

Investigating the balance between capacity and capability workloads across large scale computing platforms

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Abstract -- The focus of this paper is on the effectiveness of HEC (high-end computing) systems on meeting engineering and scientific analysis needs. Performance measurement and analysis of the applications constituting the work load, on a large commodity InfiniBand cluster, and, on a large custom Cray XT3, is used to assess the merits of the competing HEC architectures. Those applications with communication intensive algorithms show a factor of 2 to 10 better (on 1024 processors) performance on XT3, making XT3 ideal for long, large capability simulations. However, applications with moderate to low communication need have comparable performance on the cluster and these commodity clusters eminently meet the need for higher volume capacity computing cycles. We report on the reasons for the performance difference seen between the two systems. This analysis is beneficial for optimal mapping of computing resources to maximize the return on investments in HEC systems.

Introduction:

The parallel performance of applications on high performance computers is influenced by a number of hardware and software characteristics. Applications may also vary a great deal in their algorithmic characteristics and in the nature of their use by the analysts. The same application may be used to run very large capability class simulations or used with less number of processors in several runs to cover a range of parameter space for analysis like uncertainty quantification. In the context of current and future major investments in capacity and capability computing systems, it is useful to analyze mapping of workload against the available computing resources. Current HEC systems vary in the node/processor architecture, the interconnect and system software. IDC classification of HEC systems into two broad categories [1], namely, capability and capacity is widely used. However the demarcation is not strictly defined. Moreover applications and analysis that are targeted for these HEC systems again cross the definition boundaries. Our experience with a number of applications and analysts needs, clearly indicate need for large capacity compute cycles. At the same time capability computing often addresses need for interesting and new science that were often not undertaken previously due to lack of compute power. In this context, both from a management concern for providing the correct investment to meet an institutions need as well as from an analyst concern to improve the model fidelity, there exists a strong need to understand effectiveness of different classes of HEC systems on meeting the engineering and scientific analysis needs.

Table 1, is the result of a usage survey done few years ago, listing the top few applications and node-hour percentage usage. The current fraction is based on usage logs and estimated future fraction is based on user surveys reflecting programmatic needs. The recent availability of large capability computing systems like ASC Red Storm at Sandia and ASC Purple at LLNL has enabled analysts to conceive new approaches and analysis that were if not impossible, were difficult to undertake on a routine basis. The statistics of node-hours for such large capability class simulations are just beginning to emerge. However the question of appropriate allocation of computing budget to the acquisition of capability and capacity computing systems is an area of much interest.

In this paper we have attempted to answer this question. A large InfiniBand cluster with over 8000 processors and a large Cray XT3 with over 20000 processors are used to measure performance of seven applications of interest. The measured parallel efficiency on both these systems is used to understand the limits of scalability with these data sets. It is recognized that scaling behavior is data set dependent and often bigger models permit scaling to a larger number of processors. However, the performance ratio

between the two systems provides broad guidelines on optimal usage of both the systems to meet capability and capacity computing node-hours.

Table 1. SNL application node-hour usage and projections

Code	Use	Numerical Method	Current Fraction	Future Fraction
Presto	Crash/ Solid dynamics	FEM, explicit time integration	34.4%	15%
Salinas	Vibration/ Structural dynamics	FEM, spectral analysis	15.8%	10%
LAMMPS	Molecular dynamics	FFT, sparse matrix methods	12.8%	10%
DSMC	Plasma dynamics	Discrete Simulation Monte Carlo	10.4%	10%
CTH	Penetration/ Solid dynamics	Control volume, explicit time integration	7.4%	10%
ITS	Radiation transport	Monte Carlo	.08%	15%
TOTAL			81%	70%

In the following sections we first provide a short description of each application and the analysis that was benchmarked on the two systems. The wall clock run time ratio and parallel efficiency plots show the scaling characteristics of the applications. This data is used in conjunction with the projected computing cycle needs to analyze optimal use of the compute resources. Our approach is similar to the recent publication of Olikar, et.al. [2] in that we investigate the performance of full applications constituting most of the workload shown in Table 1.

Target Architecture Description:

The Red Storm machine at Sandia National Laboratories in Albuquerque, New Mexico currently consists of 12,960 dual-core nodes with a 2.4GHz Opteron CPU with a minimum 2 GB of main memory and a Cray SeaStar NIC/router attached via HyperTransport. The network is a 27x20x24 mesh topology, with 2.0 GB/s bidirectional link bandwidth and 1.5 GB/s bidirectional node bandwidth. The nearest neighbor NIC to NIC latency is specified to be 2 μ sec, with 5.4 μ sec measured MPI latency. The compute nodes run the Catamount lightweight kernel, a follow-on to the Cougar/Puma design used on ASCI Red. The I/O and administrative nodes run a modified version of SuSE Linux. The Cray-designed SeaStar communication processor / router is designed to off-load network communication from the main processor. It provides both send and receive DMA engines, a 500MHz PowerPC 440 processor, and 384 KB of scratch memory. Combined with the Catamount lightweight kernel, the SeaStar is capable of providing true OS-bypass communication. The Red Storm platform utilizes the Portals 3.3 communication interface, developed by Sandia National Laboratory and the University of New Mexico for enabling scalable communication in a high performance computing environment. The Portals interface provides true one-sided communication semantics. Unlike traditional one-sided interfaces, the remote memory address for an operation is determined by the target, not the origin. This allows Portals to act as a building block for high performance implementations of both one-sided semantics (Cray SHMEM) and two-sided semantics (MPI-1 send/receive). The Cray XT3 commercial offering was nearly identical to the Red Storm machine installed at Sandia, before the recent upgrade to dual core nodes and newer SeaStar NIC. The notable difference is that while the Red Storm communication topology is a 3-D mesh, the XT3 utilizes a 3-D torus configuration. The difference is to allow a significant portion of the Red Storm machine to switch between classified and unclassified operation.

The Thunderbird system was purchased for coordinated use as a production capacity computing cluster in a technical collaboration with Dell Computer Corporation (Computational nodes), with Cisco Systems (high-speed message passing interconnect), with Force10 Networking (Ethernet interconnect), and with the Technology Integration Group (vendor/integrator). Thunderbird is comprised of 4480 Dell PowerEdge 1850 commodity servers with 3.6GHz dual-processors linked with an InfiniBand message passing interconnect. The interconnect is a dual layer hierarchical fattree InfiniBand network. There are 140 Compute racks, each with two 24 port InfiniBand 4x switches and 32 compute nodes. There are 6 Ethernet racks with a single Force10 E1200 switch and Eight IB racks with a single 288 port IB 4x switch. All MPI traffic is conducted across the InfiniBand network and all I/O is done across the Ethernet network. Each 24 port IB switch has 16 compute nodes connected to it and a single connection to each of the eight 288 port IB switches producing a 2-to-1 over subscription. There is a core E1200 switch that is connected via 4 channel bonded 10GigE ports to the remaining 5 E1200s. 4 of the 5 lower level ethernet switches have 1024 compute nodes connecting at half GigE bandwidth and the remaining switch has 384 compute nodes also at half bandwidth. Thunderbird's software was recently upgraded to OpenFabric Enterprise Distribution (OFED) and OpenMPI - Linux-based open source software stack qualified by the OpenFabrics Alliance to operate with multi-vendor InfiniBand hardware and implement open source Message Passing Interface (MPI) protocol. Table 2 summarizes the important architectural characteristics of Red Storm and Thunderbird.

Table 2. Red Storm and Thunderbird architectural highlights

Name	Arch	Network	Network Topology	Total P	P/Node	Clock (GHz)	Peak (GF/s/P)	Streams BW(GB/s/P)	MPI Lat (μsec)	MPI BW (GB/s/P)
Red Storm	Opteron	Custom	Mesh / Z-torus	25,920	2	2.4	4.8	2.5	5.4	2.1
Thunderbird	X86_64	InfiniBand	Fattree	8960	2	3.6	7.2	3.8	6	.468

Applications and Benchmarks:

a) SIERRA/Fuego:

This application is an integral part of the SIERRA [3] multi-mechanics software development project at Sandia. Fuego represents the turbulent, buoyantly driven incompressible flow, heat transfer, mass transfer, combustion, soot and absorption coefficient model portion of the simulation software. Syrinx represents the participating-media thermal radiation mechanics. Calore represents the heat transfer within an object. Domino., et.al.[4] describe the details of the governing equations, discretization, decomposition and solution procedures. The general coupling strategy for the suite of abnormal-thermal environments is provided in Figure [1]. SIERRA/Fuego, SIERRA/Syrinx, SIERRA/Calore depend heavily on the core architecture developments provided by SIERRA for massively parallel computing, solution adaptivity, and mechanics coupling on unstructured grids.

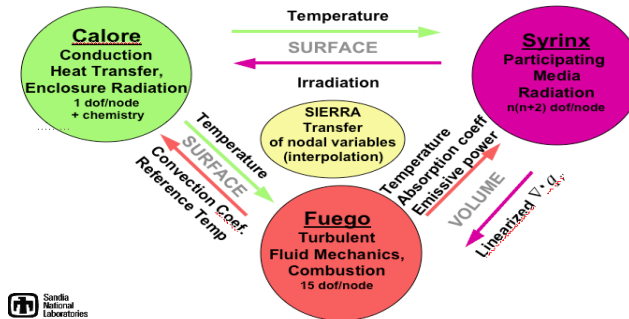


Figure 1. Abnormal-thermal coupling analysis with SIERRA/Fuego

In the application chosen for this paper, coupled fire/thermal response predictions for a weapon-

like calorimeter is validated for a quiescent fire representative of a transportation accident scenario. The model constructed was used to compare numerical predictions against experimental data. Temperature measurements were used to validate the coupled Fuego/Syrinx/Calore predictions. The model consists of fluids (Fuego), radiation (Syrinx) and object heat transfer (Calore) meshes along with an output mesh. The main Fuego fluid mesh for the scaling study was constructed with a 1M element model fluid mesh. Similar mesh sizes were used in the Syrinx radiation calculations. The Calore mesh size is much smaller as it contains only the outer shell of the object. The output mesh is a vertical slice through the centerline of the fire that is only one cell thick. The simulations solve the governing set of complex coupled equations whose solution over a broad range of time and length scales is sought. This complexity in the model and the long run times to resolve the fire for 60-90 seconds could only be carried out on massively-parallel capability class supercomputers. These simulations were routinely conducted on the Red Storm and Thunderbird computers.

Figures 2 presents side-by-side the execution time plot and the parallel efficiency plot. The most dominant computation, namely the fluid region solve is plotted. The reason that Red Storm scales better at 256 and 512 processor counts is because of the better communication to computation balance, that is required for the implicit ML solver used for the fluid solve. As this is a strong scaling analysis as the work per processor decreases, it stresses the communication fabric in the several iterations required for the solve.

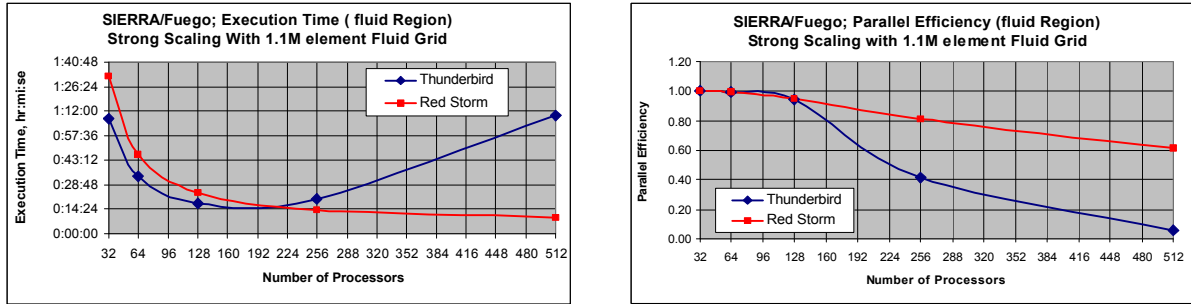


Figure 2. SIERRA/Fuego Performance on Red Storm and Thunderbird

b) ITS Monte Carlo radiation transport:

The INTEGRATED TIGER SERIES (ITS) code is an evolving Monte Carlo radiation transport code that has been used extensively in weapon-effect simulator design and analysis, radiation dosimetry, radiation effect studies and medical physics research. Many individuals from the DOE labs and NIST have been involved over the years in the development and enhancement of ITS. The different features/sections of the code in ITS: TIGER, MITS, CEPXS, XGEN etc., are applied to an analysis under investigation through the selection of appropriate pre-processor directives when the code is built. Physical rigor for the analysis is provided by employing accurate cross sections, sampling distributions, and physical models for describing the production and transport of the electron/photon cascade from 1.0 GeV down to 1.0 keV. The ITS code is capable of analyzing particle transport through both combinatorial geometry models and CAD models. It also has been significantly enhanced to permit adjoint transport calculations.

For the purposes of this paper we have analyzed the performance using as input, data from a real satellite model. The physical problem solved takes advantage of the MITS mutli-group/continuous energy electron-photon Monte Carlo transport code's capability to address realistic three-dimensional adjoint computations. The adjoint transport method is a powerful technique for simulating applications where the knowledge of the particle flux is only required for a restricted region of the phase space, but where this knowledge is required for source parameters spanning a large region of phase space. The run times for simulations for a complex combinatorial geometry model using conventional, or forward, transport are prohibitive and hence the adjoint calculations used in our satellite model. Although the code has been recently updated to improve parallel scaling, we have used the older version of the code as it amplifies the difference between a commodity cluster and a tightly integrated MPP and the difference in scaling performance related to a performance model we had developed [5].

Figure 3 presents side-by-side the execution time plot and the parallel efficiency plot for ITS. The weak scaling runs were set up with 1.6 Million histories per processor. The difference in parallel efficiency for this application can be directly related to the MPI bandwidth, as we have developed a performance model [6] that easily explains the increased overhead for the master/slave communications at the end of each batch of history computations. As noted in Ref. [5] the algorithm for gathering the statistics after each batch has been modified in newer version of ITS to improve parallel scaling even on systems with lower communication performance. However, for this exercise we chose to use the older algorithm as exaggerates the difference between Thunderbird and Red Storm, helping us understand the impact of architectural balance on scalability.

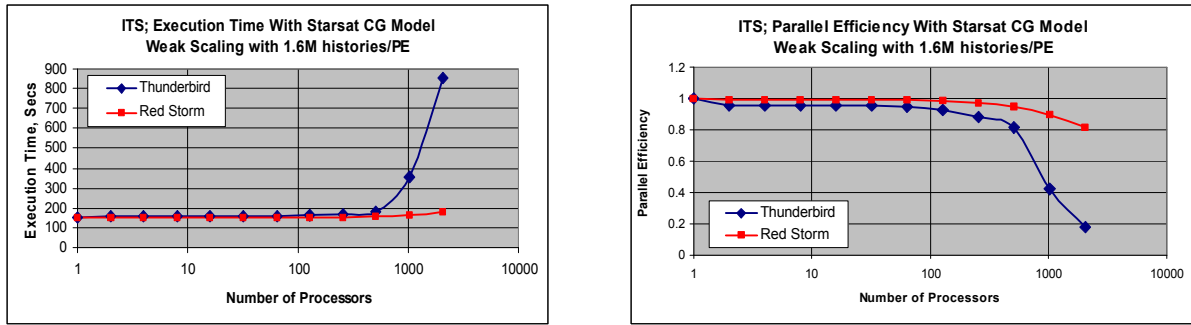


Figure 3. ITS Performance on Red Storm and Thunderbird

c) LAMMPS:

LAMMPS is a classical molecular dynamics code that models an ensemble of particles in a liquid, solid, or gaseous state. It can model atomic, polymeric, biological, metallic, granular, and coarse-grained systems using a variety of force fields and boundary conditions. LAMMPS runs efficiently on single-processor desktop or laptop machines, but is designed for parallel computers. It will run on any parallel machine that compiles C++ and supports the MPI message-passing library. This includes distributed- or shared-memory parallel machines and Beowulf-style clusters. LAMMPS can model systems with only a few particles up to millions or billions. See lammps.sandia.gov for information on LAMMPS performance and scalability, and the Benchmarks.

The current version of LAMMPS is written in C++. Earlier versions were written in F77 and F90. In the most general sense, LAMMPS integrates Newton's equations of motion for collections of atoms, molecules, or macroscopic particles that interact via short- or long-range forces with a variety of initial and/or boundary conditions. For computational efficiency LAMMPS uses neighbor lists to keep track of nearby particles. The lists are optimized for systems with particles that are repulsive at short distances, so that the local density of particles never becomes too large. On parallel machines, LAMMPS uses spatial-decomposition techniques to partition the simulation domain into small 3d sub-domains, one of which is assigned to each processor. Processors communicate and store "ghost" atom information for atoms that border their sub-domain. LAMMPS is most efficient (in a parallel sense) for systems whose particles fill a 3d rectangular box with roughly uniform density.

lj.inp used in this study is a weak scaling analysis with the Lennard-Jones liquid benchmark. The dynamics of the atomic fluid with 864,000 atoms per processor for 100 time steps is timed. Other parameters used are: reduced density = 0.8442 (liquid), force cutoff = 2.5 sigma, neighbor skin = 0.3 sigma, neighbors/atom = 55 (within force cutoff), with NVE time integration. The execution time and parallel efficiency is shown in Fig. 4.

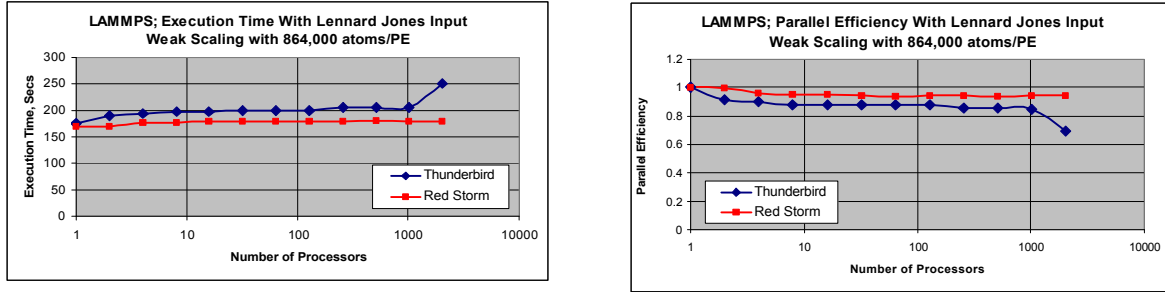


Figure 4. LAMMPS Performance on Red Storm and Thunderbird

d) SIERRA/Presto:

Presto is a Lagrangian, three-dimensional explicit, transient dynamics code for the analysis of solids subjected to large, suddenly applied loads [6]. Presto is designed for problems with large deformations, nonlinear material behavior, and contact. There is a versatile element library incorporating both continuum and structural elements. The contact algorithm is supplied by ACME[6]. The contact algorithm detects contacts that occur between elements in the deforming mesh and prevents those elements from interpenetrating each other. This is done on a decomposition of just the surface elements of the mesh. The contact algorithm is communication intensive and can change as the problem progresses.

The analysis used in this investigation is The Brick Walls problem consists of two sets of two brick walls colliding with each other. It is a weak scaling investigation where each processor is assigned 80 bricks. Each brick is discretized with 4 x 4 x 8 elements, for a total of 10240 elements per processor. Each brick is located on one processor so the only communication for the finite element portion of the code is for the determination of the length of the next timestep. As the problem grows with the number of processors, the contact problem also grows. Figure 5. shows the parallel performance of Presto on this problem.

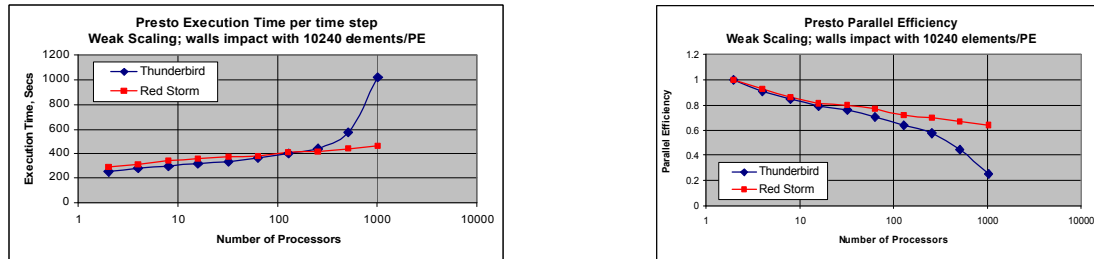


Figure 5. SIERRA/Presto Performance on Red Storm and Thunderbird

e) SAGE:

SAGE is a LANL/SAIC multi-dimensional multi-material Eulerian hydrodynamics code with adaptive mesh refinement. The code uses second order accurate numerical techniques. SAGE was tested extensively on Red Storm with simple inputs and complex asteroid impact input decks in the early days of bringing up Red Storm. SAGE performance has been studied extensively by Kerbyson, et.al.,[7] and is frequently used by LANL to predict performance of new HPC architectures, using their application performance model. We have used SAGE (version 20030505) to investigate scaling characteristics of Thunderbird and Red Storm. The code was executed in a weak-scaling mode with a constant sub-grid per processor, thereby increasing the global problem with increasing processor count. The input deck used is called timing_c and the problem was set up with approximately 80,000 cells per process, and it performs

only hydro calculations. This input deck imposes a high communication time to computation time ratio. Figure 6 shows the wall time and parallel efficiency with this input deck. The parallel efficiency is calculated using the 2 processor timing as the reference, as there is significant increase in wall time in going from single to two processor.

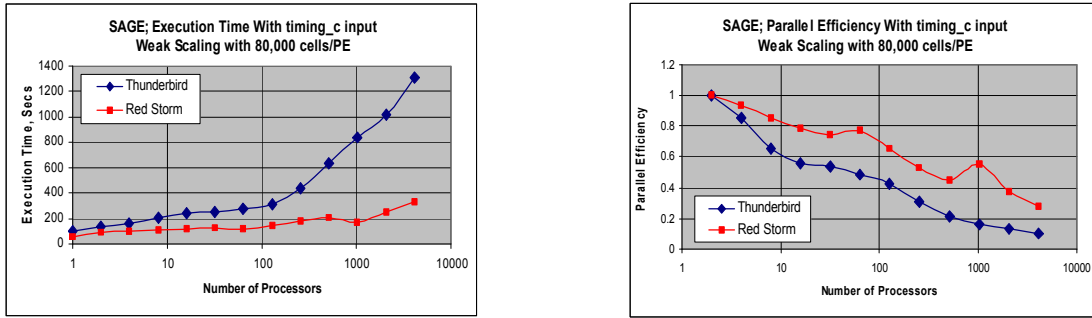


Figure 6. SAGE Performance on Red Storm and Thunderbird

f) ICARUS/DSMC:

The Direct Simulation Monte Carlo (DSMC) method is the only proven method for simulating noncontinuum gas flows because continuum methods break down where particles move in ballistic trajectories with mean free path larger than cell dimensions, often because the device is small (micro-or nano technology) or the fluid is very low pressure as in plasma or upper atmosphere. Unlike most flow-simulation methods, DSMC uses computational molecules (“simulators”) that mimic real molecules by moving through space, reflecting from solid boundaries, and colliding with one another. By sampling the velocities of large numbers of computational molecules, the gas flow is determined.

Since DSMC is a Monte Carlo technique using computational molecules, the phases of computation corresponding to movement, reflection and collision of the molecules parallelizes easily. However, based on the density distribution and the decomposition of the particle grid, between stages of computations, there could be significant messaging overhead as particles migrate among the cells. In addition based on the analyst request to periodically dump particle, surface, and chemistry states at desired intervals, I/O overheads can impact scalability in large parallel simulations. Unsteady DSMC simulations for a two-dimensional microbeam investigated by Gallis and Torczynski [8] is used to set up a weak scaling study, fixing the number of simulators per processor.

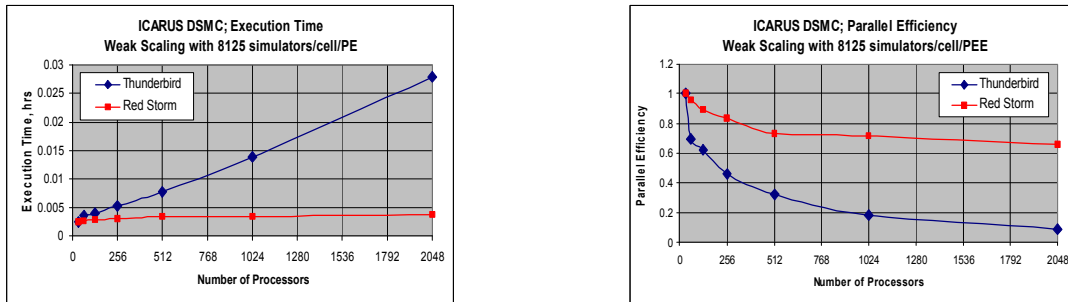


Figure 8. DSMC/ICARUS Performance on Red Storm and Thunderbird

g) CTH:

CTH is an explicit, three-dimensional, multimaterial shock hydrodynamics code which has been developed at Sandia for serial and parallel computers. It is designed to model a large variety of two- and three-dimensional problems involving high-speed hydrodynamic flow and the dynamic deformation of solid materials, and includes several equations of state and material strength models [9]. The numerical algorithms used in CTH solve the equations of mass, momentum, and energy in an Eulerian finite

difference formulation on a three-dimensional Cartesian mesh. CTH can be used in either a flat mesh mode where the faces of adjacent cells are coincident or in a mode with Automatic Mesh Refinement (AMR) where the mesh can be finer in areas of the problem where there is more activity. We will be using the code in a flat mesh mode for this study.

The shaped-charge consists of a cylindrical container filled with high explosive capped with a copper liner. When the explosive is detonated from the center of the back of the container, the liner collapses and forms a jet. The problem is run in quarter symmetry and includes a target material. The weak scaling analysis with CTH was setup with 90x216x90 computational cells per processor. Figure 10 shows the wall clock time per time step and the parallel efficiency.

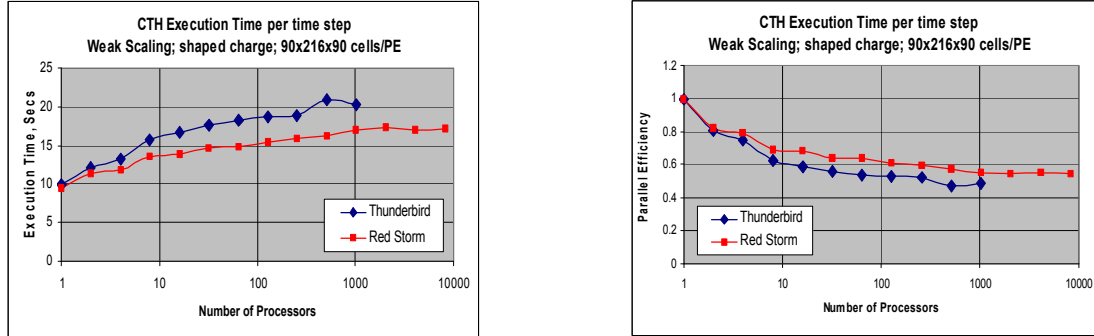


Figure 9. CTH Performance on Red Storm and Thunderbird

Application Performance Scaling Analysis:

As stated in the introduction we shall analyze the performance of various applications that constitute our workload with a view to understanding why we see differences in performance between the two compute systems considered and to find the capacity and capability computing balance. It is recognized that this analysis may not correctly represent the current and future workload that would be undertaken in these two systems. Application scaling behavior is strongly dependent on the amount of computation assigned per processor, which in turn is a function of the model size (or such similar parameter) that influences the compute time to communication time balance. However we hope to understand through this analysis computer architectural balance issues that has big impact on matching the workload to the system. The first obvious conclusion that can be drawn from these application performance charts, is that for many of our usual analysis needs that fall in 64 to 256 processor range the performance of the capacity cluster is good. This is further evident from the efficiency ratio between Red Storm and Thunderbird at a few discrete processor configurations listed in Table 4.

Table 4. Efficiency ratio, Red storm to Thunderbird

Apps.\PEs	64	256	1024
ITS	1.047637	1.10075	2.120773
SAGE	1.589619	1.692137	3.41284
Fuego	0.999329	1.932846	10.13348
Icarus	1.384615	1.8	3.942857
LAMMPS	1.074405	1.108991	1.108383
CTH SC	1.182684	1.044647	1.048238
Presto	1.09138	1.21369	2.562817

To analyze this further it is instructive to use a simple model of parallel efficiency as, $E = 1 / (1 + f)$, Where f is the ratio of communication time to compute time. One way to investigate the impact of the parameter, f , is to plot parallel efficiency as function of communication load to computation load. When this ratio is multiplied by the key platform balance characteristic, Bytes/Flop, a plot such as shown in Figure 10 may be constructed. In this figure possible Bytes/Flop balance ratio of 0.41 and 0.069 is taken to represent Red Storm and Thunderbird, respectively. The ratios result from using a measured MPI ping-pong bandwidth of 2GB/s for Red Storm and 500 MB/s for Thunderbird, (see Figure 11 below), while using their peak flop rate from Table 2. Also shown in the plot is the efficiency ratio between these two cases. This chart in conjunction with the table above and knowledge of the application and associated algorithms sheds much light on the impact of balance on scalability.

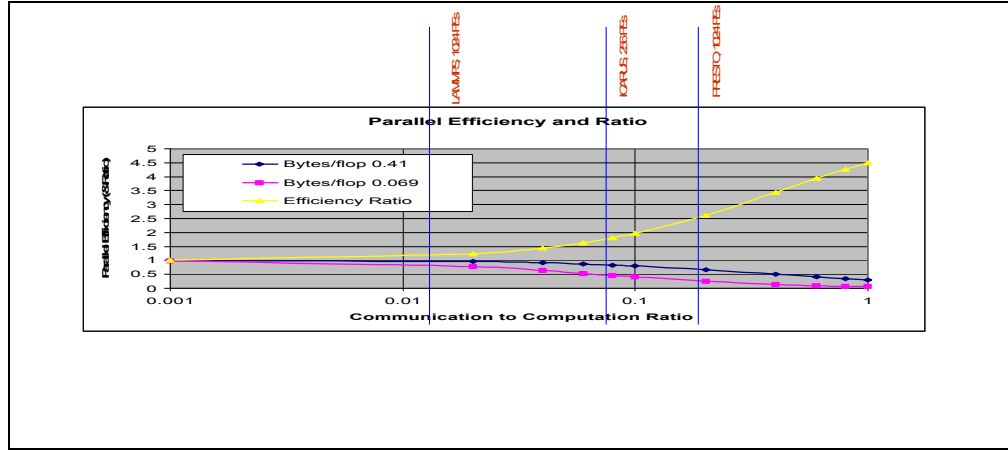


Figure 10. Simple parallel efficiency model and impact of communication to computation ratio of different applications

Another probable cause for the lower parallel efficiency of Thunderbird is the cost of global operations as typified by the Allreduce time shown in Figure 11. At the time of writing this paper, the almost order of magnitude increase (after 128 processors) in time for a eight byte allreduce on Thunderbird when compared to Red Storm, is not consistent with the message latency numbers measured. But it is certainly a major source for the poor efficiency in an application like ICARUS requiring global operations between fine grained particle movement computations.

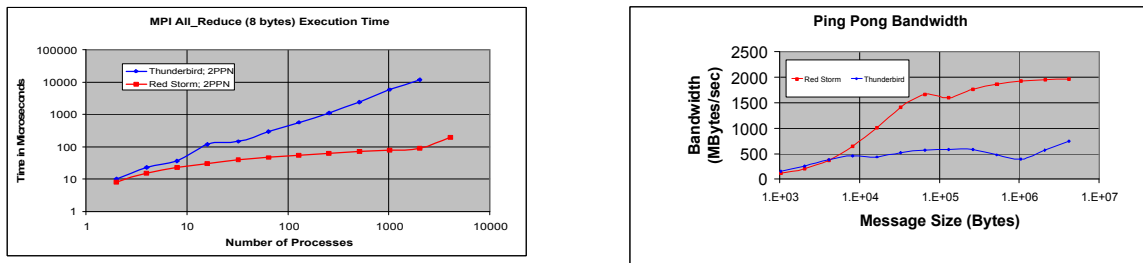


Figure 11. MPI Allreduce and ping-pong performance comparison

Our measurements on Thunderbird showed up to 30% variation in run times, whereas variations on Red Storm were less than 2-3%. Thunderbird run time variations were observed in as few as 64 processor jobs. The cause for the variation is suspected to be OS noise sources, similar to the observations by others investigators[11], although job placement on the mesh leading to network contention is also likely to play a part. As simple test, parallel independent computations for 100 seconds (a matmul loop was used) on 100 processors shows a maximum variation of 0.4% on Red Storm while variations on Thunderbird were as high as 2.5%. Since no network activity is involved this variation is suspected to be

caused by OS interrupts. A similar simple test, to measure impact of variations in communication operations was constructed by 50 pairs of nodes exchanging 2GB messages for a nominal total run time of 100 seconds. Red Storm tests showed a maximum difference in time of 3% between any pair of nodes, while Thunderbird tests showed maximum difference of 42% in the run time between any pair of nodes. This implies that applications that spend significant fraction of their compute cycle time in messaging are likely to see degraded performance, especially if there are frequent global operations or barriers requiring all the processors to synch up.

Conclusions:

From performance analysis of application workload encompassing several applications to thousands of processors, we have measured parallel efficiency ratio between a tightly integrated HEC system, Red Storm, and a large InfiniBand cluster, Thunderbird. Applications whose communication time to computation time ratio grows as a consequence of the inherent algorithm or as a consequence of poorer bytes/flop ratio at large processor counts, lead to less than desired parallel efficiency. Such applications reveal a factor of 2 to 10 better performance on a tightly integrated HEC system like Red Storm. This analysis also investigates the non-linear increase observed bytes/flop ratio on commodity clusters and postulates that OS noise and/or network contention and/or lack of maturity of the interconnect network software layers may be source of the differences seen between Red Storm and Thunderbird. While this analysis exposes the symptoms, further work remains in finding its root cause and remedying the deficiencies. Peak bytes to flop ratio between the two systems is quite reasonable, but does not explain the differences in parallel efficiencies at large processor counts.

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