

# Spectroscopic Temperature Inferences from Downward Burning Solid Rocket Propellants



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# Outline

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- Introduction
- Experimental Summary
- Calculation of Diatomic AlO Spectra
- Thermal Continuum Analysis
  - Wavelength Dependent Emission Models
- Results
- Summary/Future Considerations



# Introduction

- The goal is to use optical emission spectroscopy to probe solid propellant plumes to determine the temperature field
  - Relatively Noninvasive and Relatively Easy
- Diatomic AlO emissions are used to infer the temperature of aluminum particles
  - AlO observed from the flame surrounding individual Al particles
- Thermal continuum emissions are used to characterize the flame temperature



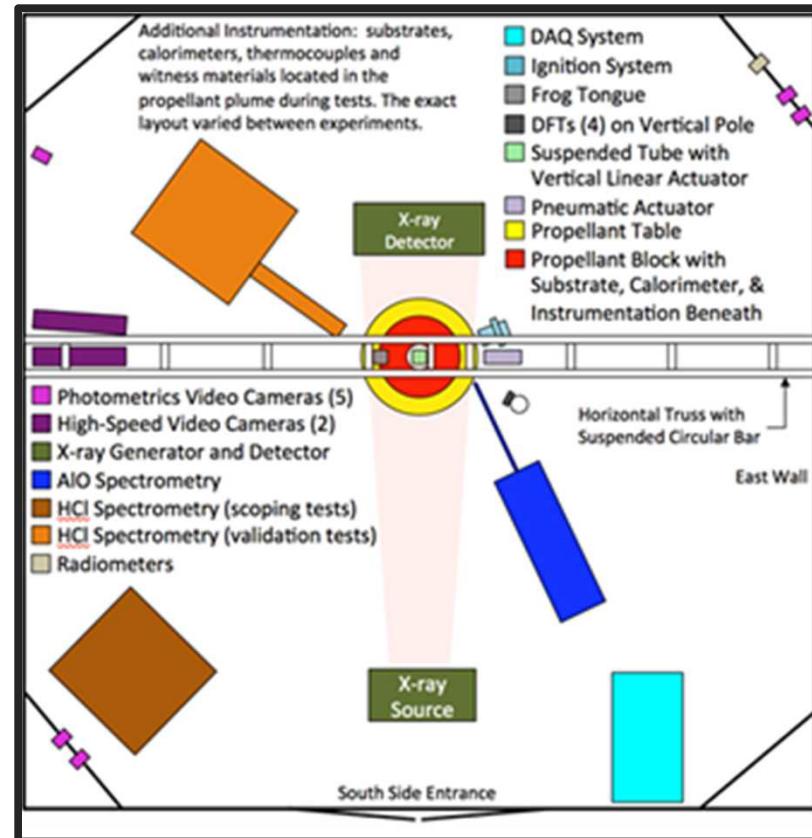
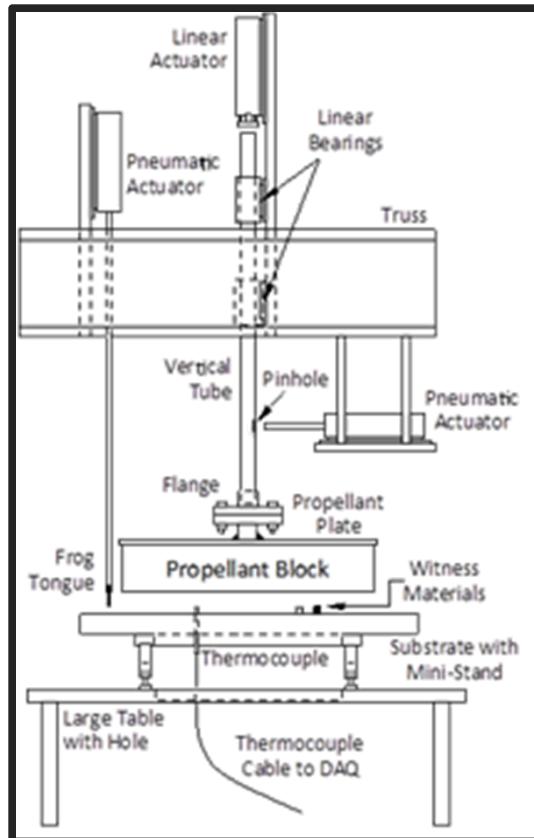
# Experimental Summary

- Probe was inserted into propellant plume to measure emission spectra at various positions
- Fiber coupled spectrometer collected narrowband (460-530 nm) and broadband (500-950 nm) spectral data
- Investigated several gap heights and substrate materials



# Test Set Up

- Varied position of probe within each test (~1-2 in.)
- Varied position of probe from test to test (~2-12in)



# Data Reduction

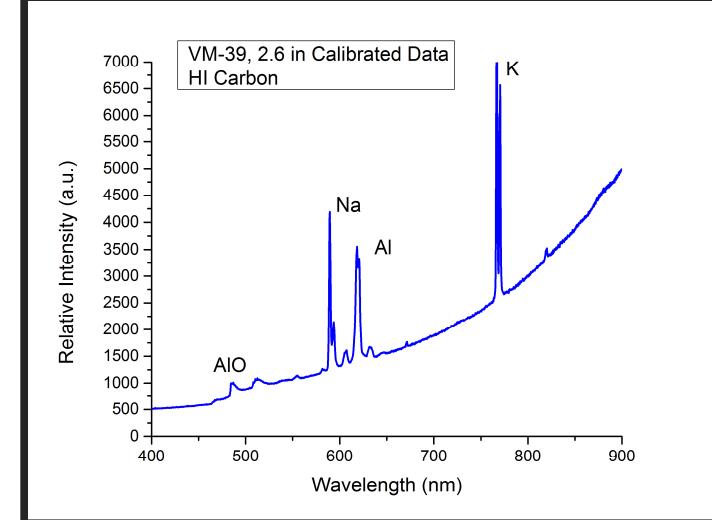
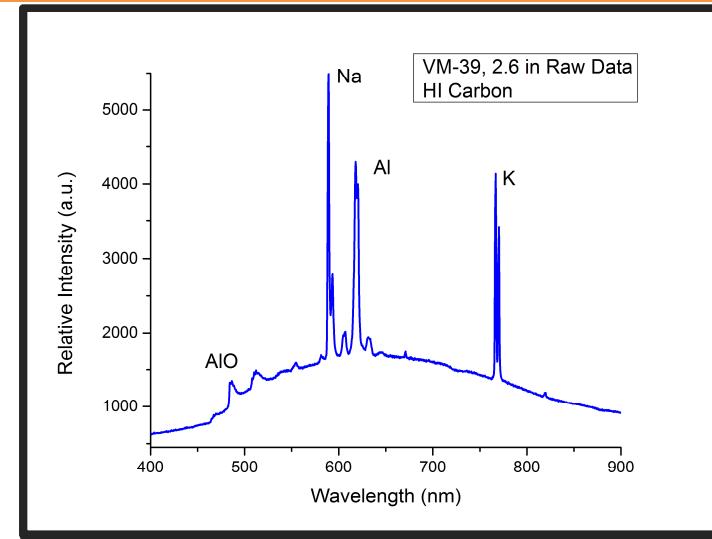
Data are analyzed in five steps

1. Spectral data are visualized
2. Calibrated for detector sensitivity and background
3. Analyze AlO spectra for the  $B\ ^2\Sigma^+ \rightarrow X\ ^2\Sigma^+$  transition
4. Analyze background thermal emissions for wavelength dependent emissivity
5. Comparisons are made between fitting models



# Spectral Calibration

- Prior to analysis all spectra are properly calibrated for detector response and sensitivity
- Xe, Hg, Ar, Ne pen-ray lamps for detector response
- Halogen light source for detector sensitivity



# Calculation of Diatomic Spectra

## Recipe for calculating diatomic spectra

1. Calculate positions of all possible transitions
2. Invoke electronic selection rules;
3. Calculate Hönl-London factors  $S(J'J)$ ;
4. Calculate upper and lower energy level potentials;
5. Determine Franck-Condon factors  $q(v'v)$ ;
6. Evaluate r-centroids, combine with FCF to form  $S_{elec}$
7. Product of HLF and of electronic transition strength,  $S_{elec}$ , yield total line strength.



# Calculation of Diatomic Spectra

AlO emission spectra are calculated using diatomic line strengths,  $S_{ul}$ , for transitions from upper state,  $u$ , to lower state,  $l$ , [14]

$$S_{ul} = \sum_u \sum_l \left| \langle u | \hat{T}_k^{(q)} | l \rangle \right|^2, \quad \hat{T}_k^{(q)} \dots \text{Electric Dipole Operator}$$

Analytically calculate line strength in factorized form:

$$S_{ul}(n'v'J'M', nvJM) = S_{elec}(n'v', nv)S(J', J)$$

Model the intensity, ( $I_{ul}$ ) incident on a detector pixel as

$$I_{ul} = \frac{16\pi^3 c (a_0 e)^2 v^4}{3\varepsilon_0 Q} N_0 C_{abs} C_v \tilde{v}_{ul}^4 S_{ul} \exp\left(\frac{-hF_u}{k_B T}\right)$$

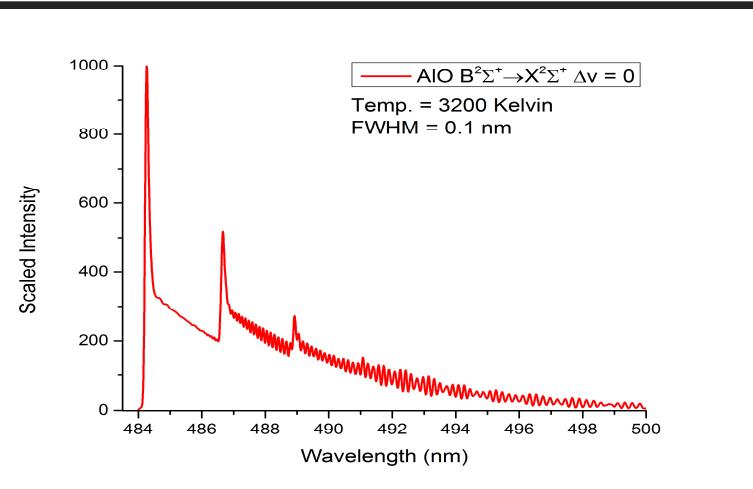
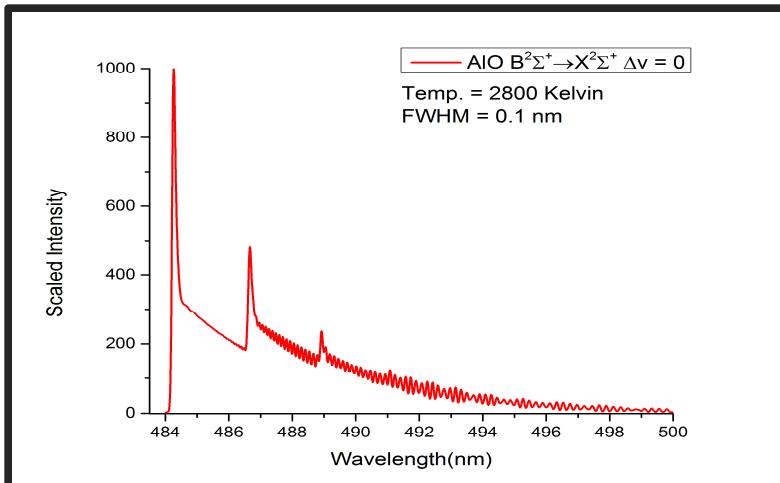
Leads to a simple yet rigorous selection rule

- **Allowed Transitions have Non-Vanishing Line Strengths**

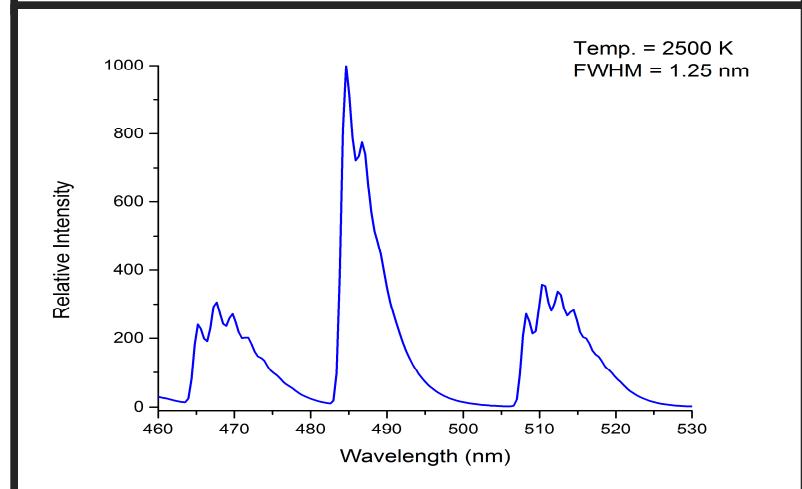
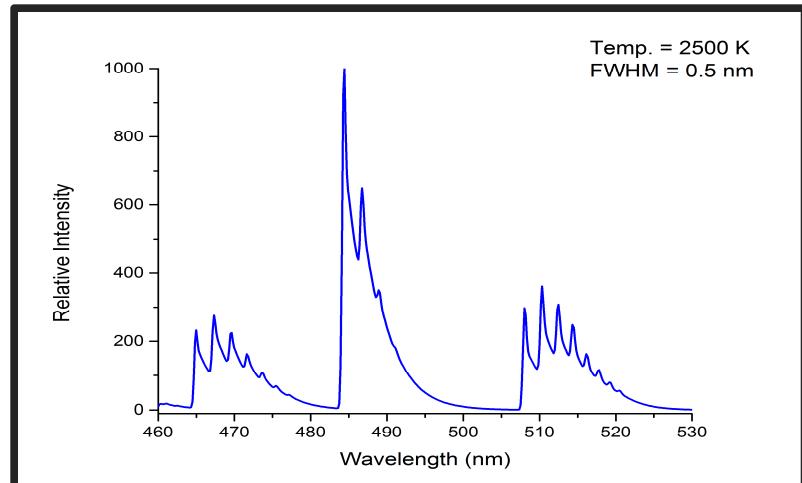


# Calculation of Diatomic Spectra

High resolution AlO B-X  $\Delta v = 0$



Lower Resolution AlO B-X



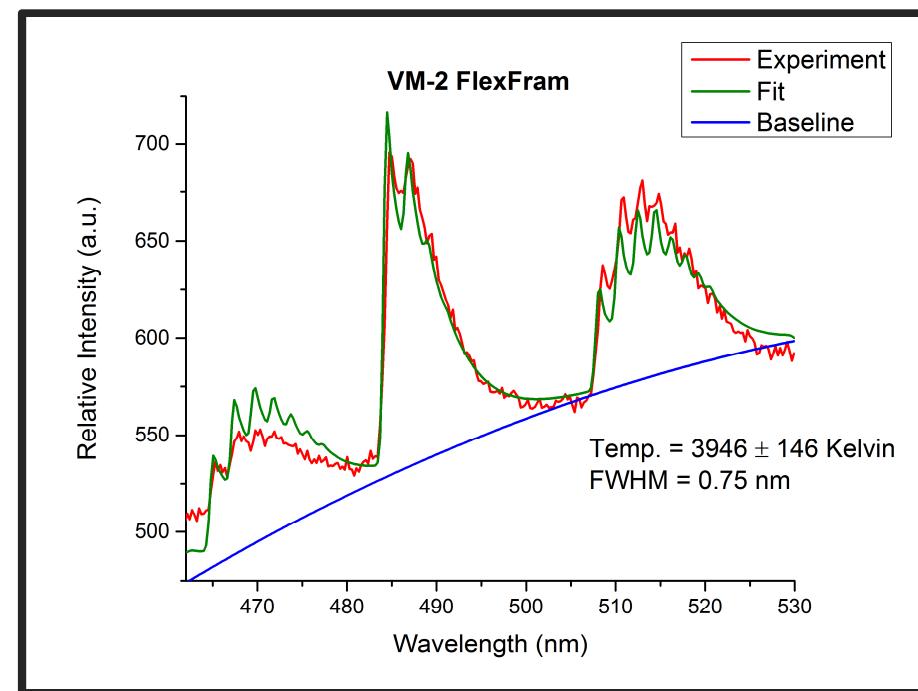
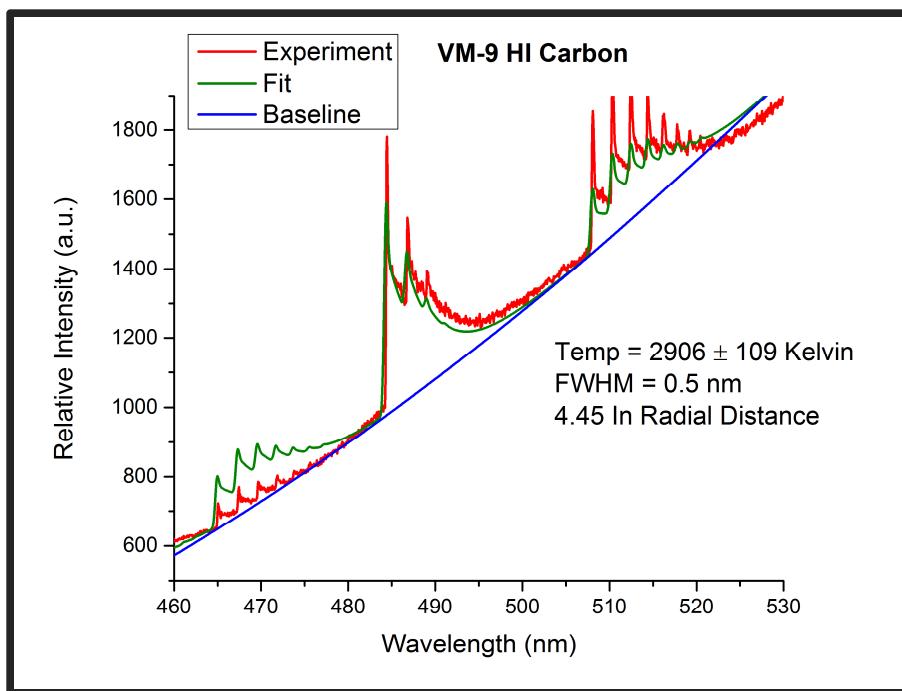
# Fitting Algorithm

- Use the Nelder-Mead algorithm to fit diatomic spectra to theoretical calculations of spectra
- Utilizes a downhill, simplex fitting method to minimize input parameters
- Nelder-Mead algorithm chosen for its ability to fit multiple parameters simultaneously
  - Temperature, Baseline Offset, Spectral Resolution (FWHM)



# AlO Emissions

- Error bars for AlO emissions are inferred by varying the resolution parameter



# Wavelength Dependent Emissions

- Small particles, with a size distribution on the order of the wavelength of emission, indicate wavelength dependent emissivity [6].
- Use poly-logarithms,  $Li_s(z)$ , and Lambert functions,  $W(z)$ , to compute Wien's Displacement law [7]:

$$\lambda_{\max} \times T = \frac{hc}{k_B} \times \frac{1}{5 + W_0(-5e^{-5})} = 2.898 \times 10^6 \text{ nmK}$$



# Wavelength Dependent Emissions

## Derivation of Wavelength Dependent Emission Model [7]

$$Li_s(z) = \sum_{k=1}^{\infty} \frac{z^k}{k^s}, |z| < 1$$

$$\frac{d}{dz}(Li_s(z)) = \frac{Li_{s-1}(z)}{z}$$

Consider

$$Li_1 = \sum_{k=1}^{\infty} \frac{x^k}{k} = -\ln(1-x)$$

Now apply to Planck's law

$$I(\lambda, T) = \frac{2\pi hc^2}{\lambda^5} \frac{1}{\exp(\beta) - 1}, \beta = \frac{hc}{\lambda k_B T}$$

$$= \frac{2\pi hc^2}{\lambda^5} Li_0(\exp(\beta))$$

Maximize wrt  $\lambda$  to derive Wien's Law

$$5Li_0(e^{-\beta}) - \beta Li_{-1}(e^{-\beta}) = 0$$

$$(\beta - 5)e^{\beta - 5} = -5e^{-5}$$

Solve using the Lambert Function

$$W(z)e^{W(z)} = z$$

$$\beta = 5 + W_0(-5e^{-5})$$

$$\lambda_{\max} \times T = \frac{hc}{k_B} \times \frac{1}{5 + W_0(-5e^{-5})}$$



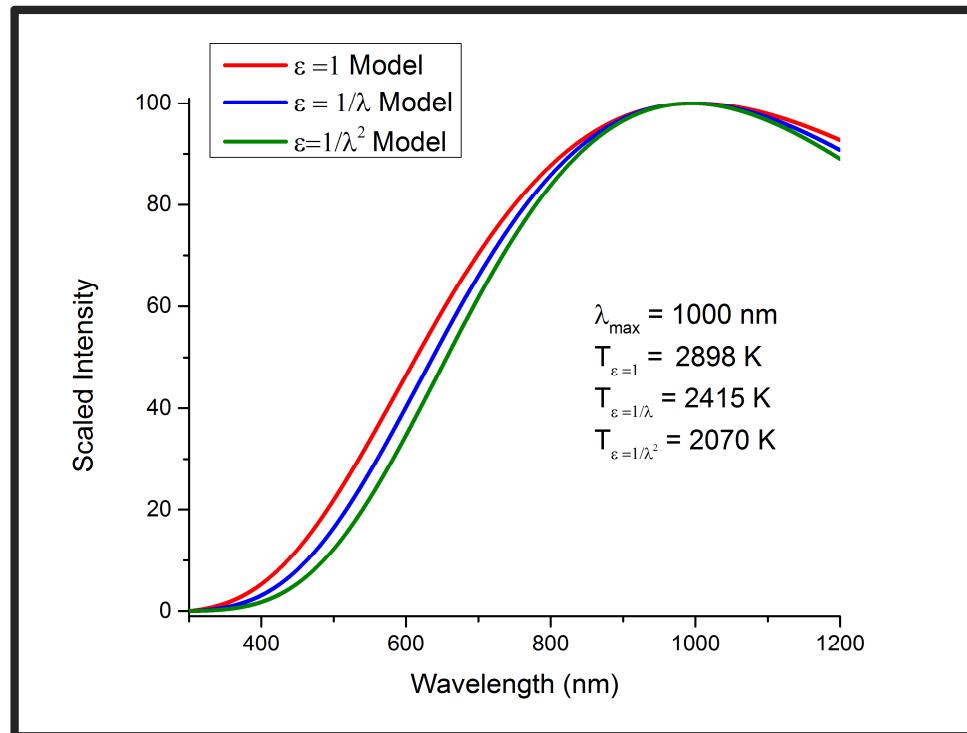
# Wavelength Dependent Emissions

- Applying the same method, we find:

$$\lambda_{\max} \times \bar{T} = 2.415 \times 10^6 \text{ nmK}$$

and

$$\lambda_{\max} \times \bar{T} = 2.070 \times 10^6 \text{ nmK}$$



# Planck Fitting

Wavelength dependency may be used with Planck's Law:

$$I(\lambda, T) = \frac{\varepsilon(\lambda, T)}{\lambda^5} \frac{2\pi hc^2}{\exp\left(\frac{hc}{\lambda k_B T}\right) - 1}$$

Linearize, semi-log plot for fitting

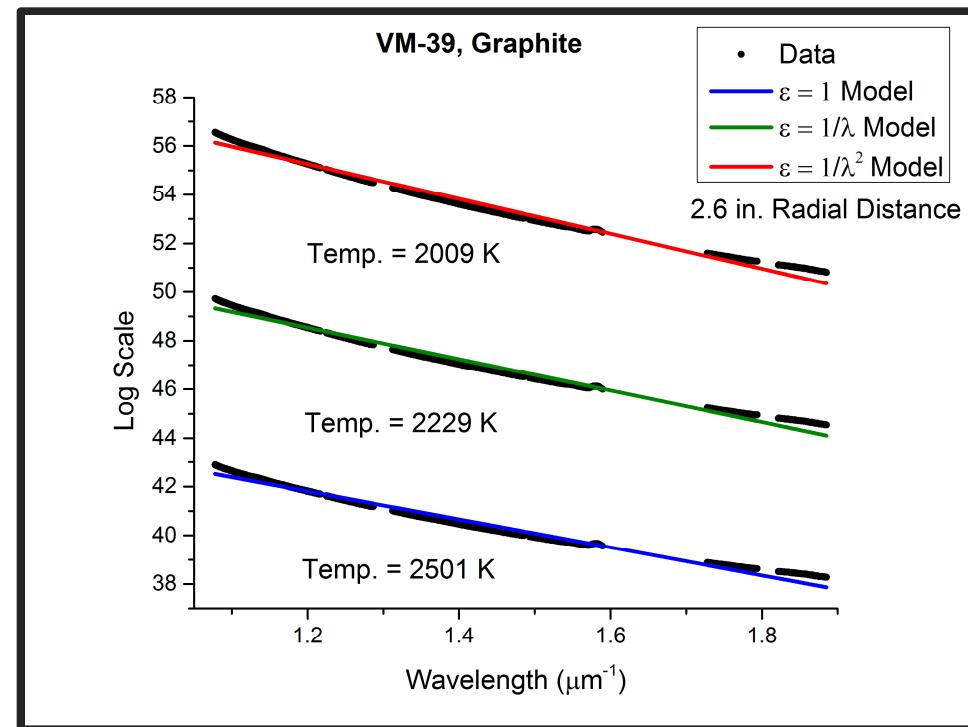
$$\ln\left(\frac{I(\lambda, T) \times \lambda^5}{\varepsilon(\lambda, T)}\right) = -\ln\left(\exp\left(\frac{hc}{\lambda k_B T}\right) - 1\right)$$

$$\ln\left(\frac{I(\lambda, T) \times \lambda^5}{\varepsilon(\lambda, T)}\right) \cong -\frac{hc}{k_B T} \frac{1}{\lambda}$$



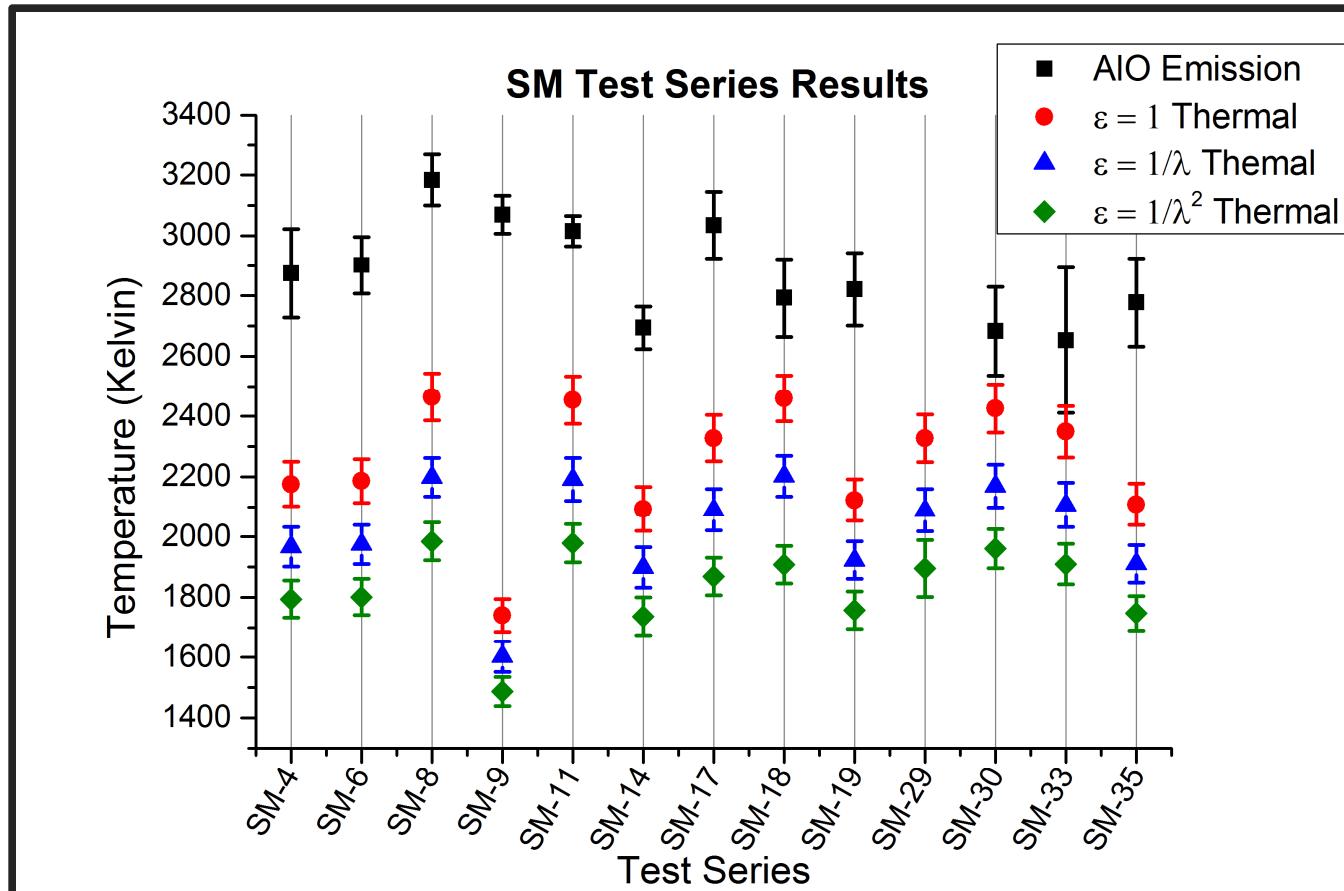
# Planck Fitting

- Only consider  $\epsilon = 1$ ,  $1/\lambda$ ,  $1/\lambda^2$  emissivity dependence (for now)
- Remove atomic and molecular emissions for straight line fitting
  - Al, AlO, Fe, Na, and K



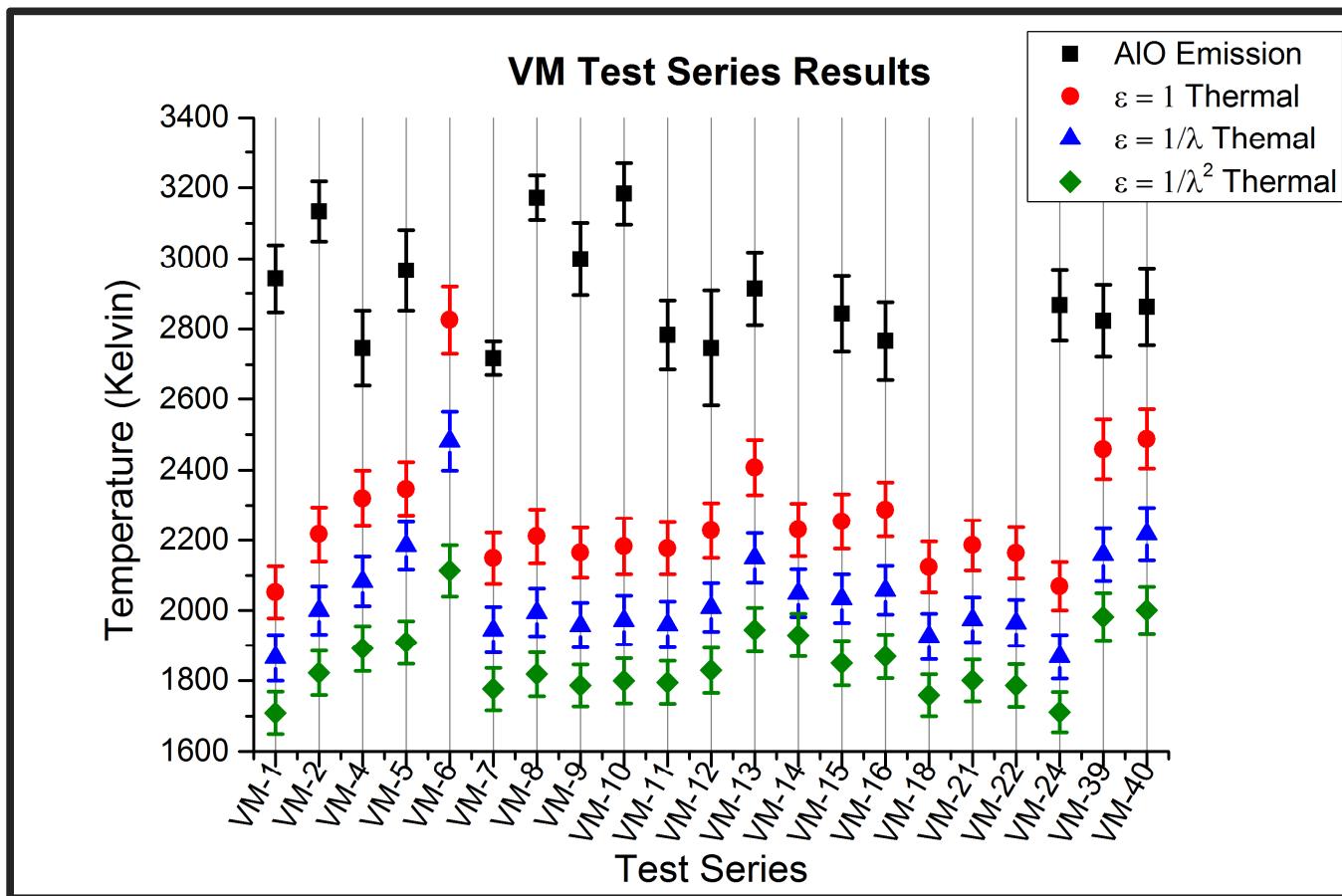
# Results

Graphite, Wet Concrete, FlexFram, HI Carbon, Sandbed, Dry Concrete, Substrates



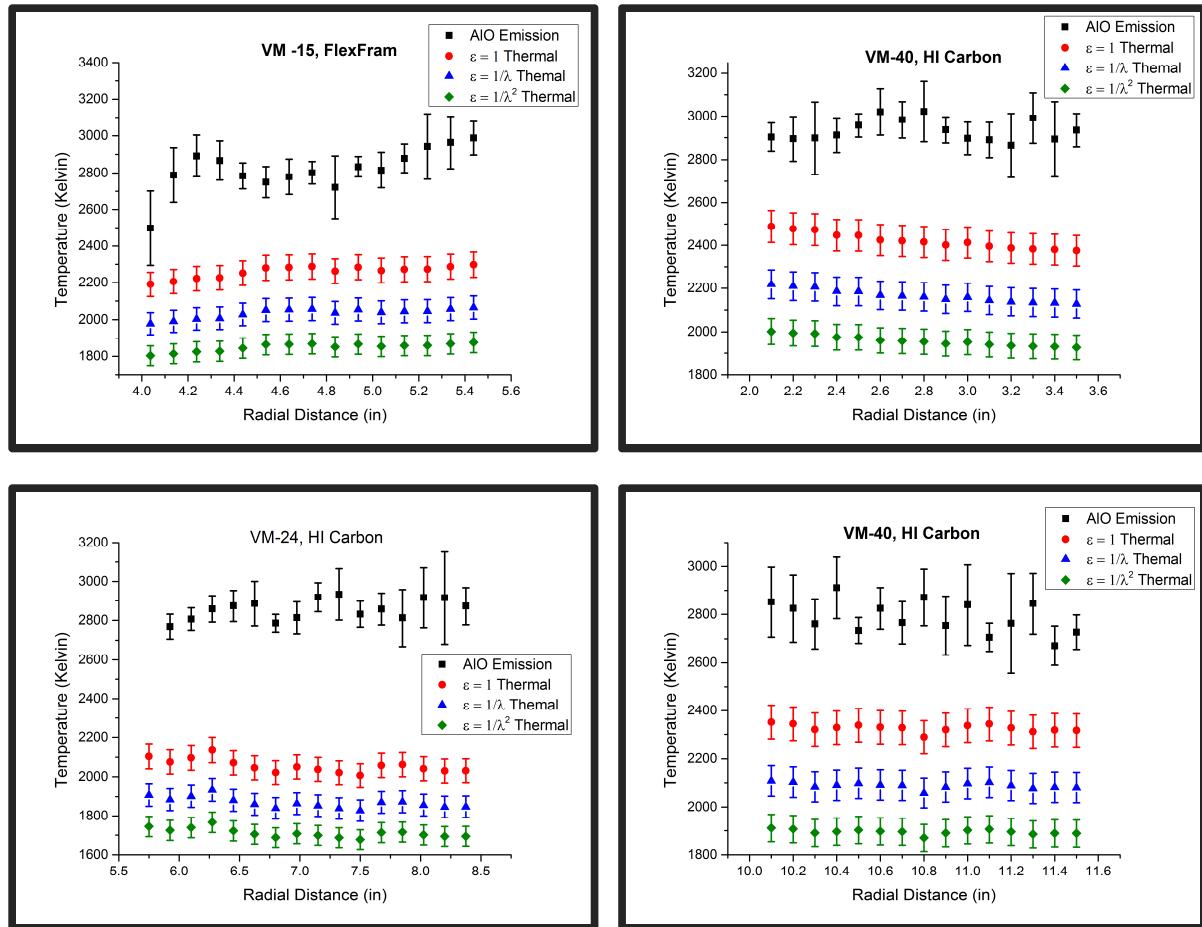
# Results

## Graphite, Wet Concrete, FlexFram, and HI Carbon Substrates



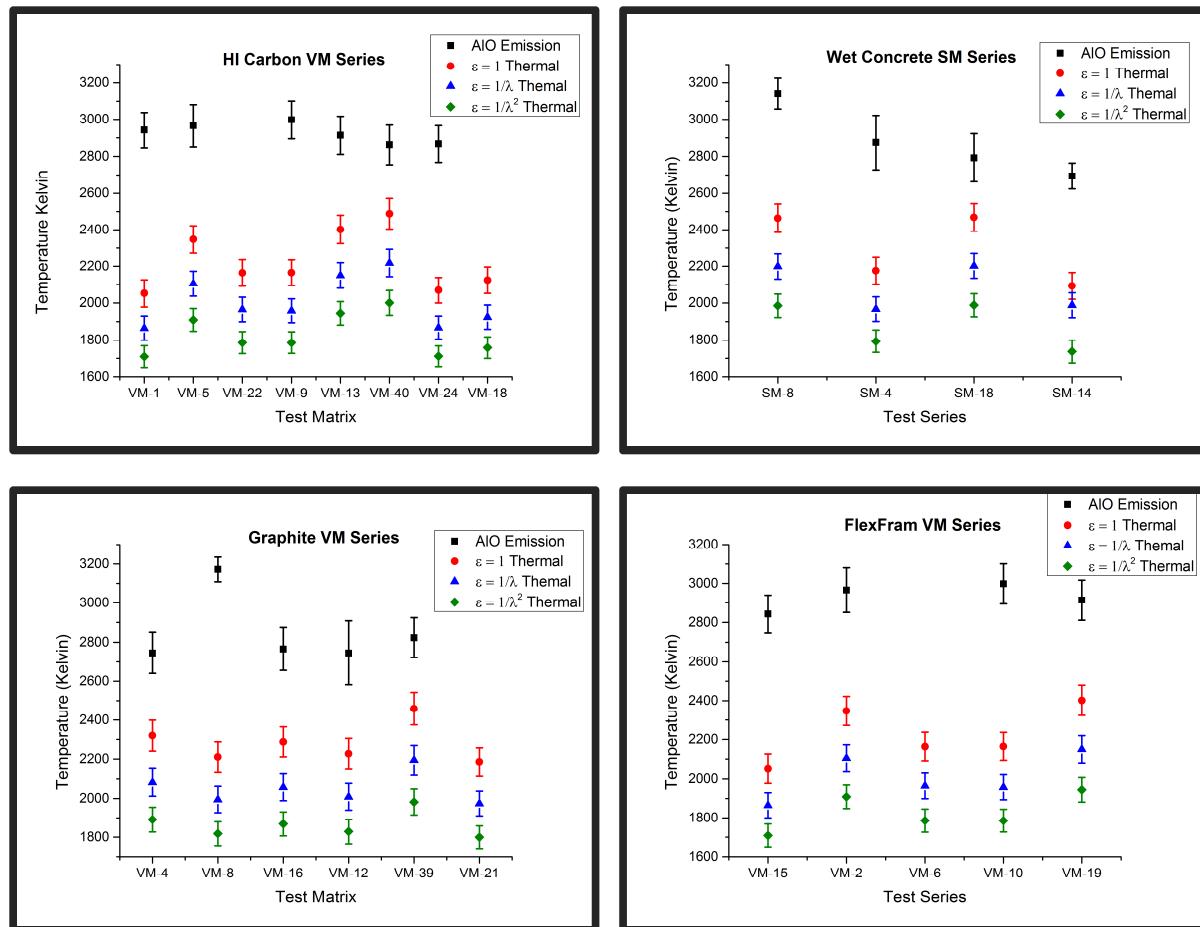
# Results-Positional Dependence

- Slight positional dependence observed
- AIO emissions show larger variation over a data set than thermal emissions



# Results-Substrate Dependence

- Substrates are consistent within a temperature range
- 2800-3200 Kelvin for AlO emissions
- 2000-2400 Kelvin for thermal emissions



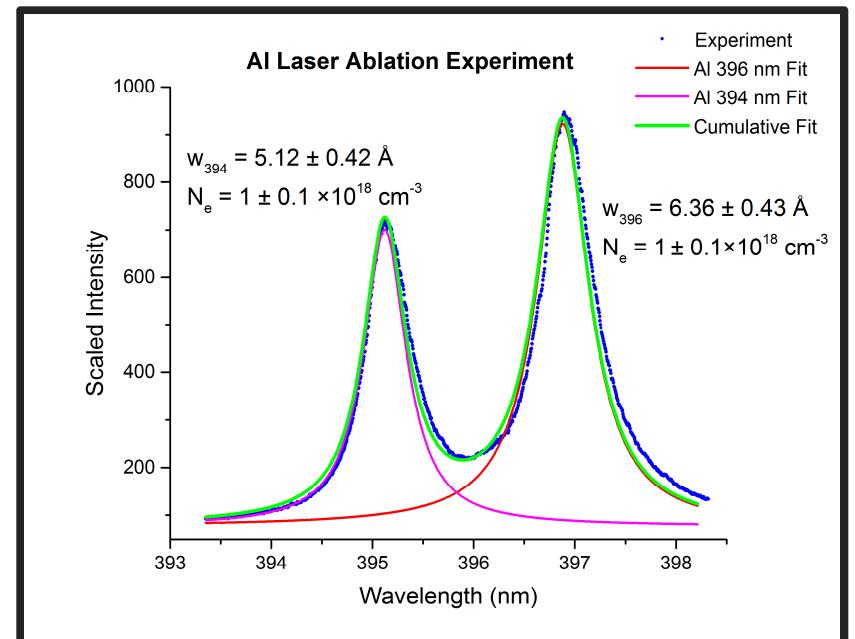
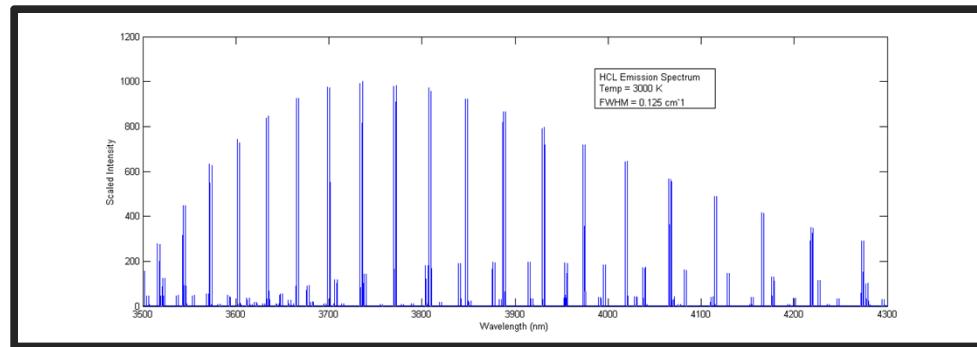
# Summary

- Temperatures are fairly consistent with each other;
- Very few data sets showed positional dependence;
- Gap size and propellant size does not have an apparent effect on the temperature;
- Substrates appear to be consistent with each other
- AlO emission temperatures 2800-3200 Kelvin;
- Thermal emissions 2000-2400 Kelvin;
- Wavelength dependence of emissivity is of continued interest.



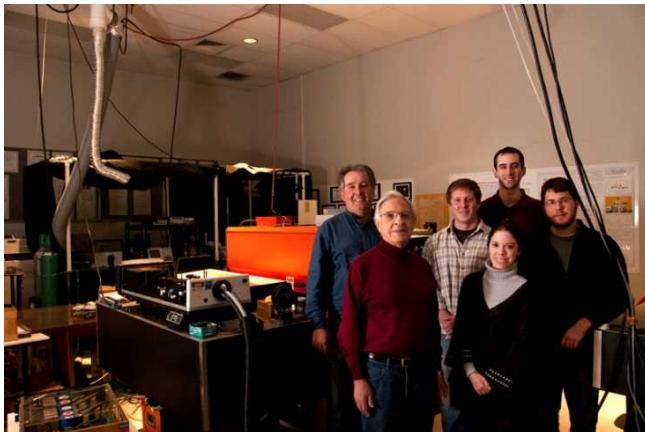
# Future Considerations

- Continued laboratory scale testing
- Inclusion of HCl emissions with our diatomic line strength method
- Development of a species density diagnostic (LIBS)



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**Sandia  
National  
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