

# Spectrum Isolation in Multi-Source Image Reconstruction Using a Dual-Particle Imager

J. K. Polack<sup>1</sup>, M. C. Hamel<sup>1</sup>, A. Poitrasson-Rivière<sup>1</sup>, P. Marleau<sup>2</sup>, M. Flaska<sup>1</sup>, S. D. Clarke<sup>1</sup>, S. A. Pozzi<sup>1</sup>

<sup>1</sup>Department of Nuclear Engineering and Radiological Sciences, University of Michigan, Ann Arbor MI, 48109, USA

<sup>2</sup>Sandia National Laboratory, Livermore, California, 94550, USA

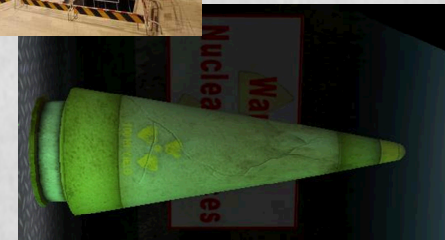
Institute of Nuclear Materials Management, 56<sup>th</sup> Annual Meeting  
Indian Wells, California, USA

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# Motivation

## *The Need for Versatile Imaging Systems*

- Localization and characterization of special nuclear material is a cross-cutting global need
  - Hidden special nuclear material within large-scale containers
  - International safeguards
  - Treaty verification (disarmament, warhead counting)
  - Build-up within nuclear facilities
  - Medical treatment planning and dose monitoring
- Passive special nuclear material signatures can be obtained by:
  - Particle counting
  - Spectroscopy
  - Multiplicity and coincidence counting
  - Imaging
- **Our research aims to develop versatile systems able to obtain the most information possible from these signatures**



# Dual-Particle Imager

## *A Versatile Imaging System*

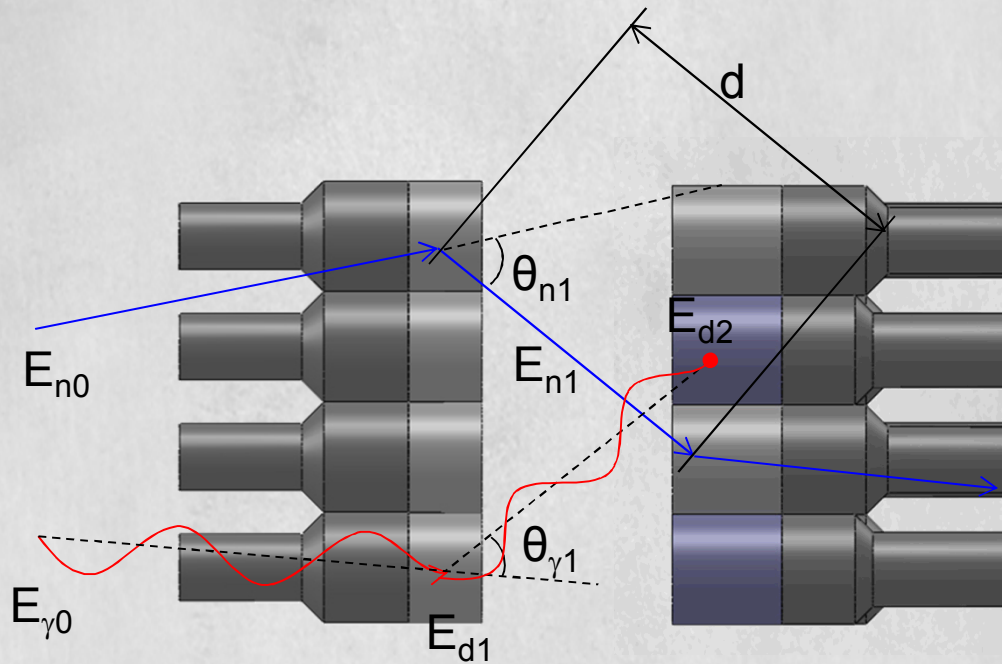
- One system capable of localizing and characterizing both neutron and photon sources
- The use of commercially-available components yields a fully scalable and relatively inexpensive system, adaptable to any need or facility
- The strength of the system is its versatility which enables it to image heavily shielded material as well as characterize diverse nuclear materials, from fission sources to single-decay gamma sources
- Potential end users: emergency response, DTRA, DNDO, IAEA

# Dual-Particle Imager *Design & Principle*

$$\cos^2 \theta_{n1} = \frac{E_{n1}}{E_{n0}}$$

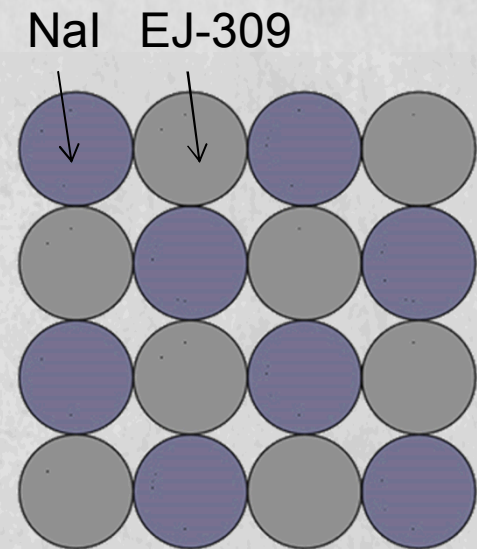
$$E_{n1} = \frac{m_n}{2} \times \frac{d^2}{TOF^2}$$

$$\cos \theta_{\gamma 1} = 1 - \frac{m_e c^2 \times E_{d1}}{E_{d2}(E_{d1} + E_{d2})}$$



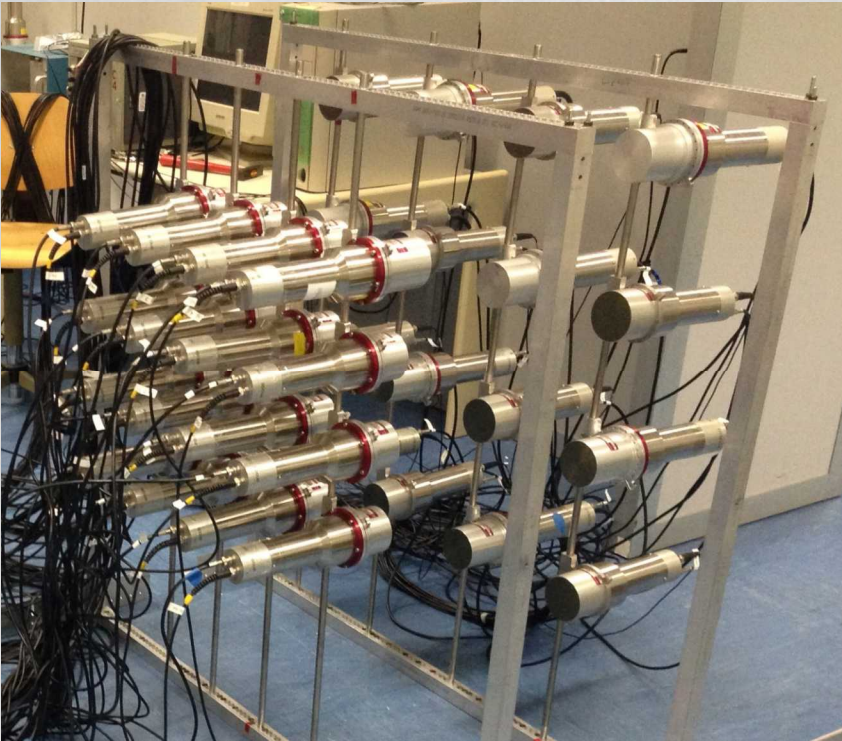
EJ-309

EJ-309 & NaI



Back Plane

# Dual-Particle Imager *Prototype Geometry*

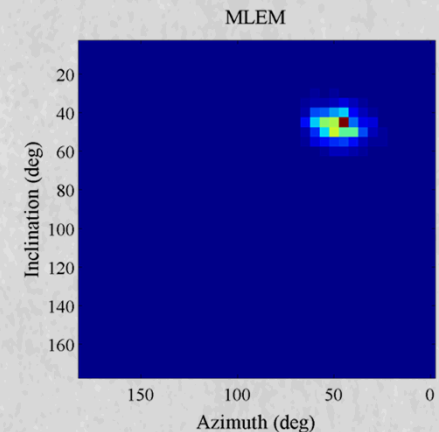
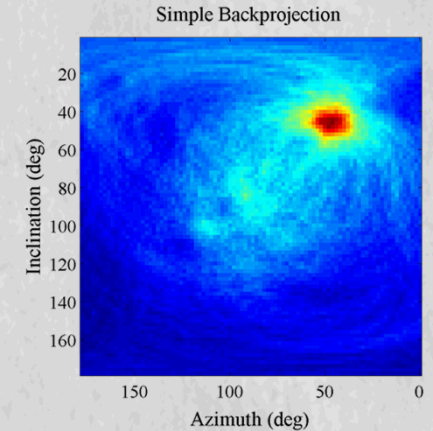


- 30-cm separation between planes
- 15 cm between detector centers in the front plane
  - 7.38-cm gap between detectors
- 25 cm between detector centers in the back plane
  - 17.38-cm gap between detectors

# Image Reconstruction

## *Advanced Algorithms*

- Simple backprojection reconstruction is easy to implement but results in blurry images
- Advanced reconstruction algorithms can improve signal-to-noise ratio
  - Filtered backprojection
  - Maximum-likelihood expectation-maximization (MLEM)
  - Stochastic origin ensembles (SOE)
- Ability to estimate individual energy spectra when multiple sources are present



Neutron images for a simulated 26 hour measurement of a 170k neutrons/second  $^{252}\text{Cf}$  source at 5 meters.

# MLEM

## *Algorithm*

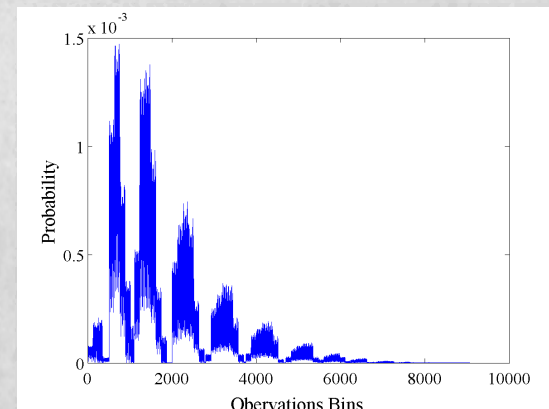
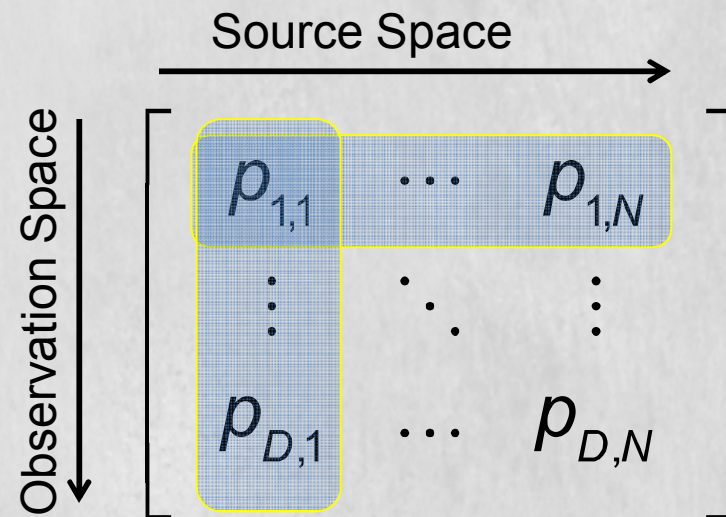
- The MLEM algorithm is used to estimate the true spatial distribution using the observed data
- The system matrix,  $P$ , maps the system response to the spatial distribution of a source

$$\begin{array}{c} \left( \begin{array}{c} \text{Observed data} \end{array} \right) \\ b \end{array} = \begin{array}{c} \left( \begin{array}{c} \text{System response} \\ \text{matrix} \\ \text{(observed data for} \\ \text{different source} \\ \text{locations)} \end{array} \right) \\ P \end{array} \begin{array}{c} \left( \begin{array}{c} \text{True spatial distribution} \end{array} \right) \\ x \end{array}$$

# MLEM

## System Matrix

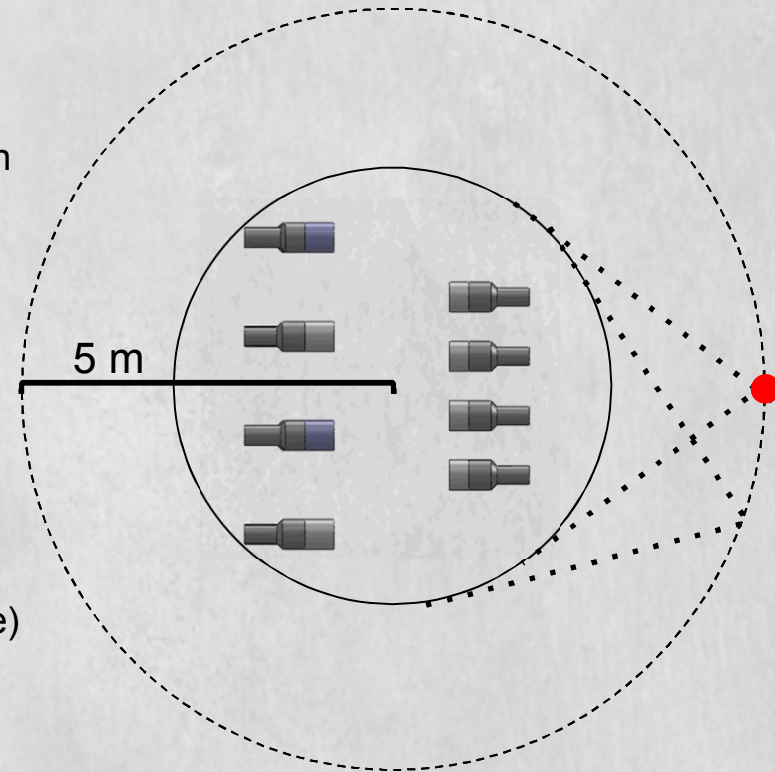
- $p_{d,n}$  is the probability that an emission from the  $n^{\text{th}}$  source position is recorded in the  $d^{\text{th}}$  observation bin
- Observation space can be binned by detector pair, reconstructed energy and reconstructed scattering angle
- Source space is binned by location (on an angular mesh), as well as by energy
- Energy bins along source space allow for reconstruction of emitted energy spectra at each location



# MLEM

## *System Matrix Creation*

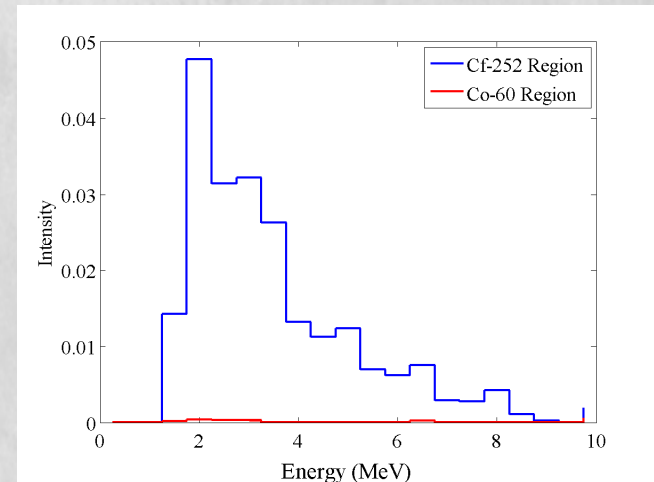
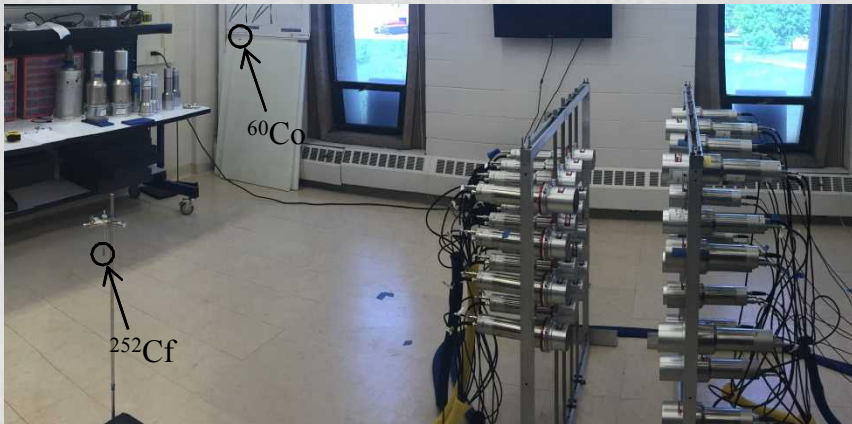
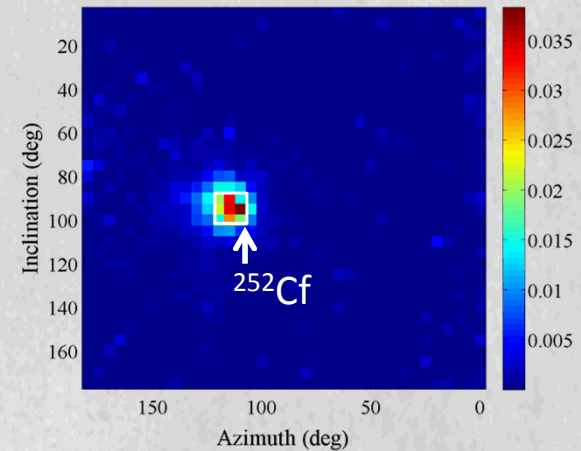
- System matrix calculated by simulating the response from a source in each spatial bin around the system
  - 5° bins are used in both the azimuthal and inclination (1295 locations for  $2\pi$  hemisphere)
  - Particles are emitted in a cone directed toward a sphere surrounding the system
- Neutrons
  - Source is distributed from 0-10 MeV
  - ~18 hours to simulate  $3 \times 10^8$  neutrons at each spatial bin
  - Typical system matrix size might be  $138,240 \times 51,800$  (when energy binning source space)
- Photons
  - Source is distributed from 0-5 MeV
  - ~15 hours to simulate  $3 \times 10^8$  photons at each spatial bin
  - Typical system matrix size might be  $207,360 \times 64,750$  (when energy binning source space)



# Spectrum Isolation

## Neutrons

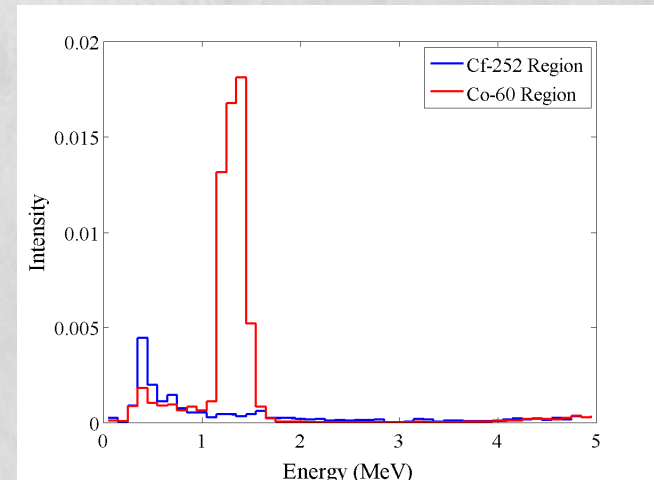
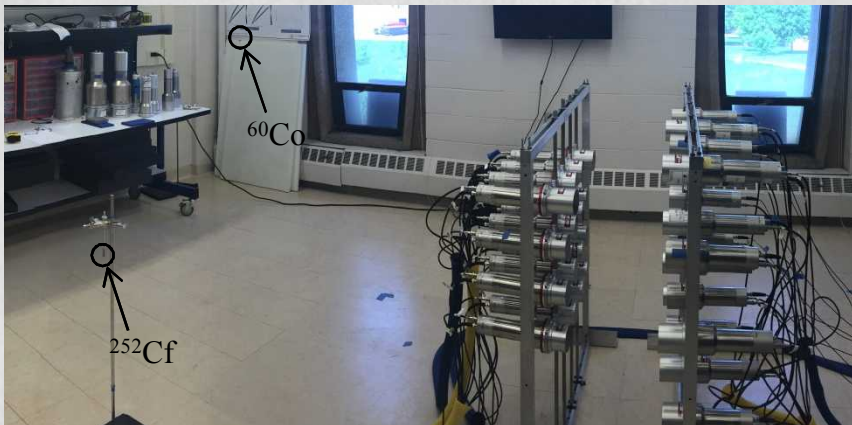
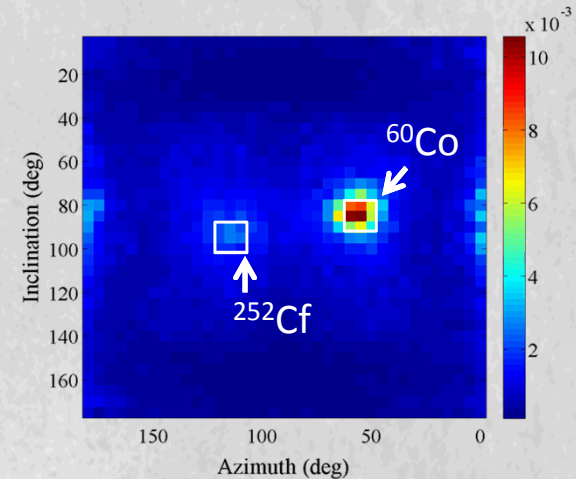
- 350-minute measurement of:
  - ~ $3.3 \times 10^4$  fissions per second  $^{252}\text{Cf}$  located 175 cm from the system at ( $114^\circ$ ,  $93^\circ$ )
  - ~68  $\mu\text{Ci}$   $^{60}\text{Co}$  source located 390 cm from the system at ( $58^\circ$ ,  $84^\circ$ )
- ~11,500 neutrons measured
- ~1,440,000 photons measured



# Spectrum Isolation

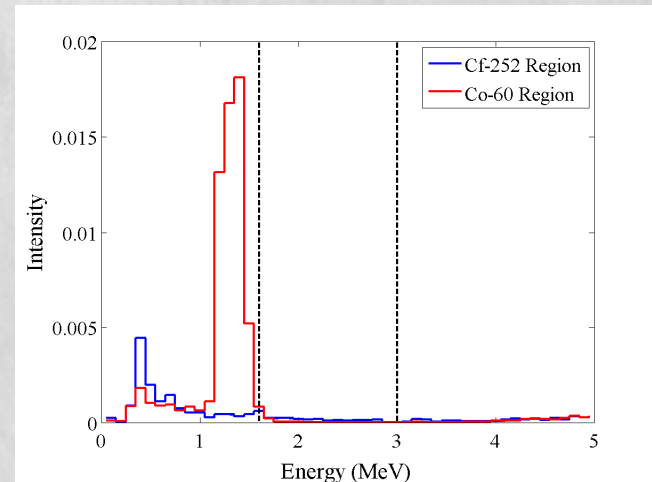
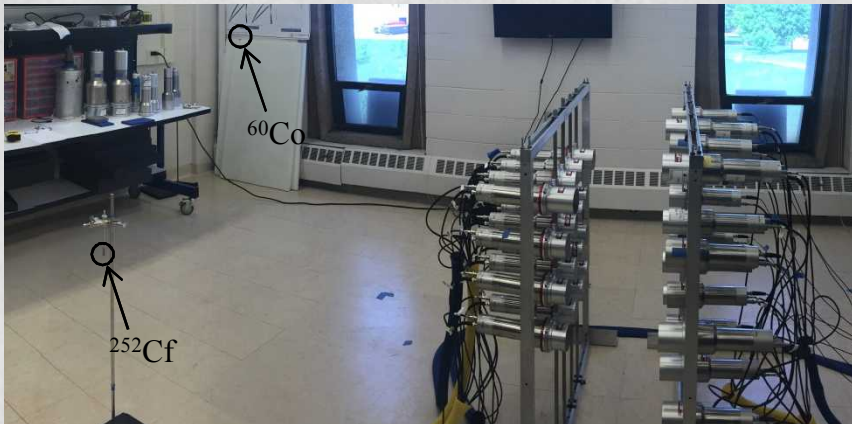
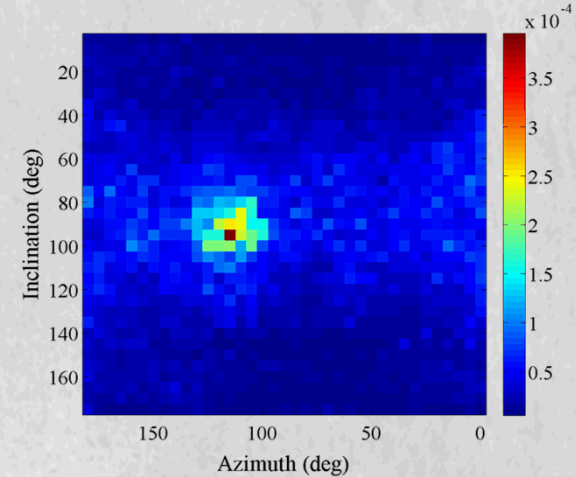
## Photons

- 350-minute measurement of:
  - ~ $3.3 \times 10^4$  fissions per second  $^{252}\text{Cf}$  located 175 cm from the system at ( $114^\circ$ ,  $93^\circ$ )
  - ~68  $\mu\text{Ci}$   $^{60}\text{Co}$  source located 390 cm from the system at ( $58^\circ$ ,  $84^\circ$ )
- ~11,500 neutrons measured
- ~1,440,000 photons measured



# Spectrum Isolation High-Energy Window

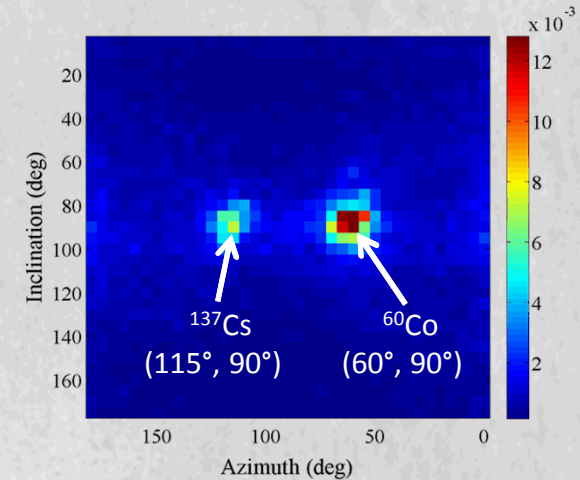
- 350-minute measurement of:
  - ~ $3.3 \times 10^4$  fissions per second  $^{252}\text{Cf}$  located 175 cm from the system at ( $114^\circ$ ,  $93^\circ$ )
  - ~68  $\mu\text{Ci}$   $^{60}\text{Co}$  source located 390 cm from the system at ( $58^\circ$ ,  $84^\circ$ )
- ~11,500 neutrons measured
- ~1,440,000 photons measured



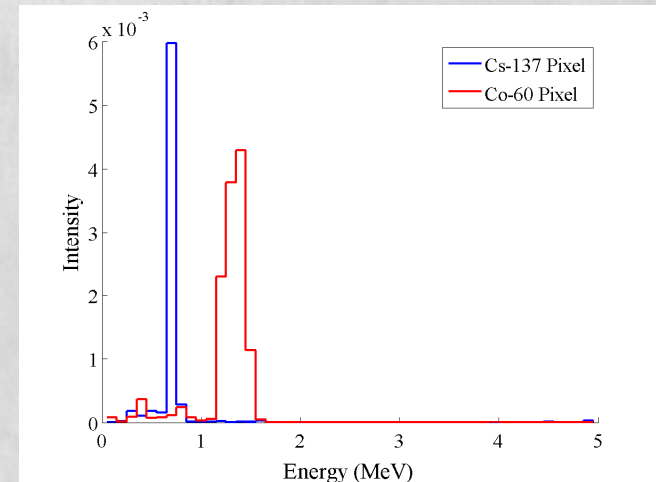
# Spectrum Isolation

## *Gamma-ray Check Sources*

- 15-minute measurement of:
  - ~89  $\mu\text{Ci}$   $^{137}\text{Cs}$  source located at  $(117^\circ, 90^\circ)$
  - ~68  $\mu\text{Ci}$   $^{60}\text{Co}$  source located at  $(61^\circ, 90^\circ)$
- 3.8-meter standoff for both sources
- ~58,000 photons measured

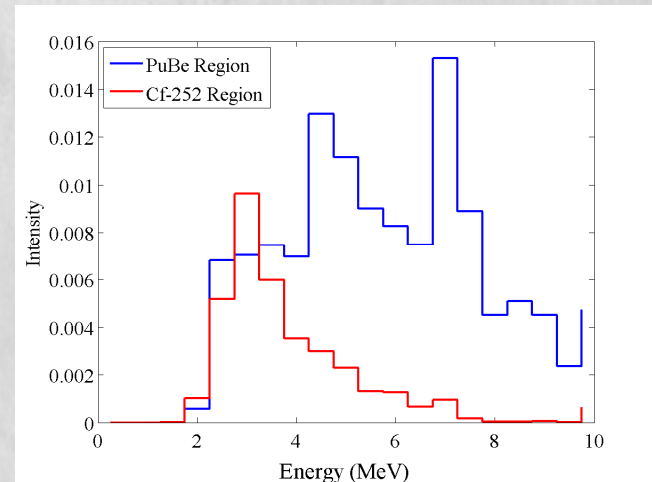
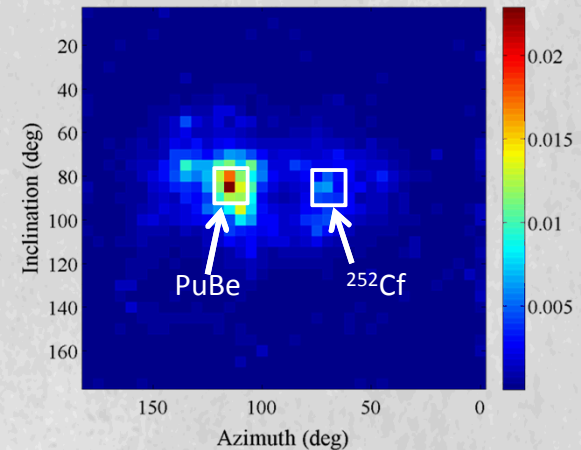
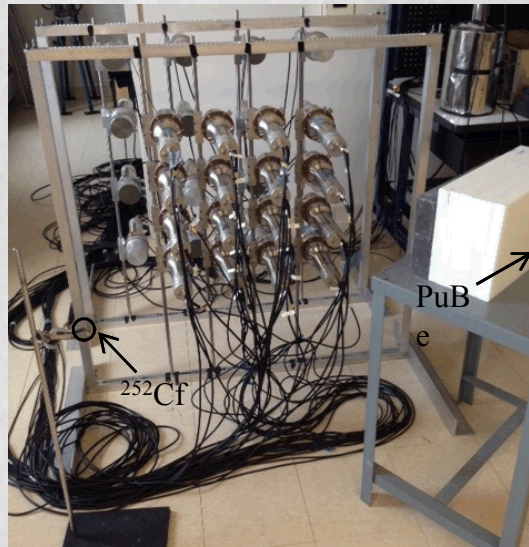


Add photo if possible



# Spectrum Isolation *Neutron Sources*

- 480-minute measurement of:
  - ~ $1.75 \times 10^6$  neutrons/second PuBe source shielded by 15.5 cm of poly and 5 cm of lead located at (120°, 98°)
  - ~ $1.35 \times 10^5$  neutrons/second  $^{252}\text{Cf}$  source unshielded located at (60°, 90°)
- 1-meter standoff for both sources
- ~103,000 neutrons measured



# Summary and Conclusions

- MLEM allows for reconstruction of of the energy spectrum at each spatial location
- The DPI was able to successfully locate photon and neutron sources and reasonably estimate their corresponding energy spectra
- Energy windowing can be used to improve localization and identification capabilities
- The DPI is a viable tool when locating and identifying multiple sources is important: hold-up measurements, cargo screening, warhead verification, etc.

# References

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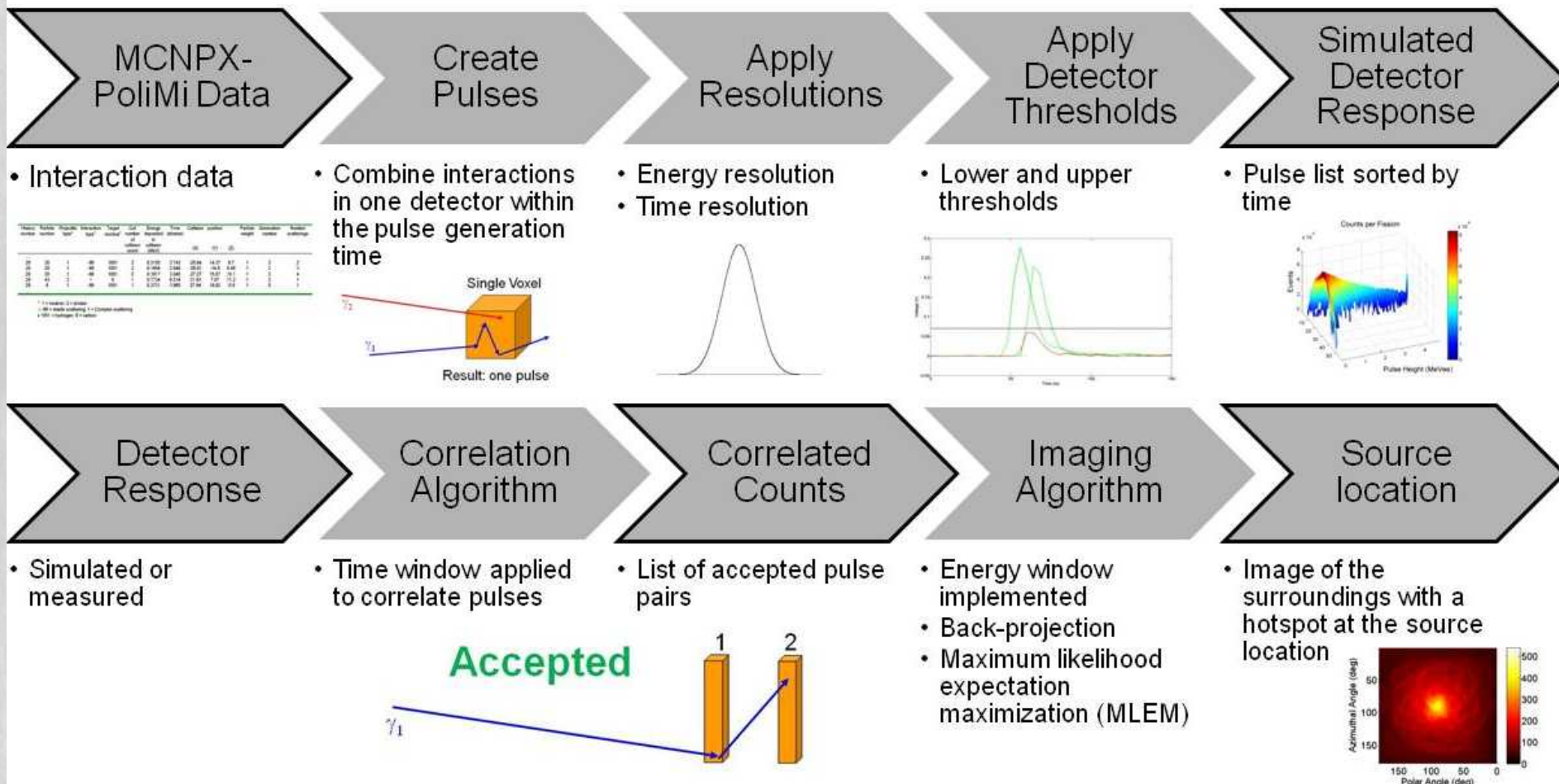
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# Data Analysis

## *MPPost*



# MLEM Algorithm

$$\hat{x}_s^{(k+1)} = \hat{x}_s^{(k)} \sum_{d=1}^D \left[ \frac{b_d}{\sum_{s'=1}^S P_{ds'} \hat{x}_{s'}^{(k)}} P_{ds} \right], s=1, \dots, S$$

Calculation performed at each iteration of the MLEM algorithm

$x$  – true source distribution

$\hat{x}$  – estimated spatial distribution

$b$  – Observed data vector

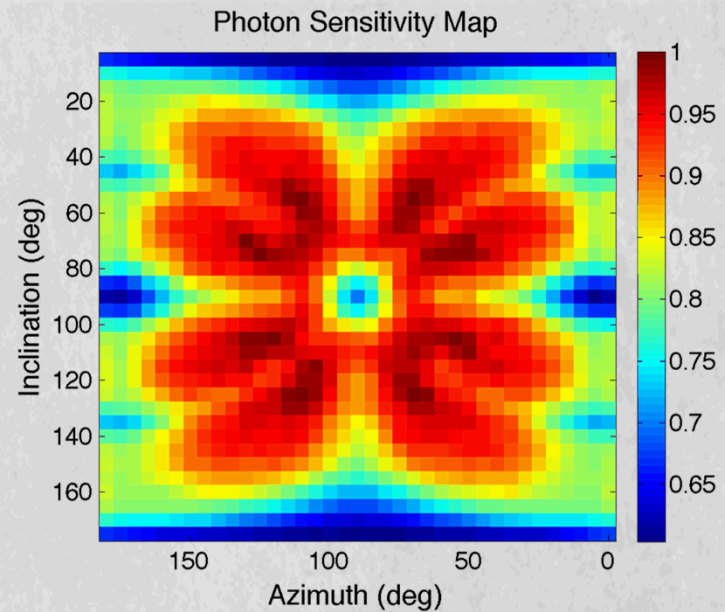
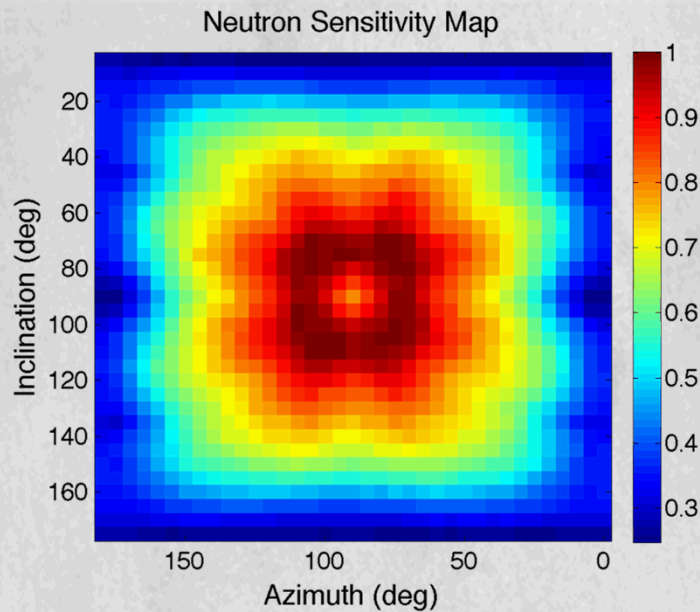
$P$  – System response matrix

$k$  – Iteration number

$D$  – Number of observation bins

$S$  – Number of spatial bins

# $^{252}\text{Cf}$ Sensitivity Maps



Relative sensitivity as a function of source location based on simulations of  $^{252}\text{Cf}$

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