

# Used Fuel Disposition Campaign

## Thermal-Mechanical Data for Argillite Disposal Systems: Beyond Standard Density Functional Theory

**Philippe F. Weck, Carlos F. Jove-Colon**  
**Sandia National Laboratories**

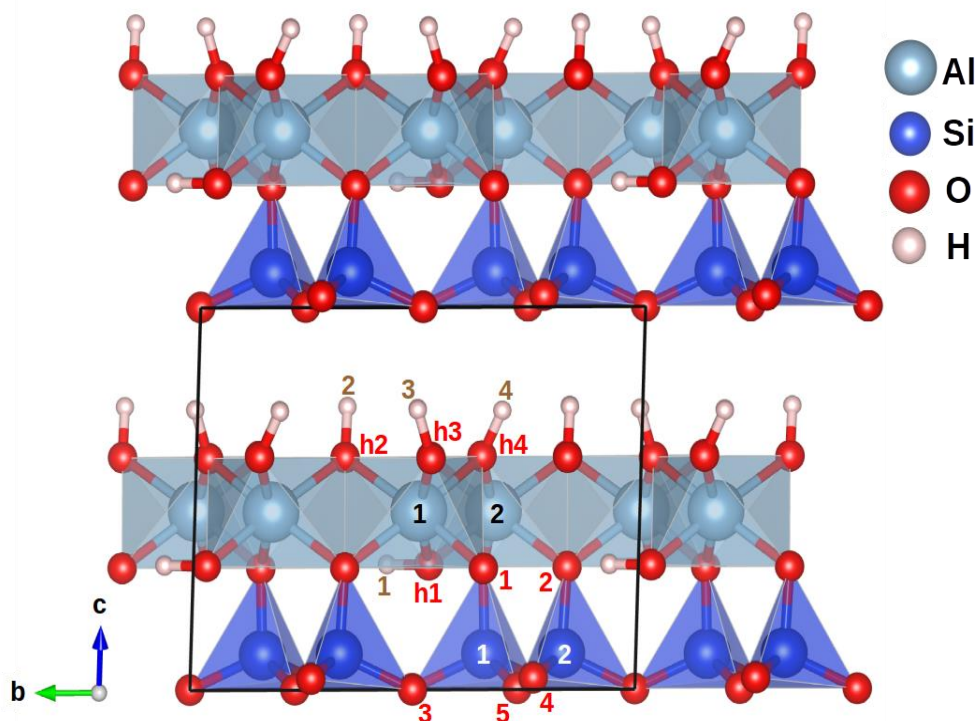
**Eunja Kim, University of Nevada Las Vegas**

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## Introduction, Objectives and Approach

- **Thermal-mechanical data for natural system (NS) minerals and engineered barrier systems (EBS) materials** are critical to assess their stability and behavior in geologic disposal environments for safety assessments.
- **Data Gaps and Research Needs:** NS minerals surrounding the waste package (e.g. clays, complex salts, granite...).
- **Objectives:** Using parameter-free first-principles methods to:
  - Calculate missing thermodynamic data needed for geochemical & SNF degradation models, as a **fast and systematic way to predict materials properties and to complement experiments**.
  - Provide an **independent assessment** of existing experimental thermodynamic data and resolve contradictions in existing calorimetric data.
  - Validate our computational approach using high-quality calorimetric data.
- **Approach**
  - Structural optimization using density functional theory (DFT) [VASP code].
  - Use density functional perturbation theory (DF-PT) to calculate the phonon properties of materials relaxed with DFT and derive their thermal properties.

# Structure of Kaolinite ( $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ )



*Layered crystal structure of kaolinite,  $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ , relaxed with DFT-D2. The unit cell is indicated by solid black lines.*

■ **Expt.:  $V = 328.708 \text{ \AA}^3$**

$a = 5.153 \text{ \AA}$ ,  $b = 8.942 \text{ \AA}$ ,  $c = 7.391 \text{ \AA}$   
 $\alpha = 91.93^\circ$ ,  $\beta = 105.05^\circ$ ,  $\gamma = 89.80^\circ$ .

■ **Standard DFT:  $V = 340.11 \text{ \AA}^3$**

$a = 5.21 \text{ \AA}$ ,  $b = 9.05 \text{ \AA}$ ,  $c = 7.48 \text{ \AA}$   
 $\alpha = 91.8^\circ$ ,  $\beta = 105.1^\circ$ ,  $\gamma = 89.7^\circ$ .

■ **DFT + van der Waals correction  
(DFT-D2):  $V = 329.03 \text{ \AA}^3$**

$a = 5.18 \text{ \AA}$ ,  $b = 8.99 \text{ \AA}$ ,  $c = 7.33 \text{ \AA}$   
 $\alpha = 91.6^\circ$ ,  $\beta = 105.1^\circ$ ,  $\gamma = 89.8^\circ$ .

**Volume calculated with DFT-D2 agrees with experiment within ca. 1%** (while standard DFT overestimates expt. by ca. 3.5 %).

Thermal evolution of the bulk modulus computed for single-crystal kaolinite with:

## 1. Birch-Murnaghan 3rd-order (BM3) equation of state (EOS):

$$P(V) = \frac{3K_0}{2} \left[ \left( \frac{V_0}{V} \right)^{\frac{7}{3}} - \left( \frac{V_0}{V} \right)^{\frac{5}{3}} \right] \left\{ 1 + \frac{3}{4} (K'_0 - 4) \left[ \left( \frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right] \right\},$$

where  $P$  is the pressure,  $V_0$  is the reference volume,  $V$  is the deformed volume, and

$$K_0(T) = -V \left( \frac{\partial P}{\partial V} \right)_{P=0} \quad \text{and} \quad K'_0(T) = \left( \frac{\partial K}{\partial P} \right)_{P=0}.$$

## 2. Universal Vinet EOS:

$$P(V) = 3K_0 \frac{(1-x)}{x^2} \exp \left[ \frac{3}{2} (K'_0 - 1)(1 - x) \right],$$

$$\text{where } x = \left( \frac{V}{V_0} \right)^{\frac{1}{3}}.$$

Elastic properties and bulk modulus computed for polycrystalline kaolinite:

Elastic constants ( $C_{ij}$ ) calculated with DFPT as the second derivatives of the energy with respect to the strain:

$$C_{ij} = \frac{1}{V} \left( \frac{\partial^2 U}{\partial \varepsilon_i \partial \varepsilon_j} \right) \rightarrow \text{elastic compliances } (S_{ij}) \text{ obtained by } S = C^{-1}$$

with volume  $V$ , total energy  $U$  of the system, and infinitesimal displacement  $\varepsilon$ .

**1. Voigt approximation:** Fixed strain and average over stress → *upper limit*

**Bulk modulus:**  $K_V = \frac{C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})}{9}$

**Shear modulus:**  $G_V = \frac{C_{11} + C_{22} + C_{33} - C_{12} - C_{13} - C_{23} + 3(C_{44} + C_{55} + C_{66})}{15}$

**2. Reuss approximation:** Fixed stress and average over strain → *lower limit*

**Bulk modulus:**  $K_R = [S_{11} + S_{22} + S_{33} + 2(S_{12} + S_{13} + S_{23})]^{-1}$

**Shear modulus:**  $G_R = \frac{15}{4(S_{11} + S_{22} + S_{33} - S_{12} - S_{13} - S_{23}) + 3(S_{44} + S_{55} + S_{66})}$

**3. Hill approximation:** Average of Voigt and Reuss values

# Thermal-Mechanical Properties of Kaolinite ( $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ )

$C_{ij}$	DFT	DFT-D2	Experiments
$C_{11}$	187.20	175.16	171.51 <sup>a</sup> 48.1 <sup>b</sup> 79.3 <sup>b</sup> 121.1 <sup>b</sup> 126.4 <sup>c</sup>
$C_{22}$	180.56	168.65	
$C_{33}$	88.02	133.99	52.62 <sup>a</sup> 45.2 <sup>b</sup> 72.5 <sup>b</sup> 112.5 <sup>b</sup> 57.8 <sup>c</sup>
$C_{44}$	9.63	10.07	14.76 <sup>a</sup> 16.7 <sup>b</sup> 25.6 <sup>b</sup> 41.1 <sup>b</sup> 31.6 <sup>c</sup>
$C_{55}$	12.36	12.78	
$C_{66}$	62.10	62.30	66.31 <sup>a</sup> 16.9 <sup>b</sup> 26.3 <sup>b</sup> 41.3 <sup>b</sup> 53.6 <sup>c</sup>
$C_{12}$	66.42	54.10	
$C_{13}$	15.63	28.58	27.11 <sup>a</sup> 12.9 <sup>b</sup> 24.1 <sup>b</sup> 34.8 <sup>b</sup> 8.5 <sup>c</sup>
$C_{14}$	-0.74	-1.90	
$C_{15}$	1.18	-0.79	
$C_{16}$	-6.14	-5.79	
$C_{23}$	16.00	28.46	
$C_{24}$	-0.30	-2.70	
$C_{25}$	-0.04	-1.42	
$C_{26}$	0.58	0.96	
$C_{34}$	-0.96	-3.57	
$C_{35}$	-0.56	-2.44	
$C_{36}$	0.37	0.71	
$C_{45}$	-0.45	-0.84	
$C_{46}$	-1.20	-1.78	
$C_{56}$	-0.02	-0.13	

## Elastic constants of kaolinite:

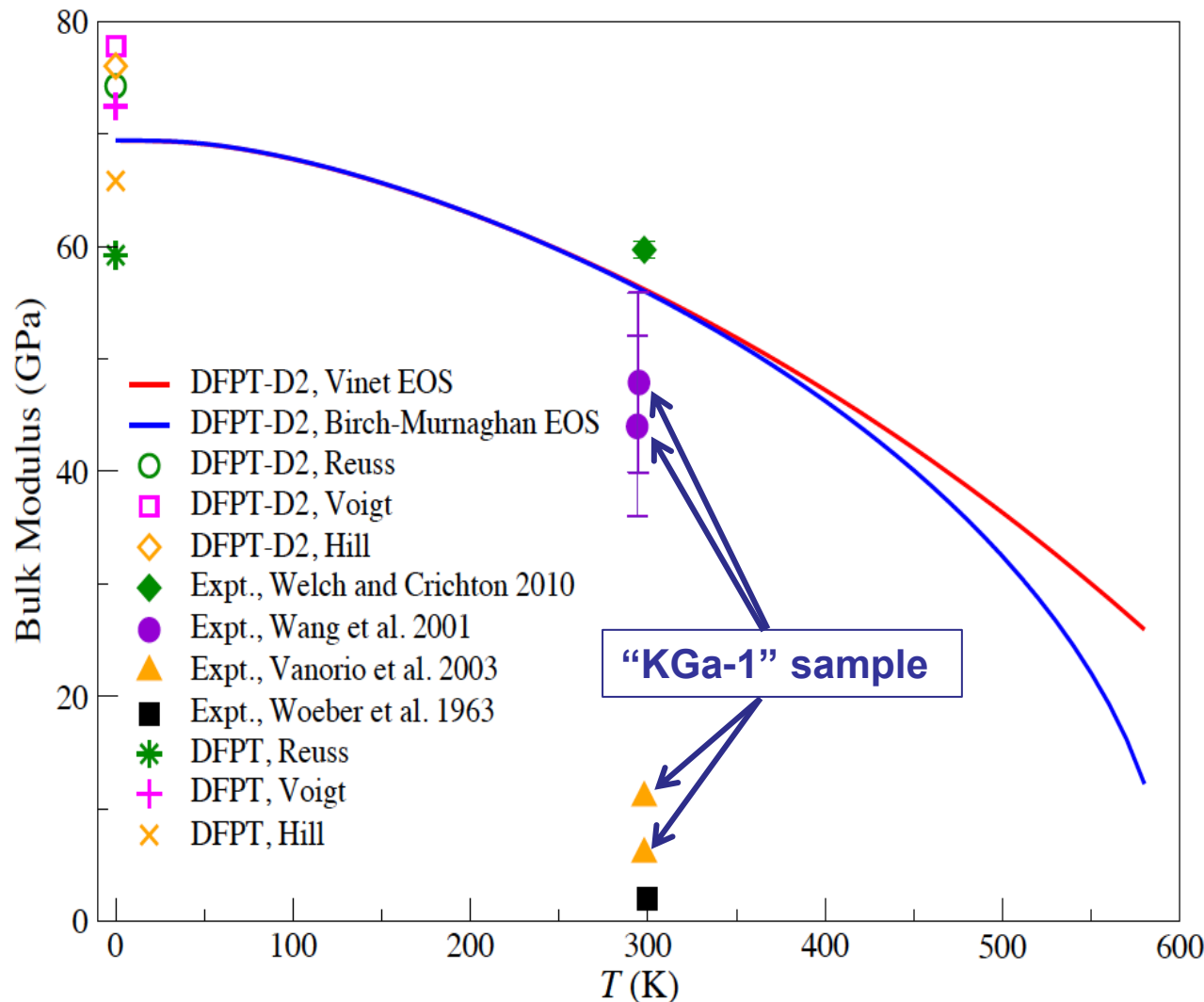
- Large variability of experimental data due to different samples crystallinity, water and impurity content, measurement techniques,...
- First-principles calculations can help to assess the accuracy of some data sets and predict missing data.
- Overall good agreement between predicted and measured elastic constants.

<sup>a</sup> Katahara, 1996.

<sup>b</sup> Lonardelli *et al.*, 2007.

<sup>c</sup> Wenk *et al.*, 2008.

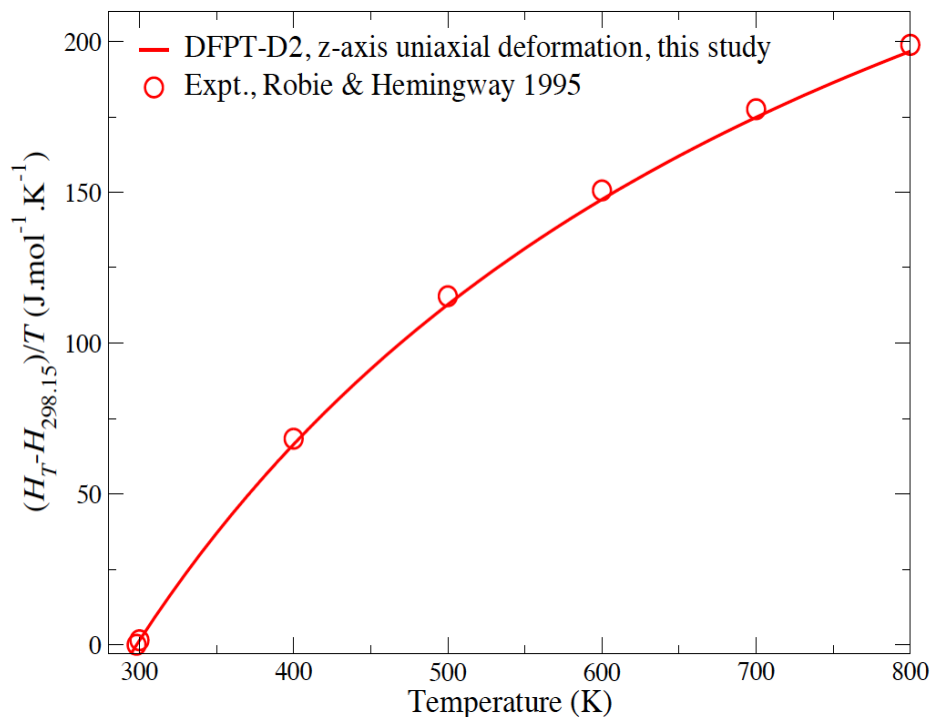
# Thermal-Mechanical Properties of Kaolinite ( $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ )



## Thermal evolution of the bulk modulus of kaolinite:

- Large variability of experimental bulk modulus data using the high-crystallinity “KGa-1” Georgia kaolinite sample.
- A significant bulk modulus softening is predicted from first-principles in the 0-600K range.
- Differences in EOSs above ~300 K.

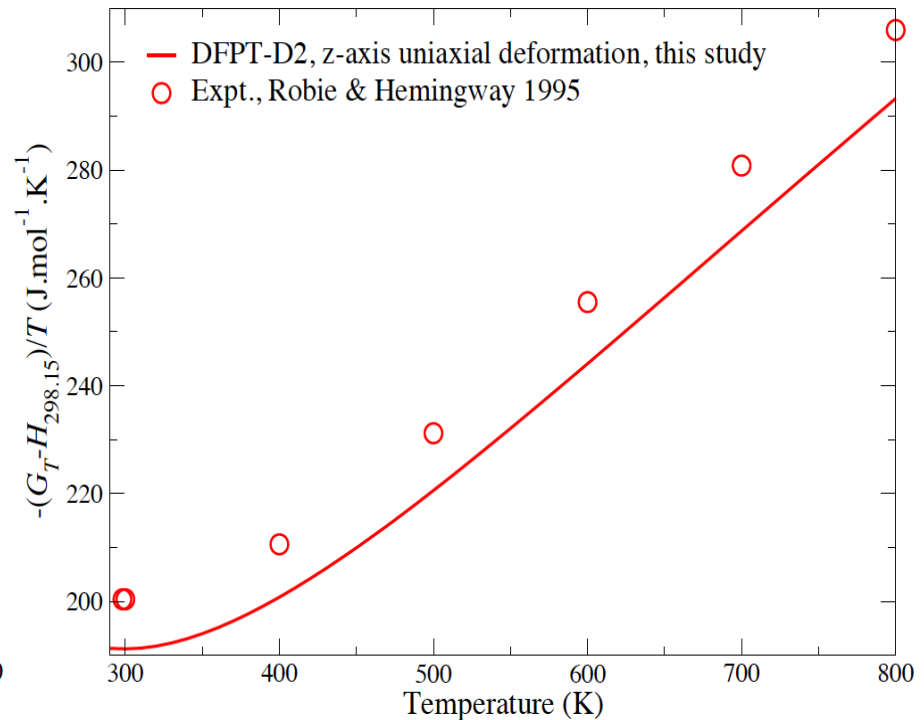
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**Enthalpy function of kaolinite**

$$(H_T - H_{298.15}).T^{-1} = \int_{298.15}^T C_P dT$$

*Differences of 2.0–2.5% in the 298–600 K range, and only 1% at 800 K.*



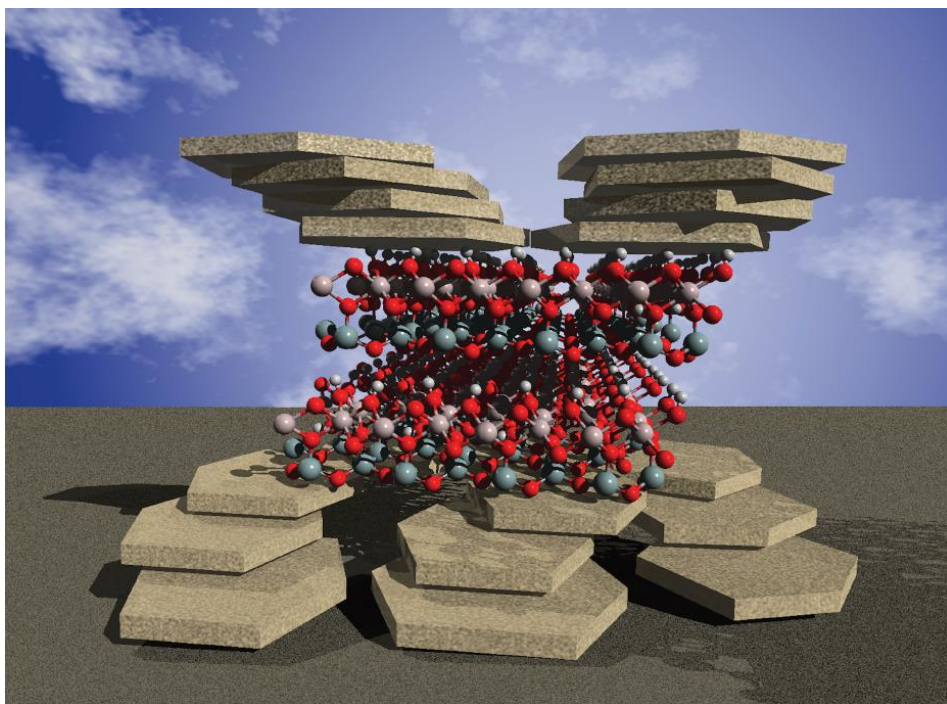
**Gibbs energy function of kaolinite**

$$-(G_T - H_{298.15}).T^{-1} = S_T - (H_T - H_{298.15}).T^{-1}$$

*Differences of 4.1–4.6% in the 298–800 K range.*

## Paper selected as Cover Page of *Dalton Transactions* (July 2015):

Weck P.F., Kim E., Jove-Colon C.F., "*Relationship Between Crystal Structure and Thermo-Mechanical Properties of Kaolinite Clay: Beyond Standard Density Functional Theory*", *Dalton Transactions*, in press (2015); DOI: 10.1039/C5DT00590F



## FY16 outlook:

- Testing the present theoretical approach using more complex clays, such as Na/Ca-montmorillonite.
- Extend structural and thermal-mechanical calculations within the framework of DFT/DFPT to other NS minerals (clays, salts, granite...) and EBS materials.