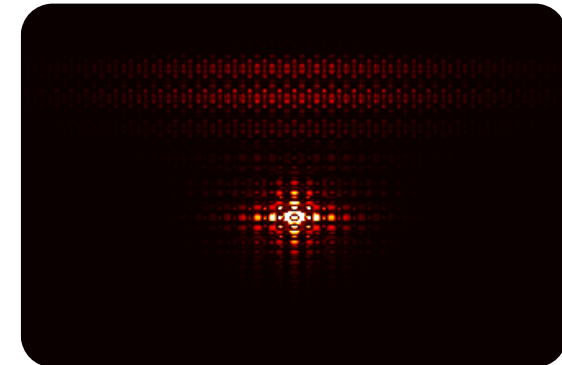
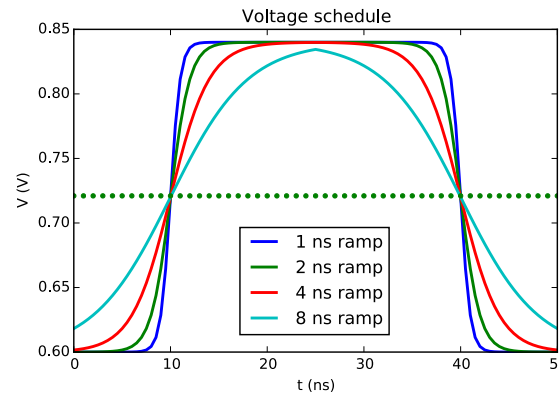
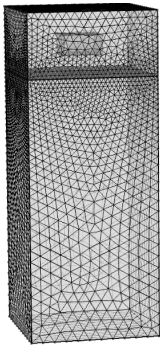


Exceptional service in the national interest

Multi-valley effective mass theory for device-level modeling of open quantum dynamics



Collaborators:

John K. Gamble, Andrew Baczewski,
Wayne Witzel, Inès Montañó, Erik Nielsen, Rick Muller – *Sandia*
Adam Frees – *Univ. Wisconsin-Madison*

Toby Jacobson

Sandia National Laboratories



U.S. DEPARTMENT OF
ENERGY



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Modeling device *operation* requires dynamics

Multi-valley effective mass theory: [Gamble, et al. [arXiv:1408.3159](#)]

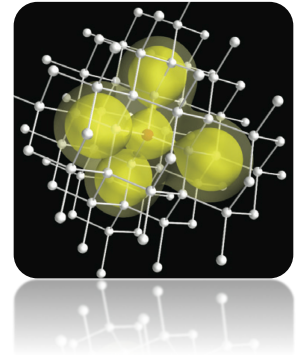
Cartesian Gaussian basis

Central cell correction tuned-up for P in Si

Inhomogeneous strain (a la [Herring & Vogt, Phys Rev 1956])

Realistic electrostatic potentials (from e.g. QCAD, COMSOL)

Electron-phonon coupling



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Multi-valley effective mass theory: [Gamble, et al. [arXiv:1408.3159](#)]

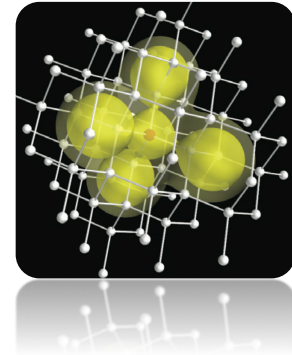
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Central cell correction tuned-up for P in Si

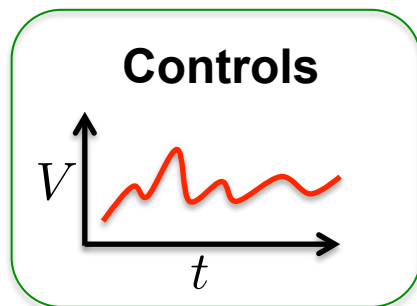
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extending this framework into the time domain...



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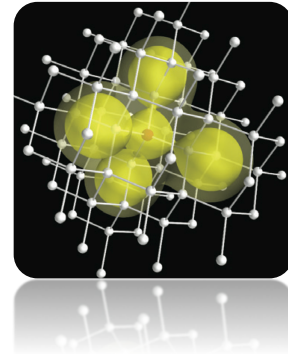
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Central cell correction tuned-up for P in Si

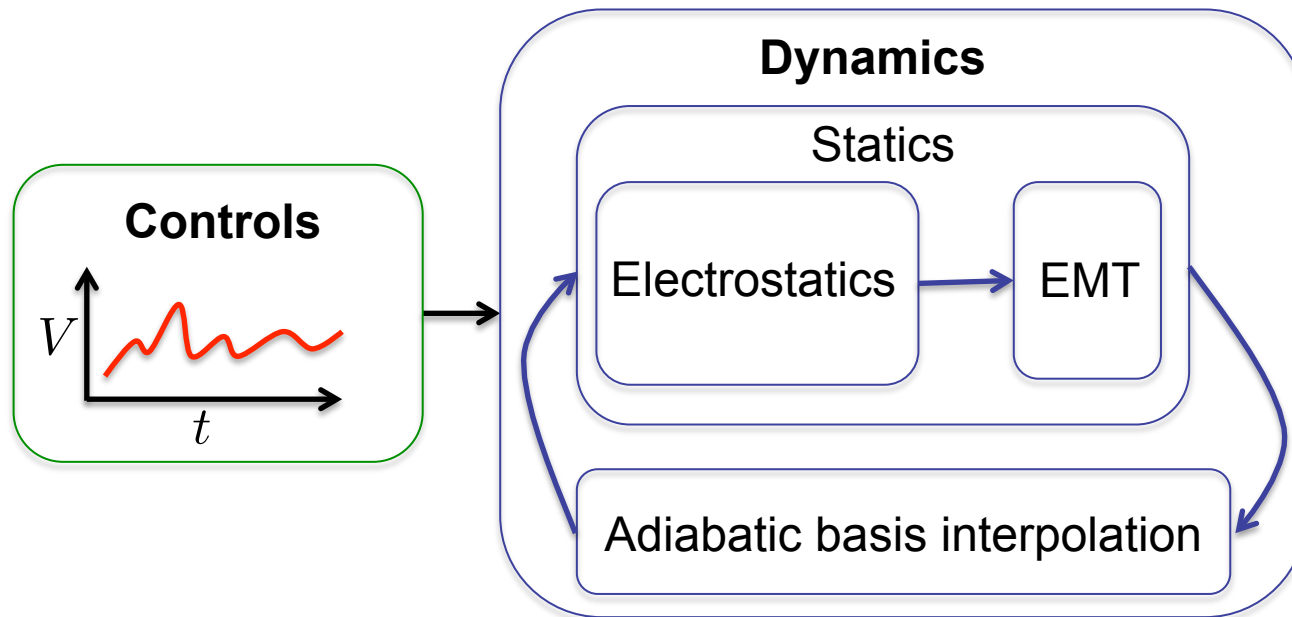
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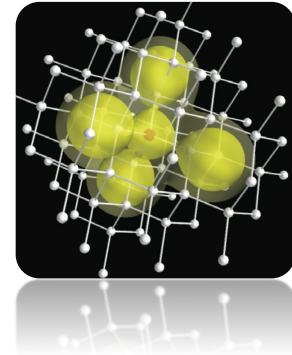
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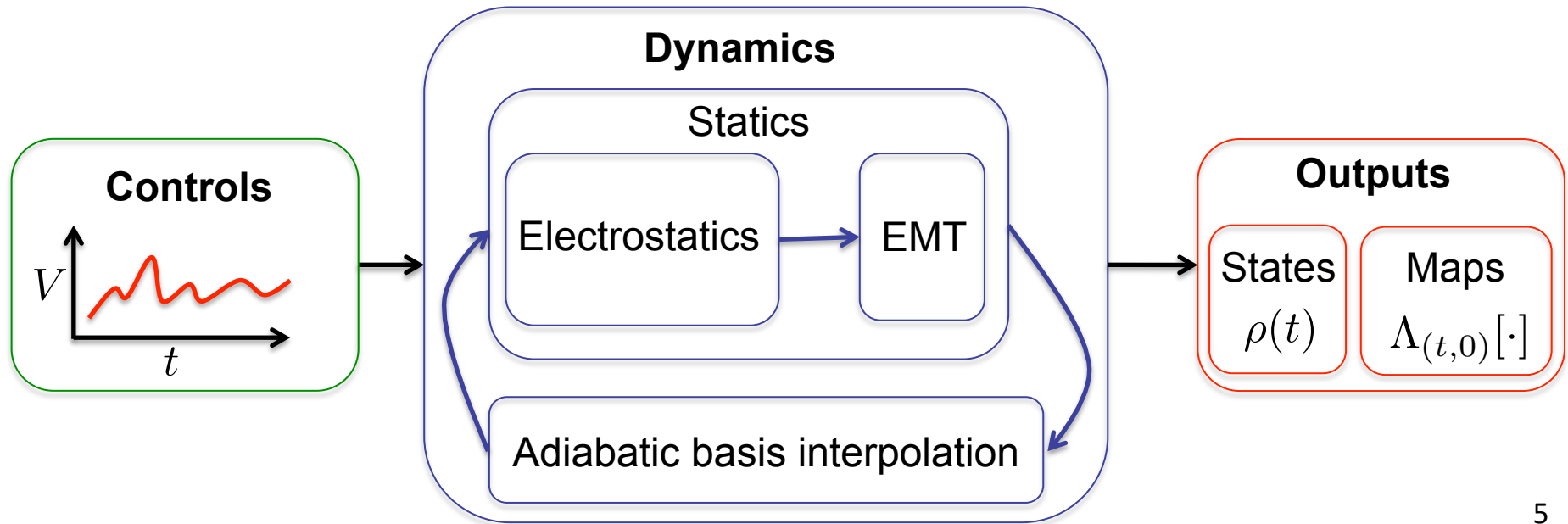
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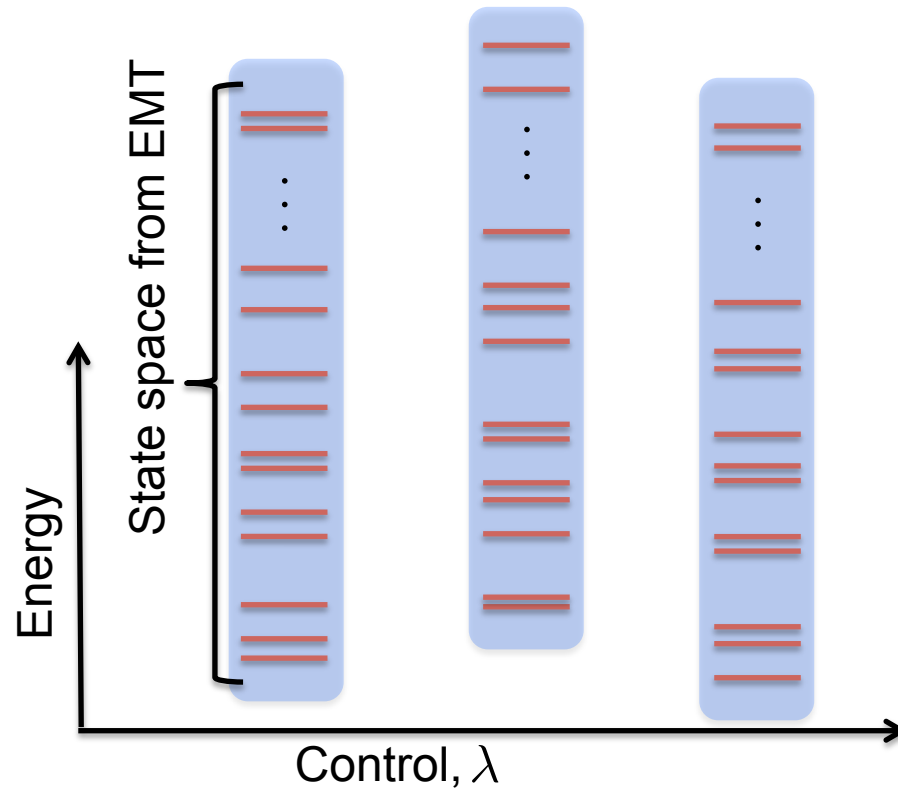
Electron-phonon coupling



extending this framework into the time domain...



Dynamics framework

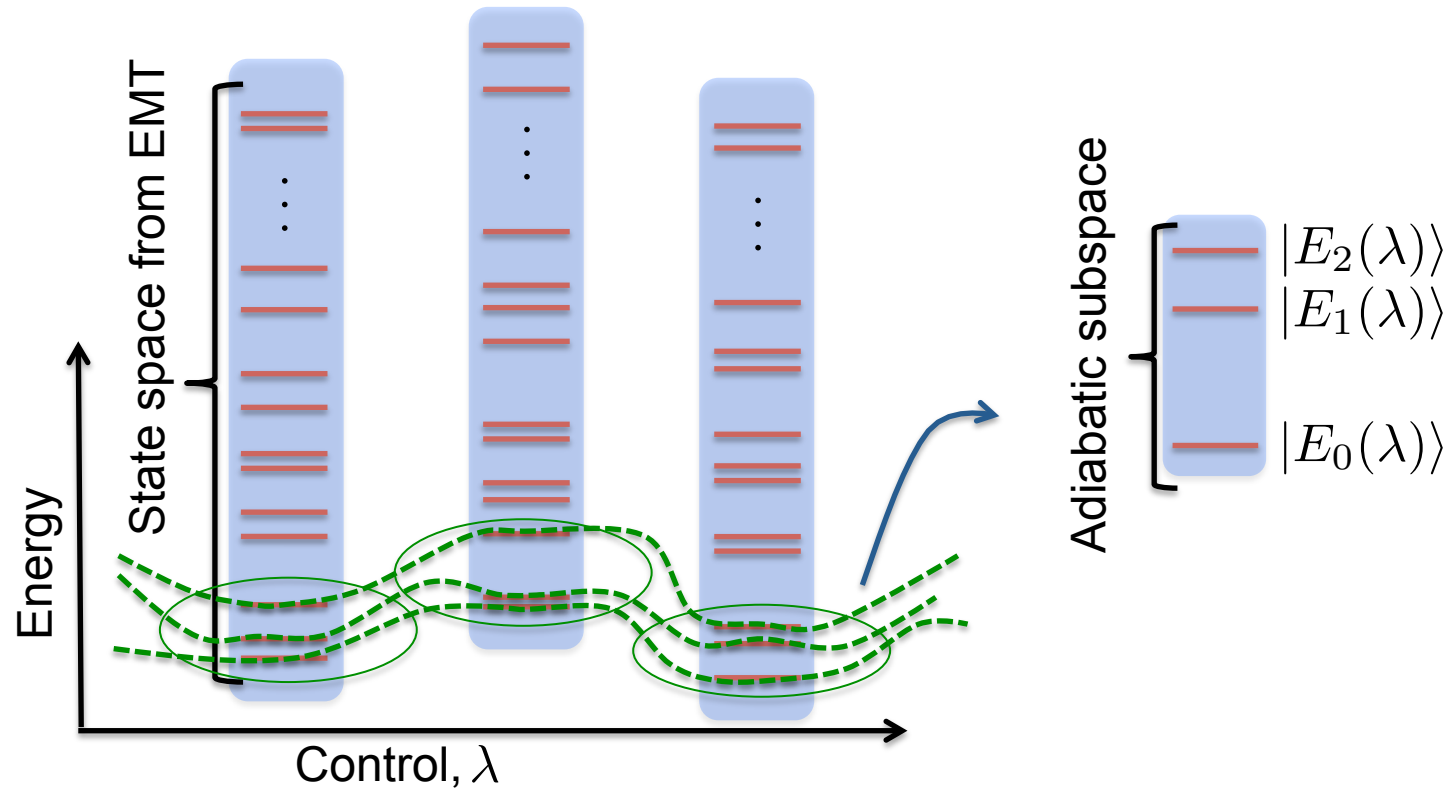


Equation of motion:

Time-local master equation

$$\dot{\rho} = -\frac{i}{\hbar} [H(t), \rho] + \mathcal{D}_t\{\rho\}$$

Dynamics framework



Equation of motion:

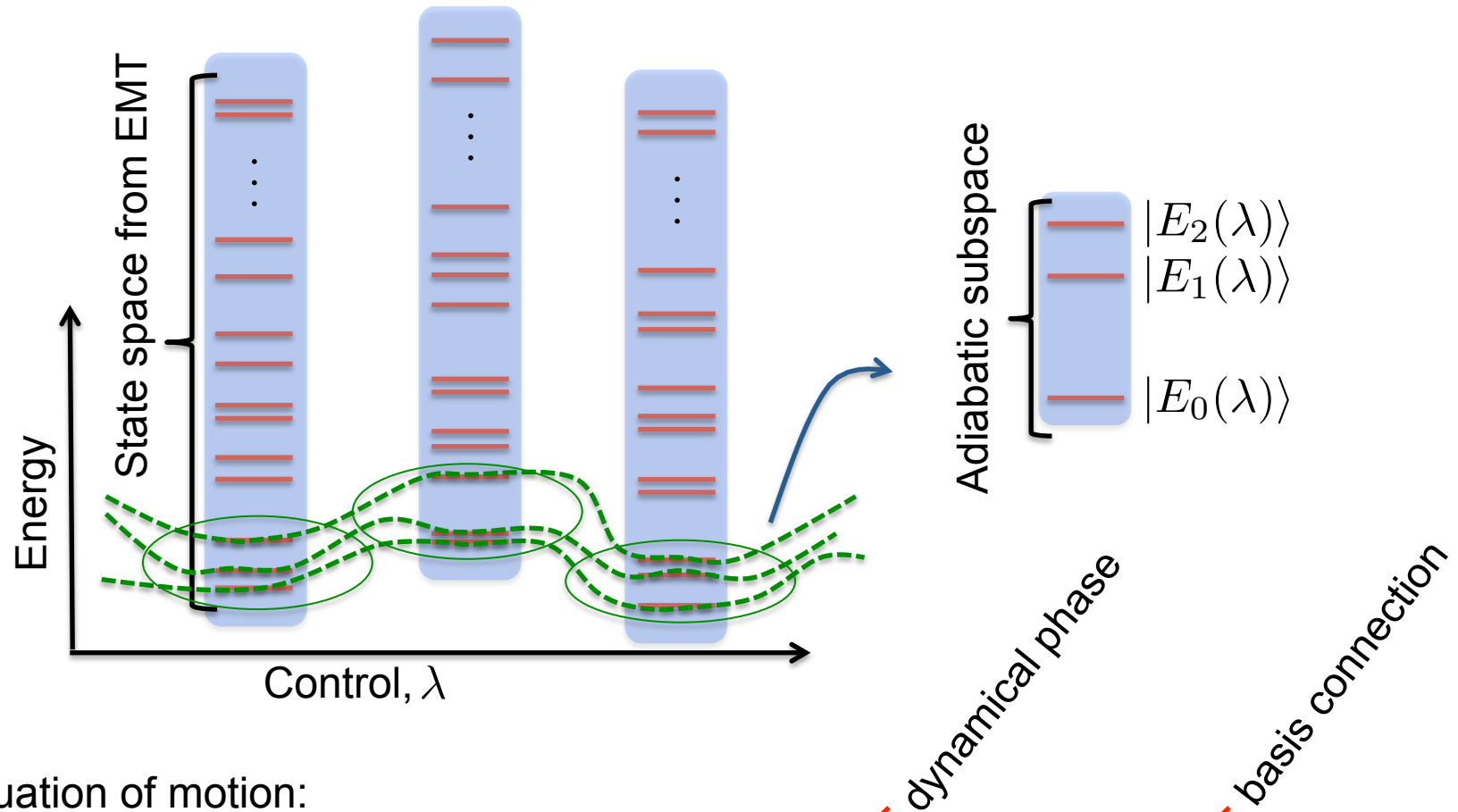
Time-local master equation

$$\dot{\rho} = -\frac{i}{\hbar} [H(t), \rho] + \mathcal{D}_t\{\rho\}$$

...within instantaneous low-energy subspace

$$\dot{\tilde{\rho}} = -\frac{i}{\hbar} [\mathbf{E}(t), \tilde{\rho}] + \{\dot{\lambda}(t) \cdot \mathbf{B}(t), \tilde{\rho}\} + \mathcal{D}_t\{\tilde{\rho}\}$$

Dynamics framework



Equation of motion:

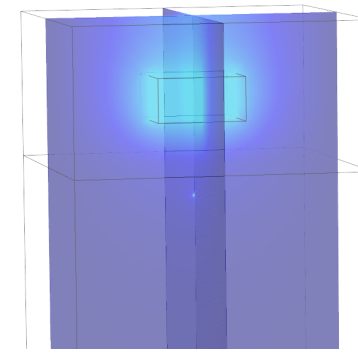
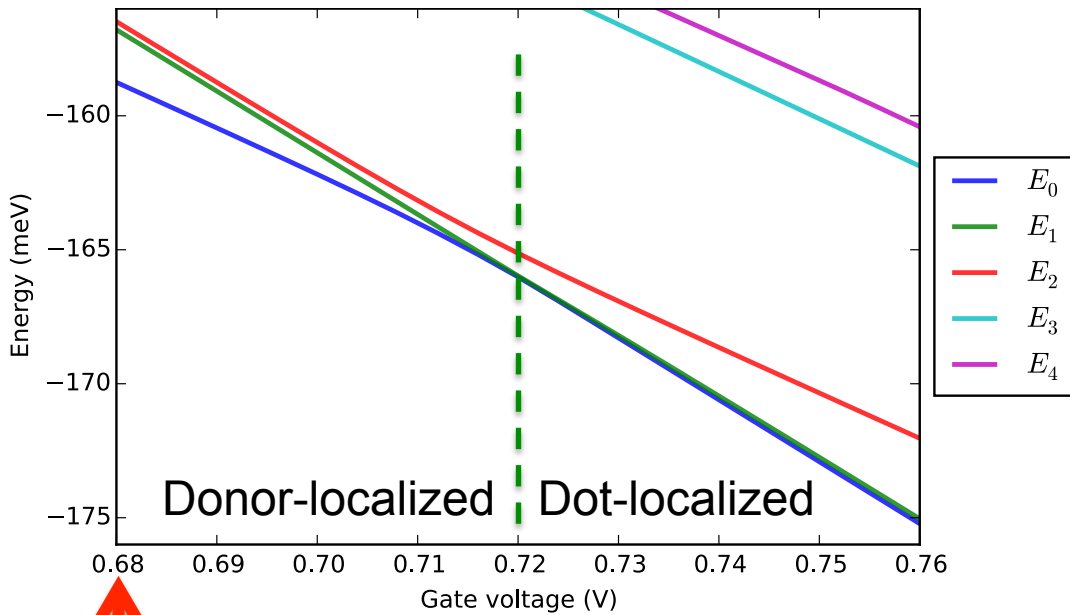
Time-local master equation

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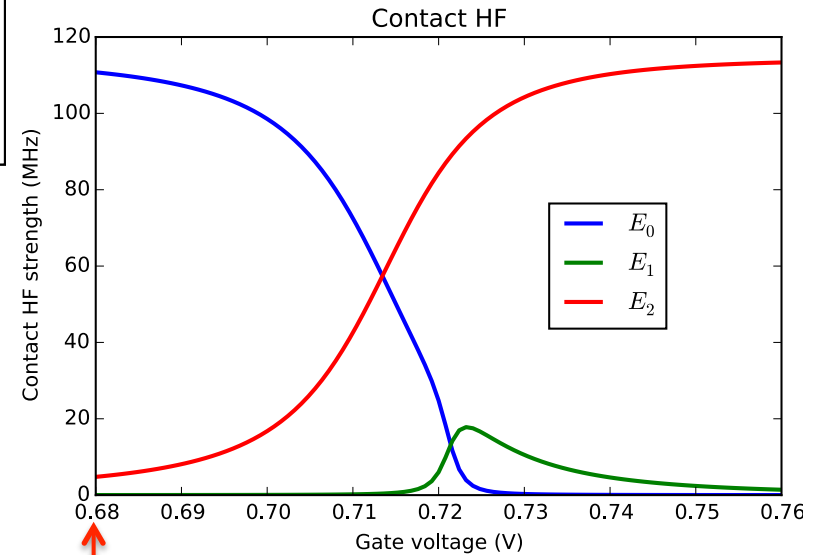
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Shuttling between donor and interface dot



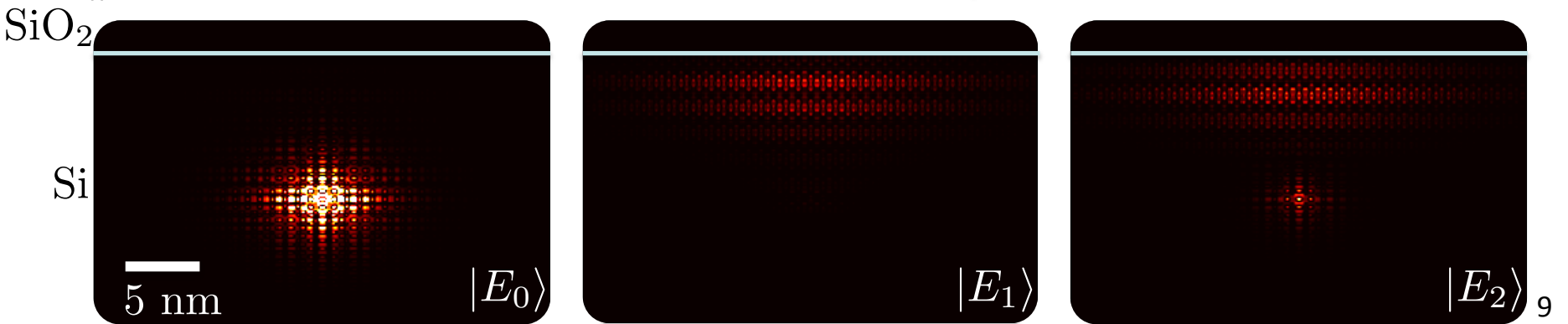
0.68 V



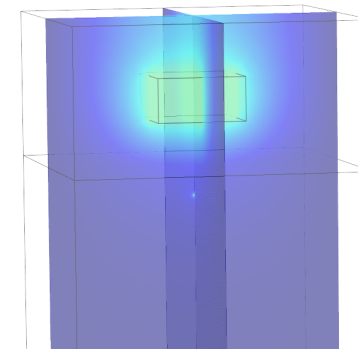
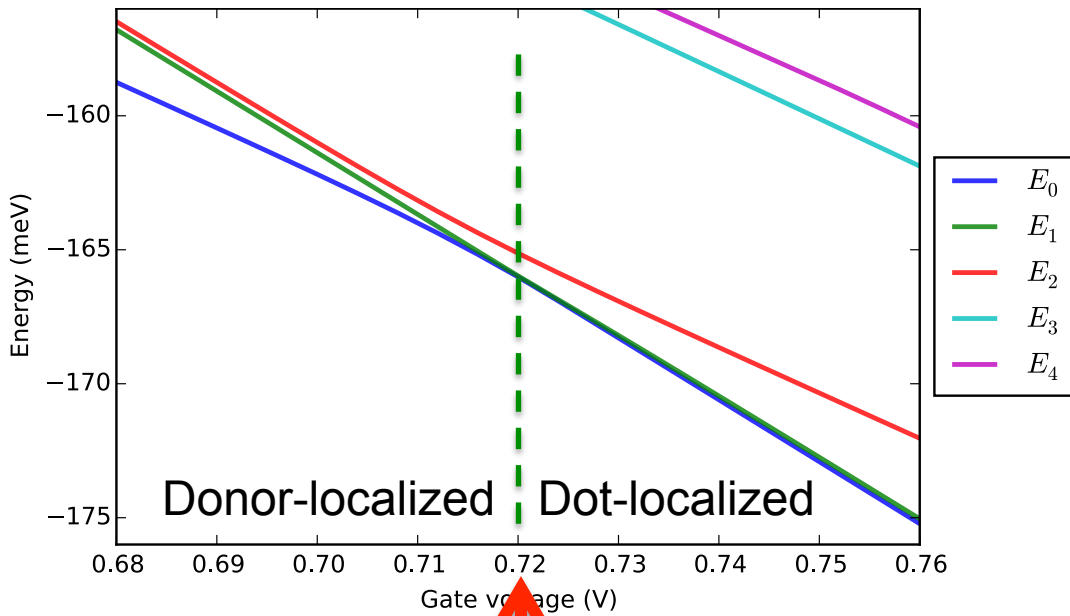
z

x

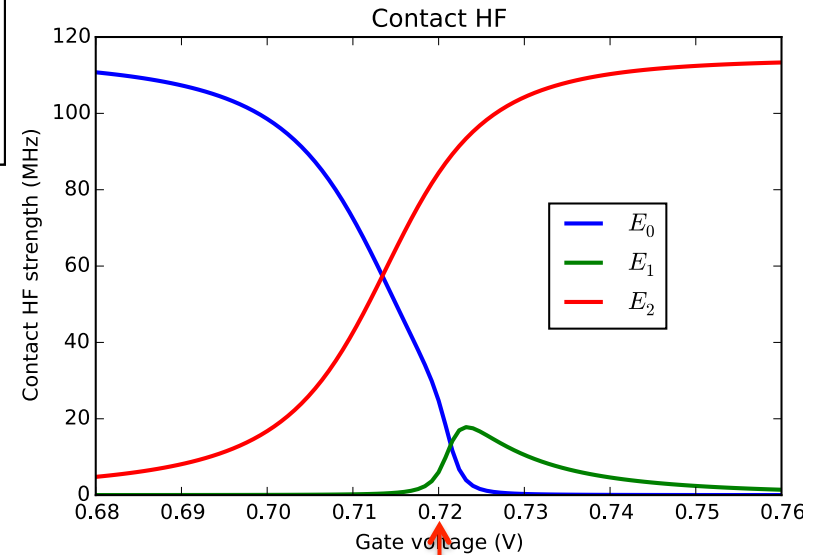
[Calderón, et al. PRL 2006, PRB 2007, PRB 2008]
[Baena, et al. PRB 2012]



Shuttling between donor and interface dot



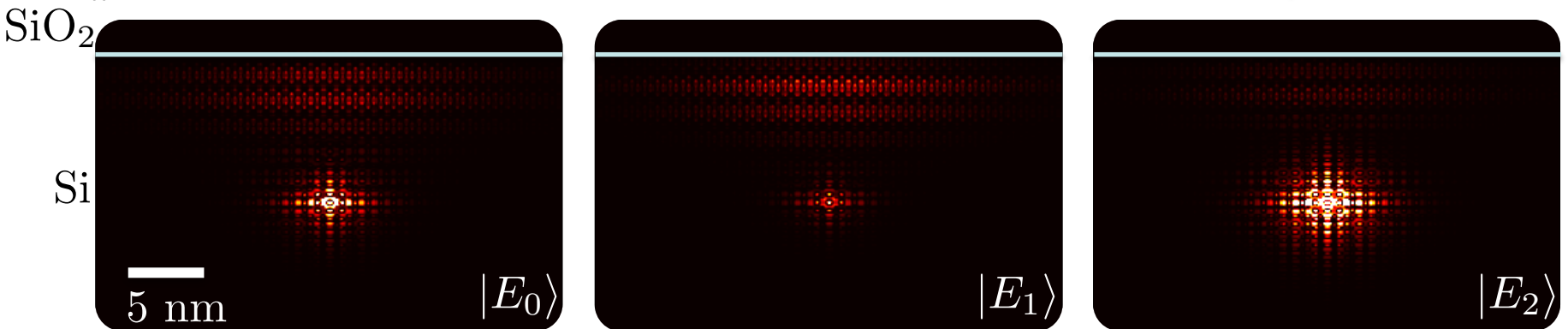
0.72 V



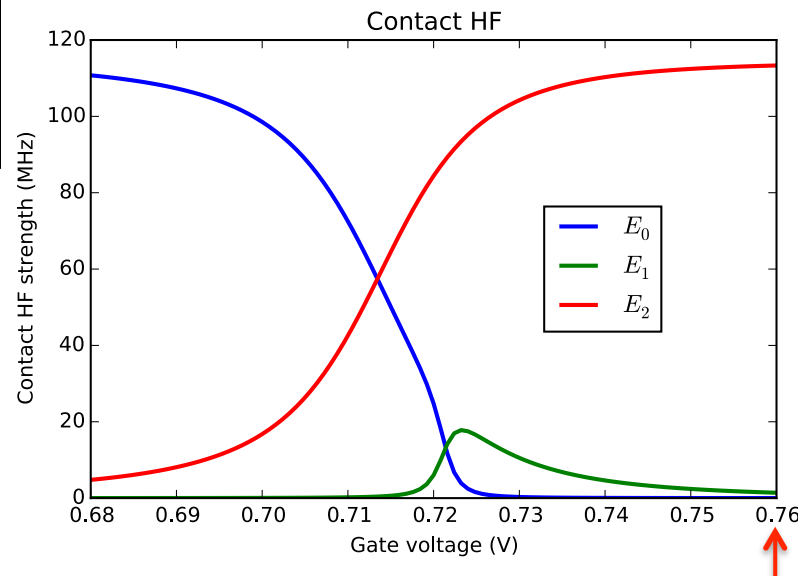
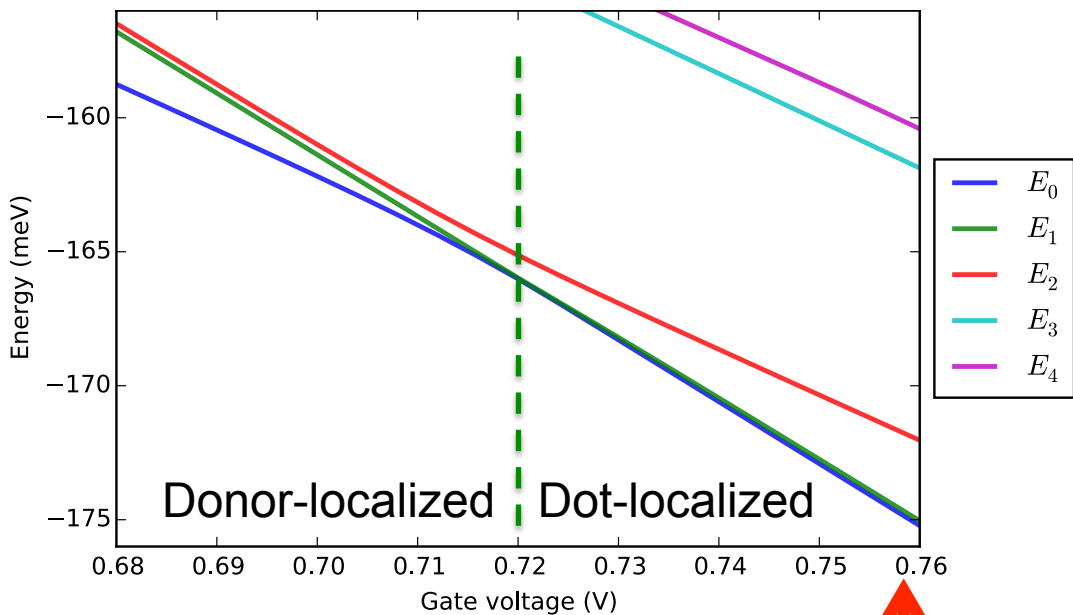
z

x

[Calderón, et al. PRL 2006, PRB 2007, PRB 2008]
[Baena, et al. PRB 2012]

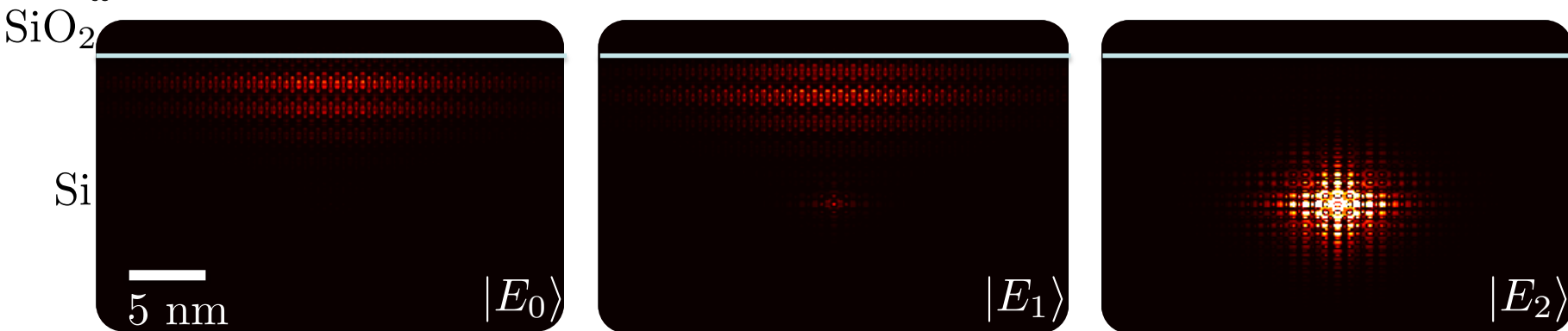


Shuttling between donor and interface dot

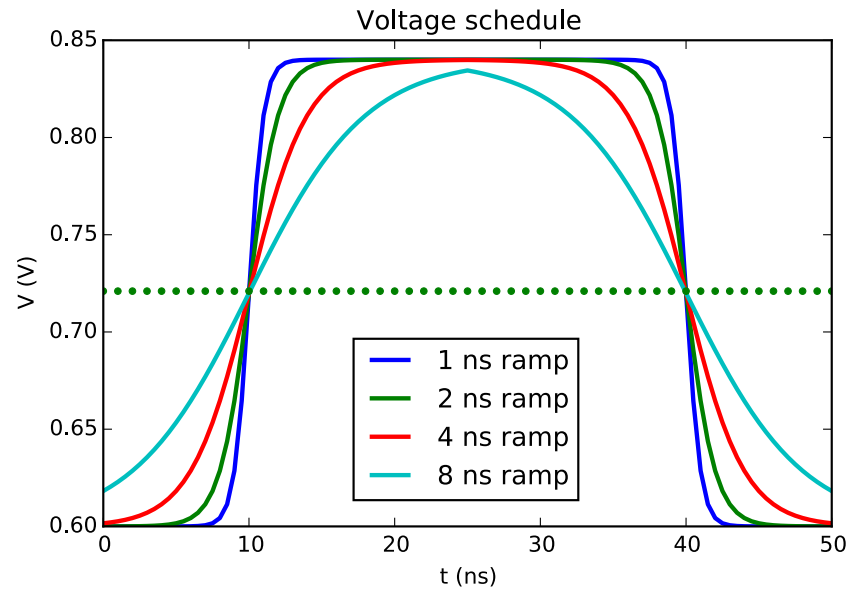


z
 x

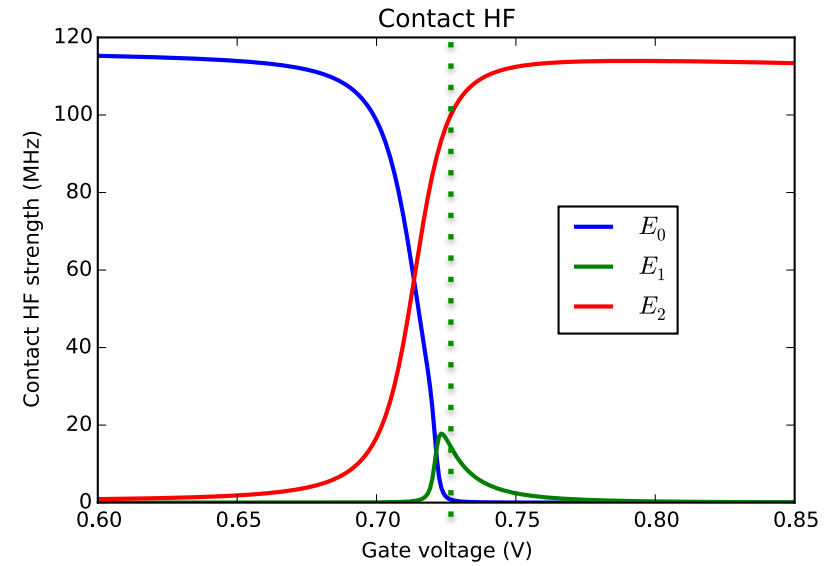
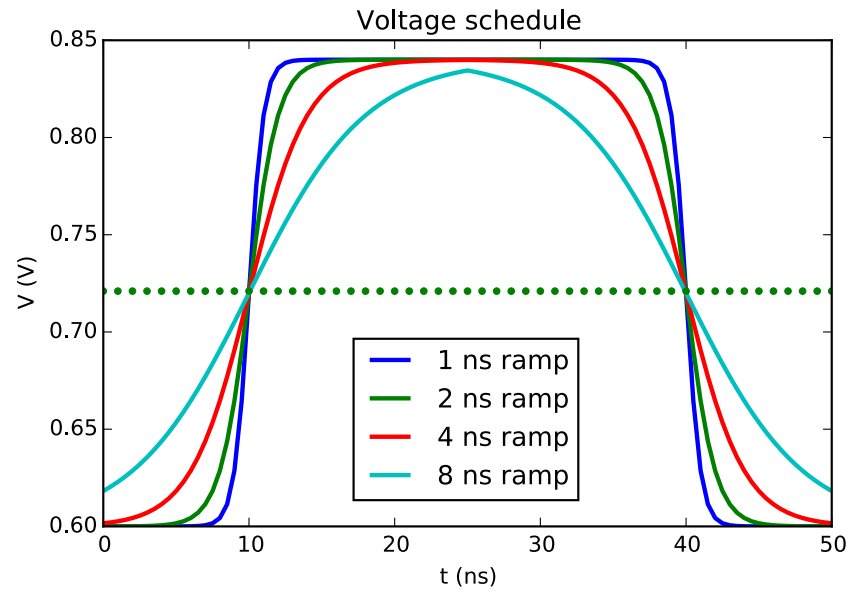
[Calderón, et al. PRL 2006, PRB 2007, PRB 2008]
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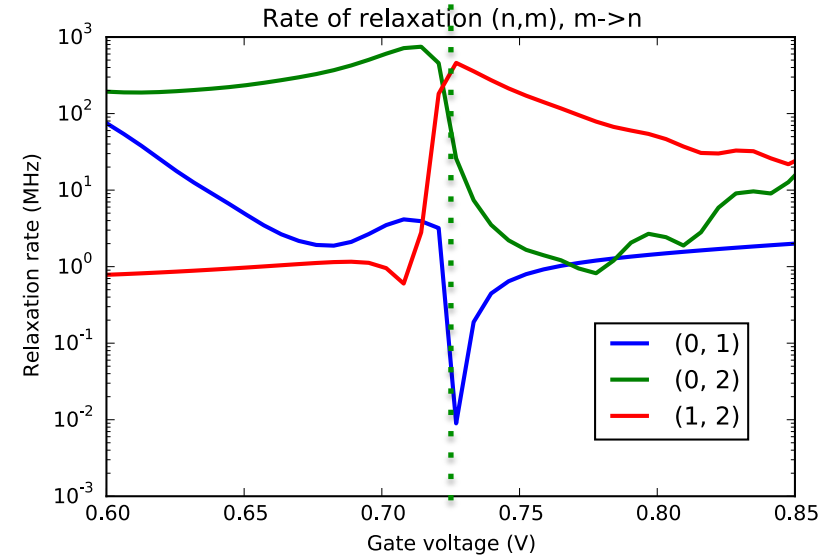
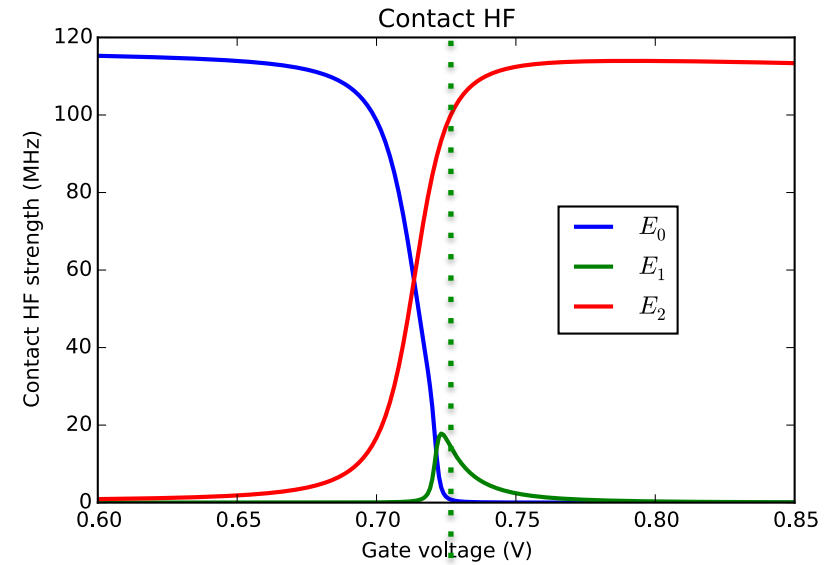
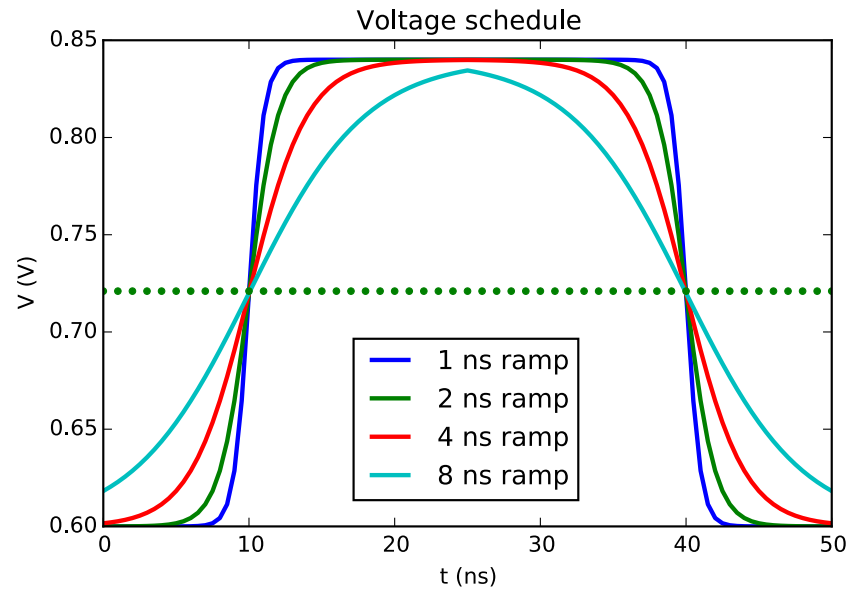
Closed/open dynamics



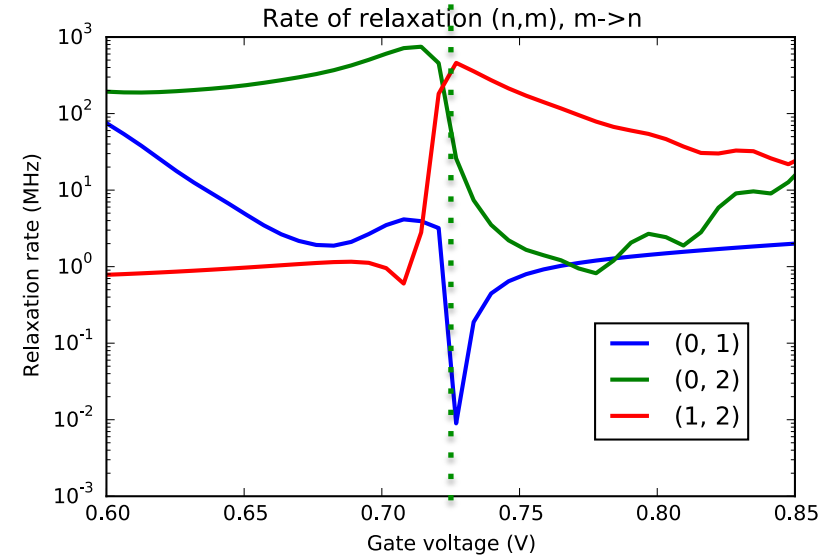
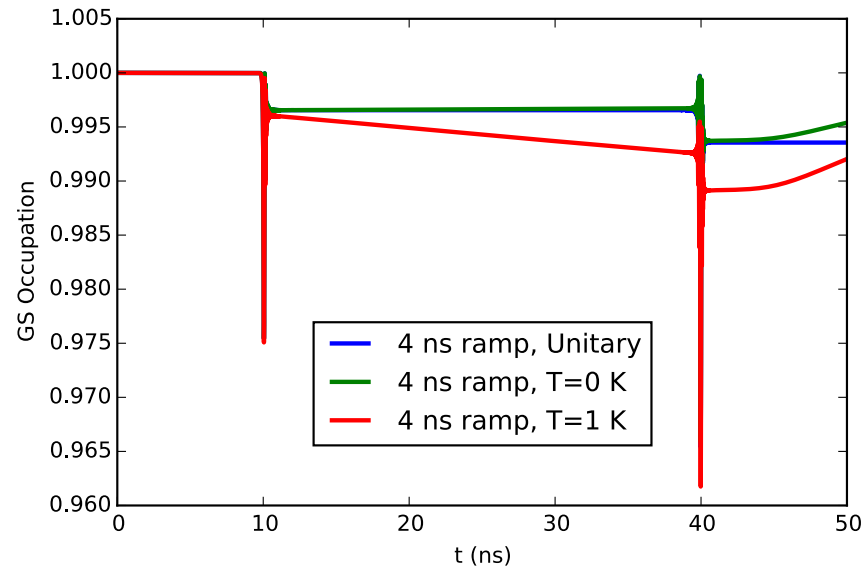
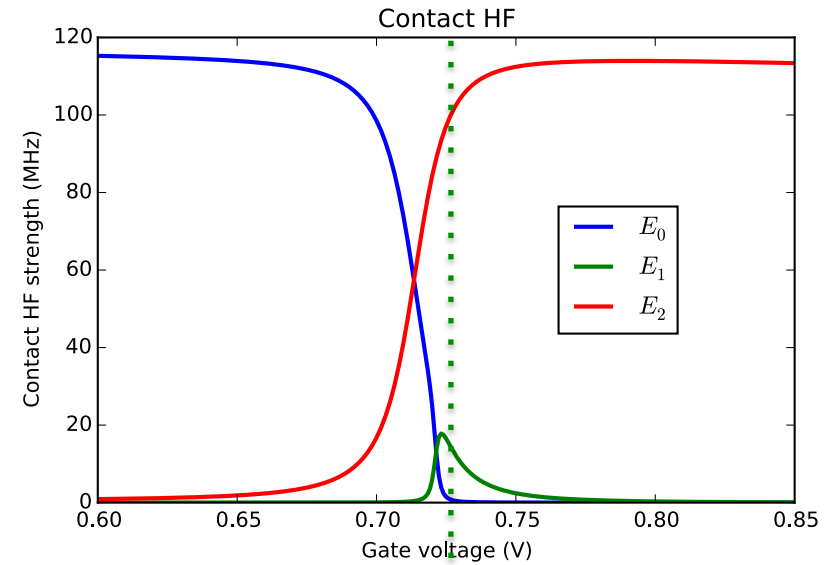
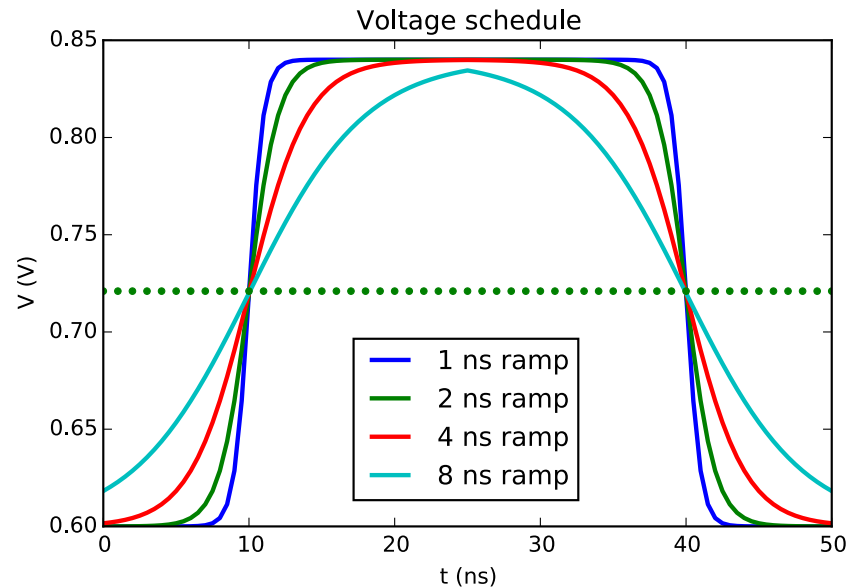
Closed/open dynamics



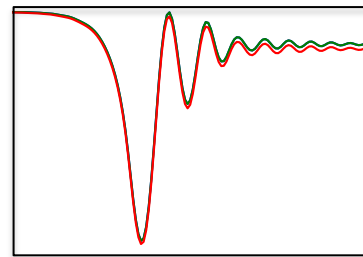
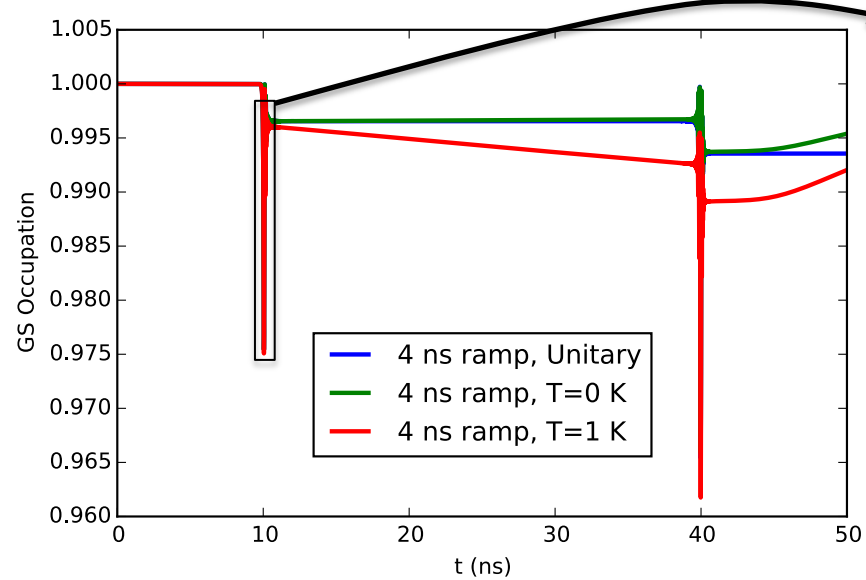
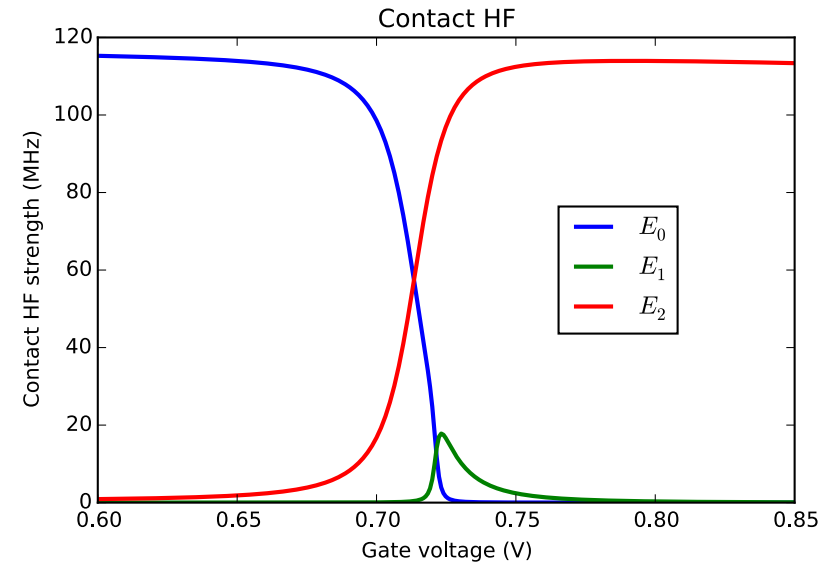
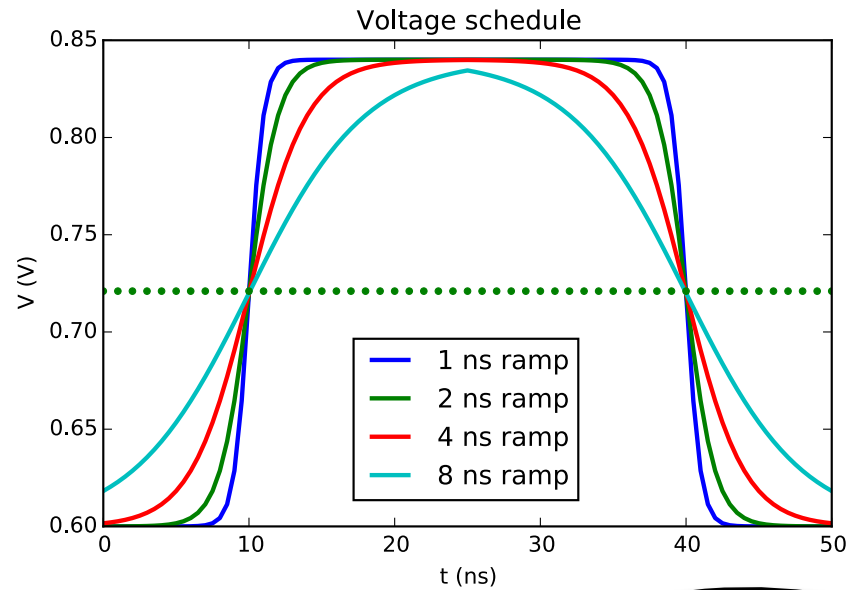
Closed/open dynamics



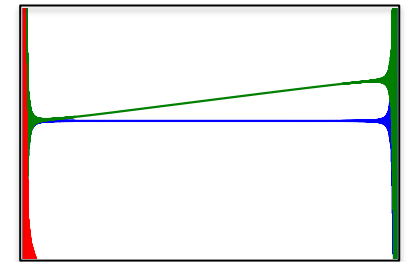
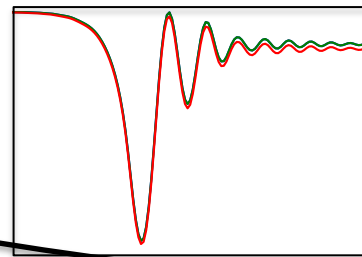
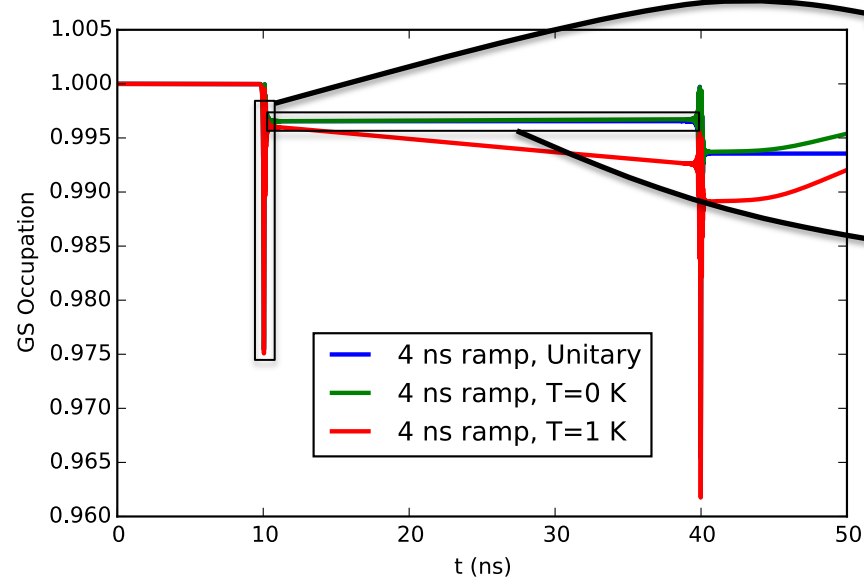
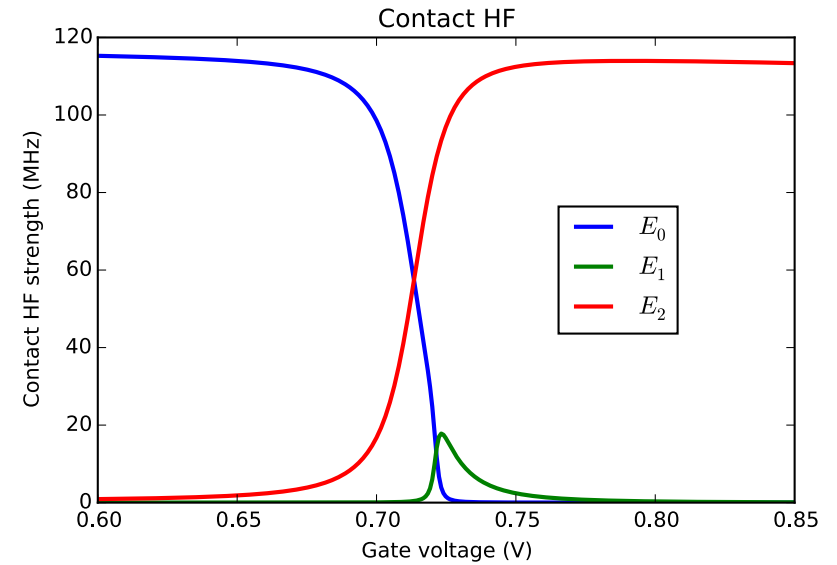
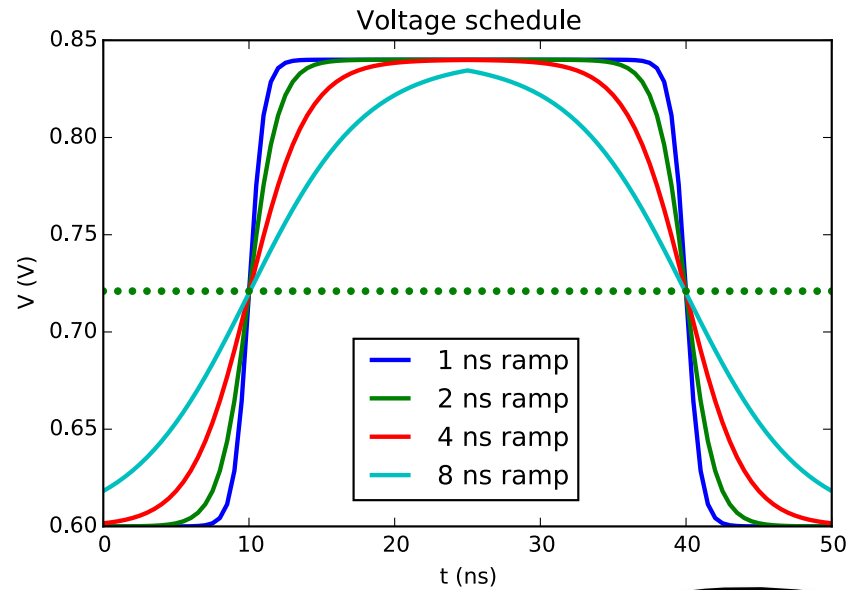
Closed/open dynamics



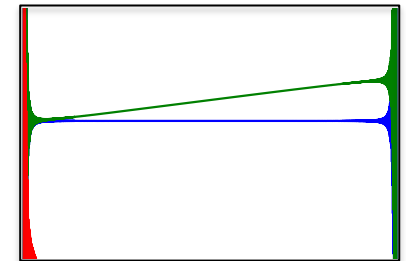
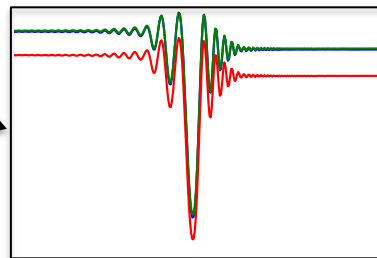
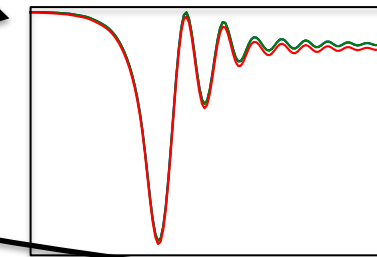
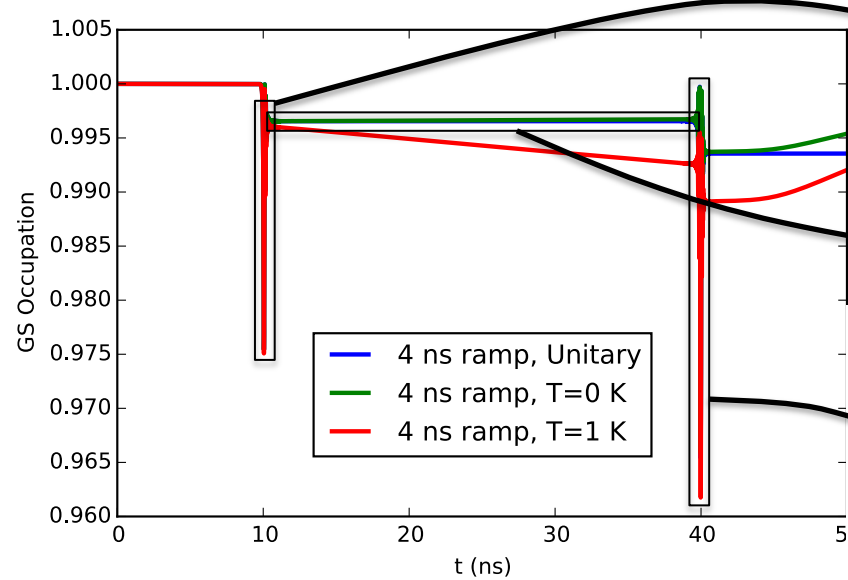
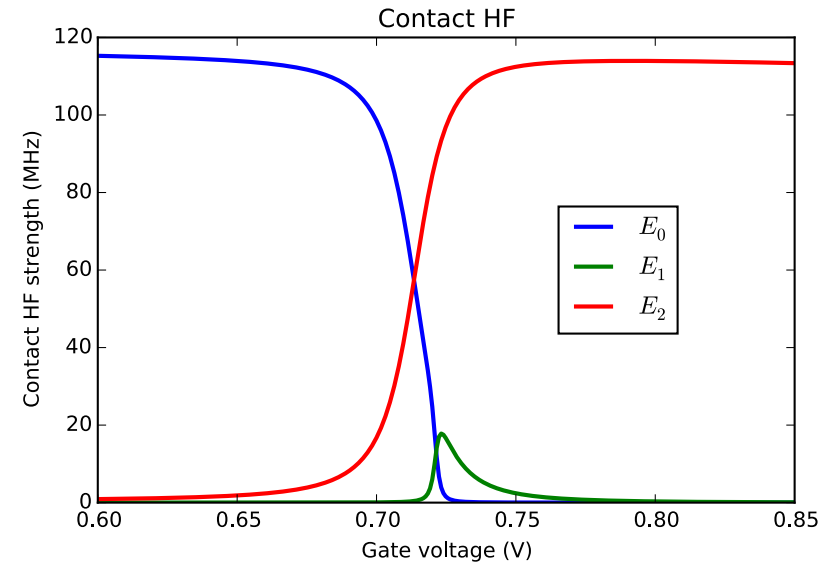
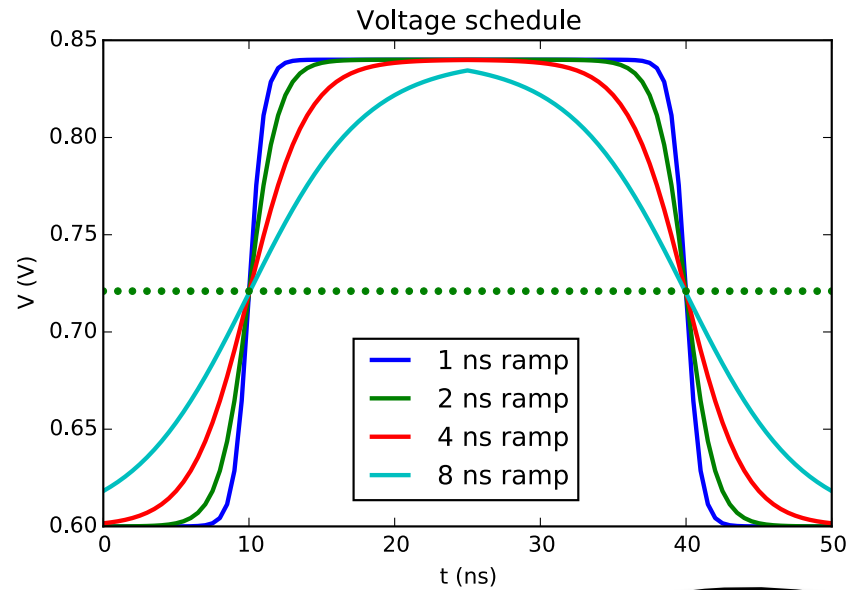
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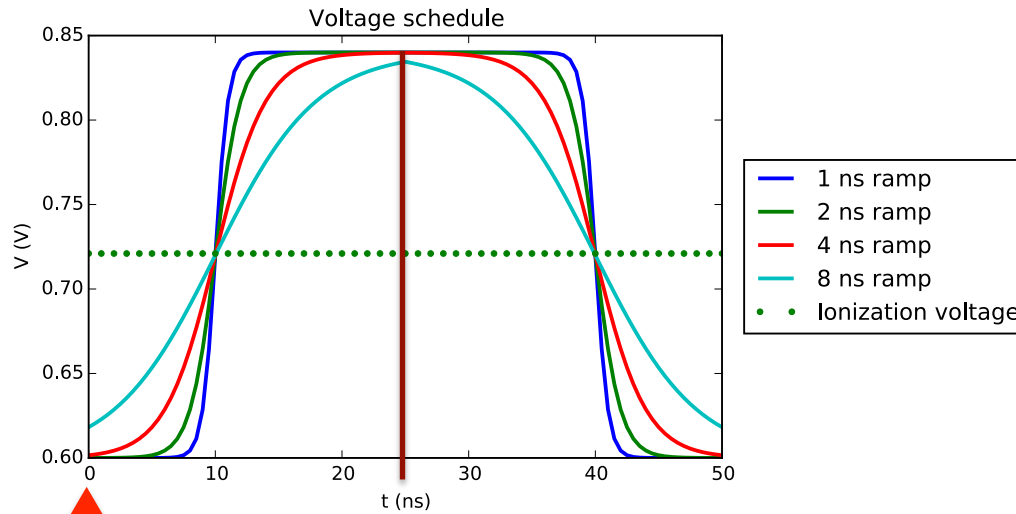
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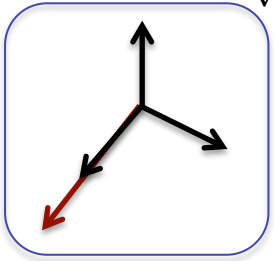
Closed/open dynamics



Spin-echo fidelity during shuttling



Prepare $\frac{|\uparrow\rangle + |\downarrow\rangle}{\sqrt{2}}$



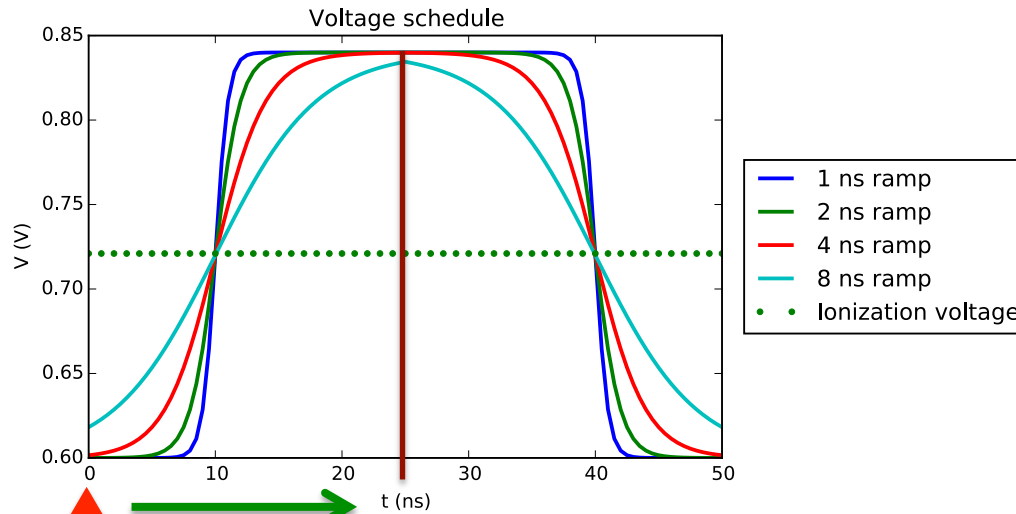
Errors:
 Non-adiabaticity
 Thermalization

$$H_{\text{spin}}(t) = A(t) \vec{\sigma}_e \cdot \vec{\sigma}_n$$

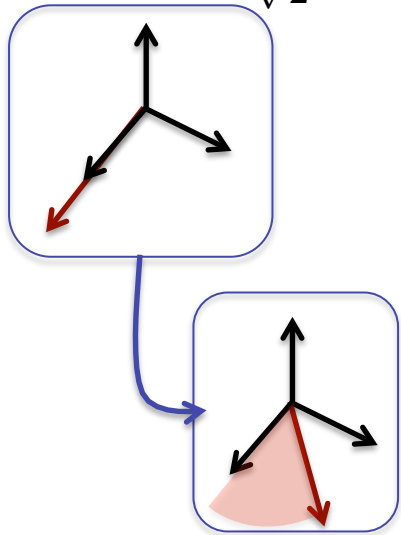
$$\delta\theta = \int_0^{T/2} dt [A(t) - A(t + T/2)] / \hbar$$

$$\mathcal{I} = 1 - \cos(\delta\theta)^2$$

Spin-echo fidelity during shuttling



Prepare $\frac{|\uparrow\rangle + |\downarrow\rangle}{\sqrt{2}}$



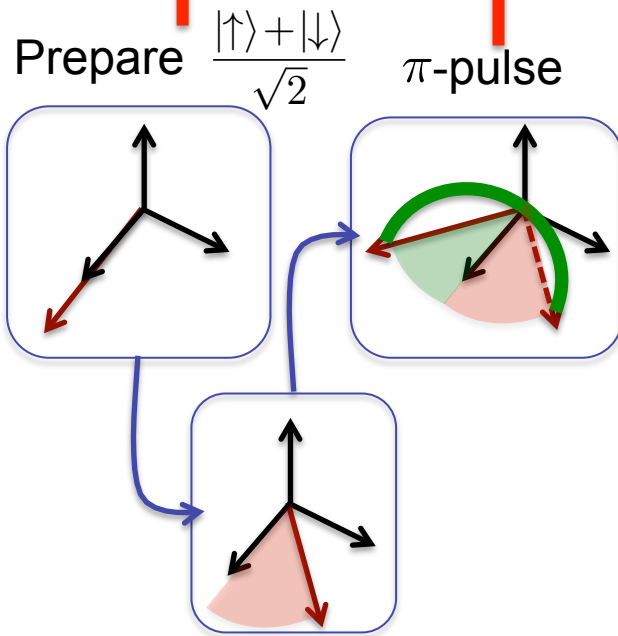
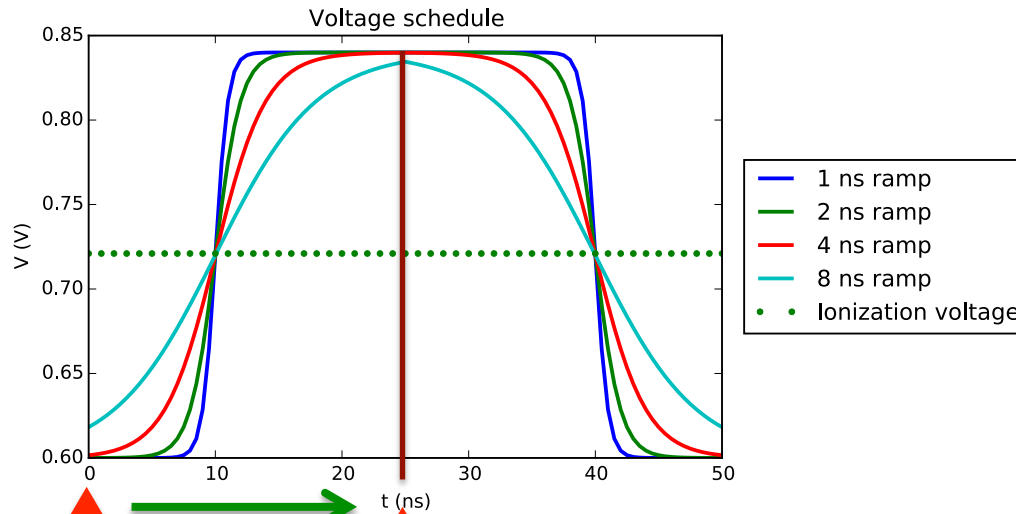
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Spin-echo fidelity during shuttling



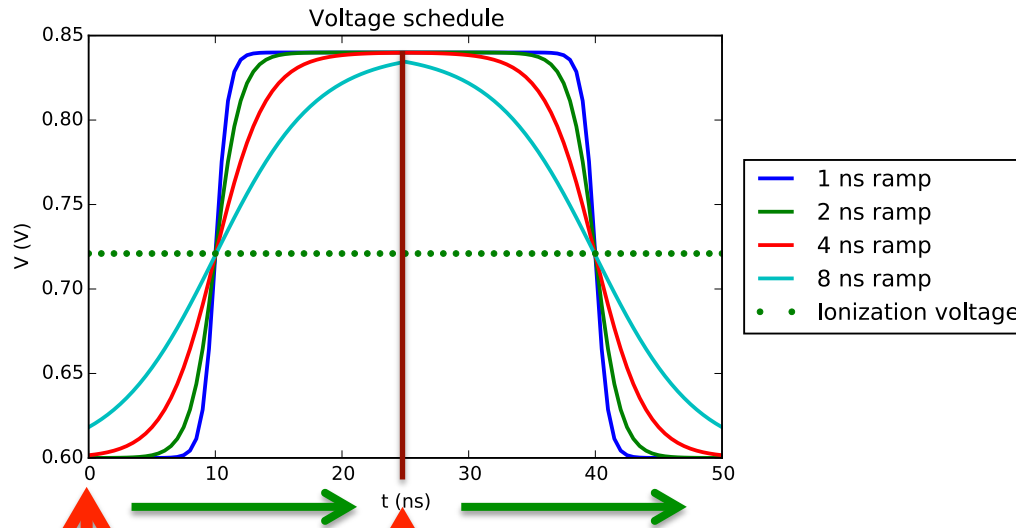
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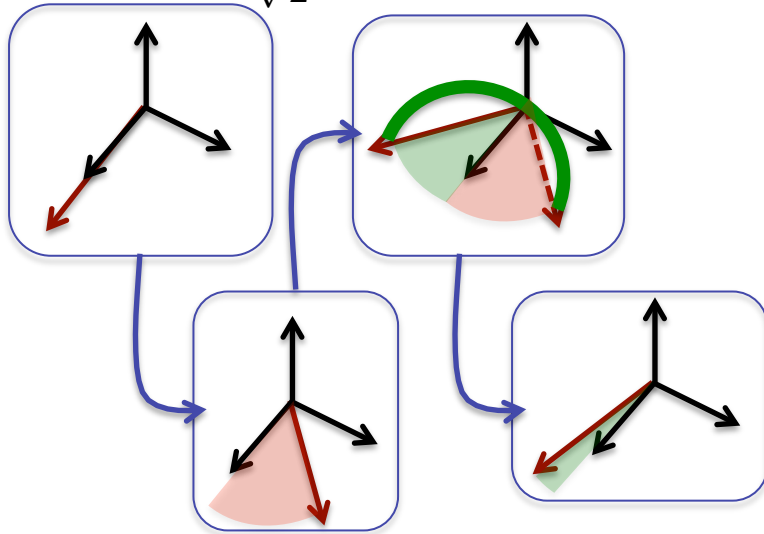
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$$\mathcal{I} = 1 - \cos(\delta\theta)^2$$

Spin-echo fidelity during shuttling



Prepare $\frac{|\uparrow\rangle + |\downarrow\rangle}{\sqrt{2}}$ π -pulse



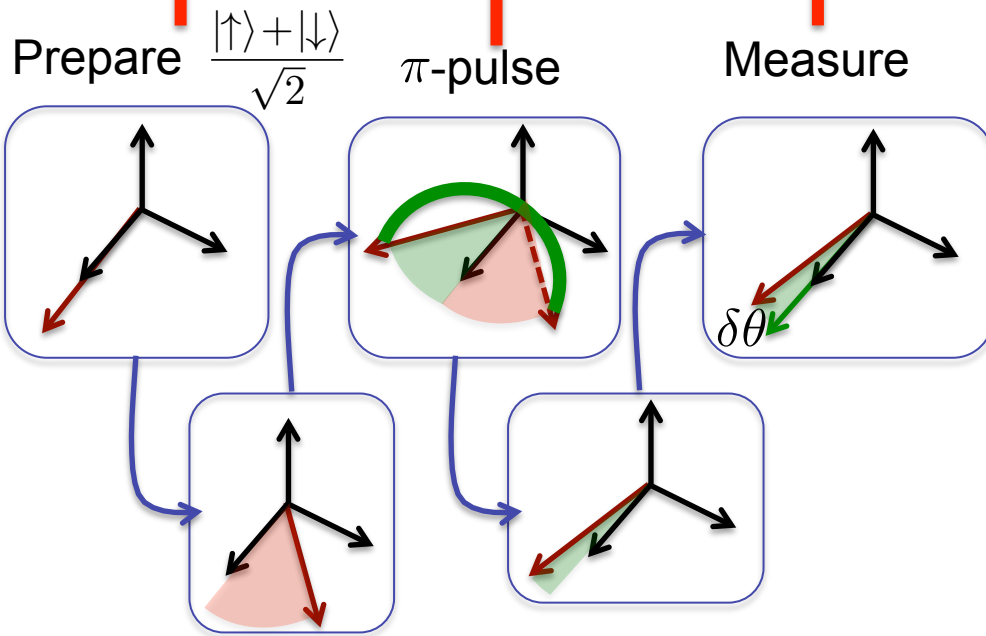
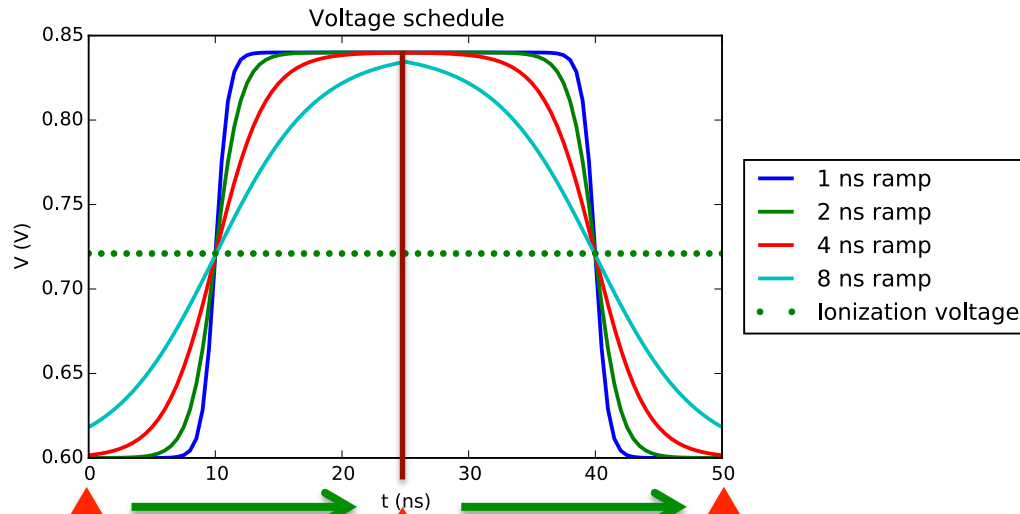
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$$\mathcal{I} = 1 - \cos(\delta\theta)^2$$

Spin-echo fidelity during shuttling

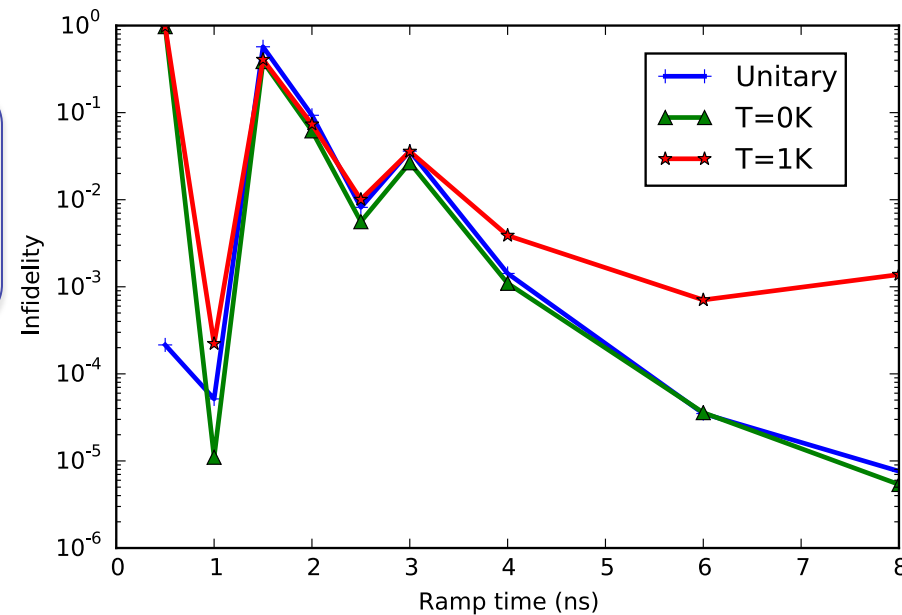


Errors:
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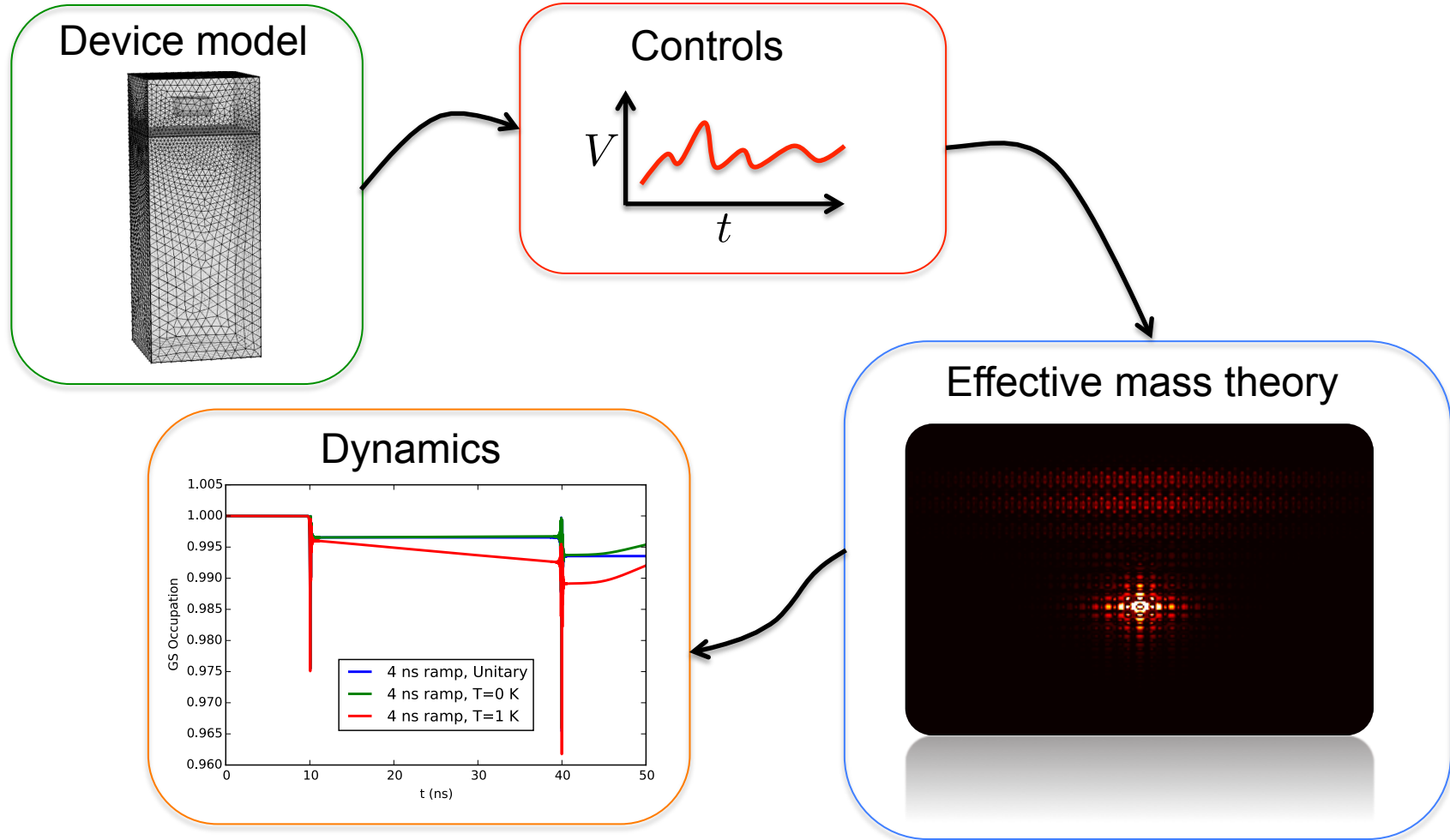
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Summary



Collaborators:
 John K. Gamble, Andrew Baczewski,
 Wayne Witzel, Inès Montañó, Erik Nielsen, Rick Muller – *Sandia*
 Adam Frees – *Univ. Wisconsin-Madison*

Thank you!