

# **Development, Characterization, and Modeling of a TaOx ReRAM for a Neuromorphic Accelerator**

**Electrochemical Society Fall Meeting**

**Cancun**

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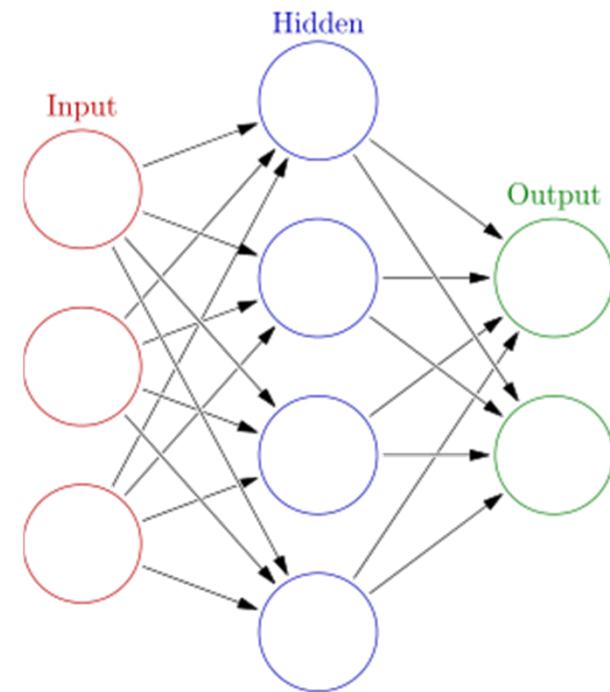
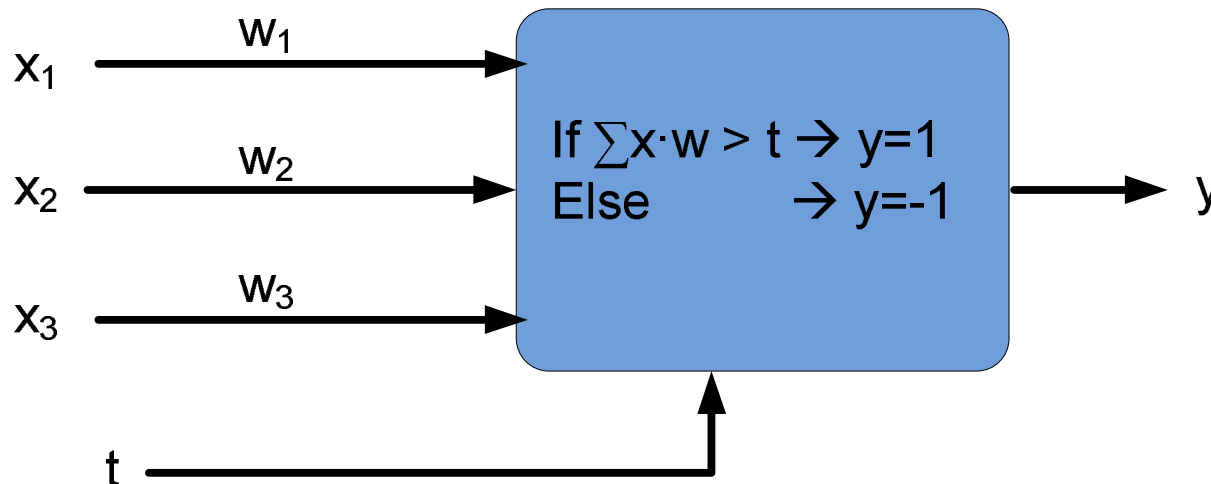


# Outline

- **Neuromorphic Computing with ReRAM**
- **Development of a CMOS/ReRAM Process**
- **Characterization of Device Behavior**
- **Modeling**
  - Analytical
  - DFT
- **Conclusion and Future Work**

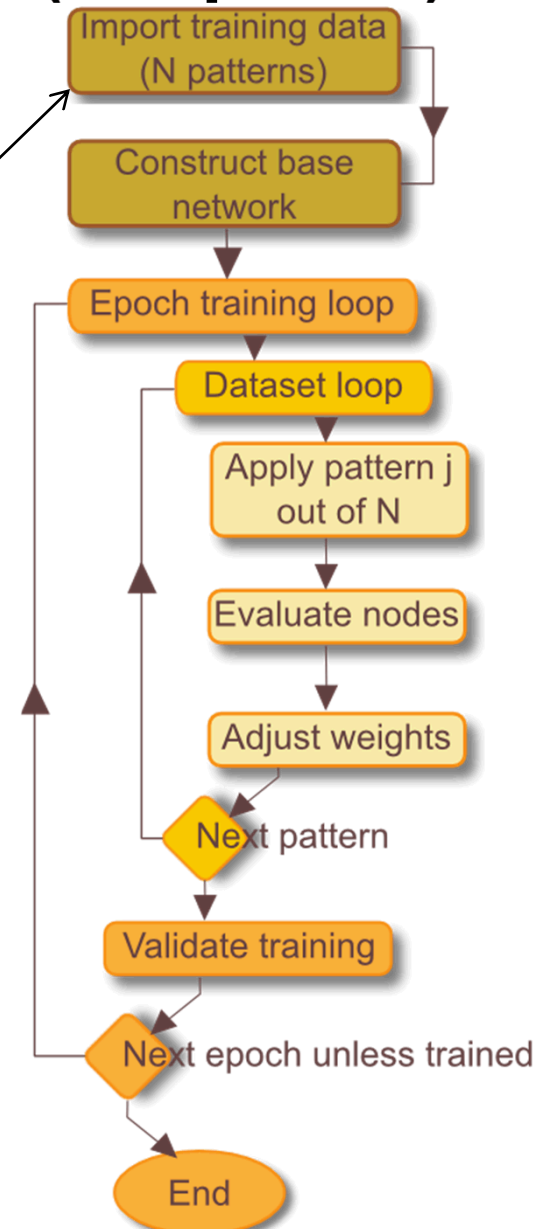
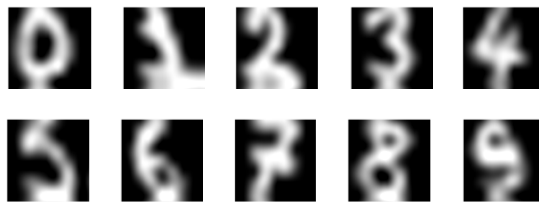
# Perceptron Based Neural Nets

- Perceptron is the simplest model of a neuron
- Feed forward network
- Single node can learn linearly separable logic functions
- Applications:
  - Field programmable gate arrays
  - Pattern recognition



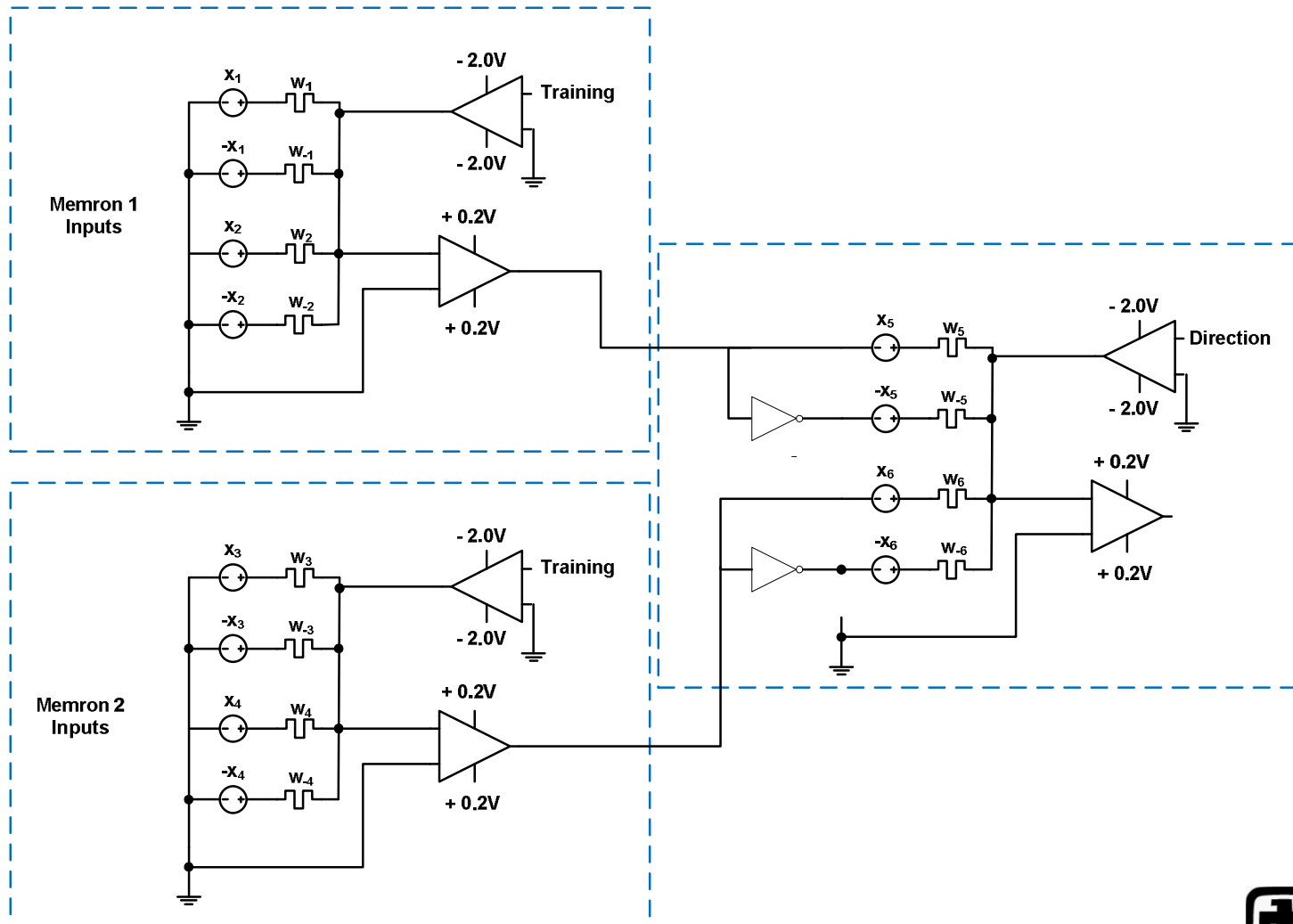
Wikipedia.org

# Perceptron Network (Simplified)



# Memron

- Requires 3 Memrons to learn XOR:



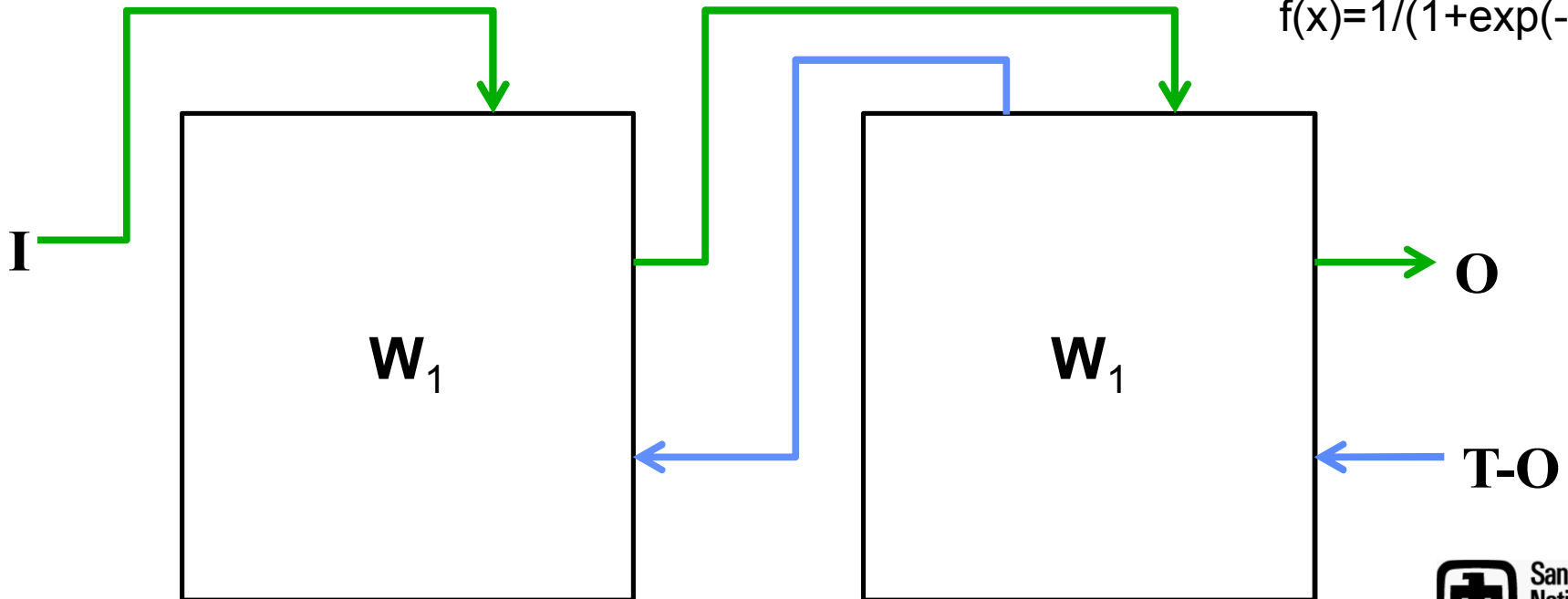
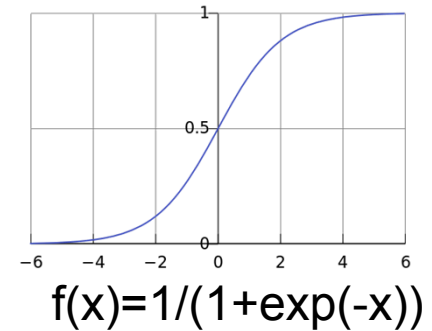
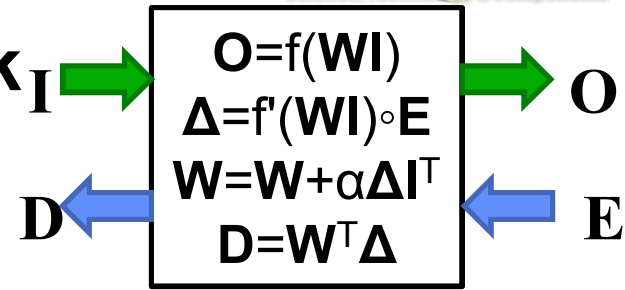
# Why Do We Need an HW Accelerator?

- Use simulation results for similar algorithm as example
- Significant power savings using a memristor-based HW accelerator :
- 16x reduction in power over SRAM ASIC
- 6x reduction in chip area over SRAM ASIC
  - Equivalent to 6x improvement in performance/area

Example 1: 25,600 neurons 100,000 iterations/s					
Configuration	# of chips	Chip area (mm <sup>2</sup> )	% active	Power (W)	Power eff. over Xeon
Memristor Analog (config 4)	1	5.9	38.6%	0.07	234,859
Memristor Digital (config 5)	1	18.2	89.6%	0.62	16,968
SRAM (config 6)	1	29.1	89.6%	1.13	8,215
NVIDIA M2070	12	529.0	99.2%	2700.00	6
Intel Xeon X5650	179	240.0	99.9%	17005.00	1

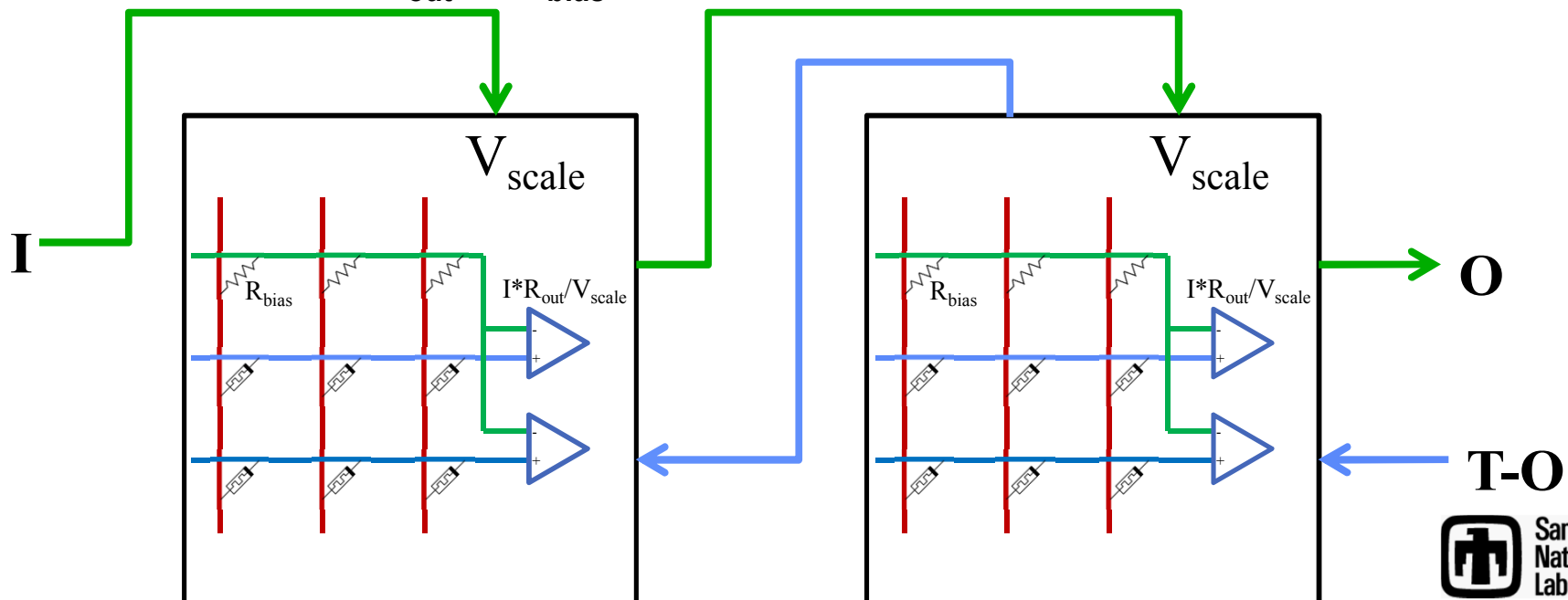
# Perceptron Network

- Compute output **O** based on input **I**, weight matrix **W**, and squashing function  $f()$ .
- Delta-rule: Update **W** based on the outer product of **I** and the partial derivative  $\Delta$ , scaled by learning rate  $\alpha$ .
- Back-propagation: Allocate error on outputs (**E**) to error on inputs (**D**) by passing partial derivatives back through **W**.
- Training: Feed a bunch of (**I**,**T**) pairs, until convergence.



# ReRAM-Neural Hardware Simulation

- Purely in software
- Uses data table to emulate each memristor
- Replaces MLP block with a crossbar and some hypothetical surrounding circuitry.
- Values passed between blocks in floating point.
- Converted internally to voltages via  $V_{\text{scale}}$  (at present simply 1).
- Weights mapped to numbers via  $R_{\text{bias}}=4,000$  and  $R_{\text{out}}=40,000$ .
  - $R=1/(W/R_{\text{out}}+1/R_{\text{bias}})$



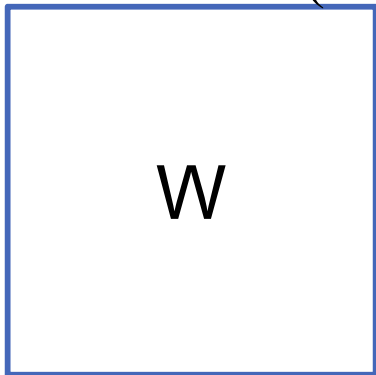


# Performance of various network structures

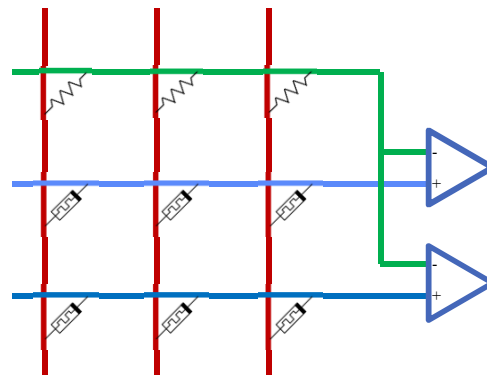
- Train conventional perceptron.
- Convert weight matrix directly to memristor values.
- Test on MNIST handwriting dataset, with and without model noise.



Conventional (CPU) Fixed bias resistors

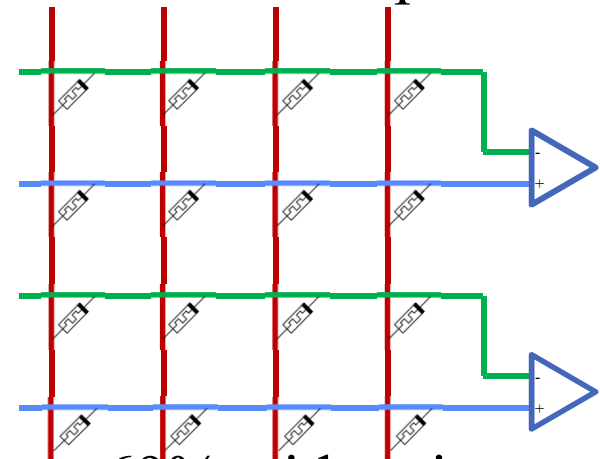


96%



88% with noise  
96% noise-free

Bias memristor per element

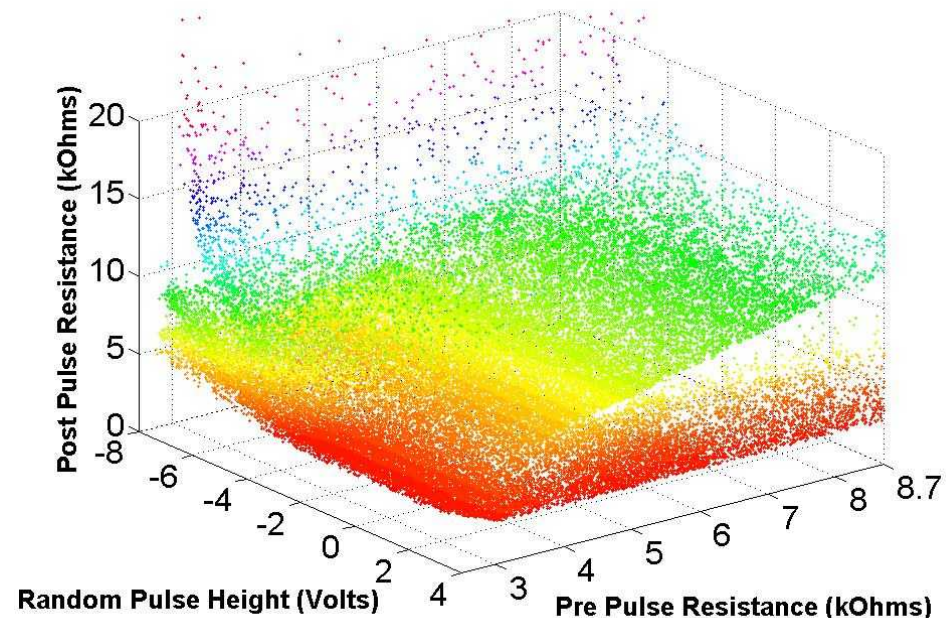


69% with noise  
96% noise-free

Why? – Each memristor introduces more noise, so fixed-bias network is more accurate.

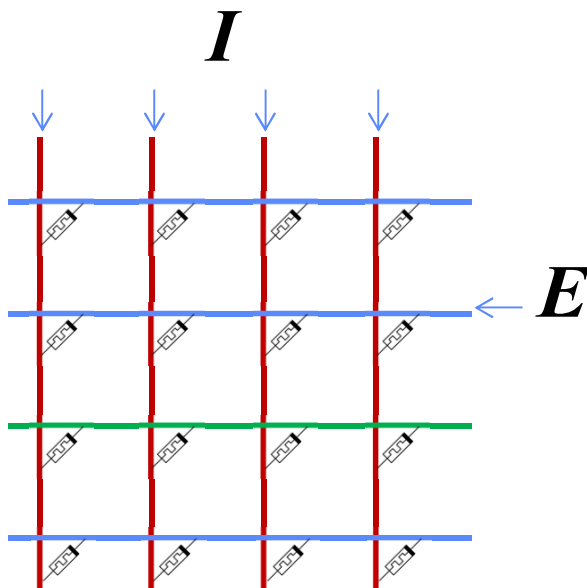
# Empirical memristor model

- Represented by a lookup table
- Binned 10M-sample data (100  $\Omega$  x 0.1 V bins)
- Table contains  $\Delta\Omega$  values
- Standard deviation of each cell used to simulate noise.
- Chart on left is slice through 4K $\Omega$
- Flat between -1.6V and 1.6V



# Empirical memristor model

- Backpropagation training
- $dW = \alpha EI^T$  where  $E$  is error vector and  $I$  is input
- Update each row separately so column values can be set appropriately for given error value.
- Test on handwritten digit recognition (MNIST dataset).
- Accuracy = 91.8% (classic methods reach 99.9%)



# Representing Weight As Resistance

**Relationship of weight to resistance:**  $W = R_{out} \left( \frac{1}{R} - \frac{1}{R_{bias}} \right)$

**Sensitivity of weight to resistance (with  $R_a = R_b + R'$ ):**

- $$\begin{aligned}
 W' &= W_a - W_b = R_{out} \left( \frac{1}{R_a} - \frac{1}{R_{bias}} \right) - R_{out} \left( \frac{1}{R_b} - \frac{1}{R_{bias}} \right) \\
 &= R_{out} \left( \frac{1}{R_b + R'} - \frac{1}{R_b} \right) \\
 &= R_{out} \left( \frac{-R'}{R_b(R_b + R')} \right)
 \end{aligned}$$

**Example:**

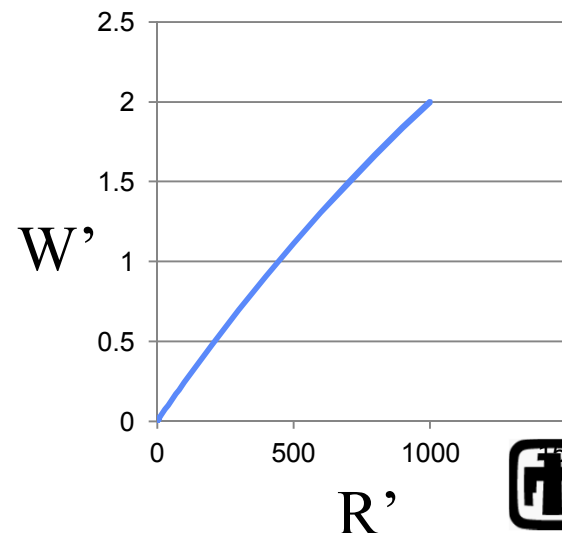
$$R_{bias} = 4k\Omega$$

$$R_{out} = 40k\Omega$$

$$R_b = R_{bias}$$

$$R' = 100\Omega$$

$$W' = 0.244$$



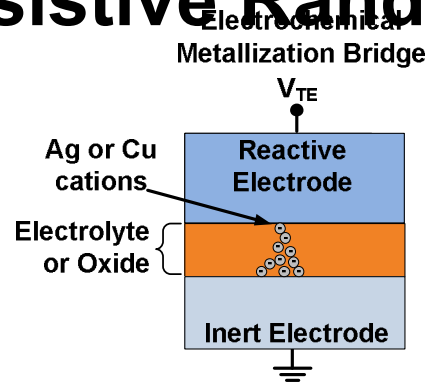
# Sensitivity of Error to Resistance:

- Let  $WI$  be close to 0, so  $f'(WI)=0.25$  (derivative of sigmoid function)
- Let  $I=1$  (for simplicity)
- $\alpha=0.01$
- $W'=\alpha\Delta I=0.01*0.25*E*1$
- $E=W'/0.0025=0.244/0.0025=97.6$  (with  $R'=100\Omega$  as on previous slide)
- That is, at typical values, the smallest error achievable is 2 orders of magnitude larger than typical output range for an MLP neural network!

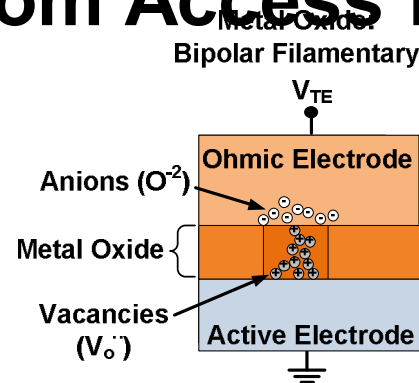
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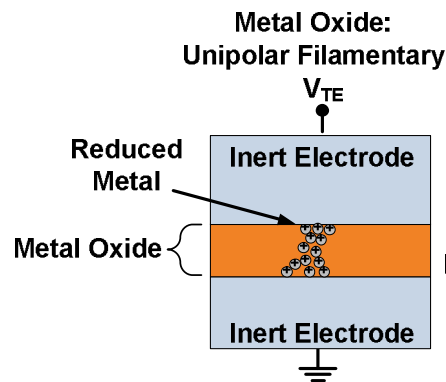
# Resistive Random Access Memory



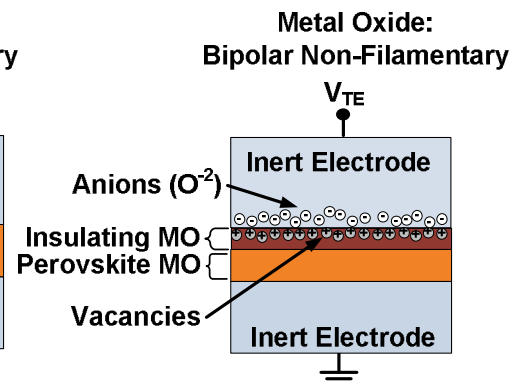
- Switching: Electrochemical formation and dissolution of Ag or Cu filament
- Cation motion (Ag or Cu)
- Chalcogenide or oxide insulating layer
- Switching depends on E-field direction
- R/W current independent of device area



- Switching: Valence change and migration of oxygen vacancies
- Anion motion (O<sup>2-</sup>)
- HfO<sub>x</sub>, TaO<sub>x</sub> most common insulators
- Switching depends on E-field direction
- R/W current independent of device area



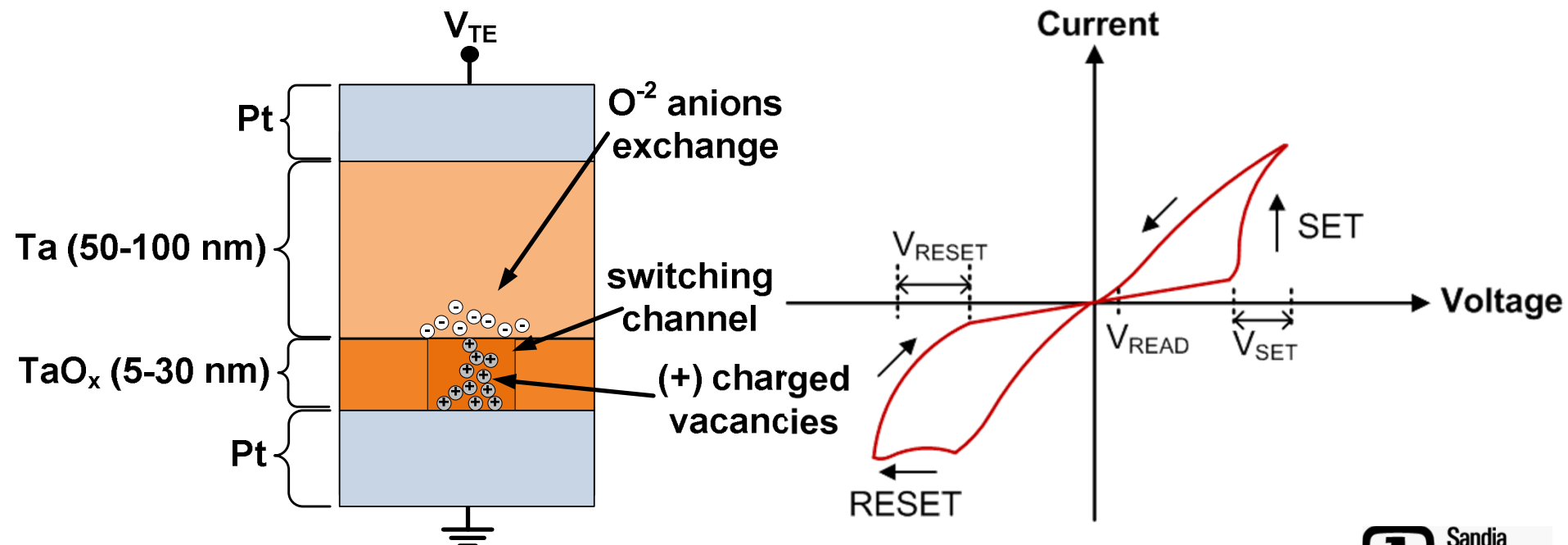
- Switching: Thermochemical change in oxide valence state
- Anion motion (O<sup>2-</sup>)
- Symmetric structure
- NiO<sub>x</sub> most common material
- Switching independent of E-field direction
- R/W current independent of device area



- Switching: Oxygen exchange causes Schottky barrier height change at interface
- Anion motion (O<sup>2-</sup>)
- Perovskite and insulating metal oxide
- Switching depends on E-field direction
- R/W currents depend on device area

# Valence Change ReRAM

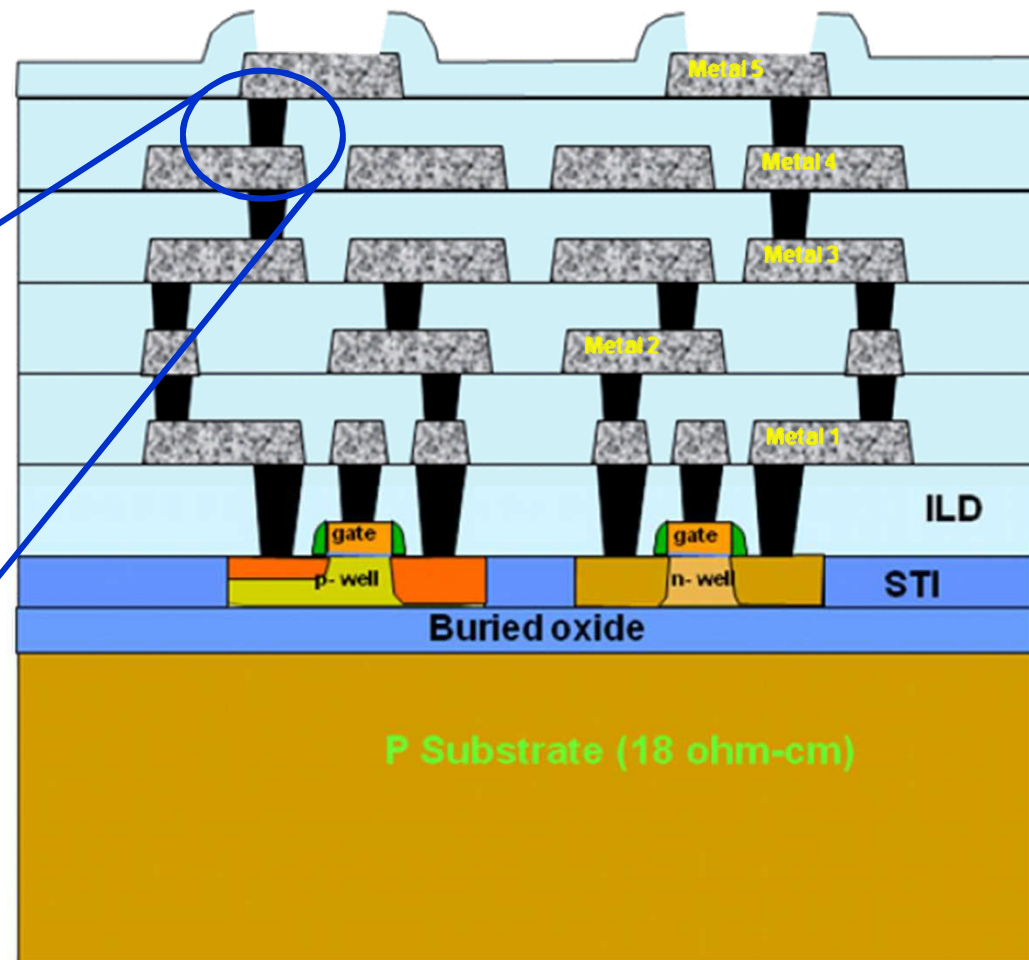
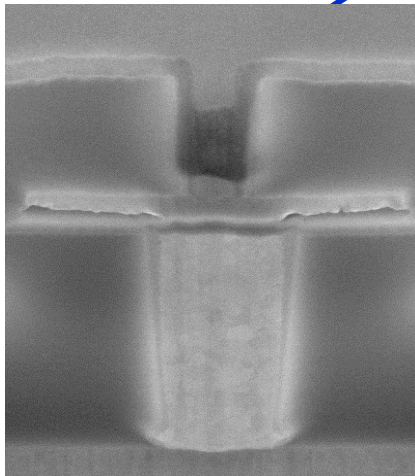
- “Hysteresis loop” is simple method to visualize operation
  - (real operation through positive and negative pulses)
- Resistance Change Effect (polarities depend on device):
  - Positive voltage/electric field: low R –  $O^{2-}$  anions leave oxide
  - Negative voltage/electric field: high R –  $O^{2-}$  anions return
- Common switching materials:  $TaO_x$ ,  $HfO_x$ ,  $TiO_2$ ,  $ZnO$





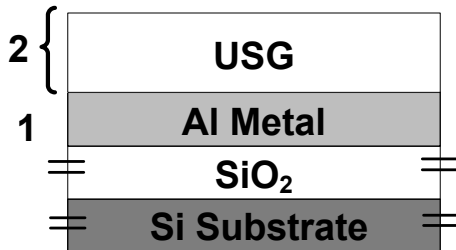
# Memristors + CMOS

- Sandia CMOS7 Process
  - 3.3V, 350 nm, MOSFETs
  - SOI substrate
- Baseline for memristor integration

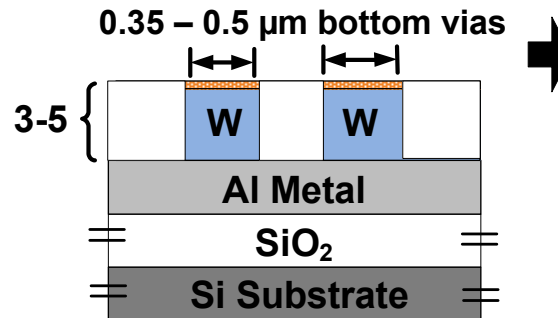


# Process Flow

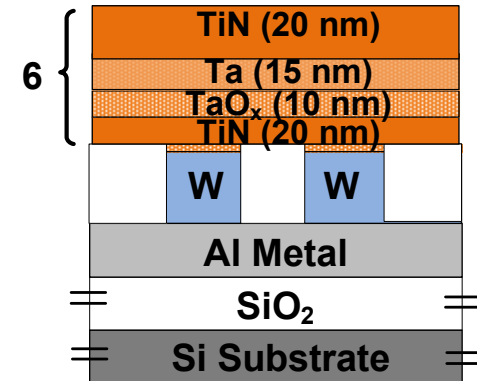
1. Deposit Bottom Metal (Al)
2. Deposit USG



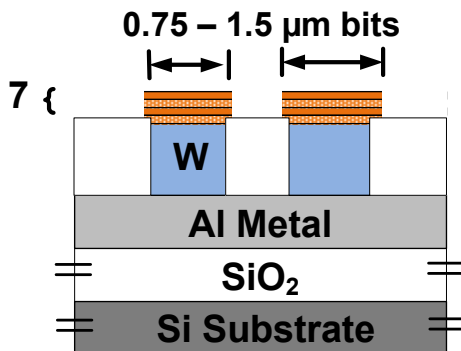
3. Etch via holes in USG
4. Deposit W and TiN layers
5. CMP



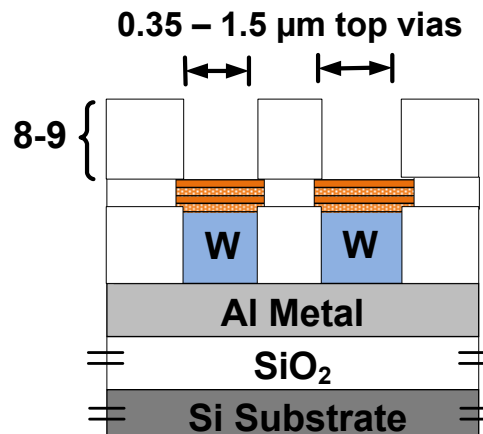
6. Deposit bit stack (layers enlarged for clarity)



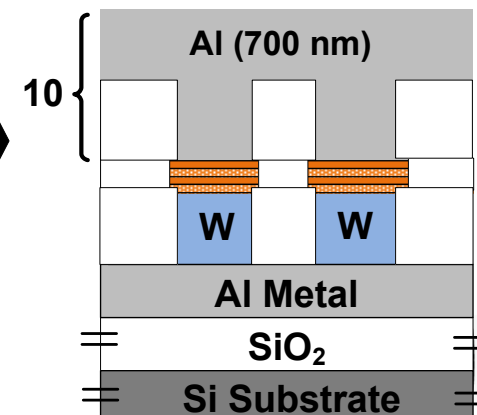
7. Etch bits



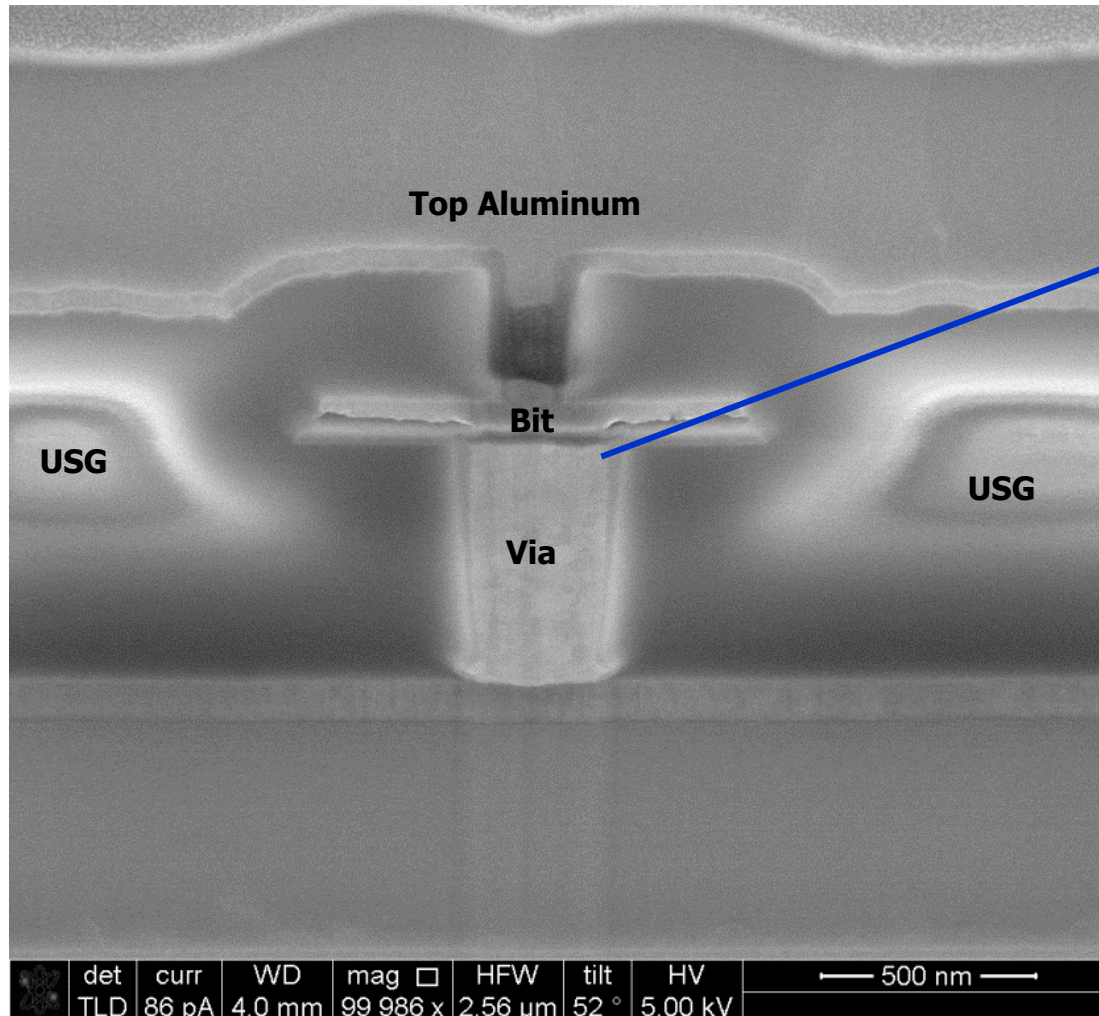
8. Deposit top USG
9. Etch top via holes in USG



10. Deposit top Al

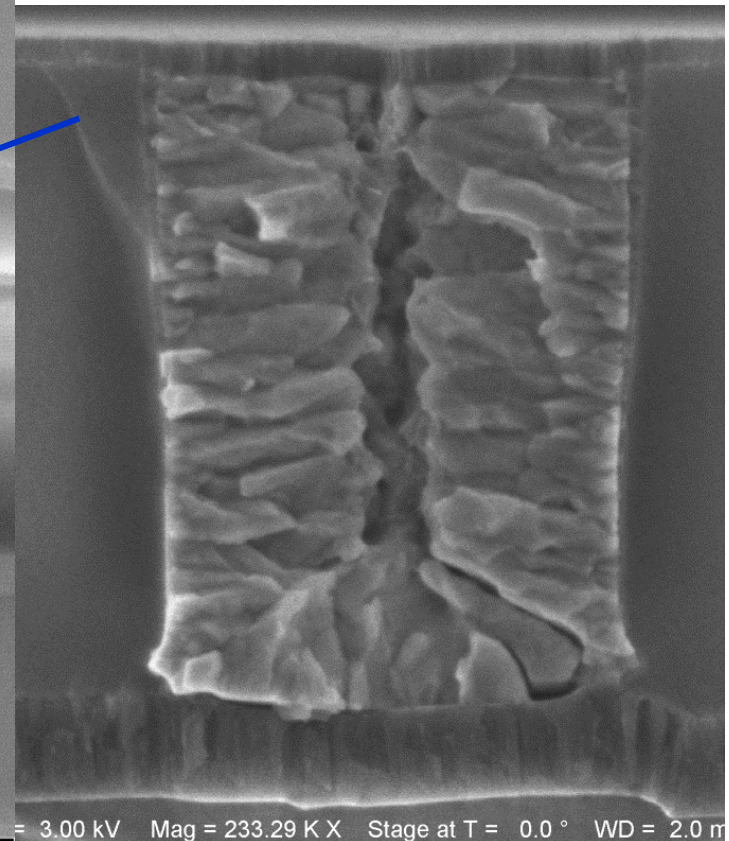


# Final Structure



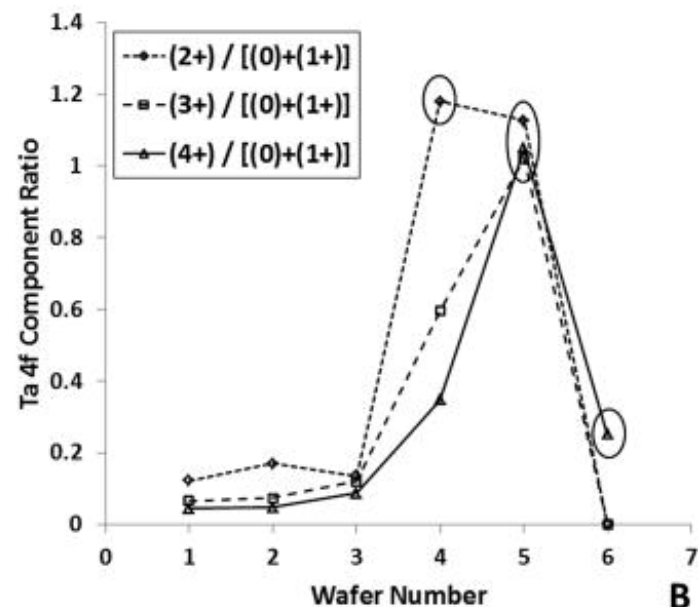
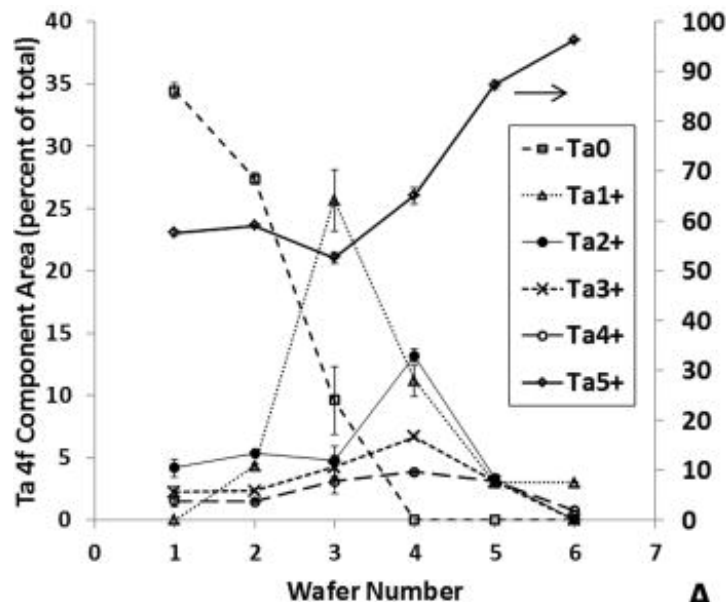
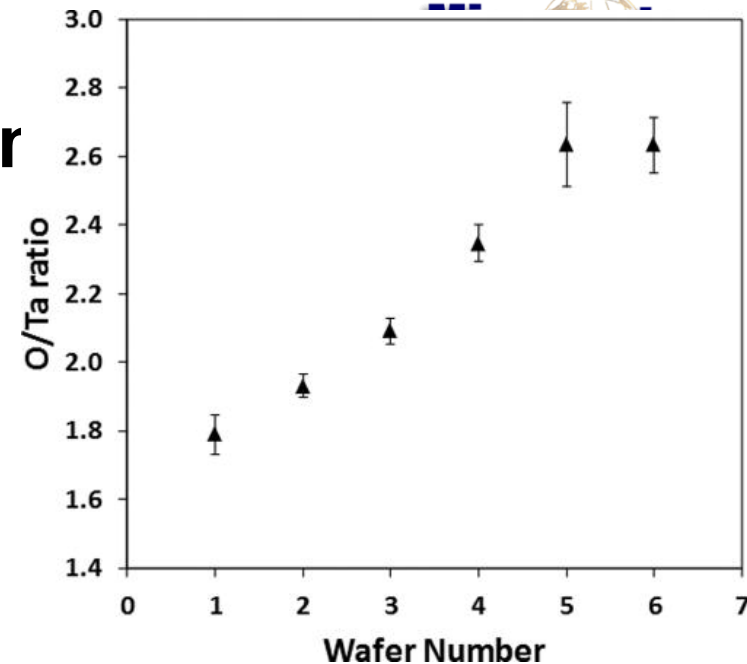
**Important to have extremely flat surface under bit**

**Polished TiN Surface**



# Beyond Stoichior

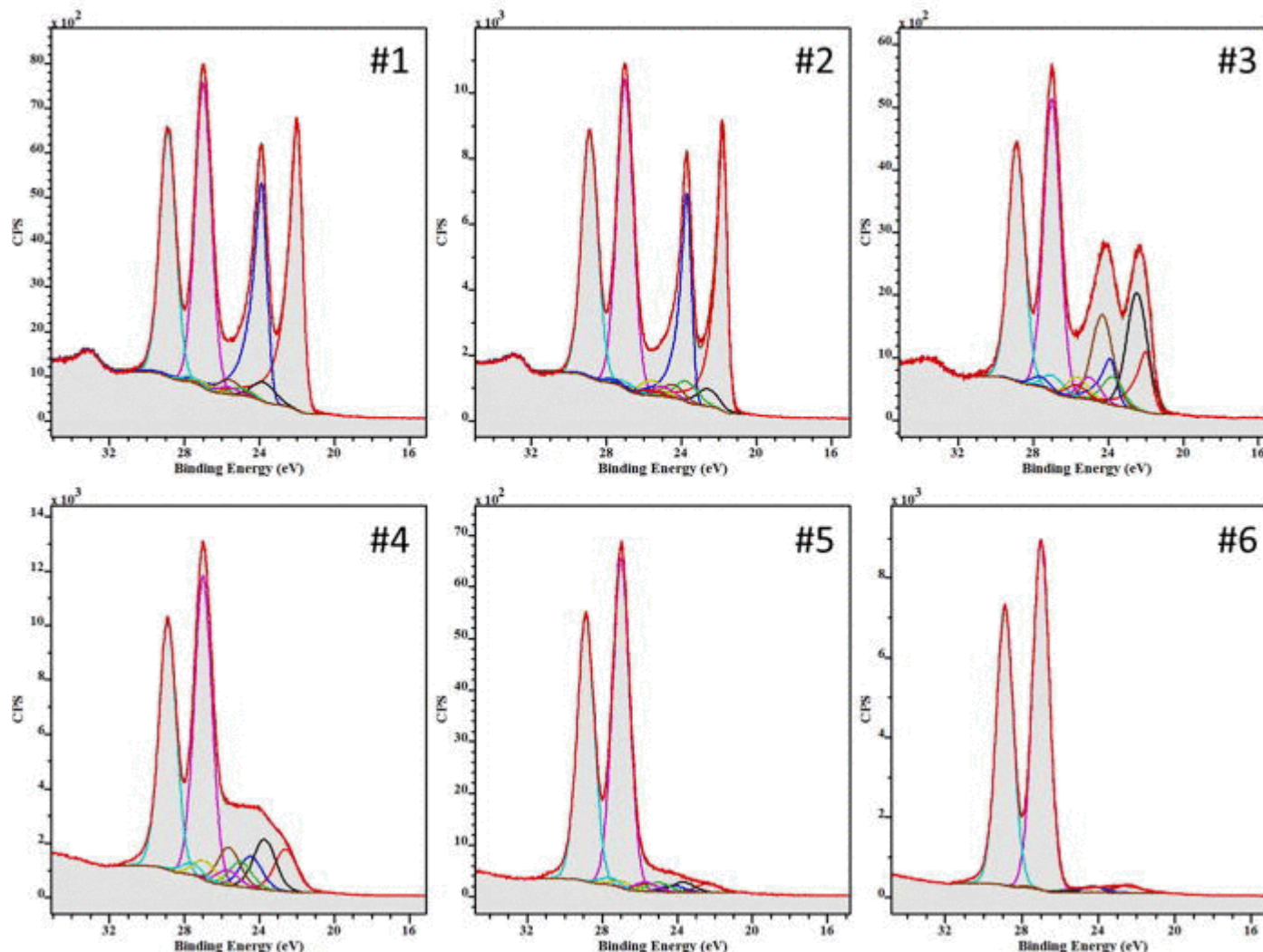
- Goal: Assess properties that make a “good” memristor
- Stoichiometry doesn't tell the entire story
- Deconvolving XPS spectra provides Ta valence makeup



Brumbach et al, JVST 2014



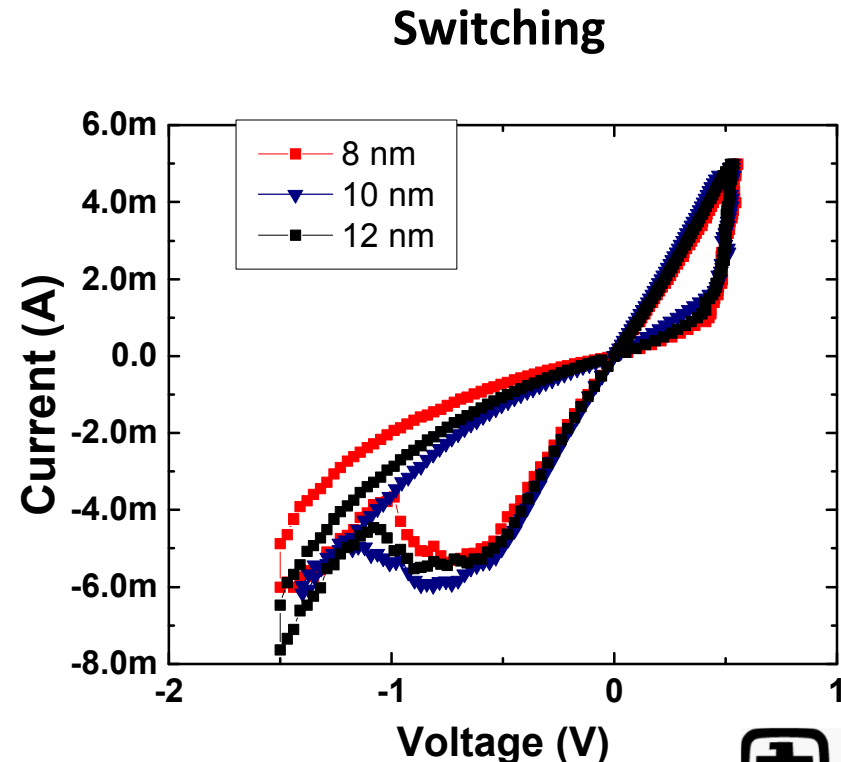
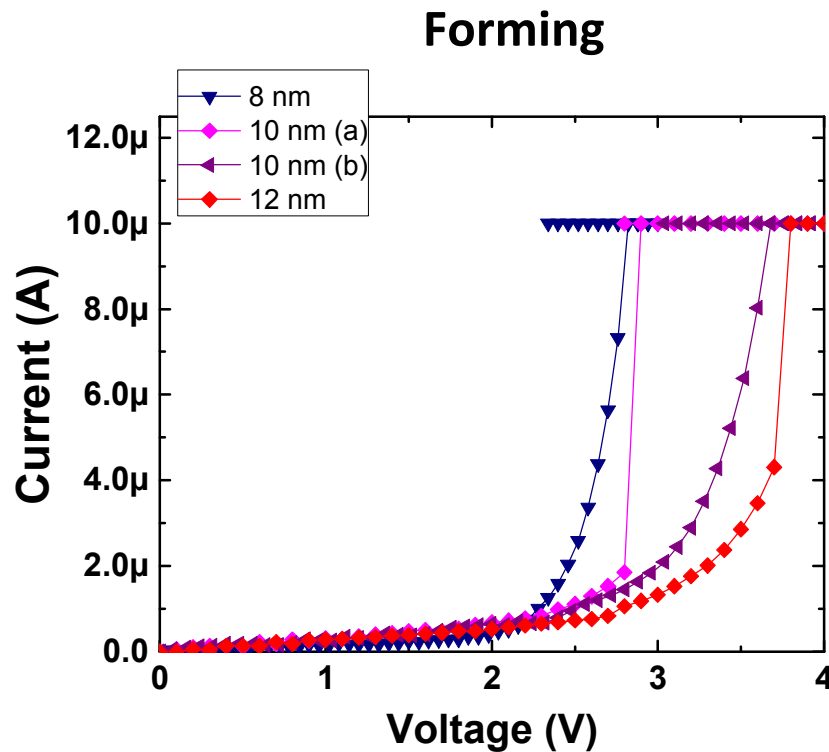
# XPS: Properties of a Switching TMO



Brumbach et al, JVST 2014

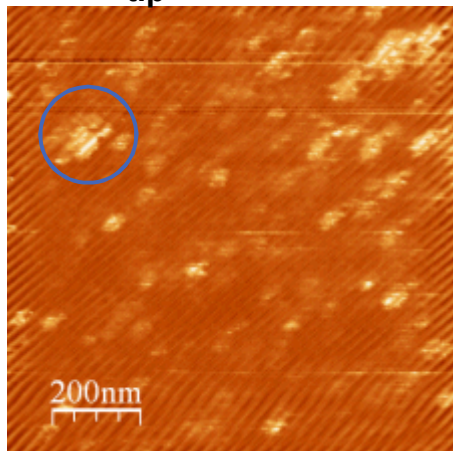
# Forming Process

- Roughly depends on film thickness (still varies)
- Macroscopic (wafer scale) and nanoscopic variations in thickness

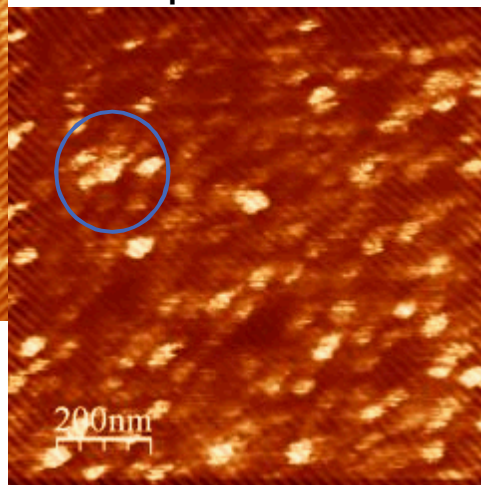


# “Hot Spot” Formation

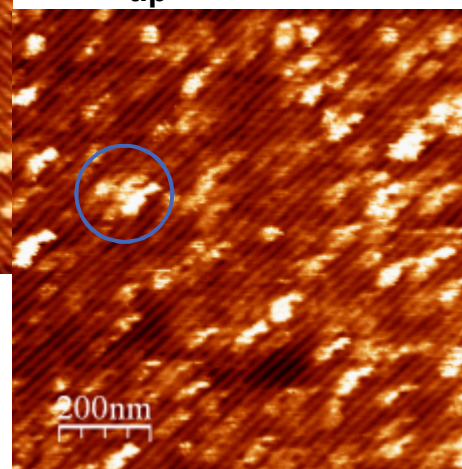
$V_{\text{tip}} = 2.4 \text{ V}$



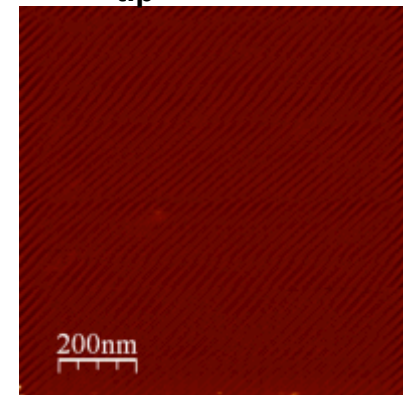
$V_{\text{tip}} = 2.6 \text{ V}$



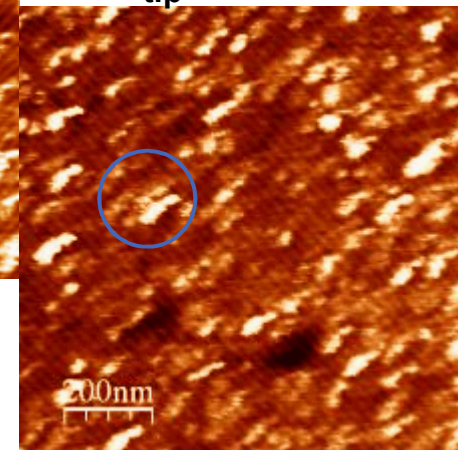
$V_{\text{tip}} = 2.8 \text{ V}$



$V_{\text{tip}} = 2.0 \text{ V}$



$V_{\text{tip}} = 3.0 \text{ V}$

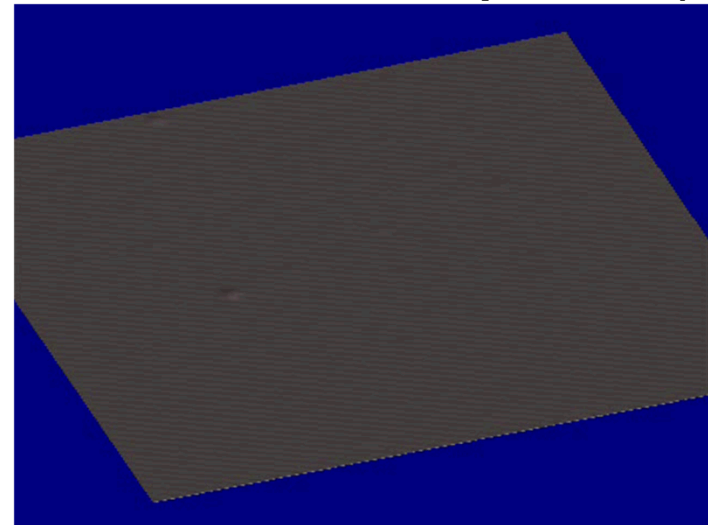


# Hot Spot Evolution

C-AFM Current Map Movie (2D)



C-AFM Current Map Movie (3D)

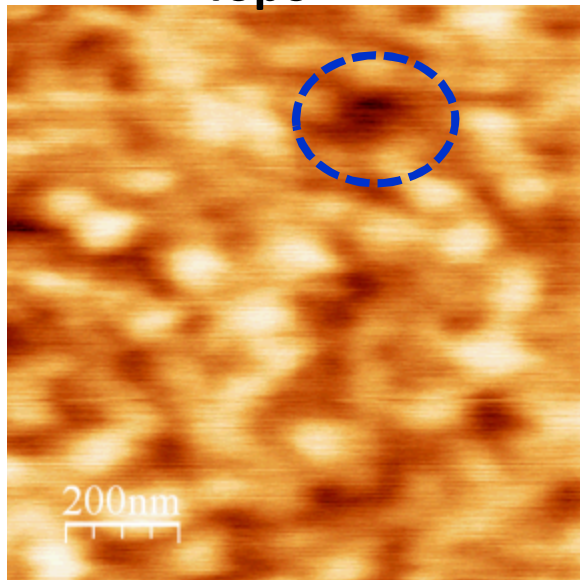




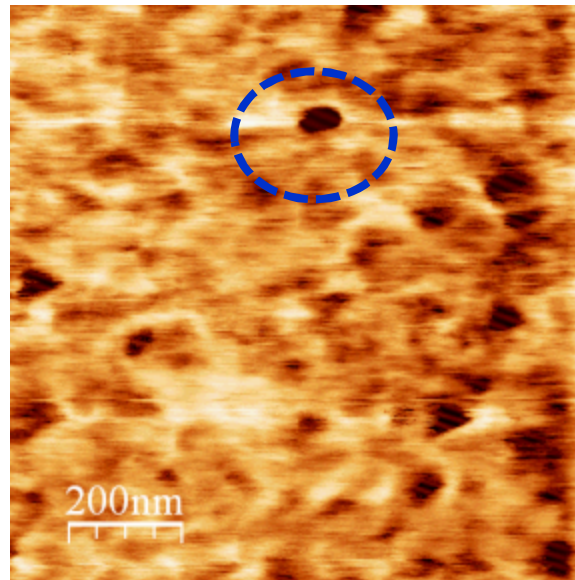
# Topography versus Conductivity

- Prominent hot spot appears to depend on geometry
- Other hot spots do not necessarily correlate with geometric defect

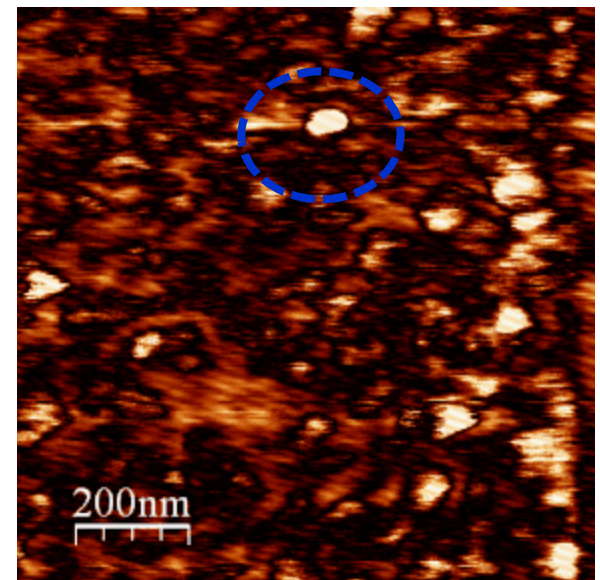
Topo



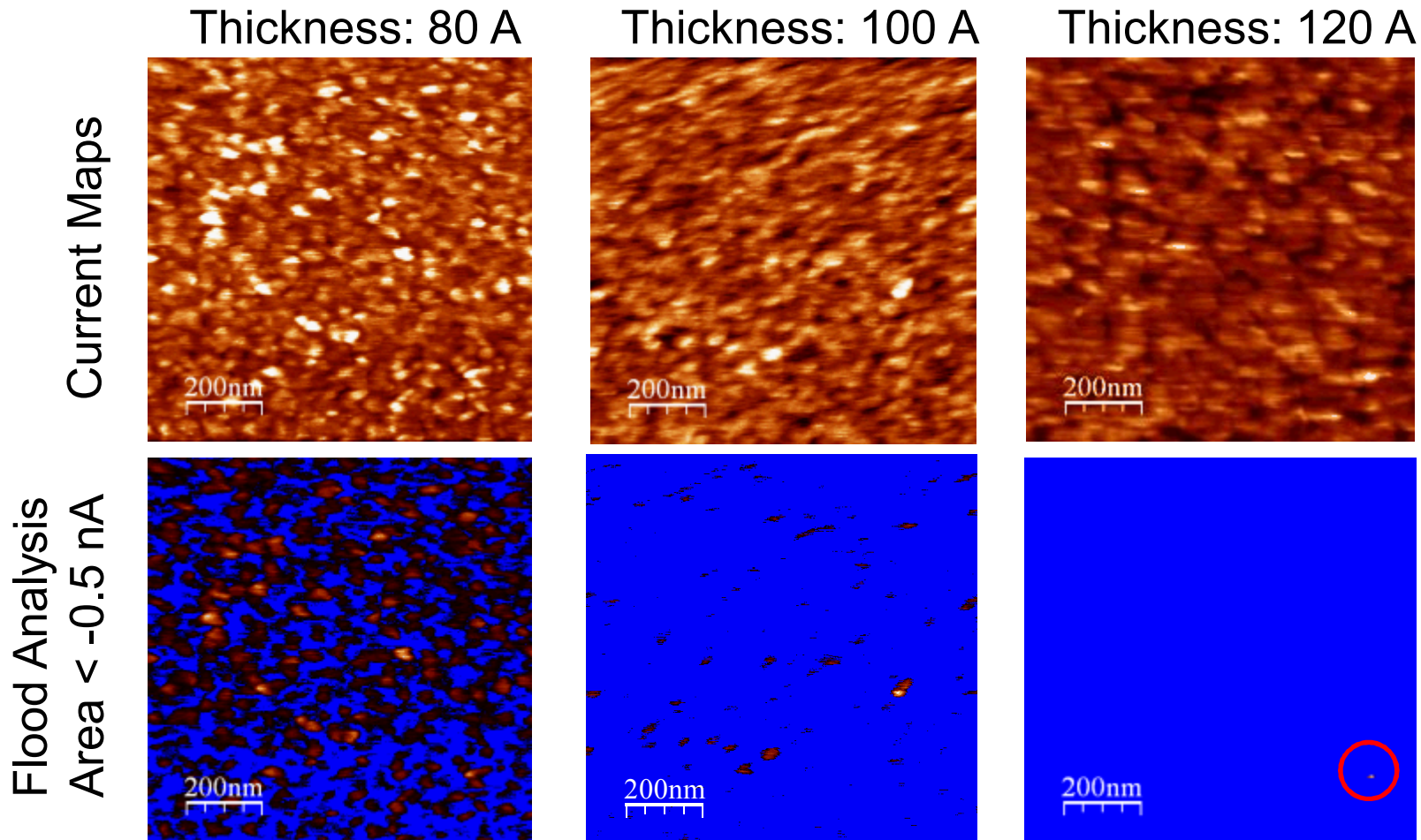
Current



Merged (And)



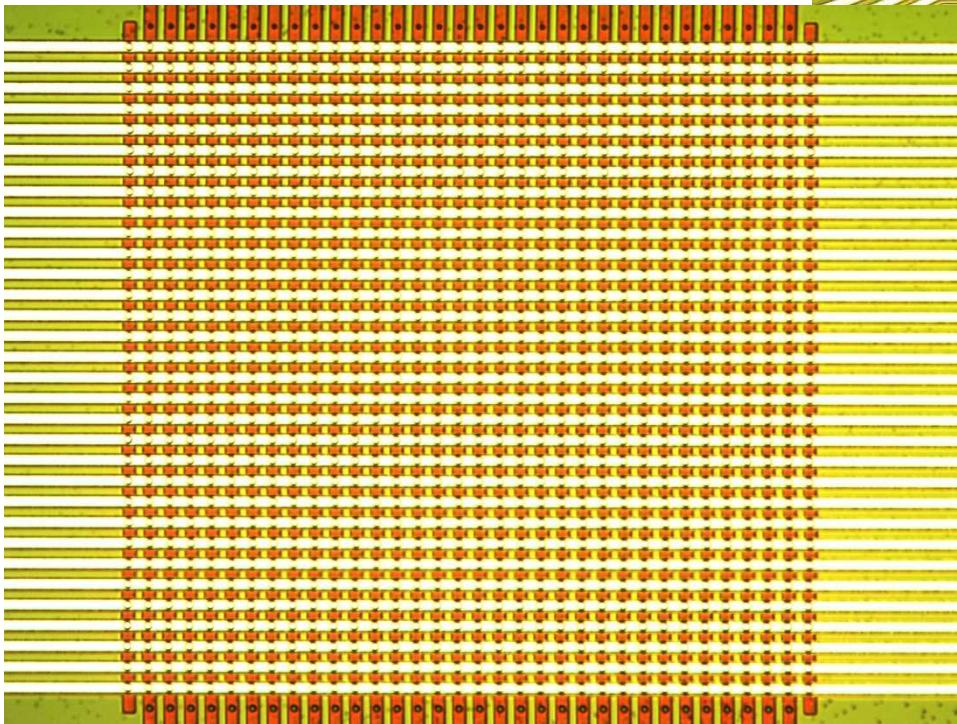
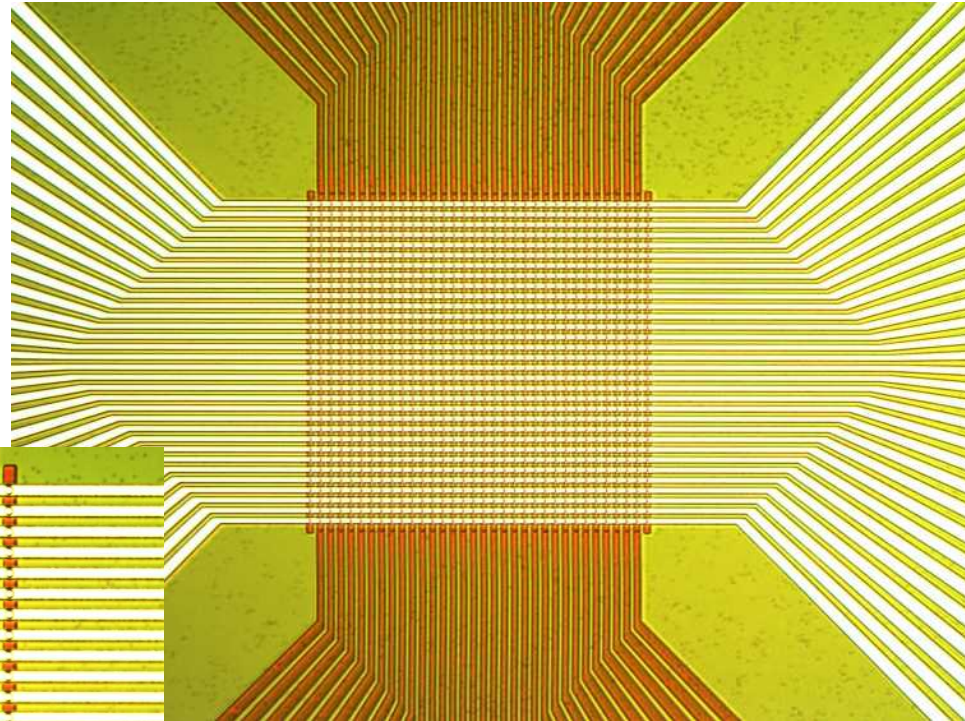
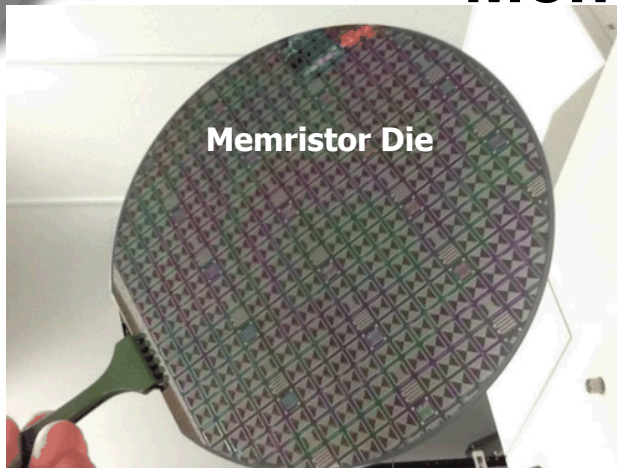
# Hot Spot Density vs Thickness



Sample Voltage: -3.5 V  
Same tip used for all imaging

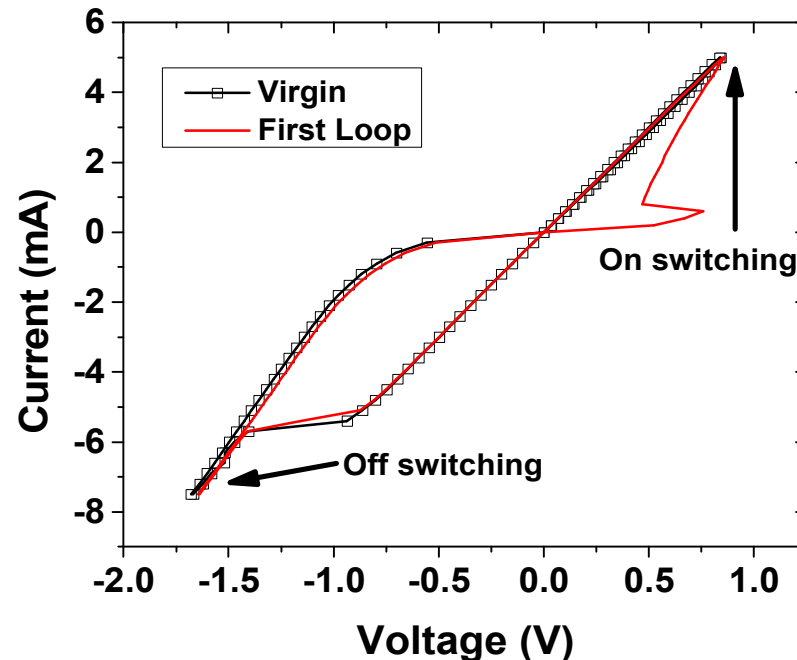


# Memristor Crossbar Die



# Basic Device Performance

- Typical devices form at very low currents
- Appear “forming free” in current sweep mode
- Do not need a high voltage transistor!!
  - Unlike flash/SONOS
- Can be tailored by stoichiometry



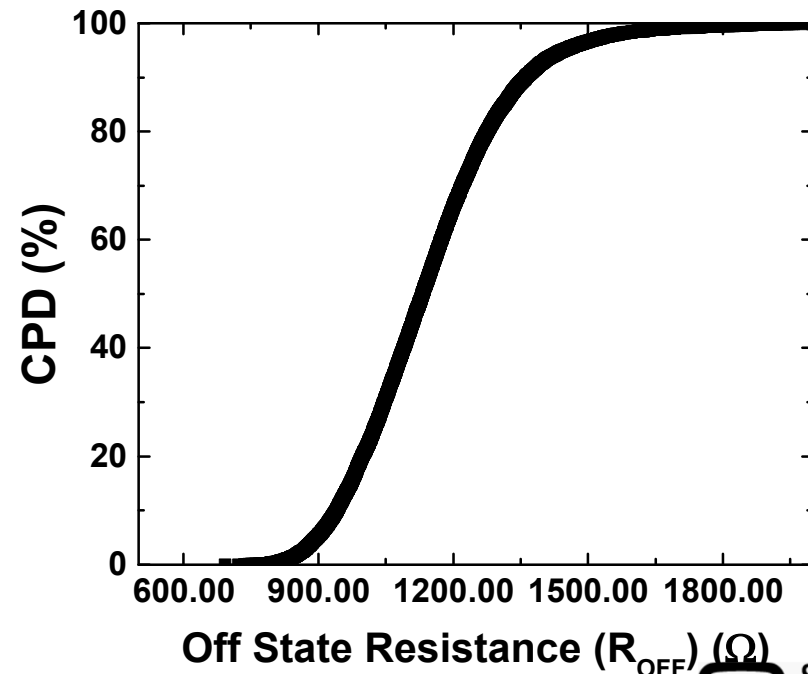
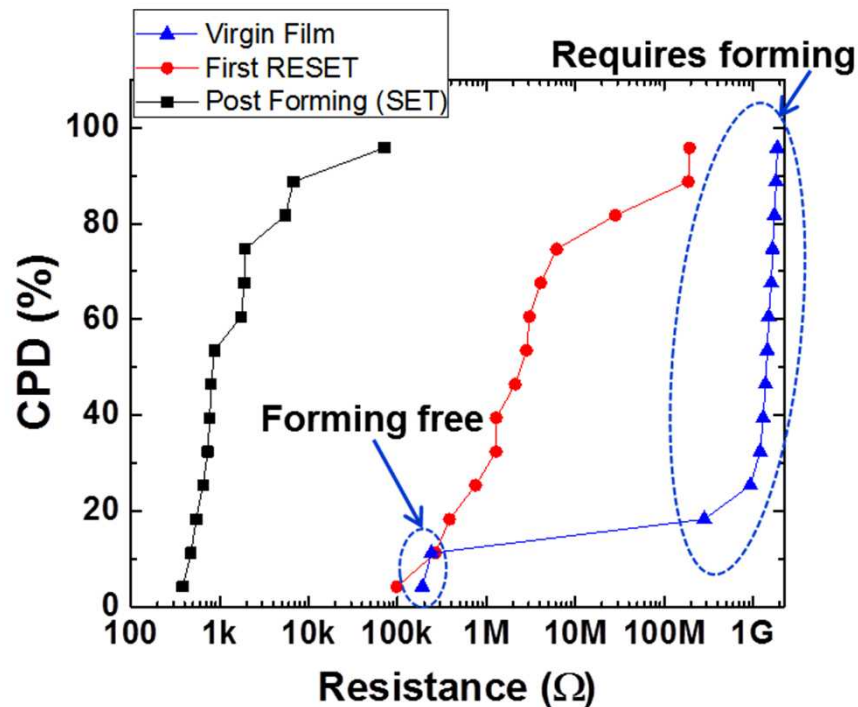


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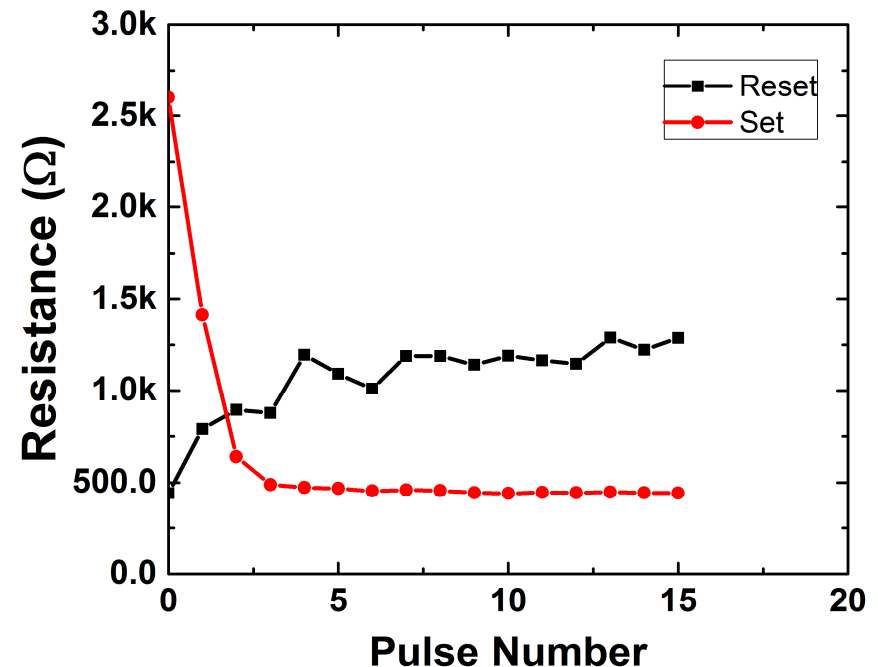
# Variability

- Between different devices
  - Manufac
- Cycle to cycle
  - Fundamental physical attribute



# Set and Reset Transition

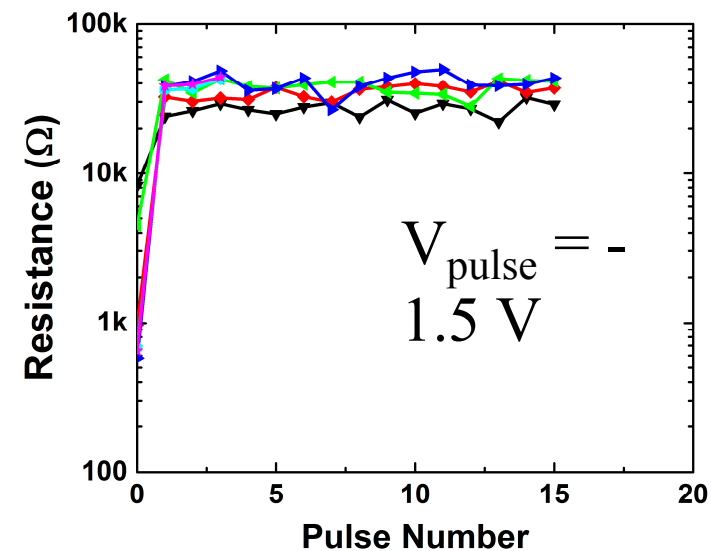
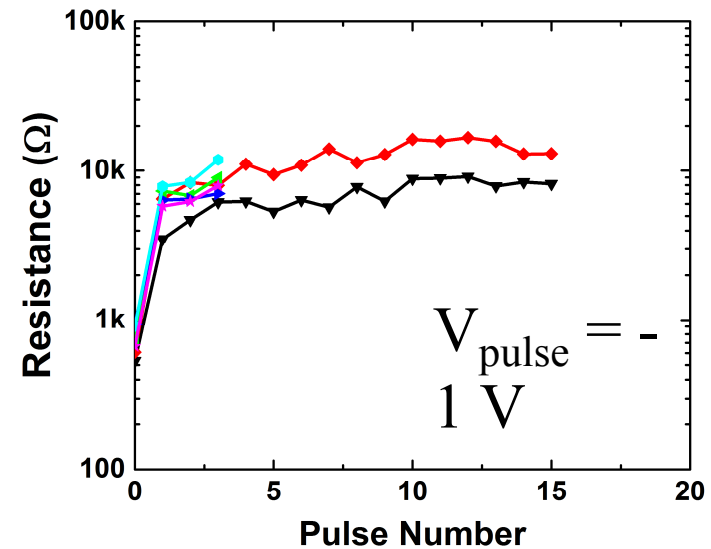
- Repeated pulsing can gradually change resistance
  - SET transition more abrupt





# Transitions to Varying Resistance Levels

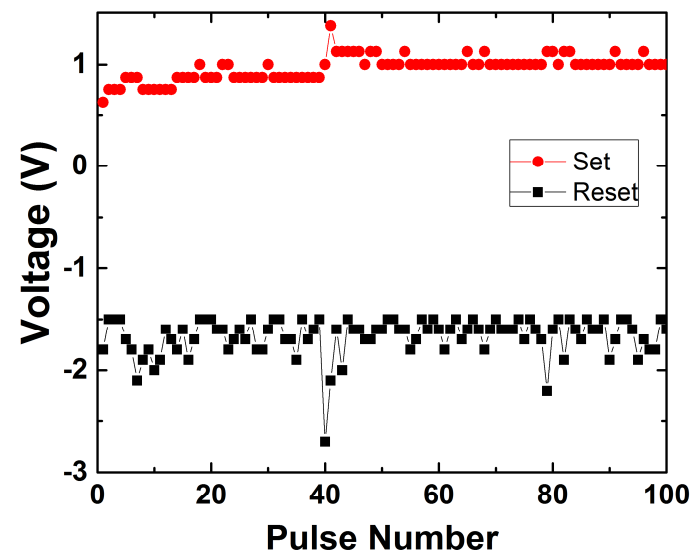
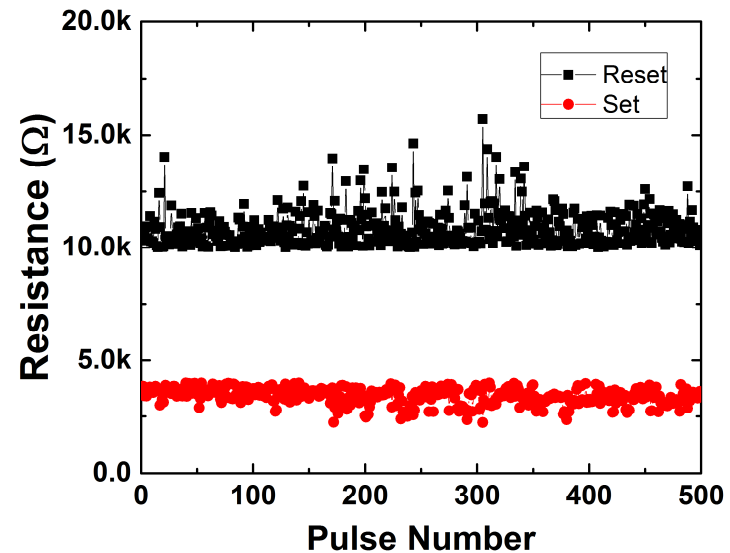
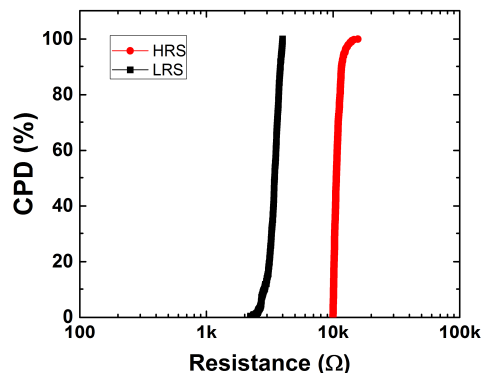
- Resistance level can begin to saturate for different voltage levels
  - Repeated pulsing may change resistance very gradually
  - Transitions occur from multiple starting resistance values
- Resistance usually falls into a typical band within the first three pulses





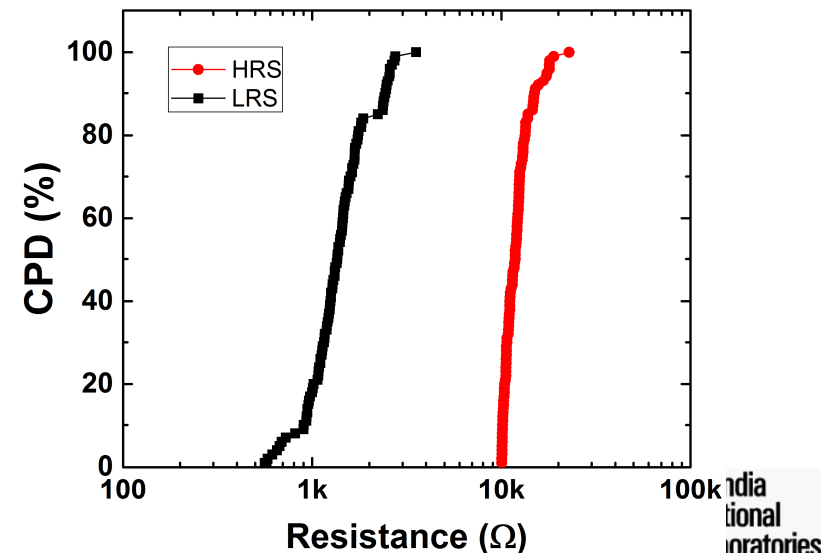
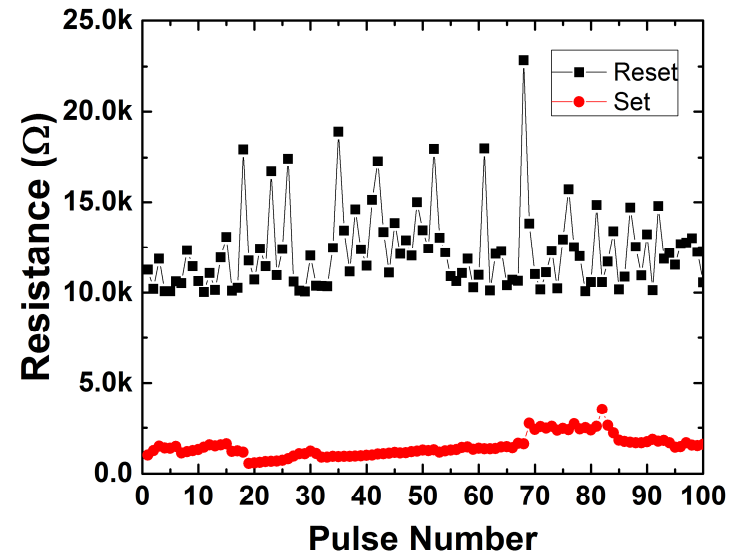
# Closed Loop Cycling

- Continues pulsing until a threshold resistance value is passed
  - Allows for tighter resistance values
  - Helps with initial characterization of parts to determine ideal pulse heights



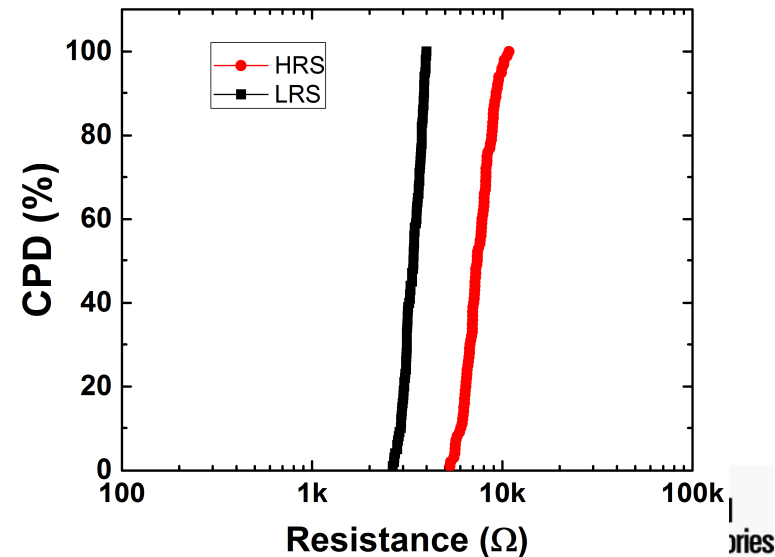
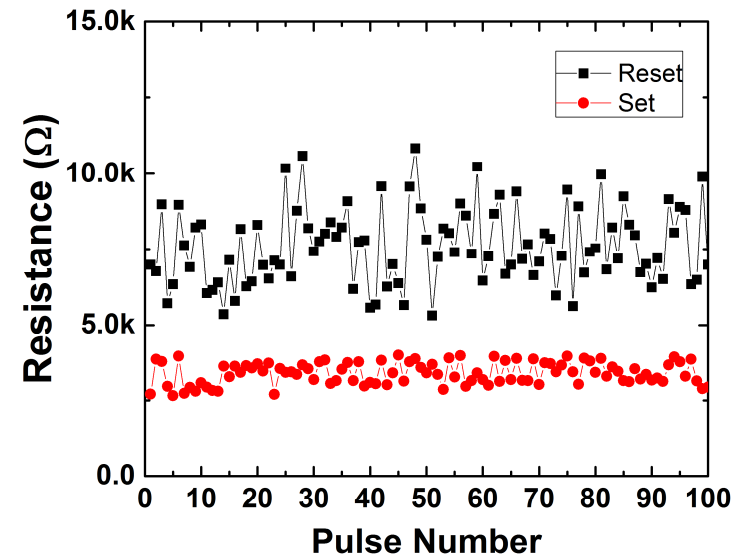
# Open Loop Cycling (Set)

- Based off the closed loops tests, a value of 1 V is used for an open loop test of the Set function
- The CPD for the LRS state has a larger spread of resistance values




# Open Loops Cycling (Reset)

- For the reset open loop, a value of -2 V was used
  - More spread and lower resistances than the closed loop
- Feedback from closed loop tests can continue to improve open loop results



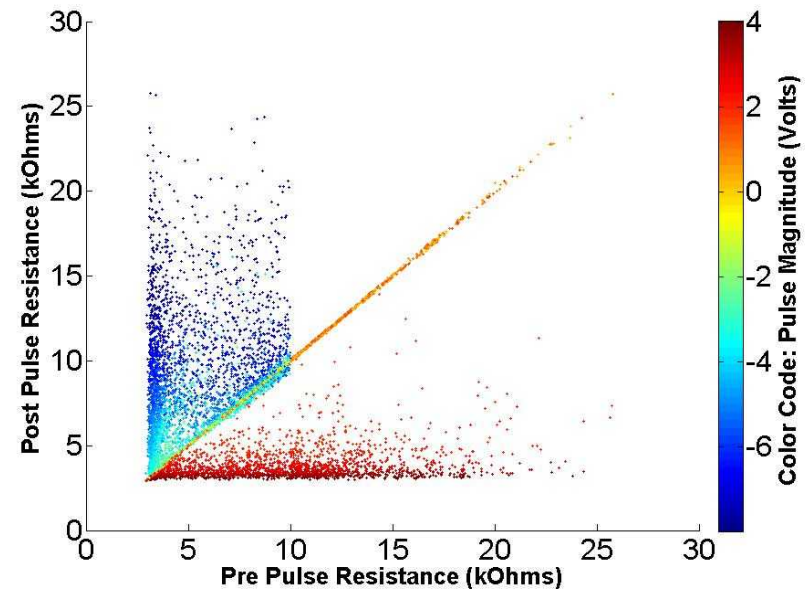
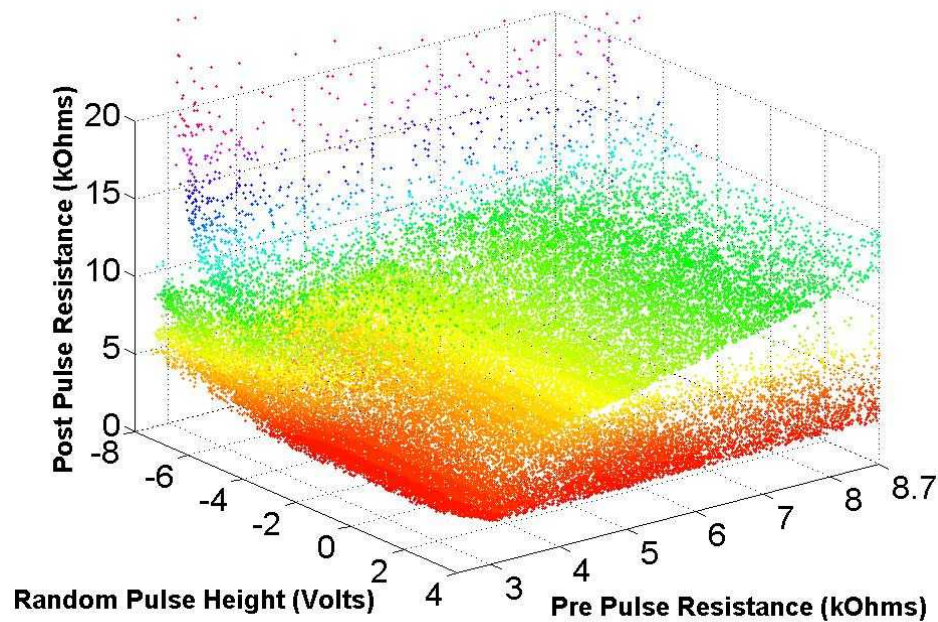
# Megasample collection method

- Use HP test board
  - Capable of reading or pulsing a given row-column pair
  - Voltage pulse time set to constant 2us
  - Read voltage level = 0.25V
  - 10 samples averaged per read
- Interleave voltage pulses and resistance readings: R V R V R V ...
- No attempt to force a particular starting resistance
- Careful control of voltage pulses to keep R within operating range
- 10M reads in working dataset
- Construction of table-based model
 


- Sliding window over readings
- Table has two axes:  $R_0$  and  $V$
- Cell size:  $100\Omega \times 0.1V$
- Cell contains change in resistance:  $D=R_1-R_0$

# Array Test Board

- Random pulse technique

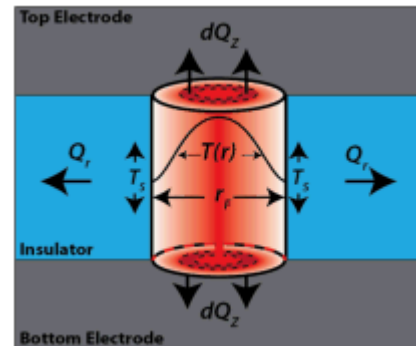
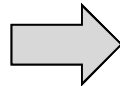
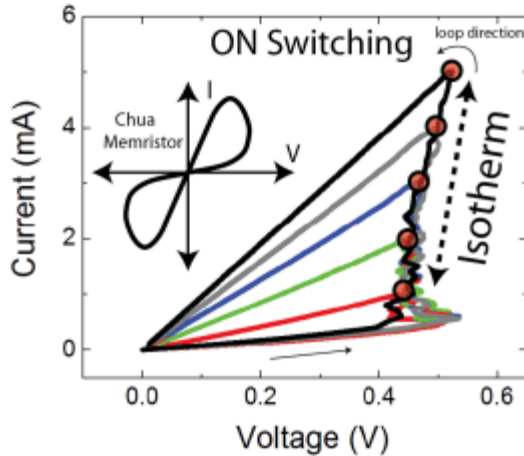


# Outline

- Neuromorphic Computing with ReRAM
- Development of a CMOS/ReRAM Process
- Characterization of Device Behavior
- Modeling the Source of Intradvice Variation
- Conclusion and Future Work

# Thermal Model

Isothermal signatures identified in IV data, which encouraged a thermal model

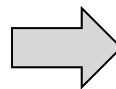


Approximation of heat equation for cylindrical filament gives temperature profile within the filament:

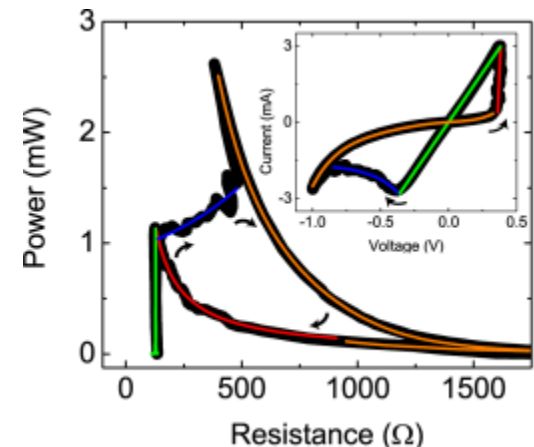
$$T(r) = T_{RT} + \frac{\sigma V^2 d_E}{2k_E d_O} \left[ 1 + \frac{k_E r_F^2 - 2r^2}{k_F 4 d_E d_O} \right]$$

Temperature can be transformed into electrical parameters of power and resistance:

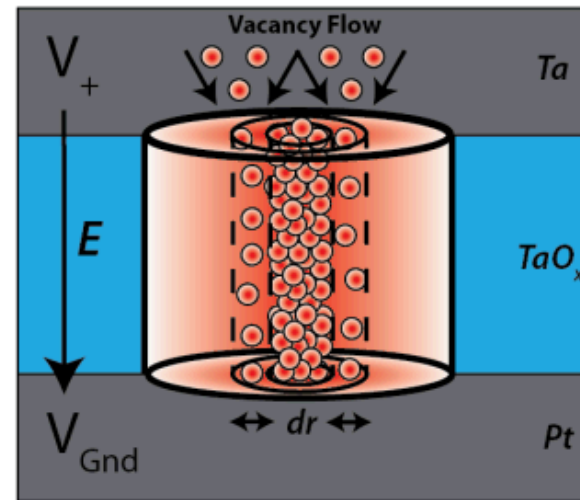
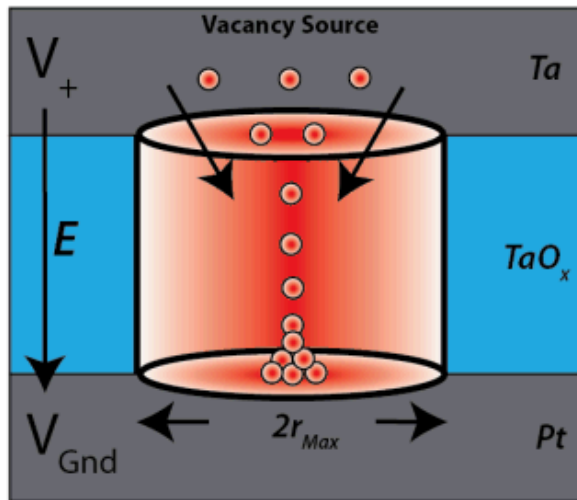
$$P = \frac{\Delta T / R}{\frac{d_E \sigma}{2k_E d_O} - \frac{r_F^2}{8L_{WF} T_{crit} d_O^2}}$$



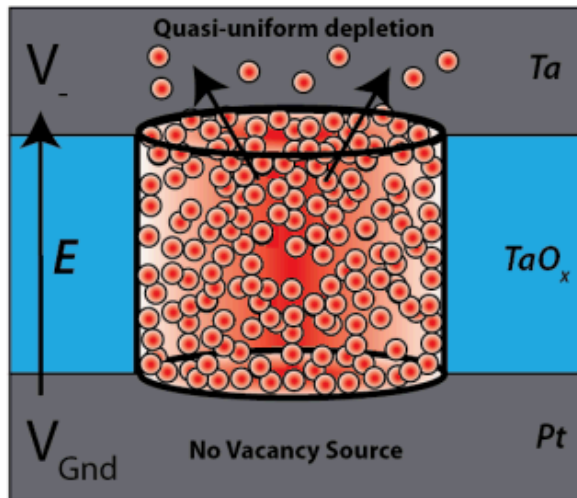
Quantitative agreement w/data



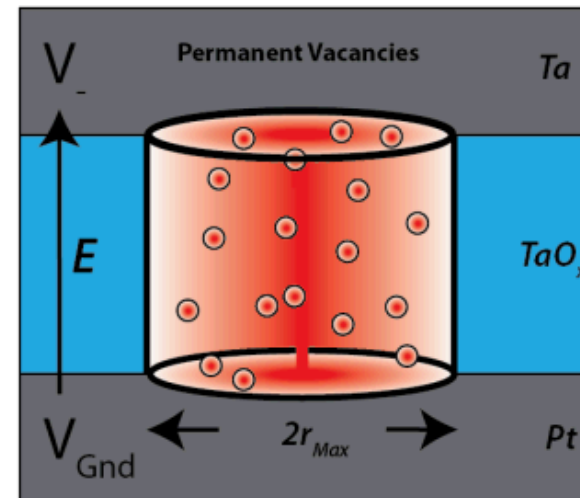
# Thermal Model



c)



d)





## Two State Variables

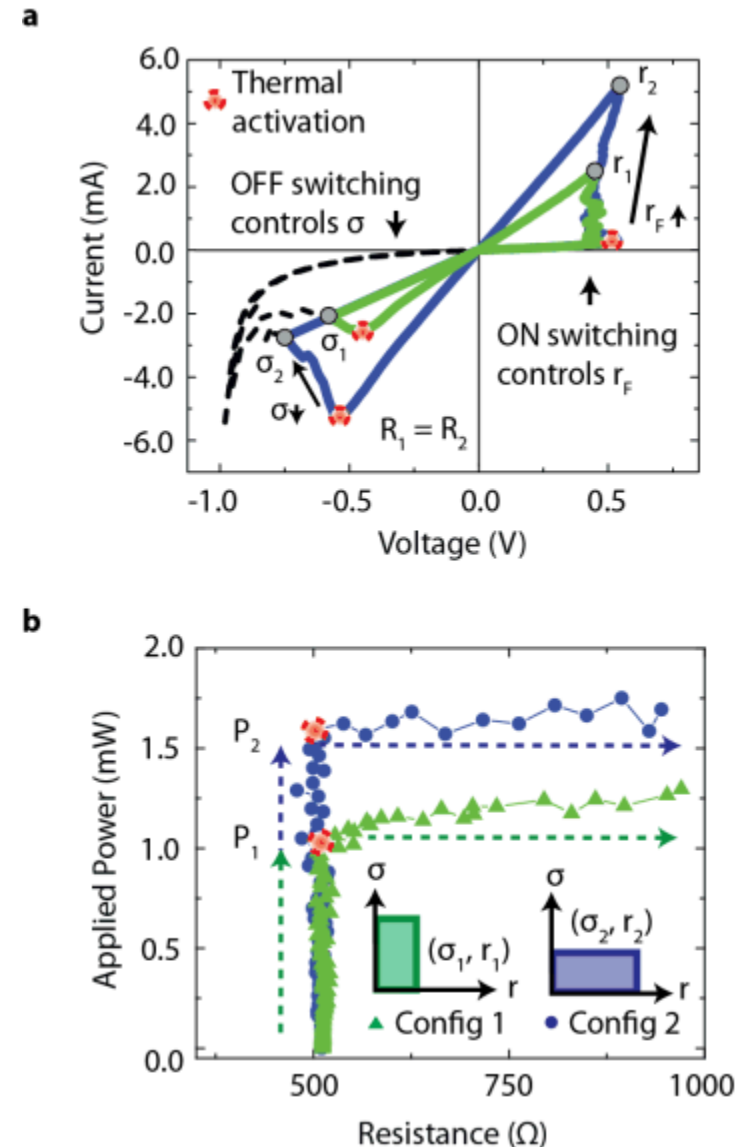
Independent control of  $\sigma$  and  $r$  means degenerate resistances can be set.

$$R = \frac{d_O}{\sigma \pi r_F^2}$$

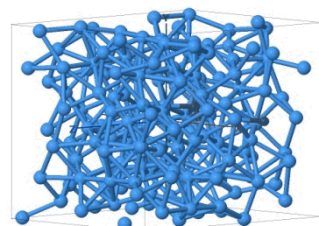
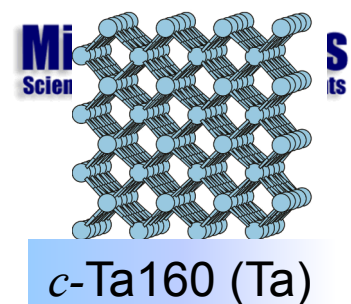
However, degenerate resistance states will activate at distinct applied powers

$$P = \frac{\Delta T / R}{\frac{d_E \sigma}{2k_E d_O} - \frac{r_F^2}{8L_{WF} T_{crit} d_O^2}}$$

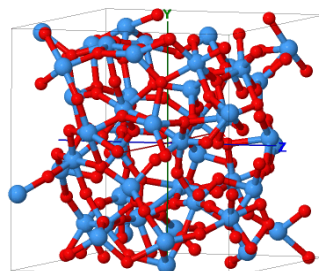
This additional parameter gives another “dimension” in which to encode analog or digital information



# Ta<sub>2</sub>O<sub>x</sub> Atomistic Structure Set



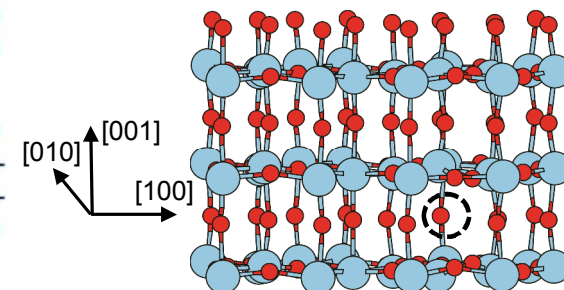
**α-Ta160O<sub>2</sub>**



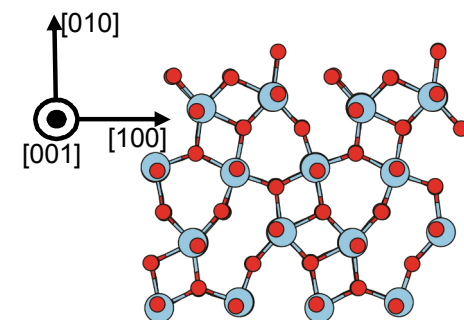
**α-Ta48O<sub>120</sub>**

Ta <sub>2</sub> O <sub>x</sub>		amorphous		
structure	x	O%	V <sub>O</sub> %	charge
α Ta160	0.00	0.0	n/a	0
α Ta160O1	0.01	0.6	n/a	0
α Ta160O2	0.03	1.2	n/a	0
α Ta160O3	0.04	1.8	n/a	0
α Ta152O8	0.11	5.0	n/a	0
α Ta144O16	0.22	10.0	n/a	0
α Ta128O32	0.50	20.0	n/a	0
α Ta112O48	0.86	30.0	n/a	0
α Ta80O80	2.00	50.0	n/a	0
α Ta48O84	3.50	63.6	30.0	0
α Ta48O96	4.00	66.7	20.0	0
α Ta48O108	4.50	69.2	10.0	0
α Ta48O114	4.75	70.4	5.0	0
α Ta48O117	4.88	70.9	2.5	0
α Ta48O117	4.88	70.9	2.5	2+
α Ta48O118	4.92	71.1	1.7	0
α Ta48O118	4.92	71.1	1.7	2+
α Ta48O119	4.96	71.3	0.8	0
α Ta48O119	4.96	71.3	0.8	1+
α Ta48O119	4.96	71.3	0.8	2+
α Ta48O120	5.00	71.4	0.0	0

Ta <sub>2</sub> O <sub>x</sub>		crystalline		
structure	x	O%	V <sub>O</sub> %	charge
c Ta160	0.00	0.0	n/a	0
c Ta160O1	0.01	0.6	n/a	0
c Ta160O2	0.03	1.2	n/a	0
σ <sub>0,xx</sub> , c-Ta <sub>2</sub> O <sub>5</sub>				
c Ta48O119	4.96	71.3	0.8	0
c Ta48O119	4.96	71.3	0.8	1+
c Ta48O119	4.96	71.3	0.8	2+
c Ta48O120	5.00	71.4	0.0	0
σ <sub>0,yy</sub> , c-Ta <sub>2</sub> O <sub>5</sub>				
c Ta48O119	4.96	71.3	0.8	0
c Ta48O119	4.96	71.3	0.8	1+
c Ta48O119	4.96	71.3	0.8	2+
c Ta48O120	5.00	71.4	0.0	0
σ <sub>0,zz</sub> , c-Ta <sub>2</sub> O <sub>5</sub>				
c Ta48O119	4.96	71.3	0.8	0
c Ta48O119	4.96	71.3	0.8	1+
c Ta48O119	4.96	71.3	0.8	2+
c Ta48O120	5.00	71.4	0.0	0



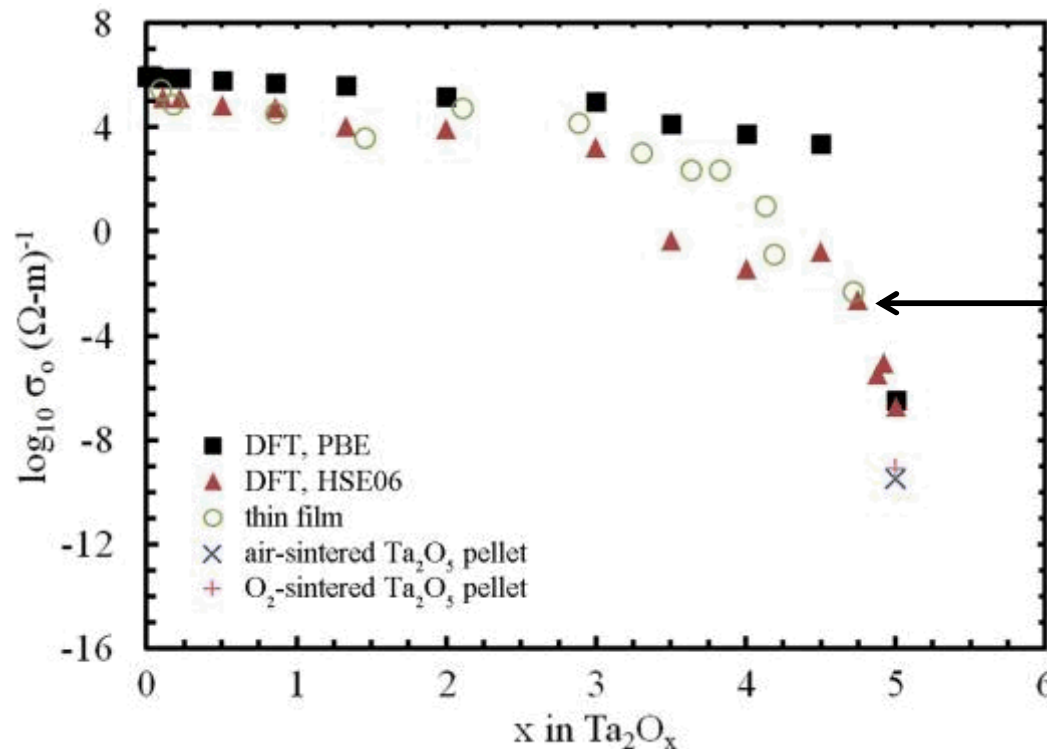
**c-Ta48O119 (V<sub>O</sub><sup>2+</sup>)**



**c-Ta48O120 (Ta<sub>2</sub>O<sub>5</sub>)**

- Ta<sub>2</sub>O<sub>x</sub> structure library generated for conductivity calculations
- Parameter space samples composition, phase, temperature, and charge state

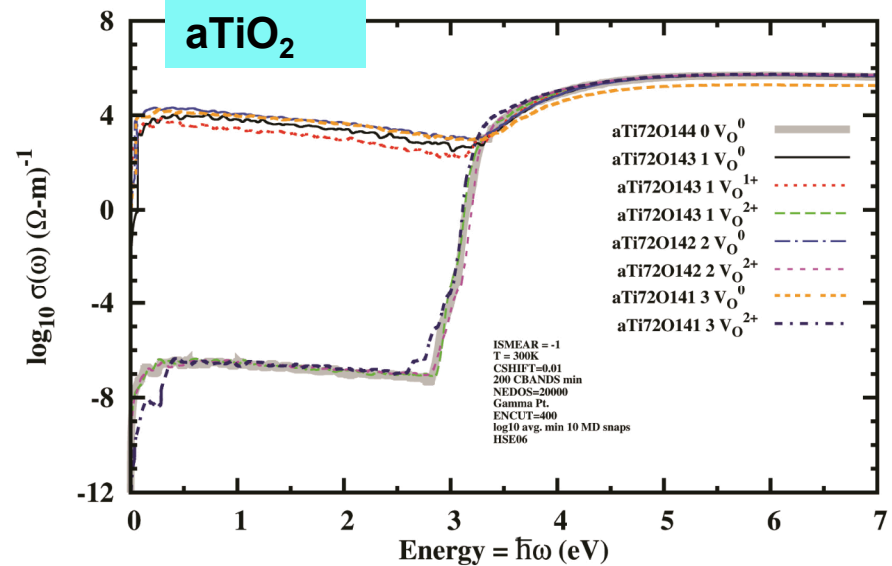
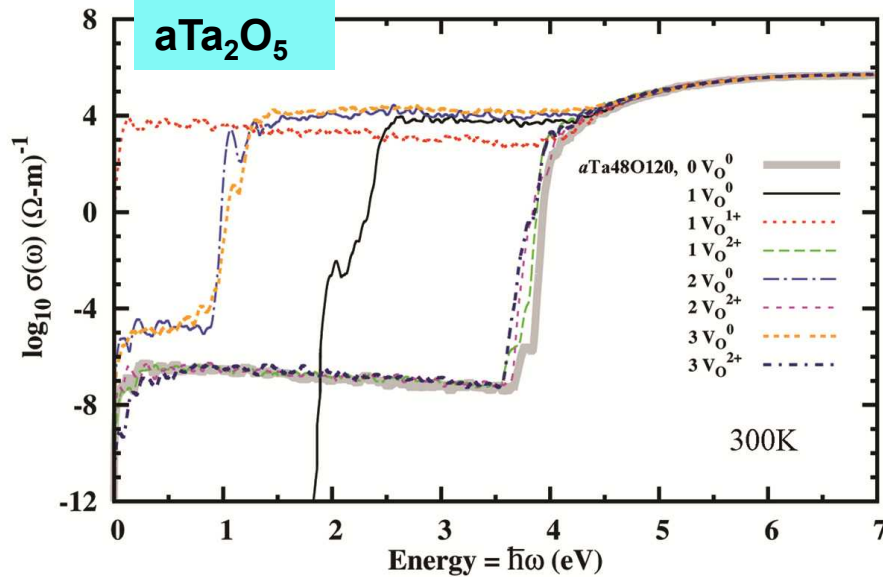
# DFT vs. Experiment: $\alpha$ -Ta<sub>2</sub>O<sub>x</sub> $\sigma$



DFT outlier at  $x=4.75$  joins trend with increased sampling ( $\log_{10} \sigma_0$  decreases from 3.5 to -2.6)

- DATA:  $T=300K$ ; DFT conductivities sampled at 0.5 ps intervals on minimum 12-14 (6) configuration snapshots for PBE (HSE06) functionals; MESA thin film resistivities measured with 4-pt probes; Ta<sub>2</sub>O<sub>5</sub> pellets used to assess true bulk resistivity
- Sampling additional independently-quenched amorphous structures at each composition improves DFT trends (outlier at  $x=4.75$  used as test case)
- DFT overestimation of  $\sigma_0$  is evident at  $x=5$  (finite cell sizes are in part responsible)

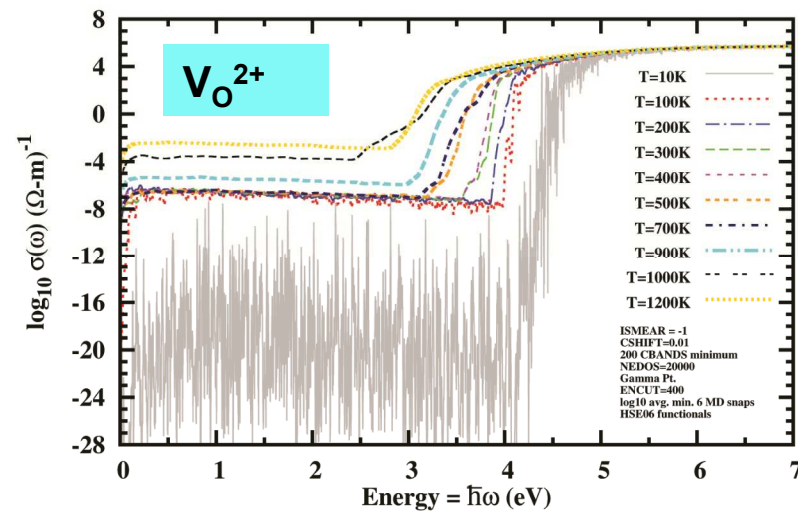
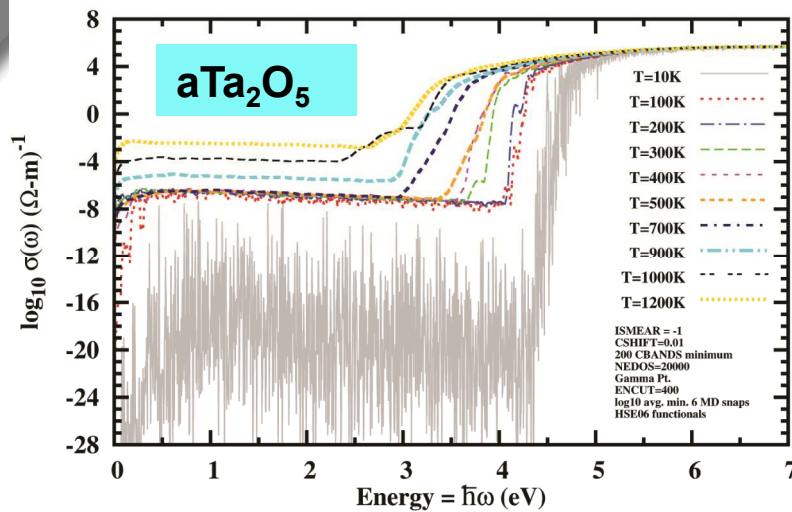
# Conductivity: Oxidation State



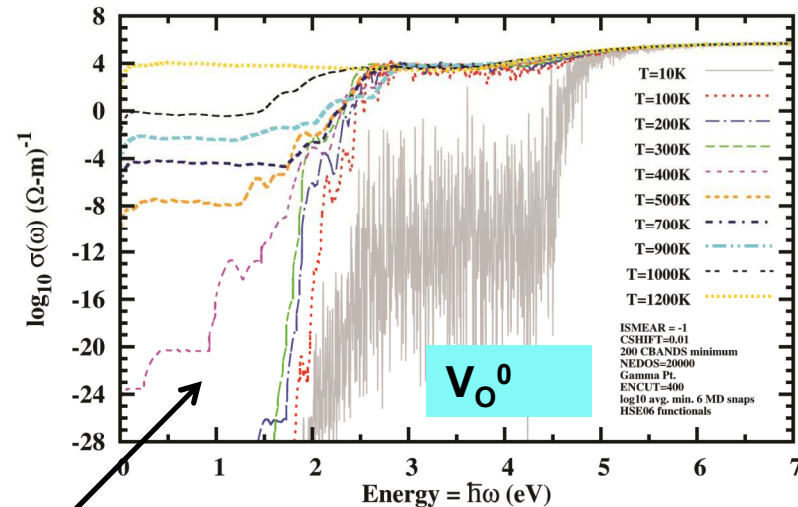
- **DATA: 300K, HSE06 functionals**
- Rough Ta<sub>2</sub>O<sub>5</sub> trend established for increasing  $\sigma_0$  as V<sub>O</sub><sup>0</sup> conc. increases (dopant-like behavior)
- Influence of V<sub>O</sub><sup>n</sup> (n=0,1<sup>+</sup>,2<sup>+</sup>) oxidation state is significant;  $\sigma(\omega)$  responses for all n = 2<sup>+</sup> cases essentially indistinguishable from stoichiometric oxides
- Possible that oxidation/reduction reactions are involved in memristor switching that effectively act as dopant deactivation/activation mechanisms for V<sub>O</sub><sup>0</sup>.



# Ta<sub>2</sub>O<sub>x</sub> Conductivity: T and Vacancies

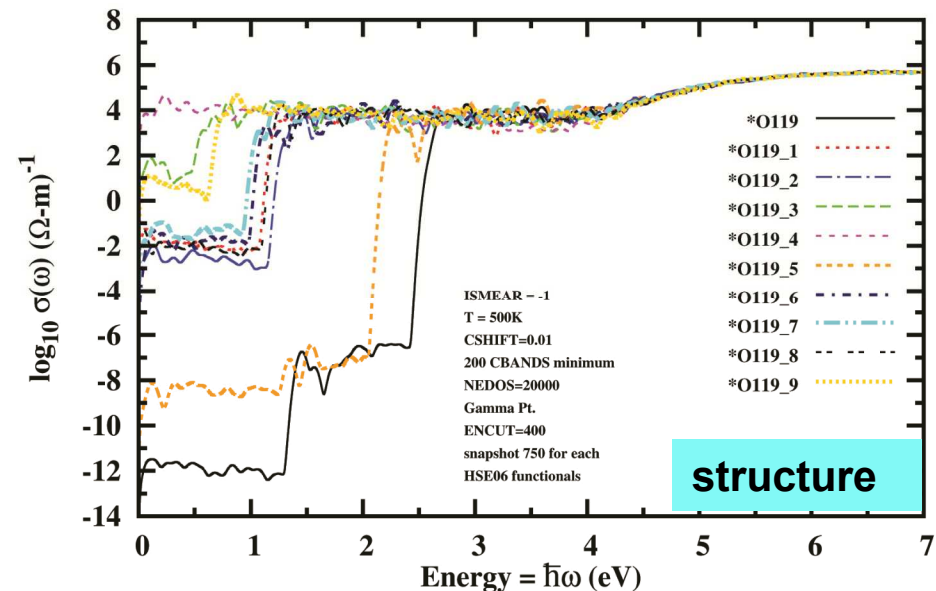
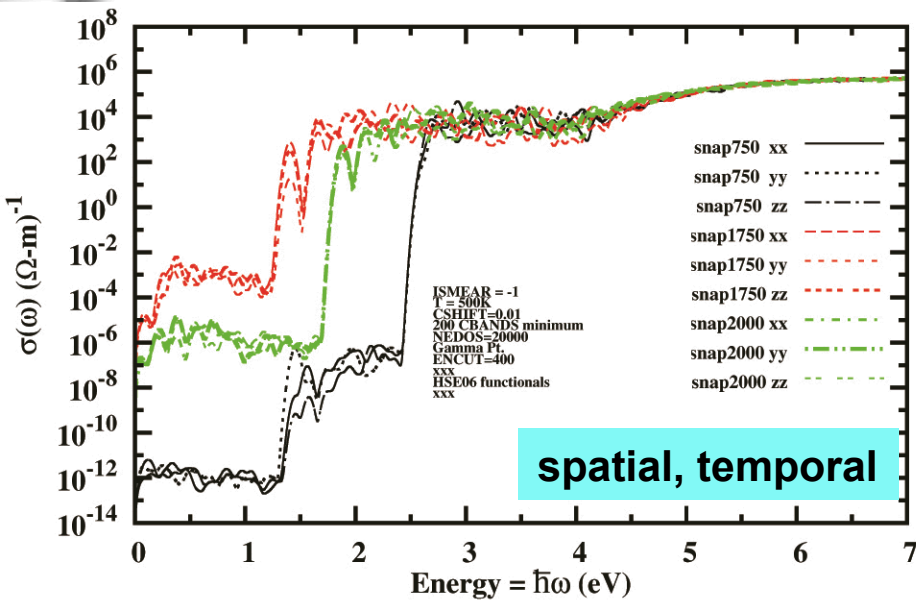


- DATA:** 168-atom basis supercells, HSE06 functionals, 6 QMD configs. sampled at each of 10 to 11 temps., noisy gray curves are low T reference (10K)
- T dependence for stoich. oxide and V<sub>O</sub><sup>2+</sup> case are very similar, while V<sub>O</sub><sup>0</sup> case is much different
- V<sub>O</sub><sup>0</sup> case exhibits stronger T-dependence of  $\sigma_o$  than other cases

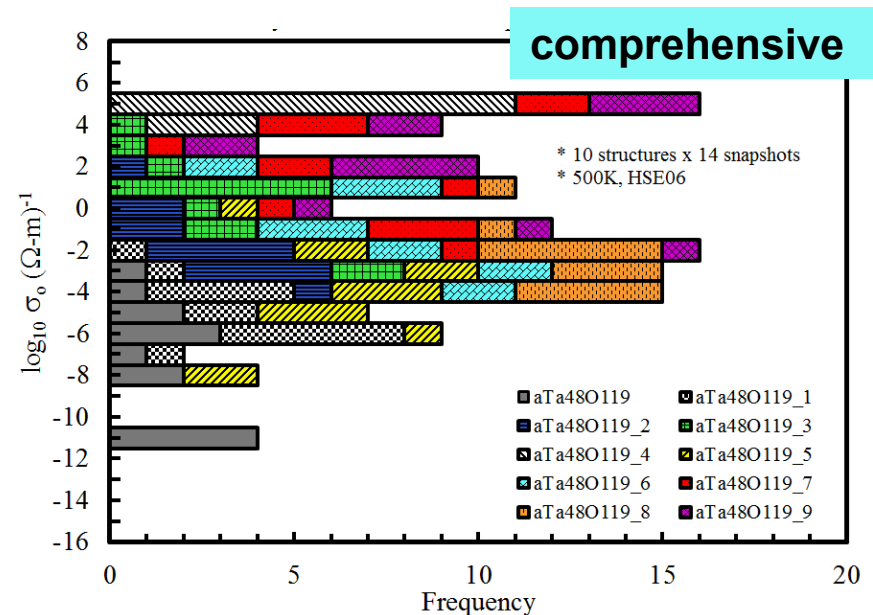


V<sub>O</sub><sup>0</sup> shows transition from zero  $\sigma_o$  to finite  $\sigma_o$  between 300 and 400 K. This is suggestive of “freeze-out” dopant behavior.

# Statistical Contributions to Nanoscale $\sigma$



- **DATA:** 167-atom amorphous supercells containing 1  $V_O^0$ , HSE06 functionals,  $T=500K$
- **Spatial variation:** 1-2 orders of magnitude in  $\sigma_o$
- **Temporal variation:** 9-10 orders of magnitude in  $\sigma_o$
- **Structural variation:** 16 orders of magnitude in  $\sigma_o$
- **Anisotropy in  $\sigma_o$**  relatively small effect at nanoscale







# Outline

- Neuromorphic Computing with ReRAM
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## Conclusions

- Neuromorphic computing is superior to traditional computing for certain applications, especially those involving pattern recognition
- Execution of certain neuromorphic algorithms can be significantly improved using a custom analog-mode CMOS/ReRAM accelerator
- Metal Oxide ReRAM cells have relatively high cycle to cycle variability, which may significantly limit the resolution of an analog accelerator
- Possible physical origins have been studied using analytical and DFT models and two reasons hypothesized:
  - Degenerate resistance states
  - Different same-stoichiometry makeup



# Acknowledgements

- **This project was funded in part by Sandia's Laboratory Directed Research and Development (LDRD) Program**
- **Useful discussions with our collaborators at HP Labs, esp. Jianhua Yang, Yoocharn Jeon, John Paul Strachan, Si-Ty Lam, Brent Buchanan, Dick Henze, and Stan Williams**

# Backup Slides



# Neural Hardware Simulation

- **Greatest challenge is to generate row and column pulses that train memristors correctly.**
- **Both write noise and bin size are 6 orders of magnitude larger than weight update.**
- **Training curve of memristor contains highly sensitive “cliff” in one direction.**



# Neural Hardware Simulation

- **Methods:**
- **Direct conversion** – Compute all weights using float. Simply write resistance values into simulated crossbar without “burning” them. **Works.**
- **Direct set** – Store weights as resistances, but do all math in float. **Works.**
- **Isolated pulse** – Apply a voltage pulse to each memristor in isolation to set it. **Works**
- **Binary** – Pulse all rows and columns at once. Voltage is minimal fixed increment. Only applied if given row had error or given column had input. **Diverges.**
- **Binary Row** – Similar to binary, but only pulse row with largest error. **Diverges.**

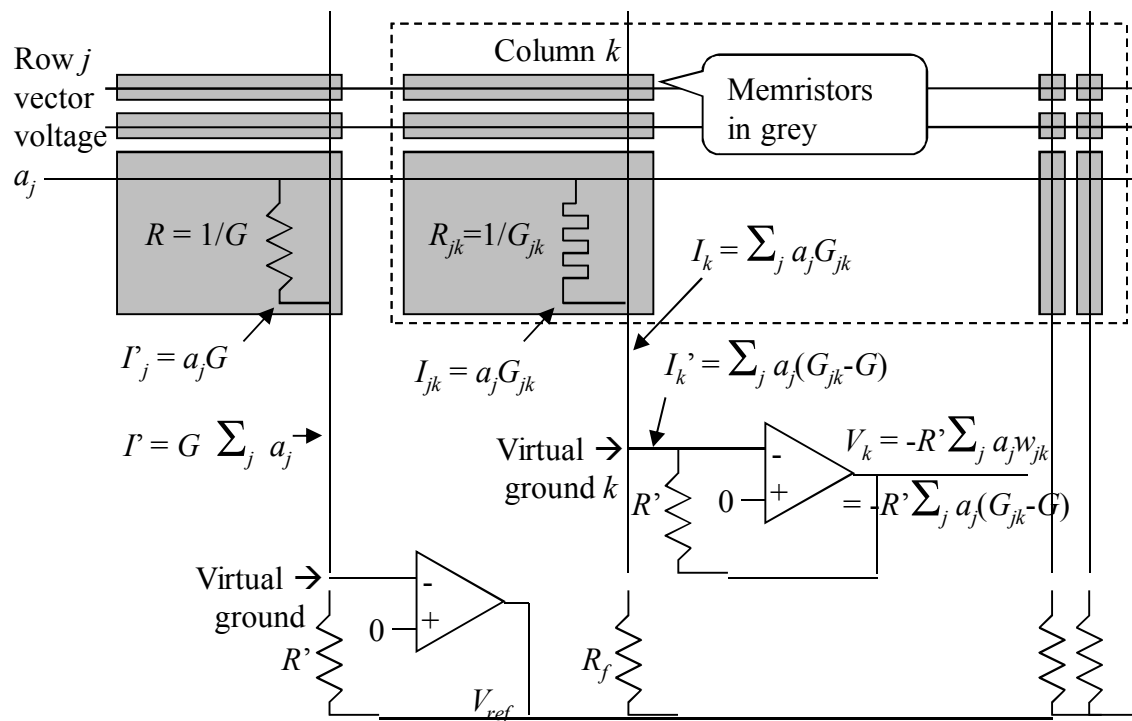




# Neural Hardware Simulation

- **Methods (continued):**
- **Linear Row – Pulse only the row with largest error, but use a scaling factor to convert error to voltage. Works.**
- **Linear Rows – Pulse each row separately, using same method as Linear Row. Works.**
- **Linear – Pulse all rows and columns at once, using scaling factor to convert input or error to voltage. Diverges.**
- **Polynomial – Similar to Linear, but use polynomial fit of memristor data with one real exponent. Diverges.**

# ReRAM Neural Circuit





# Emerging Memory

- This is a great era for emerging memory
- NAND Scaling is visibly slowing
  - Memory manufacturers refusing to name nodes by physical dimensions (now we have 2x and 1x nodes)
  - 16 nm retention and endurance degraded
  - 3D will quench density issues temporarily
- DRAM scaling is also becoming a problem
  - struggling to maintain reasonable equivalent oxide thickness
  - Dielectric for cells 30nm to 20 nm still TBD
- **Opportunity: Storage Class Memory**
  - Magnetic to DRAM latency gap
- New memory technologies on the horizon are rapidly maturing which can replace NAND *and* DRAM

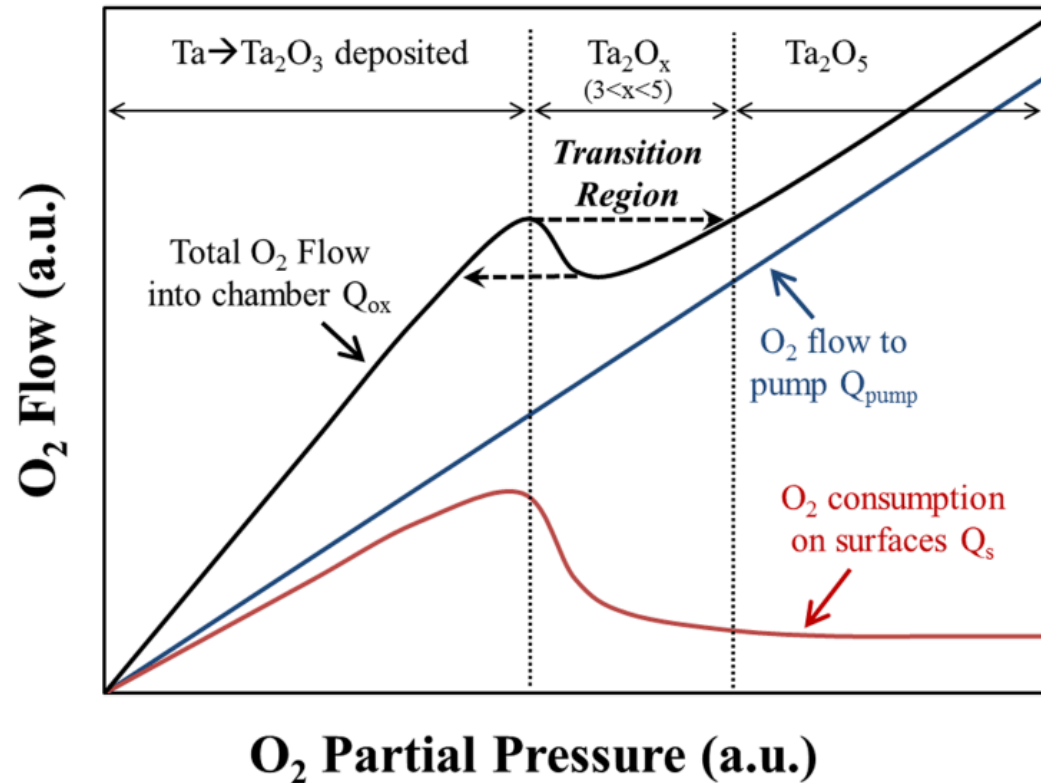


# Categorization of ReRAM

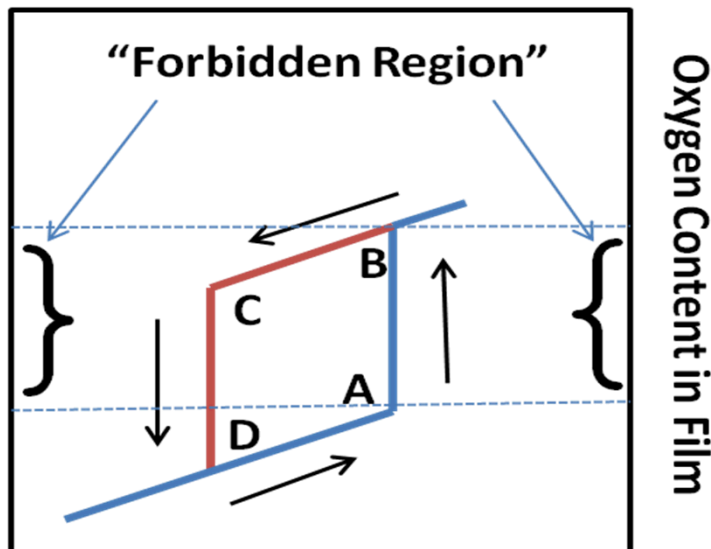
- **Electrochemical Metallization Bridge (CBRAM)**
  - Bipolar
  - Cation motion
  - Ag or Cu filament
- **Metal Oxide: Bipolar Filamentary**
  - Current independent of area
  - Anion (oxygen vacancy) motion
  - Valence change dominates
- **Metal Oxide: Unipolar Filamentary**
  - Current independent of area
  - Thermochemical mechanism dominates
- **Metal Oxide: Bipolar Non-filamentary**
  - Current depends on area
  - Anion motion near interface

# Switching Film Development: Overcoming the “Forbidden Region”

- Forbidden oxygen flow-pressure region occurs due to target poisoning
- This is the region we need to be in to get ideal ReRAM stoichiometry



J.E. Stevens et al, accepted for publication  
by J. Vac Sci. Tech., 2013.



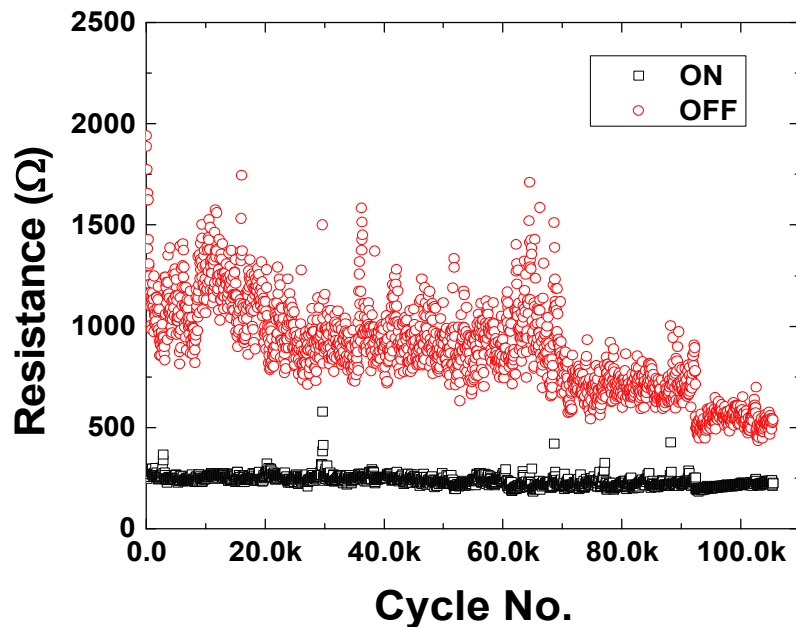
Oxygen Flow

A.J. Lohn et al APL 103, 063502 (2013)

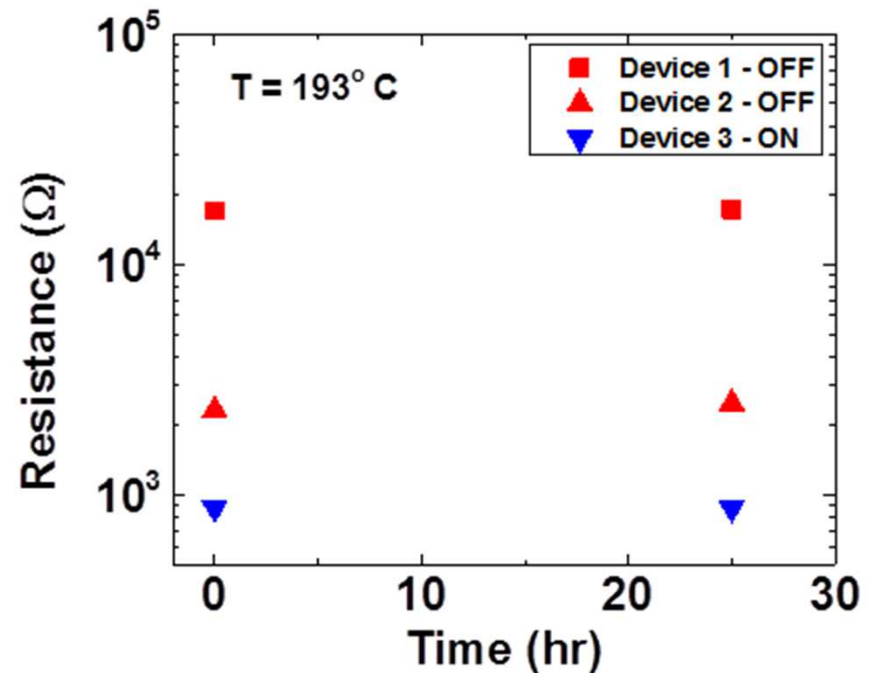
# Endurance and Retention

- Basic characteristics

## Endurance



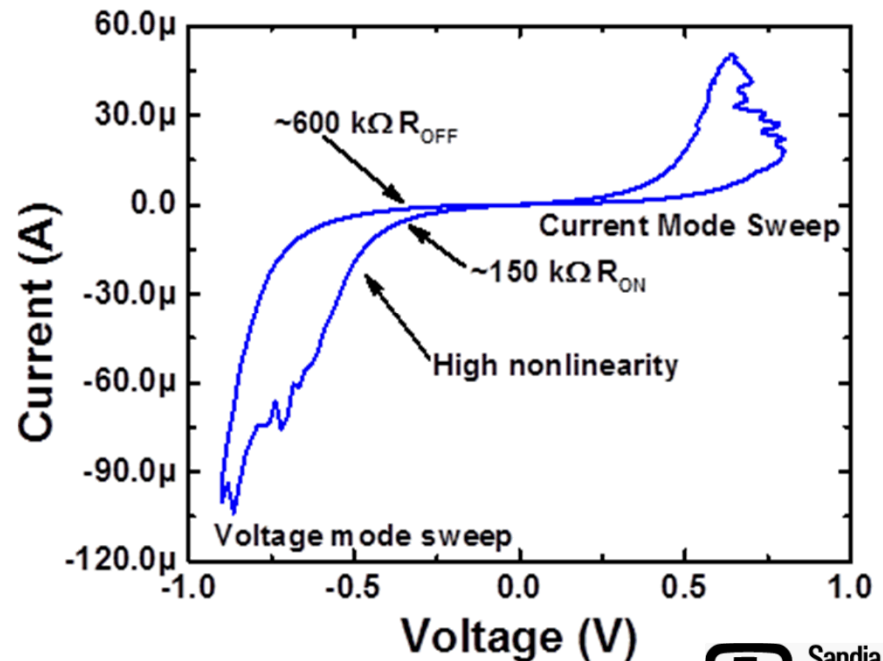
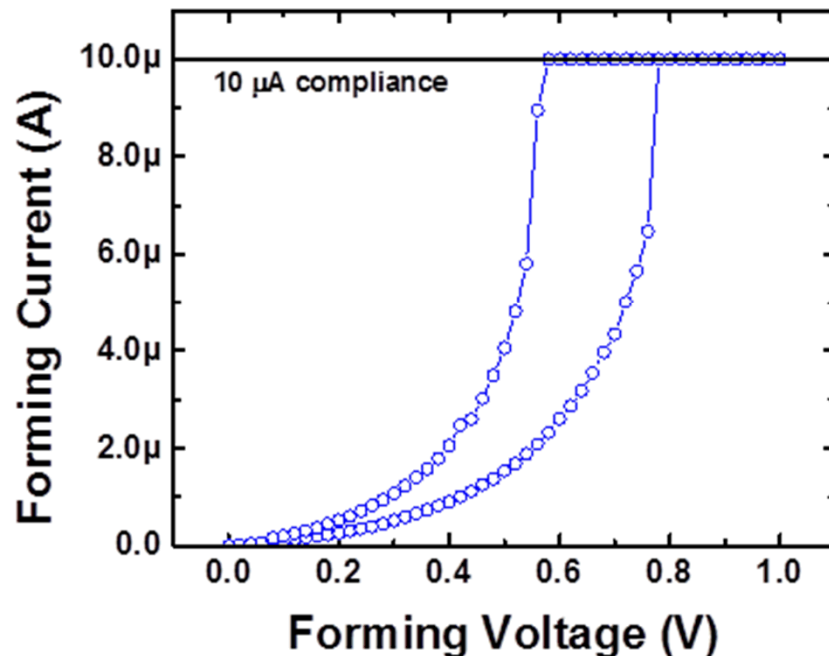
## Retention





# High Resistance Behavior

- Significant performance improvement can be achieved by careful electrical forming and control
- Power limited switching
- Very high resistance and  $R_{\text{OFF}}/R_{\text{ON}}$  possible (~100 mV read)



# Analog Computing

- Vector matrix operations often comprise  $\gg 90\%$  of operations in pattern matching algorithms
- A monolithically integrated memristor accelerator can greatly improve power and throughput for these operations
- This could comprise a node of a future HPC system

