

From Modeling to Implementation of High Index Contrast Microphotonics

Michael R. Watts
Applied Photonic Microsystems
Sandia National Labs
Albuquerque, New Mexico USA



Overview

Goals: To communicate the following . . .

- The importance of analytical intuition
- The importance of rigorous numerical design
- The ease of implementing numerical codes
- The need for both multiphysics and VLSI codes

Outline

- The Finite Difference Time Domain (FD-TD) Technique
- Mode Evolution Devices
- Filter Design and a Polarization Independent Microphotonic Circuit
- Some Special Cases: Periodic Boundary Conditions and Conductors
- A Multi-Physics Problem: Thermal Microphotonic Focal Plane Array (TM-FPA)

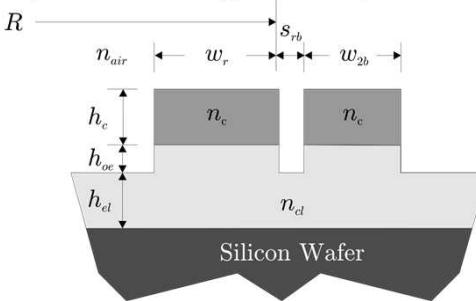


Analytic Intuition: Coupled Mode Theory

Coupled Mode Theory (CMT) Application

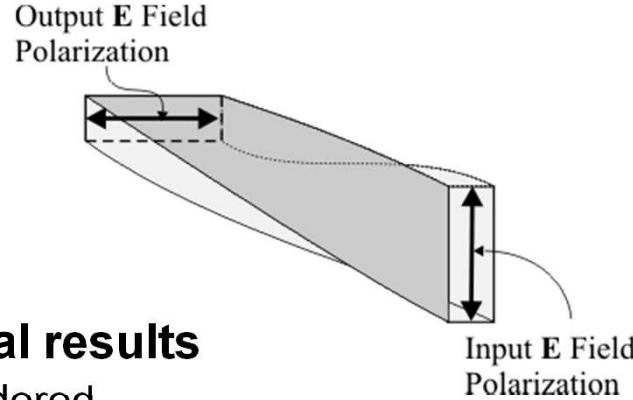
- Between a pair of waveguides: The coupling between otherwise orthogonal modes is determined by the degree of the overlap in the region of perturbation

$$\kappa_{mn} = -j \frac{\omega}{4} \int_A \Delta \epsilon e_m^* \cdot e_n dA$$



- Adiabatic Transition:

$$\kappa_{mn} = -j \frac{\omega}{4\delta\beta(z)} \int_A e_m^* \cdot e_n \frac{d}{dz} \epsilon(z) dA$$



Use CMT for intuition but not numerical results

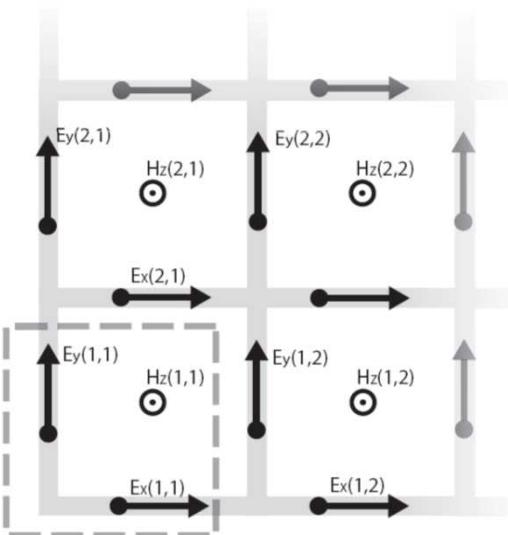
- CMT is limited by number of modes considered
- Scattering, loss, and even coupling strength are generally off
- CMT will not provide generate non-intuitive results
- Computers have become sufficient fast to do rigorous numerical simulations

Finite-Difference Time-Domain Technique

Why choose FD-TD?

- Simple discretization of Maxwell's equations with no other approximations
- Why not Beam Propagation Method and/or Eigenmode Expansion?
 - Beam Propagation Method based on Paraxial Wave Equation (limited angles)
 - Eigenmode Expansion great for tapers, but not for abrupt transitions

How FD-TD is implemented



$$\frac{\partial E_x(z, t)}{\partial t} = -\frac{1}{\epsilon_0} \frac{\partial H_y(z, t)}{\partial z}$$

$$\frac{\partial H_y(z, t)}{\partial t} = -\frac{1}{\mu_0} \frac{\partial E_y(z, t)}{\partial z}.$$

$$E_x(z', t' + \frac{\Delta t}{2}) = E_x(z', t' - \frac{\Delta t}{2}) - \frac{\Delta t}{\epsilon_0 \cdot \Delta x} \left(H_y(z' + \frac{1}{2} \Delta z, t') - H_y(z' - \frac{1}{2} \Delta z, t') \right)$$

$$H_y(z', t' + \frac{\Delta t}{2}) = H_y(z', t' - \frac{\Delta t}{2}) - \frac{\Delta t}{\mu_0 \cdot \Delta x} \left(E_x(z' + \frac{1}{2} \Delta z, t') - E_x(z' - \frac{1}{2} \Delta z, t') \right)$$



Finite Difference Time Domain Considerations

Commercial Code, Own Code, Open Source Codes

- ❑ Commercial codes tend not to be well parallelized or portable → limited utility
- ❑ FD-TD is easy to program with some guidance (book by A. Taflove)
- ❑ If you write your own code, you will always know what you is in the code
- ❑ Also, open source codes by (e.g. Steven Johnson's MEEP)

Computer Selection

- ❑ Why is FD-TD so slow? Memory bandwidth code, cores alone will not help
- ❑ Specfp benchmark *swim_m.f* www.spec.org a good metric of performance
 - 32-core SGI Altix 4700 Bandwidth System, *swim_m.f* (**62.8 seconds**)
 - 16-core IBM, *swim_m.f* (**58.8 seconds**)
 - 8-core Intel (i.e. Xeon Quad Cores), *swim_m.f* (**834 seconds**)
- ❑ What is the difference between these machines → Memory Bandwidth





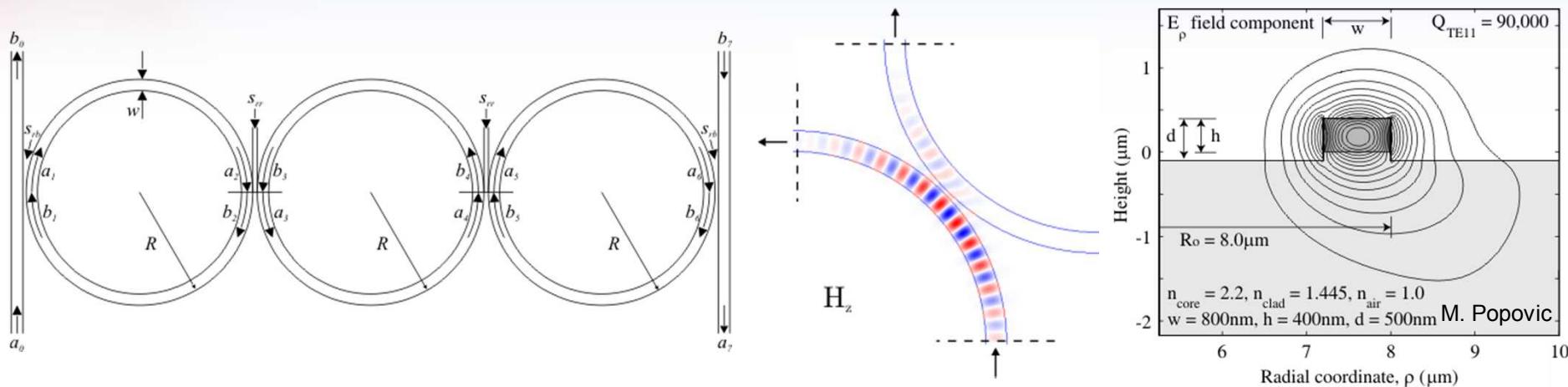
Microring-Resonator Based Filters and the first Polarization Microphotonic Circuit

**Michael R. Watts, Milos Popovic, Tymon Barwicz,
Peter Rakich, Luciano Soccia, Hermann A. Haus,
Henry I. Smith and E. P. Ippen**

**Research Performed at the
Massachusetts Institute of Technology**

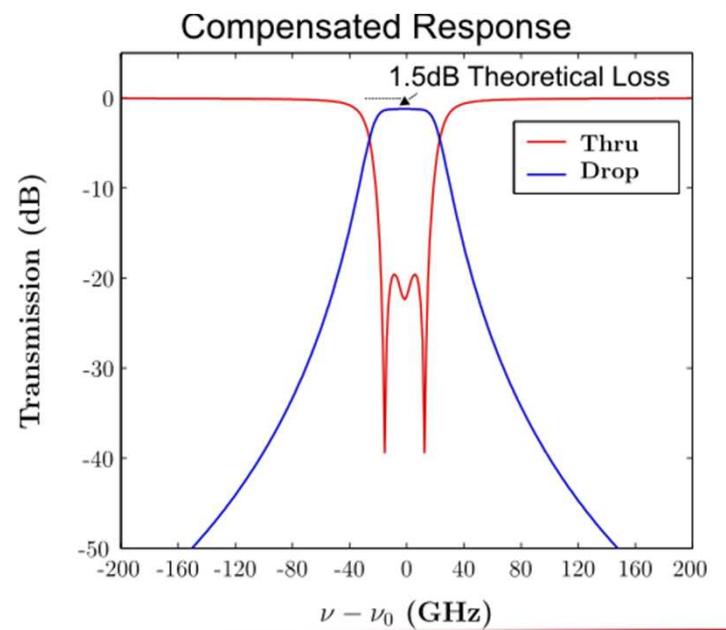


Implementation of FD-TD



Procedure

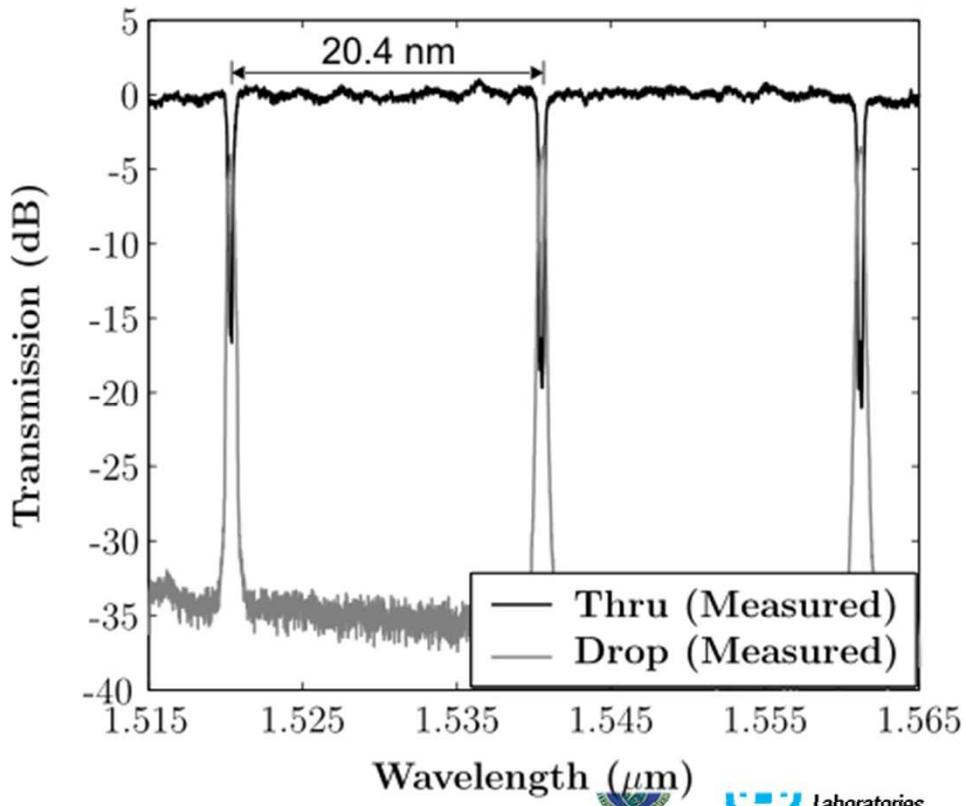
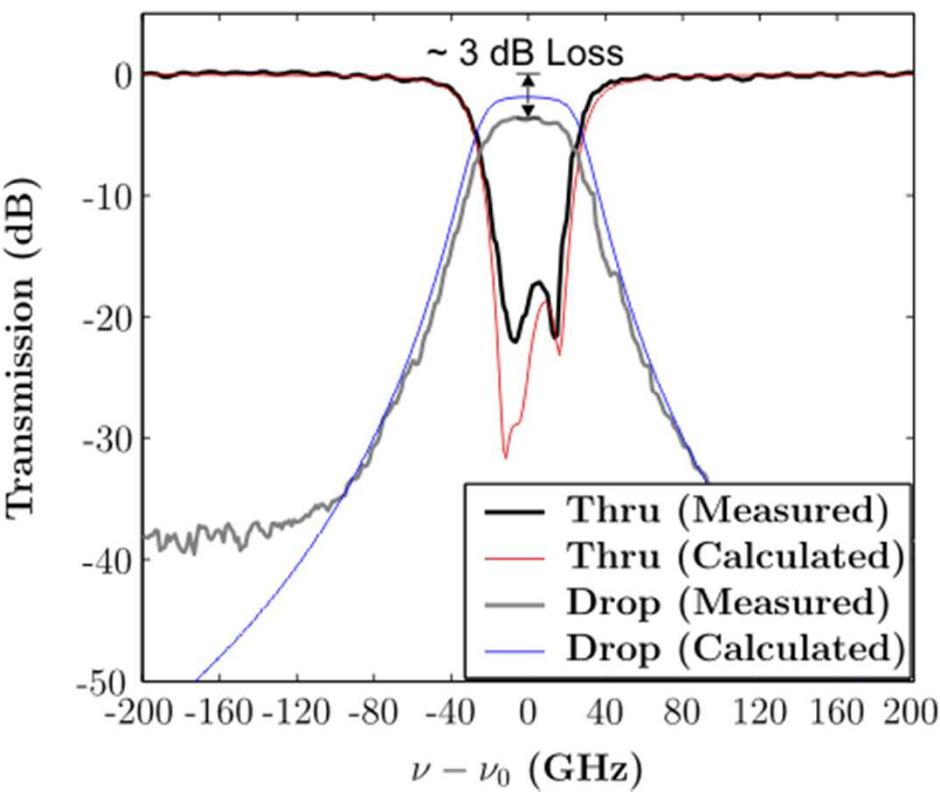
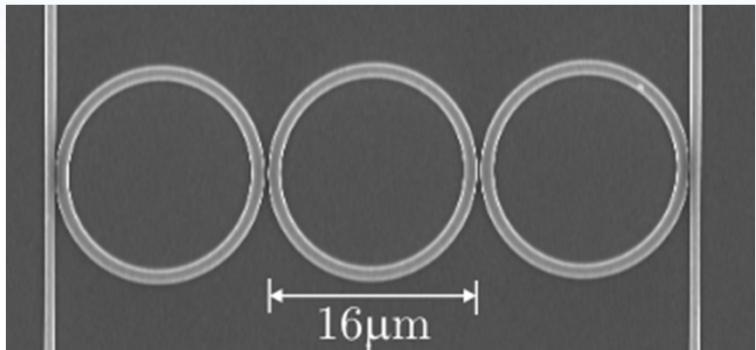
- Complex vector mode-solver to determine Q and find bus and ring waveguide modes
- Launch appropriate modes as Gaussian pulse
- Take Discrete Fourier Transforms (DFTs) & overlaps to determine complex scattering coefficients
- Use scattering coefficients in Transfer Matrix Method to generate filter response



Redesigned Filters

Improvements

- ❑ Advanced coupler design incorporated
- ❑ Higher-Q ring waveguide utilized
- ❑ Slightly wider bandwidth
- ❑ Achieved 3dB drop-port losses
- ❑ > 15 dB thru-port extinction





Mode Evolution Based Devices

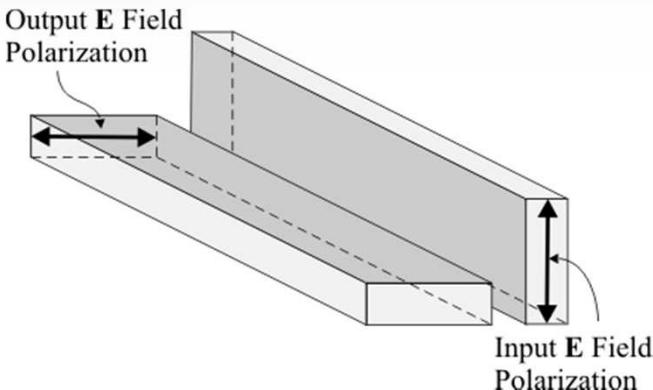
**Michael R. Watts, Minghao Qi, Tymon Barwicz,
Luciano Soccia, Hermann A. Haus, Henry I. Smith
and E. P. Ippen**

**Research Performed at the
Massachusetts Institute of Technology**



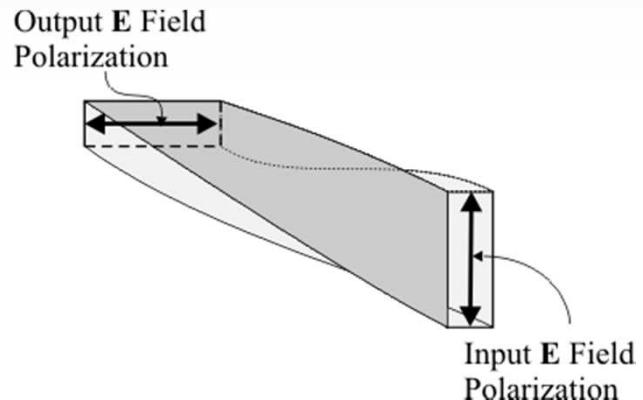
Example: Microphotonic Polarization Rotator

Mode Coupling



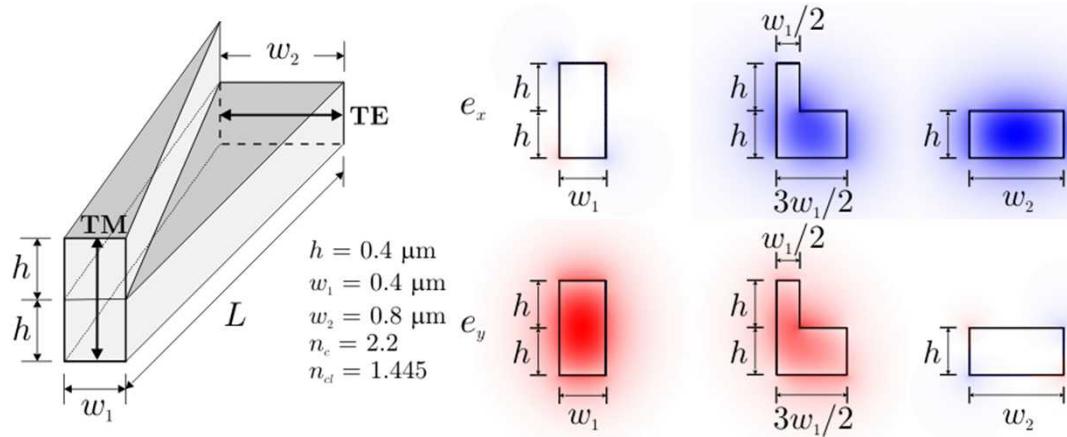
- ❑ **Requires:** Precise coupling & phase matching
- ❑ **Result:** Wavelength & fabrication sensitive

Mode Evolution



- ❑ **Requires:** Prevent mode coupling ($\max \Delta\beta/\kappa$)
- ❑ **Result:** Inherently wavelength & fabrication insensitive
- ❑ **Challenge:** Implementing a twist on a chip

Mode Evolution Based Polarization Rotator

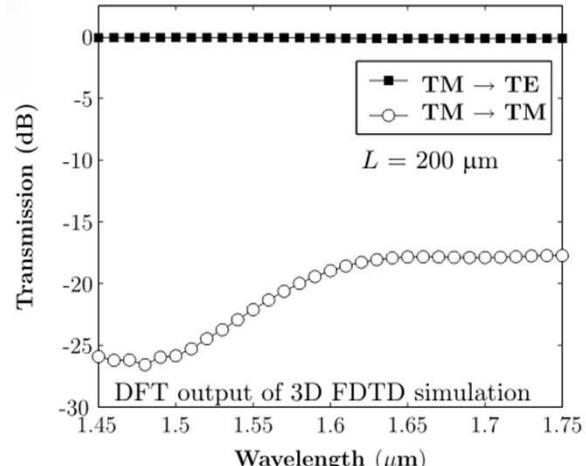
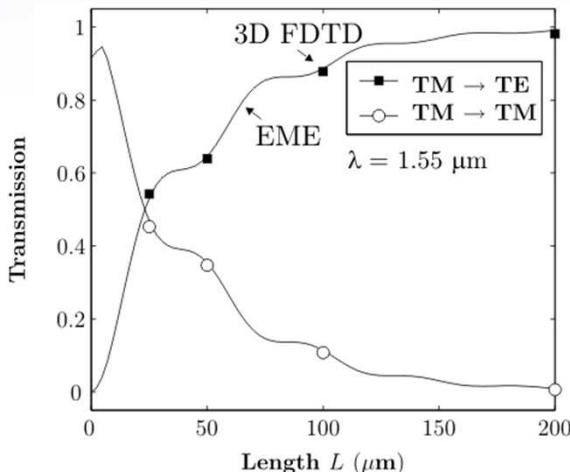
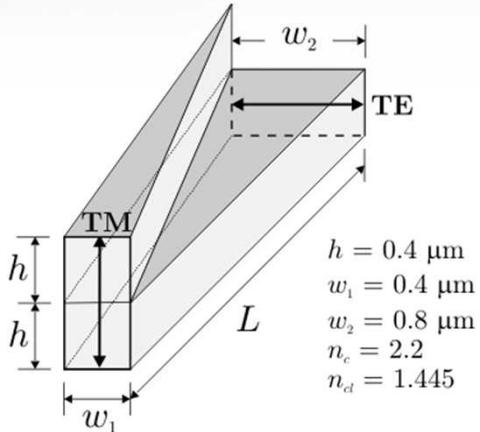


- ❑ Most confined mode aligned to geometric axis of guide (result of Gauss' Law)
- ❑ Large aspect ratio enhances $\Delta\beta/\kappa \rightarrow$ minimizes coupling
- ❑ Intuition indicates it should work, but rigorous simulations are required to confirm the design



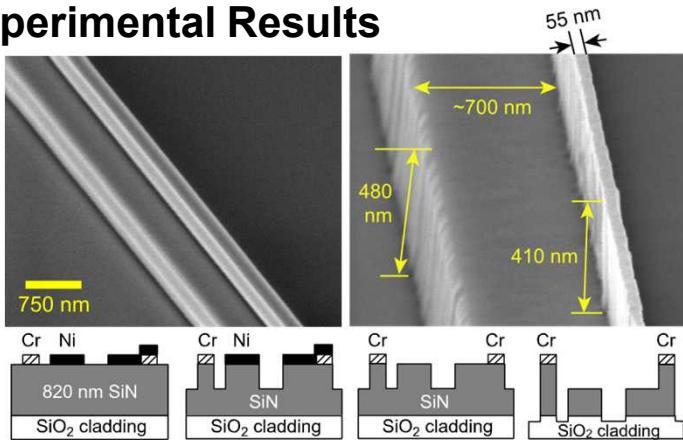
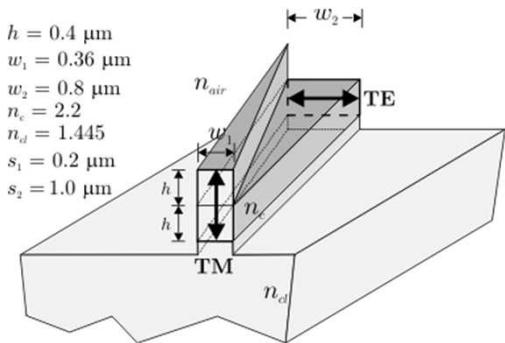
Design and Experimental Results

Polarization Rotator - Numerical Results

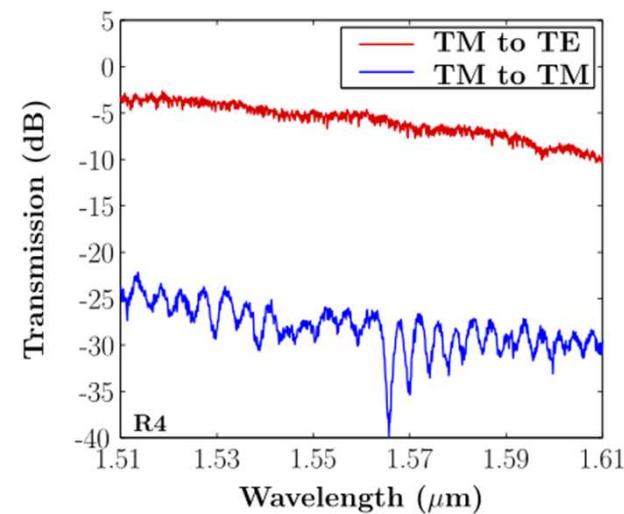


M. R. Watts and H. A. Haus, "Integrated mode-evolution-based polarization rotators," *Optics Letters* **30**, 138-140 (2005).

Polarization Rotator - Experimental Results

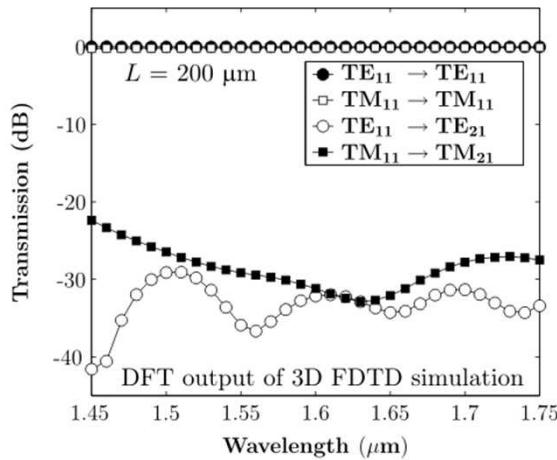
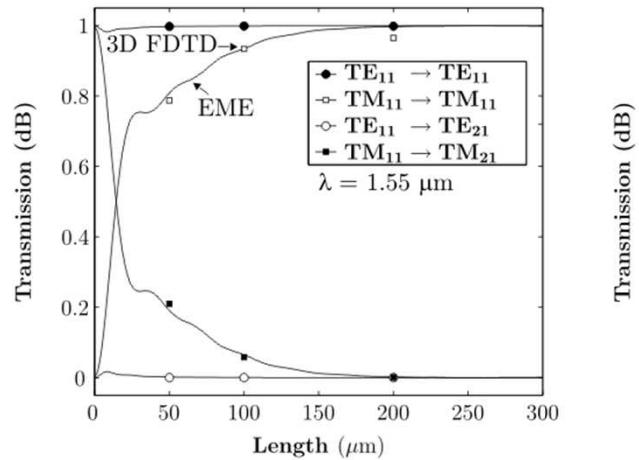
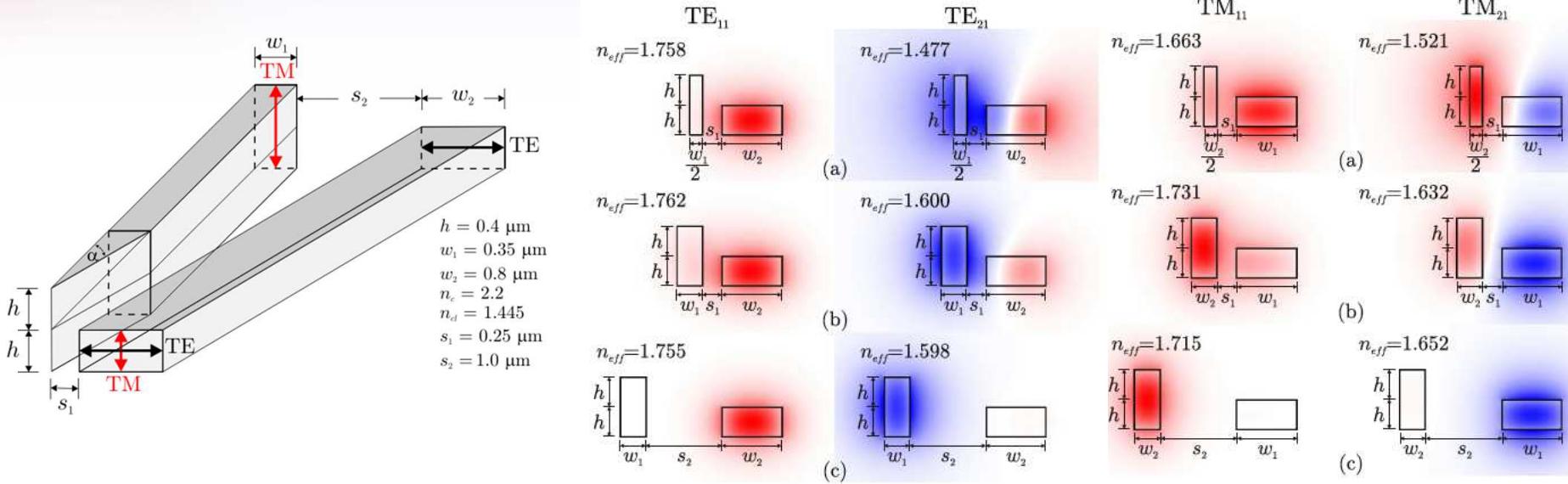


Fabrication performed by Minghao Qi



Sandia
National
Laboratories

Mode Evolution Based Polarization Splitter



Polarization Splitter Design

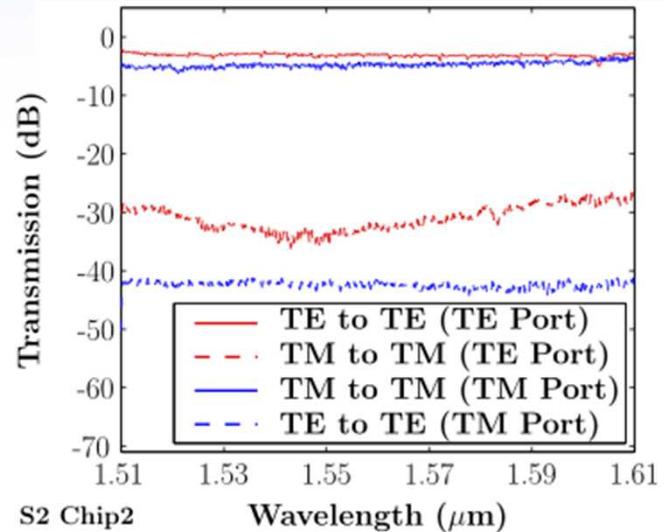
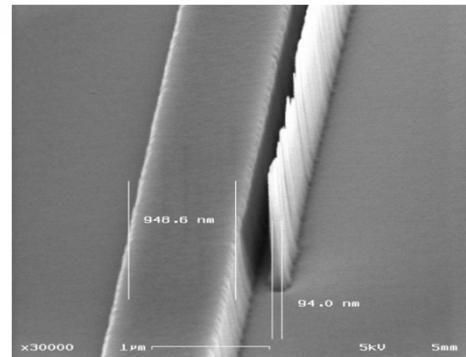
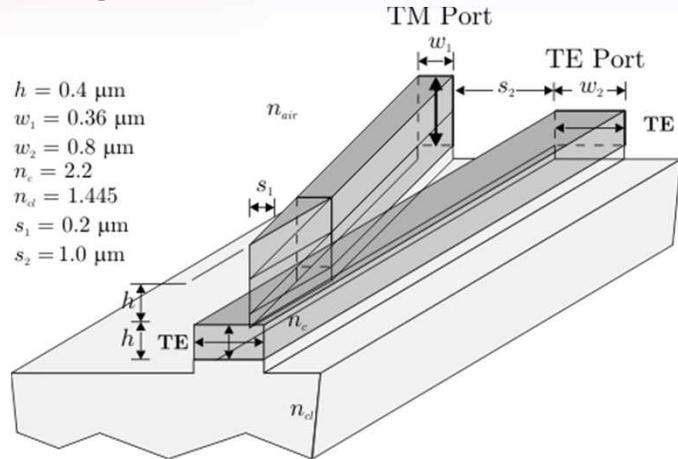
- ❑ TE_{11} and TM_{11} modes separate
- ❑ Large ratio of $\Delta\beta/\kappa$ by geometry
- ❑ Coupling between TM_{11} and TM_{21} modes limits device performance
- ❑ Splitter / Rotator can be combined

M. R. Watts, H. A. Haus, and E. P. Ippen "An integrated mode-evolution-based polarization splitter," to be published *Optics Letters*

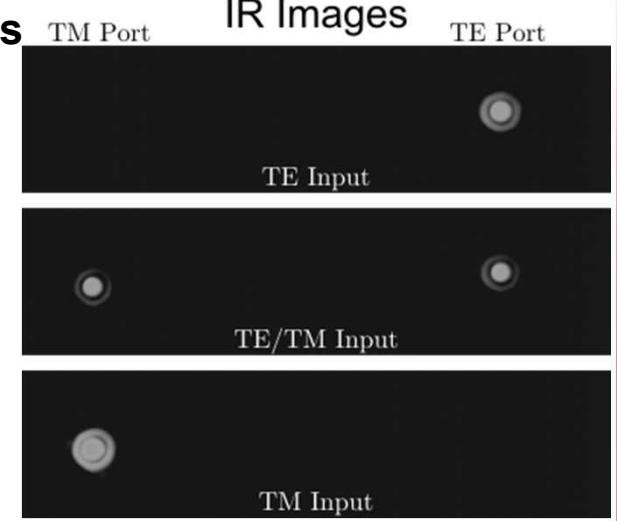
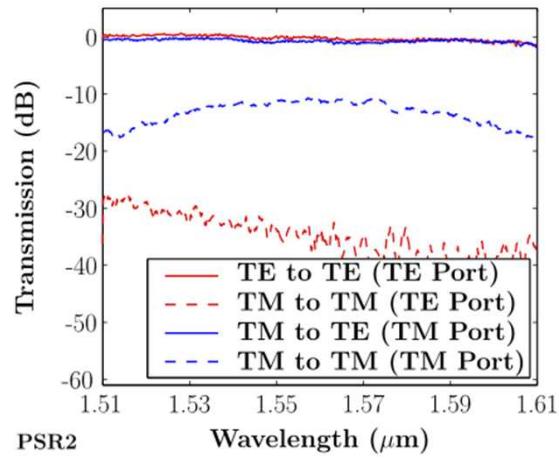
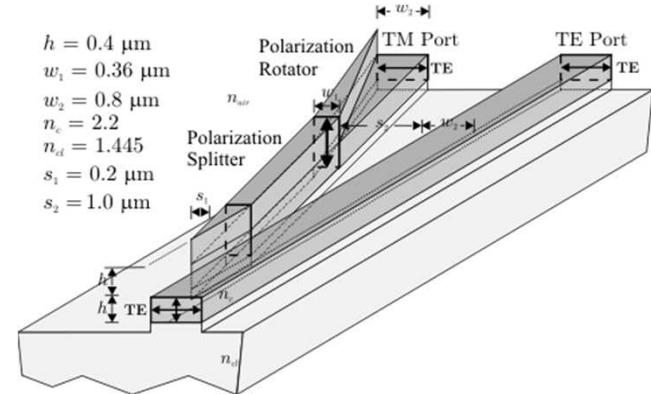


Polarization Splitter-Rotators

Integrated Polarization Splitter - Experimental Results



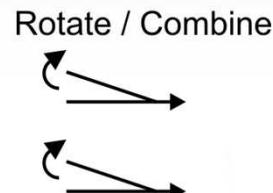
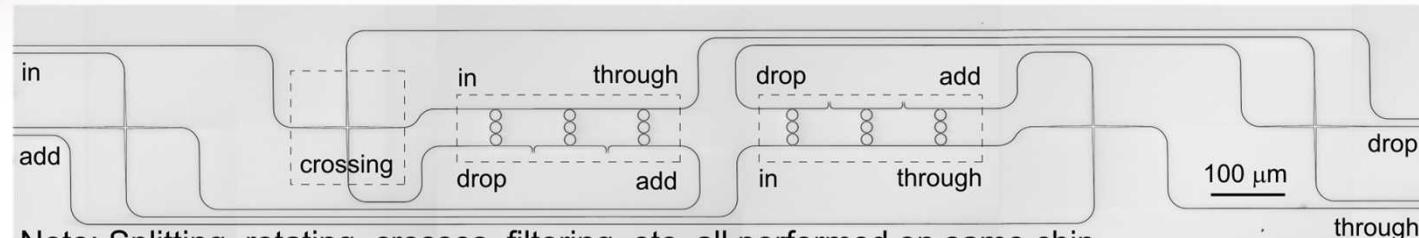
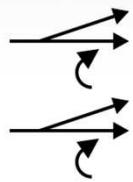
Integrated Polarization Splitter-Rotator - Experimental Results



Sandia
National
Laboratories

Integrated, P-Independent Optical Add-Drop

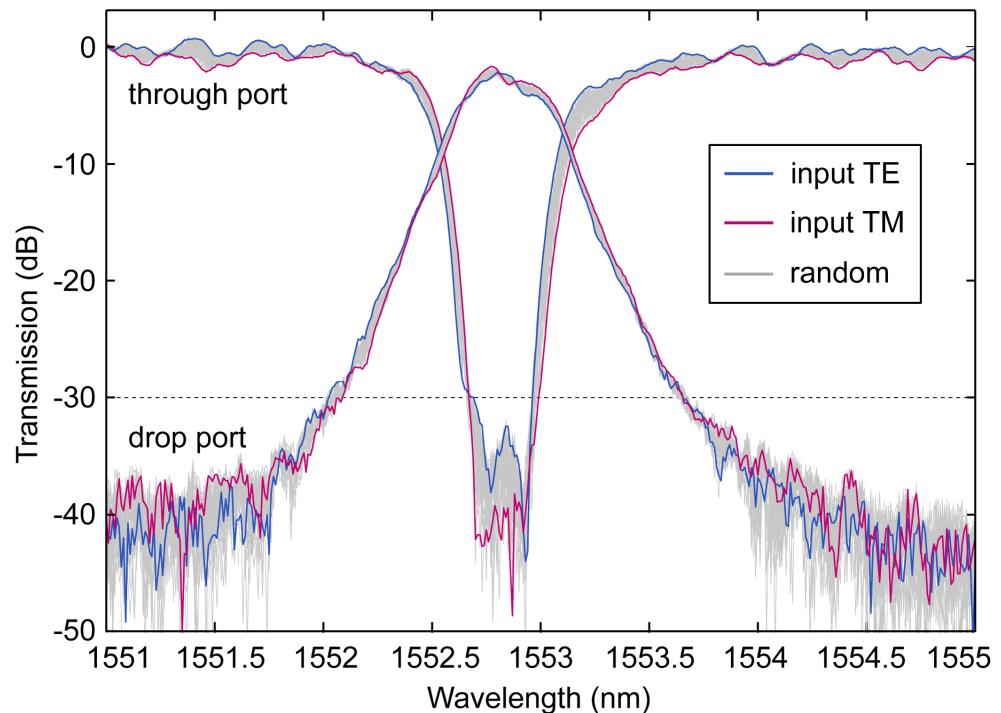
Split / Rotate



Note: Splitting, rotating, crosses, filtering, etc. all performed on same chip

Results

- Demonstrated polarization independence in terms of frequency matching and loss
- Matching of resonant frequencies to ~1GHz
- Worked on the 1st try with all devices on the chip





Some Special Cases of FD-TD: Conductors and Periodic Boundary Conditions

Michael R. Watts and David W. Peters

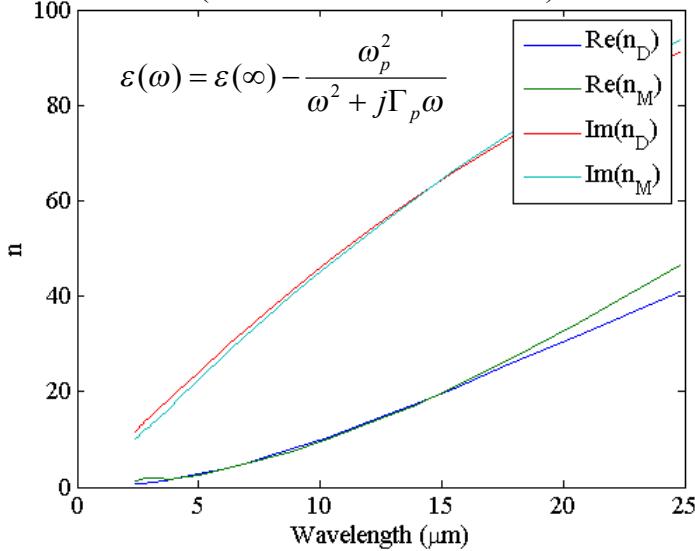
**Applied Photonic Microsystems
Sandia National Laboratory
Albuquerque, NM USA**



The Introduction of Metals

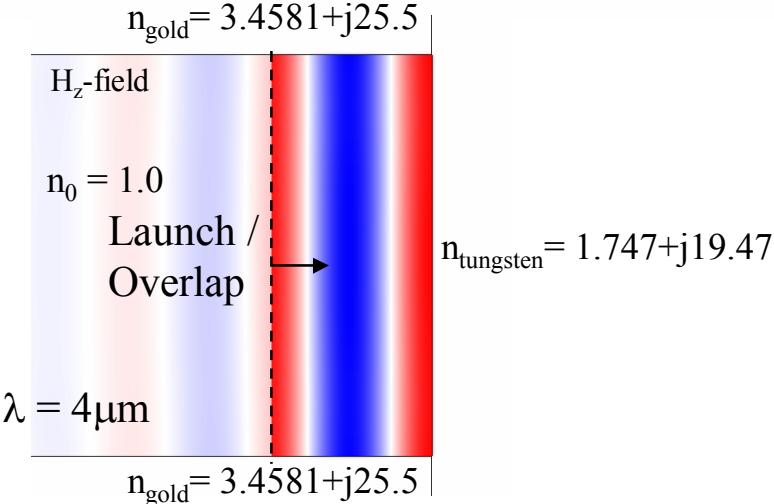
Tungsten Drude Model

(Measured Data from Palik)



Example: Reflection from Closed Metal Waveguide

$$R_{\text{analytic}} = 0.98192$$
$$R_{\text{FD-TD}} = 0.98198$$



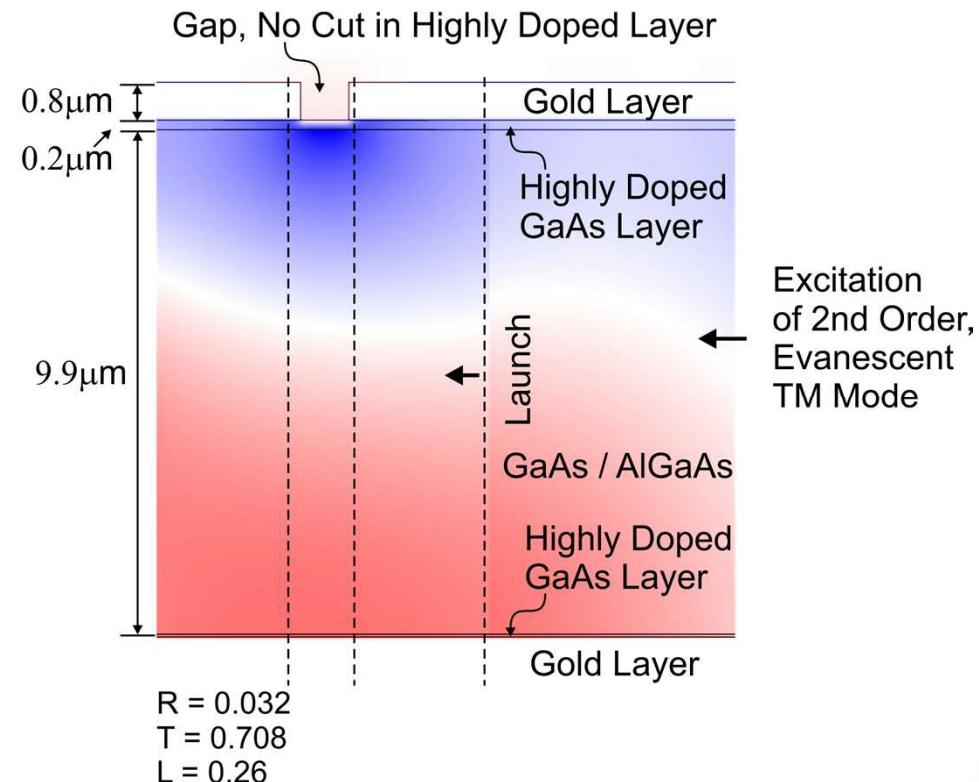
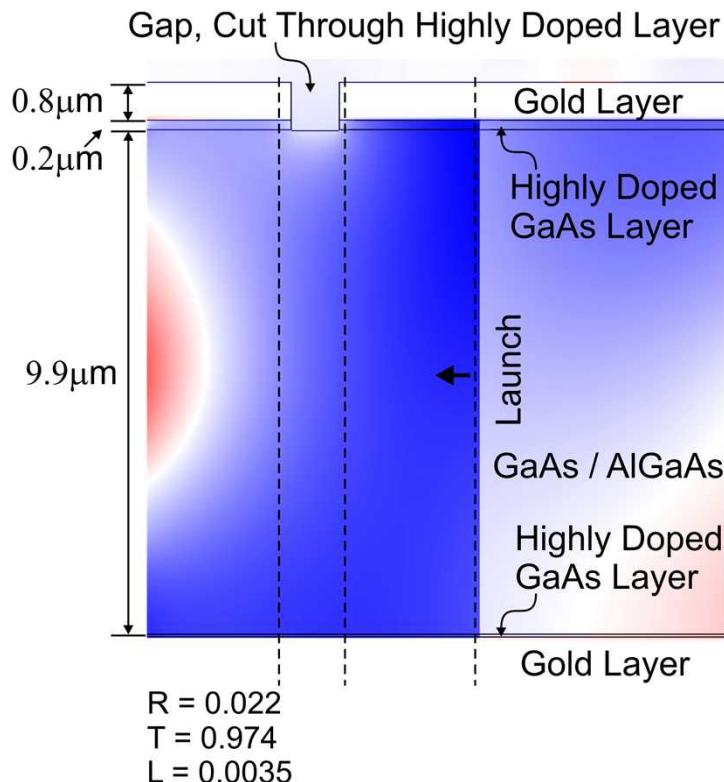
How do we implement metals

- Metals introduced by adding terms for the current densities J_x , J_y , and J_z
- Note: Frequency dependent refractive index and conductivity
 - Dispersion accounted for by implementing the Drude Model
- Drude Model Accurately Models Complex Refractive Index in Mid-to-Long IR
- Analytic & FD-TD Reflection Coefficients Nearly Identical (0.98192 vs. 0.98198)

Simulation in the Terahertz Domain

Simulation of cut in contact of a Terahertz Quantum Cascade Laser

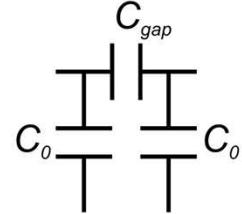
- Question: Do you cut through the highly doped GaAs layer or not?
- Intuition (Optics): Leaving highly doped GaAs layer intact will minimize radiation
- Answer: Leaving the highly doped GaAs layer intact can cause massive losses
- Why?



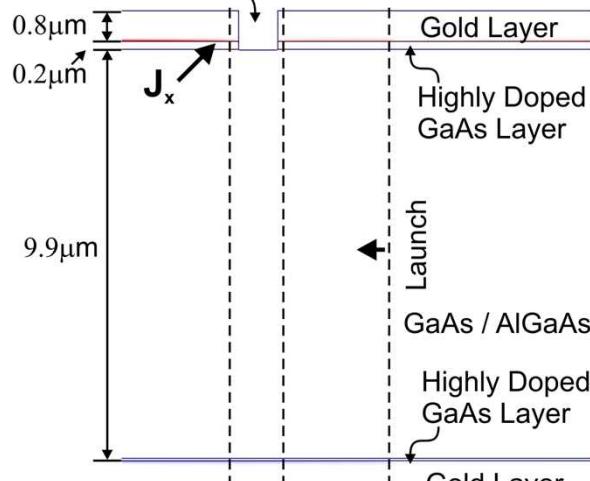
Well . . . Circuit Theory, Look at J_x

Case 1

Equivalent Circuit



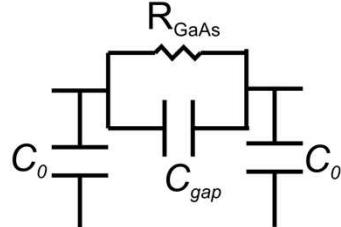
Gap, Cut Through Highly Doped Layer



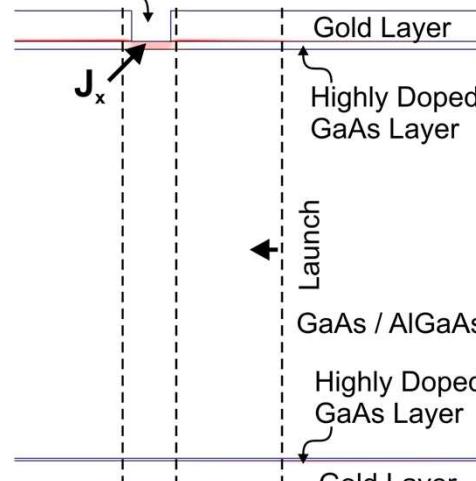
$R = 0.022$
 $T = 0.974$
 $L = 0.0035$

Case 2

Equivalent Circuit



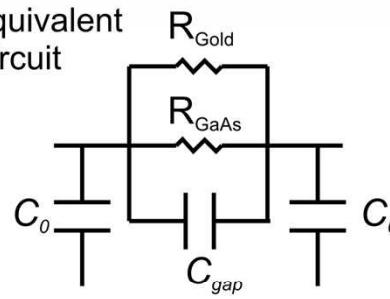
Gap, No Cut in Highly Doped Layer



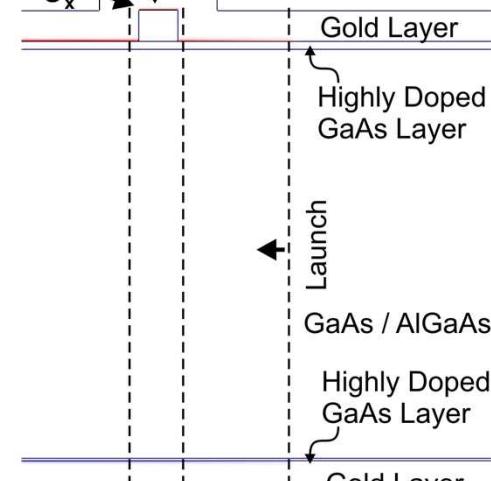
$R = 0.032$
 $T = 0.708$
 $L = 0.26$

Case 3

Equivalent Circuit



Gap, Gold Short Inserted In



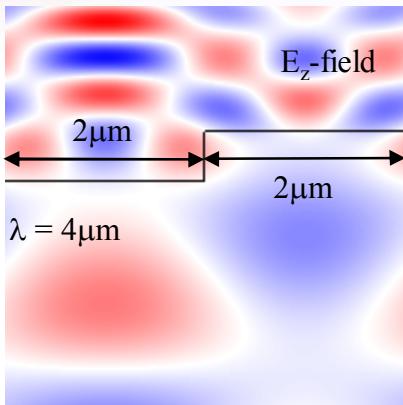
$R = 0.0003$
 $T = 0.9915$
 $L = 0.0055$

Note: J_x is depicted in Red and Blue



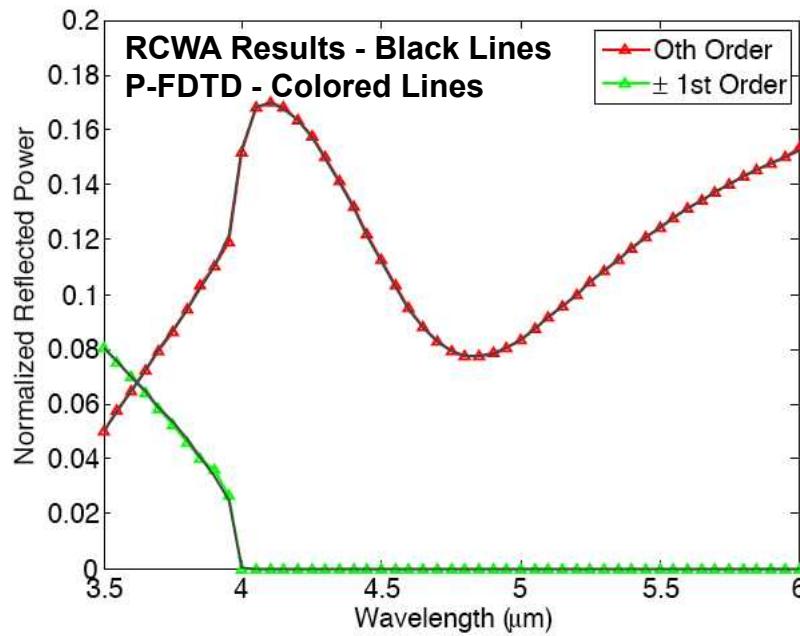
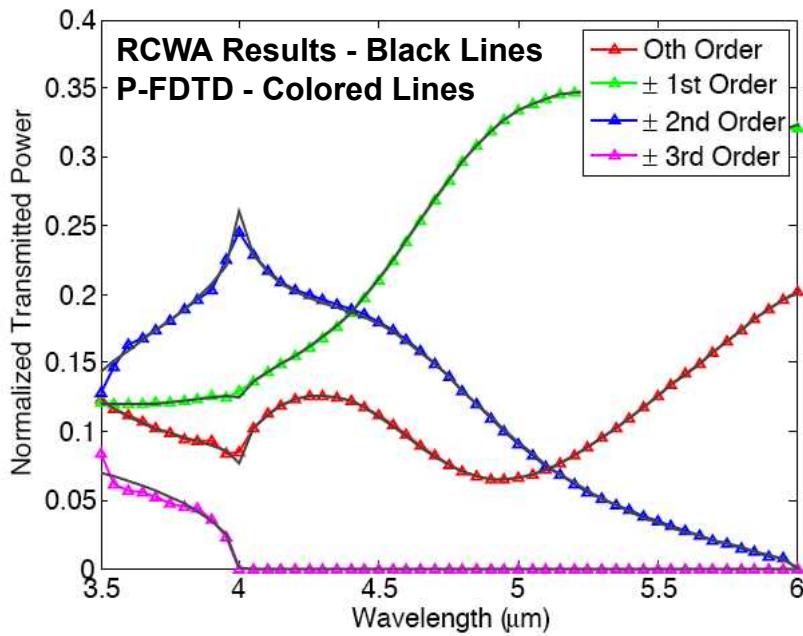
Sandia
National
Laboratories

Periodic FD-TD



Periodic Boundary Conditions Introduced

- ❑ Normal incidence is straightforward
- ❑ Off-normal incidence requires substitution of variables that complicates the code a bit
- ❑ Agreement between RCWA and P-FDTD quite good



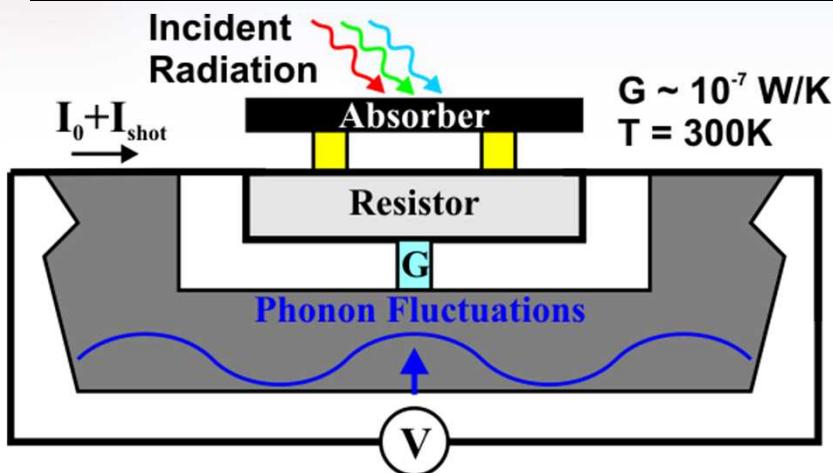


A Multi-Physics Problem: Thermal Micromechanical Focal Plane Array (TM-FPA) for Uncooled Thermal Imaging

**Michael R. Watts, Michael J. Shaw, Gregory N.
Nielson, Jeremy B. Wright, and Frederick B.
McCormick**



Limits to Room Temperature Bolometric Detection



$$S(t) = S_0 \frac{P_{abs}}{G} \frac{dR/dT}{R}$$

Scale Factor

$$\frac{S(t)}{S_0 P_{abs}} = \frac{\Delta V}{V} = 2 \times 10^{-7} / pW$$

Bolometric Detection: Detect change in resistance due change in temperature

- Despite great strides in past decades, bolometric performance has plateaued
- Non-ideal thermal detector: Dissipating power in sensor, inducing temperature change

Fundamental Limits

- Shot Noise: (1) Measurement of current/voltage, and (2) induced thermal fluctuations

- Johnson Noise (Thermal Electron Fluctuations)

$$NEP = \sqrt{4k_B T P} = 4 \times 10^{-12} W / \sqrt{Hz}, P = 1 mW$$

- Phonon Noise (Thermal Phonon Fluctuations)

$$NEP = \gamma \sqrt{4k_B G T} = 7 \times 10^{-13} W / \sqrt{Hz}$$

← **Fundamental Limit**

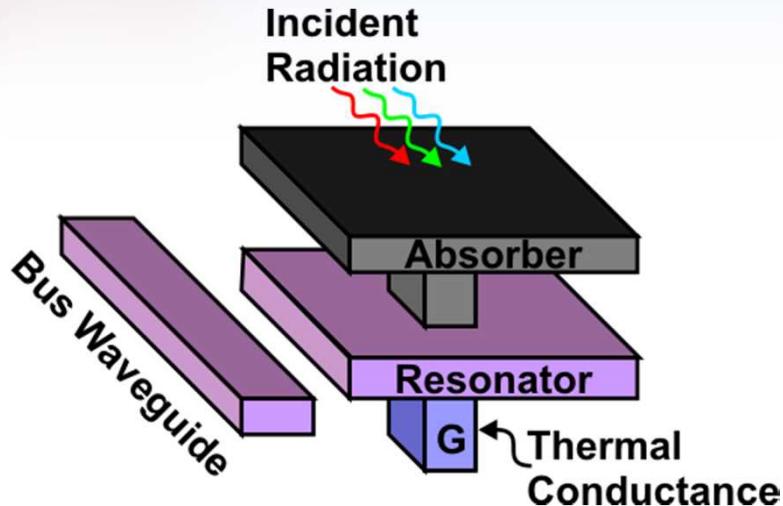
Practical Limits

- Best bolometers achieve $NEP > 2 \cdot 10^{-11} W / \sqrt{Hz}$ (NETD $\sim 30 mK$)

- Perturbing measurement / small scale factor
make bolometers susceptible to Johnson, 1/f, etc.



Thermo-Micromechanical Detection



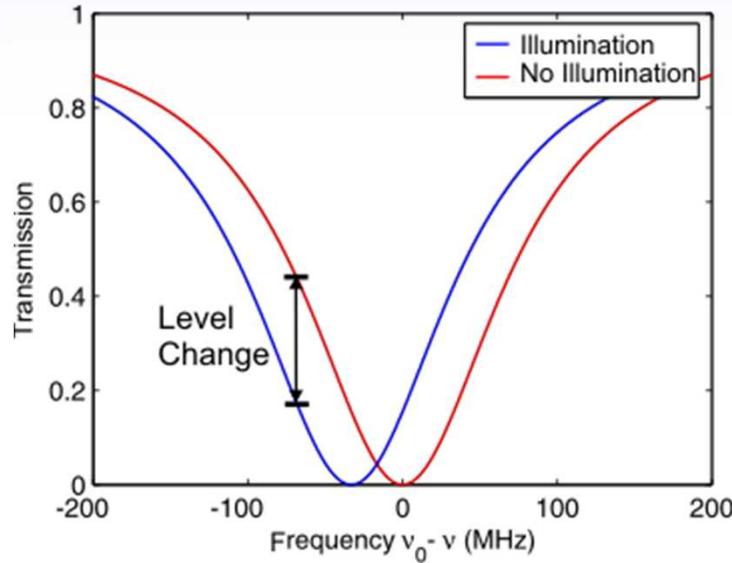
Scale Factor of the T-O Approach

$$S(t) = \frac{S_0}{2} \frac{2}{\Delta v} \frac{dv}{dT} \frac{P_{abs}}{G} \Rightarrow \frac{S(t)}{S_0 P_{abs}} = \frac{Q}{G} \frac{dn}{dT}$$
$$\frac{dv}{dT} = \frac{dv}{dn} \frac{dn}{dT} \approx \frac{v}{n} \frac{dn}{dT}$$

For $Q = 10^6$, and $G = 10^{-8} \text{ W/K}$ in Si

$$\frac{S(t)}{S_0 P_{abs}} = \frac{\Delta V}{V} \approx 6 \times 10^{-3} / pW$$

~30,000X Larger than
bolometric approaches



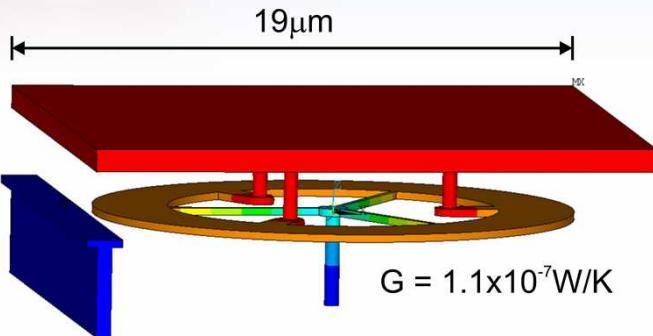
Noise Limitations

- No Johnson noise
- Large scale factor min. impact of shot noise
- Fundamentally, limited only by Phonon Noise
- Measurement does not perturb sensor
- No metal paths back to substrate



Sandia
National
Laboratories

Simulation of a Multiphysics Problem

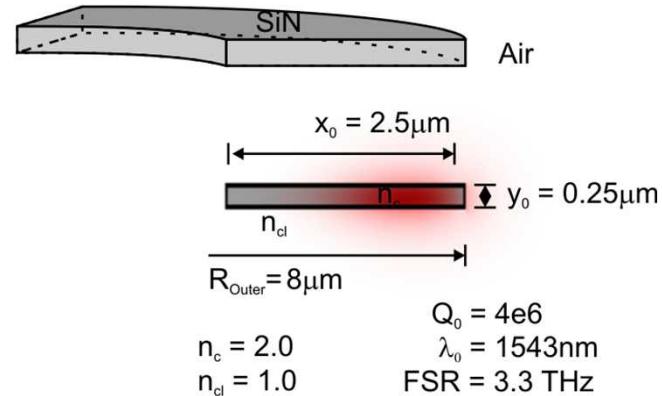


Thermal Design in Silicon Nitride

- Silicon nitride (200nm wide) tethers to minimize G
- ANSYS FEM predicts $G = 1.1 \times 10^{-7} \text{ W/K}$
- Thermal Time Constant $\tau \approx 2 \text{ ms}$
- Corresponding Phonon $NEP = 7 \times 10^{-13} \text{ W}/\sqrt{\text{Hz}}$

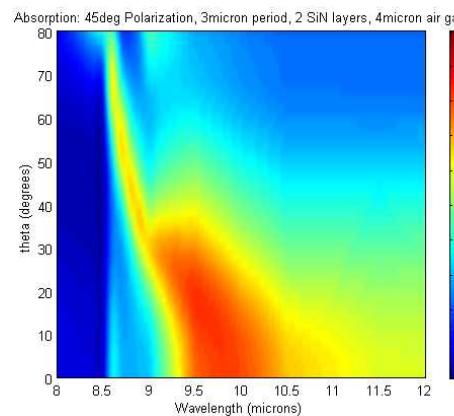
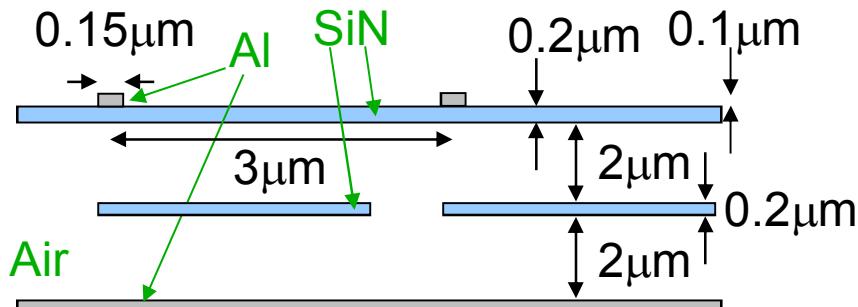
Microphotonic Design Considerations

- Sufficiently small bend radii ($R = 8 \mu\text{m}$)
- High-Q ($>10^5$) demonstrated in SiN (M. Shaw, Sandia)
- Sufficiently large thermo-optic response ($\Delta f \sim 2 \text{ GHz/K}$)
- No significant nonlinearities



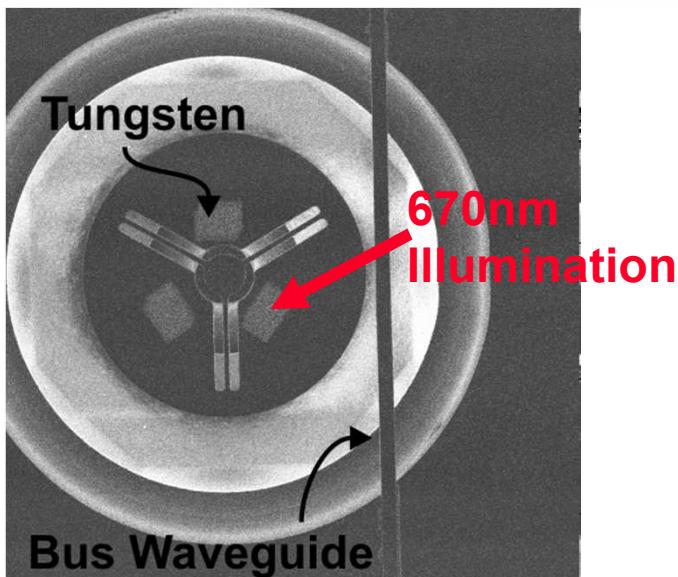
Antenna / Absorber Design (RCWA Analysis)

- Fortunately, silicon nitride absorbs from 9-12 μm

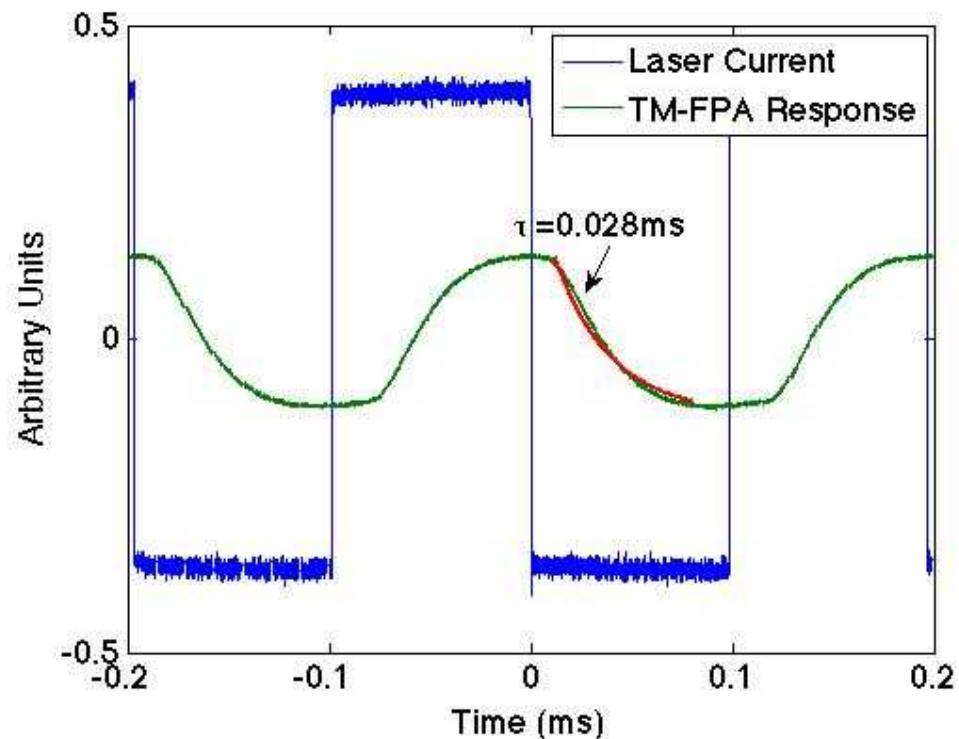


Initial Experimental Results

FIB Image of SiN Suspended Disk with Deposited Tungsten



Response to Illuminations by 670nm Laser



Preliminary Results

- Correct sign on thermo-optic shift
- Time Constant of $\sim 0.028\text{ms}$ indicating a conductivity of $G \sim 6 \times 10^{-6}$ (Limited by Air)
- Not yet prepared to comment on Signal-to-Noise Ratio



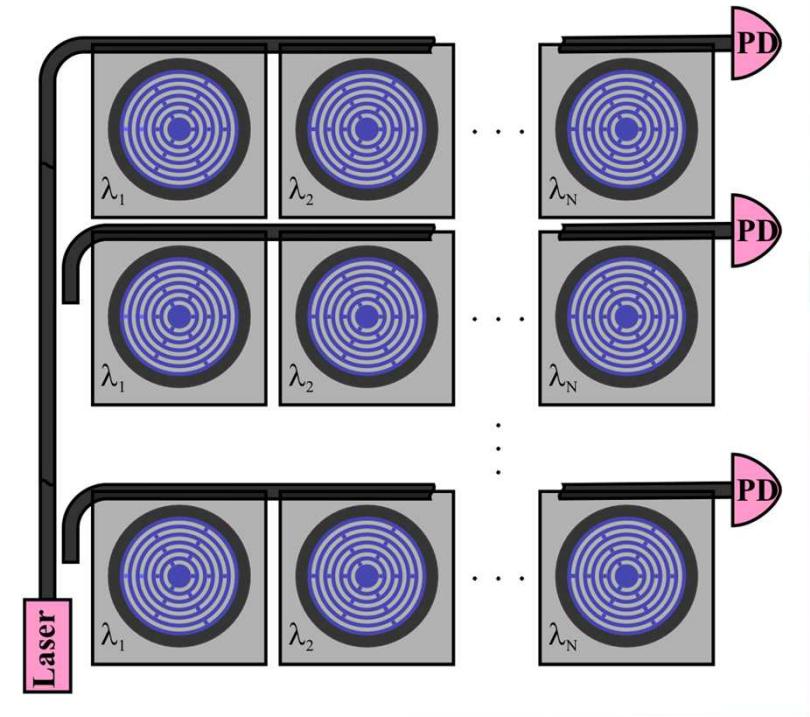
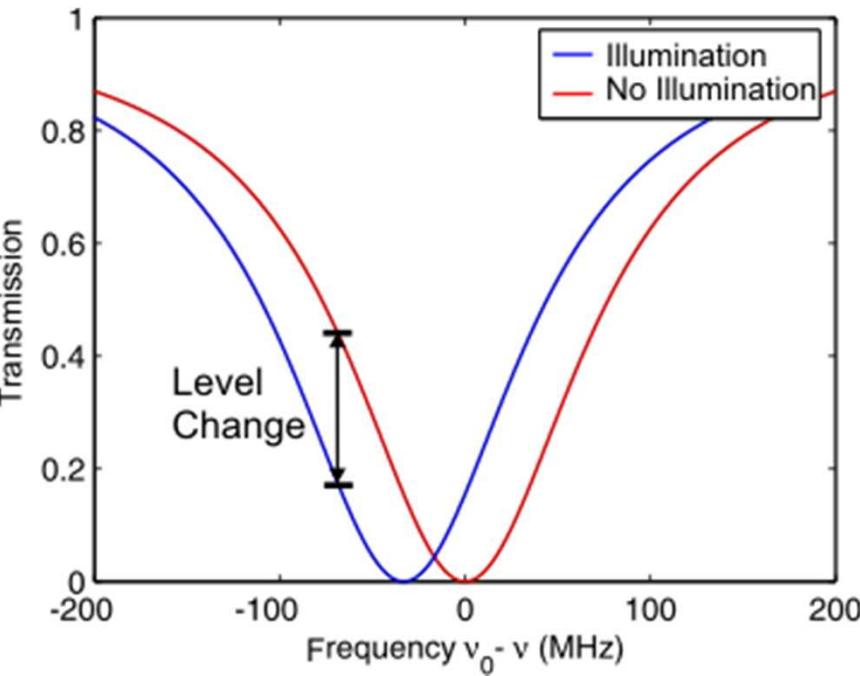


TM-FPA on a Large Scale

Like any Focal Plane Array, there is a desire to reach Millions of Pixels

- Approach: Use a WDM-based readout
- Is this reasonable?
- How do we model this in various states?
- Certainly, some challenges lie ahead to deal with complex VLSI microphotonic systems

Many Partially Overlapping Resonances





Summary and Conclusions

Design Approach

- ❑ Coupled Mode Theory for used for intuition
- ❑ 3D FD-TD / EME for electromagnetic simulations
- ❑ Transfer Matrix Method for large scale problems

Matching Numerical Models with Experiment

- ❑ Quite good on passive devices
- ❑ Active / multiphysics devices - not yet there
 - All domains simulated independently - very much imperfect
 - Quantum fluctuations not captured

Future Needs

- ❑ Need for multiphysics codes (electromagnetic, thermal, mechanical, electrical etc.)
 - Nice to see a time domain code with all effects captured & statistical noise sources
- ❑ Need for object oriented transfer matrix code for VLSI with device library capability

