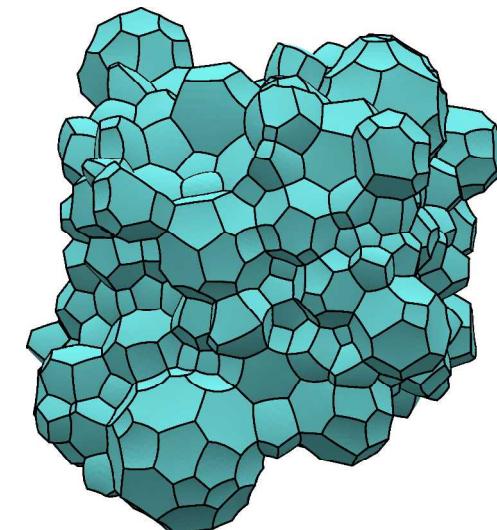
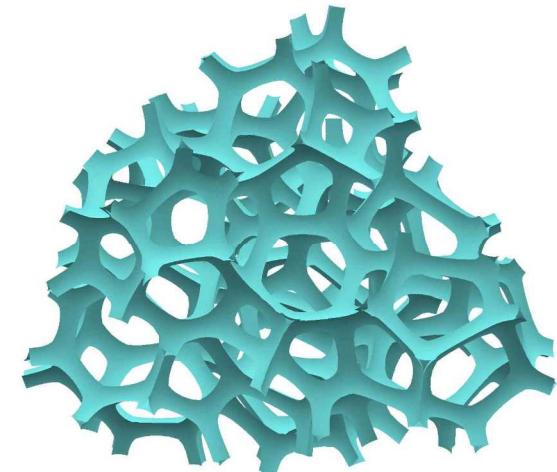
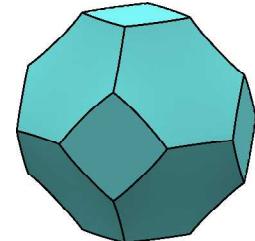
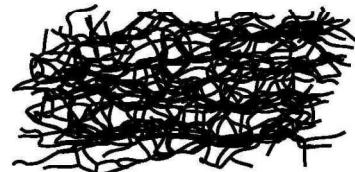
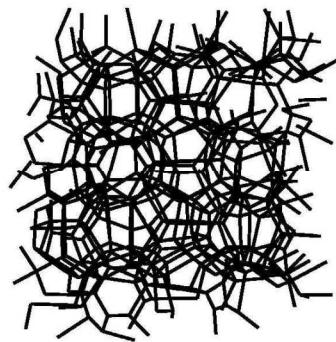
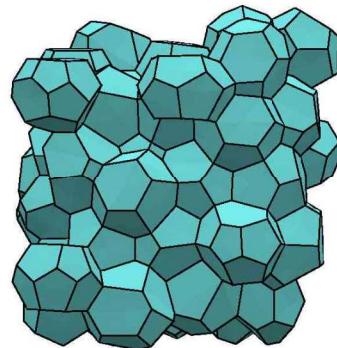
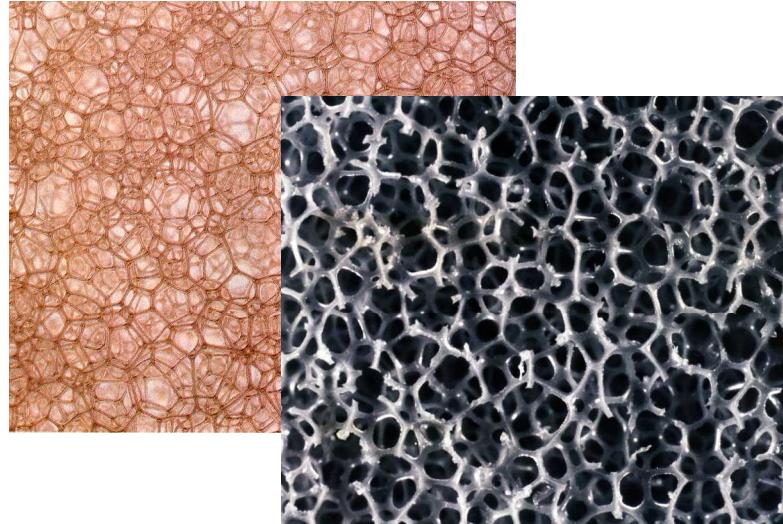


# *The Structure of Open-Cell Foams with Finite Density*

*Andy Kraynik*

*Sandia National Laboratories, Albuquerque*

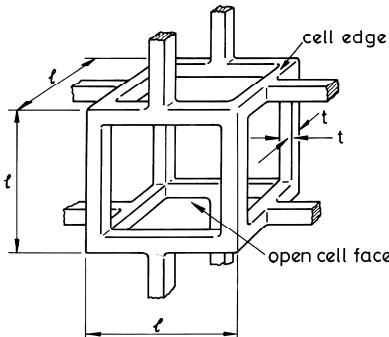


Sandia is a multiprogram laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the U.S. Department of Energy's National Nuclear Security Administration under contract #DE-AC04-94AL85000.

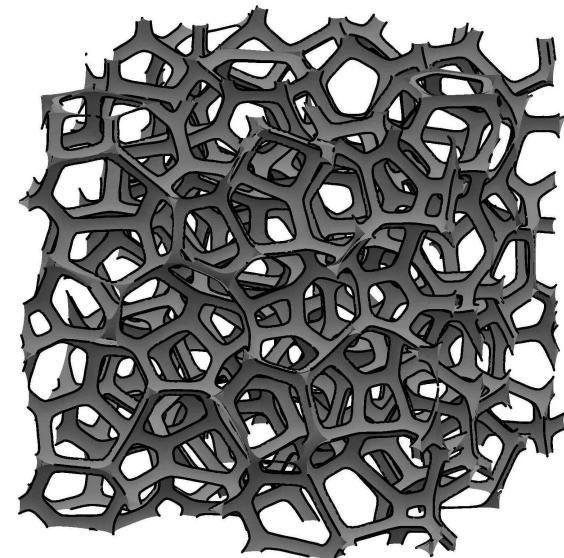
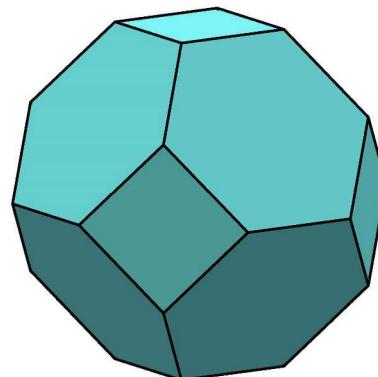
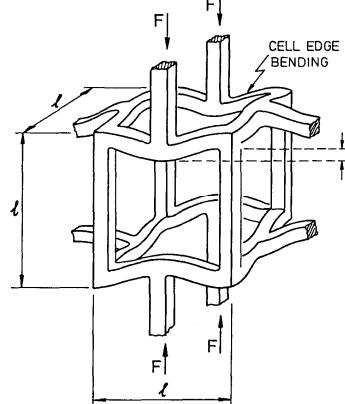
Realistic models of foam structure enable  
prediction of structure-property-processing relationships  
development of constitutive models

What are the important characteristics of foam structure?  
How much do they influence foam properties?

Which models of foam structure are realistic?  
Which are useful?



$$\frac{E^*}{E_s} \approx \left( \frac{\rho^*}{\rho_s} \right)^2$$
$$\frac{G^*}{E_s} \approx \frac{3}{8} \left( \frac{\rho^*}{\rho_s} \right)^2$$
$$\nu^* \approx \frac{1}{3}$$



# Familiar Foams

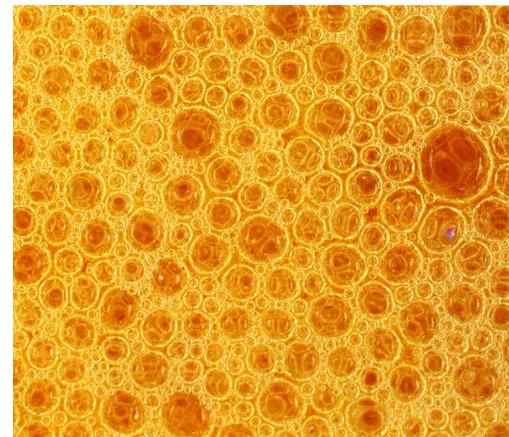
## Low-Density Foams



## Liquid Foams

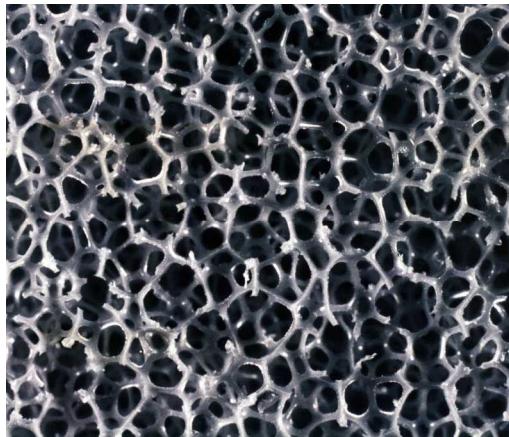
Soap Froth - “Dry” Foam  
Drained Beer Foam

## Dense Foams

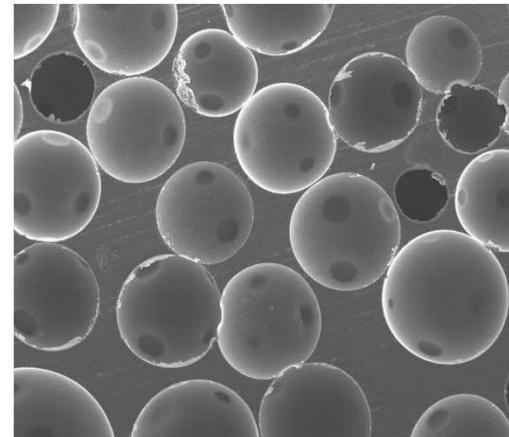


“Wet” Foam  
Fresh Beer Foam

## Solid Foams



Low-Density Open-Cell Foam  
Flexible Polyurethane Foam

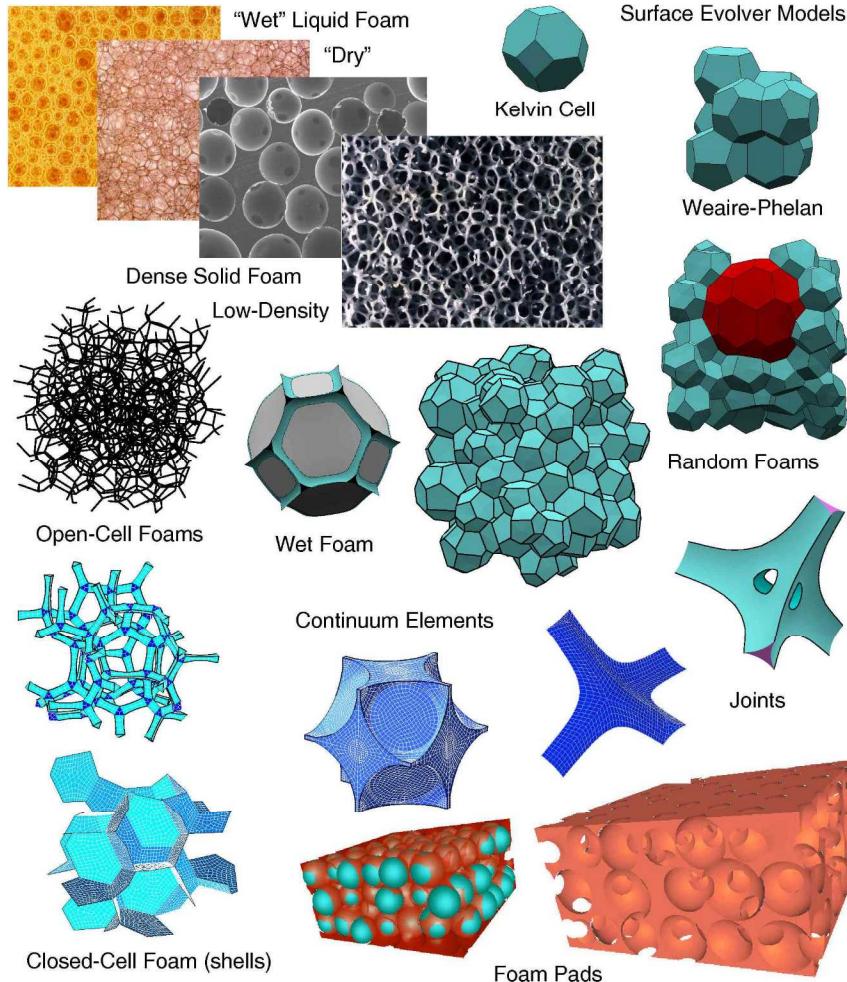


Dense Closed-Cell Foam  
Rigid Polyurethane Foam

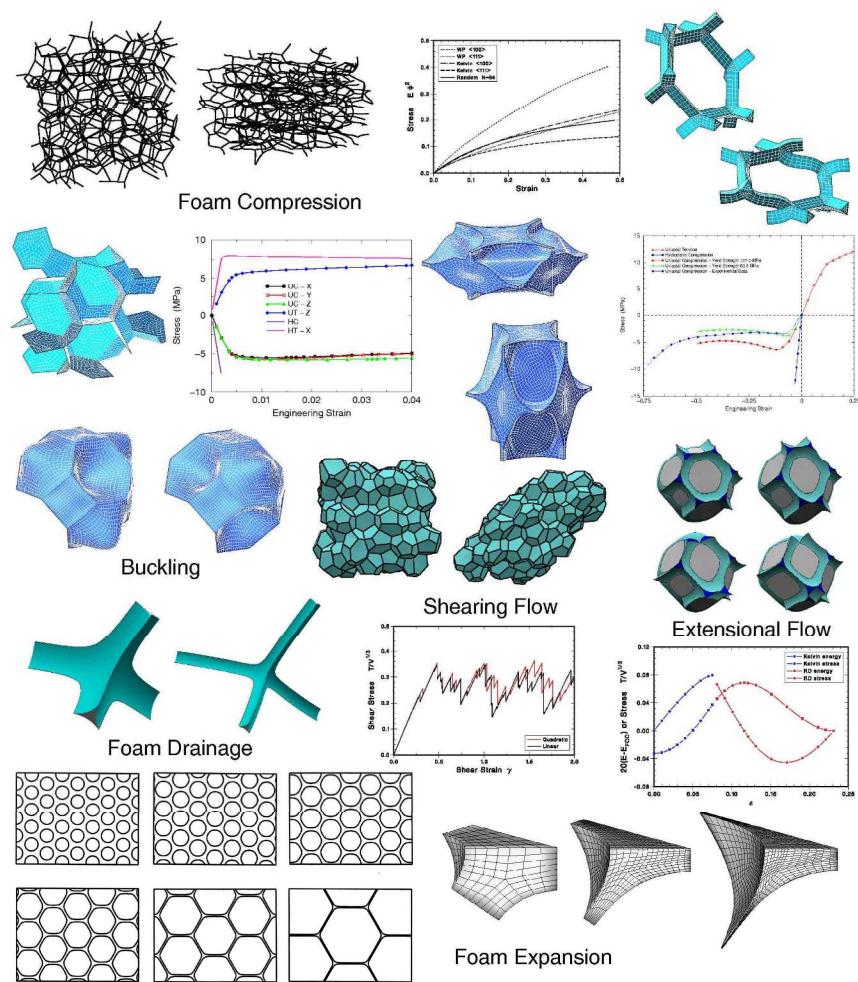
# Predicting structure-property-processing relationships involves the fluid mechanics and solid mechanics of foams



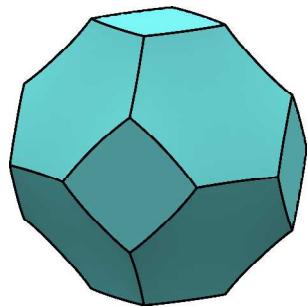
## Foam Structure: Micrographs and Models



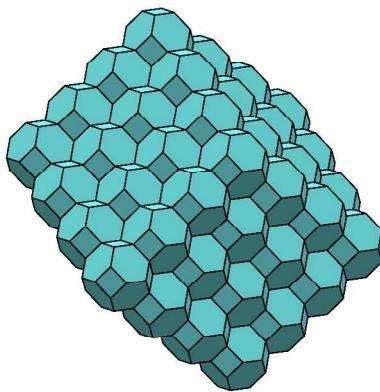
## Foam Micromechanics: Fluids and Solids



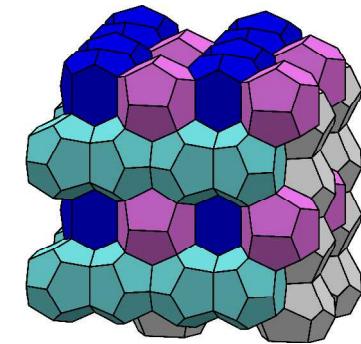
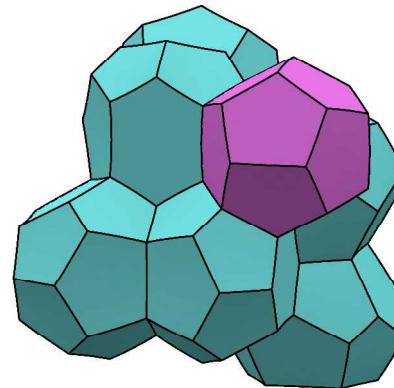
## Ordered Foams



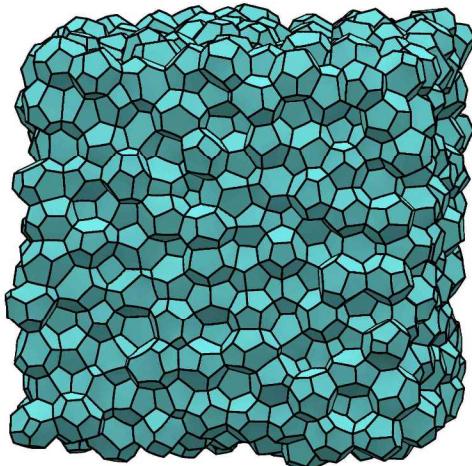
Kelvin Cell



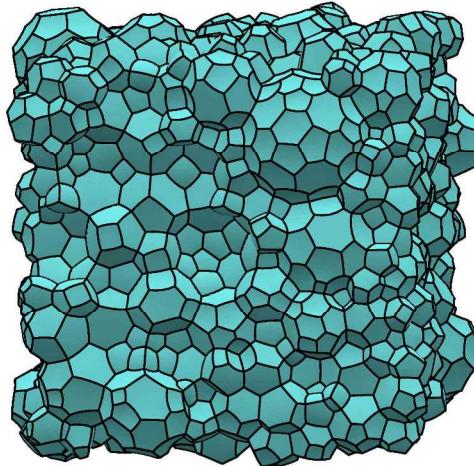
Weaire-Phelan (A15)



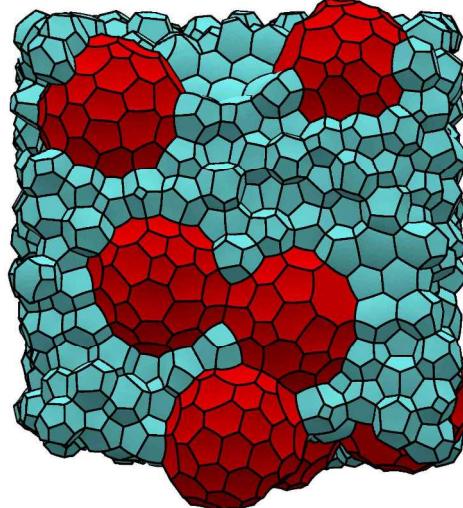
## Random Foams



Monodisperse



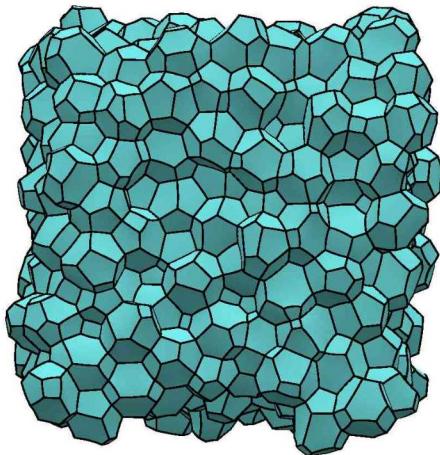
Polydisperse



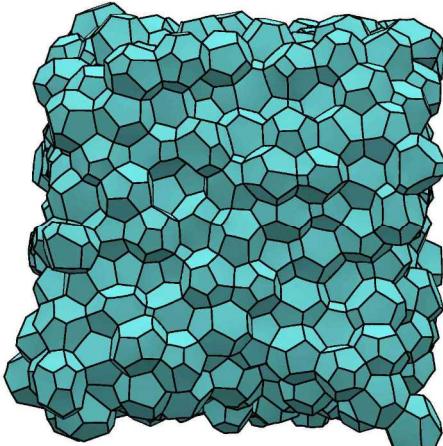
Bidisperse

# Cell Shapes in Random Monodisperse Foam

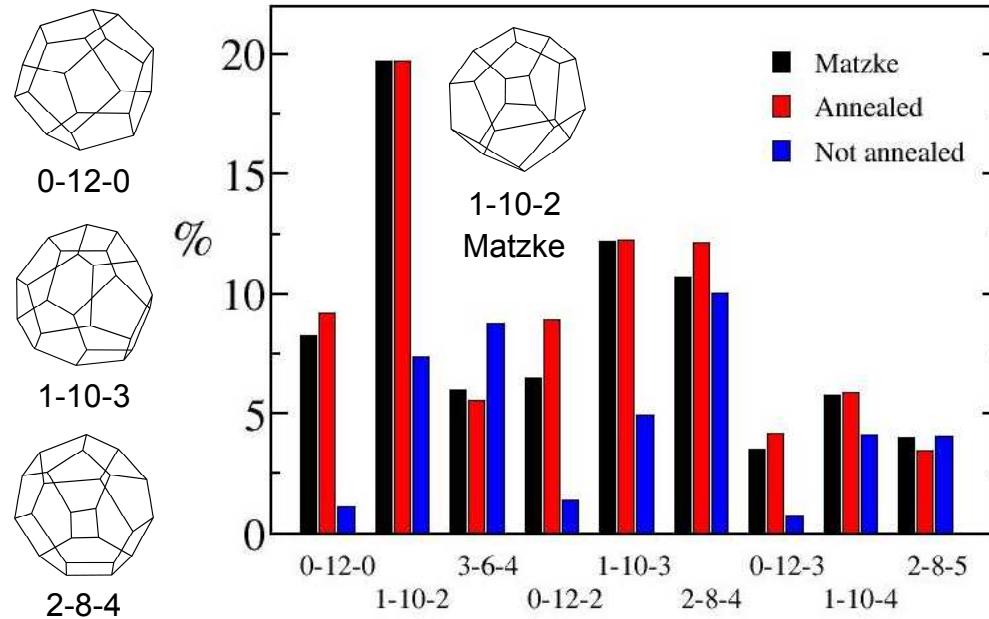
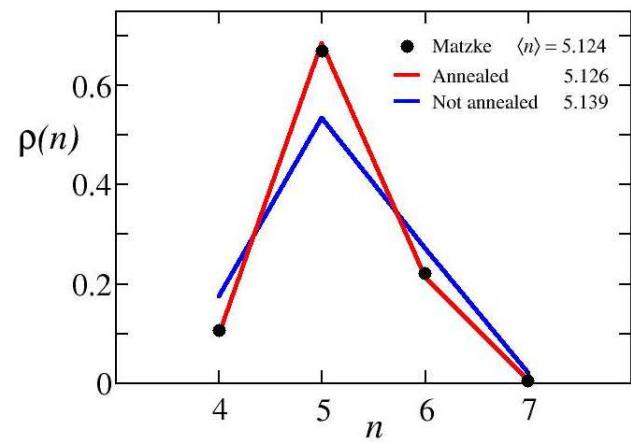
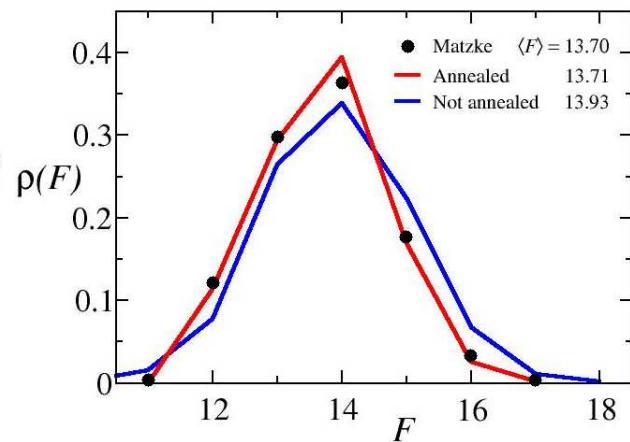
Kraynik, Reinelt & van Swol (2003) *Phys Rev E* **67**, 031403.



before annealing  
 $E = 5.369$

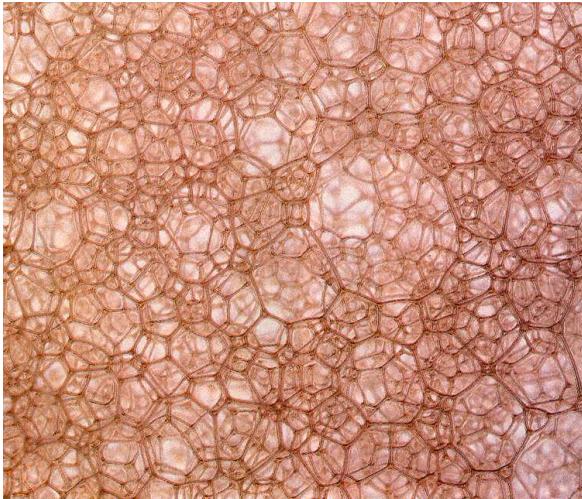


after annealing  
 $E = 5.326$

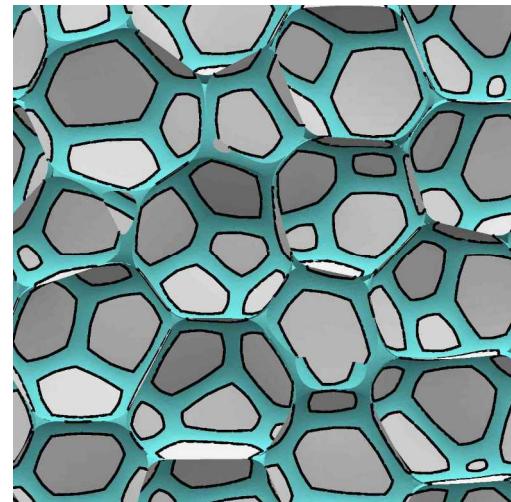
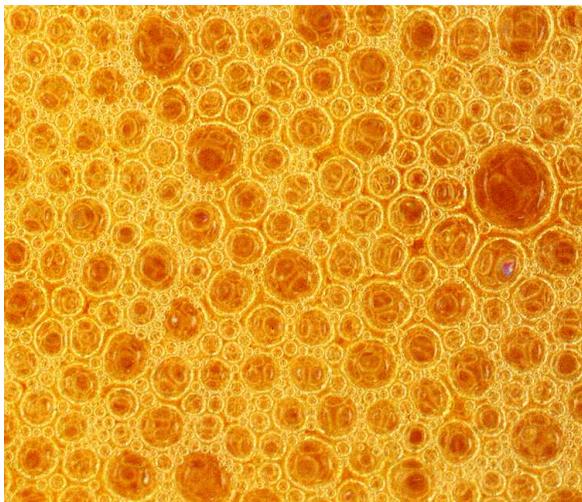
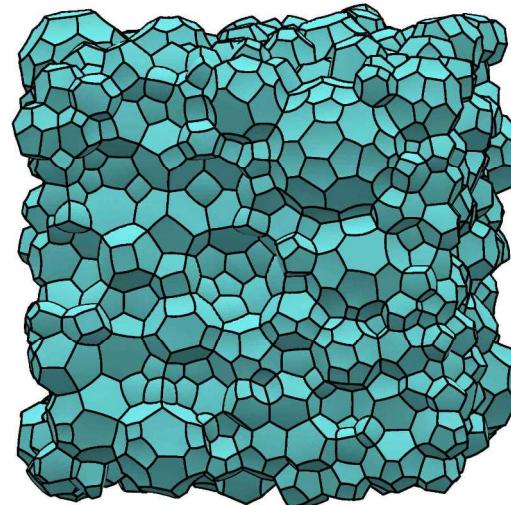


# Random Foam Structure

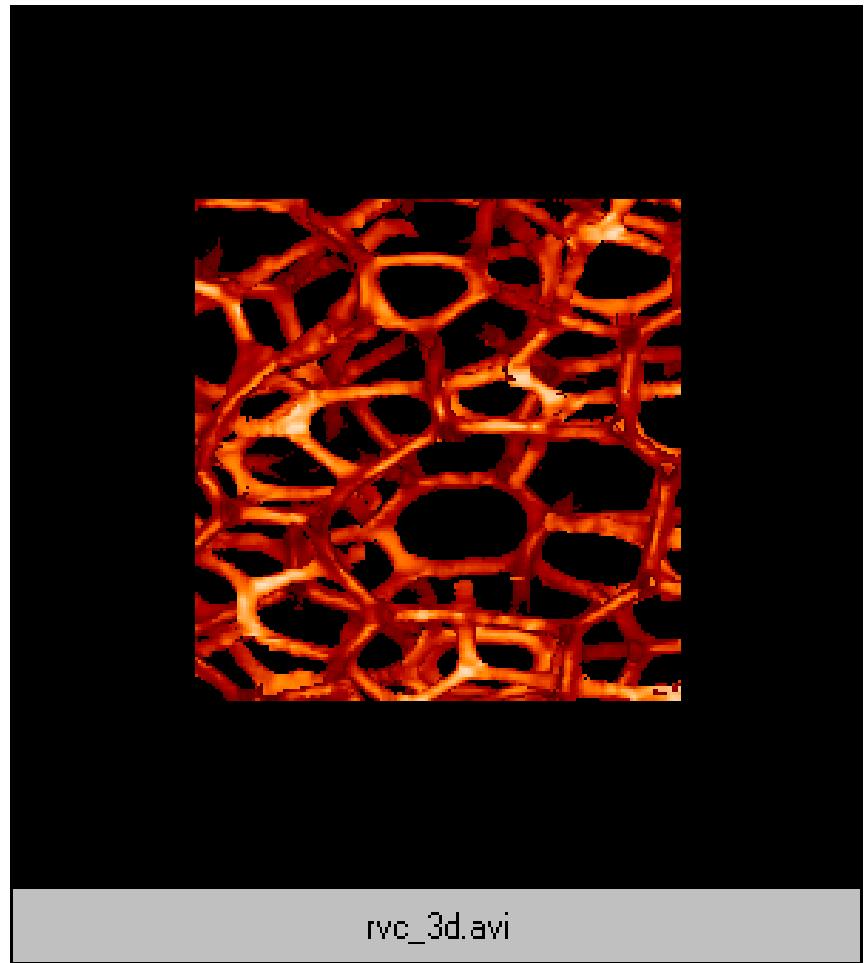
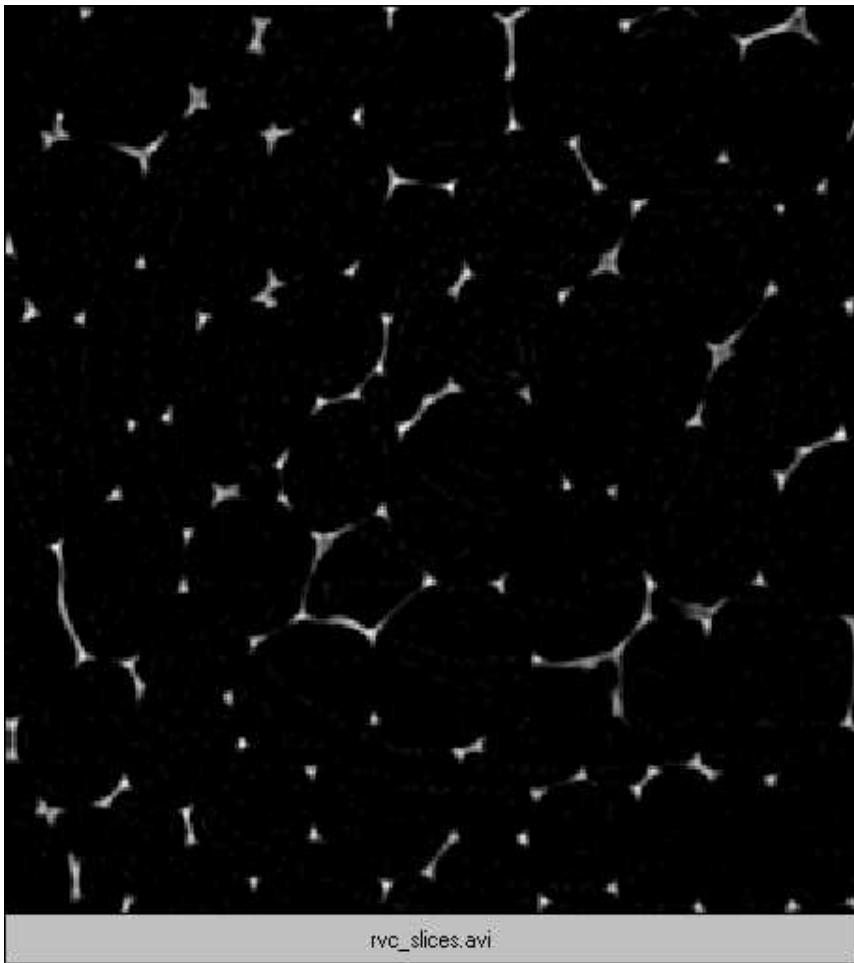
Liquid Foams



Surface Evolver Models

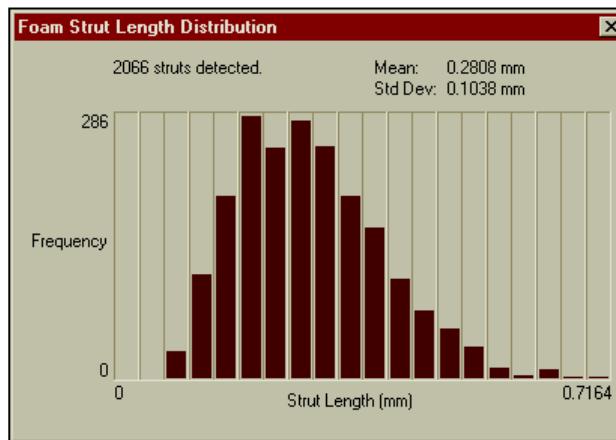
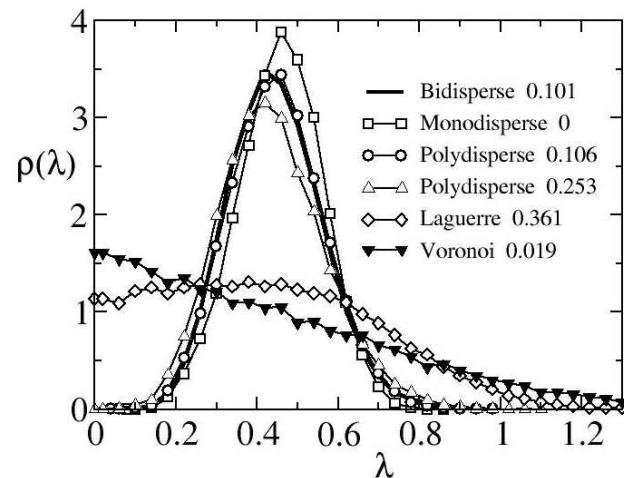
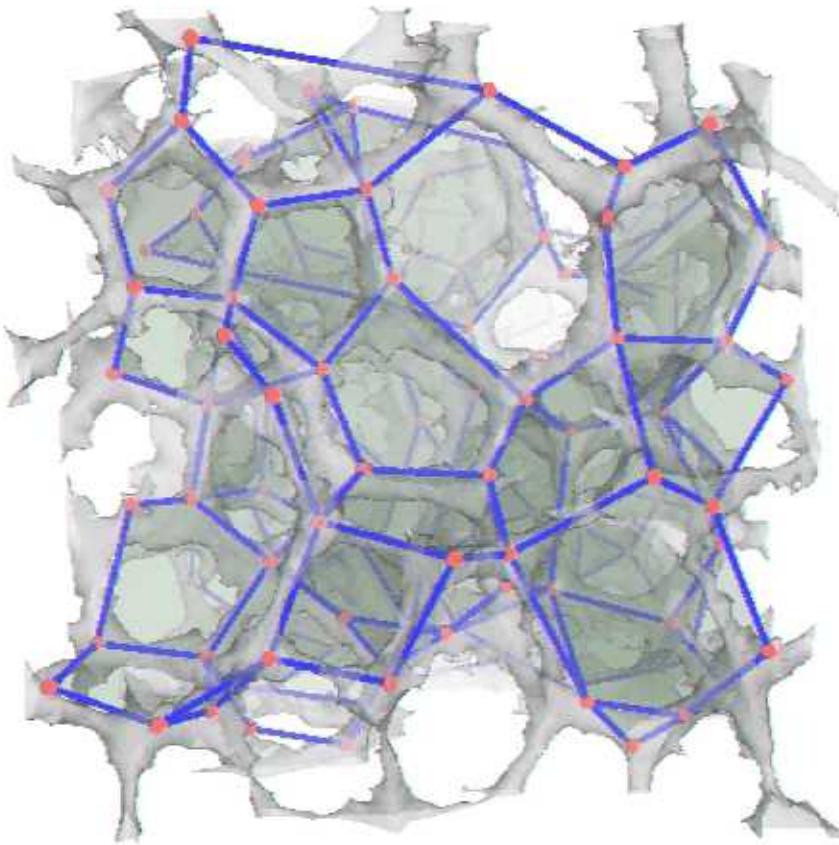


# X-ray microtomography of open-cell foams



Jerry Seidler, Physics Department, University of Washington

# Foam skeleton from image analysis of MRI and XMT data

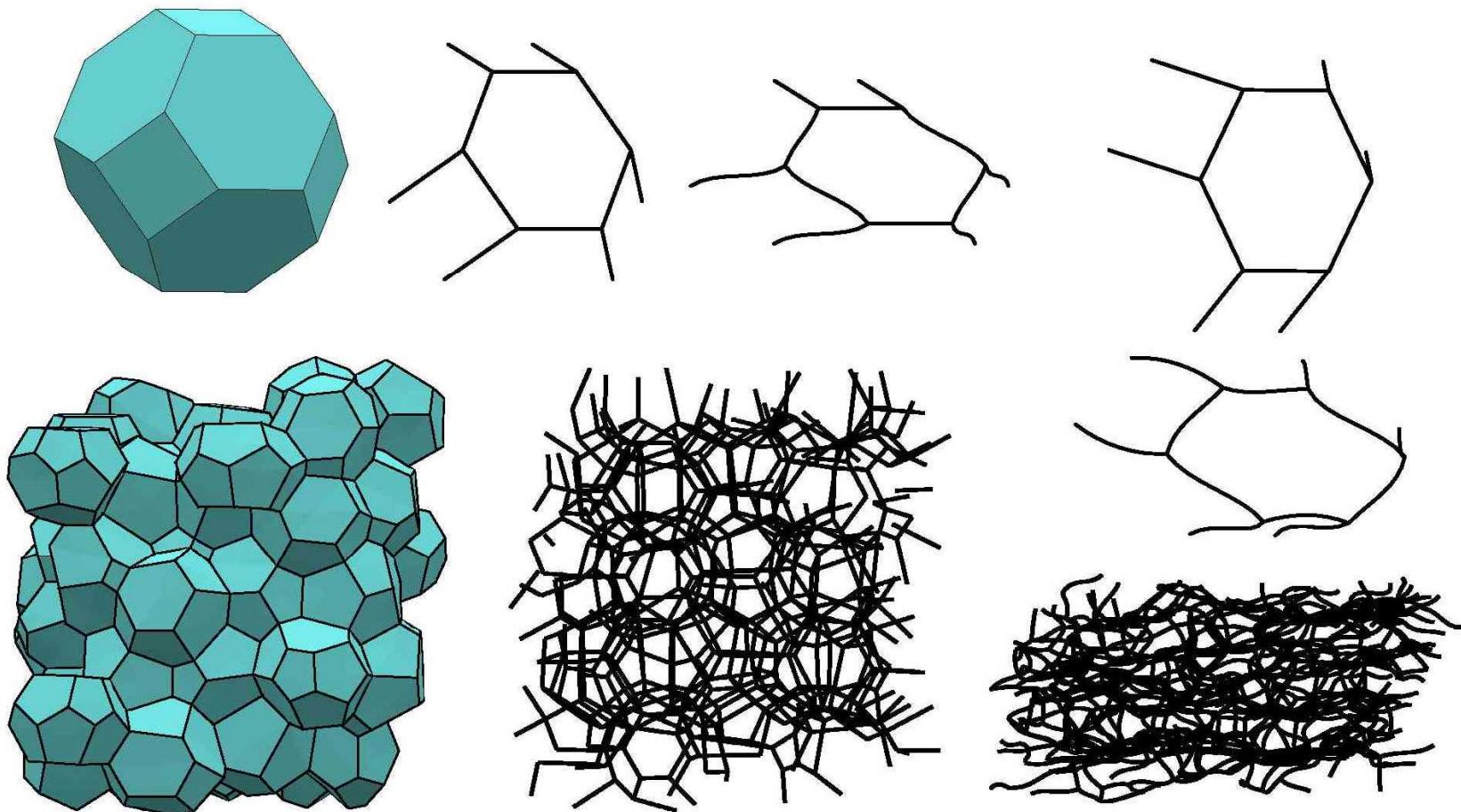


Strut length distribution

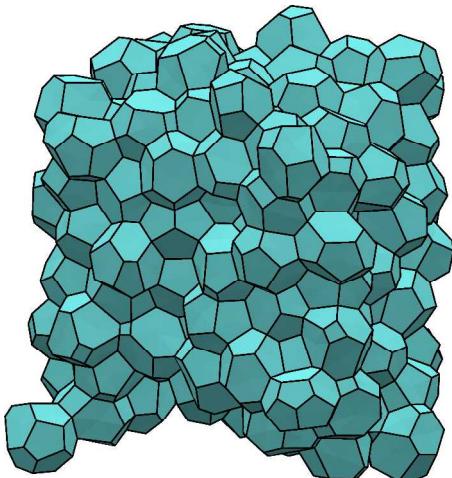
Matt Montminy, PhD thesis, Univ. Minnesota (2001)

M.D. Montminy, A.R. Tannenbaum and C.W. Macosko,  
The 3D structure of real polymer foams, *J. Coll. Int. Sci.* **280** 202-211 (2004).

## Modeling low-density open-cell foams

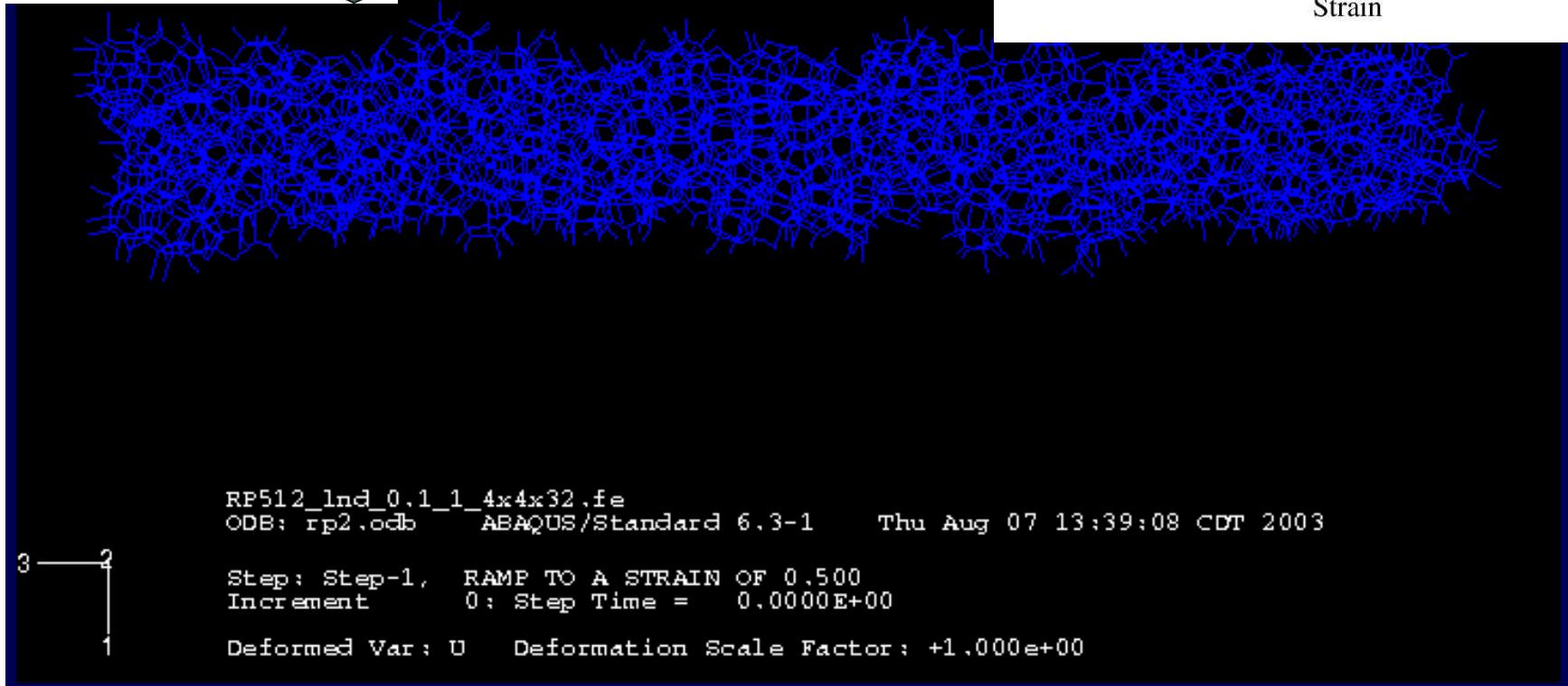
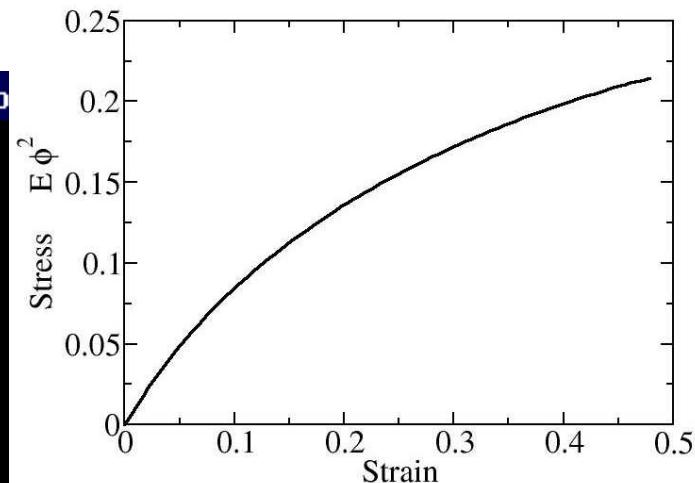


# Simulation of Uniaxial Compression

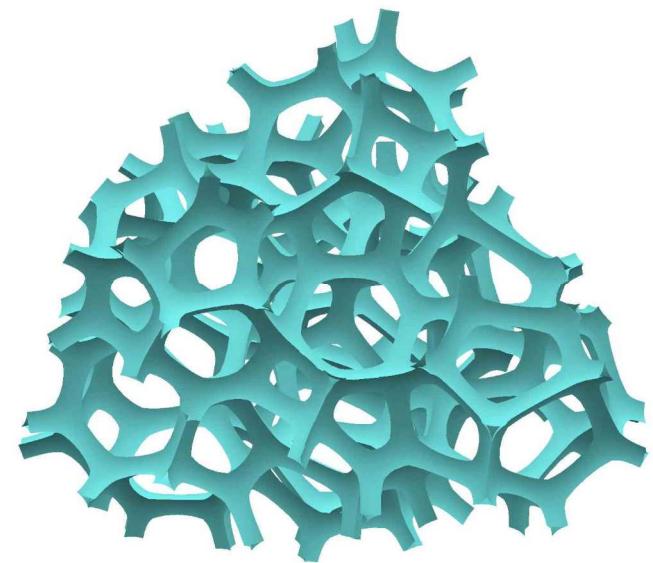
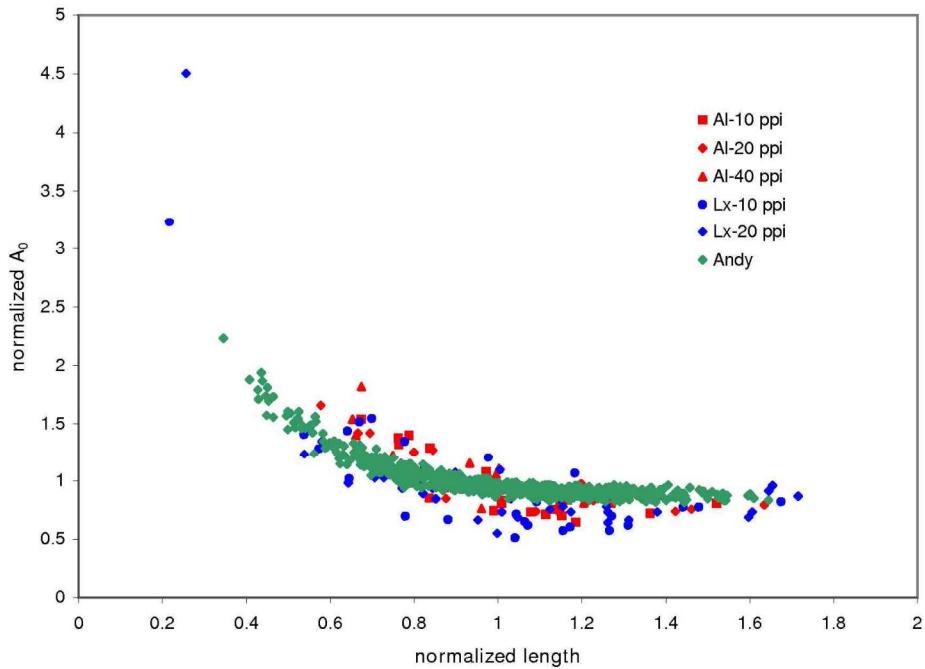


Animation by Mike Nielsen

Viewport: 1 ODB: /scratch/u99932/rp



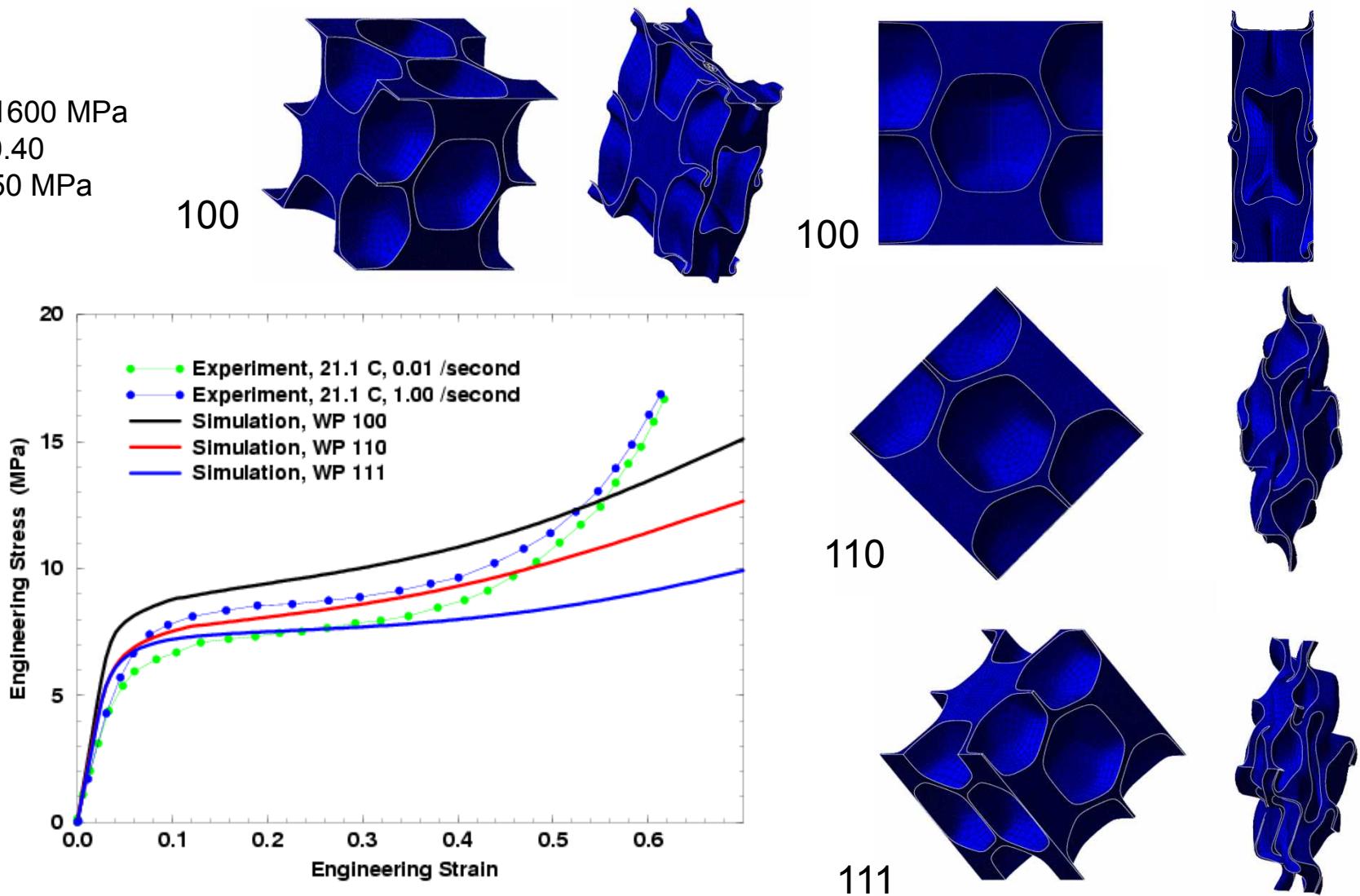
# Material Distribution in Struts



Kyriakides and Jang, UT, Austin

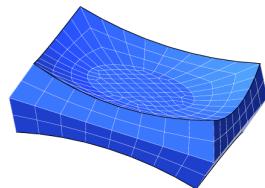
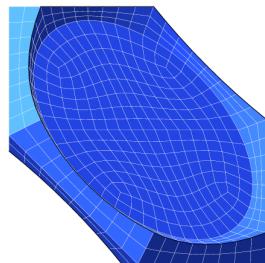
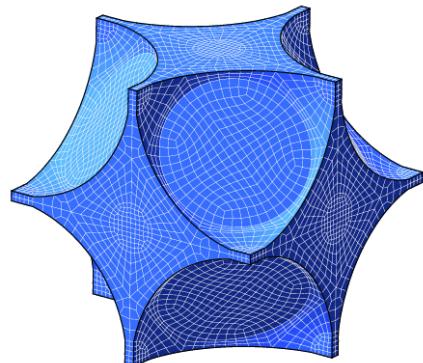
# Uniaxial Compression of a Closed-Cell Weaire-Phelan Foam

$$\begin{aligned}E_s &= 1600 \text{ MPa} \\v_s &= 0.40 \\{\sigma}_y &= 50 \text{ MPa}\end{aligned}$$

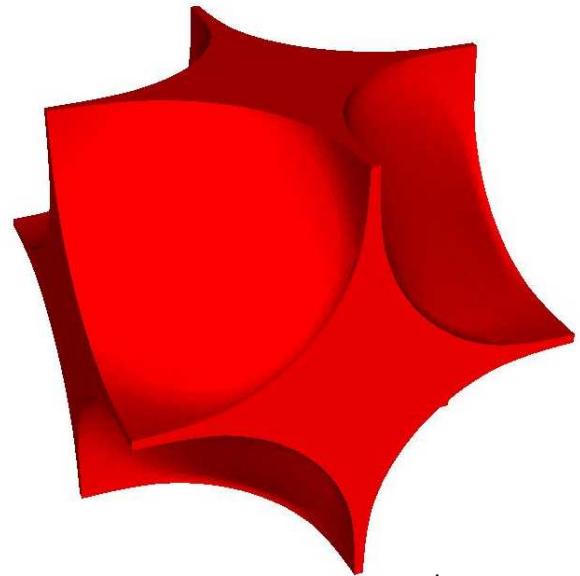


# Microstructure of Closed-Cell Kelvin Foam

Simple model based on flat plates and spherical cavities

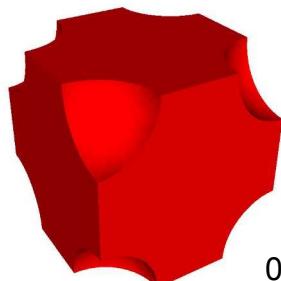


Mike Nielsen

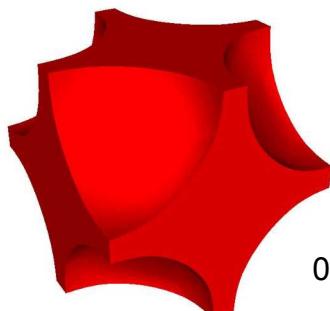


$\phi = 0.075$

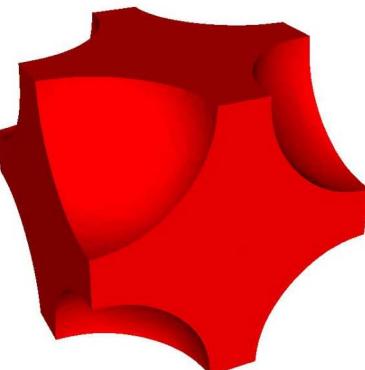
Use GOMA to model foam evolution by simulating bubble growth in viscous fluids.



0.748

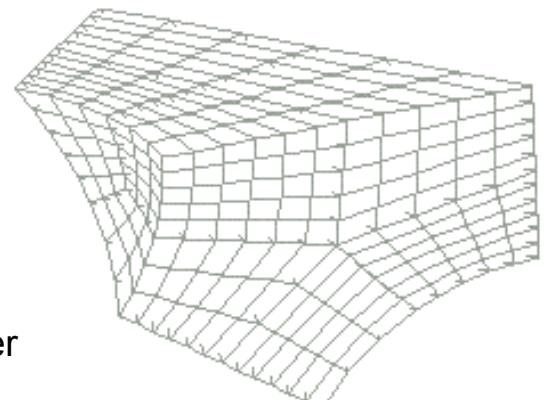


0.449

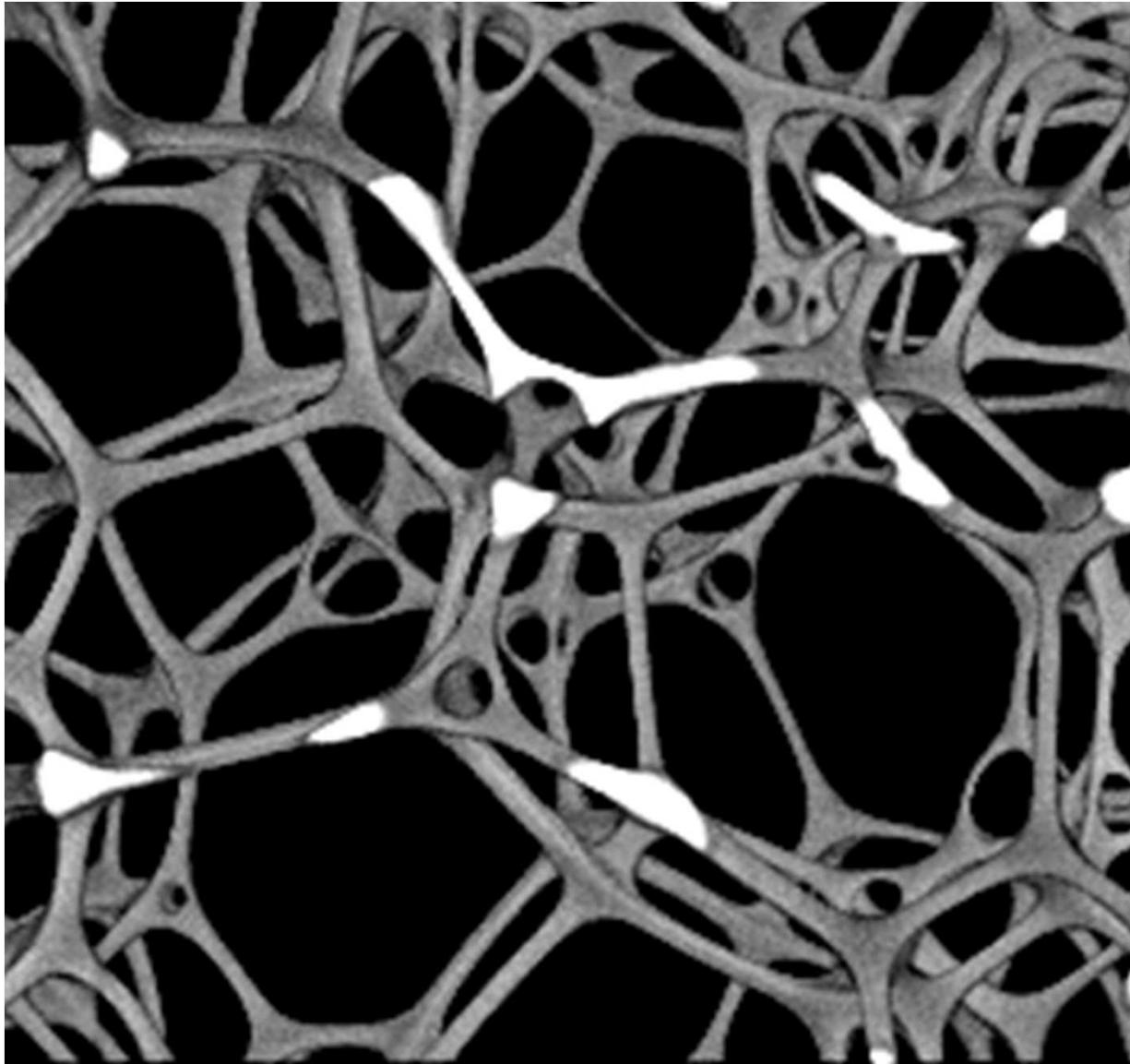


0.284

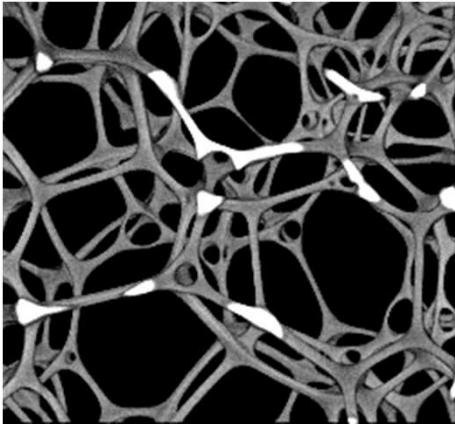
Animation by Tom Baer



# Confocal microscopy of Plateau borders in emulsions

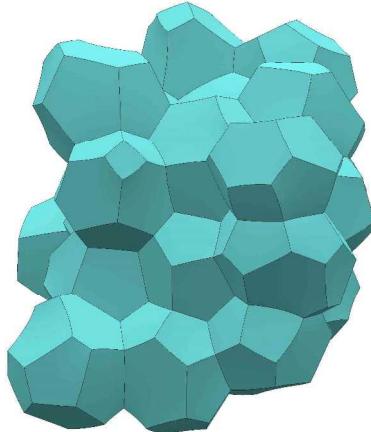


Eric Weeks, Physics, Emory University and Doug Wise, Physics, Harvard University

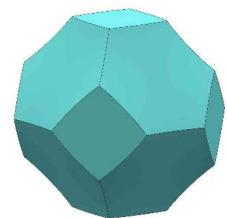


Confocal microscopy of Plateau borders  
in an emulsion

Eric Weeks (Emory), Doug Wise (Harvard)



"Dry" Random foam  
with 27 cells

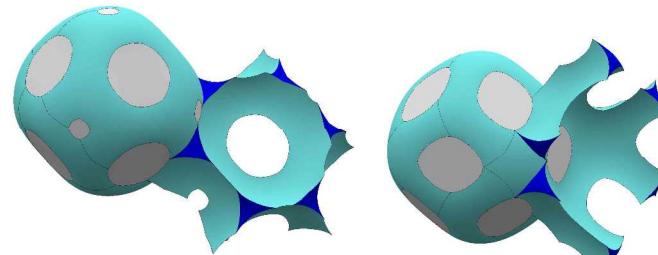


"Dry" Kelvin

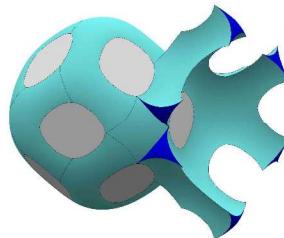
## Surface Evolver Simulations of Wet Foams with 8% liquid



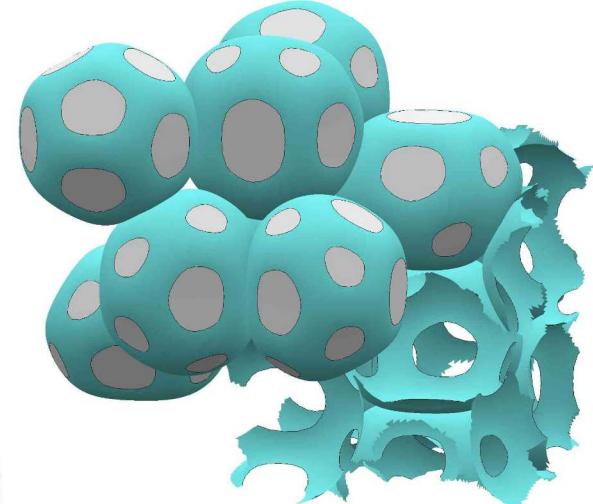
Andy Kraynik  
[amkrayn@sandia.gov](mailto:amkrayn@sandia.gov)



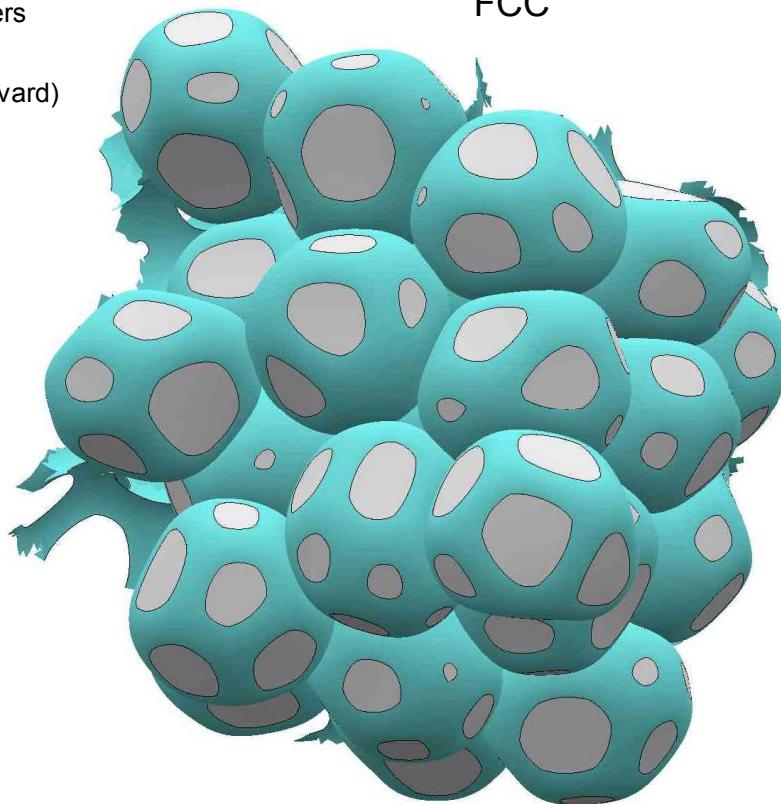
Kelvin



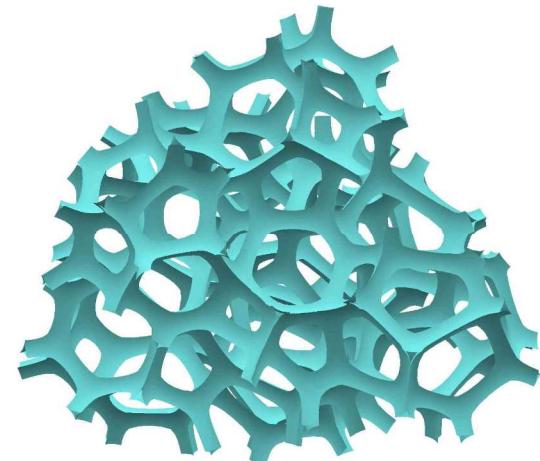
FCC



Weaire-Phelan

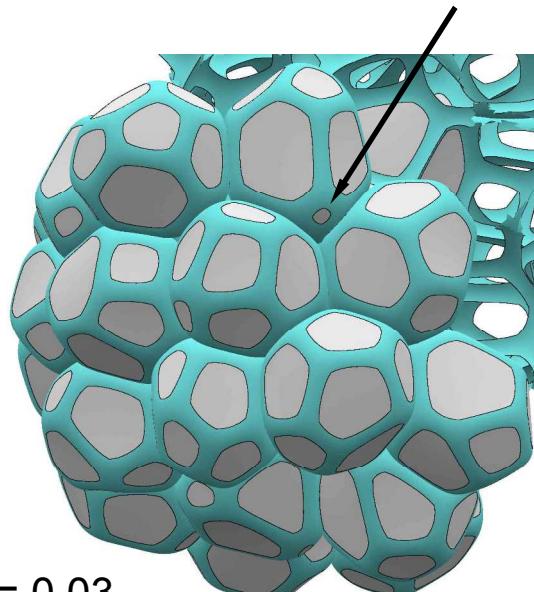


Random foam with 27 bubbles



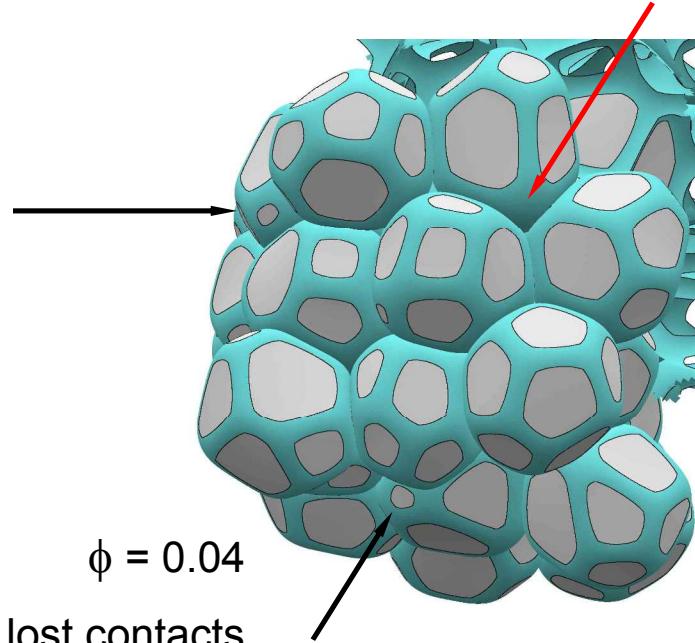
Plateau borders

Random  
Monodisperse  
27 cells



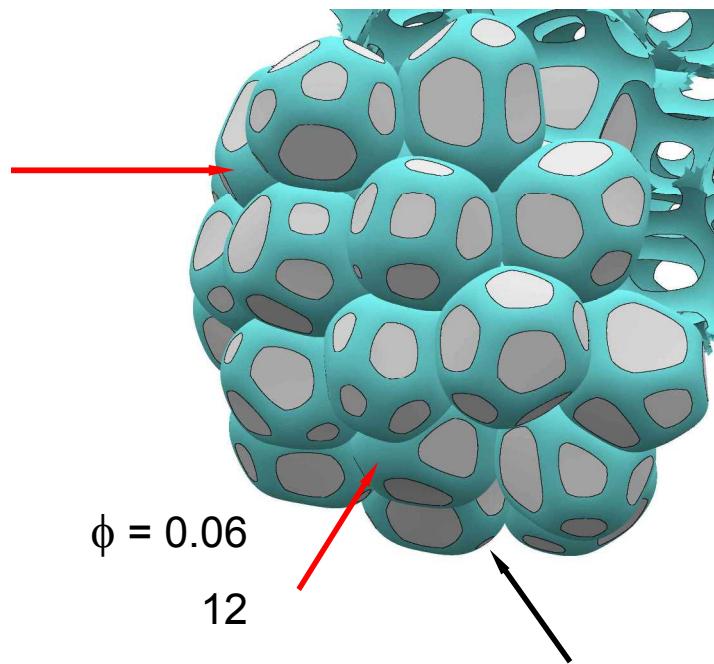
$$\phi = 0.03$$

0



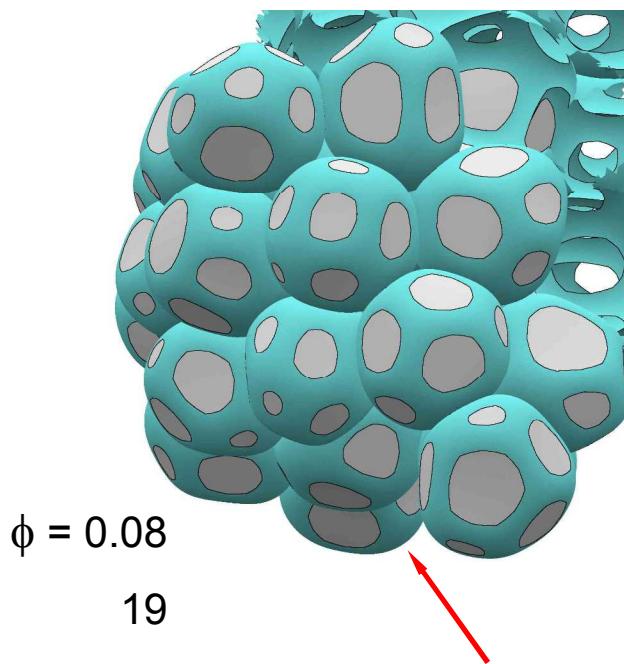
$$\phi = 0.04$$

7 lost contacts



$$\phi = 0.06$$

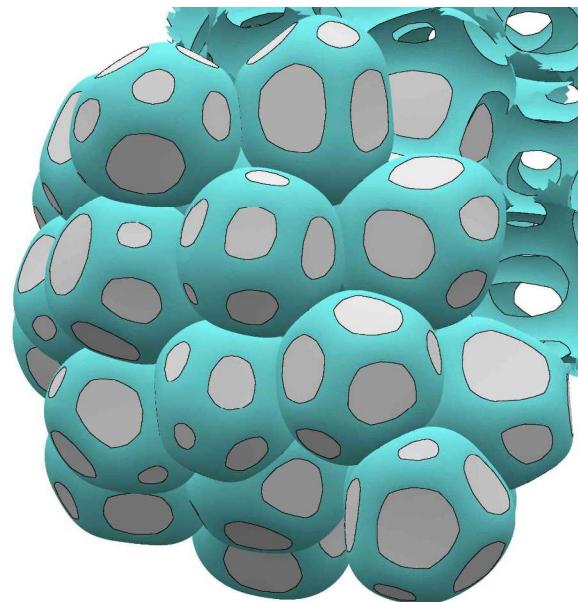
12



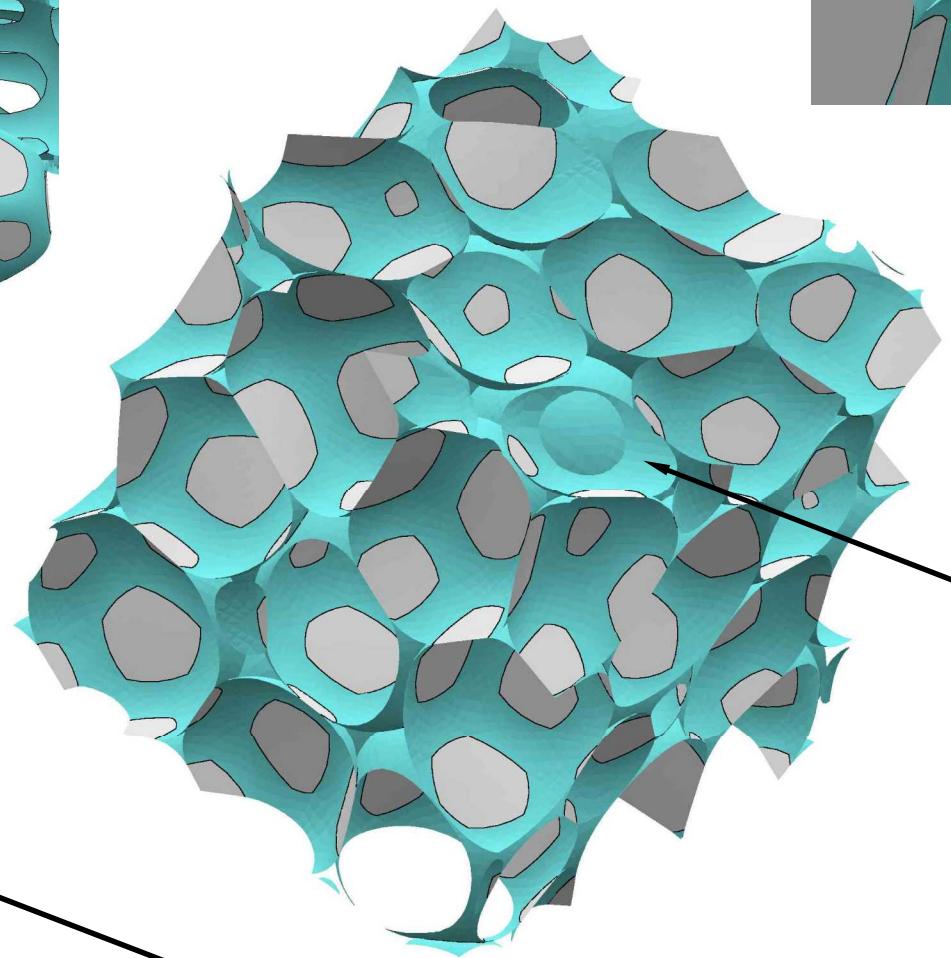
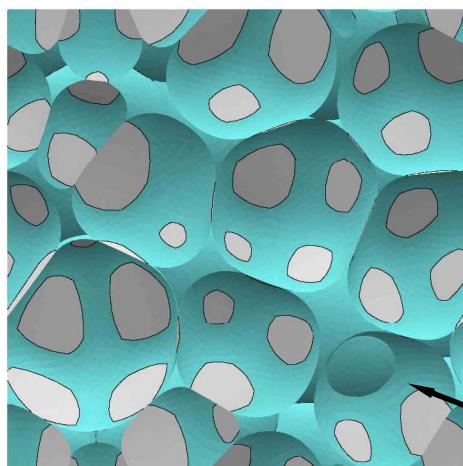
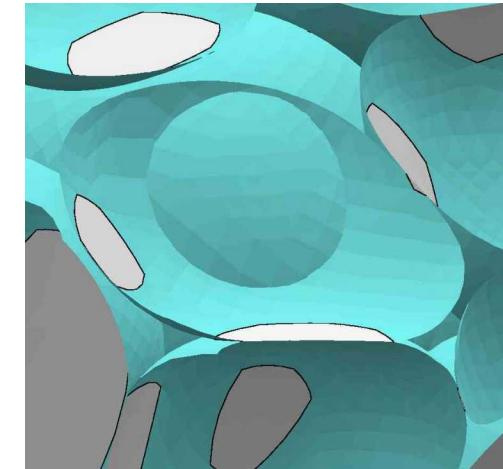
$$\phi = 0.08$$

19

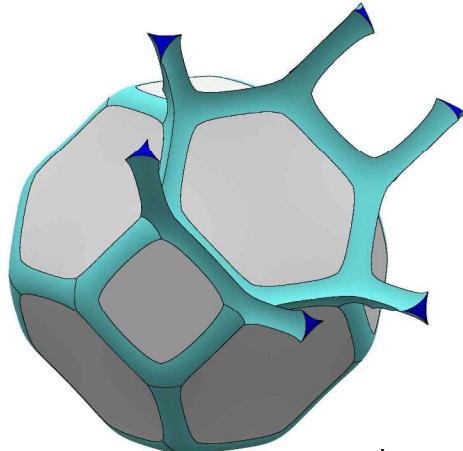
## Bubble Overlap



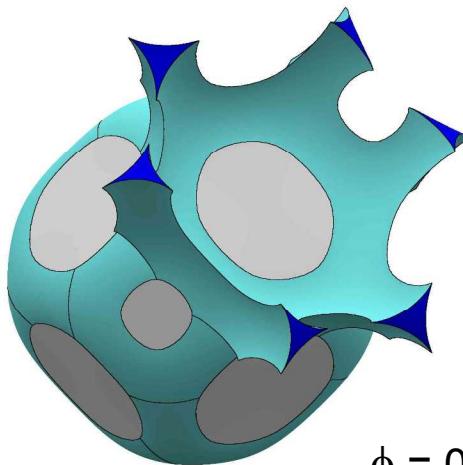
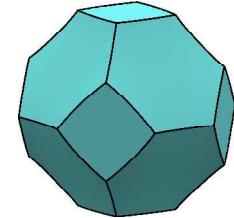
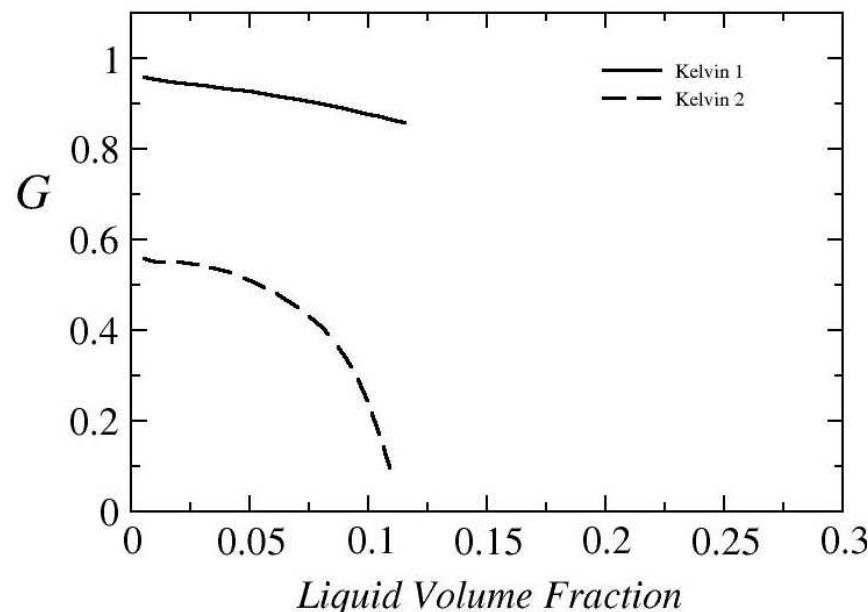
$\phi = 0.08$  19 lost contacts



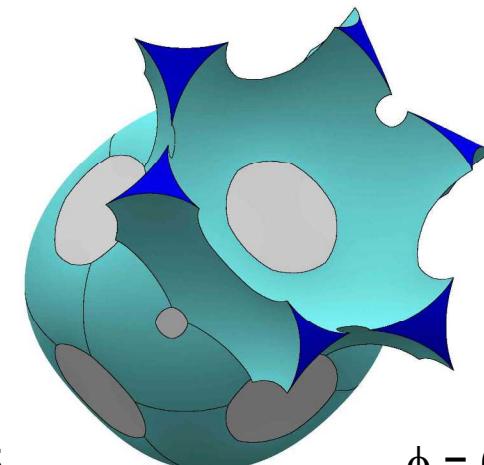
# Wet Kelvin Foam BCC



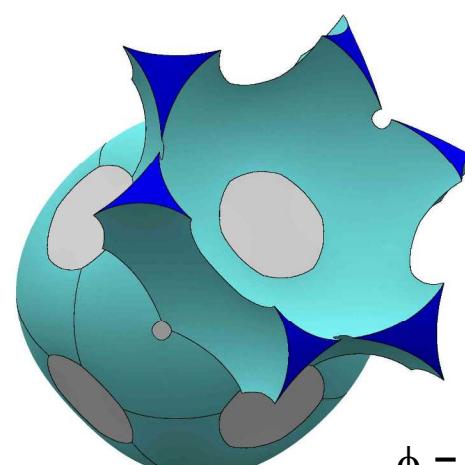
$\phi = 0.01$



$\phi = 0.05$

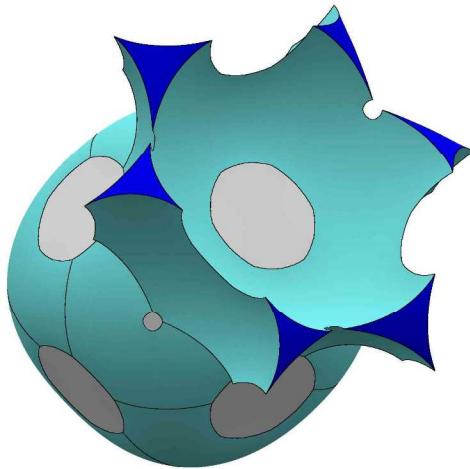


$\phi = 0.1$

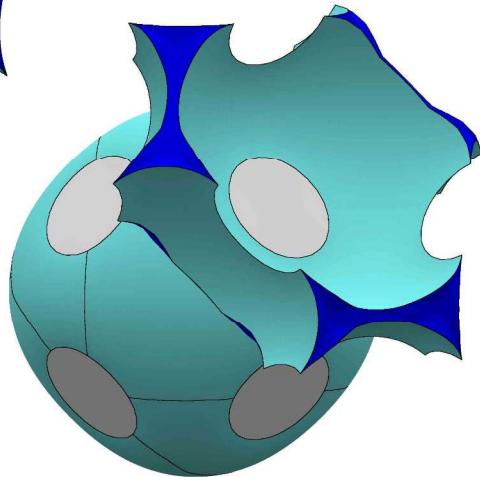


$\phi = 0.115$

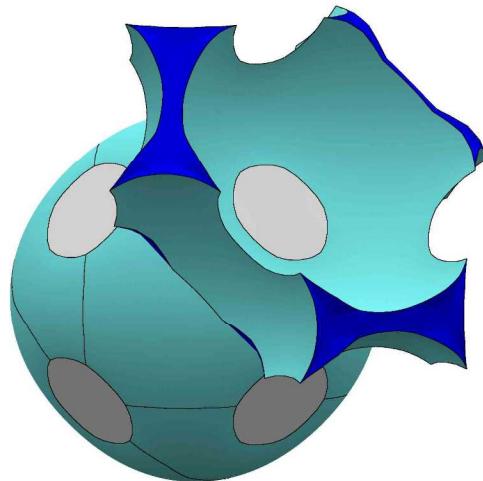
# Very Wet Kelvin Foam



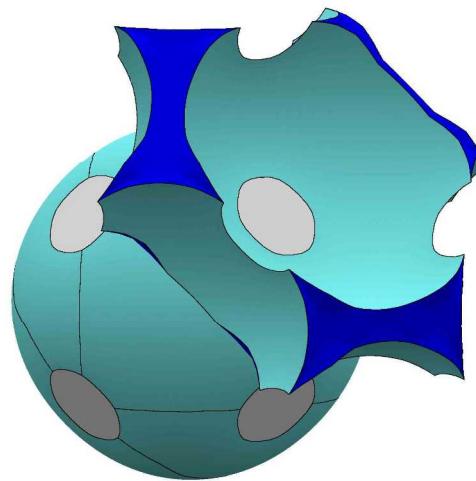
$\phi = 0.115$



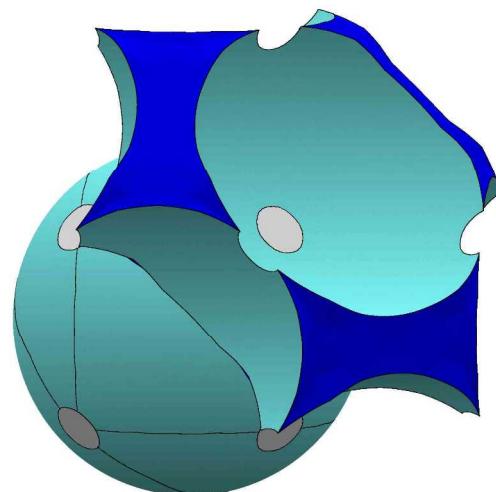
$\phi = 0.12$



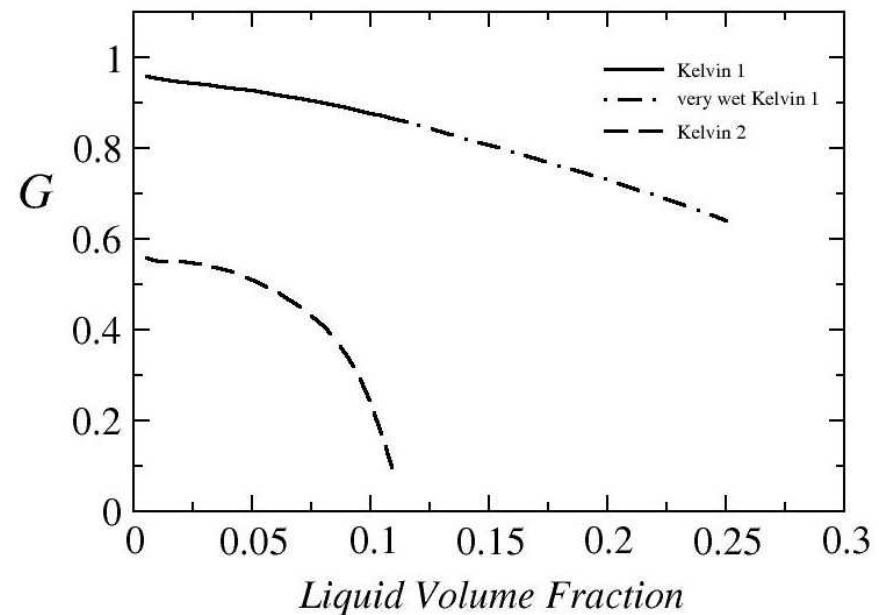
$\phi = 0.15$



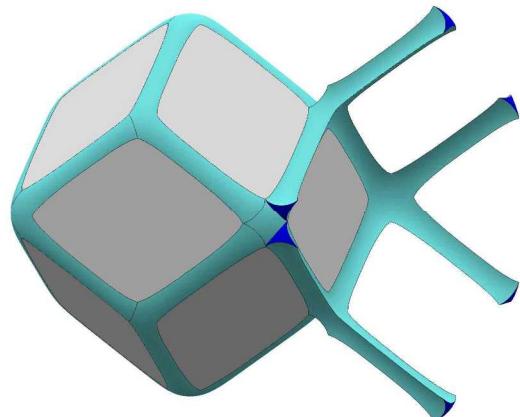
$\phi = 0.2$



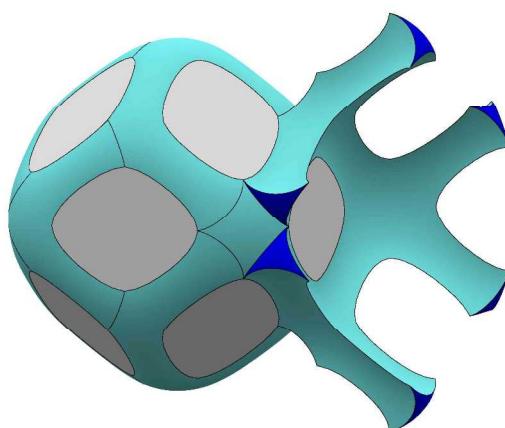
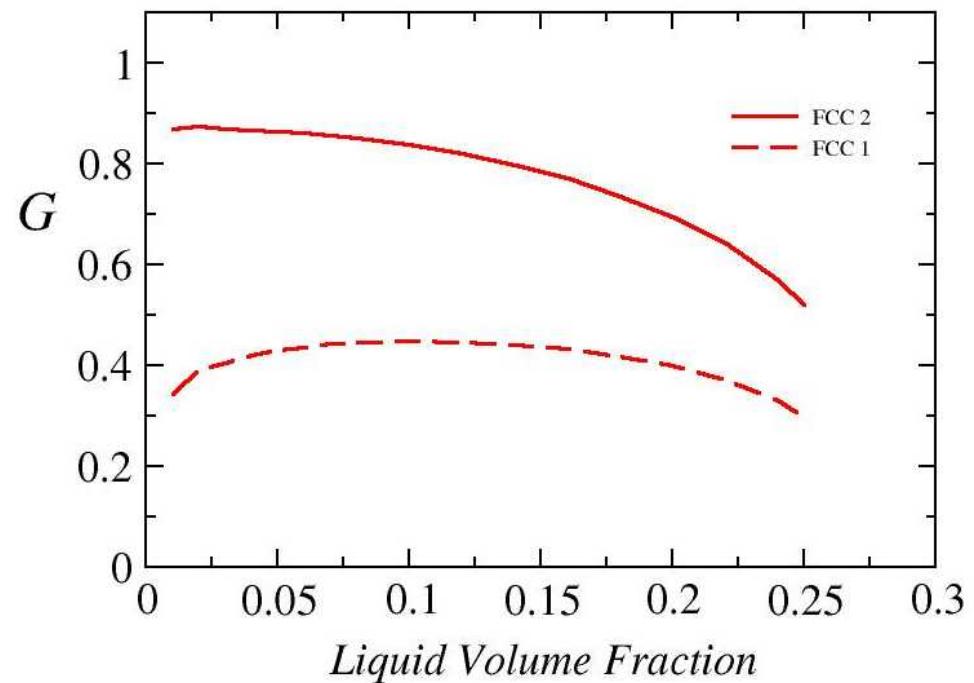
$\phi = 0.3$



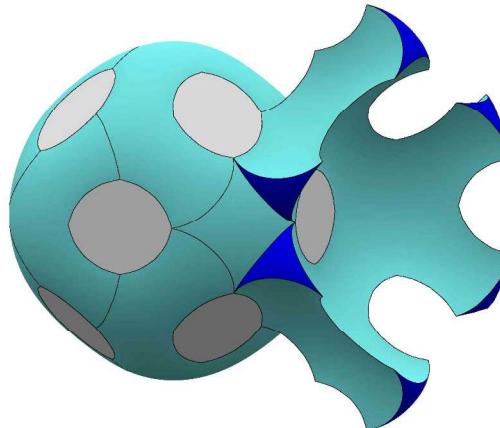
# Wet Rhombic Dodecahedra FCC



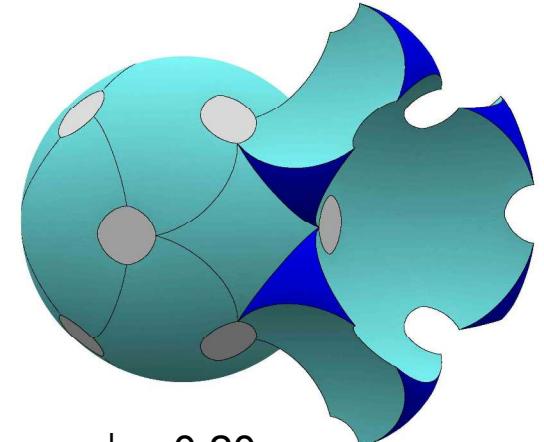
$\phi = 0.01$



$\phi = 0.05$

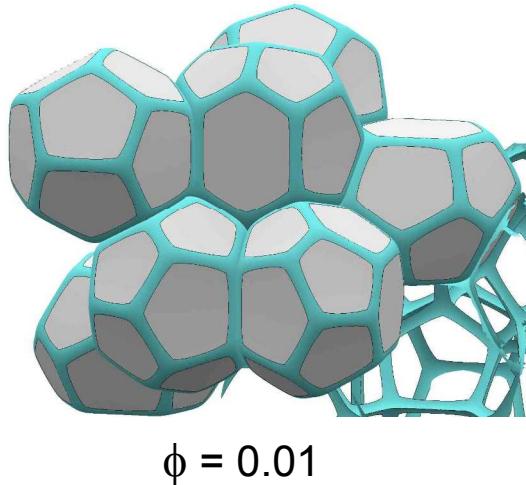


$\phi = 0.1$

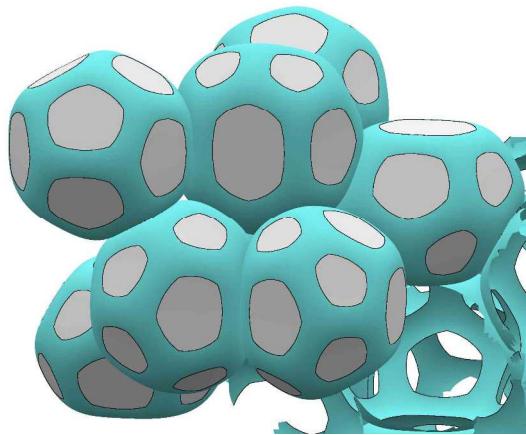


$\phi = 0.20$

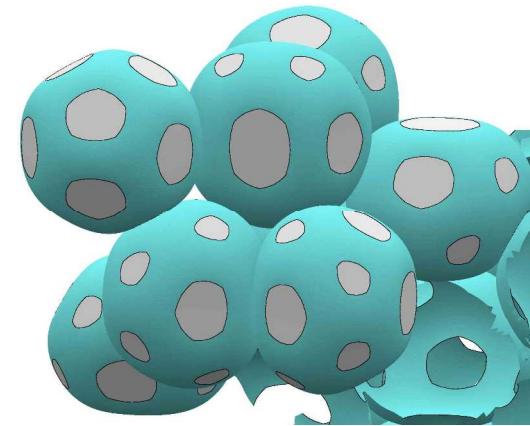
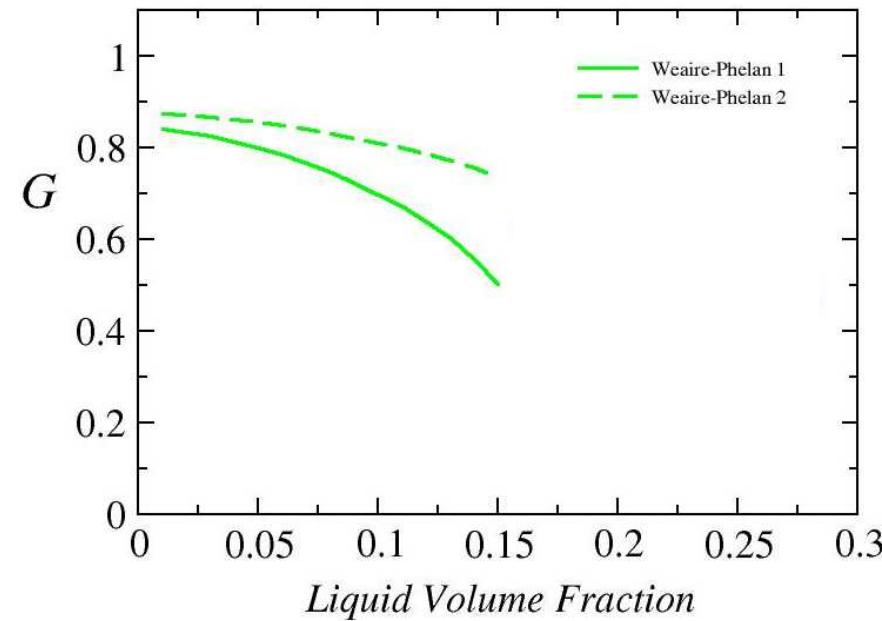
# Wet Weaire-Phelan



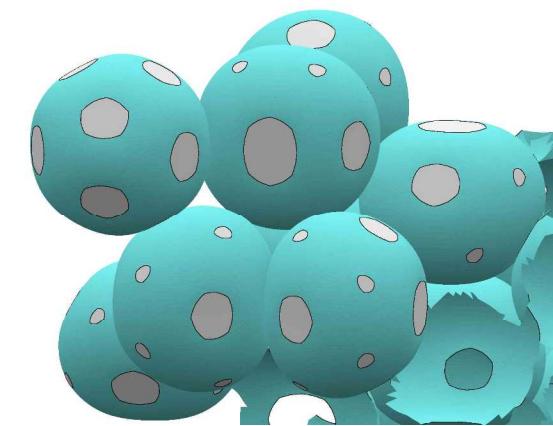
$\phi = 0.01$



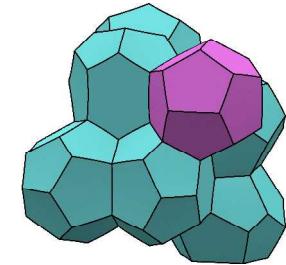
$\phi = 0.05$



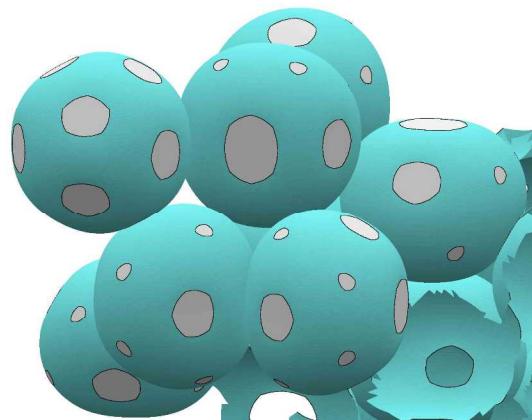
$\phi = 0.1$



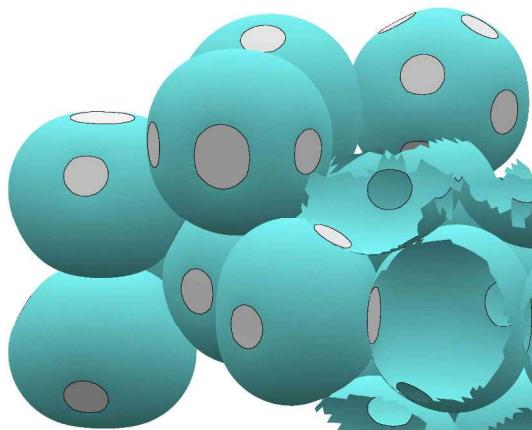
$\phi = 0.15$



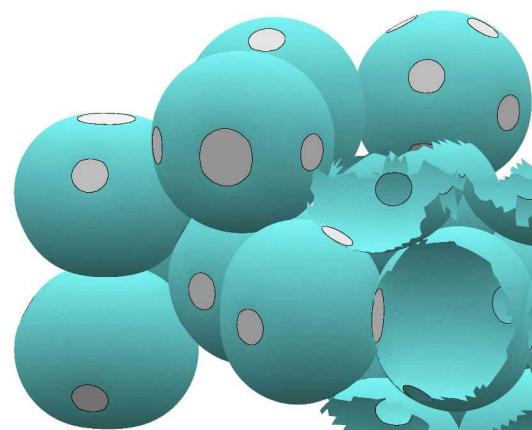
## Very Wet Weaire-Phelan



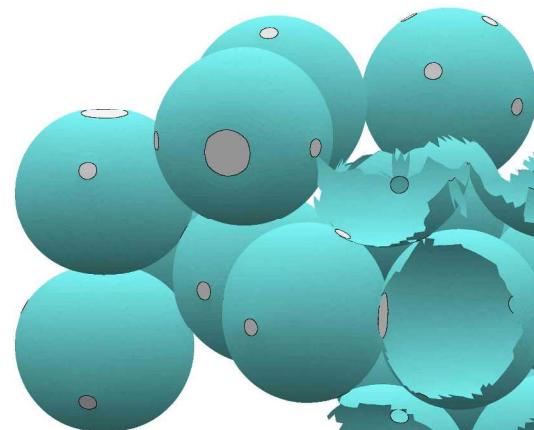
$\phi = 0.15$



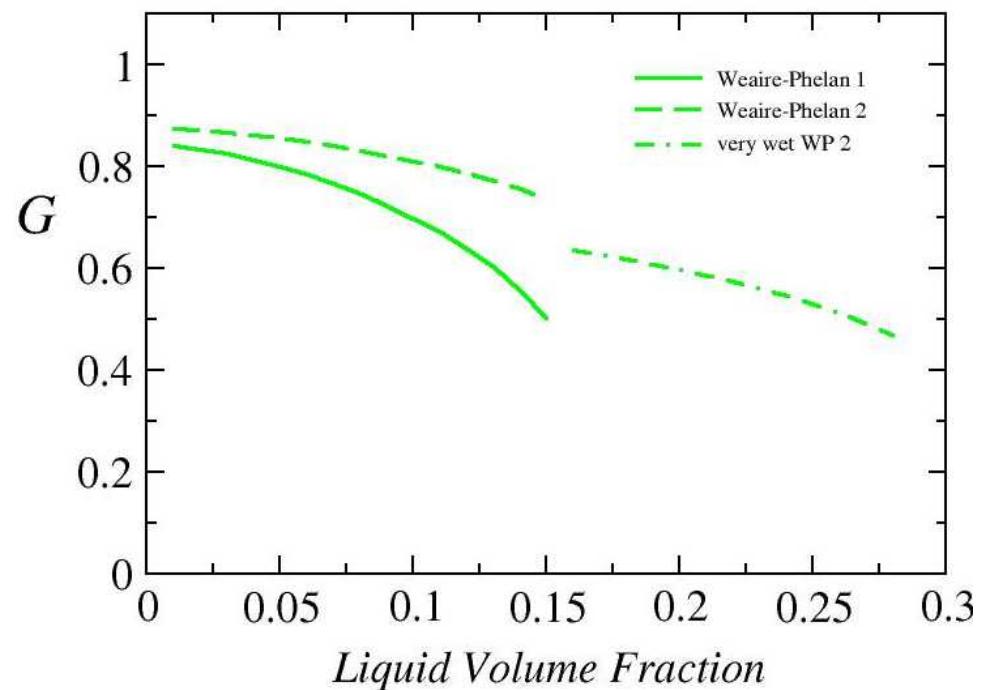
$\phi = 0.16$



$\phi = 0.2$



$\phi = 0.3$



## Overview

Foams are ubiquitous materials but the connection between the macroscopic behavior and cell-level microstructure is poorly understood.

Accurate structure-property-processing relationships and constitutive models are needed to develop foams and predict response.

Complementary experiments and theoretical studies are needed to accomplish this goal.

Micromechanical analysis is used to predict the connection between foam structure and behavior.