

LA-UR-

12-00612

Approved for public release;  
distribution is unlimited.

*Title:* Modeling the Reliability of Complex Systems with Multiple  
Data Sources: A Statistical Engineering Case Study

*Author(s):* C.M. Anderson-Cook

*Intended for:* American Statistical Association Conference on Statistical  
Practice, Orlando, FL, Feb 16-18, 2012



Los Alamos National Laboratory, an affirmative action/equal opportunity employer, is operated by the Los Alamos National Security, LLC for the National Nuclear Security Administration of the U.S. Department of Energy under contract DE-AC52-06NA25396. By acceptance of this article, the publisher recognizes that the U.S. Government retains a nonexclusive, royalty-free license to publish or reproduce the published form of this contribution, or to allow others to do so, for U.S. Government purposes. Los Alamos National Laboratory requests that the publisher identify this article as work performed under the auspices of the U.S. Department of Energy. Los Alamos National Laboratory strongly supports academic freedom and a researcher's right to publish; as an institution, however, the Laboratory does not endorse the viewpoint of a publication or guarantee its technical correctness.

**Title:** Modeling the Reliability of Complex Systems with Multiple Data Sources: A Statistical Engineering Case Study

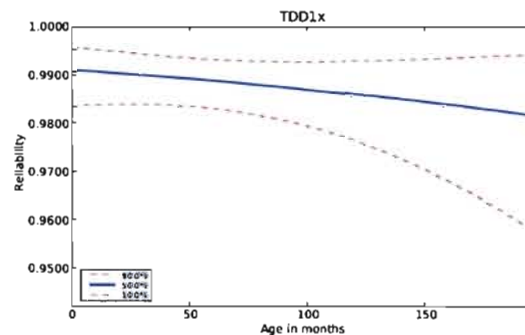
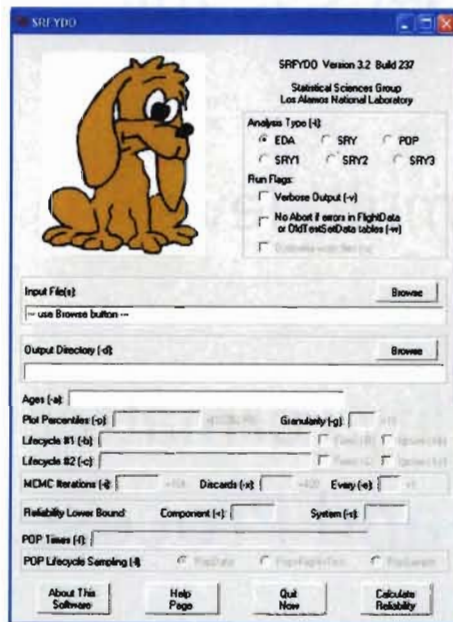
**Abstract Text:**

Estimating the reliability of complex systems with many parts and components often involves using multiple data sources, including expensive full system tests, as well as less expensive subsystem and component level tests. Using statistical methodology developed by the Statistical Sciences Group at Los Alamos National Laboratory, a process for estimating and predicting future reliability was developed. A multi-phase software tool, SRFYDO, was developed to make this process accessible and understandable to the system engineers who need to perform these analyses. In this talk, we present a short overview of the method, but focus on how the software was developed to incorporate multiple statistical tools with the goal of guiding engineers through an analysis.

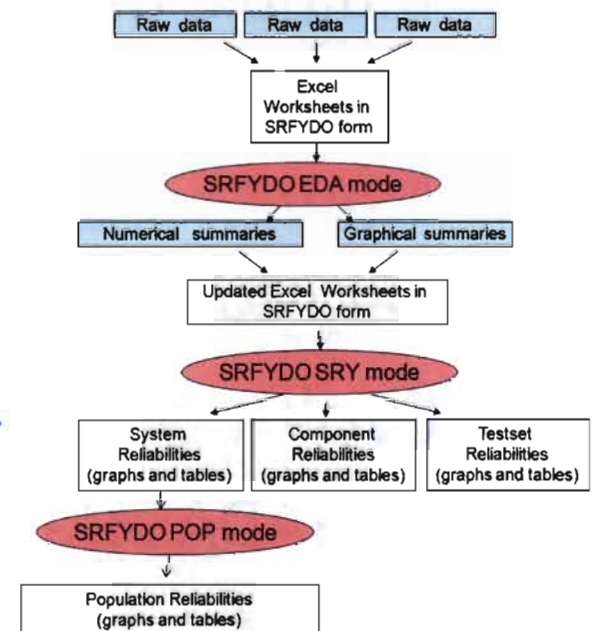
**Keywords:** Full-system data, component data, software development, SRFYDO

1: Anderson-Cook, Christine - Los Alamos National Laboratory (presenting)

# Modeling the Reliability of Complex Systems with Multiple Data Sources: A Statistical Engineering Case Study



Christine Anderson-Cook



Statistical Sciences Group, Los Alamos National Laboratory

February 2012

# Outline

- What is Statistical Engineering? - Background
- Motivation for System Reliability Approach – multiple data sources available with expensive full system tests
- New Statistical Method – Bayesian multi-level data combination
- Evolution of SRFYDO (System Reliability Formatter for YADAS Data and Output) Software and Process
- Final Product and Process
- Lessons Learned

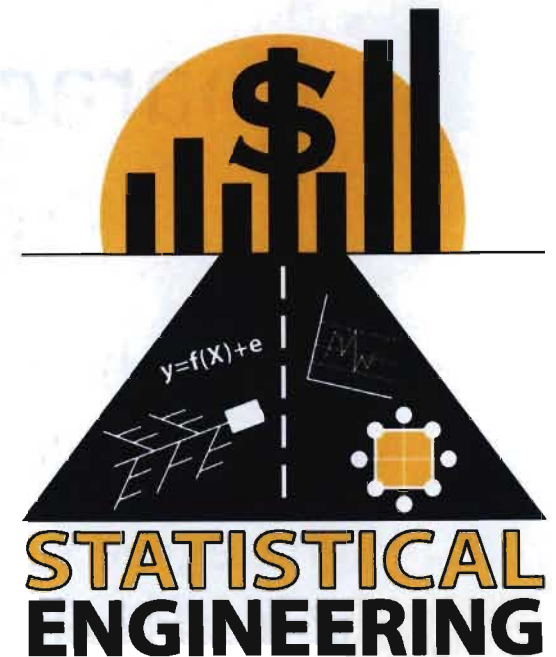
# Statistical Engineering –

What is it? and Why is it important?

- Definition: Statistical Engineering is the collaborative study and application of the tactical links between statistical thinking and statistical and discipline-specific tools with the objective of guiding better understanding of uncertainty in knowledge and decision-making to generate improved results to benefit the organization and/or society.

ASQ Statistic Division Resource Page:

<http://asq.org/statistics/quality-information/statistical-engineering>



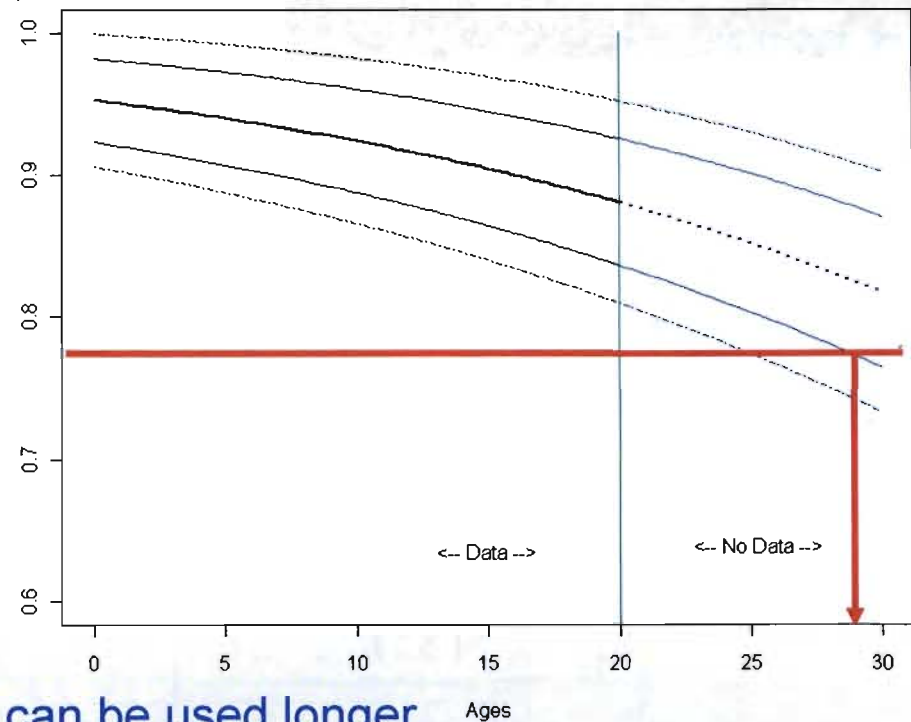
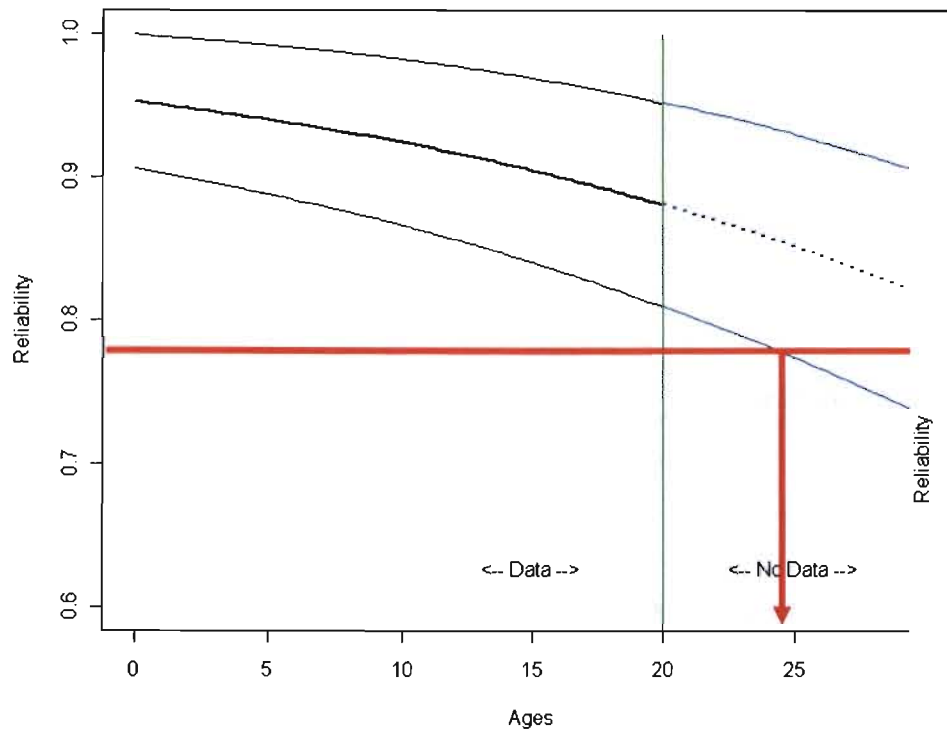
# Characteristics of a Statistical Engineering Solution

- Satisfies a high-level need of the organization.
- No known solution to the problem.
- High degree of complexity involving both technical and non-technical challenges.
- More than one statistical technique required for solution.
- Long-term success requires imbedding solutions into work processes.
- The whole is greater than the sum of the parts.
- A solid theoretical foundation is required to guide development of a solution.
- The solution can be leverage to similar problems elsewhere



# Motivation for New System Reliability Approach

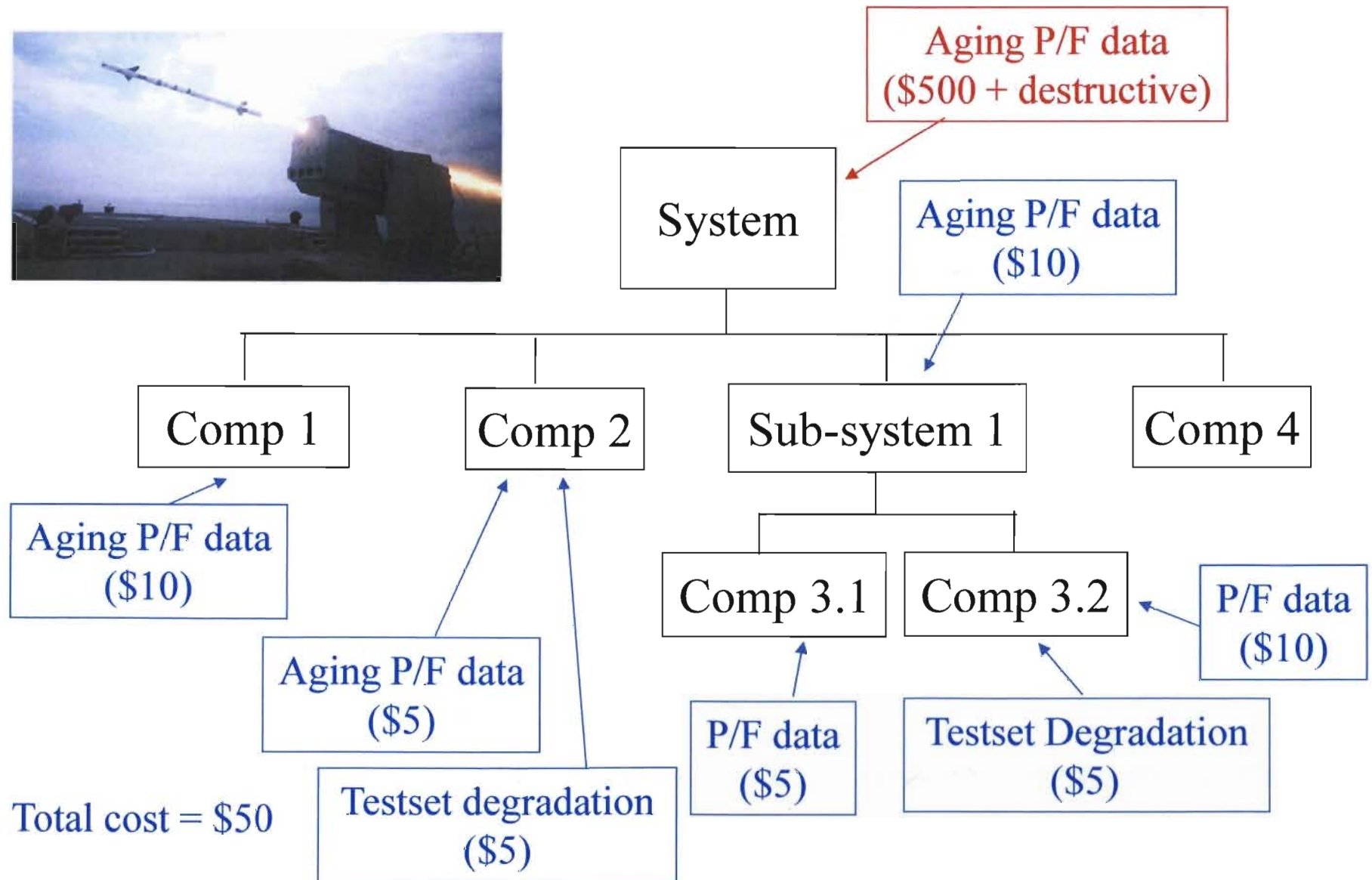
- Problem: Insufficient system level data to estimate system reliability to the required precision



Better analysis increases precision → units can be used longer

Solution requires engineering knowledge of system structure and components

# Motivation (continued)



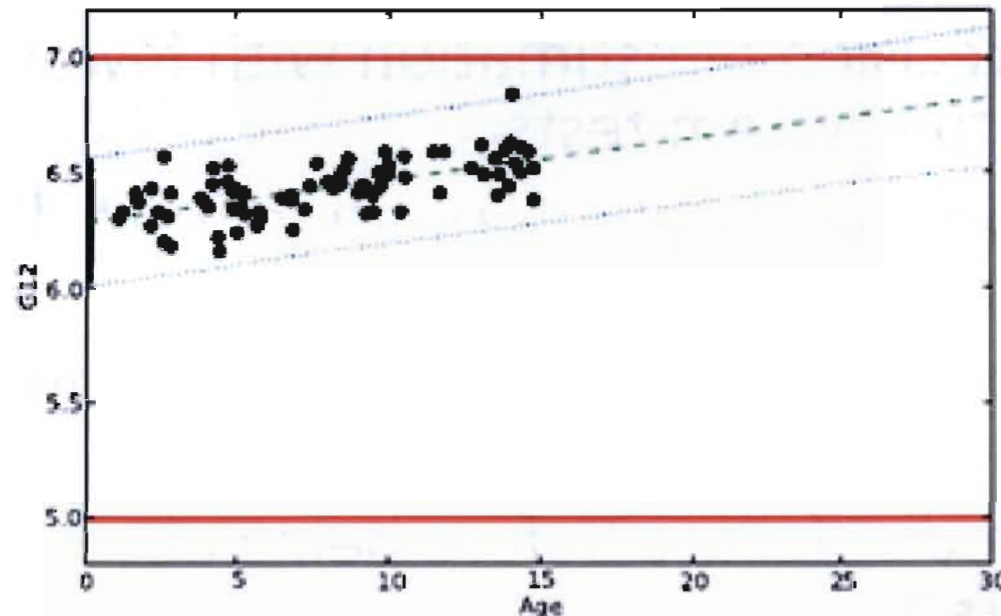


# Advantages of SRFYDO Approach

- Uses data already available and thought to be relevant to predict reliability
- Improves precision of estimation with fewer destructive full-system tests
- Check on consistency of information from different data sources
- Flexibility to incorporate partial information into model
- Ability to predict failure before being observed in full-system test
- Component level reliabilities – leverage from different versions of system + better understanding

**Disadvantage:** More complex statistical method requiring more engineering knowledge to obtain results

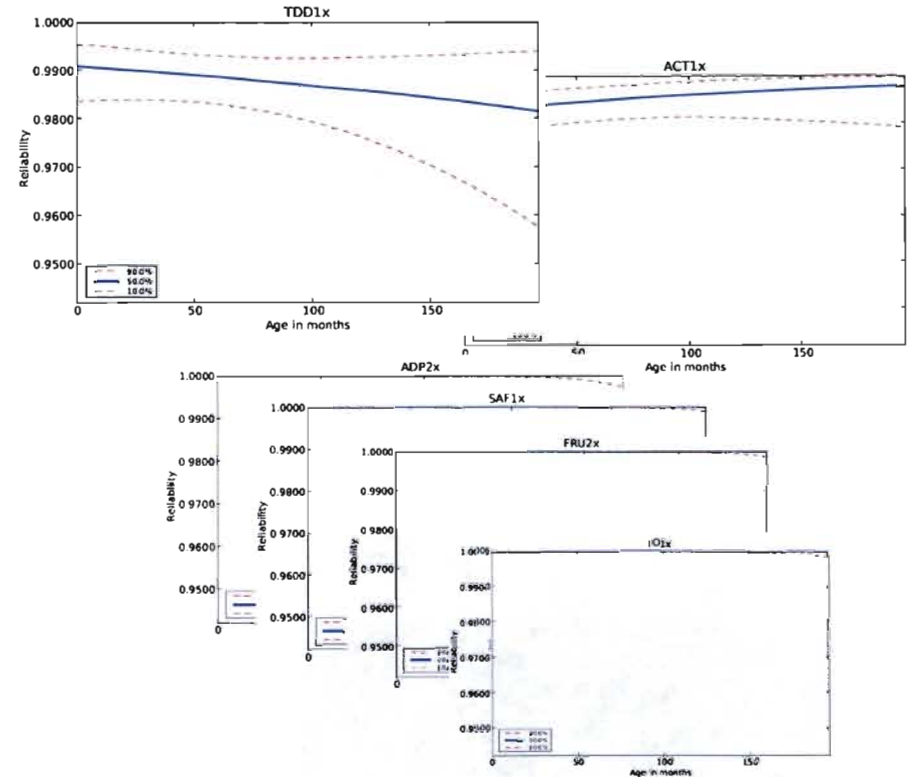
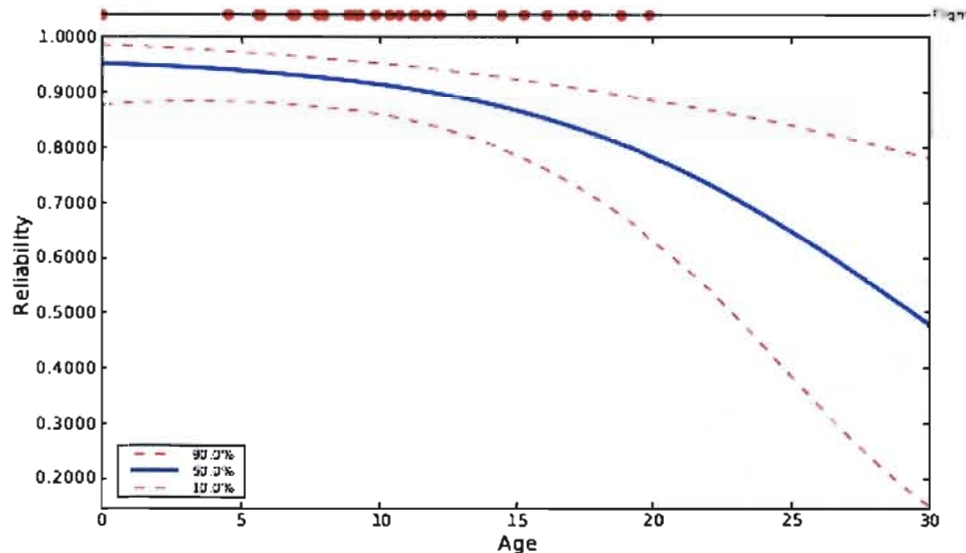
Advantage: Ability to predict failure before being observed in full-system test



- Because we can track a trend in some of the continuous measurements, we can anticipate when failures might start to occur, before they actually have been observed

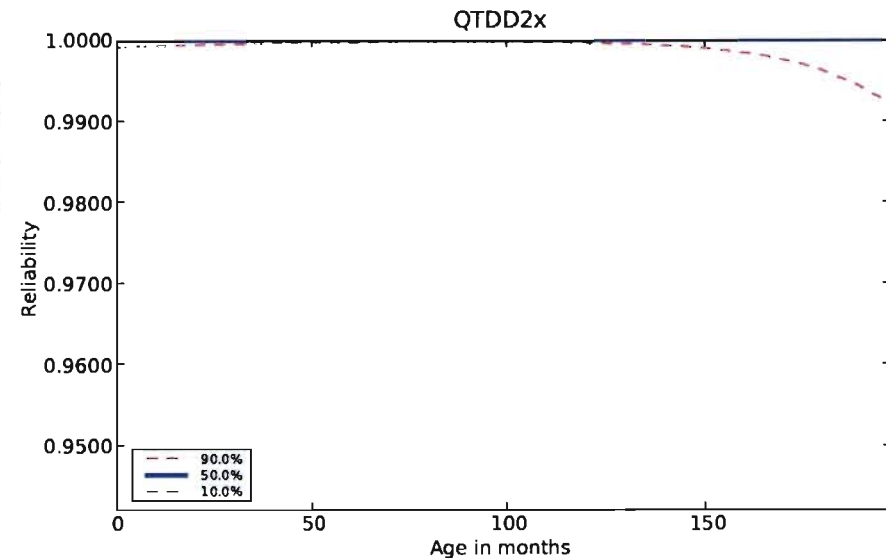
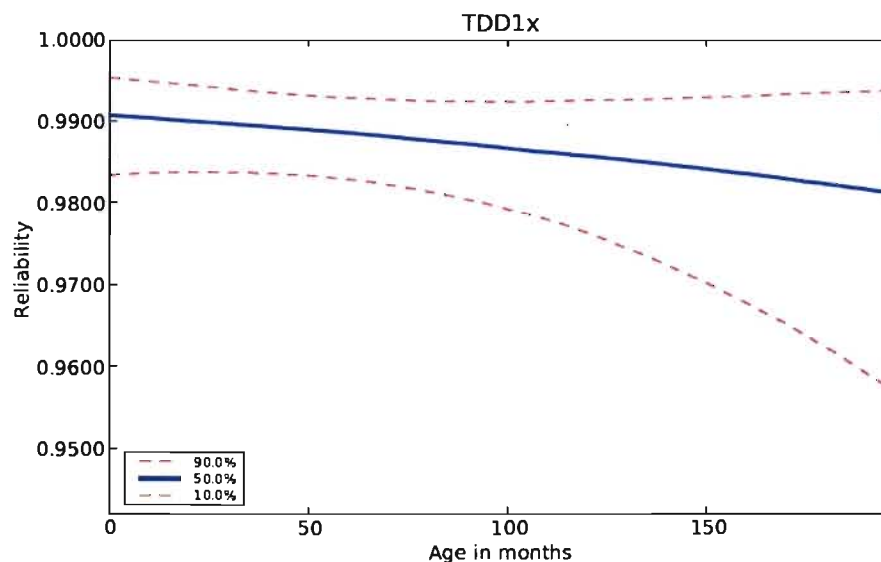
# Advantage: Component Level Summaries

- Better understanding of system and important drivers of system reliability
- Ability to identify critical components and critical specs to implement corrective action



# Advantage: Component Level Summaries (cont'd)

- Ability to compare different versions of the same component



# Advantage: Component Level Summaries (cont'd)

- Ability to leverage data across different variants with common components
- Data used to estimate reliability:
  - SAF2x + 21 others → 75+47 = 122
  - ADP1x + 6 others → 75
  - ADP2x + 6 others → 47

%VariantDef			
Version	Component		
Lot4_5	SAF1x	Lot6_7	SAF1x
	WH1x		WH1x
	ACT1x		ACT1x
	BPS1x_Rear		BPS1x_Rear
	RD11x		RD11x
	FinSquib1x		FinSquib1x
	MBC1x		MBC1x
	ECU2x		ECU2x
	ADP1x		ADP2x
	Harness1x		Harness1x
	FP1x		FP2x
	FRU1x		FRU2x
	HH1x		HH1x
	IFR1x		IFR2x
	IO1x		IO2x
	LS1x		LS2x
	PM1x		PM1x
	RC1x		RC2x
	RT2x		RT2x
	IRU2x		IRU2x
	TDD1x		TDD1x
	BPS1x_Front		BPS1x_Front
	SS1x		SS1x
75	XMTR2x	47	XMTR2x
	AFD1x		AFD1x
	RocketMotor1x		RocketMotor1x
	RFA1x		RFA1x
	TIVs1x		TIVs1x
	RFPIx		RFPIx

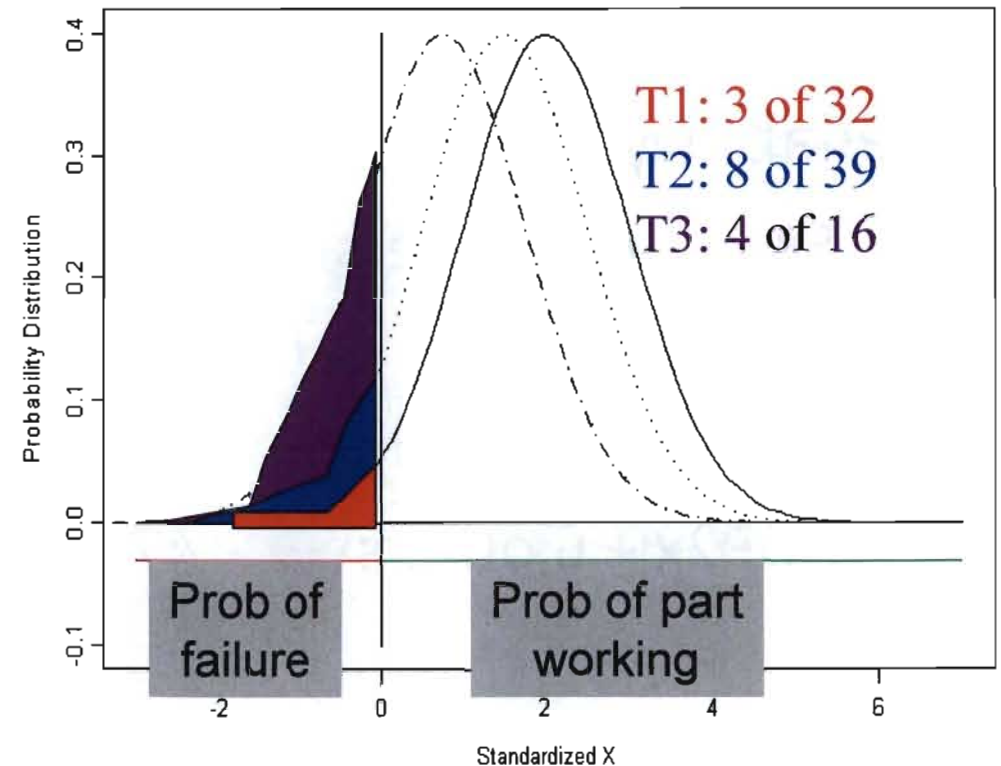
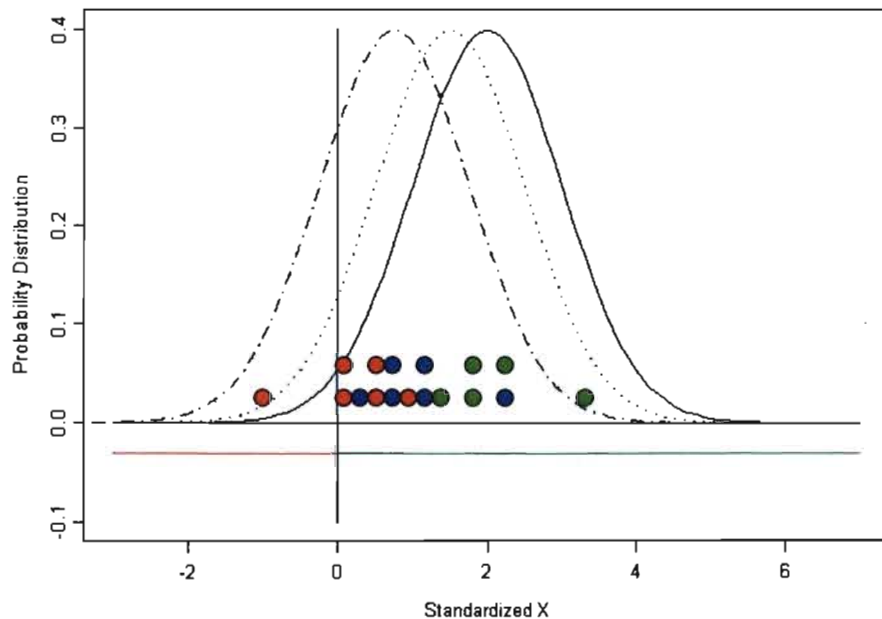


# Basic Building Block

- Here we have two potential sources of information about this component:

From testset data, we obtain the mean of the characteristic at each time

From the full system data, we obtain a proportion of success/failure at each time





# Statistical Formulation

- For the probability that a particular component, say component with spec 1, will function correctly

$$p_1(x) = \Phi\left(\frac{\beta_{0,1} + \beta_{1,1}x - \theta_1}{\sqrt{\gamma_1^2 + \sigma_1^2}}\right)$$

$\Phi$  = cdf of Normal distribution

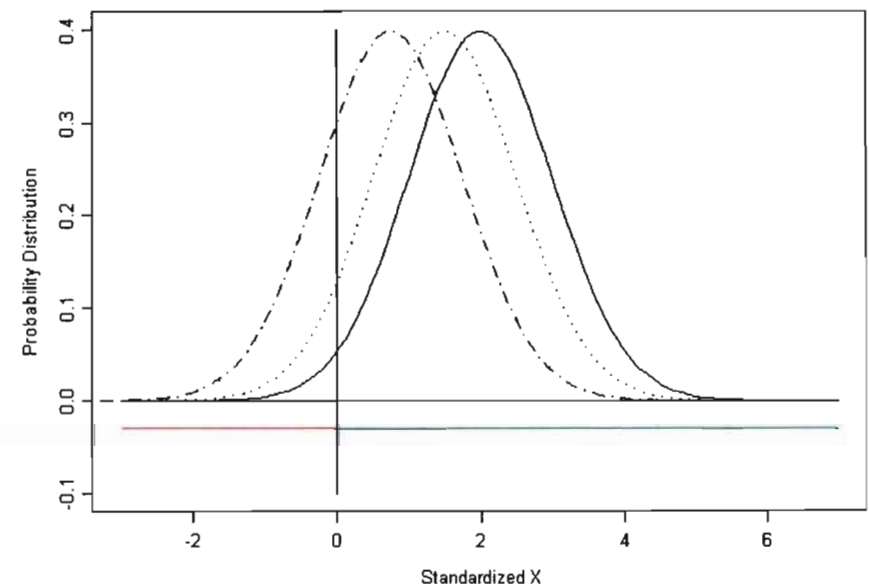
$\beta_{0,1}$  – initial mean of testset distribution

$\beta_{1,1}$  – rate of shift of testset distribution

$\gamma_1^2$  – variance of testset distribution

$\theta_1$  – discrepancy between means of spec and full system

$\sigma_1^2$  – additional variance from full system distribution



# Background of Users

- Subject Matter Experts (SME) on particular system
  - System Engineers
  - Data Analysts
- Little or no formal statistical training



- Customers
- Department of Defense
  - NSWC Corona (RAM, ESSM, SeaSPARROW)
  - NSWC Yorktown / Indian Head (AMRAAM)
  - AMCOM/AMRDEC (Hellfire, Stinger)
  - MCPD Fallbrook (TOW)
- Department of Energy
  - LANL Enhanced and Core Surveillance Campaign

# Evolution of SRFYDO

## 1. Development of methods

- LANL statisticians sat down with team of SMEs
  - Develop system model (identify components and how connected, map available data to components, obtain priors for analysis)
  - Statisticians did analysis
  - Sat down with SMEs to interpret results, fine-tune model

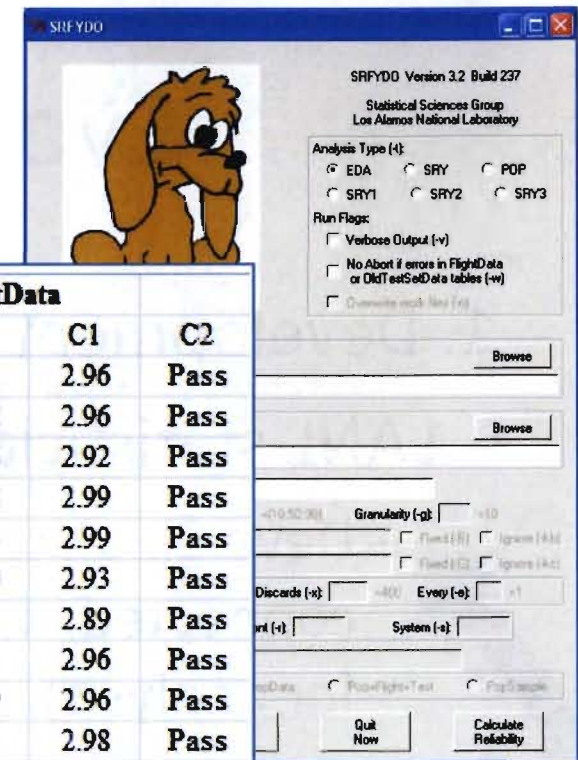
### Characteristics:

- Helpful for development of new methodology – key problems identified
- Long lag for engineers until methods available
- New data added to analysis as it became available
- Methodology implemented with unfriendly code (usable only by creators)
- Very time intensive – not scalable to many systems

# Evolution (continued)

## 2. Development of prototype of SRFYDO

- Formal analysis from GUI
- EXCEL spreadsheet



%ComponentDef					0	3.09	2.96	Pass			
Component	SpecName	SpecType	LowerSpec	UpperSpec	0	3.11	2.98	Pass			
Control	%FlightKey				2	3.16	2.62	Pass			
	Result	Variant	%FlightData		2			Pass	Armament		
	Success	Block1	Missile	Age	NumTrans	Variant					
	Success	Block2	891230	3.26	9	Block 1	2	3.19	2.64	Pass	1
Guidance1	Success	Block3	891060	3.3	15	Block 1	2			Pass	1
	Dud	Block1	891064	4.51	17	Block 1	2		2.6	Pass	1
	Dud	Block2	891001	4.65	15	Block 1	2.06	3.23		Pass	2
Guidance2	Dud	Block3	%PriorSystem								
	Crash	Block1	Age	NumTrans	Variant	WorstRel	LikelyRel	BestRel			
Propulsion1	Crash	Block2	0	0	Block1	0.9	0.97	1			
Propulsion2	Crash	Block3	0	0	Block2	0.9	0.97	1			
TargetDetection	MissTarget	Block1	0	0	Block3	0.9	0.97	1			
Armament	MissTarget	Block2	20	49	Block1	0.7	0.85	0.9			
	NoExplosion	Block1	20	49	Block2	0.65	0.8	0.9			
	NoExplosion	Block2	20	49	Block3	0.65	0.8	0.9			
	Undiagnosed	Block3	%end								
	Undiagnosed	Block1	891044	12.18	37	Block 1	Success	3	3		
	Undiagnosed	Block2	891004	12.38	42	Block 1	Success	3	3		



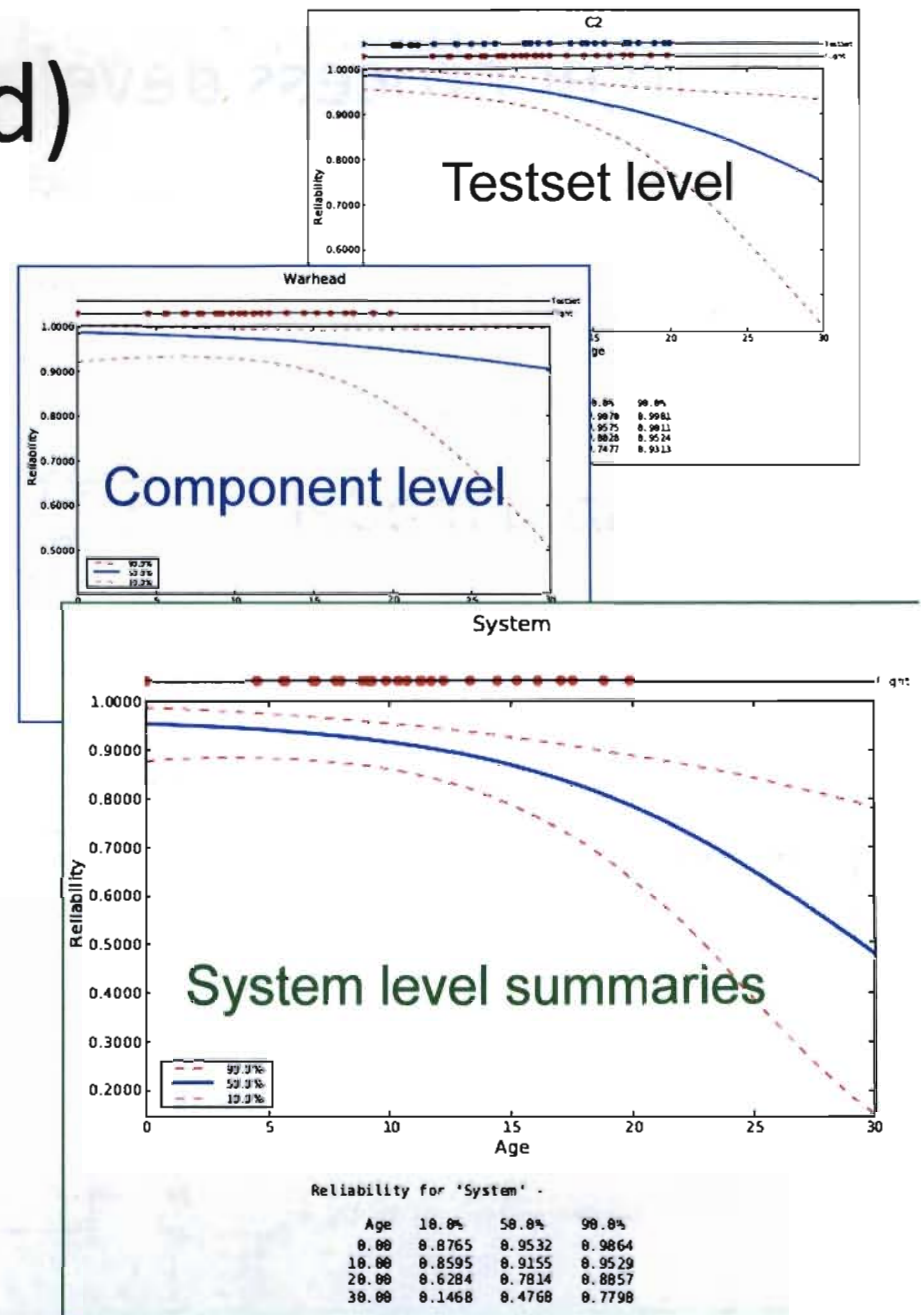
# Evolution (cont'd)

- Output as PDF and flat text

## Characteristics:

- SMEs able to function more independently
- Much more timely
- Many requests for special summaries (often integrated into SRFYDO later)

- When applied to new systems, system modeling was often difficult
- Much of data and model assumption checking that LANL did in early stages was not happening (constructing summaries in own software was easy to skip)

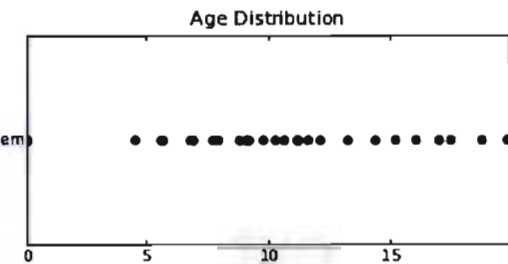


### 3. Larger process developed with EDA stage in SRFYDO

- EDA graphics
- Sanity checks
- Itemized model

#### Stage 1: Understanding System and Data

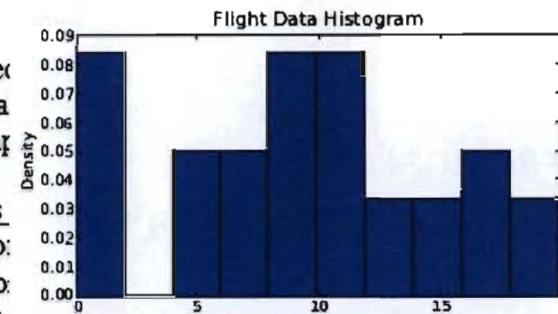
- Collect engineering knowledge about the system
- Identify how components are connected
- Determine how available data may be used
- Identify and collect relevant lifecycle data
- Quantify existing knowledge about the system in the Bayesian priors



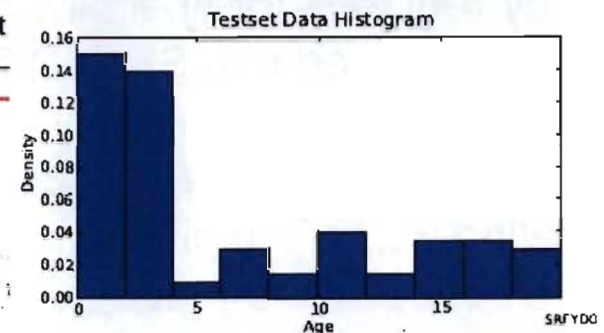
data included

#### Stage 2: Exploratory Data Analysis

- Perform error checking for correct data
- Generate numerical and graphical summaries of data to assume



errors



```
#####
EDA Analysis for "EG1.xls" (in EDA#01)
Thu, 17 Jun, 2010 09:35:38
#####

***** Lifecycle Range Summaries *****

Age:      min      max      avg
Control   0.00     19.96    6.88

***** Component-Level Summaries *****

Control   TestSet(Age>0)      F1: 30:
-MARGINAL-> C1 = 30 (20): 100.0%(100.0%)
              C2 = 50 (40): 94.0%(92.5%)
              TestSet Total: 94.0% (92.5%)

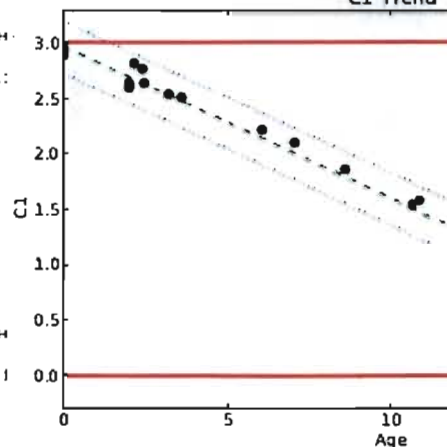
Motor     M1 = 20 (10): 100.0%(100.0%)
-WITHHOLD-> TestSet Total: 100.0%(100.0%)

Warhead   29:

***** System-Level Summaries *****

System    TestSet(Age>0): 94.0% (92.5%)
          Pass = 27:
          F4 = 1:
          F3 = 1:
          F2 = 1: 3.3%
```

Model Assumptions  
numerical summaries of data  
graphical summaries of data  
match requirements  
select appropriate subset of data  
C1 Trend



SRFYDO)  
by SRFYDO, phase #1)  
estimates for IIT model (by

model parameter estimates to generate summary tables and plots for system, component and testset measure reliabilities (by SRFYDO, phase #3)



The assumptions of the model are listed below:

- System Structure
  1. System is a series system.
  2. Only critical testset measures are included in the analysis.
  3. Stockpile of systems is a homogeneous population (or we have lifecycle measures to distinguish between sub-populations).
- Matching Data Types
  4. Full system (flight) tests are considered the most accurate assessment of system reliability.
  5. Surrogacy assumption (systems selected for flight and testset tests have similar lifecycle properties and can be sensibly combined into a single analysis).
  6. Testset data limits correspond to operational limits for what is required of component during a full-system test.
- Testset data:
  7. Linear shift as component ages.
  8. Data at a given time are approximately normally distributed (symmetric, non-extreme outliers).
  9. Only a single operational limit is important for failure.
- Lifecycle covariates
  10. Lifecycle covariates not highly correlated.

Process for verifying assumptions:

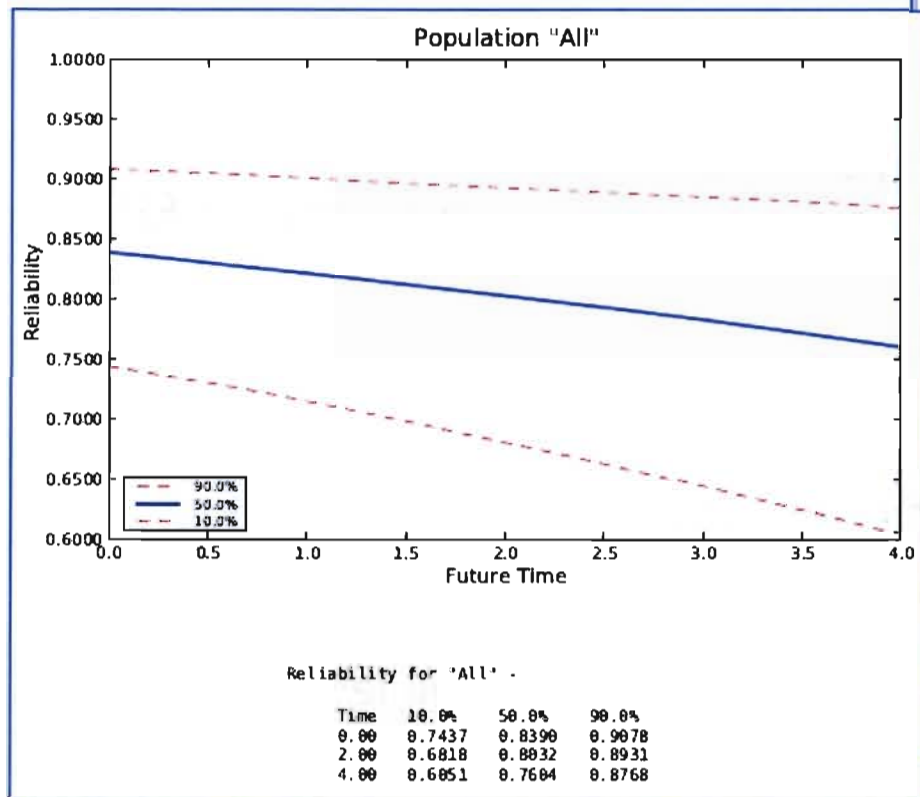
- Engineering knowledge
- Examining summaries from EDA
- Both

#### Characteristics:

- SMEs able to function more independently
- Many more discussions about assumptions and boundaries of where model appropriate
- Many fewer re-analyses (huge time-saving)
- More scalable – getting a new system ready for analysis more timely
- SME gaining confidence and expertise with method

## 4. New methodology added

- Population reliability for group of systems added (POP stage)



%PopData
Age
12.7
18.6
17.2
14.7
19.6
16.1
17.3
13.5
11.8
12.3
12.7
18.3
19.9
19.5
18.9
20
17.5
15.3
12.2
11.9

SRFYDO Version 3.2 Build 237  
Statistical Sciences Group  
Los Alamos National Laboratory

Analysis Type (-t):  
☒ EDA   ☐ SRY   ☐ POP  
☐ SRY1   ☐ SRY2   ☐ SRY3

Run Flags:  
☐ Verbose Output (-v)  
☐ No Abort if errors in FlightData or OldTestSetData tables (-w)  
☐ Overwrite work files (-o)

Input File(s):

Use Browse button ---

Output Directory (-d):

Log File(s) (-a):

Plot Percentiles (-p):  Granularity (-g):

Recycle #1 (-b):  ☐ Fixed (-B) ☐ Ignore (-I.b)  
 Recycle #2 (-c):  ☐ Fixed (-C) ☐ Ignore (-I.c)

CMC Iterations (-i):  Discards (-x):  Every (-e):

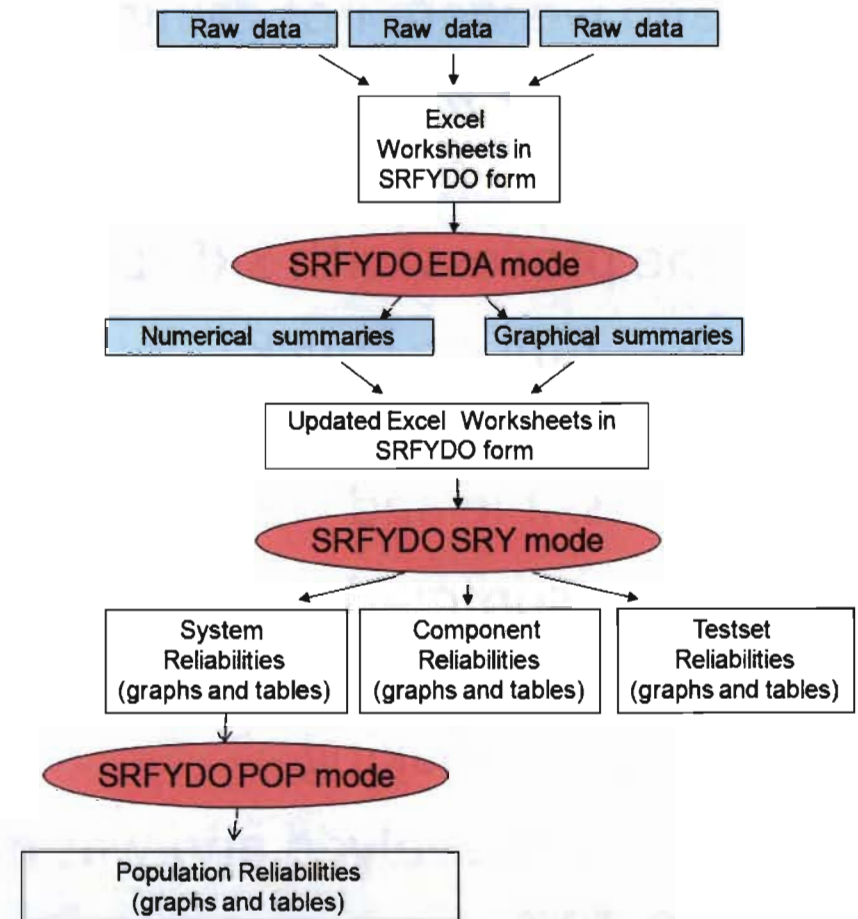
Reliability Lower Bound   Component (-r):  System (-s):

POP Times (-t):

POP Lifecycle Sampling (-l): ☒ PopData   ☐ Pop+Flight+Test   ☐ PopSample

# Final Product and Process

- SRFYDO is the computational engine to guide a process
- EDA mode uses common statistical summaries and graphics which builds in assumptions checking
- Systems analyzed range from:
  - 5 components with one variant
  - 35 components with 8 variants (60+ total components)



**Users functioning relatively independently**  
**LANL offers annual training and consulting support**



# Lessons Learned

- When the focus was on software, our scope was too limited and we were not gaining much traction
- The shift to a guided process (with built in tools for each step) was transformational to our success – the training focuses on the process with SRFYDO being its support
- Assumption check is intuitive for many statisticians, but is built on a foundation of statistical training – making this concrete, accessible and well defined for our customers was essential
- If the summaries / tools needed to perform an analysis are easily available, then the focus shifts to interpretation and decision-making
- The plan evolved and was driven by both the users and the creators

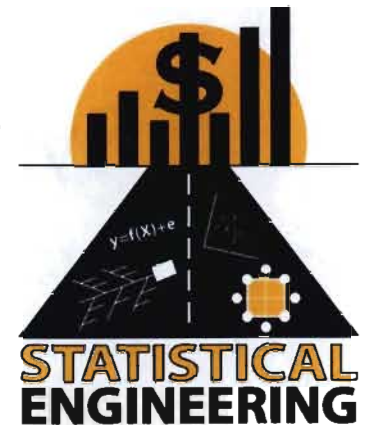
# System Reliability - Conclusions

- The process for obtaining system reliability estimates using multiple sources of data using SRFYDO offers a way of incorporating relevant sub-system and component level data to supplement full-system data, which leads to better understanding and potential improvements to estimation and prediction precision
- It allows SMEs to use a sophisticated statistical approach without having to master all of the details of the analysis, but depends of engineering judgment to make sure we have answered the right question

SRFYDO runs on a PC (requires Python, JAVA and Excel) and is available to any US Government agency free of charge [srfydo@lanl.gov](mailto:srfydo@lanl.gov)

Christine Anderson-Cook [candcook@lanl.gov](mailto:candcook@lanl.gov)

# Statistical Engineering - Conclusions



- Characteristics:
  - Satisfies a high-level need of the organization.
  - No known solution to the problem.
  - High degree of complexity involving both technical and non-technical challenges.
  - More than one statistical technique required for solution.
  - Long-term success requires imbedding solutions into work processes.
  - The whole is greater than the sum of the parts.
  - A solid theoretical foundation is required to guide development of a solution.
  - The solution can be leverage to similar problems elsewhere

**Quality Engineering** Special Issue on Statistical Engineering (March 2012): 17 papers – 2 panel papers, 3 general, 3 on SE education, 9 case studies

ASQ Statistic Division Resource Page:  
<http://asq.org/statistics/quality-information/statistical-engineering>

Christine Anderson-Cook [candcook@lanl.gov](mailto:candcook@lanl.gov)