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# 2015 IEEE PVSC Tutorial on PV System Performance

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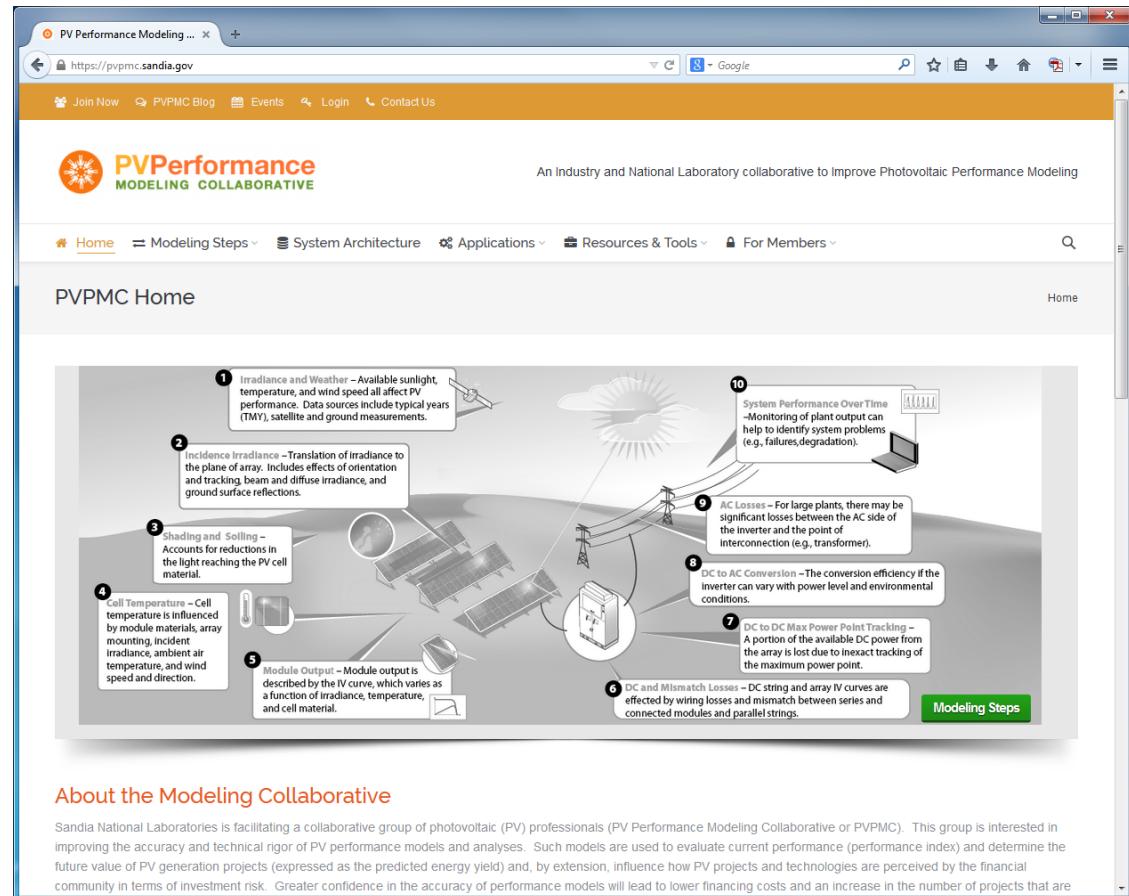
# PV Performance Modeling Collaborative



- Find it at <http://pvpmc.sandia.gov>
- Started after 1st PV Performance Modeling Workshop (Albuquerque, NM, Sept. 2010)
- PV performance modeling lacked organization.
  - Accurate information about algorithms, validation data, best practices difficult to find and access.
- PVPMC.org started to provide an information hub on PV performance modeling
  - Model agnostic, focus on algorithms, methods, data, etc.
  - Detailed Modeling Steps (online textbook)
  - Modeling function library in Matlab [and Python](#) (PV\_LIB)
  - Member contact list, document library, bibliography, glossary, blog, events, ...
- 2<sup>nd</sup> PV Performance Modeling Workshop (Santa Clara, CA, May 2013)
- 3<sup>rd</sup> PV Performance Modeling Workshop (Santa Clara, CA, May 2014)
- 4<sup>th</sup> PV Performance Modeling Workshop (Cologne, Germany, Oct. 22-23 2015)
  - Registration open at [www.tuv.com/solarenergy](http://www.tuv.com/solarenergy)

# Website: <http://pvpmc.sandia.gov>

- 2058 Members (and growing)
- 10,000 to 15,000 visits per month
- 205 web pages published



PV Performance  
MODELING COLLABORATIVE

An Industry and National Laboratory collaborative to Improve Photovoltaic Performance Modeling

Home Modeling Steps System Architecture Applications Resources & Tools For Members

PVPMC Home

1 Irradiance and Weather – Available sunlight, temperature, and wind speed all affect PV performance. Data sources include typical years (TMY), satellite and ground measurements.

2 Incidence Irradiance – Translation of irradiance to the plane of array. Includes effects of orientation and tracking, beam and diffuse irradiance, and ground surface reflections.

3 Shading and Soiling – Accounts for reductions in the light reaching the PV cell material.

4 Cell Temperature – Cell temperature is influenced by module materials, array mounting, incident irradiance, ambient air temperature, and wind speed and direction.

5 Module Output – Module output is described by the IV curve, which varies as a function of irradiance, temperature, and cell material.

6 DC to AC Conversion – The conversion efficiency of the inverter can vary with power level and environmental conditions.

7 DC to DC Max Power Point Tracking – A portion of the available DC power from the array is lost due to inexact tracking of the maximum power point.

8 DC and Mismatch Losses – DC string and array IV curves are effected by wiring losses and mismatch between series and connected modules and parallel strings.

9 AC Losses – For large plants, there may be significant losses between the AC side of the inverter and the point of interconnection (e.g., transformer).

10 System Performance Over Time – Monitoring of plant output can help to identify system problems (e.g., failures, degradation).

**Modeling Steps**

About the Modeling Collaborative

Sandia National Laboratories is facilitating a collaborative group of photovoltaic (PV) professionals (PV Performance Modeling Collaborative or PVPMC). This group is interested in improving the accuracy and technical rigor of PV performance models and analyses. Such models are used to evaluate current performance (performance index) and determine the future value of PV generation projects (expressed as the predicted energy yield) and, by extension, influence how PV projects and technologies are perceived by the financial community in terms of investment risk. Greater confidence in the accuracy of performance models will lead to lower financing costs and an increase in the number of projects that are

When you join you will set up a *username* and *password*

# Standard Modeling Steps (PVPMC)



## Irradiance and Weather

- [Definitions and Overview](#)
- [Sun Position](#)
  - [Solar Position Algorithm \(SPA\)](#)
  - [Simple models](#)
  - [Sandia's code](#)
- [Irradiance and Isolation](#)
  - [Extraterrestrial radiation](#)
  - [Air Mass](#)
  - [Direct Normal Irradiance](#)
    - [DISC Model](#)
    - [DIRINT Model](#)
  - [Global Horizontal Irradiance](#)
  - [Diffuse Horizontal Irradiance](#)
  - [Spectral Content](#)
    - [AM 1.5 Standard Spectrum](#)
  - [Satellite derived data](#)
- [Weather Observations](#)
  - [Air Temperature](#)
  - [Wind Speed and Direction](#)
  - [Precipitation](#)
  - [Air Pressure](#)
- [Irradiance Data Sources for Performance Modeling](#)
  - [National Solar Radiation Database](#)
  - [Typical Meteorological Years](#)
  - [Site-Specific Data](#)
  - [Measure Correlate Predict](#)
  - [Irradiance Modeling](#)
- [Uncertainty and Variability](#)
  - [Characterization of Irradiance Variability](#)
    - [Interannual variability](#)
    - [Short-term variability](#)
    - [Spatial variability](#)
  - [Clear Sky Irradiance models](#)

## Incident Irradiance

- [Definitions and Overview](#)
- [Array Orientation](#)
  - [Fixed tilt](#)
  - [Single Axis Tracking](#)
    - [1-Axis Horizontal Roll](#)
    - [1-Axis Tilted Roll](#)
    - [1-Axis Equatorial](#)
  - [Two-Axis Tracking](#)
    - [2-Axis Azimuth-Elevation](#)
    - [2-Axis Polar](#)
    - [2-Axis Tilt-Roll](#)
  - [Array Orientation Errors](#)
    - [Effect of Array Tilt Errors](#)
    - [Effect of Array Azimuth Errors](#)
- [Plane of Array \(POA\) Irradiance](#)
  - [Measuring POA Irradiance](#)
  - [Calculating POA Irradiance](#)
    - [POA Beam](#)
    - [Angle of Incidence](#)
    - [POA Ground Reflected](#)
      - [Albedo](#)
    - [POA Sky Diffuse](#)

- » [Isotropic Sky Diffuse Model](#)
- » [Simple Sandia Sky Diffuse Model](#)
- » [Hay Sky Diffuse Model](#)
- » [Reindl Sky Diffuse Model](#)
- » [Perez Sky Diffuse Model](#)

## Shading, Soiling, and Reflection Losses

- [Definitions and Overview](#)
- [Shading](#)
  - [Far Shading](#)
  - [Near Shading](#)
- [Soiling and Snow](#)
  - [Soil Monitoring Studies](#)
  - [Snow Effects](#)
- [Incident Angle Reflection Losses](#)
  - [Physical Model of IAM](#)
  - [ASHRAE Model](#)
  - [Martin and Ruiz IAM Model](#)
    - [Soiling effects on Incident Angle Losses](#)
  - [Sandia Model](#)

## Cell Temperature

- [Definitions and Overview](#)
- [Module Temperature](#)
  - [Thermocouple](#)
  - [Voc method](#)
  - [Sandia Module Temperature Model](#)
  - [Faiman Module Temperature Model](#)
- [Cell temperature](#)
  - [Sandia Cell Temperature Model](#)
  - [PVsyst Cell Temperature Model](#)
  - [Transient Cell Temperature Models](#)

## Module IV Curve

- [Definitions and Overview](#)
- [Effective Irradiance](#)
  - [Spectral Mismatch](#)
- [Single Diode Equivalent Circuit Models](#)
  - [De Soto "Five-Parameter" Module Model](#)
  - [PVsyst Module Model](#)
- [Point-value models](#)
  - [Sandia PV Array Performance Model](#)
  - [Loss Factor Model](#)
  - [PVWatts](#)
    - [Improvements to PVWatts](#)

## DC and Mismatch Losses

- [Definitions and Overview](#)
- [Module IV Curves](#)
- [String IV Curves](#)
  - [String Mismatch Losses](#)
- [Array IV Curves](#)
  - [Array Mismatch Losses](#)
- [DC Wiring Losses](#)

## Uncertainty and Validation Studies

### Maximum Power Point Tracking

- [Definitions and Overview](#)
- [Array Utilization](#)
- [MPPT Voltage](#)
- [MPPT Efficiency](#)
- [MPPT Algorithms](#)
- [Uncertainty and Validation](#)

### DC to AC Conversion

- [Definitions and Overview](#)
- [Inverter Efficiency](#)
  - [IEC Inverter Test Protocol](#)
  - [Operating Temperature](#)
  - [Sandia Inverter Model](#)
  - [Driesse Inverter Model](#)
- [Inverter Saturation](#)
- [Loss of Grid](#)
- [Advanced Inverter Features](#)
  - [Power Factor Control](#)
- [Uncertainty and Validation](#)

### AC Losses

- [Definitions and Overview](#)
- [AC Wiring Losses](#)
- [Transformer Losses](#)

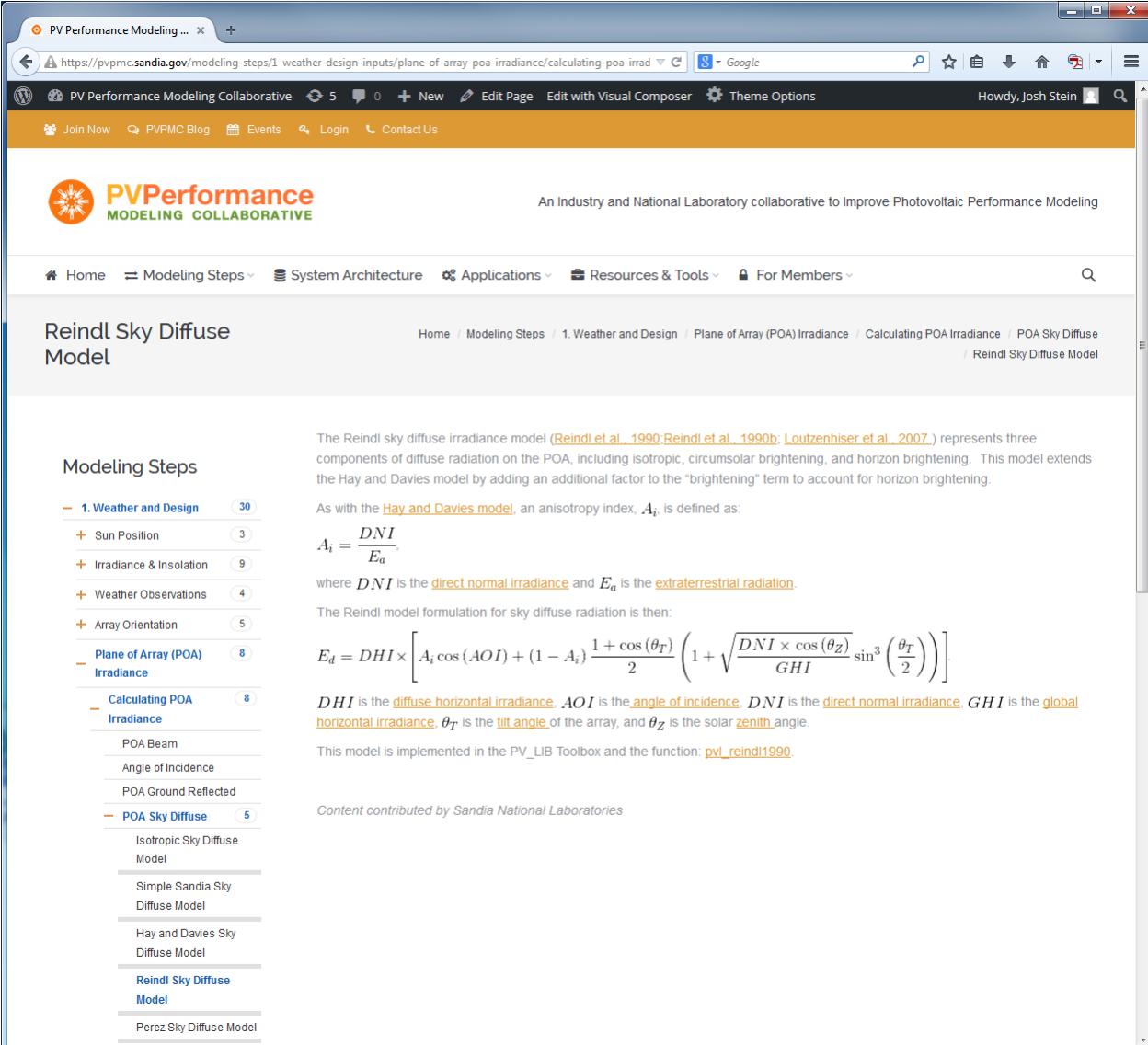
### PV System Output

- [Definitions and Overview](#)
- [PV System Monitoring](#)
  - [Monitoring Equipment](#)
  - [Data Filtering](#)
  - [Data Filling](#)
- [PV Performance Metrics](#)
  - [Performance Ratio](#)
  - [Performance Index](#)
  - [Annual Yield](#)
- [PV Systems Operations and Maintenance](#)
  - [Definitions and Overview](#)
  - [Availability](#)
  - [Failure Mode and Rates](#)

### References

# Example Model Description

- Brief description
- Equation support
- Hyperlinking
- Link to PV\_LIB functions
- References
- Contributor info
  
- We are looking for additional models and process descriptions



The screenshot shows a web browser displaying the PV Performance Modeling Collaborative website. The page title is "Reindl Sky Diffuse Model". The left sidebar lists "Modeling Steps" including "1. Weather and Design" (30 items), "Plane of Array (POA) Irradiance" (8 items), and "POA Sky Diffuse" (5 items). The main content area describes the Reindl sky diffuse irradiance model, which represents three components of diffuse radiation on the POA. It extends the Hay and Davies model by adding a factor for horizon brightening. The formula for sky diffuse radiation is given as  $E_d = DHI \times \left[ A_i \cos(AOI) + (1 - A_i) \frac{1 + \cos(\theta_T)}{2} \left( 1 + \sqrt{\frac{DNI \times \cos(\theta_Z)}{GHI}} \sin^3\left(\frac{\theta_T}{2}\right) \right) \right]$ . The text also mentions that  $DHI$  is diffuse horizontal irradiance,  $AOI$  is angle of incidence,  $DNI$  is direct normal irradiance,  $GHI$  is global horizontal irradiance,  $\theta_T$  is tilt angle, and  $\theta_Z$  is zenith angle. The model is implemented in the PV\_LIB Toolbox with the function `pvl_reindl1990`. The page footer credits "Content contributed by Sandia National Laboratories".

# PV Performance Modeling Steps

**1. Irradiance and Weather** – Available sunlight, temperature, and wind speed all affect PV performance. Data sources include typical years (TMY), satellite and ground measurements.

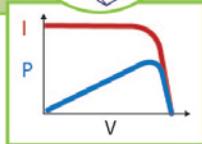


**2. Incidence Irradiance** – Translation of irradiance to the plane of array. Includes effects of orientation and tracking, beam and diffuse irradiance, and ground surface reflections.

**3. Shading and Soiling** – Accounts for reductions in the light reaching the PV cell material.



**4. Cell Temperature** – Cell temperature is influenced by module materials, array mounting, incident irradiance, ambient air temperature, and wind speed and direction.

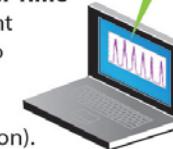


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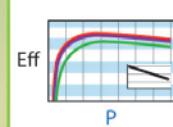


**6. DC and Mismatch Losses** – DC string and array IV curves are affected by wiring losses and mismatch between series connected modules and parallel strings.

**10. System Performance Over Time** – Monitoring of plant output can help to identify system problems (e.g., failures, degradation).



**9. AC Losses** – For large plants, there may be significant losses between the AC side of the inverter and the point of interconnection (e.g., transformer).



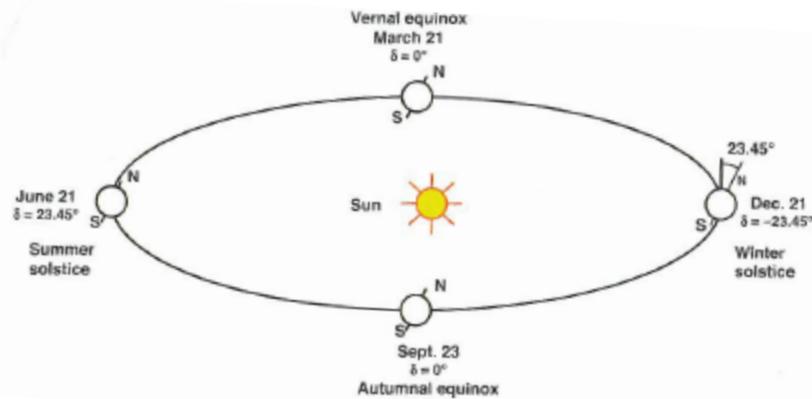
**8. DC to AC Conversion** – The conversion efficiency of the inverter can vary with power level and environmental conditions.

**7. DC to DC Max Power Point Tracking** – A portion of the available DC power from the array is lost due to inexact tracking of the maximum power point.

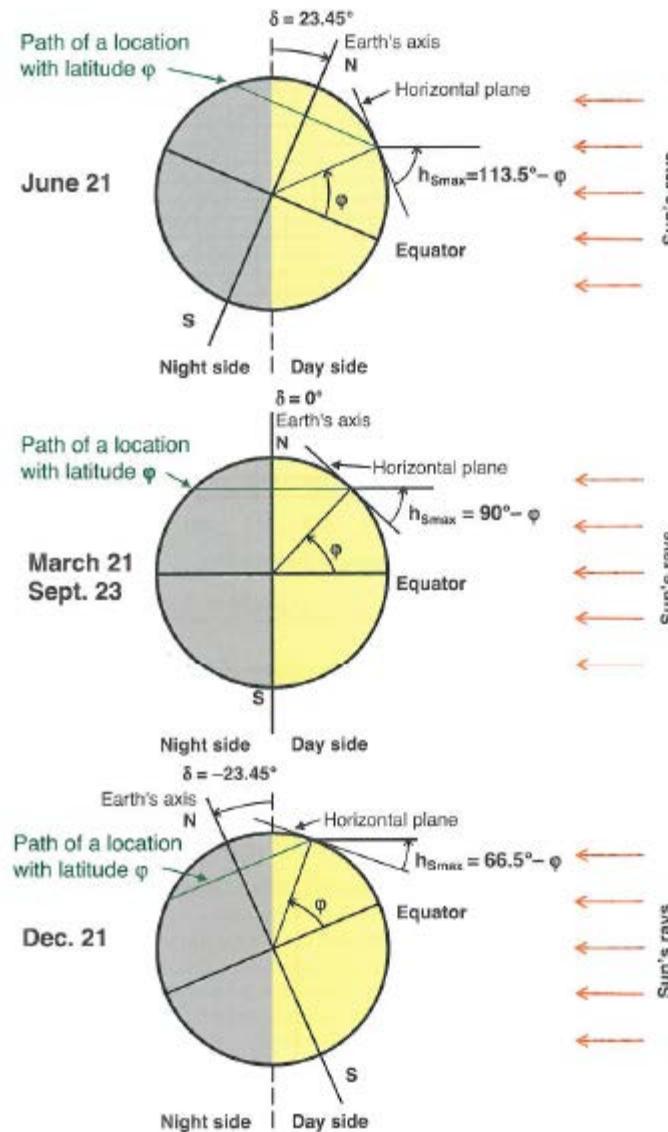
# Earth-Sun System

## Two Important Facts

- Earth's axis is tilted (23.45 deg) relative to Earth's orbital plane
  - Seasons!
- Orbit is elliptical (closest on Jan 4)
  - Affects extraterrestrial irradiance (6-7%)  
(1,415-1,322 W/m<sup>2</sup>)



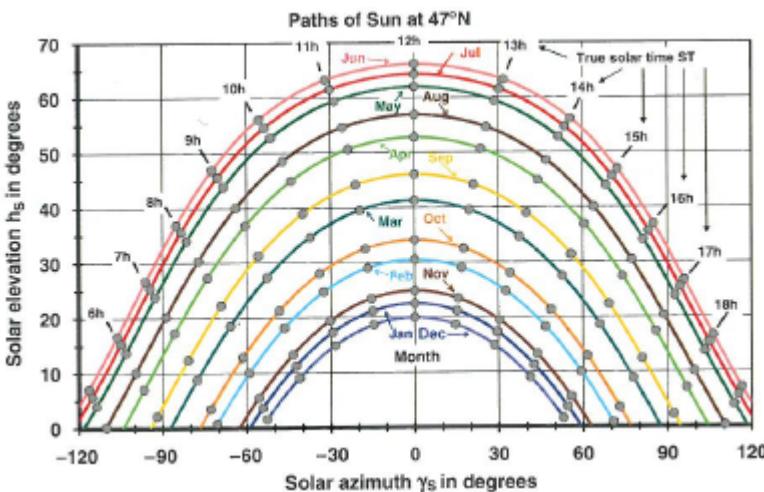
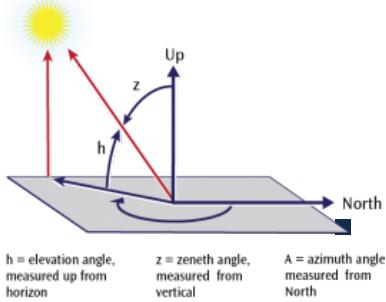
Source: Häberlin, 2012



Source: Häberlin, 2012

# Solar Position

- Solar position relative to an observer on Earth is a critical input to PV performance models.
- Imbedded in PV simulation programs
- Described with:
  - Sun Elevation Angle
    - Zenith = 90-elevation angle)
  - Sun Azimuth Angle



Source: Häberlin, 2012

## Example Algorithms

- Various online calculators
  - <http://www.esrl.noaa.gov/gmd/grad/solcalc/azel.html>
  - <http://solardat.uoregon.edu/SolarPositionCalculator.html>
  - <http://www.pveducation.org/pvcdrom/properties-of-sunlight/sun-position-calculator>
  - <http://www.suncalc.net>
  - [http://www.sunearthtools.com/dp/tools/pos\\_sun.php](http://www.sunearthtools.com/dp/tools/pos_sun.php)

## NREL Solar Position Algorithm (SPA) (also available in PV\_LIB)

- “Gold Standard” (Most Accurate)
- NREL Solar Position Algorithm (SPA) (also available in PV\_LIB)

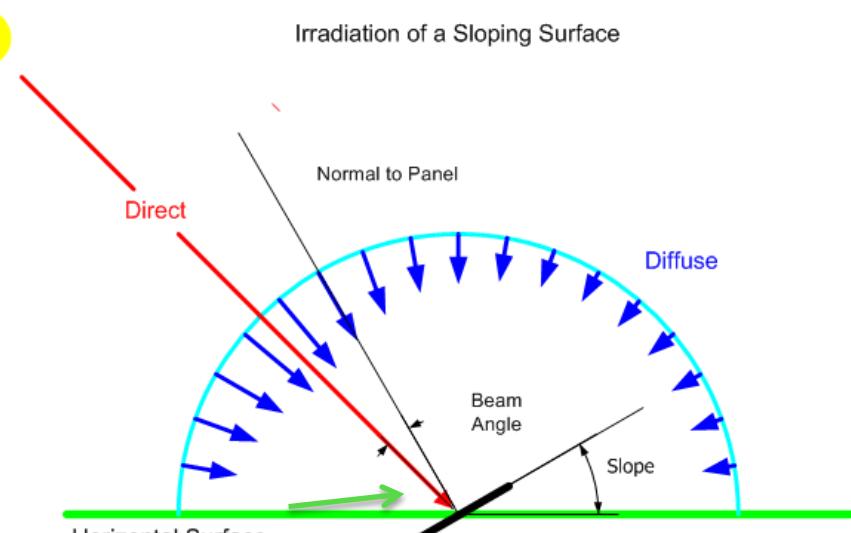
PV\_LIB functions

- `pvl_spa`
- `pvl_ephemeris`

# Irradiance Components

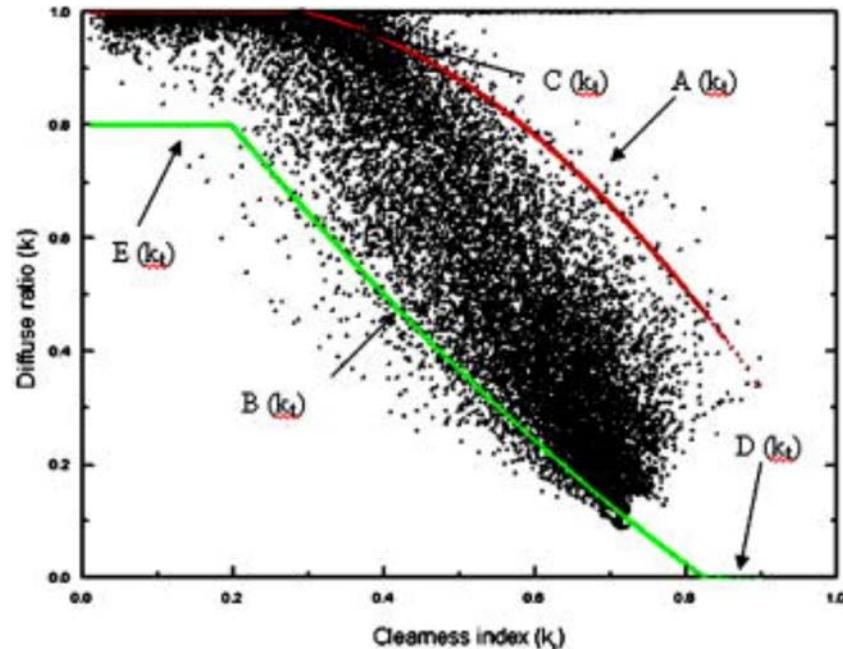
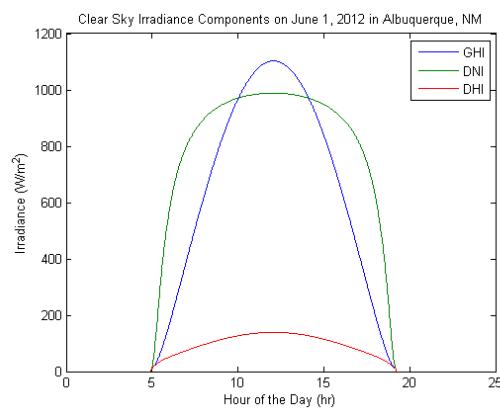
## Reference Quantities

- Direct Normal Irradiance (DNI)
  - Light hitting a plane normal to the sun's rays that comes directly from the sun.
- Global Horizontal Irradiance (GHI)
  - All light hitting a horizontal plane
  - Horizontal beam irradiance =  $DNI * \cos(\text{Zenith Angle})$
- Diffuse Horizontal Irradiance (DHI)
  - Light hitting a horizontal plane that does NOT come directly from the sun
- Albedo
  - Relative reflectivity of the ground surface (usually  $\sim 0.2$ , which means about 20% of the light hitting the ground is reflected)



# More Irradiance Concepts

- Decomposition models
  - Timescale matters (1-min, 1-hr, 1-day)
  - Estimate DNI from GHI
    - Erbs model
    - DISC model
    - DIRINT model
    - Many more...
- Extraterrestrial radiation
  - Irradiance outside atmosphere
- Clear Sky Irradiance Models
  - Assumes atmosphere but no clouds



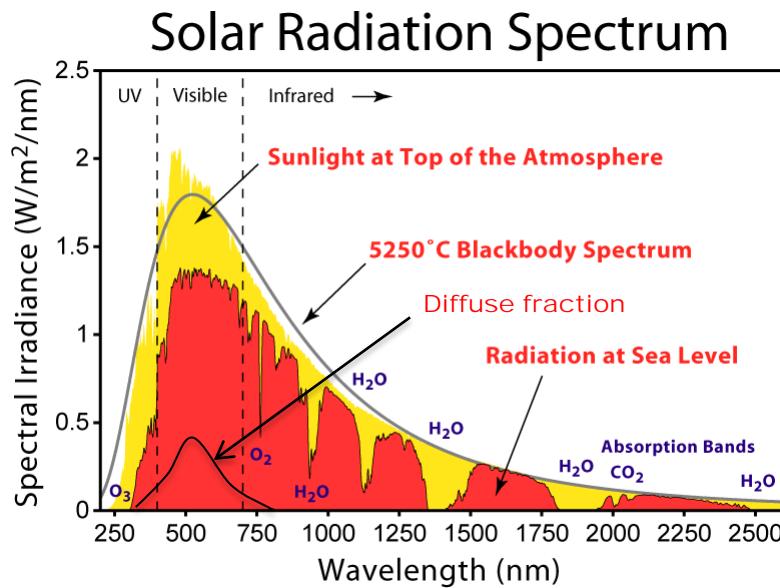
Source: J. Sol. Energy Eng.. 2005;128(1):104-117. doi:10.1115/1.2148972

## Example PV\_LIB functions

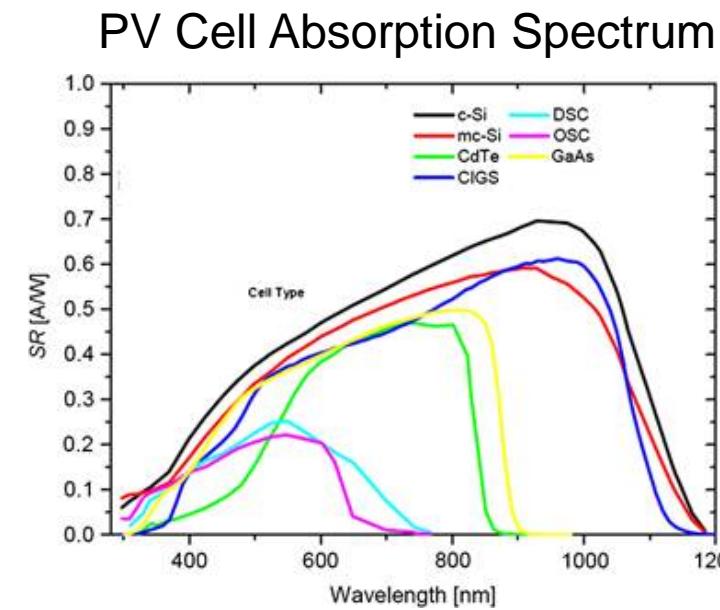
- `pvl_disc`
- `pvl_dirint`
- `pvl_extraradiation`
- `pvl_clearsky_haurwitz`
- `pvl_clearsky_ineichen`
- `pvl_erbs, pvl_louche, pvl_orgill_hollands, pvl_reindl_1, pvl_reindl_2`

# Solar Spectrum

- Sunlight has a spectrum is influenced by the sun and thickness and composition of the atmosphere.
- PV cell technologies respond to the spectral range differently
- PV is rated a standard spectrum (AM1.5 – computer model)



- CdTe and GaAs cells do not respond to wavelengths above ~950 nm.
- c-Si and CIGS do respond.
- Because both are rated at same spectrum, performance differences do occur (H<sub>2</sub>O).
- Spectral mismatch accounts for differences.



# Air Mass

- Air mass is a relative measure the optical length or thickness of the atmosphere. It is used as a proxy for spectral changes in sunlight at the ground.
- At sea level, with the sun is directly overhead (zenith angle = 0) the air mass is equal to 1. As the zenith angle becomes larger, the path of direct sunlight through the atmosphere grows longer and air mass increases. In contrast, as land elevation increases, the thickness of the atmosphere lessens and the air mass is reduced.
- The simplest estimate of relative air mass (ignoring land elevation effects) assumes a spherical earth and atmosphere. The relative air mass is simply a trigonometric function of the zenith angle:

$$AM = \frac{1}{\cos(Z)}$$

- Absolute air mass (AMa) includes effects of elevation.
- PV modules are rated at AM1.5

## PV\_LIB functions

- `pvl_pres2alt`
- `pvl_alt2pres`
- `pvl_relativeairmass`
- `pvl_absoluteairmass`

# 1. Irradiance and Weather Data

- One of the primary inputs for a PV performance model
  - e.g., 8760 hourly values of **irradiance**, temperature, precipitation, wind speed, etc.
  - Three options to choose from:
    - Typical years (Irradiance is mostly modeled from other measurements)
    - Satellite modeled data (everywhere, indirect measurement)
    - Ground measurements from site (short time period, accurate)
  - Varies with time and location (and instruments used for measurements). Data quality is important
  - Largest source of uncertainty in PV performance modeling

# Irradiance and Weather Data

- NSRDB '61-90, '91-10, TMY2/3  
[http://rredc.nrel.gov/solar/old\\_data/nsrdb/](http://rredc.nrel.gov/solar/old_data/nsrdb/)
  - Many years of hourly values (most are modeled)
  - “Average” months are selected from collection to develop a TMY.
  - TMY2 (237 locations) 1961-1990
  - TMY3 (1,454 locations) 1991-2005
    - 1991-2010 Update available
- NSRDB 2005 – 2012 (beta)  
<https://mapsbeta.nrel.gov/nsrdb-data-viewer/>
  - 30 min., 2km grid
  - New NREL GSIP algorithm for irradiance from GOES
  - Includes other meteorological data (air temp, RH, etc.) (model results)
- Purchased satellite irradiance data
  - CleanPowerResearch, Meteonorm, GeoModel, AWSTruepower, ...
  - Validation studies are leading to higher accuracies (e.g., snow)
- Sources for other weather data
  - NOAA National Climatic Data Center (recent years)
- Ground measurements

PV\_LIB functions

- `pvl_readtmy2`
- `pvl_readtmy3`

## 2. Incident Irradiance

### Array Tilt Angle



### Array Azimuth Angle

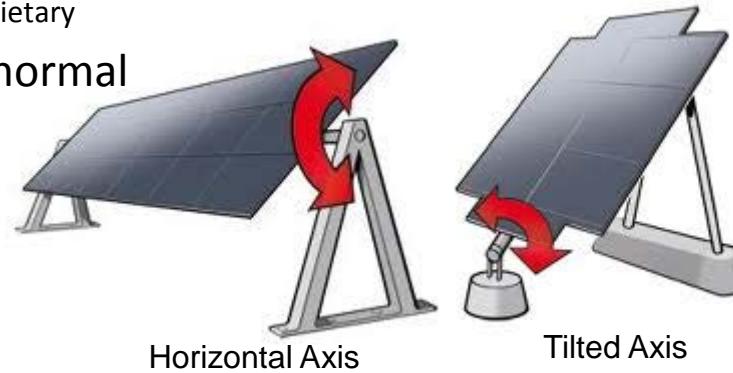


$$AOI = \cos^{-1} [\cos(\theta_Z) \cos(\theta_T) + \sin(\theta_Z) \sin(\theta_T) \cos(\theta_A - \theta_{A,array})]$$

- Single axis tracking moves array to partially follow sun
  - Backtracking methods are usually proprietary
- 2-axis tracking can keep array normal to the sun (AOI=0)

### PV\_LIB functions

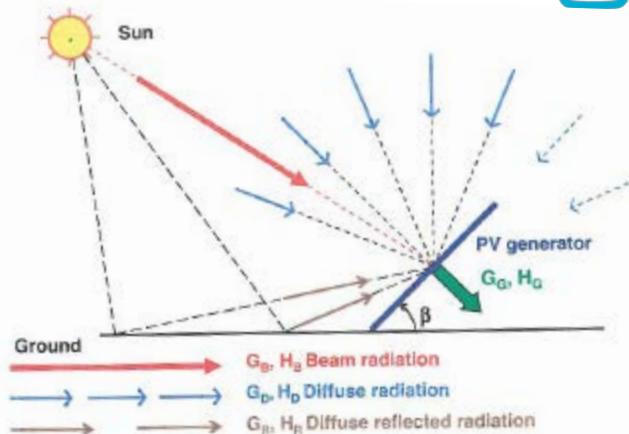
- `pvl_singleaxis`
- `pvl_getaoi`



Vertical Axis

## 2. Incident Irradiance

- Incident irradiance is the light that hits the plane of the array (a.k.a Plane-of-array irradiance).
  - Beam component
  - Sky diffuse component
  - Ground reflected
- Beam irradiance = DNI \* cos(AOI)
- Ground reflected irradiance
  - Array tilt angle
  - Ground surface albedo
    - Grass = 0.15-0.25
    - Snow = 0.5 -0.82



Source: Häberlin, 2012

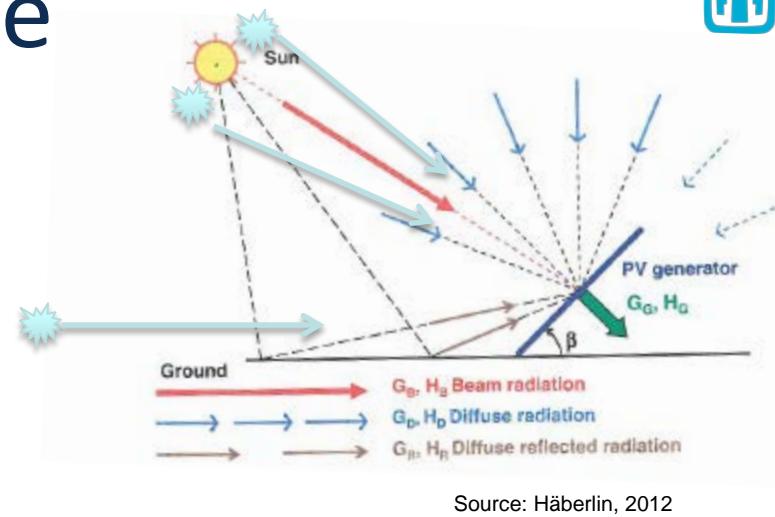
### PV\_LIB functions

- pvl\_getaoi
- pvl\_grounddiffuse
- pvl\_isotropicsky
- pvl\_haydavies1980
- pvl\_klucher1979
- pvl\_perez
- pvl\_kingdiffuse
- pvl\_reindl1990

# 2. Incident Irradiance

## Sky Diffuse Models

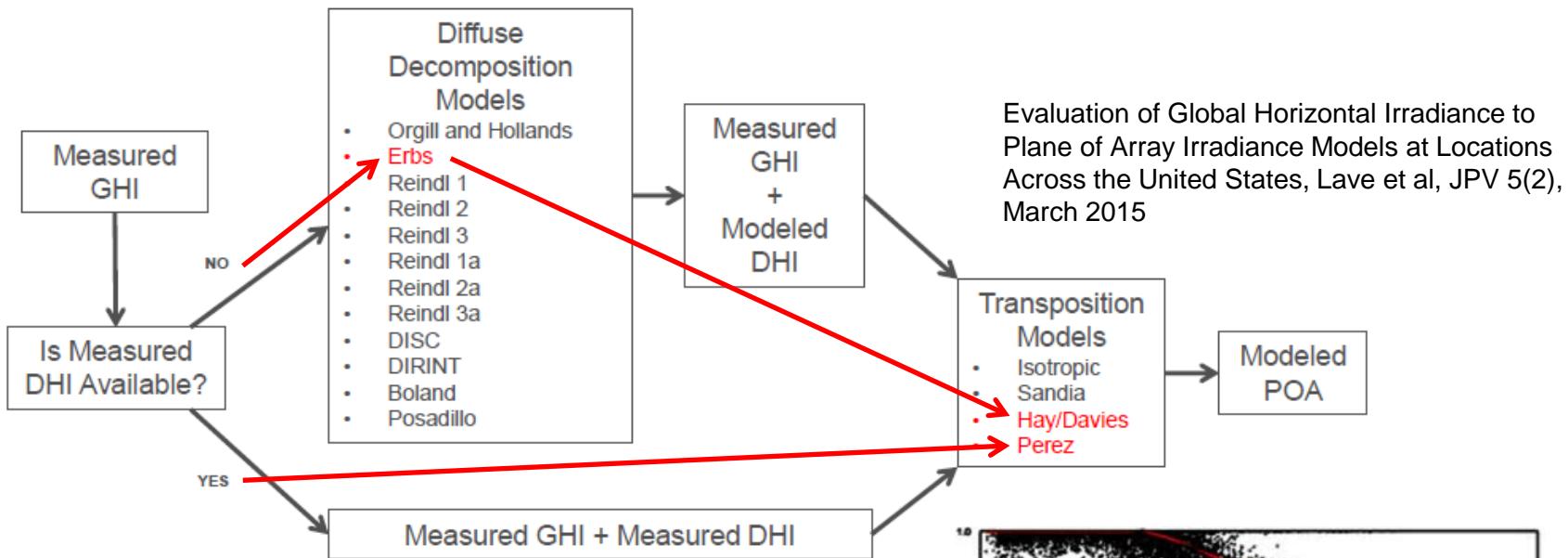
- Diffuse on a tilted plane
- Account for:
  - Circumsolar – forward scattering around sun disk
  - Horizon brightening
  - Rest of sky
- Isotropic model
  - Assumes uniform diffuse light and is geometric
- Hay and Davies model
  - Isotropic model + circumsolar enhancement (PVsyst)



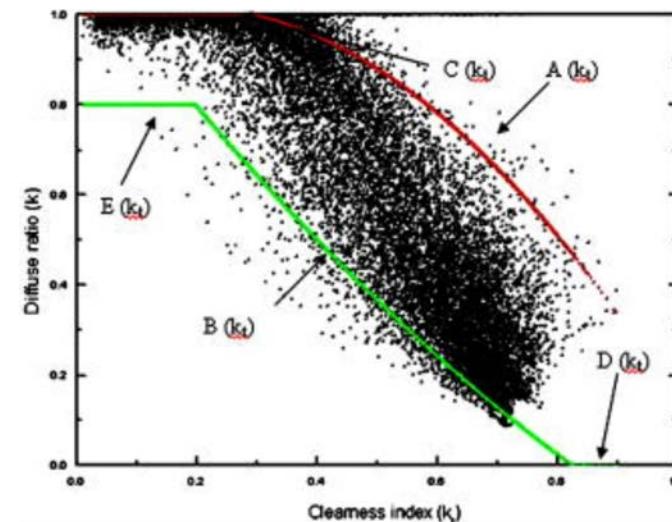
Source: Häberlin, 2012

- Reindl model
  - Isotropic + circumsolar + horizon brightening
- Perez model (1991)
  - Isotropic + circumsolar + horizon brightening, where circumsolar and horizon components are empirical functions based on clearness. Site calibration may be needed. (PVsyst)

# 2. Incident Irradiance Modeling



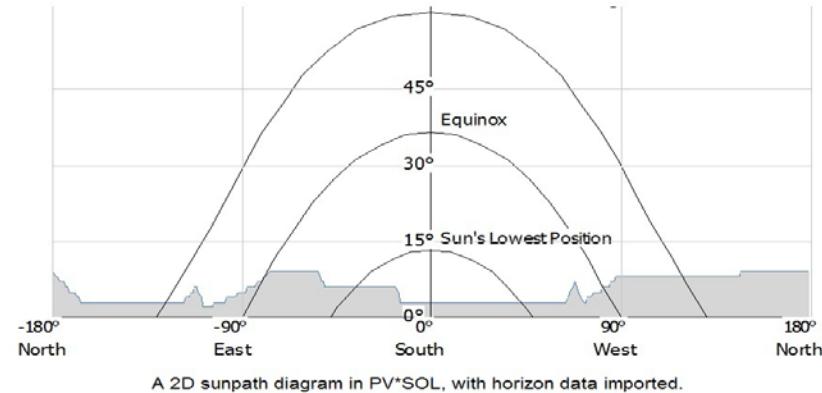
- Diffuse Decomposition
  - Fraction of GHI that is diffuse (direct)
  - Dozens of models in literature
  - Which is best? Not a simple answer
  - General recommendations from mean bias in annual insolation
  - Site-specific empirical model can be best



Source: J. Sol. Energy Eng.. 2005;128(1):104-117. doi:10.1115/1.2148972

# 3. Shading, Soiling, and Reflections

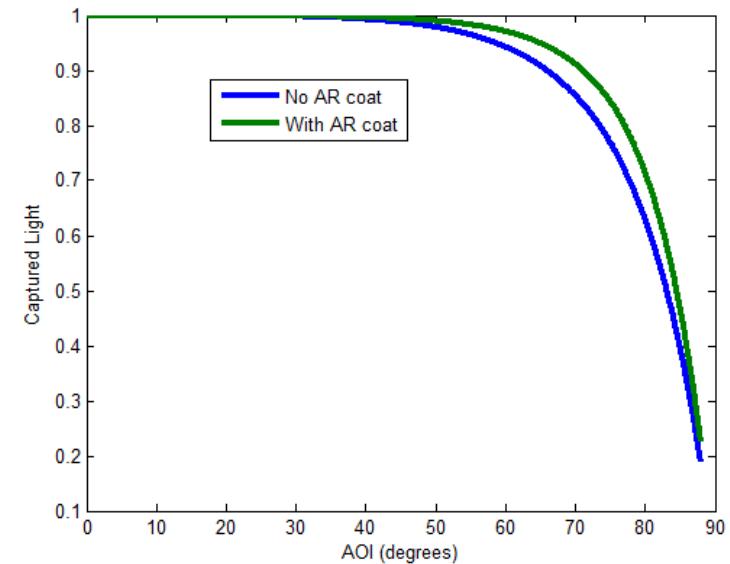
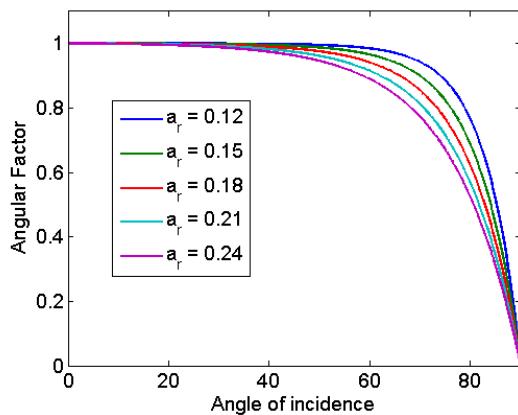
- Not all POA irradiance is available
- Dirt and grime prevent light from getting to the cells (soiling)
- Snow can cover all or part of array (soiling)
  
- Objects and terrain shade array
- Near shade has sharp edges
  - Buildings, trees, appliances, wires, chimney, etc.
  - Row-row shading within array
- Far shade is more diffuse
  - Mountains, horizon



- Shading effects are assigned to certain time periods and irradiance is reduced.
- Partial shading is much more complex. Modeling approaches are still evolving.
- Tools are using design tools to help address shading (e.g. Helioscope and PVsyst). Near field data is required.

# 3. Shading, Soiling, and Reflections

- Reflections are influenced by:
  - Angle of incidence
  - Coatings (e.g., anti-reflective)
  - Soiling
- Reflections models include:
  - Physical (optical) model based on Snell's and Bouguer's laws
  - Empirical models
    - Sandia has used a 5<sup>th</sup> order polynomial form ( $f_2$ )
    - ASHRAE
    - Martin and Ruiz (includes effects of soiling)



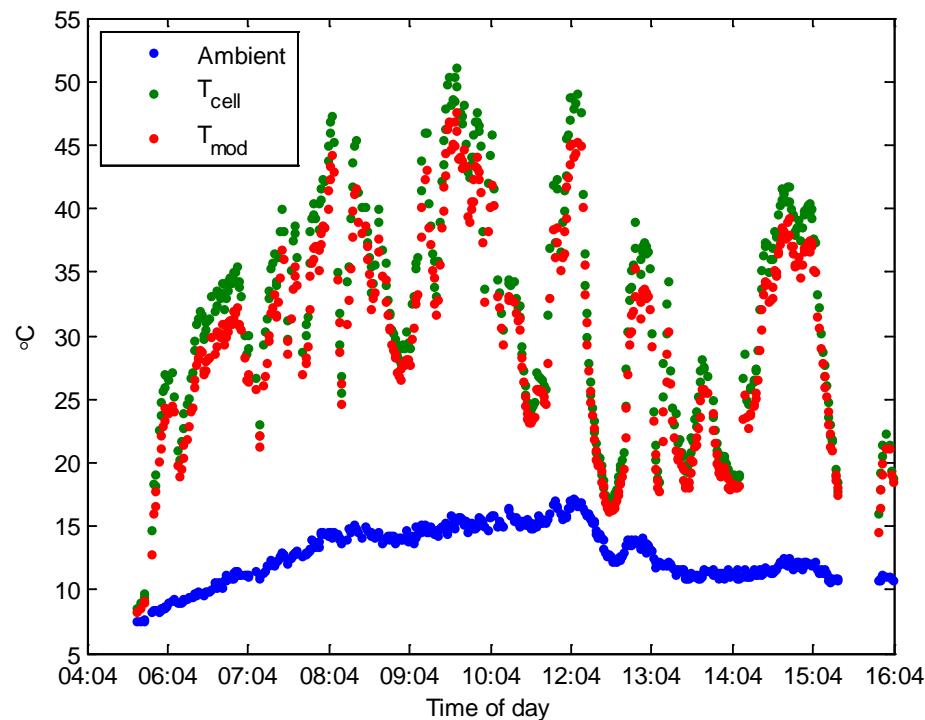
- Simple lookup tables are also being implemented in modeling tools. These may prove to be the best solution.

**PV\_LIB functions (reflection losses)**

- `pvl_physicaliam`
- `pvl_ashraeiam`
- `pvl_martinruiziam`

# 4. Cell Temperature

- Power decreases with increasing cell temperature
  - $-0.3$  to  $-0.5$  %/C (depends on cell tech., module materials)
- Cell temperature difficult to measure directly in situ
  - Can be inferred from  $V_{oc}$  and  $I_{sc}$  (e.g., IEC 60904-5)
  - Thermocouples attached to module backsheet + delta
- Cell temperature  $>$  ambient ( $\sim 30$  C difference)
- Cell temperature  $>$  back-of-module temperature ( $\sim 2$  –  $4$  C)
- Models predict cell temperature from POA irradiance, ambient temperature and wind conditions

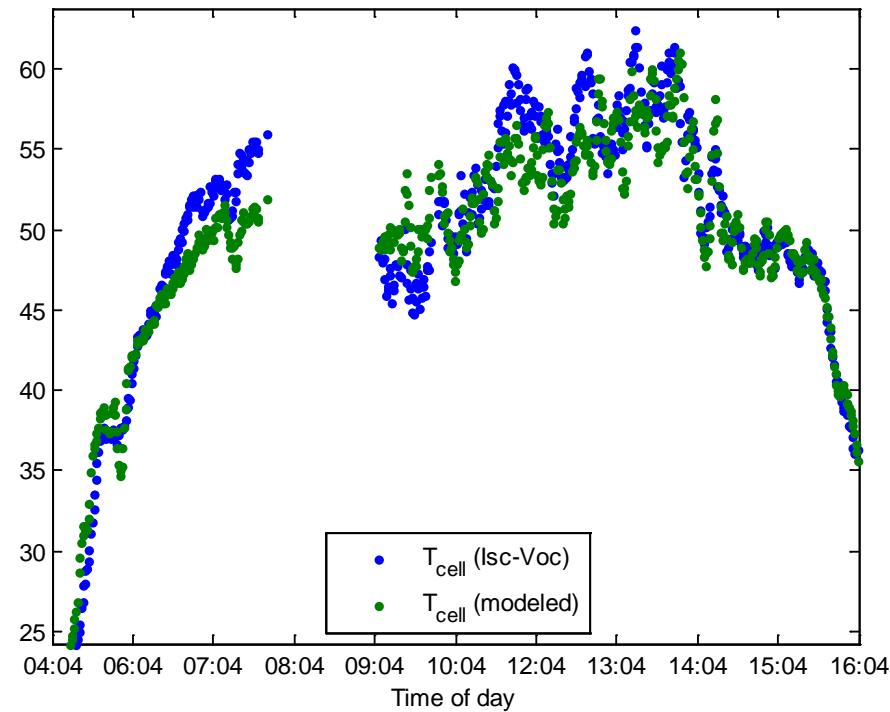


# 4. Cell Temperature Models

- Most are steady-state

$$\begin{aligned} T_C &= T_M + \frac{E}{E_0} \Delta T \\ &= T_{amb} + \frac{E}{E_0} \exp(a + b WS) + \frac{E}{E_0} \Delta T \end{aligned}$$

- Typical assumptions:
  - Represents average cell temperature across module
  - Represents average across an array

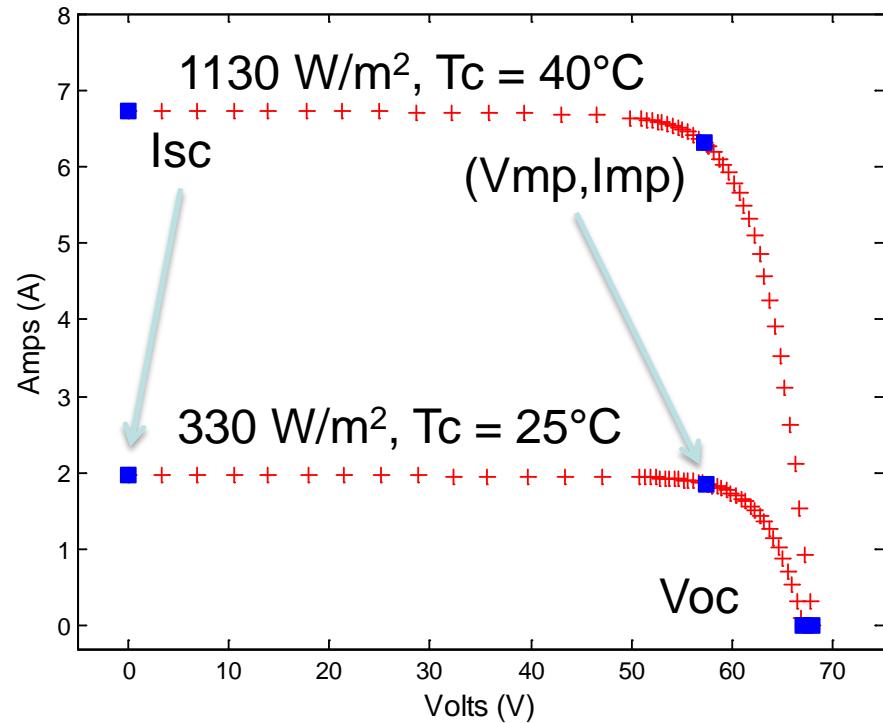


PV\_LIB functions

- `pvl_sapmcelltemp`

# 5. Module Output

- Don't confuse a model with the software that implements it
- Predict DC voltage and current over the range of POA irradiance and cell temperature
  - IV curve models (aka 'diode' models)
    - E.g., '5 parameter model'
  - Point models
    - E.g., Sandia model
  - Simple efficiency
    - E.g., PVWatts



$$P_{dc} = \frac{I_{tr}}{1000} P_{dc0} (1 + \gamma (T_{cell} - T_{ref}))$$

# The Sandia Array Performance Model

- Describes module output at SC, OC and MP points
- As a function of beam and diffuse irradiance ( $E_b$  and  $E_{diff}$ ), cell temperature ( $T_C$ ), air mass ( $AM_a$ ) and angle of incidence ( $AOI$ )
- 14 empirical coefficients, 2 empirical functions ( $f_1$  and  $f_2$ )
- With exception of  $f_2$ , coefficients determined for individual modules

$$E_e = f_1(AM_a) \left( E_b f_2(AOI) + E_{diff} f_d \right) \leftarrow \text{Effective irradiance : light flux that becomes electrical current}$$

$$I_{SC} = I_{SC0} E_e \left( 1 + \alpha_{SC} (T_C - T_0) \right)$$

$$V_{OC} = V_{OC0} + N_S n \delta(T_C) \ln(E_e) + \beta_{OC} (T_C - T_0)$$

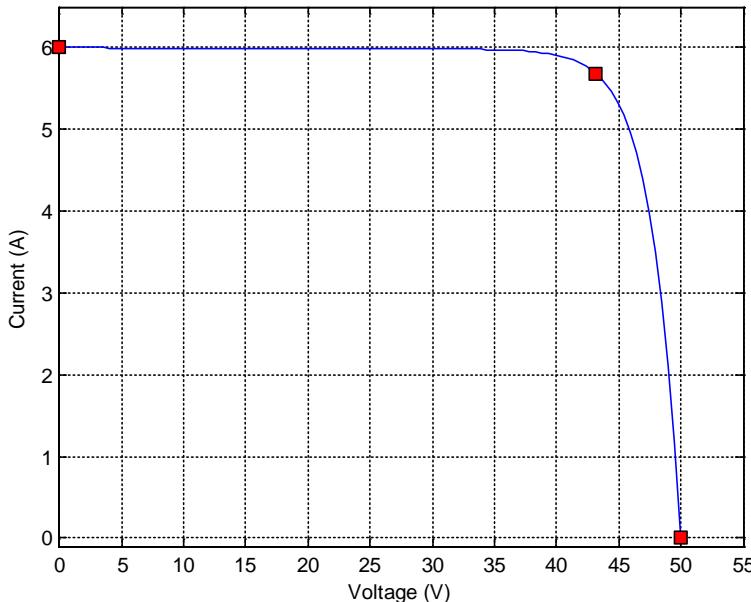
$$V_{MP} = V_{MP0} + C_2 N_S n \delta(T_C) \ln(E_e) + C_3 N_S \left( n \delta(T_C) \ln(E_e) \right)^2 + \beta_{MP} (T_C - T_0)$$

$$I_{MP} = I_{MP0} \left( C_0 E_e + C_1 E_e^2 \right) \left( 1 + \alpha_{MP} (T_C - T_0) \right)$$

PV\_LIB functions  
• pvl\_sapm

# Single Diode Models

- CEC, PVsyst, PV\*SOL, others
  - IV curve described by single diode equation
  - “5 parameters” – for each IV curve
  - Additional equations describe how parameters change with effective irradiance  $E$ , temperature  $T_C$



## PV\_LIB functions

- pvl\_singlediode
- pvl\_calcparams\_desoto

$$I = I_L - I_0 \left[ \exp\left(\frac{V + I R_s}{n V_T}\right) - 1 \right] - \frac{V + I R_s}{R_{sh}}$$

$I_L(E, T_C) = \frac{E}{E_0} [I_{L0} + \alpha_{Isc}(T_C - T_0)]$

$$I_0 = I_{00} \left( \frac{T_C}{T_0} \right)^3 \exp\left( \frac{1}{k} \left( \frac{E_{g0}}{T_0} - \frac{E_g(T_C)}{T_C} \right) \right)$$

$$R_{sh} = R_{sh0} \frac{E_0}{E}$$

$R_s, n$  constant

De Soto et al, 2006

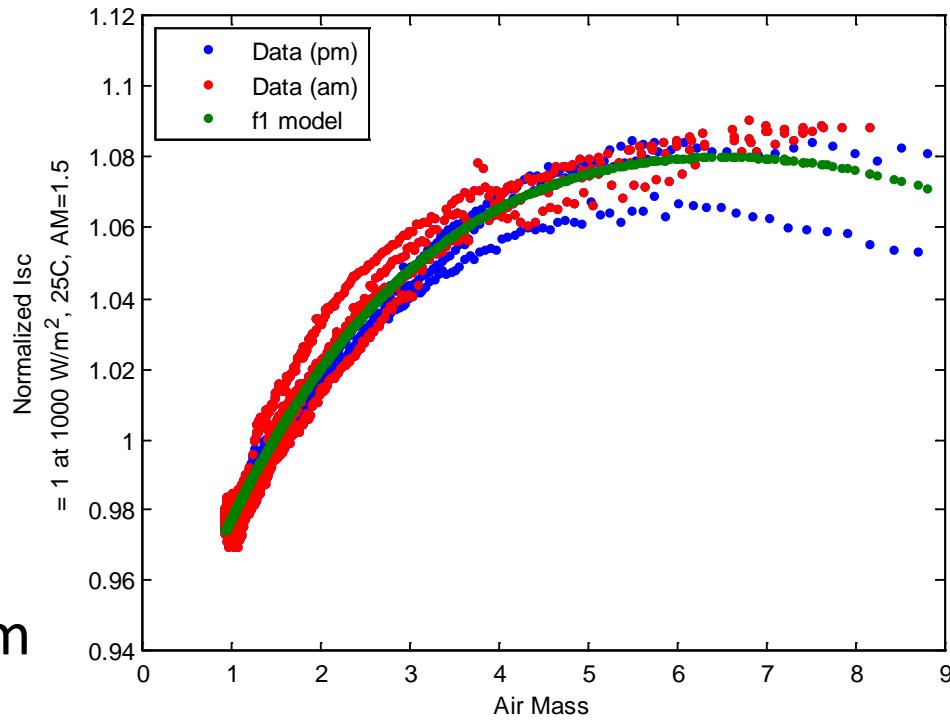
# Effective irradiance

## PV\_LIB functions

- pvl\_relativeairmass
- pvl\_absoluteairmass
- pvl\_sapm

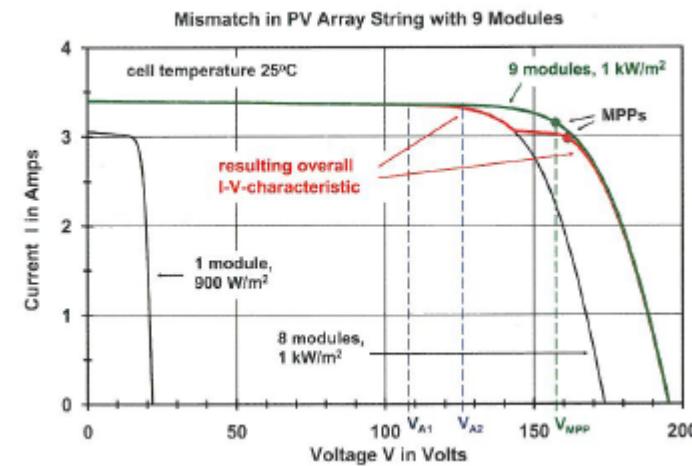
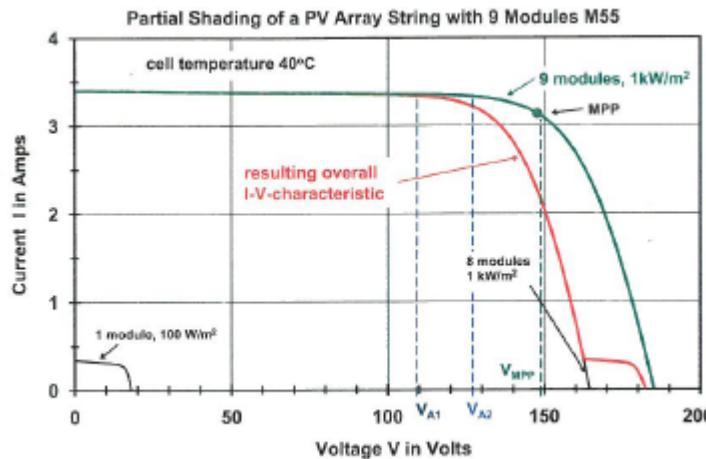
- Accounts for changing spectral content of light and response of cells
- Implemented in different ways
  - Most common, mismatch factor/function
  - Less commonly, convolution of spectrum and spectral response

$$E_e = f_1(AM_a) (E_b f_2(AOI) + E_{diff} f_d)$$



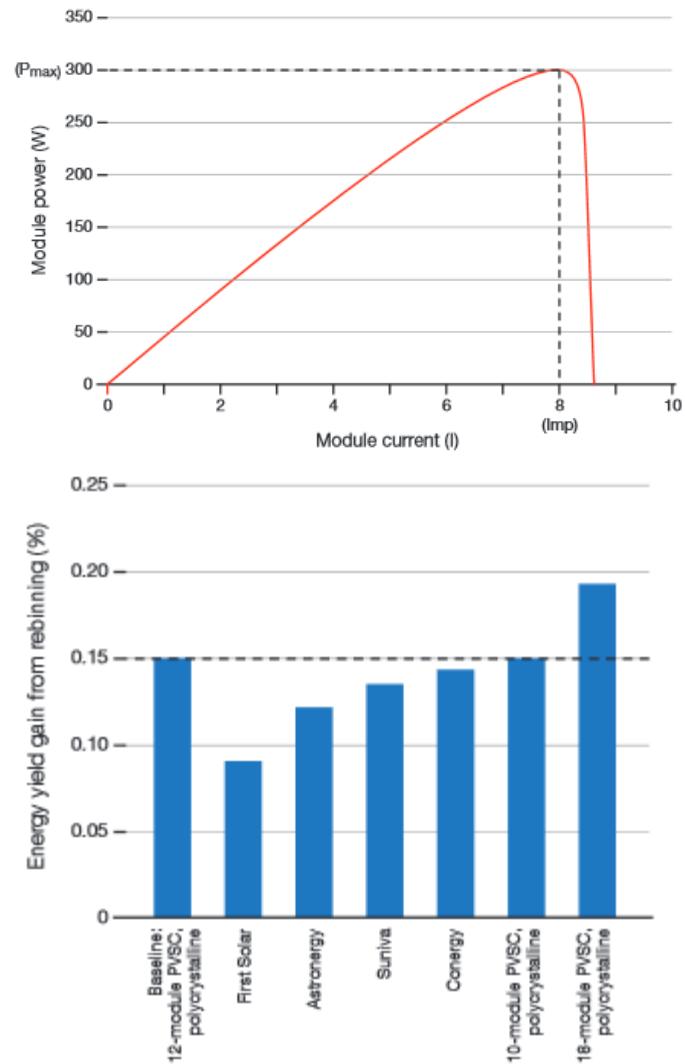
# 6. DC and Mismatch Losses

- DC wiring loss increases with the square of the current and the wire resistance ( $I^2R$ ). Increasing the wire gauge increases the system cost and designers try to calculate an optimal balance between cost and long-term performance.
- Mismatch losses can occur as the result of mismatched modules and strings, but is typically more important when it is caused by partial shading on the array.



# Mismatch from Module Binning?

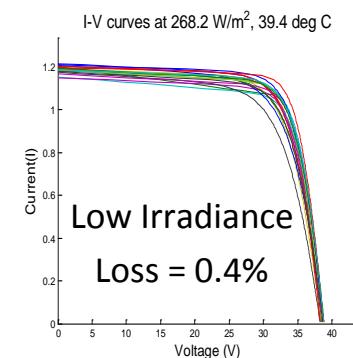
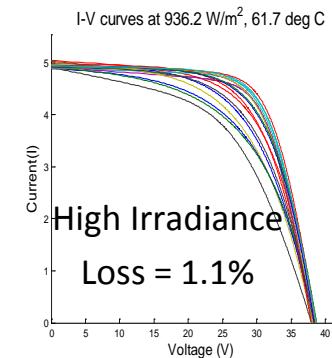
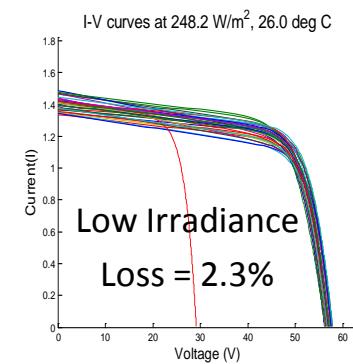
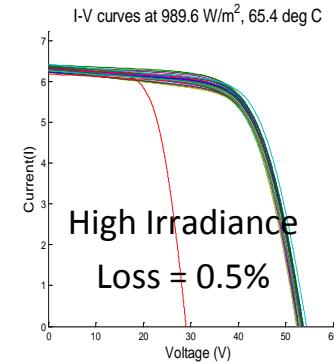
- Many people ask about the effect of module binning tolerance on energy production.
- Most modules are +/- 5% based on power or current.
- Is it worth insisting on tighter bins? Or testing on site?
- Folsom Labs published a study showing that the advantages are very minor.
- Power-current curves are relatively flat at the peak.
- This result also applies to uneven soiling or degradation.



Source: Grana and Gibbs, 2014

# Mismatch Losses and Degradation

- Standard mismatch derate is 1-2%. This appears to be reasonable or even overly conservative for modern arrays.
- Losses appear to change with irradiance. Higher at low irradiance.
- Mismatch losses depend more on an individual array's panels and configuration than on age or technology



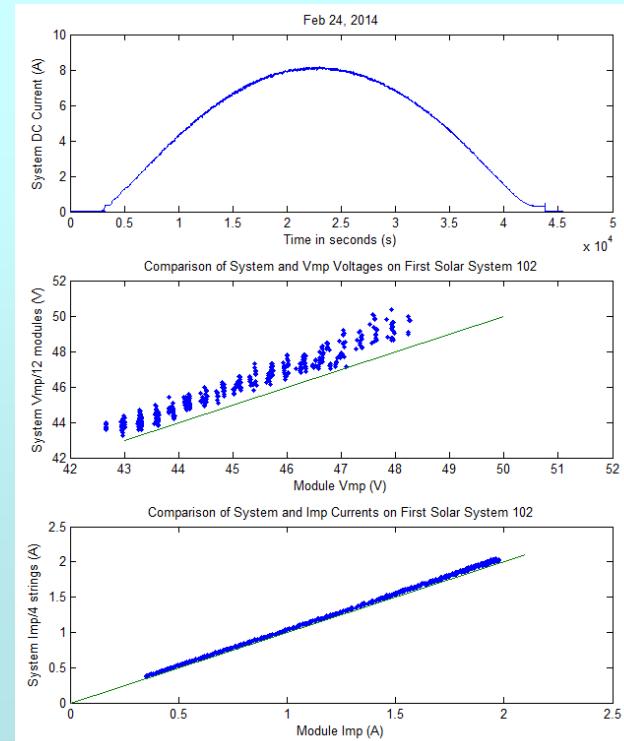
Source: S. MacAlpine, 2013

# 7. DC to DC MPPT

- This step answers the question: “How well can the inverter follow the MPP?”
- EN-50530 describes a test protocol to measure MPPT efficiency but it difficult to measure.
- Nearly all modern inverters can hold MPPT at >99% efficiency!

## Example Field Evaluation:

- We measured module IV curves while simultaneously measuring current and voltage at the inverter of a PV system.
- Inverter dithered +/- about 2V (clear day)
- Offset by approximately 1V is likely measurement error
- Dither increases when irradiance varies



# 8. DC to AC Conversion

- Inverters experience power conversion losses
  - Losses that vary with  $I^2$  (e.g., resistance)
  - Losses that vary with I (e.g., switching, voltage drops)
  - Losses that are constant (e.g., parasitic loads)
- Inverter losses vary with voltage
  - How it varies depends on topology (single/multi stage), input vs. output voltage, and other design factors → modeled empirically



# 8. DC to AC Conversion

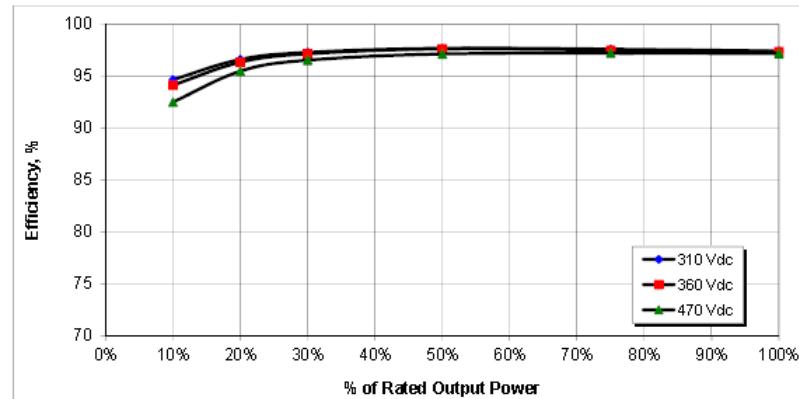
- Input Data: Efficiency measured in a lab at 3 voltages and 6 power levels.

Newer 3-phase, multistage inverter

Vmin: 310 Vdc Vnom: 360 Vdc Vmax: 470 Vdc

| Input Voltage (Vdc) | Power Level (%; kW) |      |      |      |      |      | Wtd  |
|---------------------|---------------------|------|------|------|------|------|------|
|                     | 10%                 | 20%  | 30%  | 50%  | 75%  | 100% |      |
| Vmin                | 310                 | 0.37 | 0.74 | 1.11 | 1.85 | 2.77 | 3.69 |
| Vnom                | 360                 | 94.7 | 96.6 | 97.3 | 97.7 | 97.6 | 97.4 |
| Vmax                | 470                 | 94.1 | 96.4 | 97.2 | 97.6 | 97.5 | 97.3 |

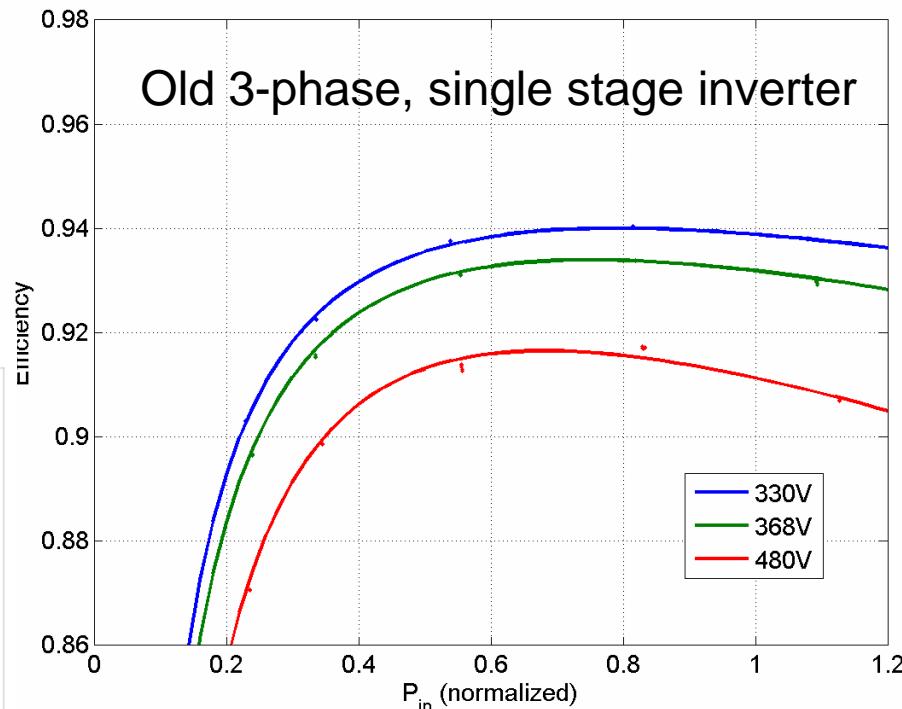
CEC Efficiency = 97.0%



## CEC List of Eligible Inverters

Vmin: 330 Vdc Vnom: 368 Vdc Vmax: 480 Vdc

| Input Voltage (Vdc) | Power Level (%; kW) |      |      |      |      |      | Wtd  |
|---------------------|---------------------|------|------|------|------|------|------|
|                     | 10%                 | 20%  | 30%  | 50%  | 75%  | 100% |      |
| 2.05                | 84.7                | 90.3 | 92.3 | 93.8 | 94.0 | 93.8 | 93.2 |
| 4.10                | 83.9                | 89.7 | 91.6 | 93.1 | 93.4 | 93.0 | 92.5 |
| 6.15                | 81.3                | 87.1 | 89.9 | 91.3 | 91.7 | 90.7 | 90.7 |
| 10.25               |                     |      |      |      |      |      |      |
| 15.37               |                     |      |      |      |      |      |      |
| 20.49               |                     |      |      |      |      |      |      |

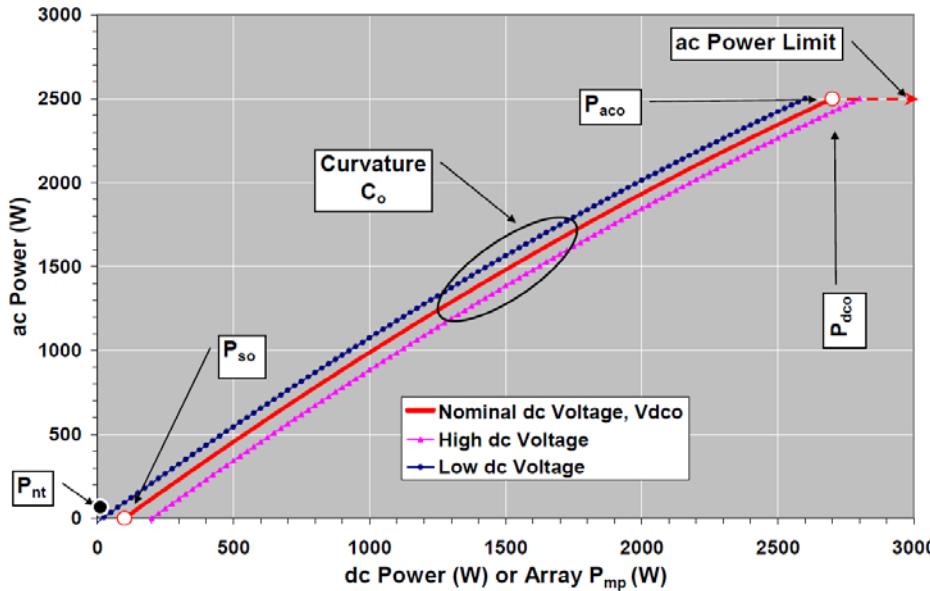


<http://www.gosolarcalifornia.ca.gov/equipment/inverters.php>

# 8. DC to AC Conversion

- Sandia Inverter Performance Model

$$P_{ac} = \left\{ \left( \frac{P_{aco}}{P'_{dco} - P'_{so}} \right) - C'_o (P'_{dco} - P'_{so}) \right\} (P_{dc} - P'_{so}) + C'_o (P_{dc} - P'_{so})^2$$



PV\_LIB functions

- pvl\_snlinverter
- pvl\_snlinverterdb
- pvl\_adrinverter

$$P'_{dco} = P_{dco} \{ 1 + C_1 (V_{dc} - V_{dco}) \}$$

$$P'_{so} = P_{so} \{ 1 + C_2 (V_{dc} - V_{dco}) \}$$

$$C'_o = C_o \{ 1 + C_3 (V_{dc} - V_{dco}) \}$$

- PVsyst does a quadratic interpolation between the 3 CEC efficiency curves.

# 9. AC Losses

- AC losses include transformer and AC cabling conductive losses. These losses are very project specific and depend where the revenue meter is located.
- Some larger projects have to move AC power considerable distances and these losses can be significant.
- Most models assume a fixed percent loss derate.

# 10. Performance over Time

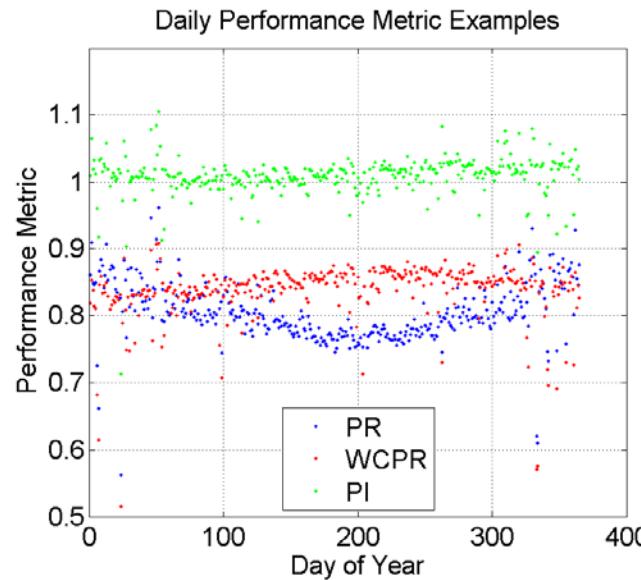
- Long term performance must account for equipment degradation and loss of availability due to grid disturbances and O&M events.
- Degradation is usually expressed as a %/yr reduction (e.g., 0.5%/yr)
- **Performance Ratio (PR)** is AC energy / (DC rating\*sun hours)
  - IEC 61724
  - 500 W/m<sup>2</sup> for 1 hour = 0.5 sun hours
  - PR values are typically ~0.8-0.9
- **“Performance Index” (PI)** is AC energy (measured) / AC energy (predicted) using a performance model.
  - PI values should be close to 1. Analysis of deviations from 1 (residual analysis) can help identify problems with model or system.

# 10. Performance over Time

- **Weather-Corrected Performance Ratio (WCPR)** is AC energy / (DC rating \* sun hours \* temperature correction term)

- Temperature correction =  $\left(1 - \frac{\delta}{100} (T_{cell,avg} - T_{cell})\right)$

- $\delta$  is temperature coefficient for power (%/ degC)
- $T_{cell,avg}$  is the annual average computed cell temperature
- $T_{cell}$  is the cell temperature



Source: Stein and Green, 2015

# 10. Performance over Time

Other reasons PV system performance can deviate from expectations.

- PV systems are required to disconnect from the grid if voltage or frequency deviates from limits (IEEE 1547)
  - Inverters stay off for 5 minutes
  - Neighbor causes voltage fluctuations (utility issue)
- Operation of inverters at non-unity power factor results in decreases in inverter efficiency
- Equipment failures
  - PV systems have many separate components
  - Small proportion of failures may be “invisible” but can contribute to modeling errors when comparing to measured data
- “Availability” is a term used in the energy industry to describe such issues but there is no recognized definition for solar.
  - Is the system available at night?

# PV Performance Modeling Steps

**1. Irradiance and Weather** – Available sunlight, temperature, and wind speed all affect PV performance. Data sources include typical years (TMY), satellite and ground measurements.

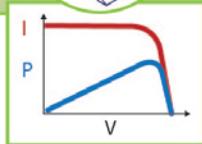


**2. Incidence Irradiance** – Translation of irradiance to the plane of array. Includes effects of orientation and tracking, beam and diffuse irradiance, and ground surface reflections.

**3. Shading and Soiling** – Accounts for reductions in the light reaching the PV cell material.



**4. Cell Temperature** – Cell temperature is influenced by module materials, array mounting, incident irradiance, ambient air temperature, and wind speed and direction.

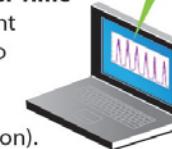


**5. Module Output** – Module output is described by the IV curve, which varies as a function of irradiance, temperature, and cell material.

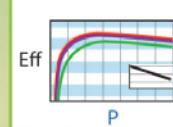


**6. DC and Mismatch Losses** – DC string and array IV curves are affected by wiring losses and mismatch between series connected modules and parallel strings.

**10. System Performance Over Time** – Monitoring of plant output can help to identify system problems (e.g., failures, degradation).



**9. AC Losses** – For large plants, there may be significant losses between the AC side of the inverter and the point of interconnection (e.g., transformer).



**8. DC to AC Conversion** – The conversion efficiency of the inverter can vary with power level and environmental conditions.

**7. DC to DC Max Power Point Tracking** – A portion of the available DC power from the array is lost due to inexact tracking of the maximum power point.

# Thank You!

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