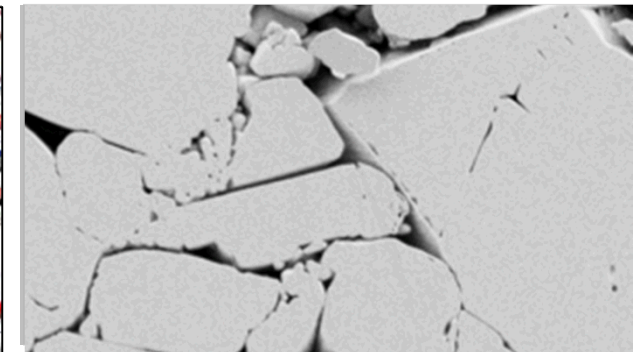
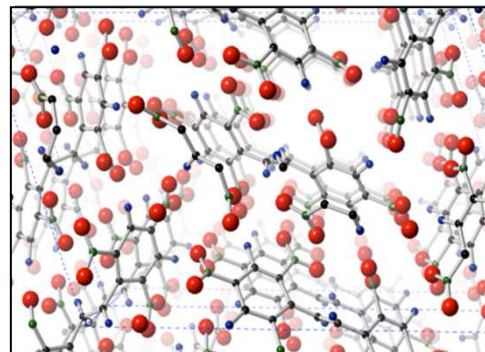
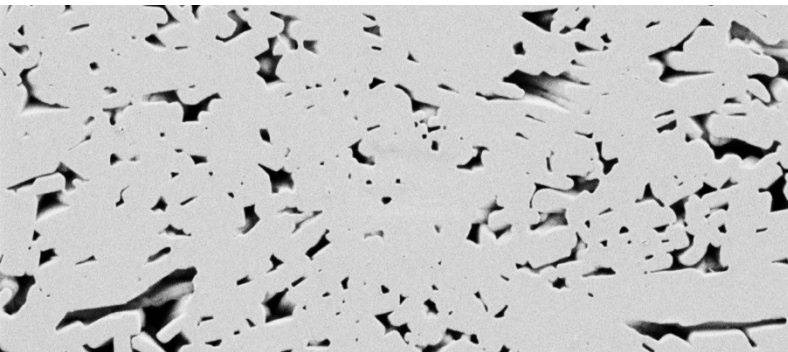


Exceptional service in the national interest



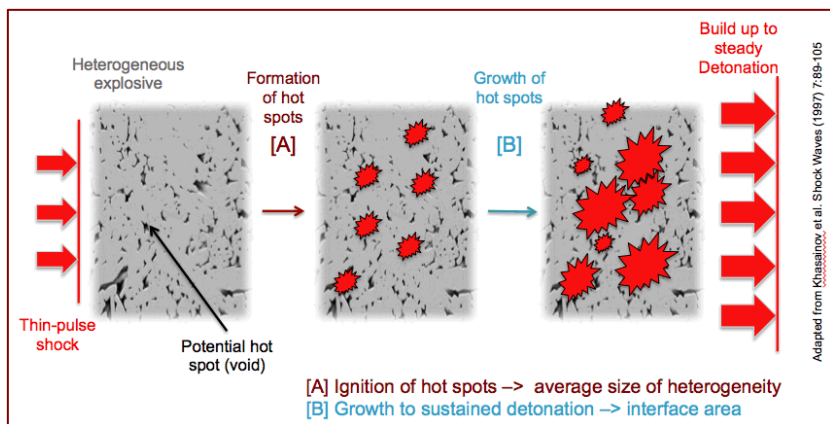
The Growing Impact of Grain-Scale Modeling

Cole Yarrington, Ryan Wixom



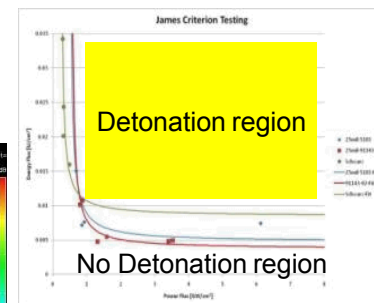
Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

Science-based understanding of shock initiation.

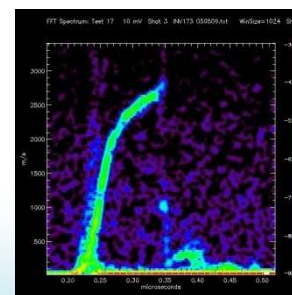


Performance Char.

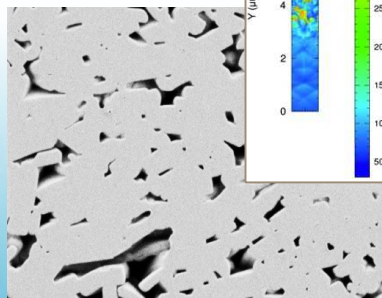
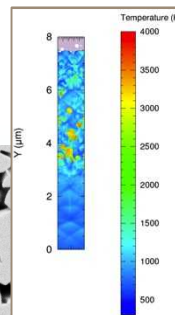
Microstructure Characterization



Energy flux vs. power flux of slapper for HNS-FP initiation

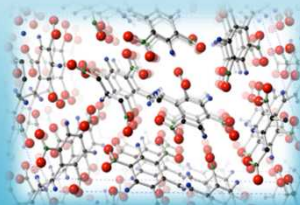
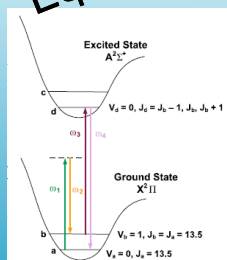


Velocimetry of flyer



X-section of HNS pellet, and grain-scale hydrocode simulation

Equation of State / Chemistry



HNS crystal structure

Time scale: $10^{-12} - 10^{-9}$ s

Technology

Science

Atomic

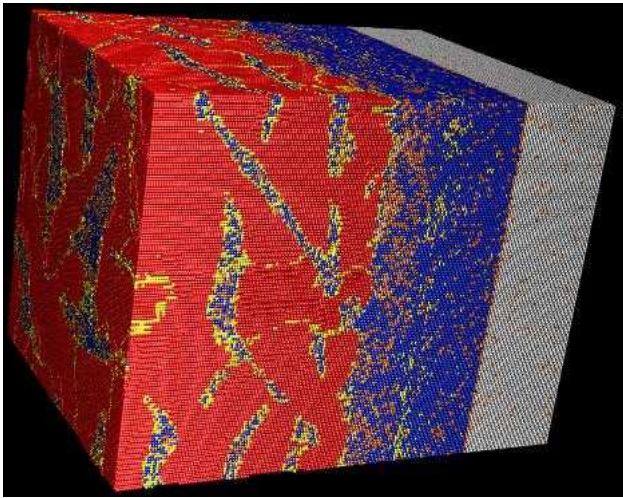
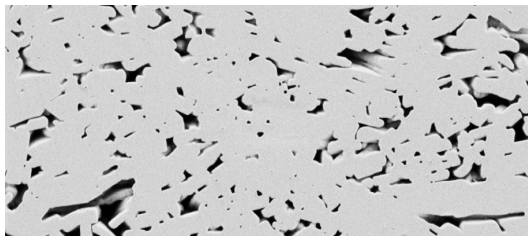
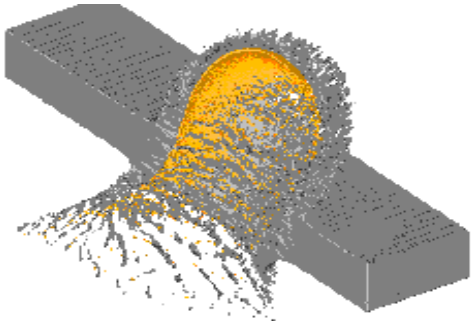
Molecular

Microscale

Mesoscale

Continuum

Mesoscale Approaches



~Avagadro's number

Continuum

Resolution



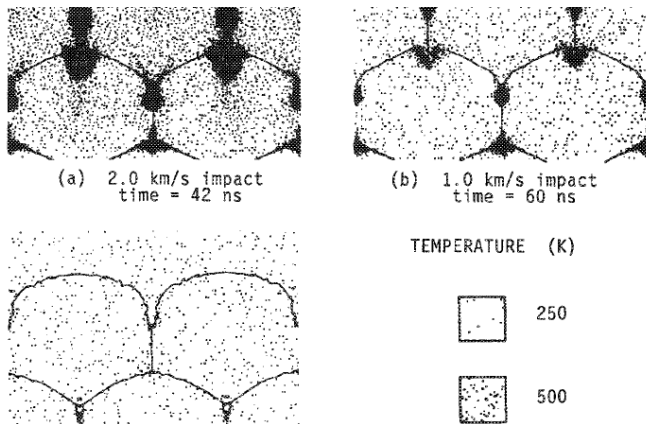
Mesoscale

~ 1×10^3 to
 1×10^9 atoms

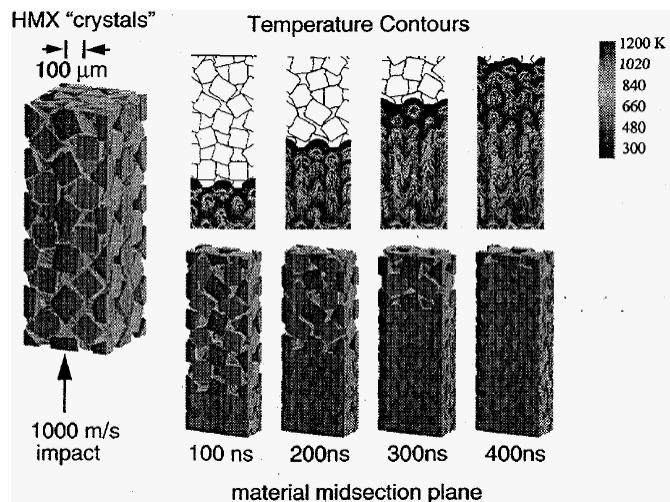
Scaling

Atomistic - Molecular

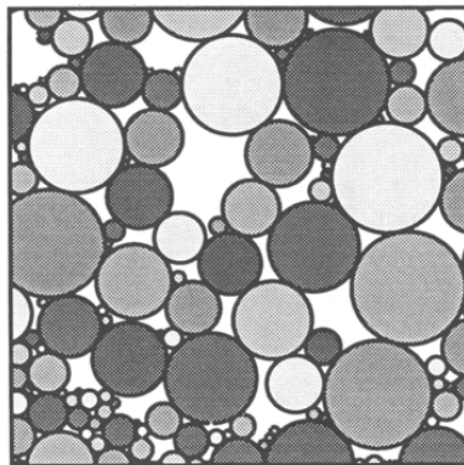
Where did it start?



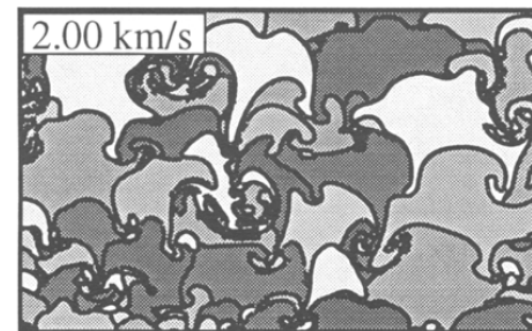
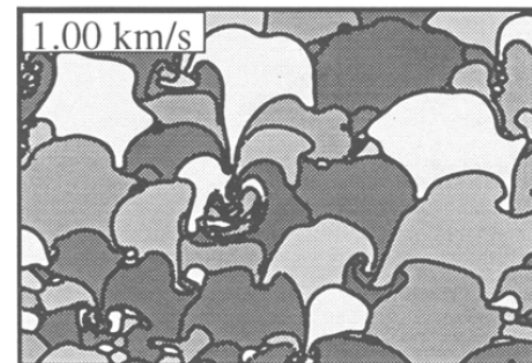
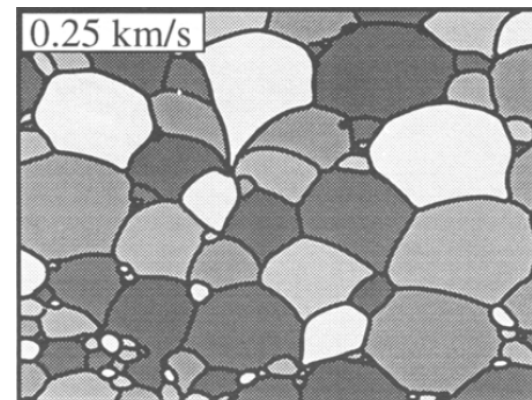
Williamson, R.L., *Parametric studies of dynamic powder consolidation using a particle-level numerical model*. Journal of Applied Physics, 1990. 68: p. 1288-1296.



Baer, M.R., Graham, R.A., Anderson, M.U., Sheffield, S.A., and R.L. Gustavsen, *Experimental and Theoretical Investigations of Shock-Induced Flow of Reactive Porous Media*. In 1996 JANNAF Combustion Subcommittee and Propulsion Systems Hazards Subcommittee Joint Meeting. 1996. Monterey, CA.



Benson, D.J., and Nellis, W.J., *Numerical simulation of the shock compaction of copper powder*. AIP Conference Proceedings, 1994. 309: p. 1243-1246.



Characterizing pellet microstructure

Ar ion cross-section polishing: 2D

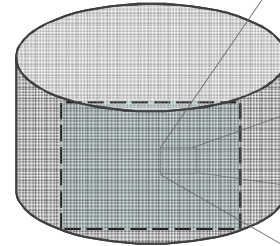
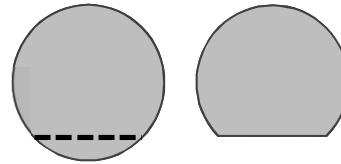
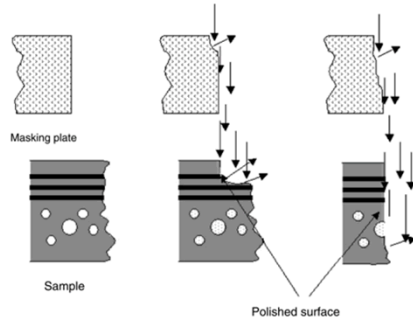
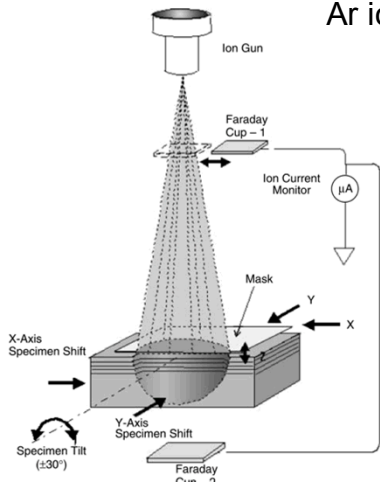
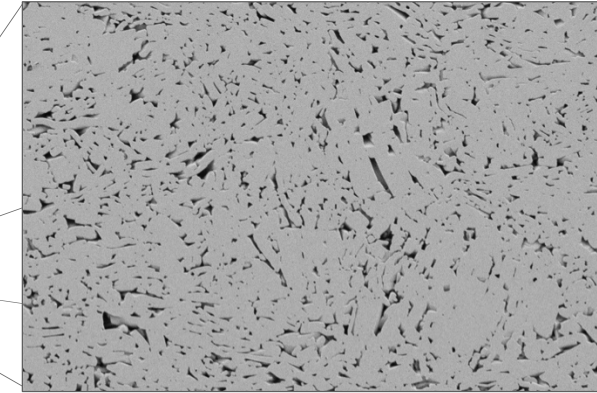
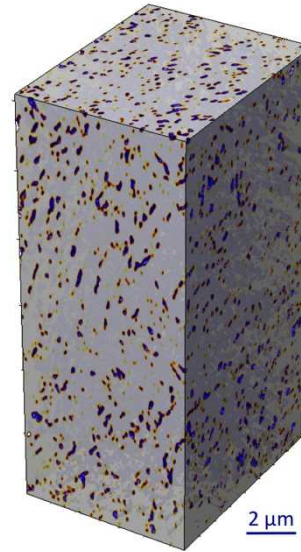
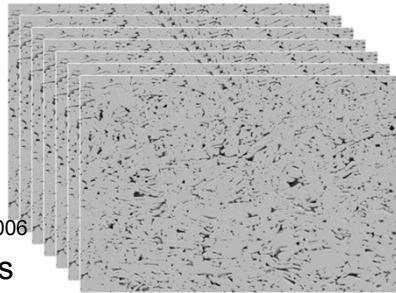
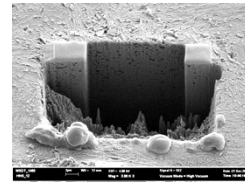
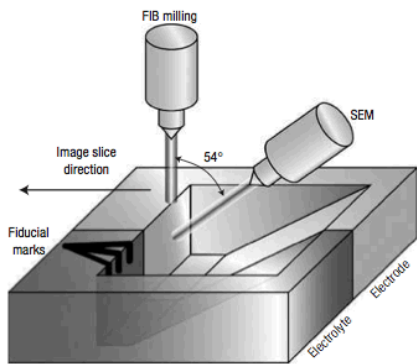


Image width: 25 μm

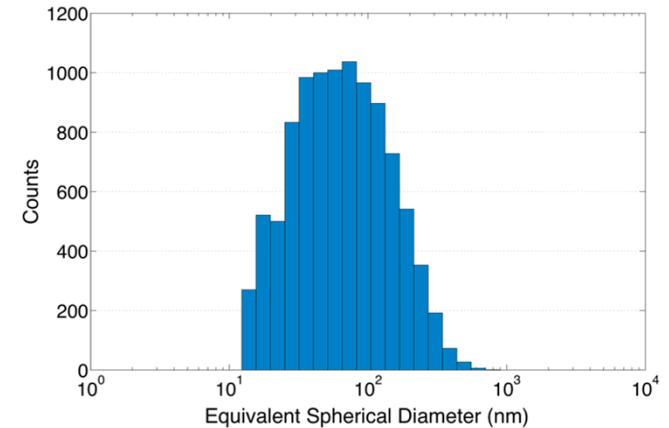


HNS-FP, 90% TMD

Focused ion beam nanotomography: 3D data



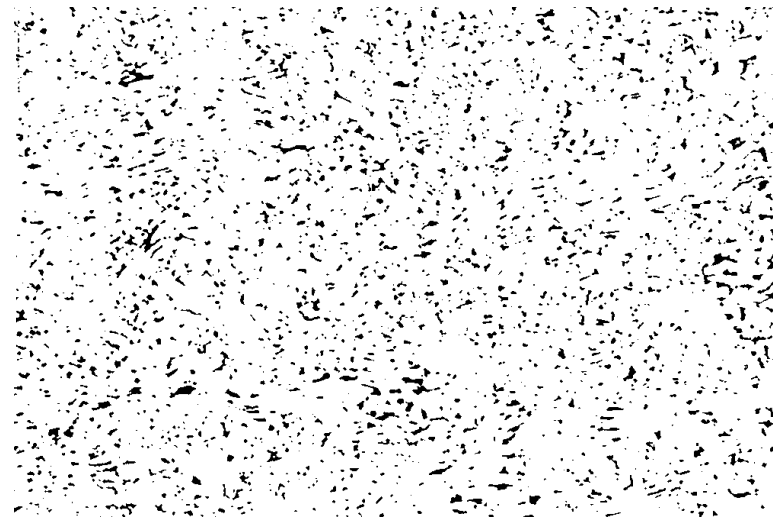
80,000 pores, mean diameter 86.3 nm



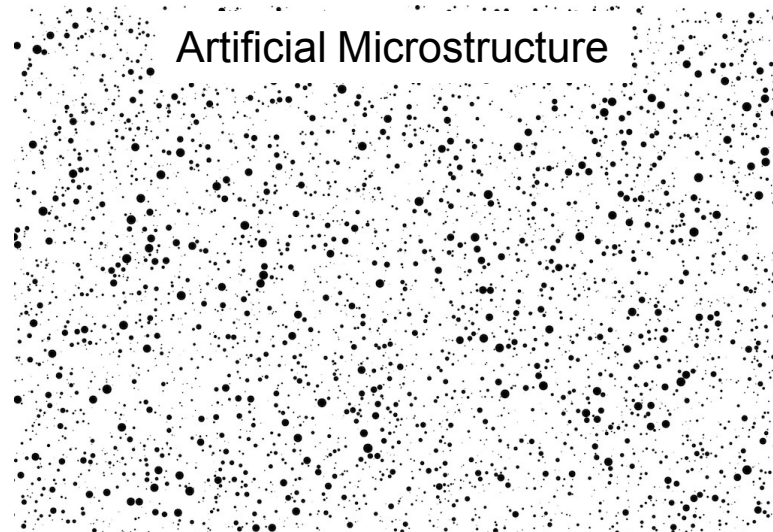
Wilson et al. Nature Materials, VOL 5, JULY 2006
Nanotomography: 25 nm slices

Grain-scale hydrocode simulation w/ statistically equivalent microstructure

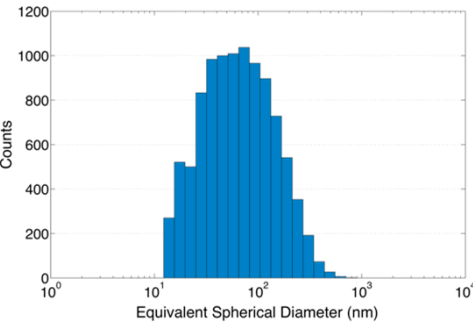
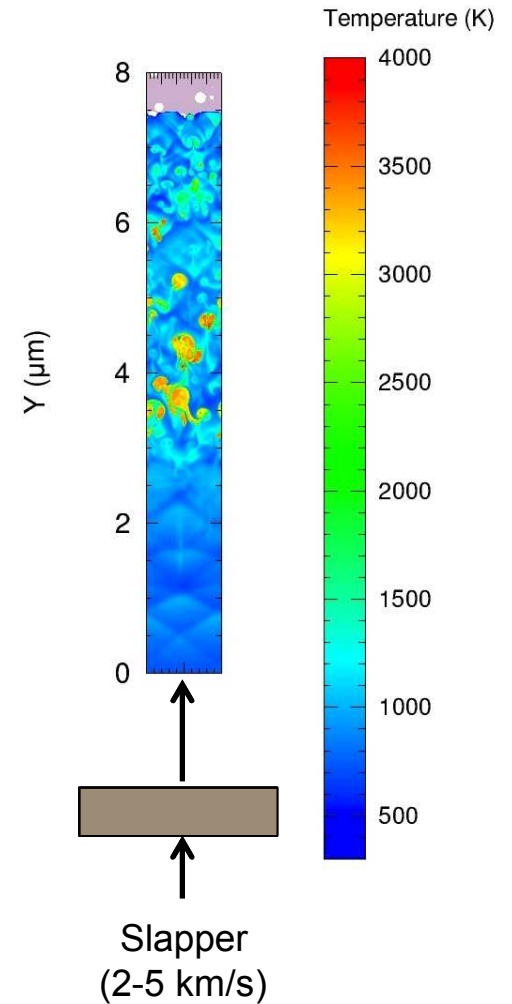
Real Microstructure



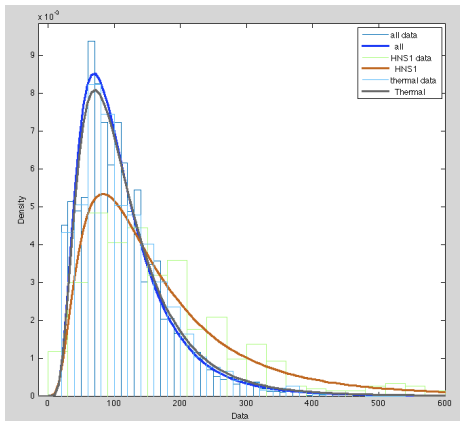
Artificial Microstructure



Snapshot from hydrocode simulation

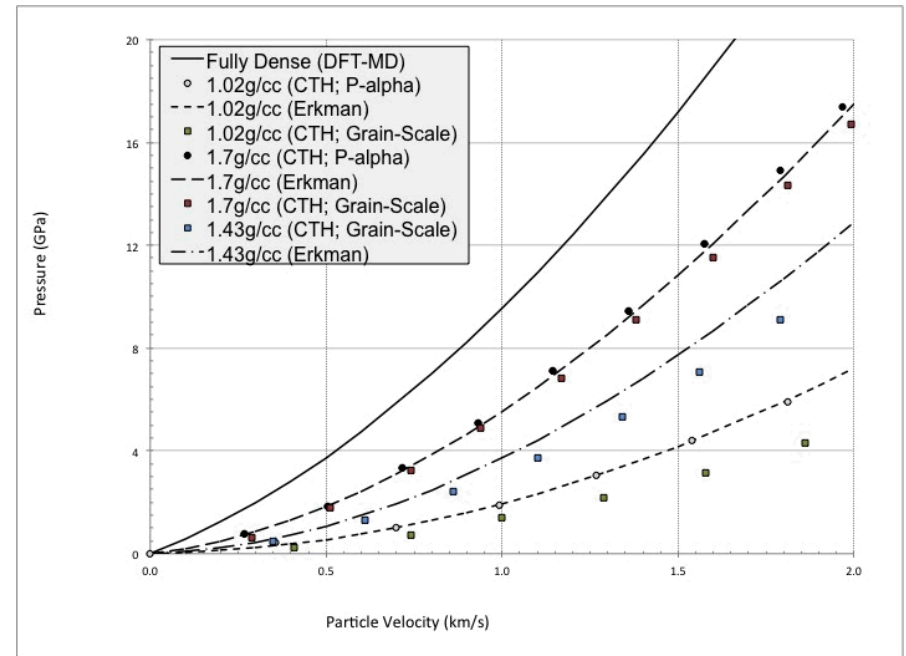
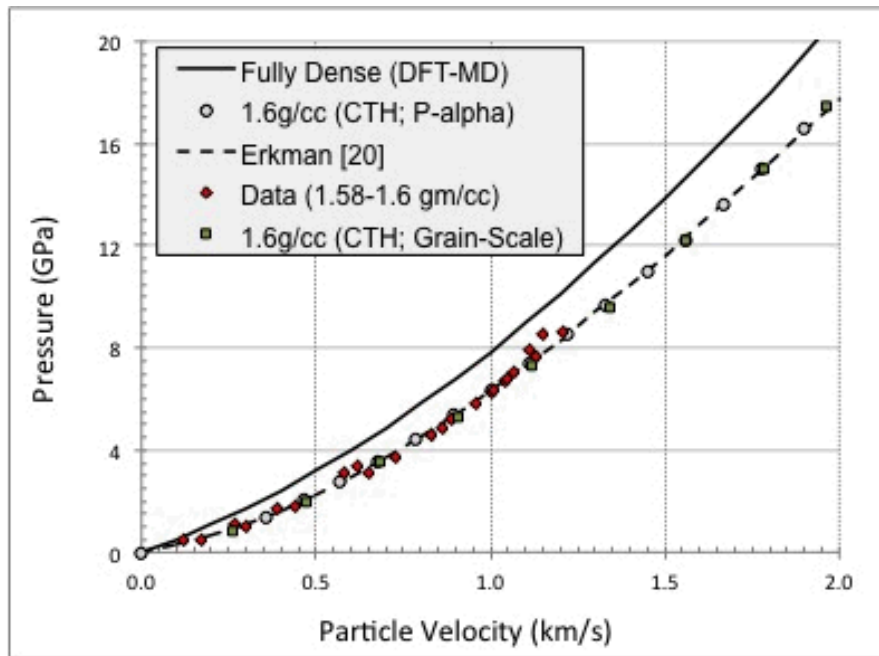


What features are important to initiation?



Bulk Hugoniot predictions

- HNS grain scale simulations were validated at 92% TMD with historical Hugoniot data
- CL-20 was simulated at 50, 70, and 84% TMD
- Strength not a factor at these conditions

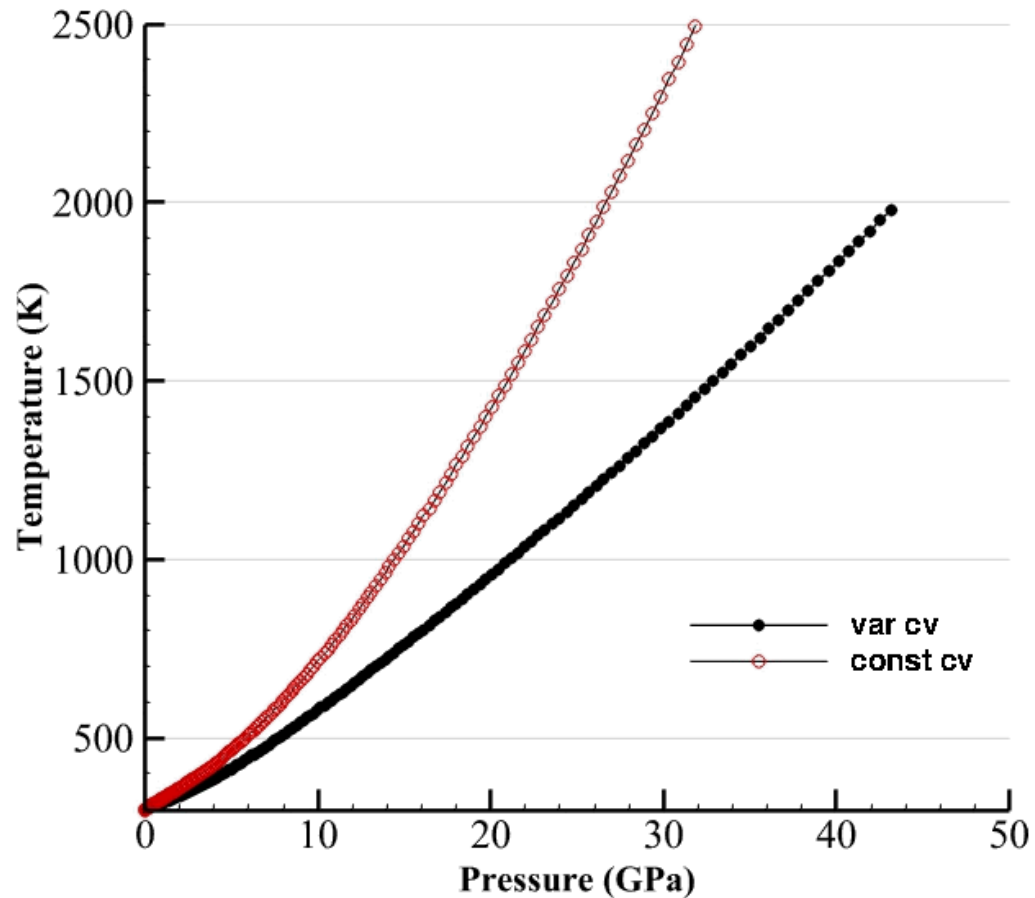


Temperature dependent reactive burn Sandia National Laboratories

$$d\lambda/dt = (1 - \lambda)F \exp(-\Theta/T)$$

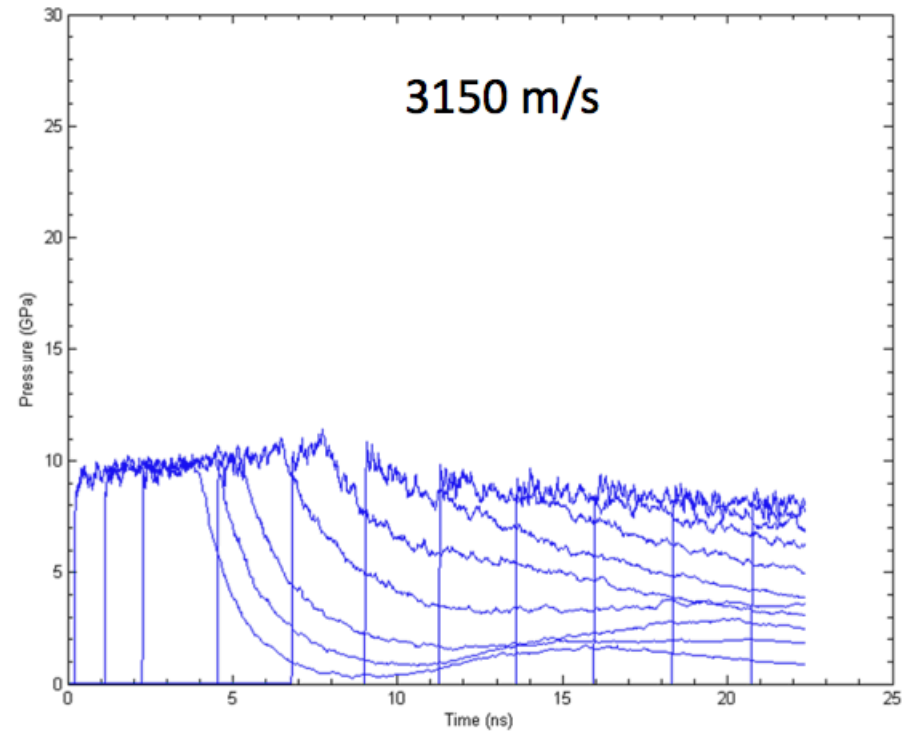
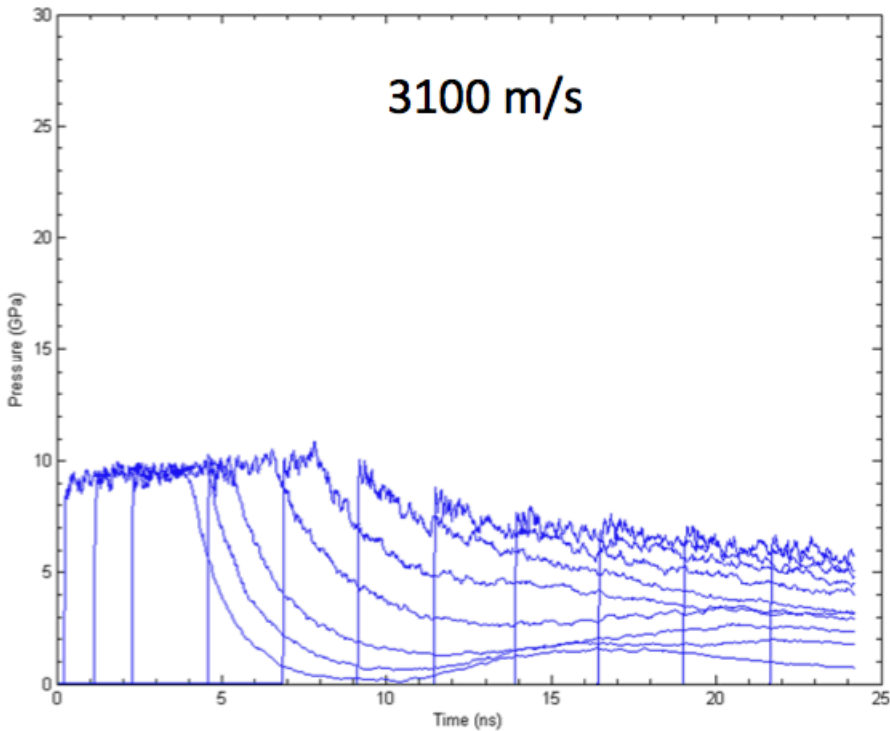
$$\Theta = \Theta_0 (1 + A_p P)$$

- Consistent temperatures obtained through variable specific heat Mie-gruneisen EOS
- Activation energy based on thermal decomposition data (127 kJ/mol [Cooper])
- Pre-exponential parameter was fit to shock initiation threshold data



Shock-to-detonation transition near threshold:

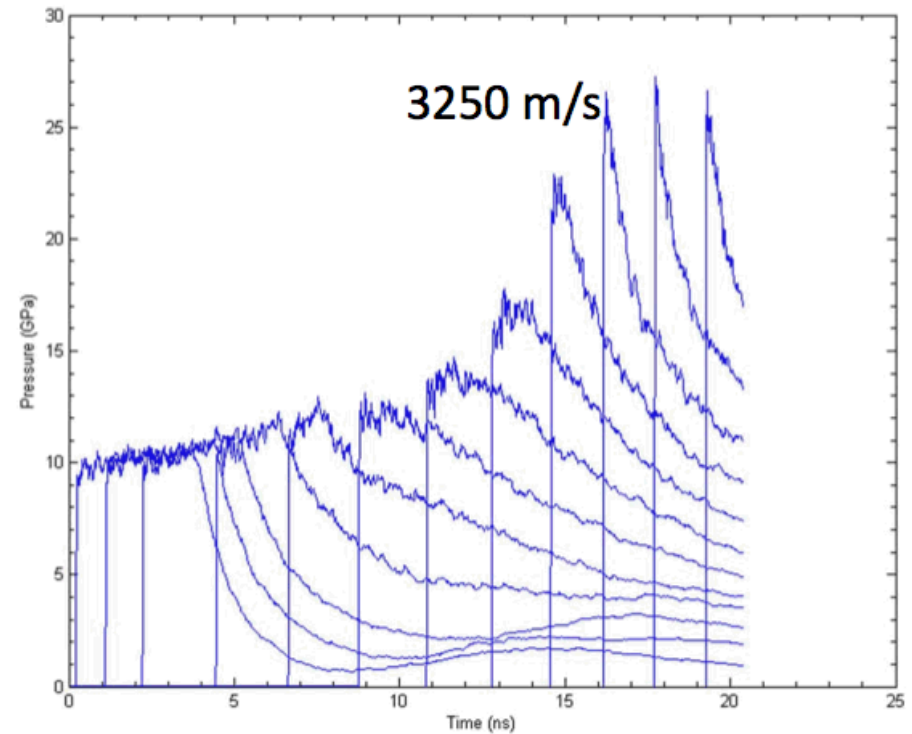
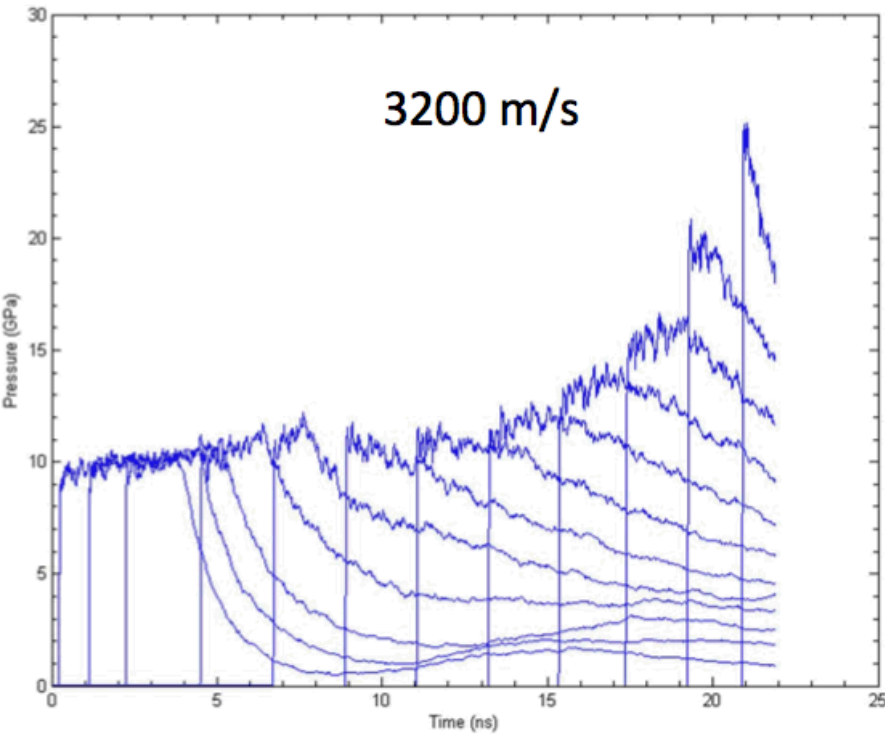
Bulk-average pressure history at various distance from the impact surface (1, 5, 10, 20, 30, 40, ... μm)



(*Experimental threshold is ~ 3200 m/s)

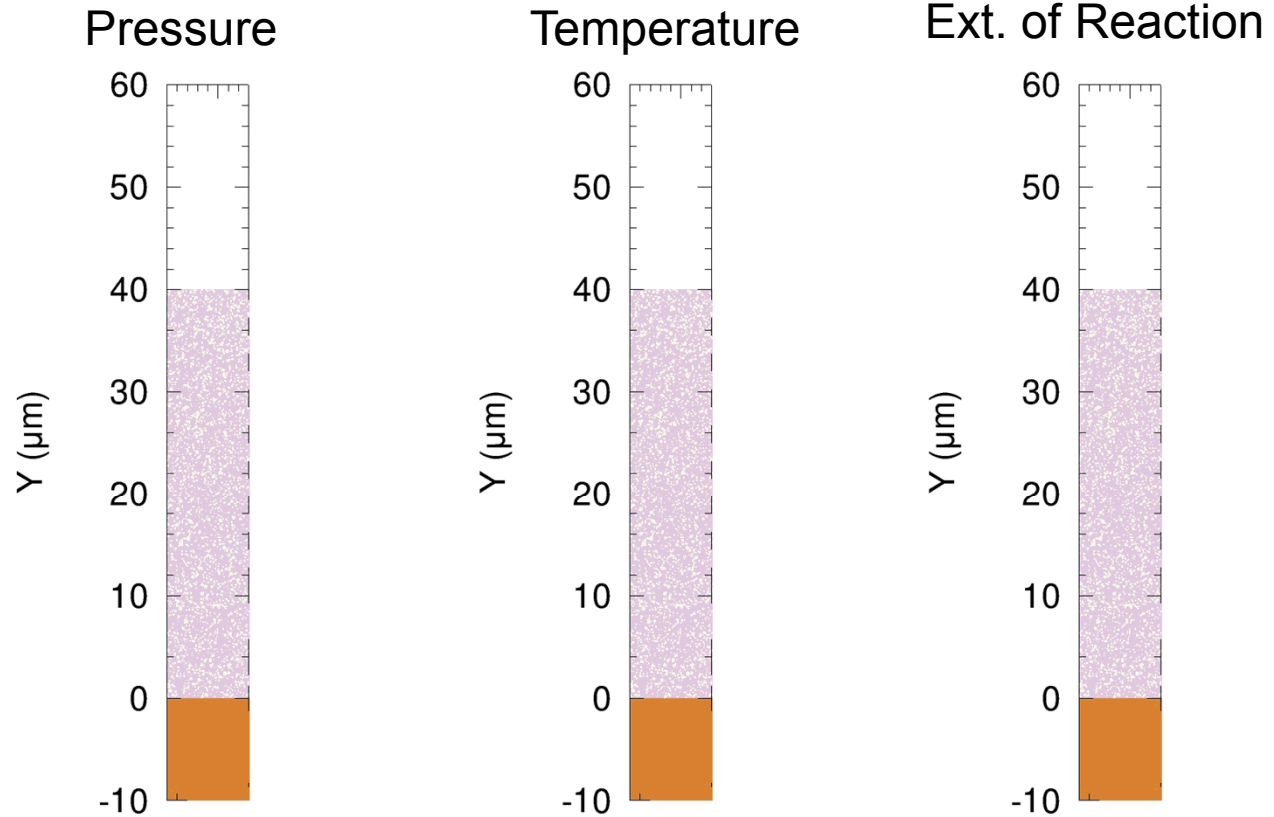
Shock-to-detonation transition near threshold:

Bulk-average pressure history at various distance from the impact surface (1, 5, 10, 20, 30, 40, ... μm)



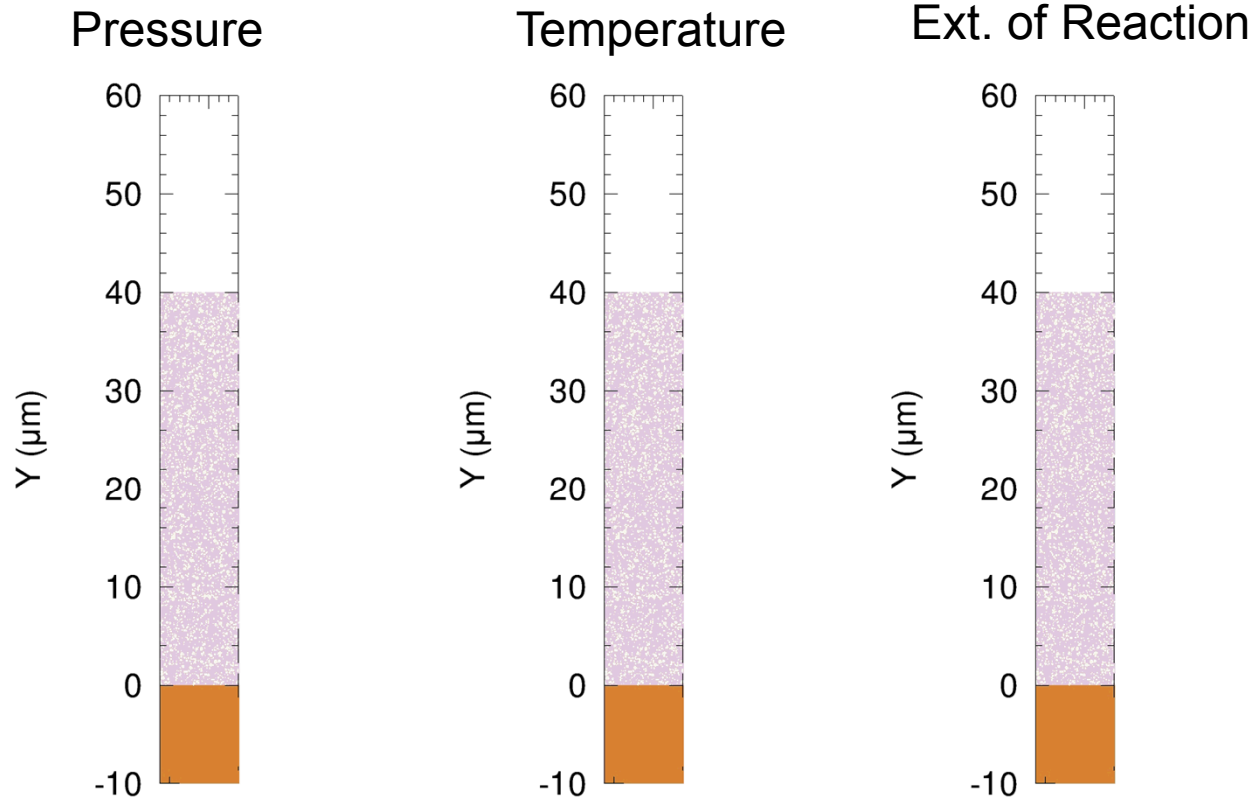
(*Experimental threshold is ~ 3200 m/s)

Shock-to-detonation transition below threshold:



P, T, & Rxn at 0.000000e+00

Shock-to-detonation transition above threshold:



P, T, & Rxn at 0.000000e+00

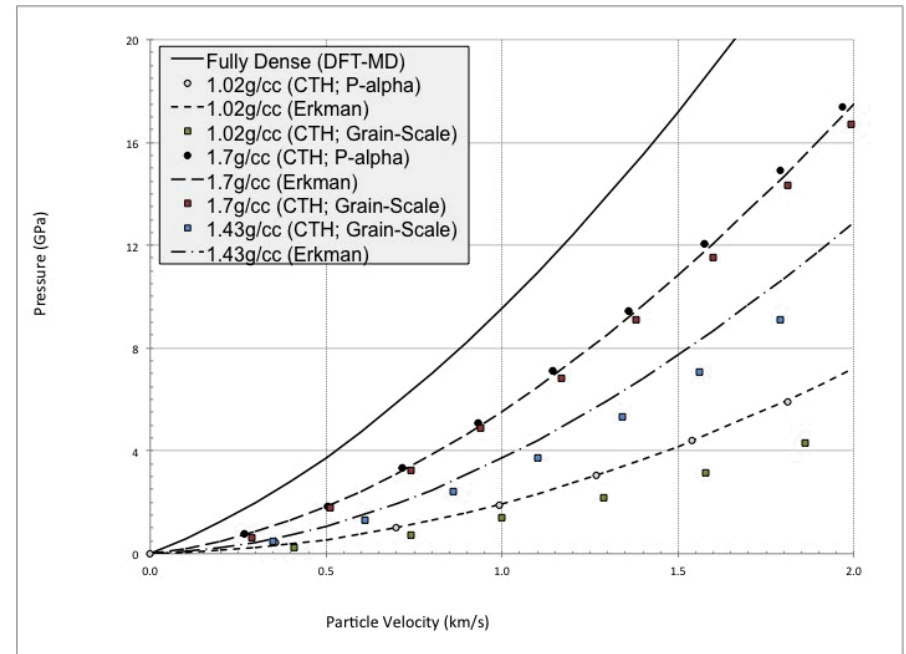
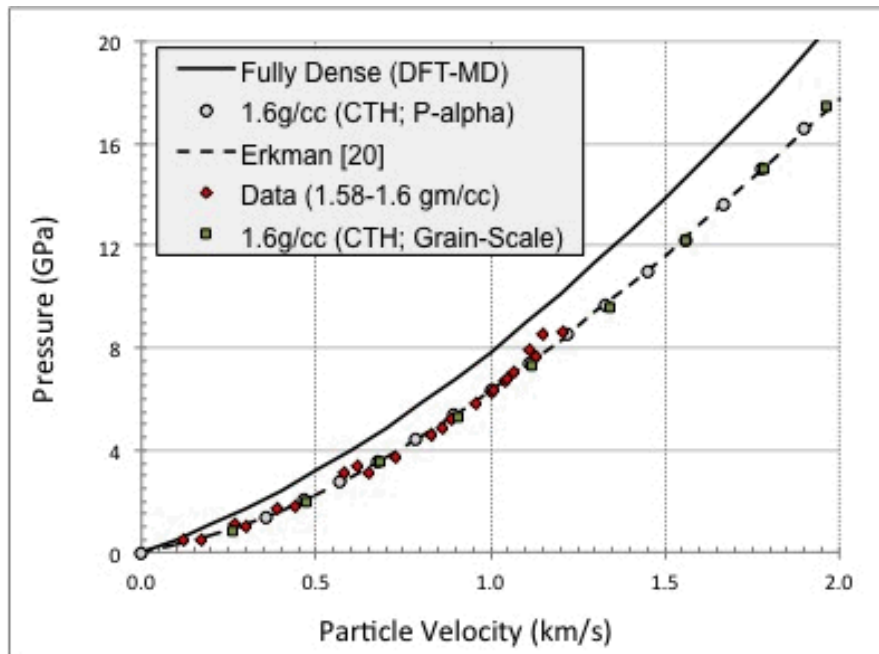
- Grain scale modeling has been used to investigate pore collapse, coalescence, prediction of bulk properties, run up to detonation and failure
- Computational cost can still be expensive
- Large impact to be gained by mining the data
- Determine statistical correlations relevant to the microstructure → response
 - What are the key metrics
- Suggest model forms for next generation continuum models

Questions?

Extras

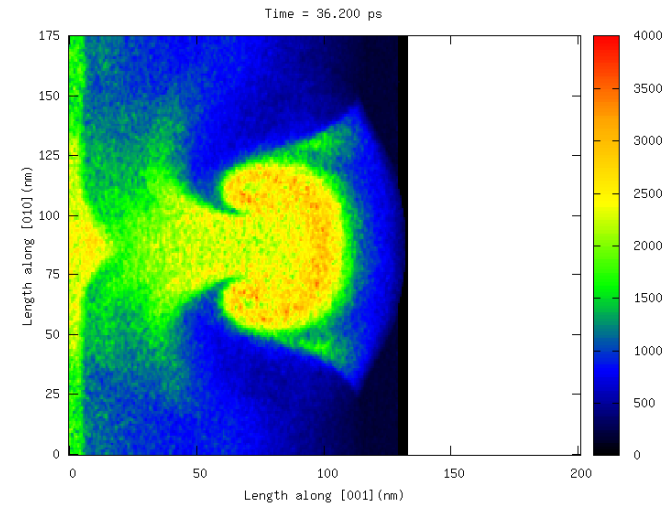
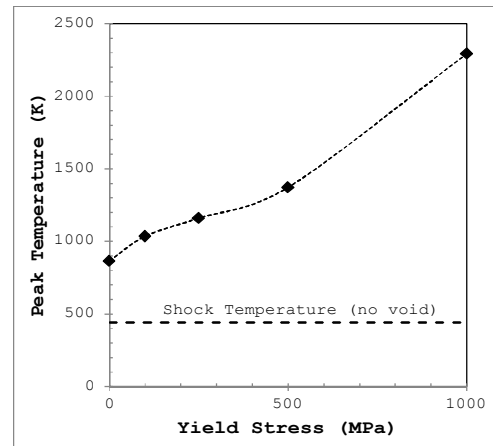
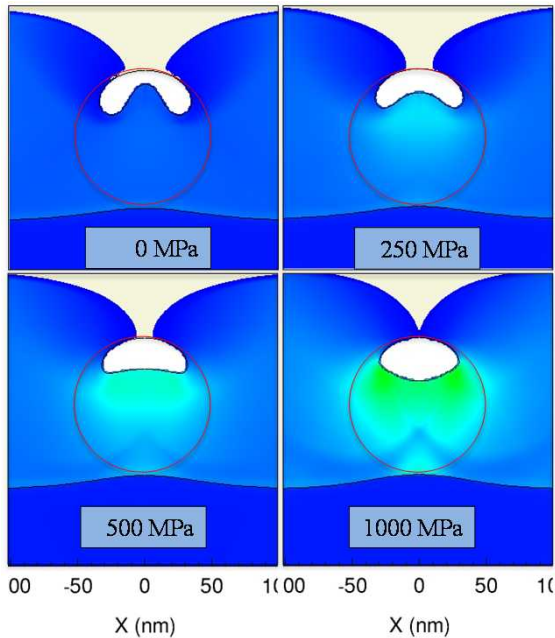
Bulk Hugoniot predictions

- HNS grain scale simulations were validated at 92% TMD with historical Hugoniot data
- CL-20 was simulated at 50, 70, and 84% TMD



Material Strength

- Material strength has been shown to have a strong effect on pore collapse states
 - 6 Gpa shock ($U_s - 4.2$ km/s)
 - 0 – 1000 Mpa
 - 443 K – 765 K (before jet impact)
 - 1030 K – 1200 K (after jet impact)
- MD simulations of pore collapse
- ReaxFF based on CHO combustion and CHNO nitramine force fields



Calibrating Strength Models

- Lack of experimental data on HNS
- MD pore collapse used as substitute
- Lagrangian tracers surrounding pore
- Average state time history used as objective function
- Convergence achieved for two strength models
- Future work will focus on irreversible work as an objective, calibration at multiple stress conditions

$$Y = Y(\epsilon^p, \dot{\epsilon}^p, T) = \left[A + B(\epsilon^p)^N \right] \left[1 + C \ln(\dot{\epsilon}^p) \right] \left[1 - \Theta_h^m \right]$$

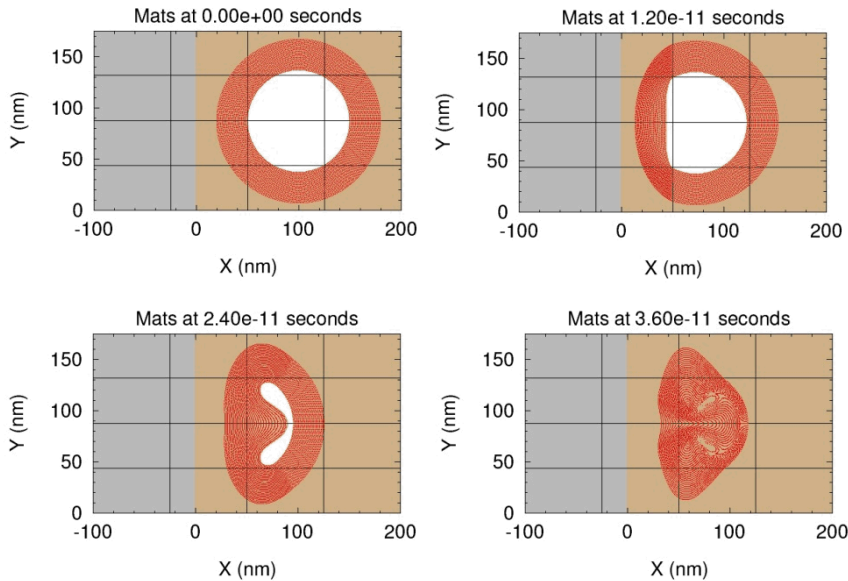
$$\Theta_h = \frac{T - T_r}{T_M - T_r}$$

EPPVM

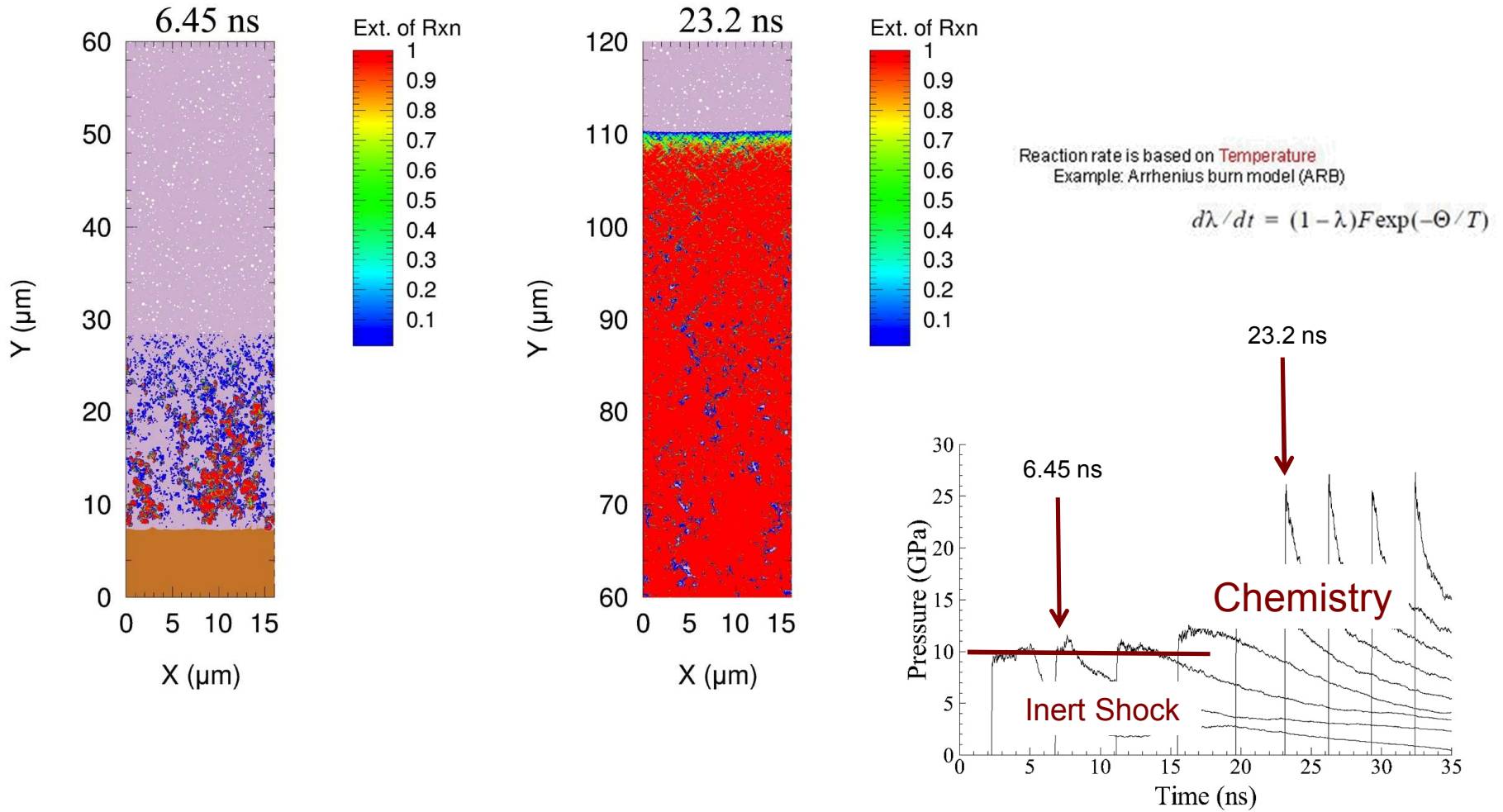
- Yield Strength –
- Poisson's Ratio –
- Melt Temp. – 316 ° C

Johnson Cook

- A –
- B –
- C –
- N –
- M –

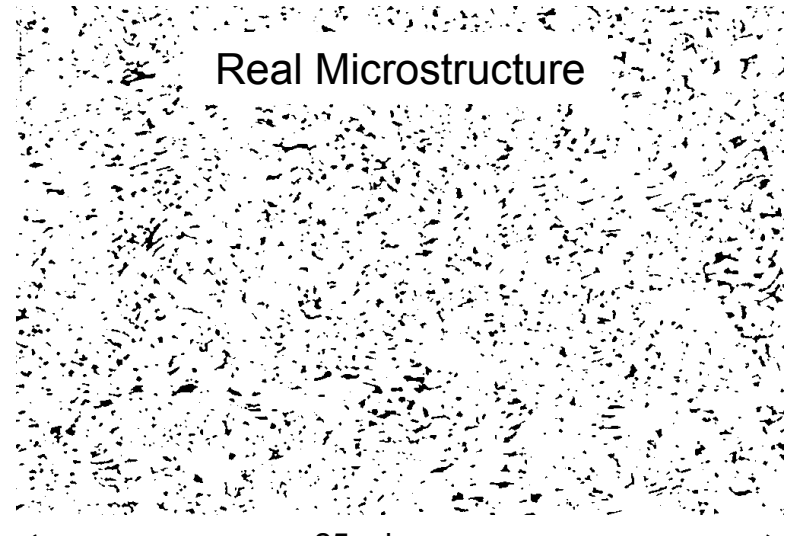
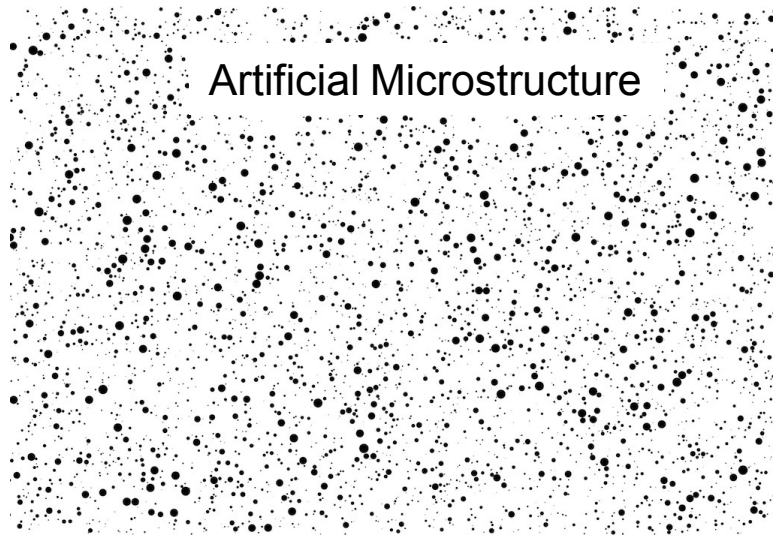


Grain-scale simulation of SDT in HNS

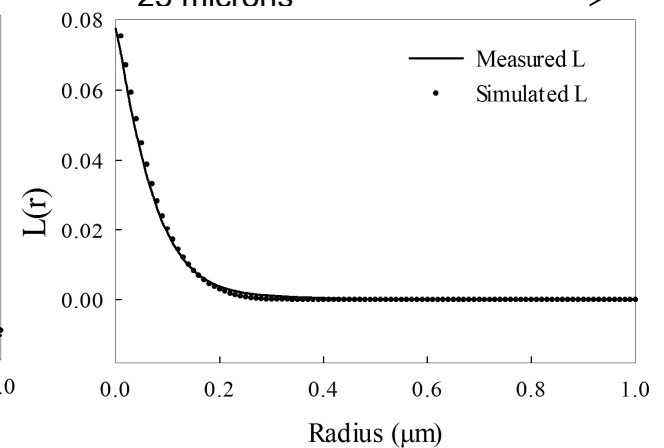
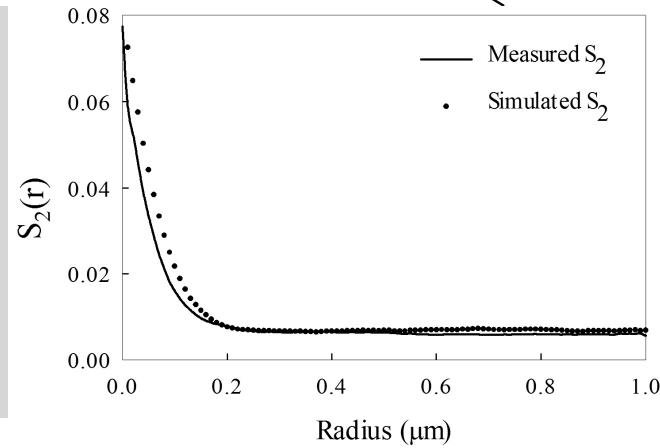
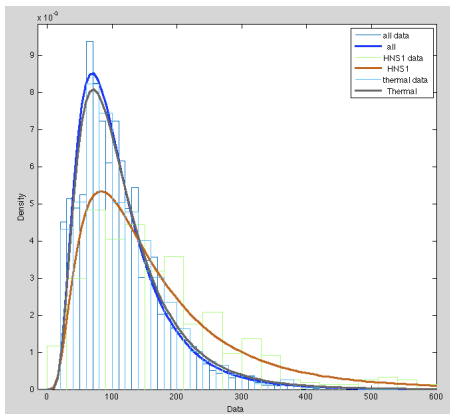


Simulations: 3.15 km/s, Mean pore size 86 μm

Reconstructed and measured microstructural statistics

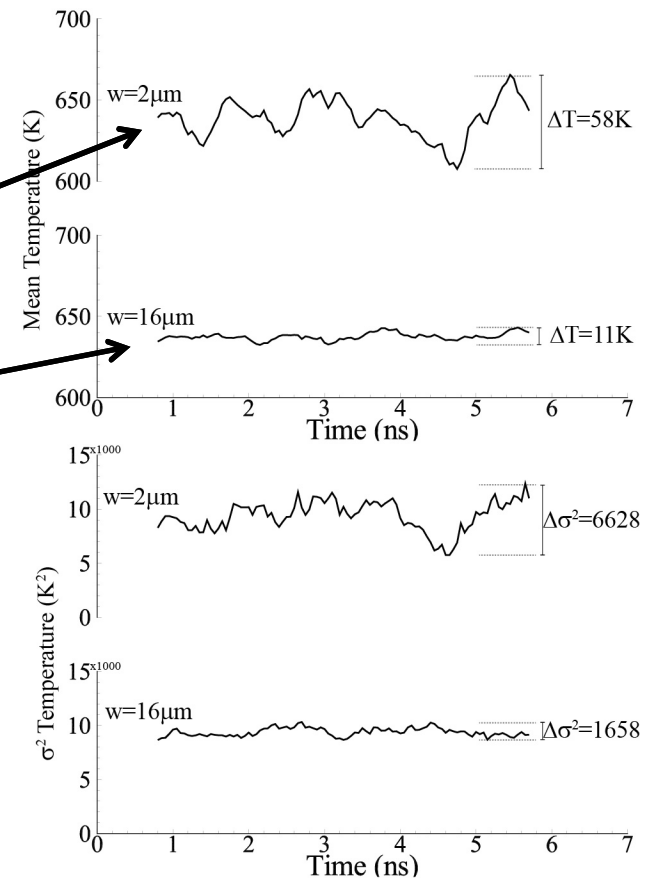
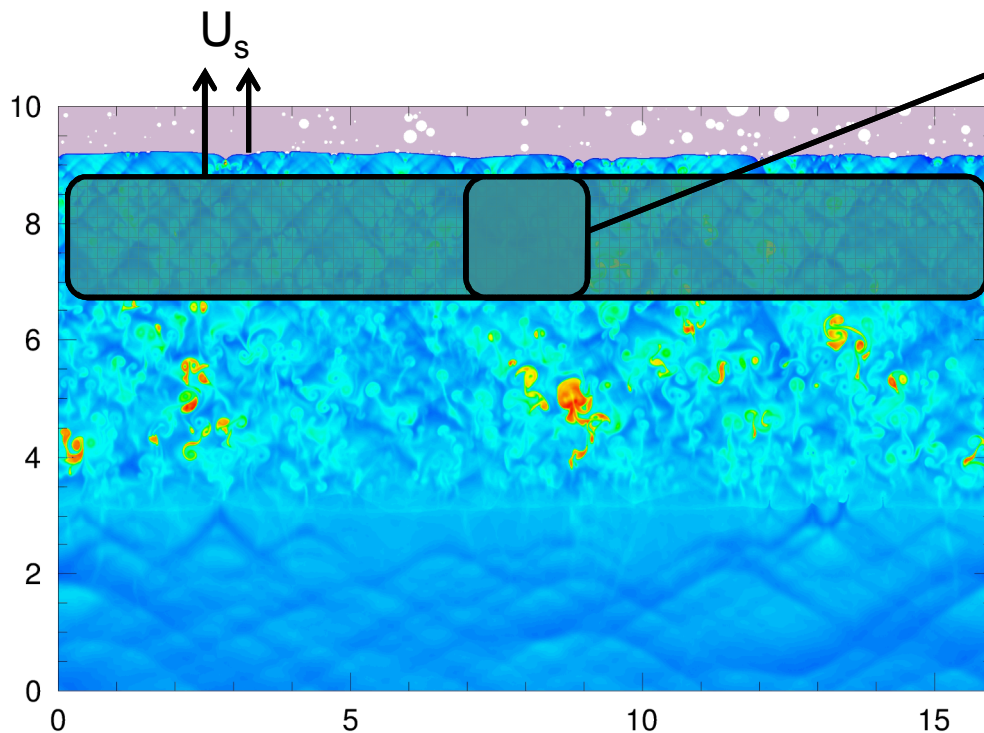


← 25 microns →



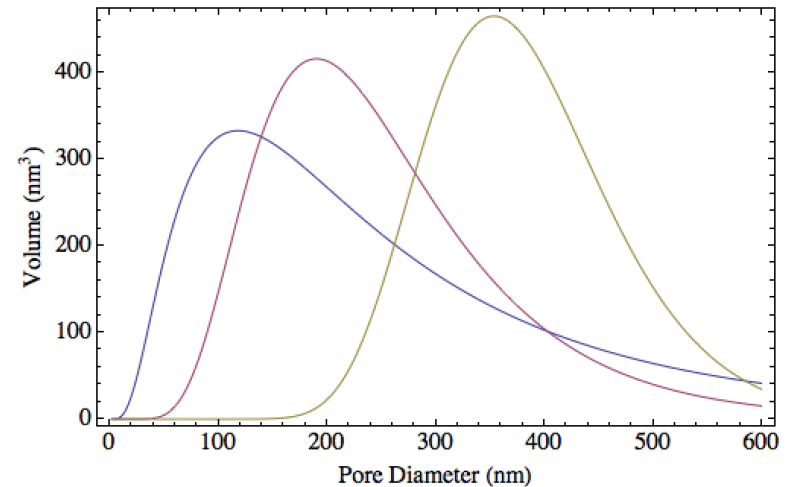
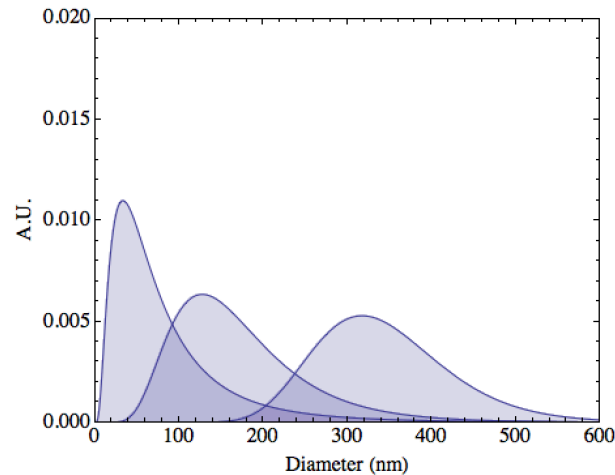
Determining the Representative Volume Element (RVE):

- Statistical relevance ensured by estimating the RVE
- RVE contains enough microstructure, but is smaller than the macroscopic length scale
- Temperature mean and variance

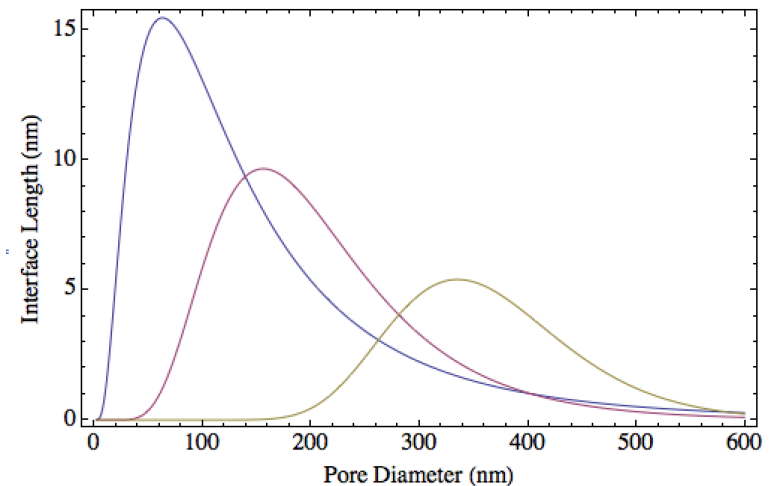


HNS initiation as a function of pore-size:

Simulations: 3.15 km/s, Mean pore size 86 nm, 172 nm, 344 nm

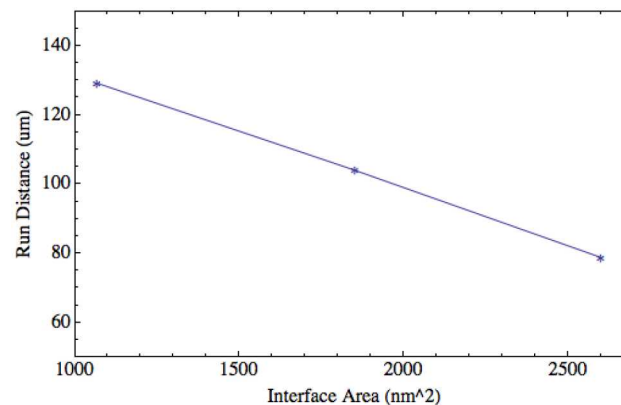
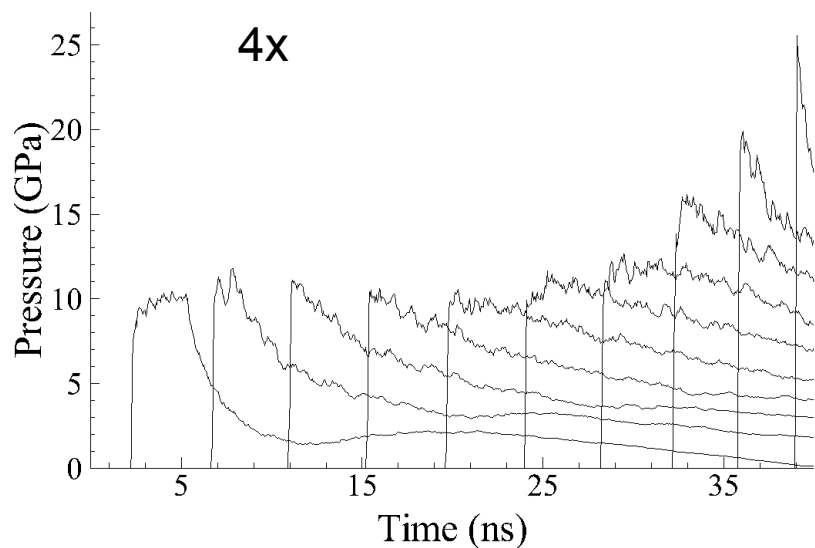
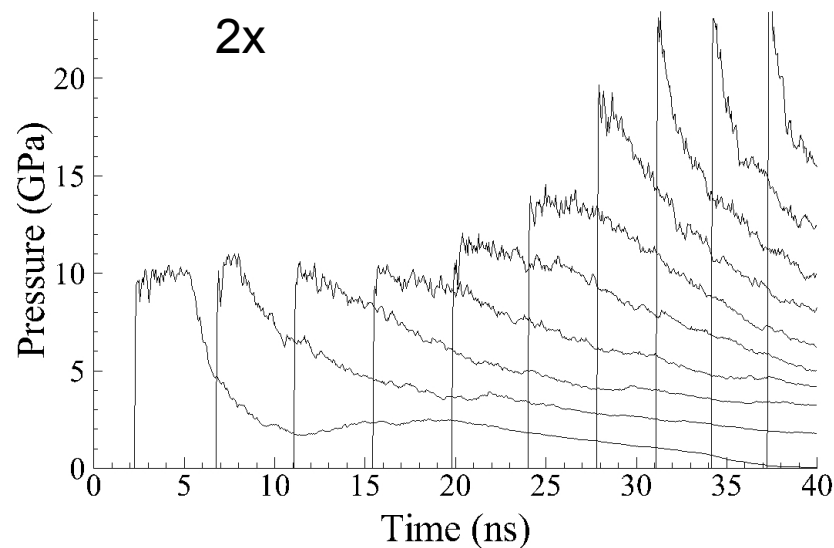
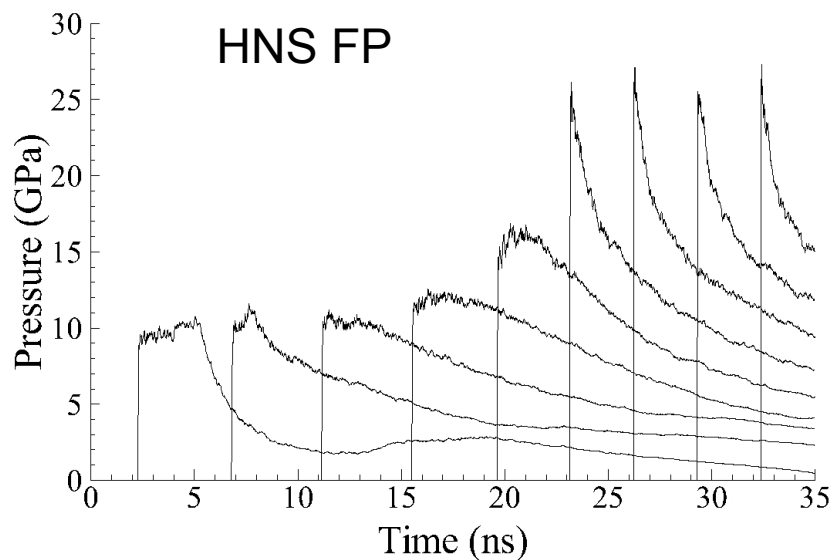


- Equal variance
- Mean increased by factor of 2 and 4
- Similar Volume, increased interface length

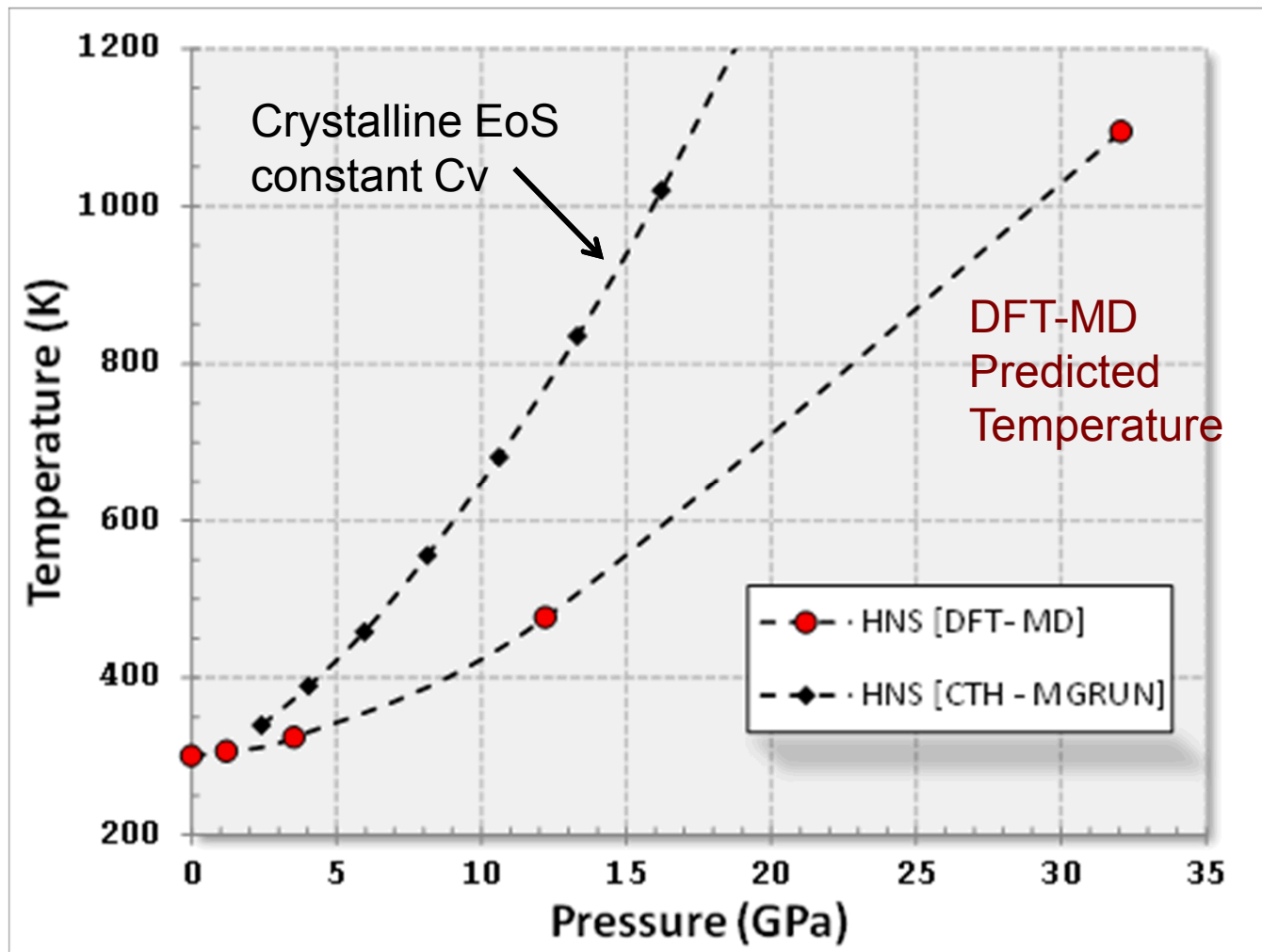


B.A. Khasainov, B.S. Ermolaev, H.N. Presles, P. Vidal, *On the effect of grain size on shock sensitivity of heterogeneous high explosives*, *Shock Waves* (1997) 7:89-105.

Run distance shifted with pore-size:

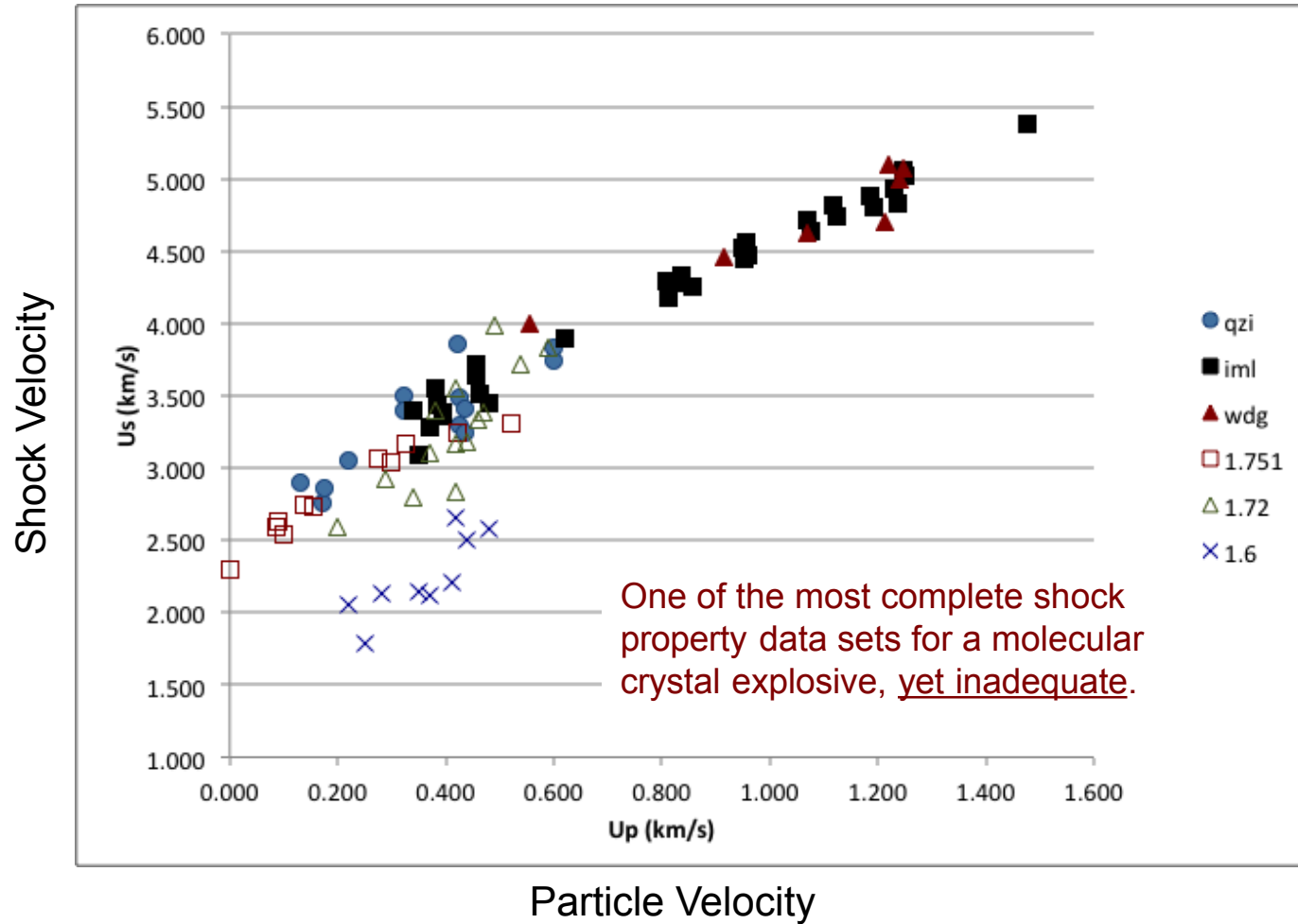


Demonstrating the EoS problem (Cv):



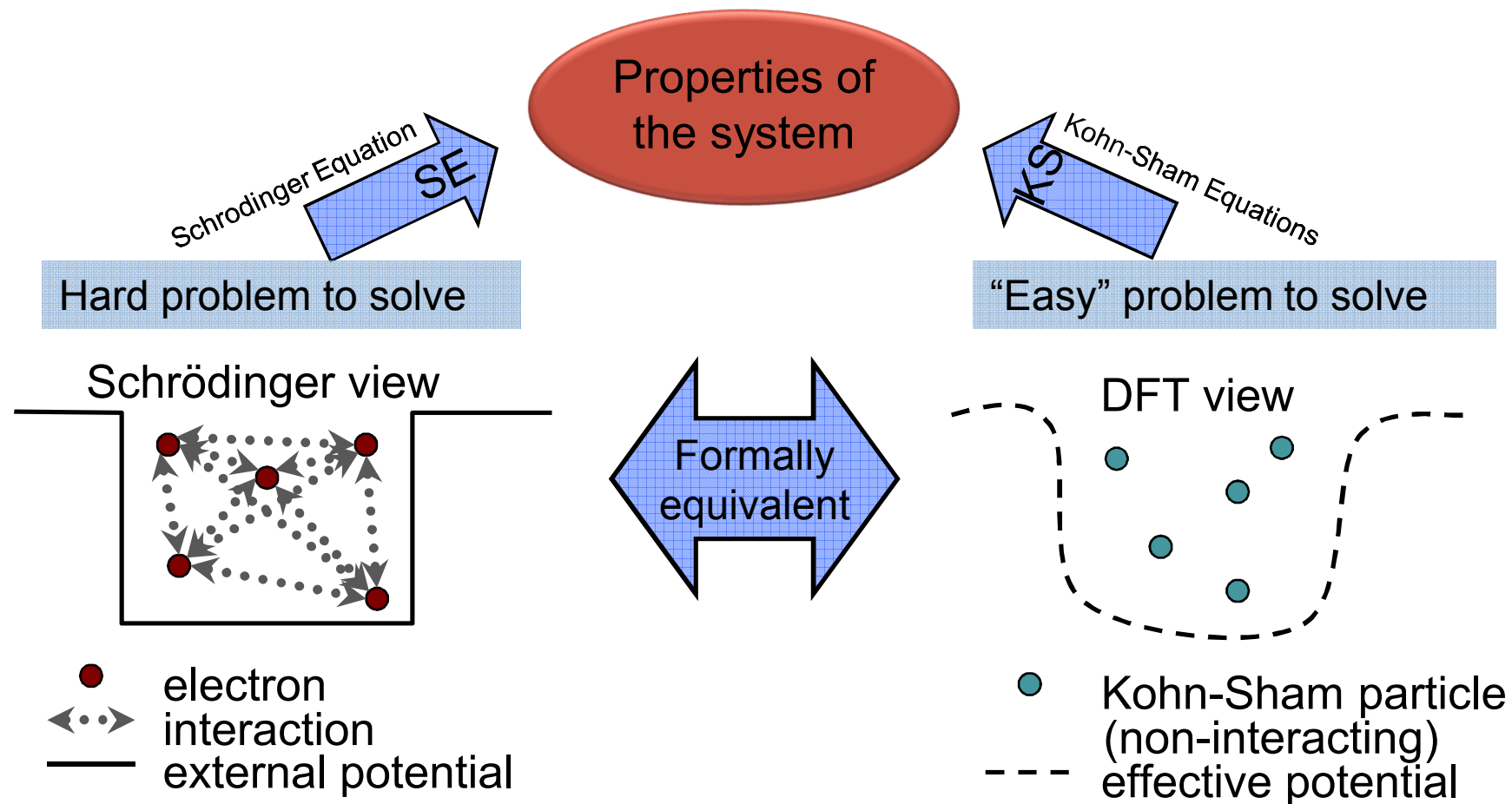
Experimental EoS for explosives

PETN Shock Hugoniot data from the LASL shock handbook (Marsh)



- 1) Not a straight line.
- 2) No information about temperature.
- 3) Data is usually low pressure.

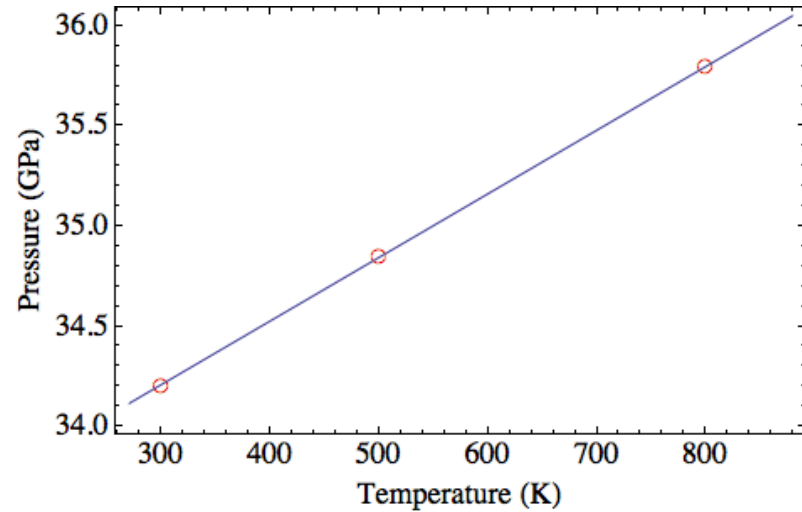
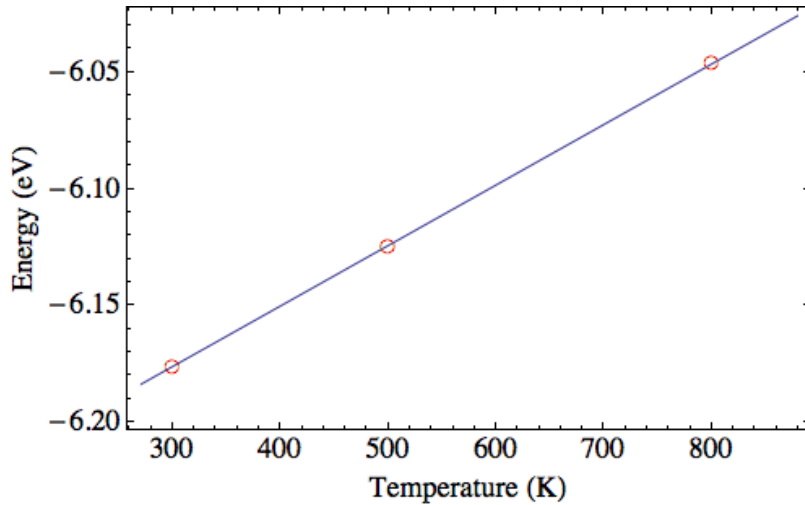
Density Functional Theory (DFT) and XC functionals:



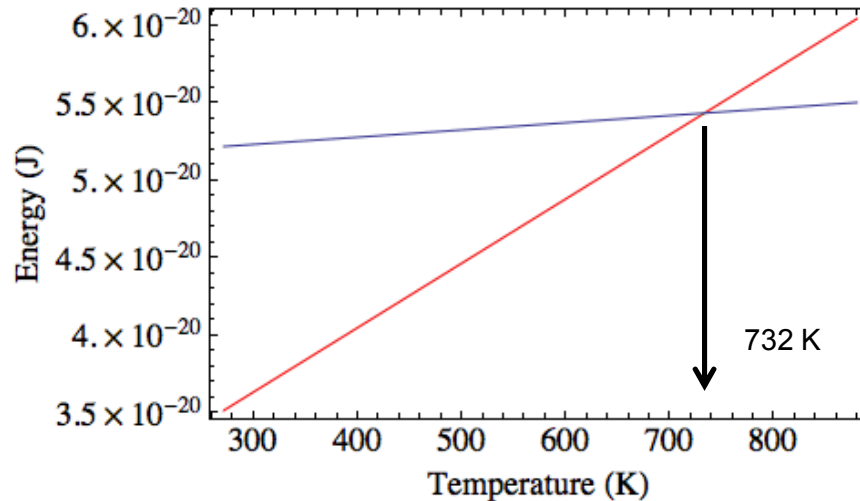
$$v_{\text{eff}}(\mathbf{r}) = v(\mathbf{r}) + \int \frac{n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} d\mathbf{r}' + \frac{\delta E_{xc}[n(\mathbf{r})]}{\delta n(\mathbf{r})}$$

AM05, LDA,
GGA, Meta-GGA,
Hybrids

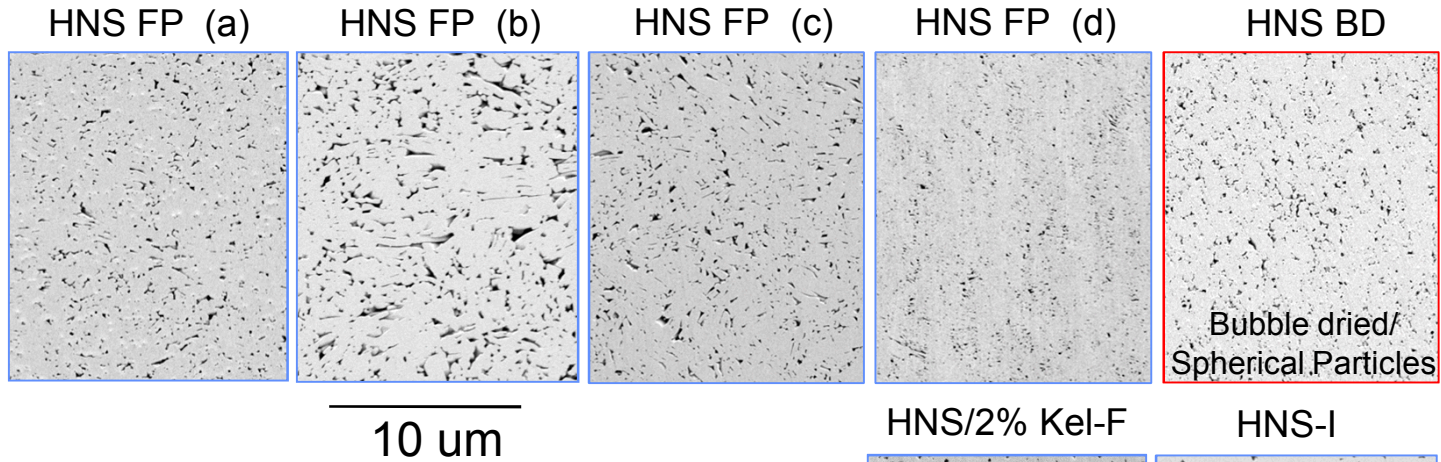
Finding the Hugoniot (TATB $V=0.85V_o$):



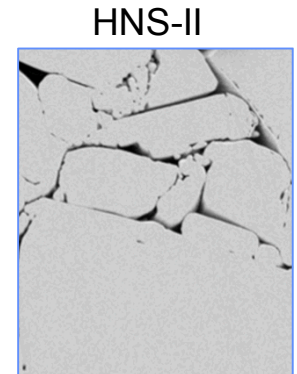
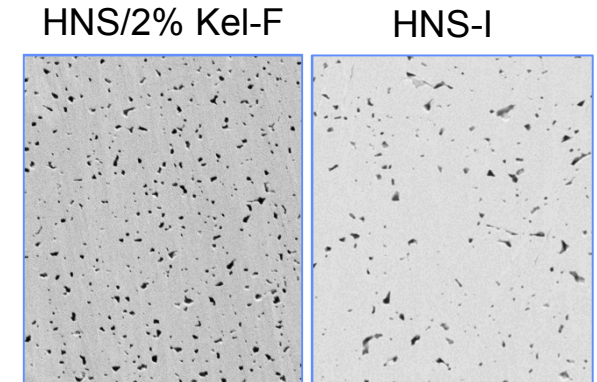
$$E(T) - E_o = \frac{1}{2}[P(T) + P_o][V_o - V]$$



Cataloging microstructures: X-sections of different types of HNS



Type	Powder SSA (m ² /g)	Interface Area (m ² /g)	Avg. DIA (nm)	Avg dist to a pore (nm)	Density %TMD
		(0.15)	(10.0)	(10.0)	(.01)
HNS-FP (a)	6	1.77	136.6	136.0	0.925
HNS-FP (b)	5	2.10	254.5	130.7	0.875
HNS-FP (c)	10	1.98	152.6	131.2	0.914
HNS-FP (d)	16	3.61	74.2	78.3	0.921
HNS-BD	12	2.41	113.5	107.3	0.899
HNS+Binder	?	1.10	211.6	214.6	0.928
HNS-I	?	0.71	233.0	345.6	0.960
HNS-II	1	0.24	1363.8	1703.5	0.950



We have also have x-sections of thermally cycled HNS FP (a)