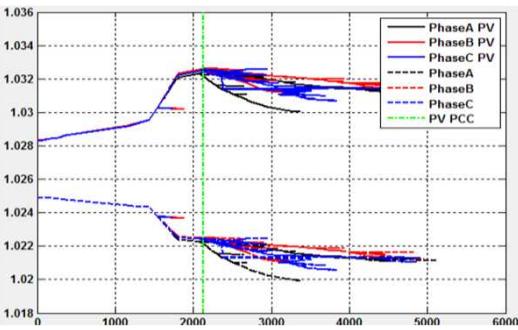
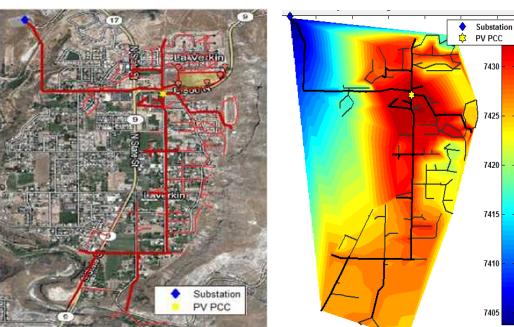


# Evaluation of Reactive Power Control Capabilities of Residential PV in an Unbalanced Distribution Feeder



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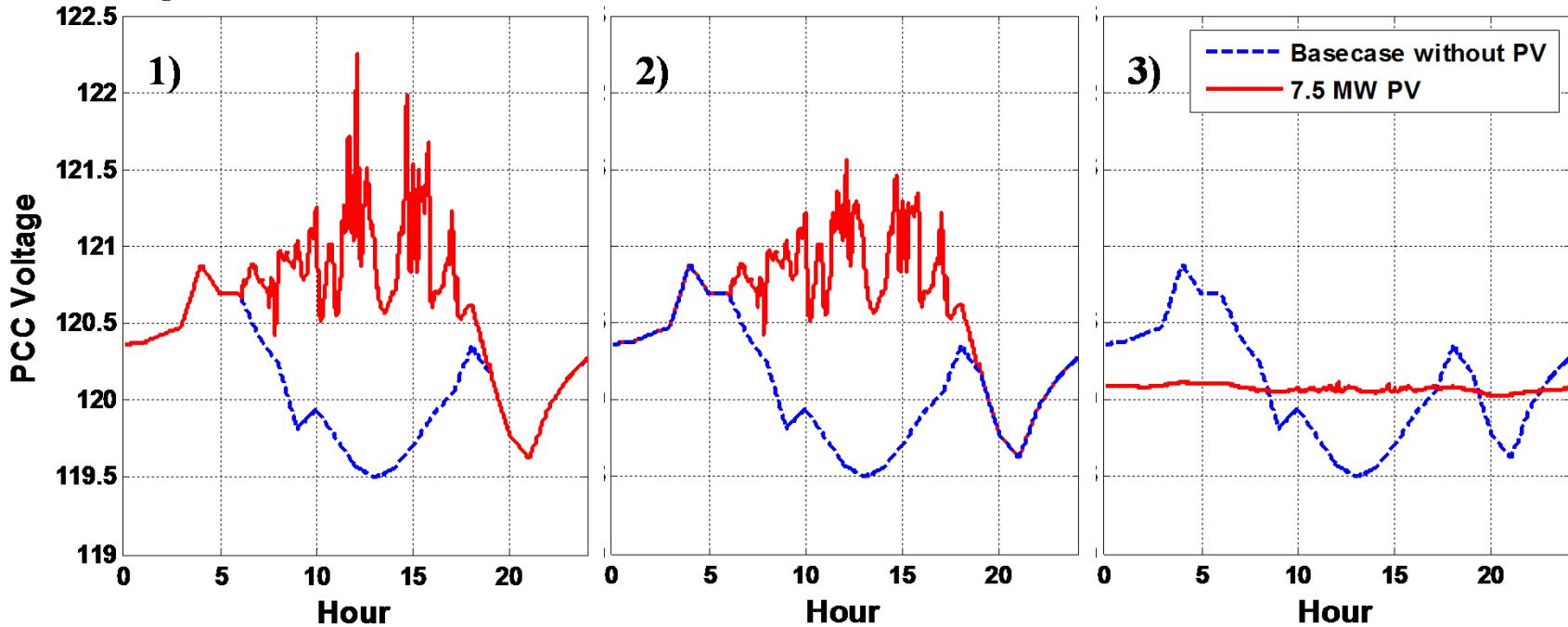
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# Outline

- Introduction
- Optimal dispatch of reactive power
- Results
- Analysis
- Conclusions / Future Work

# Motivation for Work

- Voltage violations on distribution feeders due to large scale PV deployment is becoming a problem
  - PV inverter reactive power can help mitigate this



- What is the capability of PVs to perform voltage regulation?

# Optimization Problem

- The general formulation of the problem is:

$$\min_{\mathbf{u}} J(\mathbf{x}, \mathbf{u}) = w_1 \sum_{i=1}^n (V_i - V^*)^2$$

$$s.t. \quad \mathbf{G}(\mathbf{x}, \mathbf{u}, \mathbf{d}) = 0$$

$$|u_i| \leq q_i^{g,max}(t)$$

Losses term is  
needed for  
uniqueness of  
solution

$$L_j = r_j |I_j|^2$$

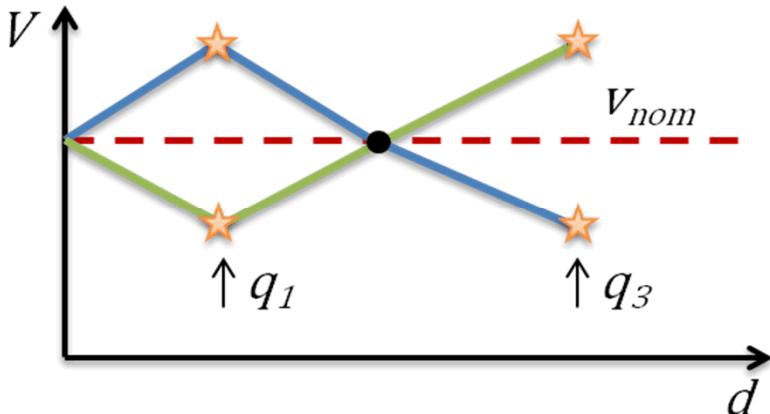
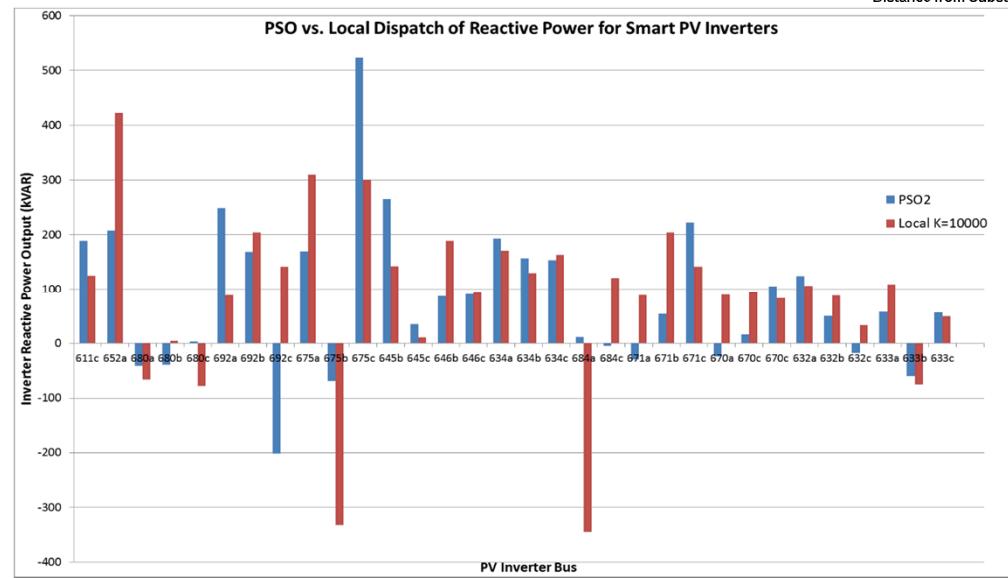
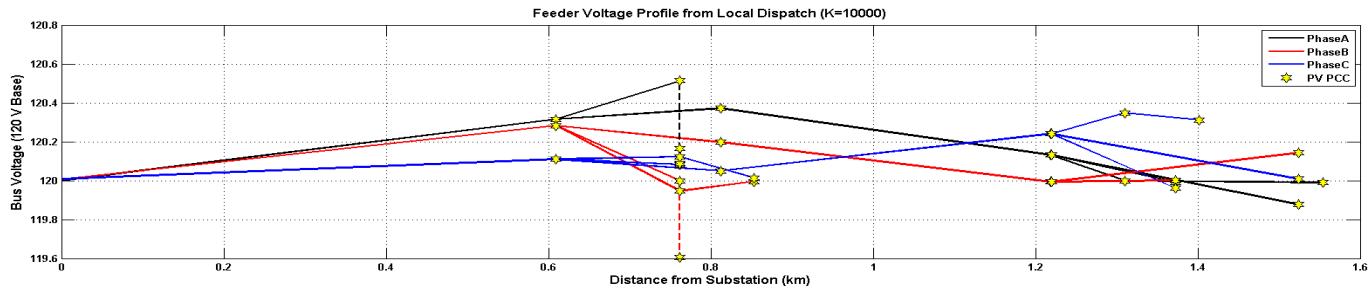
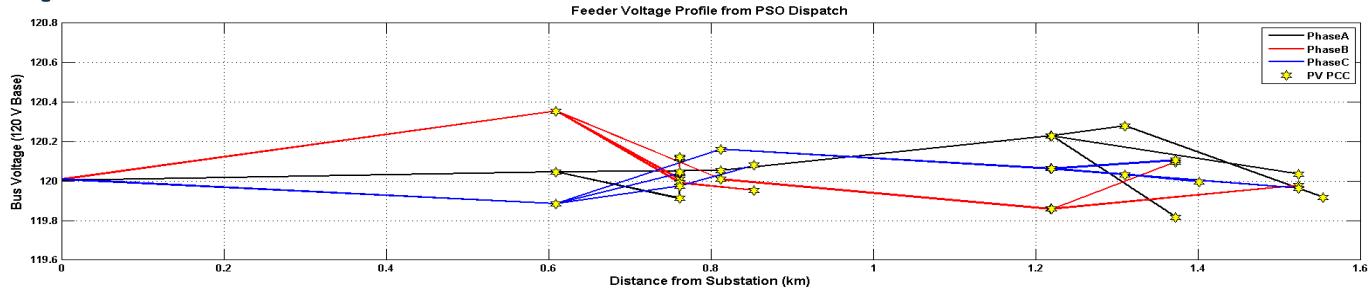
- Some key assumptions:

- Unbalanced, three-phase feeder
- No inverter power factor limitations
- Watt priority control:

$$p_i^g(t) = S_i^{rated} I(t)$$

$$q_i^{g,max}(t) = \sqrt{(S_i^{rated})^2 - (p_i^g(t))^2}$$

# Uniqueness of Solution



# Nonlinear Solution

- Solution via PSO algorithm:

$$\mathbf{u}_i(k) = \mathbf{u}_i(k-1) + \mathbf{v}_i(k)$$

$$\mathbf{v}_i(k) = \gamma \mathbf{v}_i(k-1) + \varphi_1 \text{rand}_1[\mathbf{p}_i(k) - \mathbf{u}_i(k-1)] + \varphi_2 \text{rand}_2[\mathbf{g}(k) - \mathbf{u}_i(k-1)]$$

$$\mathbf{p}_i(k) = \operatorname{argmin}_{\mathbf{u}_i} \left( \tilde{J} \right), \forall k \quad \mathbf{g}(k) = \operatorname{argmin}(\mathbf{p}_i), \forall k$$

- To handle inequality constraints:

$$\min_{\mathbf{u}} \tilde{J}(\mathbf{x}, \mathbf{u}) = J(\mathbf{x}, \mathbf{u}) + \rho \sum_k^p \varphi_k(u_k)$$

$$\varphi_j(u_j) = \begin{cases} 0, & |u_j| \leq q_j^{g,\max}(t) \\ \mu + \frac{|u_j|}{q_j^{g,\max}(t)}, & \text{otherwise} \end{cases}$$

# Linearized Solution

- $G(x, u)$  can be linearly approximated:

$$\begin{aligned} P_{j+1} &= P_j + \Delta p_{j+1} \\ Q_{j+1} &= Q_j + q_{j+1}^c - q_{j+1}^g \\ V_{j+1} &= V_j - r_j P_j - x_j Q_j \end{aligned}$$

- Updated objective function:

$$\hat{J} = J(x, u) + \lambda^T G(x, u, d)$$

$$L_j(x) \approx \frac{r_j}{V_0^2} (P_j^2 + Q_j^2)$$

- Solution must satisfy:

$$\left[ \frac{\partial \hat{J}}{\partial u}, \frac{\partial \hat{J}}{\partial \lambda} \right]^T = [0, 0]^T$$

# Linearized Solution (cont.)

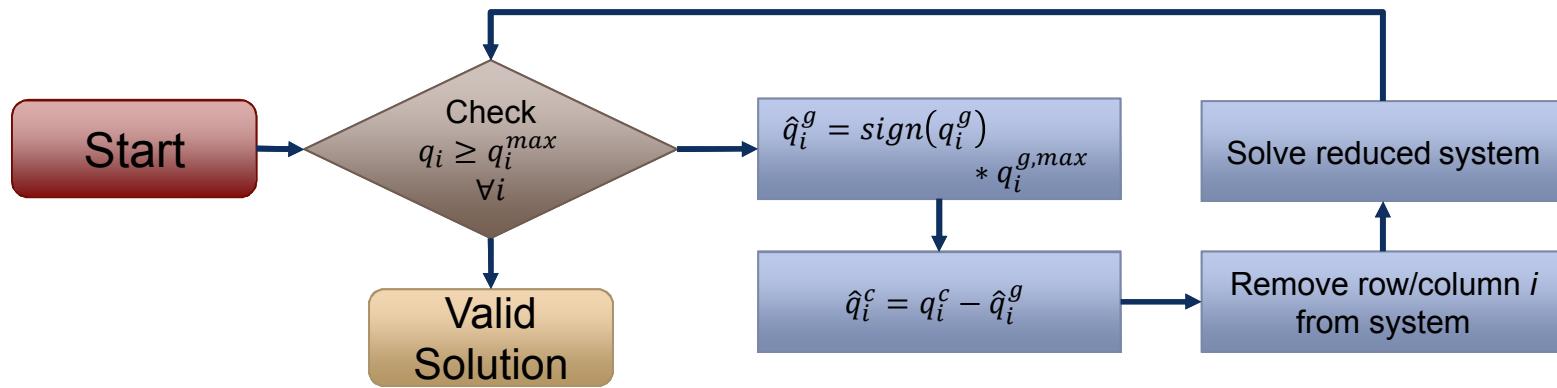
- Linearized solution:

$$\begin{bmatrix} \mathbf{u} \\ \mathbf{P} \\ \mathbf{Q} \\ \mathbf{V} \end{bmatrix} = \begin{bmatrix} 0 & 0 & \mathbf{R} & \mathbf{S} \\ 0 & \mathbf{I} - \mathbf{N} & 0 & 0 \\ \mathbf{U} & 0 & \mathbf{I} - \mathbf{N} & 0 \\ 0 & \text{diag}(\mathbf{r}_i) & \text{diag}(\mathbf{x}_i) & \mathbf{I} - \mathbf{N}^T \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{T} \\ \Delta \mathbf{p} \\ \mathbf{q}^c \\ \mathbf{V}_n \end{bmatrix}$$

$$\mathbf{R} = \{[(\mathbf{I} - \mathbf{N})^{-1} \mathbf{U}] \circ [\mathbf{r} \mathbf{1}^T]\}^T$$

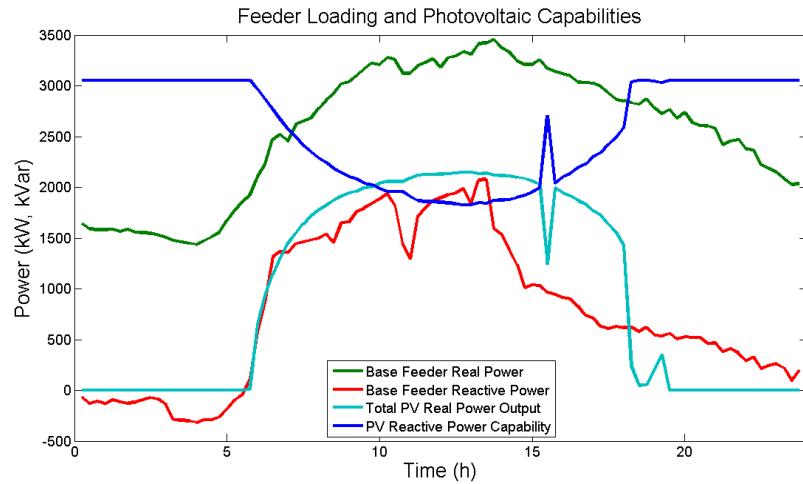
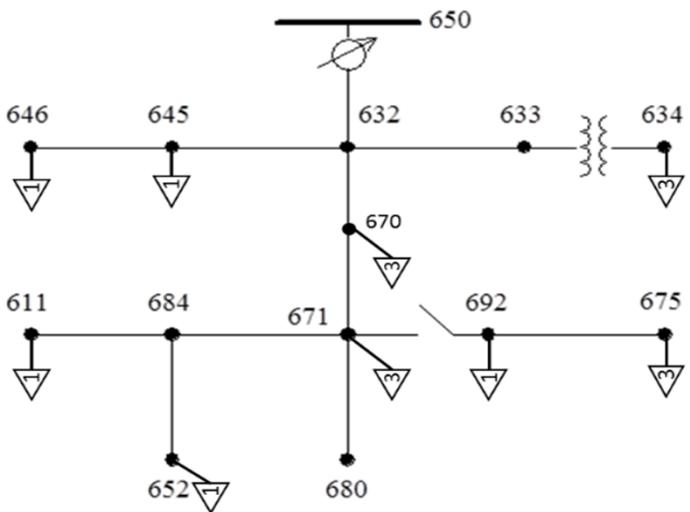
$$\mathbf{S} = (\text{path}_i \cap \text{path}_j) \cdot 2x$$

$$\mathbf{T} = \sum_i (\text{path}_i \cap \text{path}_j) \cdot 2x$$

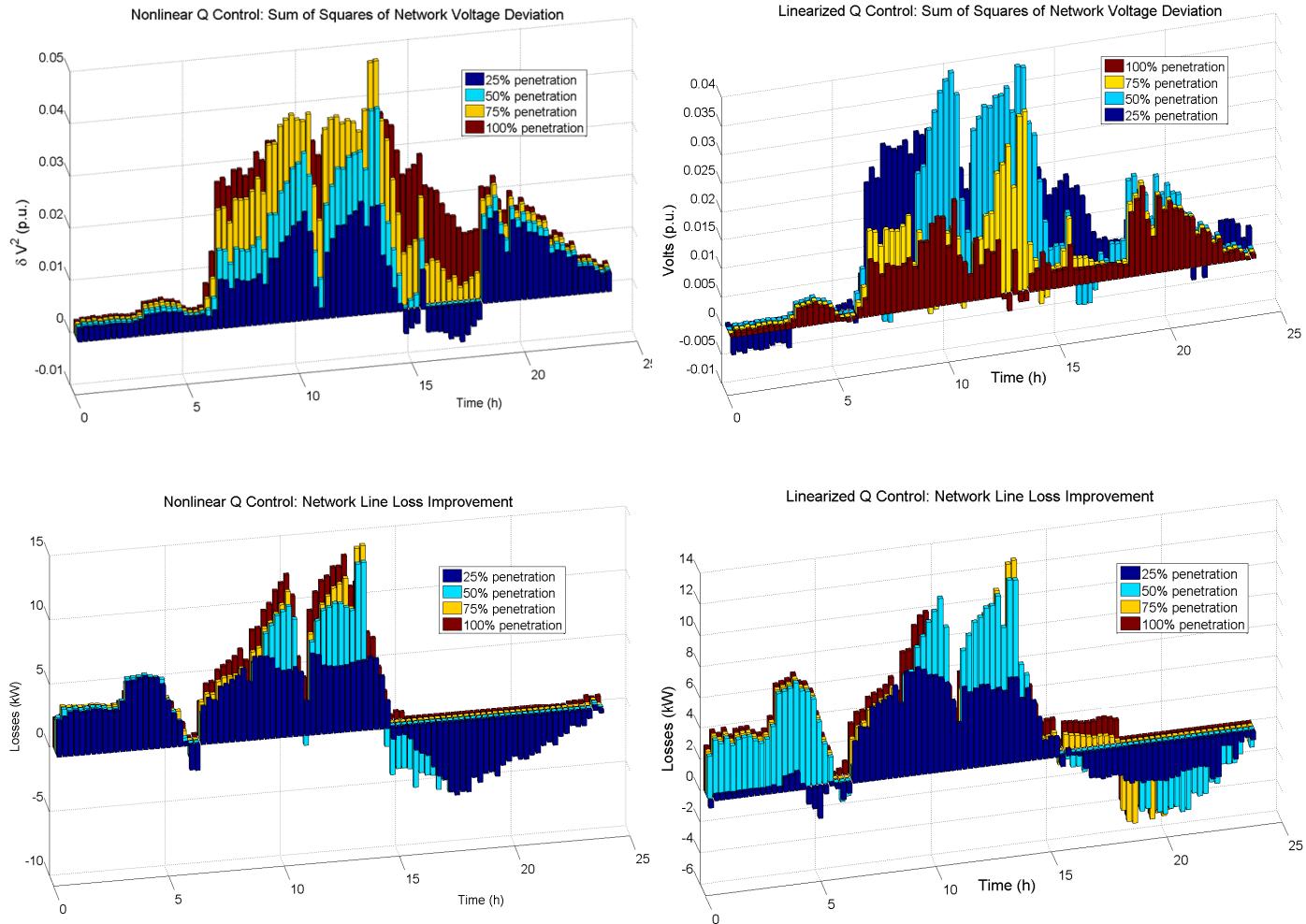


# Study Feeder

- IEEE 13-bus feeder
  - 3-phase, 4kV distribution feeder
  - 4.05 MVA peak load
  - 2 cap banks at Bus 675 and 611
  - Single voltage regulator sets Bus 632 to  $1.0V_{pu}$  for all simulations
- PVs placed at each load, sized as a percent of local peak load based on penetration
  - $S_{PV,i}^{rated} = penetration * S_{load,i}^{peak}$
- Real and reactive load and solar insolation each scaled by separate daily curves of 15 min. intervals



# Results



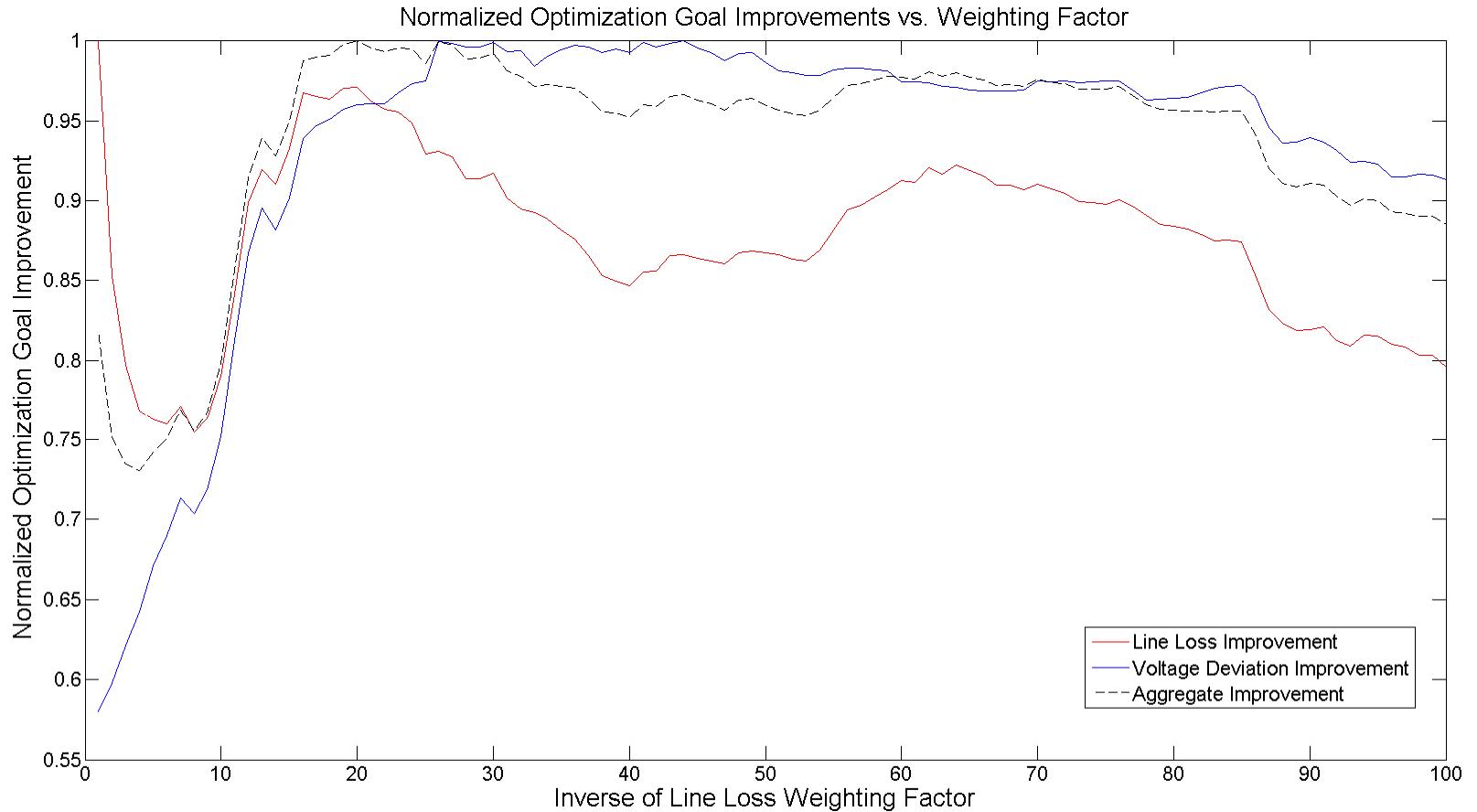
Optimization Improvement over Base Case (no Q control)

# Analysis of Results

	Nonlinear PSO Optimization	Linearized Optimization	Local VAR Matching
<b>Sum of Line Loss Improvements</b>	890.3kW	719.9kW	368.7kW
<b>Avg. Node Voltage Improvement (120V base)</b>	3.11V	2.47V	2.57V
<b>Computation Time (seconds)</b>	54,639.51	7.69	7.02

- Nonlinear optimization is clearly the most accurate
  - Not adequate for running thousands of PV placement studies on large, realistic feeders
- Linearized approximation is orders of magnitude faster than nonlinear solution, with only about a 20% reduction in result accuracy

# Analysis of Results



**Linearized Objective Sensitivity to Weighting Factor Ratio  $w_1/w_2$**

# Conclusions / Future Work

- Demonstrated
  - Linearized approximate dispatch can be used to quickly gauge a feeder's PV reactive power benefits
- Future:
  - More complex feeders investigated under varying conditions
  - Test a large number of PV placement scenarios
  - Compare benefit of dispatched reactive power to local control of reactive power

# Thank you