

Effect of Cylindrical Inclusions on the Strength Distributions of Brittle Materials

Rajan Tandon

Materials Reliability Department

Sandia National Laboratories, Albuquerque, NM 87185

**Sandia is a multiprogram laboratory operated by Sandia Corporation, a Lockheed Martin Company,
for the United States Department of Energy's National Nuclear Security Administration
under contract DE-AC04-94AL85000.**

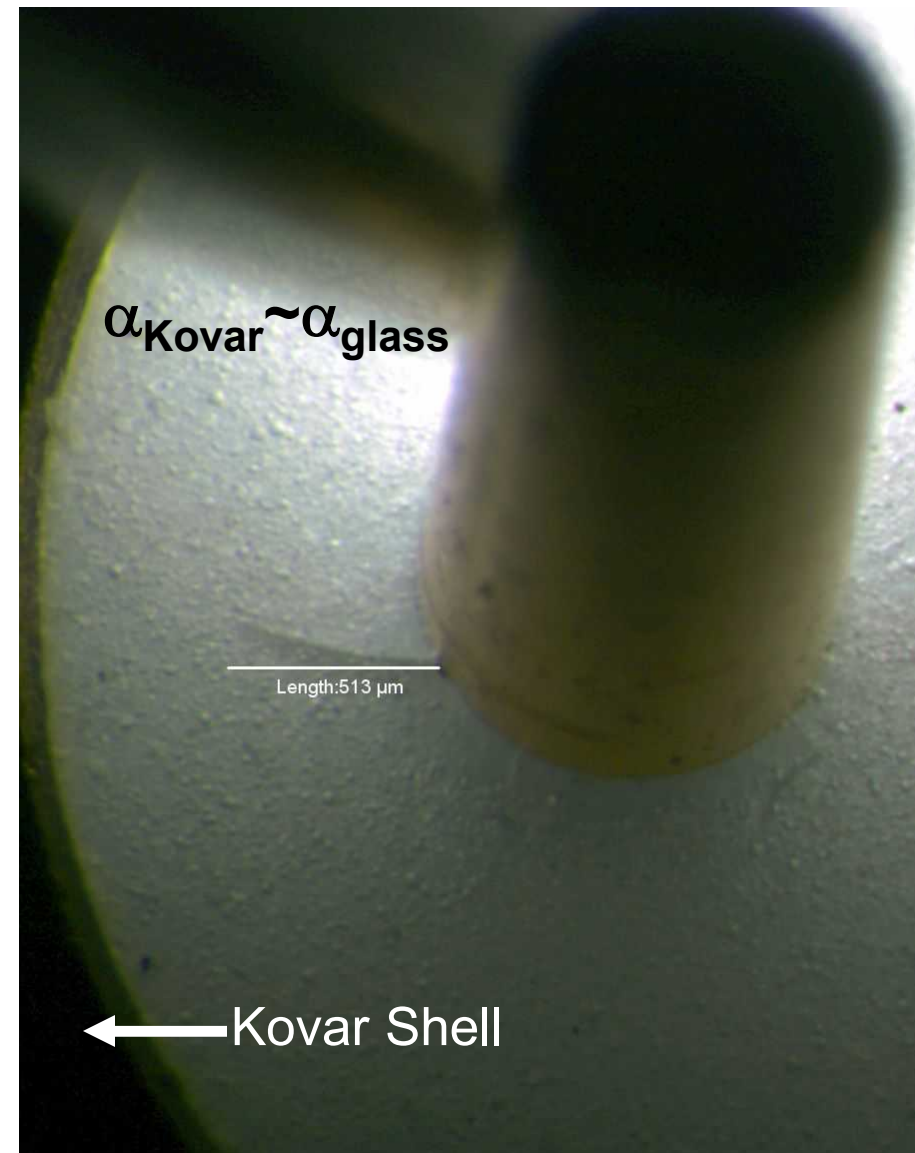
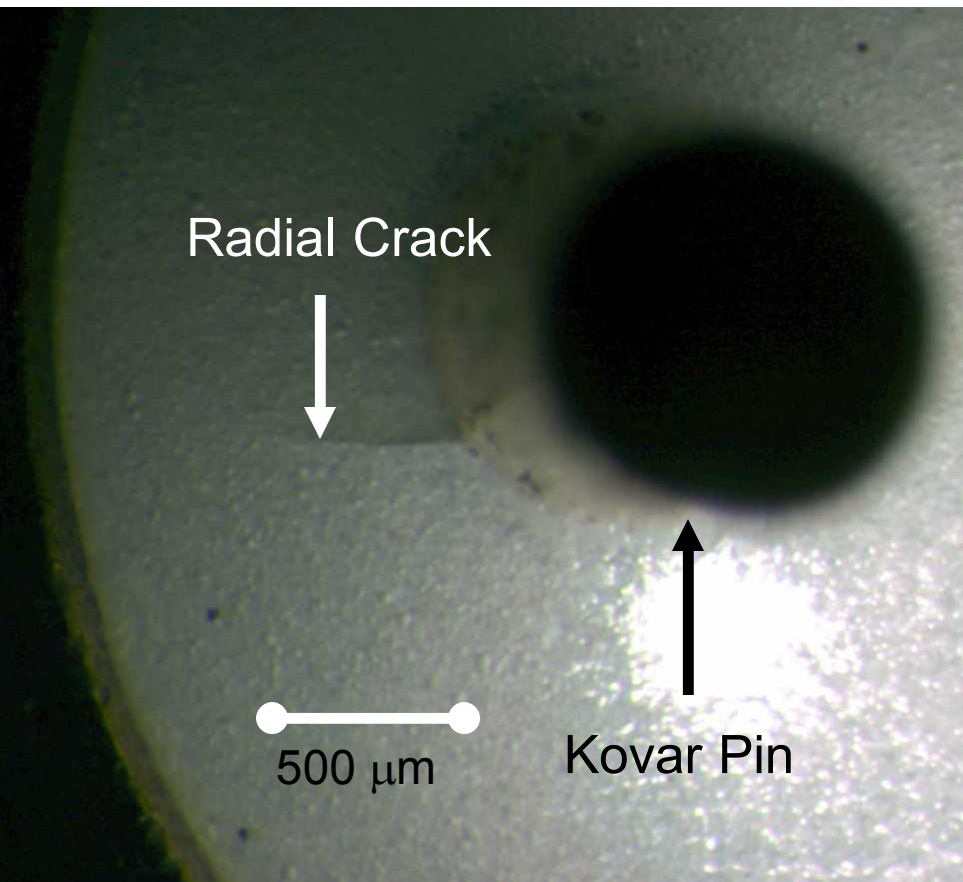


Outline

- **Rationale**
Examples of failures from cylindrical inclusions
 - **Impact on SCG ?**
- **Fracture Mechanics Analysis**
 - **Describe behavior of radial cracks**
- **Effect on Strength Variability**
- **Considerations for Design of Material Systems**

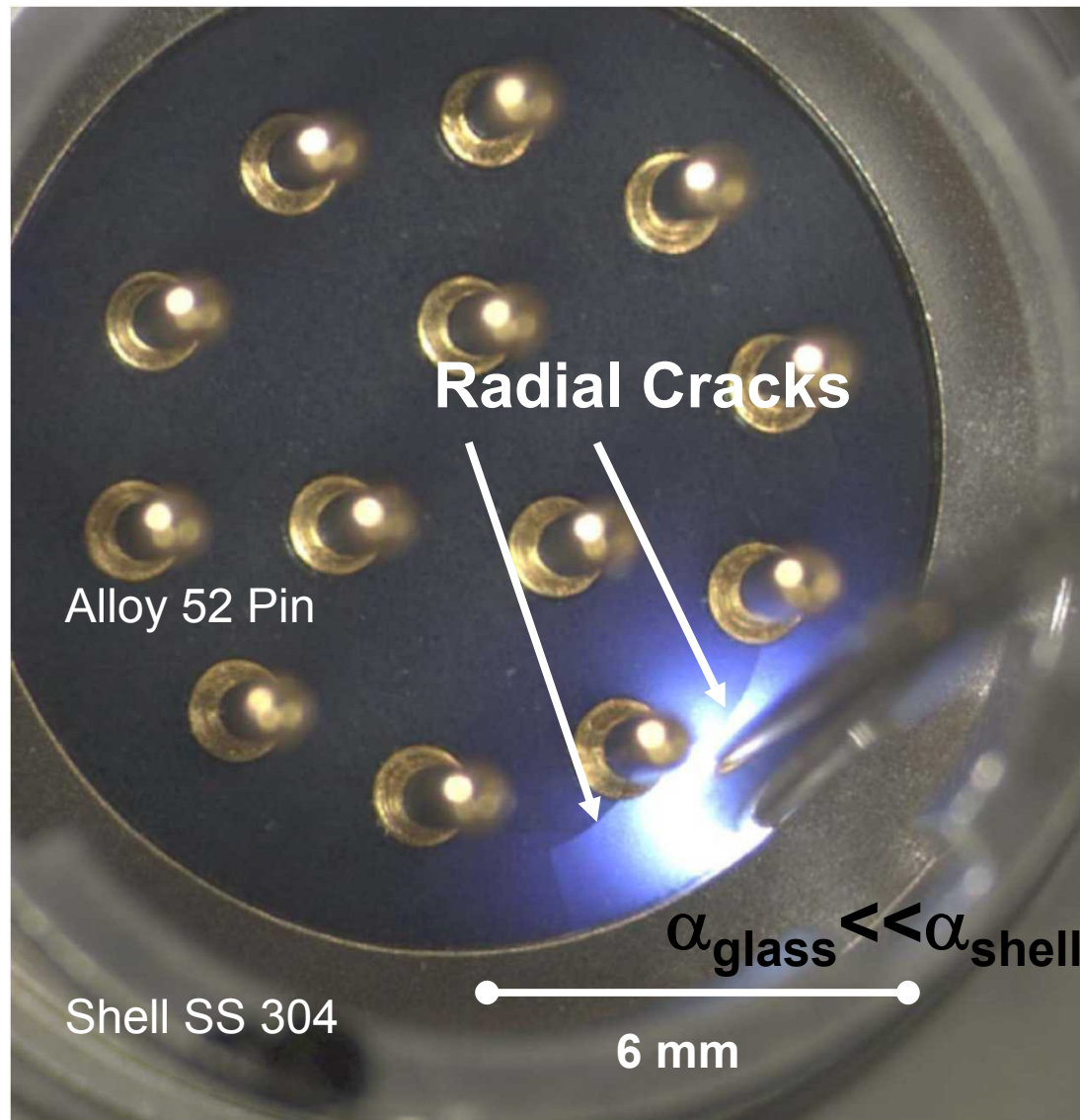


Crack at Pin in a Glass-to-Metal Seal



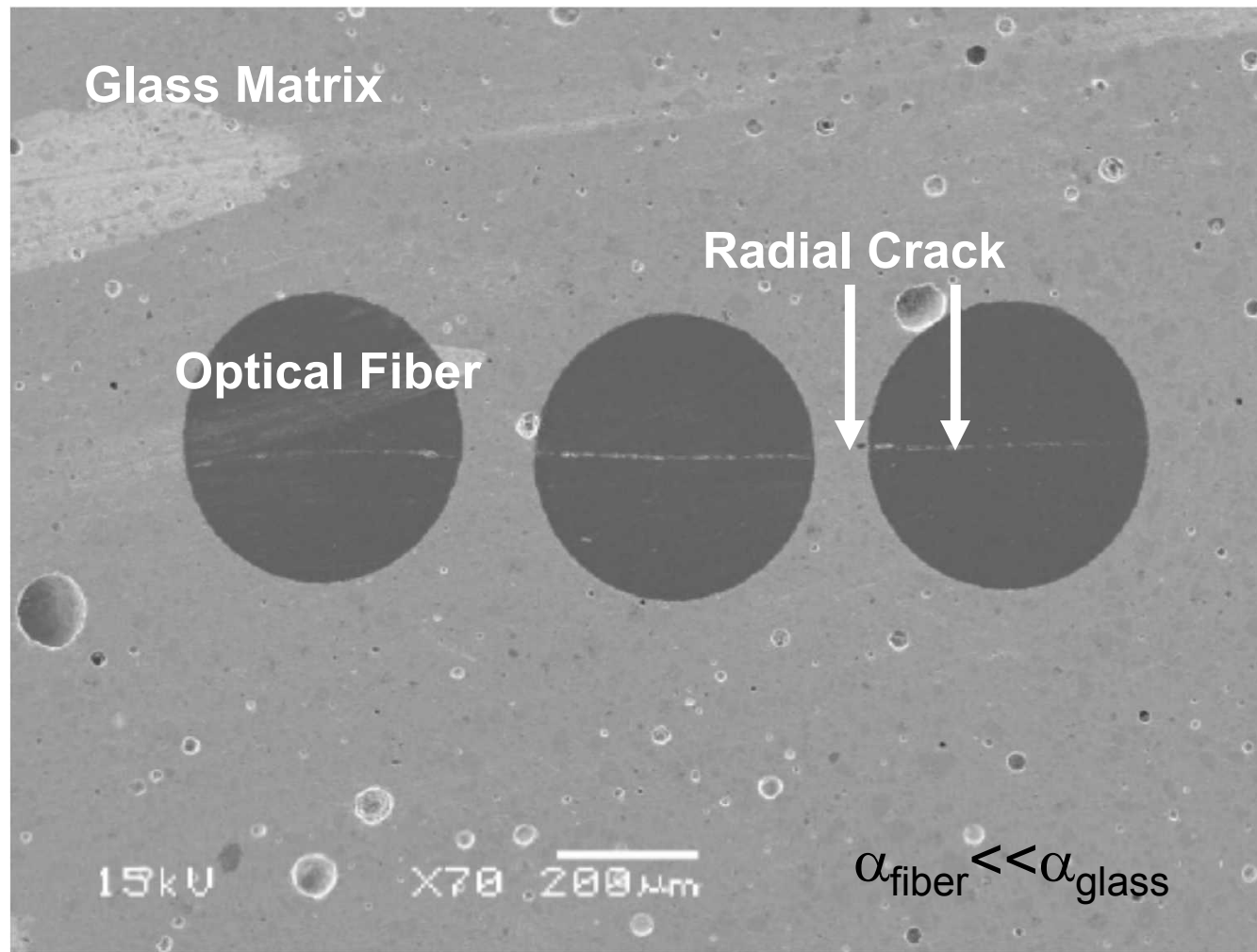
- Electrical breakdown issue

Cracks in Multi-Pin Glass-to-Metal Seal



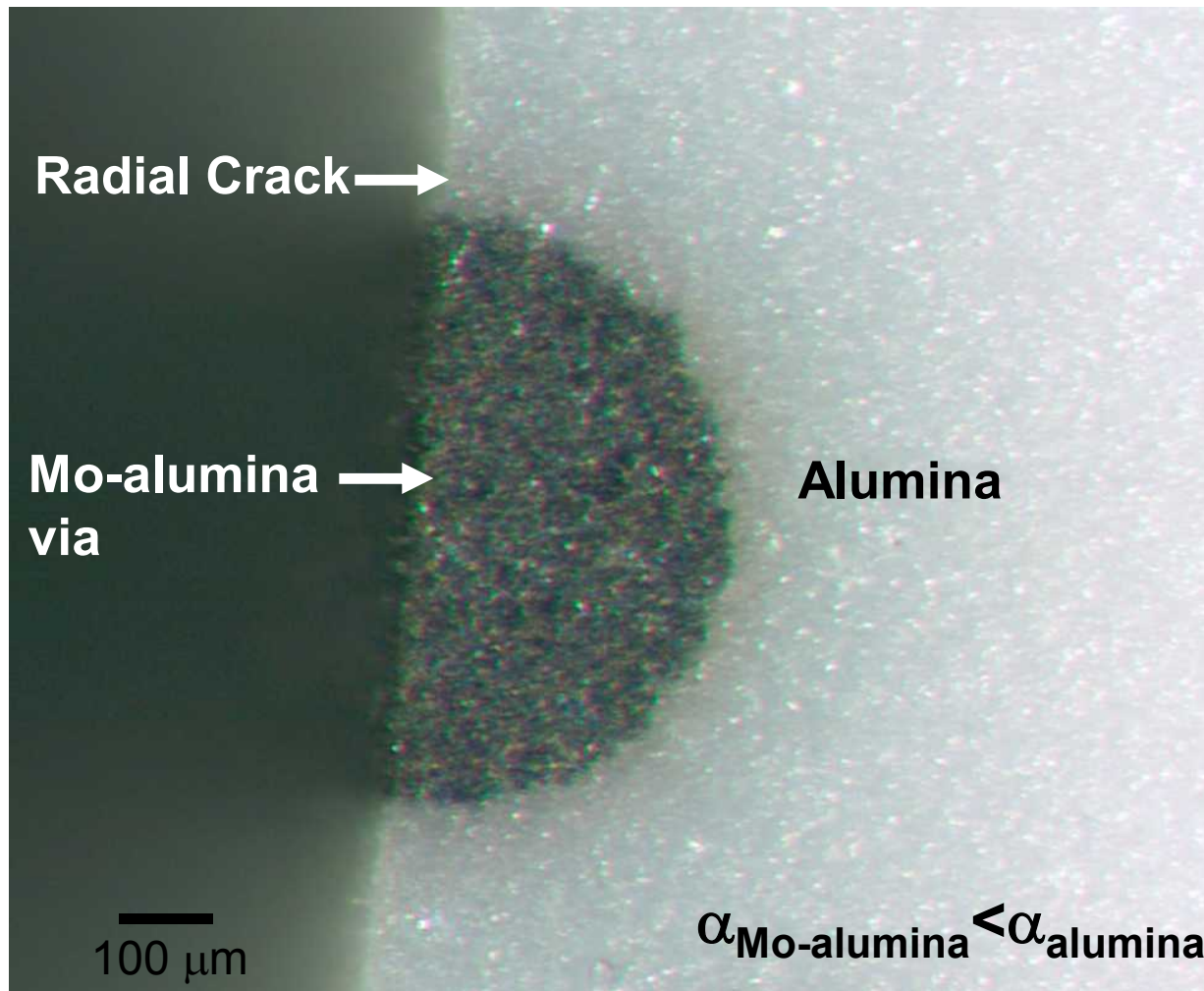
- Hermeticity and electrical breakdown issues

Radial Cracks Within and Outside fiber



- Loss of power-transmission functionality

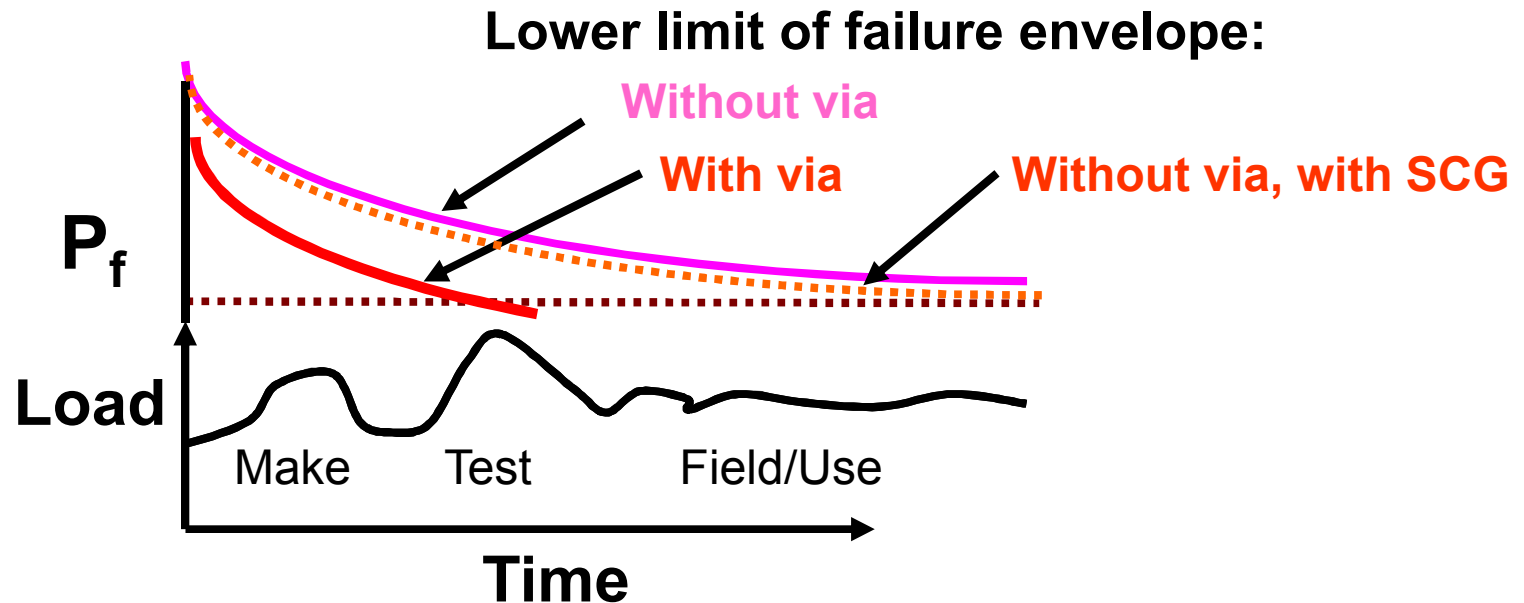
Radial Crack at Via in Packaging Material



- Strength testing reveals radial cracking at via to be failure mechanism

Stress Fields Around Vias Influence Fracture Behavior

A. Effect on strength variability of components ?



B. Failure envelopes degrade with time due to SCG . How does this stress field impact lifetime predictions of components ?

Fracture Mechanics Description

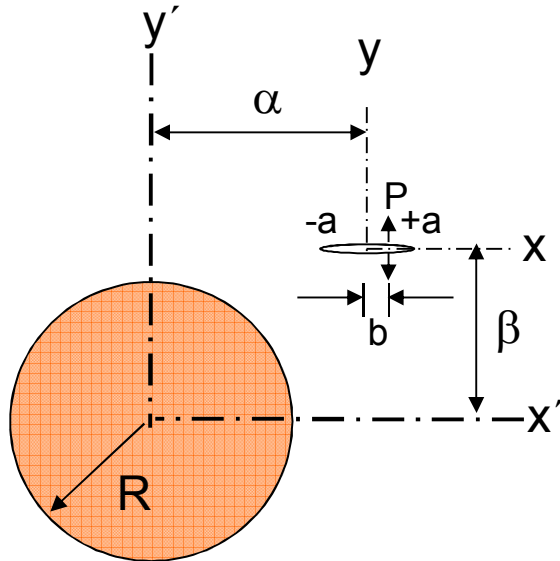
Stress due to inclusion acting on crack

$$\sigma_{\theta\theta} = -\sigma_{rr} = \Lambda T_{diff} \left(\frac{R}{r} \right)^2$$

where

$$\Lambda = \frac{E_m E_i [\eta_m (1 + \nu_m) - \eta_i (1 + \nu_i)]}{E_i (1 + \nu_m) + E_m (1 - \nu_i - 2\nu_i^2)}, \text{ and } \Lambda = \frac{E_m E_i (\eta_m - \eta_i)}{E_i (1 + \nu_m) + E_m (1 - \nu_i)}$$

for plane strain, and plane stress respectively.

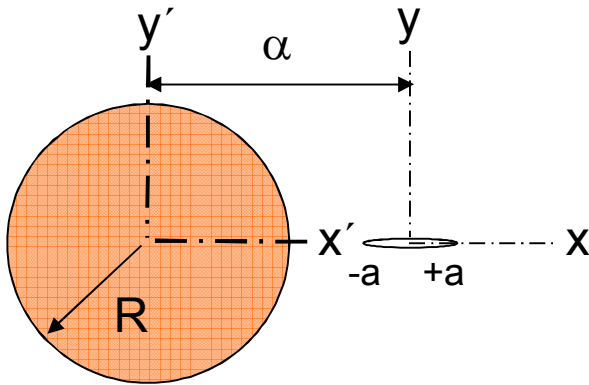


Point force solution acting on crack

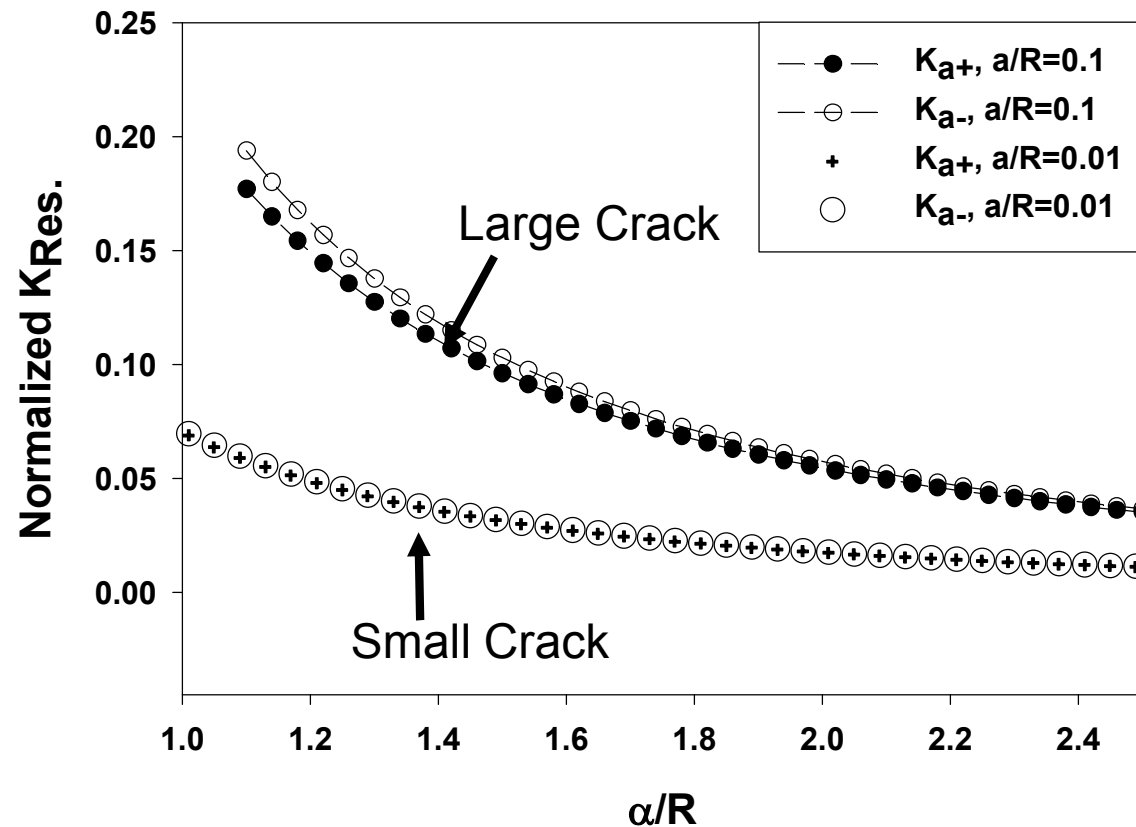
$$K_{Res.}|_{\pm a} = \frac{1}{\sqrt{\pi a}} \int_{-a}^{+a} \left(\Lambda T_{diff} R^2 \frac{[(x + \alpha)^2 - (y + \beta)^2]}{[(x + \alpha)^2 + (y + \beta)^2]^2} \right) \sqrt{\frac{a \pm x}{a \mp x}} dx$$

Does not include effect of crack on the inclusion
Does not include stresses due to elastic mismatch

Simplification: $\beta=0$



$$K_{\text{Res.}}|_{\pm a} = \frac{\Lambda T_{\text{diff}} R^2 \sqrt{\pi a}}{(\alpha \pm a) \sqrt{\alpha^2 - a^2}}$$

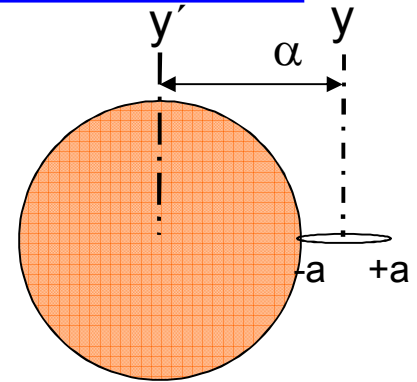


$$K_{-a} > K_{+a}$$

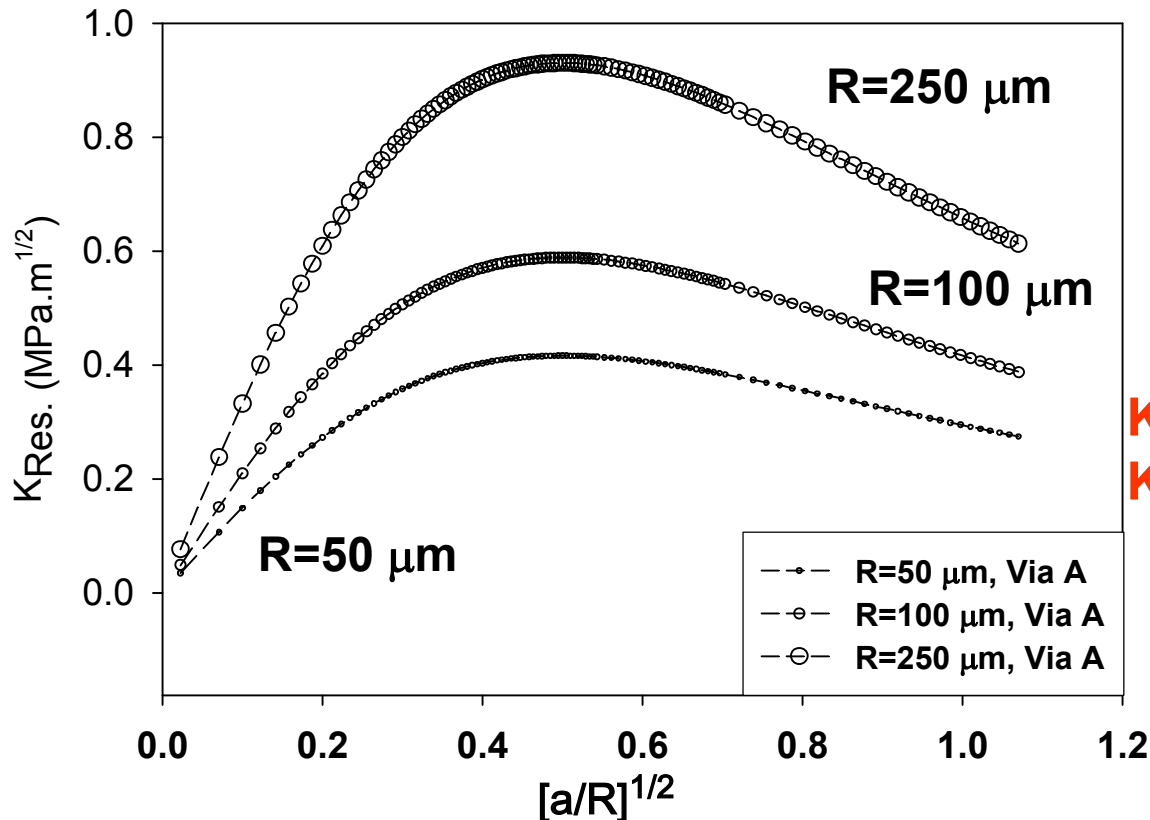
ΔK increases as $\alpha \rightarrow R$

Simplification: $\alpha = R + a$

If $K_{-a} > K_{1c}$, $-a$ tip jumps to inclusion; arrests
Jump likely on external stress application



Results for Materials Systems of Interest



Matrix: Alumina
Via A: Cermet =
Mo + alumina

K_{Res} has a maximum
 K_{Res} increases with radius

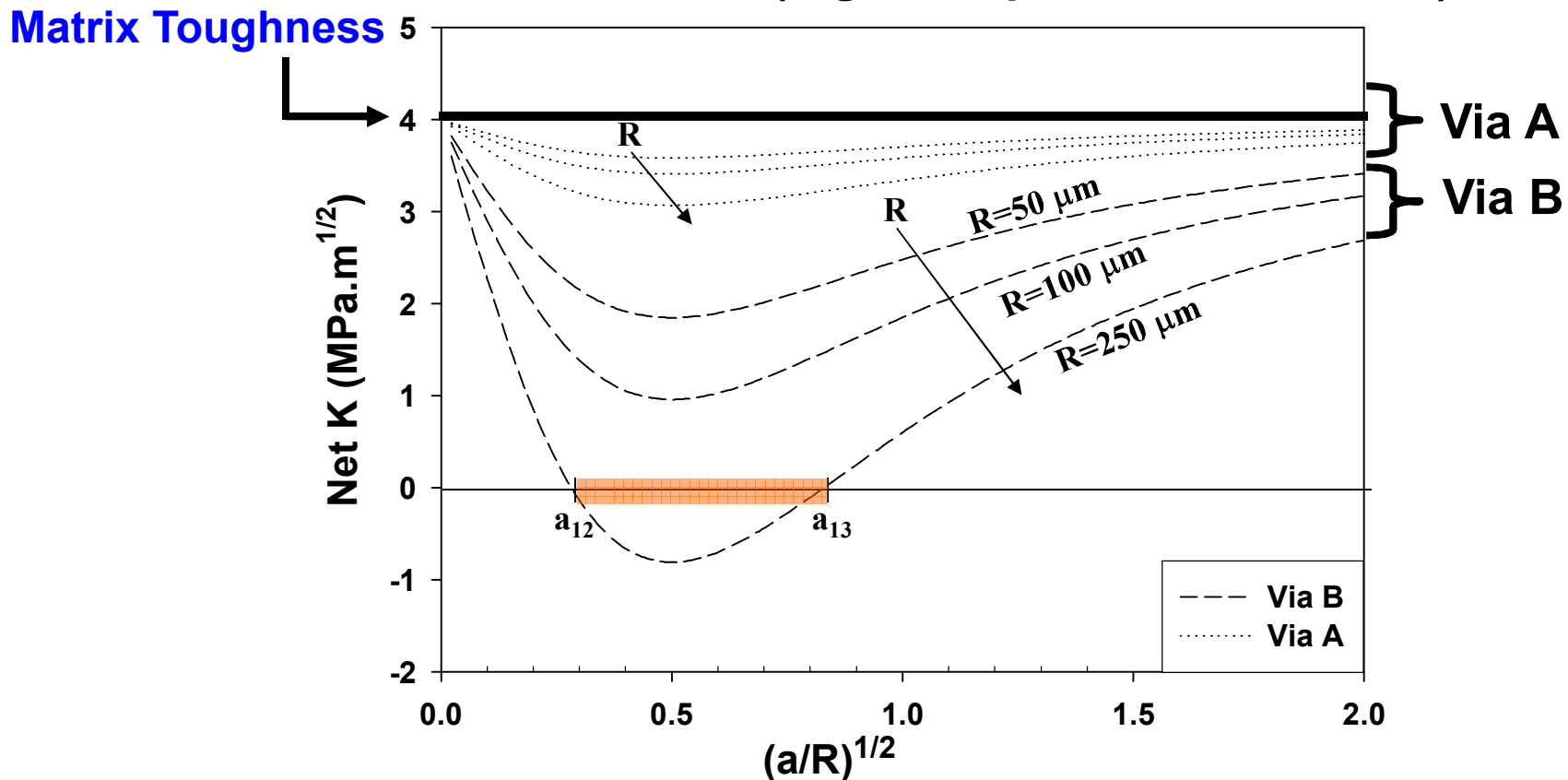
Destabilizing-Stabilizing Fields

Net K = **Matrix Toughness** - $K_{\text{Res.}}$ due to inclusion

RESULTS FOR TWO VIA MATERIALS

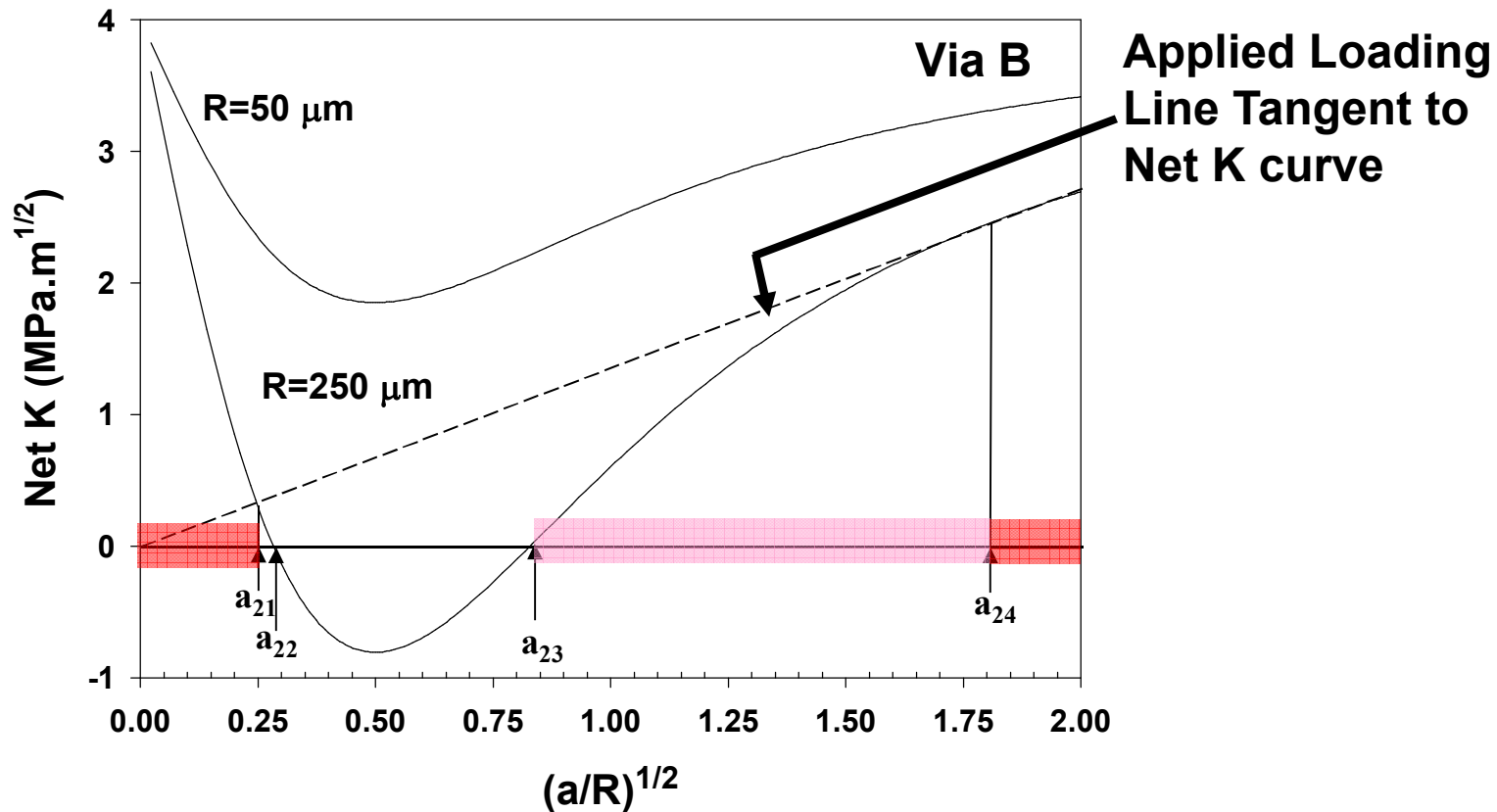
Via A: Mo-alumina

Via B: Pure Mo (higher expansion mismatch)



For largest via, Via B, cracks $a_{12} < a < a_{13}$ grow spontaneously to a_{13}

Behavior of crack at R=250 μm , Via B under Applied Tension

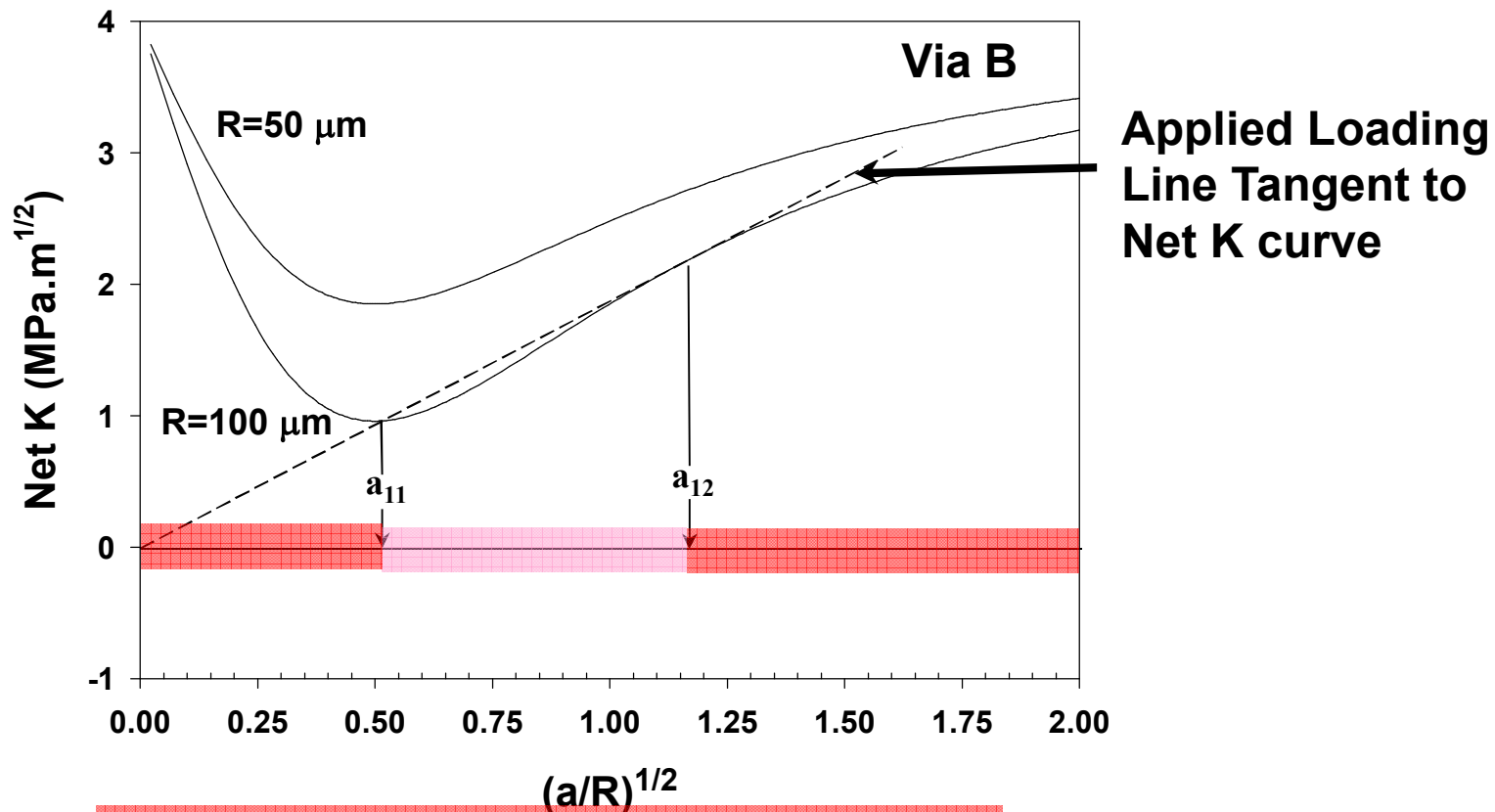


$a_{21} < a$: Unstable fracture; failure at a

$a_{23} < a < a_{24}$: Stable crack growth, failure at a_{24}

$a > a_{24}$: Unstable fracture; failure at a

Behavior of crack at R=100 μm , Via B under Applied Tension



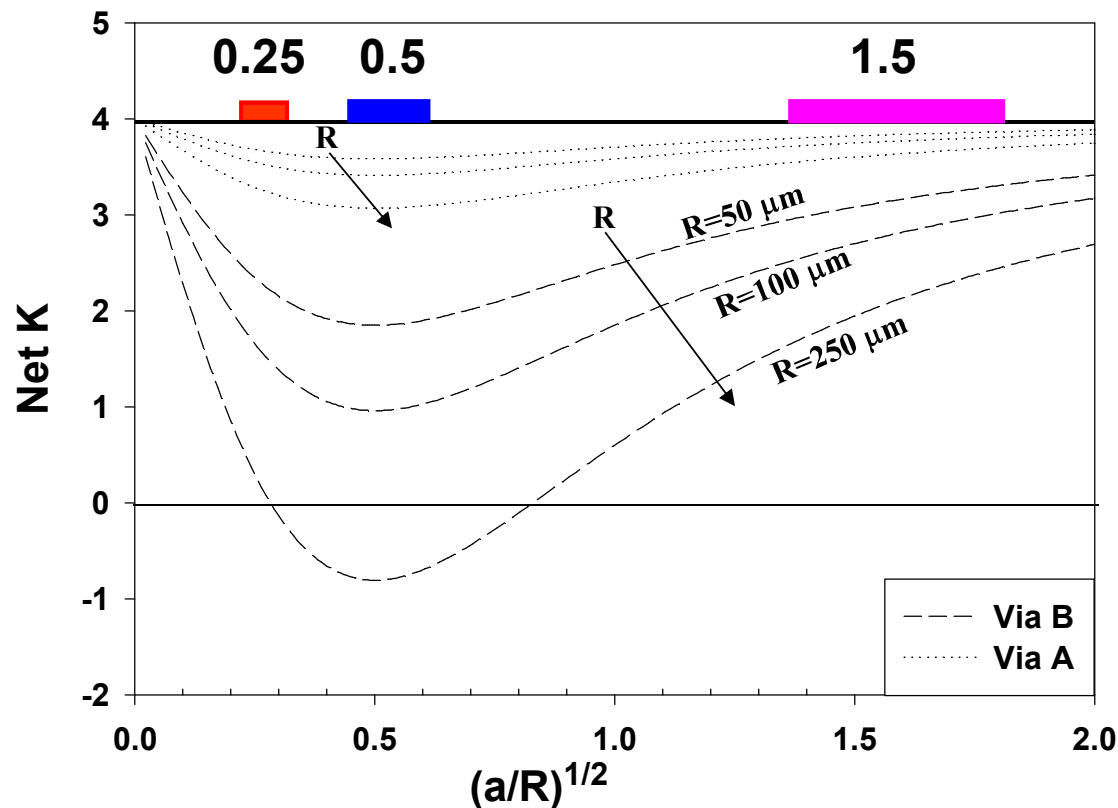
$a_{11} < a$: Unstable fracture; failure at a

$a_{11} < a < a_{12}$: Stable crack growth, failure at a_{12}

$a > a_{12}$: Unstable fracture; failure at a

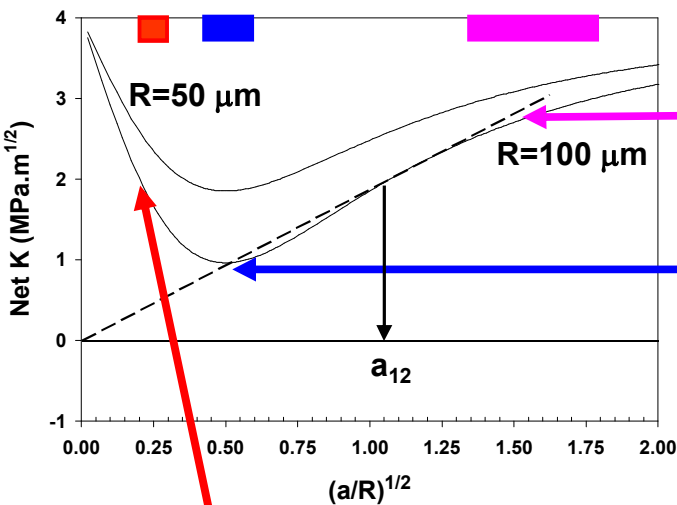


Effect on Strength Variability



Generated crack size distributions centered at various a/R locations such that the Weibull moduli=20 for each distribution on the base material

Strength Variability: $R=100\text{ }\mu\text{m}$

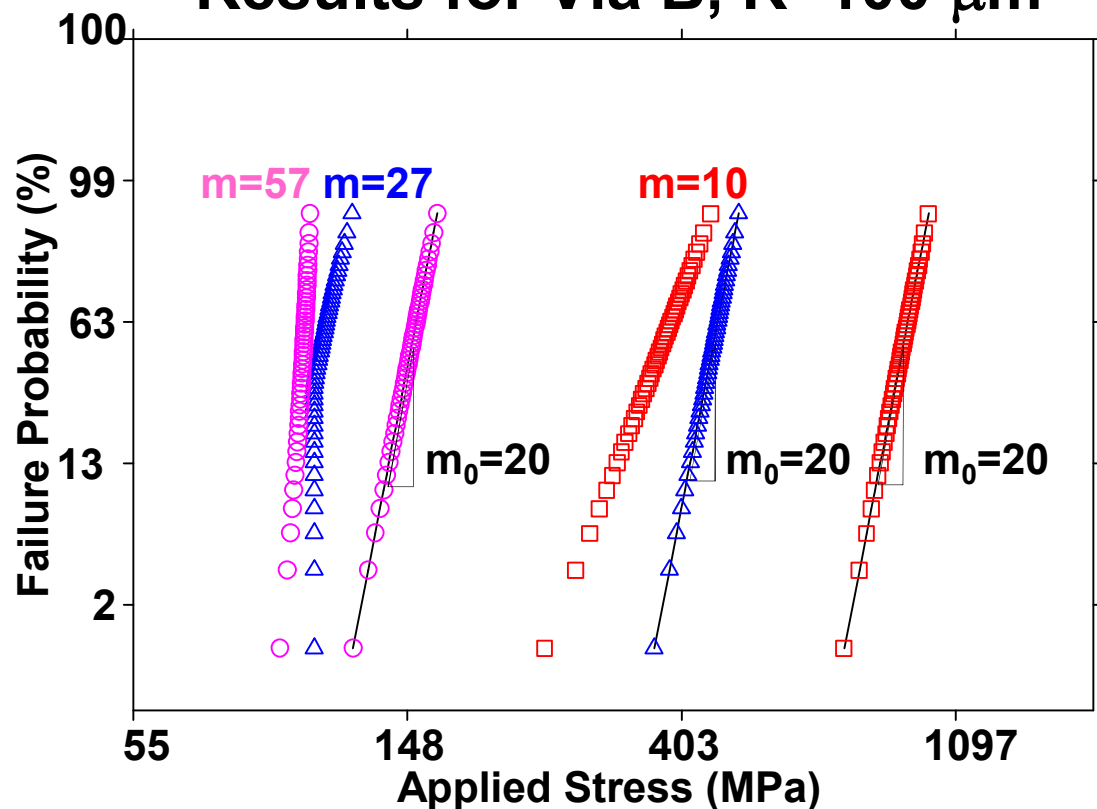


All Cracks in this set: Stabilizing Field

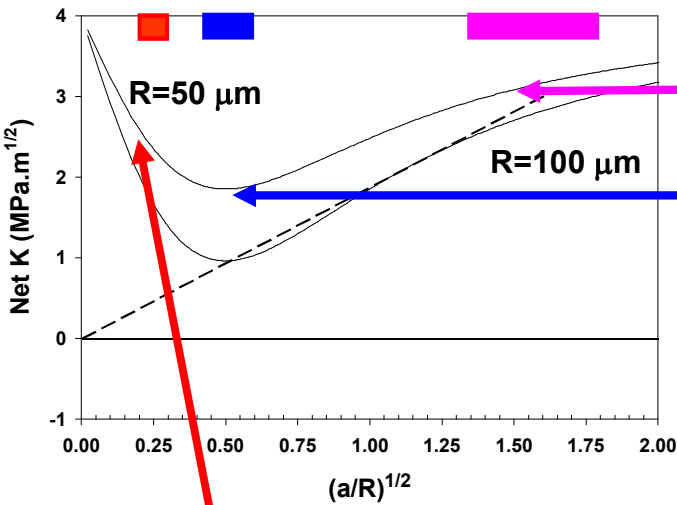
Smaller Cracks in this set: Destabilizing Field
Larger Cracks: Stable growth; failure at a_{12}

All cracks in this set:
Destabilizing Field; no stability

Results for Via B, $R=100\text{ }\mu\text{m}$



Strength Variability: $R=50\text{ }\mu\text{m}$

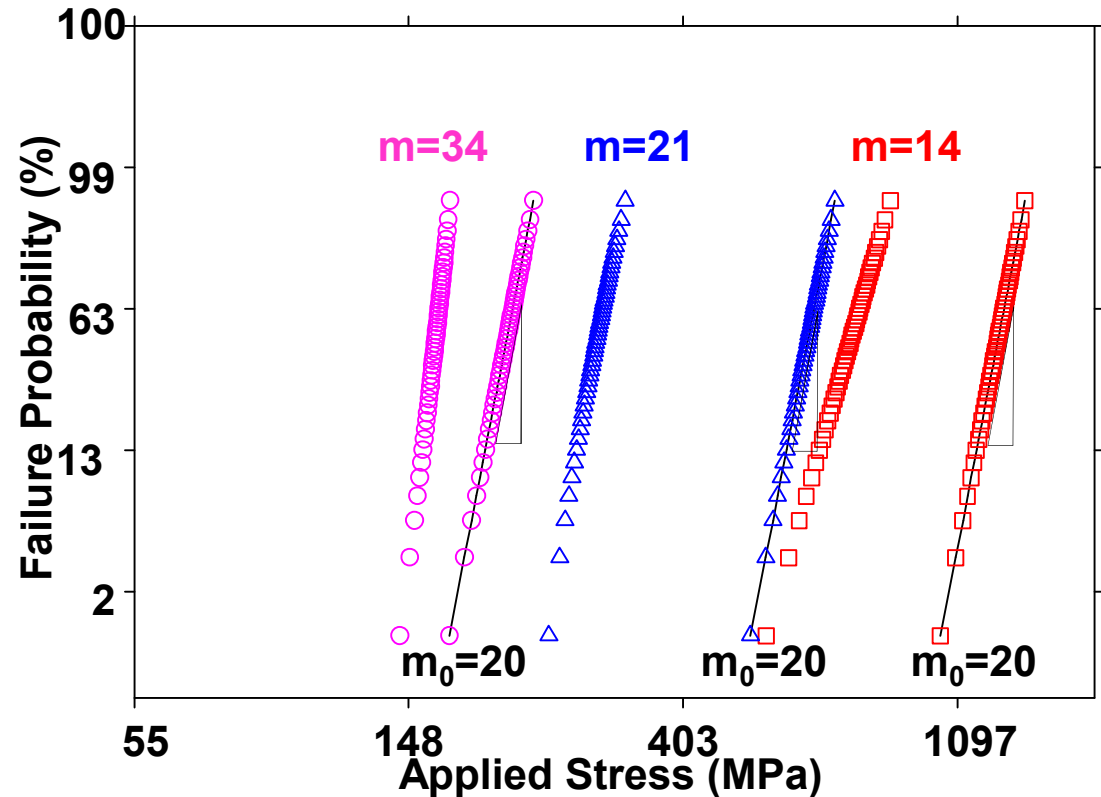


All Cracks in this set: Stabilizing Field

Smaller Cracks: Destabilizing Field
Larger Cracks: Stabilizing Field

All cracks in this set:
Destabilizing Field

Results for Via B, $R=50\text{ }\mu\text{m}$





Conclusions

Choose smallest inclusion size possible

- Retain most of the strength**
- Possibly reduce variability**

For High Retained Strength +Reduced Variability

If crack size is \sim microstructure feature size (g), then choosing $R < 4a \sim 4g$ ensures that most cracks lie on the stabilizing branch.

Fracture Mechanics Vs. Strength of Materials