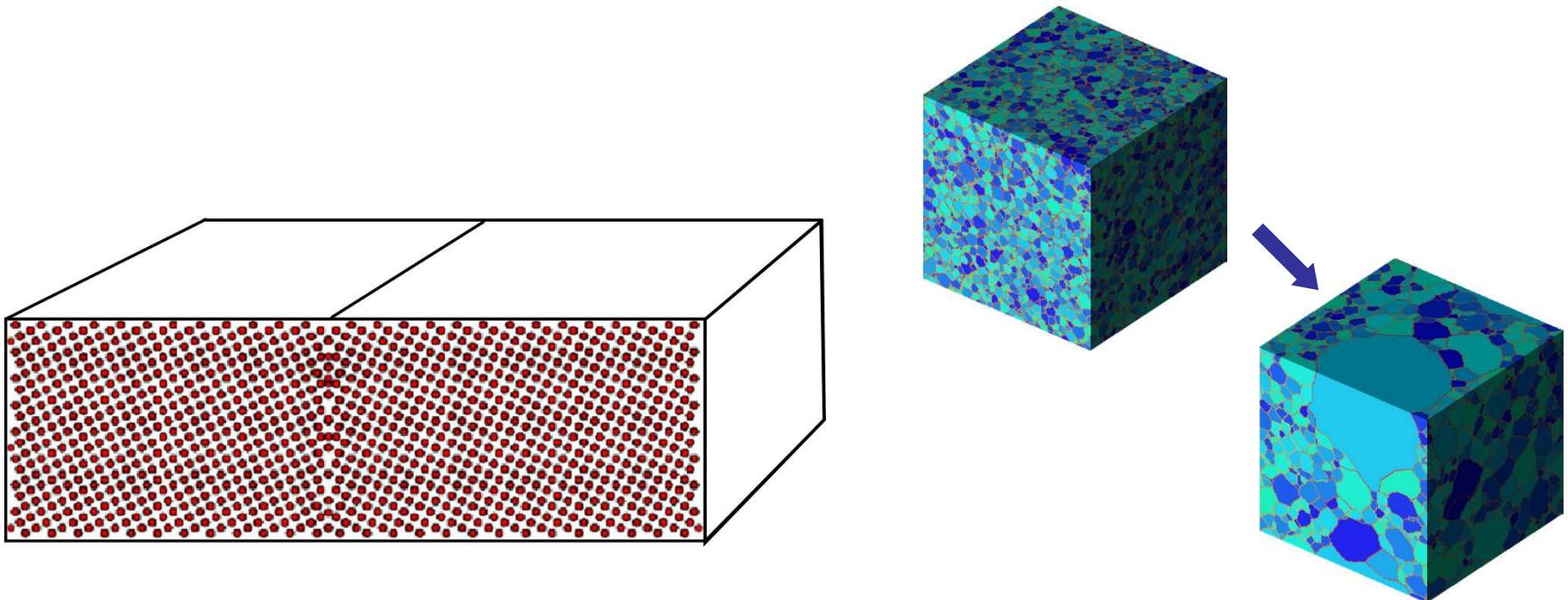


How close are two grain boundaries in the five dimensional crystallographic space?

David Olmsted
Sandia National Laboratories



Distance in 5d grain boundary space

- **Why**
- **Method**

Describe single boundary in 5d space

Define distance between two boundaries

- **Examples**

Other distances:

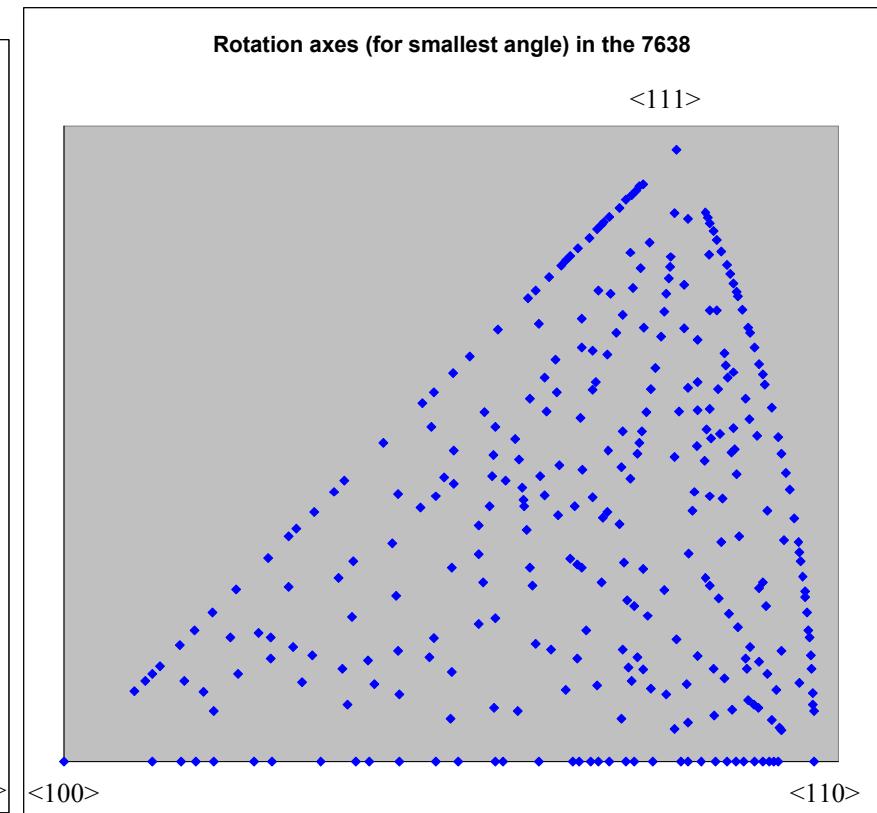
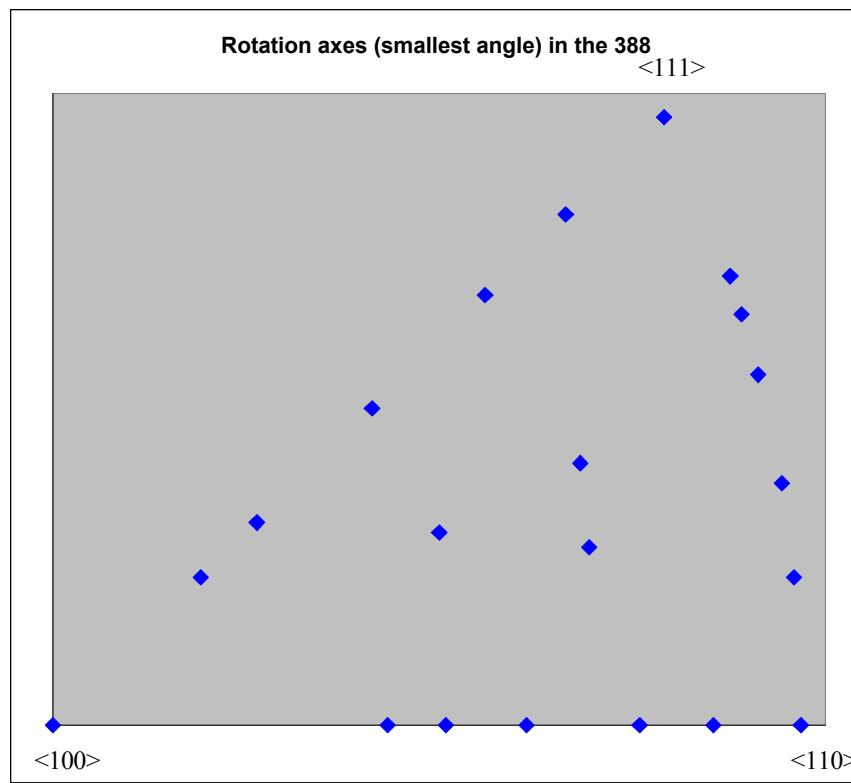
A. Moraweic, 1998

J.W. Cahn & J.E. Taylor, 2006

Need distance to interpolate

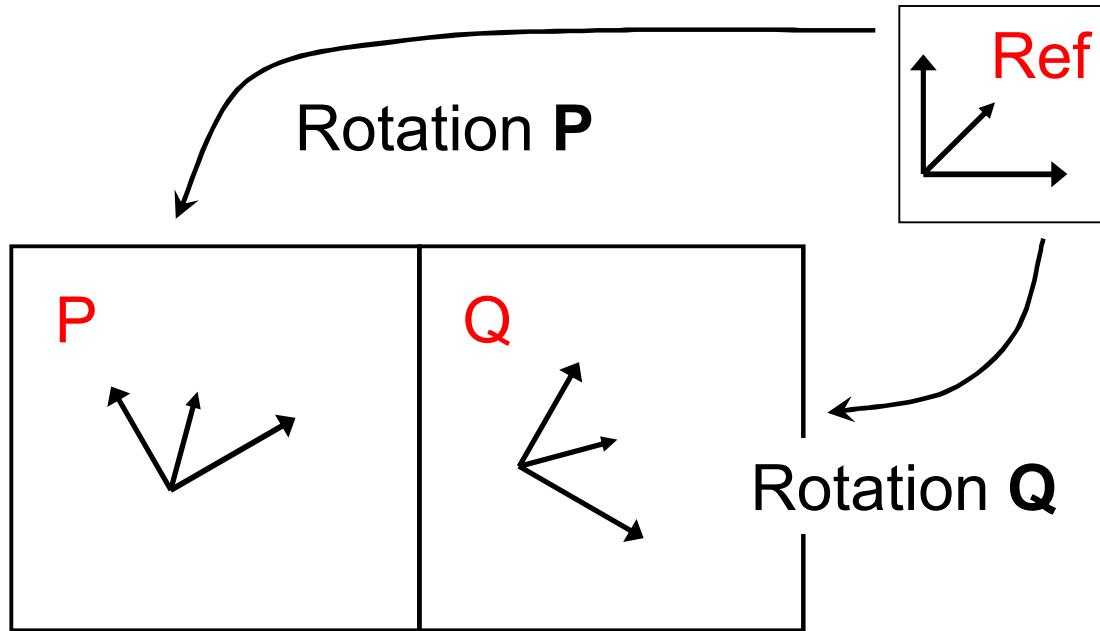
- For mesoscale simulations we need to assign properties to any boundary.
- To look up an arbitrary boundary in table, we need to find the most similar table boundary.
- Presumably this is the closest boundary in the 5d macroscopic grain boundary space.

Need distance to fill in table



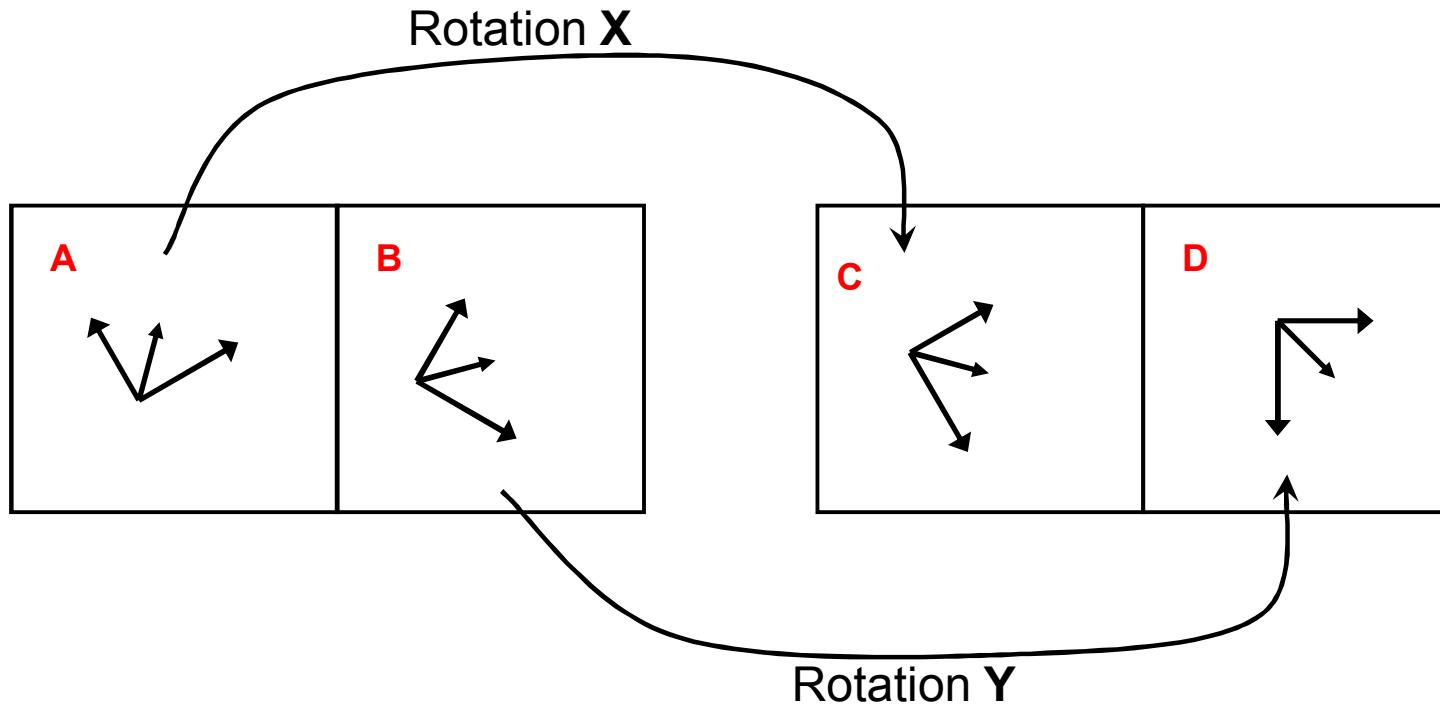
Add optimal boundaries from larger set, not all.

Describe position in 5d space



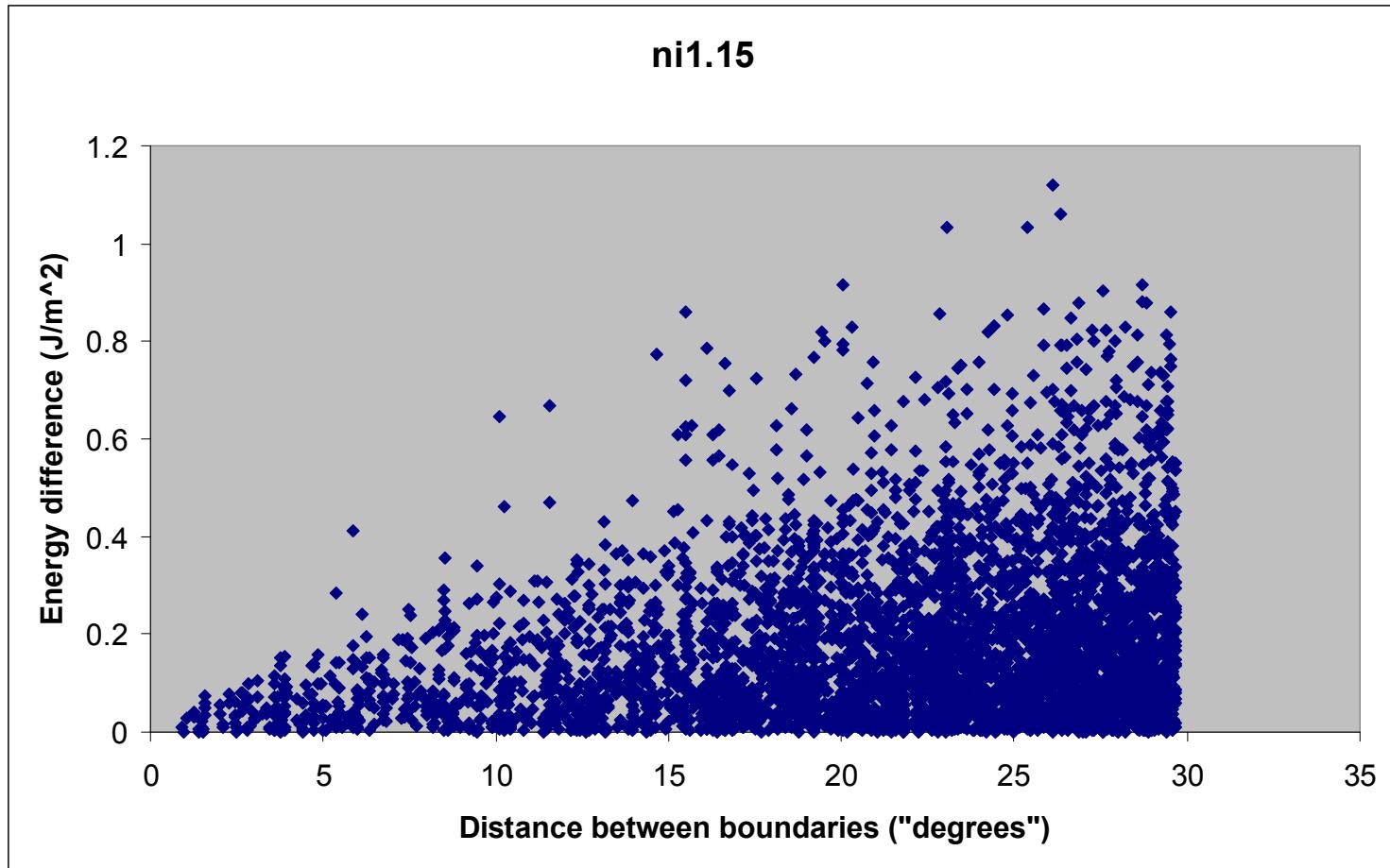
(P, Q) describes boundary, but we have to allow for fcc symmetries **and** rotations about boundary normal.

Distance between two boundaries

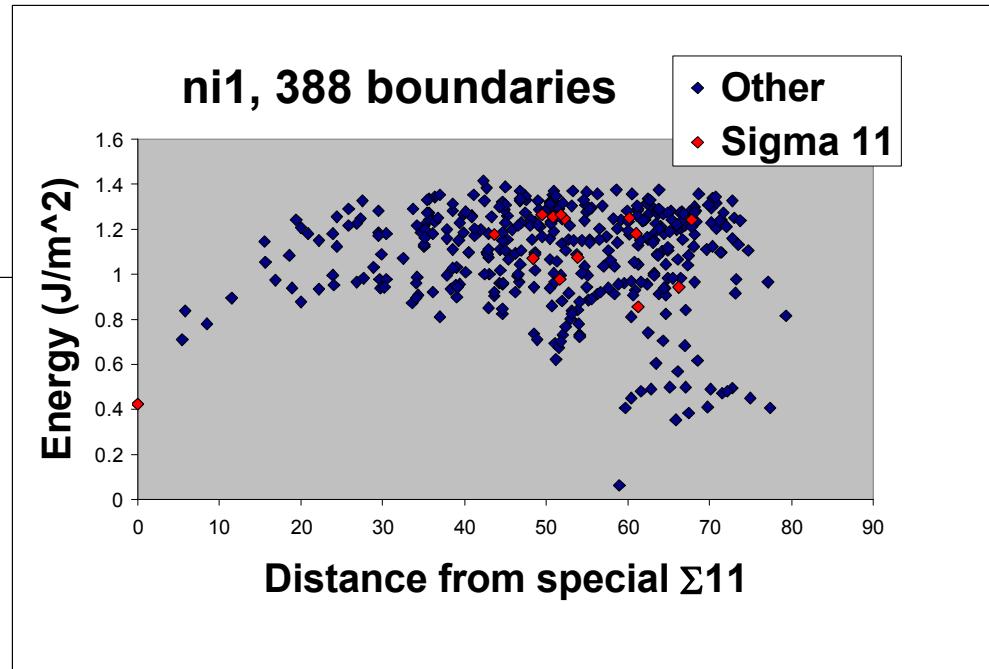
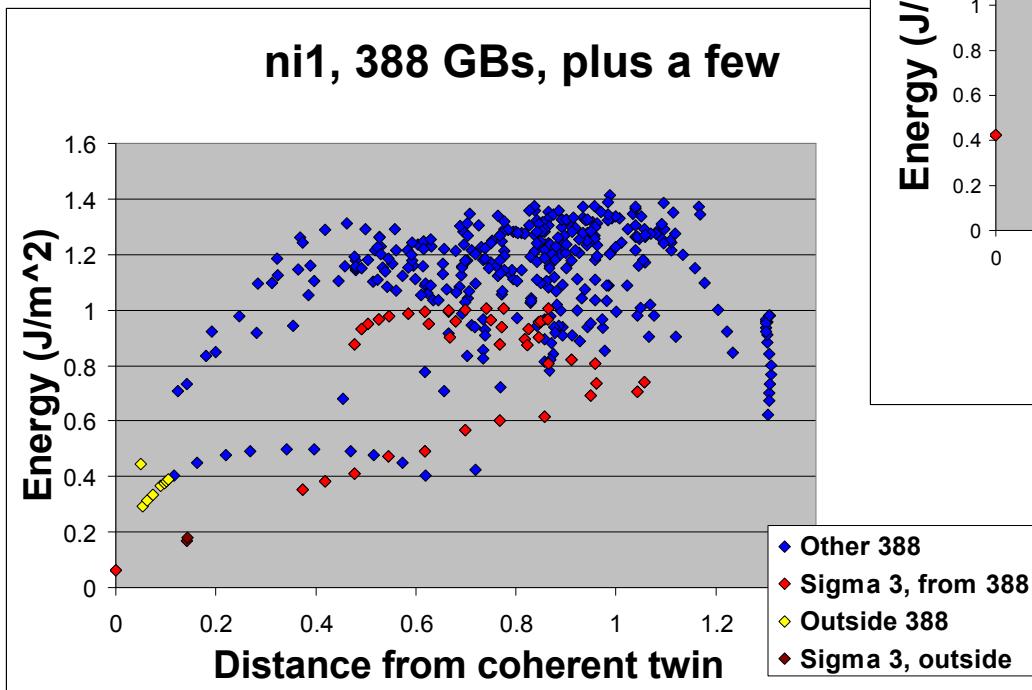


$d(AB,CD)=|X|+|Y|$ minimized over all
equivalent representations
of boundaries AB and CD

Nearby boundaries have similar energy



Energy cusps



Distance in 5d grain boundary space

- A distance is needed to access table of “388” GBs for an arbitrary boundary.
- Distance is needed to fill in holes in the table.
- For the distance shown here, nearby boundaries have similar energy.
- Distance can also be used to examine, for example, the existence of energy cusps.