

# Correlations and photon statistics in nanocavity emitters

SAND2015-3531PE

**Weng Chow, Sandia National Laboratories**

**Motivation for nanocavity emitters**

**Modeling approaches**

**Research:**

- a)  $\beta = 1$  and thresholdless lasing**
- b) Single-photon sources and photon statistics**

**Thanks to:**

**Christopher Gies and Frank Jahnke, Bremen University**

**Sandia's Laboratory Directed Research & Development (LDRD) Program**

# Why nano-emitter research?

## 1 Save energy

### Data centers and optical communication

- Reducing energy per bit
- At limits for electrical approaches
- Optical interconnects: laser energy consumption  $\propto$  volume

## 2 Safe communication

- Quantum key distribution (QKD)
- Single-photon sources
- Types of light

Laser (random)



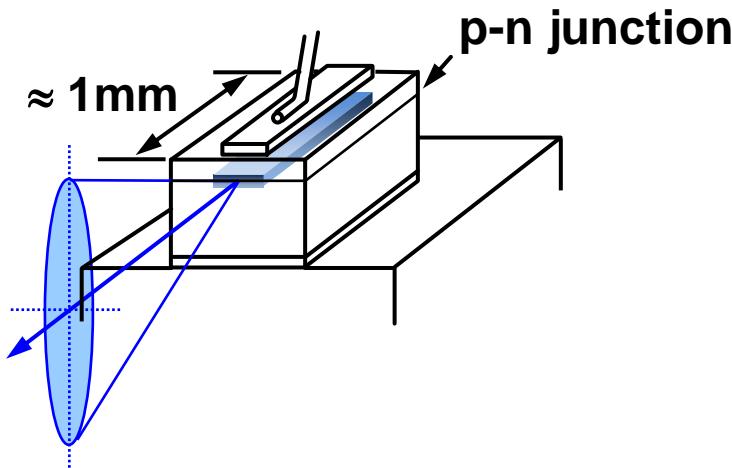
Single-photon (antibunched)



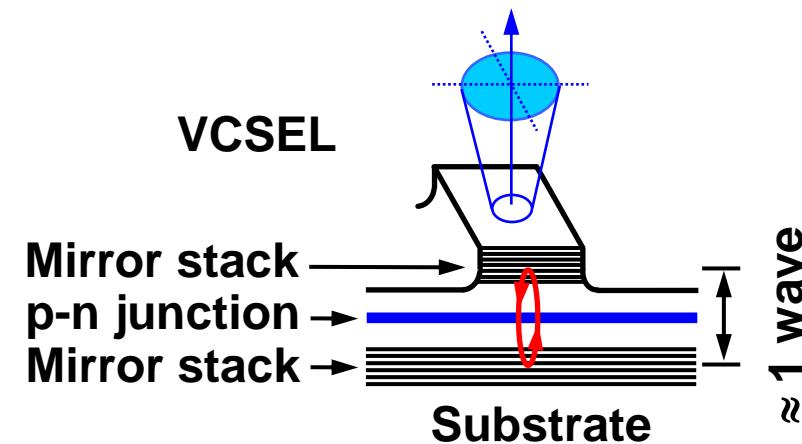
→ Time

# Towards smaller and smaller lasers

## Edge - Emitting Laser

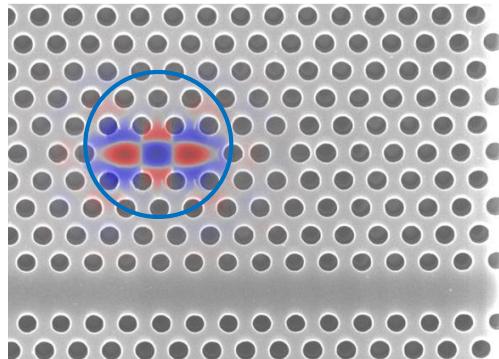


## Vertical-Cavity Surface-Emitting Laser



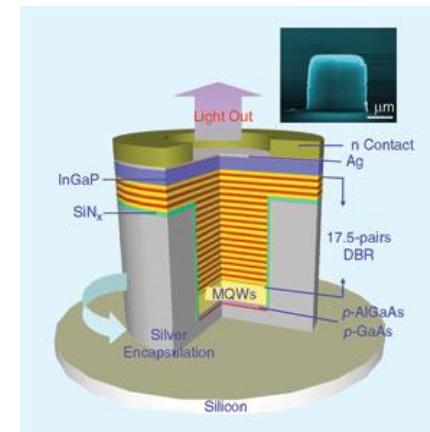
## Nanolasers

### Photonic crystal



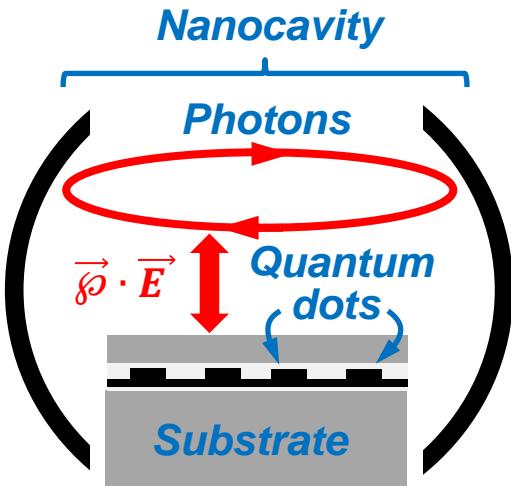
(Courtesy of Willie Luk, Sandia National Labs)

### Nanocavity

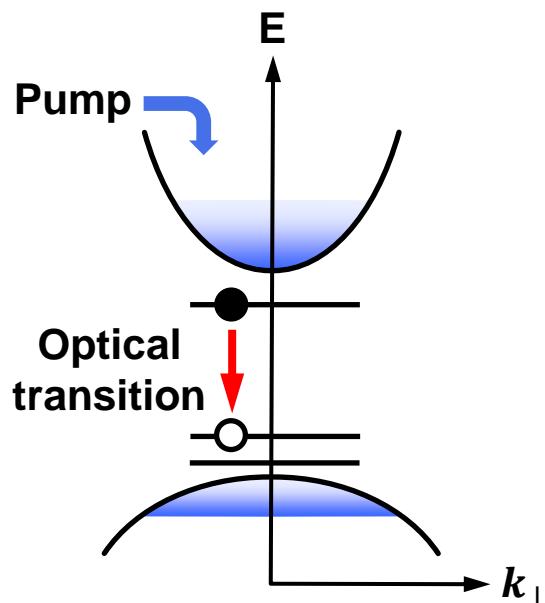


(Adapted from a figure by Lu et al., UIUC)

# Hamiltonian: physics entering into the theory



## Electronic structure



$$H = \sum_{\alpha} \varepsilon_{\alpha}^e c_{\alpha}^{\dagger} c_{\alpha} + \sum_{\beta} \varepsilon_{\beta}^h b_{\beta}^{\dagger} b_{\beta} + \hbar\omega \left( a^{\dagger} a + \frac{1}{2} \right) \quad \text{Single-particle}$$

$$- \hbar \sum_{\alpha} (g_{\alpha} b_{\alpha}^{\dagger} c_{\alpha}^{\dagger} a - g_{\alpha}^* a^{\dagger} c_{\alpha} b_{\alpha}) \quad \text{Light-carrier interaction}$$

$\propto \sqrt{\frac{v}{\hbar \epsilon_b V}} W(R_{QD}) \sum_n C_{\alpha}(R_n) V_{\alpha}(R_n)$

$$\begin{aligned}
 & + \frac{1}{2} \sum_{\alpha\beta\sigma\eta} W_{\sigma\eta}^{\alpha\beta} c_{\alpha}^{\dagger} c_{\beta}^{\dagger} c_{\eta} c_{\sigma} + \frac{1}{2} \sum_{\alpha\beta\sigma\eta} W_{\sigma\eta}^{\alpha\beta} b_{\alpha}^{\dagger} b_{\beta}^{\dagger} b_{\eta} b_{\sigma} \\
 & - \sum_{\alpha\beta\sigma\eta} W_{\sigma\eta}^{\alpha\beta} b_{\alpha}^{\dagger} c_{\beta}^{\dagger} c_{\eta} b_{\sigma} \quad \text{Matrix element of} \\
 & \qquad \qquad \qquad \frac{e^2}{4\pi\epsilon_b |r - r'|} \quad \text{Carrier-carrier}
 \end{aligned}$$

$$+ \hbar \sum_{\alpha\beta q} G_q (c_{\alpha}^{\dagger} c_{\beta} + b_{\alpha}^{\dagger} b_{\beta}) (d_q + d_q^{\dagger}) \quad \text{Carrier-phonon}$$

# Dynamical behavior of a quantum system

## Schrödinger Picture

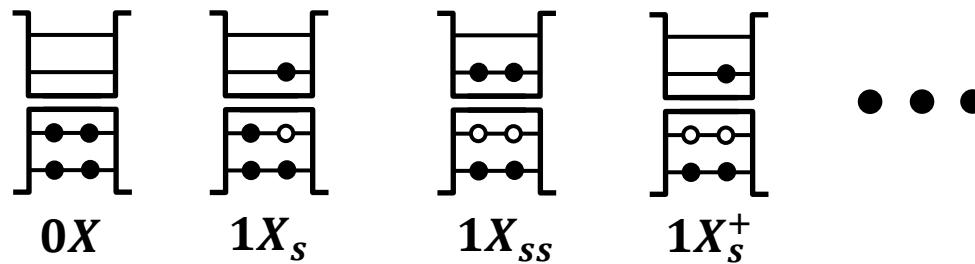
$$\frac{\partial}{\partial t} \varrho = -\frac{i}{\hbar} [H, \varrho]$$

Density operator:  $\sum_{\psi} P_{\psi} |\psi\rangle\langle\psi|$

Wave function:  $\psi(r) \equiv \langle r|\psi\rangle$

### Quantum-dot states (configurations)

Basis:  $|j, n\rangle$   
Photon number



### Observable

Expectation values:  $\langle A \rangle = \overbrace{\text{Tr}\{\varrho A\}}^{\text{Observable}} = \sum_{n,j,n'j'} \langle n,j | \varrho | j',n' \rangle \langle n',j' | A | j,n \rangle$

Photon statistics:  $P_n = \langle n, 0X | \varrho | 0X, n \rangle + \langle n, 1X_s | \varrho | 1X_s, n \rangle + \langle n, 2X_{ss} | \varrho | 2X_{ss}, n \rangle + \dots$

# Dynamical behavior of a quantum system

## Heisenberg Picture

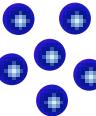
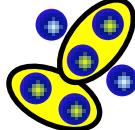
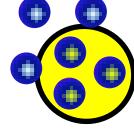
System operator

$$\frac{\partial}{\partial t} A = -\frac{i}{\hbar} [A, H]$$

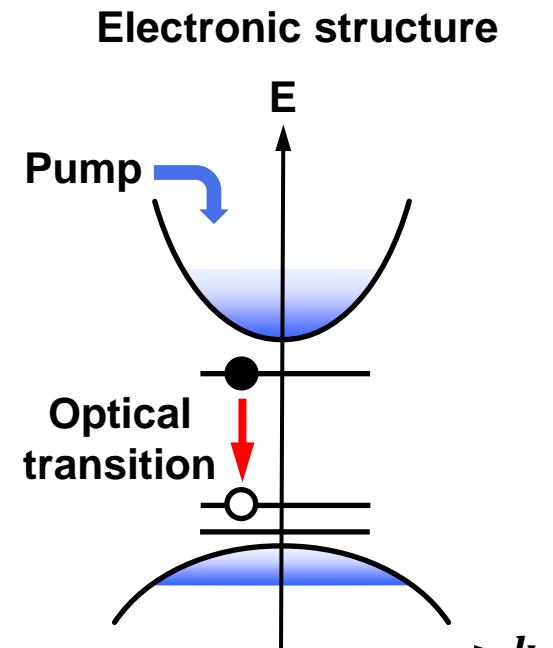
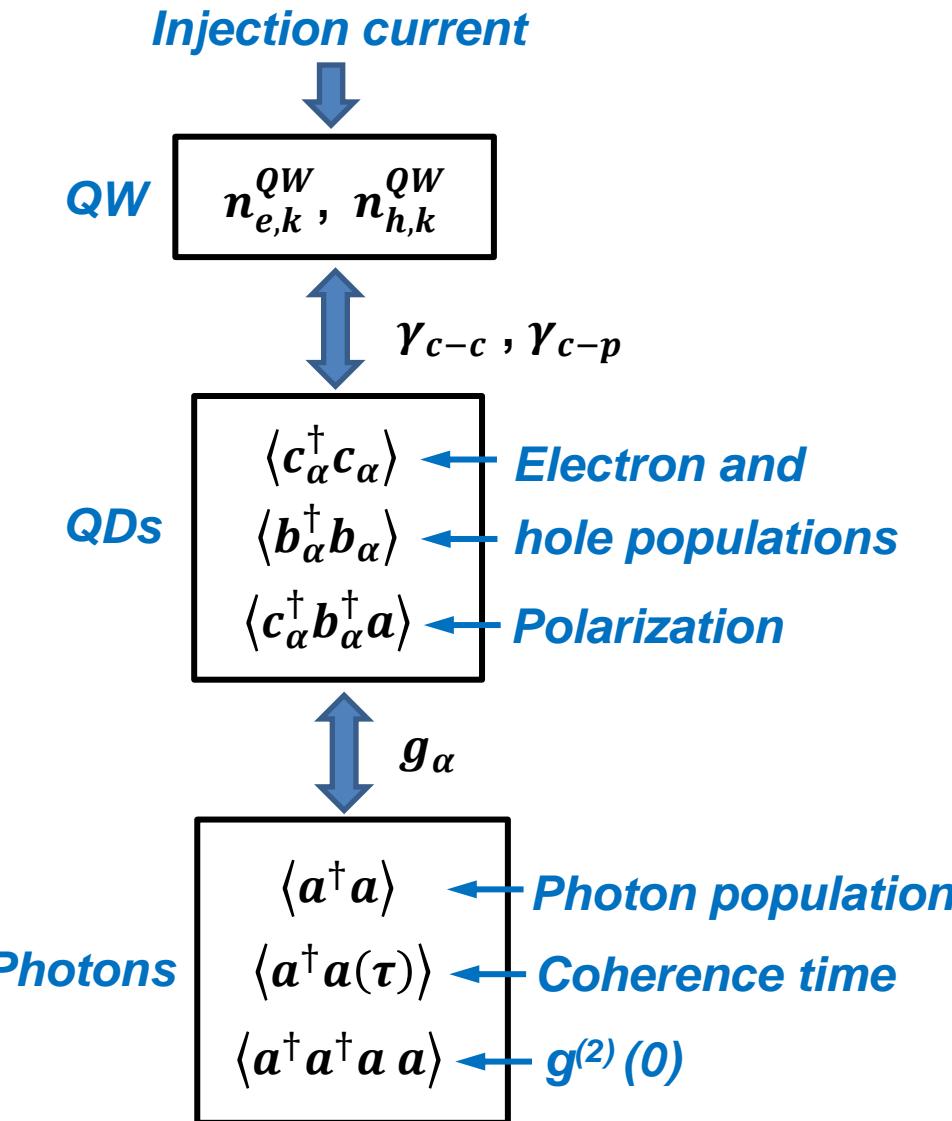
Populations and correlations:

$$\begin{aligned} & \langle c_\alpha^\dagger c_\alpha \rangle, \langle b_\alpha^\dagger b_\alpha \rangle, \langle c_\alpha^\dagger b_\alpha^\dagger a \rangle, \langle a^\dagger a \rangle \\ & \langle a^\dagger a^\dagger a a \rangle, \langle c_\alpha^\dagger c_\sigma^\dagger c_\sigma c_\alpha \rangle, \langle c_\alpha^\dagger c_\alpha a^\dagger a \rangle \end{aligned}$$

Cluster expansion:  $\langle \hat{N} \rangle =$

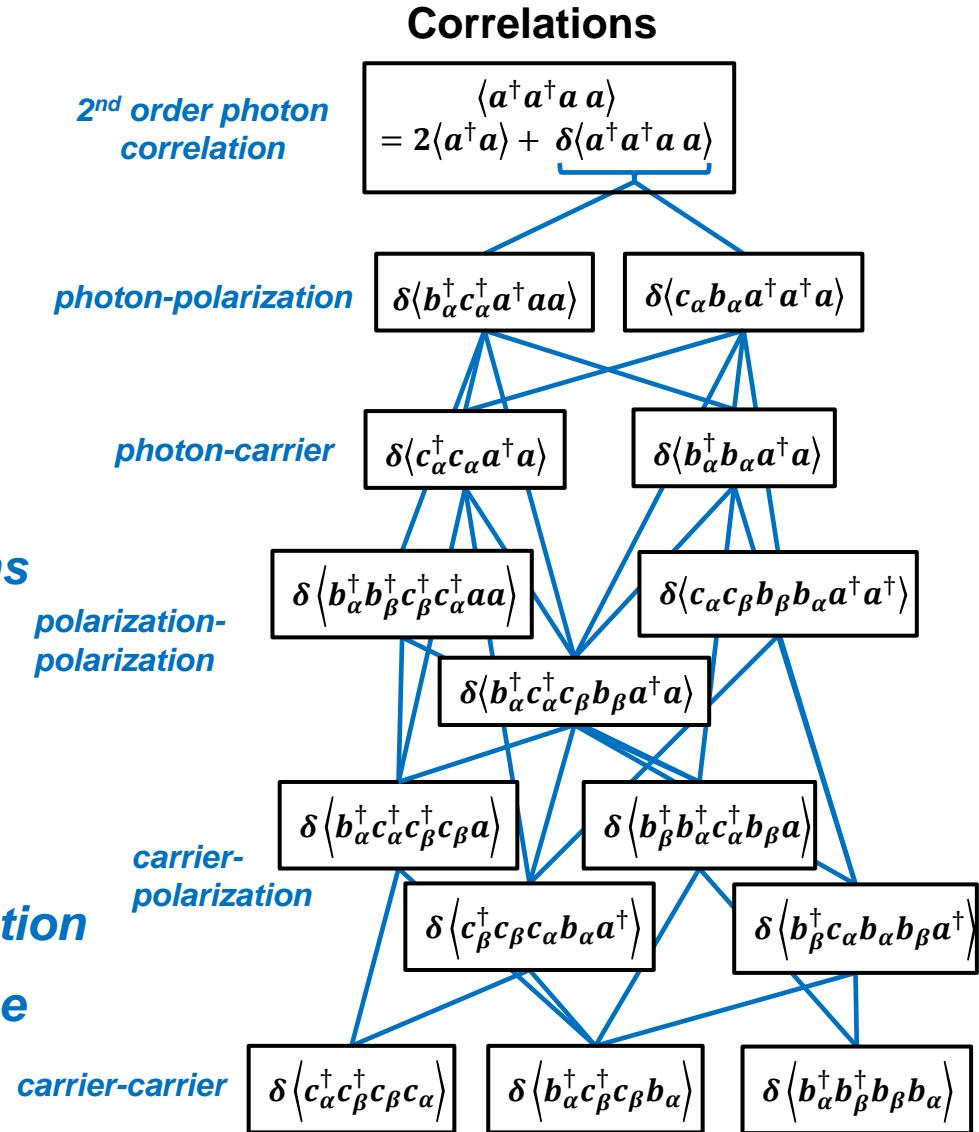
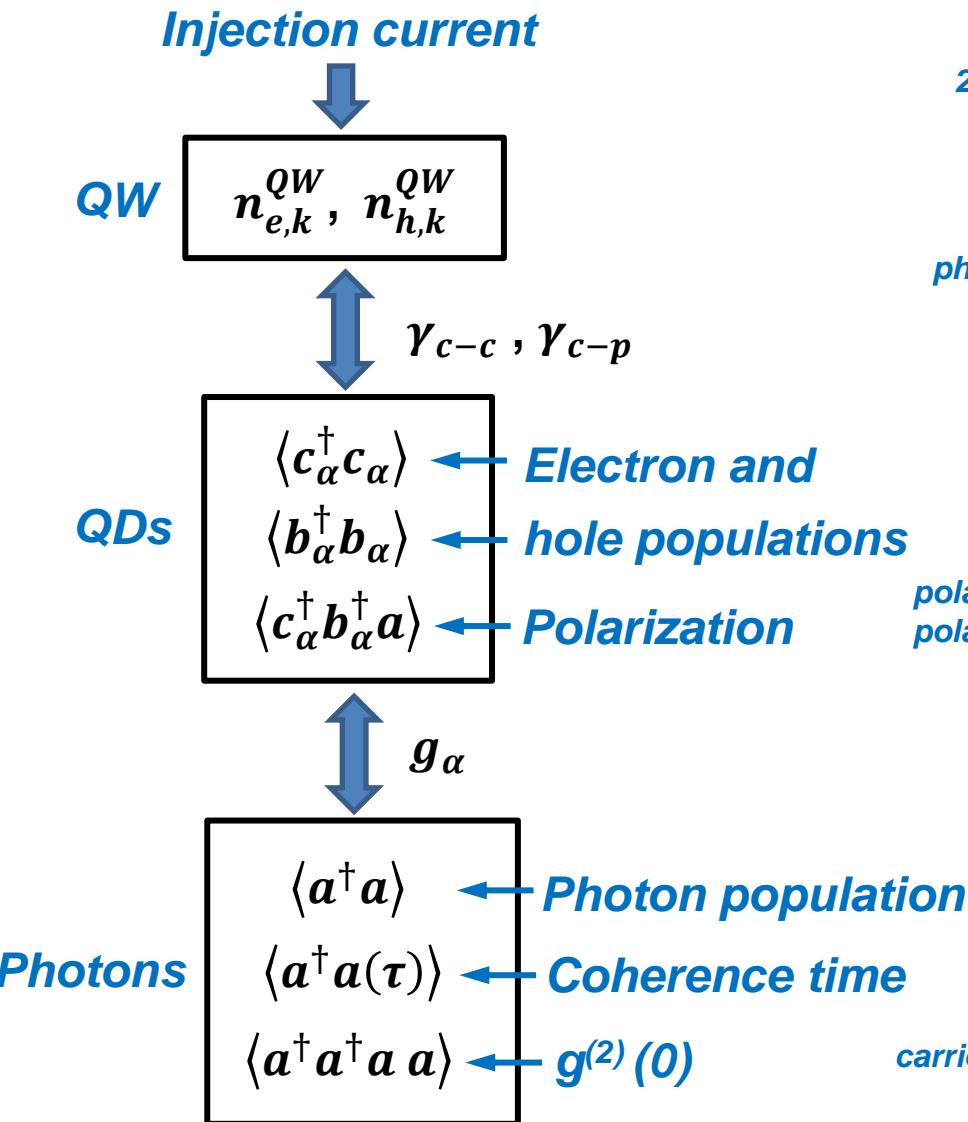
<b>Single particles</b>	<b>Correlated pairs</b>	<b>Correlated 3-particle clusters</b>
		
$+$	$+$	$+$ ...

# Nano-emitter model: population dynamics and correlations



For now emphasis is on correlations involving light-matter interaction instead of Coulomb interaction

# Nano-emitter model: population dynamics and correlations



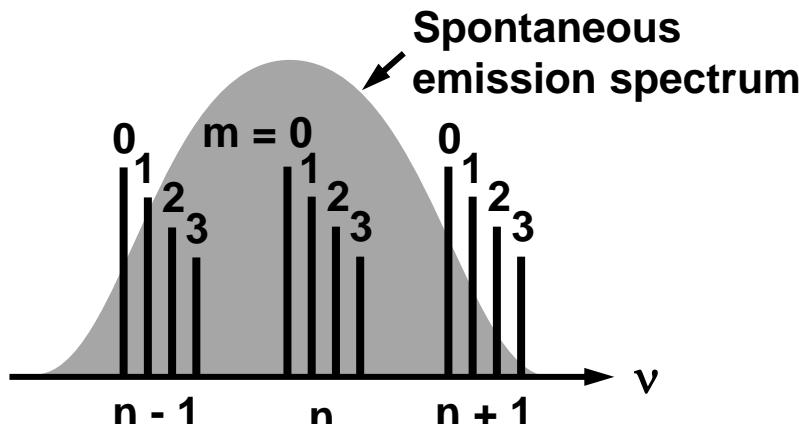
Emphasis now is on correlations involving light-matter interaction instead of Coulomb interaction

# Interesting physics with nanolasers

## Example 1: Laser threshold and thresholdless lasing

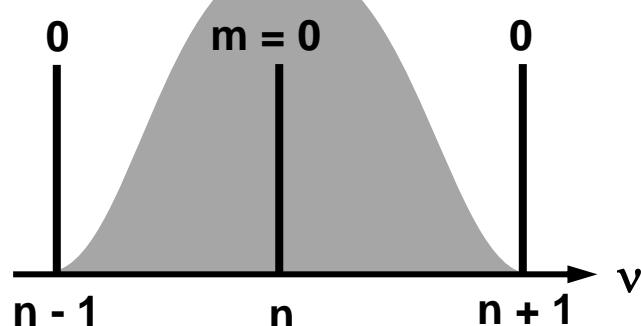
Most lasers

$\beta \ll 1$



Some nanolasers

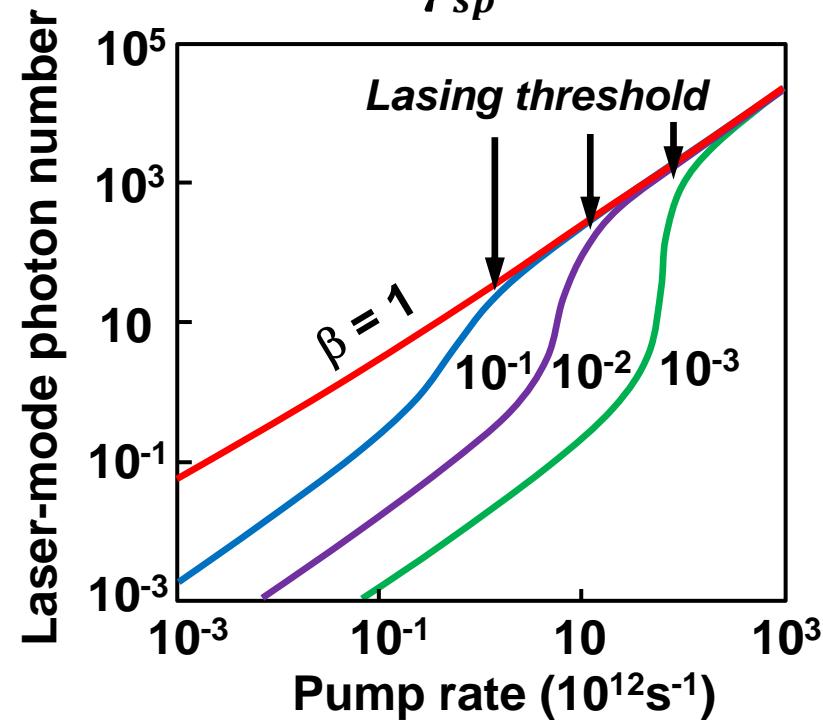
$\beta = 1$



All emission into single resonator mode

Spontaneous emission factor

$$\beta = \frac{\gamma_l}{\gamma_{sp}}$$



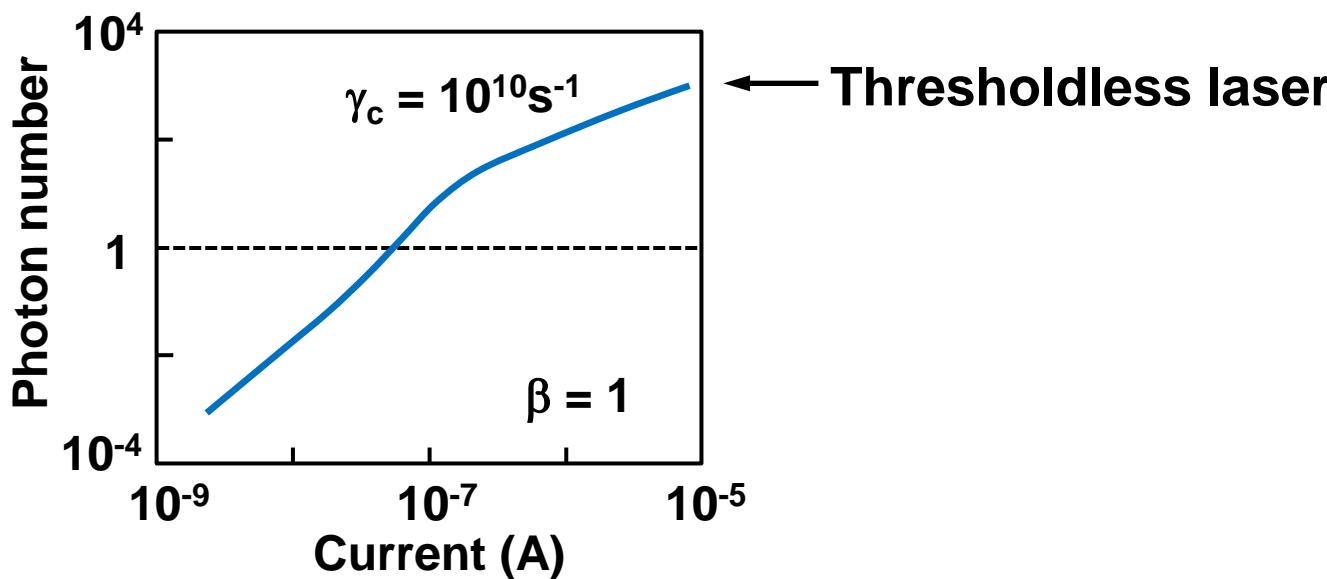
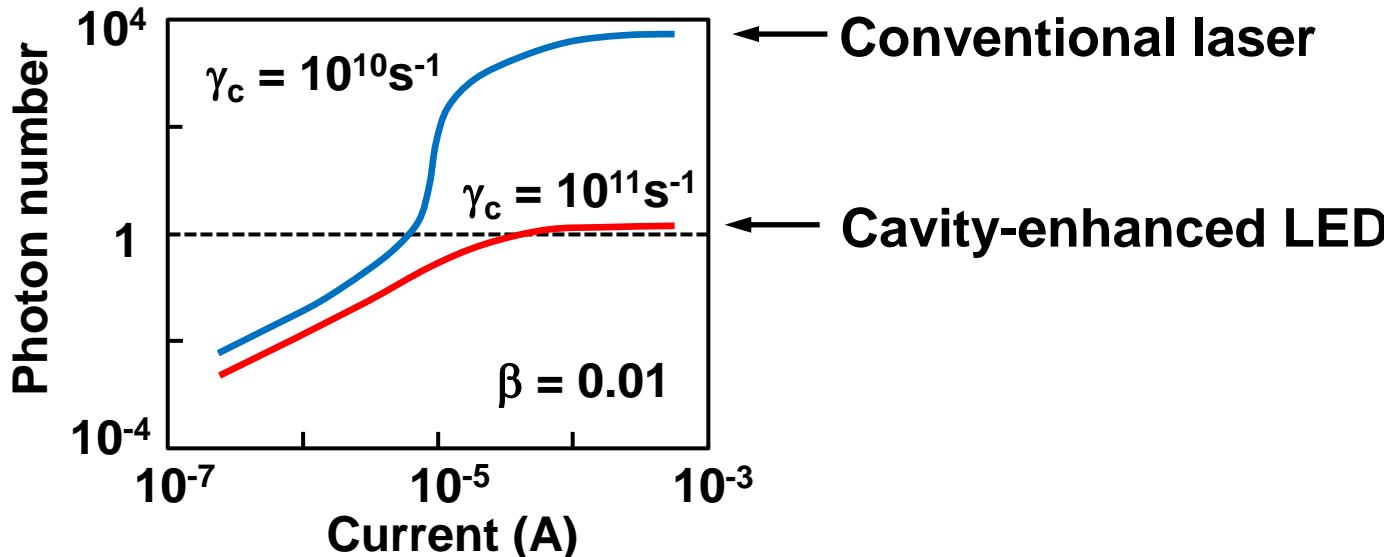
Questions:

- 1) Is thresholdless lasing real?
- 2) What is lasing?

# Criterion for lasing

$$N_{QD} = 50, \Delta_{inh} = 20\text{meV}$$

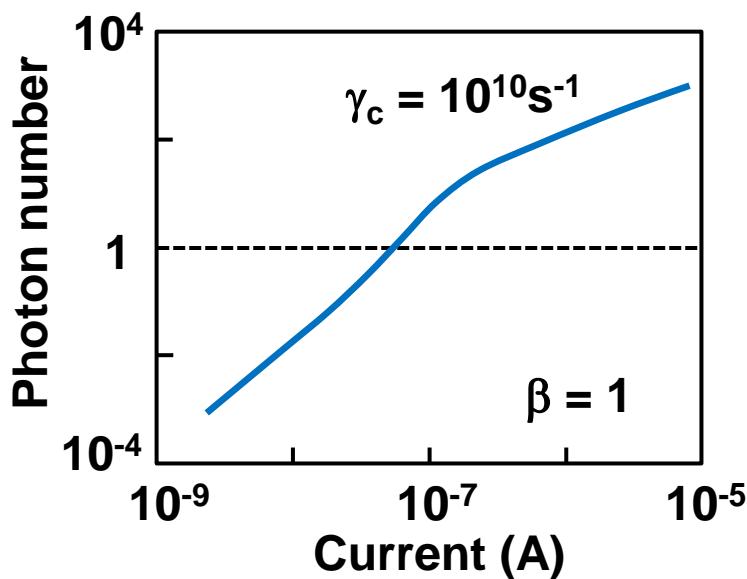
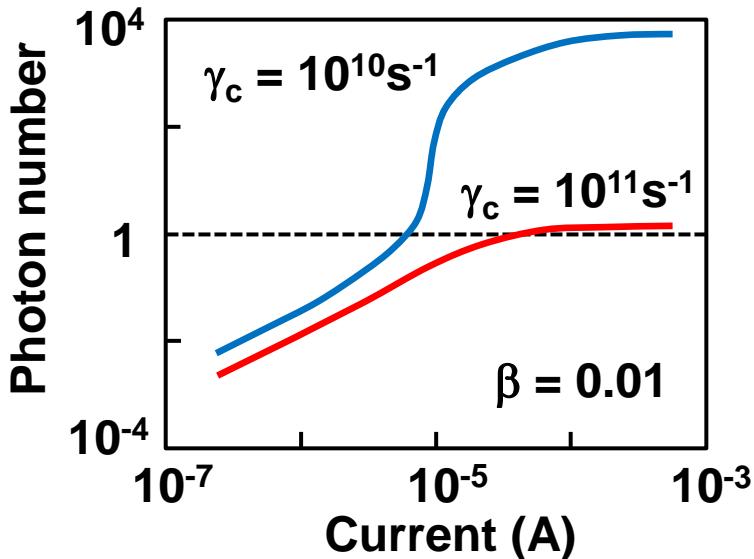
## Input/Output



# Criterion for lasing

$N_{\text{QD}} = 50, \Delta_{\text{inh}} = 20\text{meV}$

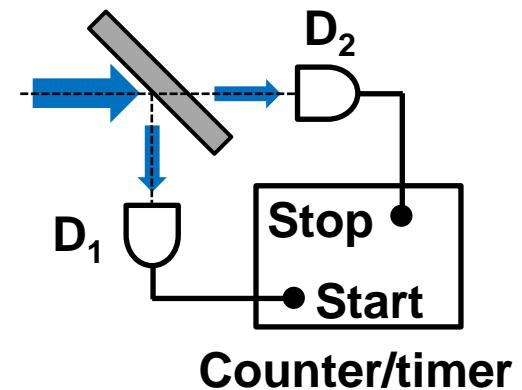
## Input/Output



## Second-order intensity correlation function

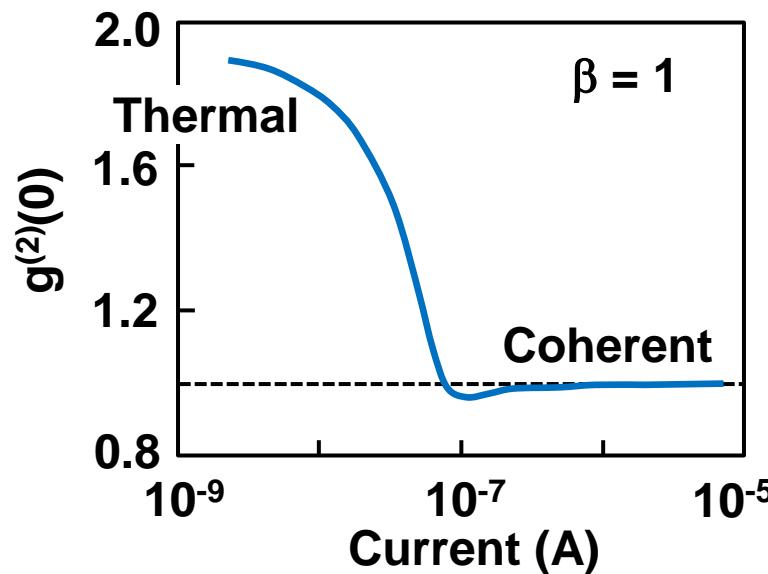
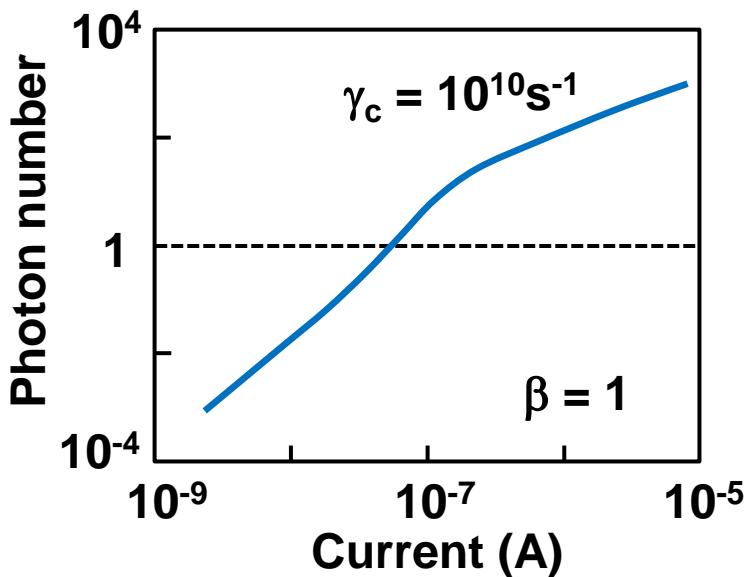
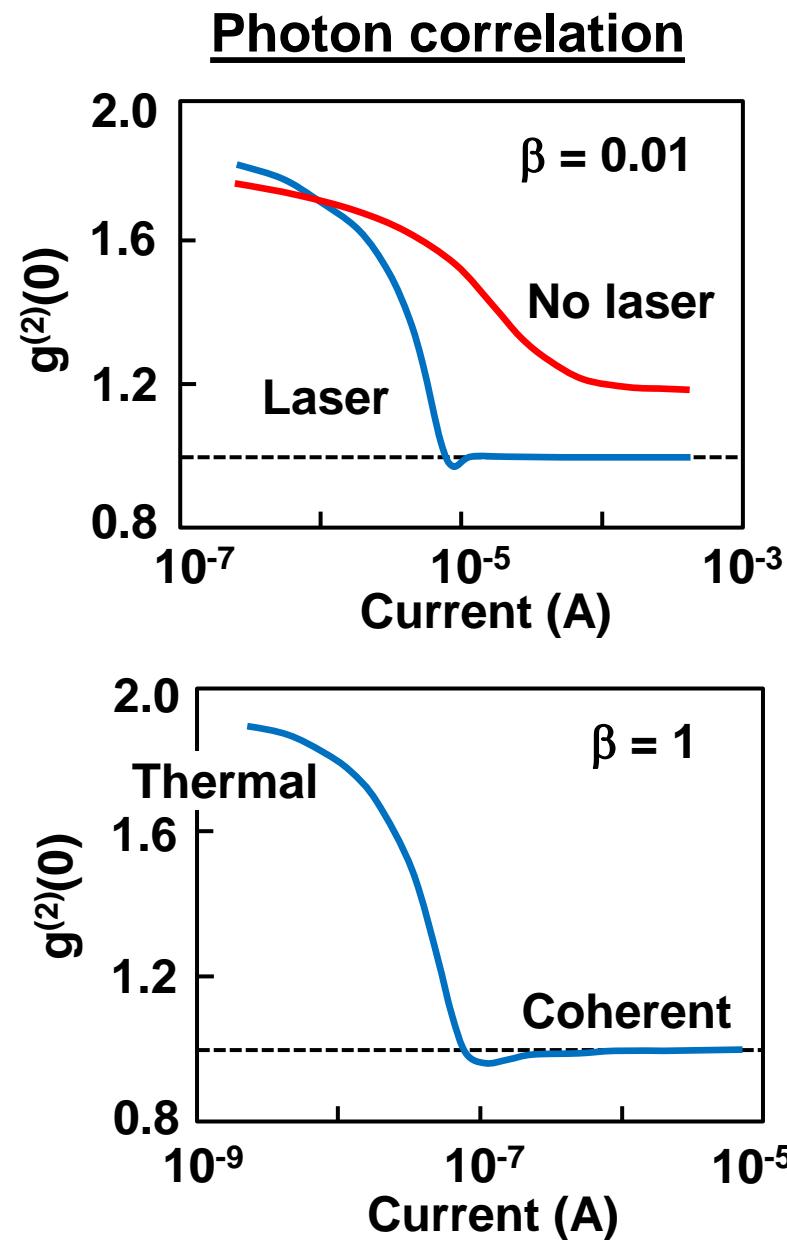
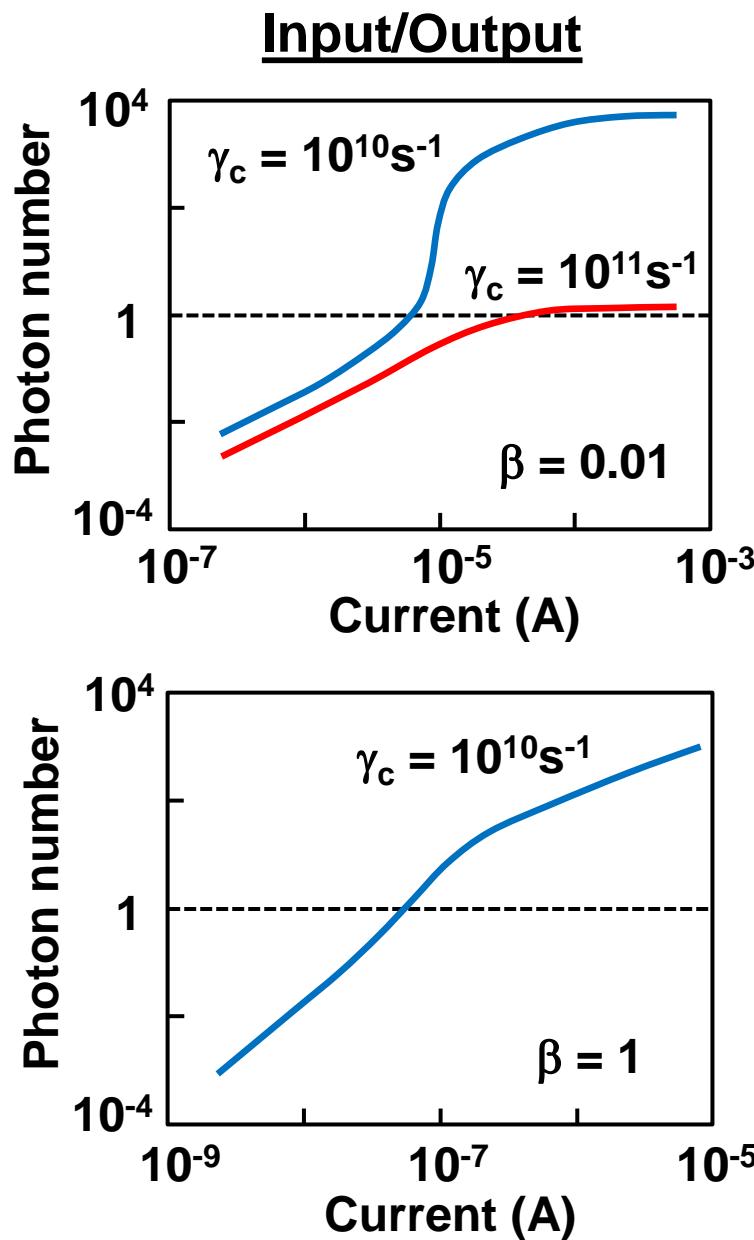
$$g^{(2)}(\tau) = \frac{\langle I(t)I(t + \tau) \rangle}{\langle I(t) \rangle^2}$$

## Hanbury-Brown-Twiss experiment



# Criterion for lasing: $g^{(2)}(0)$

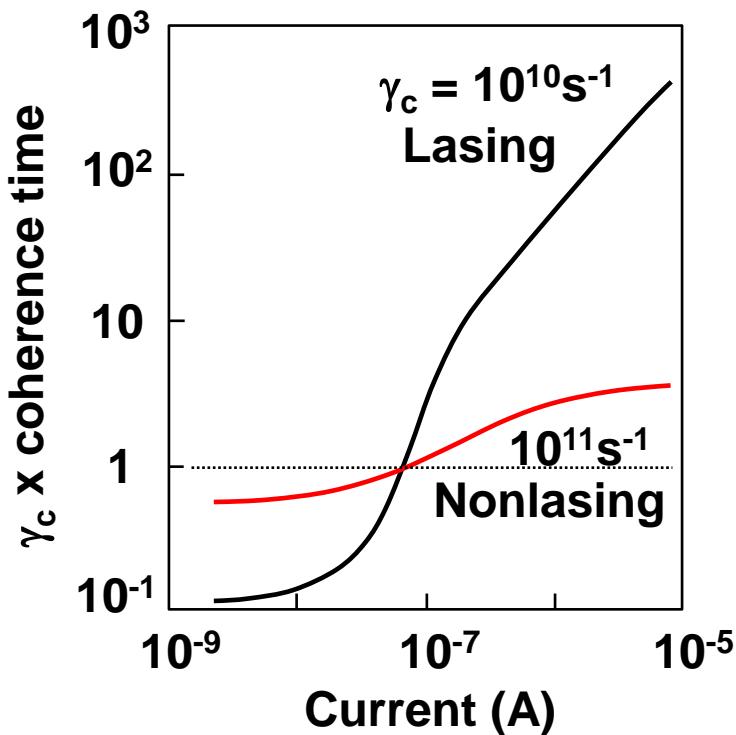
$N_{\text{QD}} = 50, \Delta_{\text{inh}} = 20\text{meV}$



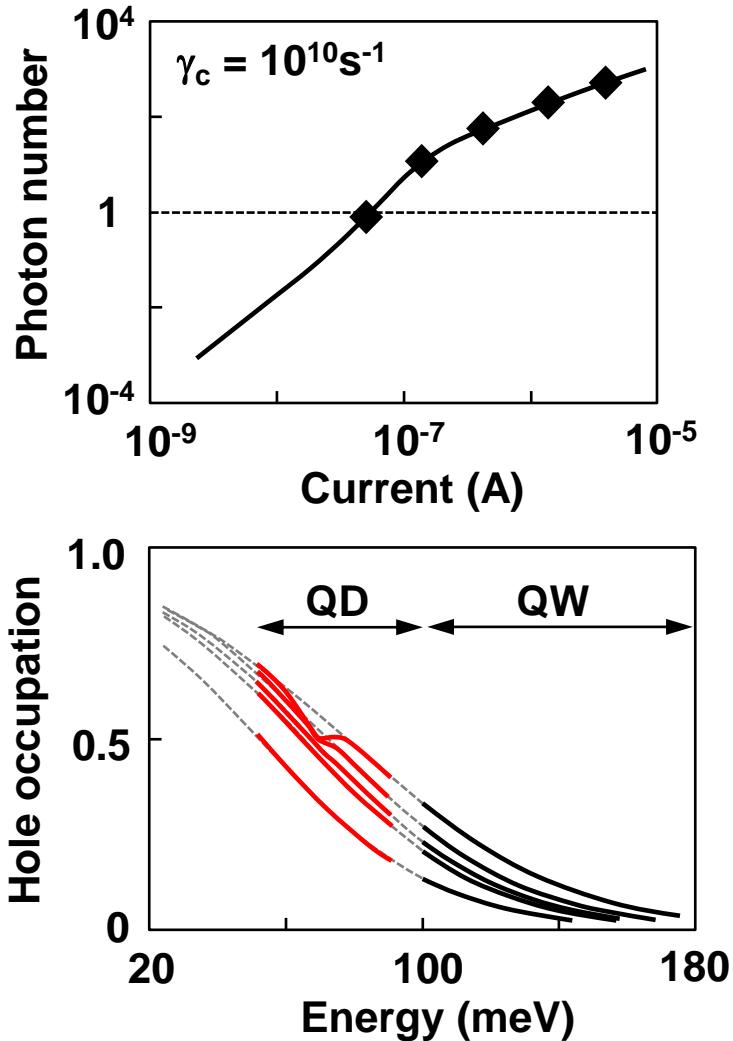
# Other criteria for lasing

## Coherence time

$$\tau_c = 2 \int_{-\infty}^{\infty} d\tau \left| \frac{\langle a^\dagger a(\tau) \rangle_{ss}}{\langle a^\dagger a \rangle_{ss}} \right|^2$$

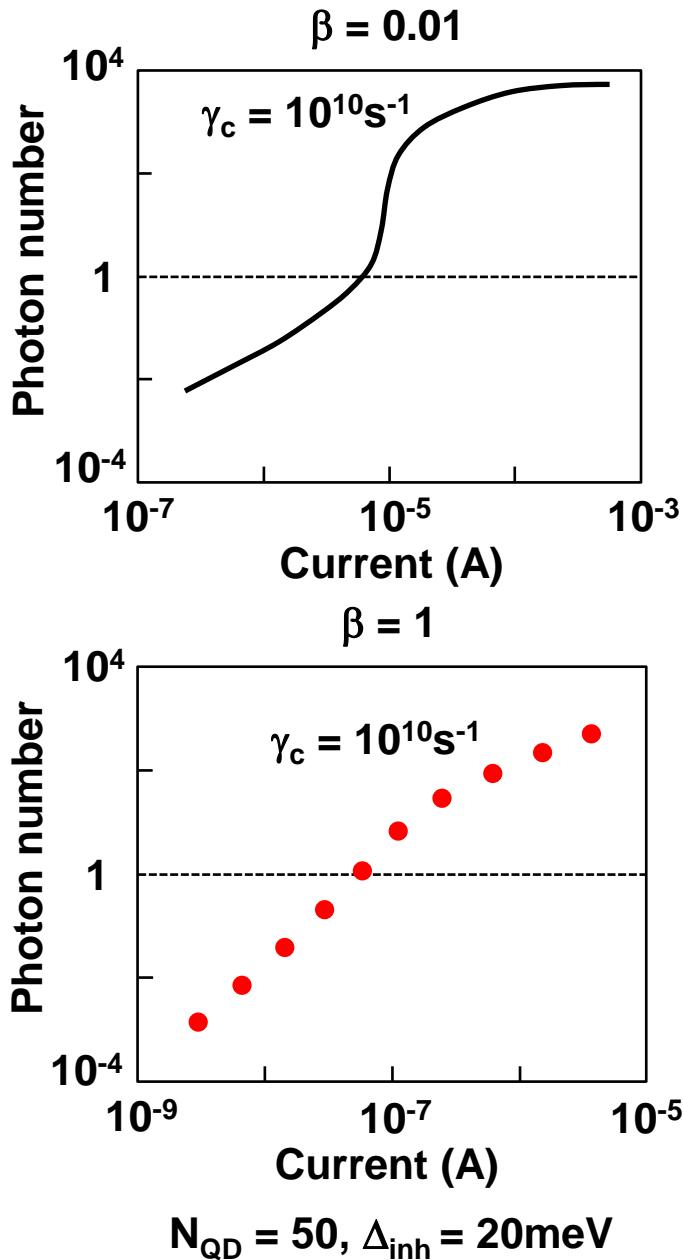


## Population clamping and hole burning



$$\beta = 1, N_{\text{QD}} = 50, \Delta_{\text{inh}} = 20 \text{ meV}$$

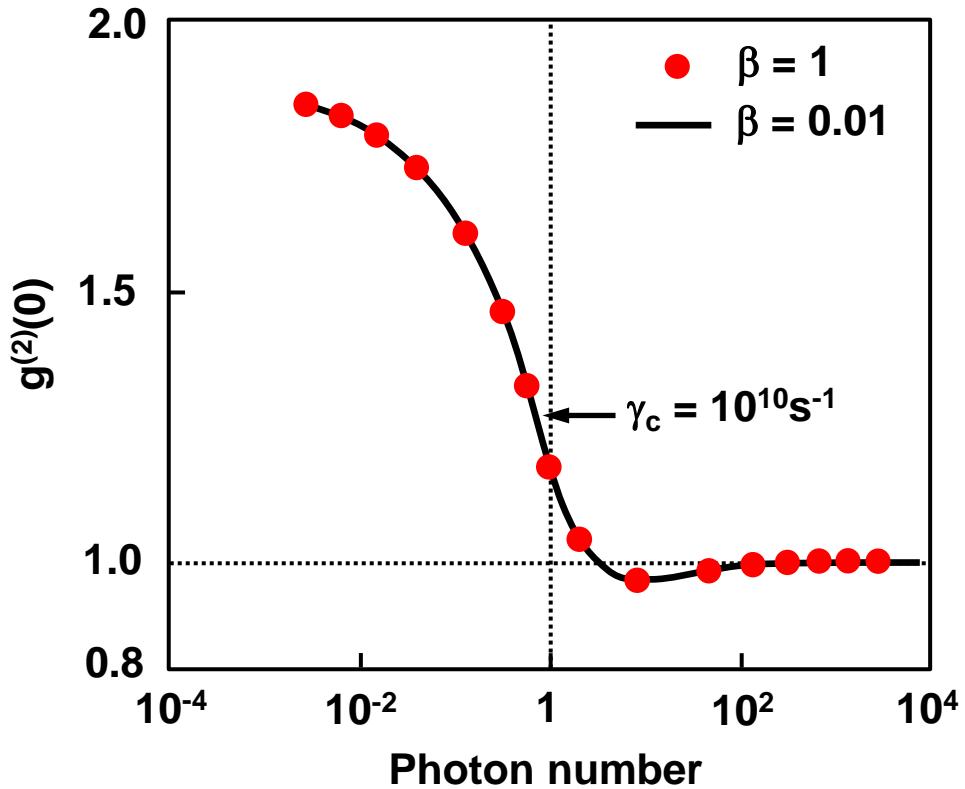
# Other criteria for laser: stimulated emission



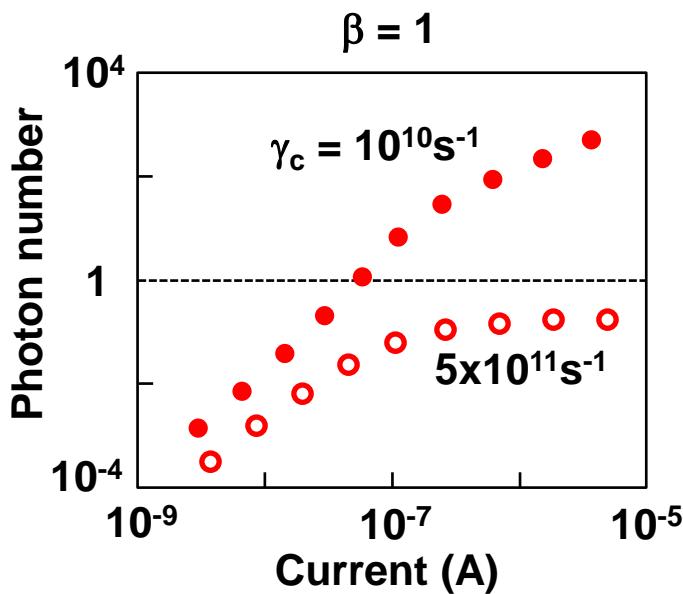
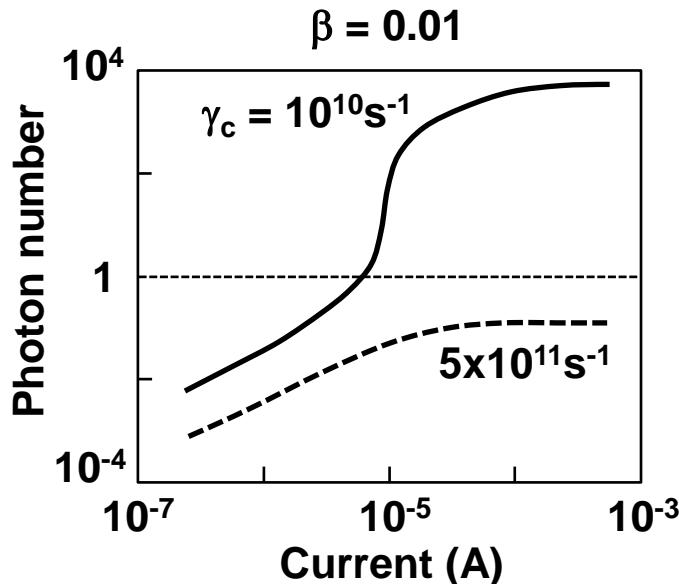
Light amplification by stimulated emission of radiation

$$\frac{dP_a}{dt} = -\gamma_l(n + 1)$$

Stimulated emission      Spontaneous emission



# Other criteria for laser: stimulated emission



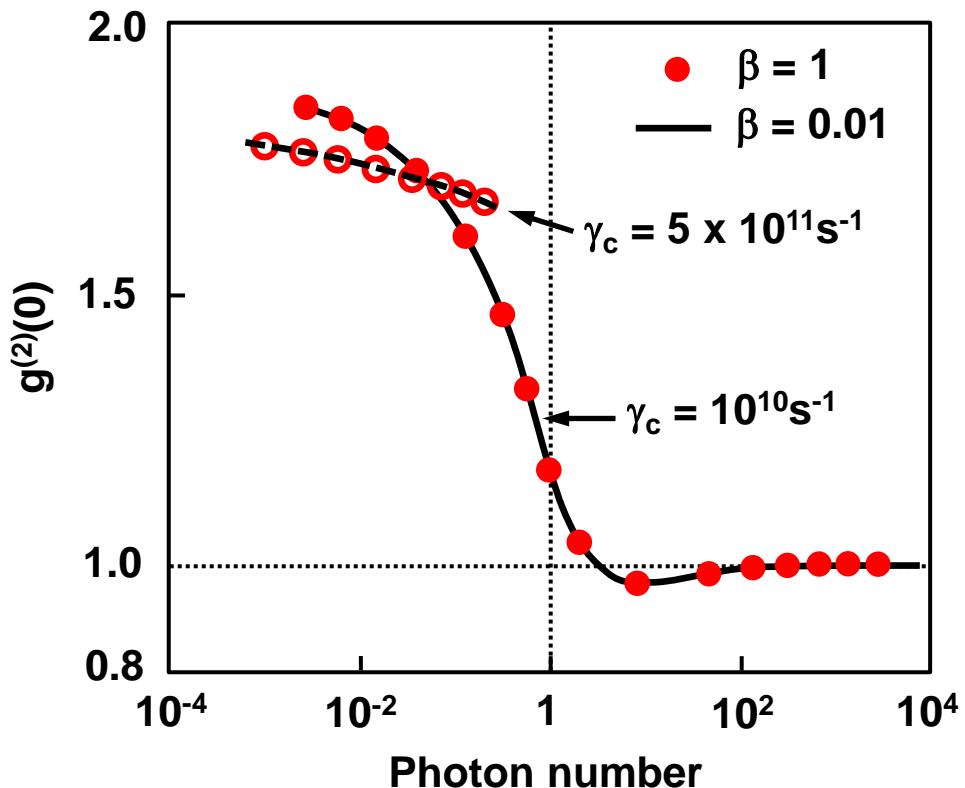
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↑                           ↑

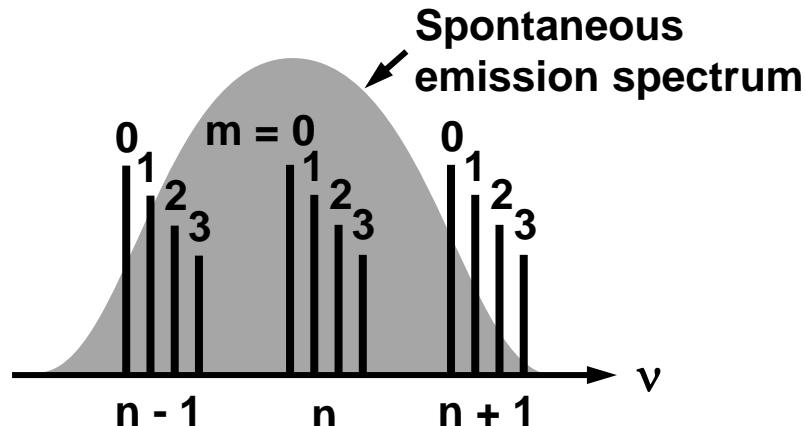
Stimulated                   Spontaneous  
emission                   emission



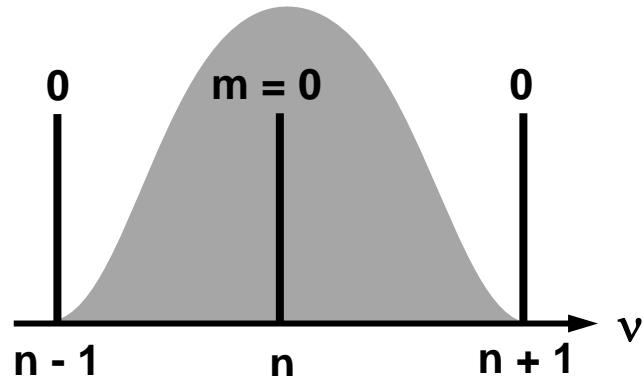
# Interesting physics with nanolasers

## Example 1 Thresholdless lasing

Most lasers  $\beta \ll 1$



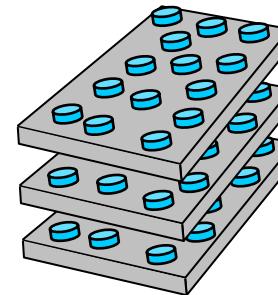
Some nanolasers  $\beta = 1$



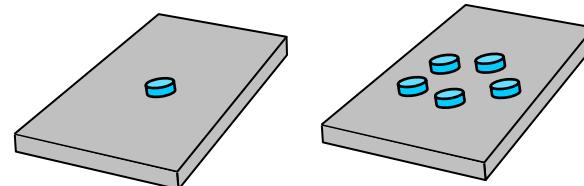
All emission into single resonator mode

## Example 2 Single-photon generation

Most QD-laser active regions



Few- QD active regions



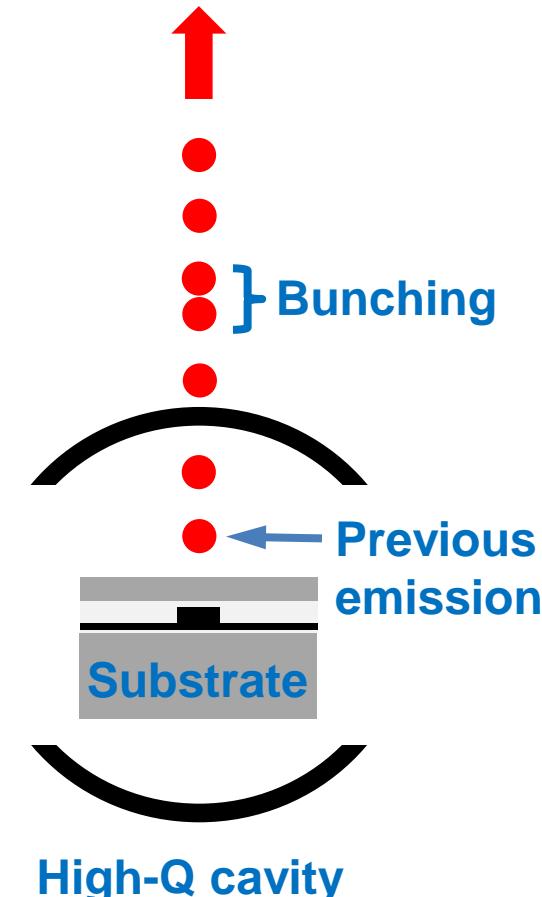
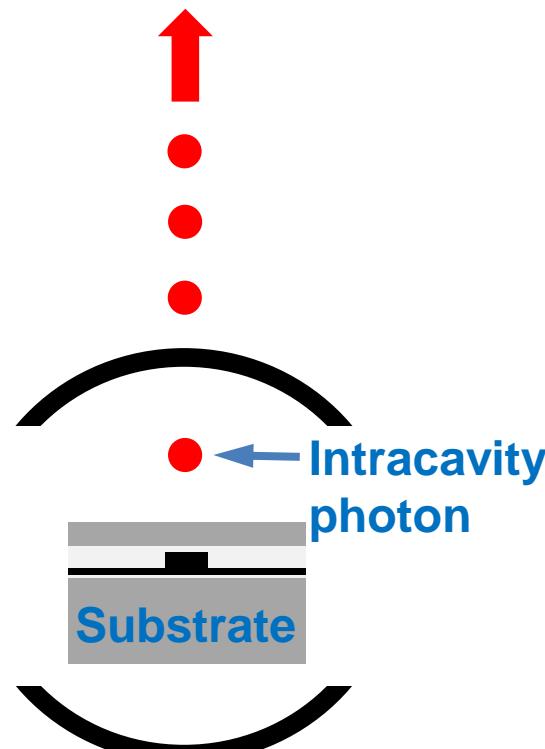
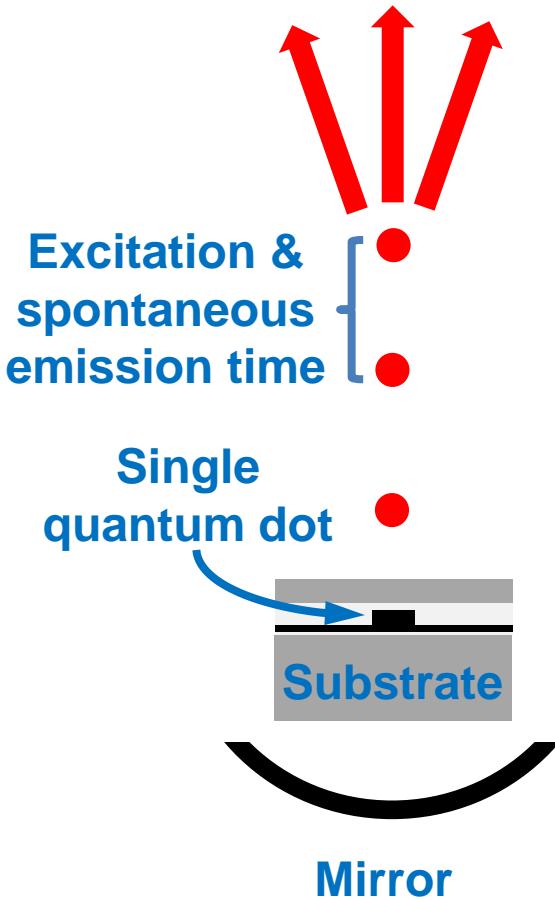
Nonclassical light

# Single-photon source

Error-free but slow

Cavity enhancement:  
Directionality and Purcell

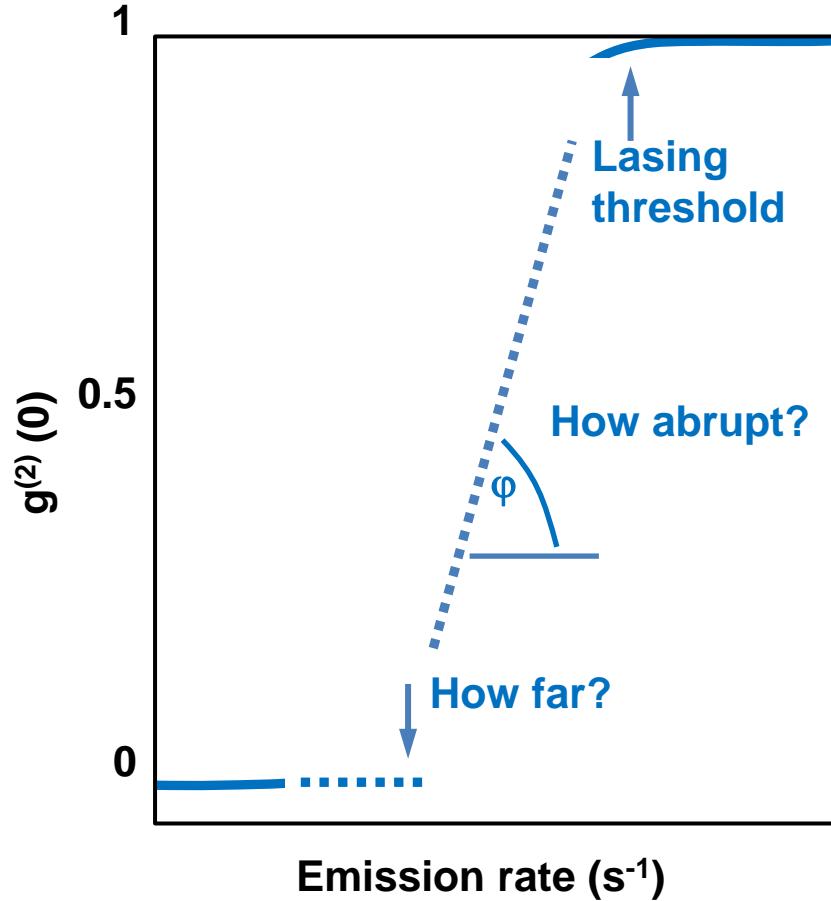
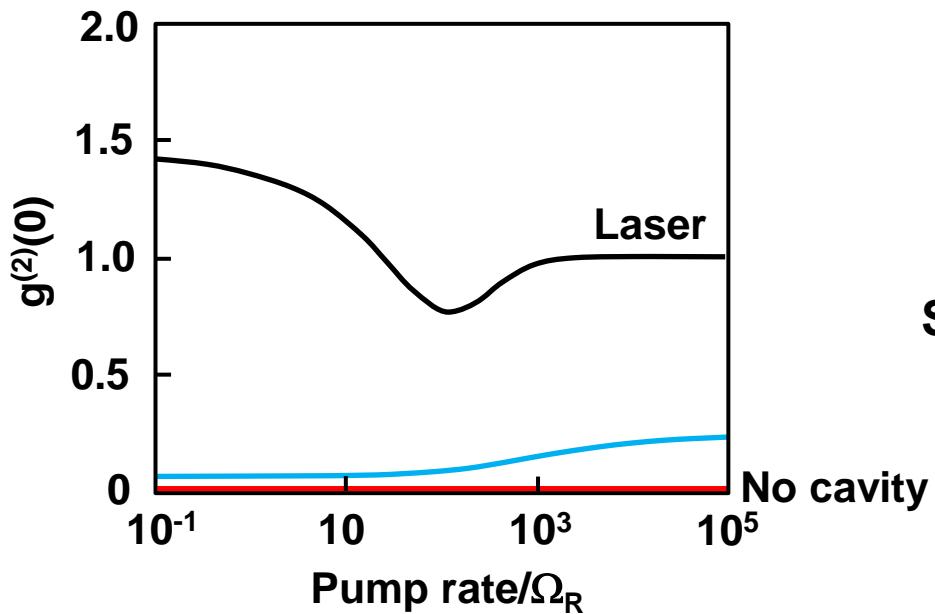
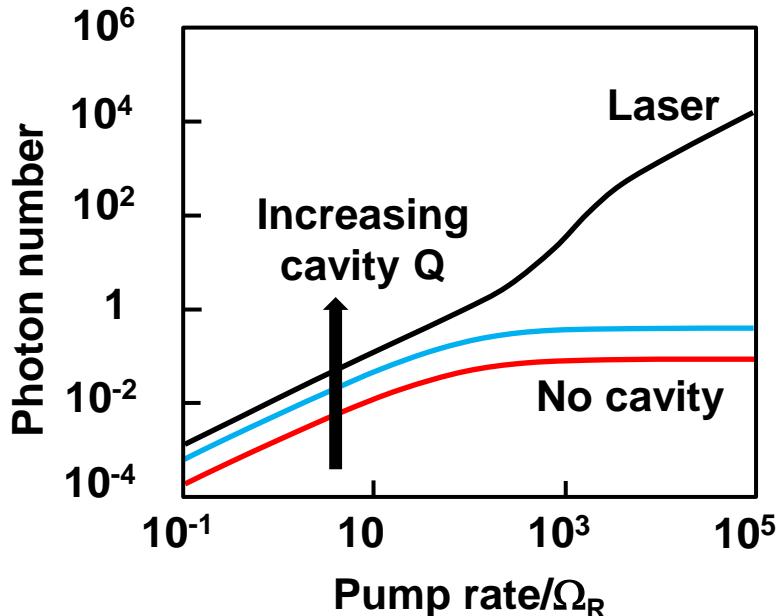
Too much cavity



What is the right Q?

Fundamental limit to efficiency, rate and error?

# Simulations

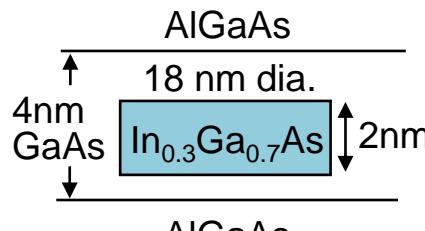
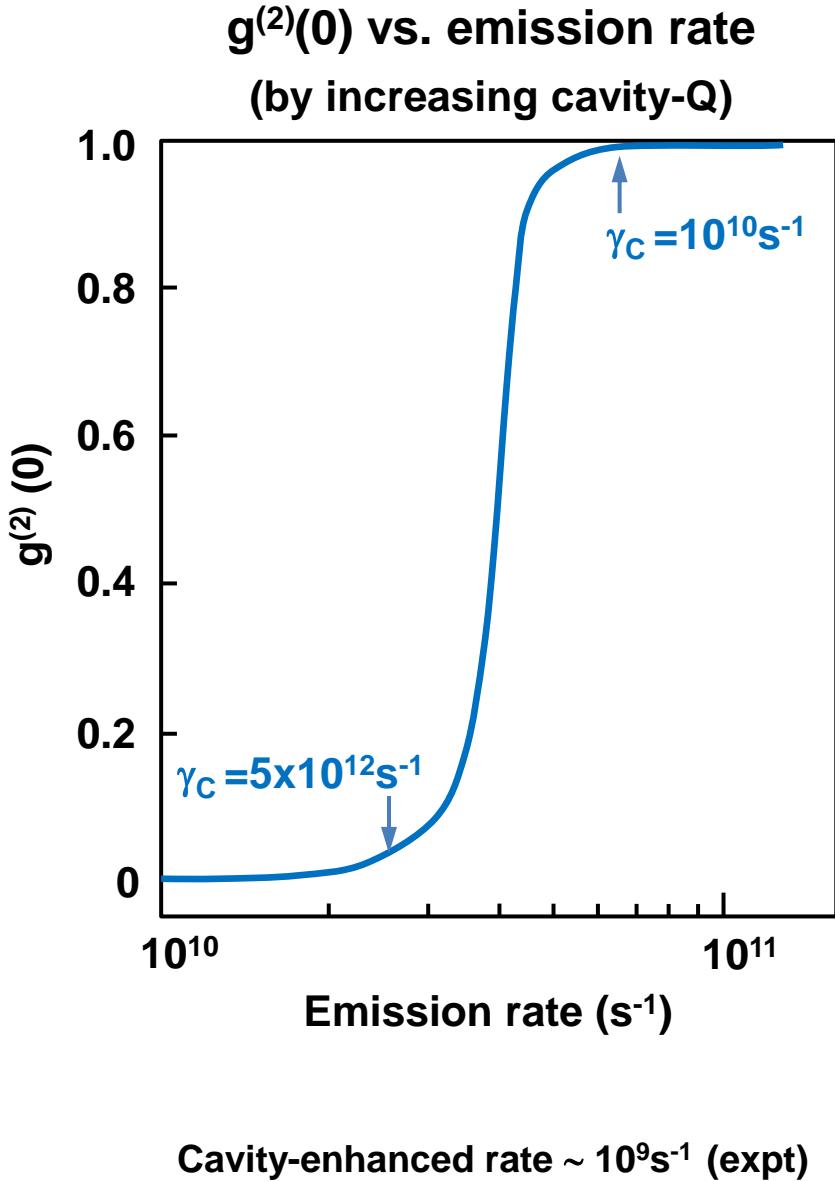


Second-order intensity correlation

$$g^{(2)}(\tau) = \frac{\langle I(t)I(t + \tau) \rangle}{\langle I(t) \rangle^2}$$

# Single-photon purity and emission rate

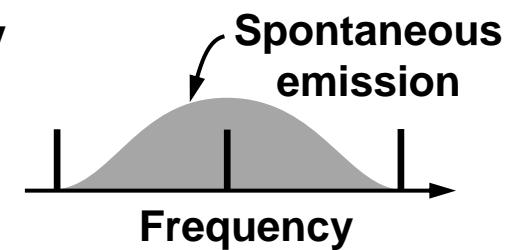
## ① Shallow quantum dot



## ② Nanocavity

$$\beta = \frac{\gamma_l}{\gamma_{sp}} = 1$$

**All emission into single resonator mode**



## ③ Scaling with electron-light coupling

$$\mathcal{W}(R_{QD}) \sum_n C(R_n) V(R_n)$$

Mode volume

Confinement factor

Electron-hole envelope overlap

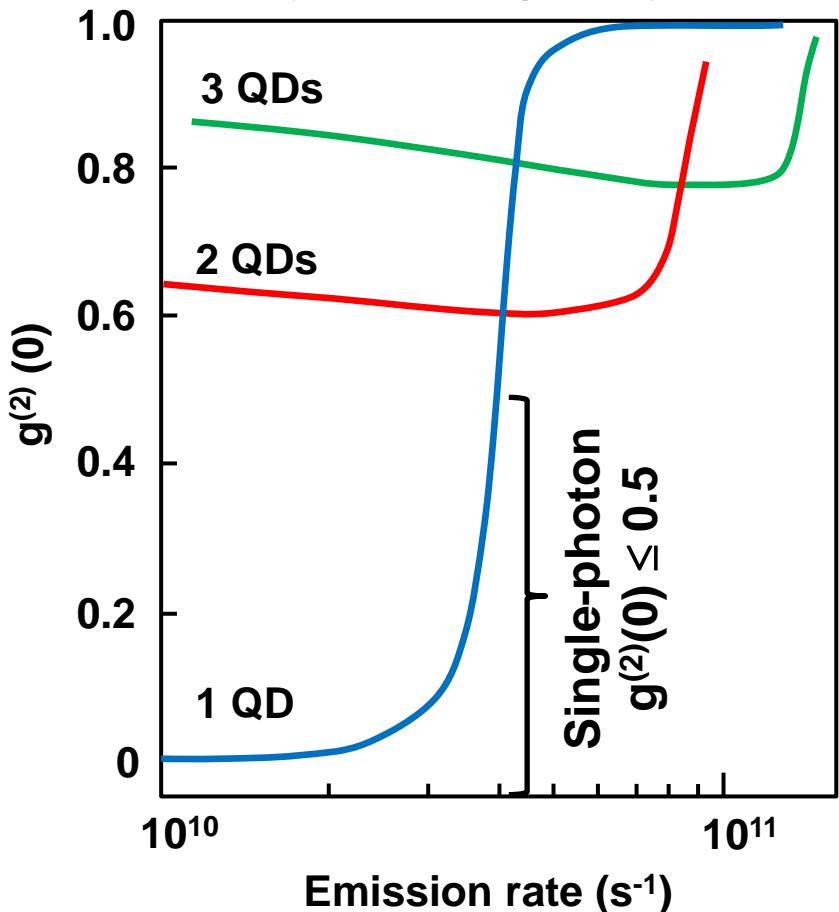
Diagram illustrating the scaling of the emission rate with electron-light coupling. The expression  $\mathcal{W}(R_{QD}) \sum_n C(R_n) V(R_n)$  is shown, where  $\mathcal{W}(R_{QD})$  is the mode volume and  $\sum_n C(R_n) V(R_n)$  is the electron-hole envelope overlap. The confinement factor is also mentioned.

# Concern: $g^{(2)}(0)$ as measure of error

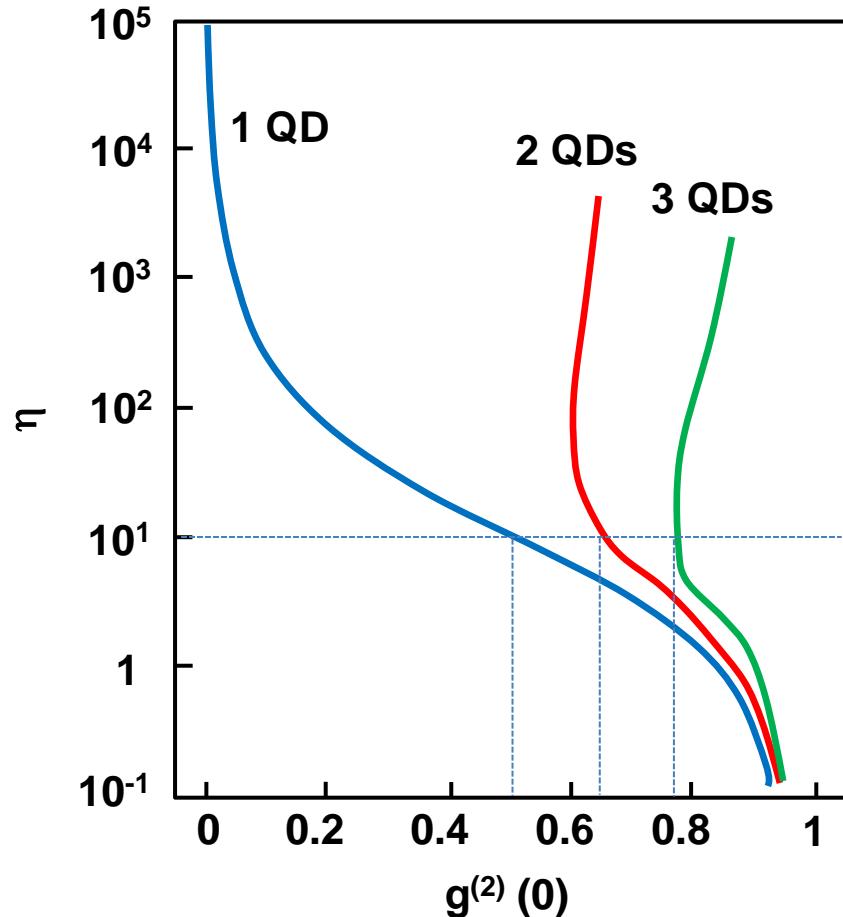
Single-photon purity:  $\eta =$

Single-photon emission probability  
Multi-photon emission probability

$g^{(2)}(0)$  vs. emission rate  
(by increasing cavity-Q)



$g^{(2)}(0)$  fails



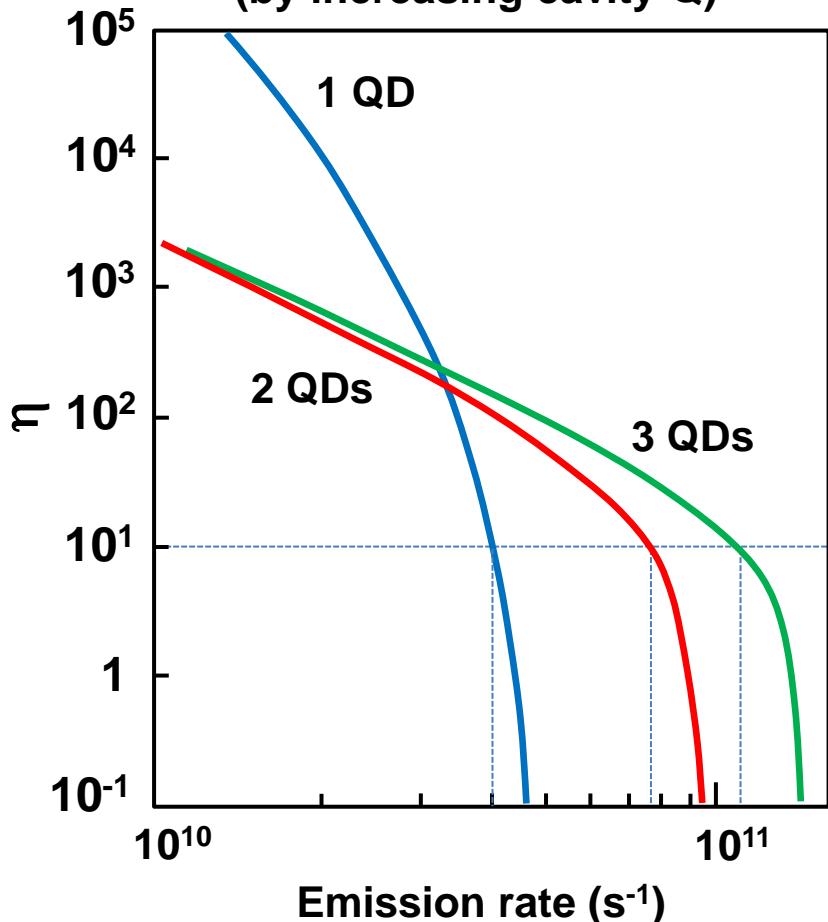
From calculating photon statistics  
Gies, Jahnke, Chow (submitted)

# Concern: $g^{(2)}(0)$ as measure of error

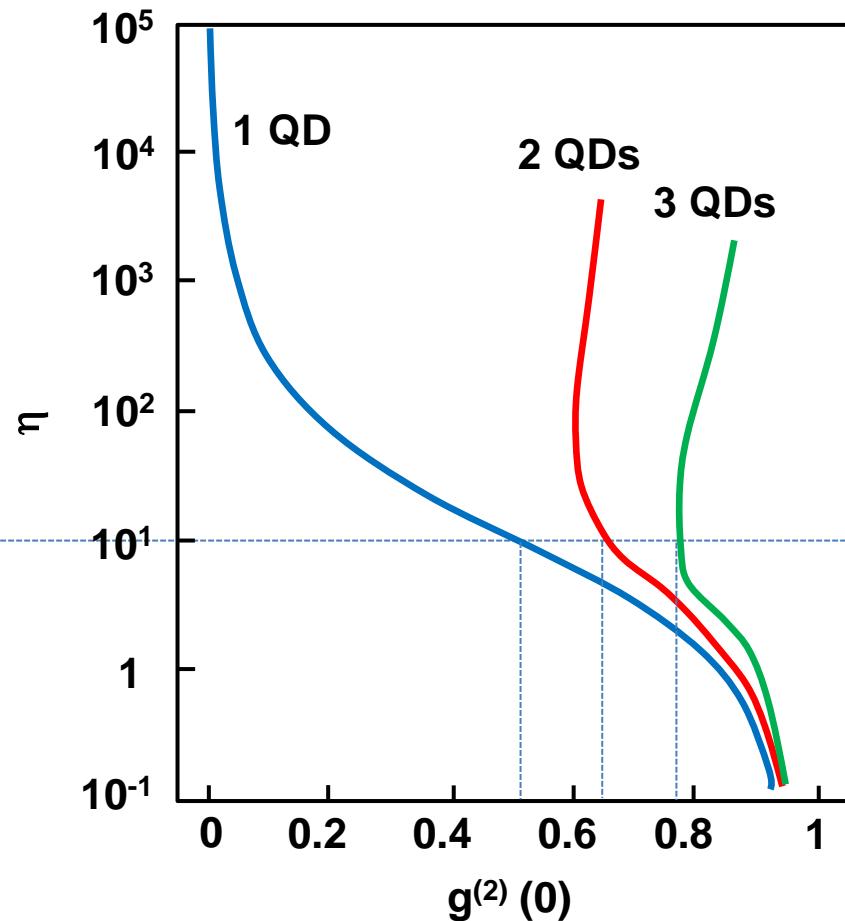
Single-photon purity:  $\eta =$

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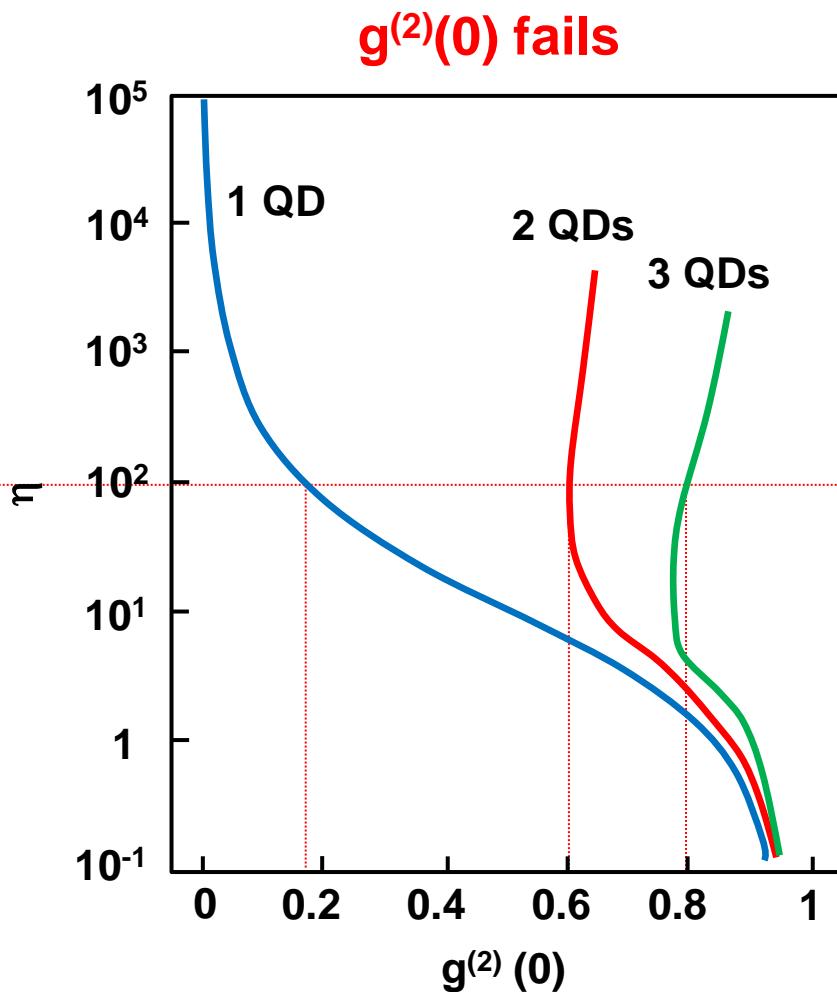
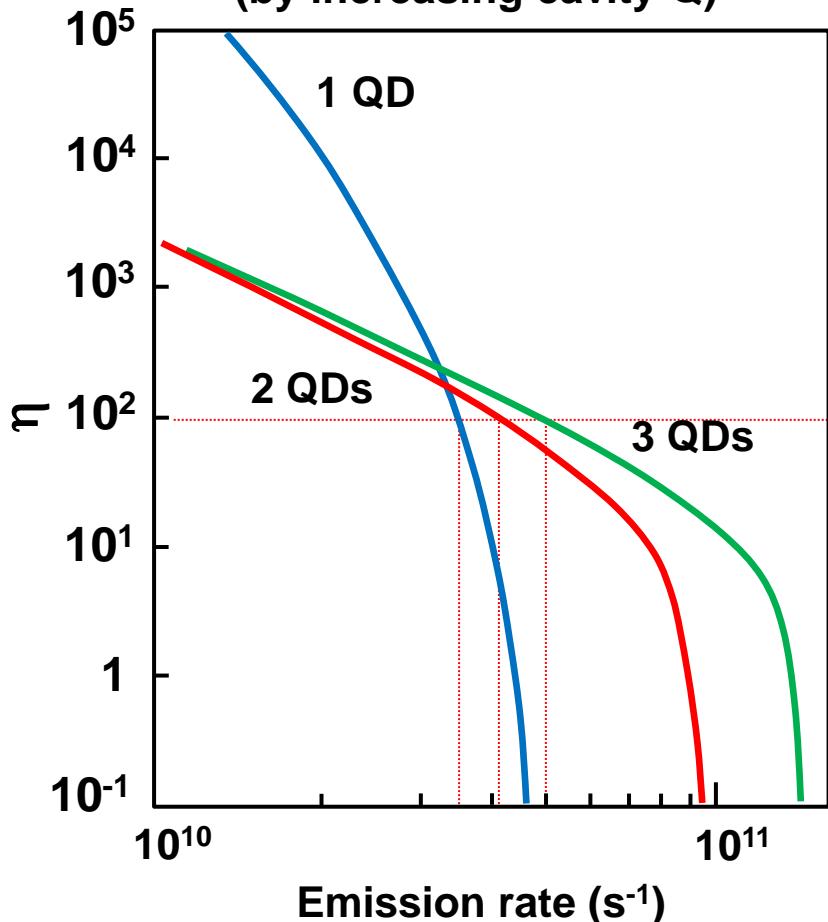


# Concern: $g^{(2)}(0)$ as measure of error

Single-photon purity:  $\eta =$

Single-photon emission probability  
Multi-photon emission probability

Purity vs. emission rate  
(by increasing cavity-Q)



# Correlations and photon statistics in nanocavity emitters

Approach

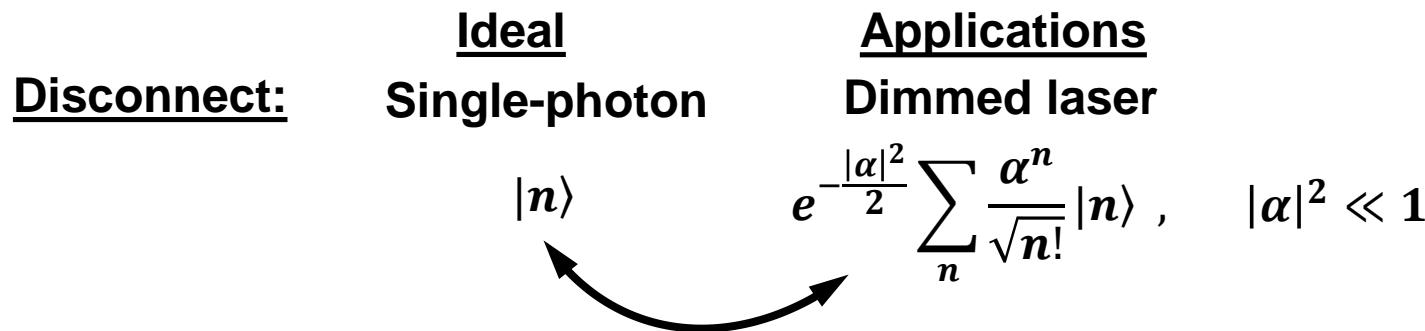
- Quantized light and carriers
- Consistent account of light-carrier correlations

## Nanolasers

- Combination of intensity &  $g^{(2)}(0)$  gives definitive description of lasing
- There is no thresholdless lasing

## Single-photon sources

### Quantum communications



Bridge: tradeoff among efficiency, rate and error

- Challenges in fabrication and modeling
- Questions concerning present measure of performance

Chow & Jahnke, Progress in Quantum Electronics 37, 109 (2013)

Chow, Gies & Jahnke, Light: Science and Applications, online 29 August, 2014

# Other applications of modeling approach

## Gain medium engineering

Chow, Lorke & Jahnke, 'Will Quantum Dots Replace Quantum Wells As the Active Medium of Choice in Future Semiconductor Lasers?' IEEE J. Selected Topics in Quantum Electron. **17**, 1349 (2011).

**Frank Jahnke, Bremen University**

Liu, Chow, Gossard, Bowers, "Extraction of inhomogeneous broadening and nonradiative losses in InAs quantum-dot lasers,' (in preparation)

**John Bowers, UC Santa Barbara**

## Solid state lighting

Chow, *Novel LED Model Offers New Insights*, Compound Semiconductor Magazine, July, 2014.

**EFRC**

## Quantum optomechanics

Carmele, Kabuss & Chow, 'Highly detuned Rabi oscillations for a quantum dot in a microcavity,' Physical Review B **87**, Rapid Communication, 041305 (2013).

**Andreas Knorr: TU-Berlin**

## BEC and Atomtronics

Chow, Straatsma & Anderson, 'An engineering design tool for atomtronic circuits' (submitted PRA).

**Dana Anderson, U Colorado and JILA**

**Stephan Koch, Philipps University, Marburg**