

# Modal Analysis and Dynamic Monitoring of a Concentrating Solar Heliostat

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# Outline

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- **Introduction and Motivation**
- **Data Acquisition & Instrumentation**
- **Operational Modal Analysis**
- **FEA Mode Shape Correlation**
- **Ray Tracing & Optical Performance**
- **Conclusion**

# National Solar Thermal Test Facility



- 200 ft. tall tower makes NSTTF one of the “tallest” and “hottest” test facilities in the country

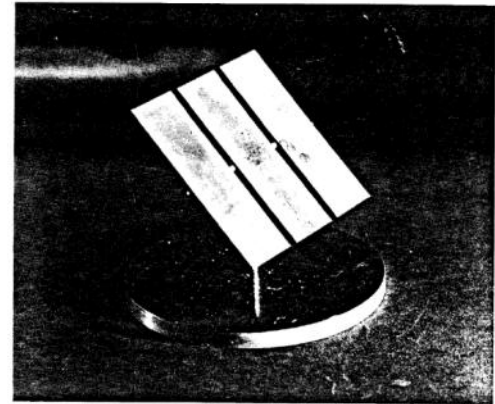
- 218 computer controlled heliostats concentrate sunlight producing temperatures up to  $5000^{\circ}\text{K}$  ( $\sim 8540^{\circ}\text{F}$ ) and 5 MW of power



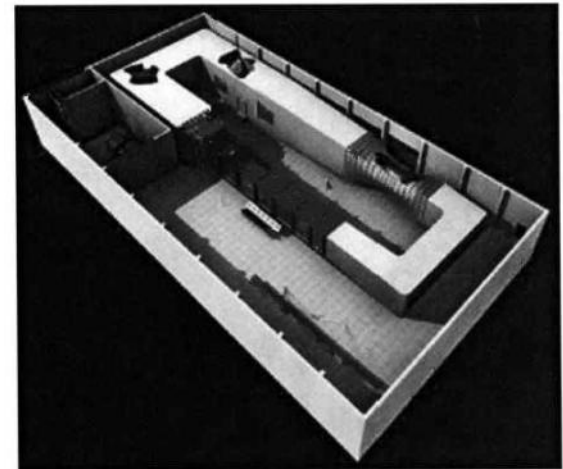
- Tower applications:
  - CSP R&D
  - Thermal performance testing
  - Space technology testing
  - Radar and Sensor testing
  - Astronomy experiments
  - Nuclear thermal flash simulations

# CSP Motivation

- Helio­stat construction costs up to 50% of initial capital required for commercial CSP plant
- There currently exists no optimum helio­stat size
  - Large area:  $\sim 130 \text{ m}^2$ 
    - Larger wind load
    - Higher cost per area ( $\$/\text{m}^2$ )
    - Higher electricity requirement
  - Small area:  $\sim 1 \text{ m}^2$ 
    - Requires more helio­stats
    - Higher wiring cost
    - Low wind load
    - Lower cost per area  $\$/\text{m}^2$
- Previous research considered static and dynamic wind loads using isolated scaled models in wind tunnels.
  - Correlation between high wind loads and vibration with turbulence intensity
  - Authors strongly urge full scale testing

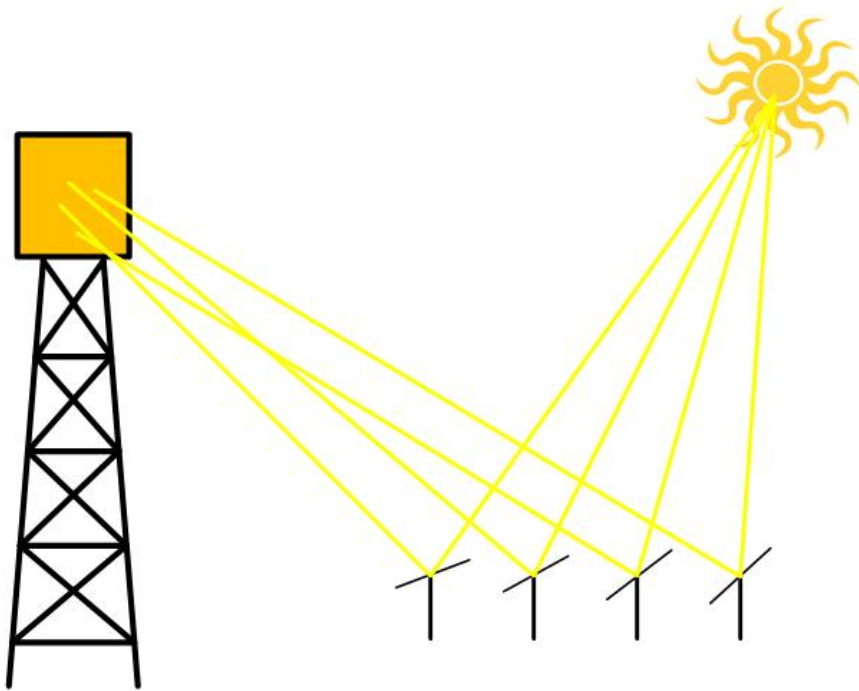


Paterka et al. 1986

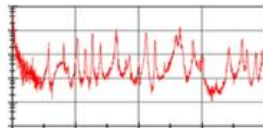
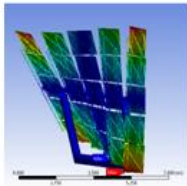
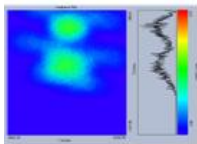


Gong et al. 2011

# OMA Motivation



- Wind induced vibration leads to increased fatigue and premature failure
- Operational mode shapes reduce maximum flux contribution per heliostat during wind events
- Experimental validation and optical characterization will lead to further design improvements
- Demonstrate a unique link between structural dynamics and CSP optics engineering fields







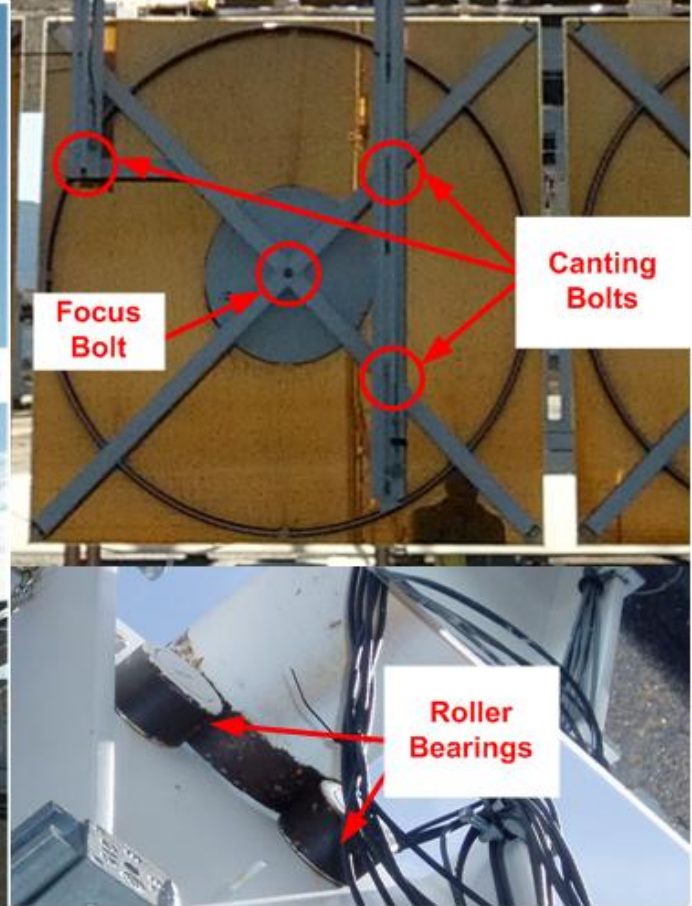
# Objective

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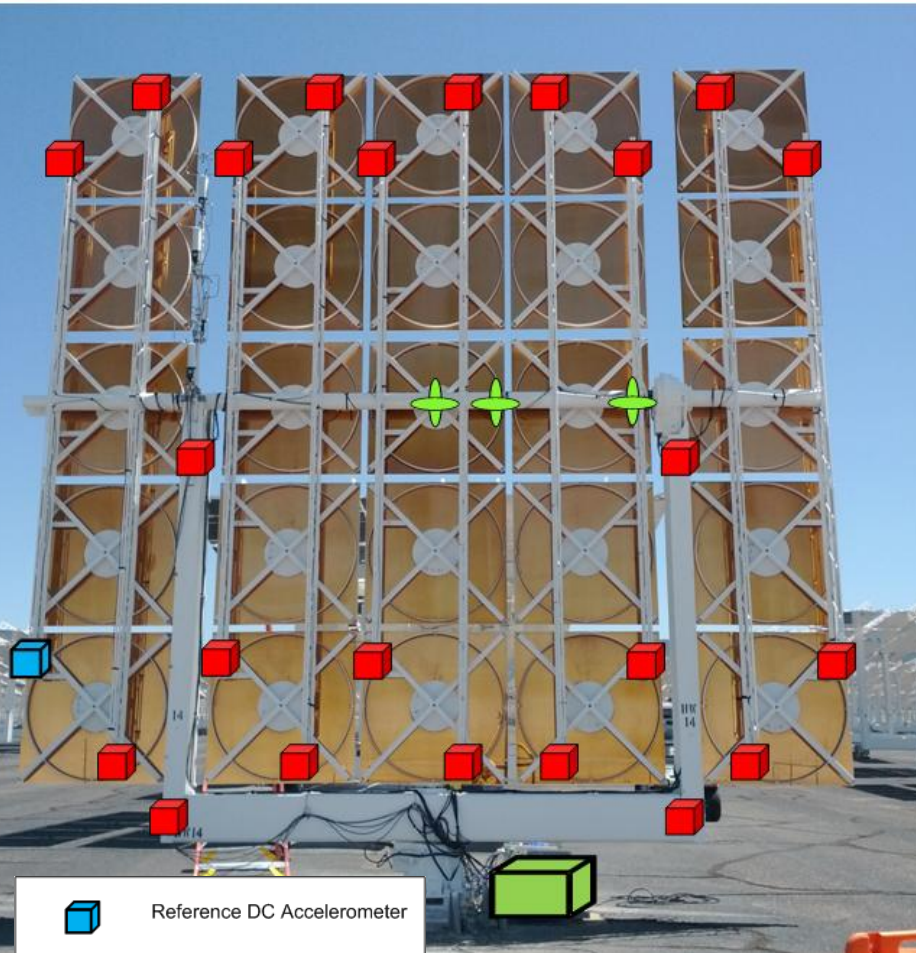
- **Instrument heliostats for dynamic monitoring capability**
  - Perform test and analysis to better characterize heliostat dynamics induced by wind loads
  - Verify FEM produced mode shapes
- **Characterize optical degradation via ray tracing methods**
  - Use scaled deformed FEM mode shapes as deformed heliostat surface
- **Mitigate wind induced fatigue and increase optical performance of next generation heliostats**
  - Improve existing heliostat design criteria which currently only considers wind induced fatigue and static loads



# NSTTF HelioStat Geometry



# Well Instrumented Heliostat



- Heliostat 11W-14 Instrumented
  - 6 3D Wind Anemometers
  - 24 Tri-axial Accelerometers
  - 6 Strain Gauges
- Data communication between field and control tower established via fiber optic comm.
- Data acquisition system installed and verified
- Six wind sensors at various heights surround heliostat on anemometer towers
- Accelerometer sensitivity: 1000 mV/G



 Reference DC Accelerometer

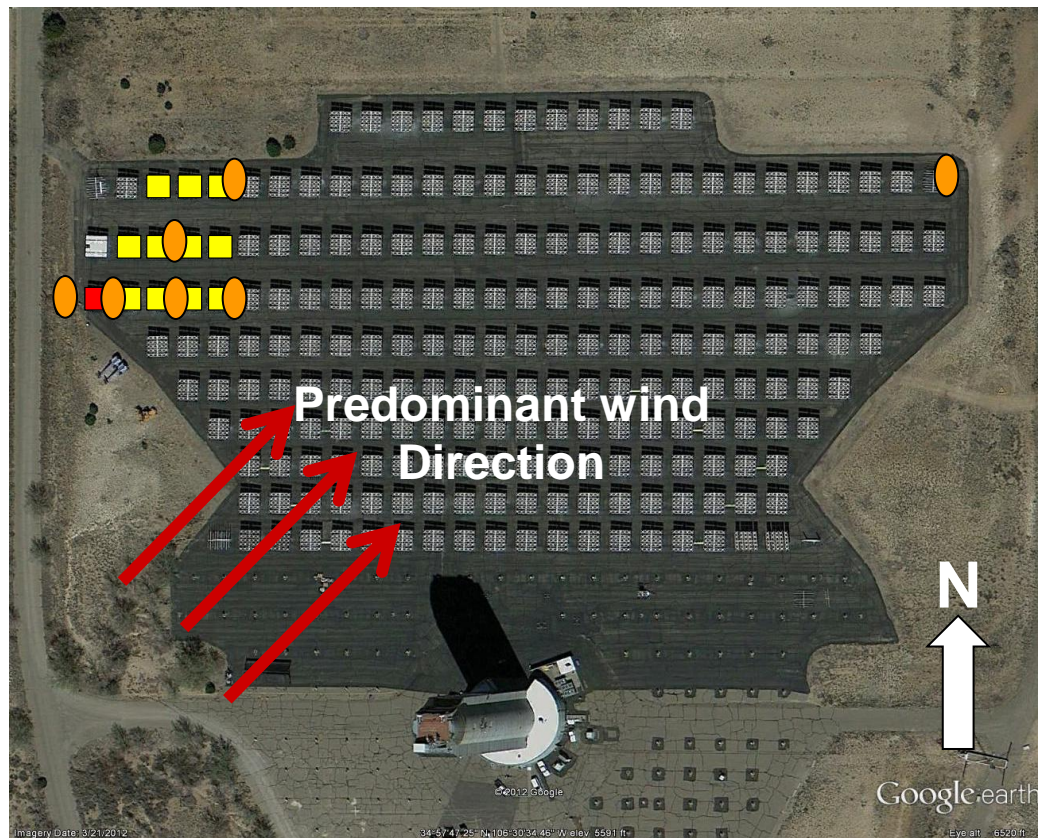
 DC Tri-Axial Accelerometer




 Strain Gauge

 Data Acquisition



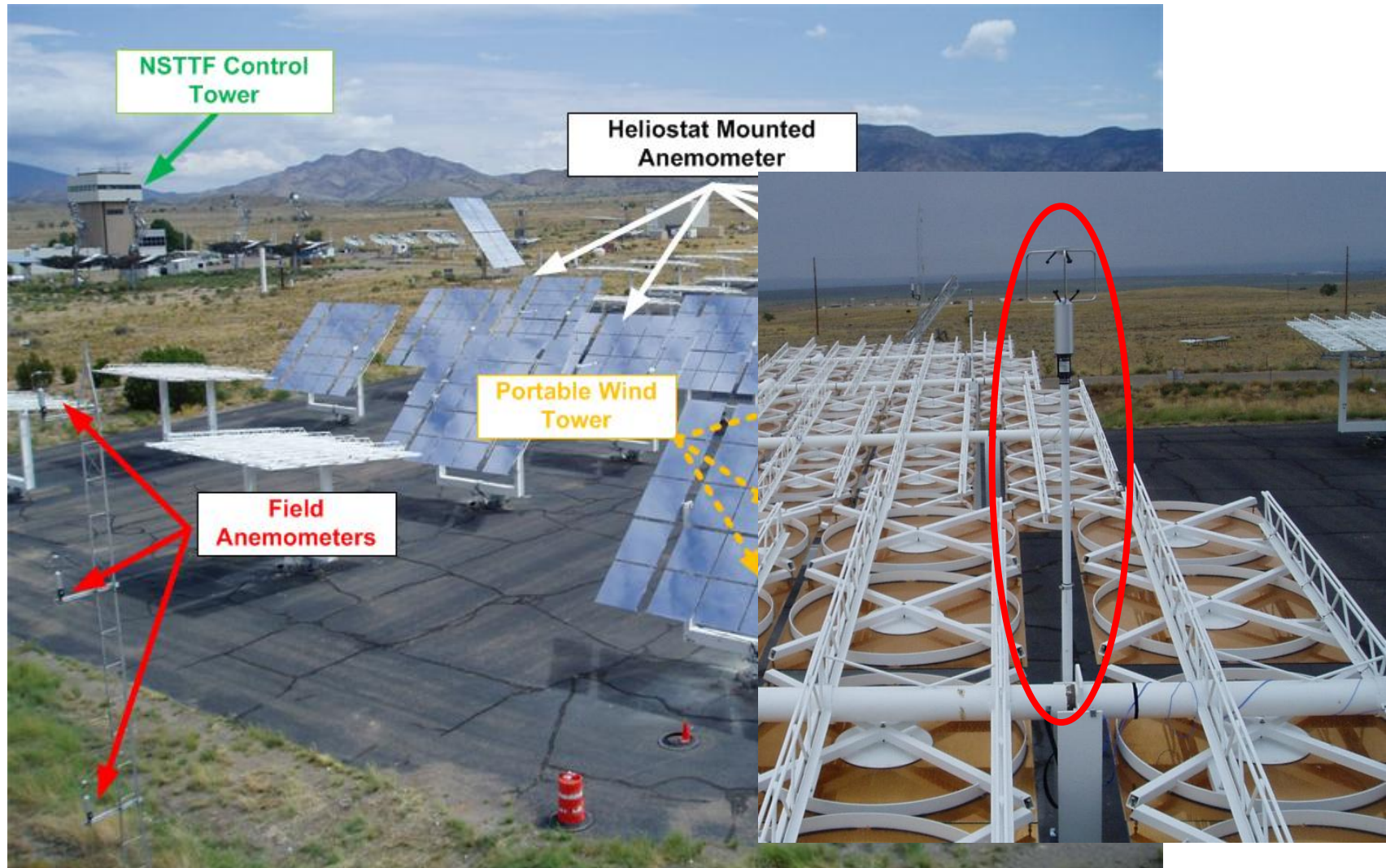
# Instrumentation and DAQ



-  Wind Anemometer
-  Nominal Heliostat
-  Well Inst. Heliostat

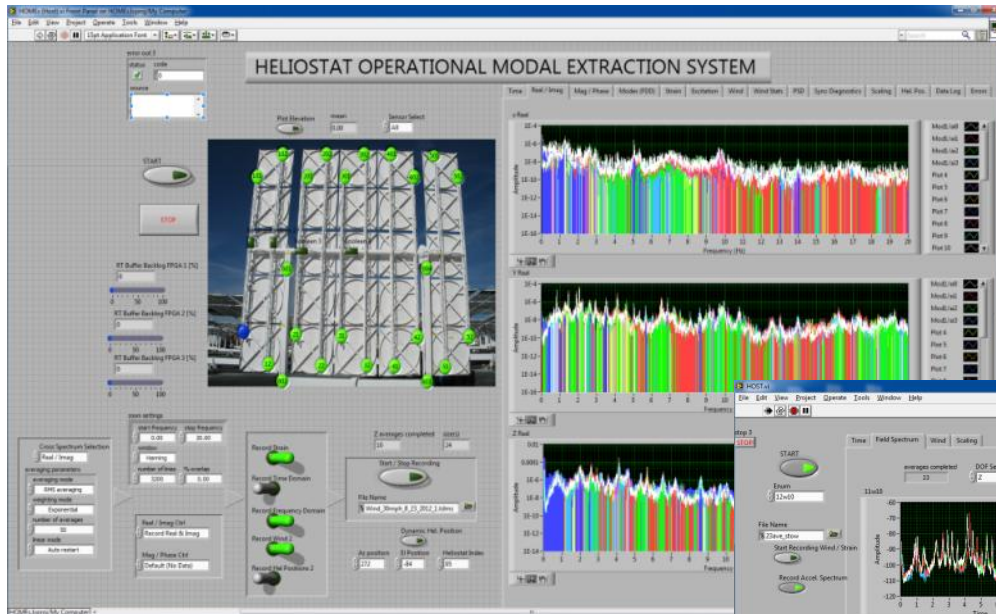
- 13 total heliostats instrumented
- One single well instrumented heliostat used for full modal testing
- 11 Nominal heliostats monitor vibration magnitudes, strain, and wind data at select locations
- 1 Wind Anemometer located on western corner
- Data acquisition developed to stream data in real time to control tower

# Instrumentation and DAQ





# Instrumentation and DAQ

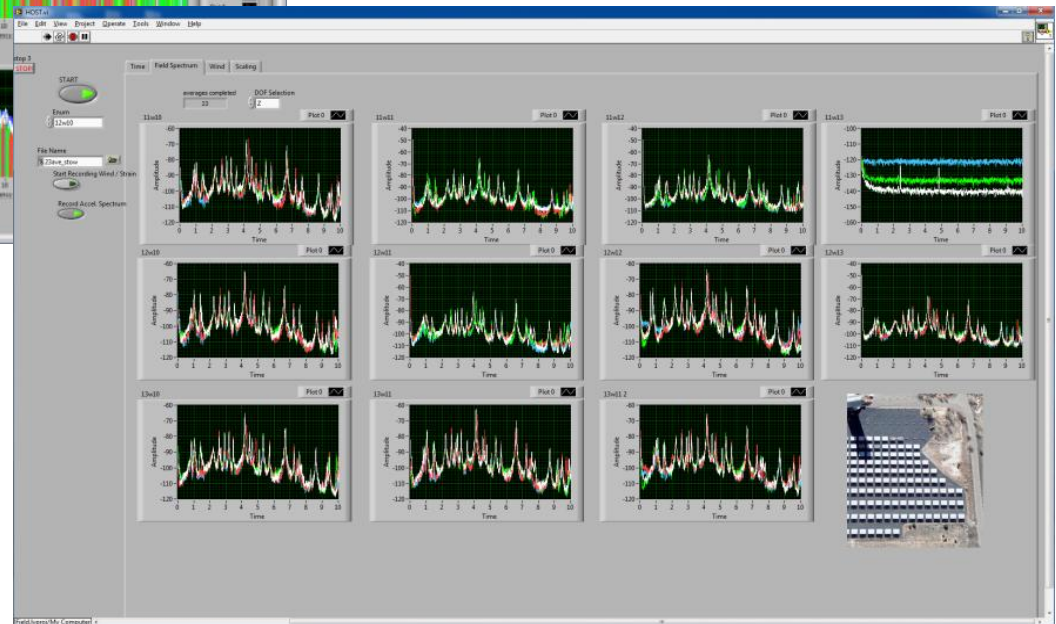


## Well Instrumented Heliostat

- Monitors 24 tri-axial accelerometers, 6 strain, and 6 3D anemometers (~102 total channels on one heliostat)

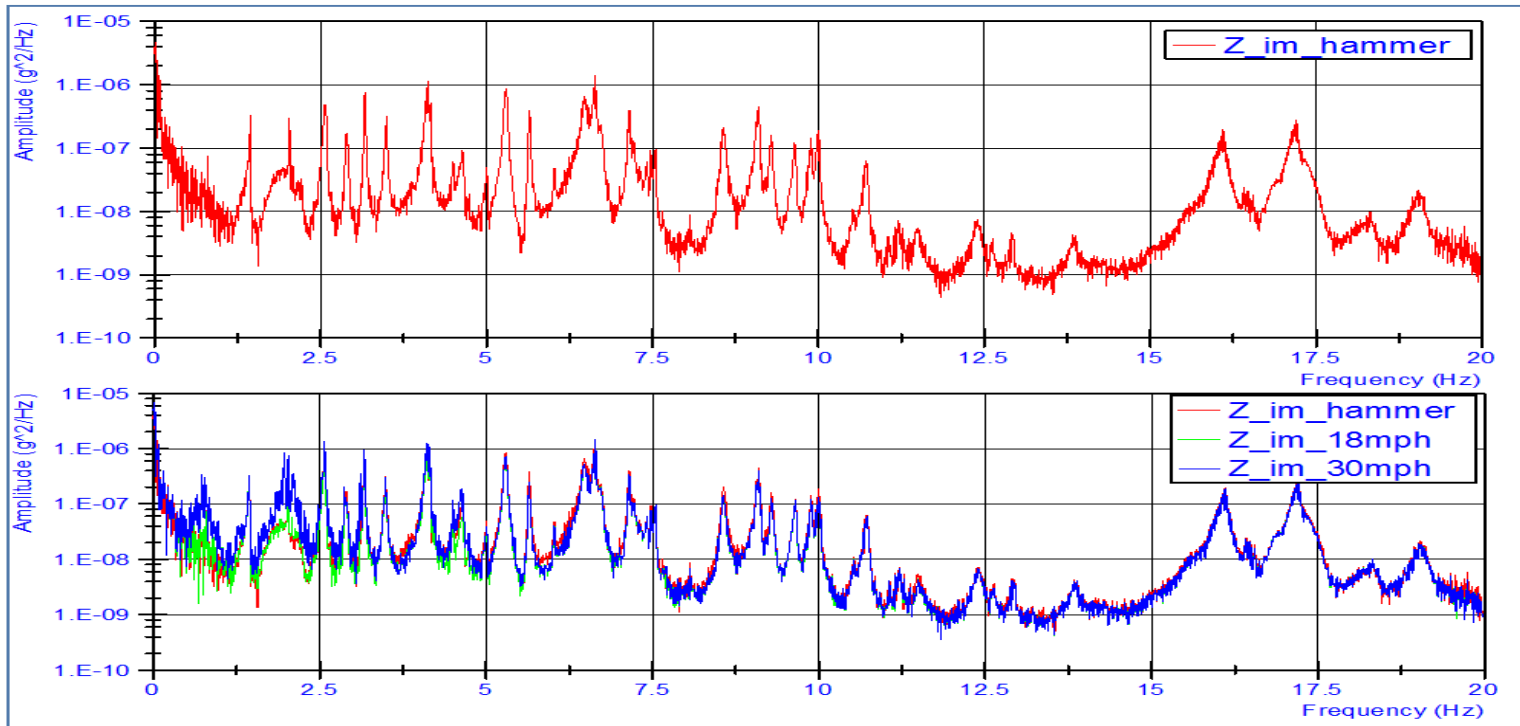
## Nominally Instrumented Heliostats

- Monitors 4 tri-axial accelerometers per heliostat, strain, and wind sensors across 11 nominally instrumented heliostats



# OMA (Random Excitation)

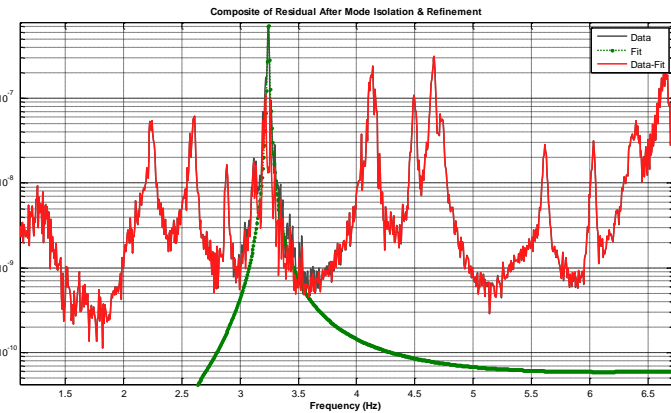
- Random excitation was shown to duplicate wind excited modes
  - Random excitation introduced via hammer input at various locations (red)
  - Power Spectra of 18-30 mph wind averages taken for comparison (blue / green)
- Random excitation technique was found replicate wind conditions and accelerate data collection
- Future monitoring of wind events will verify this method and / or provide a wind excitation profile for different wind speeds



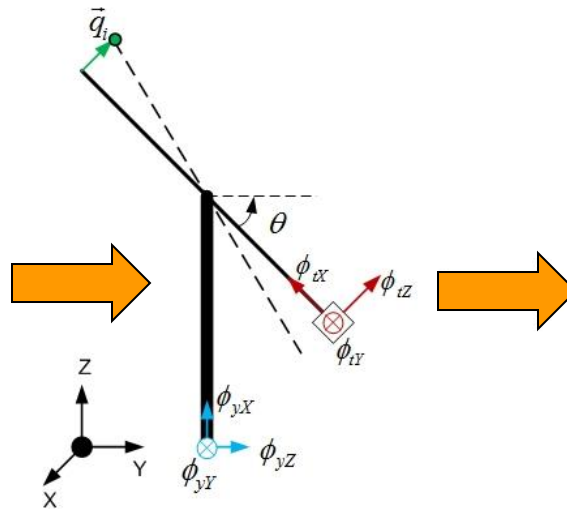


# Mode Shapes

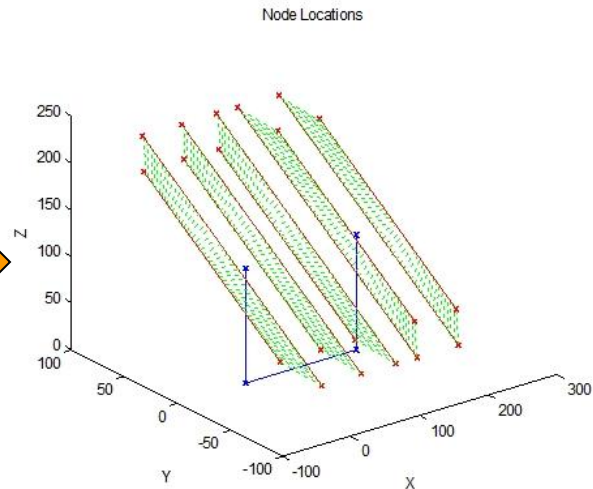
## Mode Isolation (Curve Fitting)



## Coordinate Transformation



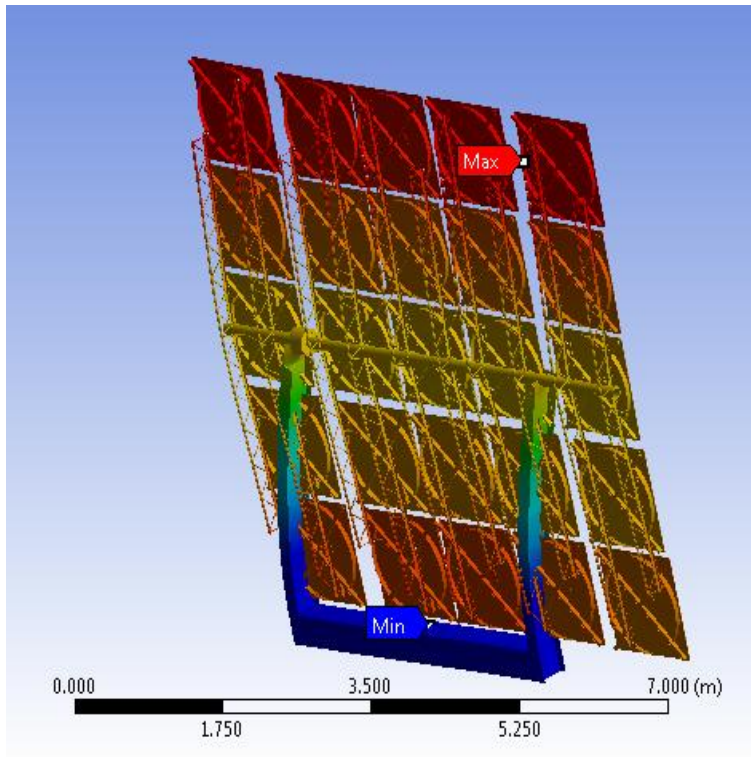
## Operational Mode Shapes



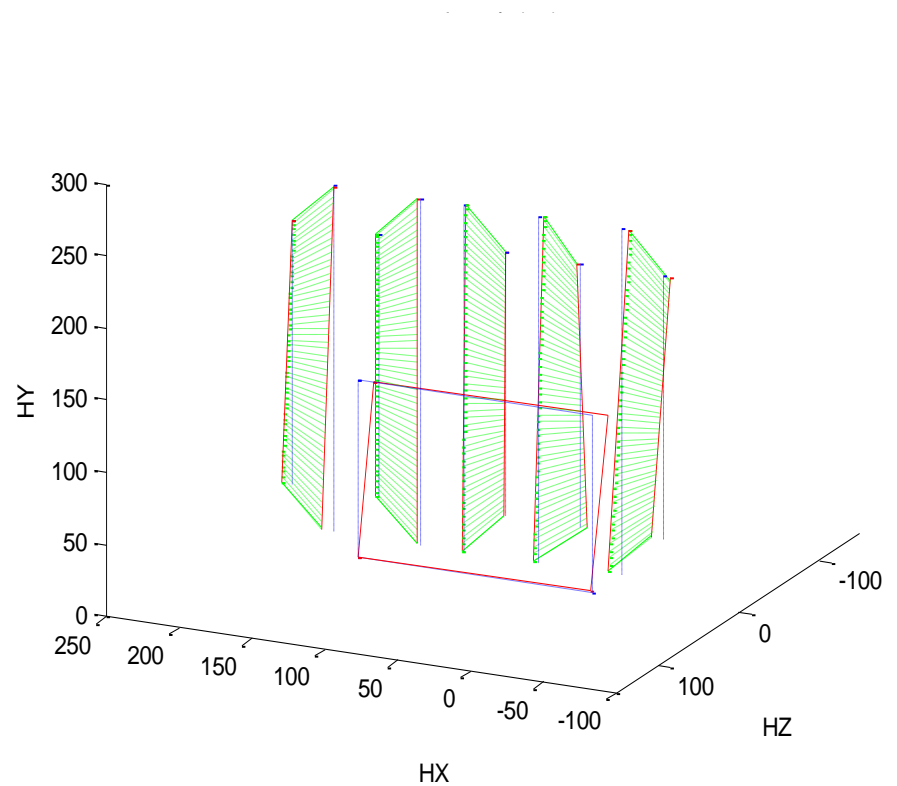
$$\vec{q}_i = \begin{Bmatrix} q_{i,x} \\ q_{i,y} \\ q_{i,z} \end{Bmatrix} = \begin{Bmatrix} q_{x0} \\ q_{y0} \\ q_{z0} \end{Bmatrix} + \begin{bmatrix} \phi_{tx} & \phi_{ty} \\ \phi_{tz} \cos(90 - \theta) - \phi_{tx} \cos(\theta) \\ \phi_{tz} \sin(90 - \theta) + \phi_{tx} \sin(\theta) \end{bmatrix} \begin{Bmatrix} M_x \\ M_y \\ M_z \end{Bmatrix}$$

# Yoke Bending Modes

Ansysis: 1.604 Hz

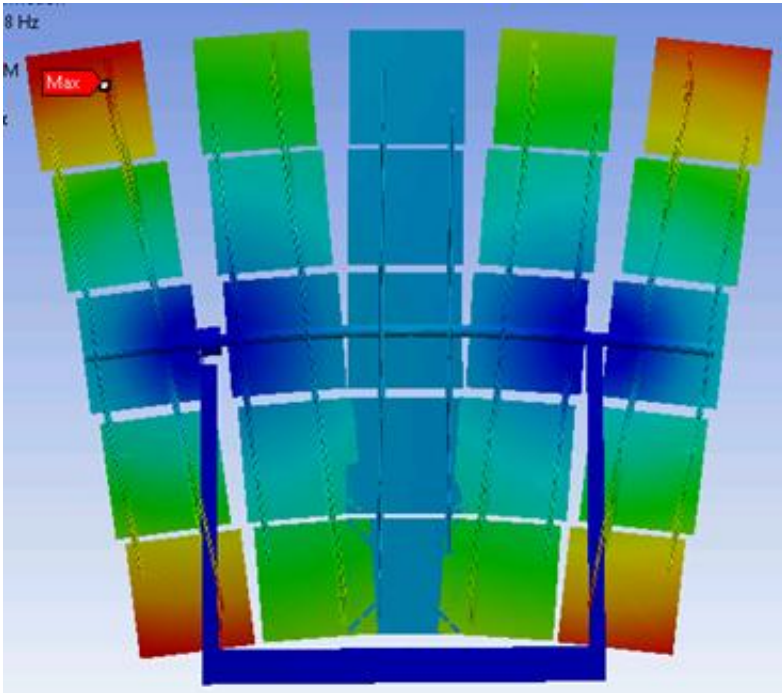


OMA: 1.63Hz

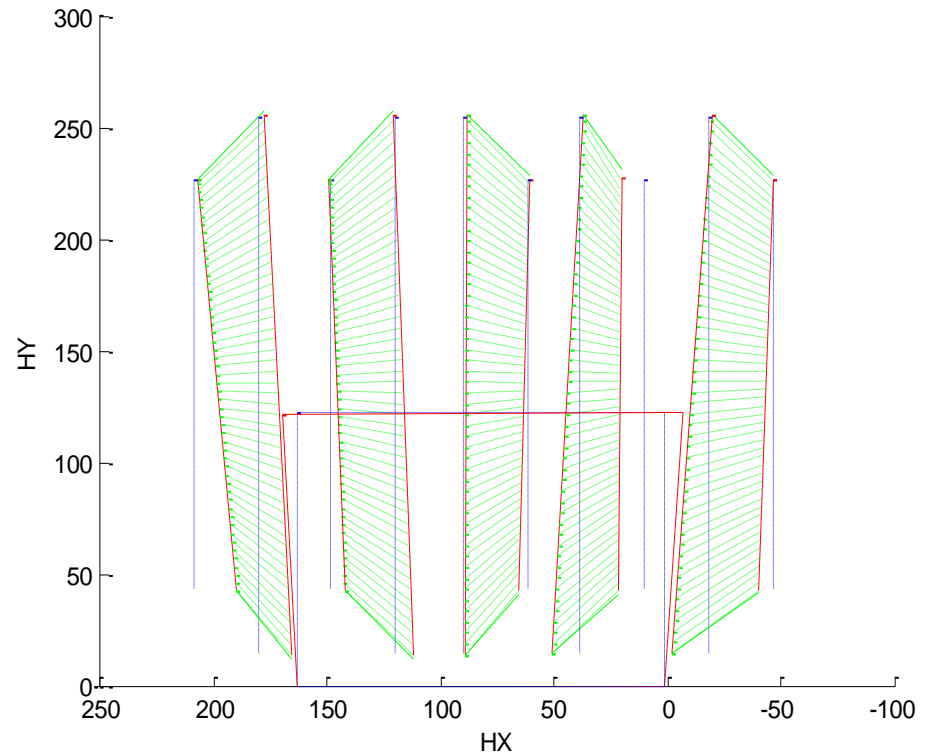


# In-Plane Modes

Ansys: 3.0 Hz



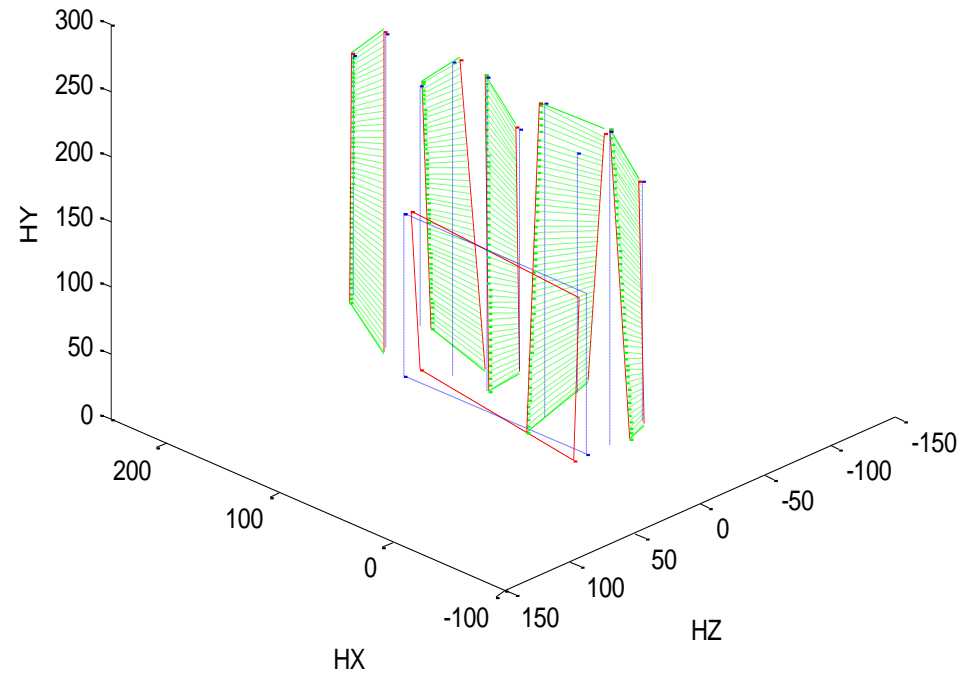
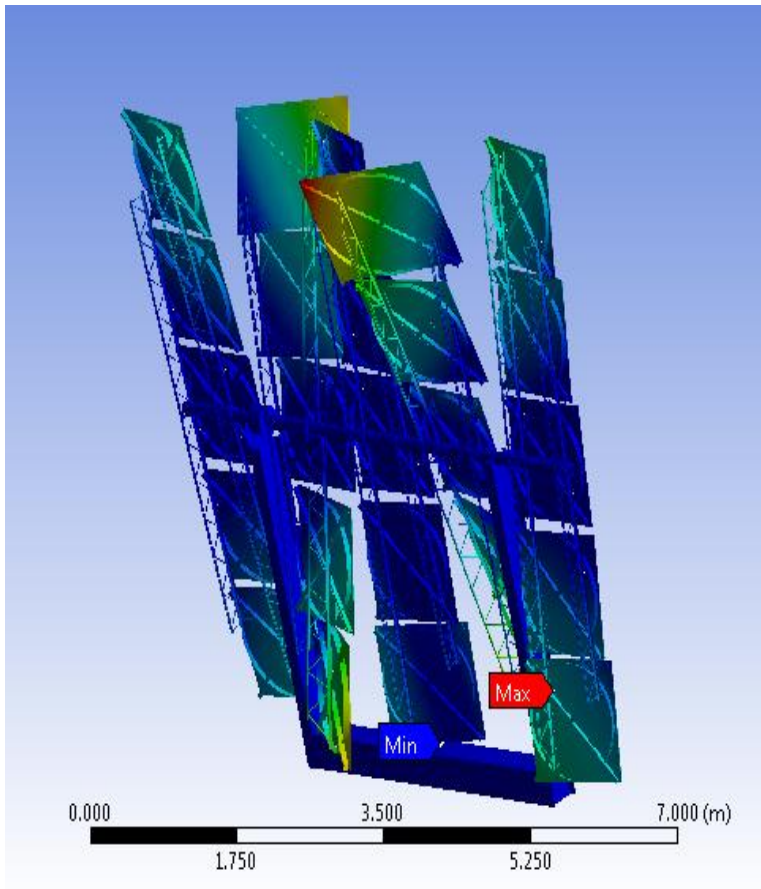
OMA: 3.24Hz



# Out-of-Plane Modes

Ansysis: 5.2 Hz

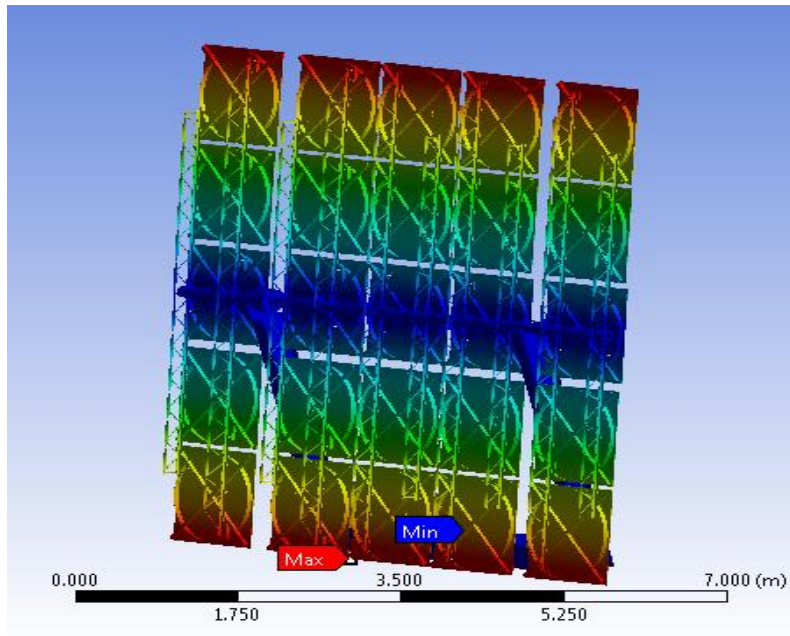
OMA: 5.61Hz



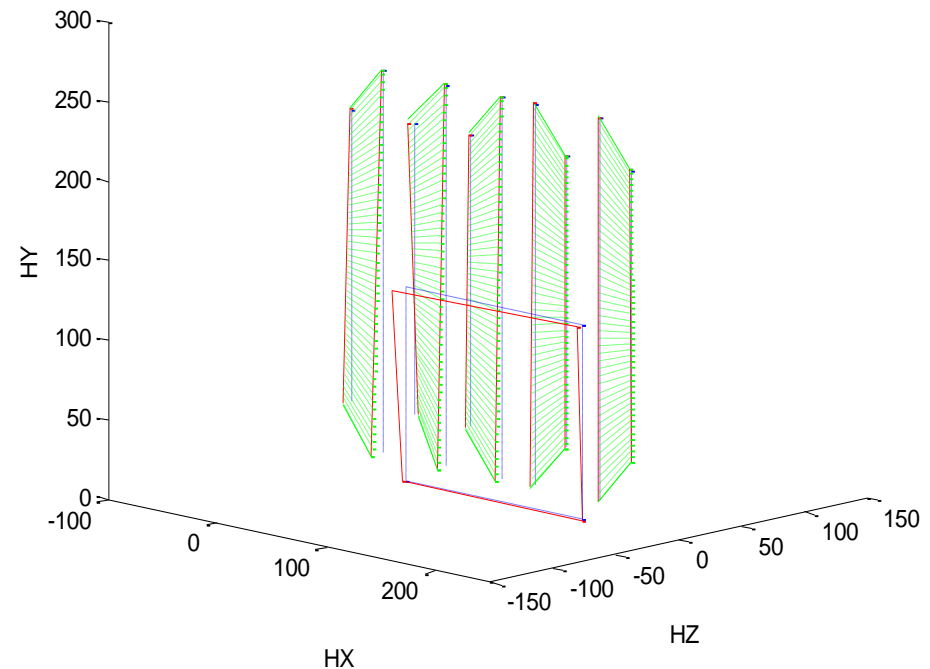


# Rigid Body Modes

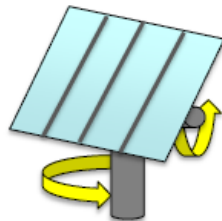
Ansys: 1.1 Hz



OMA: 0.9Hz



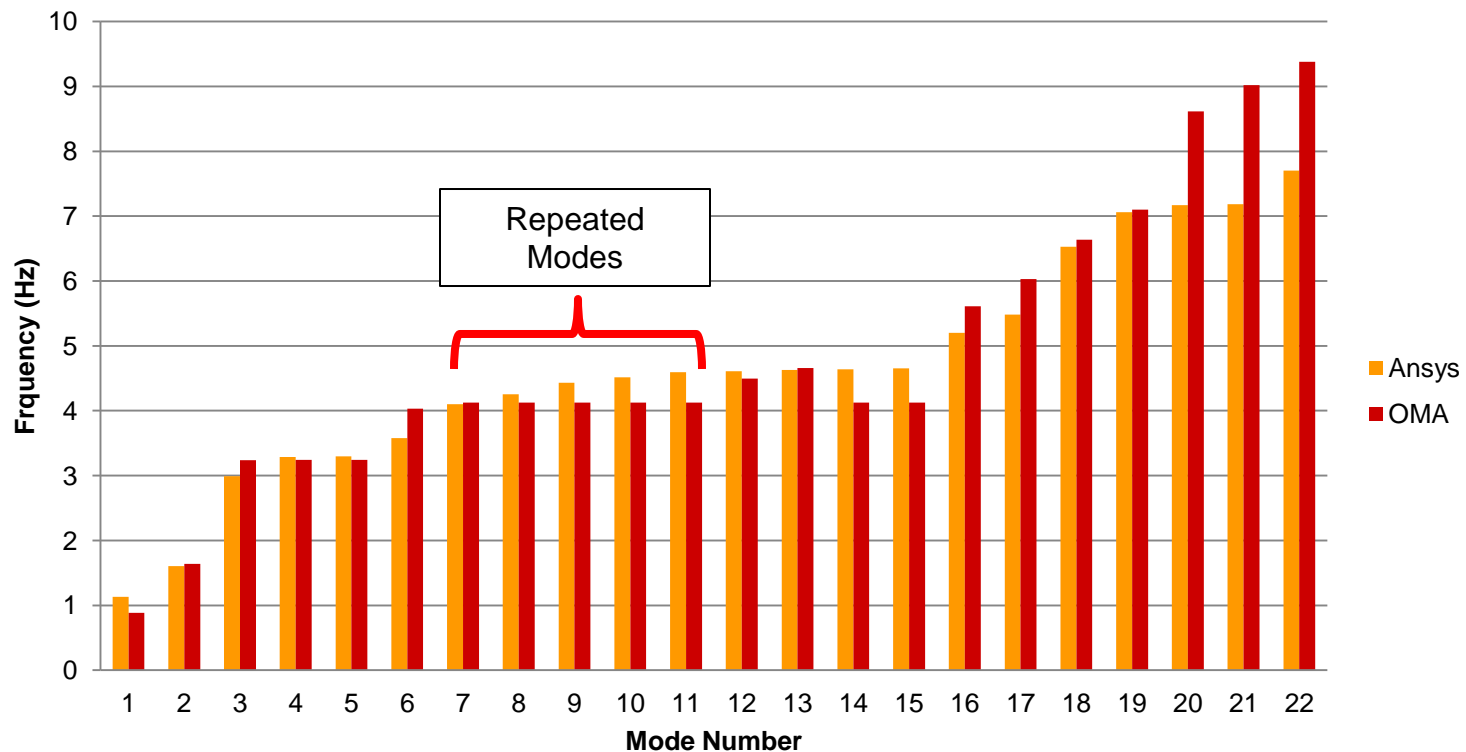
$$f_n = \frac{1}{2\pi} \sqrt{\frac{k_\theta}{I_\theta}}$$



Rigid Body Modes ~0.8-1.25 Hz

# FEA Comparison

## Ansysis - OMA Frequency Comparison

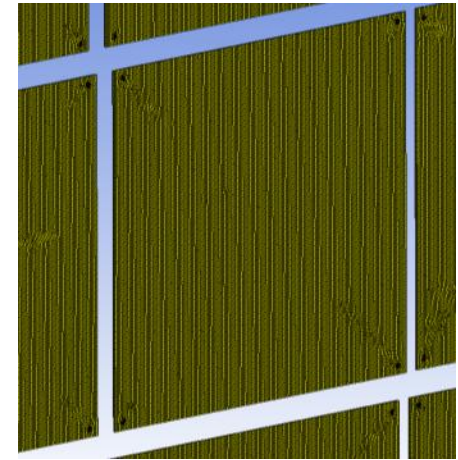
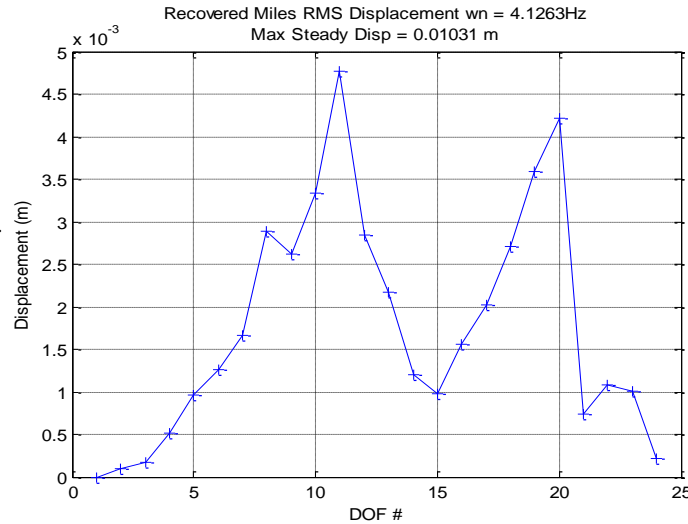
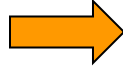
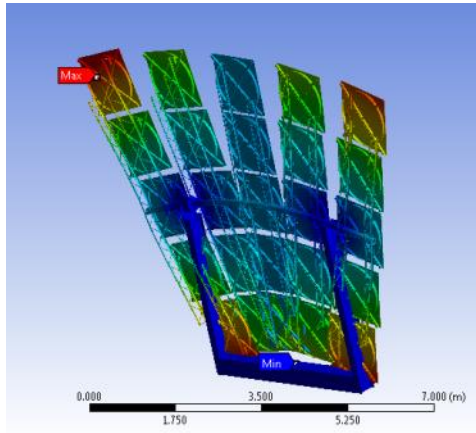


# Displacement Model

Arbitrary Displacement Result

Approximate DOF Displacements

Scale Output Mesh Surface



## Miles Equation

- Assumes 1 DOF model
- Assumes "white noise" random vibration
- $Q$  = Transmissibility factor
- $D$  = Approximate Displacement (rms)

$$D_{rms} = \sqrt{\frac{\pi}{2} f_n Q \frac{\ddot{X}_{PSD}}{-\omega^2}}$$

$$\ddot{X}(f) = -\omega^2 X(f)$$

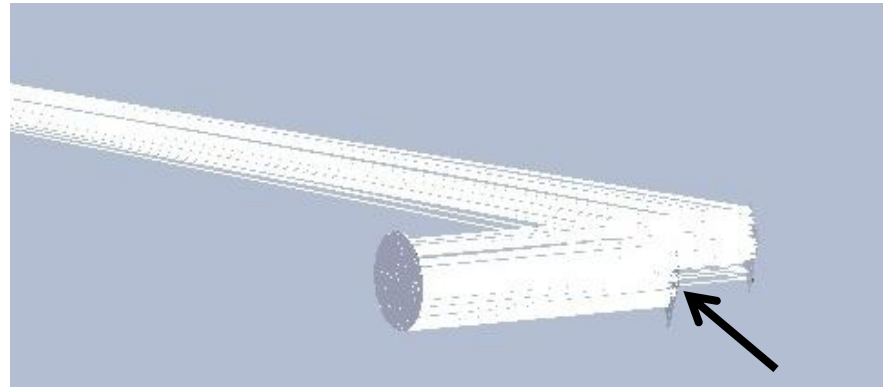
$$Q = \frac{1}{2\zeta}$$

# Ray Tracing (CAD Model)

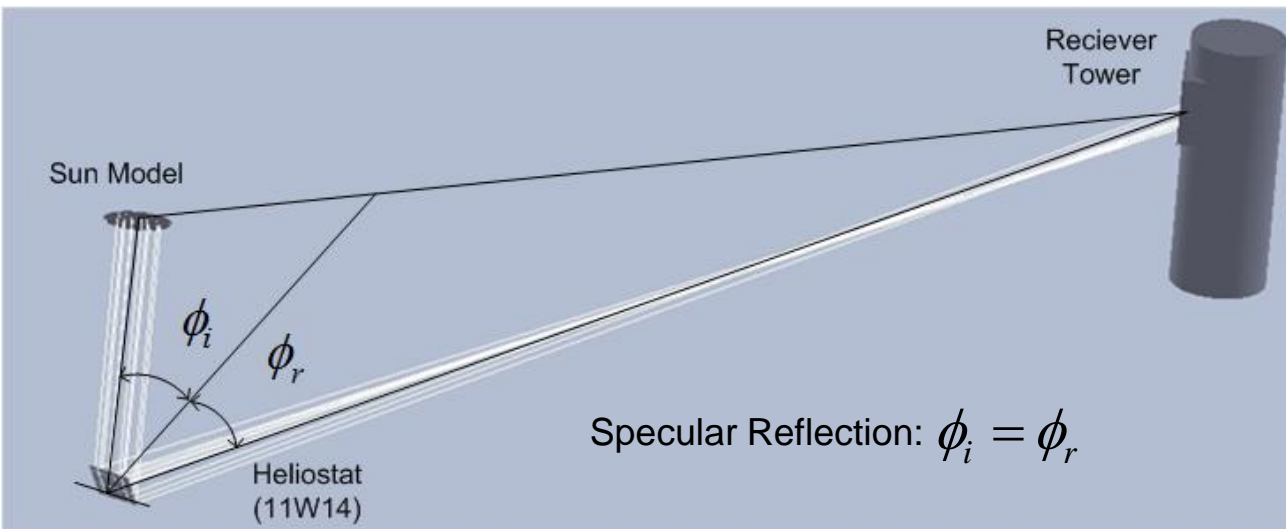
Reconfigurable model automatically updates by re-aiming heliostat for desired inputs

## Inputs

- Time of Day
- Day of Year
- Longitude & Latitude
- Solar Insolation

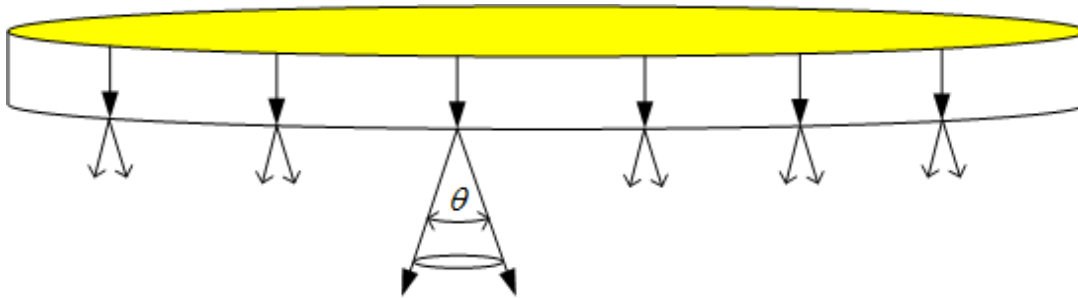


Adjacent Heliostat Added for Blockage Effects in Evening





# Ray Tracing (Sun Model)



$$Power = DNI * A_{Emmiting} * \frac{4}{\theta^2}$$

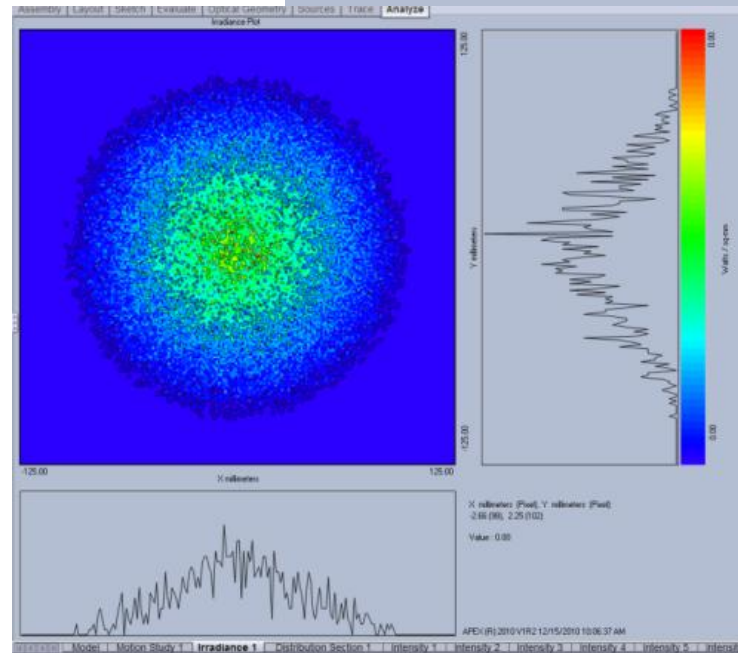
Rays Traced = 5.5 million

DNI = 1000 (W/m<sup>2</sup>)

Wave Length = 550 nm

$\theta$  = Sun Cone Angle (0.57°)

Simulations performed for March 21 at  
8 AM, Solar Noon (~1 PM), and 6 PM

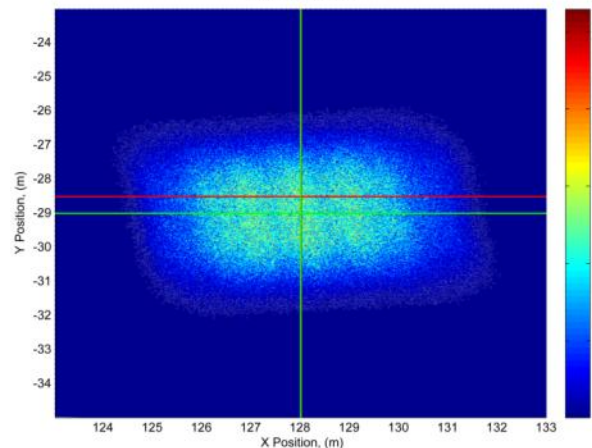


\*Courtesy Joshua Christian, SNL

# Ray Tracing: Static (Gravity)

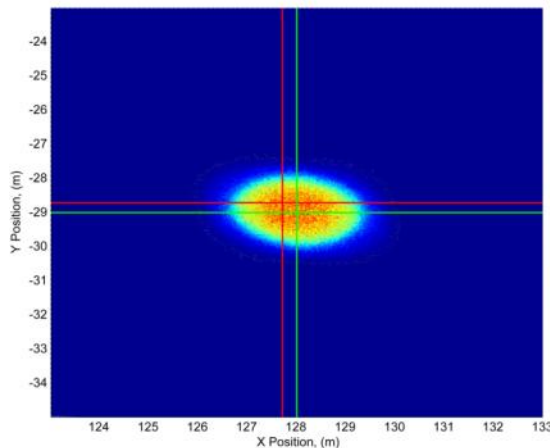
8 AM

Flux Map For Data Static 8 AM (Units W/mf)  
Max Flux = 2191.3763 W/mf  
X Offset = -0.010008 m  
Y Offset = -0.49 m



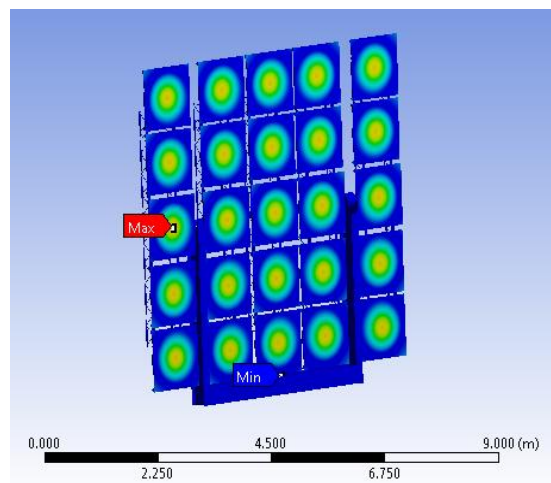
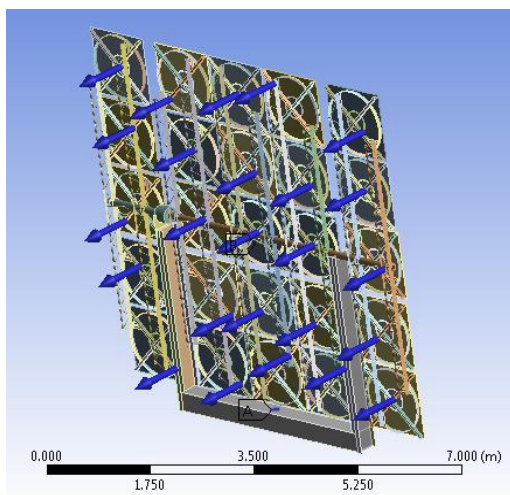
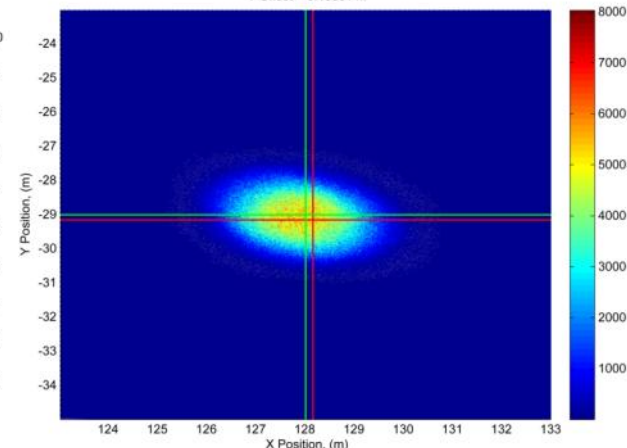
Solar Noon (~1 PM)

Flux Map For Data Solar Noon Static (Units W/mf)  
Max Flux = 10319.3669 W/mf  
X Offset = 0.28999 m  
Y Offset = -0.29 m



6 PM

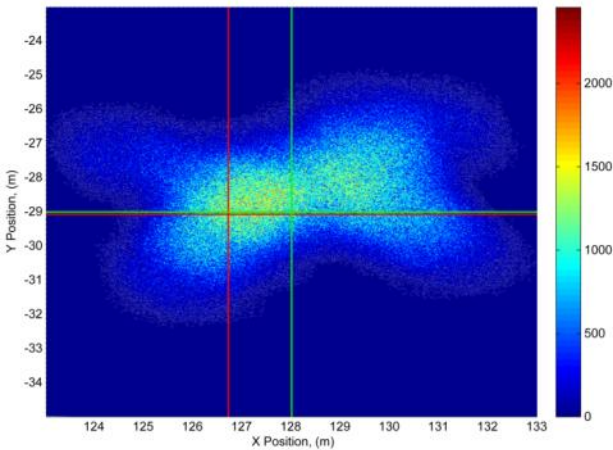
Flux Map For Data Static 6 PM Blockage (Units W/mf)  
Max Flux = 6980.1558 W/mf  
X Offset = -0.14999 m  
Y Offset = 0.15001 m



# Ray Tracing: Mode 14

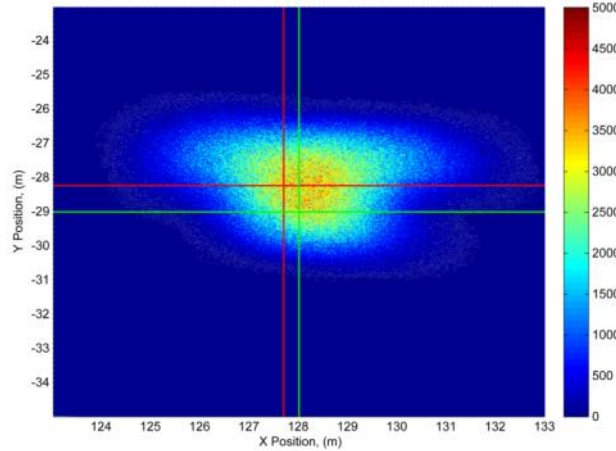
8 AM

Flux Map For Data Mode 14 8 AM (Units W/m<sup>2</sup>)  
Max Flux = 2222.8743 W/m<sup>2</sup>  
X Offset = 1.29 m  
Y Offset = 0.069996 m



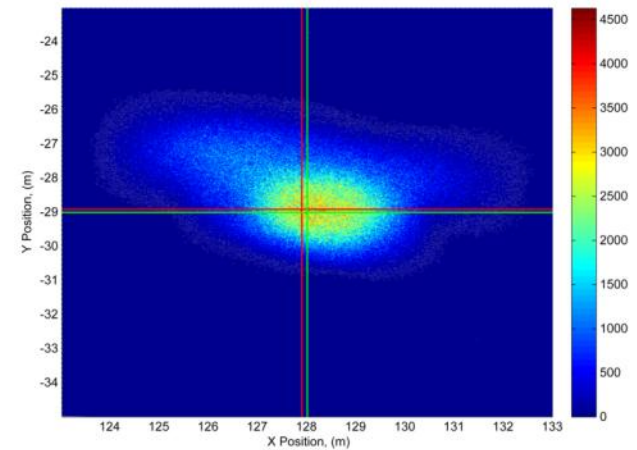
Solar Noon (~1 PM)

Flux Map For Data Solar Noon Mode 14 (Units W/m<sup>2</sup>)  
Max Flux = 4608.3876 W/m<sup>2</sup>  
X Offset = 0.31001 m  
Y Offset = -0.77001 m



6 PM

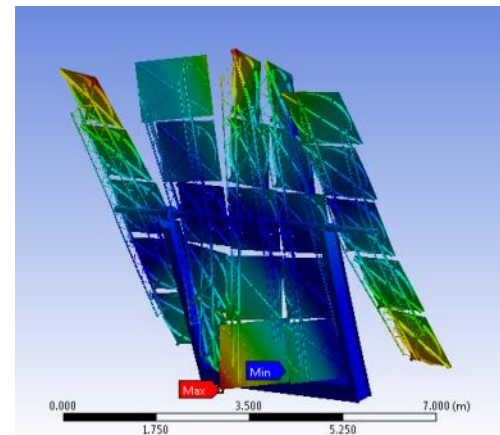
Flux Map For Data Mode 14 6 PM Blockage (Units W/m<sup>2</sup>)  
Max Flux = 4086.3848 W/m<sup>2</sup>  
X Offset = 0.11001 m  
Y Offset = -0.089999 m



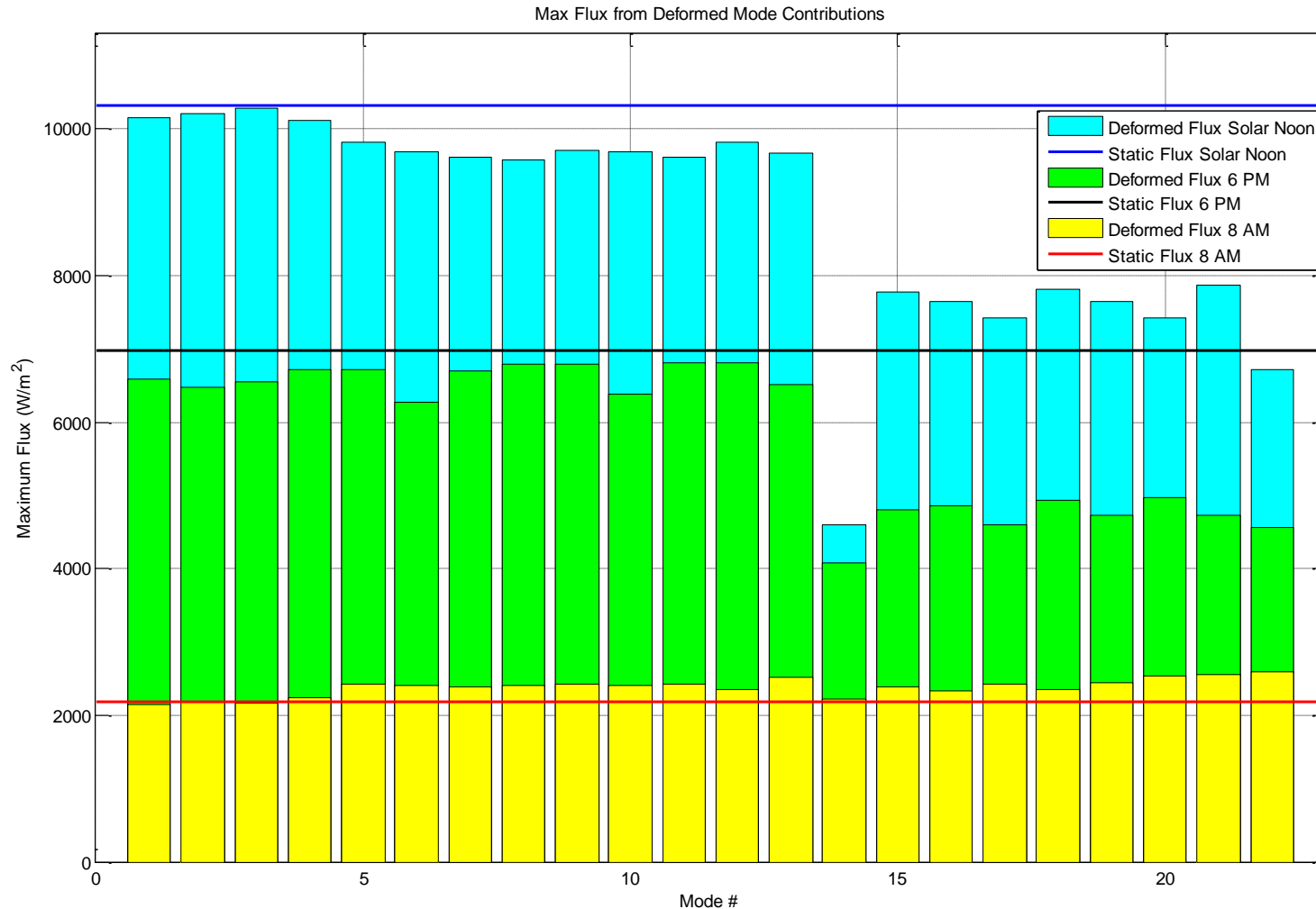
Mode #14

$F_n = 4.126 \text{ Hz}$

Max Disp. ~ 10.3 mm



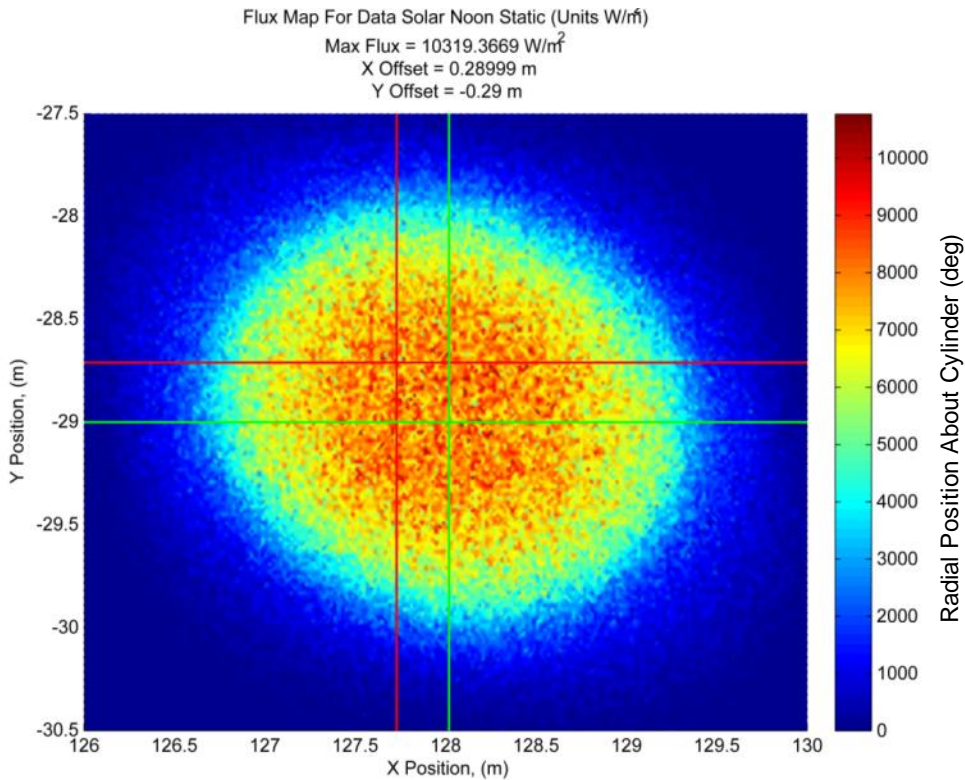
# Maximum Flux per Mode Contribution



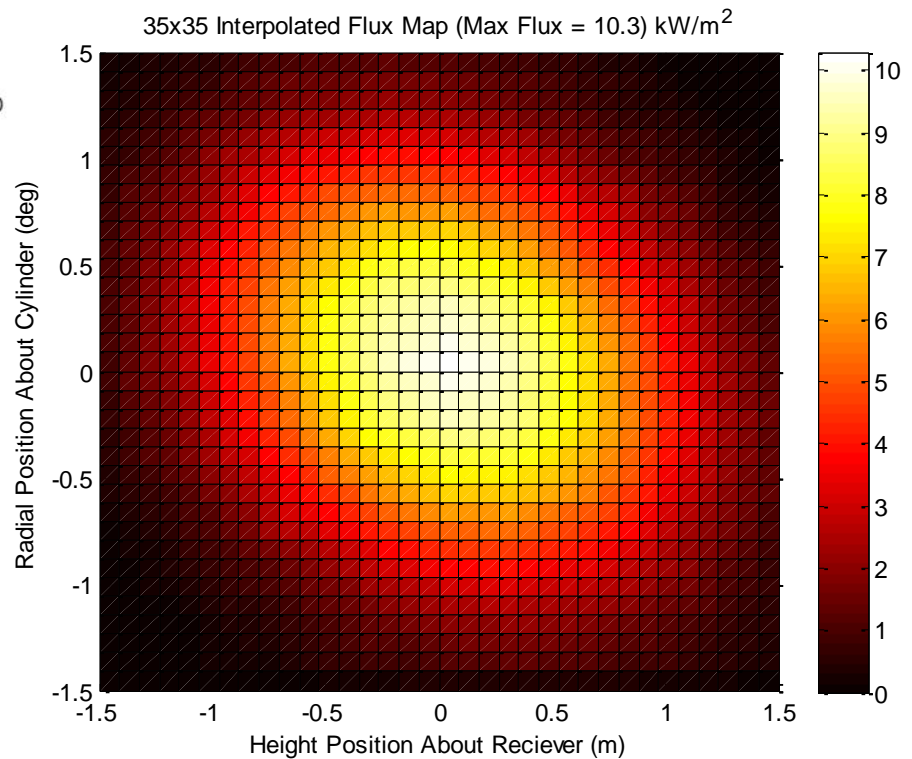


# DELSOL Model

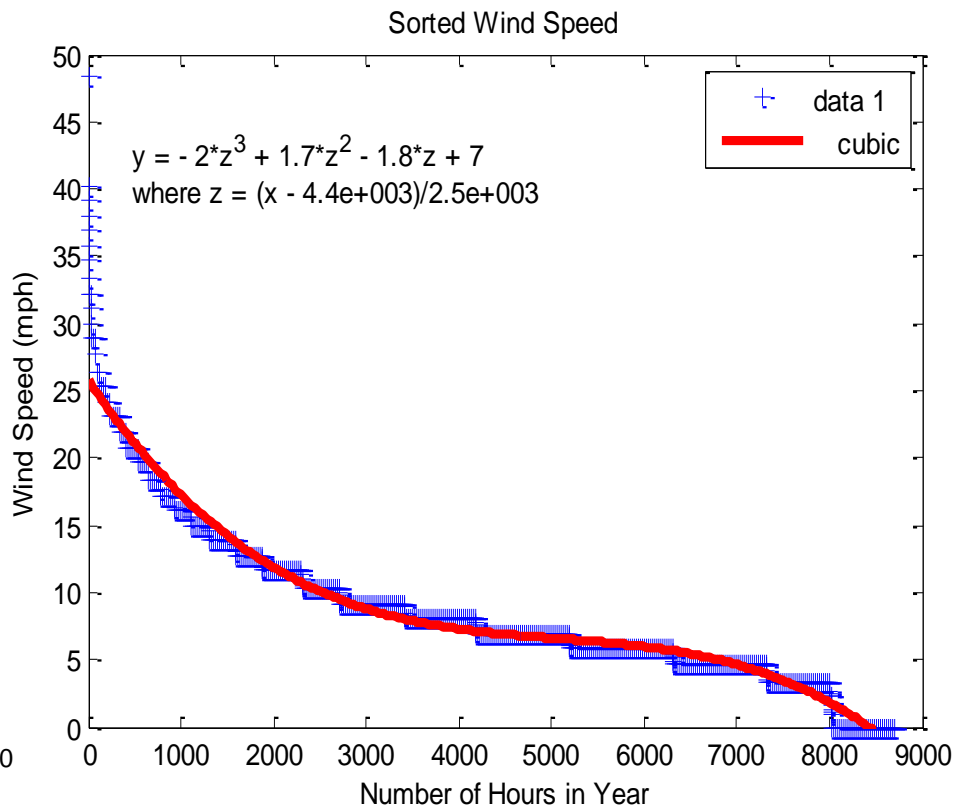
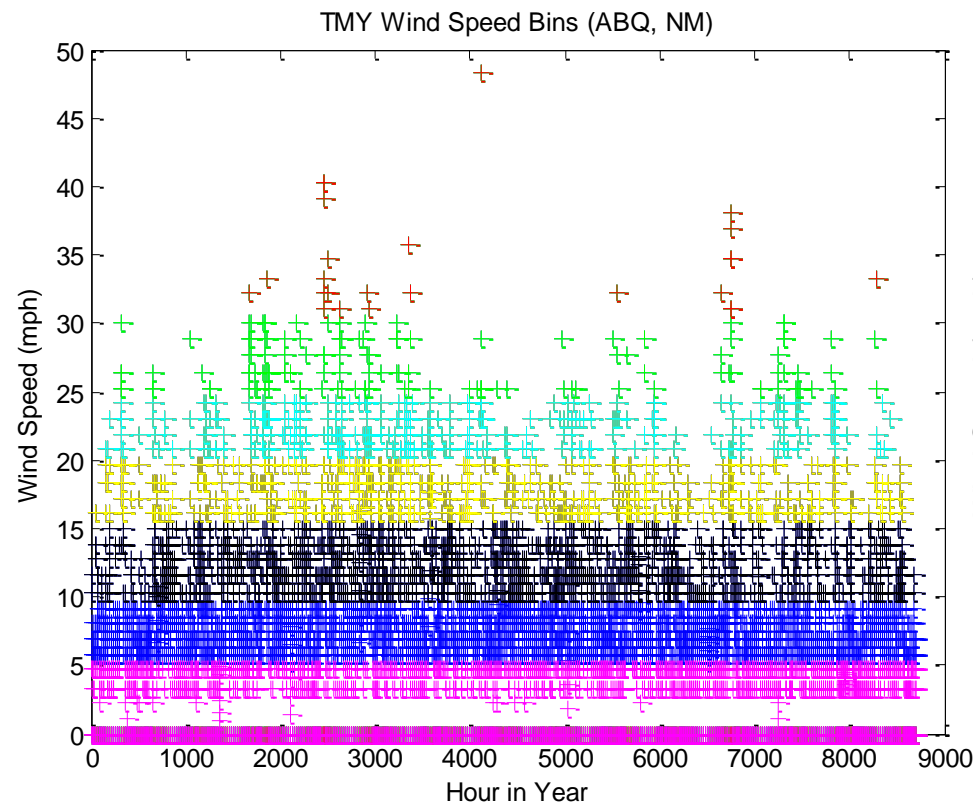
## APEX Ray Tracing Flux Map



## DELSOL Flux Map



# TMY Wind Data



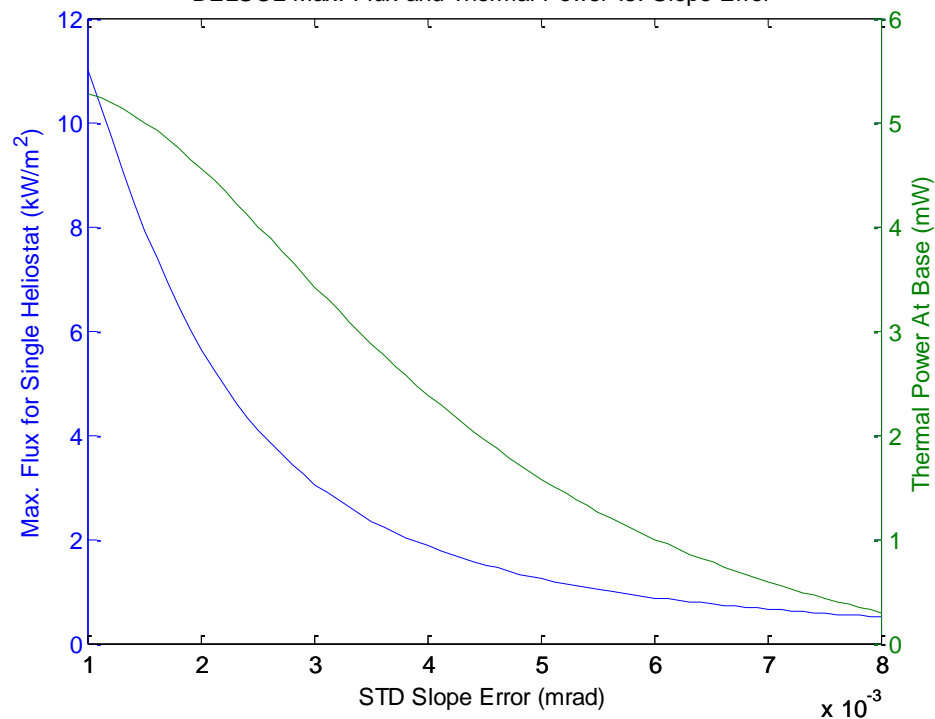
Define Wind Hrs Ratio for  
Performance Calculations

$$W_{bin} = \frac{hr_{bin}}{8766}$$

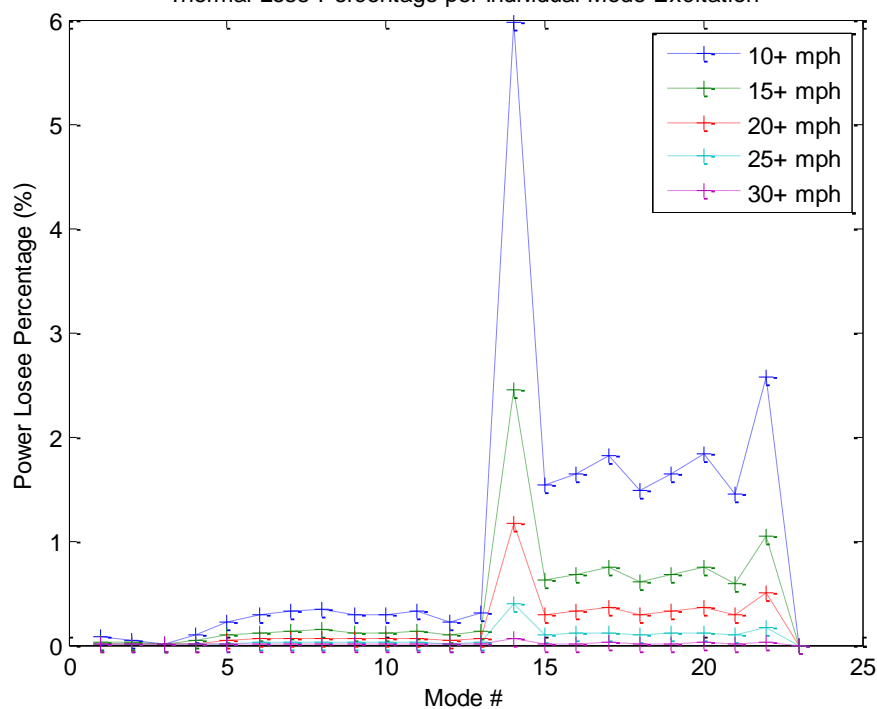
# Plant Performance

$$G_{thermal} = G_{vib} * W_{bin} + G_{Static} * (1 - W_{bin})$$

DELSOL Max. Flux and Thermal Power vs. Slope Error



Thermal Loss Percentage per Individual Mode Excitation





# Conclusion

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- Full scale modal analysis and tests have been conducted on NSTTF heliostat
  - FEA and test mode shapes and frequencies match well for most modes
  - Rigid body modes due to motion in drives are characterized
- Wind excited modes range from  $\sim 0.8 - 20$  Hz
  - Higher Frequency modes dominate response leading to largest displacement
  - Modes dampen out after ten Hz
- Out of plane modes lead to greater optical and thermal losses annually
  - NSTTF power plant simulations result in  $\sim 1-6$  % power loss
  - Future wind excited data will verify this loss
- Turbulent wind and vortex shedding is attributed to majority of excitation





# Future Work

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- **Continue to monitor and capture wind events**
  - Create field position profile for wind excited displacements
  - Analyze field performance with interior wind speed profile
  - Automate monitoring program to trigger wind recording
- **Profile wind loads and characterize fatigue in heliostat structure**
  - Compare to Paterka model
  - Develop novel design approaches to mitigate wind induced vibrations and improve optical performance
- **Lower LCOE on future heliostat designs using dynamic design approach to mitigate fatigue and optical effects**



# Questions?



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# Appendix

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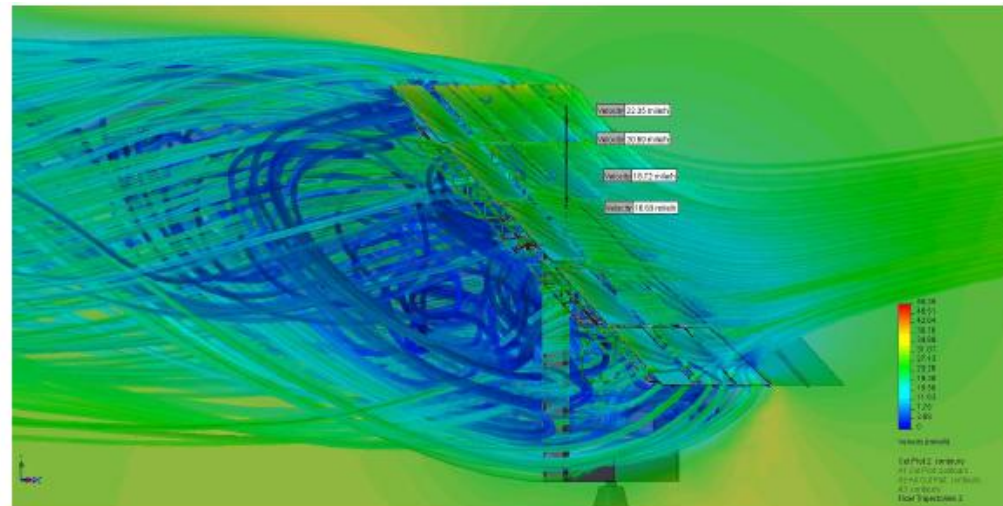
# Wind Excitation

- Mean wind spectrum contributes to low freq response ( $< \sim 1\text{Hz}$ )
- Wind gust spectrum excites mid range frequencies
- Vortex Shedding causes oscillating flow on interior heliostats
  - Strouhal number defines vortex shedding frequency

$$S_t = \frac{fD}{v}$$



Chen et al., 1996



\*Courtesy J. Sment



# Plant Performance

$$G_{thermal} = G_{vib} * W_{bin} + G_{Static} * (1 - W_{bin})$$

Scaled based on Output performance not on max flux

