

A Short Comment on the Temperature Variation of Grain Boundary Free Energy

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Once upon a time: Direct Calculation of G.B. Free Energy versus T

- Method of calculation
 - Low temperature:
 - Quasi-harmonic calculations
 - High temperature
 - Thermodynamic Integration using MC based excess enthalpy
- High-symmetry boundary
 - Cu $\Sigma 5$ (310)/[001] symmetric tilt boundary
- Dramatic reduction in grain boundary free energy

$$\frac{\gamma(T_M)}{\gamma(0)} \approx 0.4$$

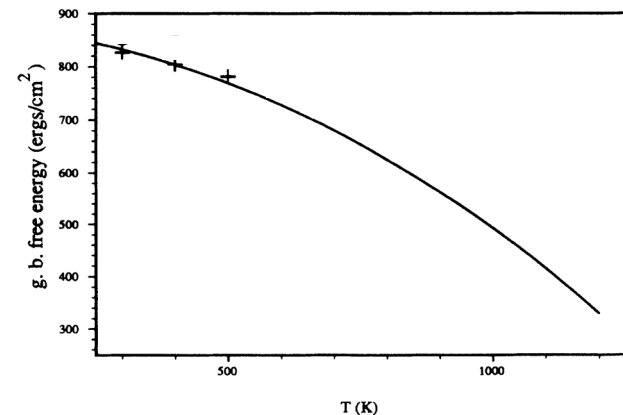
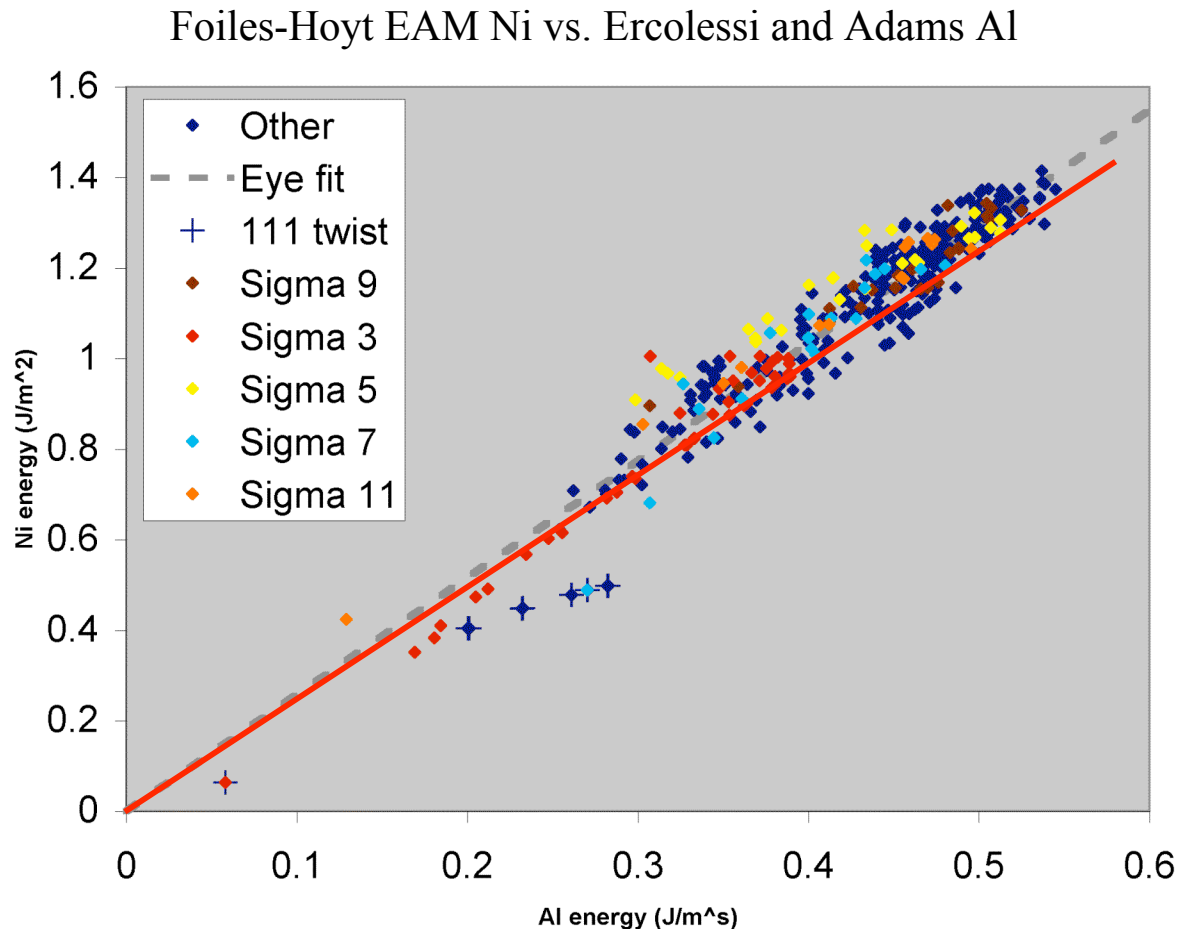


FIG. 9. The interfacial free energy of a Cu $\Sigma 5$ (310)/[001] symmetric tilt boundary as computed from the MC simulations (solid line)

S.M. Foiles, "Evaluation of harmonic methods for calculating the free energy of defects in solids", Phys. Rev. B **49**, 14930 (1994).

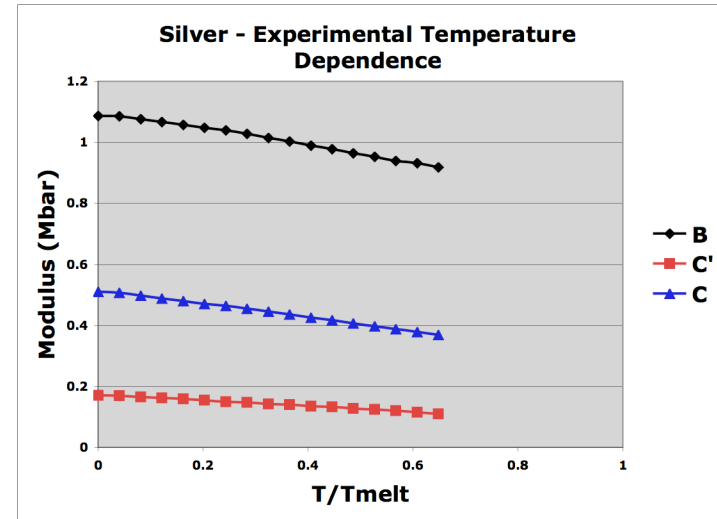
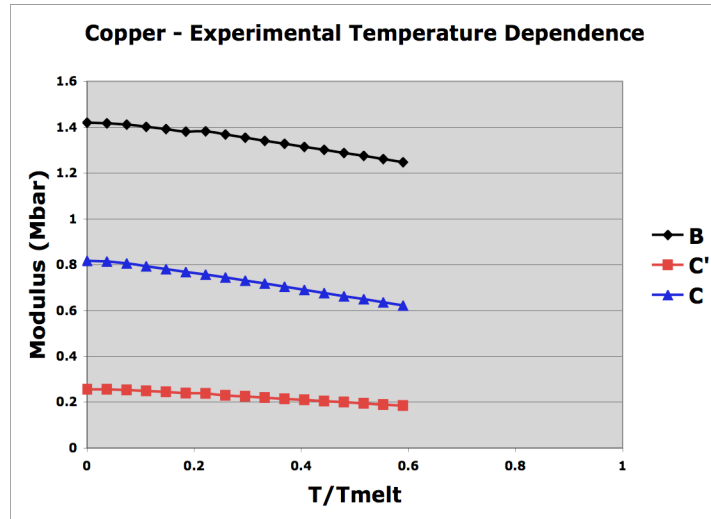
Comparison of Grain Boundary Energies in different metals: Ni vs. Al



- Most of the variation in boundary energy is structural, not chemical.
- What scales boundary energy?
 - Shear modulus ratio: 2.4

⇒ Supports a dislocation model for grain boundary structure
- $\langle 111 \rangle$ twist boundaries are relatively lower energy in Ni.
- The “special” $\Sigma 11$ boundary is relatively lower energy in Al.

Temperature Dependence of Elastic Constants: Noble Metals

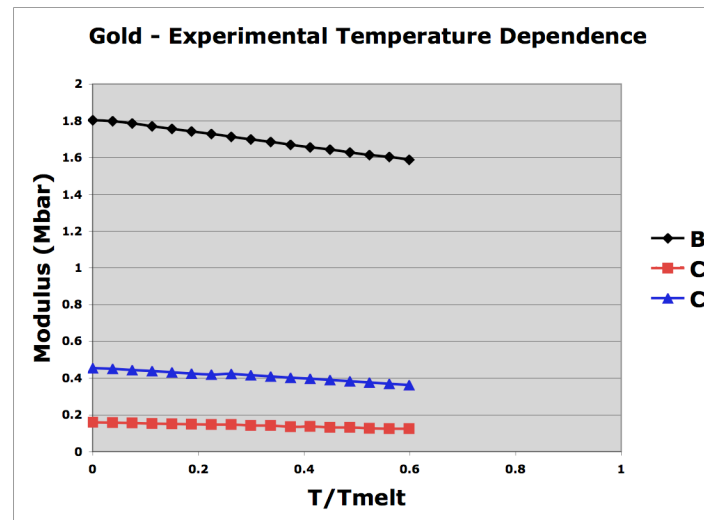


$$B = \frac{1}{3}(C_{11} + 2C_{12})$$

$$C = C_{44}$$

$$C' = \frac{1}{2}(C_{11} - C_{12})$$

Simmons & Wang, "Single Crystal Elastic Constants and Calculated Aggregate Properties" (MIT Press, 1971)



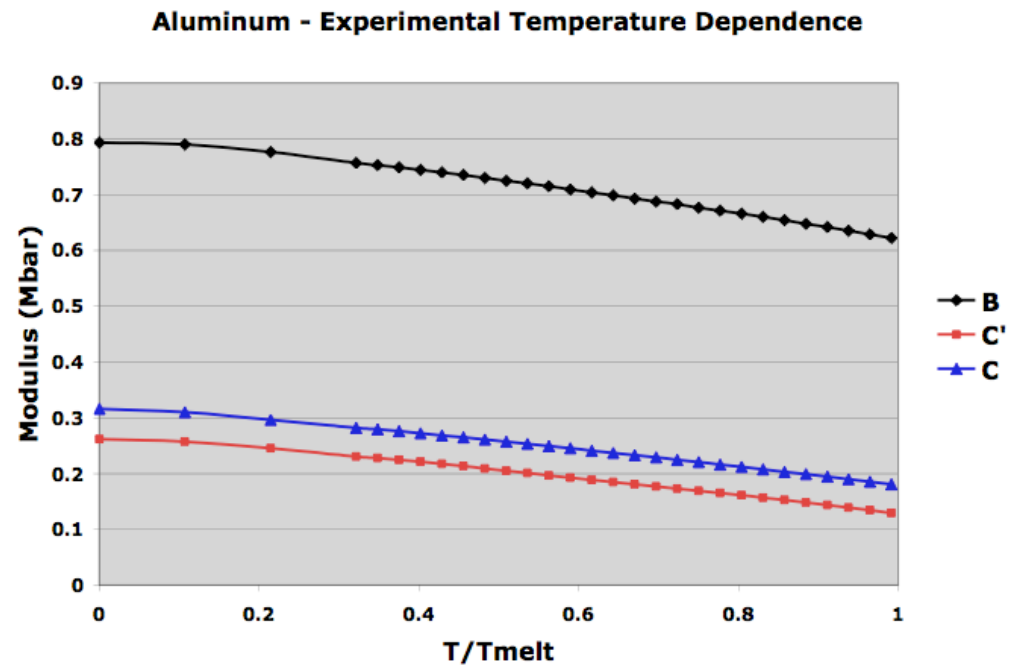
Temperature Dependence of Elastic Constants: Aluminum - Data up to T_M !

$$B = \frac{1}{3}(C_{11} + 2C_{12})$$

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Is elastic softening the main driver for reduction of grain boundary free energy with temperature?

- Physically reasonable that grain boundary energy scales with shear modulus
 - Grain boundaries are arrays of dislocations
 - at least formally
 - Elastic strain energy of a dislocation scales with shear modulus
 - Consistent with comparison of grain boundary energies for different metals
- Magnitude of shear modulus softening is comparable to (though somewhat less than) the reduction in grain boundary free energy
 - **More data needed here!**

$$\frac{\text{Modulus}(T = T_M)}{\text{Modulus}(T = 0)}$$

	B	C	C'
Cu	0.77	0.58	0.50
Ag	0.75	0.56	0.45
Au	0.80	0.65	0.61
Al	0.78	0.57	0.49

Nobel metal data extrapolated to T_M