

SAND2015-2533C

# Sensor Fusion for Intrusion Detection Under False Alarm Constraints

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<sup>1</sup>Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

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# Introduction

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## Why is this important?

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## Why is this important?

- Mostly focused on detectability
- False alarms cost money

# Motivational Questions

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**Assumption: Components function properly**

# Test Bed

## Sensor Module

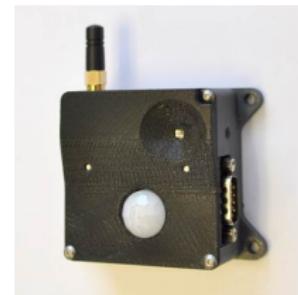
- Tri-axis accelerometer
- Photo-detector
- Passive infrared sensor

## Instrumented Room

- Placed 8 sensor modules along walls
- Modules connected via CAN bus

## Objective

- Collect background data
- Collected data during entry
- Develop algorithm to detect entry given a false alarm rate
  - Binary decision problem



# Unknown Everything?

## Binary Decision Problem: Intrusion?

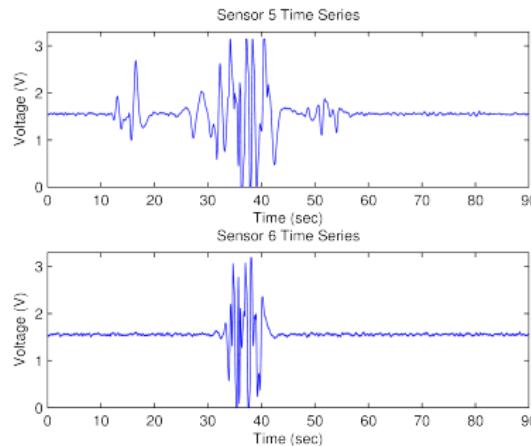
- What are the null and alternative hypotheses?
- **What is the distribution of the background noise data?**
- What is the structure/distribution of the signal?

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## Unclear how to model PIR Sensors



# Classic Example: Detection Theory

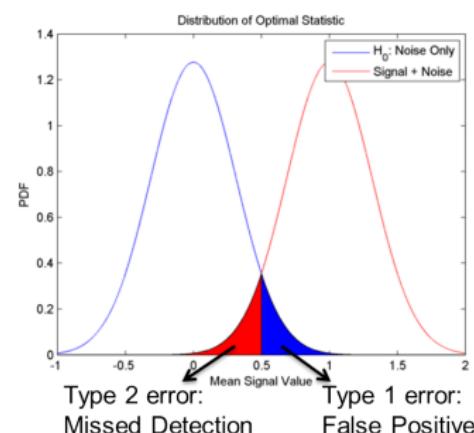
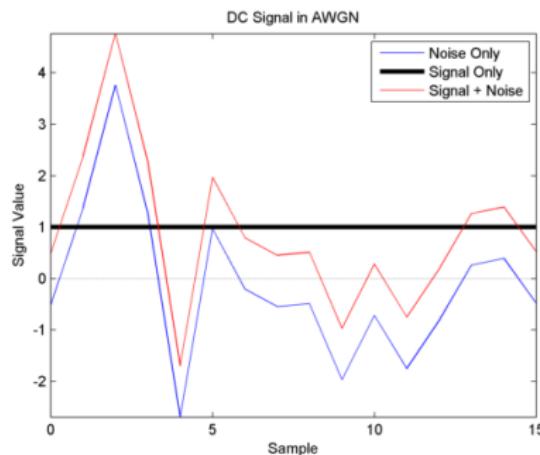
## Deciding whether or not a DC signal is present in AWGN

- $H_0$ : noise only
- $H_1$ : Known DC signal + noise
- **Note:** Signal and noise models are known!

# Classic Example: Detection Theory

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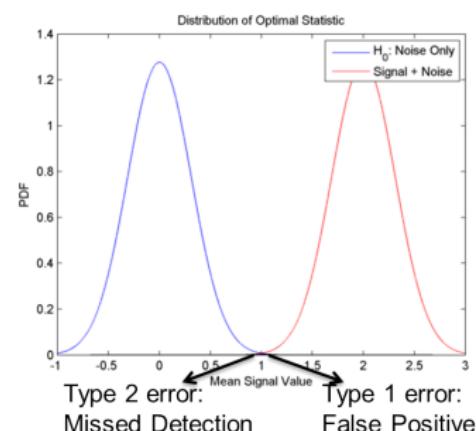
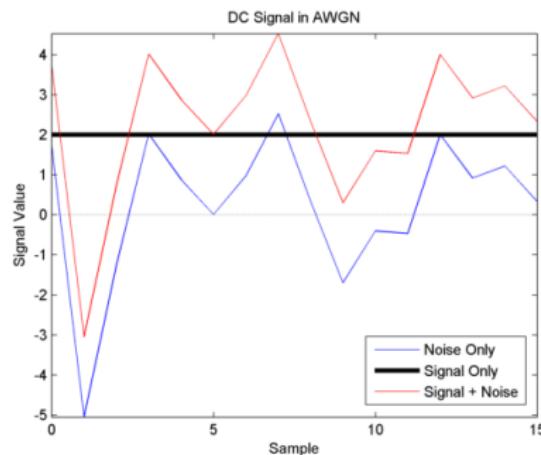
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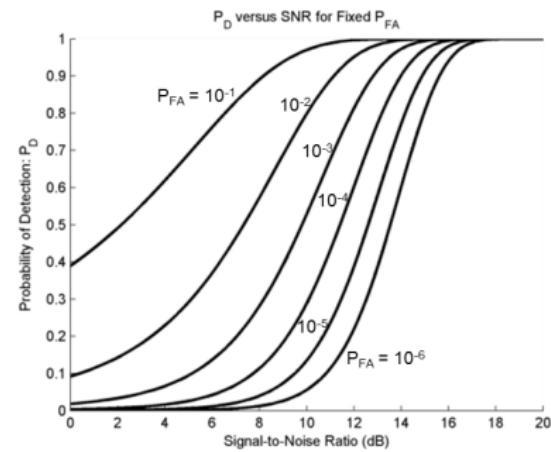
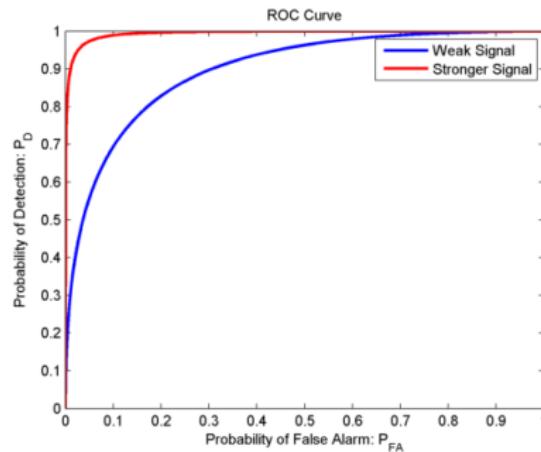
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# Classic Example: ROC Curves

**Error probabilities depend on Signal-to-Noise Ratio (SNR)**

- Signal power
- Signal length
- Noise variance

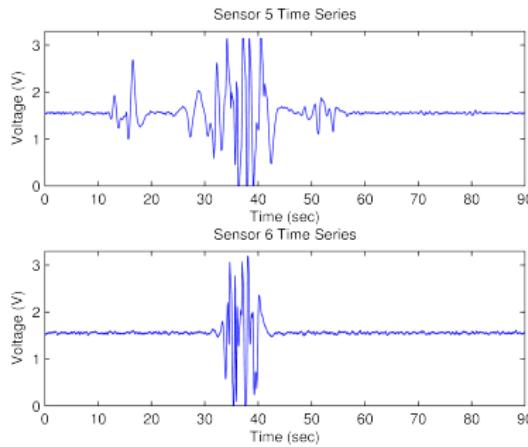


# Unknown Everything - Revisited

## Binary Decision Problem: Intrusion?

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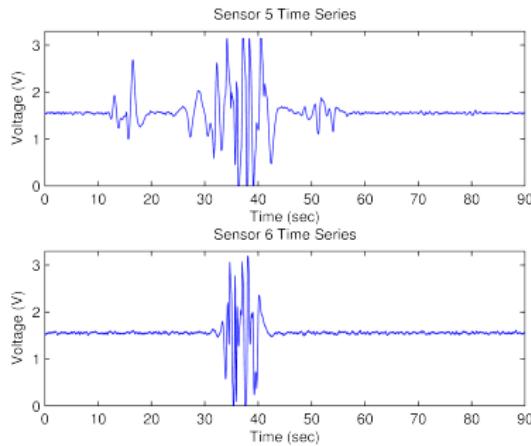


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### Approach

- Model background “noise”
- Declare an event when signal deviates from the background by a specified amount
- Threshold determined by false alarm constraint
- Theoretical ROC curves not possible

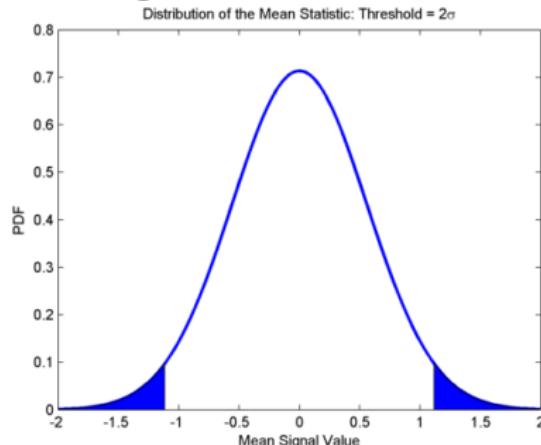
# Matching the Noise Distribution

## Statistical Model of Noise Distribution → Problem Solved

- Compute threshold to meet false alarm requirement
- Declare an event when signal metric exceeds threshold

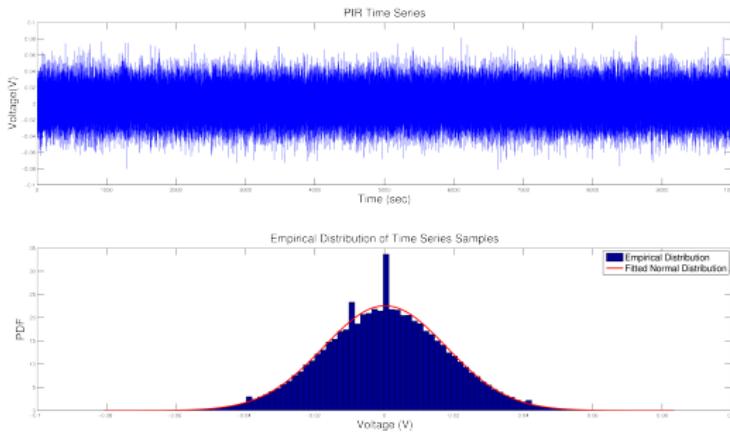
### Example

- $H_0$ : Noise only
- $H_1$ : Not noise



- Selected threshold s.t. probability of false alarm is 5%
- Threshold computed from distribution of noise metric
- What is the distribution of the noise metric?

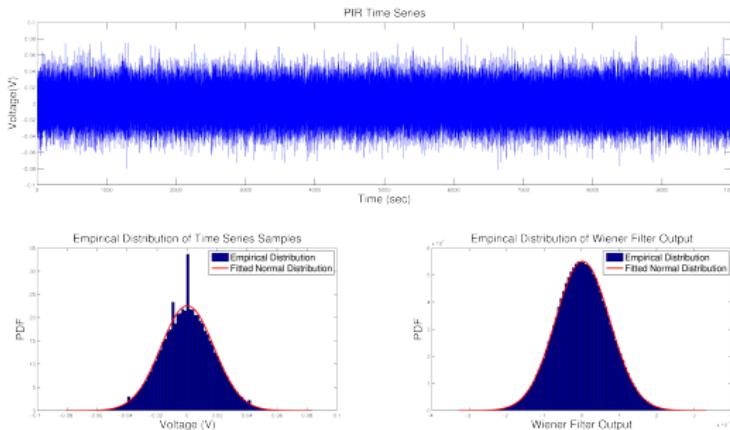
# Time Domain Approach



## Looks “close” to a Gaussian marginal distribution

- Need to be confident otherwise false alarm constraint is meaningless
- How to have confidence?
  - Match data to theoretical model
  - Gather large amounts of data for empirical estimates

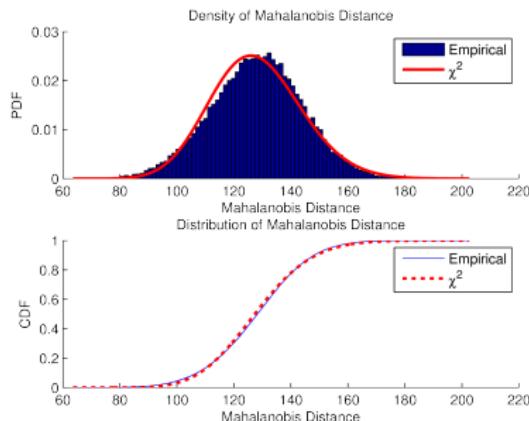
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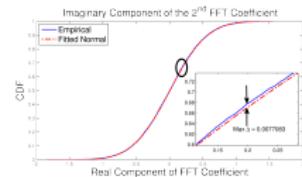
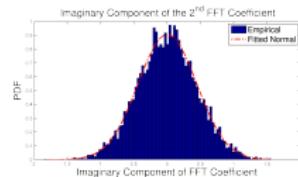
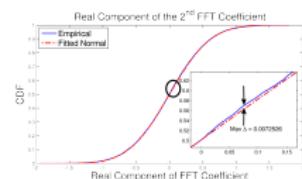
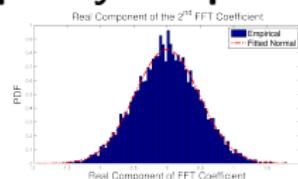
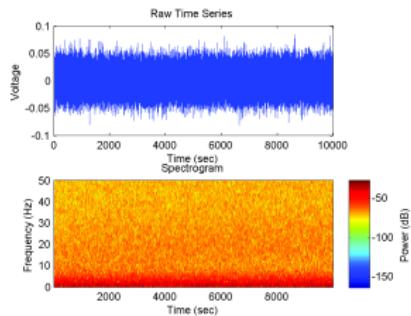


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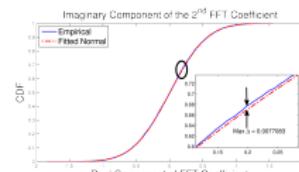
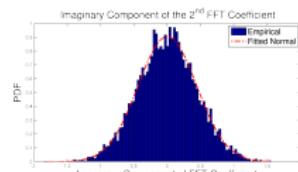
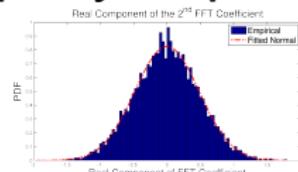
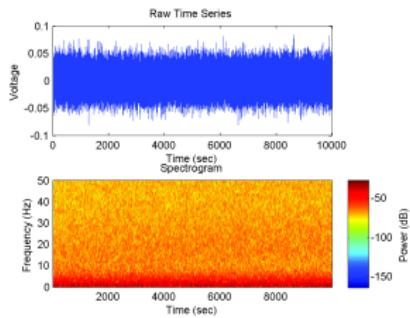
# Frequency Domain Approach

## Analyze distribution of frequency components



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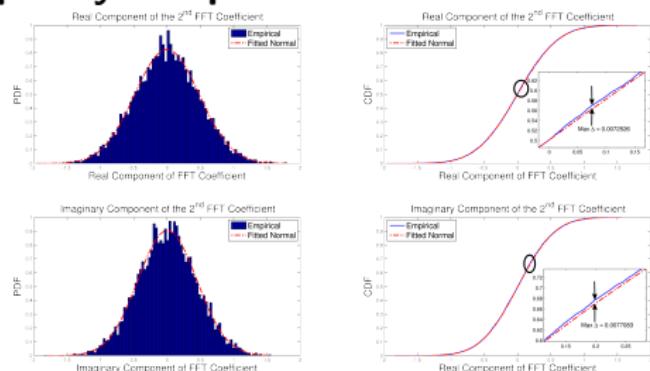
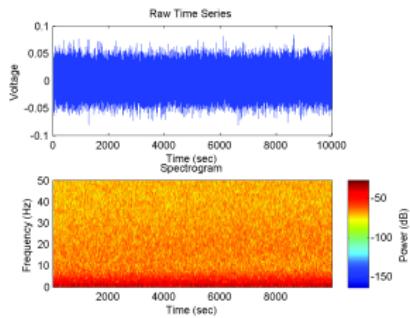
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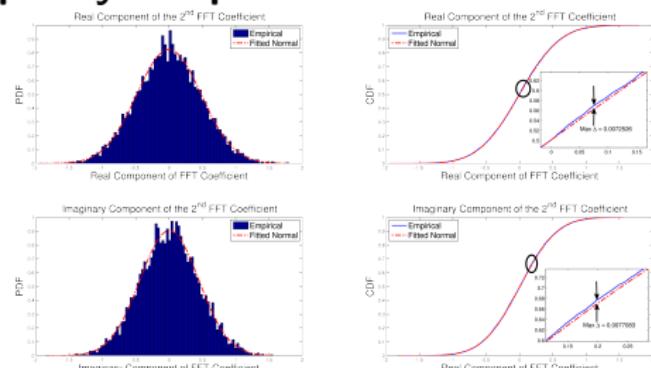
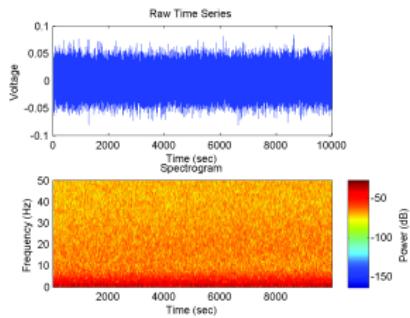
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- How to combine frequency component information?

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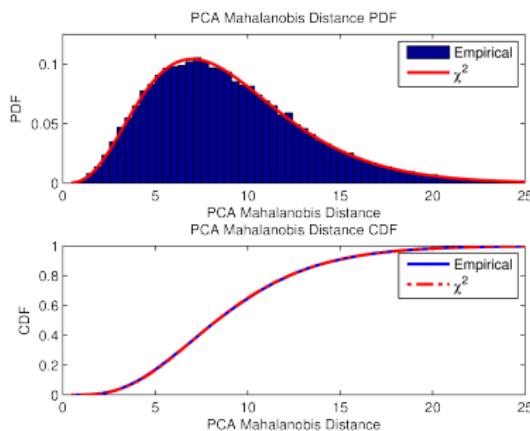
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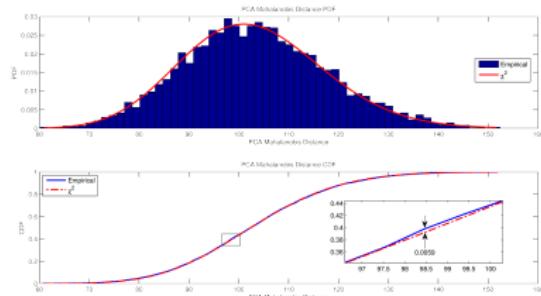
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- Known distribution given Gaussian frequency components
- $\chi^2$  distribution for Mahalanobis distance
- Closed-form threshold

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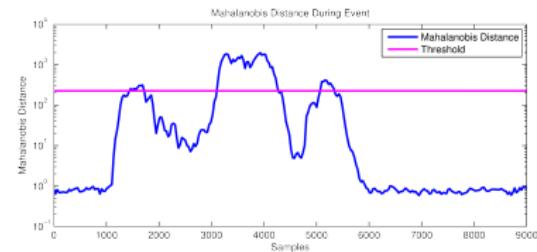
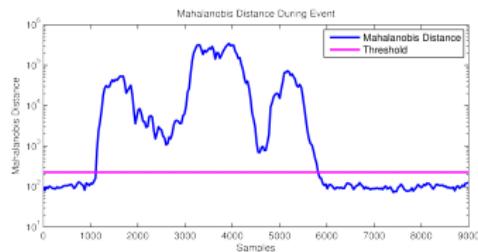
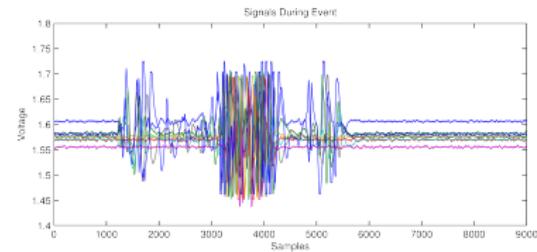
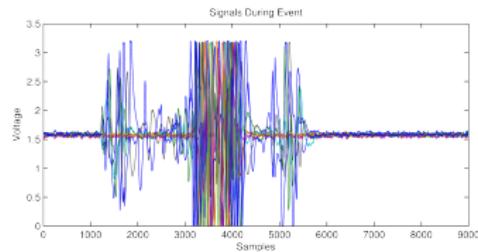
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# Combined Results

- 8 PIR sensors
- False Alarm Constraint:  $P_{FA} = 10^{-3}$  per year



Event Data

# Future Directions

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## Sensor Failure Detection

- Current algorithm declares an event when threshold is exceeded
  - Sensor failure could cause algorithm to exceed threshold
- Need to disambiguate between failures and events

# Conclusion

**Focused on development of detection algorithms with false alarm constraints**

- Found metric on background data that matches known closed-form distribution
  - Frequency components
  - **Subset Selection:** Principal Component Analysis
  - **Mahalanobis Distance:**  $\chi^2$  distributed
    - Combine all PIR sensors into a single metric
- Determine threshold to meet false alarm constraint
- Algorithm performs well on collected data

**Still a lot of work to be done**

# Conclusion

# Thank You!

Special Thanks:

Jacques Kvam  
Jerry Brewer

# Any Questions?