

# Three dimensional effects in trailing mass in the wire-array Z pinch

Edmund Yu

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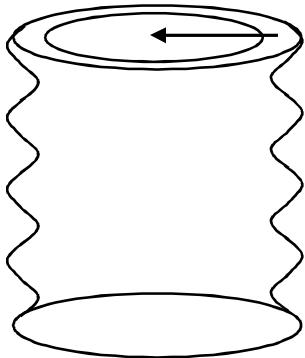
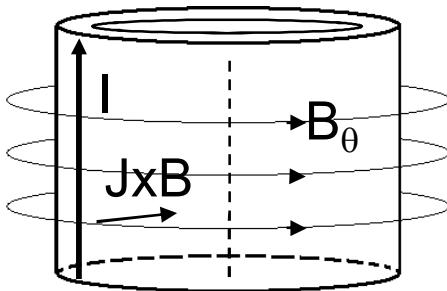
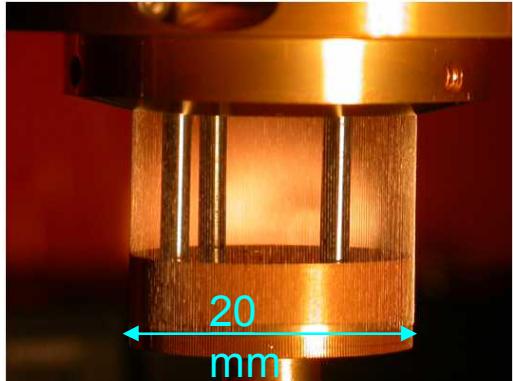
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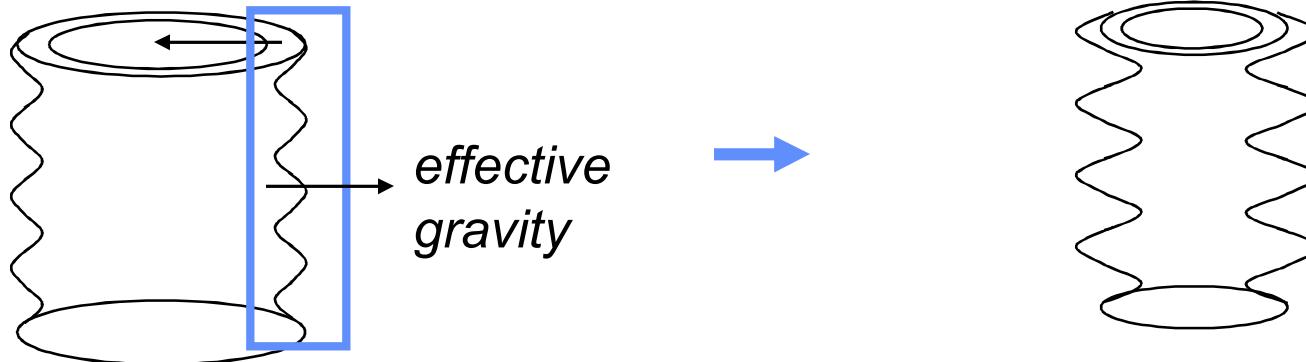
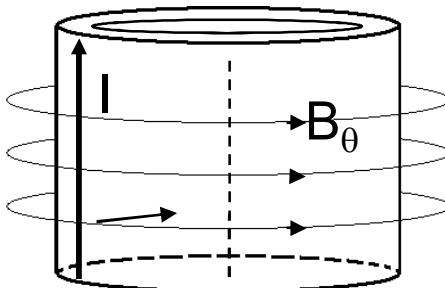
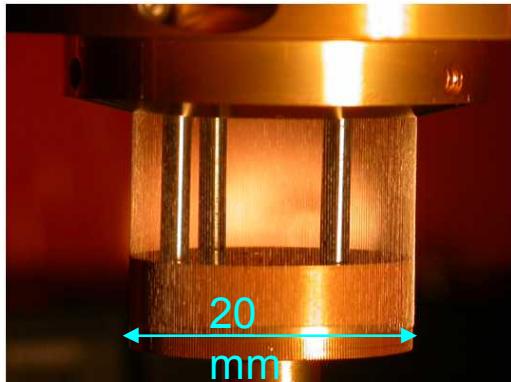
# Z pinches are susceptible to the Rayleigh-Taylor instability

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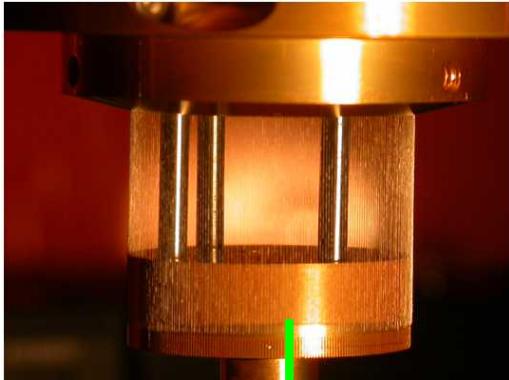


# Z pinches are susceptible to the Rayleigh-Taylor instability

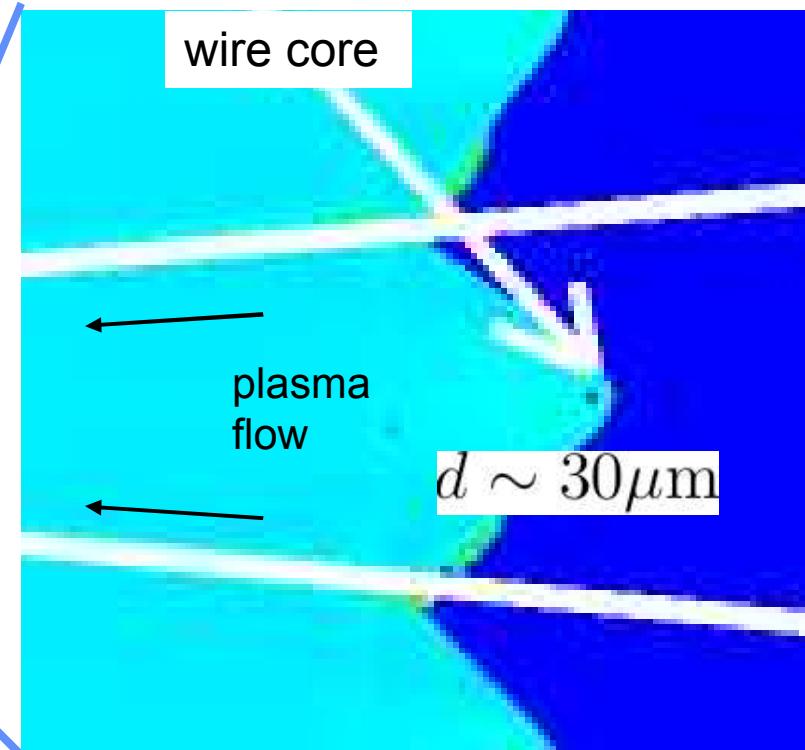
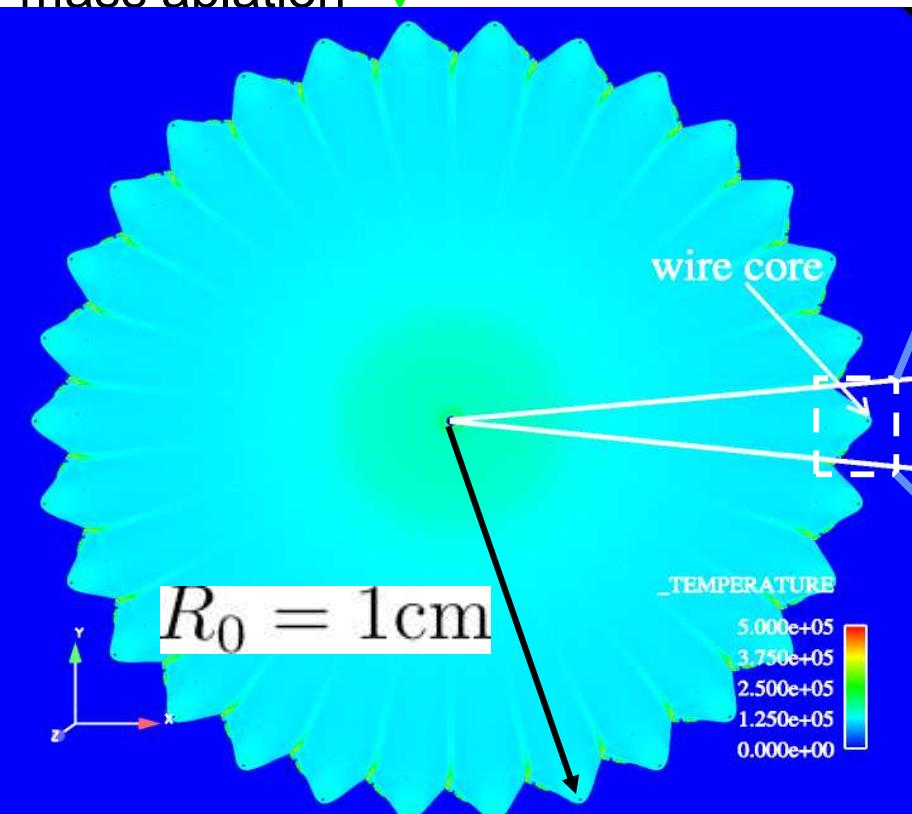
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# Wire arrays demonstrate mass ablation

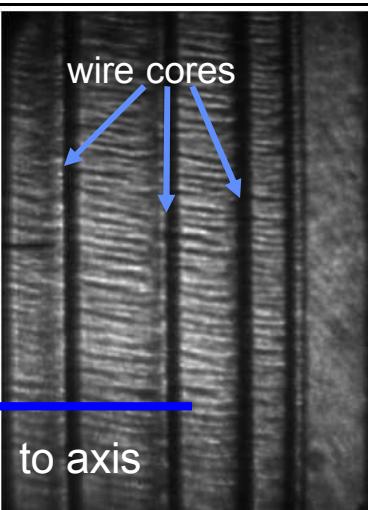
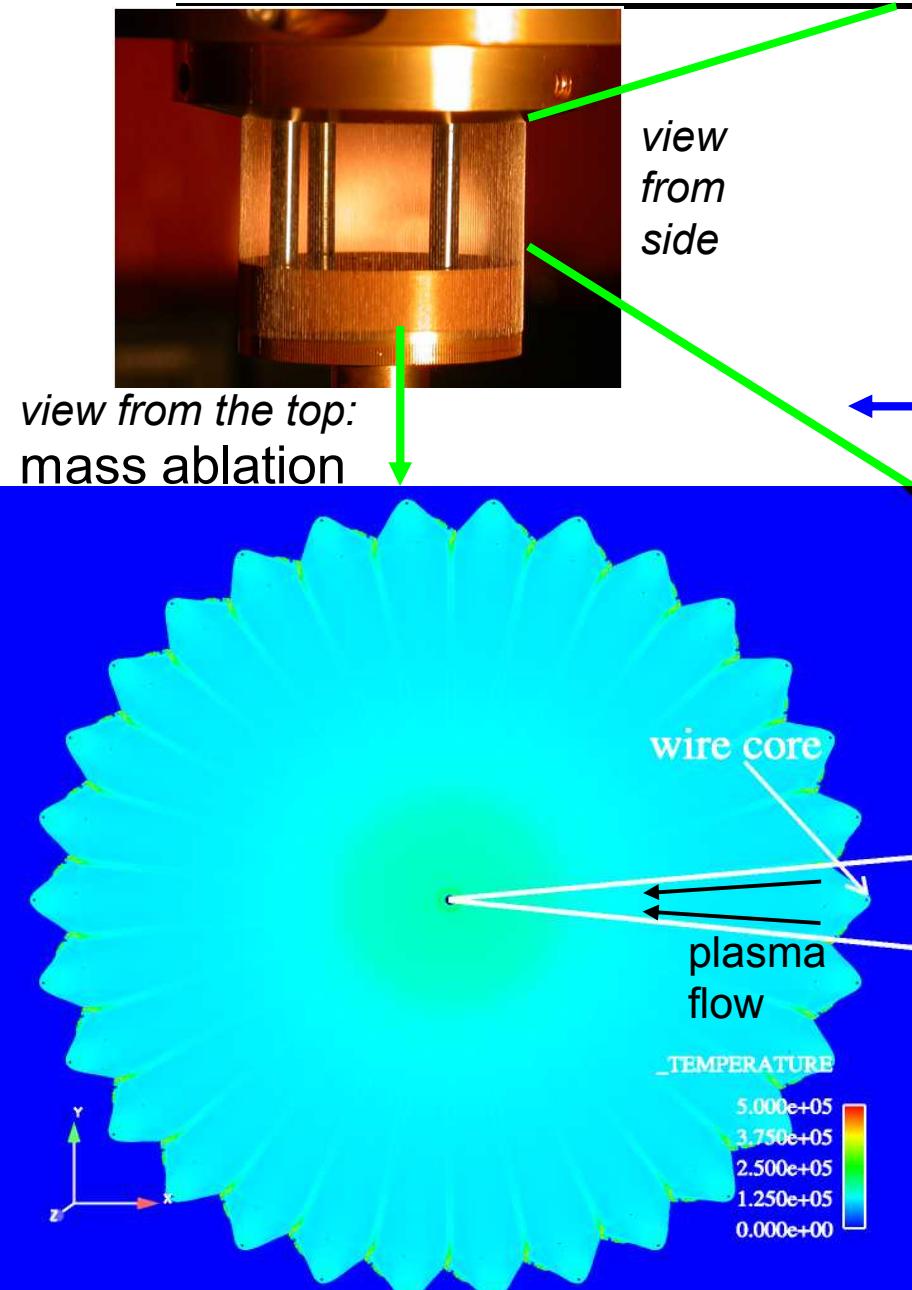


*view from the top:*  
mass ablation

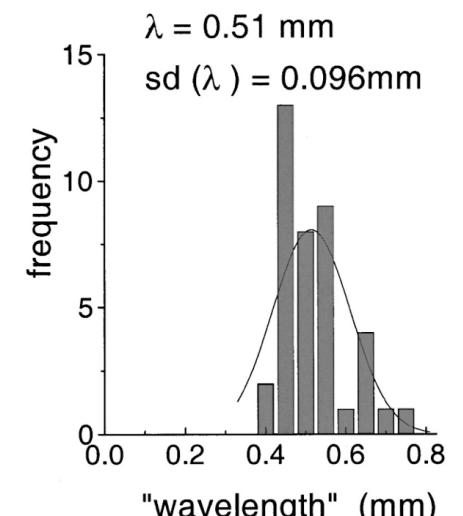


Disparity in scales makes simulation challenging

# mass ablation exhibits axial instability



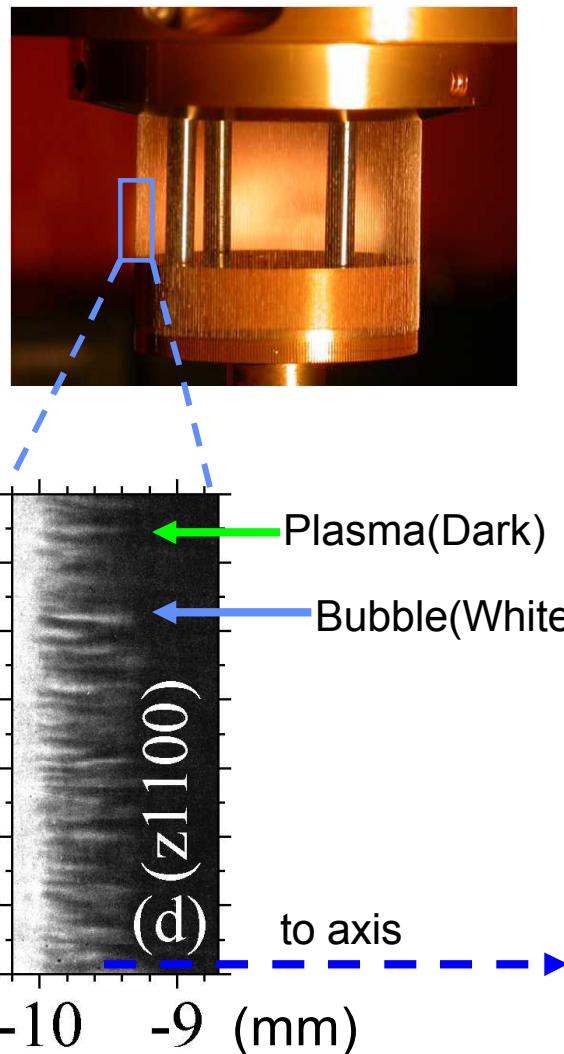
axial modulation  
of mass ablation  
(Laser shadowgraph  
courtesy D. Bliss)



S.V. Lebedev et al., Phys.  
Plasmas 8, 3734 (2001)

For more on axial instability, please see:  
J.P. Chittenden and C.J. Jennings, UO6.00002  
(Thurs)  
G.N. Hall et al., UO6.00008(Thurs)

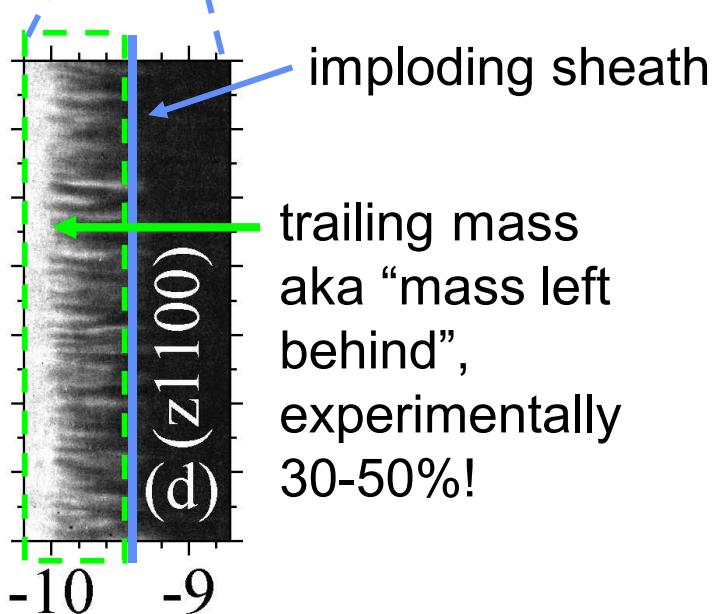
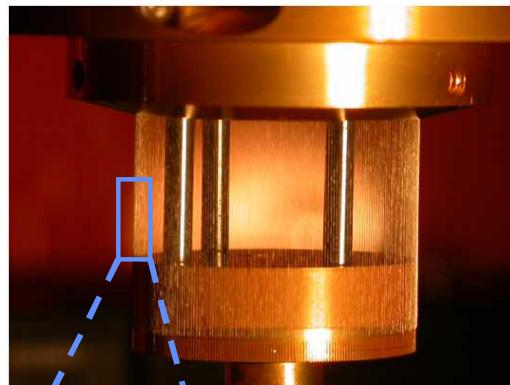
# axial instability leads to trailing mass



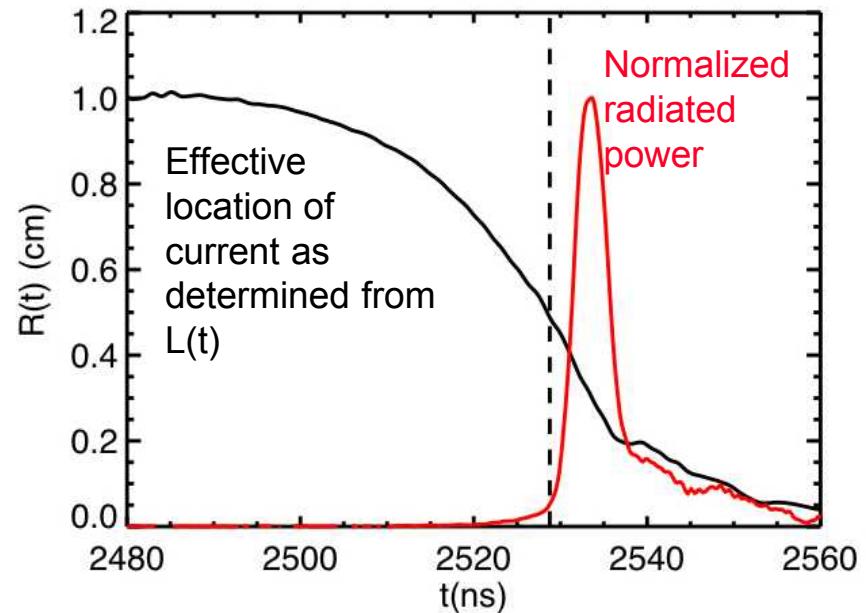
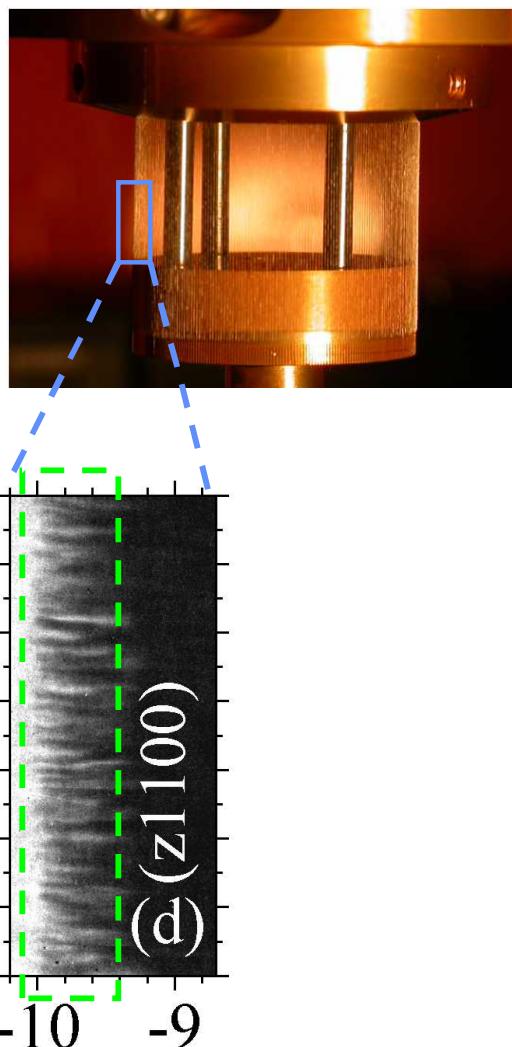
1865 keV radiograph, at time near start of implosion

# axial instability leads to trailing mass

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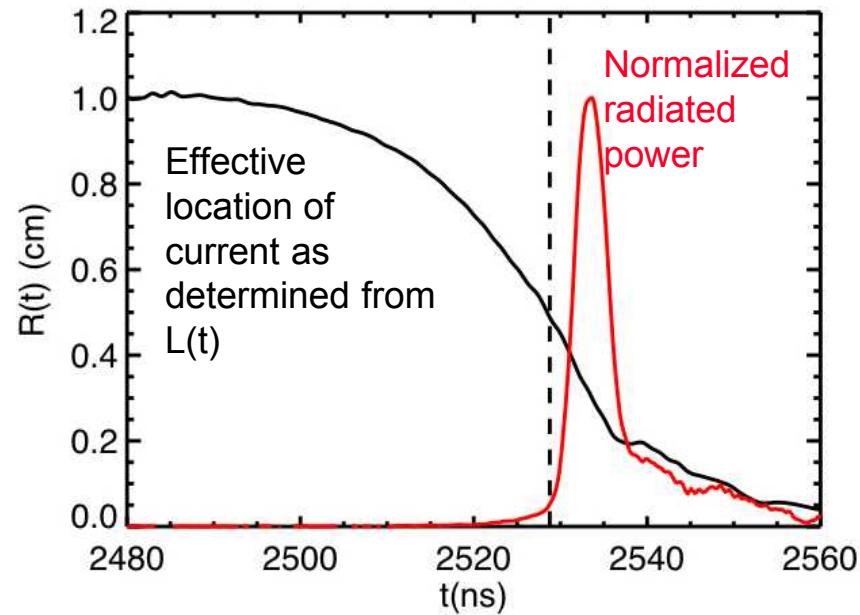
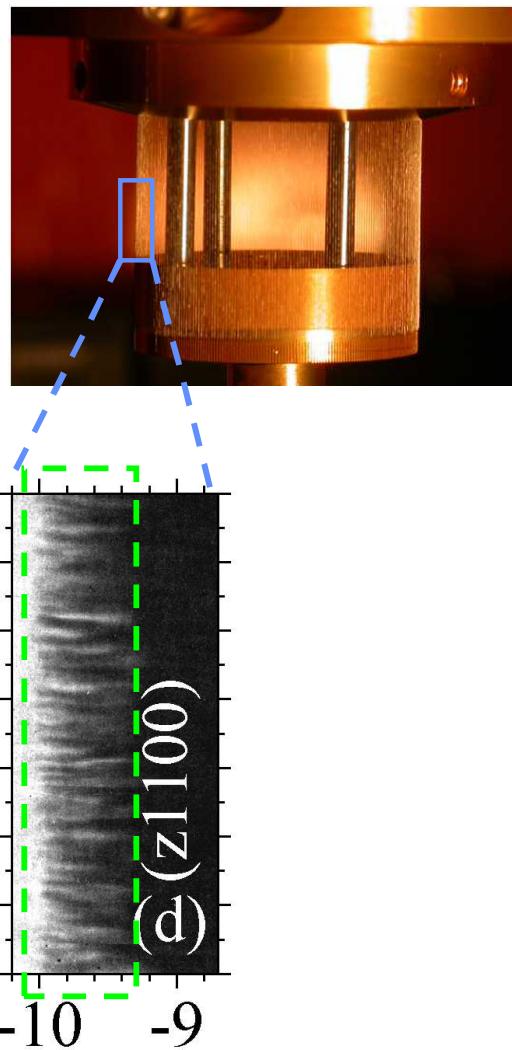
# trailing mass leads to trailing current



M.E. Cuneo et al., Phys. Rev. E 71, 046406 (2005)  
E.M. Waisman et al., Phys. Plasmas 11, 2009 (2004)

trailing mass prevents all mass from participating in implosion, provides current path preventing current from compressing on axis

# What physics drives trailing mass/current?

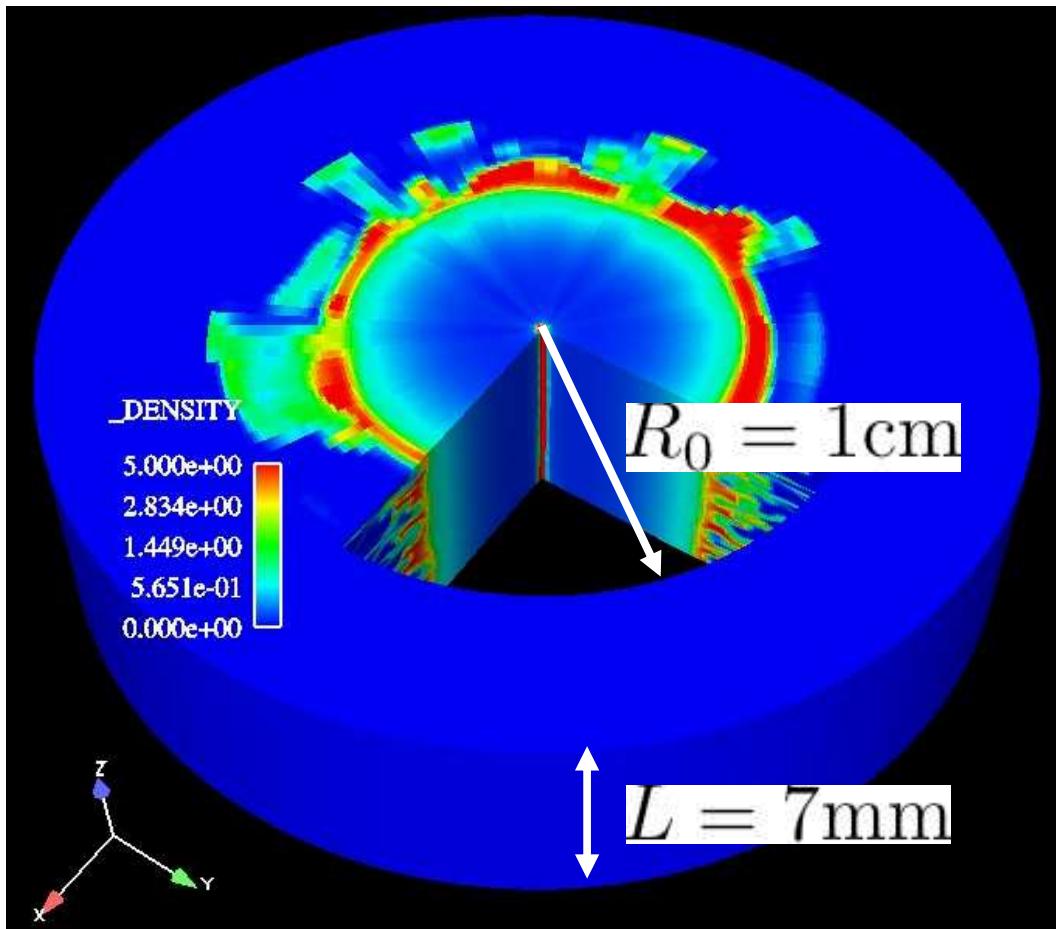


We'd like to address the following:

1. Is the effect of trailing mass entirely negative?
2. What drives the bubble growth on the imploding sheath? Is it just magneto Rayleigh-Taylor (MRT)?
3. What is the role of azimuthal correlation?

# Address these issues via 3D simulation

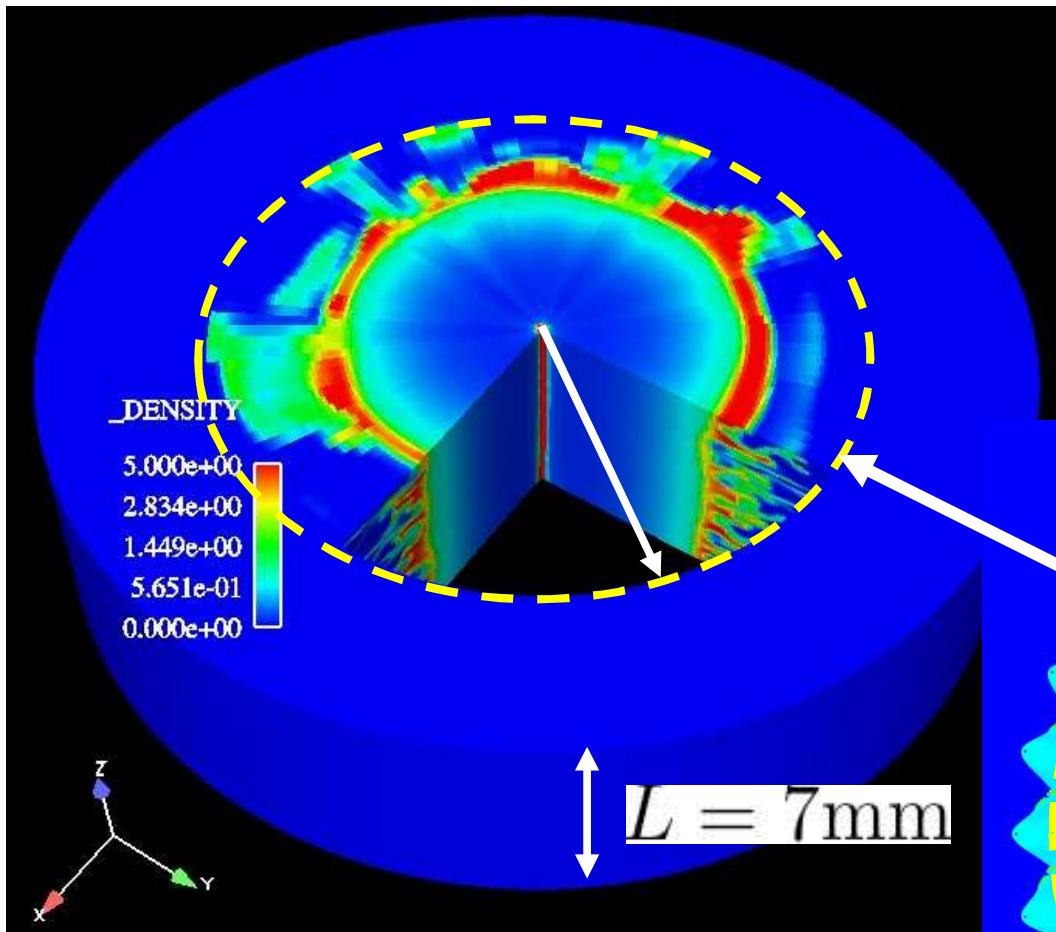
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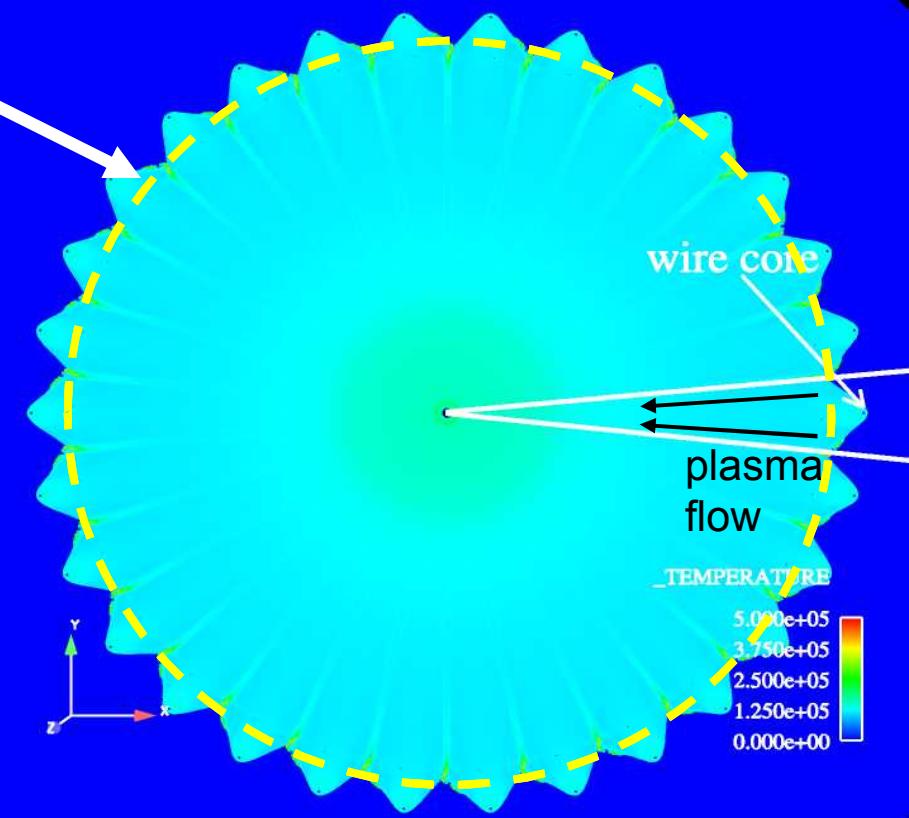
rad-MHD code:  
ALEGRA

Run with Voltage Drive

# Model ablation/implosion via mass injection



rad-MHD code:  
ALEGRA



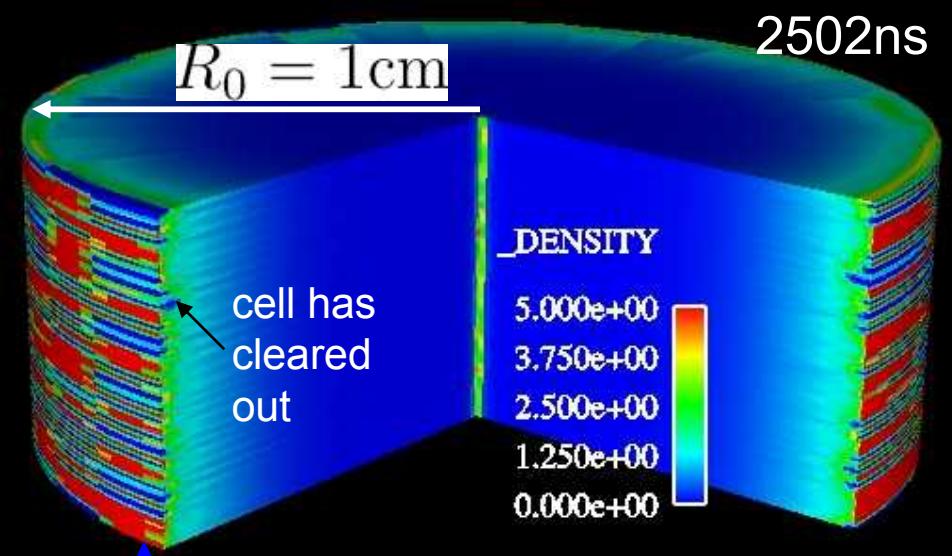
This idea has been used before:

J.P. Chittenden, et al., Phys. Plasmas 11, 1118 (2004)

P.V. Sasorov, in V.V. Aleksandrov et al., Plasma Phys. Reports, 27, 89 (2001)

# mass injection parameters constrained by experiment

$dr \sim 100 \text{ }\mu\text{m}$ ,  $dz \sim 60 \text{ }\mu\text{m}$ ,  $N\phi = 120$



Each cell has mass  $m$  and ablates according to

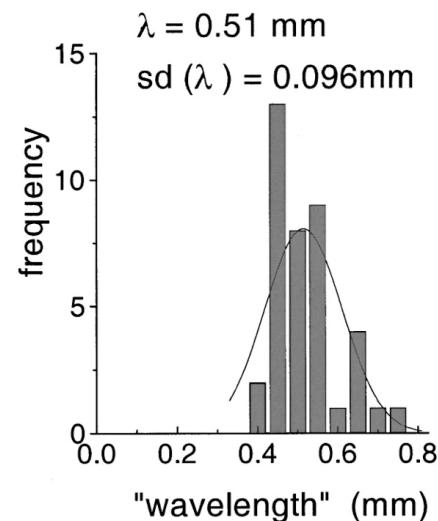
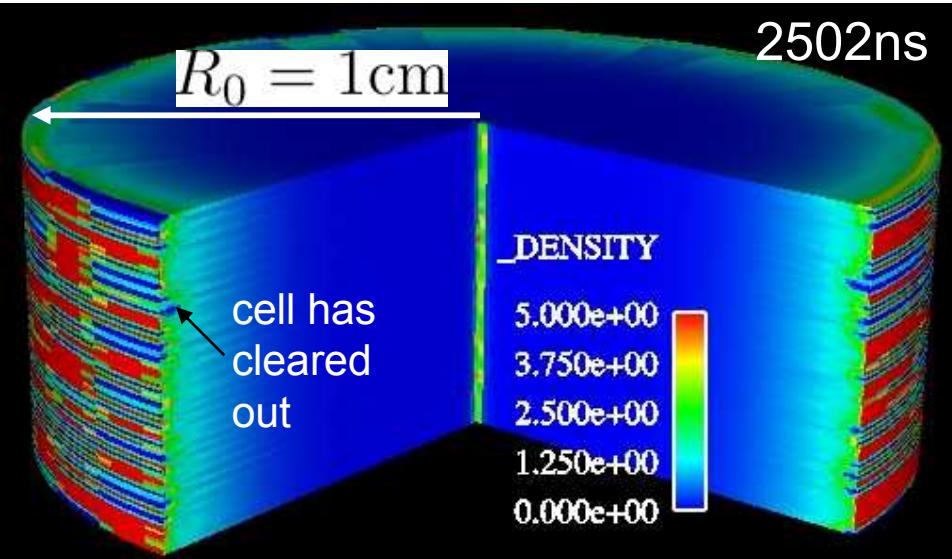
$$\dot{m} = \dot{m}_0 (I/I_0)^\alpha$$

determines when cell finishes ablating.  
Determines when array starts to implode.

currently,\*  
 $\alpha = 1.4$ ,  
determines distribution of prefill plasma.

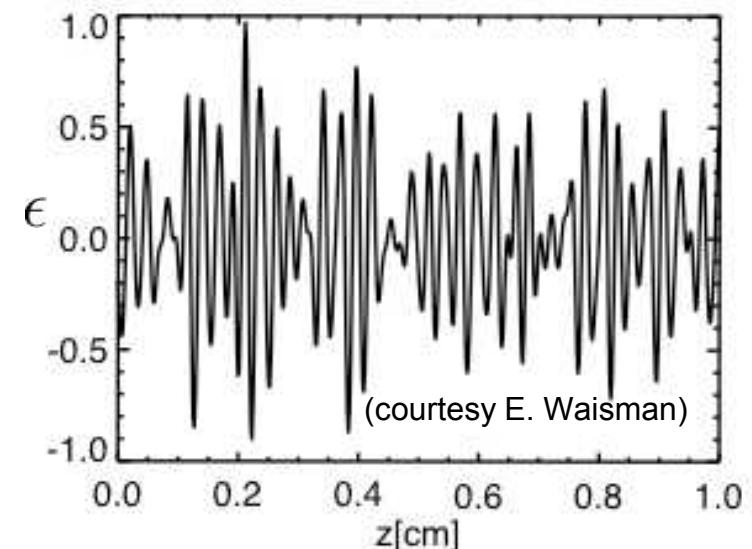
# mass injection parameters constrained by experiment

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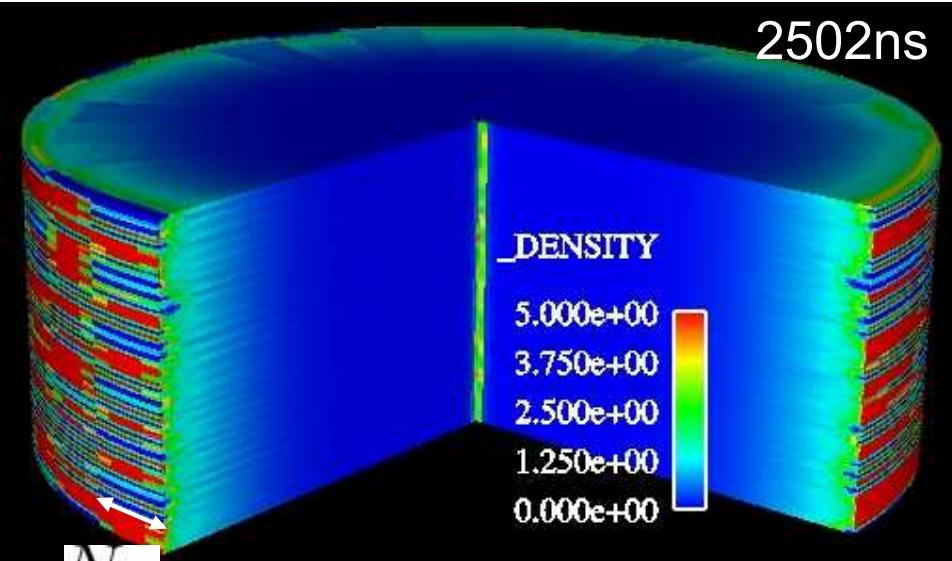
$$\dot{m} = \dot{m}_0 (I/I_0)^\alpha (1 + \epsilon(z))$$

spectral content determined by experimental histogram. Amplitude constrained by contrast ratio between streams.



# Number of wires azimuthally correlated is important

dr~100 um, dz~60 um,  $N_\phi=120$



We only consider the case where there are sufficient wires that the plasma coronas are touching azimuthally (i.e. no azimuthal gaps!)

$$C = \frac{N_C}{N_\phi} \times 100$$

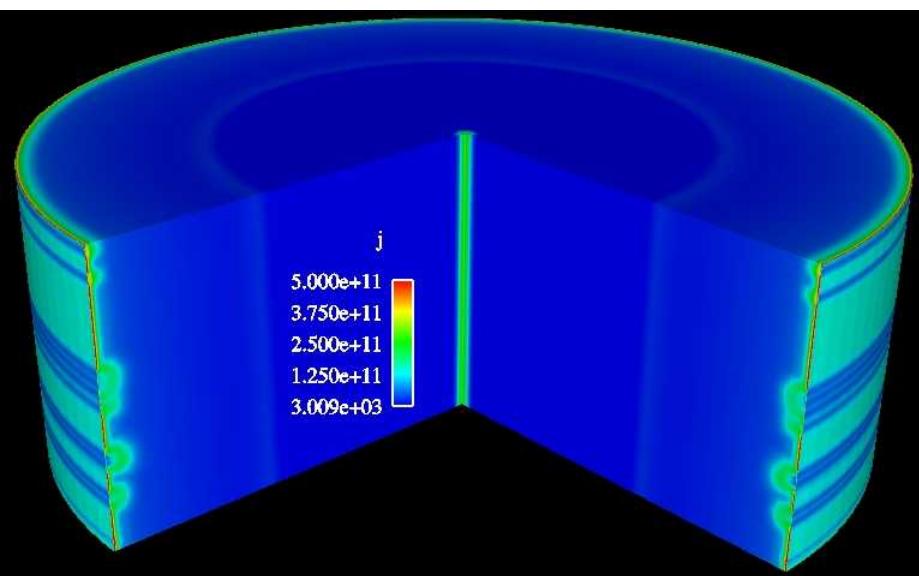
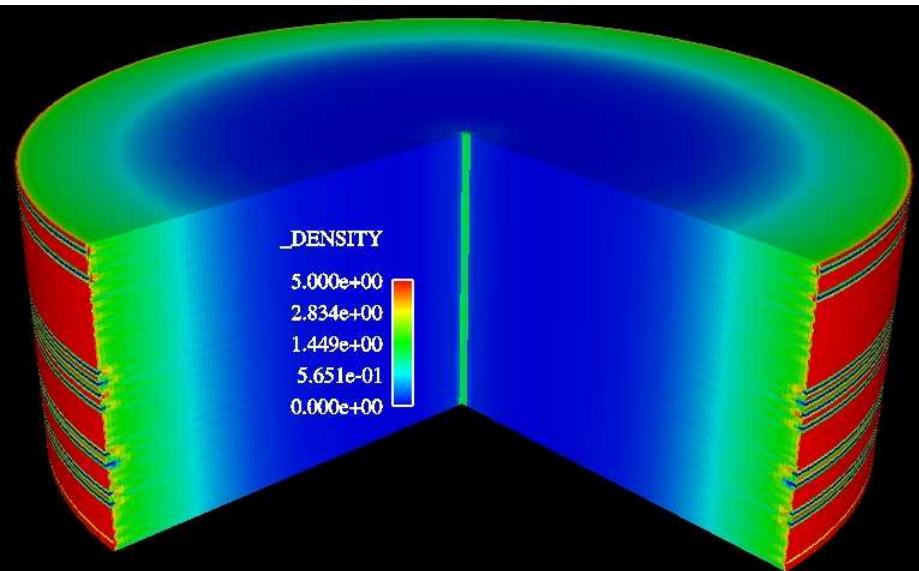
percentage of azimuthal correlation

for more on mass injection scheme, please see:

R.W. Lemke et al., PP8.00039(Wed)

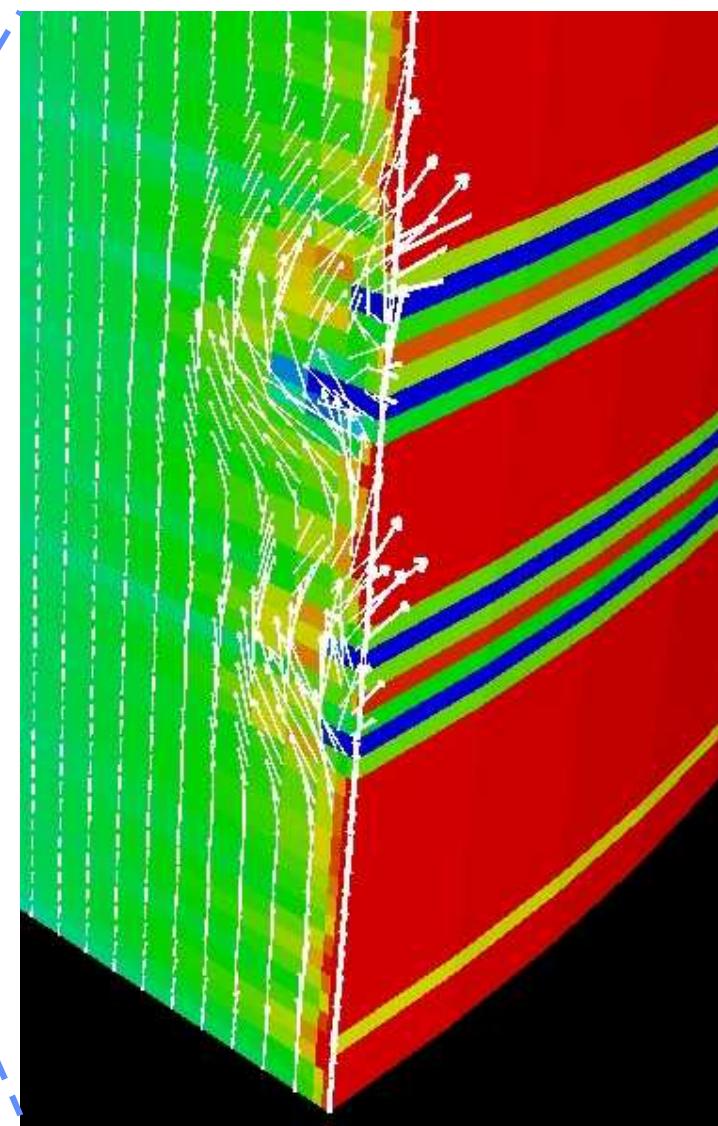
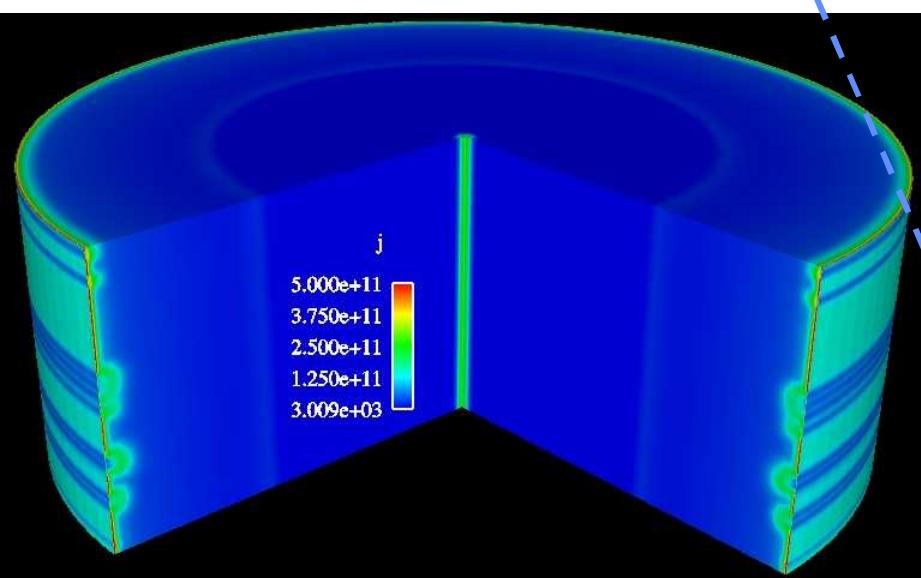
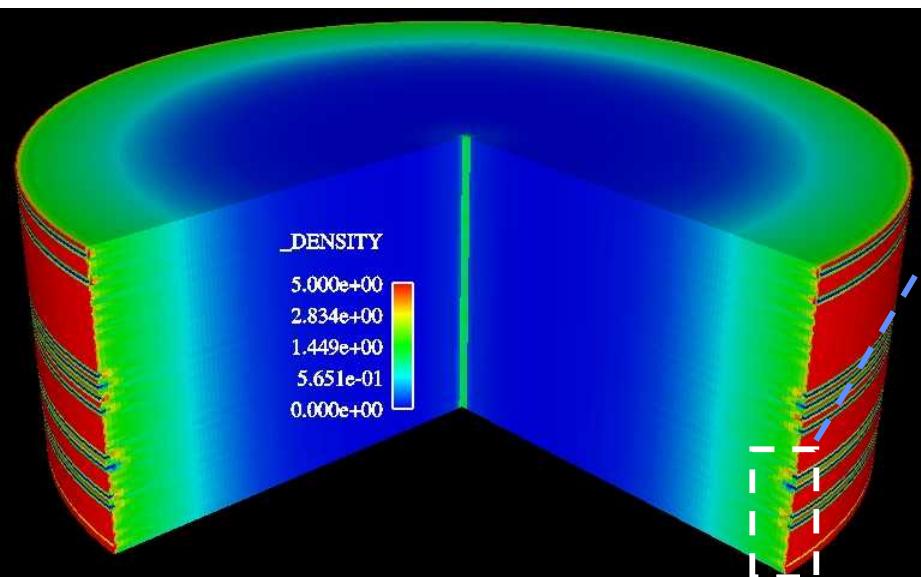
# start of implosion in C=100% case

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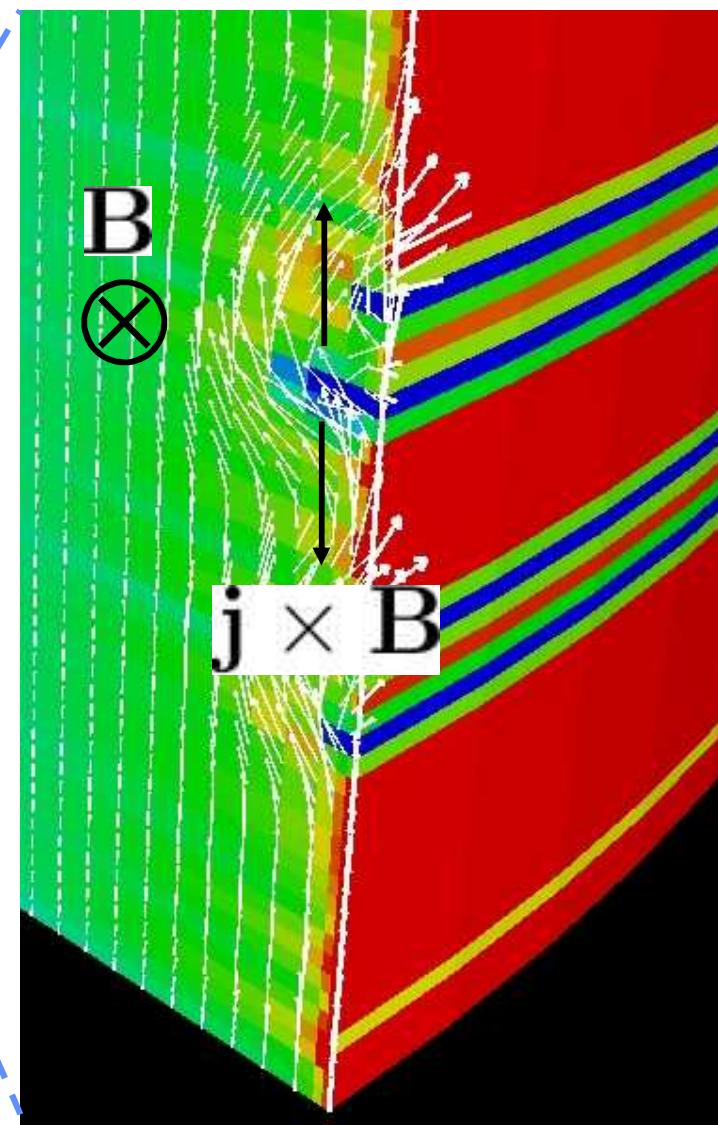
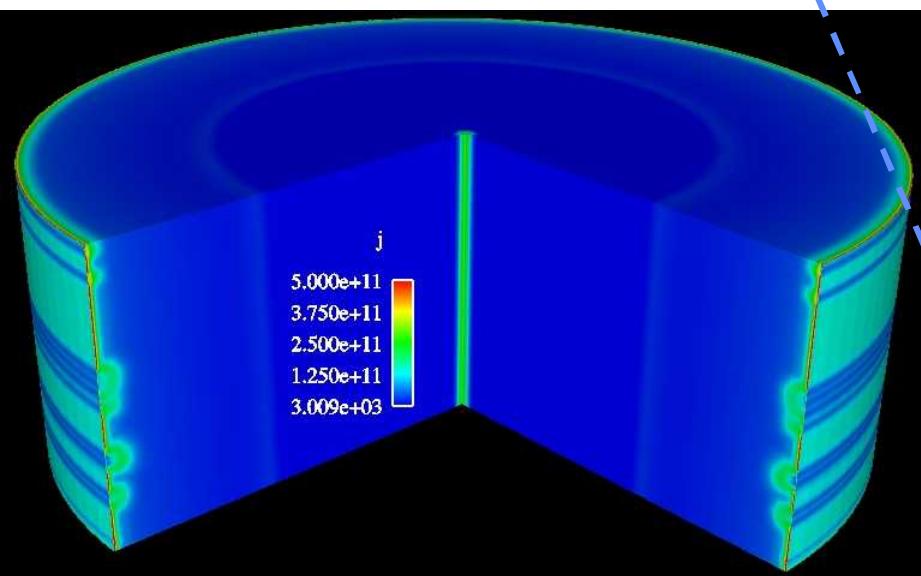
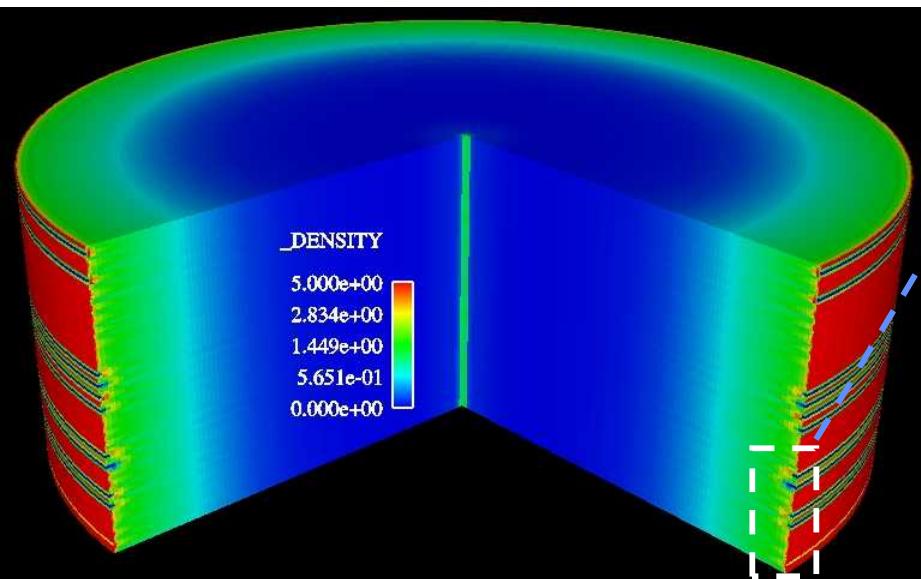
t=2500 ns

# early bubble formation determined by $j \times B$ forces



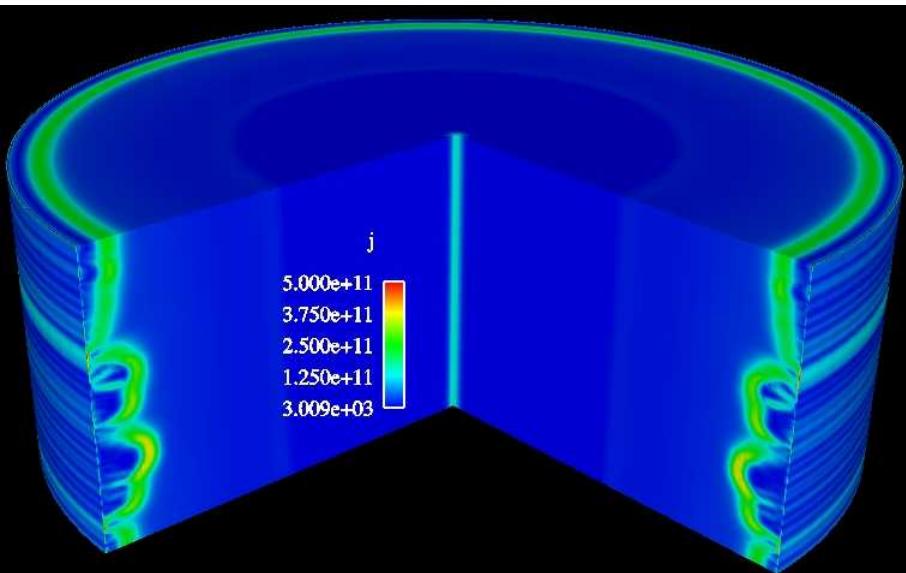
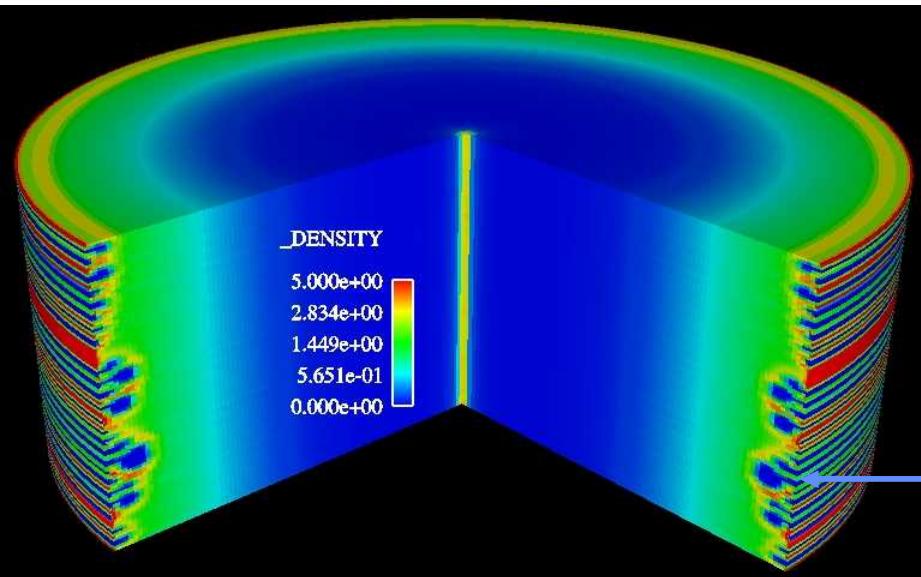
$t = 2500$  ns

# early bubble formation determined by $j \times B$ forces



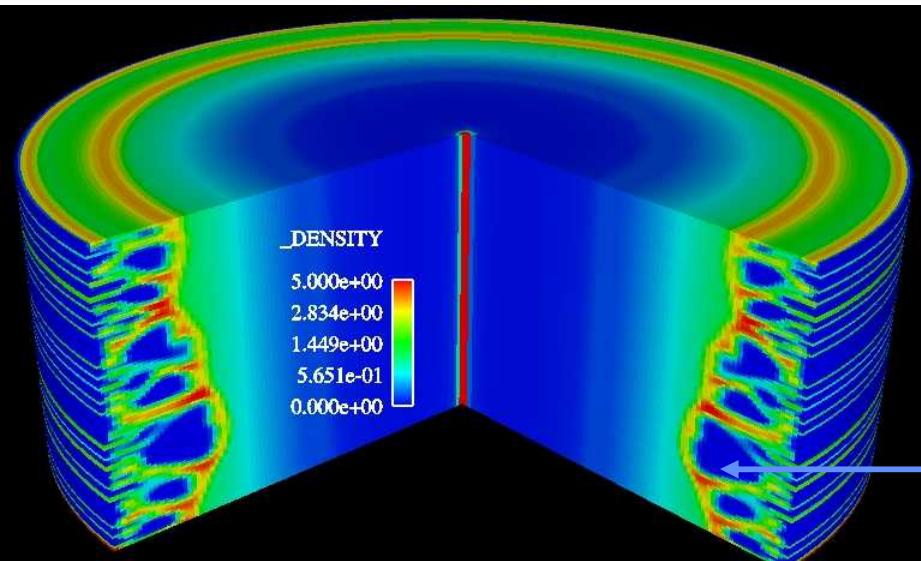
$t=2500$  ns

# bubble formation in C=100%

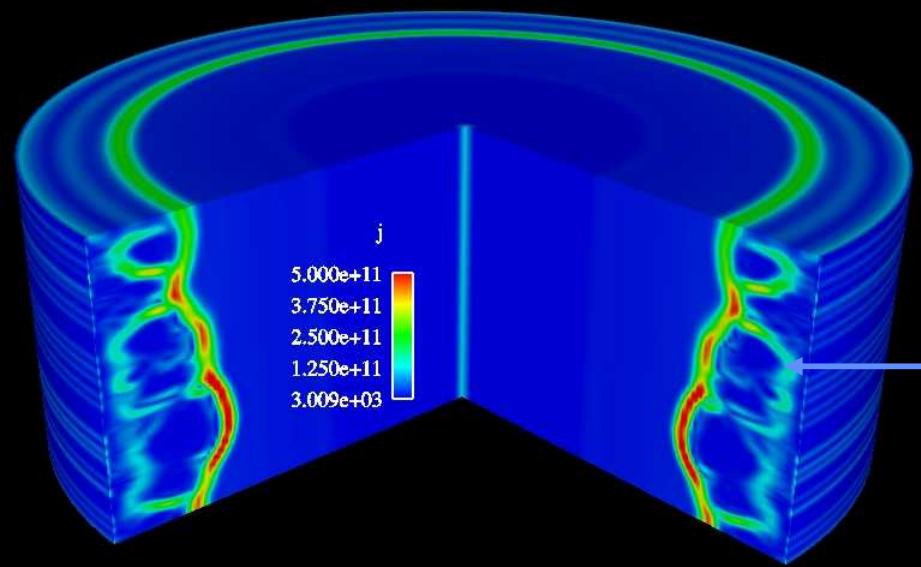


t=2504 ns

# C=100% results in large bubble growth

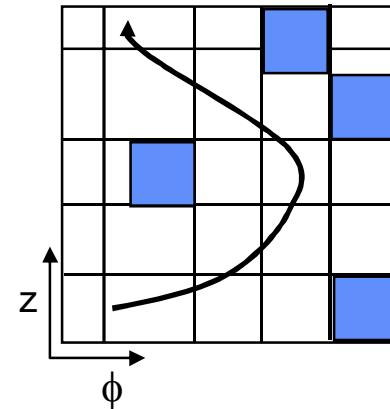
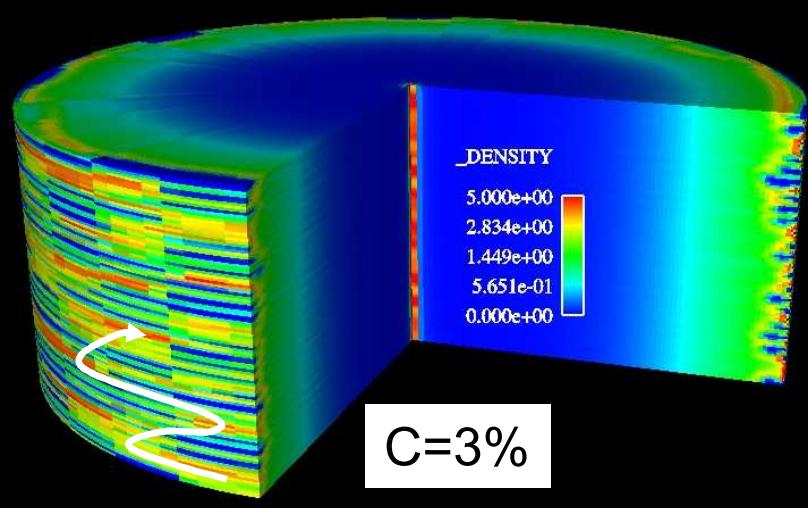


The bubble which formed first will grow the biggest

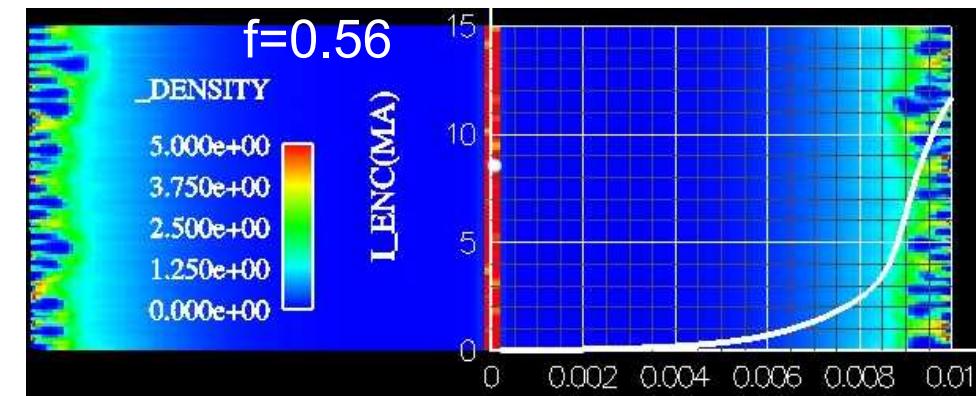
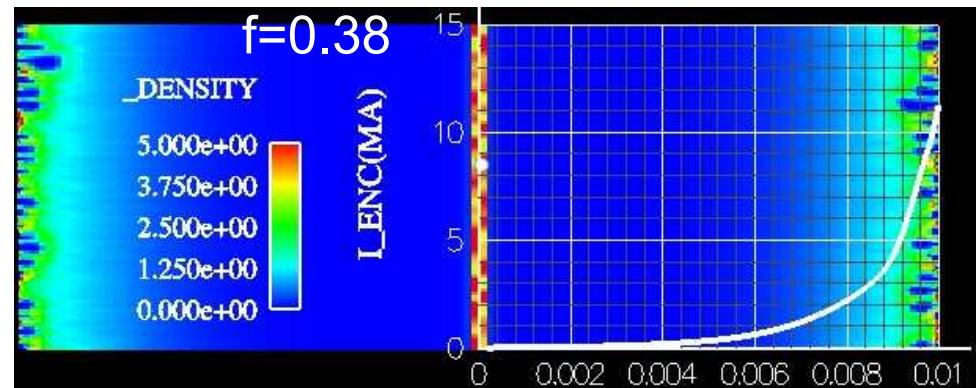
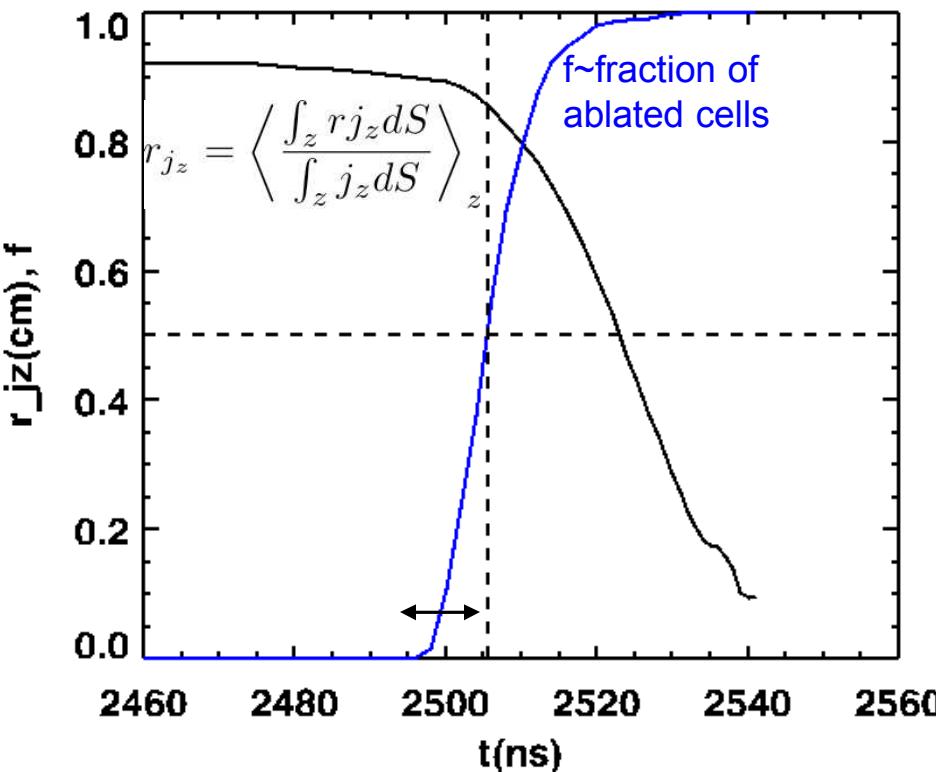


eventually trailing streams of mass reconnect, but the bubbles are already quite large

# In 3D, trigger for implosion tied to fraction of cells ablated



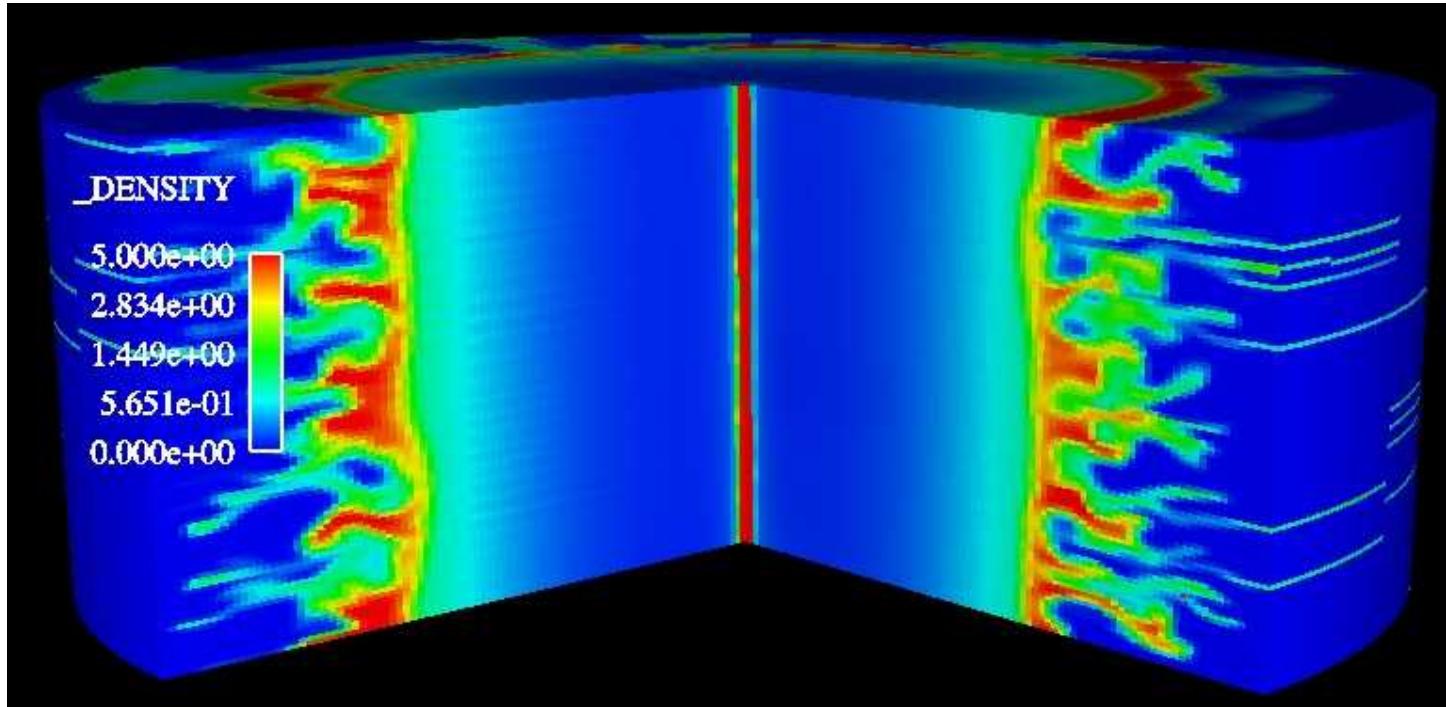
M.B. Isichenko, Rev. Mod. Phys. 64, 961 (1992)  
S. Kirkpatrick, Rev. Mod. Phys. 45, 574 (1973)



# In 3D, current can travel azimuthally, “self-regulating” bubble growth

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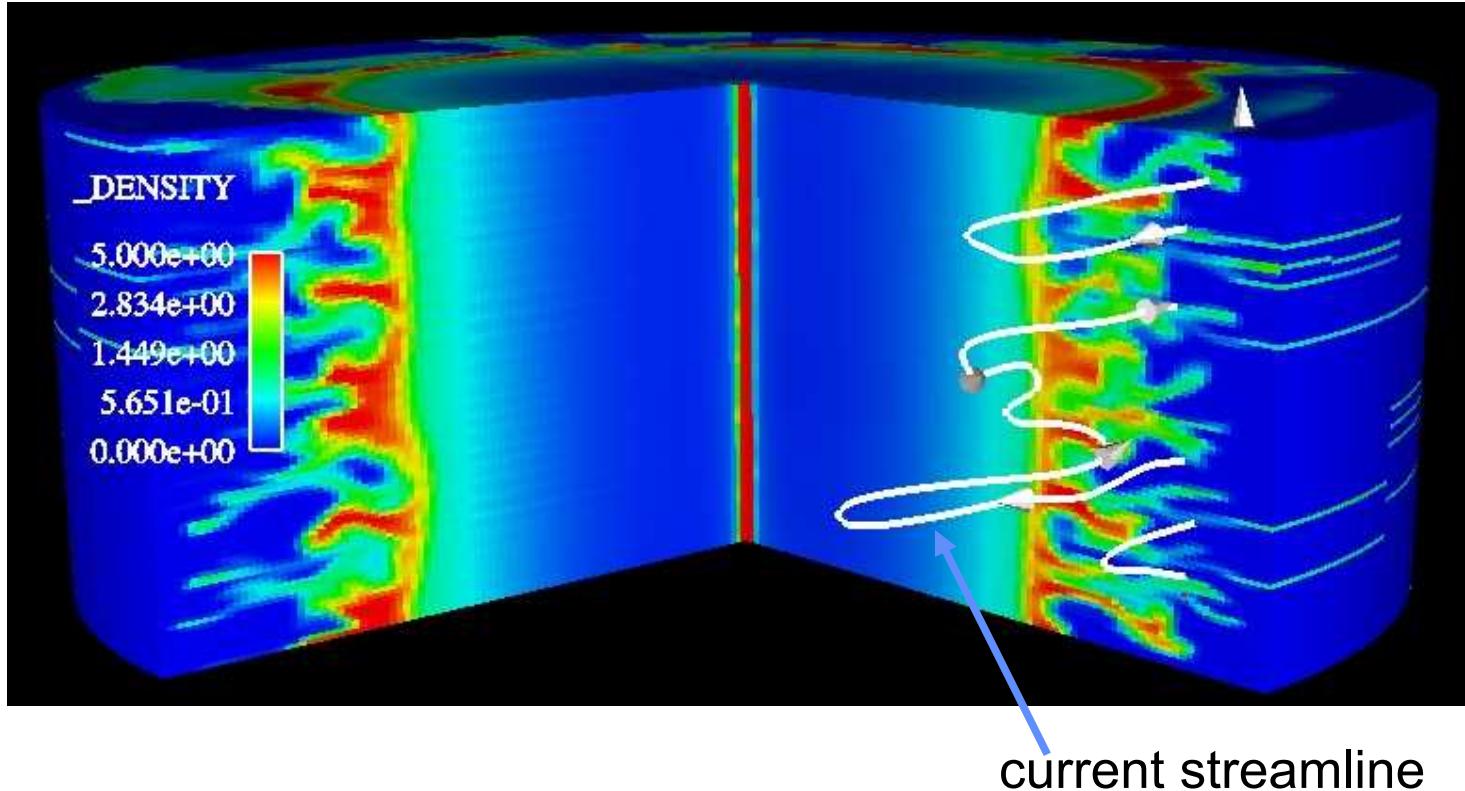
C=3%, t=2518 ns



# In 3D, current can travel azimuthally, “self-regulating” bubble growth

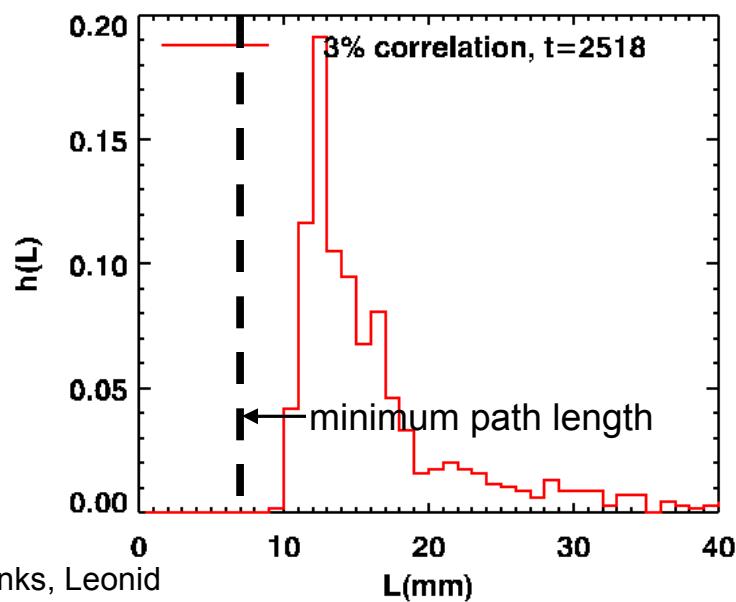
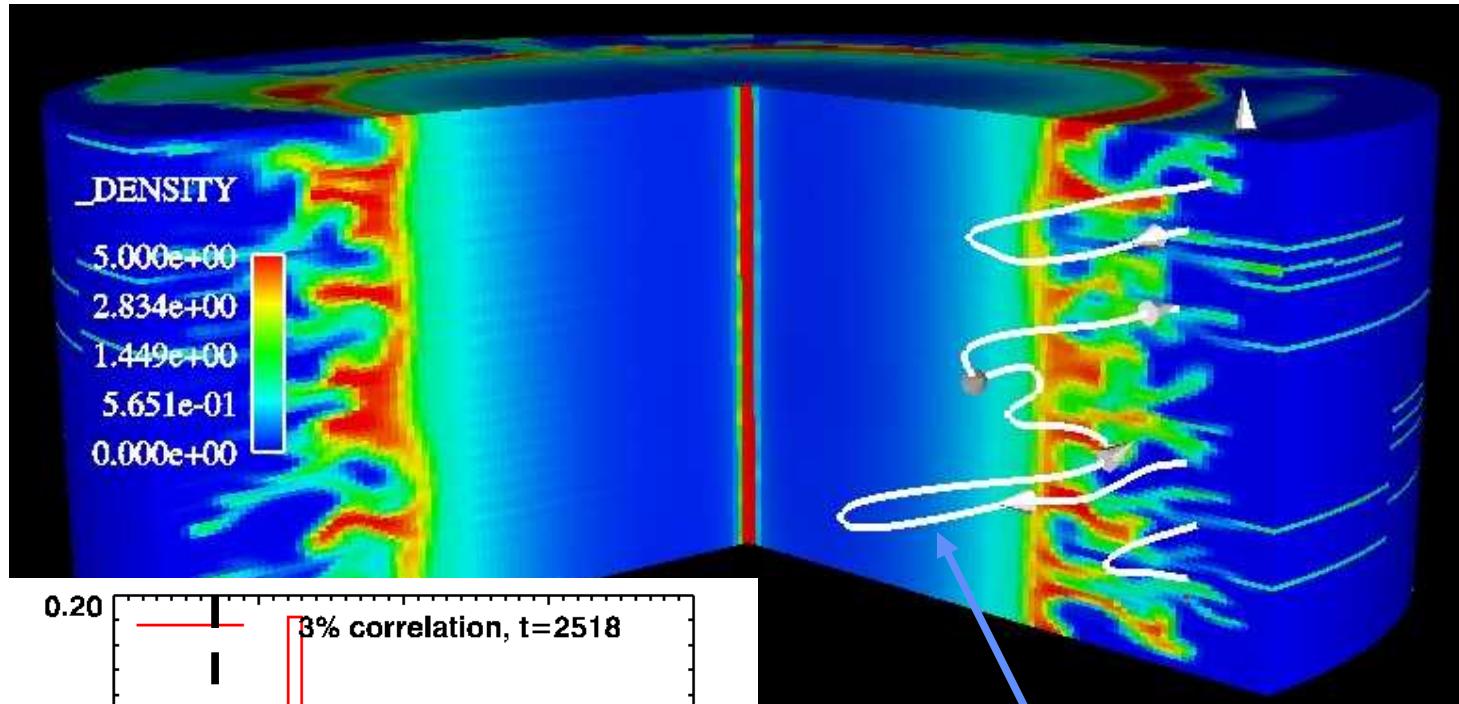
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C=3%, t=2518 ns



# Histogram of path lengths through trailing mass

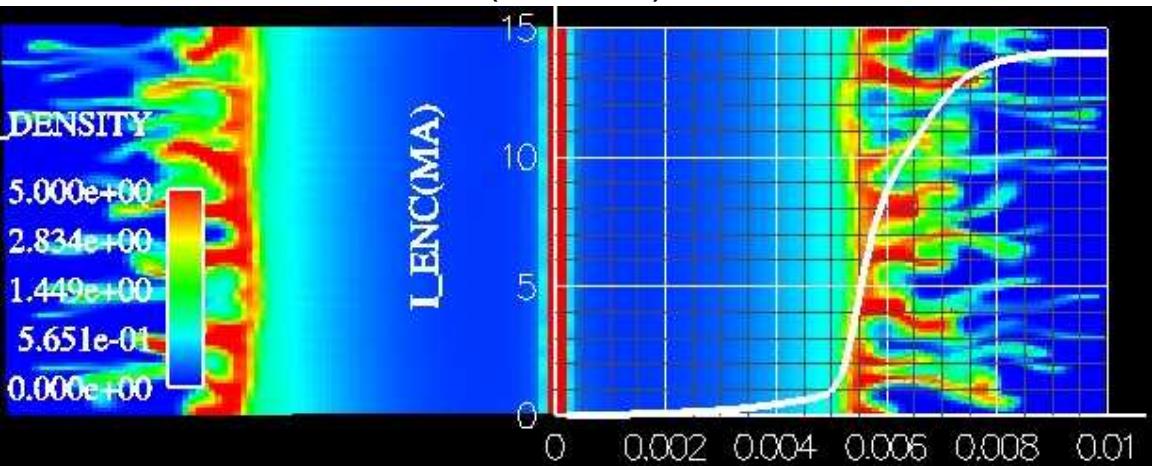
3% azimuthal correlation,  $t=2518$  ns



current streamline

# bubble growth is reduced by 3D effects

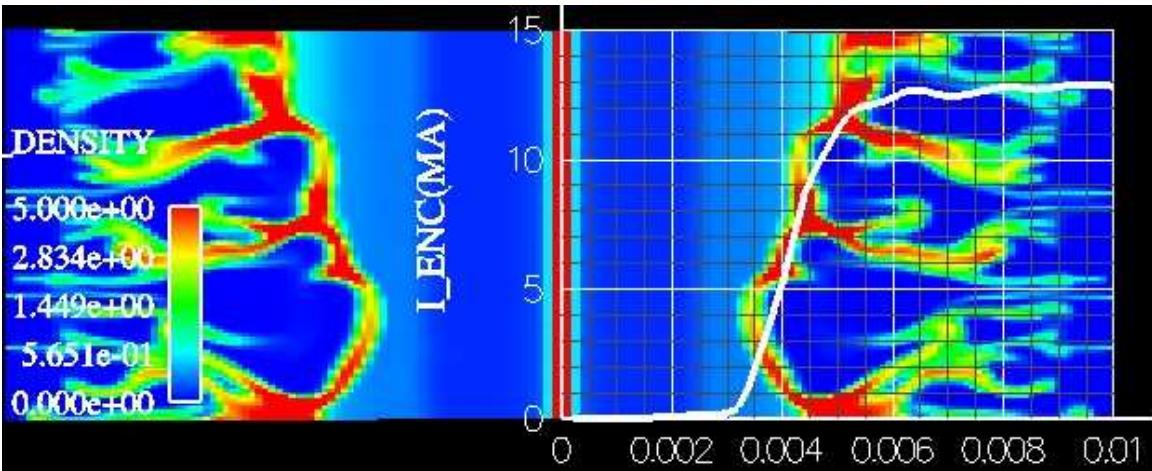
C=3% (2520 ns)



In 3% correlated problem, bubble growth is reduced because current can flow azimuthally.

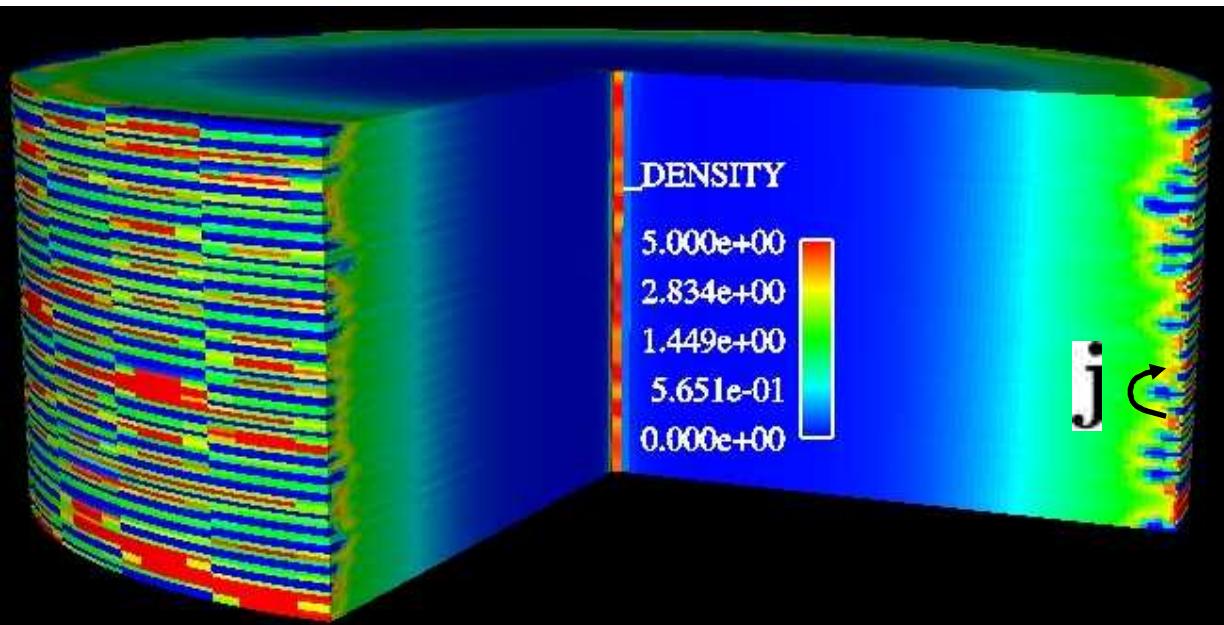
Surprisingly, in the presence of the axial instability, the 3D case is more shell-like than a 2D simulation!

C=100% (2520 ns)



# In 3D, trailing mass can fill in bubbles

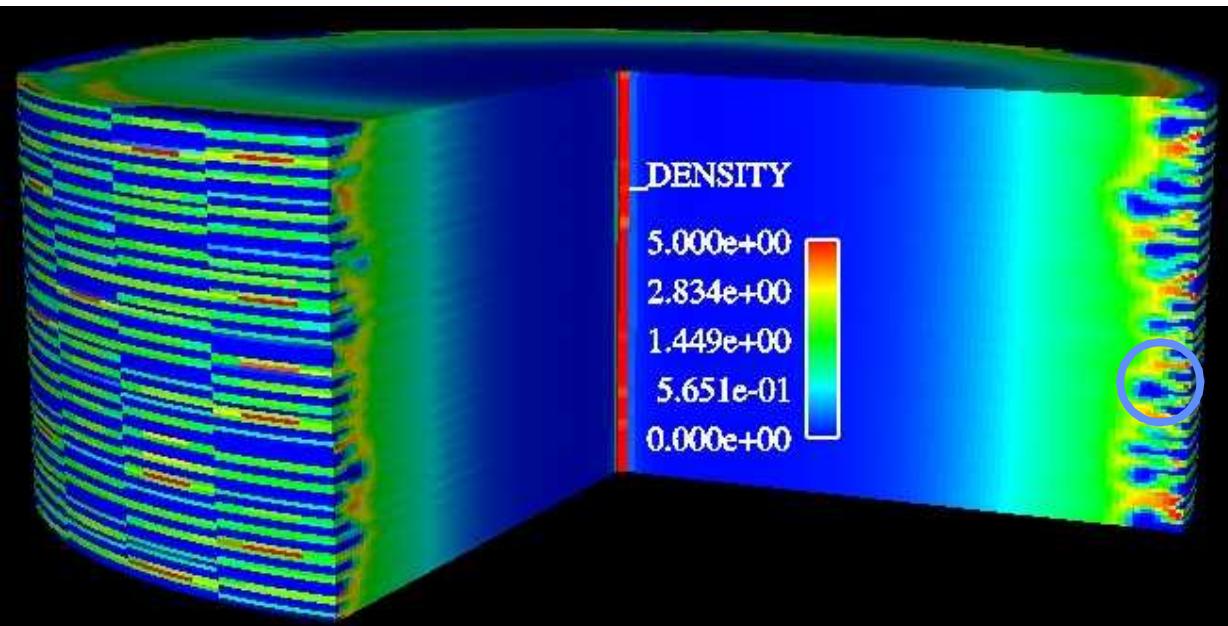
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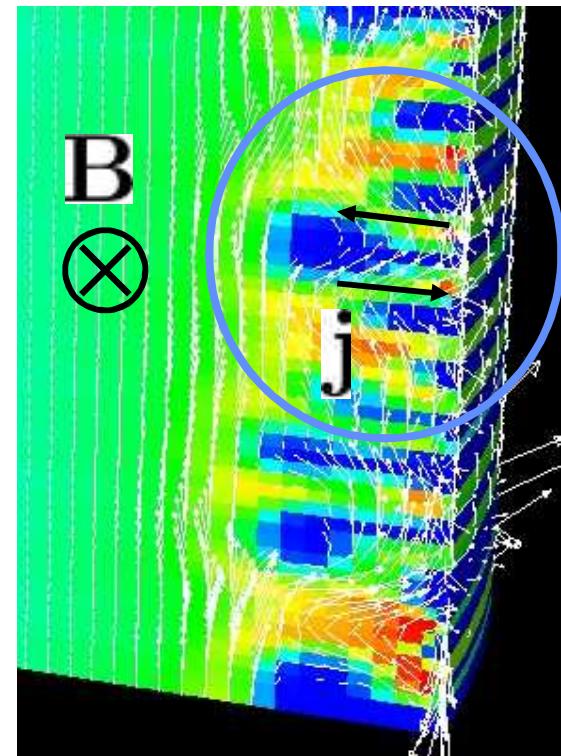
C=3%, t=2504

Initially, current bends around the bubble in such a way as to blow it up, just as in 2D

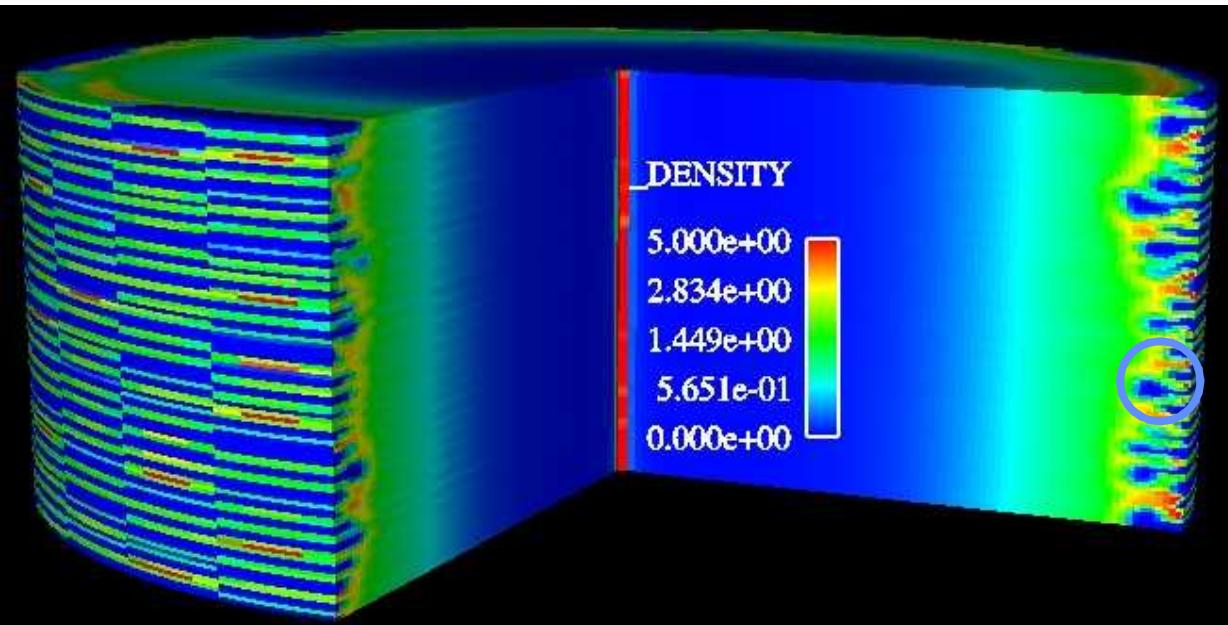
# In 3D, trailing mass can fill in bubbles



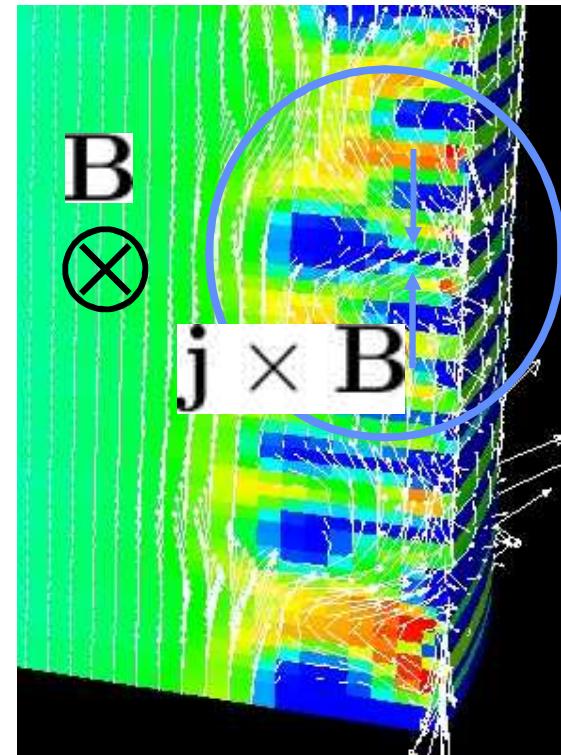
$t=2506$



# In 3D, trailing mass can fill in bubbles

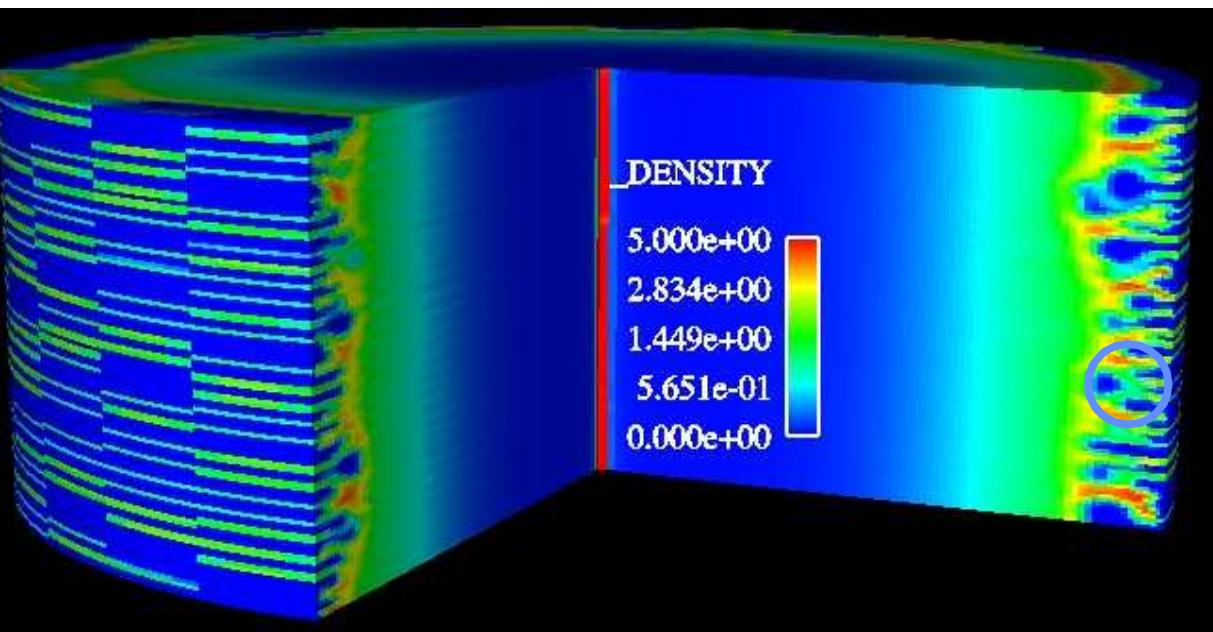


$t=2506$



# In 3D, trailing mass can fill in bubbles

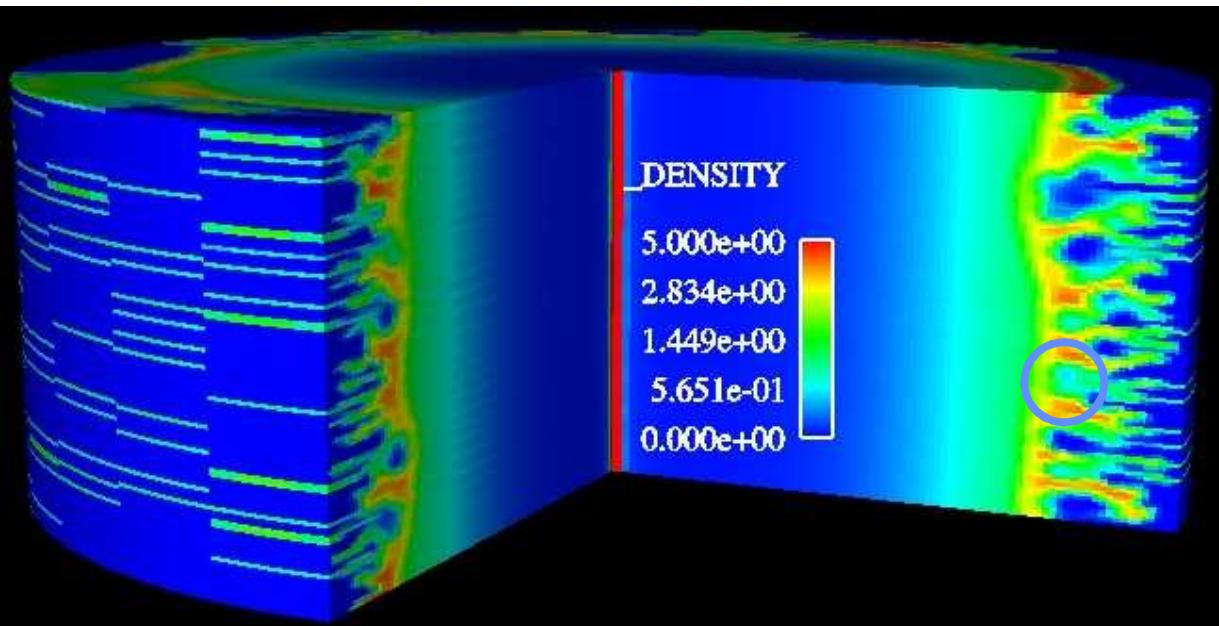
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$t=2508$

# In 3D, trailing mass can fill in bubbles

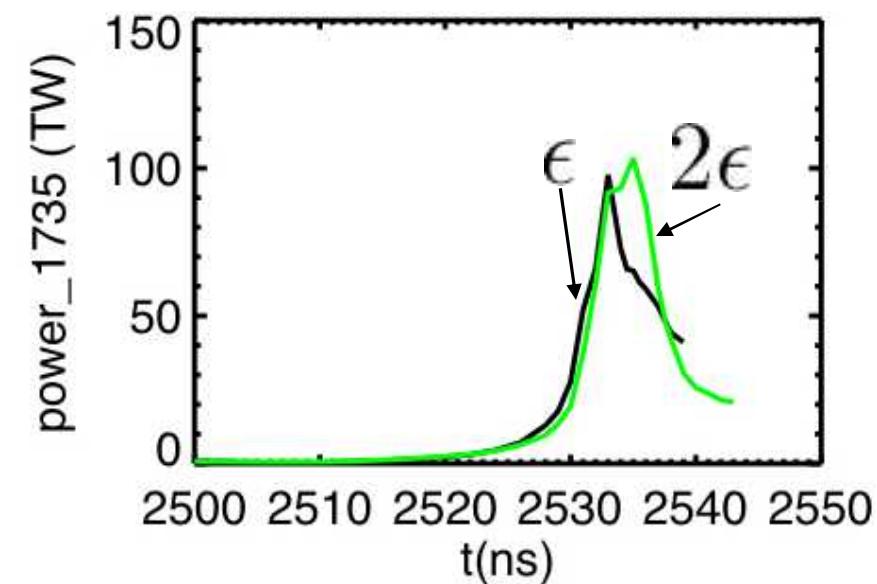
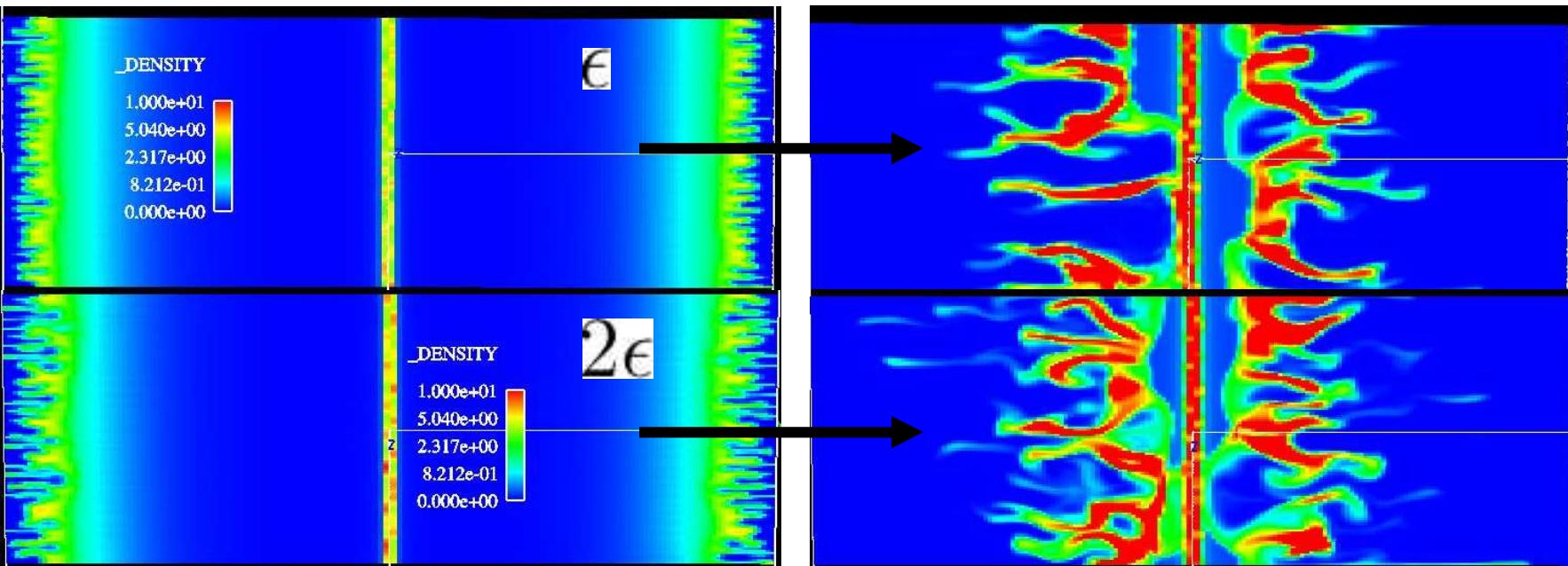
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$t=2512$

The bubble has been filled in

# In 3D, bubble growth is not determined solely by magneto Rayleigh-Taylor (MRT)

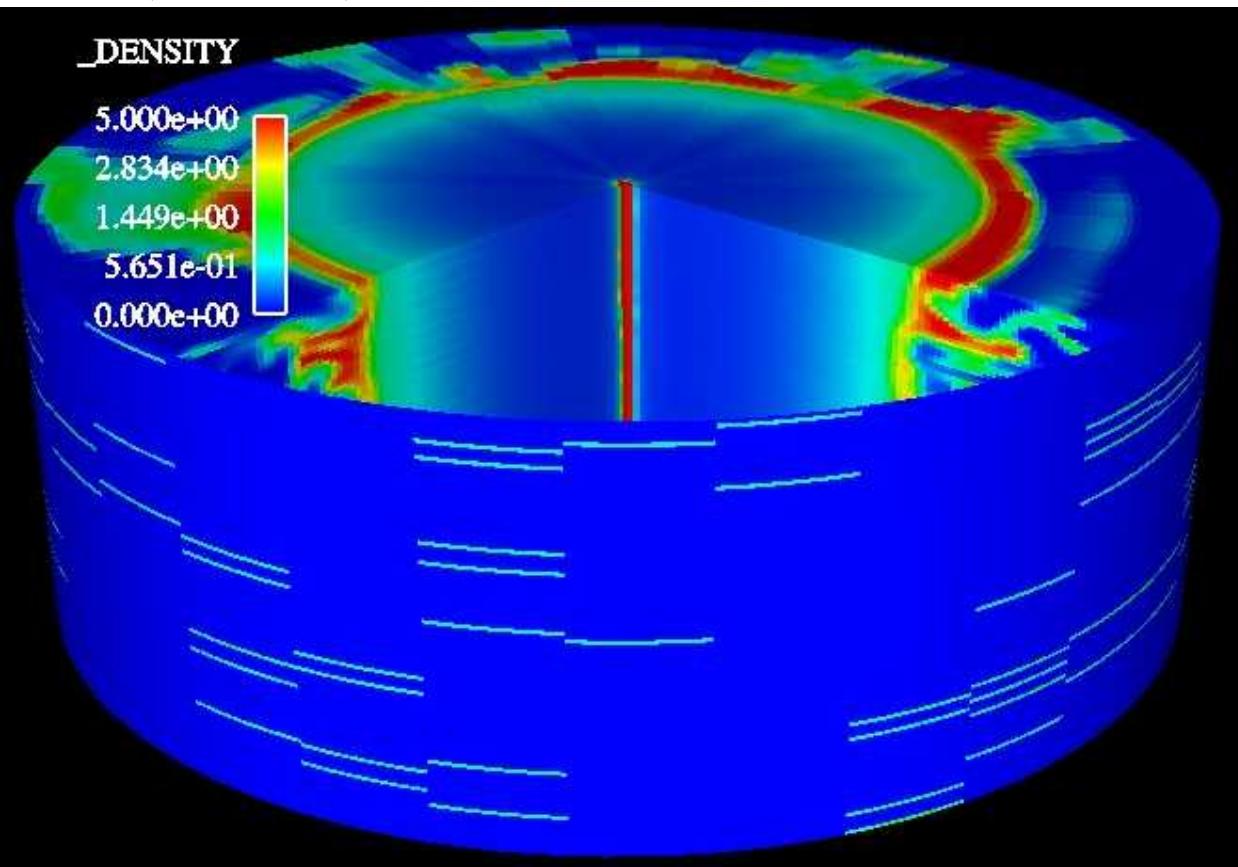


In conventional MRT, stronger perturbation  $\epsilon$  leads to a more deformed shell.

In 3D, the trailing mass can have a “healing” effect on bubble growth, which is determined by both MRT and  $j \times B$  forces

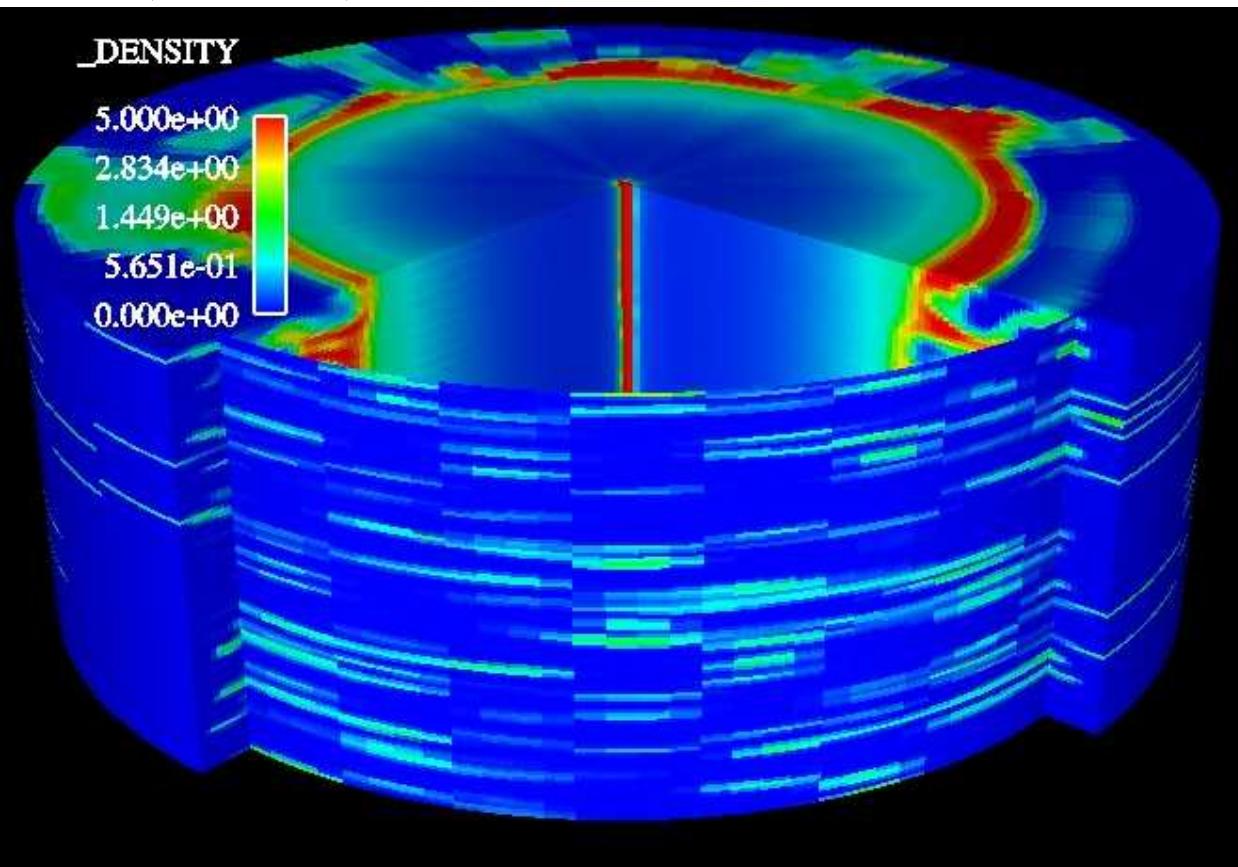
# trailing mass evolves towards force-free structure

C=3%,  $t=2518$ ,  $r=1$  cm



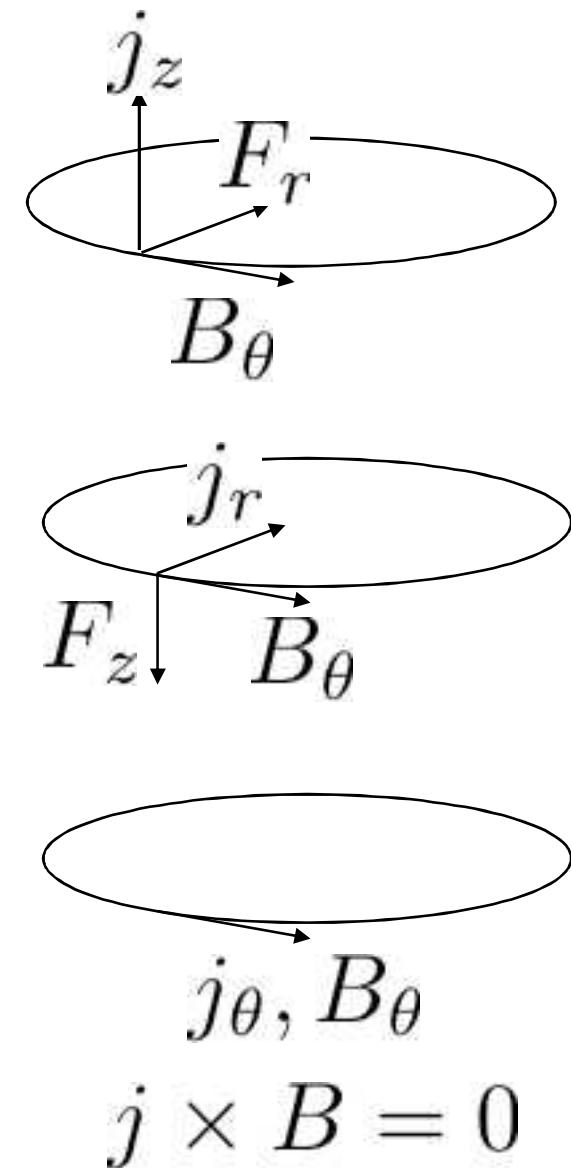
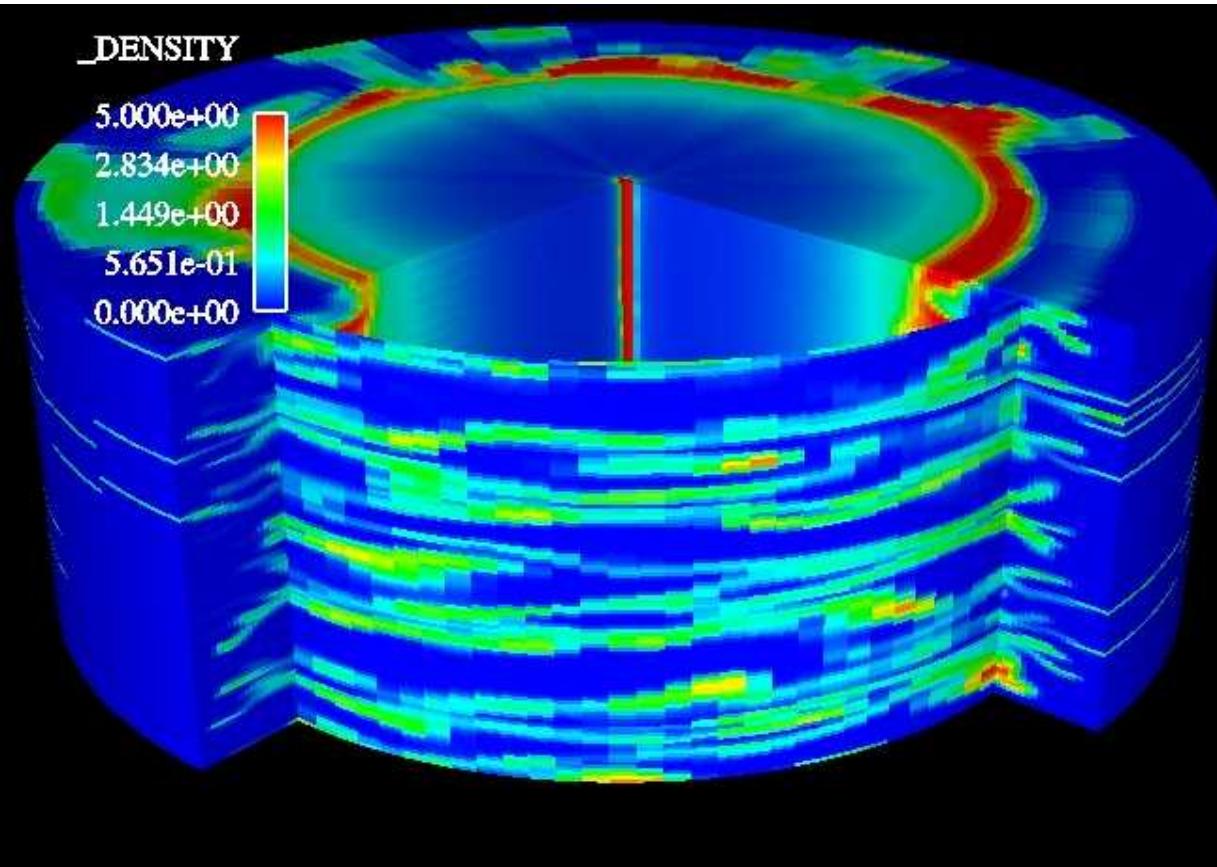
# trailing mass evolves towards force-free structure

C=3%, t=2518, r=9 mm



# trailing mass evolves towards force-free structure

C=3%, t=2518, r=8 mm

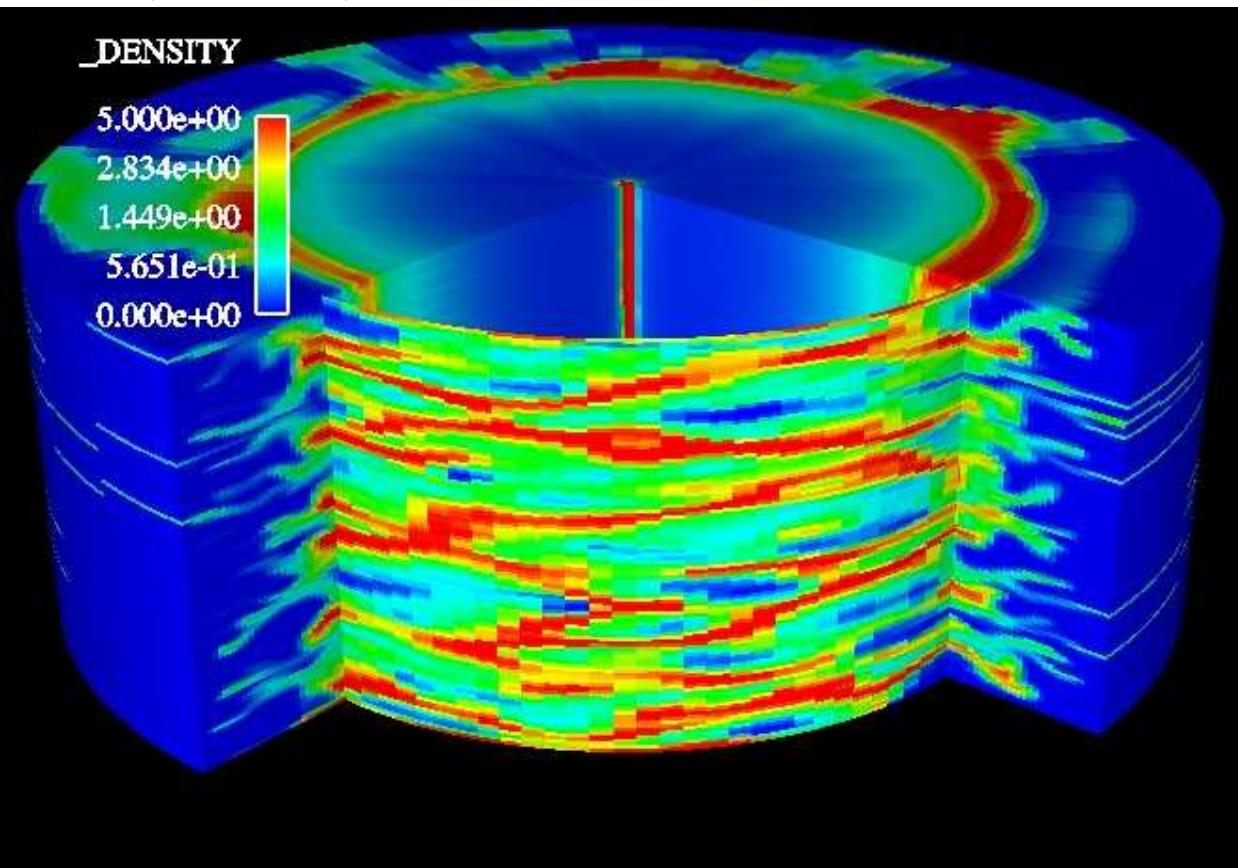


Trailing mass is evolving towards a force-free configuration. It has “forgotten” the initial azimuthal correlation C=3%

$$j \times B = 0$$

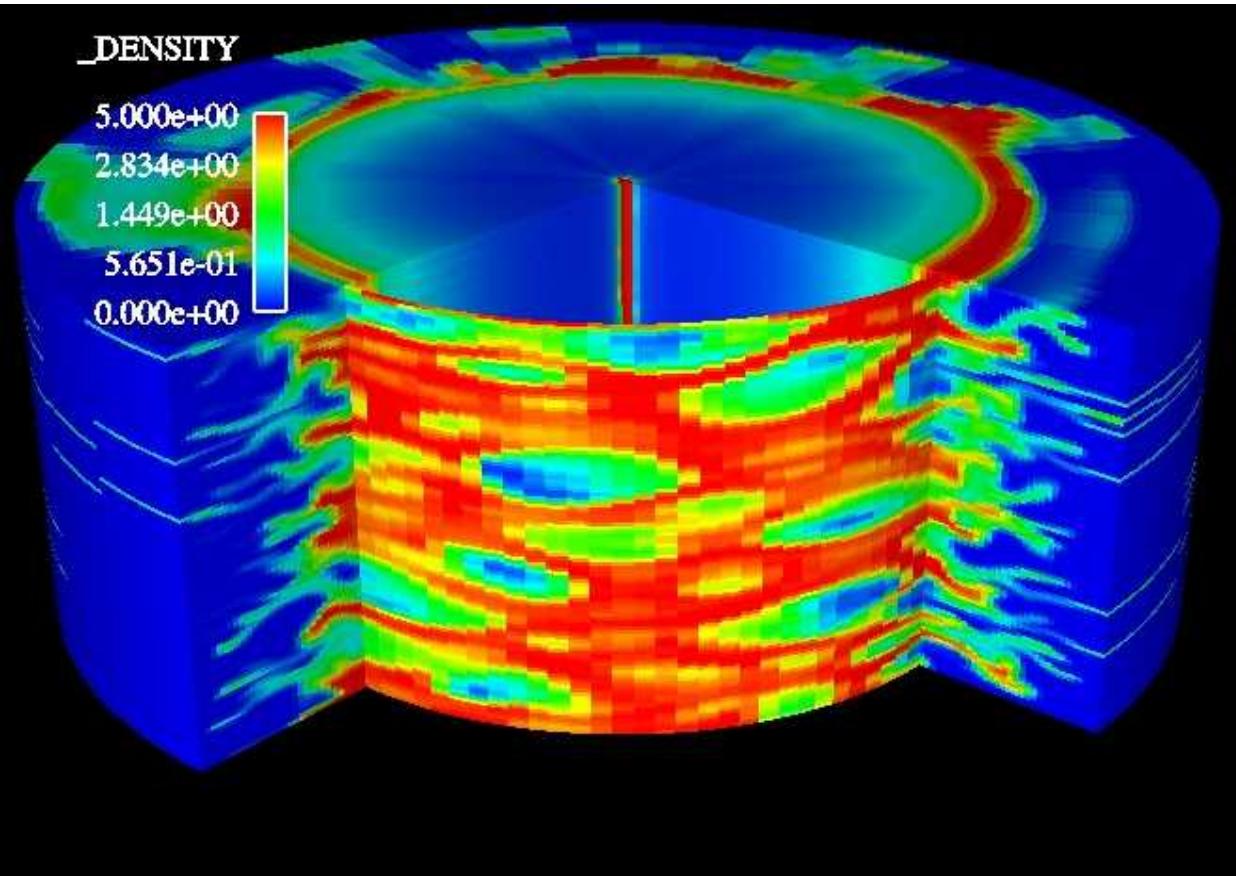
# trailing mass evolves towards force-free structure

C=3%,  $t=2518$ ,  $r=7$  mm



# trailing mass evolves towards force-free structure

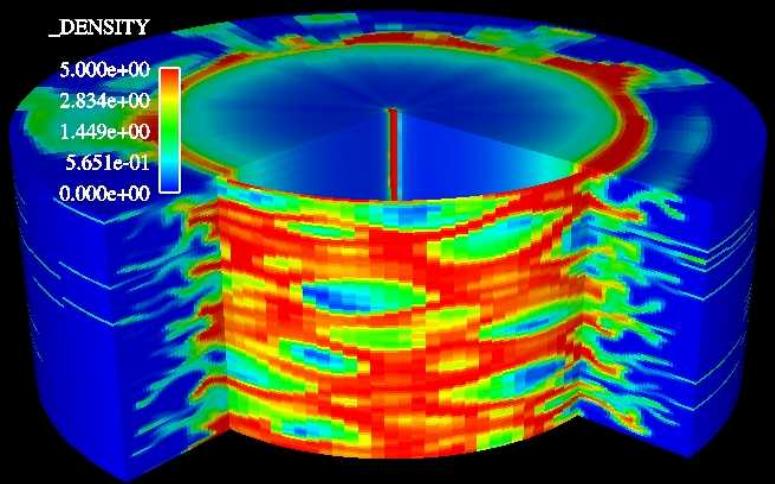
C=3%, t=2518, r=6.5 mm



We are at the imploding sheath. The original azimuthal correlation length has imprinted itself here.

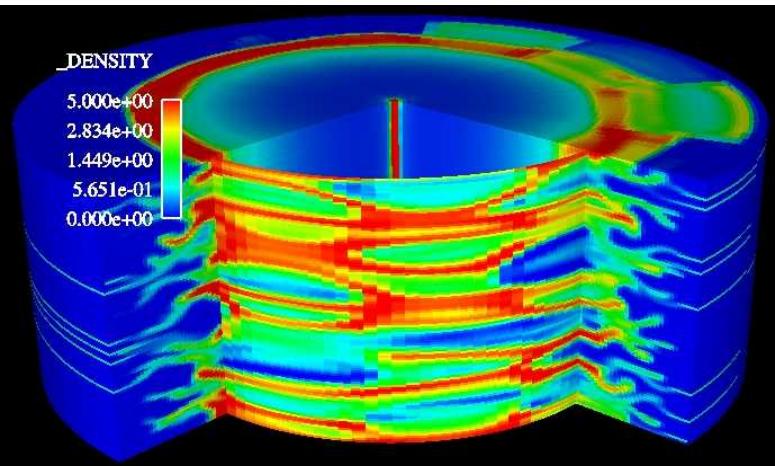
# azimuthal correlation degrades performance

C=3% (2518)

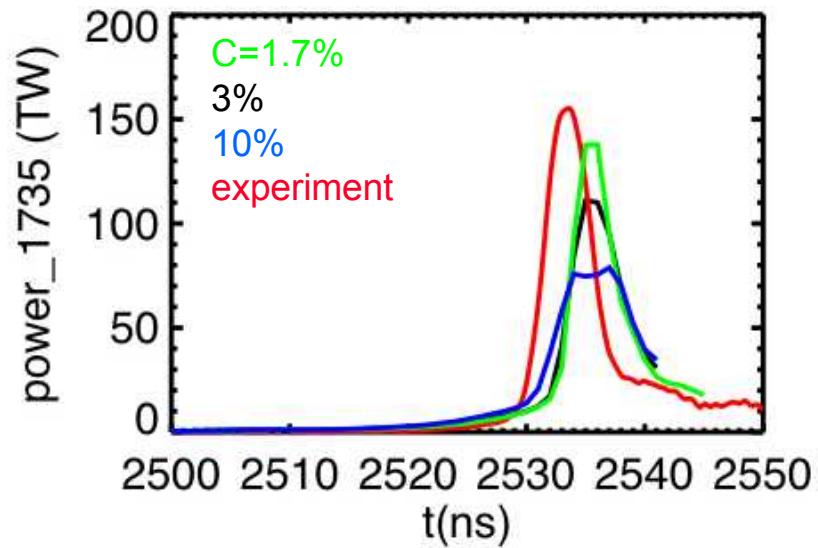
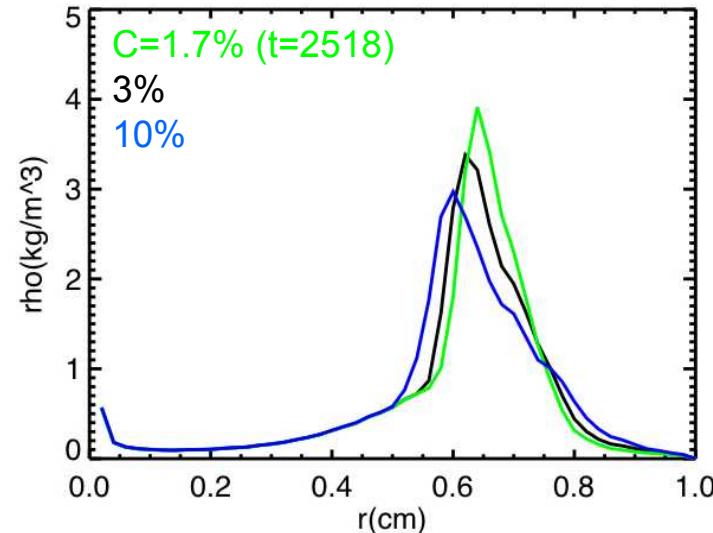


+Higher azimuthal correlation leads to more bubble growth, wider plasma sheaths, lower power

C=10% (2518)

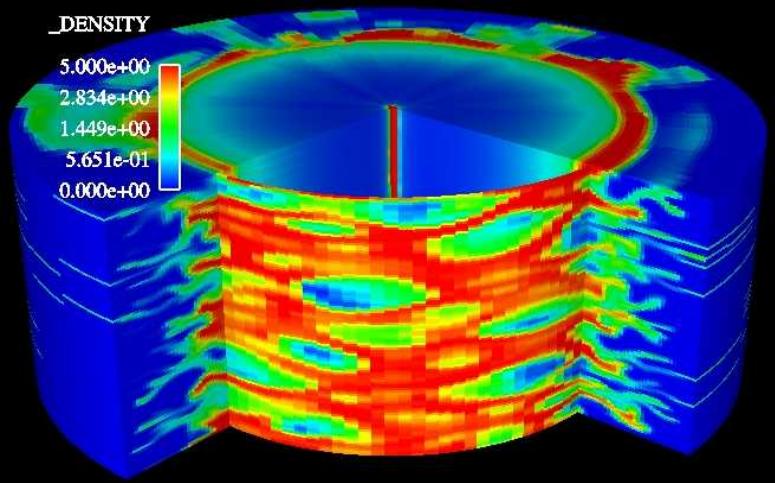


Higher azimuthal correlation on the mass injection surface results in wider azimuthal bubbles on the imploding surface.

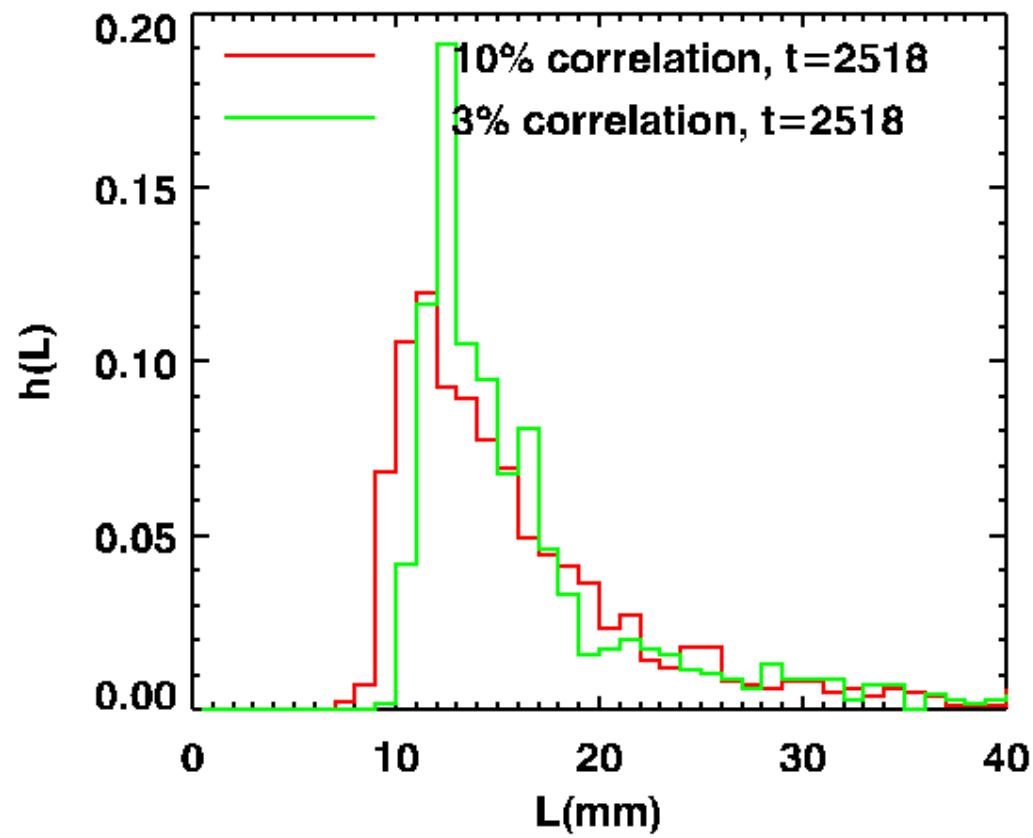
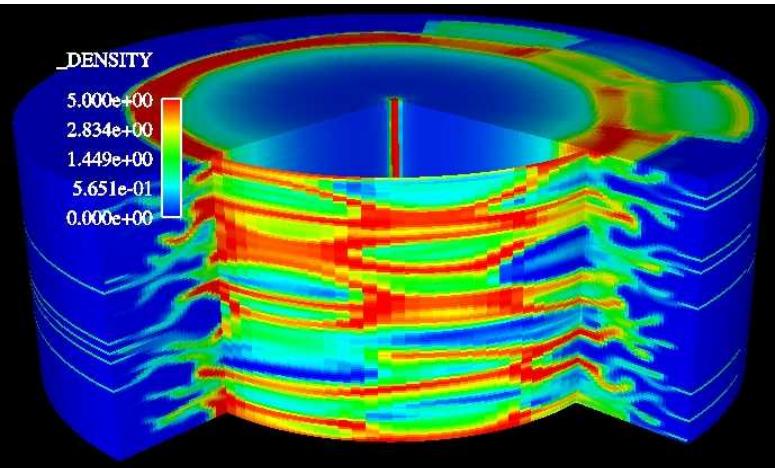


# paths through trailing mass unaffected by azimuthal correlation

C=3% (2518)



C=10% (2518)

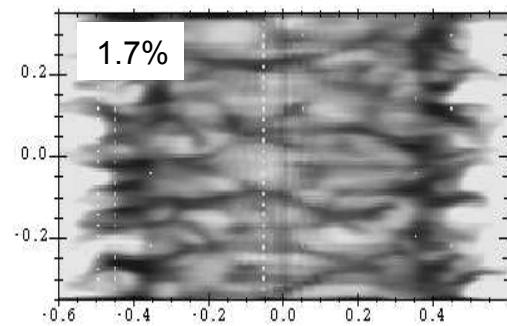
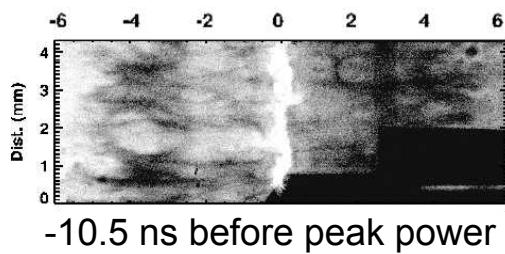
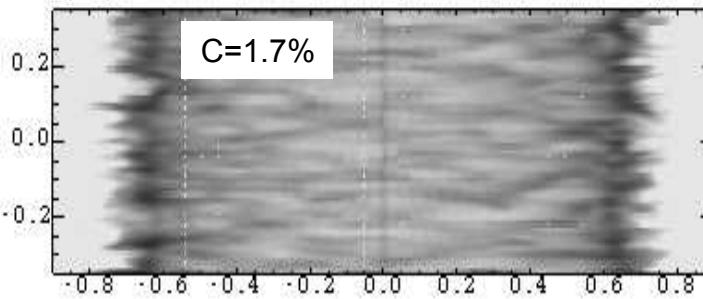
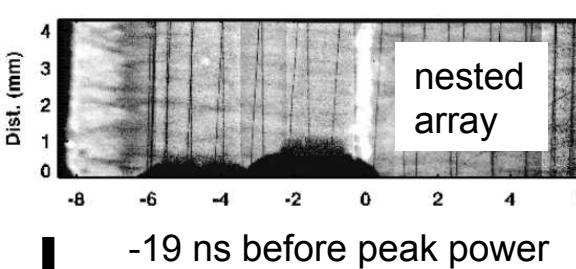


# Experiment radiographs can constrain simulations

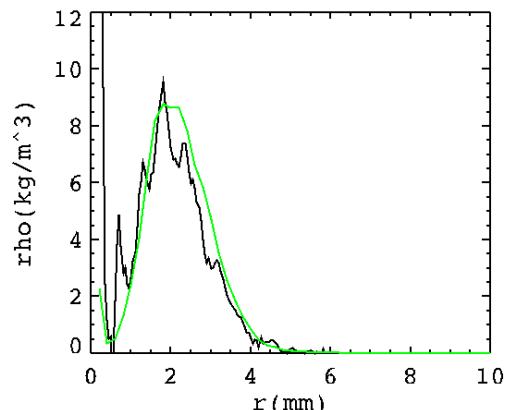
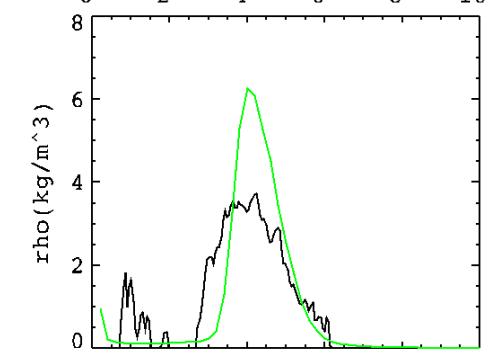
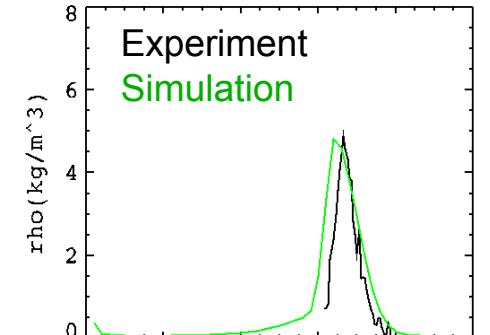
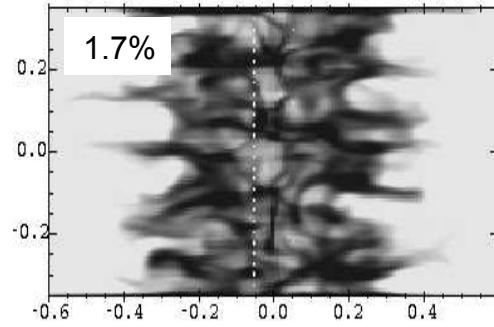
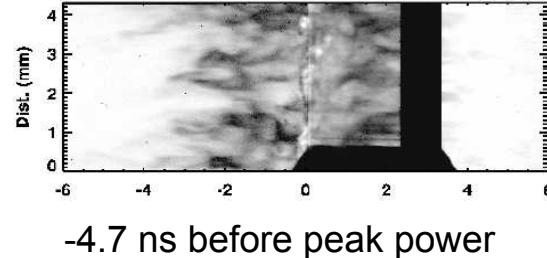
experiment: 2.42 mg

simulation (from Spect3d)

density profiles



Time

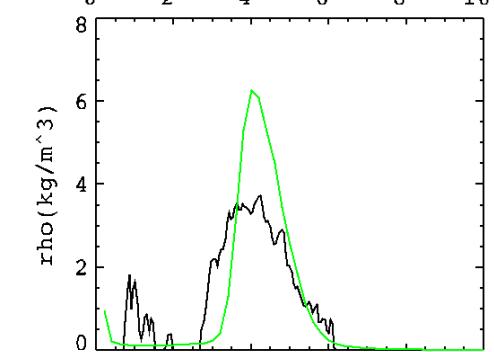
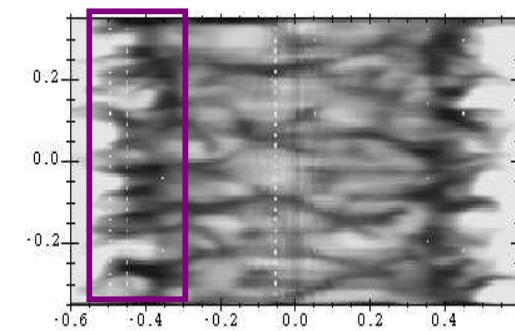
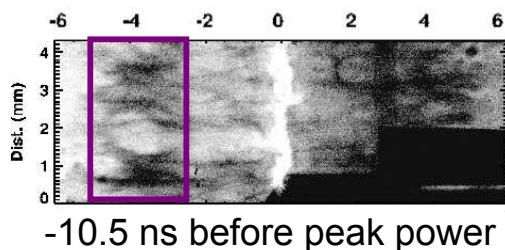
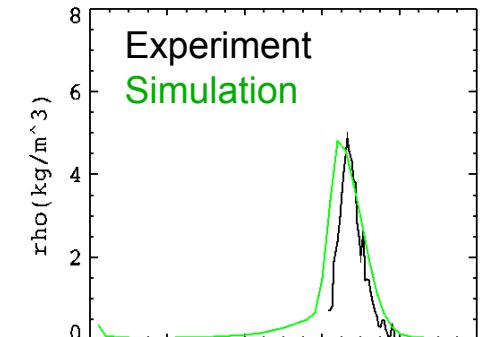
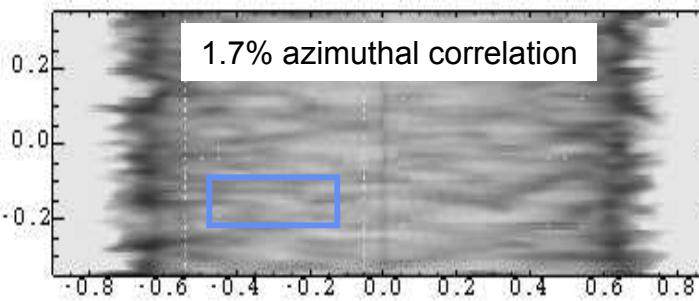
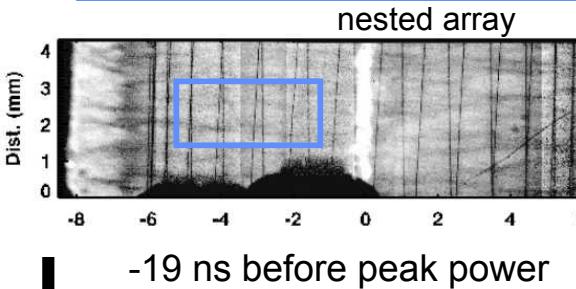


# Experiment radiographs can constrain simulations

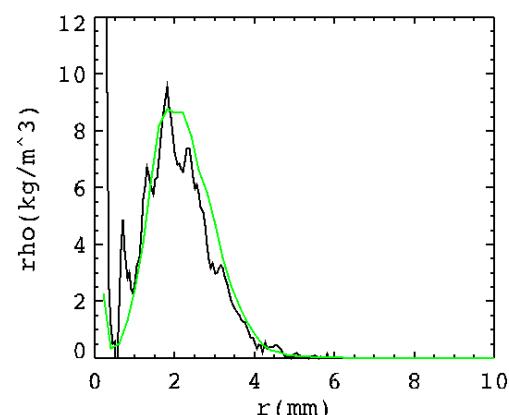
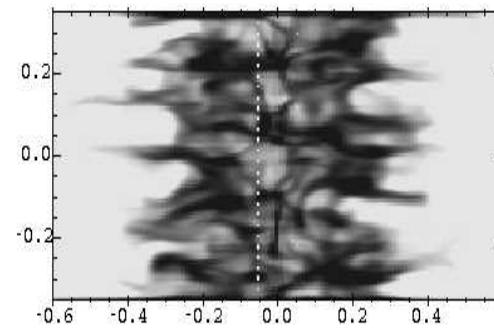
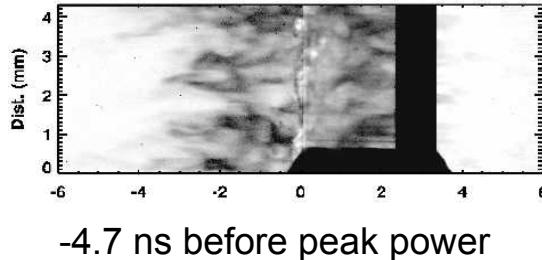
experiment: 2.42 mg

simulation (from Spect3d)

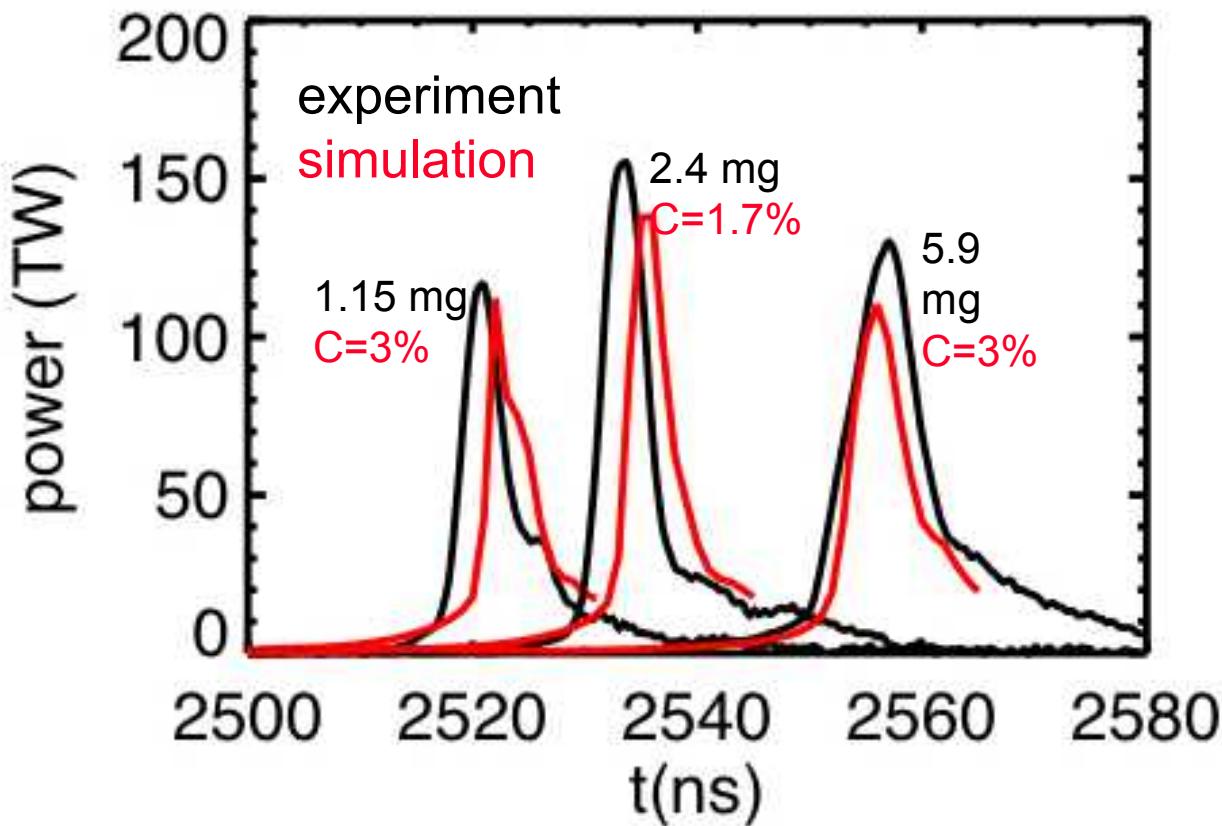
density profiles



Time



# Experimental/Simulation mass scan comparison



For more comparison to data, especially power pulse, please see:  
R.W. Lemke et al., PP8.00039(Wed)

# Conclusions

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In the presence of the axial instability, bubble growth is reduced in 3D because current can flow azimuthally.

In 3D, the trailing mass can have a “healing” effect on the bubble growth, which is determined by both MRT and  $j \times B$  forces

+Higher azimuthal correlation leads to more bubble growth, wider plasma sheaths, lower power

A set of radiographic data exists which strongly constrains data, and may help us determine the degree of azimuthal correlation

THE END

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## THANKS TO:

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