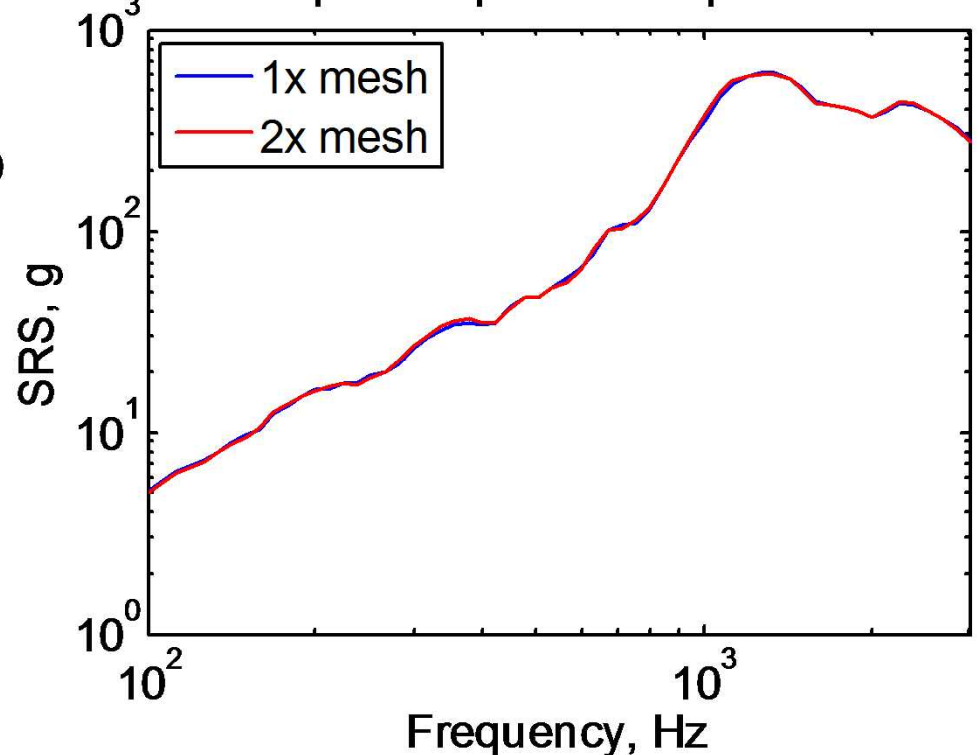
## Structural Dynamics

Acceleration response at top of enc. mass



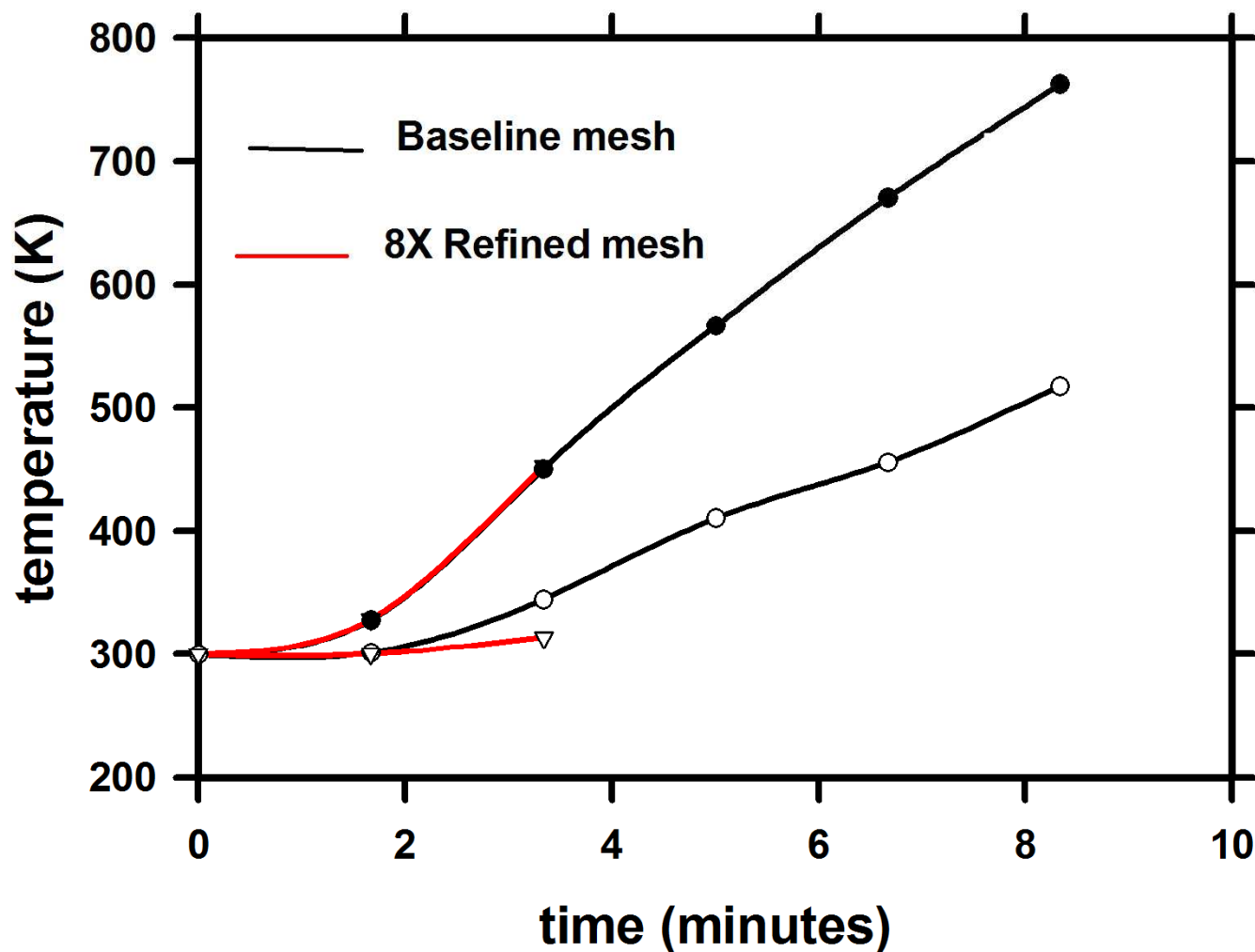
Max. relative error between  
SRS: +/- 5%

Shock response spectra at top of enc. mass

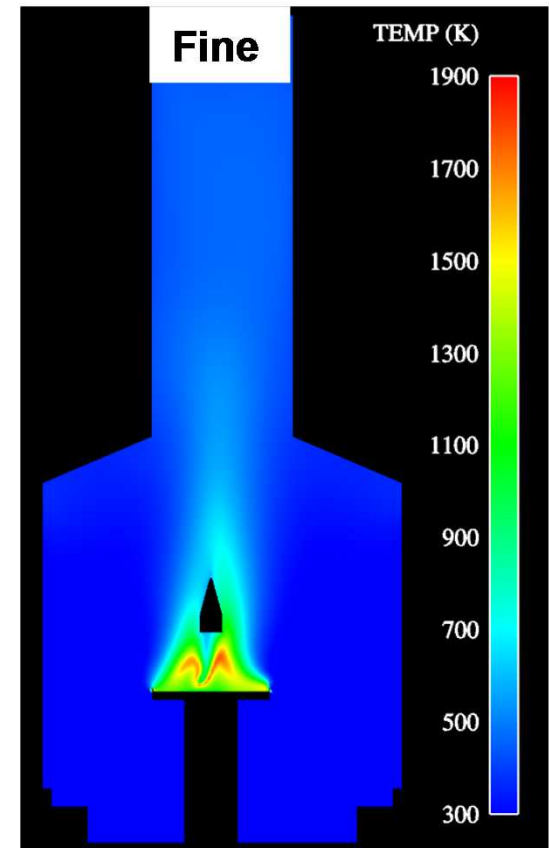
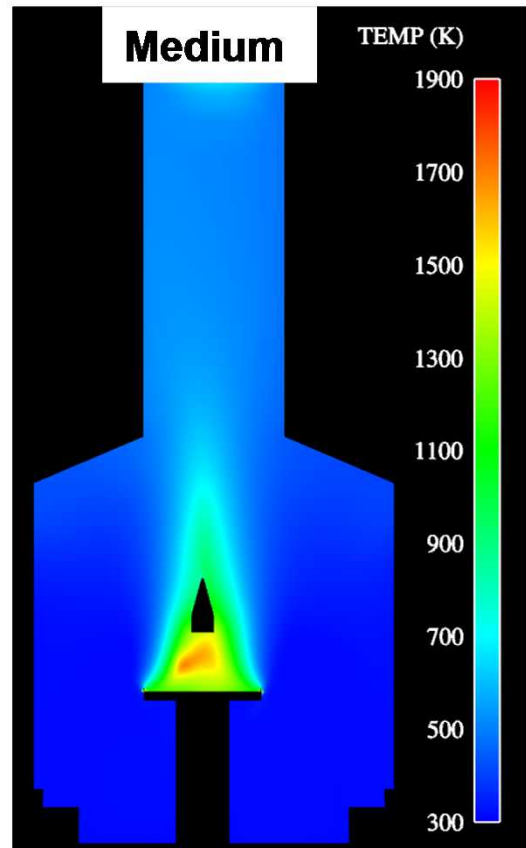
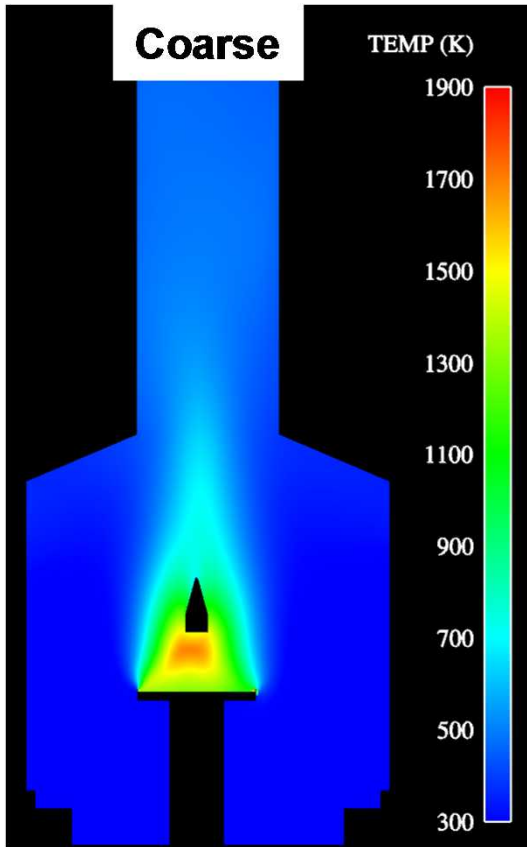


# Solution Verification on High Fidelity Models is Hard

**Solution Verification: Is the Discretization Adequate?**



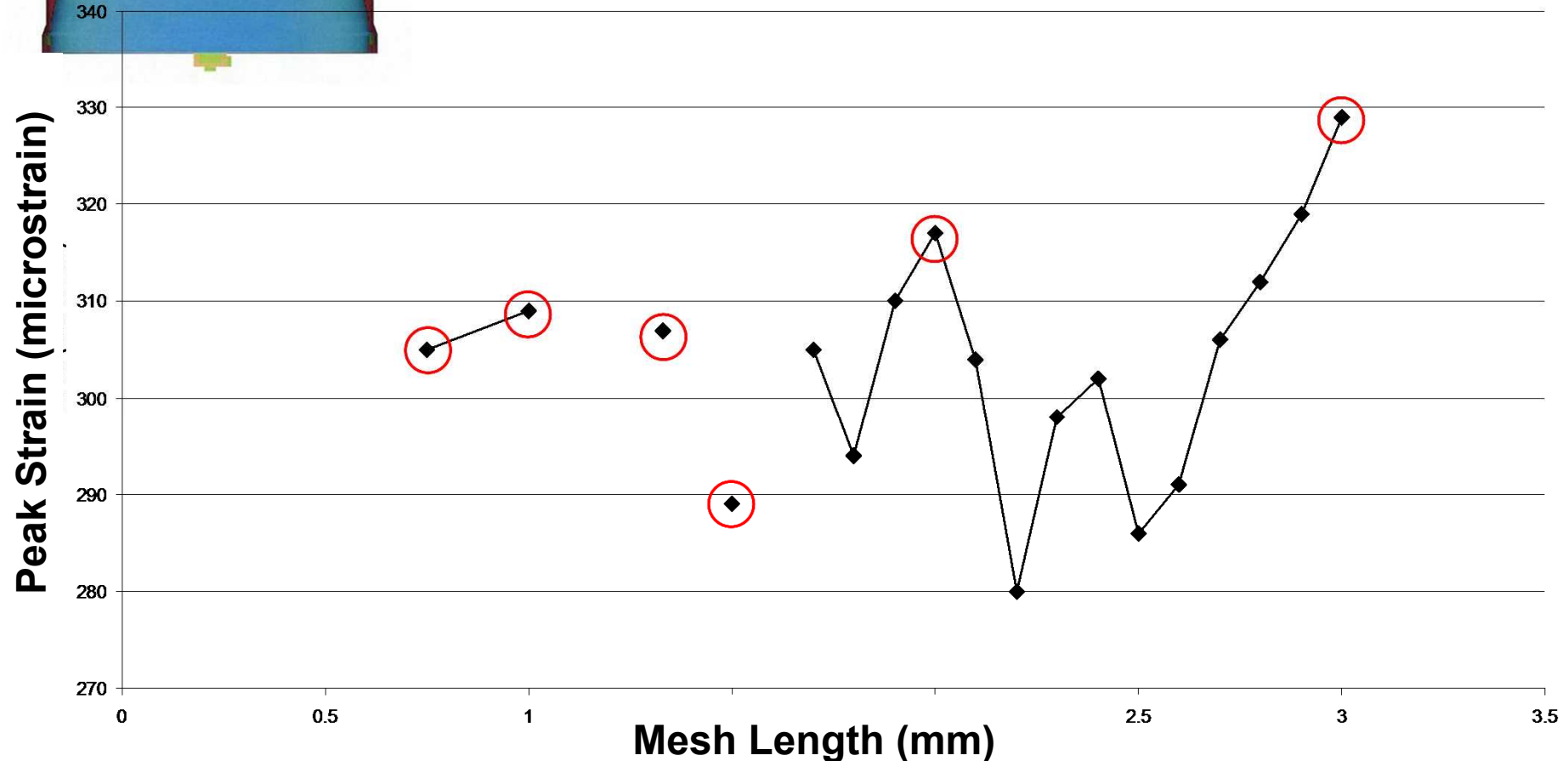
# Calorimeter Fire BVG Solutions





# Calculation Verification for a Threaded Assembly

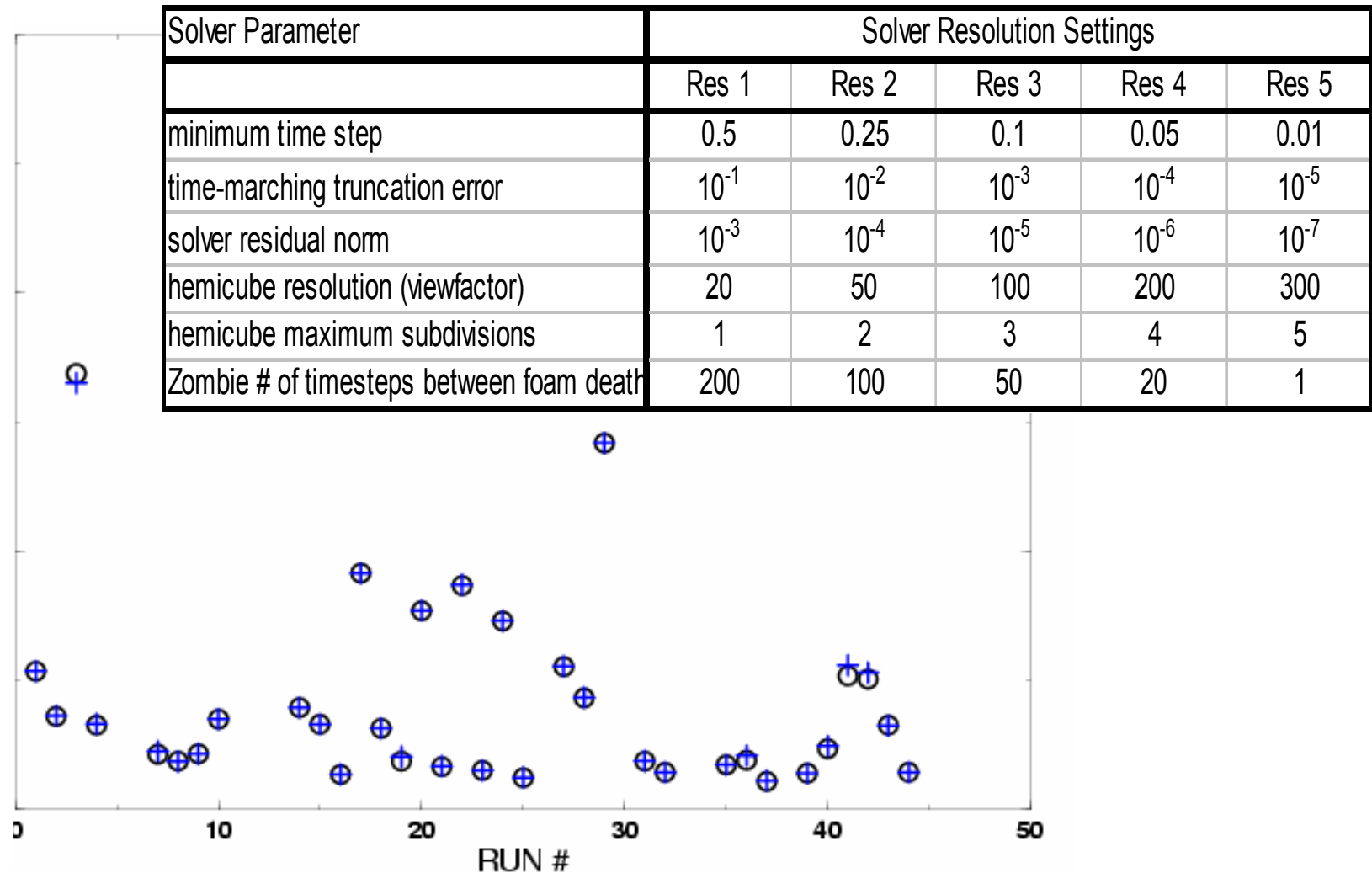
Ryan Maupin, ESA-WR, LANL: IMAC-XXIV 1/31/06



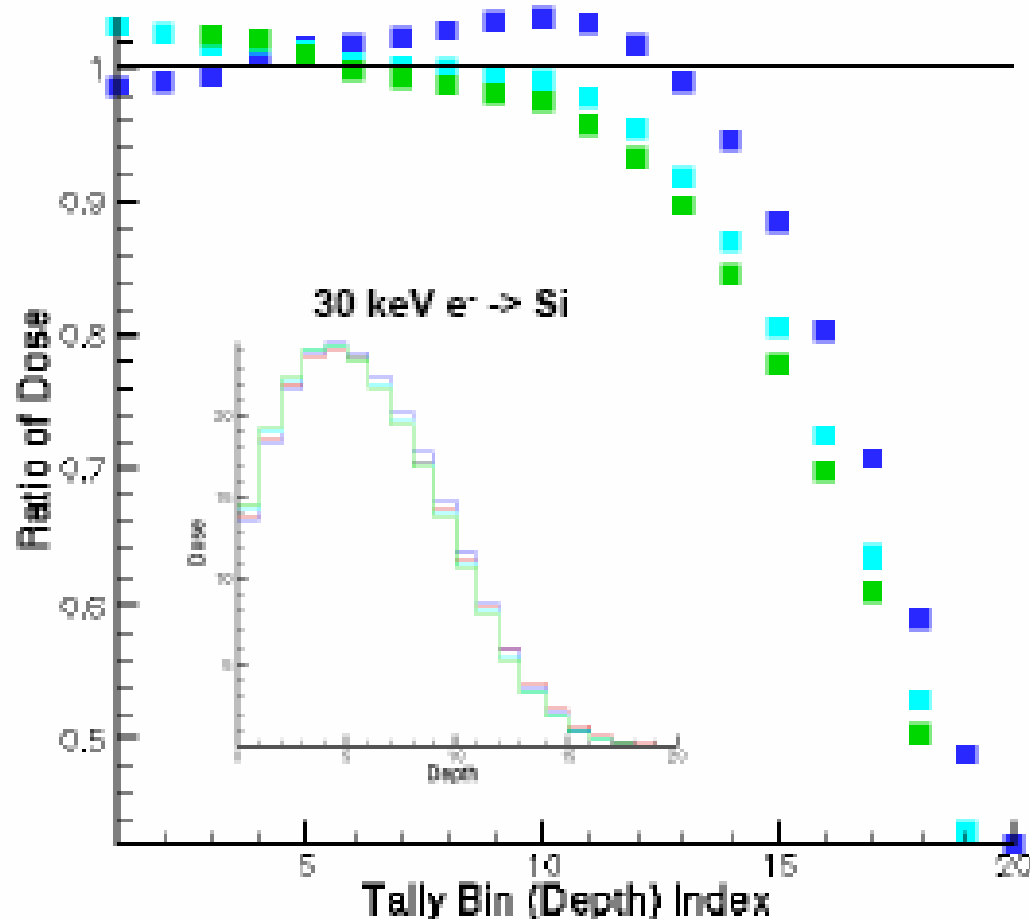
# Solver Resolution Over UQ Parameter Space

**Solution Verification: Are the solver settings adequate?**

System Response Quantity



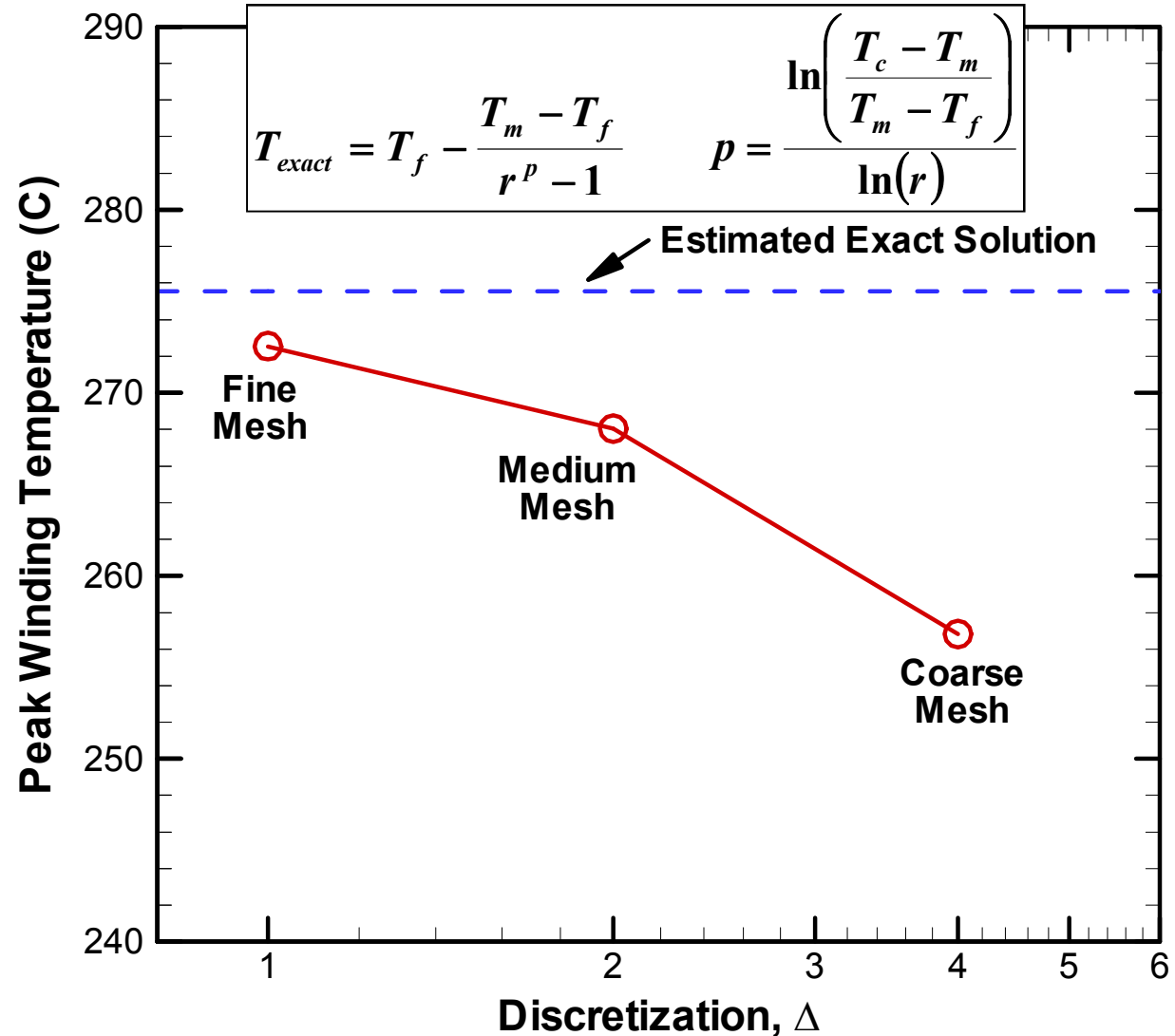
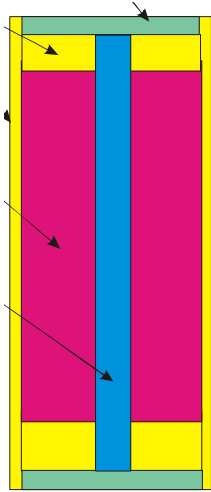
# Dose Sensitivity to Electron Boundary Crossing Algorithm



- Evaluation of ITS electron boundary-crossing error: (All with respect to no internal boundaries, default substep size.
- Blue: internal boundaries, default substep size
- Cyan: Internal boundaries half-default substep size
- Green: Internal boundaries quarter-default substep size

# Numerical Errors

## Pollute Validation Assessments



# Verification of Error Estimator and Adaptive Algorithm

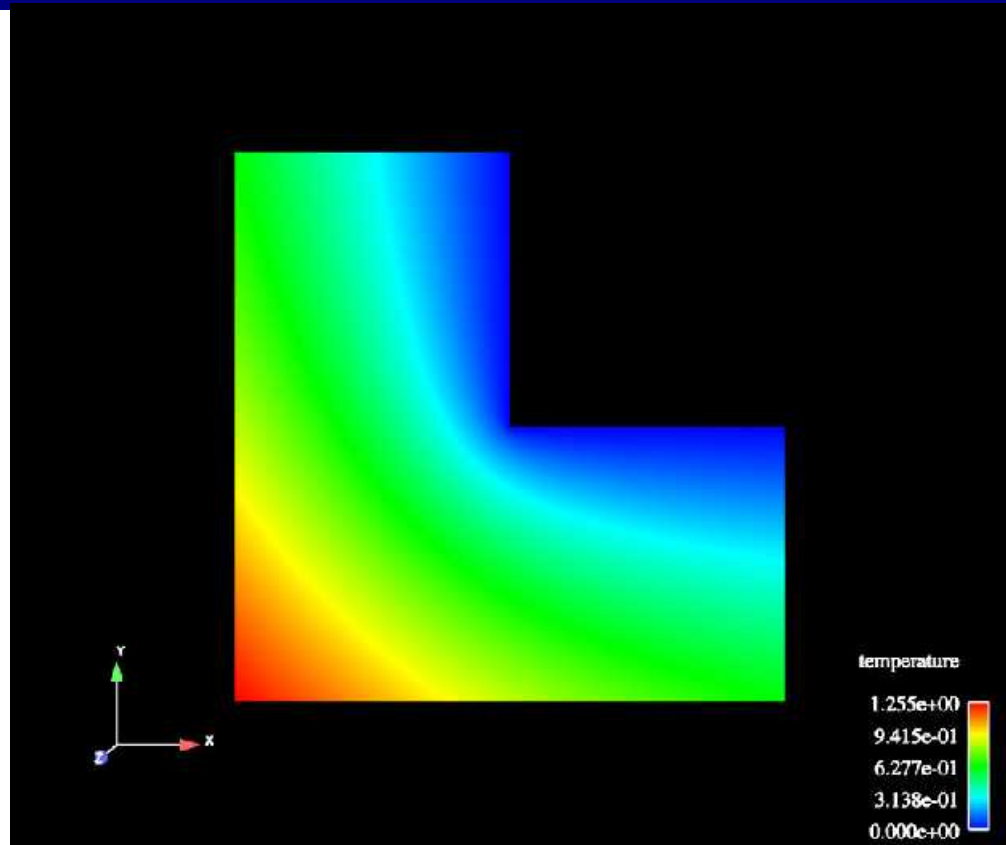
- 2D Exact Solution:

$$u = r^{2/3} \sin\left(\frac{2}{3}\theta\right)$$

- Linear elements
- ZZ error estimator

- Feedback adaptive algorithm:

if  $\left( \|e^*\|_{H_1(\omega_j)} > 0.995 \max_{1 \leq i \leq N_\omega} \|e^*\|_{H_1(\omega_i)} \right)$  then refine  $\omega_j$





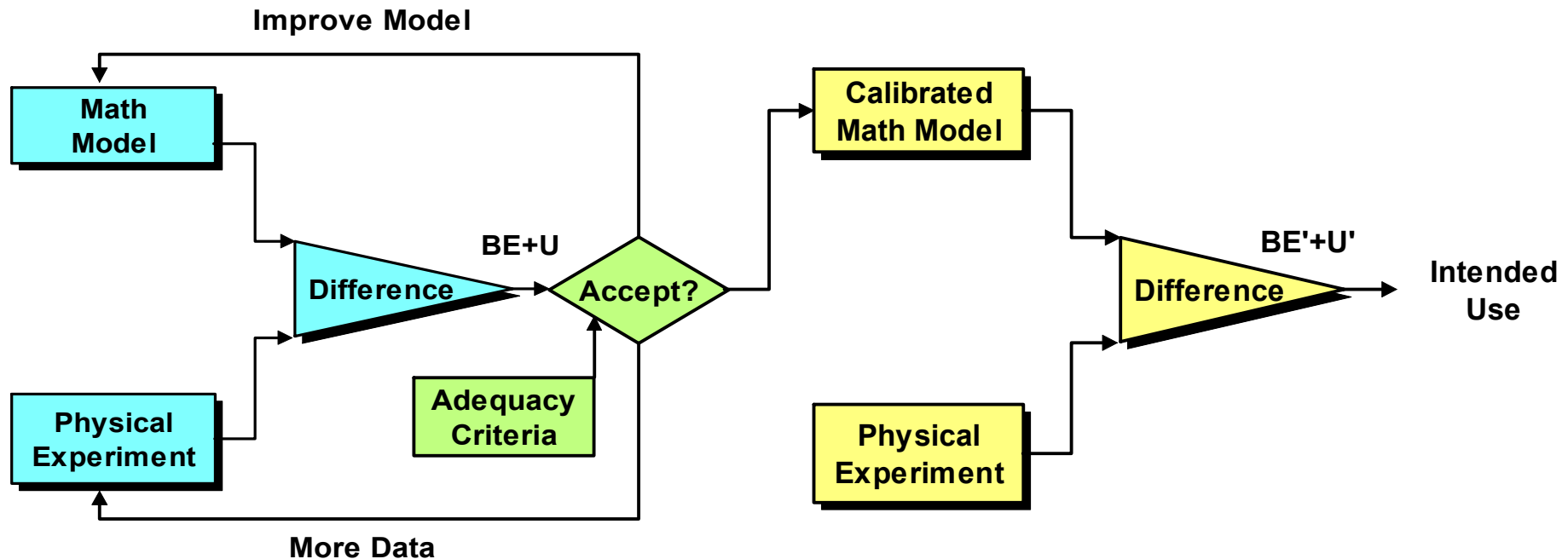
# Validation

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## Hyperlinks

# Validation is Assessment

Calibration is not Validation

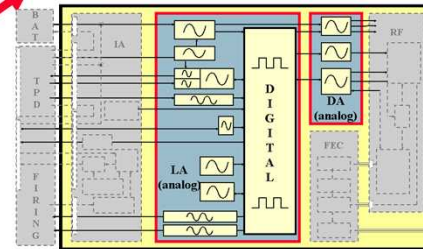


# Science-Based Validation Experiments

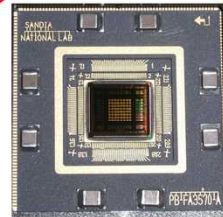
## Validation: Are You Solving the Right Equations?

**Hierarchal Validation: Right answer for the right reason**

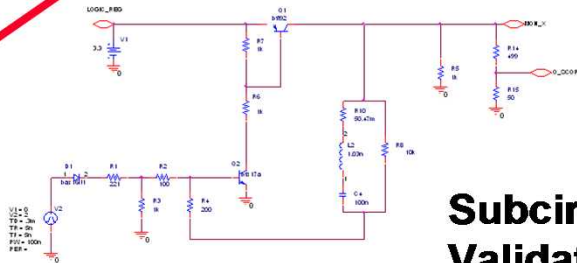
**Increasing complexity,  
Decreasing number of tests**



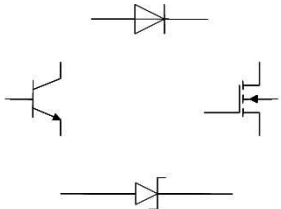
**System-Level  
Circuit  
Validation**



**Single ASIC  
Validation**



**Subcircuit  
Validation**



**Single Device  
Characterization  
and Validation**

- **Application relevant parameter space**
- **Formal DOE and replicate tests**
- **Attention to diagnostic bias and precision**



# Science-Based Validation Experiments

## Validation: Are You Solving the Right Equations?

**Hierarchical Validation: Right answer for the right reason**

**Increasing complexity,  
Decreasing number of tests**



**Joint parameter characterization**



**Single joint validation**



**Jointed structure validation**



**Mockup with jointed structure and foam embedded object**



**Full System Test**

- **Application relevant parameter space**
- **Formal DOE and replicate tests**
- **Attention to diagnostic bias and precision**

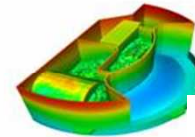
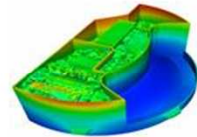
# Science-Based Validation Experiments

## Validation: Are You Solving the Right Equations?

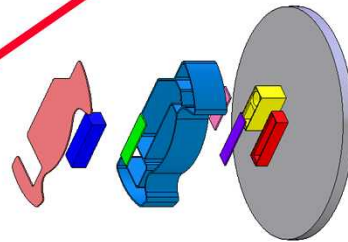
**Hierarchical Validation: Right answer for the right reason**



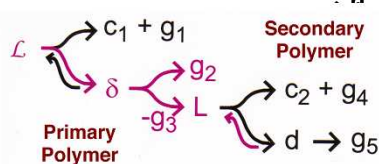
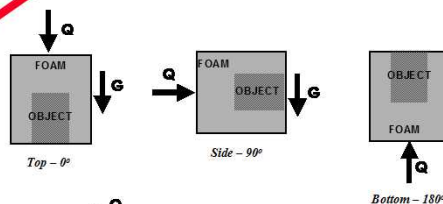
**Full System Test**



**Validation  
Real Sub-systems**



**Validation with  
mockups**

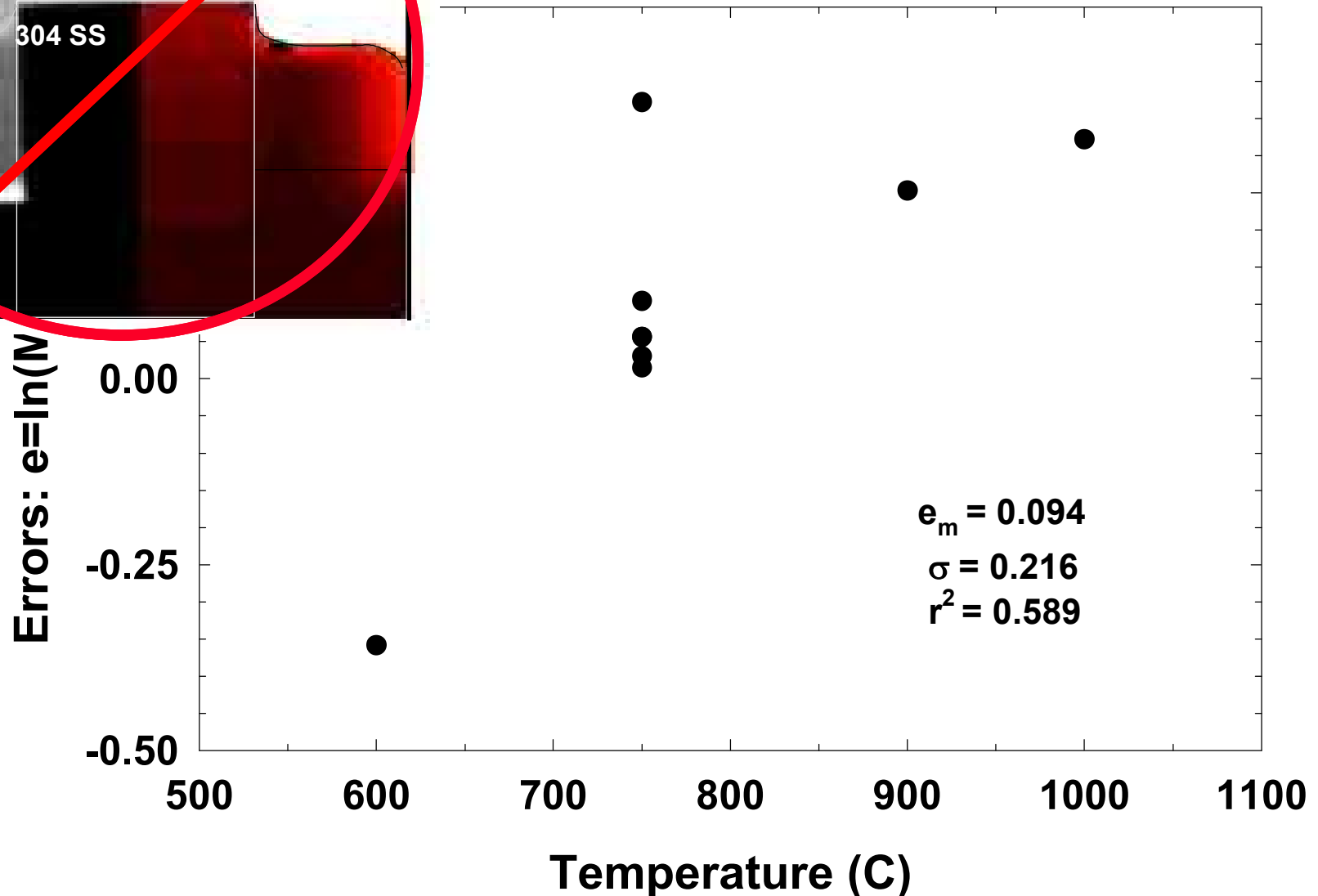


- Application relevant parameter space
- Formal DOE and replicate tests
- Attention to diagnostic bias and precision

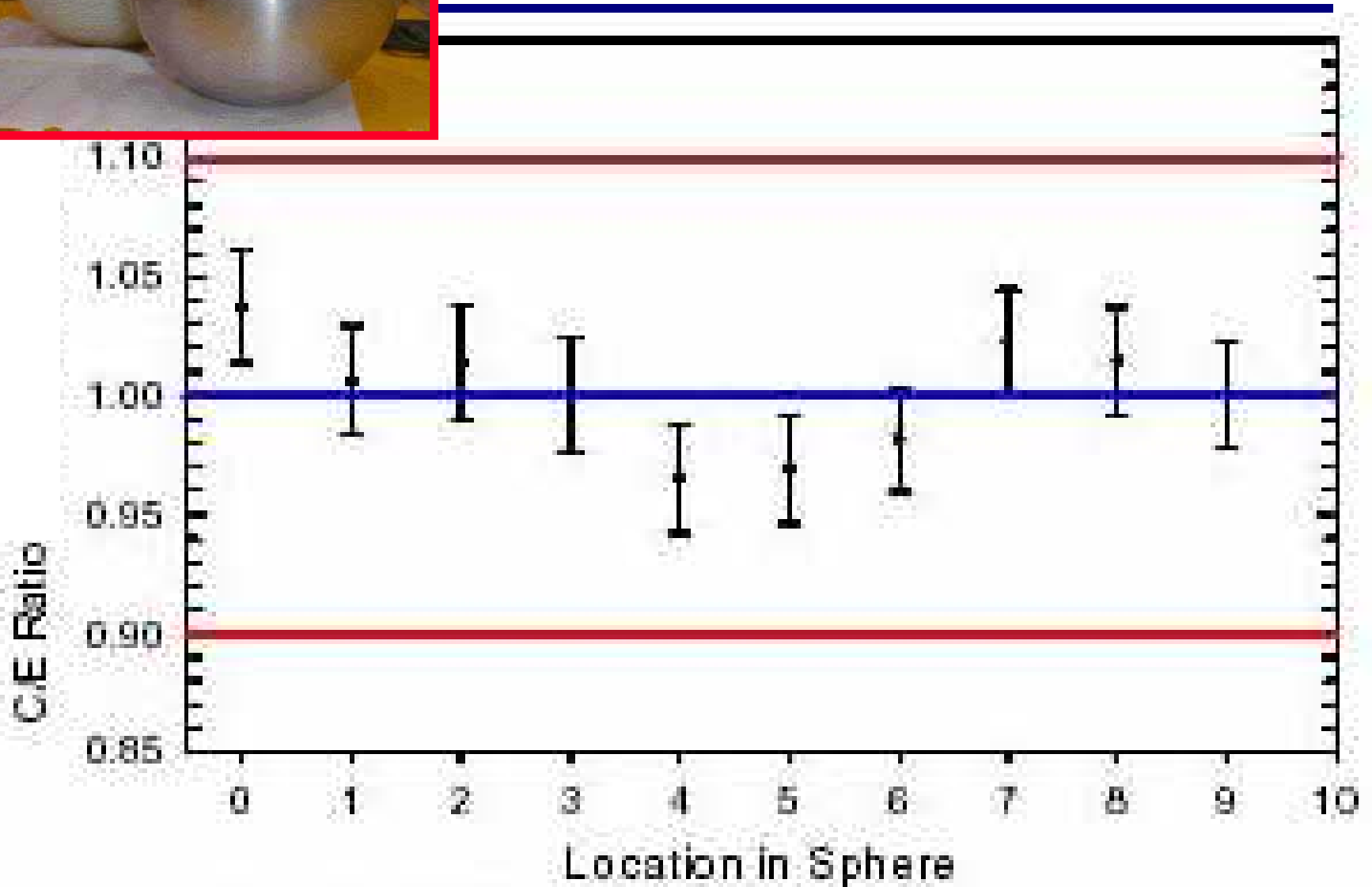


# Validation is Statistical

**Vugraph Norms  
Are Not Adequate**



# Neutron Attenuation in Test Objects





# QMU and Sensitivities

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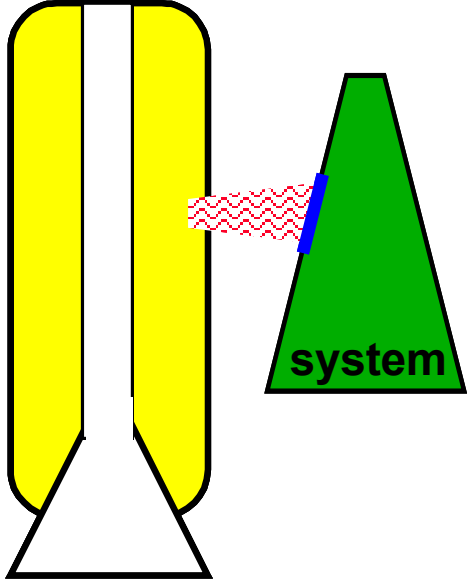
**Hyperlinks**



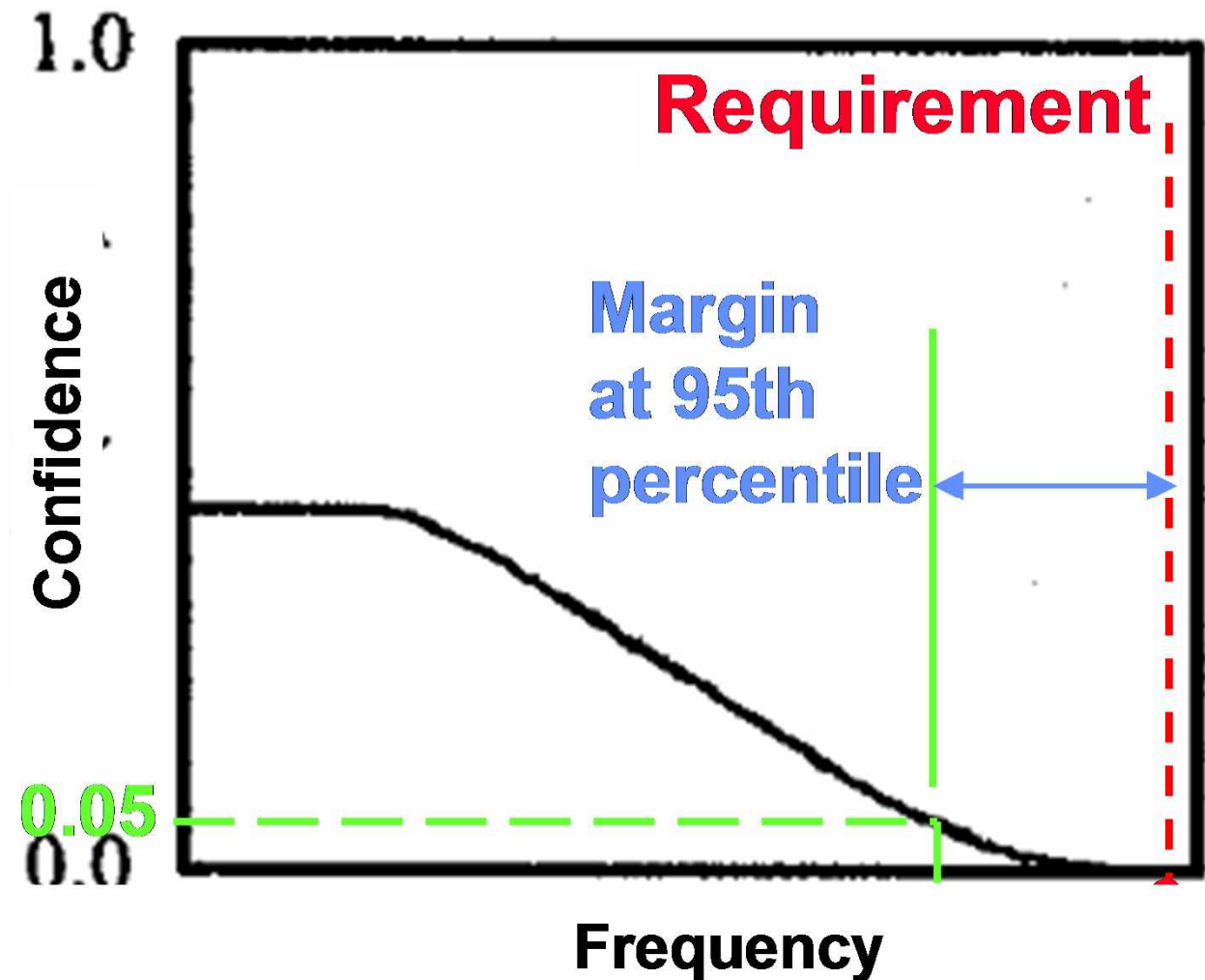
# Aleatory and Epistemic Uncertainties

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- **Aleatory uncertainty**: Inherent randomness in behavior of system under study (**frequency interpretation**)
  - Alternatives: Variability, stochastic uncertainty, irreducible uncertainty, type A uncertainty
  - Examples: component failures or material properties derived from statistically significant testing under conditions relevant to intended application
- **Epistemic uncertainty**: Lack of knowledge about appropriate value to use for a quantity that is assumed to have a fixed value in the context of a specific analysis (**confidence or belief interpretation**)
  - Alternatives: state of knowledge uncertainty, subjective uncertainty, reducible uncertainty, type B uncertainty
  - Examples: representative scenarios, unknown parameters in frequency distributions, parameters or models with defensible bounds but no sense of frequency

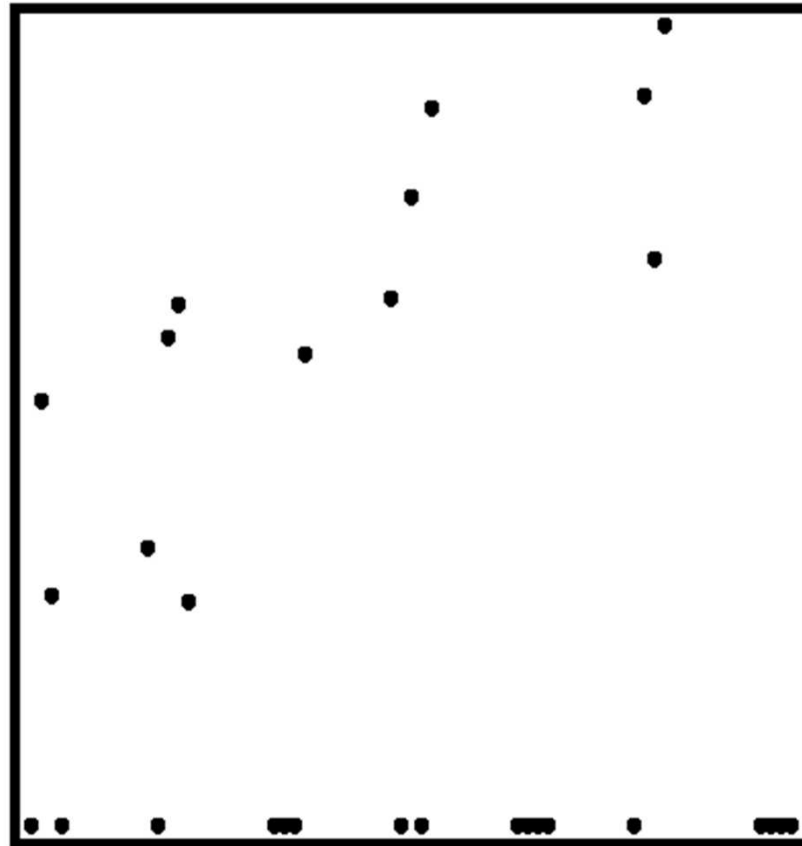


# Quantified Margins and Uncertainties

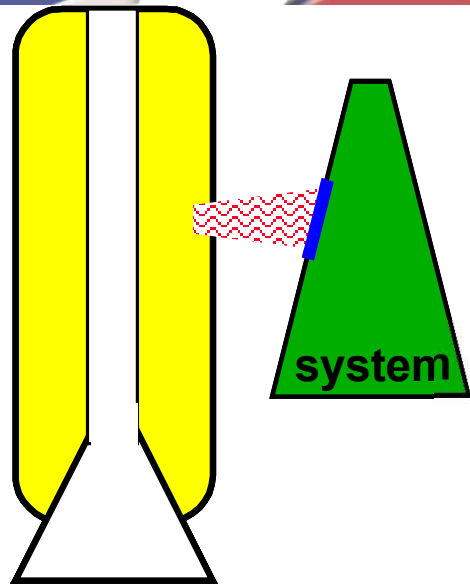


# Sensitivity Analysis

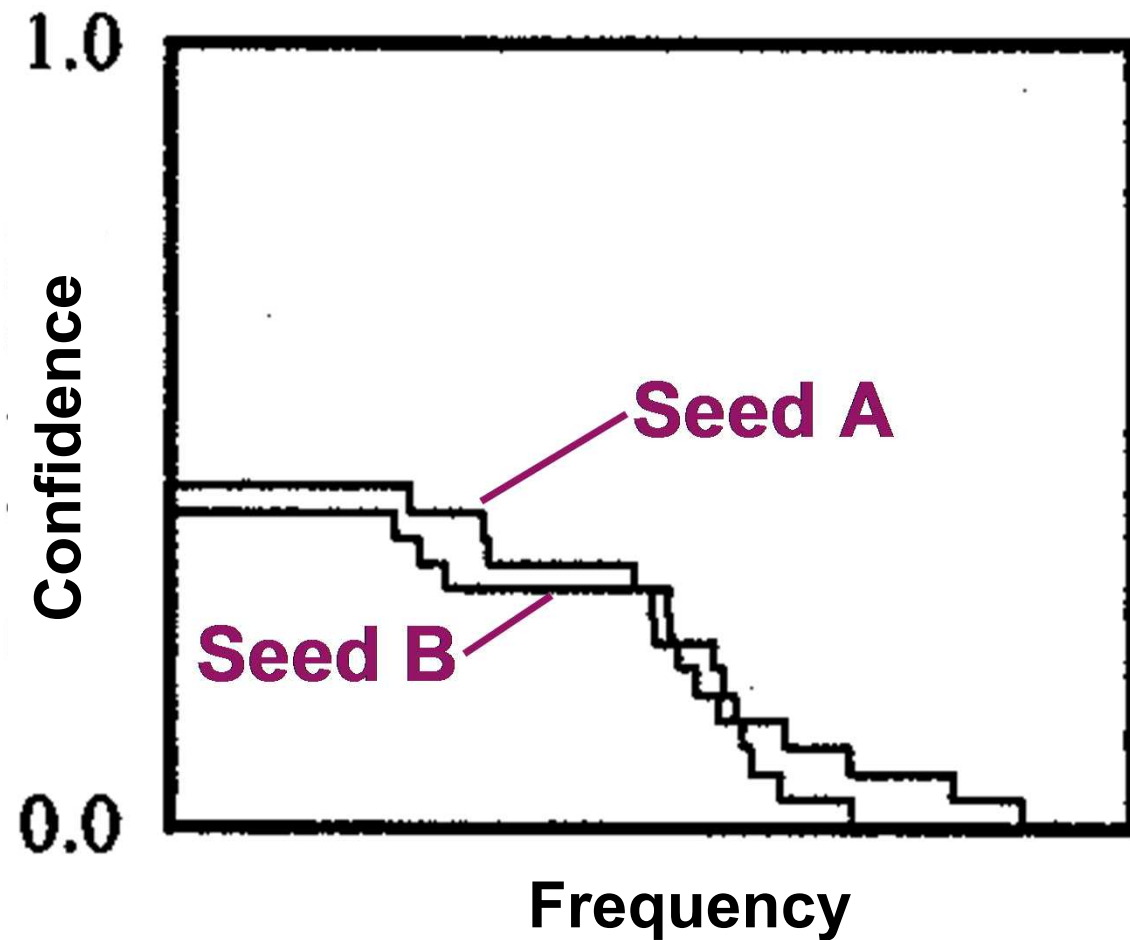
$$SCorr = 0.809$$







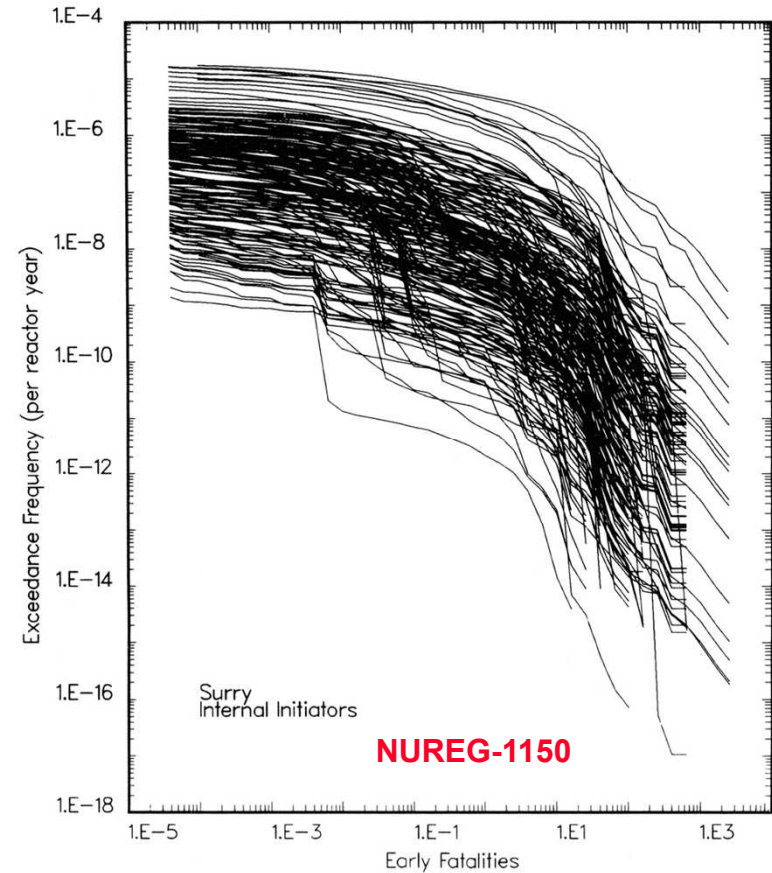
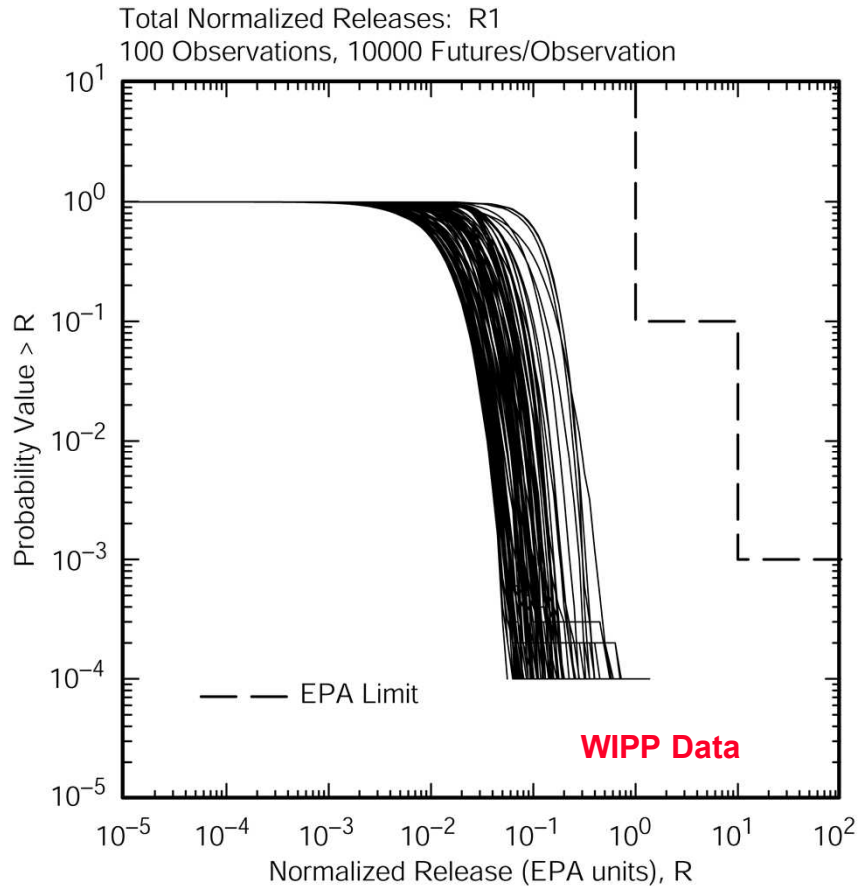
## UQ Solution Verification



**Seed Effects from limited sampling**

# WIPP and NUREG-1150 Precedents

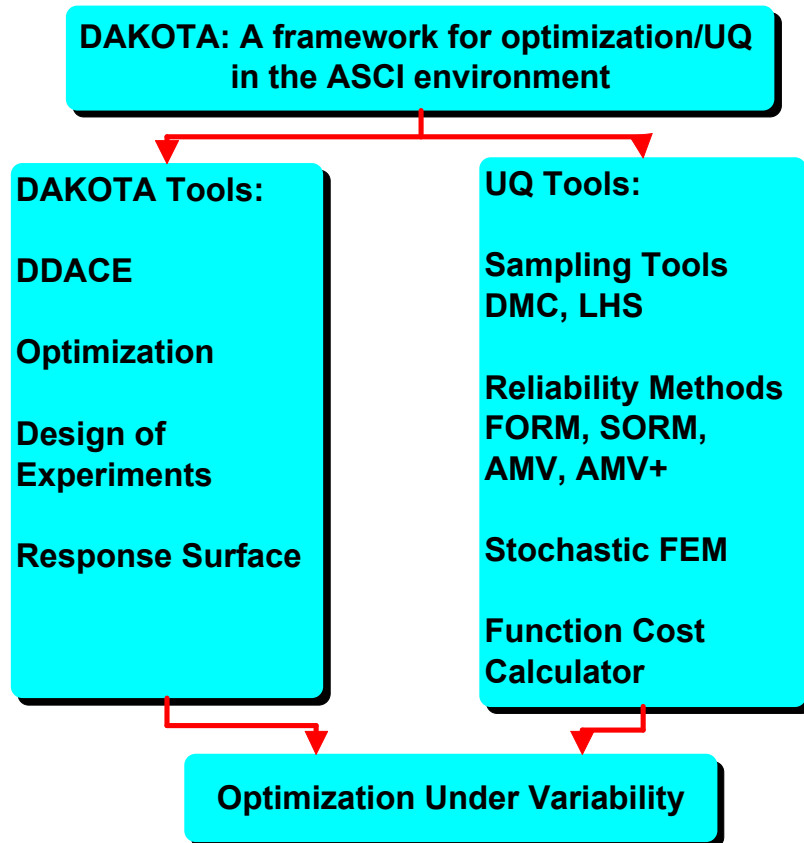
High Consequence Regulatory Issues in the National Interest  
Addressed Primary Through Modeling and Simulation



**Lessons Learned: (1) Seek BE + Uncertainty**

**(2) It takes more than one shot to get it right**

# Infrastructure for ASC-Scale UQ Analyses



1. **Algorithmic coarse-grained parallelism:** independent concurrent fn. evaluations
2. **Algorithmic fine-grained parallelism:** parallel computation of internal linear algebra
3. **Function evaluation coarse-grained parallelism:** concurrent execution of separable simulations within a fn. eval. (e.g., multiple loading cases)
4. **Function evaluation fine-grained parallelism:** parallelization of the solution steps within a single analysis code (e.g., SALINAS, MPSalsa)

