

# Application and Validation of Inter-Atomic Potentials for Modeling Helium-3 Bubble Growth in Aging Palladium Tritides

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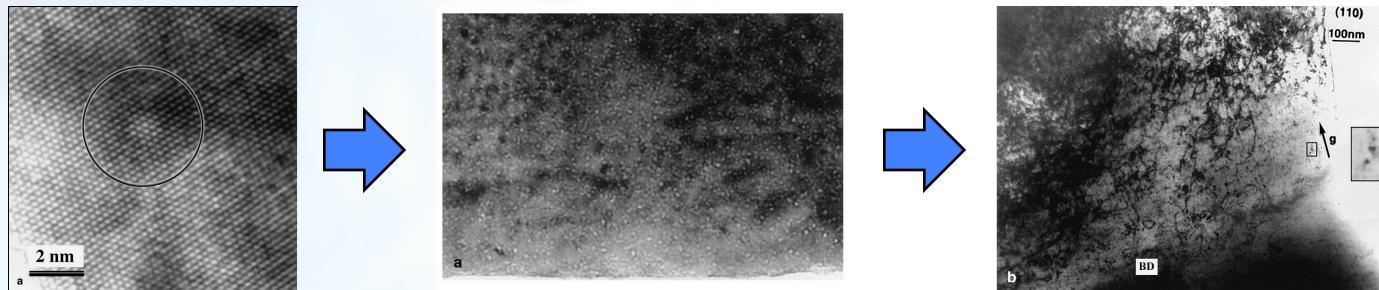
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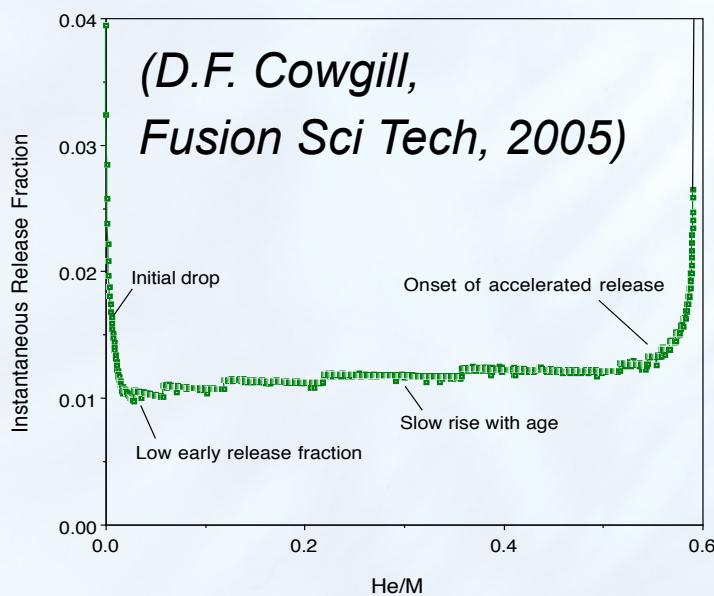
# How do hydrogen-isotope storage materials fail?

- Hydrogen (H) and hydrogen-isotopes (D,T) in metals produce a variety of defect-mediated behaviors that can result in deformation, failure and fracture, e.g. H embrittlement (HE), H enhanced localized plasticity (HELP).
- Decay of tritium produces helium (He) atoms that cluster and form bubbles.
- For He in palladium (Pd), He gas is released from the metal at an accelerated rate at some critical concentration of He/Pd.
- Experiments reveal dislocation loops and other defects in these aged samples.

# Determining the cause of accelerated release of helium gas



(S. Thiébaut et al, J Nucl Mater, 2000)



**Our focus:**

**Identify physical mechanisms leading to accelerated release of He gas.**

**We simulate and examine the material defects that originate from having He bubbles in a metal lattice using atomistic modeling methods.**

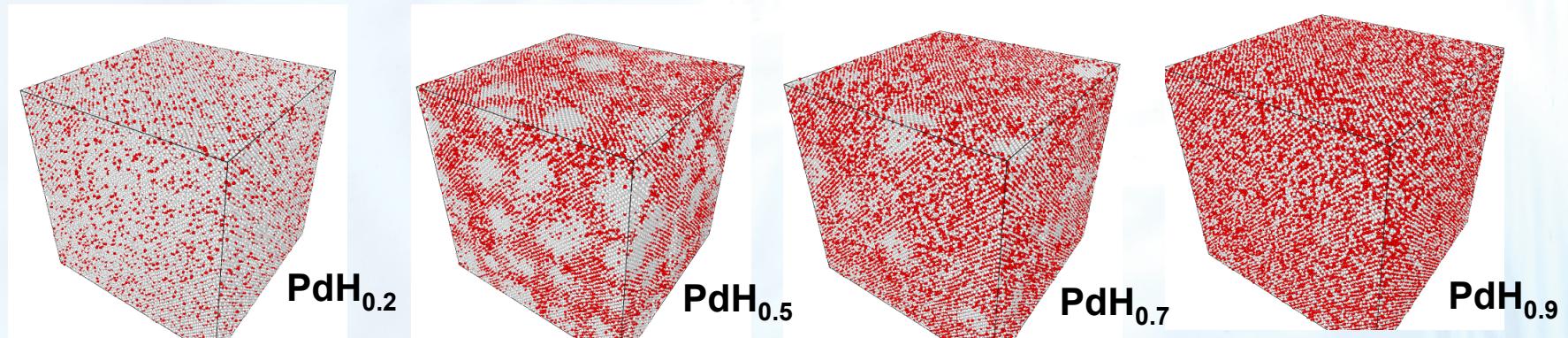
# Research plan

- Use molecular dynamic simulations to investigate progression of yield mechanisms during bubble growth in  $\text{PdT}_y$ 
  - Bubble volume and pressure
  - Dislocations and stacking faults
  - Signs of fracture
- Investigate the effect of alloying palladium with silver (Ag)
  - Perform bubble growth simulations for a variety of  $\text{Pd}_{1-x}\text{Ag}_x\text{T}_y$  compositions
- We found that MD simulations did not agree with experimental observations and expectations from analytic models
  - Perform density functional theory calculations to calculate material properties key to analytic models

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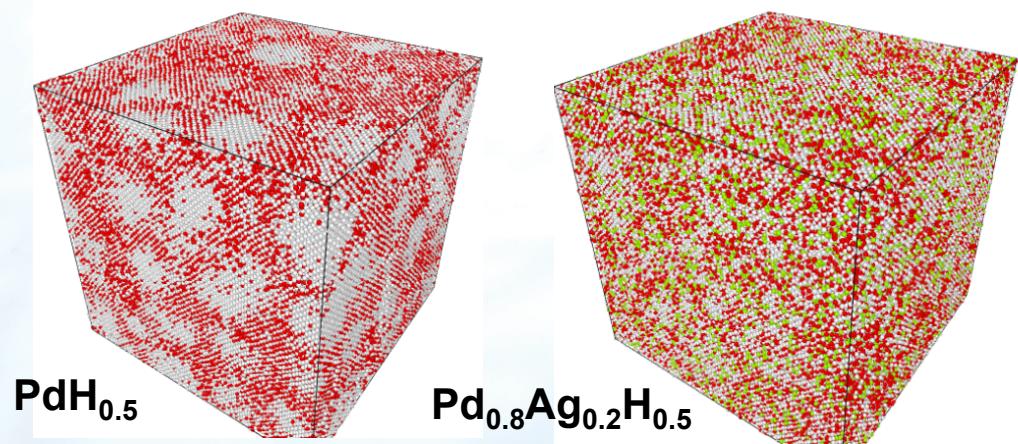
# Pd-H(T) interatomic potential

- Embedded Atom Method (EAM) model
  - Pd-Pd interaction by Foiles and Hoyt (*SAND2001-0661*)
  - Pd-H and H-H interactions by Zhou, Zimmerman, Wong, and Hoyt (*J Mater Res*, 23(3), 704-718, 2008)
- Accurately models structural properties of palladium hydride
  - Displays miscibility gap and the formation of H-dilute ( $\alpha$ ) and H-rich ( $\beta$ ) phases (expt:  $y_{\alpha} = 0.03$  and  $y_{\beta} = 0.6$ , pot:  $y_{\alpha} \approx 0.0$  and  $y_{\beta} \approx 0.85$ ); H in octahedral sites



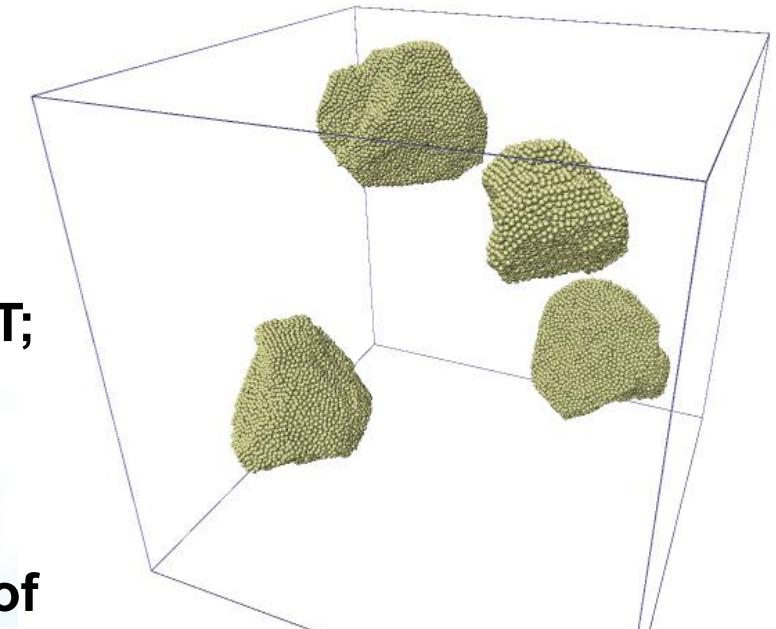
# Pd-Ag-H(T) interatomic potential

- Start with EAM potential by Williams *et al* (*MSMSE*, 2006) for Ag
- Pd-Ag and Ag-H interaction fitted to Morse-style functions using DFT energy and structural data for ideal Pd<sub>3</sub>Ag systems with H added to both octahedral and tetrahedral sites (Hale *et al*, *MSMSE*, 21, 045005, 2013)
- Loss of miscibility gap noticed between 10% and 20% Ag, experiments show this occurs at 25% Ag.
- Lennard-Jones style potential by Westergren *et al* (*J Chem Phys*, 1997) for He-He, He-Pd, and He-Ag interactions.
- Developed He-H pair potential based on all-electron *ab initio* calculation.



# Bubble growth simulations

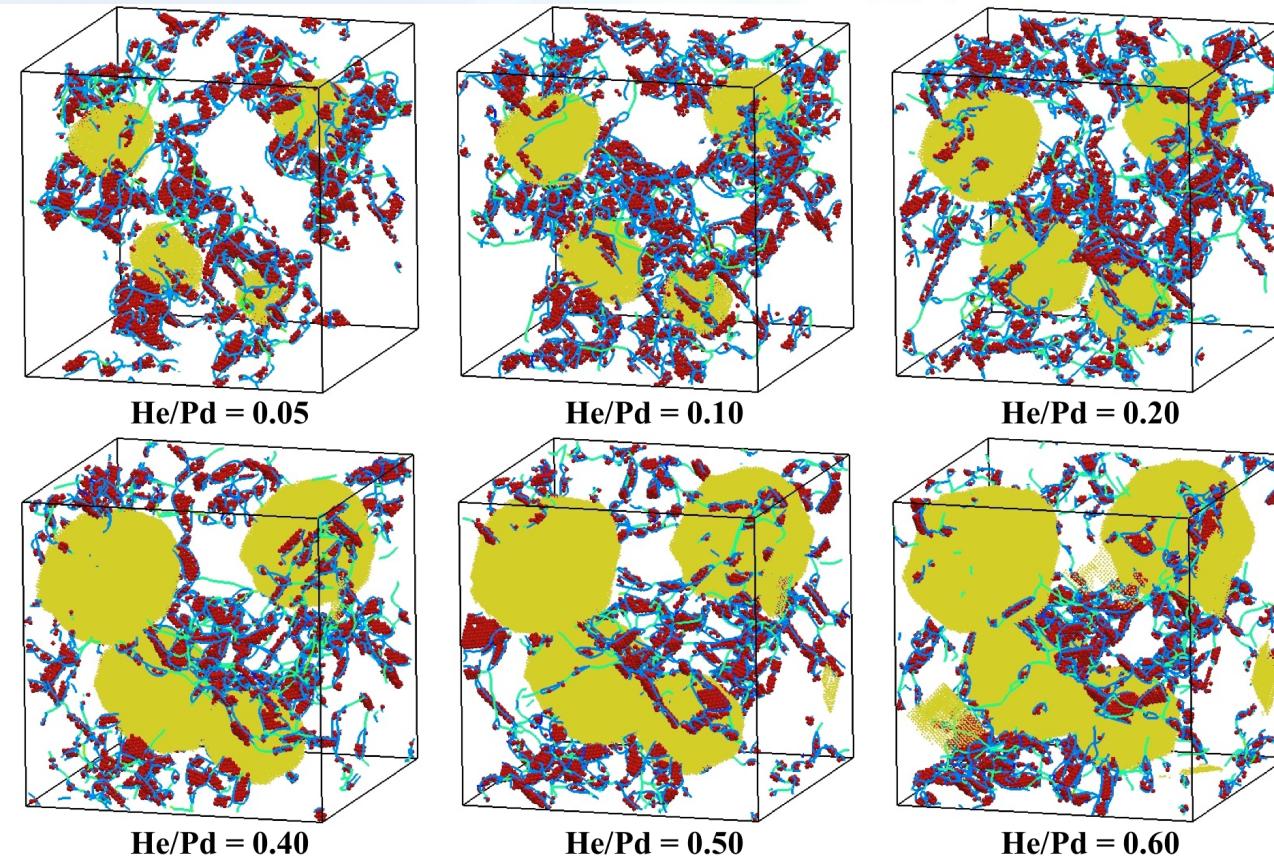
- Initial size ~740,000 atoms (cubes with sides of ~20 nm)
- Create 4 bubbles and add 20 atoms of He at a time into center of the bubbles – bubble density =  $5 \times 10^{23} \text{ m}^{-3}$
- Equilibrate the system for 11 ps before adding more He
- Isothermally held at 300 K
- Two types of (boundary) conditions:
  - Constrained volume
  - Constrained at zero pressure
- $H(T)$  concentration at  $\beta$  phase for PdT; at  $y = 0.5$  for  $\text{Pd}_{1-x}\text{Ag}_x\text{T}_y$
- Calculations done on 1024 processors at a rate of ~18 million time steps per day, roughly 80 days of running to reach experimental He concentration for rapid release



Non-spherical bubbles

# He bubble growth in PdT<sub>0.85</sub>

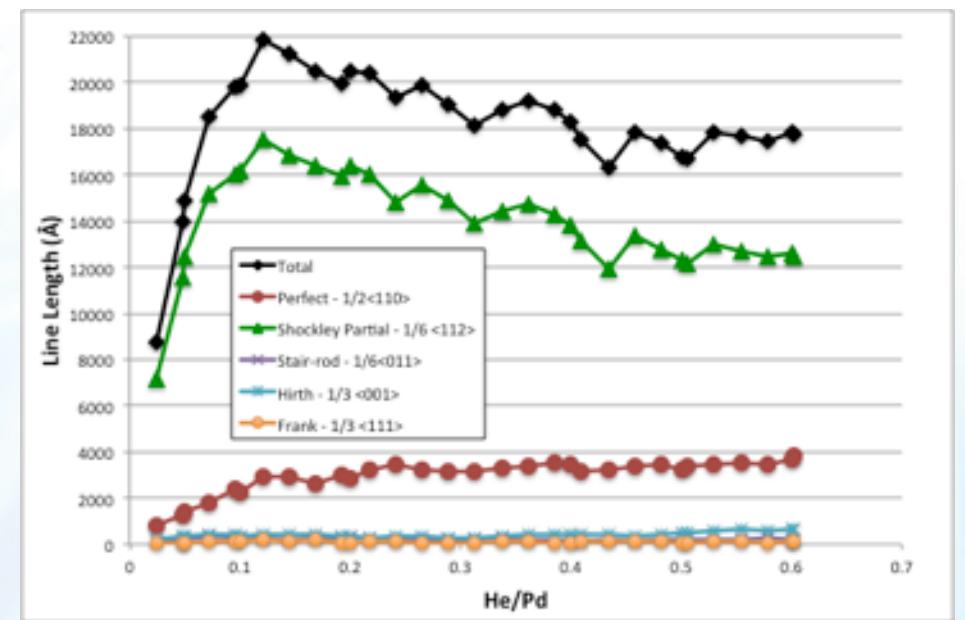
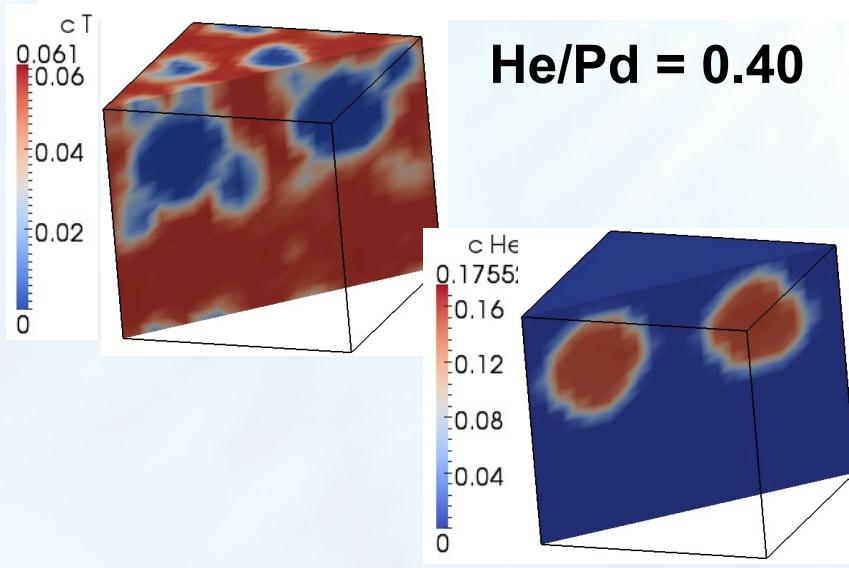
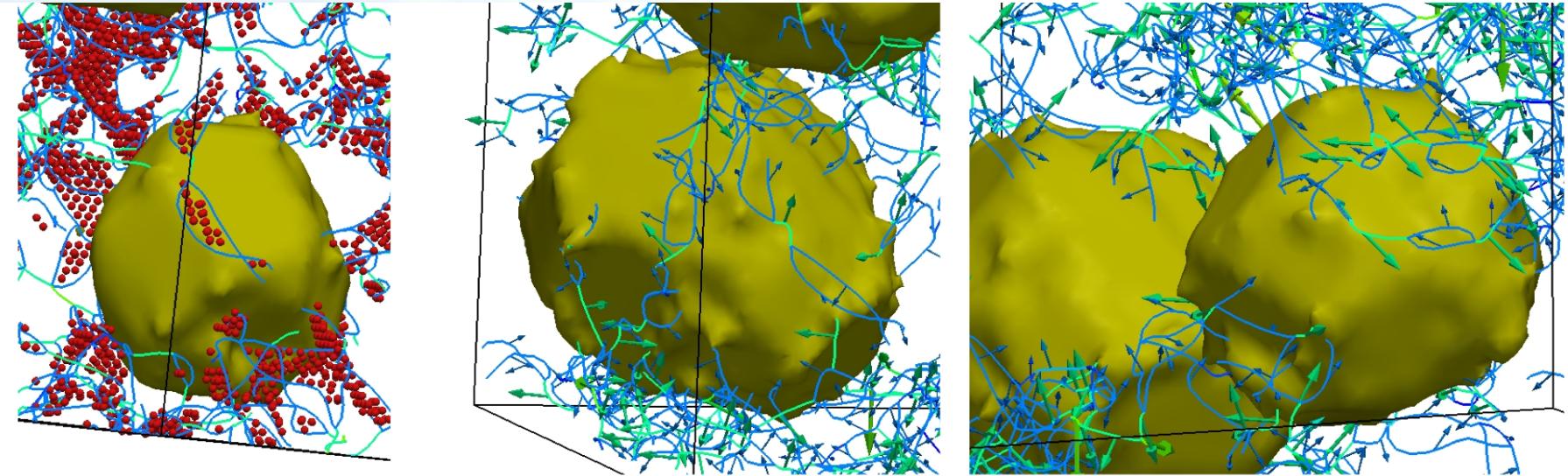
## Constrained volume simulations



- Dislocations ( $<112>$  and  $<110>$ ) and stacking faults created; content appears to saturate above  $\text{He/Pd} = 0.2$ .
- At low amounts of  $^3\text{He}$ , dislocation loops are isolated to single bubbles
- At moderate amounts of  $^3\text{He}$ , loops form a network between bubbles
- No inter-bubble fracture.

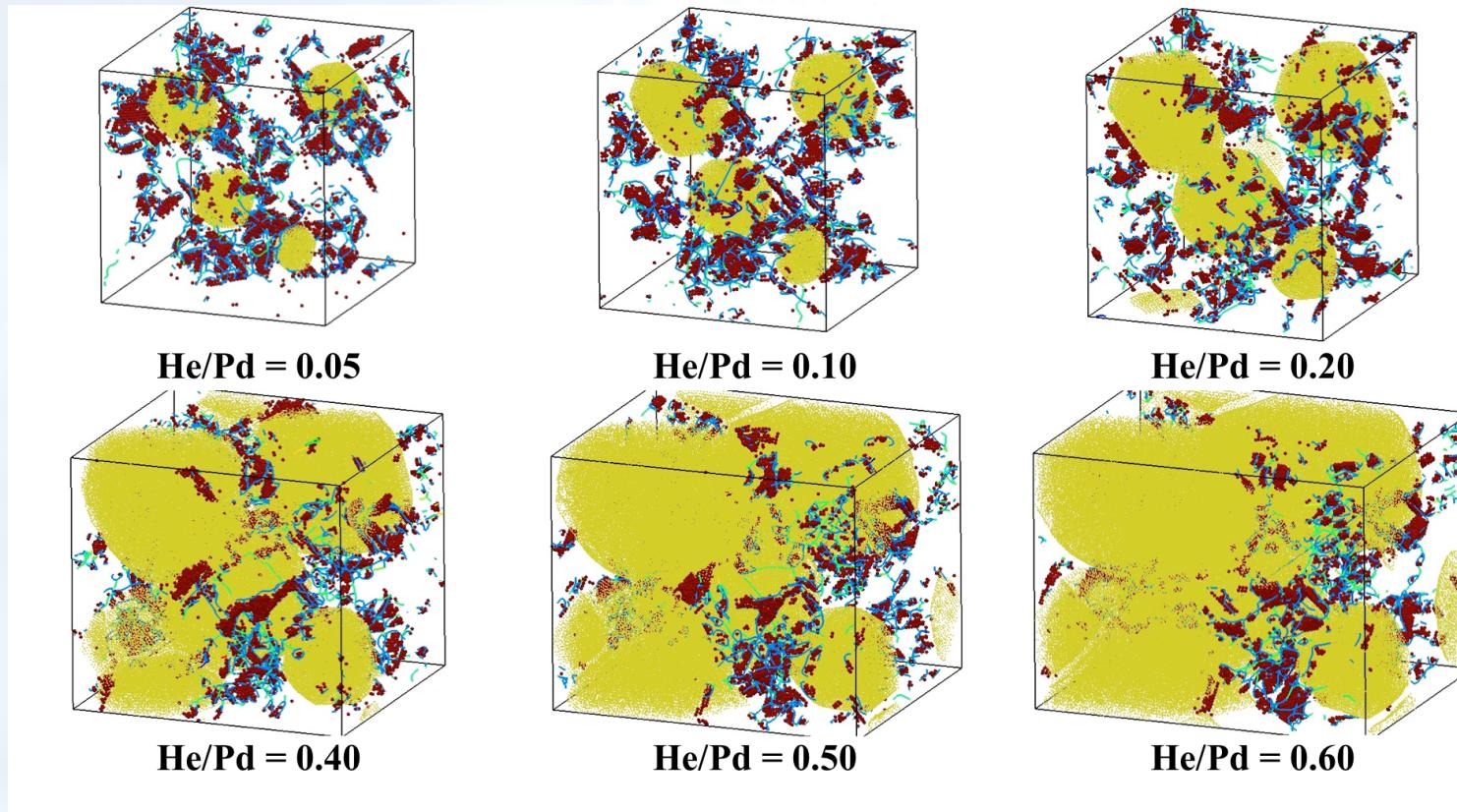
Dislocation eXtraction Algorithm (DXA, A. Stukowski and K. Albe, *MSMSE*, 2010) used for analysis

# Prismatic and shear loops are present



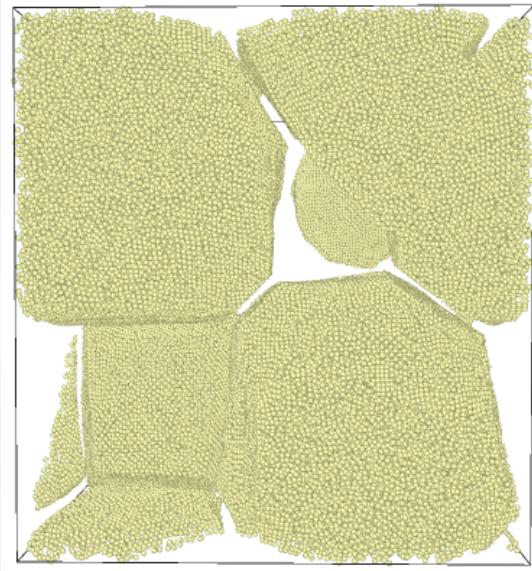
# He bubble growth in $\text{PdT}_{0.85}$

## Zero pressure simulations

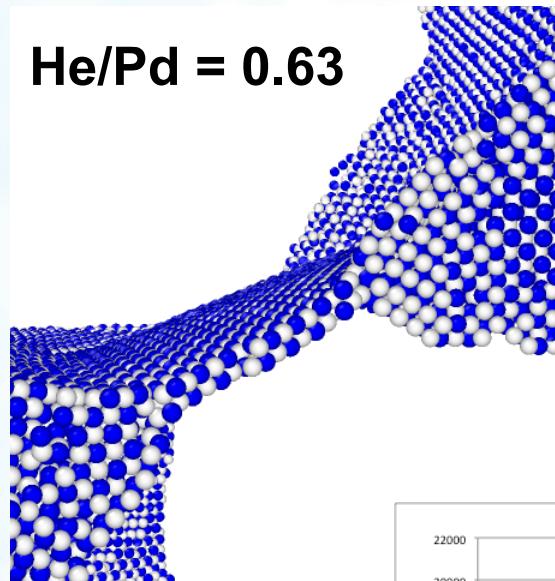


- Similar patterns of defects as for constrained volume case.
- Also evident is anisotropic swelling resulting in aspherical bubbles
- Again, no inter-bubble fracture or linkage occurs.

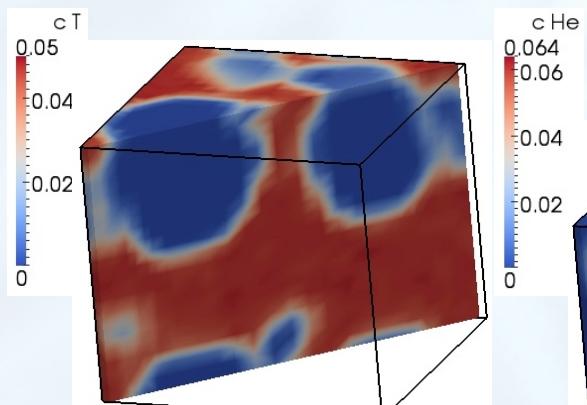
# Why no inter-bubble fracture?



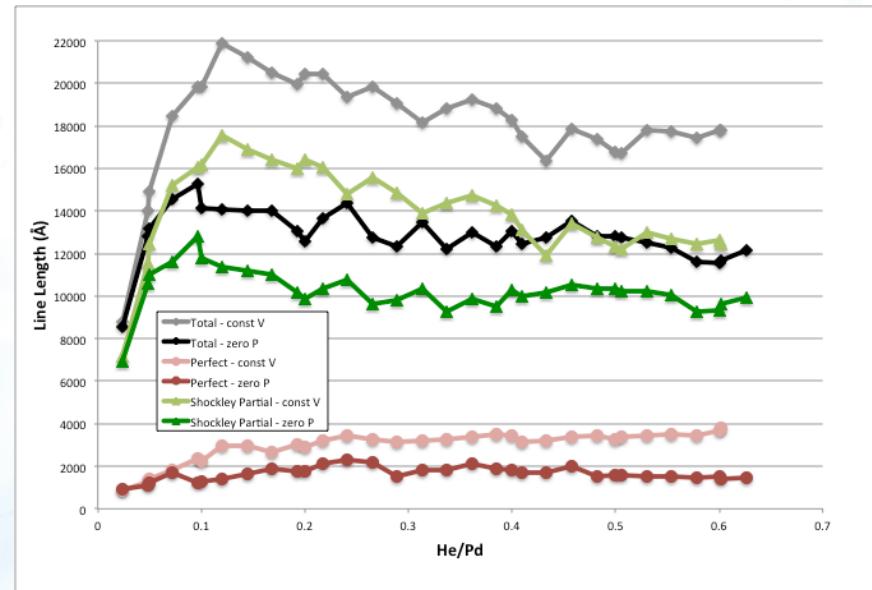
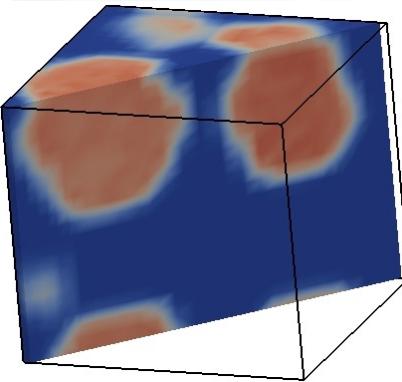
$\text{He/Pd} = 0.63$



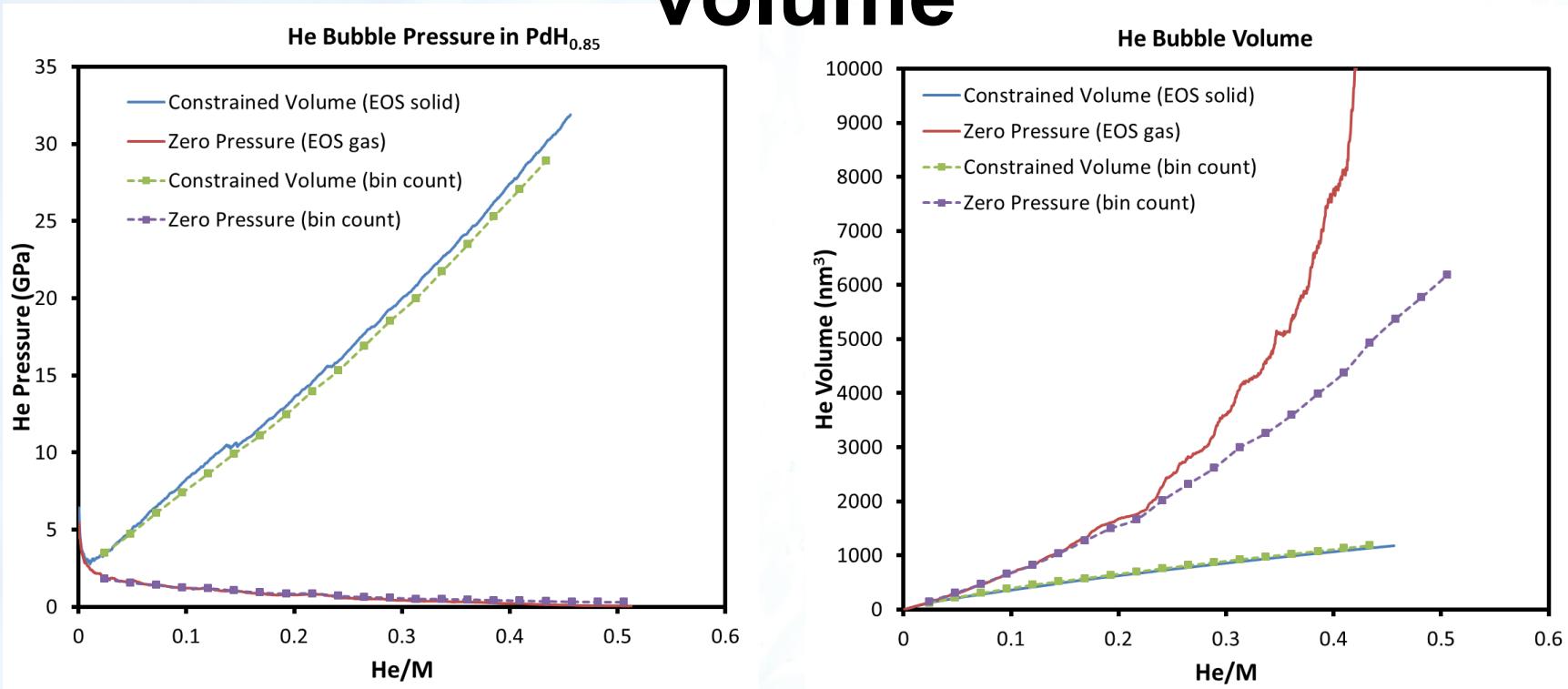
- As bubbles grow increasingly large, a thin (two atomic planes thick) metal-hydride membrane forms between bubbles.



$\text{He/Pd} = 0.40$



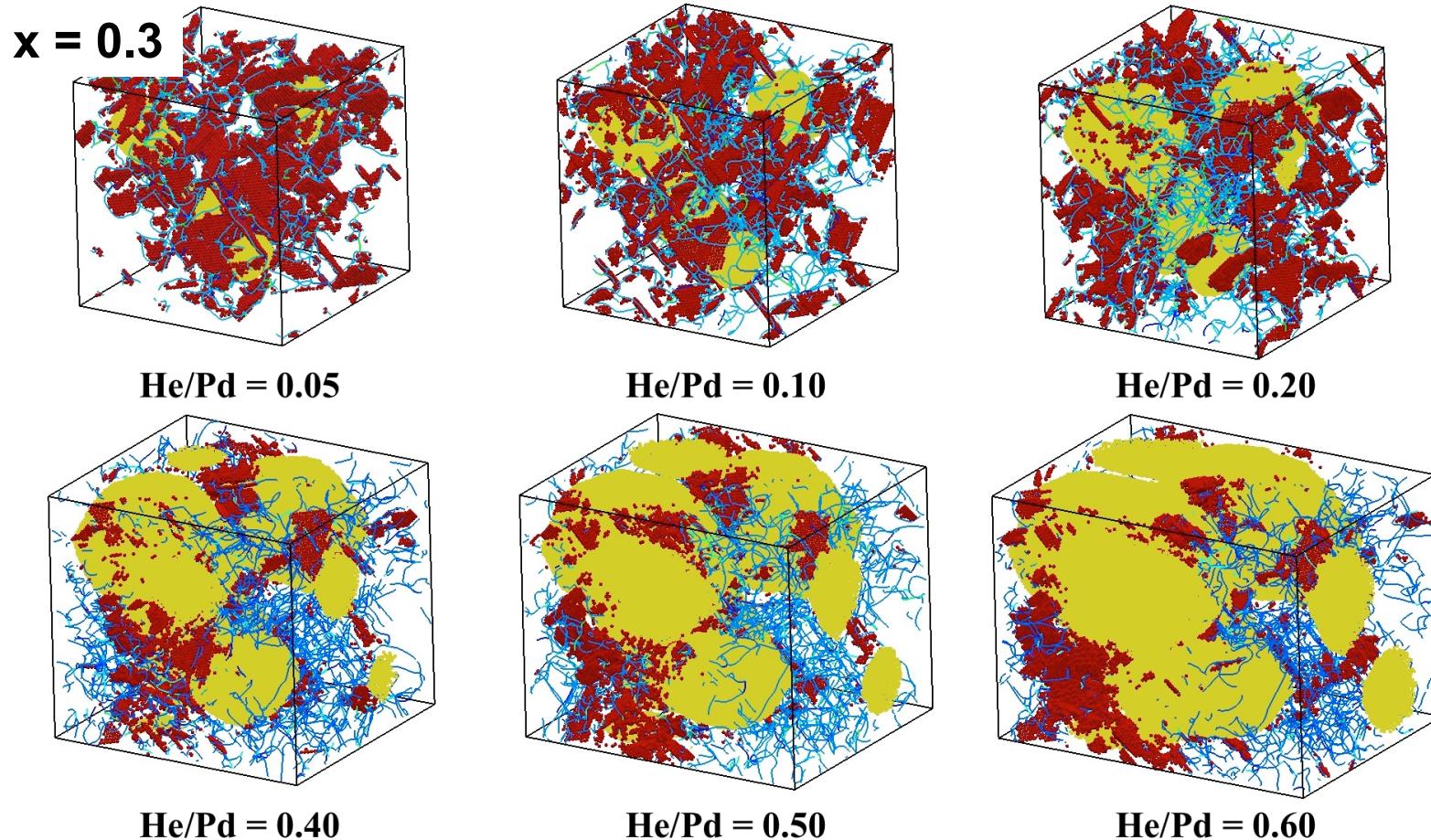
# Analysis of bubble pressure and volume



- Expected trends in bubble pressure/volume with increasing He/Pd
- MD-based equation of state (EOS) to predict volume inaccurate for large amounts of He; use bin count method instead
- Bubble pressures considerably less than those predicted by Cowgill (*Fusion Sci Tech*, 2005)

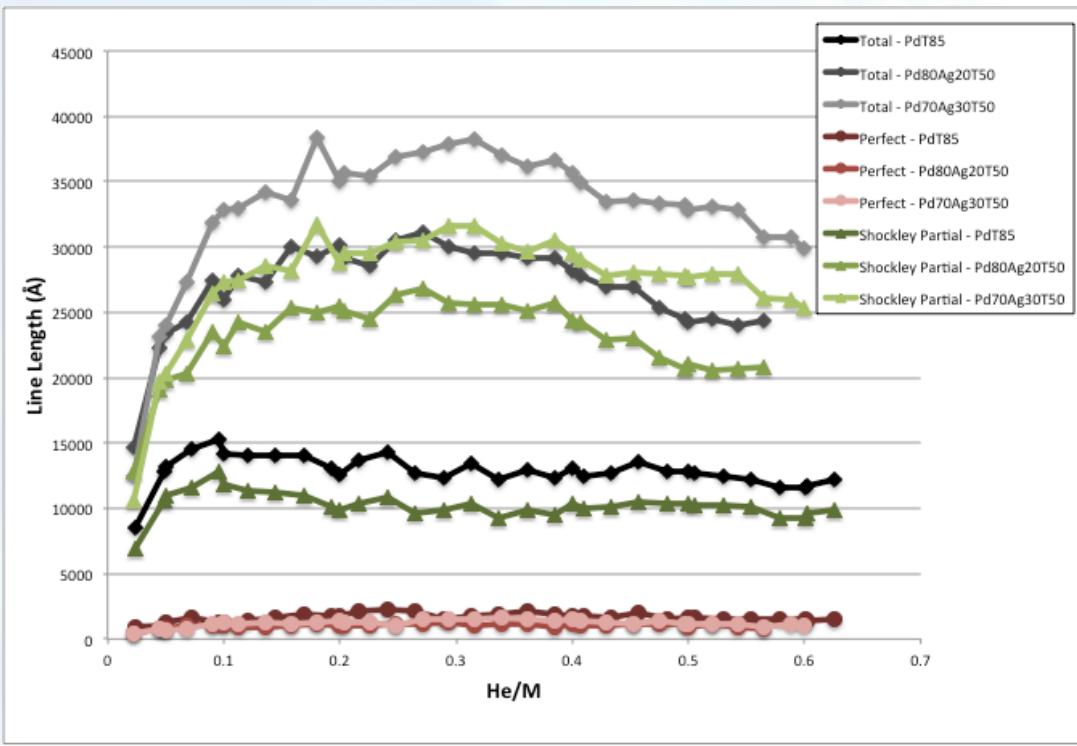
# He bubble growth in $Pd_{1-x}Ag_xT_{0.5}$

## Zero pressure simulations



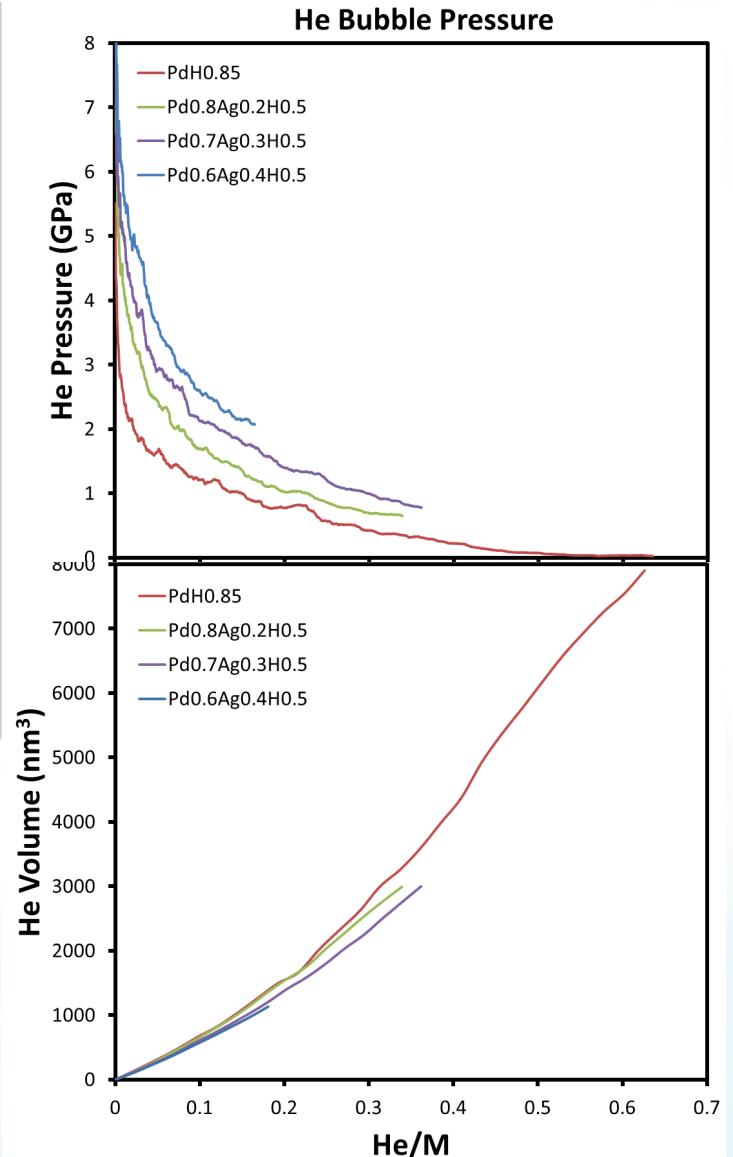
- Far more stacking faults with addition of Ag
- Similar types and behavior for dislocations

# Bubble growth characteristics

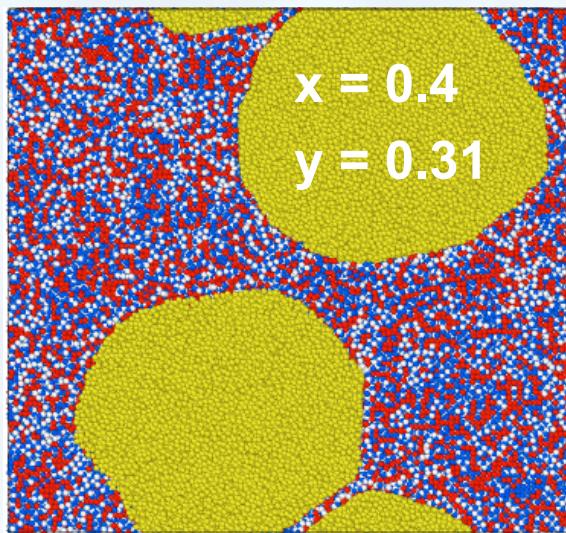
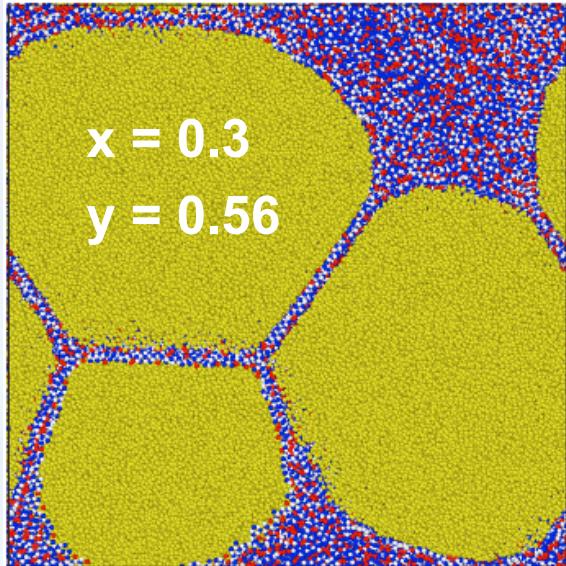


At a given He/M ratio:

- More partial/total dislocation content with increasing Ag content
- Higher bubble pressure and lower volume with increasing Ag content



# Inter-bubble linkage occurs with Ag



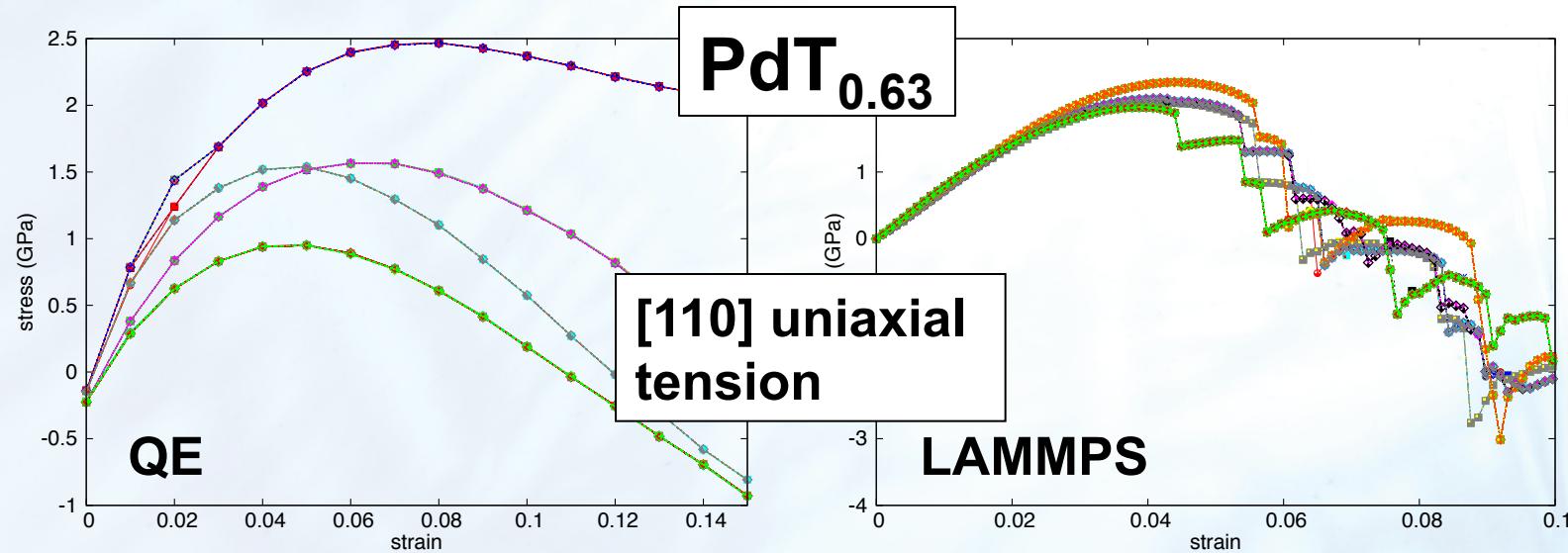
- As for the non-Ag cases, a thin membrane forms between impinging bubbles.
- Membrane collapses for 30% and 40% Ag, but not for 20%.

*Wolfer's theory predicts that inter-bubble fracture occurs at a He content that depends on the ratio of ideal tensile strength to shear strength for the MH.*

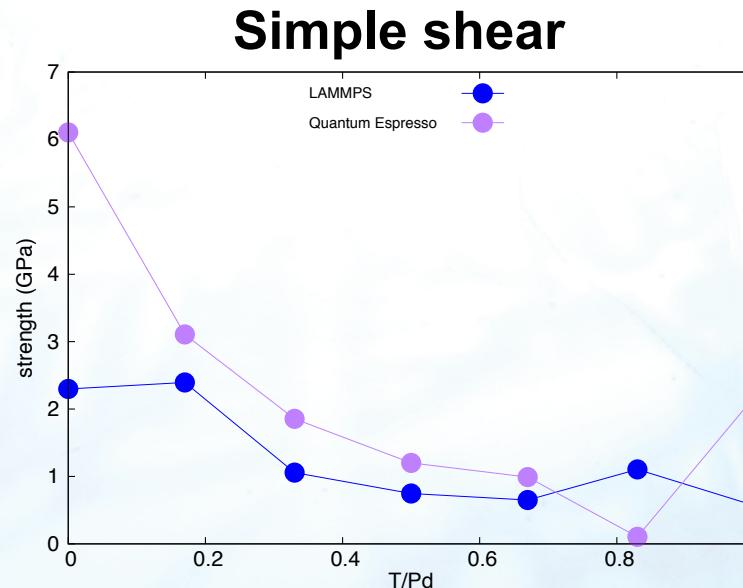
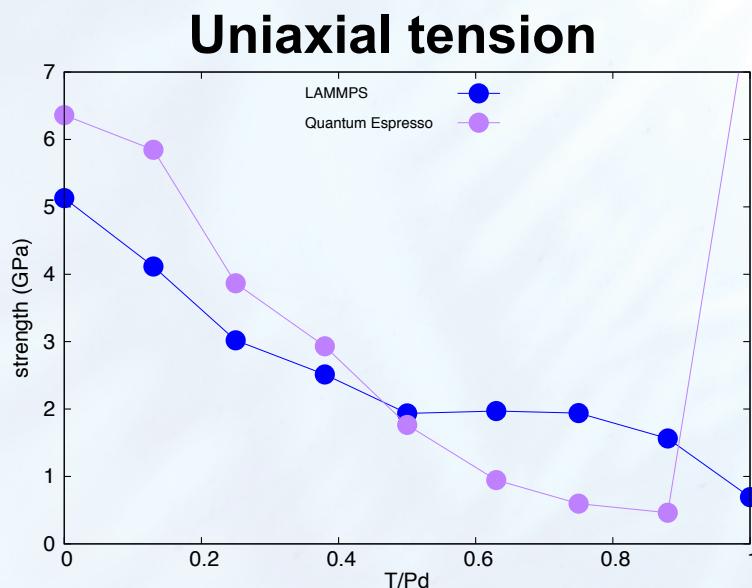
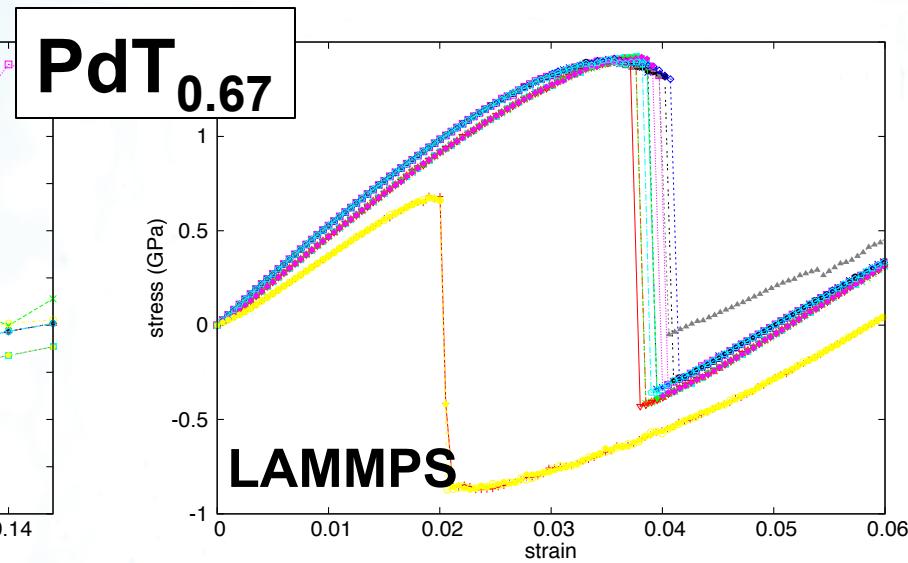
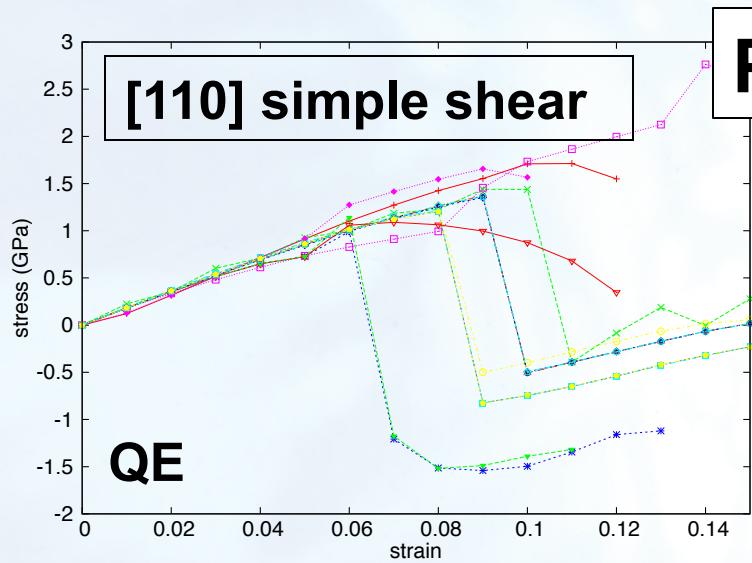
*We can use DFT to assess the fidelity of our Pd-T potential.*

# DFT analysis of tensile and shear strengths

- DFT calculations to assess tensile & shear for Pd-T alloy system
- Used PWscf module within Quantum Espresso
- GGA, PAW pseudopotentials, dispersion-corrected PBE functional
- 4 to 12 atoms
- $E_{\text{cut}} = 55 \text{ Ry} (\sim 750 \text{ eV})$ ,  $12 \times 12 \times 12$  k-point sampling
- Marzari-Vanderbilt fermi smearing (width = 0.06 Ry  $\sim 0.82 \text{ eV}$ )
- Performed similar calculations with LAMMPS for comparison



# Compositional variation of strengths



# Comparison between QE and LAMMPS

- For [110] uniaxial tension:
  - at  $T/Pd = 0.65$ ,  $\sigma_{QE} = 889 \text{ MPa}$ ,  $\sigma_{LAMMPS} = 1.966 \text{ GPa}$
  - at  $T/Pd = 0.85$ ,  $\sigma_{QE} = 493 \text{ MPa}$ ,  $\sigma_{LAMMPS} = 1.650 \text{ GPa}$
- For [110] simple shear:
  - at  $T/Pd = 0.65$ ,  $\tau_{QE} = 1.016 \text{ GPa}$ ,  $\tau_{LAMMPS} = 662 \text{ MPa}$
  - at  $T/Pd = 0.85$ ,  $\tau_{QE} = 348 \text{ MPa}$ ,  $\tau_{LAMMPS} = 1.041 \text{ GPa}$

Wolfer's theory:  $(He/M)_{cr} = 3/2 * (\sigma/\tau) - 1$

For  $T/Pd = 0.65$ ,

$(He/M)_{cr} = 0.3125$  for QE  $\rightarrow$  agrees with experiments  
by Thiébaut *et al* for continuously replenished systems  
 $(He/M)_{cr} = 3.45$  for LAMMPS  $\rightarrow$  unlimited loop punching

For  $T/Pd = 0.85$ ,

$(He/M)_{cr} = 1.38$  for LAMMPS  $\rightarrow$  disagrees with experiments

# Concluding remarks

- He bubble growth simulations show a complex evolution of defects, including perfect and partial dislocations, stacking faults, and even twins.
- This content is altered by the amount of Ag present, probably due to lower stacking fault energy of Ag to Pd.
- Inter-bubble linkage noticed only for high Ag content
- *Ab initio* calculations provide estimates of material strengths that, when used within Wolfer's theory, predict a transition from dislocation loop punching to inter-bubble rupture at a helium-to-metal ratio consistent with experimental observations.
- MD simulations performed with Sandia's LAMMPS code (<http://lammps.sandia.gov>).
- DFT calculations performed with Quantum Espresso (<http://www.quantum-espresso.org>)
- Questions? For further info: [jzimmer@sandia.gov](mailto:jzimmer@sandia.gov)