

# What is an Epsilon-Near-Zero mode?

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**Igal Brener, Salvatore Campione**



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## Surface Plasmons in Thin Films

E. N. ECONOMOU\*†

*The James Franck Institute and Department of Physics, The University of Chicago, Chicago, Illinois 60637*

(Received 15 January 1969)

Economou, 1969

Burke et al, 1986

etc

“Thin” here:  $\sim 20\text{nm}$  for  
 $\sim 400\text{nm}$  plasma  
wavelength

$\sim$  Skin depth

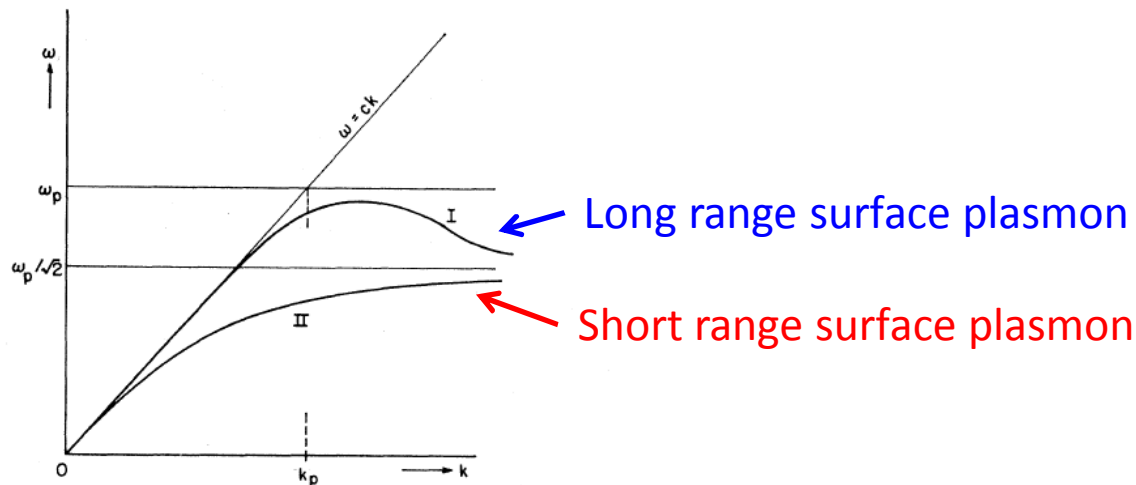
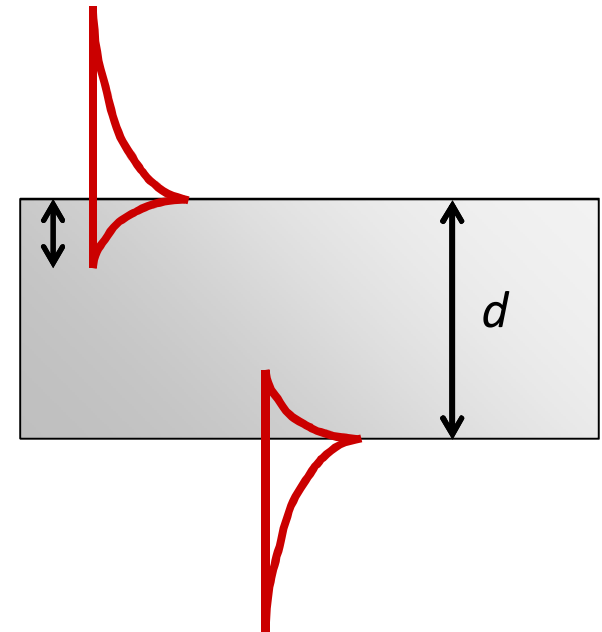
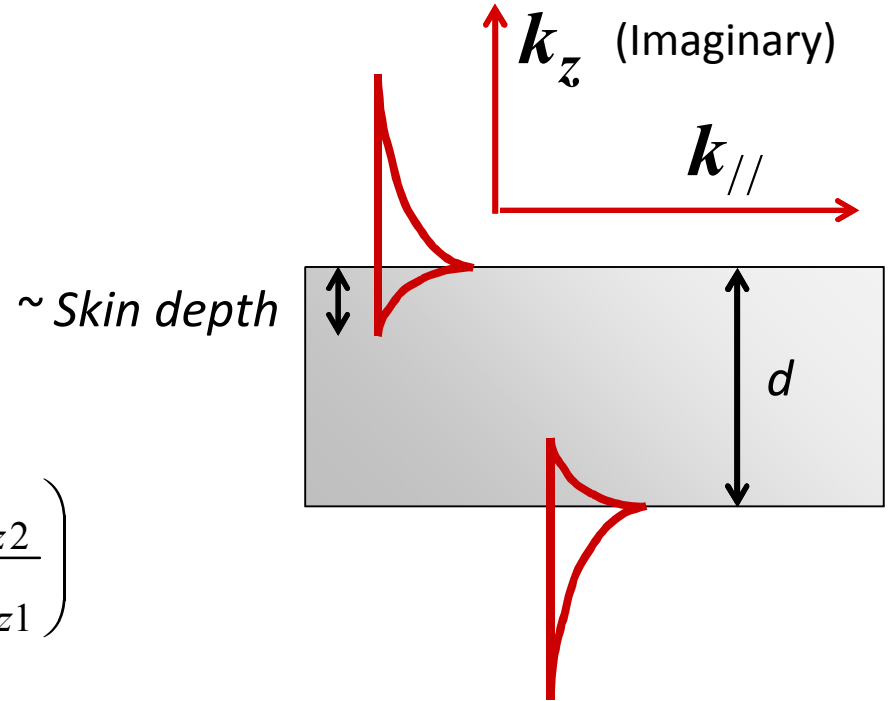


FIG. 4. Geometry and the dispersion relations for SPO of a metal film between two semi-infinite insulators ( $\epsilon_m = 1 - \omega_p^2/\omega^2$ ,  $\epsilon_i = 1$ ). The analytical expressions for  $k \gg k_p$  or  $k \ll k_p$  for the curves shown schematically here are (3.23b) and (3.18).

**What happens when the layer becomes  
much thinner?  
( $\ll$  skin depth)**

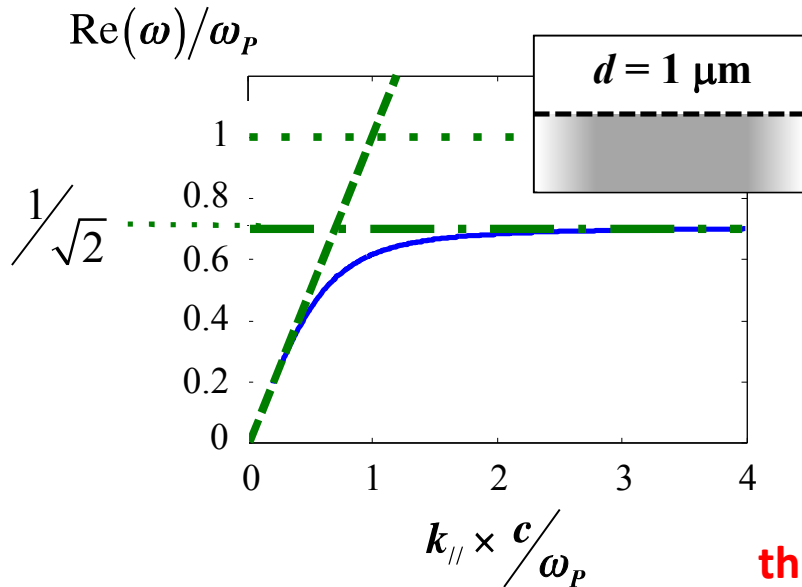
# Dispersion relations

$$1 + \frac{\varepsilon_1 k_{z3}}{\varepsilon_3 k_{z1}} = i \tan(k_{z2} d) \left( \frac{\varepsilon_2 k_{z3}}{\varepsilon_3 k_{z2}} + \frac{\varepsilon_1 k_{z2}}{\varepsilon_2 k_{z1}} \right)$$

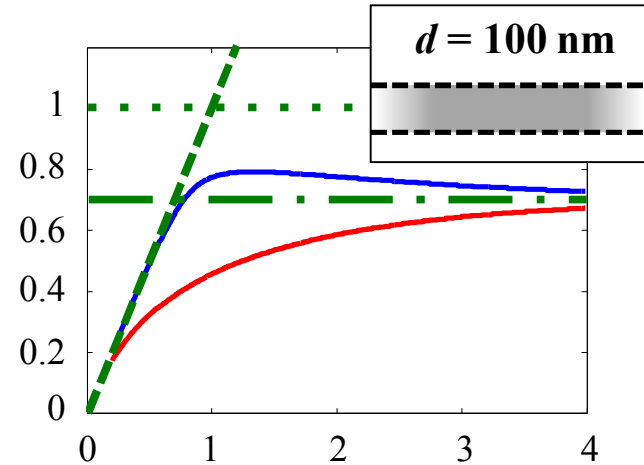


# Dispersion relations

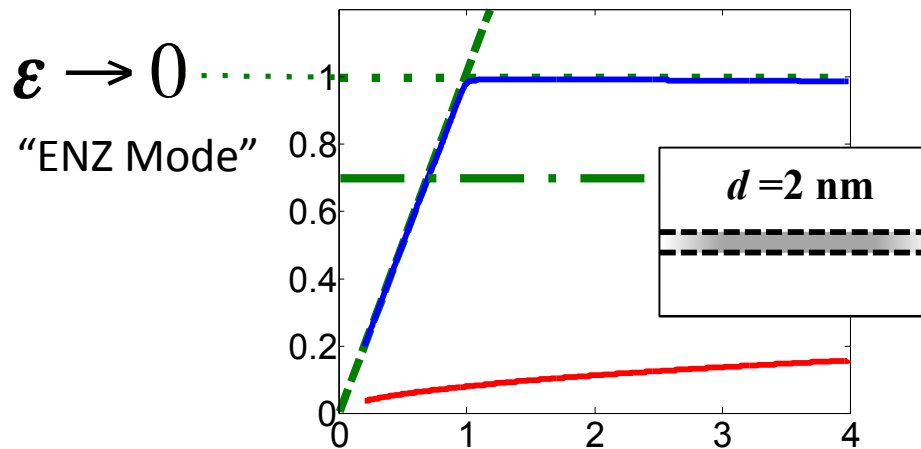
thickness  $\gg$  skin depth



thickness  $\sim$  skin depth



thickness  $\ll$  skin depth

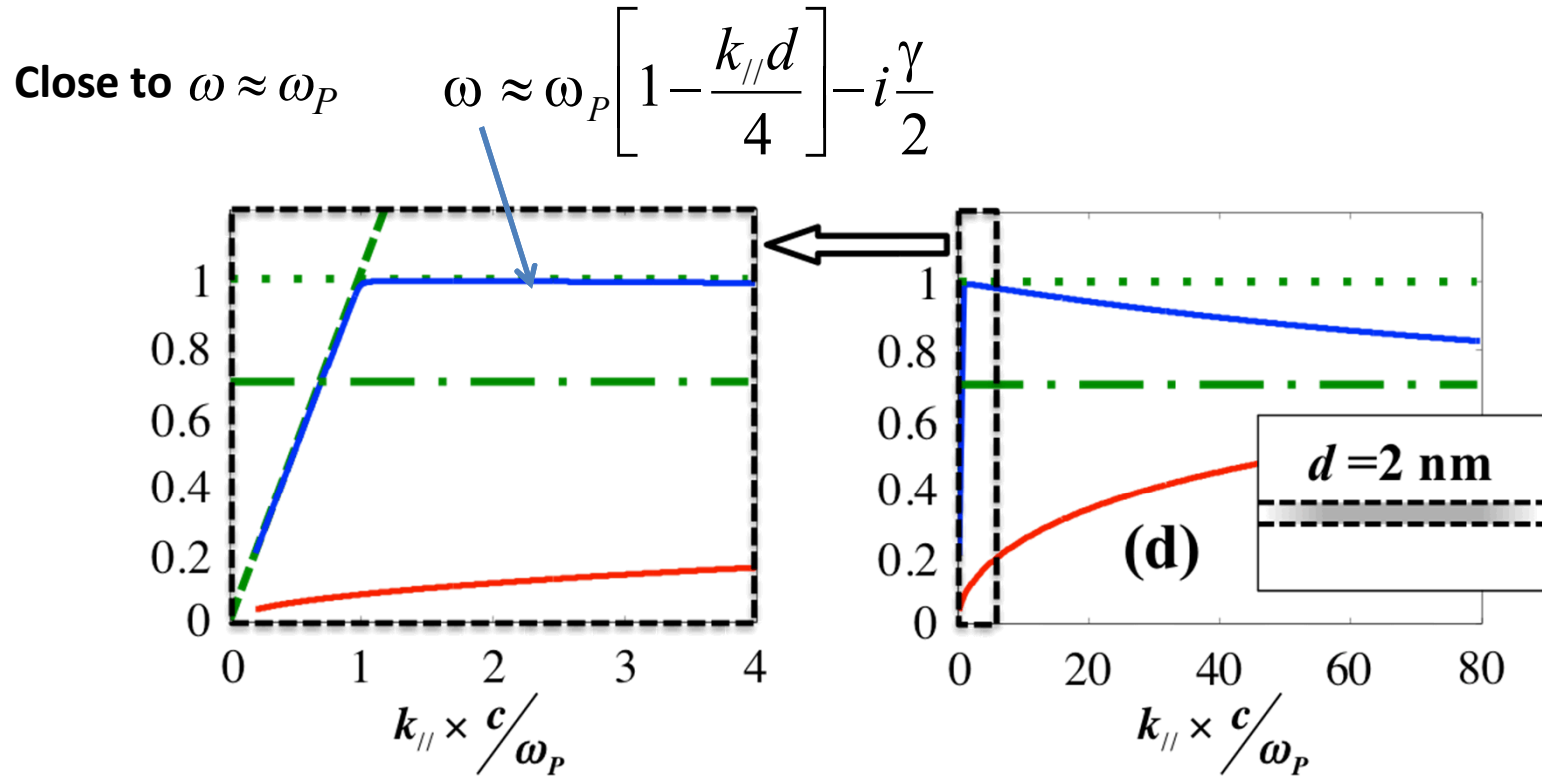


Flat dispersion?

1. Vassant, Marquier, Greffet et al., Phys. Rev. Lett. **109**, 237401 (2012)
2. Vassant, Marquier, Greffet et al., Opt. Express **20**, 23971 (2012)
3. Campione, Brener, Marquier, Phys. Rev. B Rapid Commun. **91**, 121408 (2015)

# ENZ mode dispersion

Flat?...



The ENZ mode dispersion is a part of the long-range surface plasmon dispersion that reaches the plasma frequency, where the metal dielectric constant vanishes.

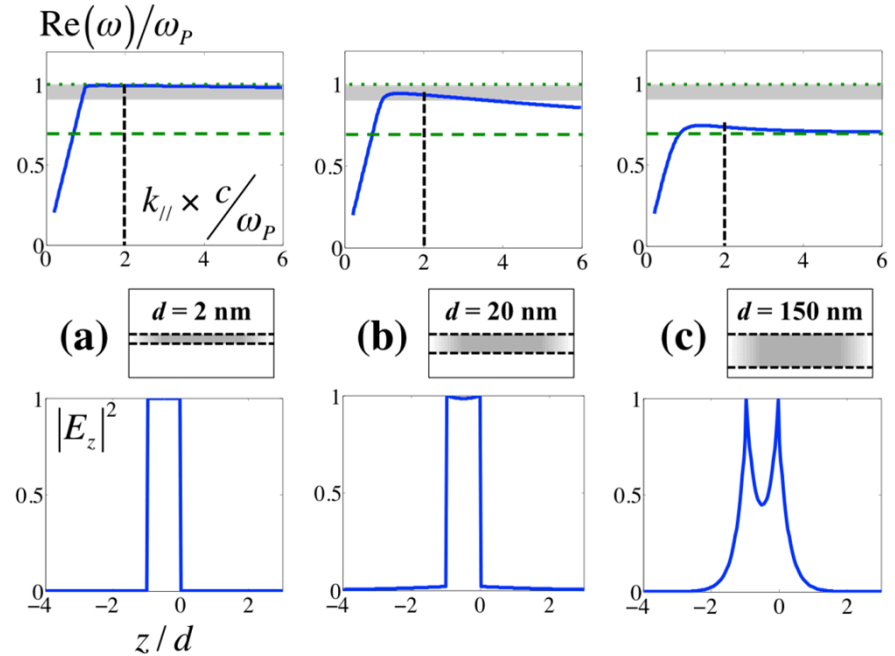
Campione, Brener,  
Marquier, Phys. Rev. B  
Rapid Commun. **91**,  
121408 (2015)

# ENZ Modes: $E_z$ is Constant and Large

$$\epsilon_1 E_{z1} = \epsilon_2 E_{z2}$$

$$\frac{\epsilon_1}{\epsilon_2} E_{z1} = E_{z2}$$

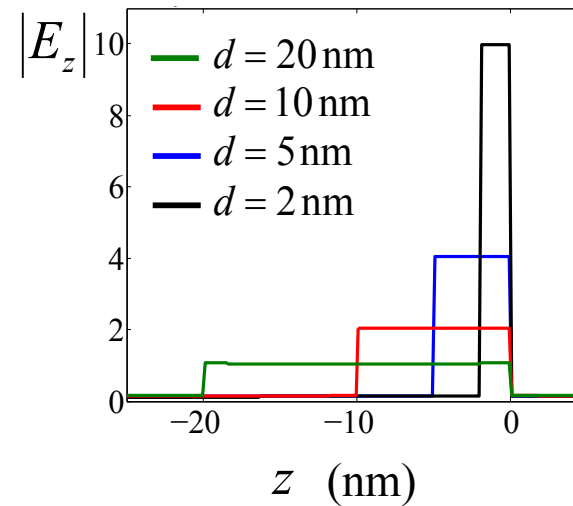
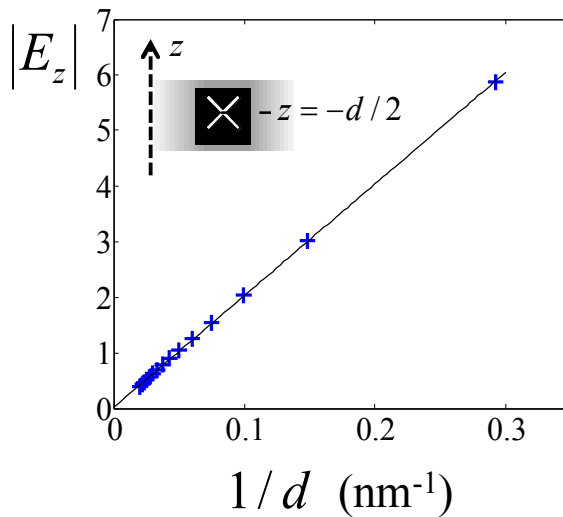
$\sim 0 \rightarrow$



Campione, Brener,  
Marquier, Phys. Rev. B  
Rapid Commun. **91**,  
121408 (2015)

# ENZ Modes: $E_z$ is Constant and Large

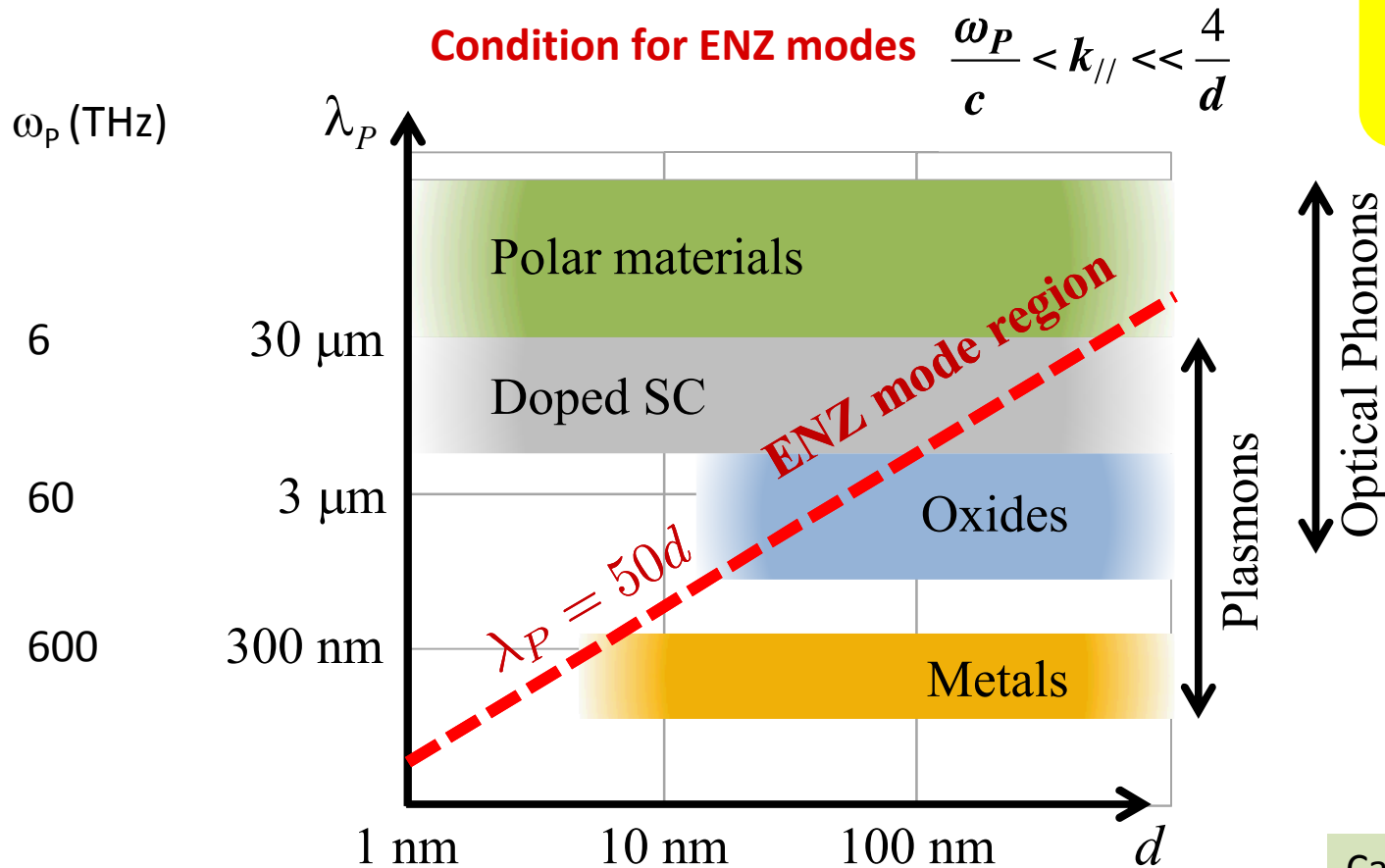
Field normalized to its value for  $d = 20\text{nm}$



$$E_z \propto \frac{1}{d}$$

Campione, Brener,  
Marquier, Phys. Rev. B  
Rapid Commun. **91**,  
121408 (2015)

# Where Can We Find ENZ Modes?



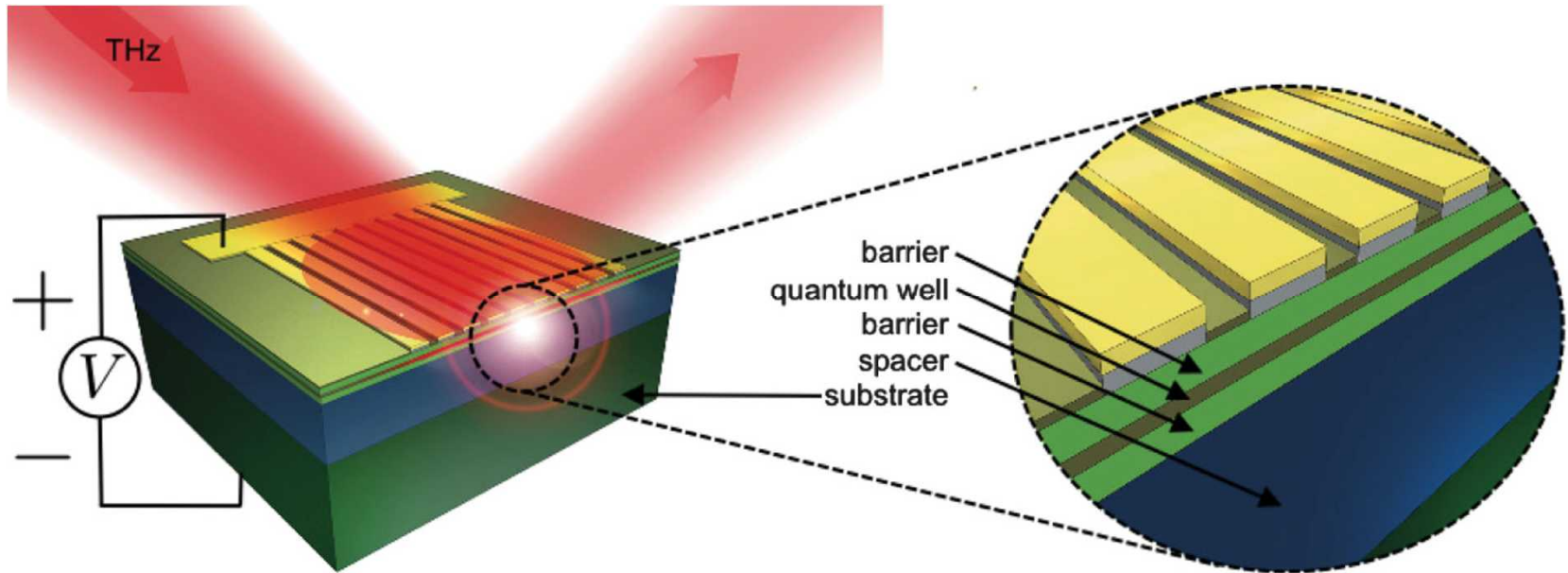
**Rule of Thumb:**

$$d < \approx \frac{\lambda_P}{50}$$

Campione, Brener,  
Marquier, Phys. Rev. B  
Rapid Commun. **91**,  
121408 (2015)

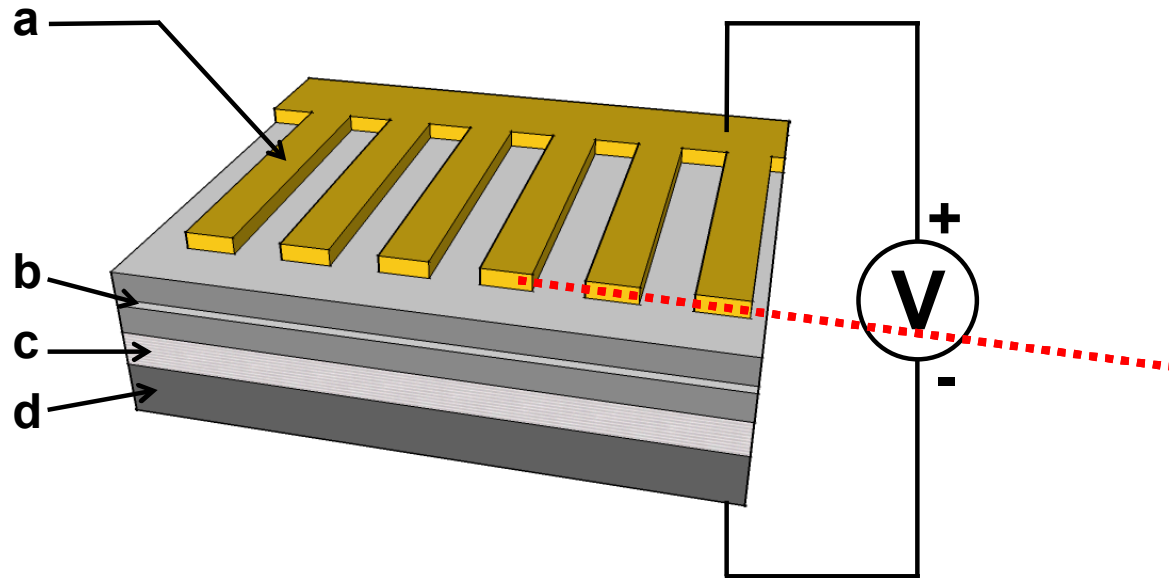


# Electrical control of the absorption



Vassant, Phys. Rev. Lett., **109**, 237401 (2012)

# Electrical control of the absorption



$$\epsilon = \begin{pmatrix} \epsilon_{//} & 0 & 0 \\ 0 & \epsilon_{//} & 0 \\ 0 & 0 & \epsilon_z \end{pmatrix}$$

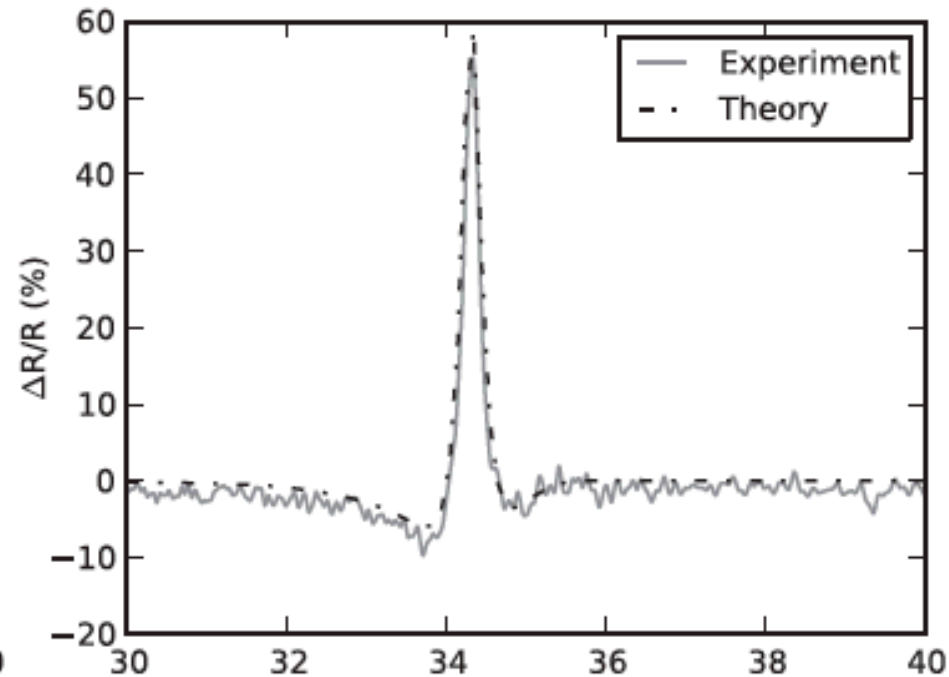
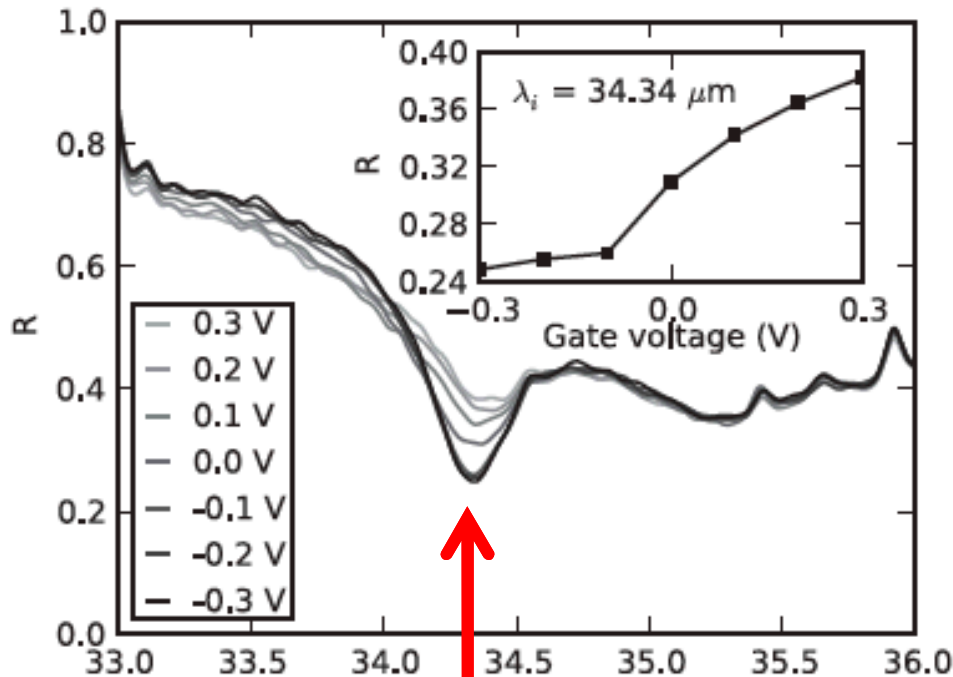
$$\epsilon_{//} = \epsilon_{\text{GaAs}} - \frac{\omega_P^2}{\omega^2 + i\gamma\omega}$$

$$\epsilon_z = \epsilon_{\text{GaAs}} - \sum_{n,n'} \frac{f_{nn'} \omega_P'^2}{\omega^2 - \omega_{nn'}^2 + i\gamma_{\text{isb}}\omega}$$

$\approx 0$

Vassant, Phys. Rev. Lett., **109**, 237401 (2012)

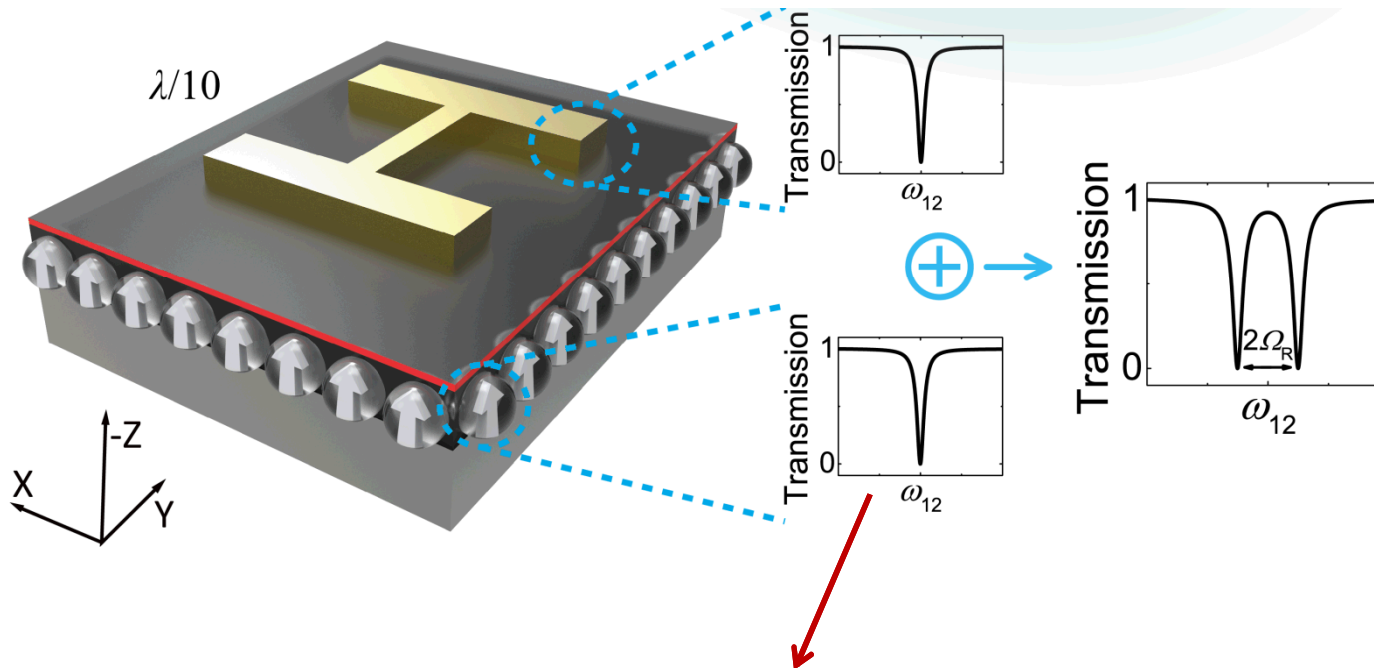
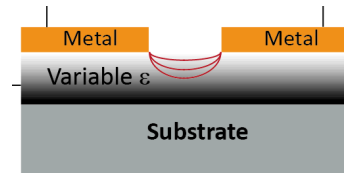
# Electrical control of the absorption



Wavelength ( $\mu\text{m}$ )

# What Can We Do With ENZ Modes: Coupling to Planar Metamaterials

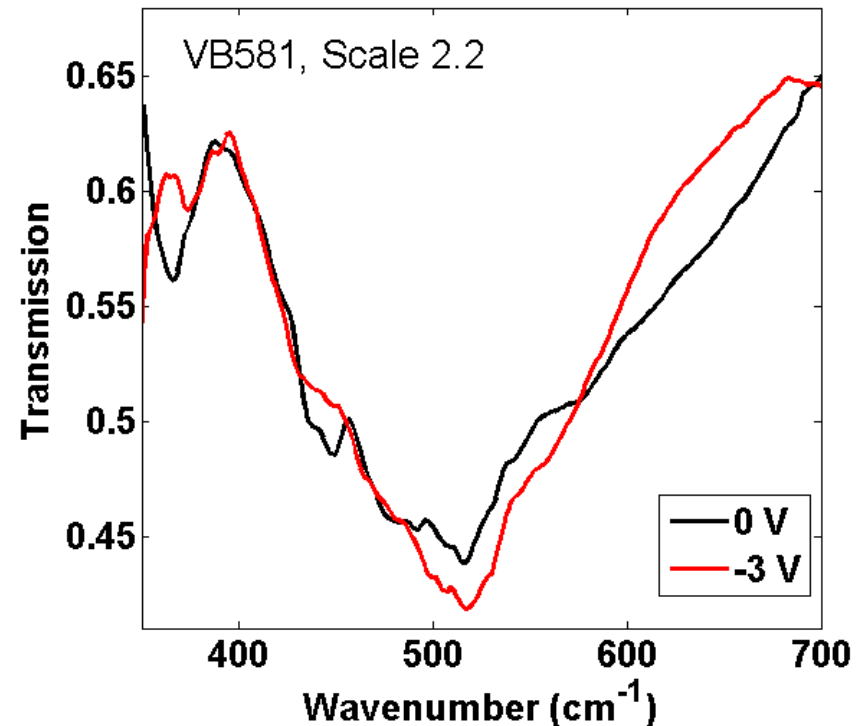
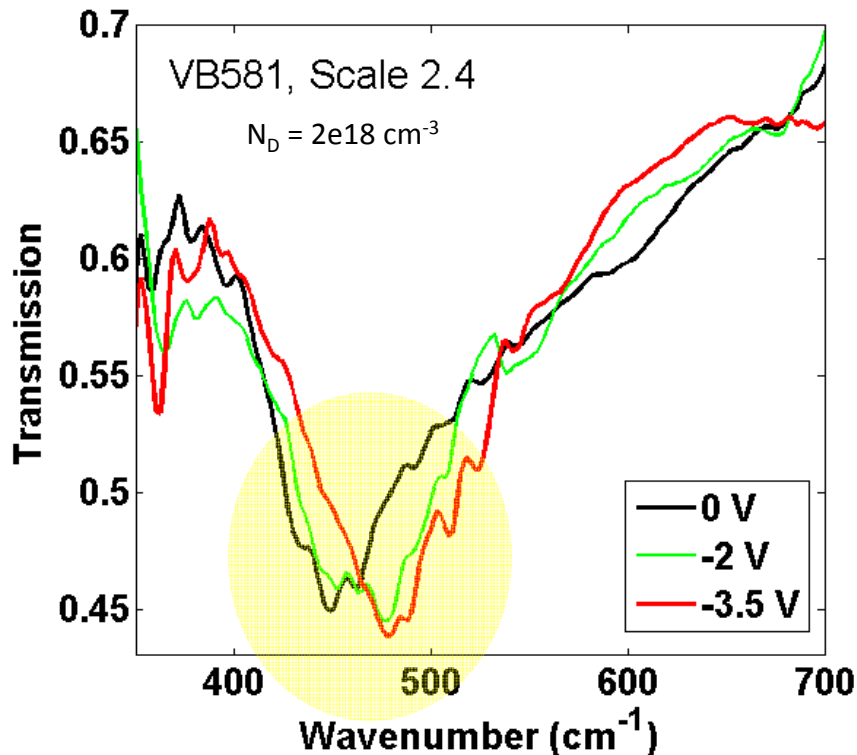
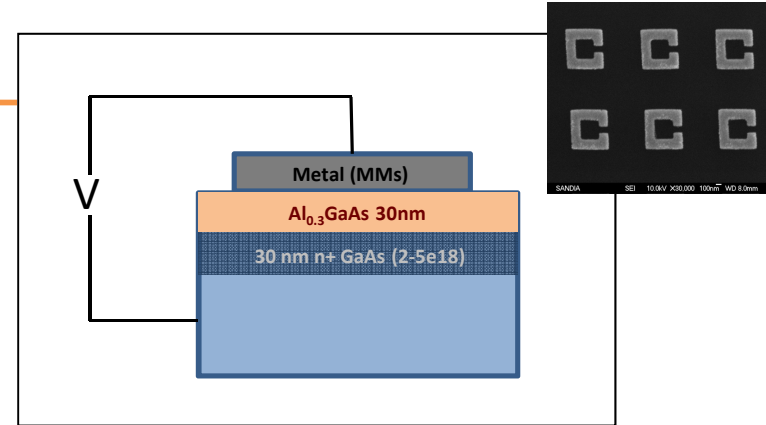
MM resonators create strong optical fields that lead to strong coupling



**Optical Phonons:** Nano Letters 11, 2104 (2011)  
**Intersubband Transitions:** Nature Communications 4, (2013)  
**Epsilon Near Zero modes:** Nano Letters 13, 5391 (2013)

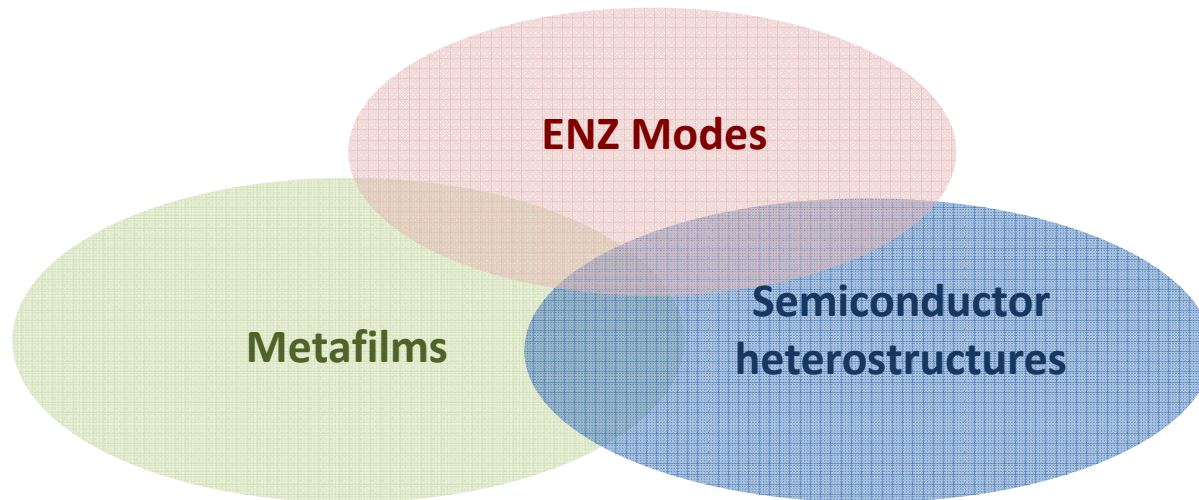
# Electrically Tuning the Coupling to the ENZ Mode

Fundamentally different than tuning just by changing a local permittivity!  
Removal of carriers  $\rightarrow$  removal of ENZ mode



“Epsilon-Near-Zero” mode:

- Transverse surface mode. Close to the plasma frequency (or longitudinal phonon...)
- Linear, almost flat, dispersion relation
- Large electric field: opportunity for enhancement of light-matter interactions



Metamaterial resonators + semiconductor heterostructures + ENZ modes : platform for tunable spectral behavior and variable coupling, enhanced nonlinearities etc.

# Acknowledgements



Igal Brener



Salvatore Campione



Young Chul Jun



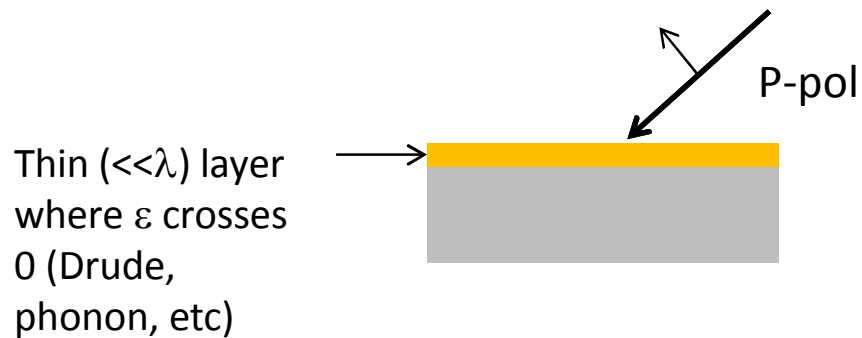
Jean-Jacques Greffet



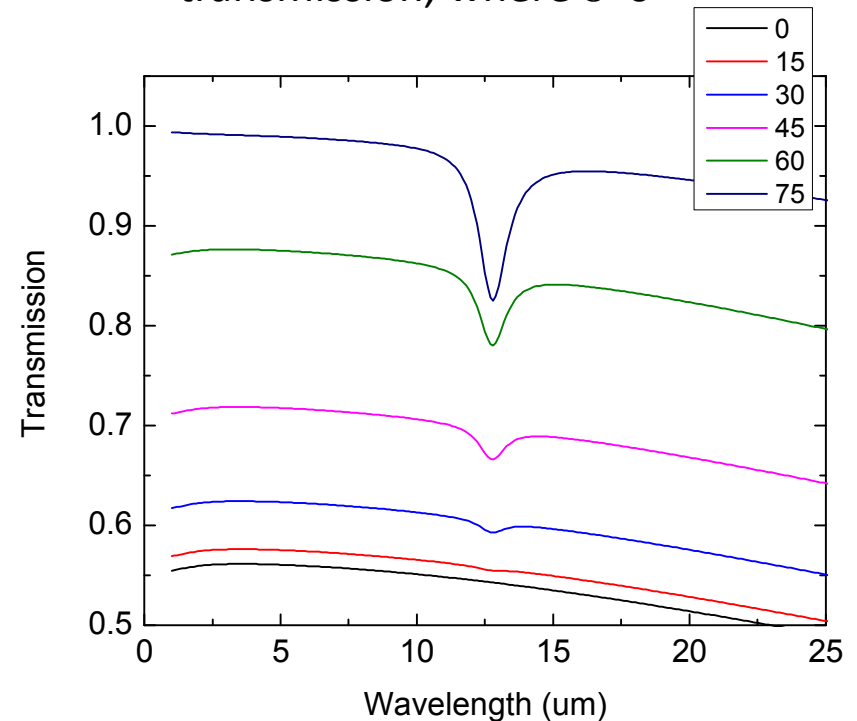
Simon Vassant



# Coupling to Berreman Modes From Free Space



Transmission vs angle (p-pol):  
A sharp dip is observed in  
transmission, where  $\epsilon \sim 0$

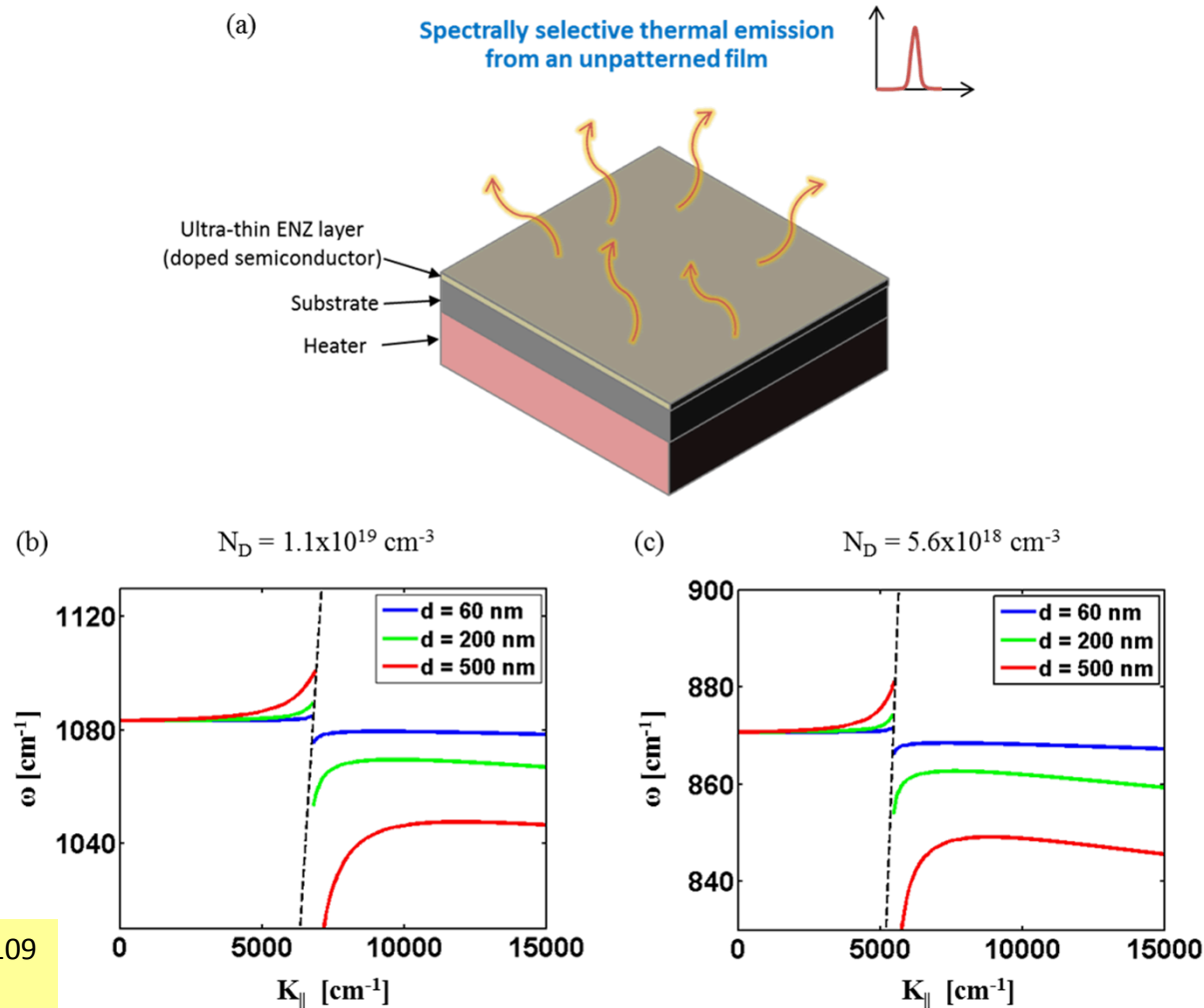


("Berreman" dip)



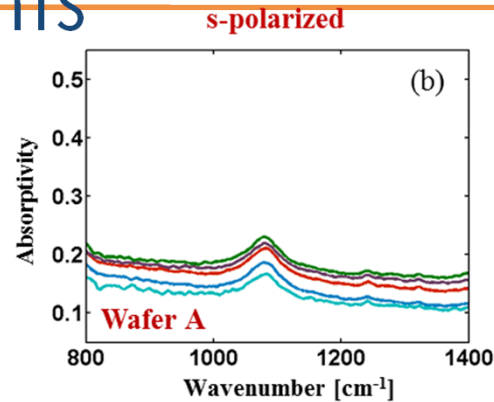
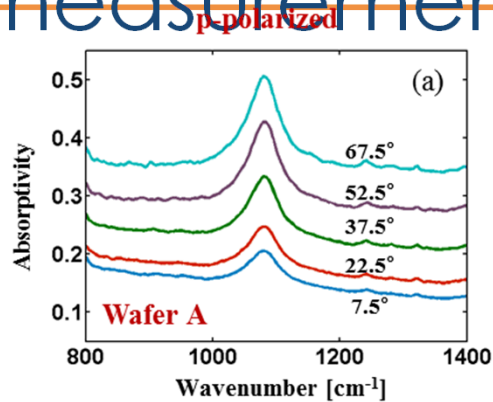
# Thermal Emission: Berreman Modes

Kirchhoff's law of thermal radiation: the absorptivity of an object should be equal to its emissivity ( $A = \epsilon$ )

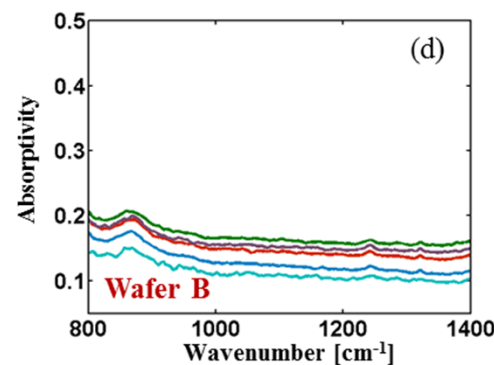
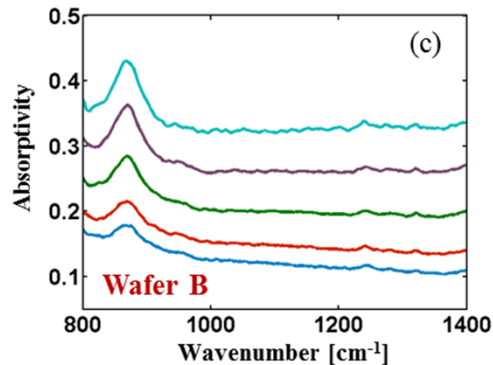


# Angle-resolved, polarization-dependent absorptivity measurements

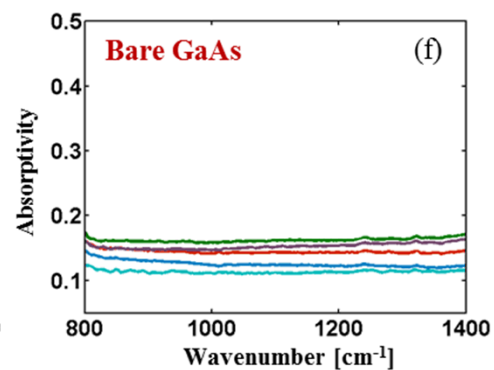
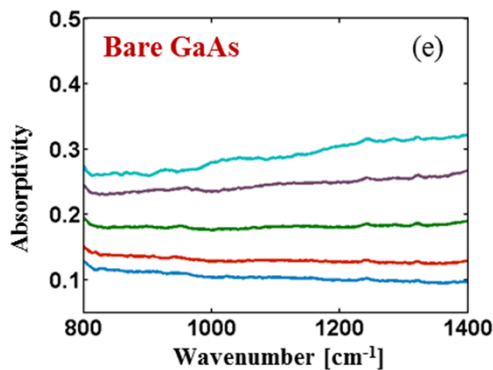
$$N_D = 1.1 \times 10^{19} \text{ cm}^{-3}$$



$$N_D = 5.6 \times 10^{18} \text{ cm}^{-3}$$



Bare GaAs



60nm InAs

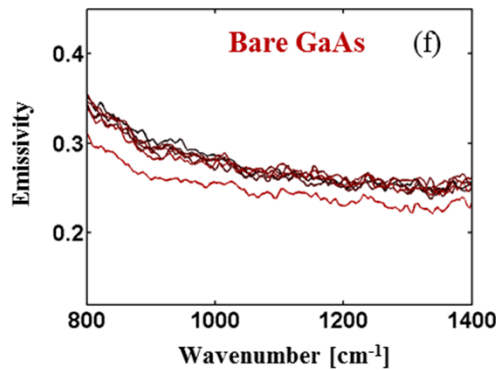
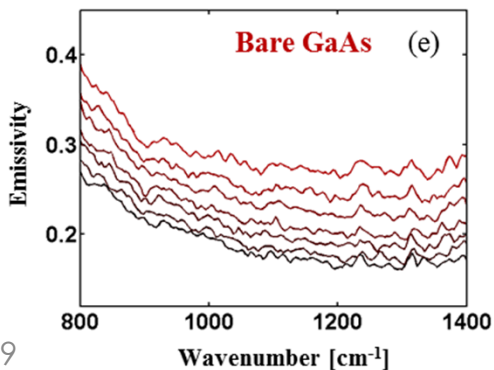
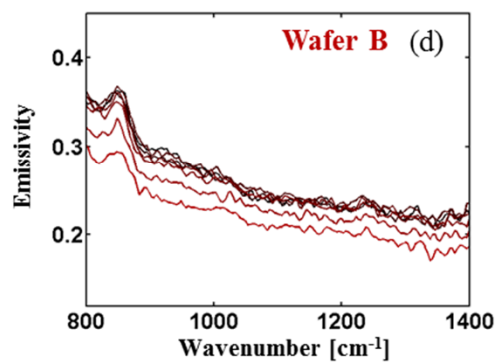
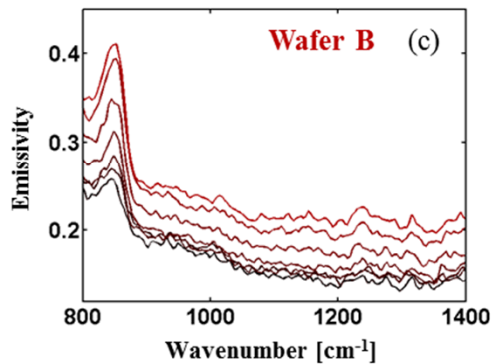
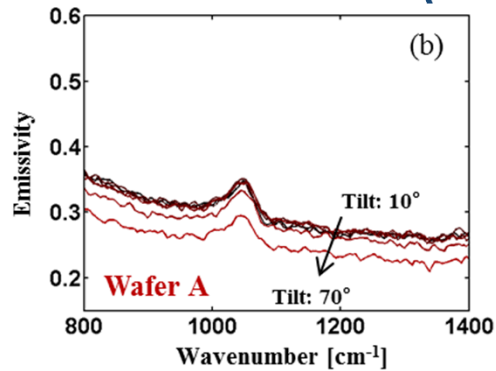
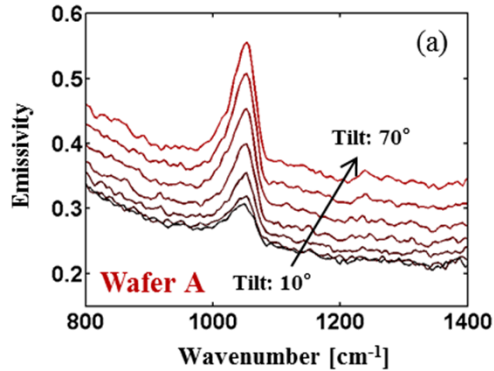
Hyperhemispherical  
Directional Reflectometer

$$A = 1 - R - T$$

# Angle-resolved, polarization-dependent emissivity measurements (140°C)

p-polarized

s-polarized



- Unpatterned semiconductor thin films generate spectrally selective thermal emission near the ENZ frequencies.
- Wavelength determined purely by doping densities
- An ENZ film works as a “leaky wave antenna”

Appl. Phys. Lett. **105**, 131109 (2014)  
See also recent work by Z. Jacob

- What are Berreman and Epsilon Near Zero (ENZ) modes, what can we do with them?
  - Fundamentals
  - ENZ modes: coupling to metamaterial resonators
  - Berreman modes: Thermal emission