

# Magnetic Insulation

## Precision Electron Flow Measurements in a Disk Transmission Line

Dissertation Proposal

Jeremy Martin



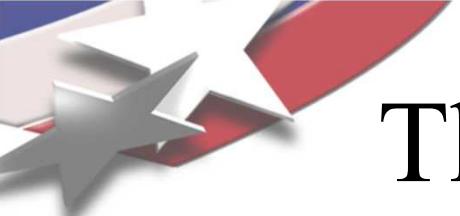
# Proposal Outline

- Research goals
- Theoretical background
- Hardware and diagnostics
- Particle-in-cell simulation



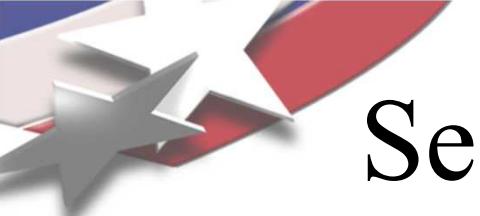
# Research Goals

- Direct measurement of MITL electron flow in a radial disk geometry
- Comparison with standard measurement techniques
- Benchmarking of QUICKSILVER simulation software

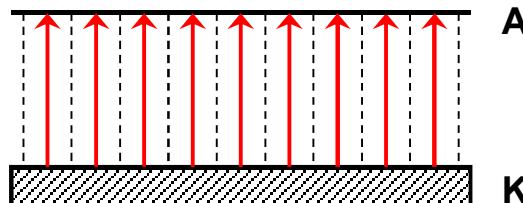


# Theory of Self-Magnetic Insulation

- Evolution of self-magnetic insulation
- Single particle analysis
- Analytical model
- Precision electron flow measurements

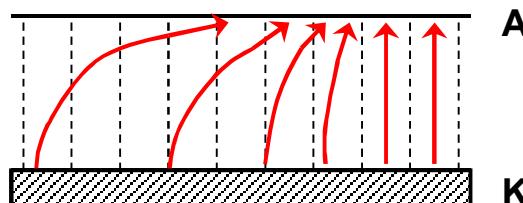


# Self-Magnetic Insulation



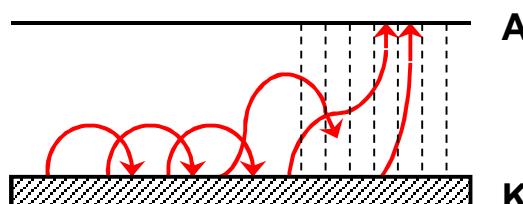
(a)

As the amplitude of the pulse rises appreciably, the cathode will begin to freely emit electrons. This conducting channel is known as the “loss front”.



(b)

Current drawn by the MITL increases as electrons are conducted through the loss front. When large enough, the **B**-field will start to deflect electrons away from the anode and toward the direction of power flow.

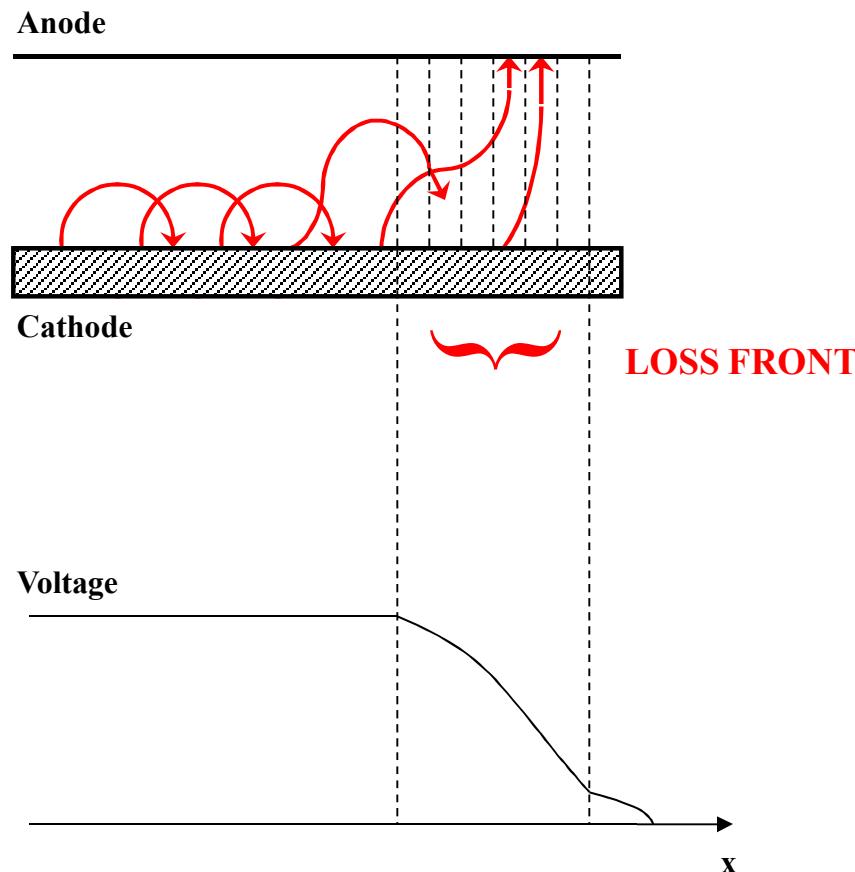


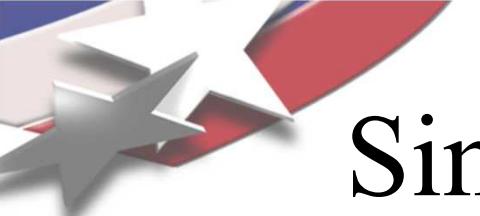
(c)

As more loss current is conducted across the gap, larger sections of the line become insulated and the impedance of the line decreases until it reaches its self-limiting value.

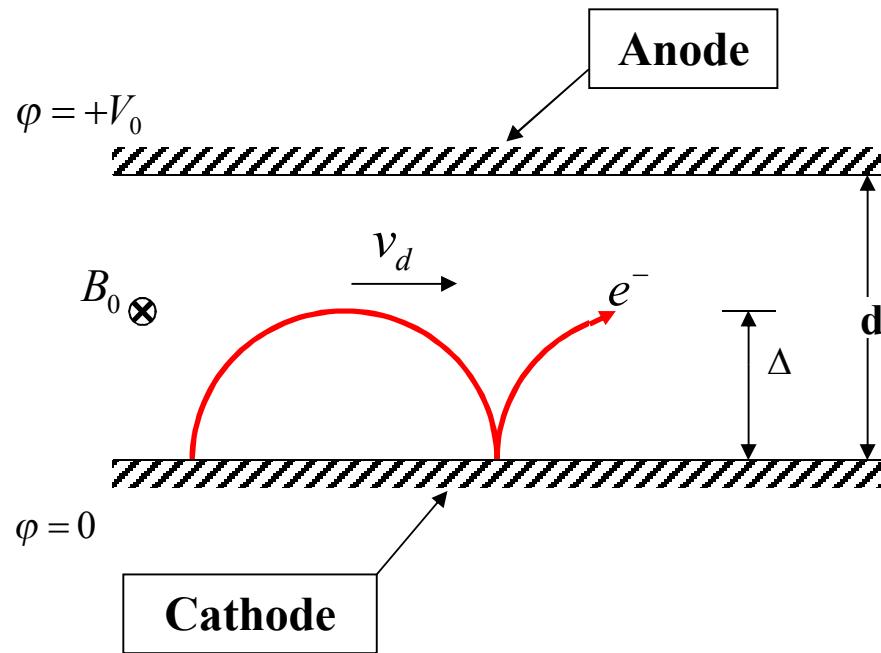


# Pulse Broadening





# Single Particle Dynamics\*



$$\frac{d}{dt}(\gamma m_e \vec{v}) = -e(\vec{E} + \vec{v} \times \vec{B})$$

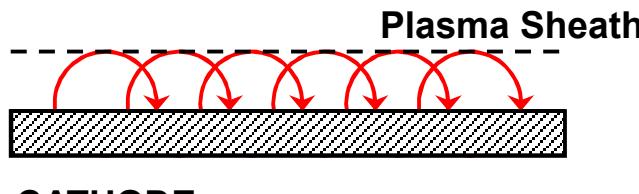
Electron drift:  $\vec{v}_d = \frac{\vec{E} \times \vec{B}}{B^2}$

\* Stationary Frame of Reference



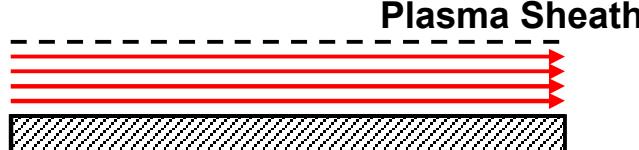
# Analytical Models

**ANODE**



**CATHODE**

**ANODE**



**CATHODE**

Quasi-laminar Flow

$$\gamma = 1 + \frac{eV_0}{m_e c^2}$$

$$\vec{v} = \frac{e\vec{A}}{m_e \gamma}$$

Parapotential Flow

$$\vec{E} = -\vec{v} \times \vec{B}$$



# Pressure Balance Theory\*

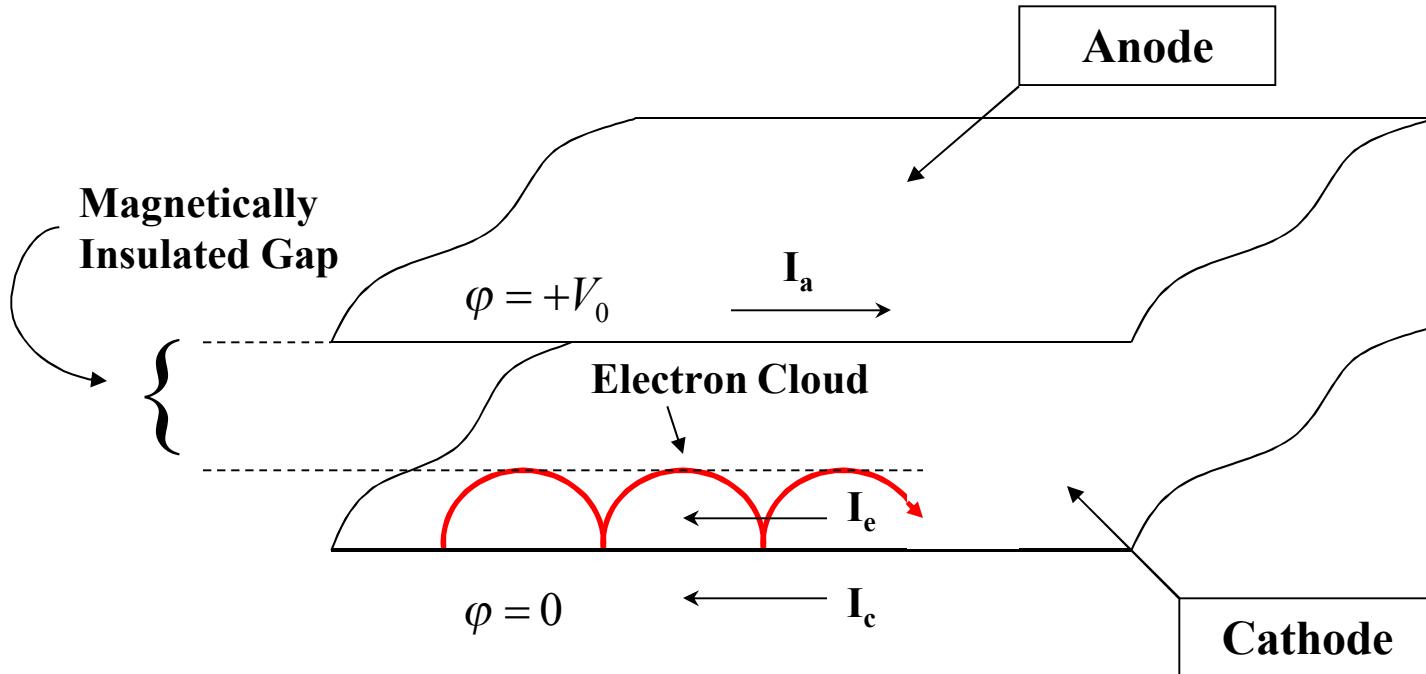
- Magnetically insulated lines are efficient
- Cathode is a space-charge-limited electron emitter

\*Mendel, Jr., Seidel, Rosenthal ('83)

Miller & Mendel, Jr. ('87)



# Parallel Plate MITL



$$I_a = I_e + I_c$$



# Pressure Balance Theory

$$\frac{B_a^2}{2\mu_o} - \frac{\varepsilon_o E_a^2}{2} = \frac{B_c^2}{2\mu_o}$$

where  $E_c = 0$        $\rightarrow$        $E_a g = Z_0 \sqrt{I_a^2 - I_c^2}$



# Pressure Balance Theory

$$V = Z_0 \sqrt{I_a^2 - I_c^2} - \frac{m_e c^2}{2e} \left( \frac{I_a^2}{I_c^2} - 1 \right)$$

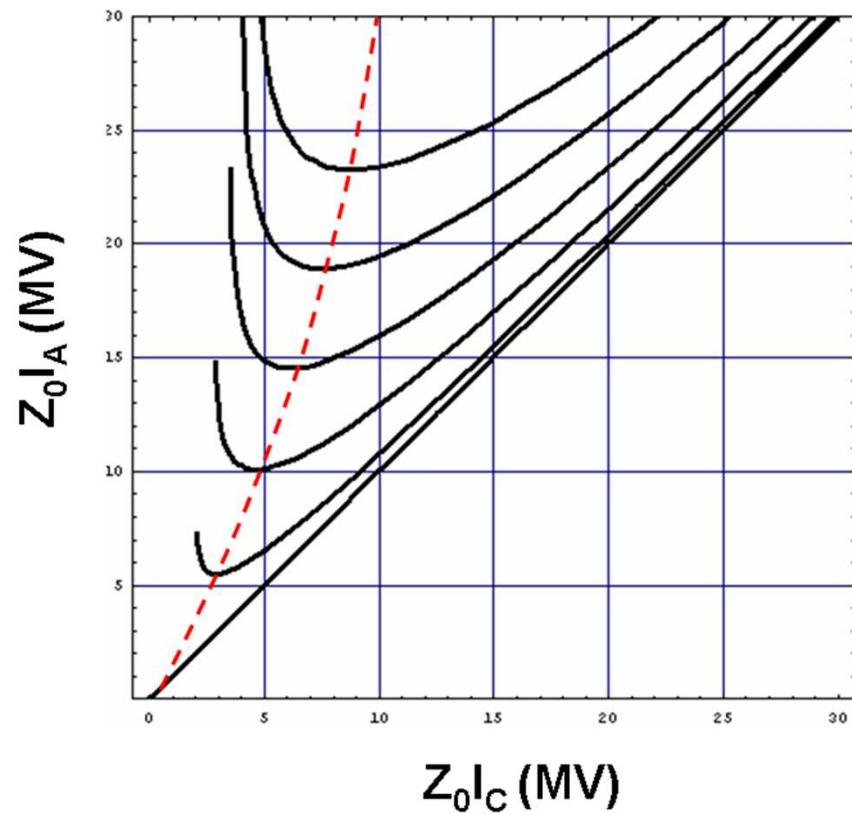

*Potential across entire gap*

*space charge correction*

$$V_s = \frac{m_e c^2}{2e} \left( \frac{I_a^2}{I_c^2} - 1 \right) \quad \longrightarrow \quad \rho_c \geq \frac{e \varepsilon_o B_c^2}{m_e}$$



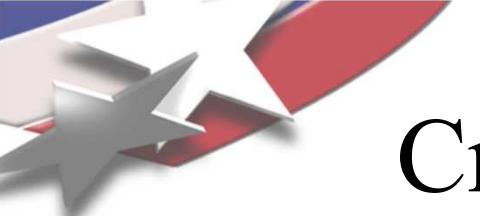
# Voltage Contours



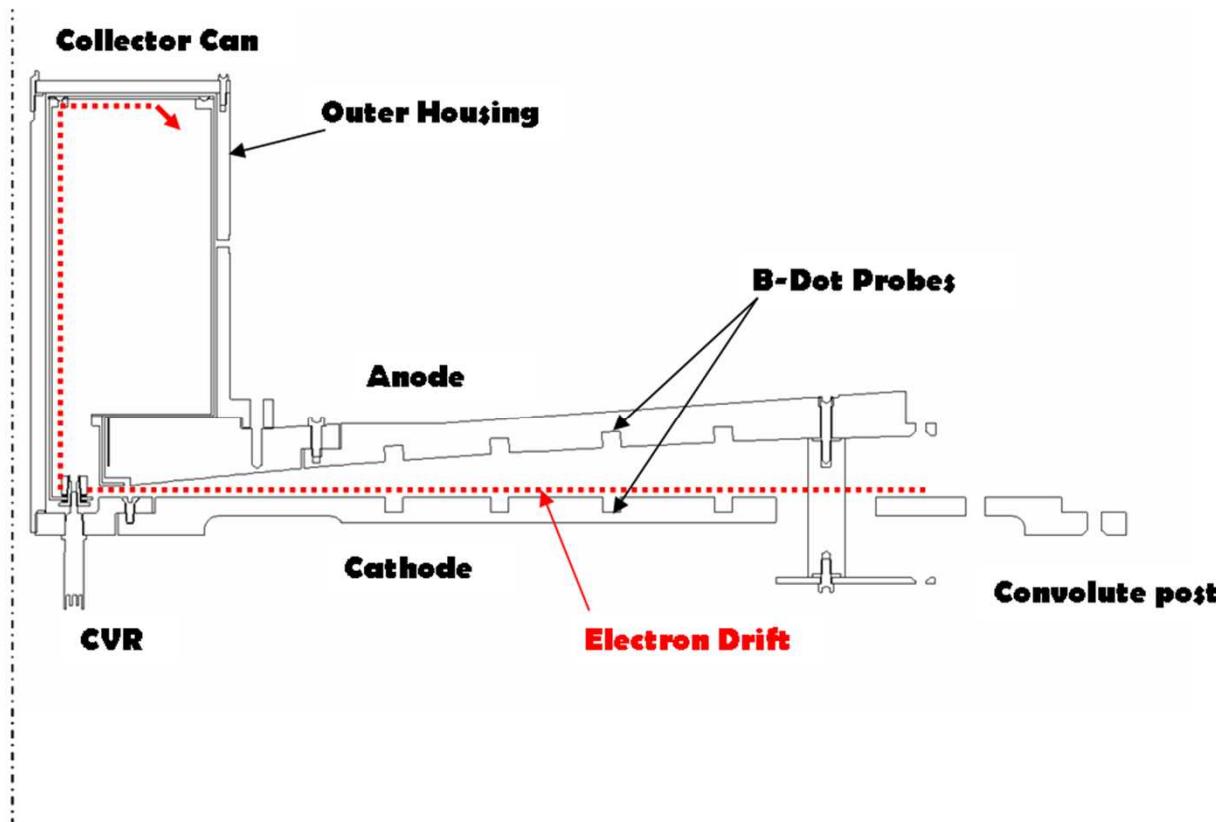


# MITL Hardware

- Radial disk geometry
- Gap spacing varies with radius
- Flat cathode
- Electron collector can



# Cross-Sectional Geometry





# Inductance Calculations

Fractional change in  
radial electron flow:

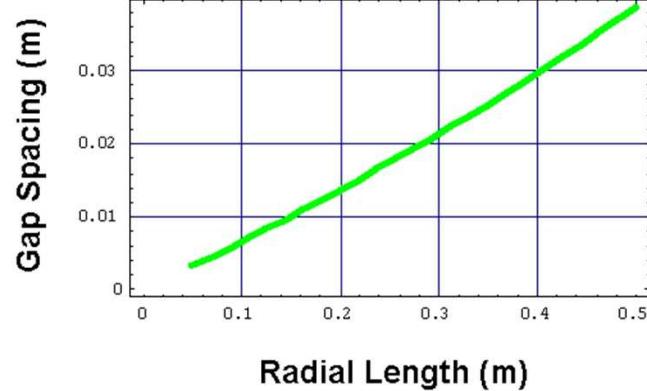
$$\beta = \frac{1}{I_e} \frac{\partial I_e}{\partial r} = 2 \frac{\dot{L}^2 - \ddot{L}L}{L\dot{L}}$$

Inductance profile:

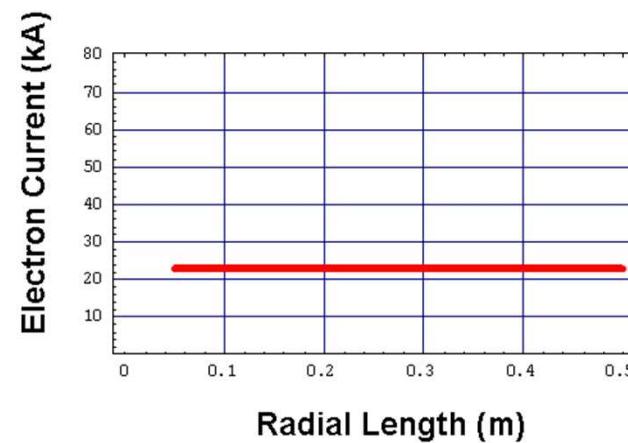
$$L(r) = C_2 \exp \left[ -\frac{2C_1}{\beta} \exp \left[ -\frac{\beta}{2} (r - r_o) \right] \right]$$



# Constant Electron Flow



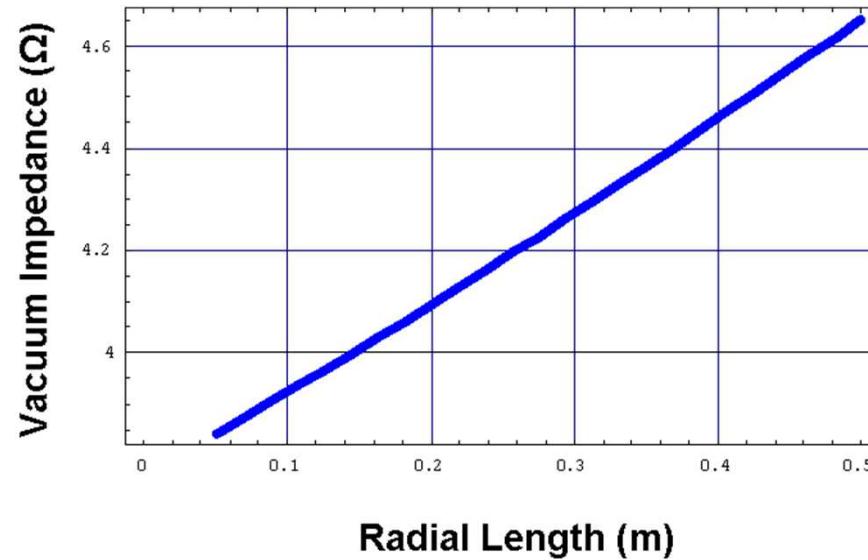
(a)



(b)

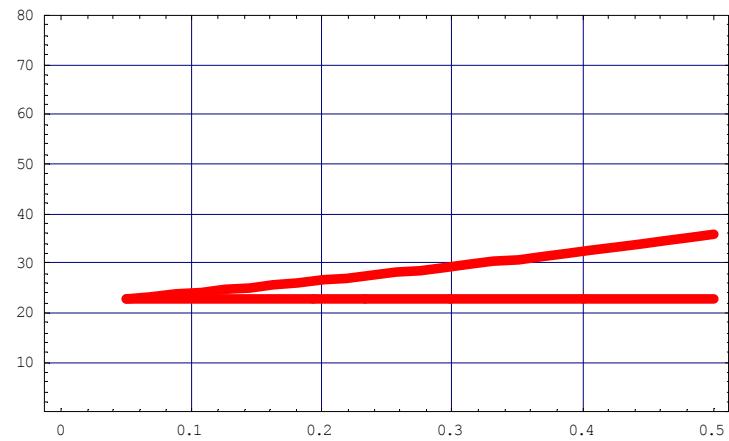
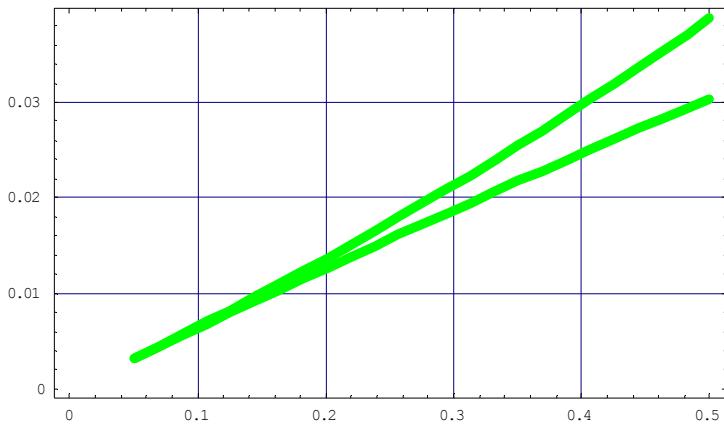
$$g_{const}(r) = \frac{g_o r}{r_o} \exp\left[ \frac{60 g_o (r - r_o)}{L_o r_o c} \right]$$

# Constant Electron Flow



$$Z(r) = \frac{60g_o}{r_o} \exp\left[\frac{60g_o(r - r_o)}{L_o r_o c}\right]$$

# Reducing Electron Flow



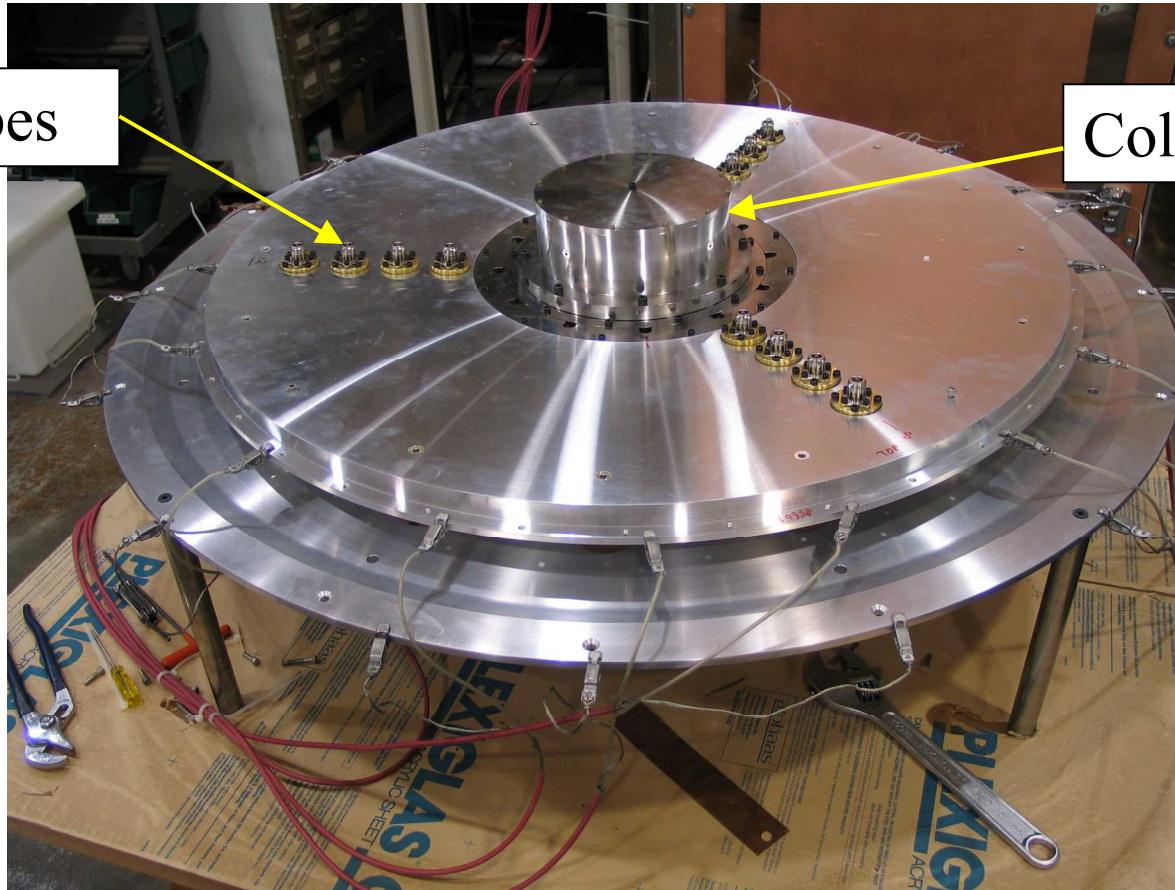
$$g_{reducing}(r) = \frac{g_o r}{r_o} \exp \left[ \frac{120g_o}{cL_o r_o} - \frac{120g_o}{cL_o r_o} \exp \left[ -\frac{1}{2}(r - r_o) \right] - \frac{1}{2}(r - r_o) \right]$$



# MITL Hardware

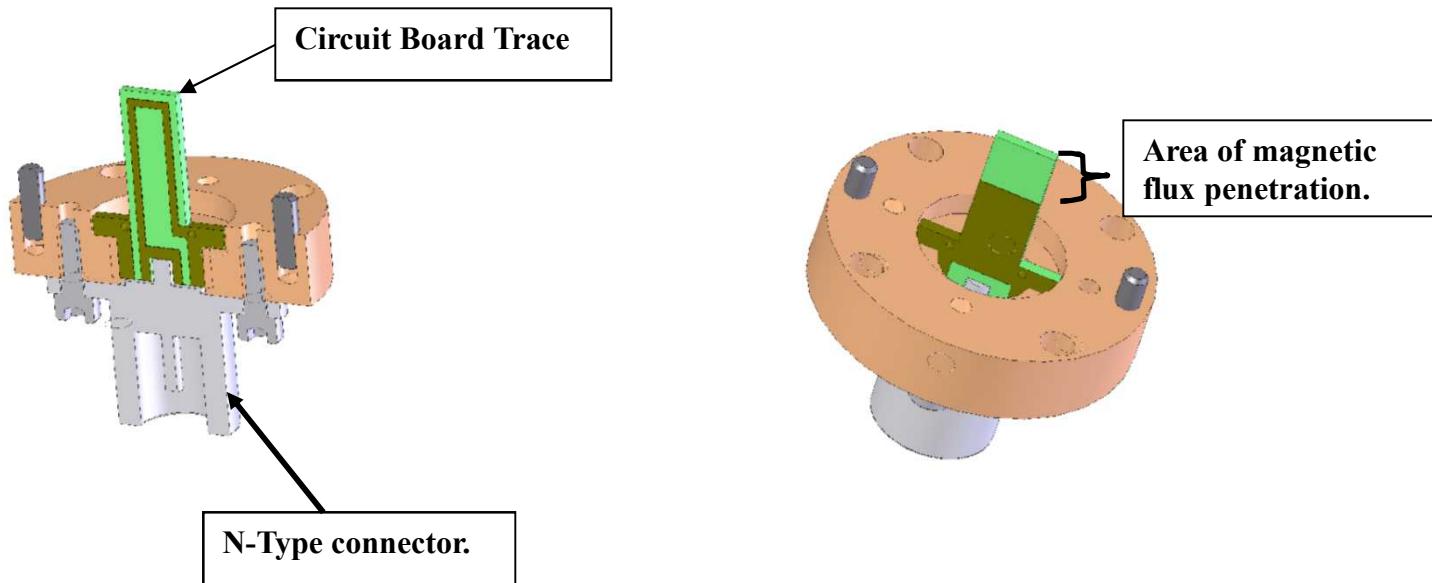
B-dot Probes

Collector Can



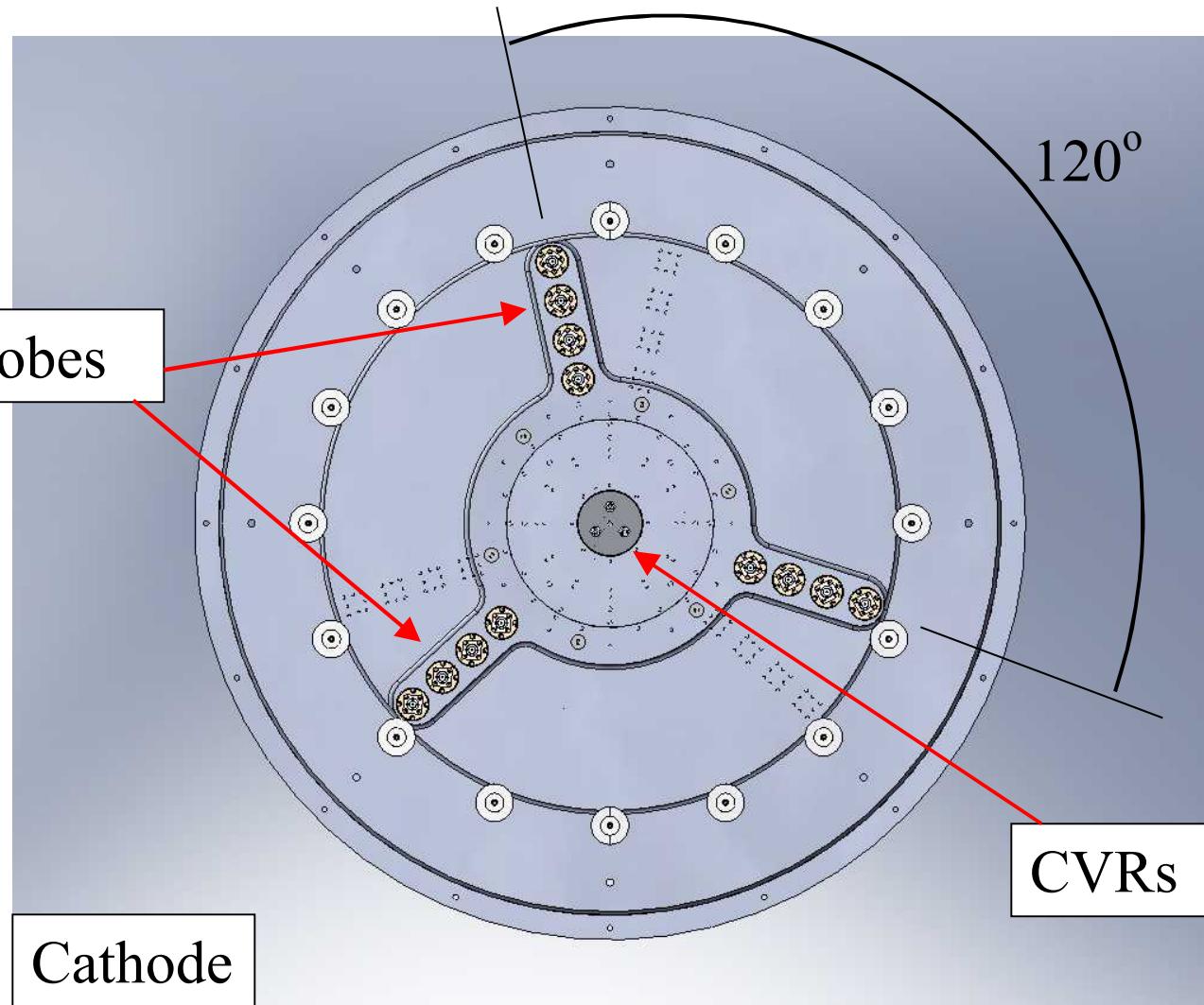


# Diagnostics



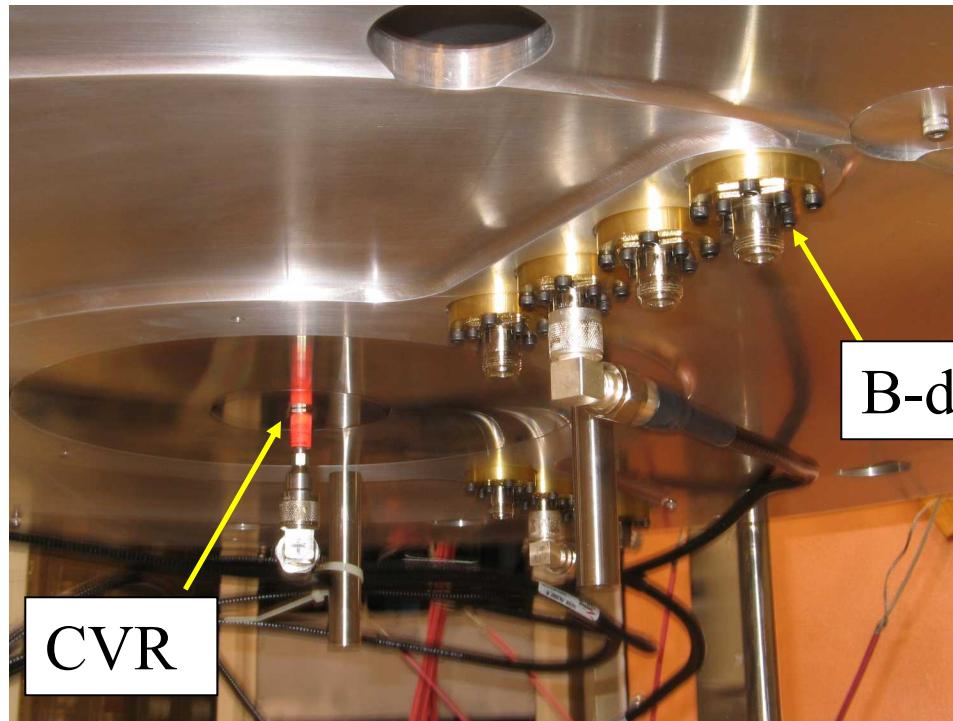


# Diagnostic Layout





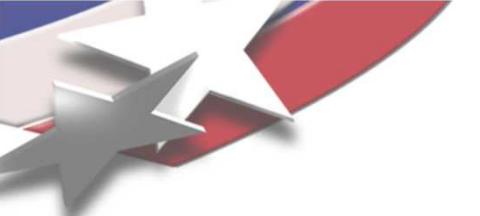
# MITL Hardware



B-dot Probes

CVR

Cathode



# Shielded Enclosure



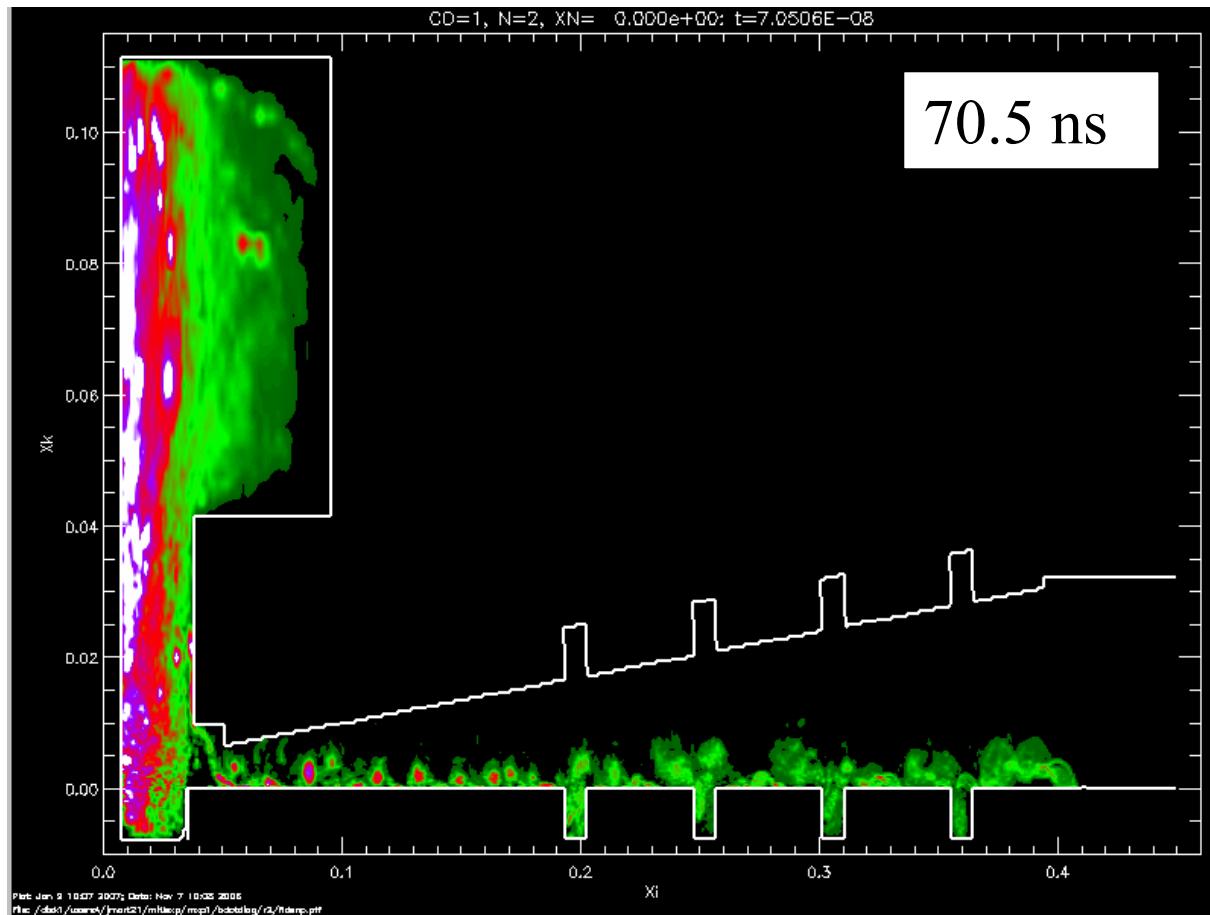


# QUICKSILVER

- FDTD, 3-D, electromagnetic PIC code
- Parallel processing
- Numerous diagnostics



# Electron Density





# Recap

- Provide method of direct measurement of the electron flow into the MITL load
- Benchmarking for Sandia National Laboratories' QUICKSILVER program suite
- Pin-point additional locations of electron loss in the line



# References

1. G. A. Mesyats, “*Pulsed Power*”, Kluwer Academic / Plenum Publishers, 2005
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3. C. W. Mendel, Jr., and S. E. Rosenthal, Phys. Plasmas 3, 4207 (1996)
4. C. W. Mendel, Jr., and D. B. Seidel, Phys. Plasmas 6, 4791 (1999)
5. C. W. Mendel, Jr., D. B. Seidel, and S. E. Rosenthal, Laser Part. Beams 1, 311 (1983)
6. P. A. Miller and C. W. Mendel, Jr., J. Appl. Phys. 61, 529 (1987)

# Vacuum Interface Region

