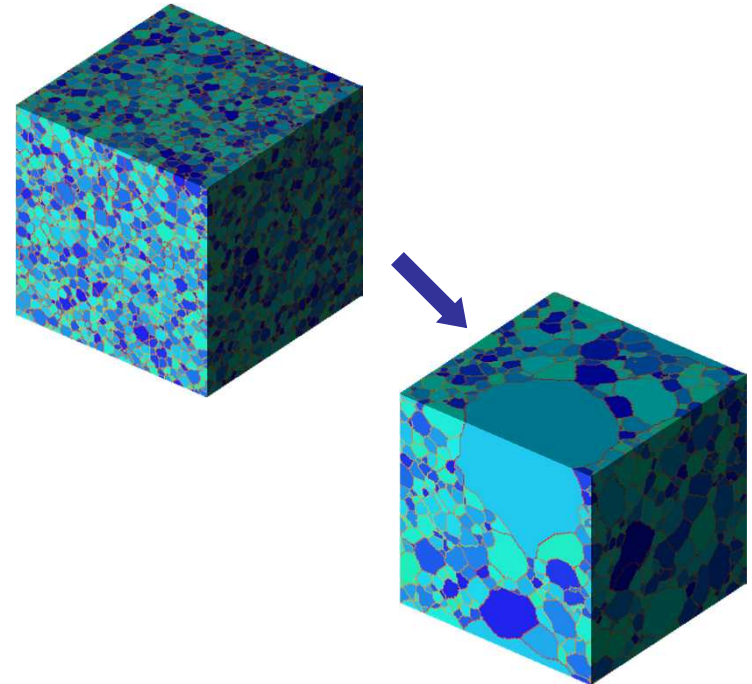
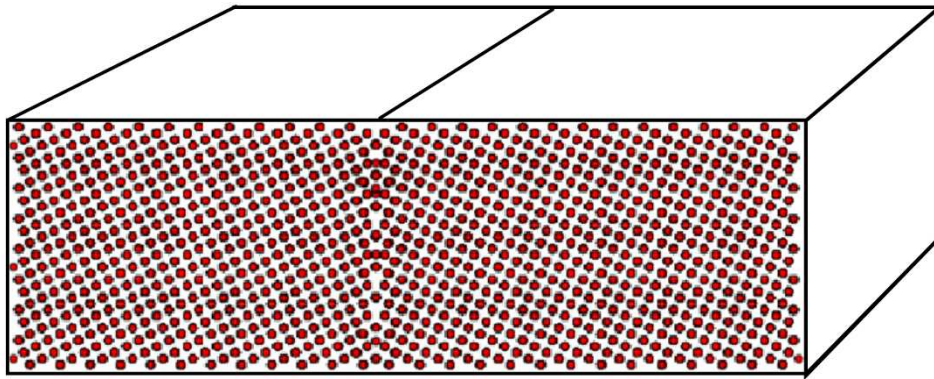


How close are two grain boundaries in the five dimensional crystallographic space?

David Olmsted
Sandia National Laboratories



Distance in 5d grain boundary space

- **Why**

- **Method**

Describe single boundary in 5d space

Define distance between two boundaries

- **Examples**

Other distances:

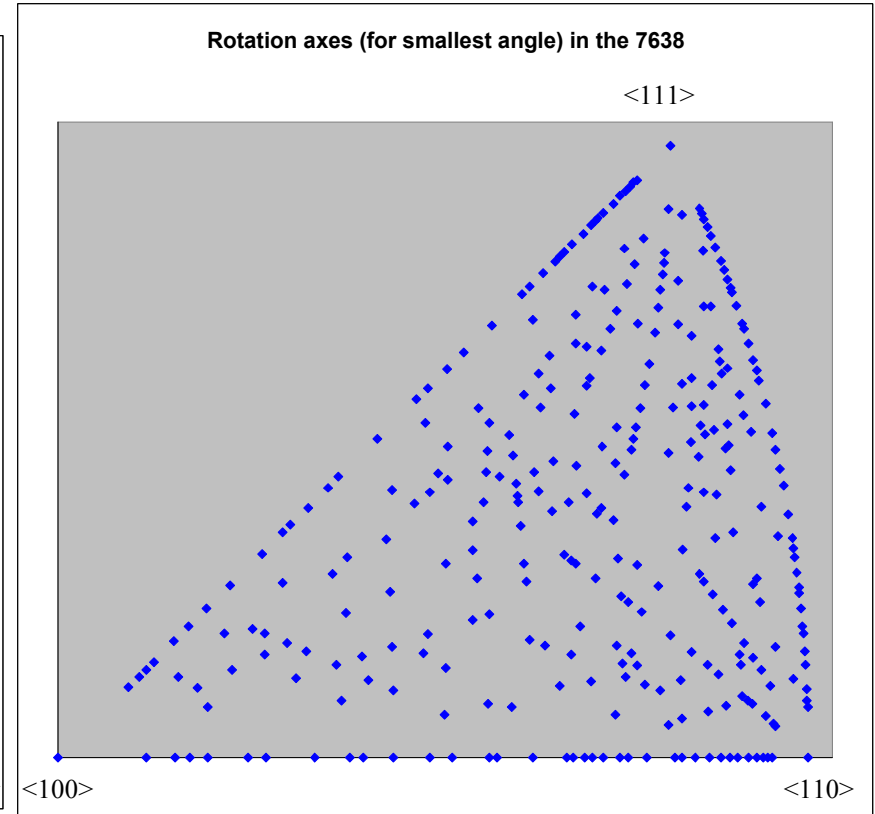
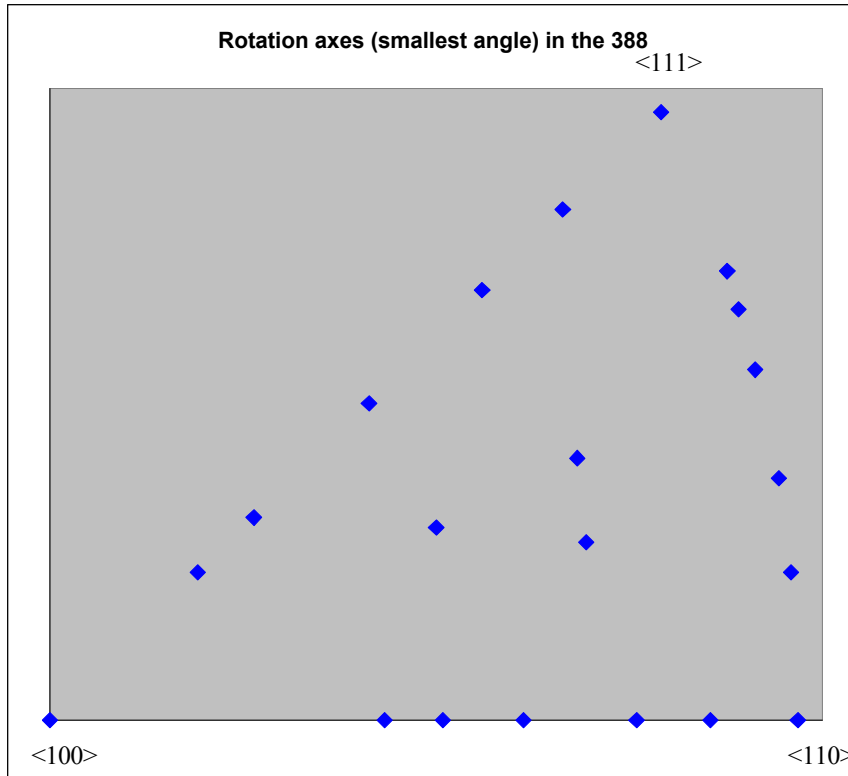
A. Moraweic, 1998

J.W. Cahn & J.E. Taylor, 2006

Need distance to interpolate

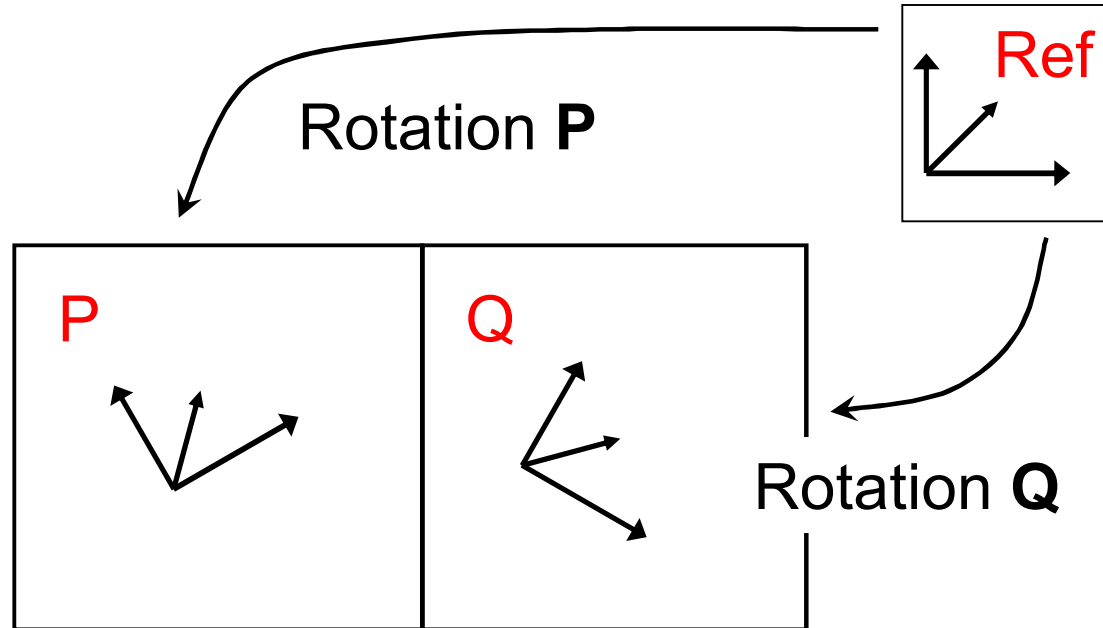
- **For mesoscale simulations we need to assign properties to any boundary.**
- **To look up an arbitrary boundary in table, we need to find the most similar table boundary.**
- **Presumably this is the closest boundary in the 5d macroscopic grain boundary space.**

Need distance to fill in table



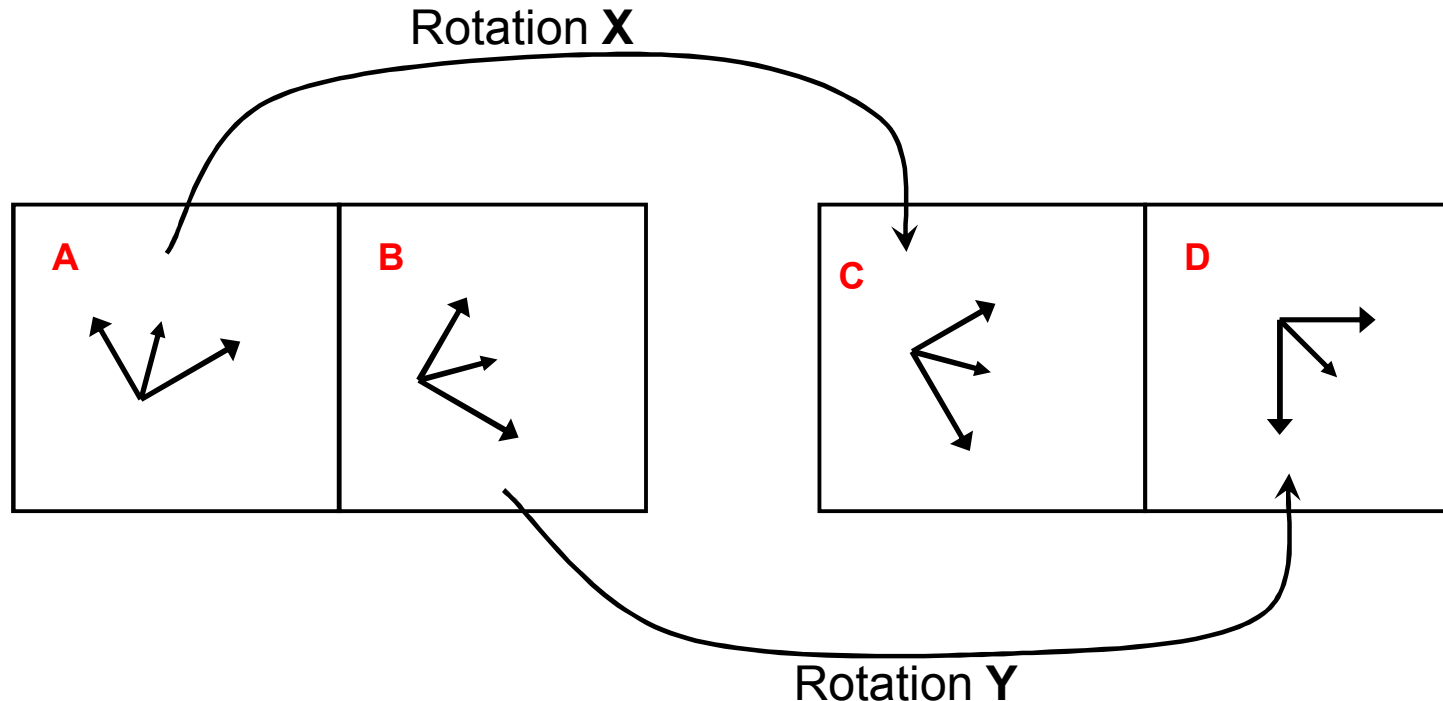
Add optimal boundaries from larger set, not all.

Describe position in 5d space



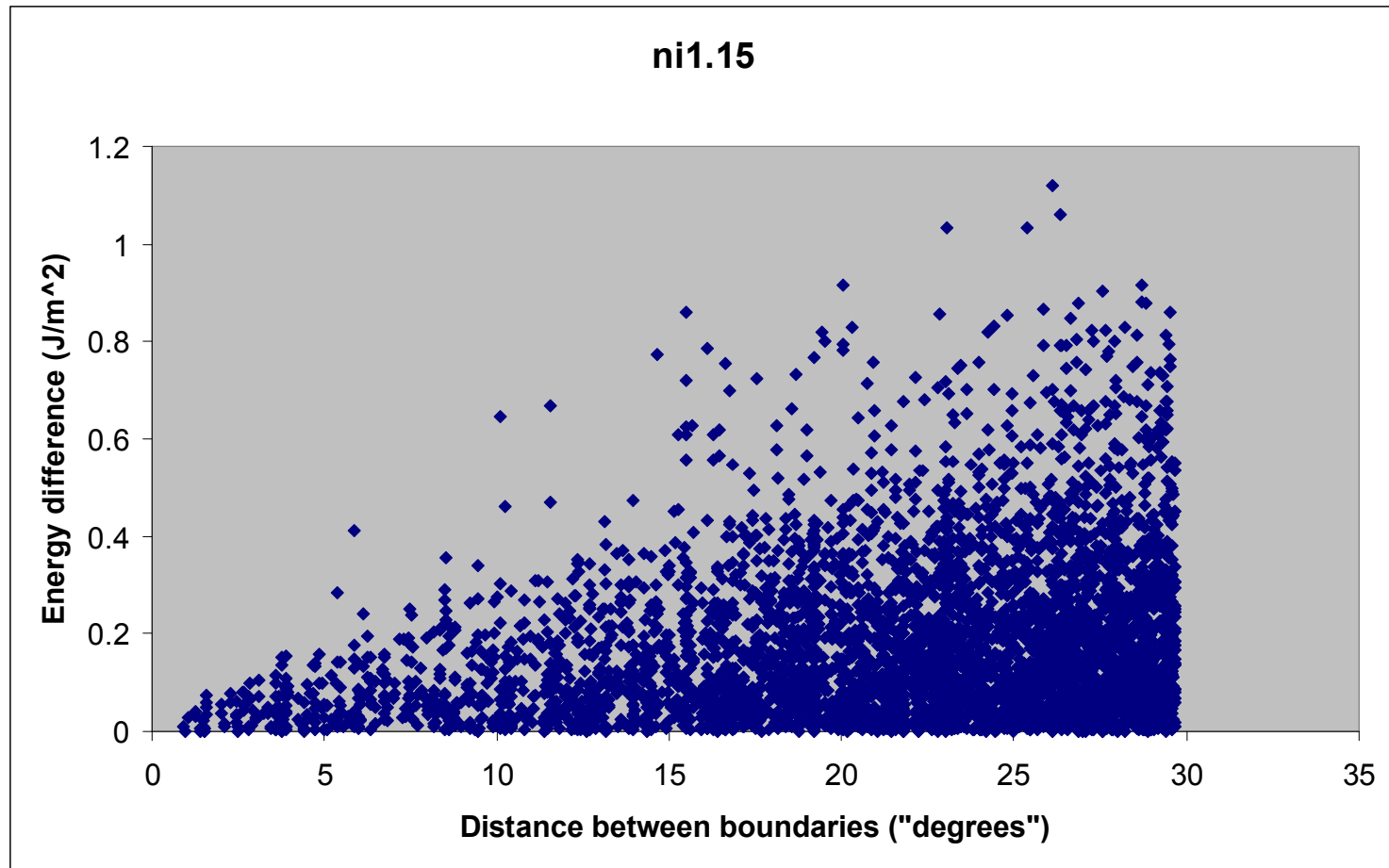
(**P**,**Q**) describes boundary, but we have to allow for fcc symmetries **and** rotations about boundary normal.

Distance between two boundaries



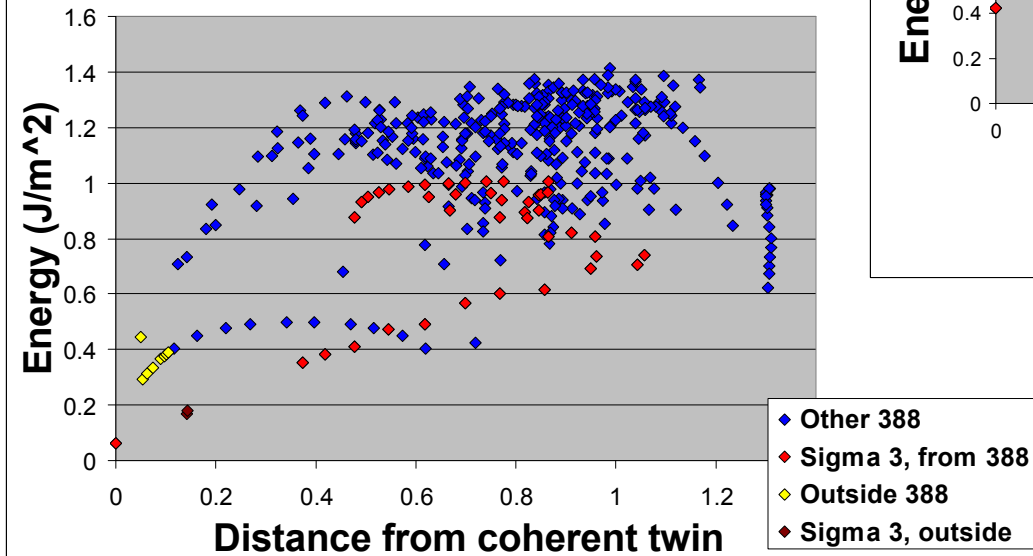
$d(AB, CD) = |X| + |Y|$ minimized over all
equivalent representations
of boundaries AB and CD

Nearby boundaries have similar energy

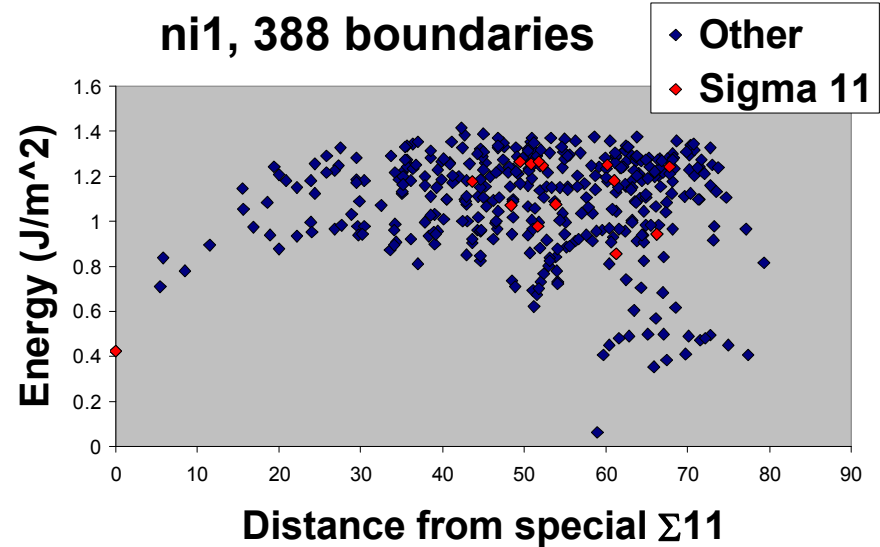


Energy cusps

ni1, 388 GBs, plus a few



ni1, 388 boundaries



Distance in 5d grain boundary space

- A distance is needed to access table of “388” GBs for an arbitrary boundary.
- Distance is needed to fill in holes in the table.
- For the distance shown here, nearby boundaries have similar energy.
- Distance can also be used to examine, for example, the existence of energy cusps.