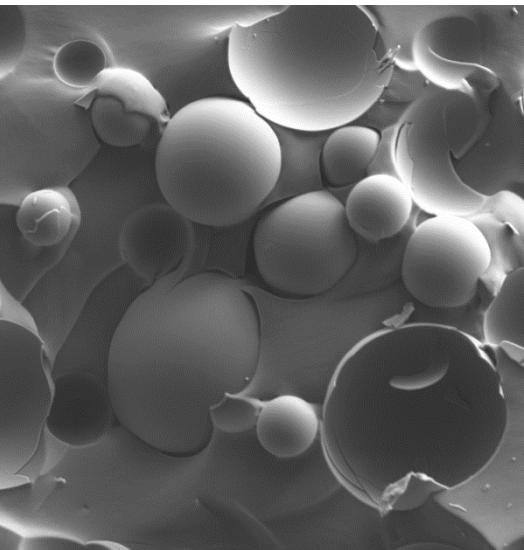


# Mechanical Behavior and Damage Mechanisms of Encapsulant-filled Elastomers



EHT = 10.00 kV   WD = 9.2 mm   Signal A = SE2   Width = 417.6  $\mu$ m



Sandia  
National  
Laboratories

*Exceptional  
service  
in the  
national  
interest*



U.S. DEPARTMENT OF  
**ENERGY**



Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000. SAND NO. 2011-XXXXP

# What is GMB-filled Sylgard®?

- **Syntactic foam**
  - **Sylgard silicone elastomer: Dimethylvinylated and trimethylated silica**
  - **Glass micro-balloons: Hollow spheres of soda-lime borosilicate glass**
- **Used in potting materials to protect components against corrosion, shock, etc.**
- **Glass micro-balloons added for many reasons**
  - **Increase stiffness**
  - **Lower thermal expansion coefficient.**
  - **Decrease density**
  - **Lower cure shrinkage**

	Pure Sylgard	Sylgard GMB (undamaged)
Coefficient of Thermal Expansion (ppm/C)	270	185
Young's Modulus (MPa)	1.84	13
Bulk Modulus (MPa)	920	71
Glass Transition Temperature (°C)	-60	-45

# Sylgard® 184/A16 GMB composition

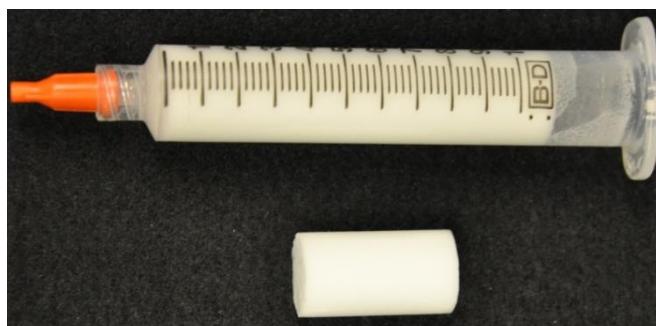
## Sylgard composition

- 100 pbw Sylgard 184 base resin
- 10 pbw Sylgard 184 curing agent
- 10 pbw 3M A16 glass microballoons
- 10 pbw silicone accelerator
- Cured 16 hours at **21°C.**

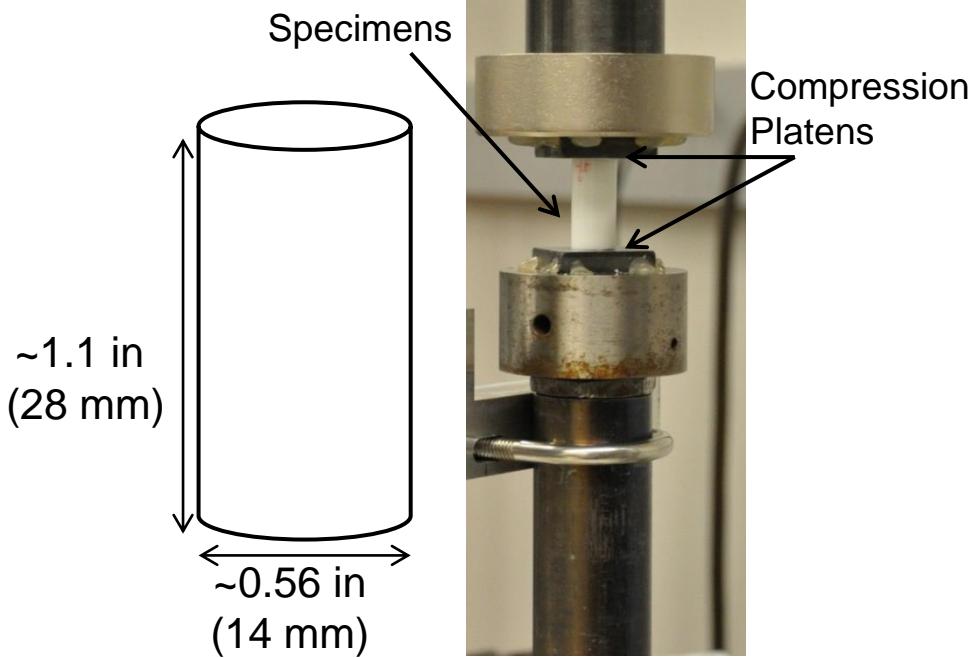
## Sylgard® 184

### 3M A16 Glass Microballoons:

- Target crush strength (90% survival ):  
500 psi, 3.45 MPa
- True Density: 0.16 g/cc
- Average particle size: 70  $\mu\text{m}$
- Particle size range: 35–115  $\mu\text{m}$



# Experimental Setup

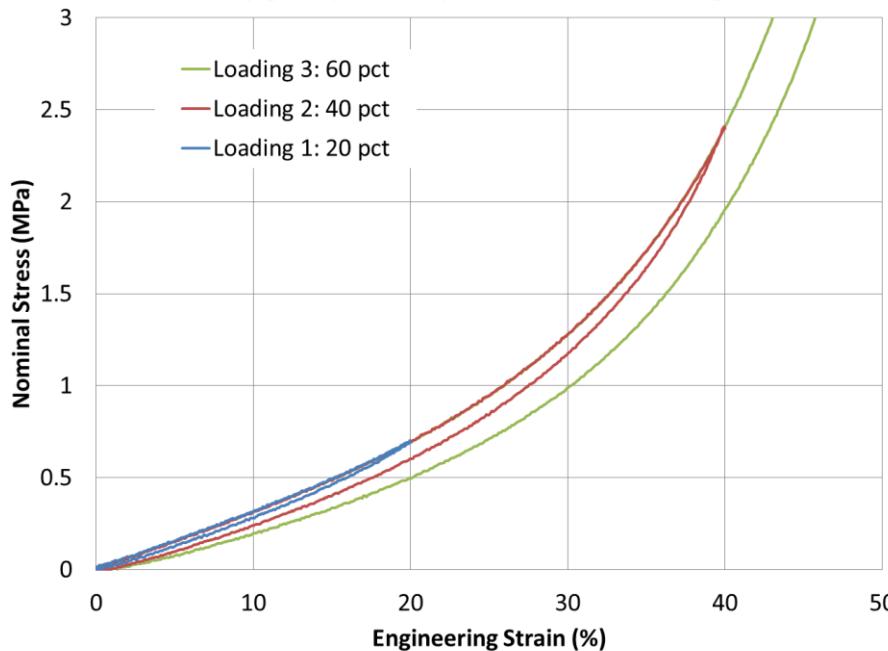


# Hysteresis in stress-strain curves

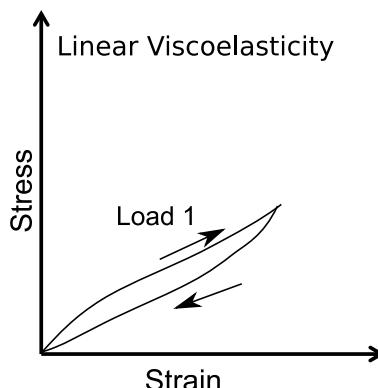
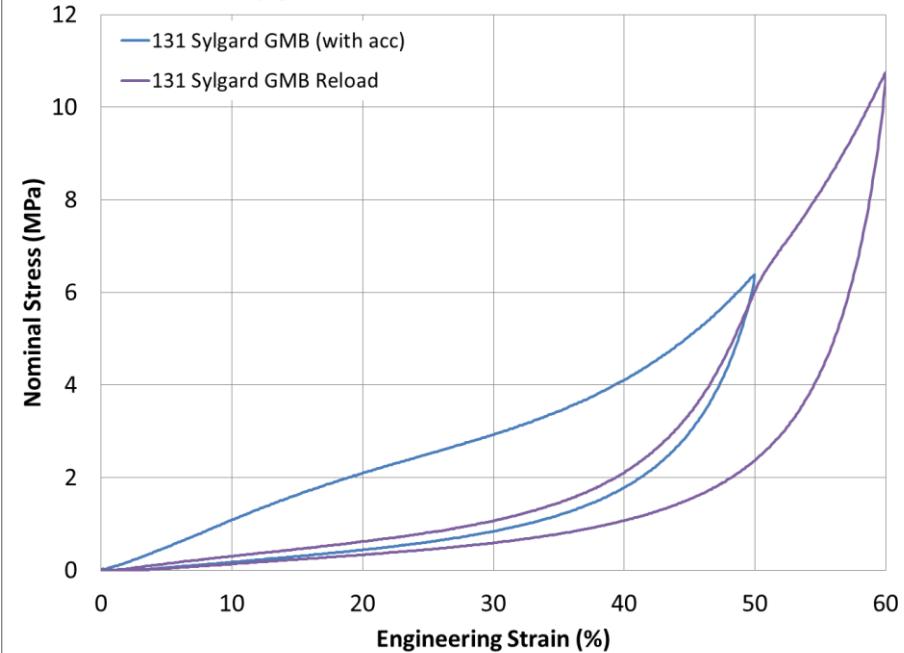
Pure Sylgard can be loaded repeatedly with no damage (minor hysteresis).

Sylgard-GMB exhibits the Mullins effect

Pure Sylgard (no GMB), Incremental Loading



Sylgard 184 with and without GMB



# No damage occurs until previous peak-load is achieved.

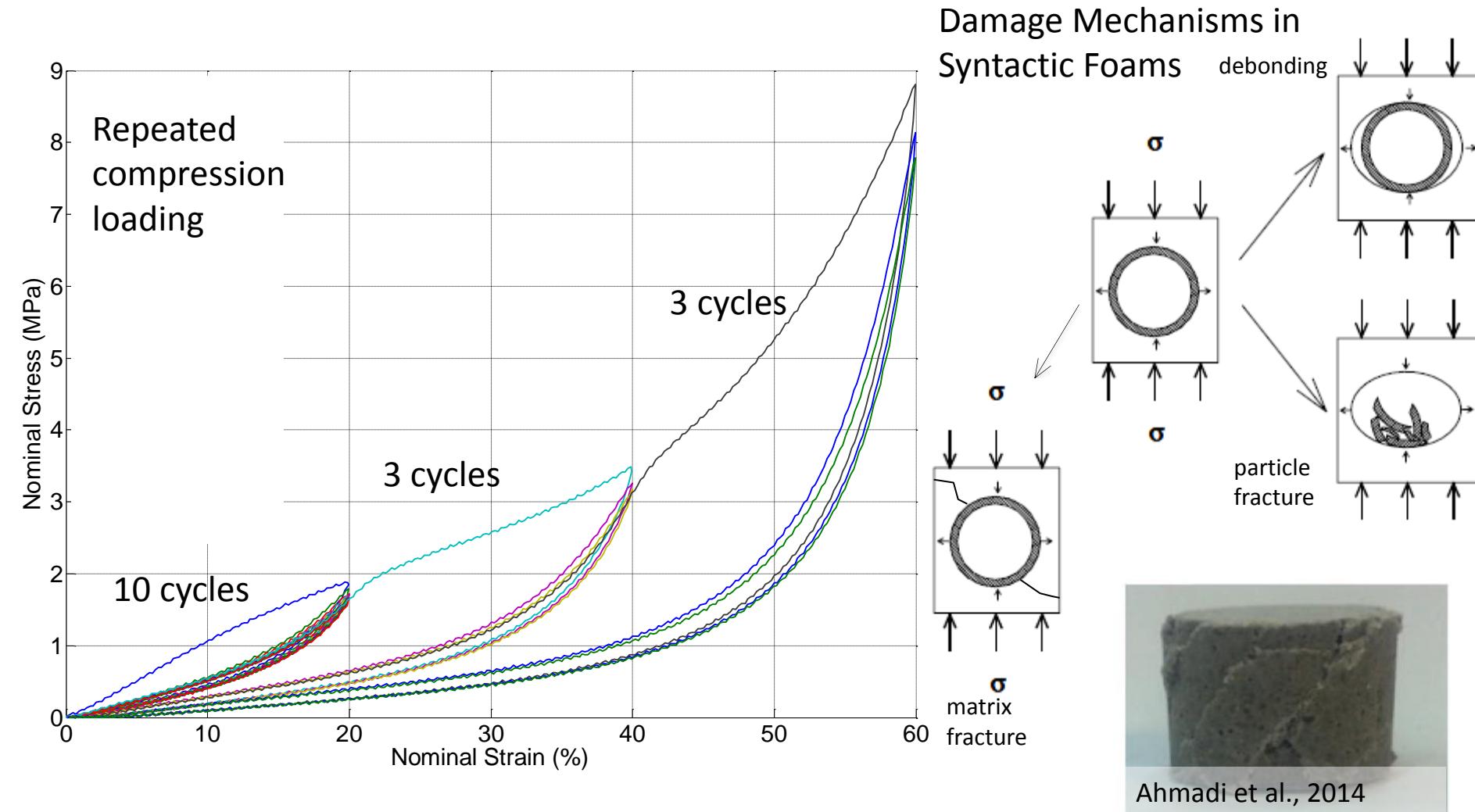


Figure 7. Shear cracks formed during plateau region on syntactic foam.

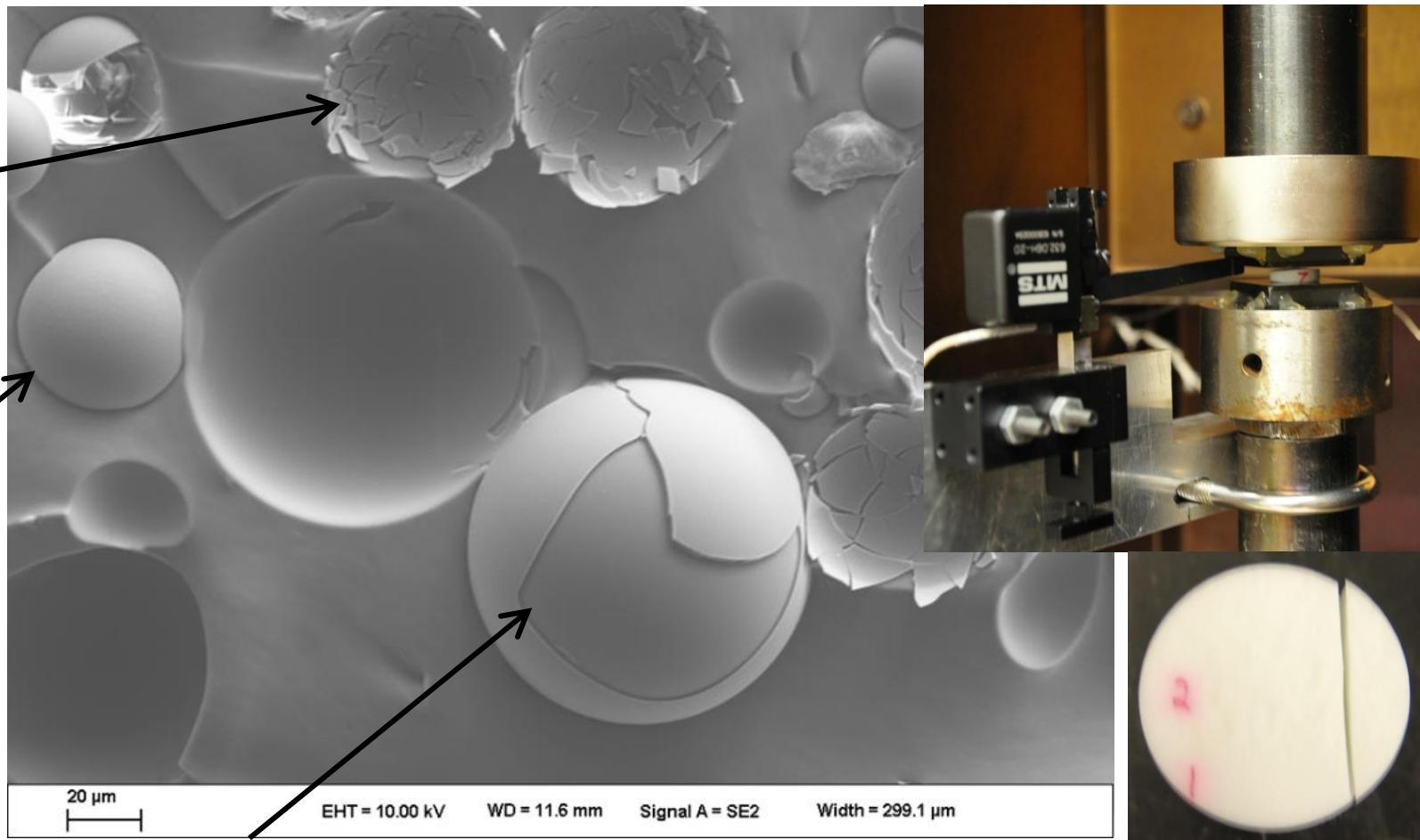
Taken after Gupta Dissertation 2003

# SEM images after loading provide insight

After compressive loading a thin disk (inner surface from tearing apart after loading)

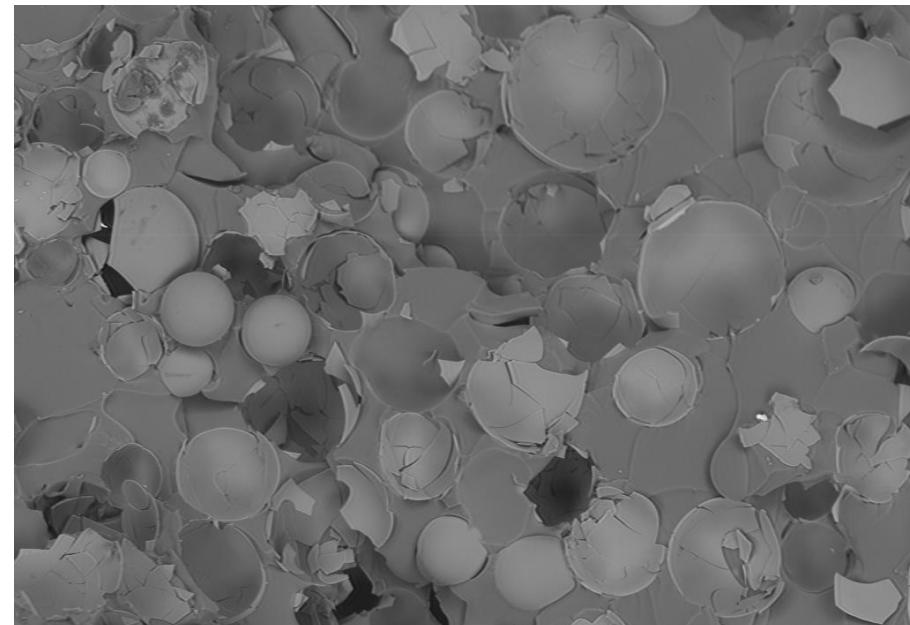
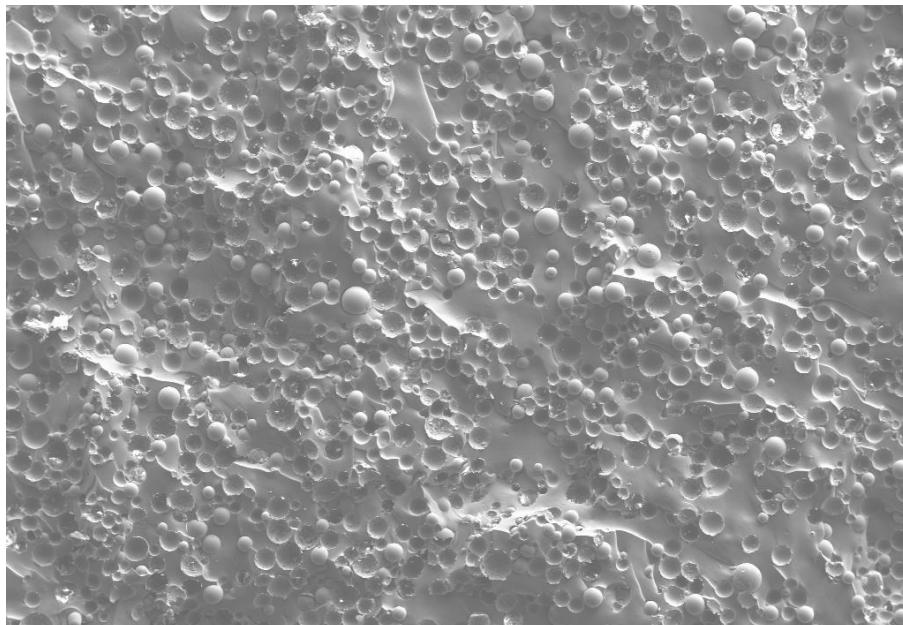
Shattered GMBs indicate fracture during loading

Intact GMBs indicate delamination

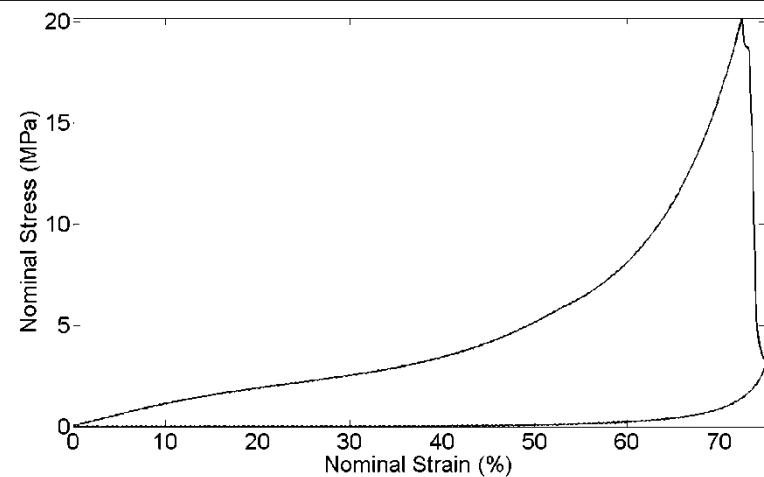


“Hard-boiled egg” structure indicates this GMB was broken before gel point. Sylgard flowed into GMB void.

# Internal fracture surface from loading specimen to compressive limit.

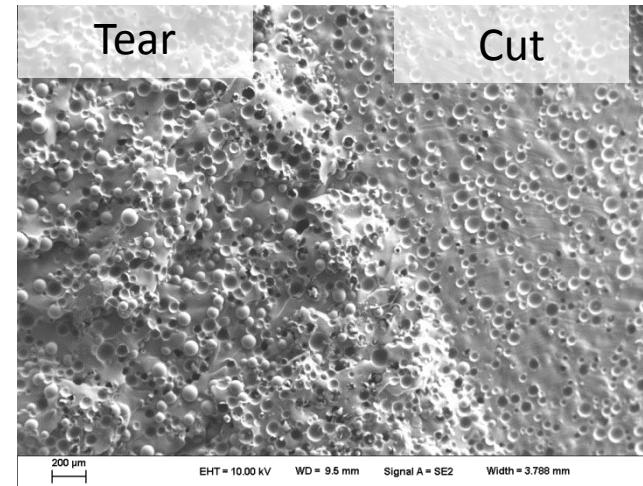


- **Undulating fracture surface**
- **Most GMBs broken**
- **Some GMBs intact**

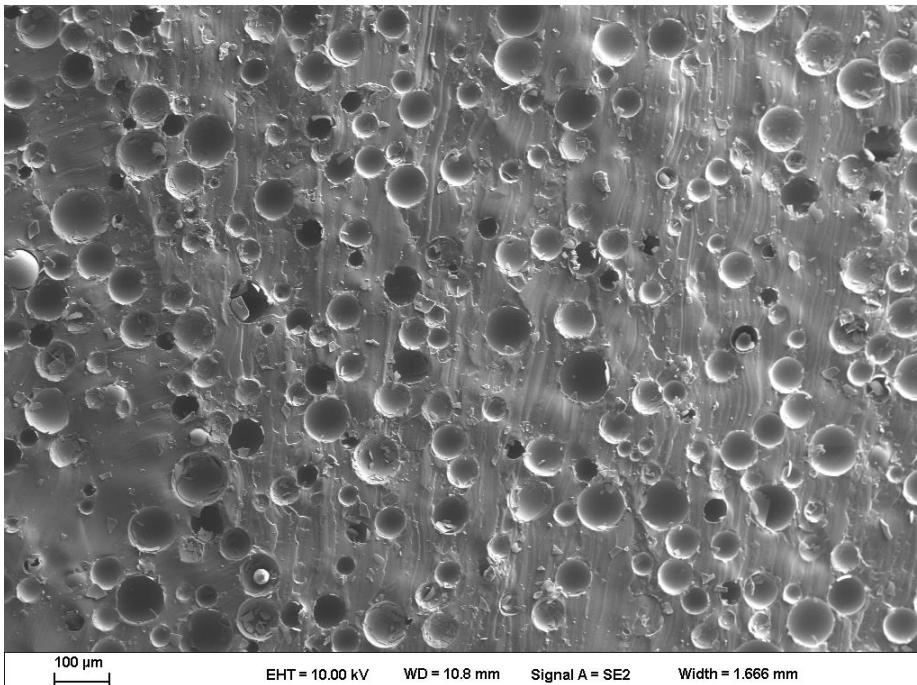


# Imaging fracture surfaces depends strongly on specimen preparation.

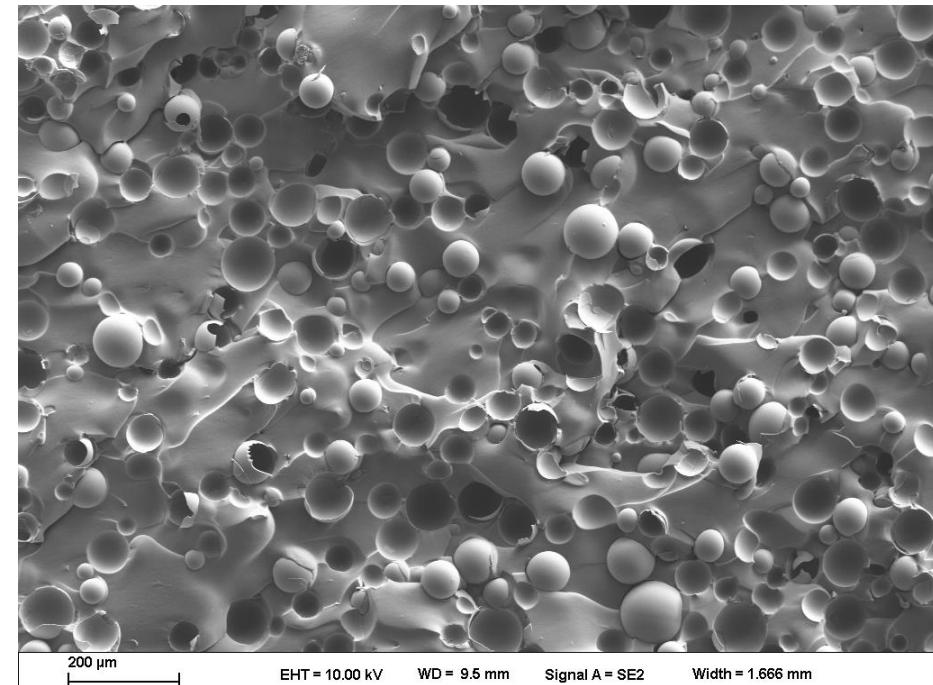
- Neither specimen experienced compressive loading before fracture.
- Tearing fracture shows some signs of delamination and GMB fracture.
- Cutting with a razor blade fractures all GMBs in path.



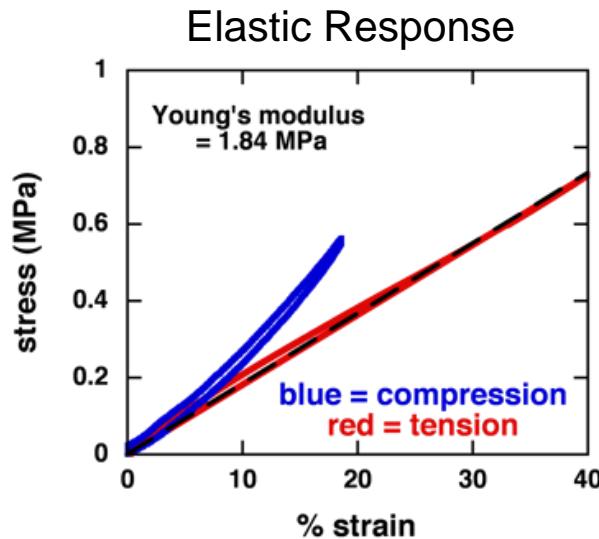
Cut surface



Tensile fractured surface



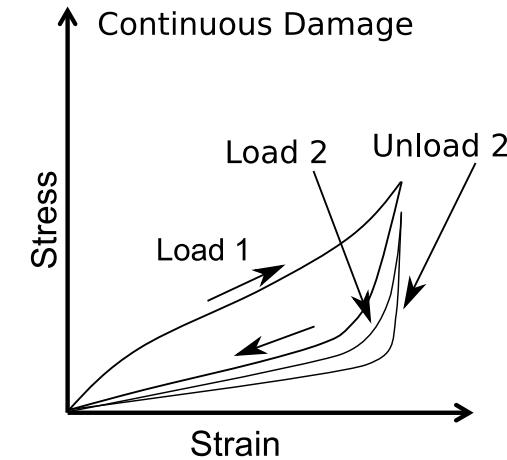
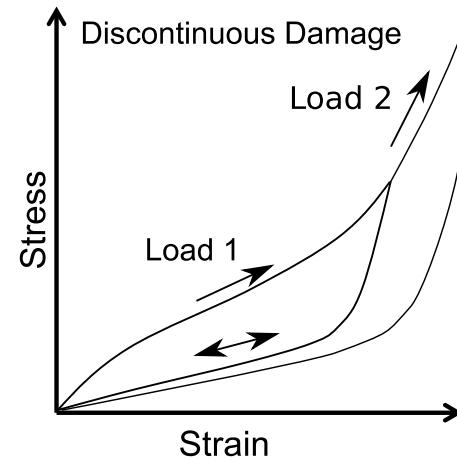
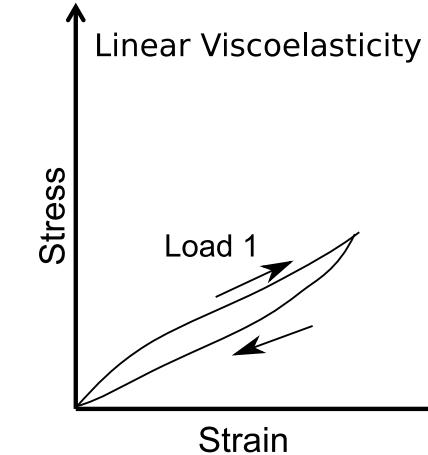
# Typical Qualitative Macroscale Response of Filled Rubbery Thermosets Under Cyclic Loading



Legacy Sylgard 184

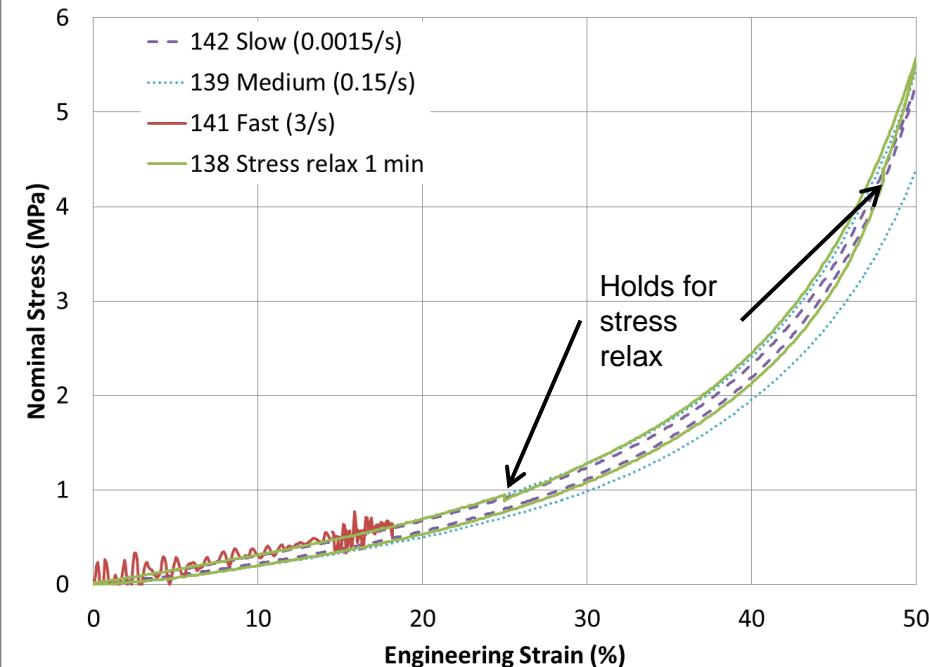
## Damage types

	Continuous	Discontinuous
Volumetric		
Isochoric		

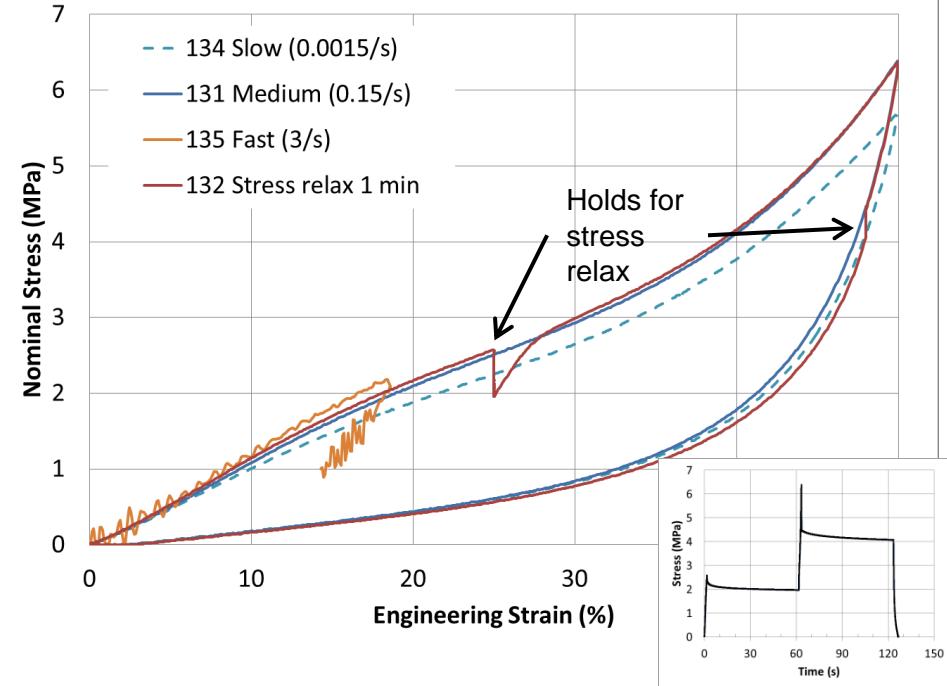


# Time dependence in pure Sylgard vs Sylgard-GMB

Pure Sylgard (no GMB) Rate Effects



Sylgard GMB Rate Effects

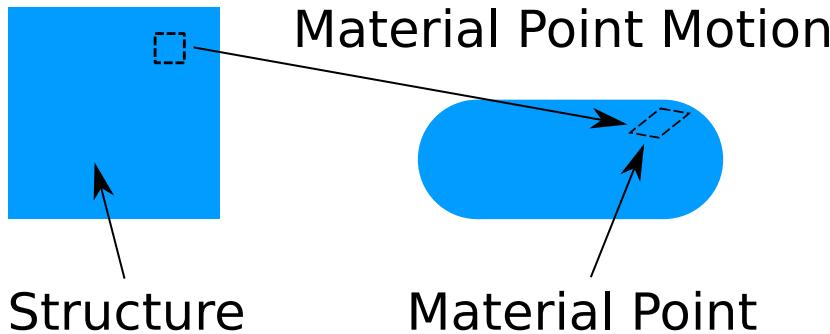


- Pure Sylgard has no measurable rate dependence. Rate effects are related to GMBs.
- Stress relax test had a 1 minute hold at 25% on loading and 48% on unloading. Pure Sylgard showed little stress relaxation.

- Sylgard/GMB has some rate dependence, particularly at slower speeds.
- Stress relax test had a 1 minute hold at 25% on loading and 48% on unloading. Sylgard GMB exhibits significant stress relaxation.

# Phenomenological Macroscale Constitutive Model: Hyperelastic Yeoh Model With Discontinuous, Continuous Damage of Both Shear (Isochoric) and Volumetric Deformation

## Kinematics of the structure and a material point



### **Deformation Gradient**

$$\mathbf{F} = \frac{\partial \mathbf{x}}{\partial \mathbf{X}} = \mathbf{x} \nabla_{\mathbf{X}}, \quad J = \det(\mathbf{F}) > 0$$

### **Jacobian of the Motion**

### **Isochoric Deformation Tensors**

$$\bar{\mathbf{F}} = J^{-\frac{1}{3}} \mathbf{F}, \quad \bar{\mathbf{b}} = \bar{\mathbf{F}} \bar{\mathbf{F}}^T = J^{-\frac{2}{3}} \mathbf{F} \mathbf{F}^T = J^{-\frac{2}{3}} \mathbf{b}.$$

### **First Invariant of the Isochoric $\mathbf{b}$**

$$\bar{I}_1 = \text{trace } \bar{\mathbf{b}}.$$

## Strain Energy Per Unit Current Volume

- Isotropic function of isochoric and volumetric deformation invariants
- Kachanov-style scalar damage in 4 damage variables
- Temperature dependence only through thermal expansion

$$\begin{aligned} \psi(\bar{I}_1, J, T, d_{iso}^d, d_{iso}^c, d_{vol}^d, d_{vol}^c) &= (1 - d_{iso}^d - d_{iso}^c) \psi_{iso}[\bar{I}_1] + (1 - d_{vol}^d - d_{vol}^c) \psi_{vol}[J], \\ \psi_{iso}[\bar{I}_1] &= \frac{1}{2} \left( \mu_1 (\bar{I}_1 - 3) + \mu_2 (\bar{I}_1 - 3)^2 + \mu_3 (\bar{I}_1 - 3)^3 \right), \\ \psi_{vol}[J] &= \frac{\kappa}{\beta^2} \left( \beta^2 J \alpha \Delta T + \beta \log[J] + J^{-\beta} - 1 \right). \end{aligned}$$

# Phenomenological Macroscale Constitutive Model: Hyperelastic Yeoh Model With Discontinuous, Continuous Damage of Both Shear (Isochoric) and Volumetric Deformation

## Non-Linear Shear Response

$$\mu_{eff} = \mu_1 + 2\mu_2 (\bar{I}_1 - 3) + 3\mu_3 (\bar{I}_1 - 3)^2$$

## Infinitesimal Shear Modulus

## Lockup Behavior

## Kirchoff Stress

$$\tau = 2b \frac{\partial \psi}{\partial b} = 2 \frac{\partial \psi}{\partial b} b = \tau_{iso} + \tau_{vol},$$

$$\tau_{iso} = 2\mu_{eff} \left(1 - d_{iso}^d - d_{iso}^c\right) \left(\bar{b} - \frac{\bar{I}_1}{3} \mathbf{1}\right) = \left(1 - d_{iso}^d - d_{iso}^c\right) \tau_{iso}^0,$$

$$\tau_{vol} = \frac{\kappa}{2} \left(1 - d_{vol}^d - d_{vol}^c\right) \left(2J\alpha\Delta T + J^2 - 1\right) \mathbf{1} = \left(1 - d_{vol}^d - d_{vol}^c\right) \tau_{vol}^0,$$

## Discontinuous Damage Evolution

### Maximum Strain Energy Densities

$$d_{iso}^d = d_{iso}^{dMAX} \left(1 - \exp \left(-\frac{\text{MAX}[\psi_{iso}[\bar{I}_1]]}{d_{iso}^{dSAT}}\right)\right),$$

$$d_{vol}^d = d_{vol}^{dMAX} \left(1 - \exp \left(-\frac{\text{MAX}[\psi_{vol}[J[t]]]}{d_{vol}^{dSAT}}\right)\right)$$

### Integrated Power Density

## Continuous Damage Evolution

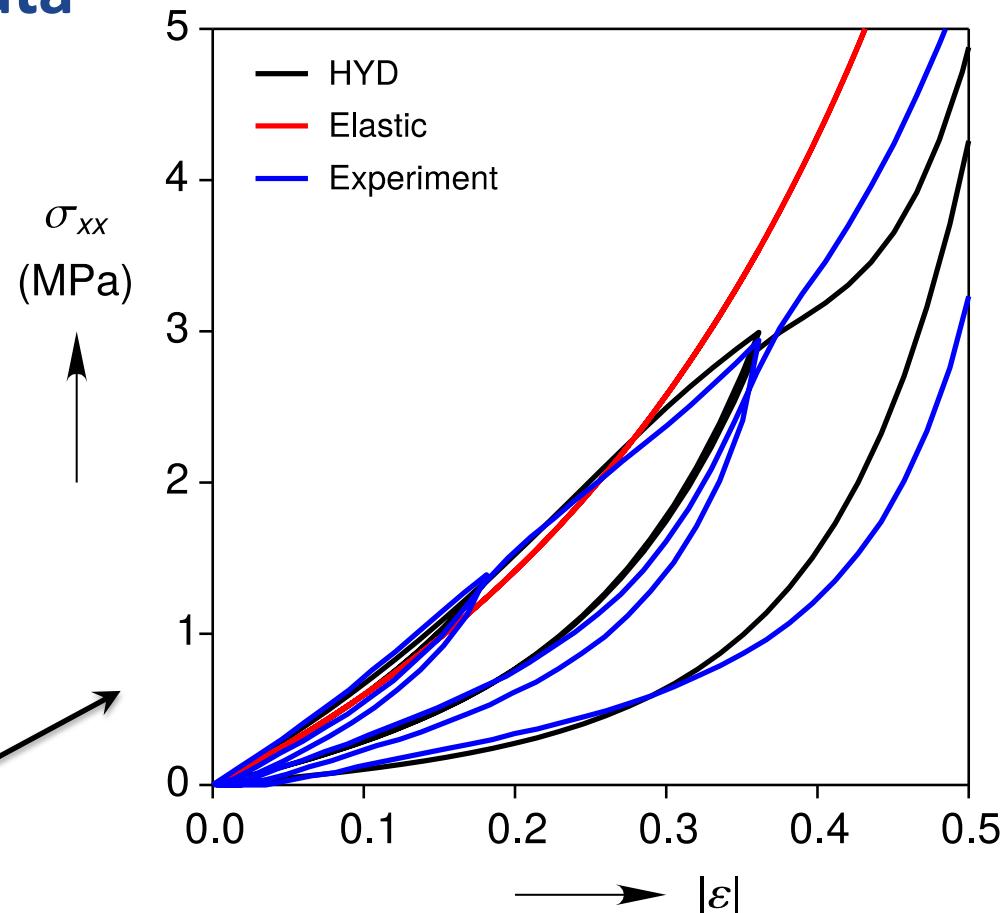
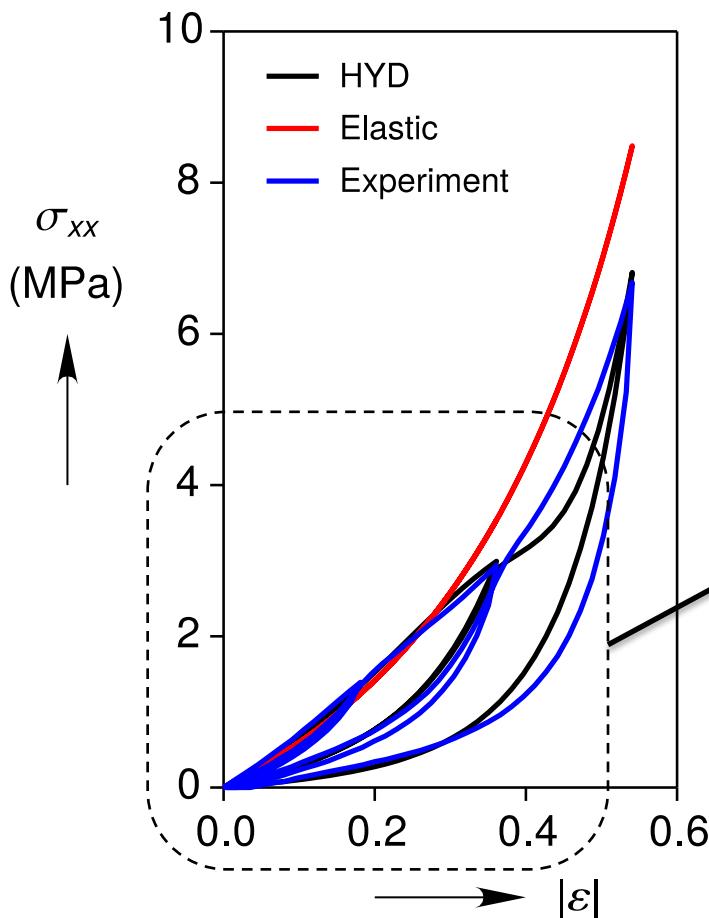
$$d_{iso}^c = d_{iso}^{cMAX} \left(1 - \exp \left(-\frac{\beta_{iso}[t]}{d_{iso}^{cSAT}}\right)\right)$$

$$d_{vol}^c = d_{vol}^{cMAX} \left(1 - \exp \left(-\frac{\beta_{vol}[t]}{d_{vol}^{cSAT}}\right)\right)$$

$$\beta_{iso, (vol)}[t] = \int_0^t |\dot{\psi}_{iso, (vol)}| dt'$$

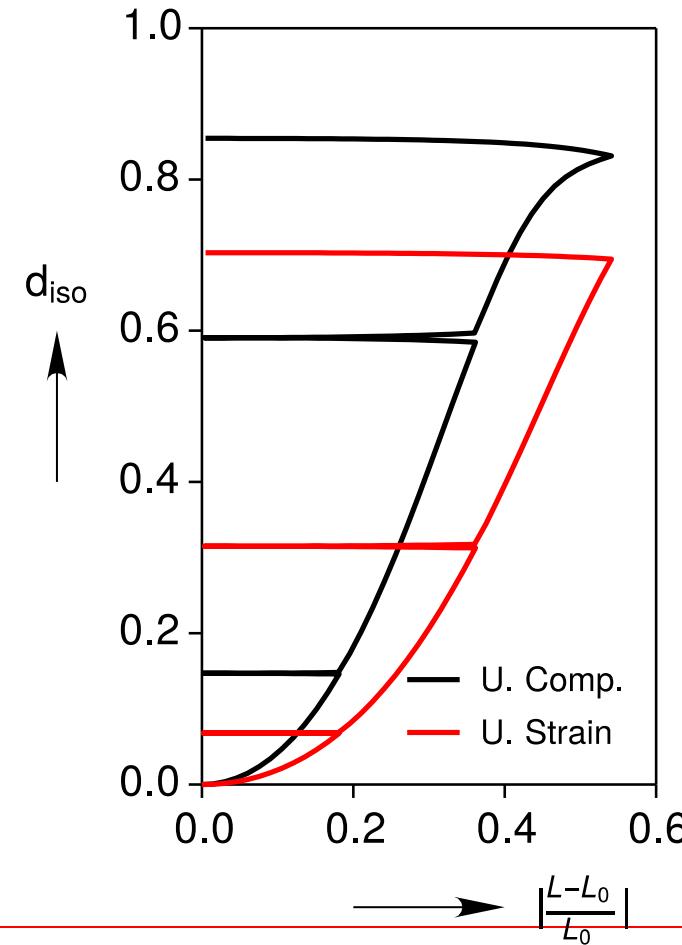
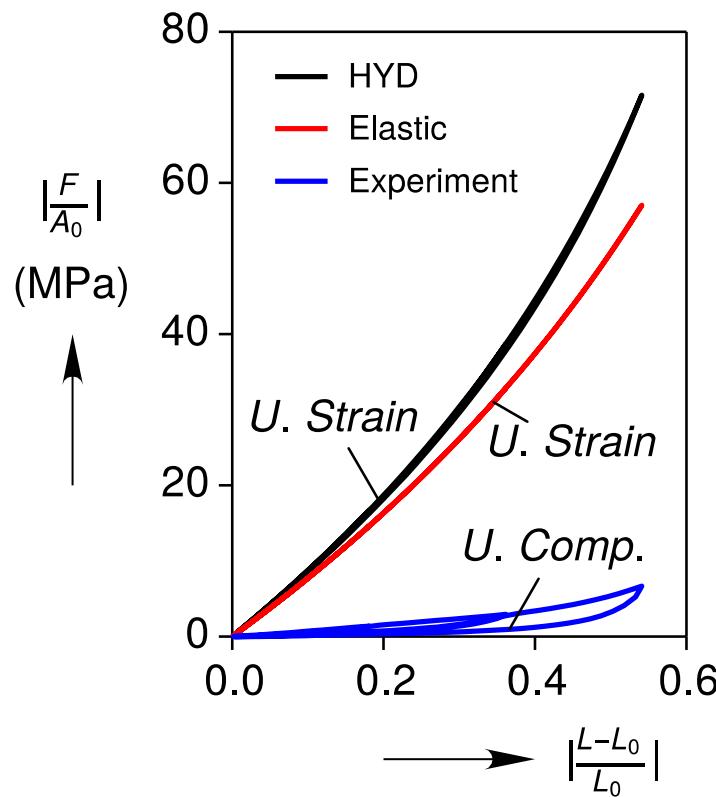
# Elastic and Damage Model Calibrations to Uniaxial Compression Data

- Isochoric Damage only
- Discontinuous and Continuous Mechanisms



HYD model reasonably fits the uniaxial compression data

# The Importance of the Boundary Value Problem (BVP): Uniaxial Compression vs. Uniaxial Strain

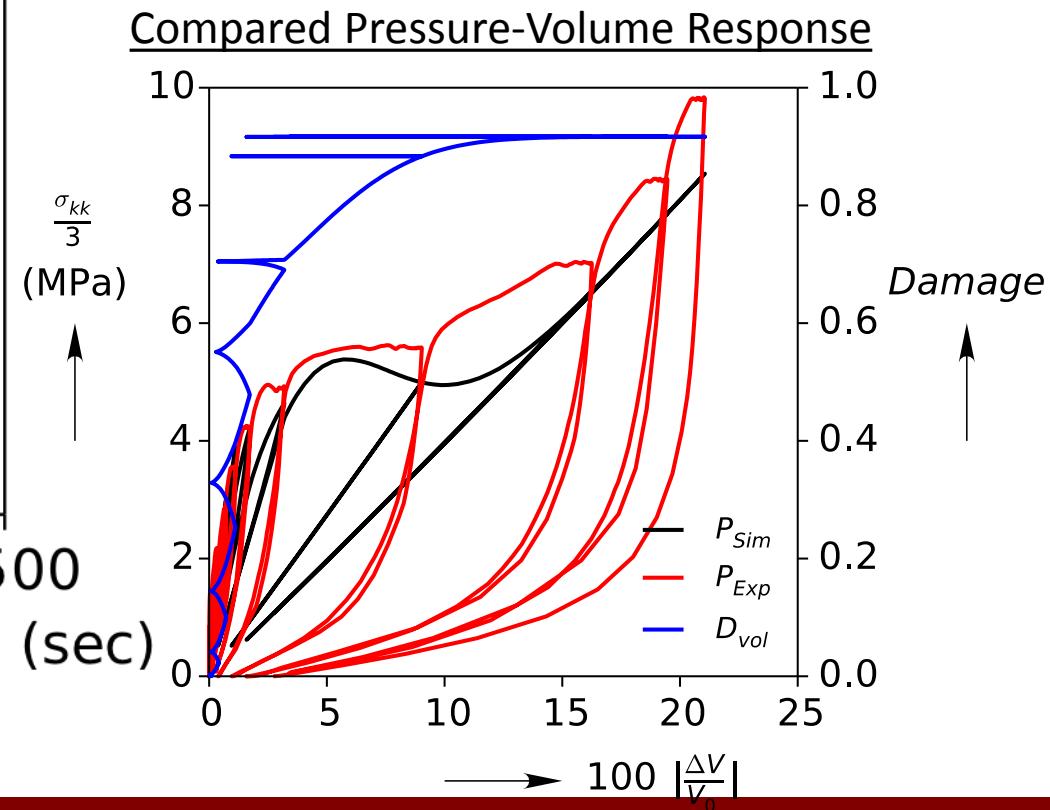
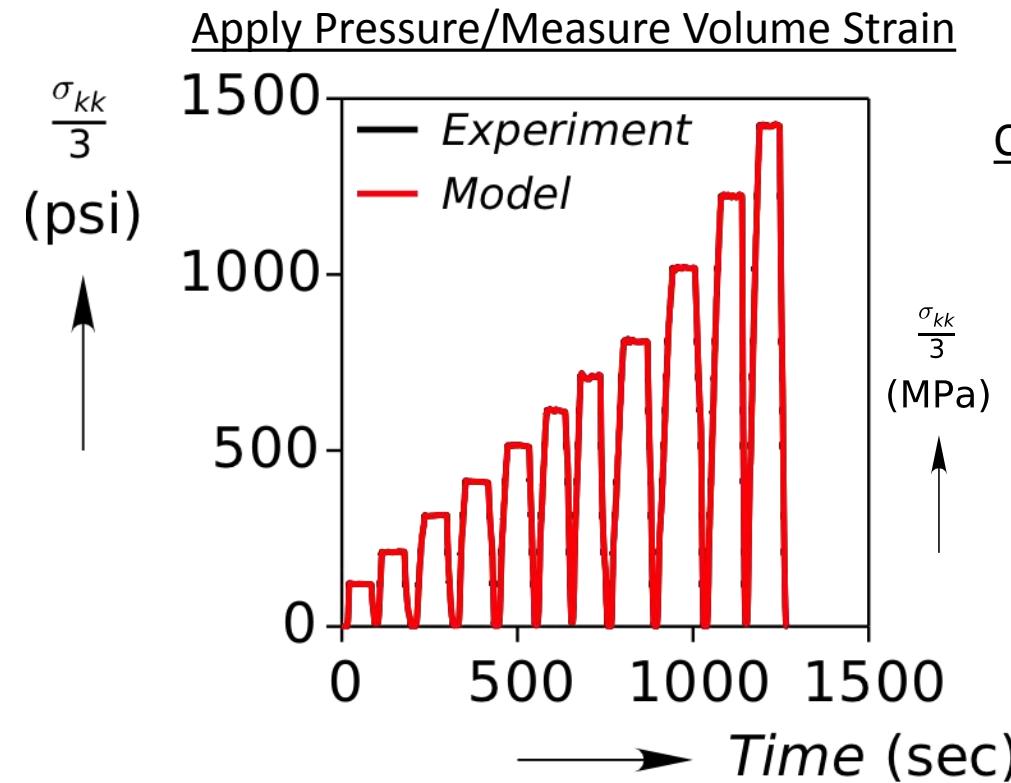


Although both BVPs similarly damage syglard GMB, isochoric damage contributes very little to the uniaxial strain response

Volumetric damage may not be negligible

# Model Performance Under Cyclic Hydrostatic Pressurization is Incorrect

**Data is Time Dependent → No Time Dependence in the Model**



- **Micromechanics model development**
- **Supporting experiments**
  - **In situ deformation**
    - Microscope
    - CT scanning
    - Digital image correlation (DIC) or digital volume correlation (DVC).
  - **Constrained compression**

In situ synchrotron CT compression of GMB-filled Sylgard.

Patterson et. Al,  
Microsc. Microanal. 20  
(suppl 3), 2014

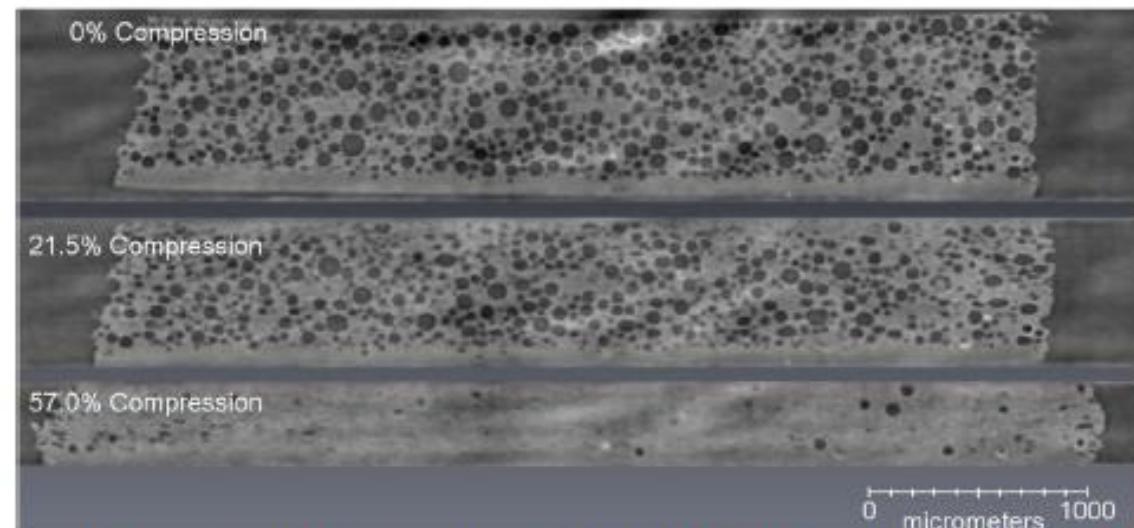
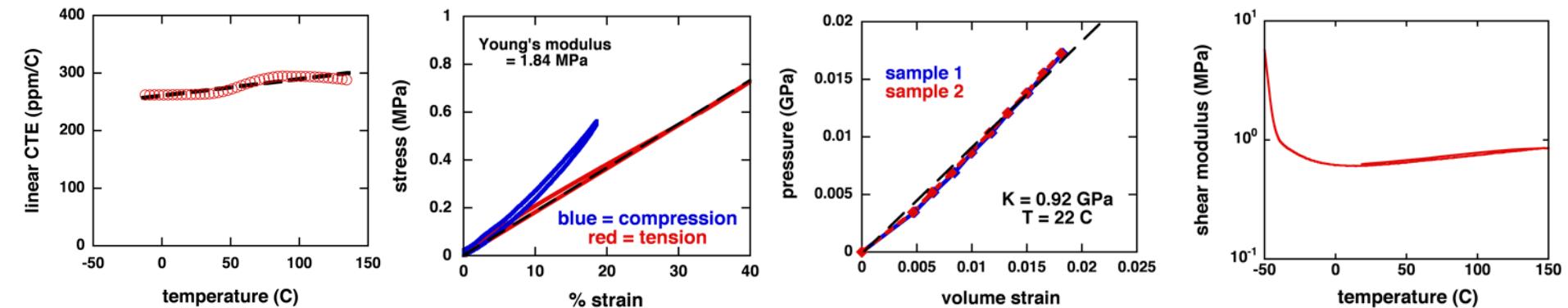


Figure 3: Compression of syntactic Sylgard foam with 100  $\mu\text{m}$  hollow glass beads. Sample is nearly incompressible with a high Poisson ratio.

# Bonus Slides

# Basic Mechanical Properties

## Pure Sylgard



## Sylgard GMB

