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# Classical and quantum chemical studies of $\text{Rb}^+$ & $\text{Cs}^+$ to understand mechanisms in K-channels

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*Sandia is a multi-program laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the U.S. Department of Energy.*

## ABSTRACT

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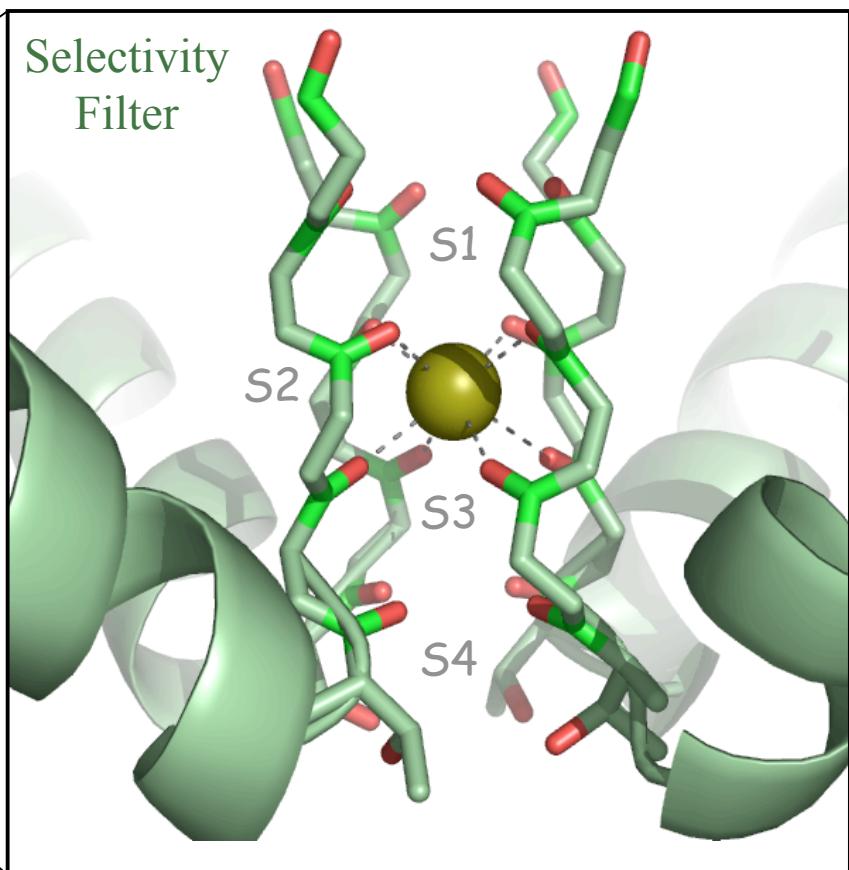
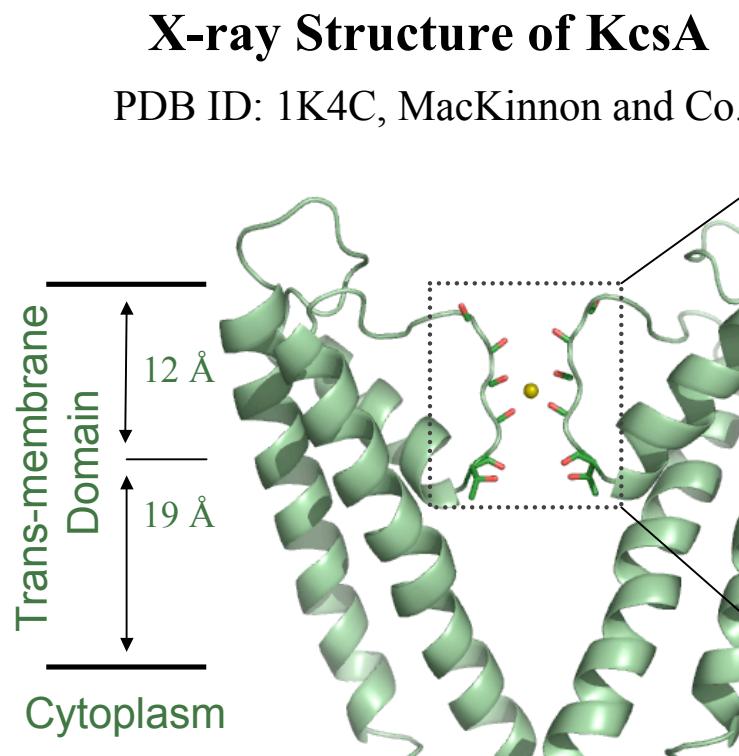
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$\text{Cs}^+$  interferes with the permeation of  $\text{K}^+$  ions through potassium (K-) channels and serves as a channel blocker. Presumably, the difference between its binding free energy to the selectivity filter and its hydration free energy must be more negative than that of  $\text{K}^+$ , or even the permeable  $\text{Rb}^+$  ions. Nonetheless, what still remains unclear regarding the mechanism by which it interacts with K-channels includes the following. In our previous quantum chemical studies, we found that highly selective K-channels maintain a special local environment around their binding sites devoid of competing hydrogen bond donor groups, which enables spontaneous transfer of  $\text{K}^+$  from states of low coordinations in water into states of over-coordination by 8 carbonyl ligands in the channel filter. This over-coordination is physiologically important to achieve  $\text{K}^+$  over  $\text{Na}^+$  selectivity. Does the binding of  $\text{Rb}^+$  or  $\text{Cs}^+$  to the 8-fold sites in the channel also require the presence of this special local phase? In addition to the properties of the solvation phase beyond the individual binding sites, are there any structural differences between the inner coordination shells of the  $\text{Cs}^+$ ,  $\text{Rb}^+$  and  $\text{K}^+$  ions that designate the former as a blocker and the latter two as permeable ions? To resolve these issues, we carry out a series of classical and quantum chemical simulations and probe the effects of such determinants as coordination number, ligand chemistry and local phase on the structural and thermodynamic solvation properties of  $\text{Rb}^+$  and  $\text{Cs}^+$  ions. We then compare these results to our previous results on  $\text{Na}^+$  and  $\text{K}^+$  ions to understand why K-channels appear to be selective for ion size (not by size).

# Representative Structure of K-channels

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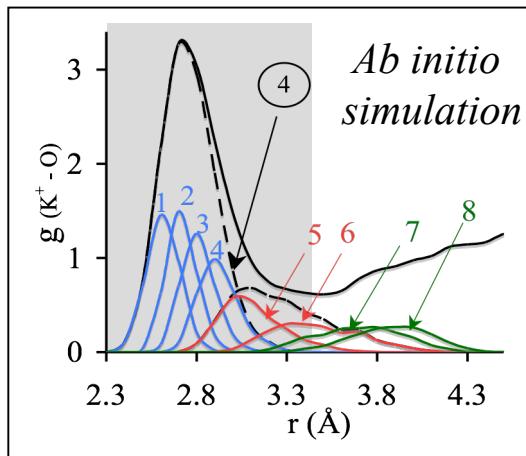
Narrowest portion of the  
permeation pathway  
in the channel's conductive state



# Summary of previous quantum chemical studies of $\text{K}^+$ over $\text{Na}^+$ selectivity

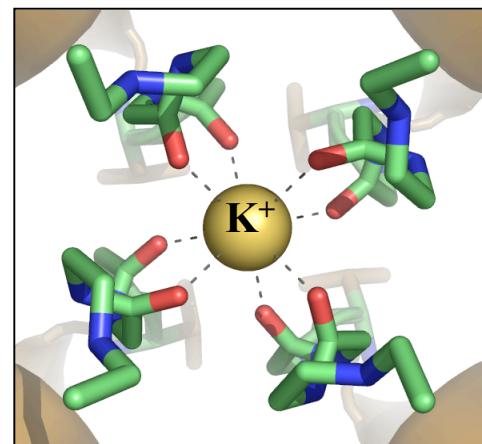
## 1. Selectivity in K-channels is due to constraints on over-coordination

$\text{K}^+$  in Bulk Water



Low coordination  
preferred

Ion selectivity  
filter



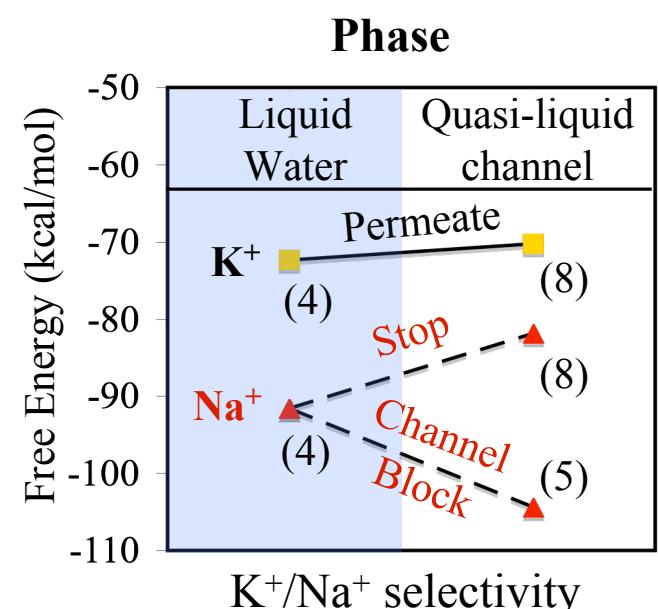
High 8-fold coordination  
in equilibrium

Introduce Special

Quasi-Liquid Phase

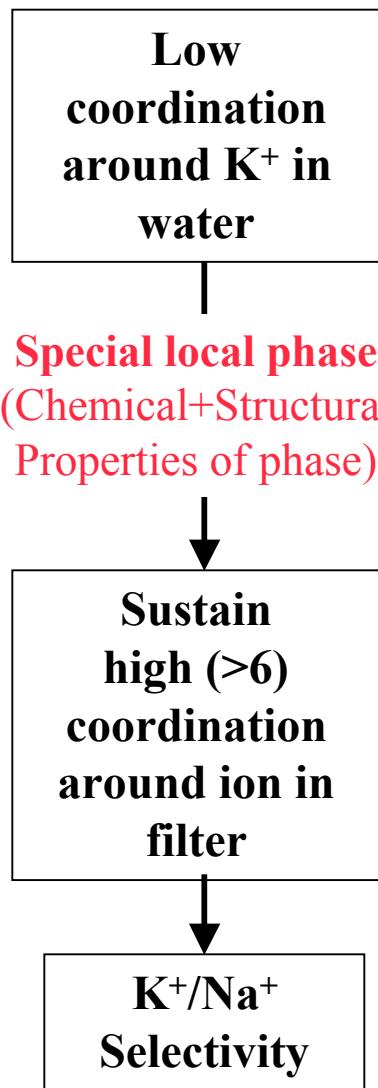
Introduce constraint

on over-coordination



Varma & Rempe, Biophys. Chem. 2006  
Varma & Rempe, Biophys. J. 2007  
Varma, Sabo & Rempe, J Mol. Biol. 2008  
Varma & Rempe, Submitted.

# Tuning ion selectivity in K-channels



Disturb phase

- 1. **Mutations** that disturb the local phase via introduction of hydrogen bond donors.  

S177W

$Na^+$        $K^+$

$10 \mu A$        $20 ms$

Bichet *et al.* PNAS, 2006
- 2. **Sequence alignment of Weakly selective K-channels**  
(Shealy *et al.* Biophys. J, 2003 )  

Weakly selective K-channels =  
Strongly selective K-channels + Arginines in local phase
- 3. **Structure**  
Introduce H-bond donors in the form of water & increase conformational freedom.  

KcsA - Strongly Selective

NaK - Weakly Selective

Out

W1, W2, W3, W4

R1, R2, R3, R4

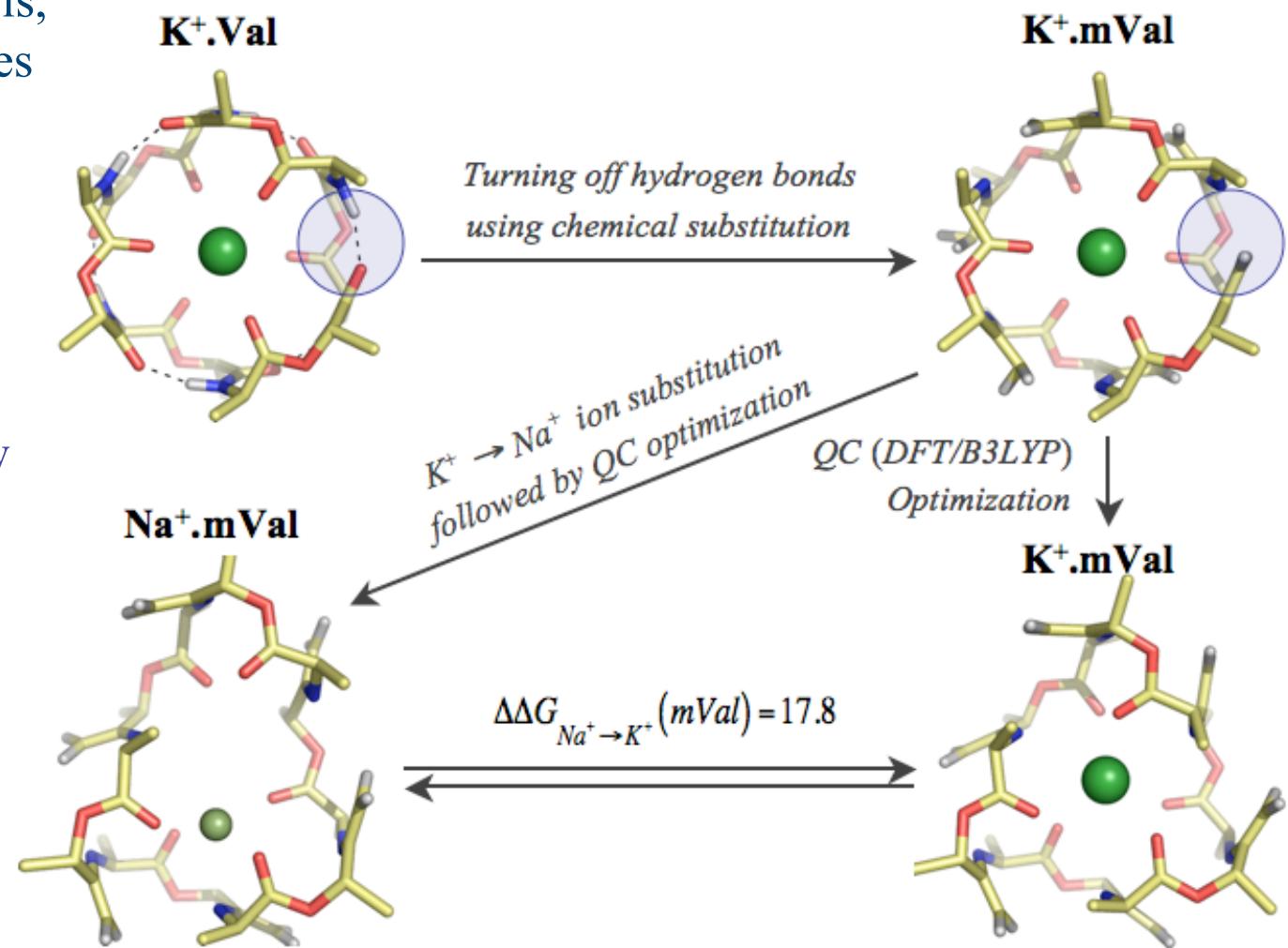
Shi *et al.* Nature Letts., 2006

## 2. Selectivity in Valinomycin is due to constraints on cavity size

In contrast to K-channels,  
**Valinomycin** molecules  
achieve K<sup>+</sup>/Na<sup>+</sup>  
selectivity by using:

**6 carbonyl ligands**  
+  
**constraints on cavity  
size**

Intra-molecular  
Hydrogen bonds play  
a vital role in  
enforcing cavity size  
constraints.



# Issues with respect to understanding $\text{Rb}^+$ and $\text{Cs}^+$ conduction through K-channels

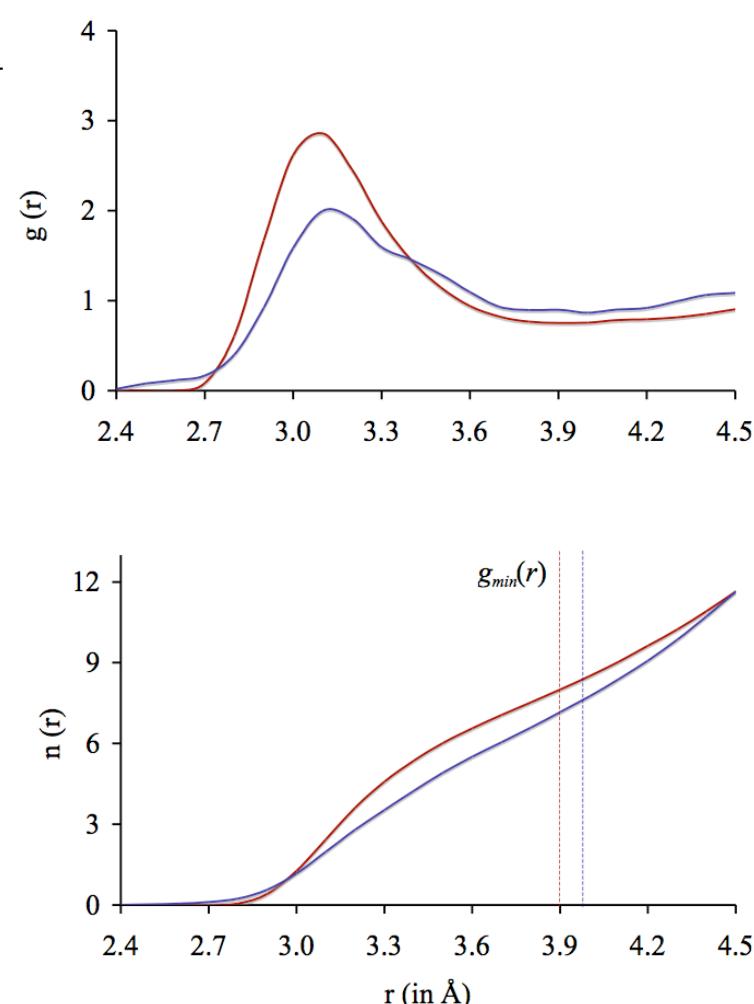
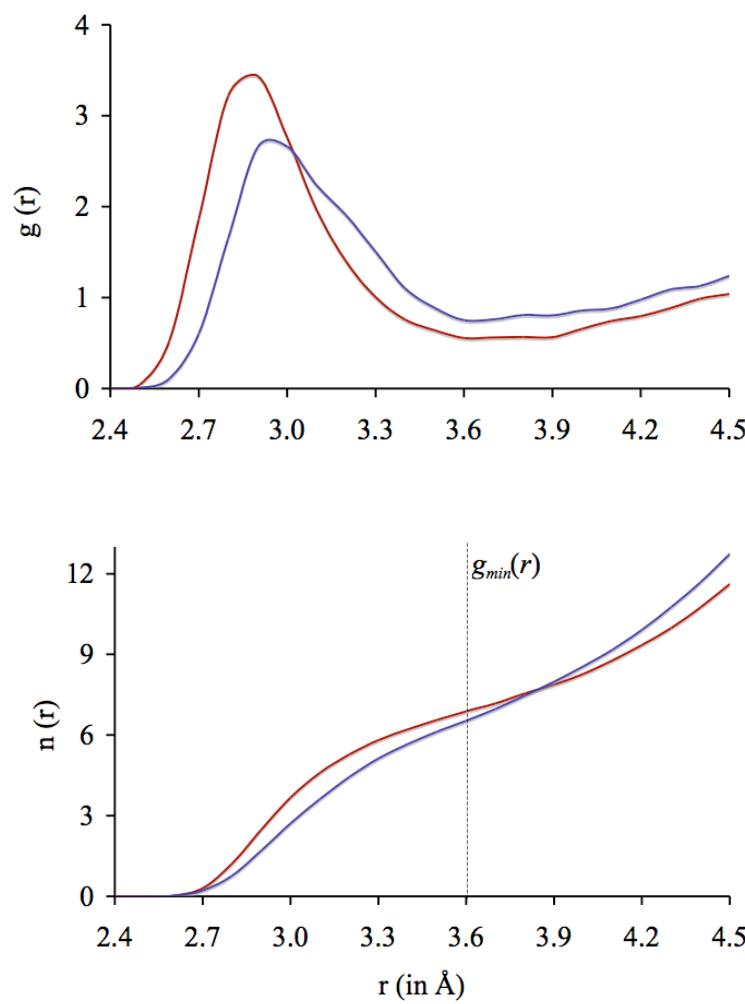
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- 1) Does the binding of  $\text{Rb}^+$  or  $\text{Cs}^+$  to the 8-fold sites in the channel also require the presence of a special local quasi-liquid phase?
- 2) In contrast to  $\text{K}^+$  and  $\text{Rb}^+$ ,  $\text{Cs}^+$  moves sluggishly through the channel. Why?
  - a) Is it because it is too large to fit through the selectivity filter?
  - b) Or does it bind more tightly to the selectivity filter as compared to  $\text{K}^+$  and  $\text{Rb}^+$ ?
    - a) If so, then is it because of specific differences between the intrinsic coordination properties of the ions?
    - b) And/or is it because specific chemical + structural properties of the binding sites make them bind more tightly to  $\text{Cs}^+$ ?
    - c) And/or, is it because specific chemical + structural properties of the region beyond the binding sites make the binding sites bind more tightly to  $\text{Cs}^+$ ?

# Structural properties of $\text{Rb}^+$ and $\text{Cs}^+$ ions in water: Classical Versus *Ab initio* simulations

Classical - Åqvist Ion + SPC/E Water  
*Ab initio* - PW91 Functional



# Hydration free energy difference between $\text{Rb}^+$ & $\text{Cs}^+$

Computed Value =  $\Delta\Delta G(aq.) =$

$$\Delta G_{\text{Rb}^+}(aq.) - \Delta G_{\text{Cs}^+}(aq.) = -7 \text{ kcal/mol}$$

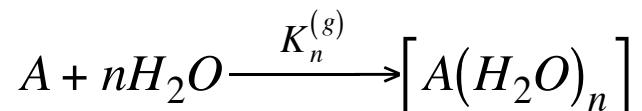
Experimental Value = -6 kcal/mol

Computed using the molecular association theory of liquids:

(Widom, 1982; Pratt & Co.)

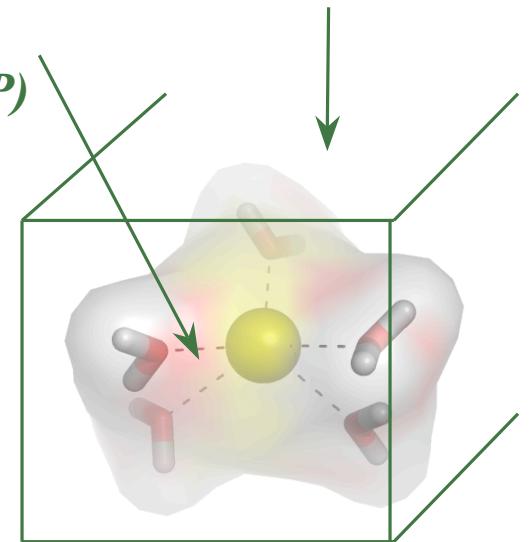
$$\beta\Delta G_A = -\ln \left\langle \prod_{j \neq \{1, \dots, n\}} (1 + f_{\sigma j}) \right\rangle_0 - \ln \left[ \sum_n K_n^{(g)} \left[ \frac{\left\langle \left\langle e^{-\beta\Delta U_\sigma} \right\rangle_0 \right\rangle_{n, \Gamma}}{\left\{ \left\langle e^{-\beta\Delta U_{H_2O}} \right\rangle_0 \right\}_n^n} \right] \rho_{H_2O}^n \right]$$

where,  $K_n^{(g)}$  is the equilibrium constant of the following gas phase reaction



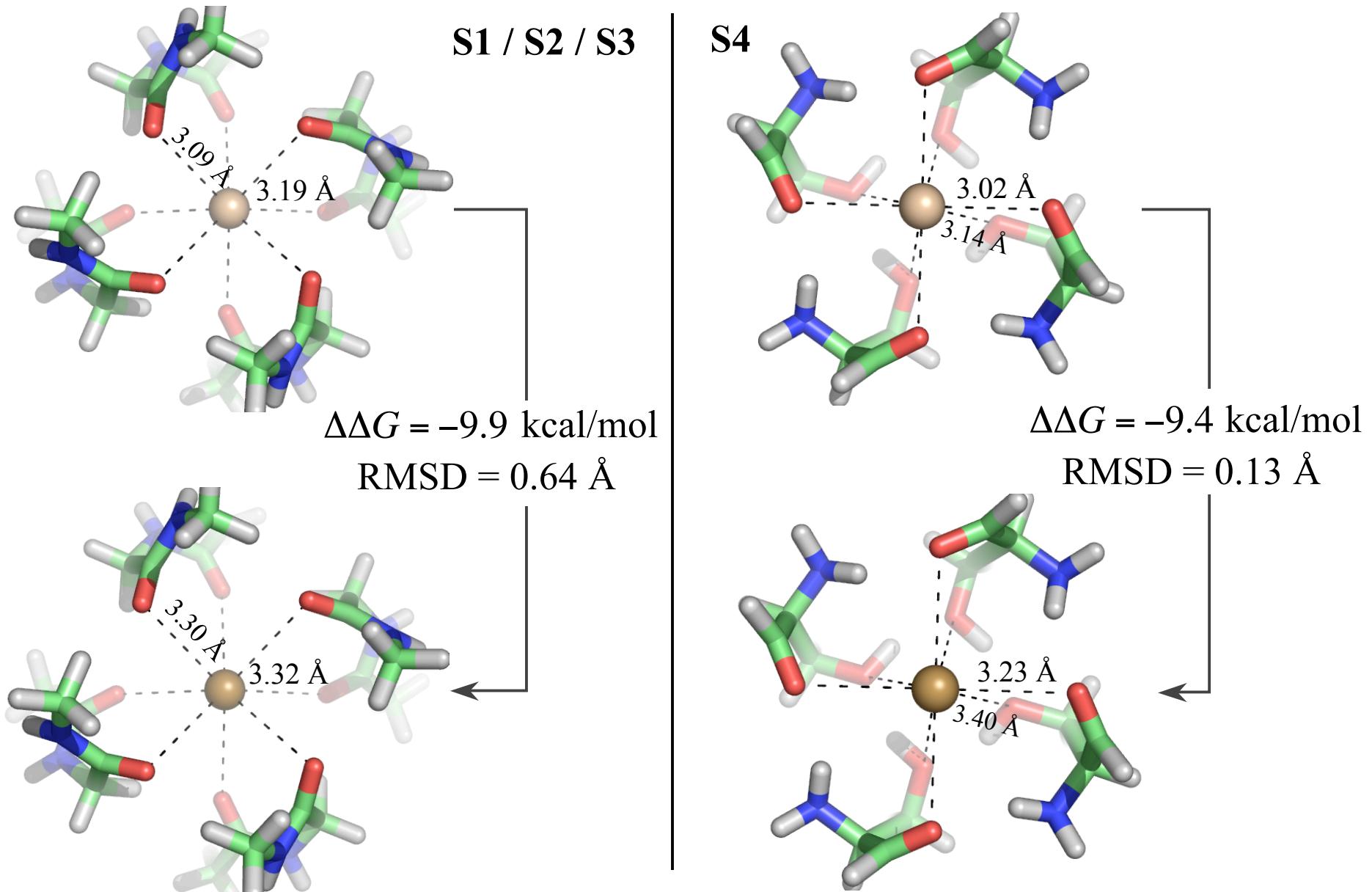
*Outer Domain  
treated classically  
(Elec./MD)*

*Inner Domain  
treated quantum  
chemically  
(DFT/B3LYP)*



# Interaction of Rb<sup>+</sup> & Cs<sup>+</sup> with Individual binding sites

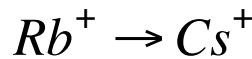
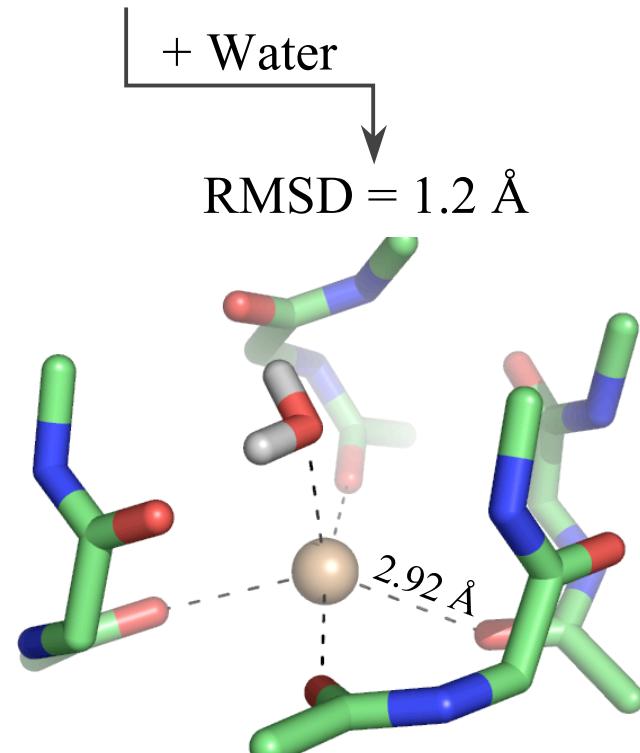
Individual binding sites are more selective for Rb<sup>+</sup>



# Interaction of Rb<sup>+</sup> & Cs<sup>+</sup> with Individual binding sites & water

## S1 with One Extra-cellular Water

Optimized S1 with Rb<sup>+</sup>

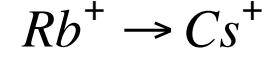
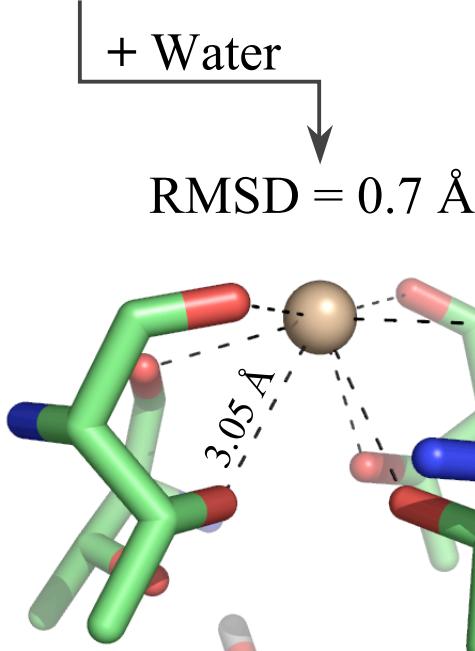


Large Distortion  
resulting in 5-fold  
coordination

$\Delta\Delta G = -10.3$  kcal/mol  
RMSD = 0.25 Å

## S4 with One Intra-cellular Water

Optimized S4 with Rb<sup>+</sup>

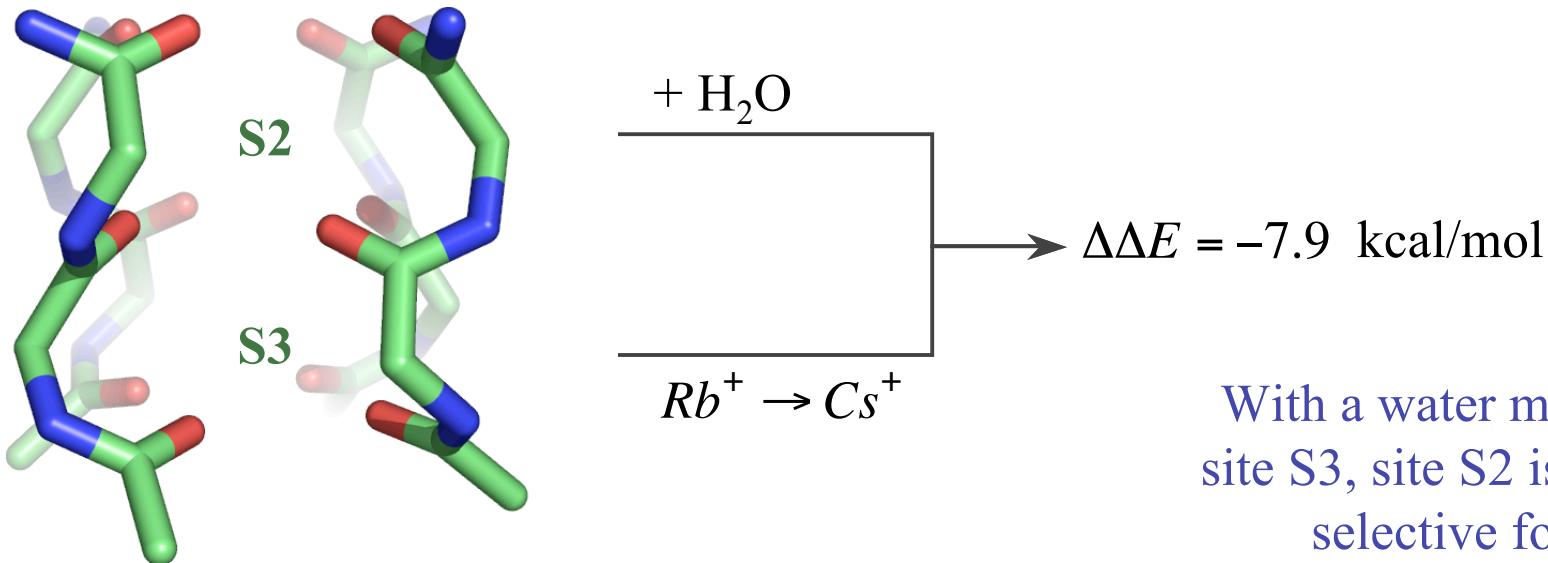


7-fold coordination,  $\Delta\Delta G = -9.4$  kcal/mol  
but not with water  
RMSD = 0.12 Å

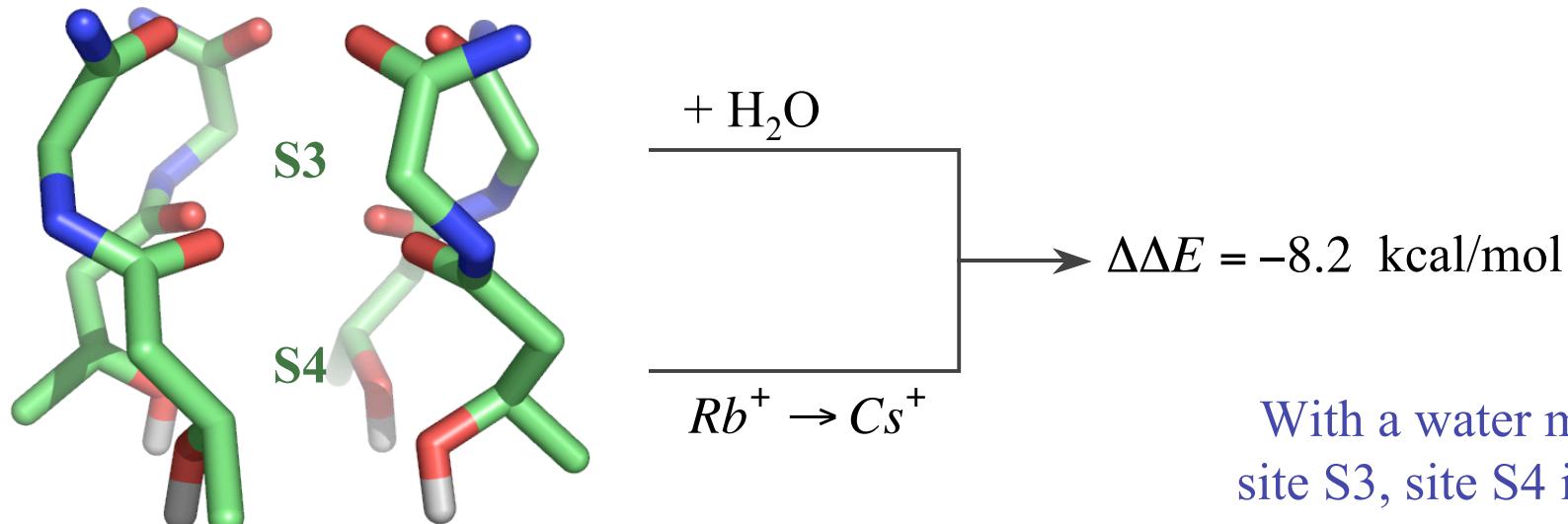
# Interaction of Rb<sup>+</sup> & Cs<sup>+</sup> with Multiple binding sites

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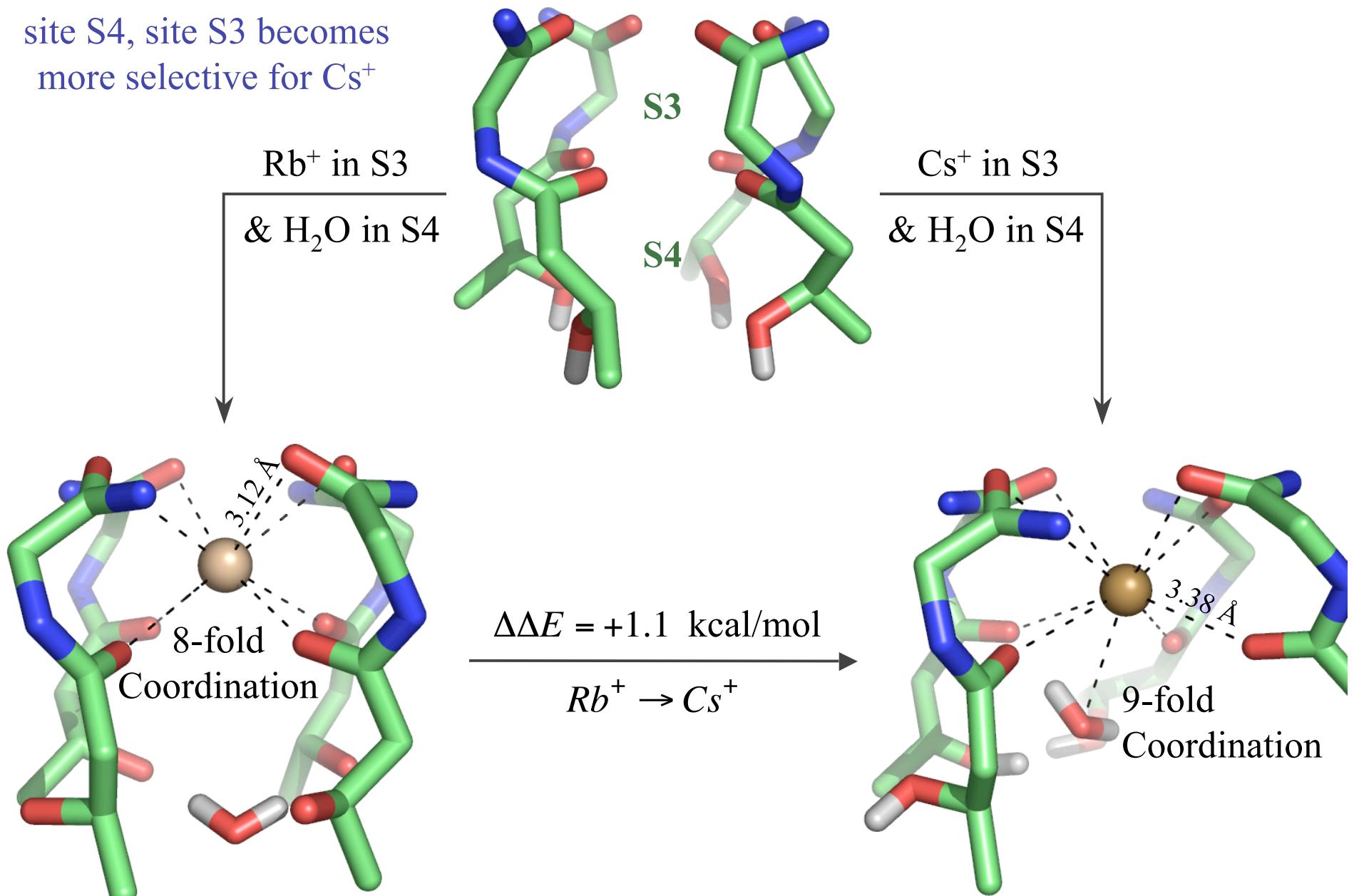
With a water molecule in site S3, site S2 is still more selective for Rb<sup>+</sup>



With a water molecule in site S3, site S4 is also more selective for Rb<sup>+</sup>

# Interaction of Rb<sup>+</sup> & Cs<sup>+</sup> with Multiple binding sites

With a water molecule in site S4, site S3 becomes more selective for Cs<sup>+</sup>



## Summary & Conclusions

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- 1) Binding of  $\text{Cs}^+$  to the 8-fold sites in the channel does not require the presence of a special local quasi-liquid phase, as it is also 8-fold coordinated in liquid water.
- 2) This is in contrast to the requirements for the binding of both  $\text{K}^+$  and  $\text{Rb}^+$  ions, which are over-coordinated in the selectivity filter.
- 3) In contrast to  $\text{K}^+$  and  $\text{Rb}^+$ ,  $\text{Cs}^+$  moves sluggishly through the channel because
  - a)  $\text{Cs}^+$  may be too large to fit through the selectivity filter (Add Citations)
  - b) In addition, it also binds more tightly to site S3, provided
    - a) site S4 is occupied by a water molecule, and
    - b) site S3 is surrounded by a quasi-liquid pocket to allow  $\text{Cs}^+$  to over-coordinate with 9 ligands

# Acknowledgements

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## Software

- (1) Classical Molecular Dynamics simulations - GROMACS v3.1  
(Lindahl *et al.*, J Mol. Mod. 2001)
- (2) *Ab initio* Molecular Dynamics simulations - VASP vX.X
- (3) Quantum Chemical calculations - Gaussian03 (Gaussian Inc.)
- (4) Implicit Solvent Simulations - APBS (Baker *et al.*, PNAS 2001)
- (5) Figures - PyMol (DeLano Scientific)
- (6) Analysis Codes - Home grown at UIUC under the auspices of the Ion Channel Portal, and at Sandia National Labs.

## Computer Time (150,000 hours)

- (1) The National Center for Supercomputing Applications at UIUC.
- (2) Sandia Supercomputing Center.

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