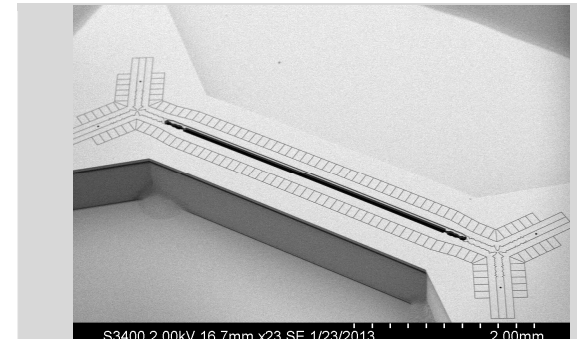
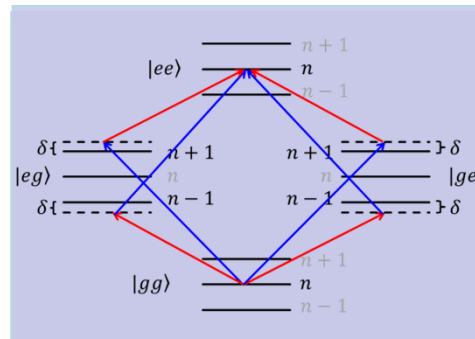
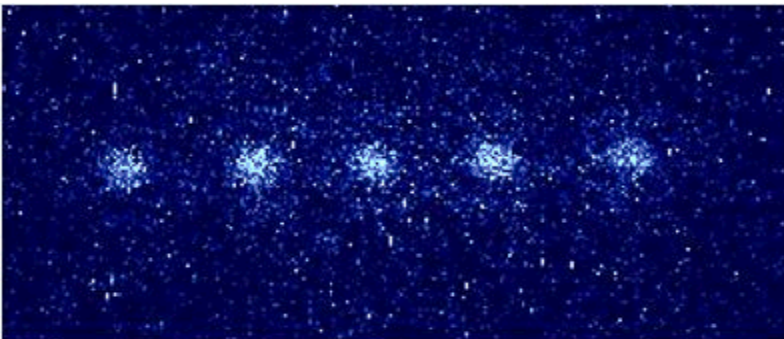


*Exceptional service in the national interest*



# Quantum Information Processing in Sandia surface traps

**Peter Maunz, Jonathan Mizrahi, Kenneth Rudinger,  
Eric Nielsen, and Robin Blume-Kohout**

February, 2015



Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

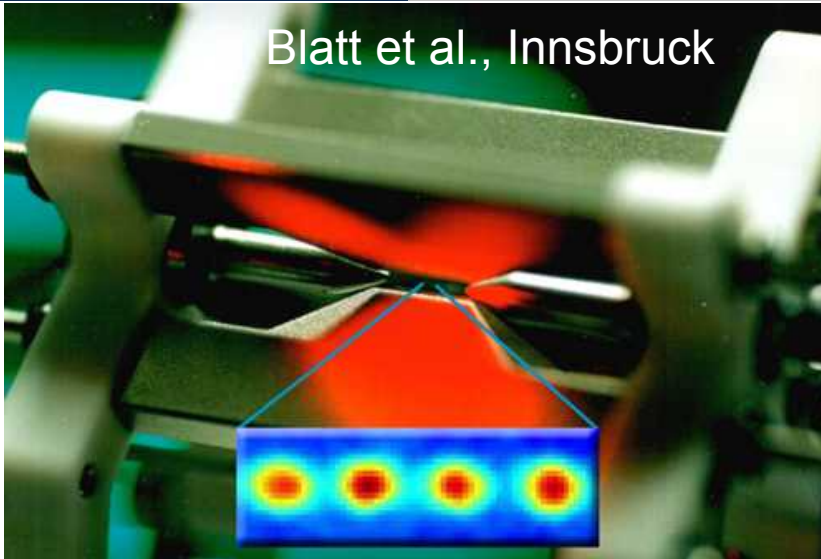




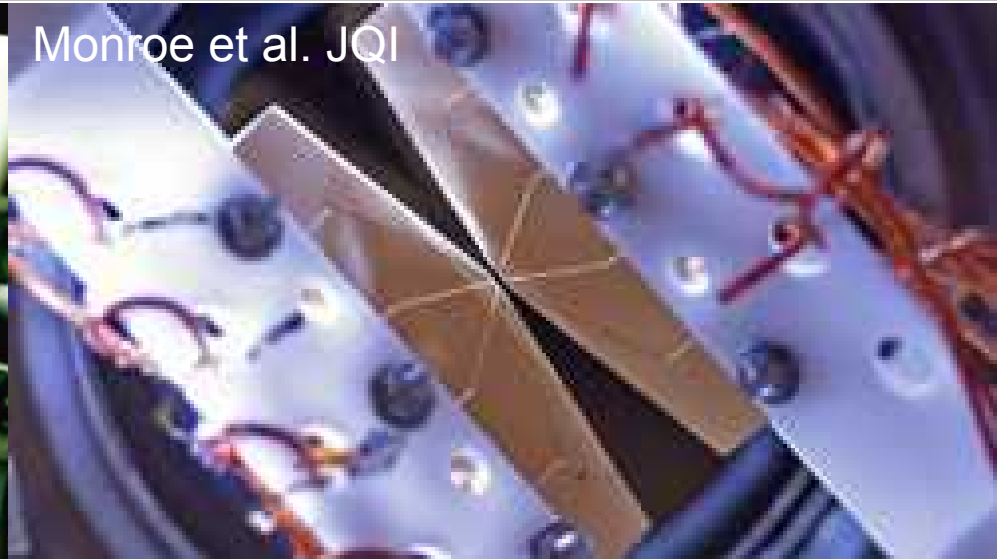
Sandia  
National  
Laboratories

# Towards scalable ion traps

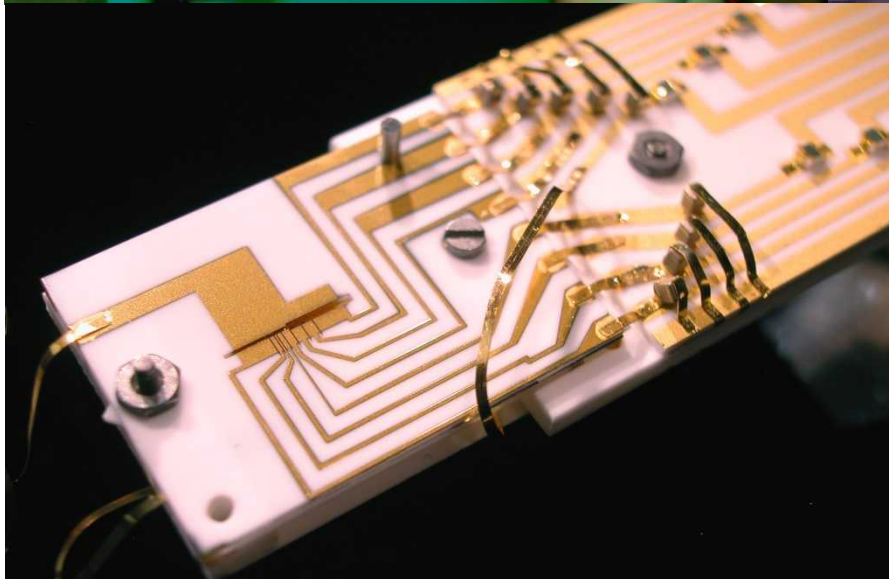
Blatt et al., Innsbruck



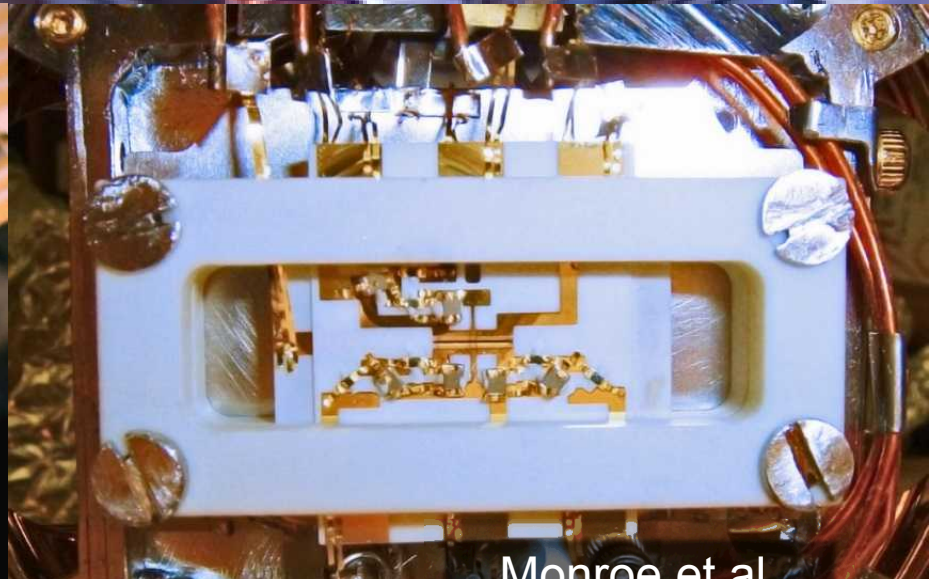
Monroe et al. JQI



Wineland et al. NIST Boulder



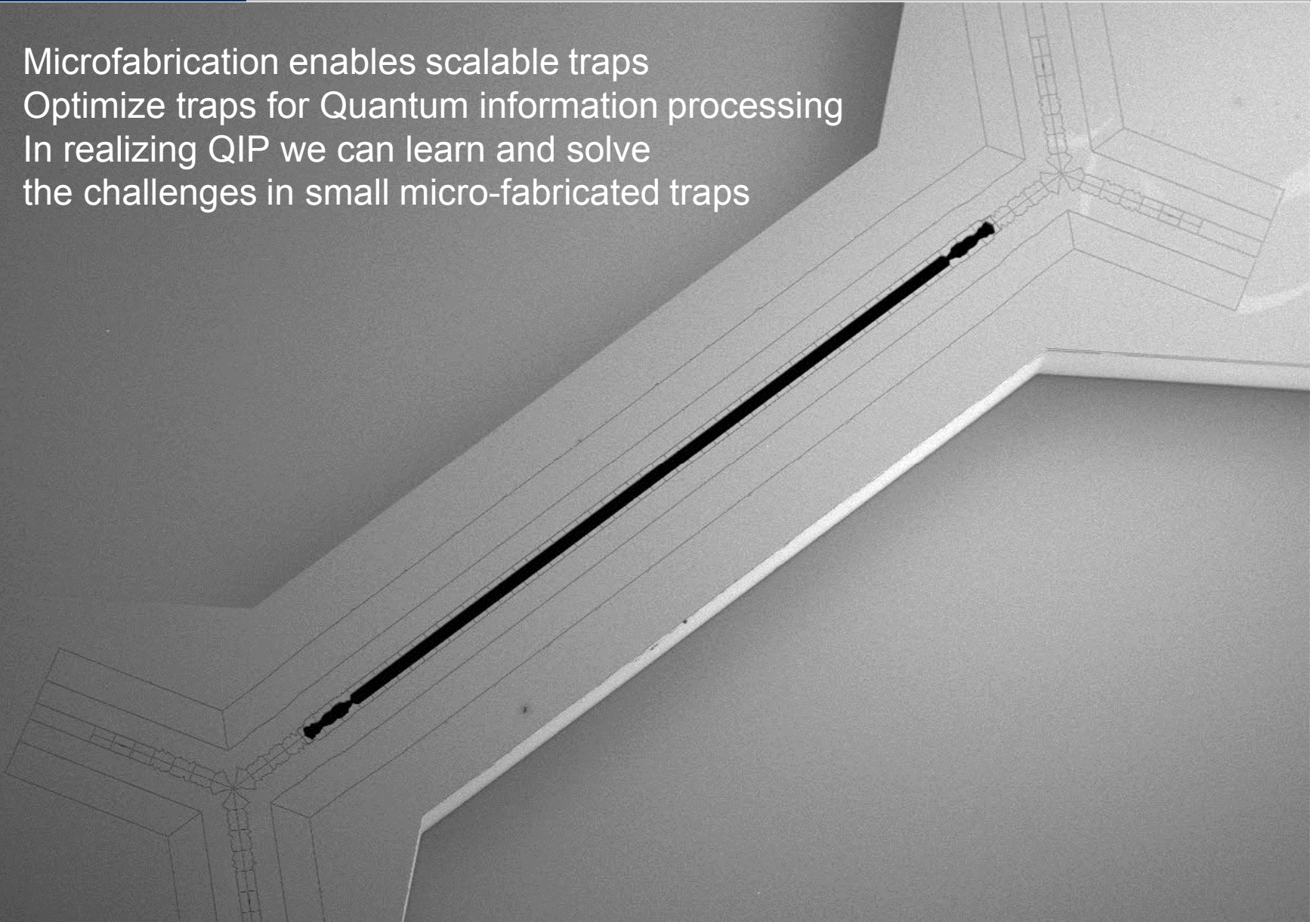
Monroe et al.  
JQI





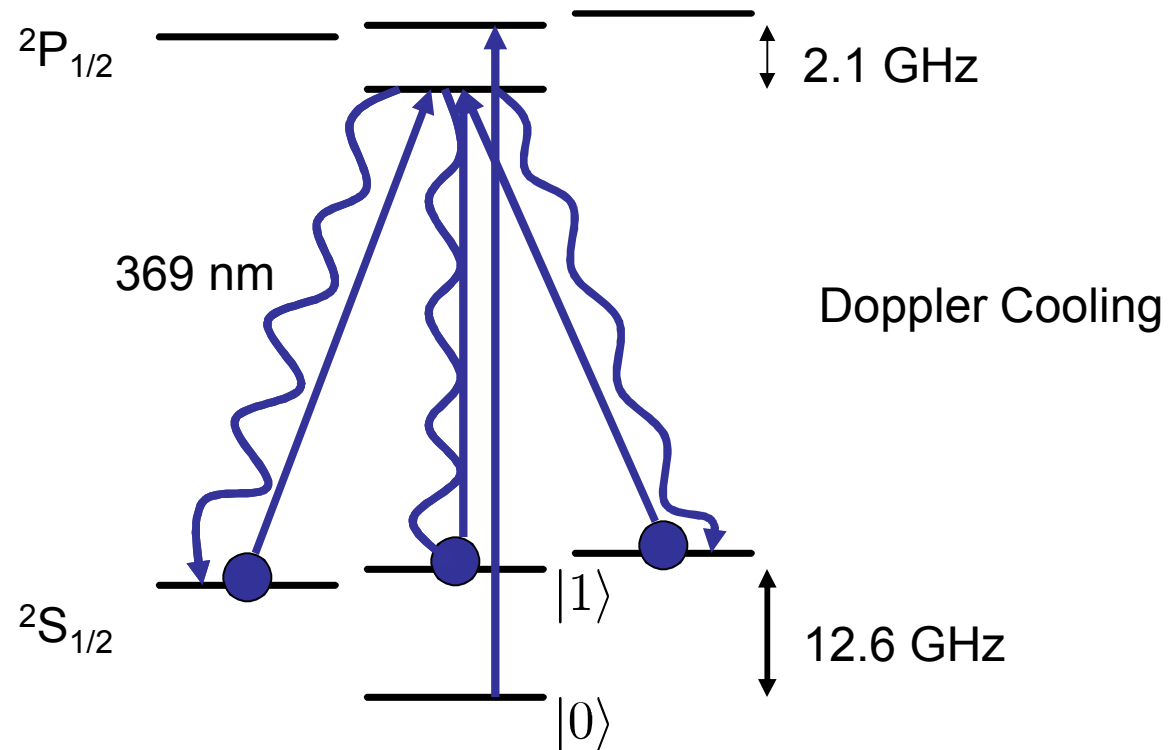
# Micro-fabrication

- Microfabrication enables scalable traps
- Optimize traps for Quantum information processing
- In realizing QIP we can learn and solve the challenges in small micro-fabricated traps





# The Ytterbium Qubit



clock state qubit, magnetic field insensitive.

S. Olmschenk *et al.*, PRA **76**, 052314 (2007)



# Gate Set Tomography

## State and Process Tomography

$$\langle\langle E_k | \quad G \langle\langle E_j | G \text{ Characterize } \rho \rangle\rangle \text{ prepare } |\rho\rangle\rangle$$

analyze characterize

- Needs perfect gates to prepare and analyze
- Often done retrospectively

## Gate Set Tomography

(Developed by Robin Blume-Kohout et al.)

- Does not rely on perfect gates, operation of gates is extracted from their operation
- Characterize the gates first, then predict the outcome of a sequence of gates



Robin Blume-Kohout et al. *Robust, Self-consistent, Closed-form Tomography of Quantum Logic Gates on a Trapped Ion Qubit*. ArXiv 1310.4492 e-print, October 16, 2013.



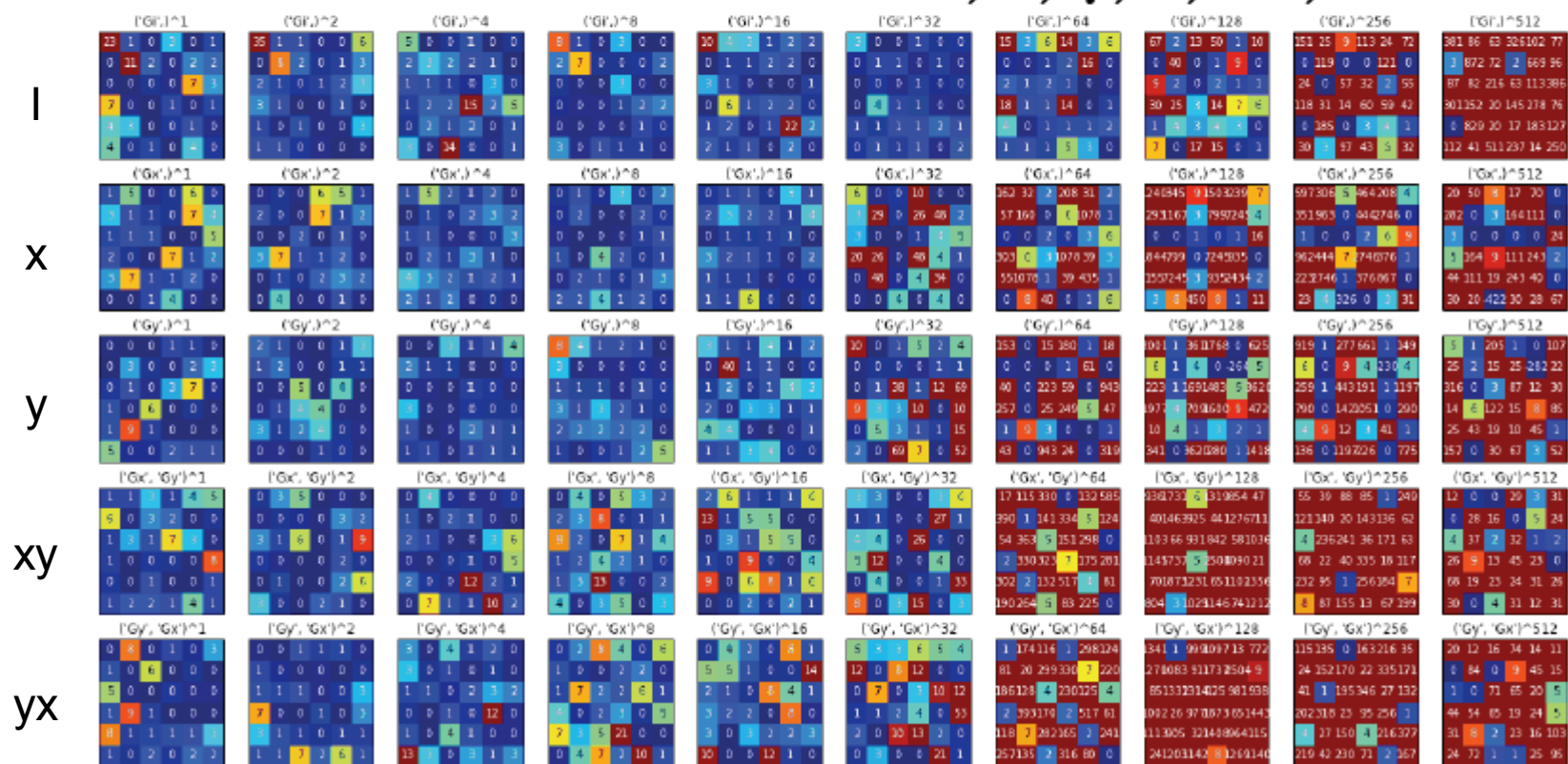
# GST: results

	ML estimate (short dataset)	ML estimate (long dataset)	Target gates
$\rho$	$\begin{pmatrix} 0.0099 & 0.0077 - 0.0046i \\ h.c. & 0.9901 \end{pmatrix}$	$\begin{pmatrix} 0.0092 & -0.0017 + 0.0088i \\ h.c. & 0.9908 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$
$E$	$\begin{pmatrix} 0.9911 & 0.0166 - 0.0006i \\ h.c. & 0.0089 \end{pmatrix}$	$\begin{pmatrix} 0.988 & 0.0019 + 0.0089i \\ h.c. & 0.012 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$
$G_1$	$\begin{pmatrix} 1.0019 & -0.0128 & -0.0198 & -0.0002 \\ -0.0066 & 0.9775 & -0.0118 & 0.0122 \\ 0.0041 & 0.0842 & 1.0138 & 0.0073 \\ -0.0035 & -0.013 & 0.0075 & 0.9969 \end{pmatrix}$	$\begin{pmatrix} 1.0001 & -0 & 0.0003 & 0.0001 \\ 0.0001 & 0.9994 & -0.0003 & -0 \\ -0.0001 & 0.0006 & 0.999 & -0.0003 \\ -0 & -0.0001 & 0.0002 & 0.9998 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$
$G_2$	$\begin{pmatrix} 1.0017 & -0.0276 & -0.0276 & -0.0048 \\ -0.0193 & 0.9582 & -0.0076 & -0.0127 \\ -0.0134 & 0.043 & 0.0082 & -0.9987 \\ -0.0072 & 0.002 & 1.0069 & 0.0192 \end{pmatrix}$	$\begin{pmatrix} 1 & -0.0001 & -0.0045 & -0.0005 \\ 0 & 0.9994 & -0.006 & -0.0018 \\ -0.005 & -0.0112 & -0.0064 & -0.9991 \\ 0.0006 & 0.0063 & 0.9993 & 0.0143 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$
$G_3$	$\begin{pmatrix} 0.99 & -0.0114 & 0.0083 & 0.0044 \\ -0.0082 & -0.0141 & -0.0045 & 0.9892 \\ 0.0121 & -0.0044 & 1.0056 & -0.0059 \\ -0.0001 & -0.9848 & 0.0017 & -0.0016 \end{pmatrix}$	$\begin{pmatrix} 1.0001 & 0.0033 & 0.0001 & 0.0049 \\ 0.0033 & -0.0001 & -0.0005 & 0.9992 \\ -0.0002 & -0.0024 & 0.9995 & -0.0161 \\ -0.0019 & -0.9989 & 0.0179 & 0.0085 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \end{pmatrix}$
$G_4$	$\begin{pmatrix} 0.9983 & -0.0217 & 0.0127 & 0.0142 \\ -0.0039 & 0.9745 & 0.0034 & 0.0077 \\ -0.0004 & -0.0145 & -1.0473 & -0.0323 \\ -0.014 & -0.0167 & -0.0072 & -1.0024 \end{pmatrix}$	$\begin{pmatrix} 1.0001 & -0 & 0.0062 & 0.0028 \\ -0 & 0.9997 & 0.0127 & 0.0022 \\ 0.0066 & 0.0164 & -0.9976 & 0.0065 \\ -0.004 & -0.0004 & -0.0066 & -0.9981 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$



# GST: non-Markovian noise

Hierarchical  $\chi^2$   
for best fit to  $L=1,2,4,8,16,32$

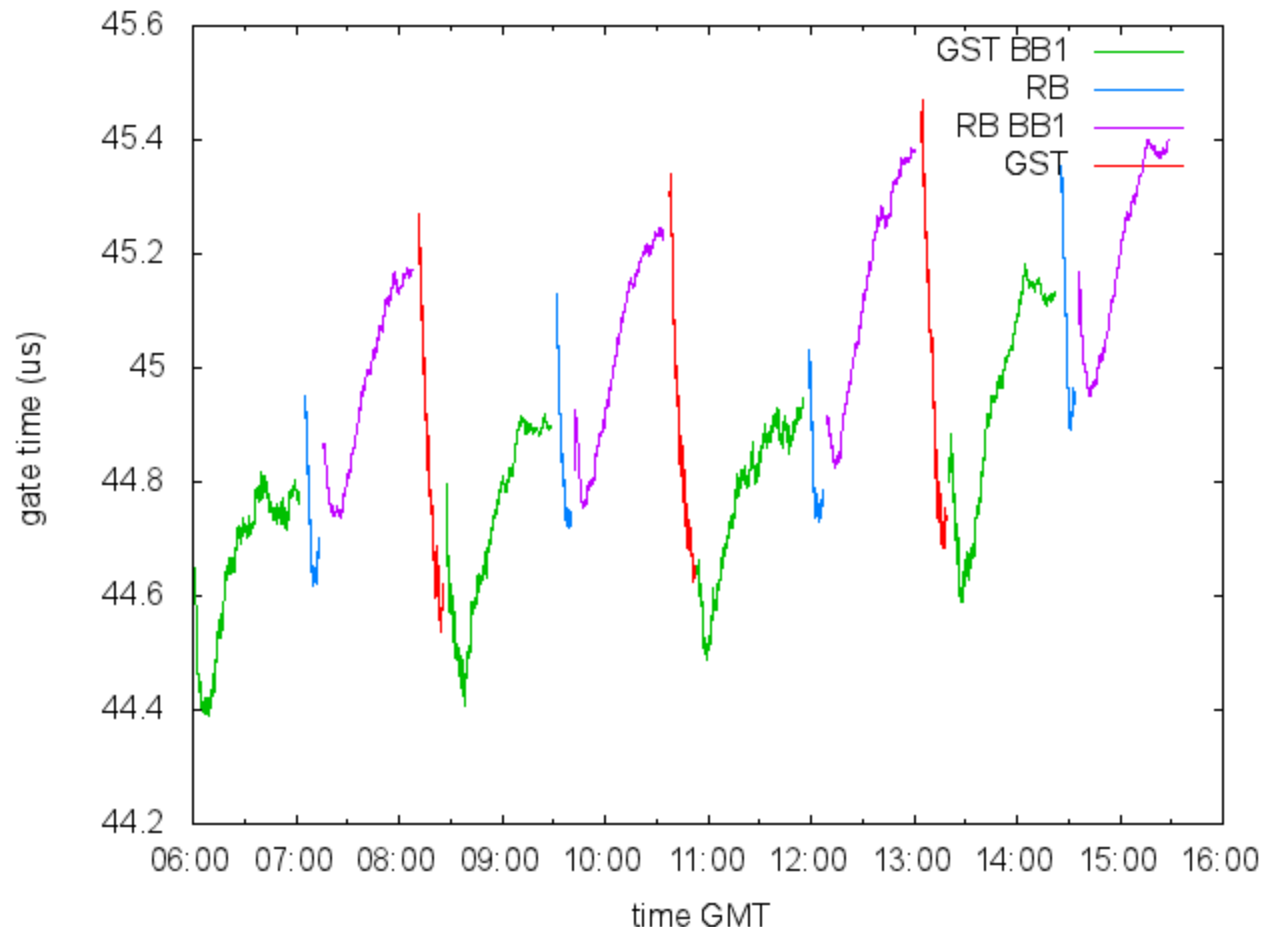




# Drift control

- Improved the system: temperature stabilization, elimination of components from microwave system
- Microwave  $\pi$ -times are measured independently and concurrently
- Feedback (locking) scheme adjusts  $\pi$ -times dynamically

Measured  $\pi/2$ -times





# Drift control algorithm

GateTimeIntegrator = GateTime << 5



GST sequence

Prepare dark state

Apply 21 GateTime microwave pulse

State detection result = 1 if bright else 0

GateTimeIntegrator -= result

GateTime = GateTimeIntegrator >> 5



## Realized gates

Gate	Matrix (Pauli basis)			
Gi	1.0	0	0	0
	0	1.0	-0.004	0.001
	0	0.009	0.998	-0.038
	0	0.001	0.037	0.992
Gx	1.0	0	0.005	0.003
	0	1.0	0	-0.003
	0.005	0.001	-0.001	-0.999
	-0.002	0.002	0.999	-0.003
Gy	1.0	-0.002	0	0
	-0.002	0	-0.004	1.0
	0	-0.003	1.0	-0.001
	0	-1.0	0.001	-0.005

## Comparison to target gates

Gate	Fidelity	Trace Dist.	Frobenius Dist.	Error Generator			
Gi	0.997424	0.054254	0.020661	0	0	0	0
				0	0	-0.004	0.001
				0	0.009	-0.001	-0.038
				0	0.001	0.037	-0.007
Gx	0.999653	0.00939	0.003764	0	0	0.005	0.003
				0	0	0	-0.003
				-0.002	0.002	-0.001	-0.003
				-0.005	-0.001	0.001	-0.001
Gy	0.999944	0.007907	0.003186	0	-0.002	0	0
				0	0	-0.001	0.005
				0	-0.003	0	-0.001
				-0.002	0	-0.004	0



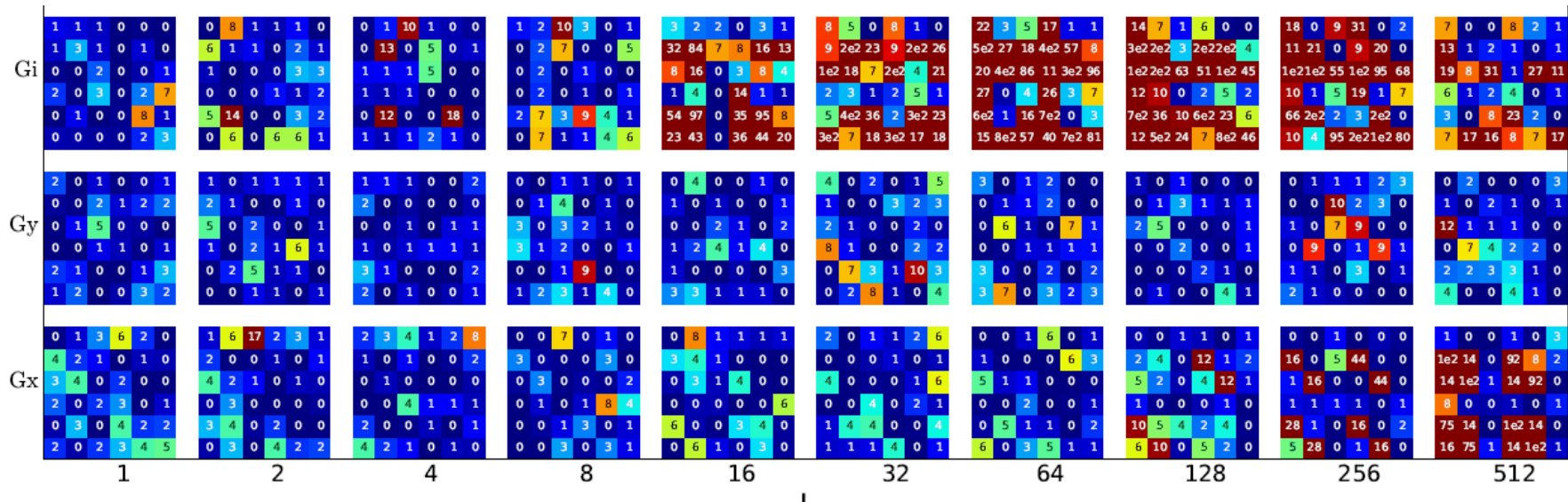
## Gate analysis

Gate	Eigenvalues	Fixed pt	Rotn. axis	Angle	Diag. decay	Off-diag. decay
Gi	$0.996e^{i0.0}$	1.0	0	$0.012037\pi$	0	0.004433
	$0.996e^{-i0.0}$	0	0.973			
	1.0	0.004	0.017			
	1.0	0.001	0.229			
Gx	$0.999e^{i1.6}$	-0.98	-0.194	$0.500574\pi$	0	0.000625
	$0.999e^{-i1.6}$	0.198	-0.981			
	1.0	-0.004	0			
	1.0	-0.001	-0.002			
Gy	$1.0e^{i1.6}$	1.0	-0.299	$0.500854\pi$	0	0
	$1.0e^{-i1.6}$	0	0.002			
	1.0	-0.558	-0.954			
	1.0	0	-0.003			



# non-Markovian noise after optimization

$\chi^2$  of GST fit (BB1 compensated microwave gates)



- Very good results for the BB1 compensated gates  $G_x$  and  $G_y$
- Programming error in compensation of  $G_i$  leads to non-Markovian noise

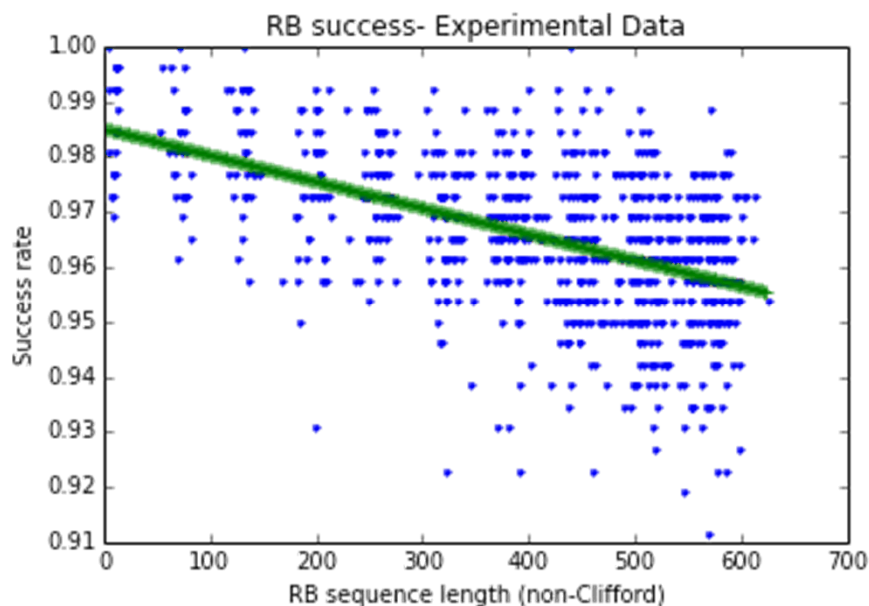


# Randomized benchmarking and GST

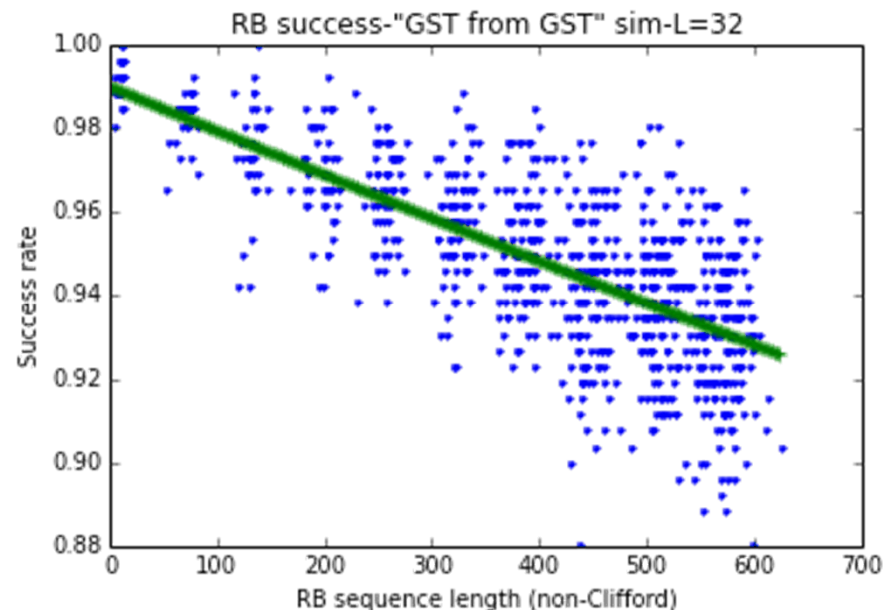
Randomized Benchmarking:

- Average infidelity per gate  $4.9 \times 10^{-5}$
- GST worst case gate infidelity  $3 \times 10^{-3}$

Randomized benchmarking  
Experimental



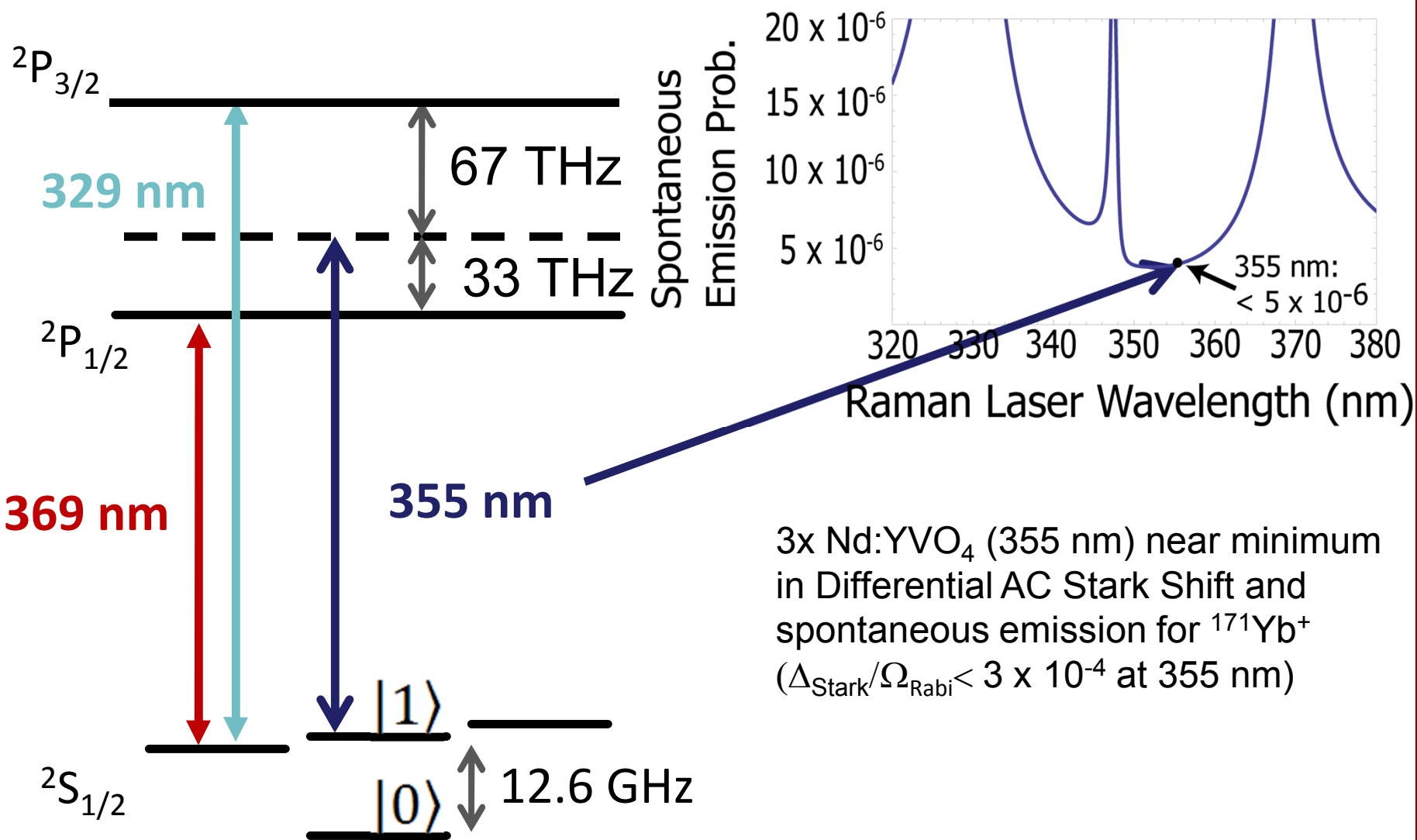
Randomized benchmarking  
Markovianized simulated data from GST



non-Markovian errors average out in Randomized benchmarking



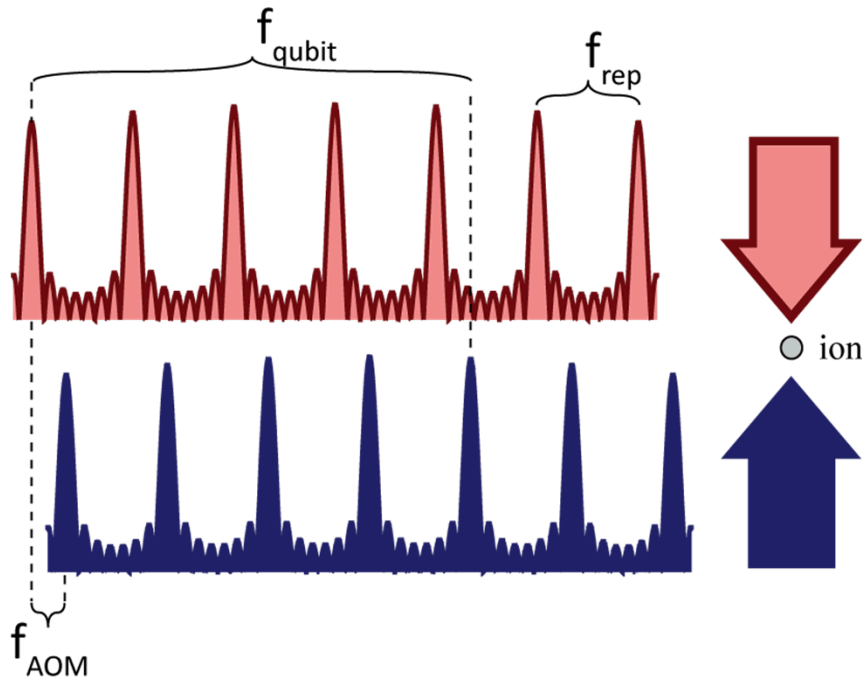
# 355 Raman transitions: $^{171}\text{Yb}^+$





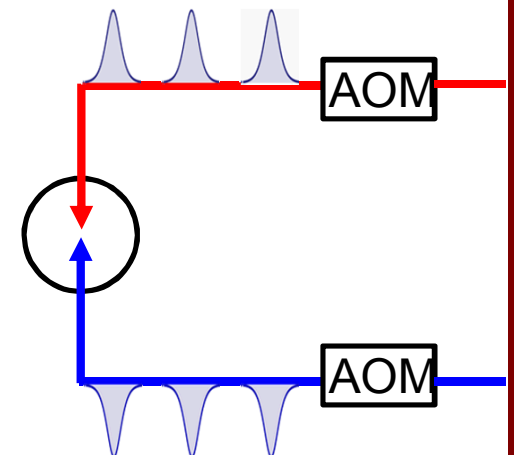
# Pulsed laser Raman transitions

- Couple to ions using 355nm frequency comb
- Beat note created by repetition rate and AOM shift
- Get large splitting for free



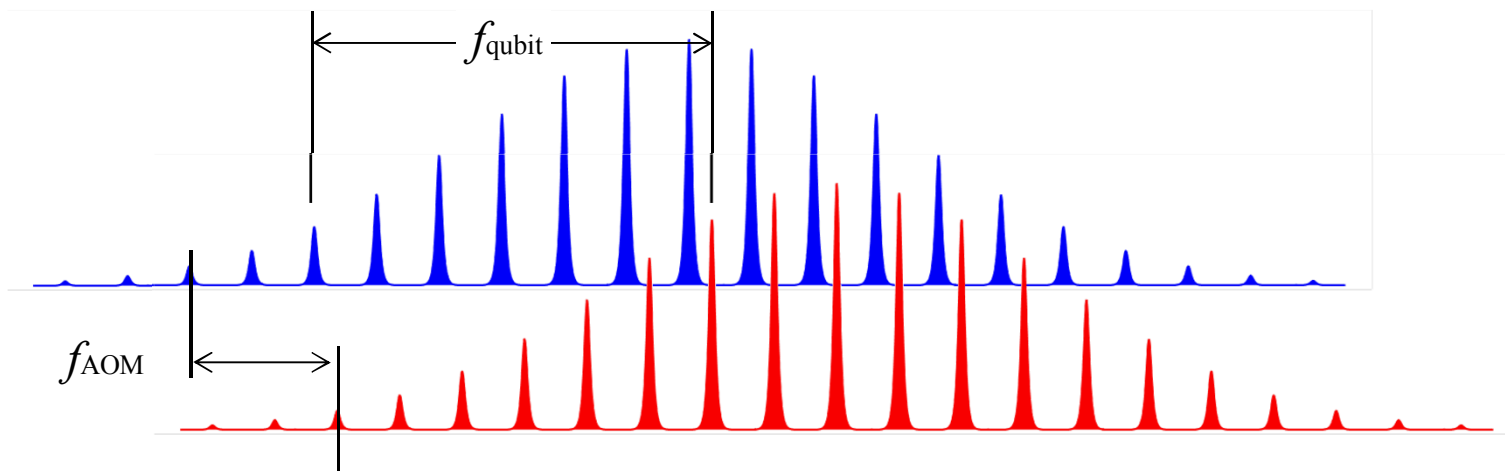
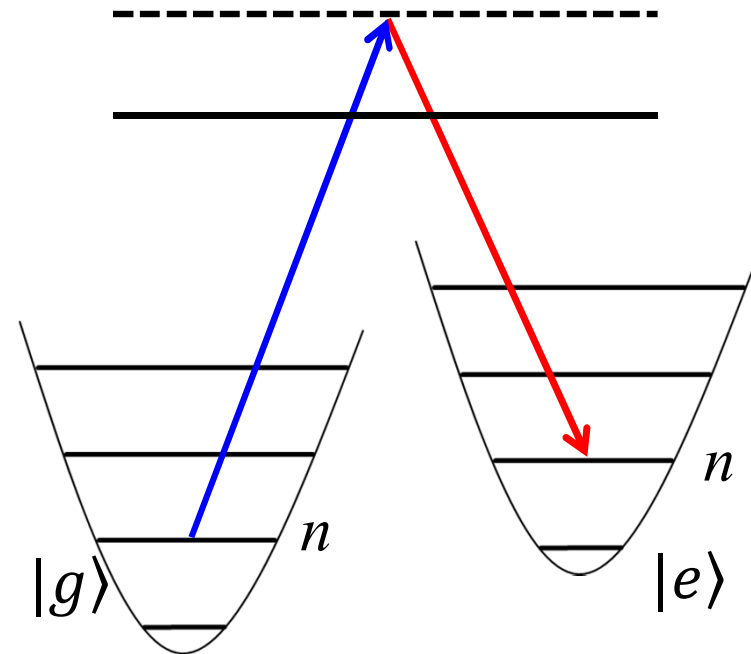
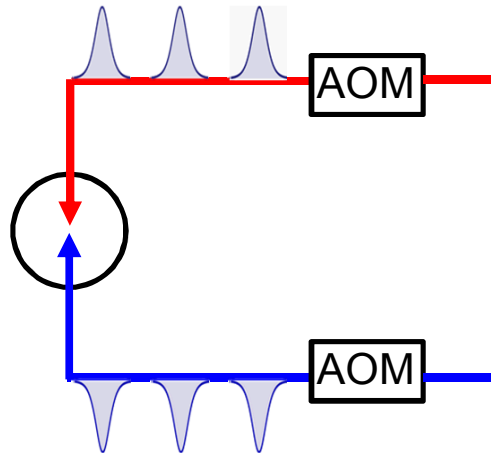
**Requirement:**

$$f_{\text{qubit}} = n f_{\text{rep}} \pm f_{\text{AOM}}$$



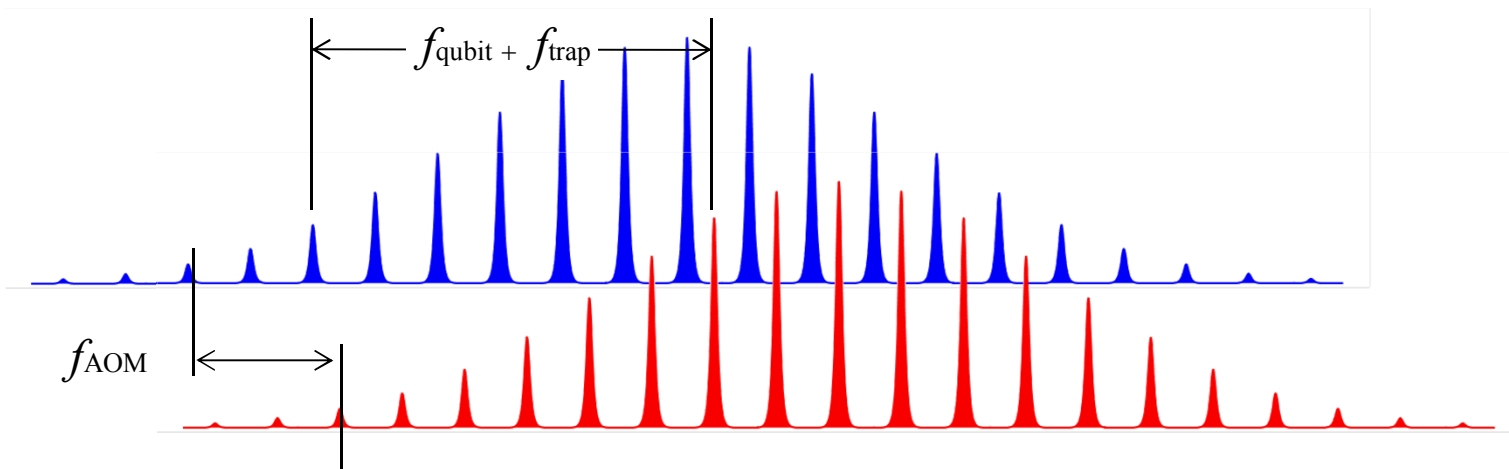
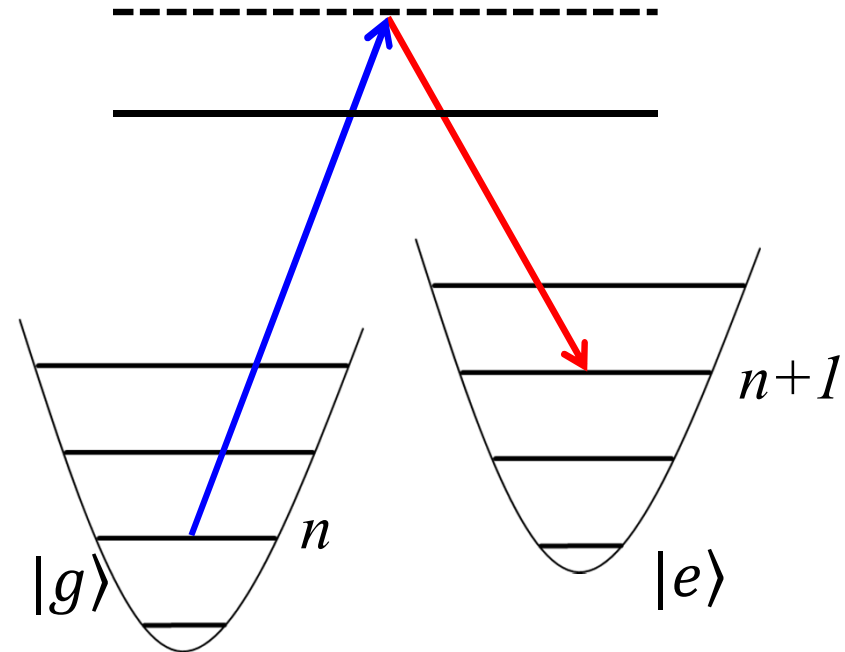
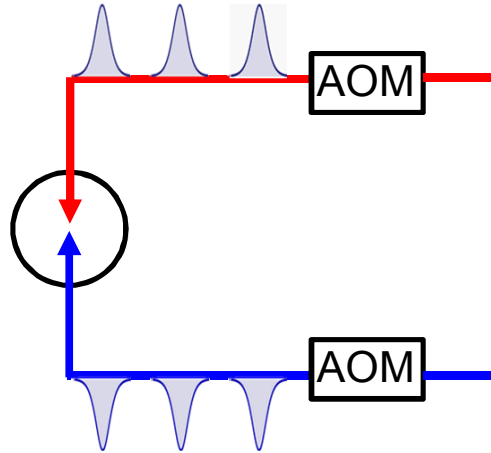


# Pulsed laser Raman transitions



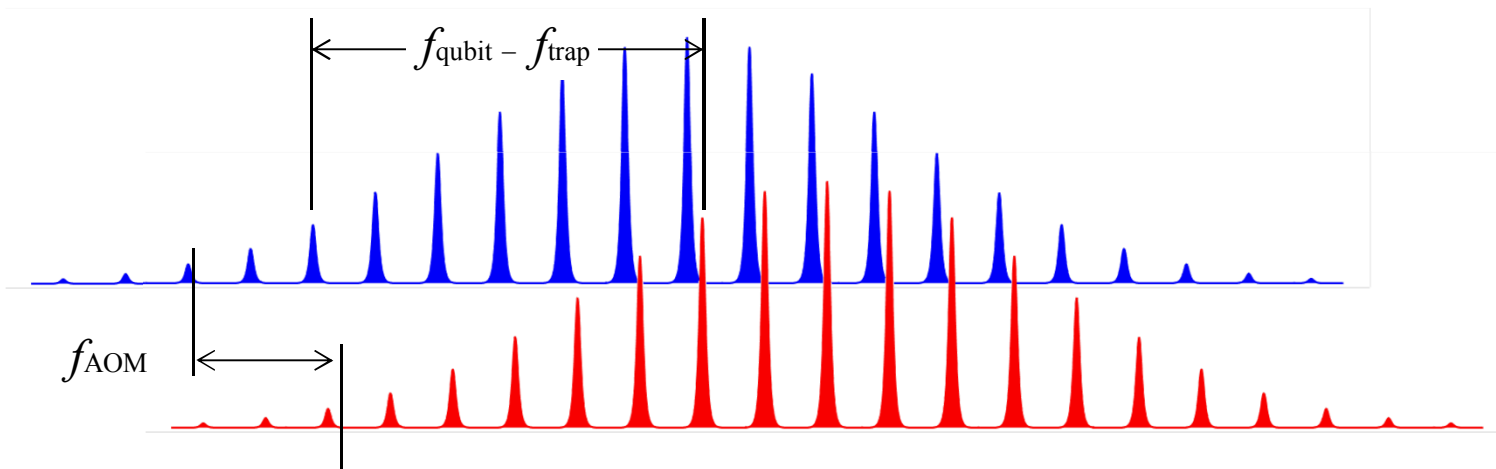
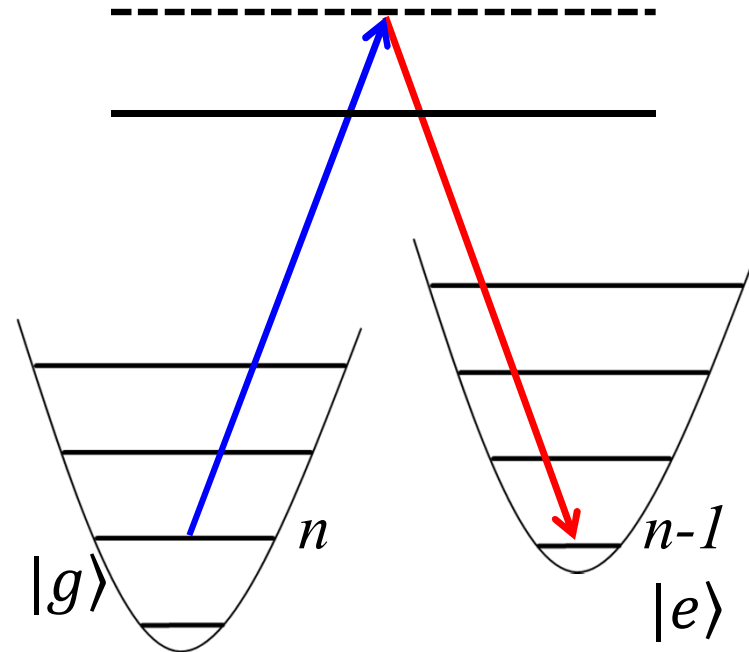
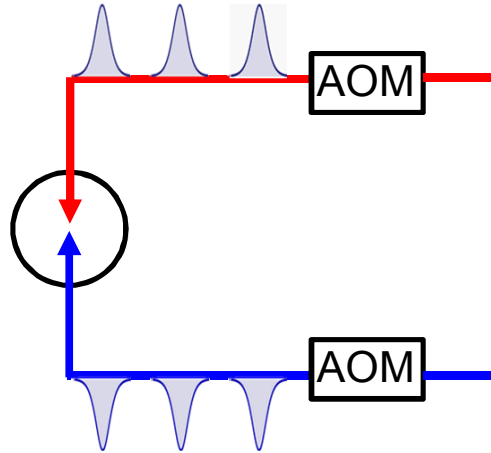


# Pulsed laser Raman transitions



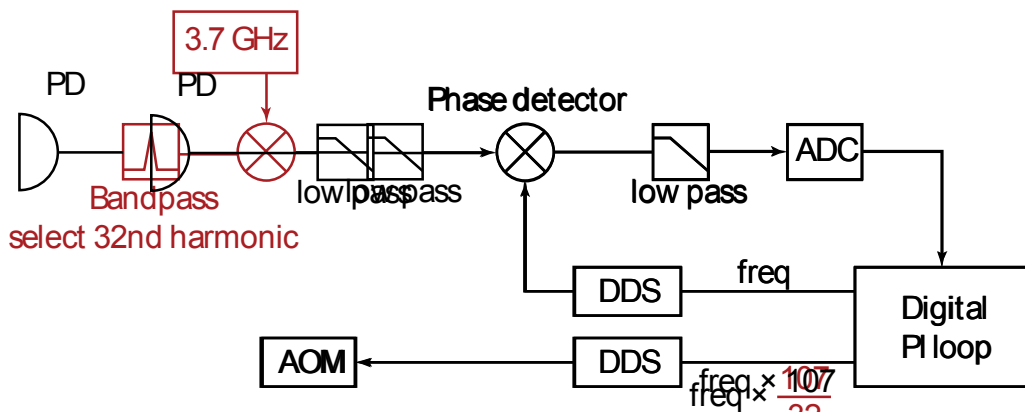


# Pulsed laser Raman transitions





# Coherence time

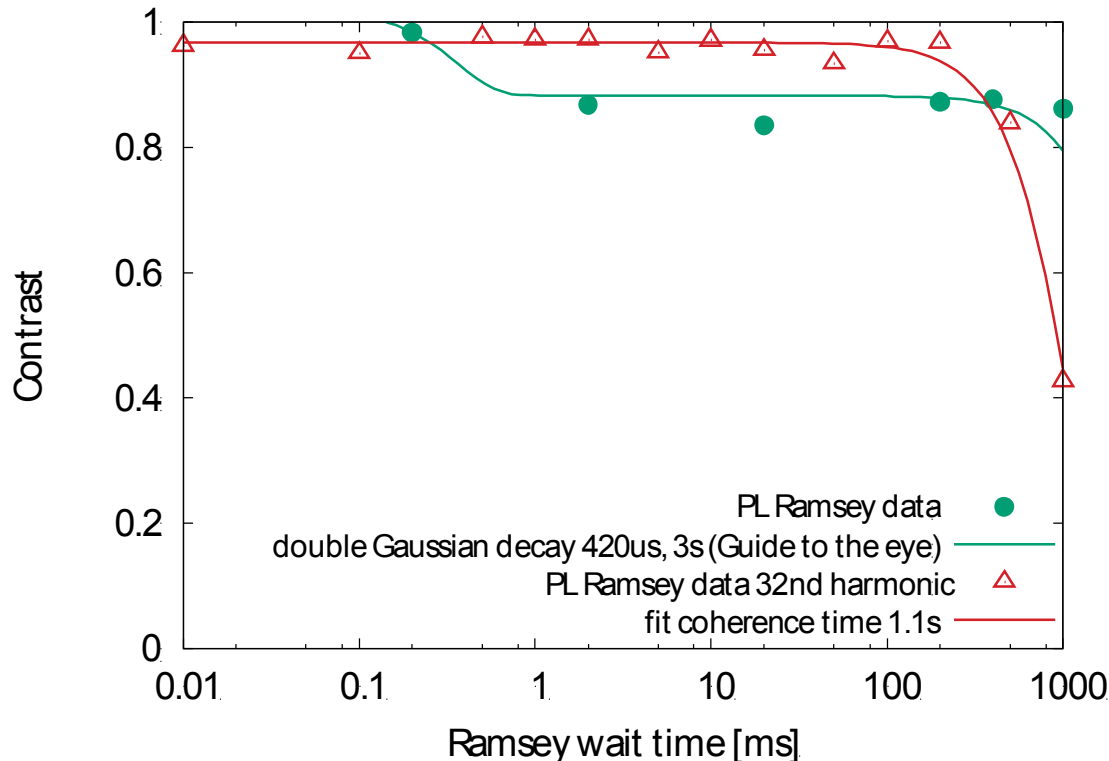


Lock at fundamental:

- 85% contrast between 100 $\mu$ s and 1s

Lock at 32<sup>nd</sup> harmonic

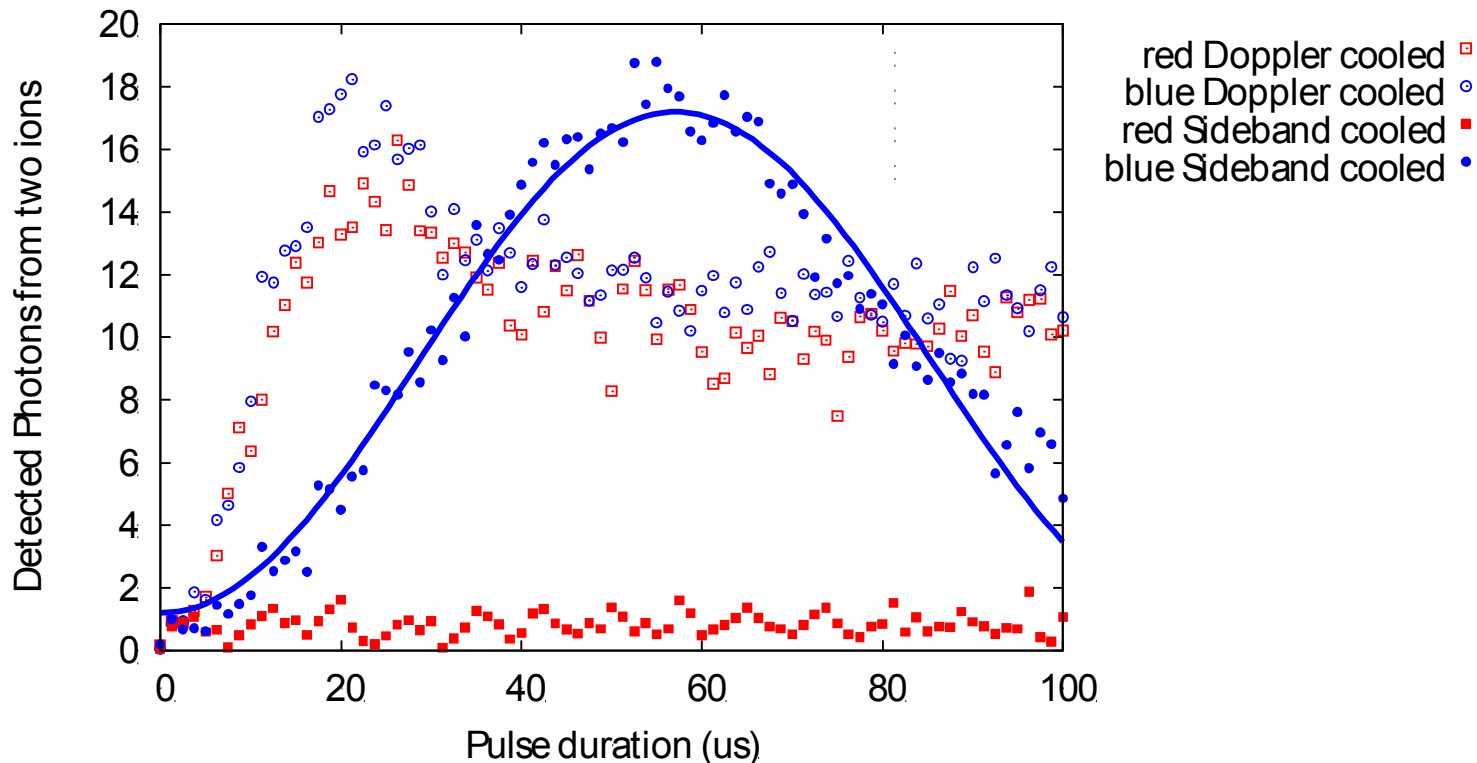
- Coherence time > 2s





# Sideband cooling

- Ground state cooling evident when red sideband cannot be driven
- Data shows ground state cooling of two ion radial tilt mode,  $\bar{n} \ll 1$





# Heating in Two Ion Chain

Transversal  
Center of Mass



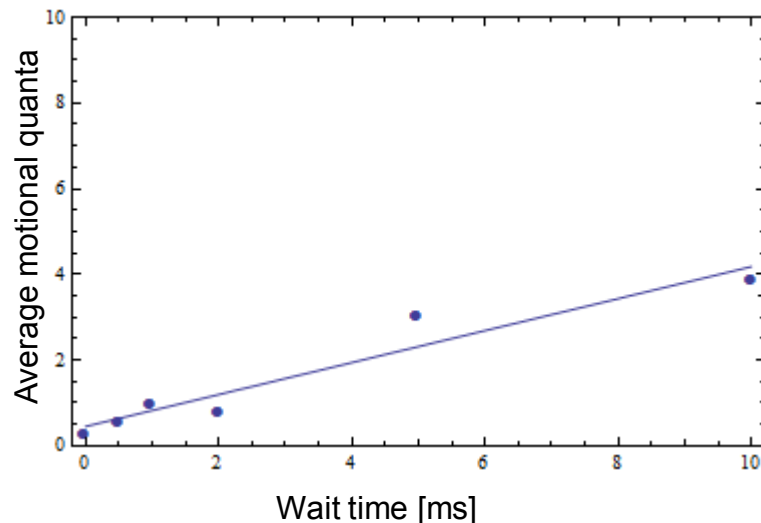
2 modes

Transversal Tilt



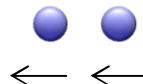
2 modes

1.94 MHz CoM

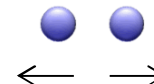


Fit: 0.4 quanta/ms

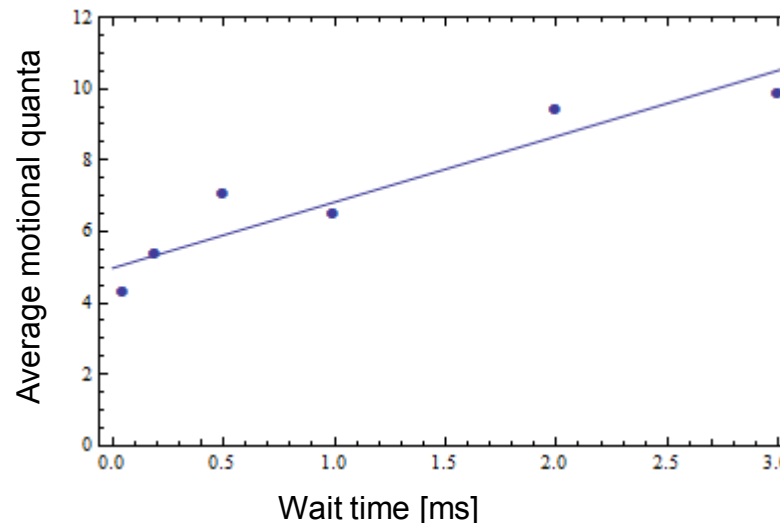
Longitudinal  
Center of Mass



Longitudinal  
Stretch



2.38 MHz CoM



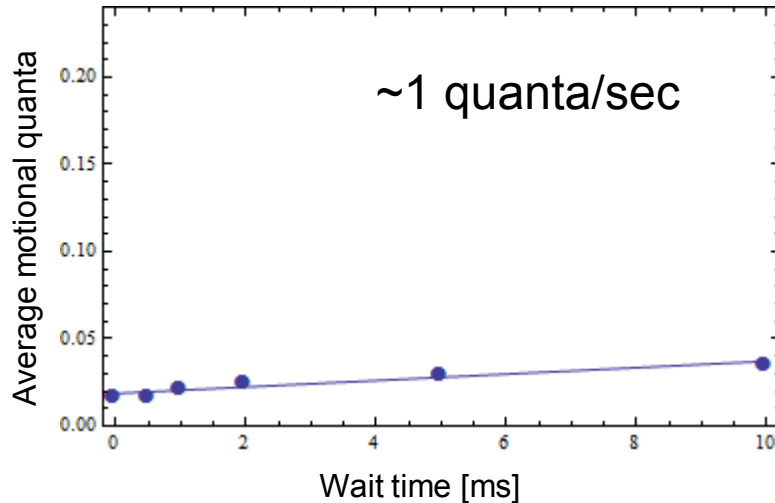
Fit: 1.8 quanta/ms

- Reduced heating to 0.3 q/ms and 1 q/ms when using battery instead of DAC
- **Currently limited by technical noise, improvements on the way**

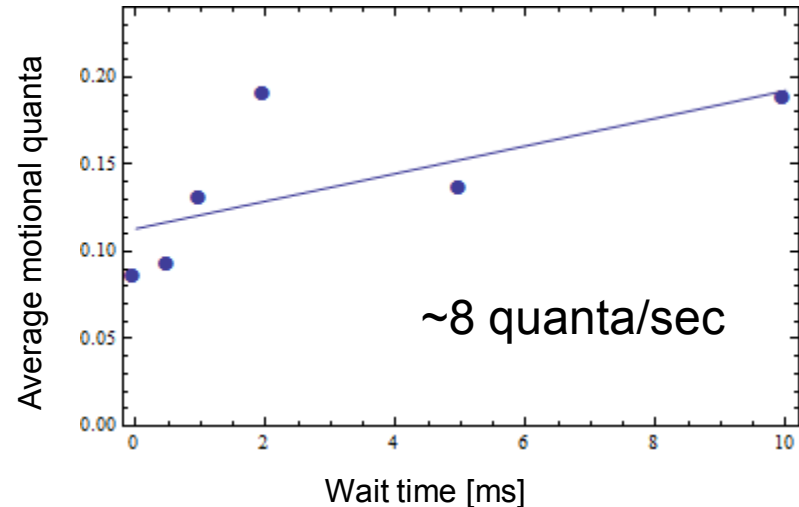


# Heating in Two Ion Chain

1.84 MHz tilt



2.32 MHz tilt

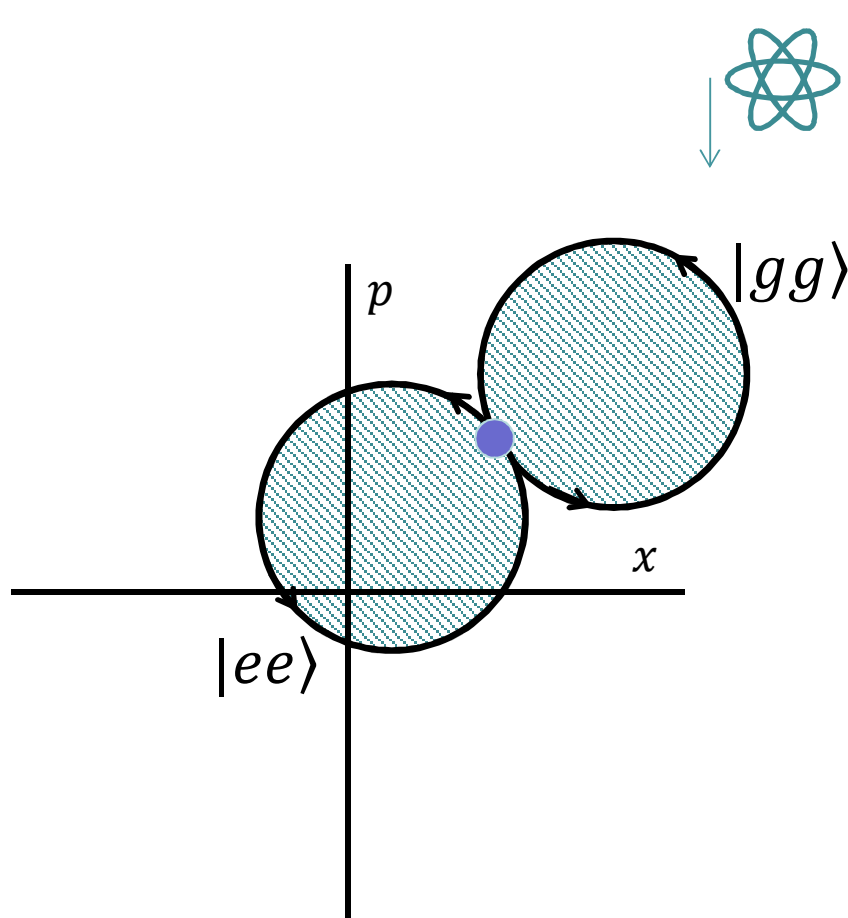


- Using tilt mode near 1.84 MHz for gate
- Lowest heating <1 quanta/sec



# Entangling Gate

Basic idea: Use common motion of the ions to mediate entanglement



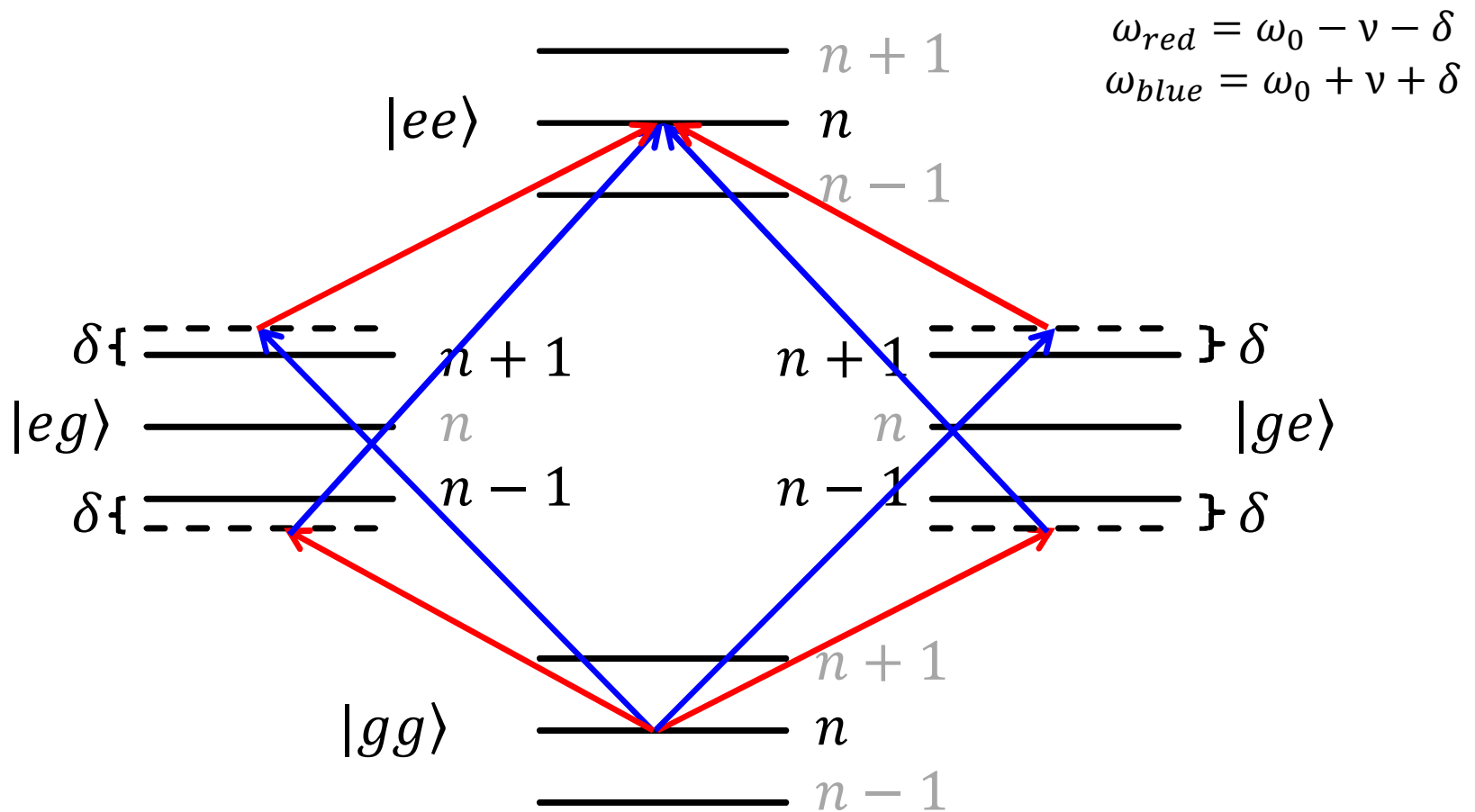
- Raman beams create *spin-dependent force*
- Force drives the ions away from and then back to their starting position
- **Spin dependent phase remains**

- [1] K. Mølmer, A. Sørensen, PRL 82, 1835 (1999)  
 [2] A. Sørensen, K. Mølmer, PRL 82, 1971 (1999)  
 [3] A. Sørensen, K. Mølmer, PRA 62, 022311 (2000)



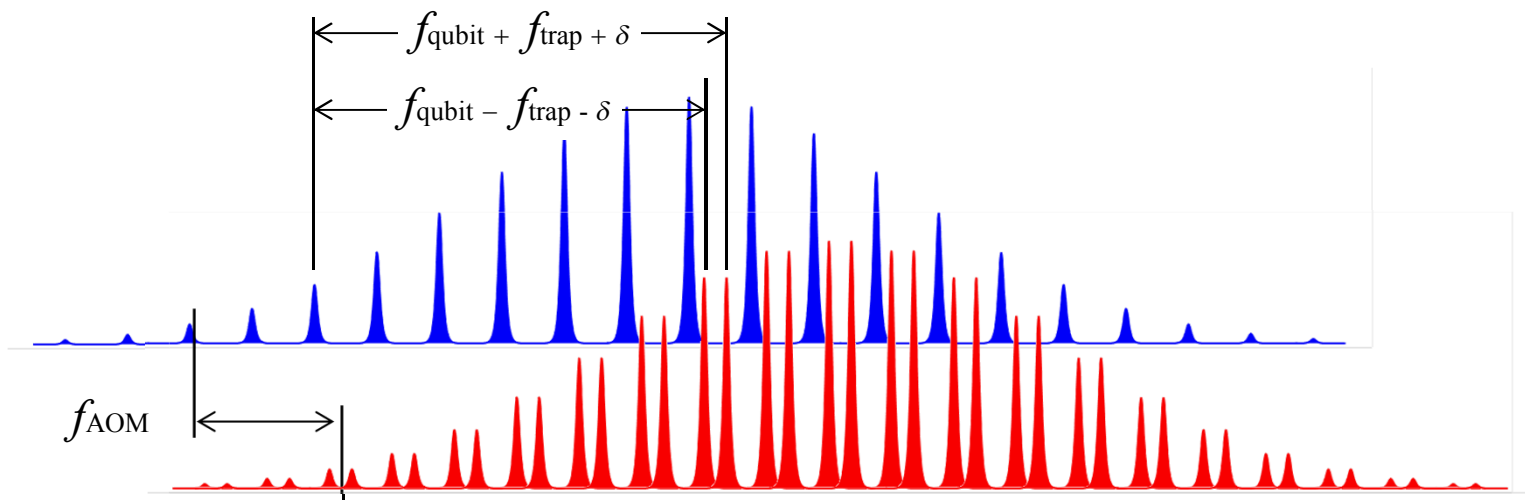
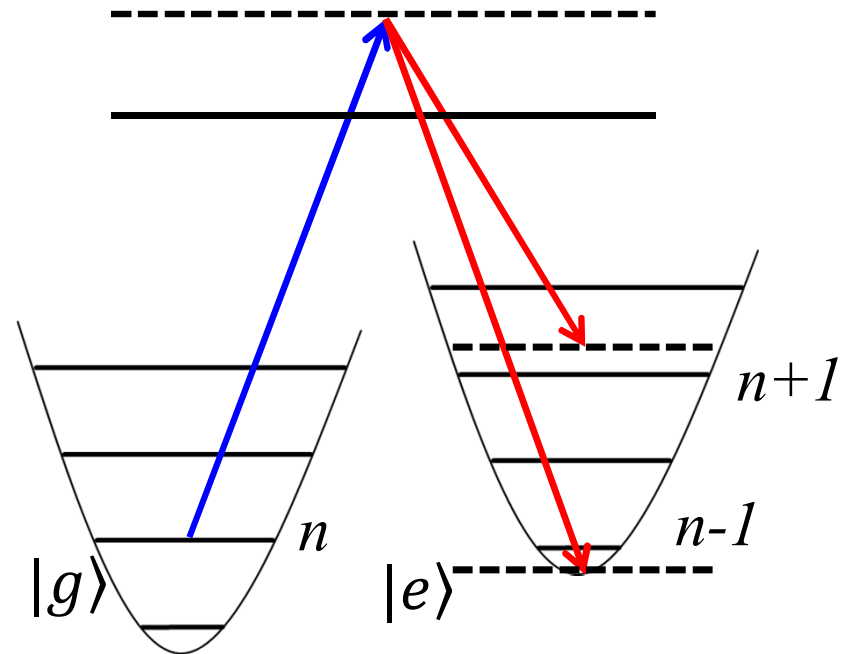
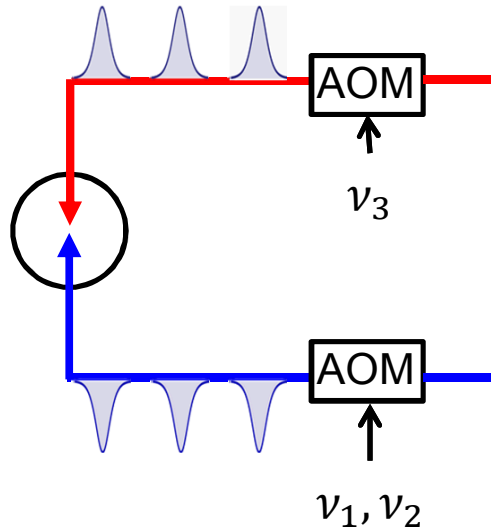
# Entangling Gate

Creating a spin-dependent force with Raman beams:  
Apply red and blue detuned sidebands simultaneously





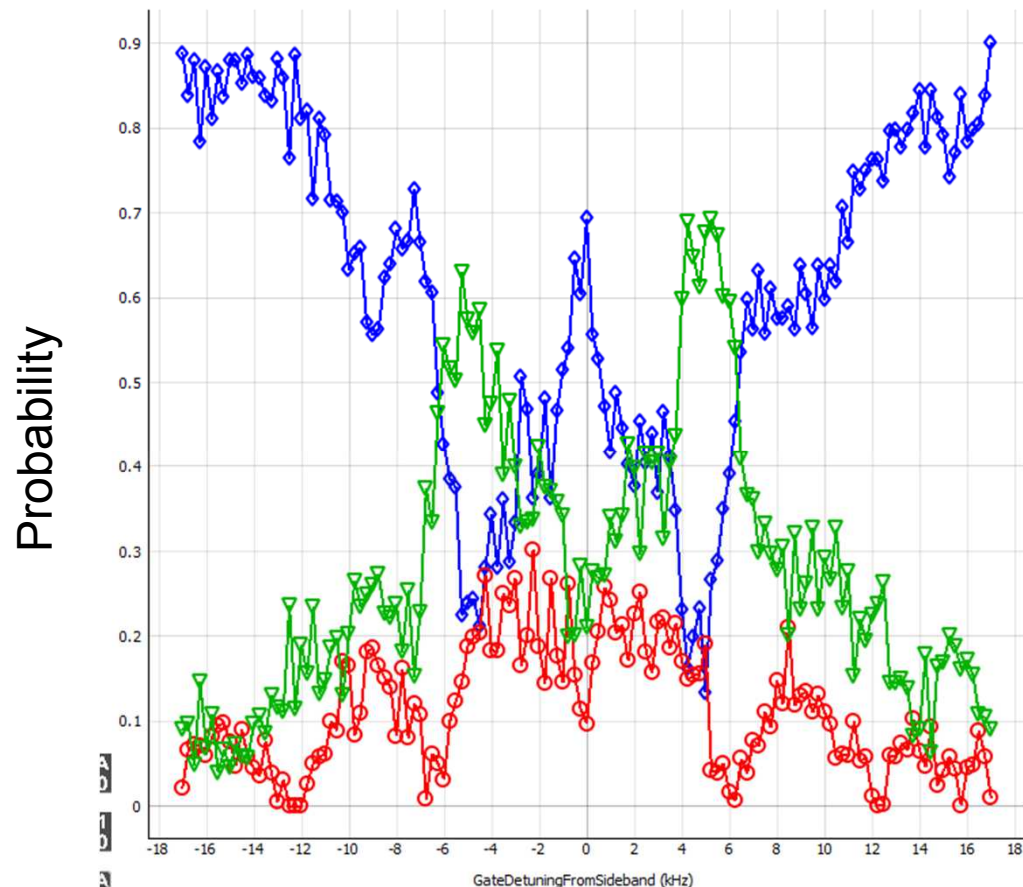
# Entangling Gate



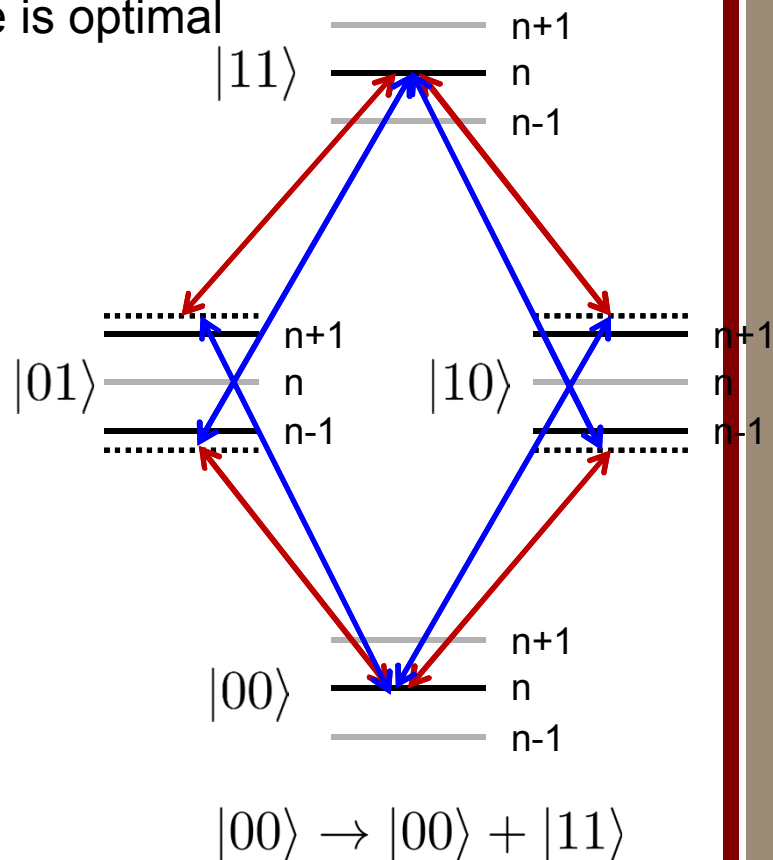


# Entangling Gate

- Scanning detuning reveals point where gate is optimal



Detuning from sideband (kHz)



Blue: Zero ions bright

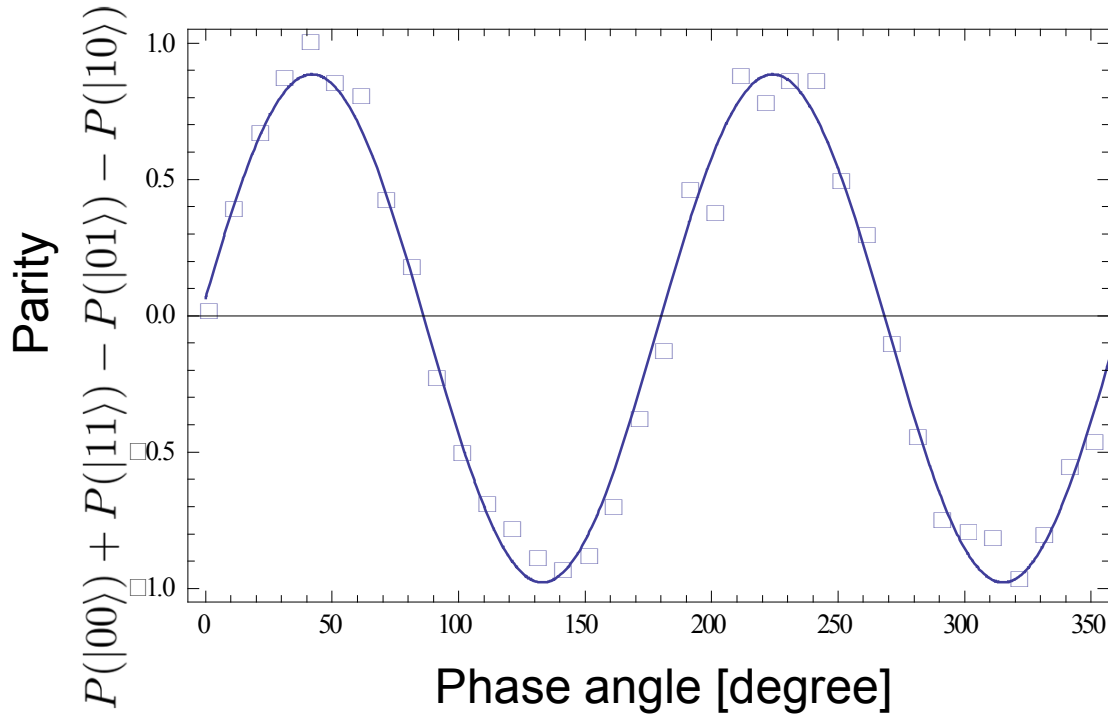
Red: One ion bright

Green: Two ions bright



# Entangling Gate – preliminary results

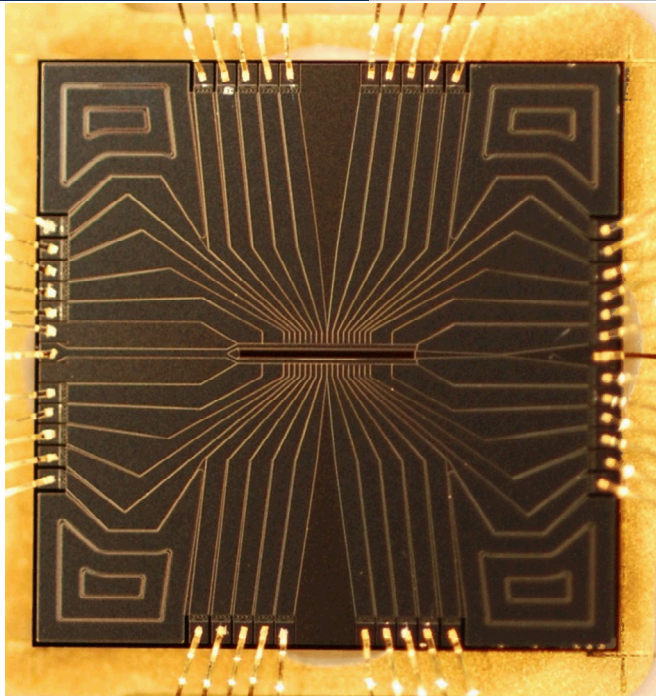
- Populations reveal diagonals of density matrix, parity scan reveals coherences
- Taken together they yield the fidelity



$$\mathcal{F} = \frac{1}{2}(P(|00\rangle) + P(|11\rangle)) + \frac{1}{4}c = 0.945$$

- Gate fidelity 94.5%
- Have yet to characterize sources of infidelity



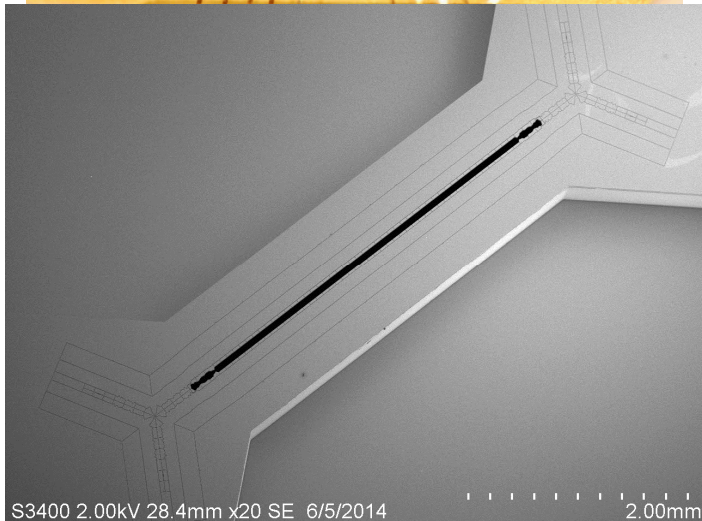


Microfabricated traps are ready for QIP

- Experiments were done in Thunderbird

Switching to HOA-2 brings advantages:

- Higher trap frequencies
- Optical access for individual addressing





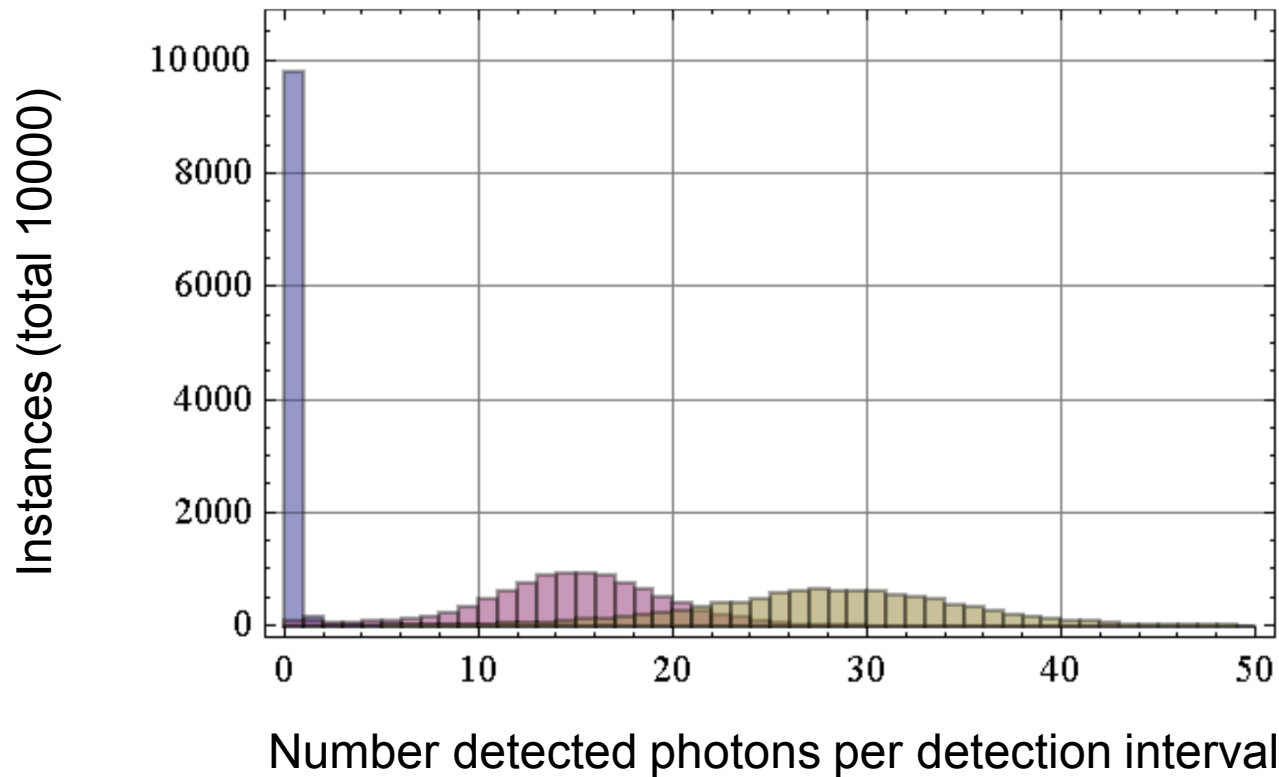
# Thank you





# State Detection using Histograms

Example histograms

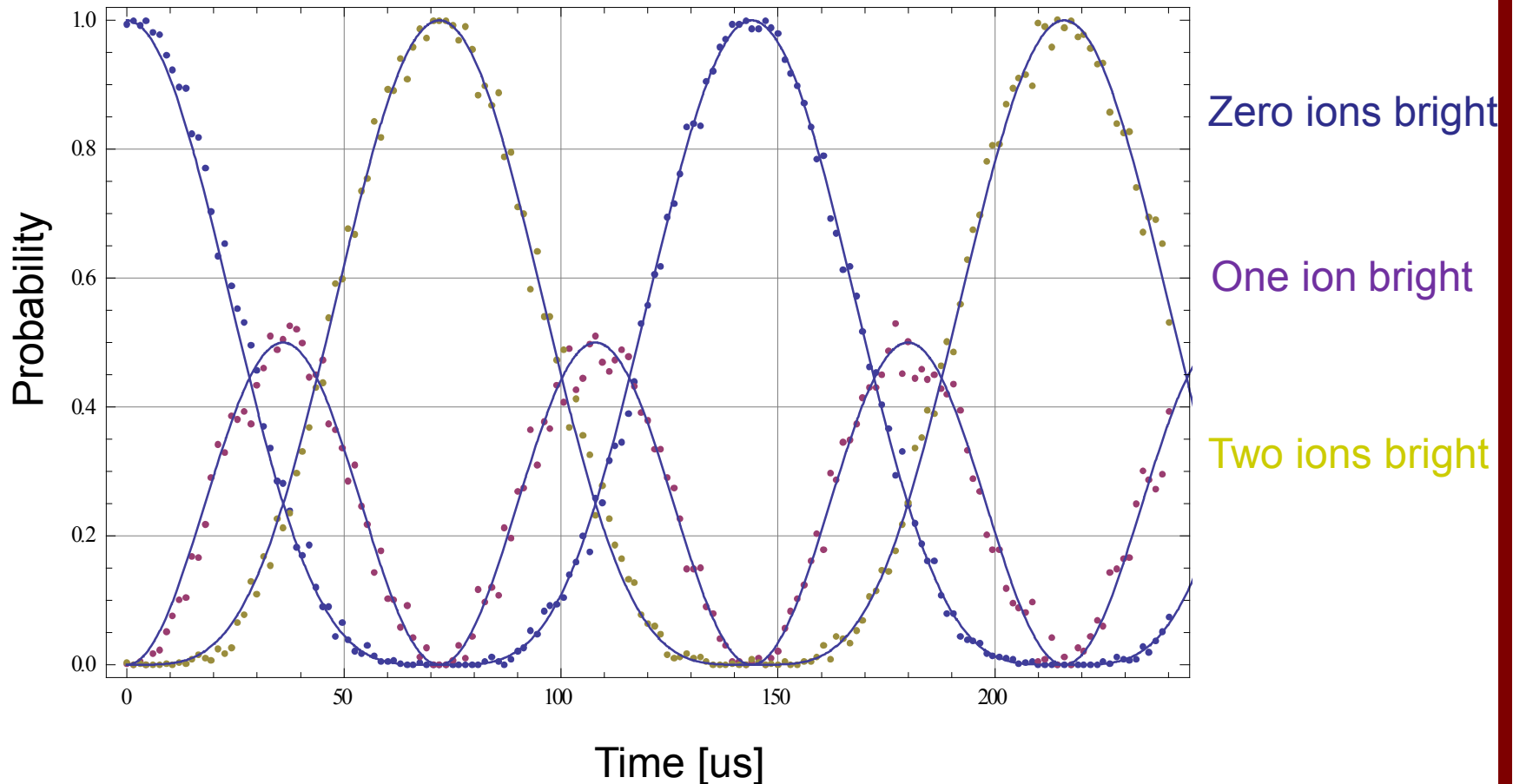


Long term plan: segmented PMT for individual state detection  
Currently limited by optical crosstalk



# State Detection Using Histograms

Global Rabi Oscillations on two ions



One parameter (Rabi time) is sufficient to simultaneously fit all three curves