

# Characterizing Solute Drag on Perfect and Extended Dislocations

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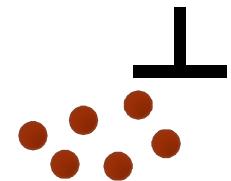
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# Overview

- Nature of solute drag
- Numerical drag calculation
- Results

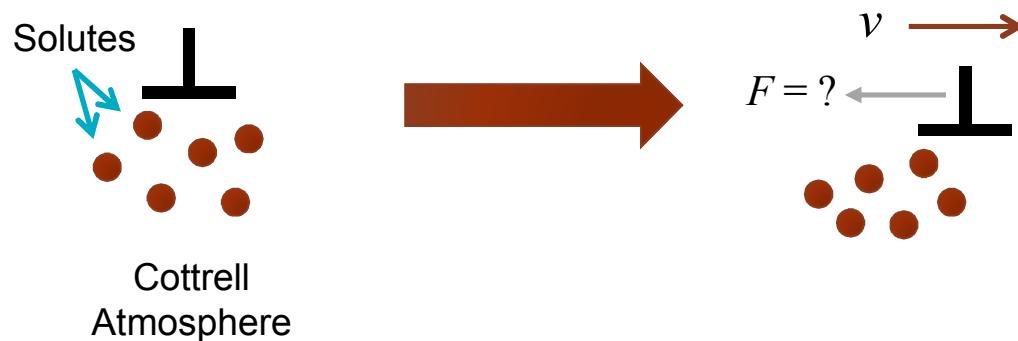
## Nature of solute drag



# Cottrell atmosphere and solute drag

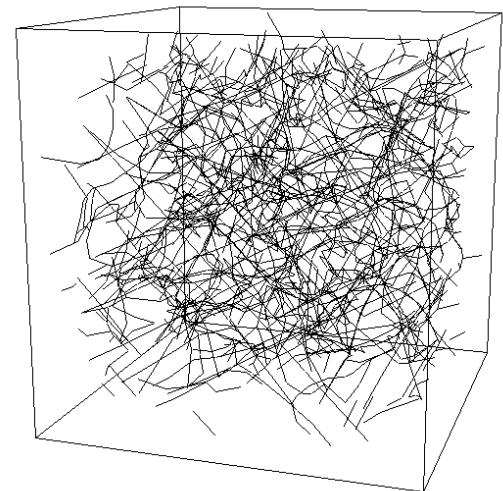
Solid solutions are ubiquitous in metallic systems

- Alloying
- Contaminants (e.g. hydrogen)



# Including solute drag in dislocation dynamics

- Interested in large-scale simulations
- Full simulation of solute field not feasible
  - › Very fine computational grid required
- Our approach: Use mobility law to incorporate drag effects

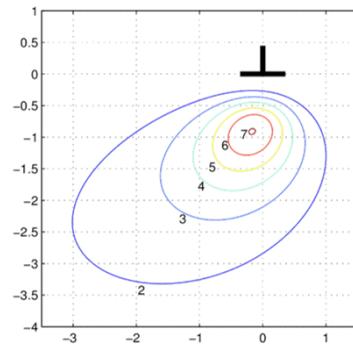


$$\mathbf{F}_{\text{drag}}(\mathbf{v}) = \mathbf{F}_{\text{drive}} \quad \longrightarrow \quad \mathbf{v} = \mathbf{M}(\mathbf{F}_{\text{drive}})$$

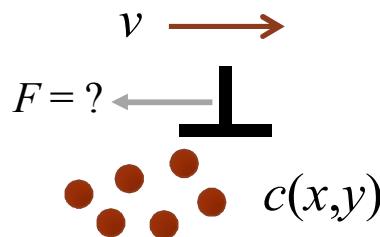
→ Need to determine  $\mathbf{F}_{\text{drag}}(\mathbf{v})$

Mobility Law

# Numerical drag calculation



# Steady-state drag calculation



*Focus on achieving convergent solution*

- Enabled by non-singular dislocation theory (Cai et al., 2006)

*Consider extended dislocations*

Cottrell and Jaswon (1949)  
Yoshinaga and Morozumi (1971)  
Takeuchi and Argon (1979)  
James and Barnett (1985)  
Hirth and Lothe (1982)  
Fuentes-Samaniego et al. (1984)  
Zhang and Curtin (2008)

## Solute concentration field calculation

$$\frac{\partial c}{\partial t} = -\nabla \cdot \mathbf{J} = 0 \quad (\text{steady state})$$

*Finite difference and solve with Newton's method*

## Drag force calculation

$$\sigma_{xy} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} [c(x', y') - c_0] \sigma_{xy}^{\text{solute}}(x_c - x', y_c - y') dx' dy'$$

Background concentration

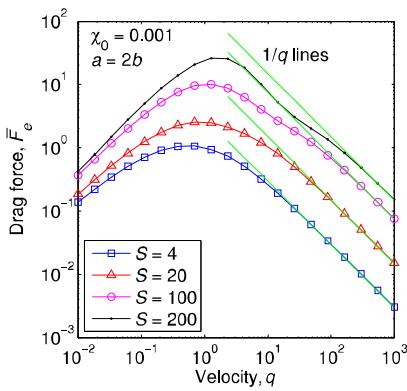
Stress field of a solute

*Evaluate with adaptive quadrature in MATLAB*

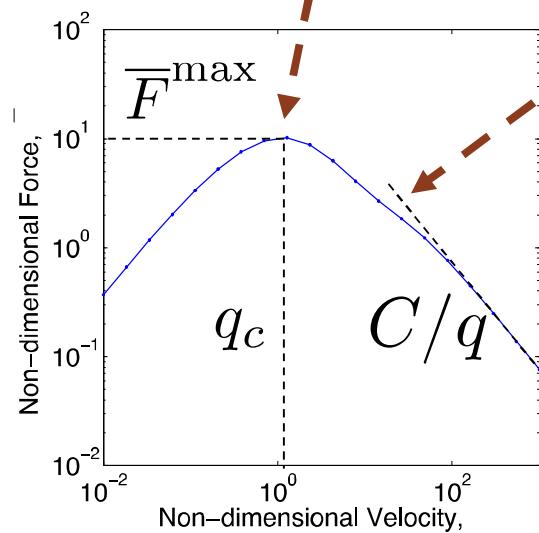
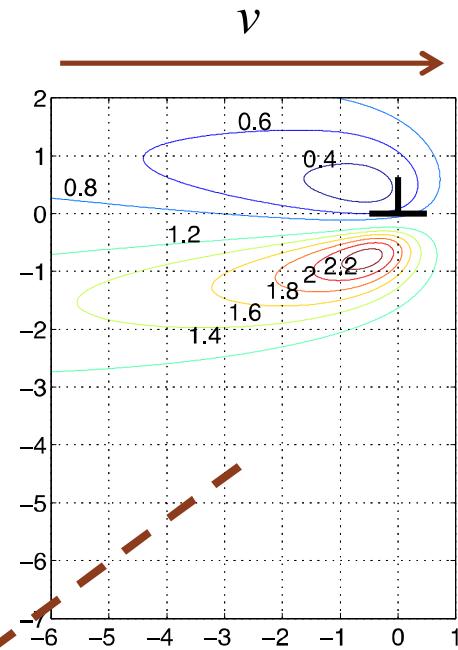
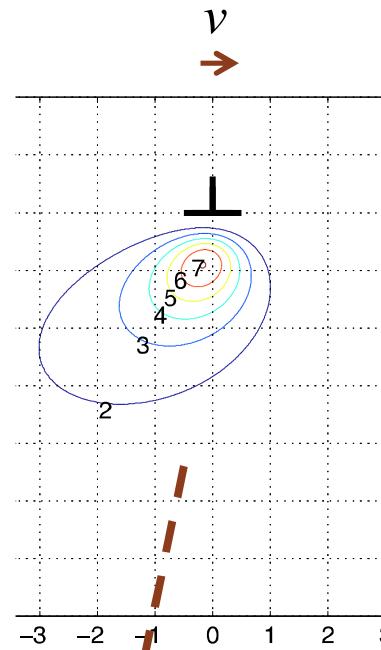
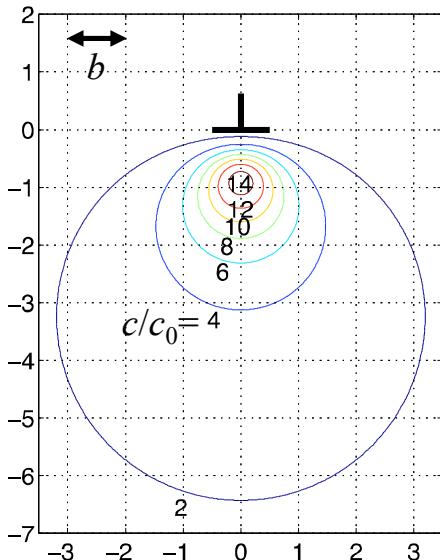
$$F = \sigma_{xy} b$$

Stanford University

# Results



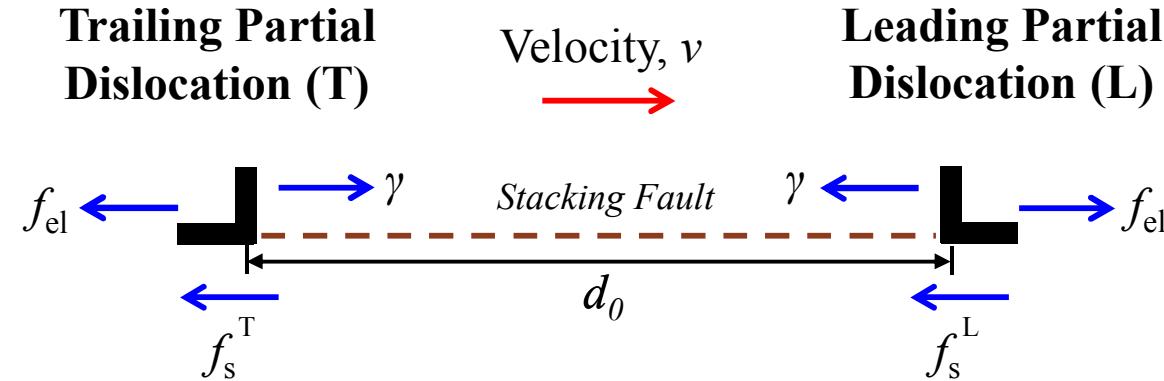
# Force-velocity curve



$$\bar{F} = \bar{F} \left( q, c_0, S, \theta, \frac{\hat{\gamma}}{\mu b}, \frac{a}{b} \right)$$

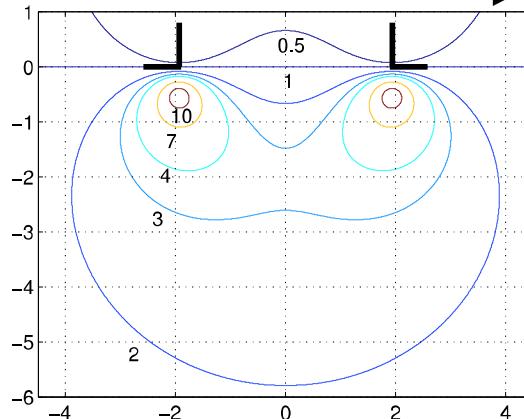
Non-dimensional Force  
Expression

# Extended dislocations – Partial separation distance

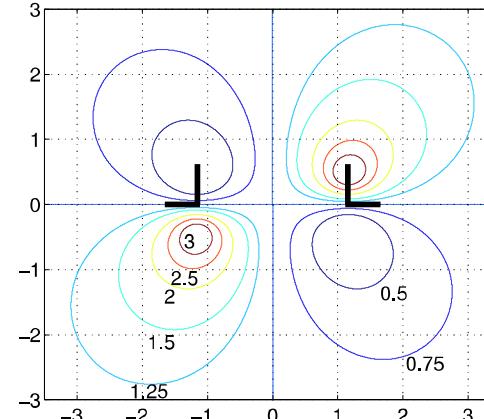


$$f_s^T(d) - f_s^L(d) = f_2(d_0) - f_{el}(d)$$

Edge,  $\theta = 90^\circ$   $\mathbf{b} \rightarrow$

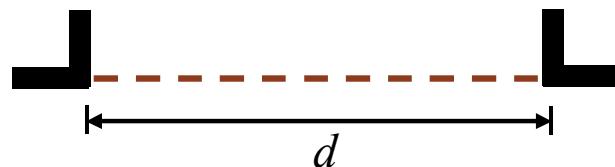


Screw,  $\theta = 0^\circ$   $\mathbf{b} \odot$



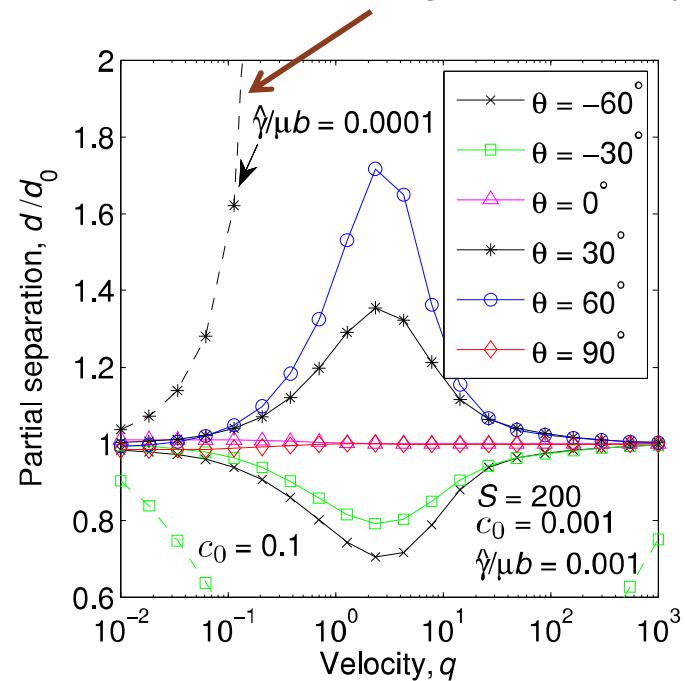
Extended edges experience 4x more drag than extended screws

# Extended dislocation results



$d_0$  = Solute-free separation distance

Separation distance goes to infinity!



- Deformation twinning in low SFE metals possibly promoted by solutes
  - Stainless steel with H (San Marchi et al., 2011)
  - Stainless steel with N (Mullner et al. 1993)

# Summary

- Analytical form for force-velocity curve and DD mobility law

$$\overline{F}(q) = \frac{Cq}{q^2 + \left(C/\overline{F}^{\max} - 2q_c\right)q + q_c^2}$$

- Can incorporate solute drag in DD simulations
- Extended screws see 75% less drag than extended edges
- Atmosphere can change partial separation significantly
  - Independent of changes in SFE
- Manuscript in-preparation
  - *Solute drag on perfect and extended dislocations*, R. B. Sills and W. Cai